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9-27-2011

Damping of turbulence by suspended sediment: fundamental ramifications for sediment dynamics

Carl T. Friedrichs
Virginia Institute of Marine Science

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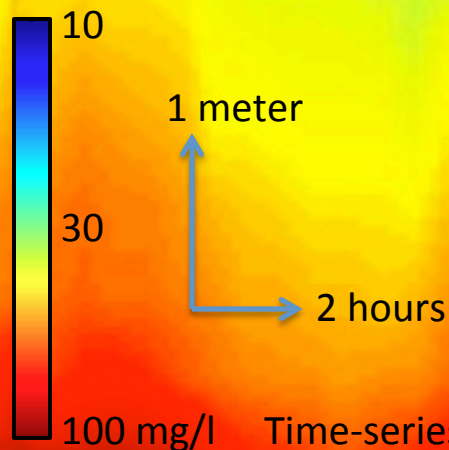
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Damping of Turbulence by Suspended Sediment: Fundamental Ramifications for Sediment Dynamics

Carl Friedrichs, Virginia Institute of Marine Science

Outline of Presentation:

- Richardson number influence on coastal/estuarine mixing
- Derivation of stratified “overlap” layer structure
- Under-saturated (weakly stratified) sediment suspensions
- Critically saturated (Ri_{cr} -controlled) sediment suspensions
- Hindered settling, over-saturation, and collapse of turbulence



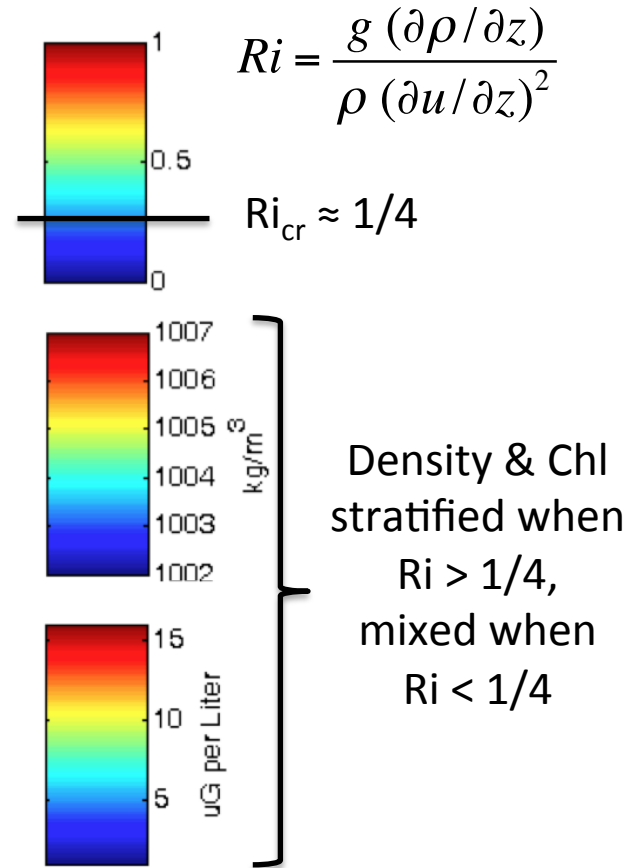
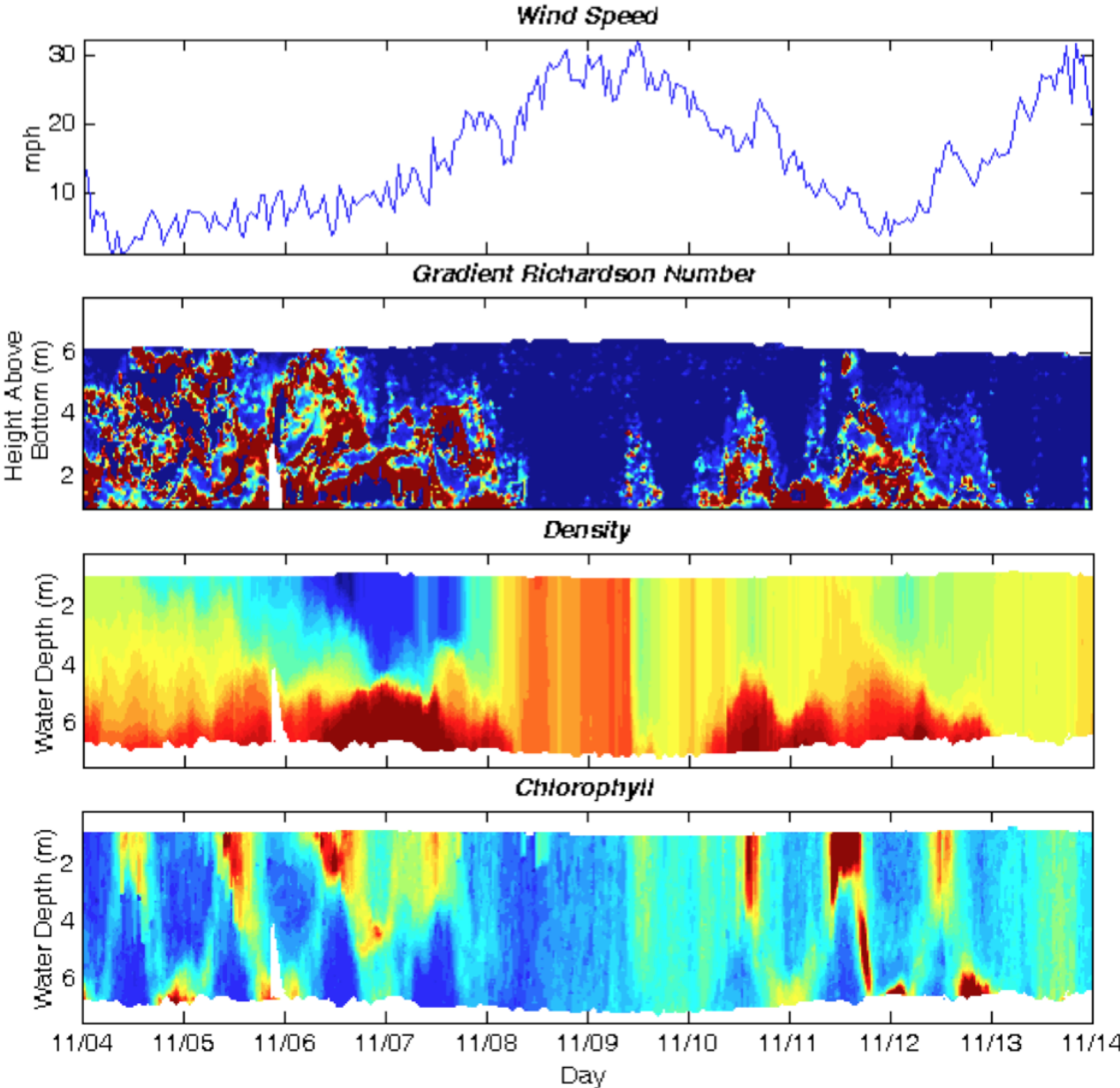
Presented at University of Delaware, 9/27/11

Time-series of suspended sediment in York River estuary (Friedrichs et al. 2000)

Gradient Richardson Number (Ri) = $\frac{\text{density stratification}}{\text{velocity shear}}$

Shear instabilities occur for $Ri < Ri_{cr}$
 “ “ suppressed for $Ri > Ri_{cr}$

Hans Paerl et al. (2004)
 Neuse River Estuary
 observations from 2003

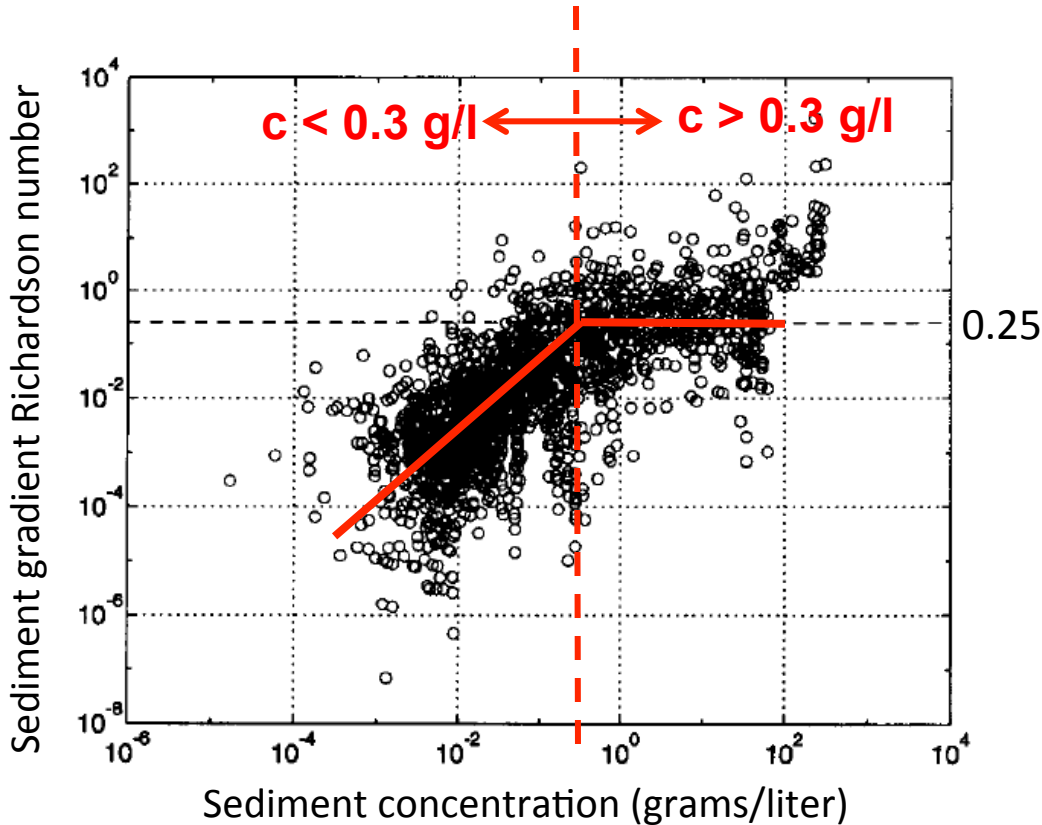


OUTLINE: **1) Ri # importance**; 2) Overlap layer; 3) Under-saturation; 4) Critical Saturation; 5) Over-saturation

When strong currents are present, mud remains turbulent and in suspension at a concentration that gives $Ri \approx Ri_{cr} \approx 1/4$:

$$\text{Gradient Richardson Number (Ri)} = \frac{\text{density stratification}}{\text{velocity shear}}$$

Shear instabilities occur for $Ri < Ri_{cr}$
 “ “ suppressed for $Ri > Ri_{cr}$



$$Ri = \frac{\text{Stratification}}{\text{Shear}}$$

$$Ri = \frac{-g s \partial c / \partial z}{\rho_s (\partial u / \partial z)^2}$$

g = accel. of gravity
 $s = (\rho_s - \rho) / \rho$
 c = sediment mass conc.
 ρ_s = sediment density

For $c > \sim 300 \text{ mg/liter}$

$$Ri \approx Ri_{cr} \approx O(1/4)$$

Figure 5. Sediment-based gradient Richardson number as a function of sediment concentration based on measurements throughout the entire water column in all of the profiles summarized in Table 1. The dashed curve corresponds to a gradient Richardson number of 1/4.

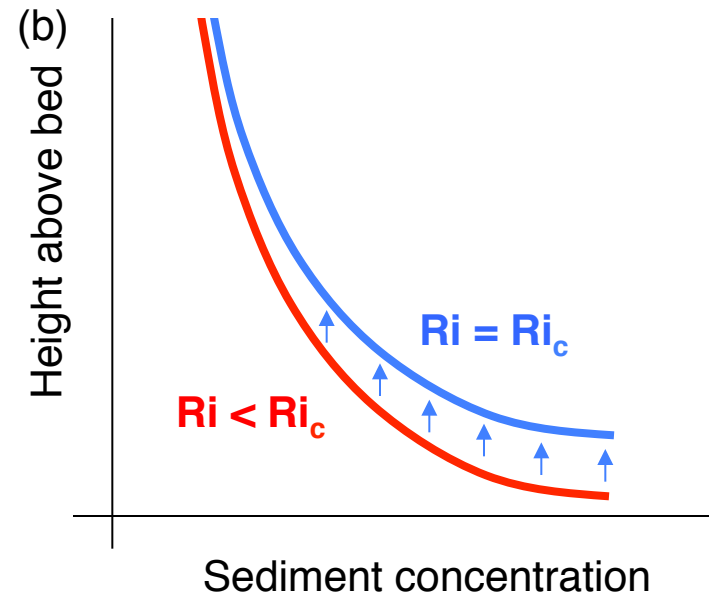
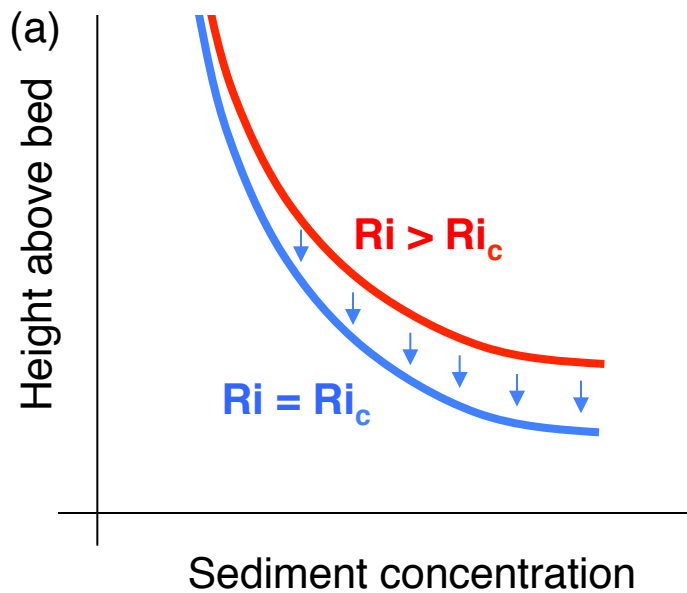
Amazon Shelf (Trowbridge & Kineke, 1994)

Are there simple, physically-based relations to predict c and du/dz related to Ri ?

