Comparative Study between Classical and Optimized Stability Margins of Quadruped Robot Creeping Gait

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Abstract

The ability of the quadruped (four-legged) robot locomotion was used in a lot of different applications like walking over soft and rough terrains. These applications needed to guarantee the flexibility and mobility. Generally, quadruped robots have three basic periodic gaits: creeping gait, running gait and galloping gait. The stability criteria are the main issue of the quadruped robot throughout walking with the slow motion gait like creeping gait. The gait of static stability is completely bases on the stability margins in the walking that was calculated in this paper. The quadruped robot legs walking sequence and creeping gait within the leg fixing and swinging phases carried out. The kinematics model of quadruped robot of the forward and inverse kinematics for each leg 3-DOF was calculated that lead to discover the minimum stability margins with walking on the vertical projection of the robot geometrical body. These stability margins needed to be optimized in order to obtain the best stability margin throughout this robot walking. In this paper we use the PSO optimization algorithm to get the best stability margins value. Simulation and results are verified the range of the stability margin values and the optimized results.

Keywords: Quadruped Robot Simulation; Stability Margins; Quadruped Robot Gait PSO Optimization.

1. Introduction

In recent years, utilization of the leg-based walking systems has been transformed into a very familiar field in robotics. These systems adapted their ability in order to deal with irregular territories especially when compared with wheel systems [1].

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This legged systems ability for transact with uneven territories also avoiding the obstacles that with the quadruped robots in the planning of standard walking gaits [2, 3]. The quadruped robots distinguish among the other legged robots by have the less complex structure, this structure give it to accomplish the requirements of the static stability gait throughout walking. The quadruped robots locomotion frequently utilized in many research that talked about the quadruped robot, its similarity in the investigation of insects and biological animals walking gaits. These studies have led to improve both dynamic running gaits and statically stable walking gait for legged robots [4]. The objective of this paper is to design and implement with robustness quadruped robot that has the static stable ability during its walking. These walking gaits are repeated to obtain the main sequence step which needed to make the quadruped robot stable on irregular places [5]. The quadruped robots also has the ability of arranging the step sequences and verification criteria of stability on incline surfaces that needed for verifying the Omni-directional statically stable throughout this walking [6]. The criteria of stability depended on some elements such as Center of Gravity (COG), Stability margin (Sm) and the support polygon which framed by the legs tip of the quadruped robot. These elements are very important particularly when the quadruped robot walking utilizing creeping gaits for walking [7, 8]. Generate of the leg sequence of placing and lifting throughout the quadruped robot walking is called gait [9]. Generally, the quadruped robot gaits are dividing in two types, the first type is the static stability gait, and the second type is dynamic stability gait [10]. During the movement of the walking the body of quadruped robot should be remain stable and has the ability to travel from one place to another. The static stability gait is the easier gait which used by the quadruped robot when it needs a slow motion movement to walk. But when the quadruped robot walking at fast speed like trotting gait, the one must be used is the dynamic gait, which aims to reality of that the vertical projection of COG is derivative of the supporting polygon and not inside it. For this case the quadruped robot will be unstable and it is imminence to drop down. thus at the quadruped robot running gaits, its need to be content with the conditions of dynamic stability instead of the requirements of static stability [11]. Generally, the quadruped robot is attempt to be statically stable with its three legs fixed on the ground while the fourth leg is swing.

In this paper, the PSO optimization algorithm utilized to obtain the best stability margins throughout the robot walking gait. The creeping gait matches the nature of the biological stable gait of animals and insects. In this case the statically stable gait is necessary in order to guarantee a stable walking. Also during the quadruped walking in the creeping gait, its stability will be achieved if and only if the COG vertical projection inside the supporting polygon which is framed by the legs tips. The basic problem is how to achieve and control of the legs sequences of lifting and putting all legs within the period of time when the quadruped robot walking.

2. Description of Quadruped Robot

There are a different models of the quadruped robot, these models is based on some attributes and guide lines to design the robot structure and the gait movement. The main criteria to achieve these attributes are [13]:

1. The standard walking of quadruped robot is repeated periodically during the planning path with a constant speed, steady state movement of the legs over even territories