Large supply of easily suspended sediment creates negative feedback:

$$\text{Gradient Richardson Number (Ri)} = \frac{\text{density stratification}}{\text{velocity shear}}$$

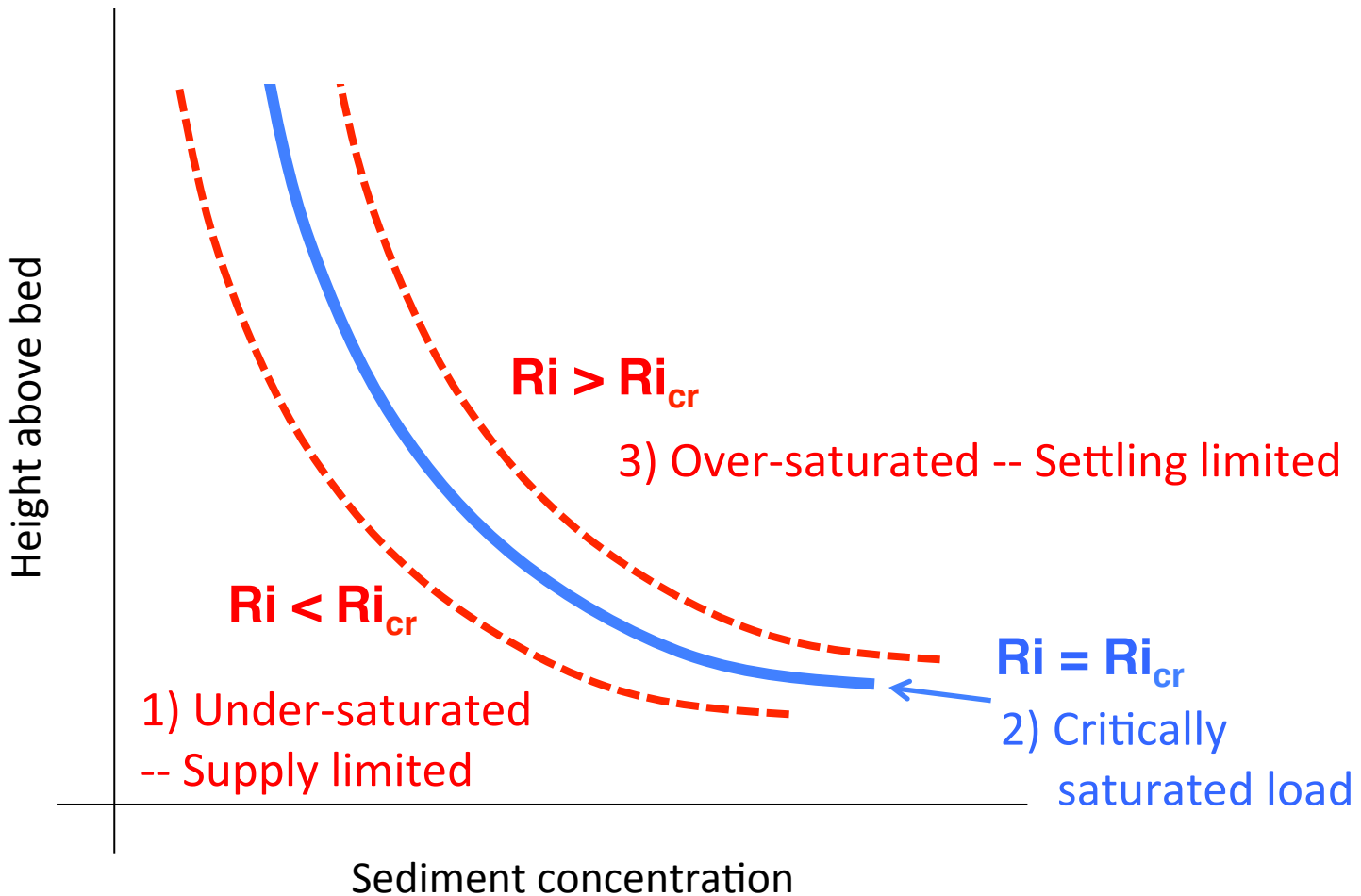
Shear instabilities occur for $Ri < Ri_{cr}$
 “ “ suppressed for $Ri > Ri_{cr}$



(a) If excess sediment enters bottom boundary layer or bottom stress decreases, $Ri \uparrow$ **beyond Ri_c** , critically damping turbulence. Sediment settles out of boundary layer. Stratification is reduced and **Ri returns to Ri_c** .

(b) If excess sediment settles out of boundary layer or bottom stress increases, $Ri \downarrow$ **below Ri_c** and turbulence intensifies. Sediment re-enters base of boundary layer. Stratification is increased in lower boundary layer and **Ri returns to Ri_c** .

Consider Three Basic Types of Suspensions

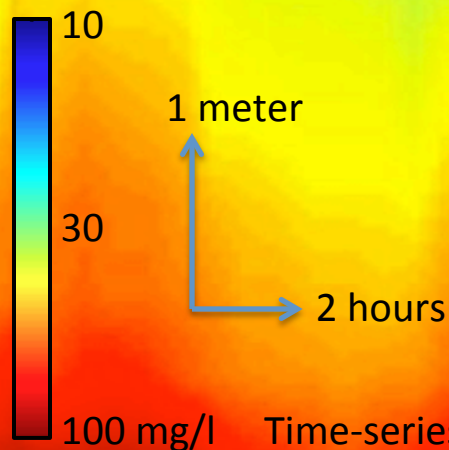


Damping of Turbulence by Suspended Sediment: Fundamental Ramifications for Sediment Dynamics

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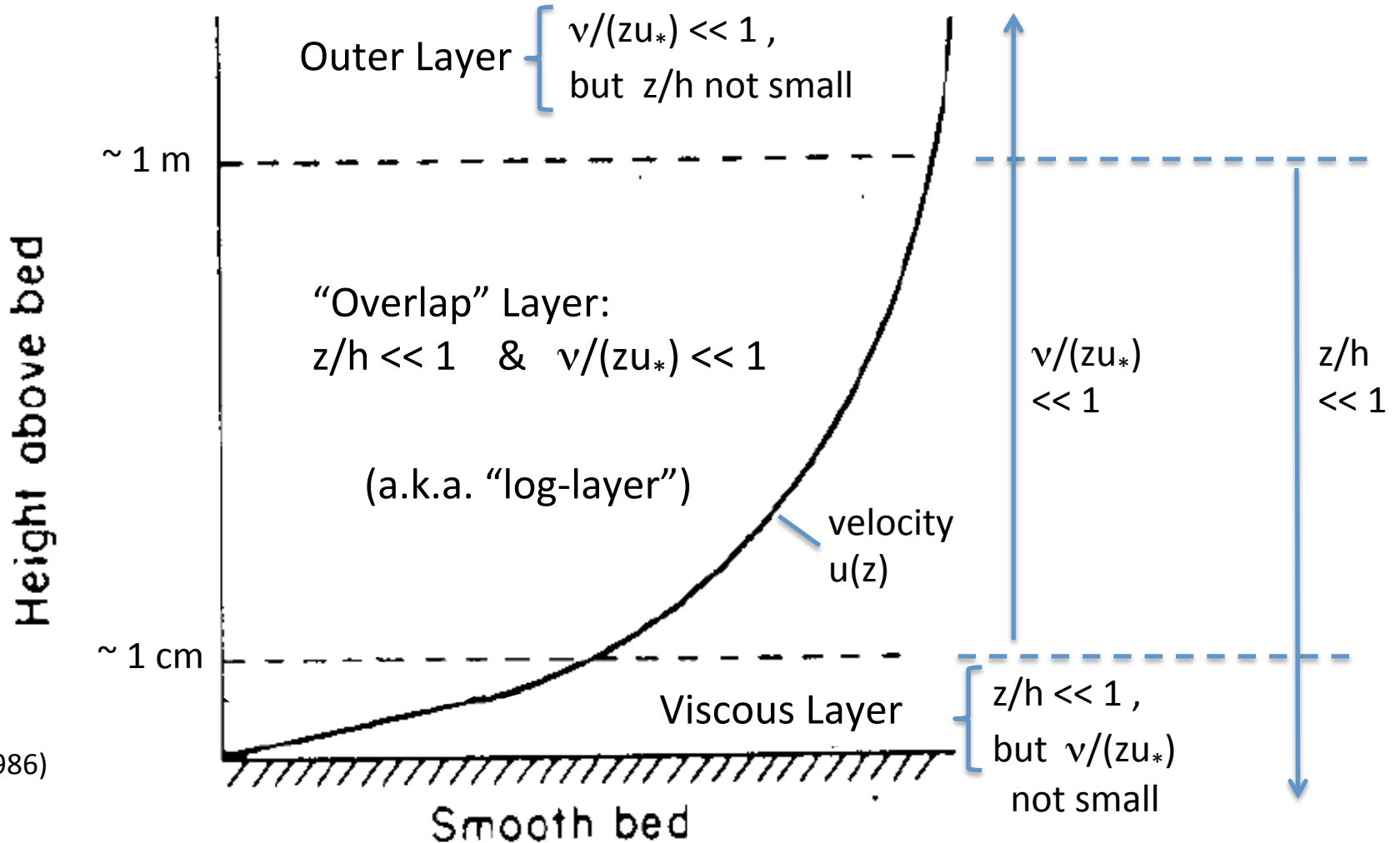
Time-series of suspended sediment in York River estuary (Friedrichs et al. 2000)

Dimensionless analysis of bottom boundary layer in the absence of stratification:

Variables $du/dz, z, h, \nu, u_*$ \longrightarrow $\frac{z}{u_*} \frac{du}{dz} = f\left(\frac{\nu}{zu_*}, \frac{z}{h}\right)$

h = thickness of bottom boundary layer, ν = kinematic viscosity, $u_* = (\tau_b/\rho)^{1/2}$ = shear velocity
 $\sim 10^{-6} \text{ m}^2/\text{s}$ $\sim 1 \text{ cm/s}$

$h \sim 10 \text{ m}$ \uparrow



(Dyer, 1986)

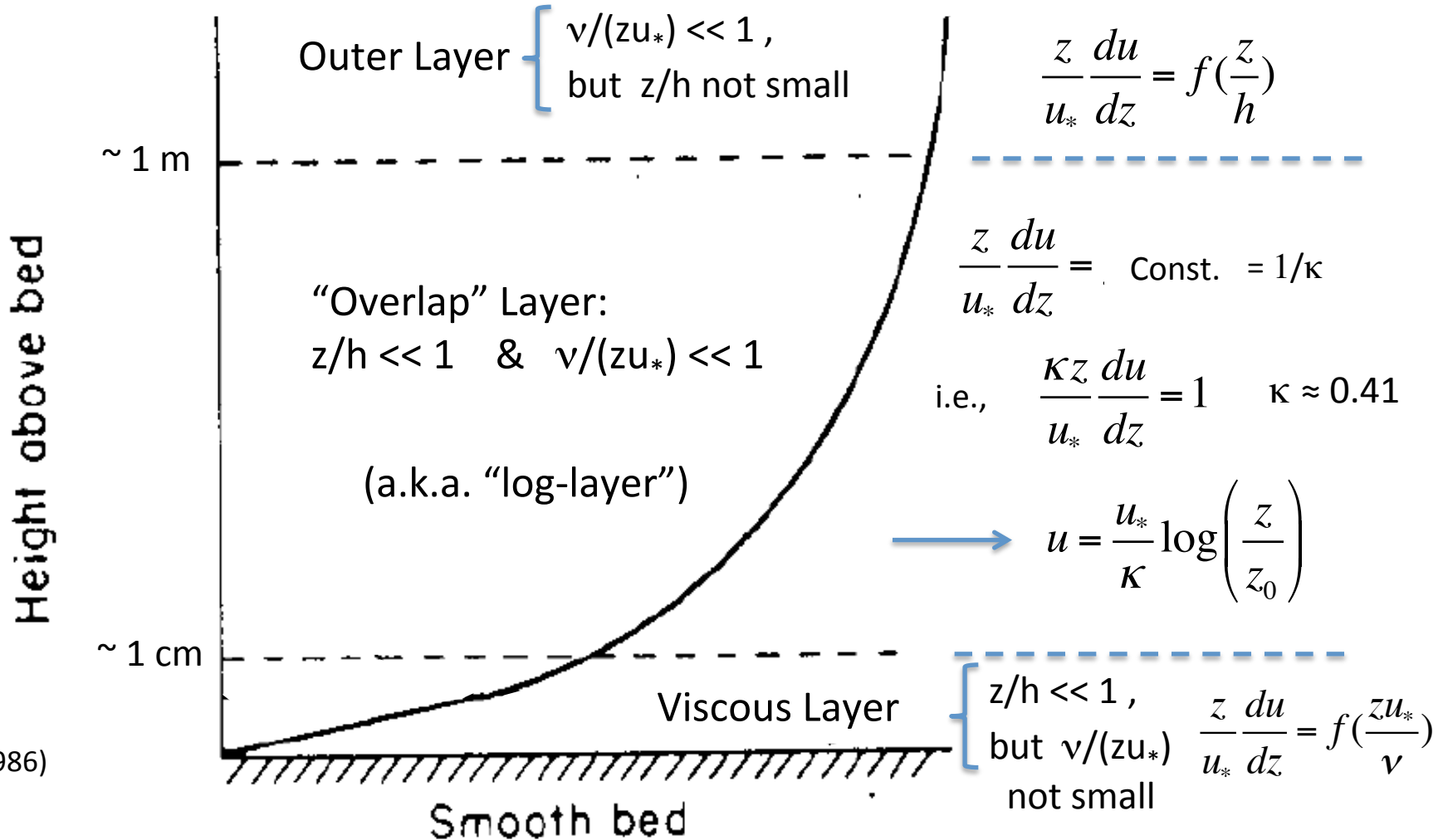
OUTLINE: 1) Ri # importance; **2) Overlap layer**; 3) Under-saturation; 4) Critical Saturation; 5) Over-saturation

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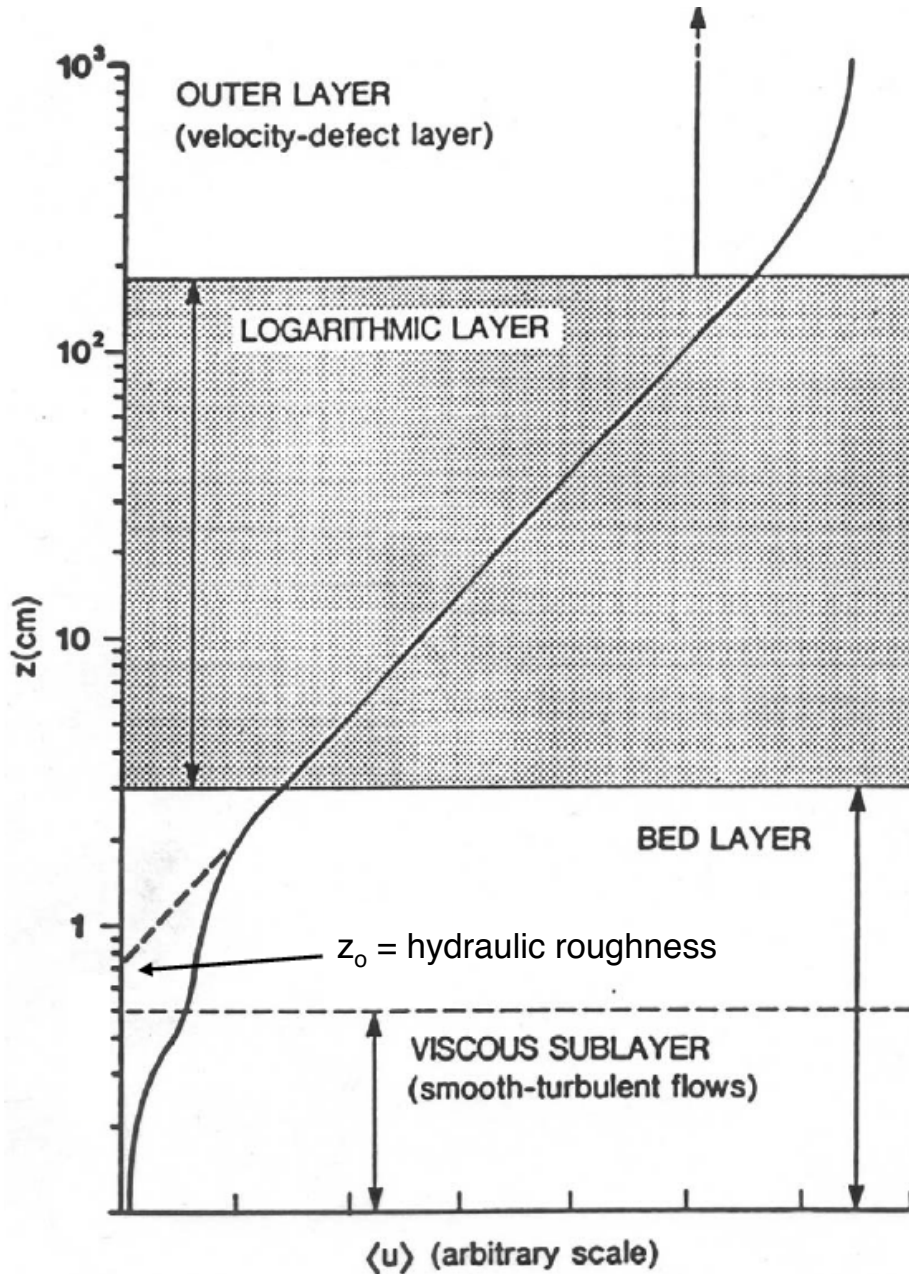
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 $\sim 10^{-6} \text{ m}^2/\text{s}$ $\sim 1 \text{ cm/s}$

$h \sim 10 \text{ m} \uparrow$



Bottom boundary layer often plotted on log(z) axis:



$$\frac{z}{u_*} \frac{du}{dz} = f(z/h)$$

$$\frac{z}{u_*} \frac{du}{dz} = \frac{1}{\kappa}$$

$$u = \frac{u_*}{\kappa} \log\left(\frac{z}{z_0}\right)$$

“Overlap” layer

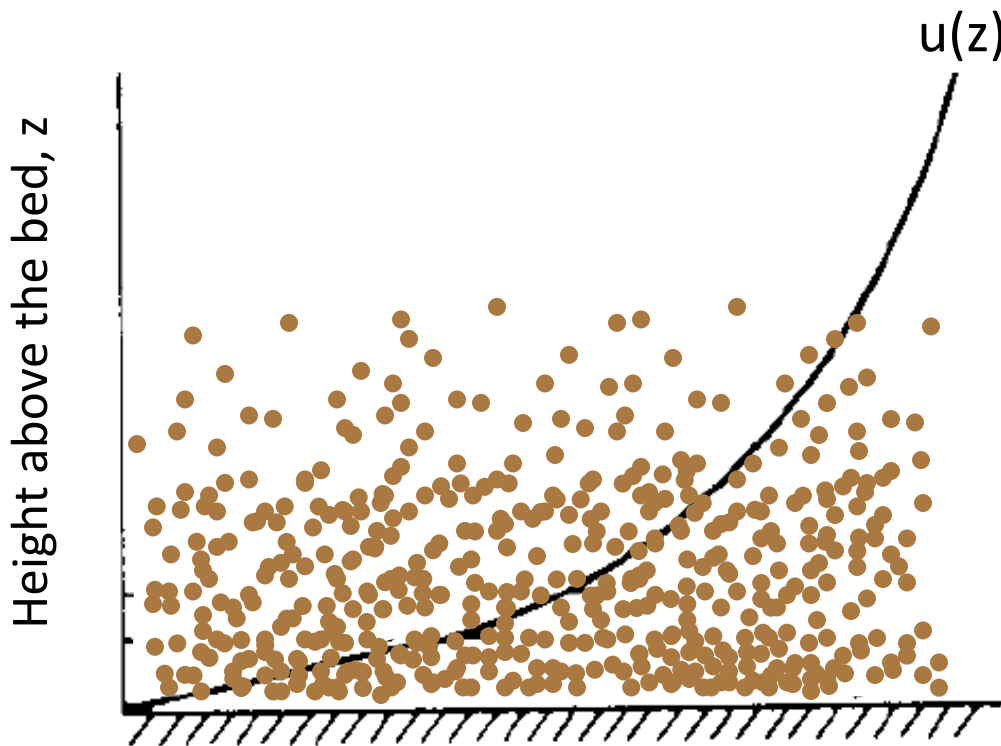
$$\frac{z}{u_*} \frac{du}{dz} = f(zu_* / \nu)$$

$z/h \ll 1$

$\nu / (zu_*) \ll 1$

(Wright, 1995)

Dimensionless analysis of overlap layer with (sediment-induced) stratification:



Additional variable
 b = Turbulent buoyancy flux

$$b = \frac{gs \langle c' w' \rangle}{\rho_s}$$

$s = (\rho_s - \rho) / \rho \approx 1.6$
 c = sediment mass conc.
 w = vertical fluid vel.

$$\frac{\kappa z}{u_*} \frac{du}{dz} = 1$$

$$\longrightarrow \frac{\kappa z}{u_*} \frac{du}{dz} = f\left(\frac{b\kappa z}{u_*^3}\right)$$

Dimensionless ratio

$$\frac{b\kappa z}{u_*^3} \equiv \zeta = \text{“stability parameter”}$$

Deriving impact of z on structure of overlap (a.k.a. “log” or “wall”) layer

$$\frac{\kappa z}{u_*} \frac{du}{dz} = f\left(\frac{b\kappa z}{u_*^3}\right) \longrightarrow \frac{\kappa z}{u_*} \frac{du}{dz} = f(\zeta)$$

Rewrite $f(\zeta)$ as Taylor expansion around $\zeta = 0$:

$$\frac{\kappa z}{u_*} \frac{du}{dz} = f(\zeta) = \underbrace{f|_{\zeta=0}}_{=1} + \zeta \underbrace{\left. \frac{df}{d\zeta} \right|_{\zeta=0}}_{=\alpha} + \frac{\zeta^2}{2} \underbrace{\left. \frac{d^2 f}{d\zeta^2} \right|_{\zeta=0}}_{\approx 0} + \dots \approx 0$$

$$\longrightarrow \frac{\kappa z}{u_*} \frac{du}{dz} = 1 + \alpha \zeta \longrightarrow u = \frac{u_*}{\kappa} \left[\log\left(\frac{z}{z_0}\right) + \alpha \int_{z_0}^z \left(\frac{\zeta}{z}\right) dz \right]$$

From atmospheric studies, $\alpha \approx 4 - 5$

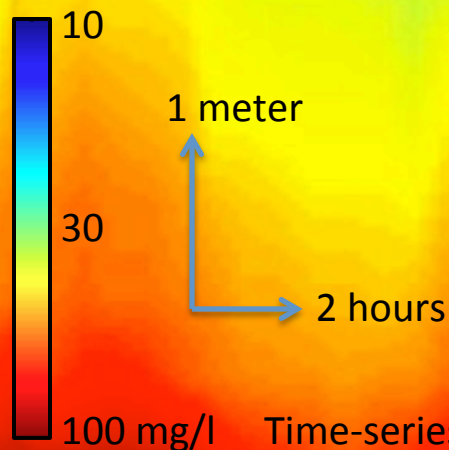
If there is stratification ($\zeta > 0$) then u(z) increases faster with ζ than homogeneous case.

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Time-series of suspended sediment in York River estuary (Friedrichs et al. 2000)

$$u = \frac{u_*}{\kappa} \left[\log\left(\frac{z}{z_0}\right) + \alpha \int_{z_0}^z \left(\frac{\zeta}{z}\right) dz \right] \quad \text{Eq. (1)}$$

-- Case (i): No stratification near the bed ($\zeta = 0$ at $z = z_0$). Stratification and ζ increase with increased z .

-- Eq. (1) gives u increasing faster and faster with z relative to classic well-mixed log-layer. (e.g., halocline being mixed away from below)

-- Case (ii): Stratified near the bed ($\zeta > 0$ at $z = z_0$). Stratification and ζ decreases with increased z .

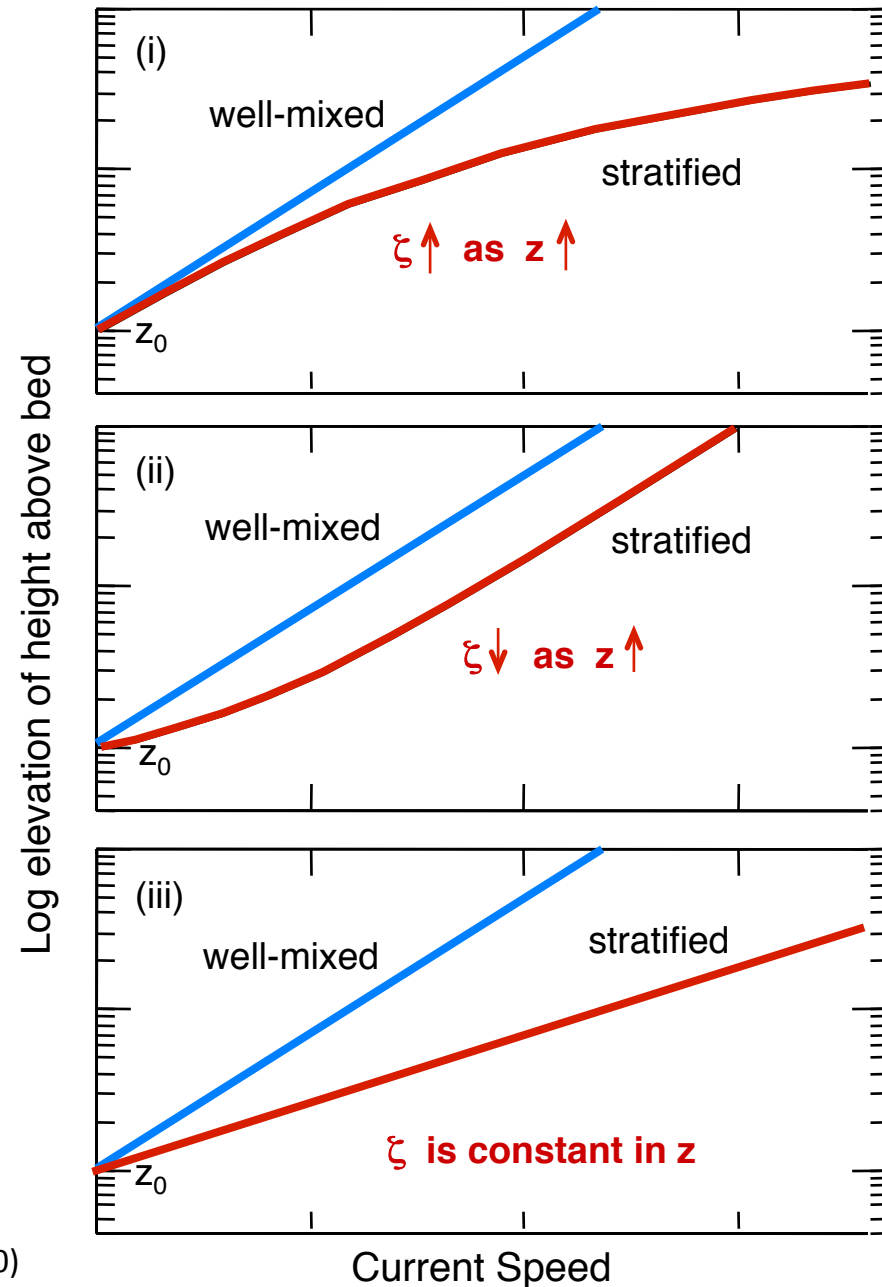
-- Eq. (1) gives u initially increasing faster than u , but then matching du/dz from neutral log-layer. (e.g., fluid mud being entrained by wind-driven flow)

-- Case (iii): uniform ζ with z . Eq (1) integrates to

$$u = \frac{u_*}{\kappa} (1 + \alpha \zeta) \log\left(\frac{z}{z_0}\right)$$

-- u remains logarithmic, but shear is increased by a factor of $(1 + \alpha \zeta)$

(Friedrichs et al, 2000)



Effect of stratification (via ζ) on eddy viscosity (A_z)

$$\frac{\kappa z}{u_*} \frac{du}{dz} = 1 + \alpha \zeta$$

Overlap layer scaling
modified by buoyancy flux

$$u_*^2 = A_z \frac{du}{dz}$$

Definition of
eddy viscosity

Eliminate du/dz and get
$$A_z = \frac{\kappa u_* z}{(1 + \alpha \zeta)}$$

-- As stratification increases (larger ζ), A_z decreases

-- If $\zeta = \text{const. in } z$, A_z increases like $u_* z$, and the result is still a log-profile.

Connect stability parameter, ζ , to shape of concentration profile, $c(z)$:

Definition of ζ :
$$\zeta = \frac{b\kappa z}{u_*^3} = \frac{g_s \langle c' w' \rangle \kappa z}{\rho_s u_*^3}$$

Rouse balance
(Reynolds flux
= settling):

$$\frac{g_s \langle c' w' \rangle \kappa z}{u_*^3} = c w_s$$

Combine to eliminate $\langle c' w' \rangle$:
$$\zeta = \left(\frac{g_s w_s \kappa}{\rho_s u_*^3} \right) c z$$

$\zeta = \text{const. in } z$ if $c \sim z^{-1}$
(Assuming w_s is const. in z)

$$\zeta = \left(\frac{g_s w_s K}{\rho_s u_*^3} \right) c z \quad \zeta = \text{const. in } z \text{ if } c \sim z^{-1}$$

Fit a general power-law to $c(z)$ of the form $c \sim z^{-A}$

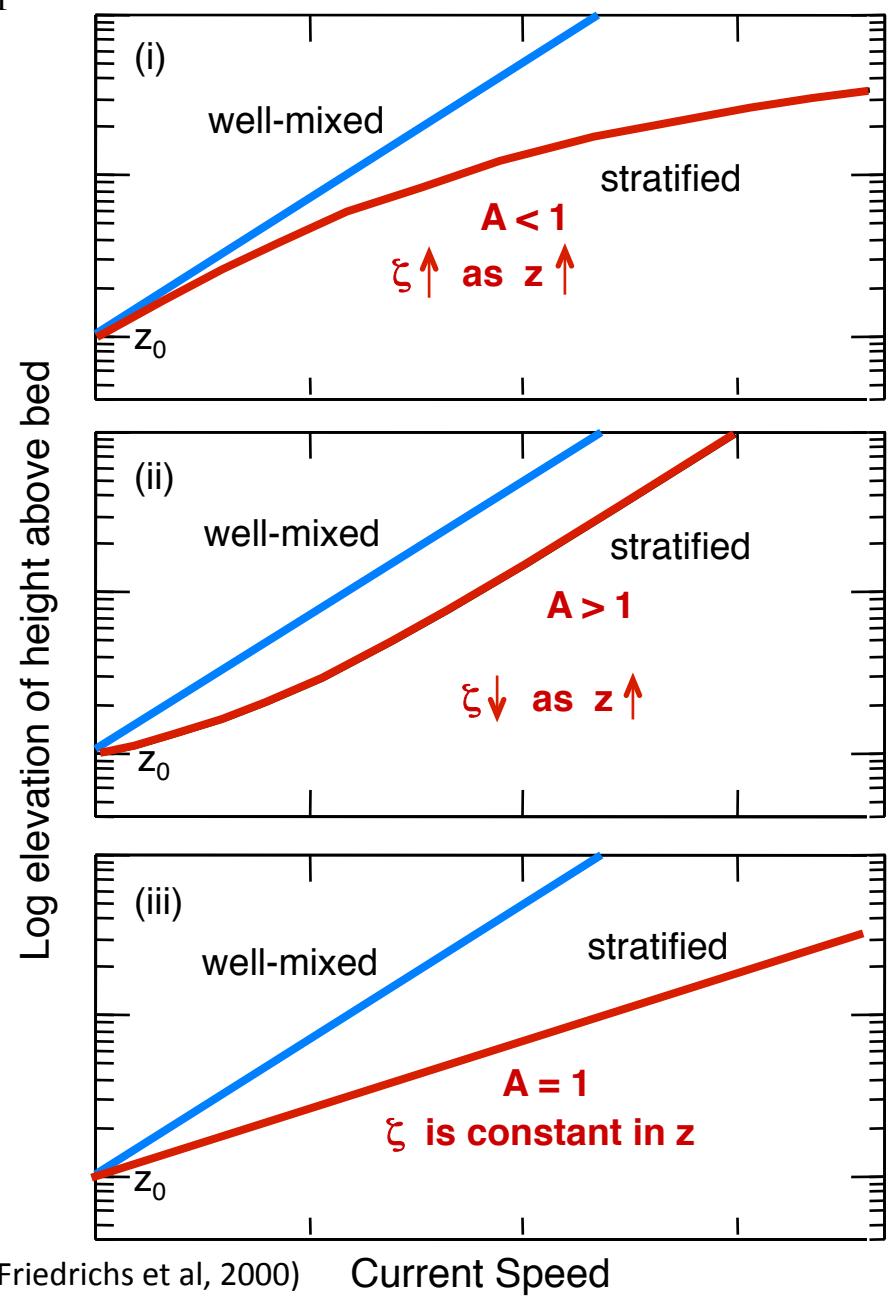
Then $\zeta \sim z^{(1-A)}$

If $A < 1$, c decreases more slowly than z^{-1}
 ζ increases with z ,
 stability increases upward,
 u is more concave-down than $\log(z)$

If $A > 1$, c increases more quickly than z^{-1}
 ζ decreases with z , stability
 becomes less pronounced upward,
 u is more concave-up than $\log(z)$

If $A = 1$, $c \sim z^{-1}$
 ζ is constant with elevation
 stability is uniform in z ,
 u follows $\log(z)$ profile

If suspended sediment concentration, $C \sim z^{-A}$
Then $A <, >, = 1$ determines shape of u profile



If suspended sediment concentration, $C \sim z^{-A}$

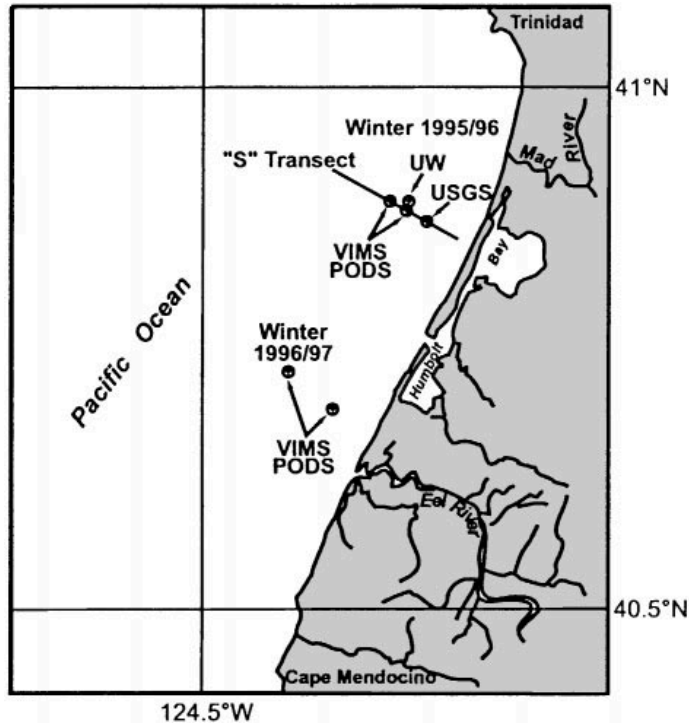
$A < 1$ predicts u more concave-down than $\log(z)$

$A > 1$ predicts u more concave-up than $\log(z)$

$A = 1$ predicts u will follow $\log(z)$

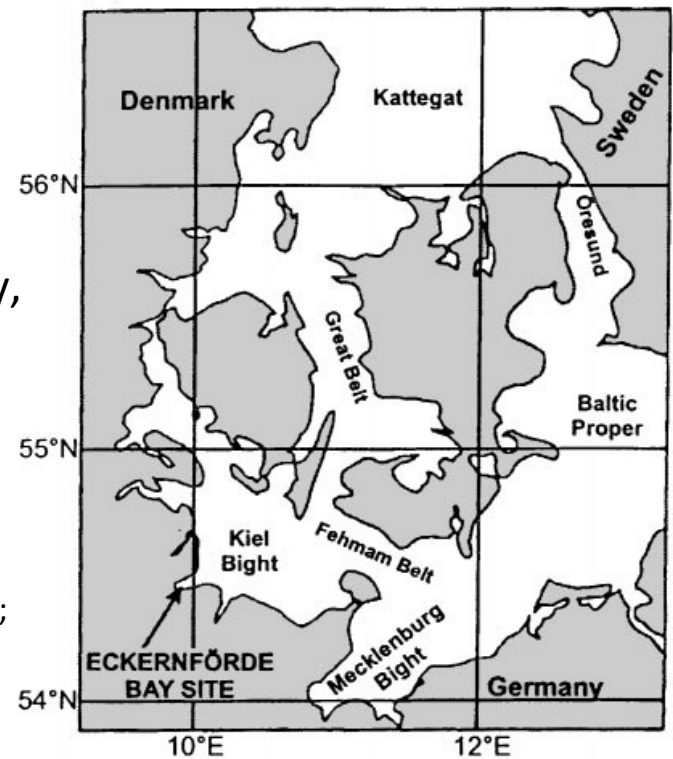
Testing this relationship using observations from bottom boundary layers:

STRATIFORM mid-shelf site,
Northern California, USA

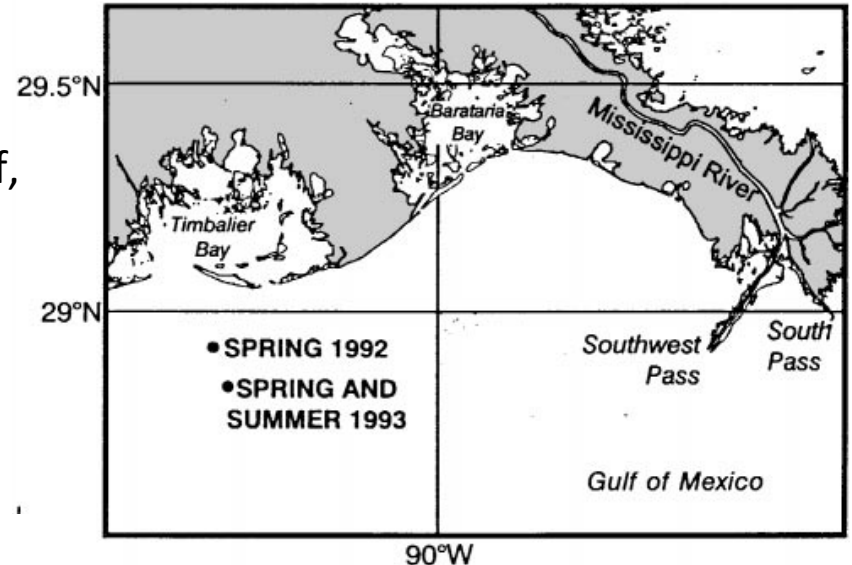


Eckernförde Bay,
Baltic Coast,
Germany

(Friedrichs & Wright, 1997;
Friedrichs et al, 2000)



Inner shelf,
Louisiana
USA



OUTLINE: 1) R_i # importance; 2) Overlap layer; **3) Under-saturation**; 4) Critical Saturation; 5) Over-saturation

If suspended sediment concentration, $C \sim z^{-A}$

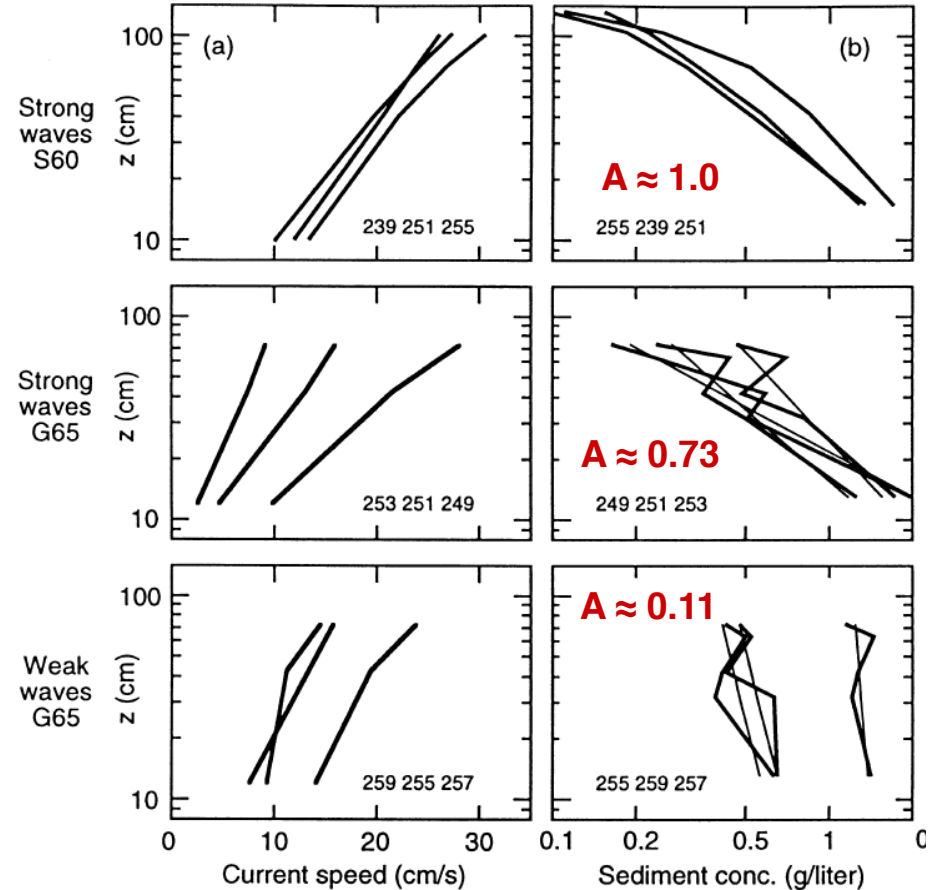
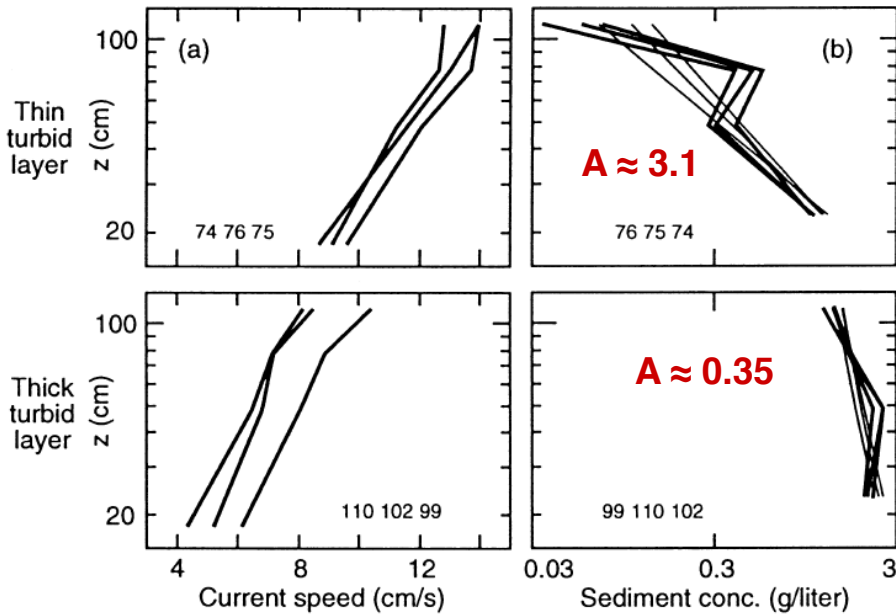
$A < 1$ predicts u more concave-down than $\log(z)$

$A > 1$ predicts u more concave-up than $\log(z)$

$A = 1$ predicts u will follow $\log(z)$

STATAFORM mid-shelf site,
Northern California, USA,
1995, 1996

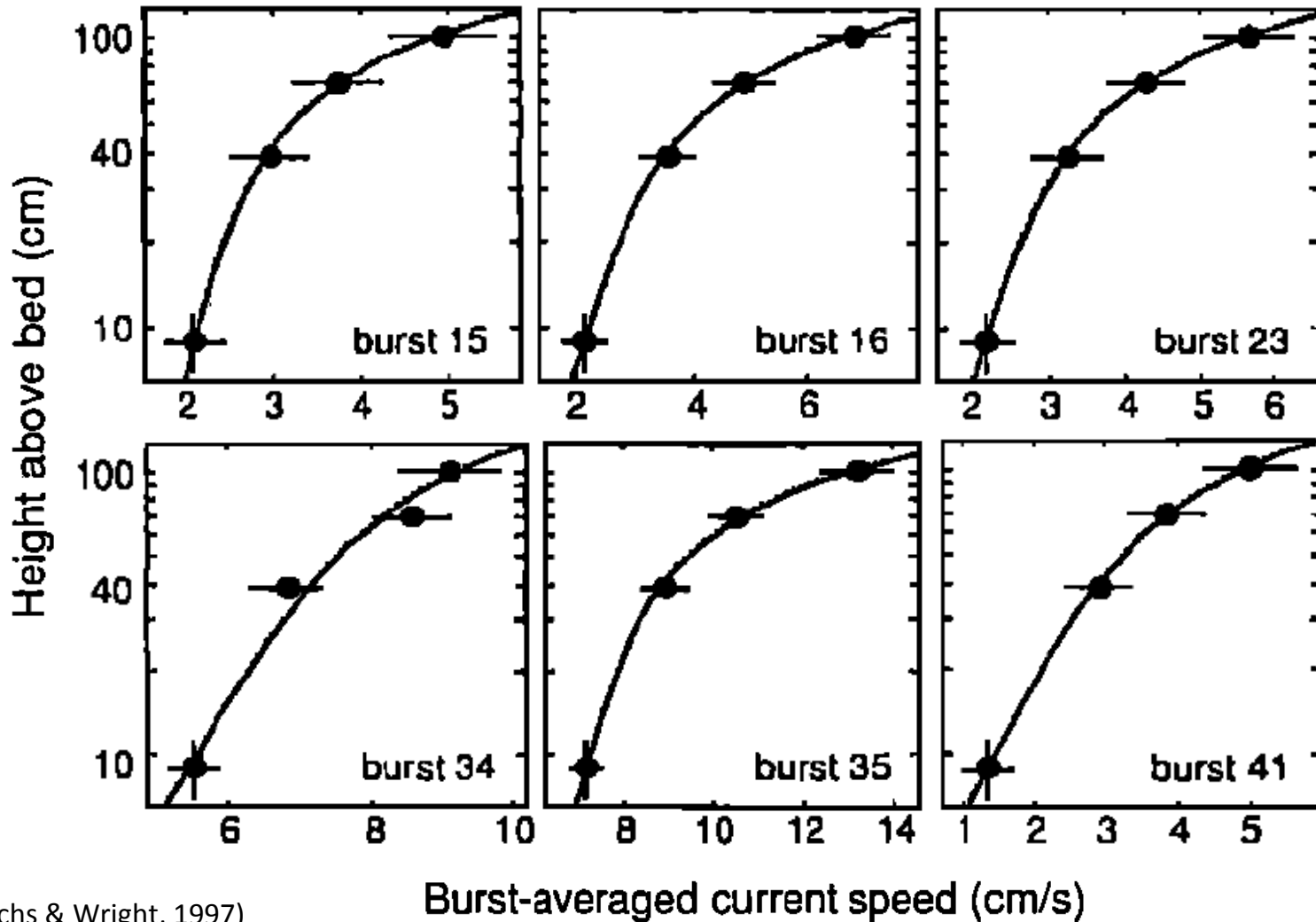
Inner shelf, Louisiana, USA,
1993



- Smallest values of $A < 1$ are associated with concave-downward velocities on log-plot.
- Largest value of $A > 1$ is associated with concave-upward velocities on log-plot.
- Intermediate values of $A \approx 1$ are associated with straightest velocities on log-plot.

OUTLINE: 1) Ri # importance; 2) Overlap layer; **3) Under-saturation**; 4) Critical Saturation; 5) Over-saturation

Eckernförde Bay, Baltic Coast, Germany, spring 1993

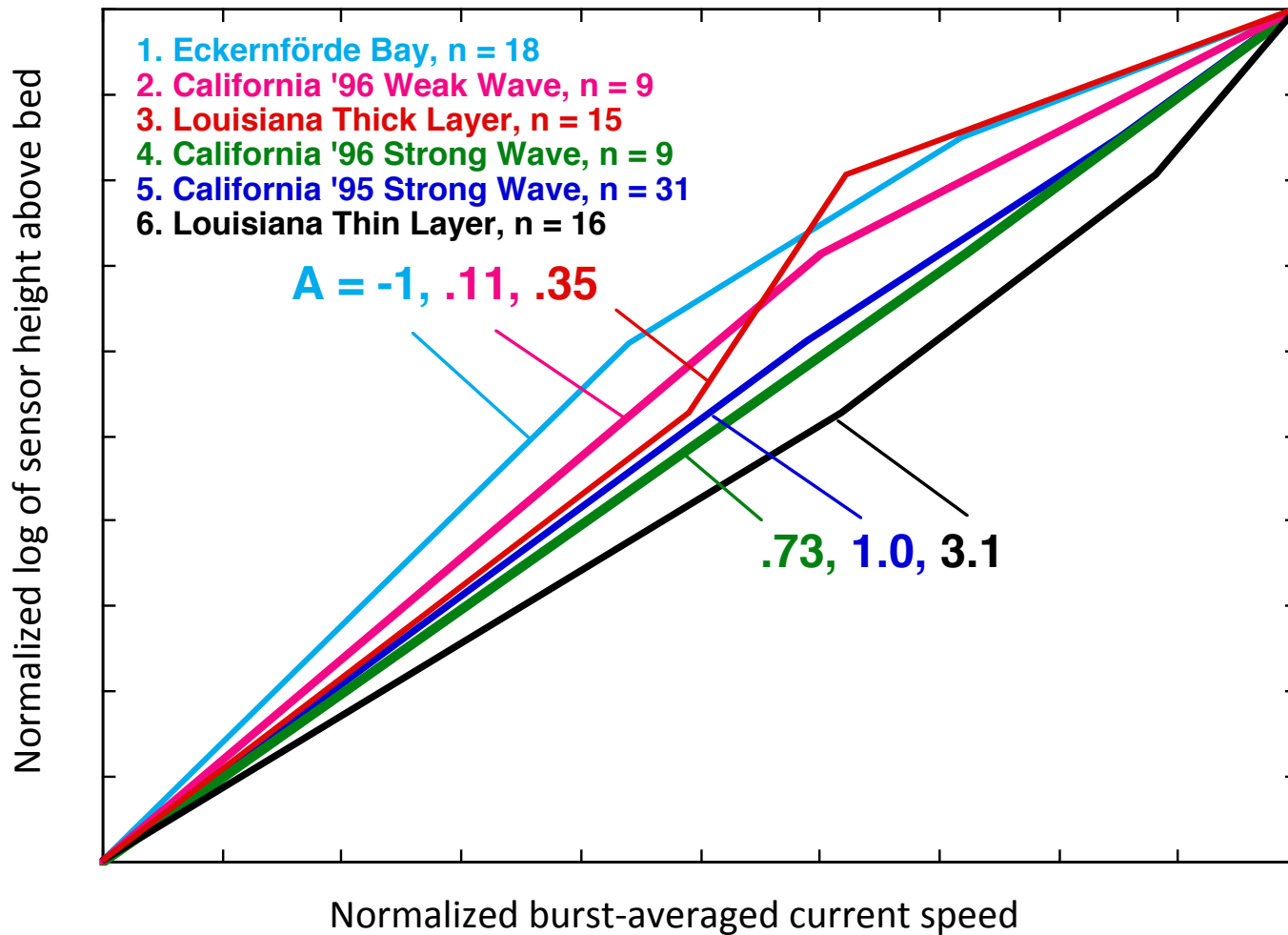


(Friedrichs & Wright, 1997)

-- Salinity stratification that increases upwards cannot be directly represented by $c \sim z^{-A}$. Friedrichs et al. (2000) argued that this case is dynamically analogous to $A \approx -1$.

OUTLINE: 1) Ri # importance; 2) Overlap layer; **3) Under-saturation**; 4) Critical Saturation; 5) Over-saturation

Observations showing effect of concentration exponent A on shape of velocity profile



Observations also show:

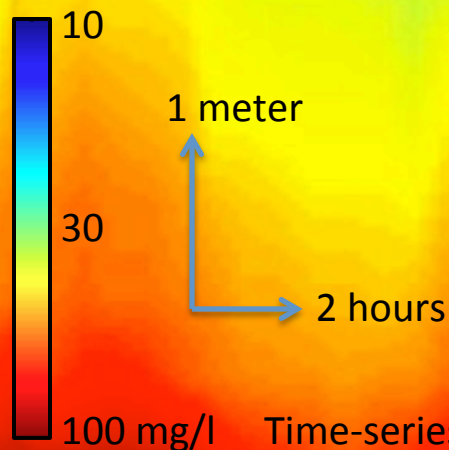
- $A < 1$, concave-down velocity
- $A > 1$, concave-up velocity
- $A \sim 1$, straight velocity profile

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Time-series of suspended sediment in York River estuary (Friedrichs et al. 2000)

Relate stability parameter, ζ , to Richardson number:

Definition of gradient Richardson number associated with suspended sediment:

$$Ri = -\frac{gs(dc/dz)}{\rho_s(du/dz)^2}$$

Original definition and application of ζ :

$$\zeta = \frac{gs \langle c'w' \rangle \kappa z}{\rho_s u_*^3} \quad \frac{\kappa z}{u_*} \frac{du}{dz} = 1 + \alpha \zeta$$

Relation found for eddy viscosity:

$$A_z = \frac{\kappa u_* z}{(1 + \alpha \zeta)}$$

Definition of eddy diffusivity:

$$-\langle c'w' \rangle = K_z \frac{dc}{dz}$$

Assume momentum and mass are mixed similarly: $A_z = K_z$

Combine all these and you get:

$$Ri = \frac{\zeta}{1 + \alpha \zeta}$$

So a constant ζ with height also leads to a constant Ri with height.

Also, if ζ increases (or decreases) with height Ri correspondingly increases (or decreases).

$$\zeta = \left(\frac{gsw_s K}{\rho_s u_*^3} \right) c z \quad Ri = \frac{\zeta}{1 + \alpha \zeta}$$

ζ and Ri const. in z if $c \sim z^{-1}$

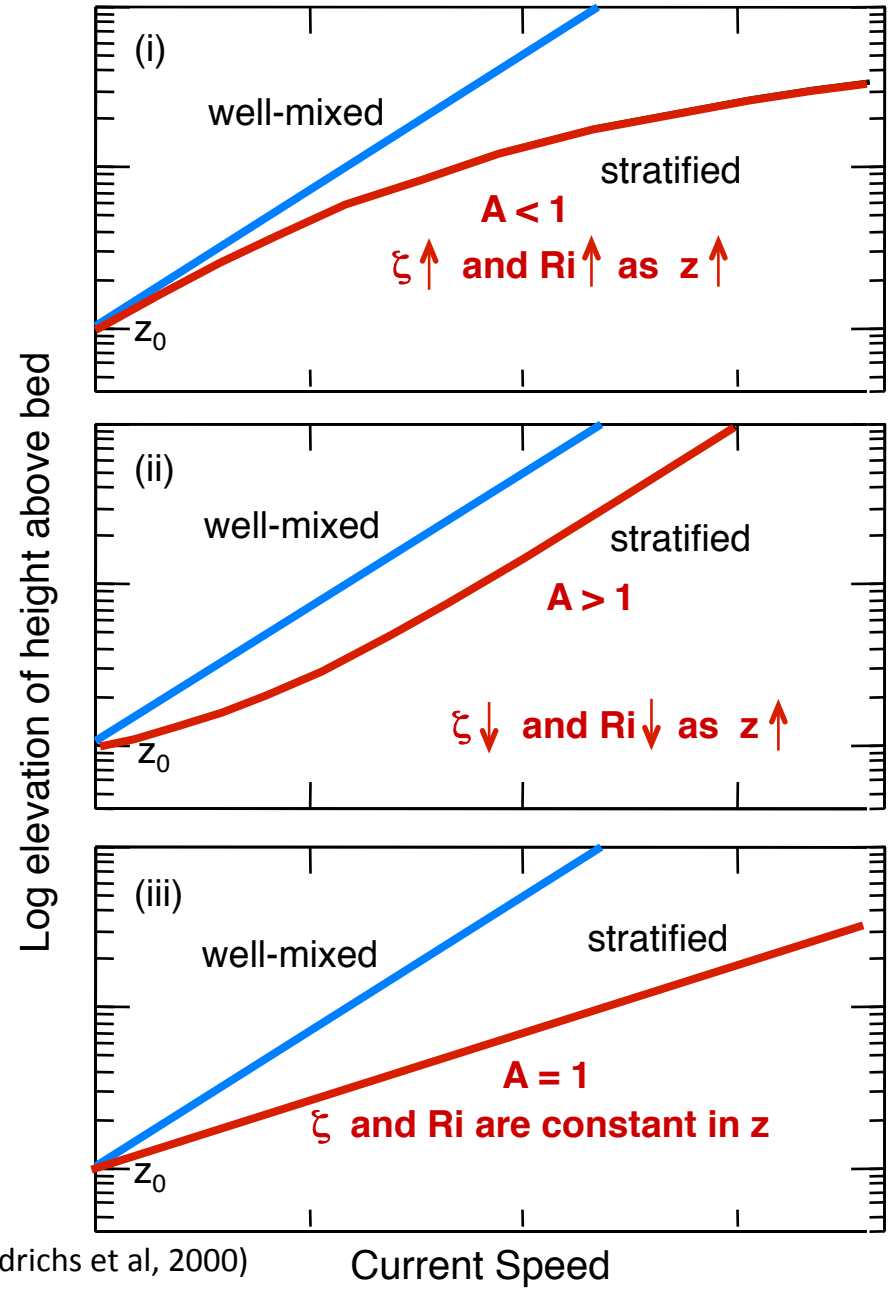
Define $c \sim z^{-A}$ then $\zeta \sim z^{(1-A)}$

If $A < 1$, c decreases more slowly than z^{-1}
 ζ and Ri increase with z ,
 stability increases upward,
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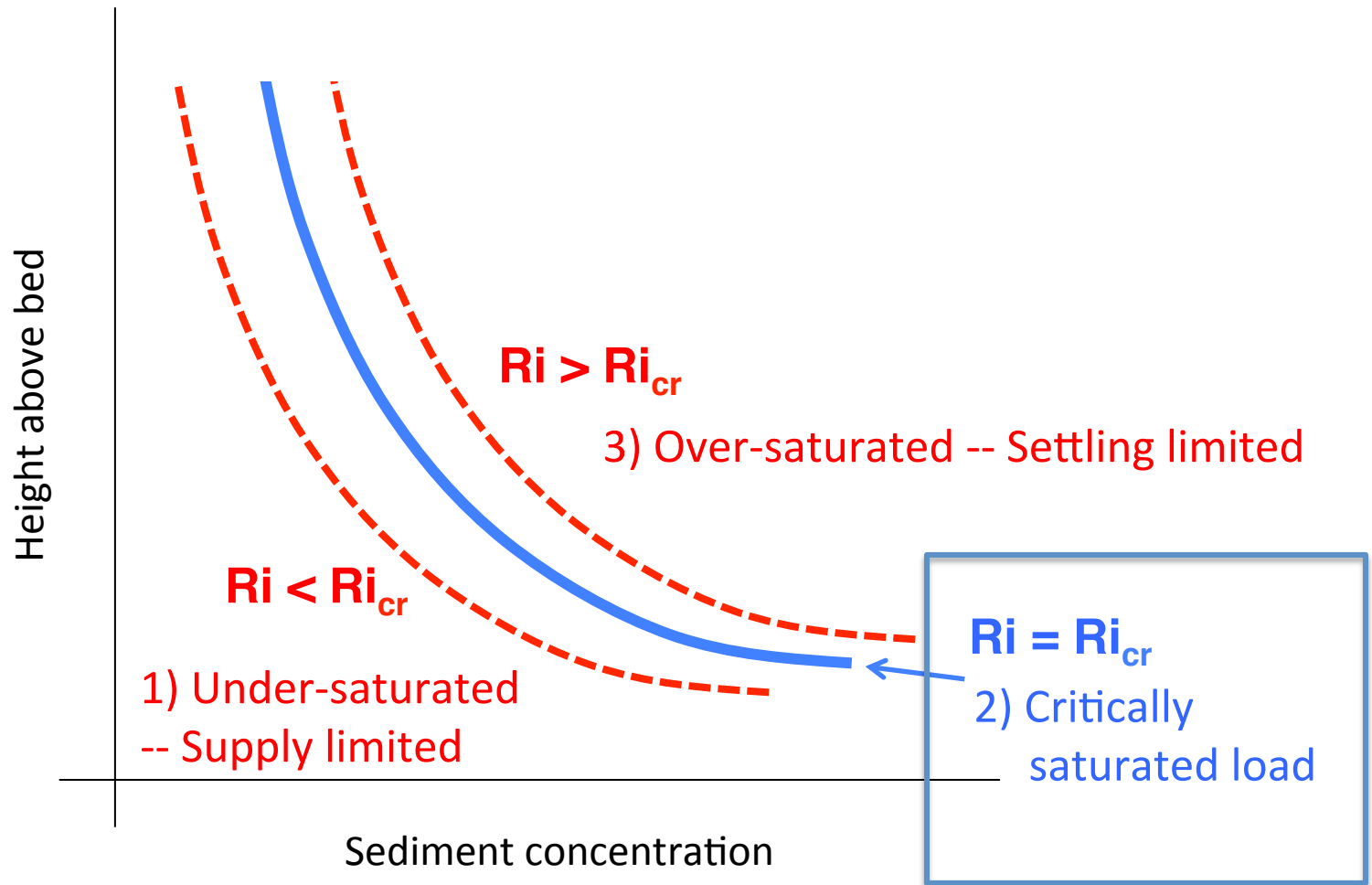
If $A = 1$, $c \sim z^{-1}$
 ζ and Ri are constant with elevation
 stability is uniform in z ,
 u follows $\log(z)$ profile

If suspended sediment concentration, $C \sim z^{-A}$
**then $A <, >, = 1$ determines shape of u profile
 and also the vertical trend in ζ and Ri**



(Friedrichs et al, 2000)

Now focus on the case where $Ri = Ri_{cr}$ (so Ri is constant in z over “log” layer)



Connection between structure of sediment settling velocity to structure of “log-layer” when $Ri = Ri_{cr}$ in z (and therefore ζ is constant in z too).

Rouse Balance:
$$w_s C = K_z \frac{dc}{dz}$$

Earlier relation for eddy viscosity:
$$K_z = \frac{\kappa u_* z}{(1 + \alpha \zeta)}$$

Eliminate K_z and integrate in z to get
$$\frac{C}{C_{ref}} = \left(\frac{z}{z_{ref}} \right)^{- \left[\frac{w_s (1 + \alpha \zeta)}{\kappa u_*} \right]}$$

But we already know $c \sim z^{-1}$ when $Ri = \text{const.}$

So
$$\frac{w_s (1 + \alpha \zeta)}{\kappa u_*} = 1 \quad \text{and} \quad 1 + \alpha \zeta = \frac{\kappa u_*}{w_s} \quad \text{when } Ri = Ri_{cr}$$

$$1 + \alpha \zeta = \frac{\kappa u_*}{w_s}$$

when $Ri = Ri_{cr}$. This also means that when $Ri = Ri_{cr}$:

$$Ri = \frac{\zeta}{1 + \alpha \zeta} \longrightarrow Ri_{cr} = \frac{w_s \zeta}{\kappa u_*}$$

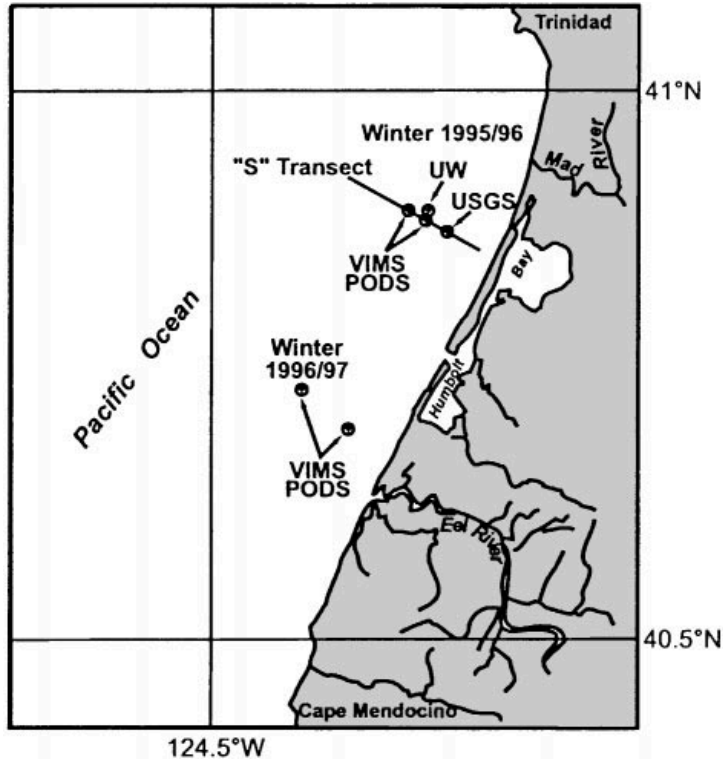
$$A_z = K_z = \frac{\kappa u_* z}{(1 + \alpha \zeta)} \longrightarrow A_z = K_z = w_s z$$

$$\frac{du}{dz} = \frac{u_*}{\kappa z} (1 + \alpha \zeta) \longrightarrow \frac{du}{dz} = \frac{u_*^2}{w_s z}$$

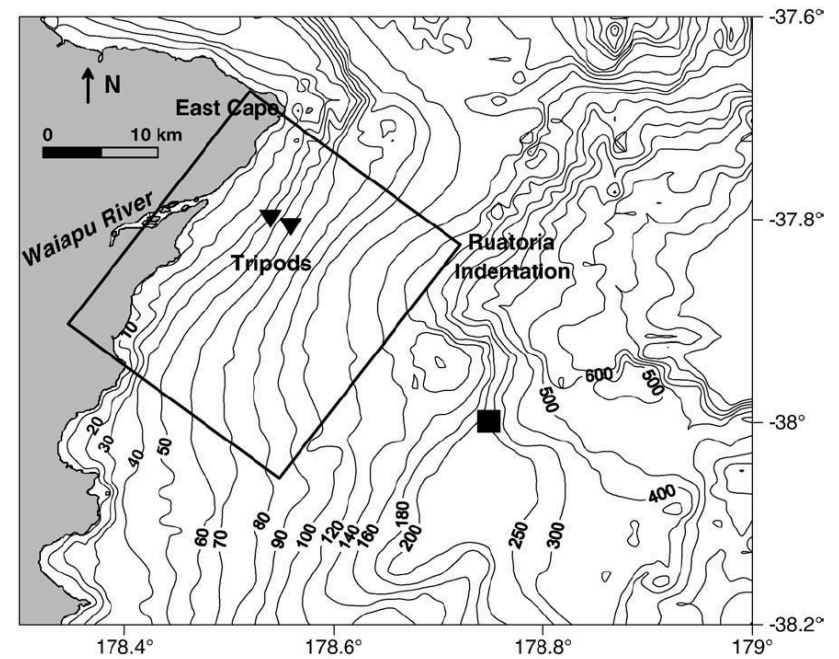
$$u = \frac{u_*}{\kappa} (1 + \alpha \zeta) \log\left(\frac{z}{z_0}\right) \longrightarrow u = \frac{u_*^2}{w_s} \log\left(\frac{z}{z_0}\right)$$

$$Ri = -\frac{gs(dc/dz)}{\rho_s (du/dz)^2} \longrightarrow c = \frac{Ri_{cr} \rho_s}{gs} \left(\frac{u_*^2}{w_s}\right)^2 z^{-1}$$

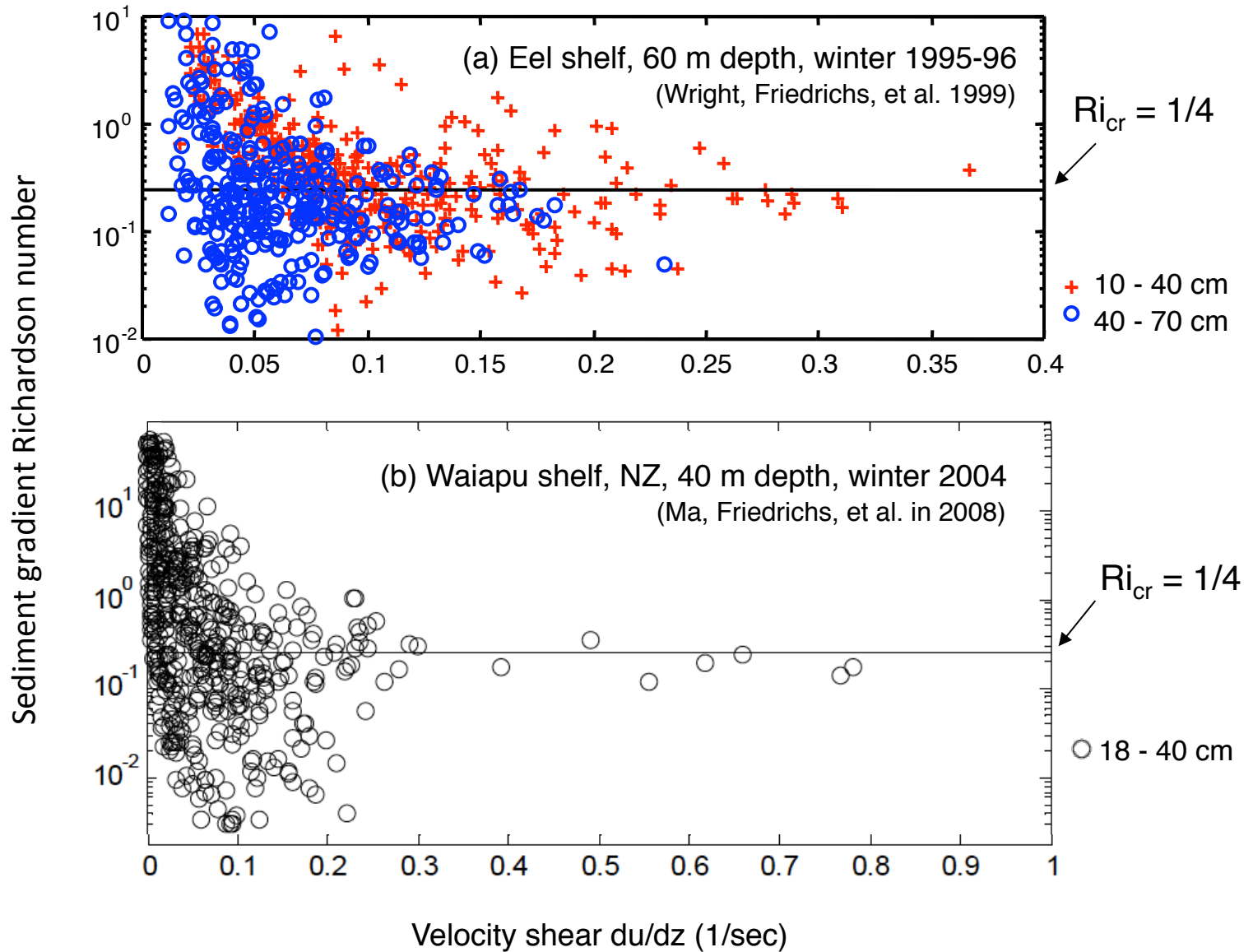
STATAFORM mid-shelf site, Northern California, USA



Mid-shelf site off Waiapu River, New Zealand

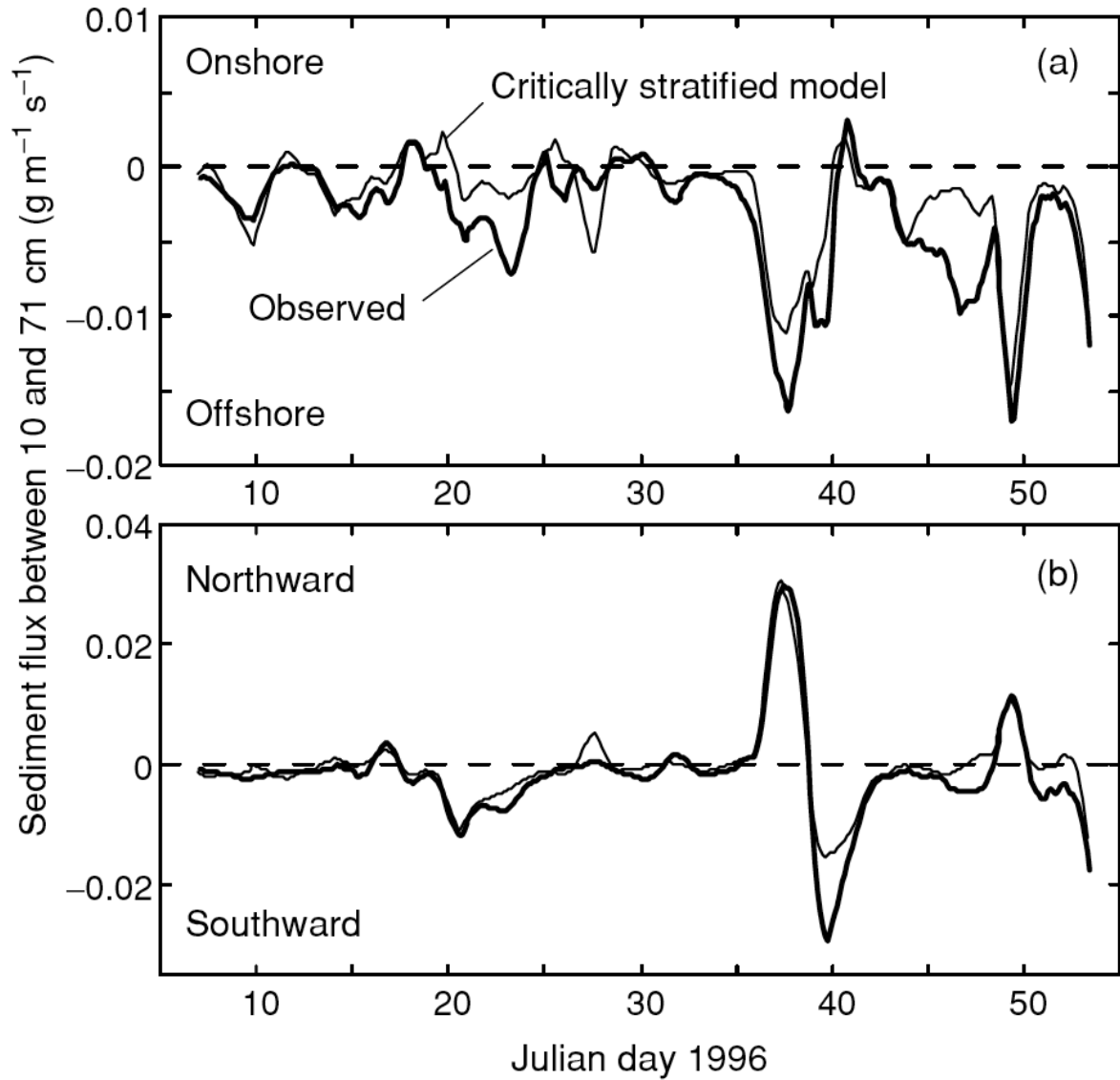


(Wright, Friedrichs et al., 1999;
Maa, Friedrichs, et al., 2010)



OUTLINE: 1) Ri # importance; 2) Overlap layer; 3) Under-saturation; **4) Critical Saturation**; 5) Over-saturation

Application of Ri_{cr} log-layer equations fo Eel shelf, 60 m depth, winter 1995-96



$$u = \frac{u_*^2}{w_s} \log\left(\frac{z}{z_0}\right)$$

$$c = \frac{Ri_{cr} \rho_s}{gS} \left(\frac{u_*^2}{w_s}\right)^2 z^{-1}$$

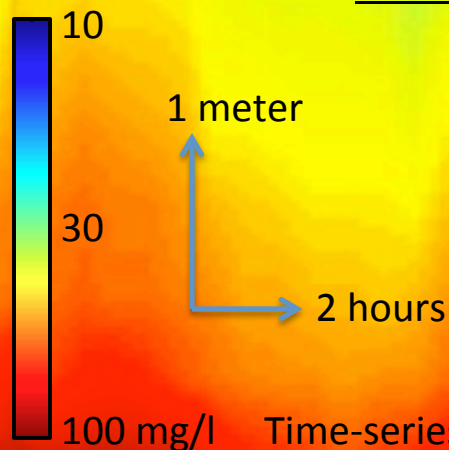
(Souza & Friedrichs, 2005)

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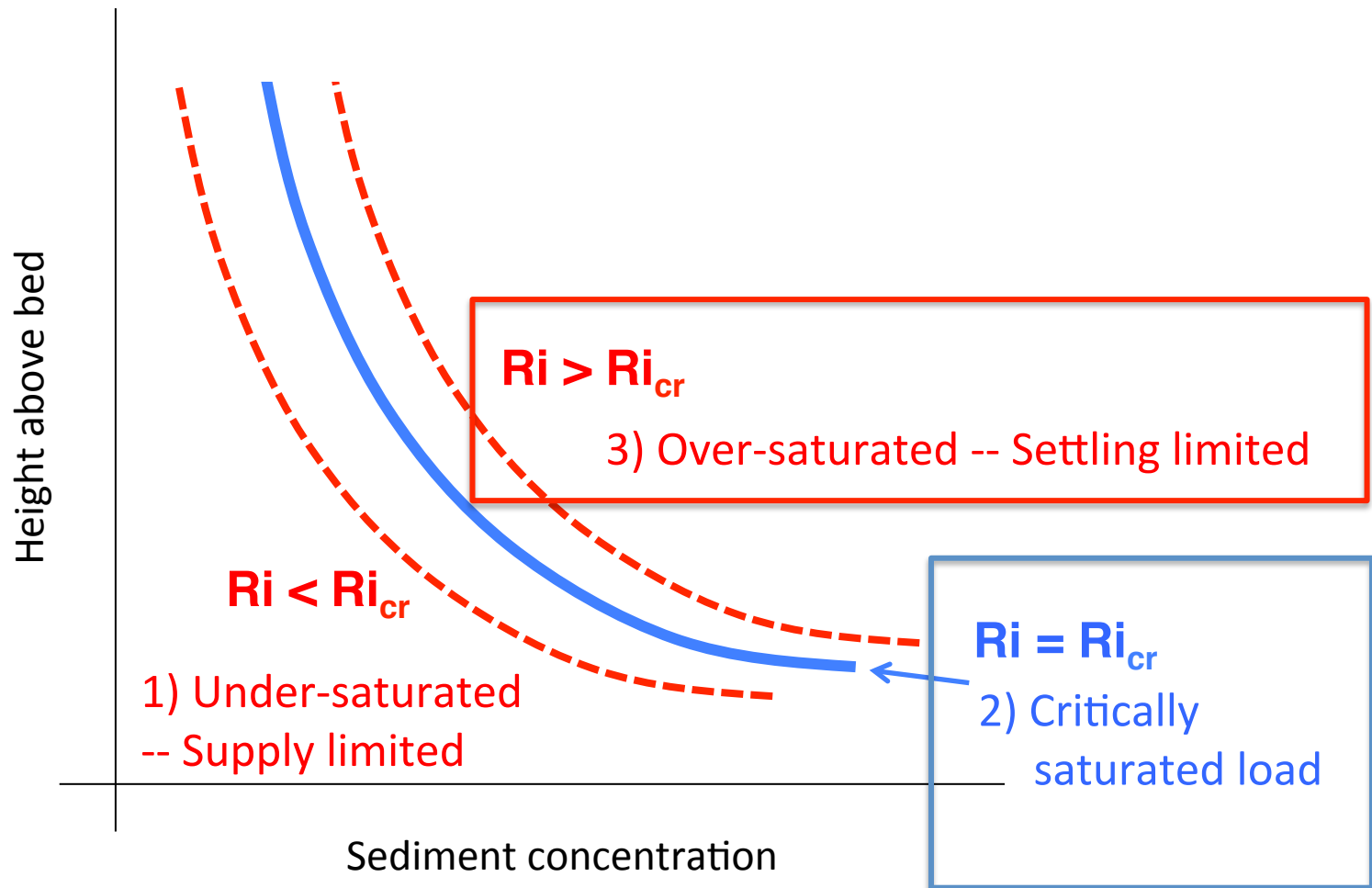
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Now also consider over-saturated cases:



(Mehta & McAnally, 2008)

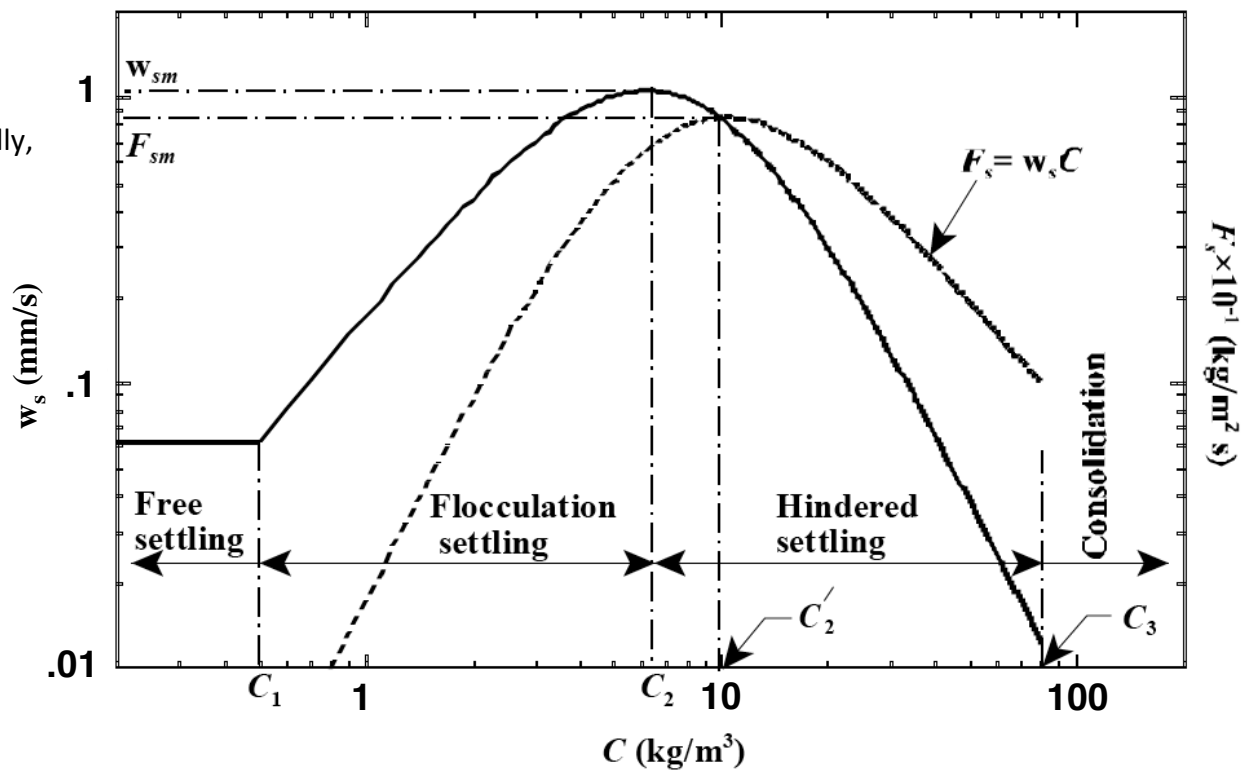


Figure 4.12 A representative plot of settling velocity and associated settling flux variation with suspension concentration.

Starting at around 5 - 8 grams/liter, the return flow of water around settling flocs creates so much drag on neighboring flocs that w_s starts to decrease with additional increases in concentration.

At ~ 10 g/l, w_s decreases so much with increased C that the rate of settling flux decreases with further increases in C . This is “hindered settling” and can cause a strong lutecline (vertical sediment gradient) to form.

A lutecline with hindered settling can cause turbulent collapse. The sediment can't leave the water column, so dC/dz keeps increasing, creating positive feedback. Ri increases further above Ri_{cr} , and more sediment to settles. Then there is more hindered settling and a stronger lutecline, increases Ri further.

OUTLINE: 1) Ri # importance; 2) Overlap layer; 3) Under-saturation; 4) Critical Saturation; **5) Over-saturation**

Fine sediment transport by tidal asymmetry in the high-concentrated Ems River: indications for a regime shift in response to channel deepening

(Winterwerp, 2011)

Fig. 6 Measured isolutals at Station 2, June 19, 1990. Note rapid settling just prior to high water and pronounced stratification during ebb (after Van Leussen 1994)

$$Ri = \frac{g s \partial c / \partial z}{\rho_s (\partial u / \partial z)^2}$$

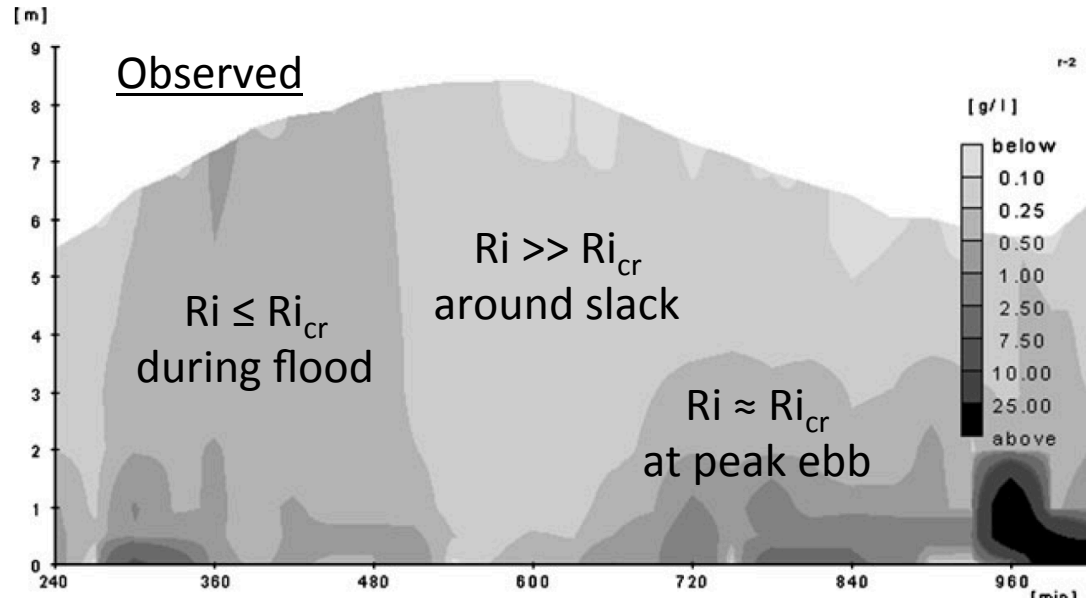
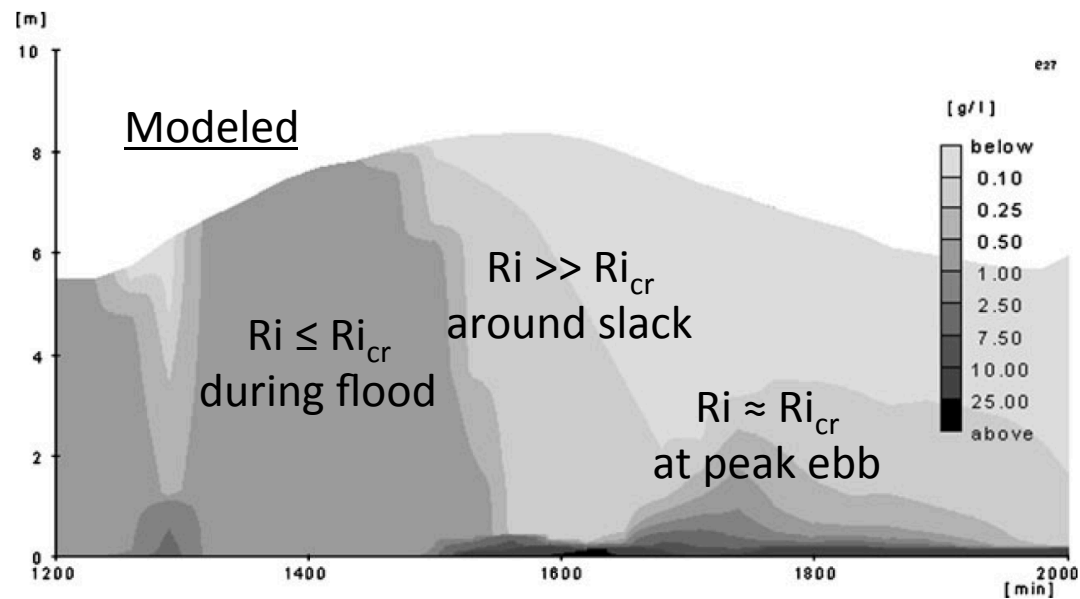


Fig. 7 Computed isolutals at Station 2, June 19, 1990. Note rapid settling just prior to high water and pronounced stratification during ebb

- 1-DV k-ε model based on components of Delft 3D
- Sediment in density formulation
- Flocculation model
- Hindered settling model

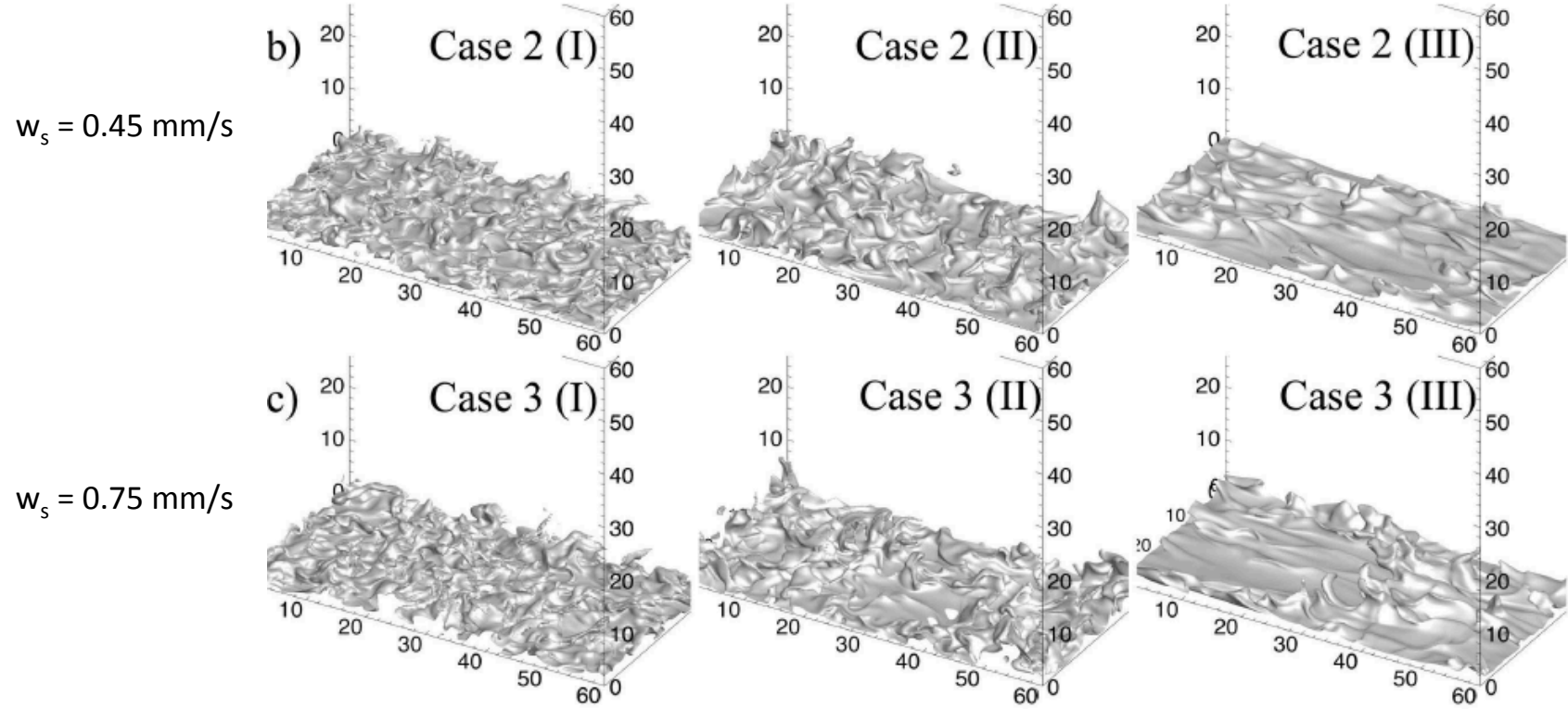
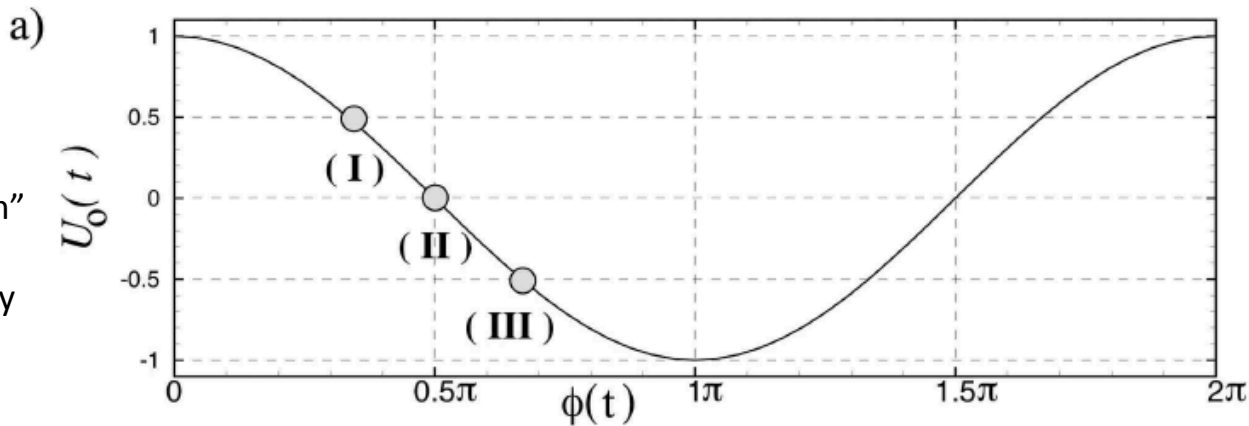


OUTLINE: 1) Ri # importance; 2) Overlap layer; 3) Under-saturation; 4) Critical Saturation; **5) Over-saturation**

A numerical investigation of lutocline dynamics and saturation of fine sediment in the oscillatory boundary layer

(Ozedemir, Hsu & Balachandar, in press)

$U \sim 60 \text{ cm/s}$
 $C \sim 10 \text{ g/liter}$
 "large eddy simulation"
 model
 Fixed sediment supply

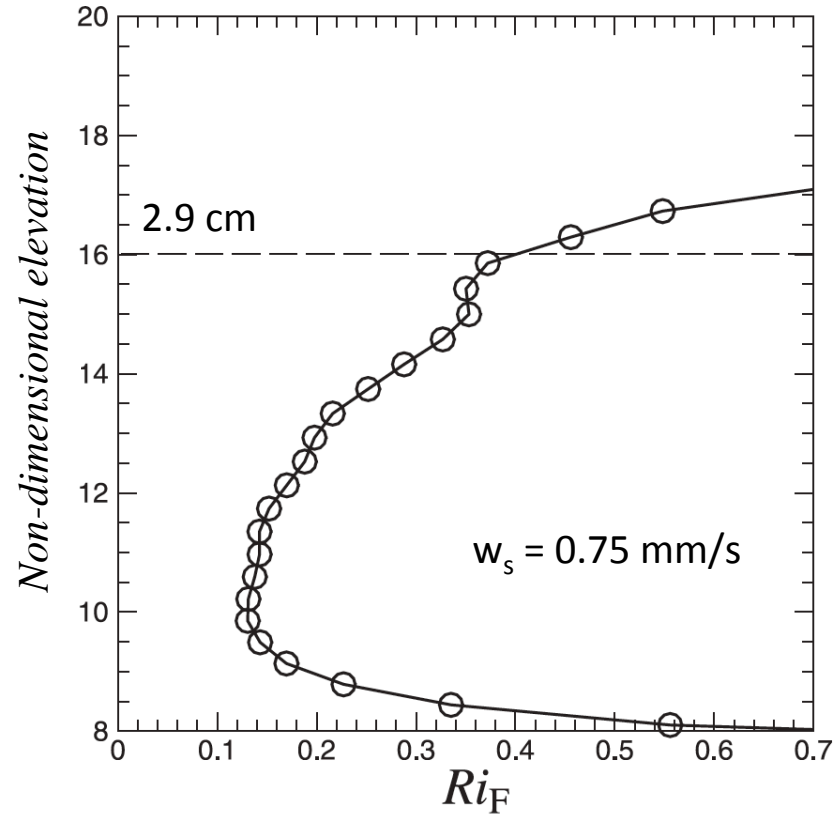
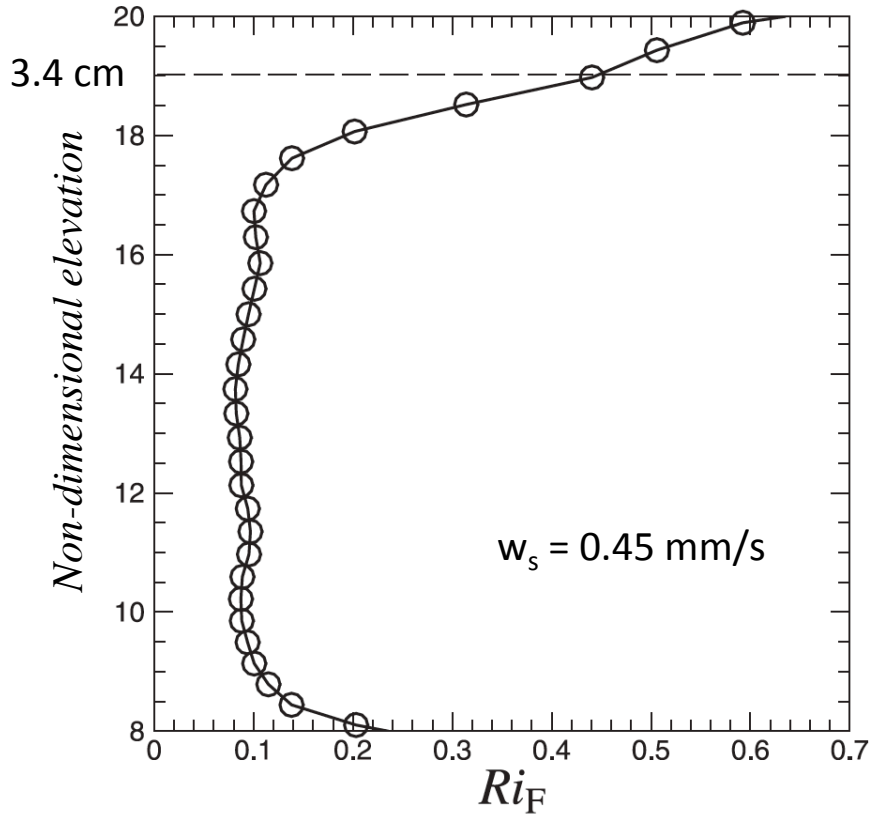


OUTLINE: 1) Ri # importance; 2) Overlap layer; 3) Under-saturation; 4) Critical Saturation; **5) Over-saturation**

$U \sim 60$ cm/s
 $C \sim 10$ g/liter
“large eddy
simulation” model

(Ozedemir, Hsu &
Balachandar, in press)

Profiles of flux Richardson number at time of max free stream U



The Richardson number is of “order” critical (relatively close to 0.25) near top of suspended layer

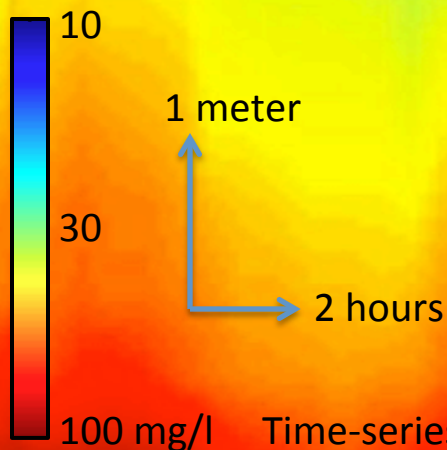
OUTLINE: 1) Ri # importance; 2) Overlap layer; 3) Under-saturation; 4) Critical Saturation; **5) Over-saturation**

Damping of Turbulence by Suspended Sediment: Fundamental Ramifications for Sediment Dynamics

Carl Friedrichs, Virginia Institute of Marine Science

Conclusions:

- Negative feedback favors sediment $Ri \approx Ri_{cr}$ in the BBL.
- $Ri < 1/4$ (vs. $> 1/4$) implies supply (vs. settling) limitation.
- Ri const. in z implies $C \sim z^{-A}$, with $A \approx 1$ and $u \sim \log(z)$.
- If $Ri \uparrow$ (vs. \downarrow) in z , then $A < 1$ (vs. > 1), u concave down (vs. up).
- $Ri \approx Ri_{cr}$ predicts max load independent of w_s and erodibility.
- Time-scales of changes in u determine whether turbulence and suspension will catastrophically collapse via positive feedback.



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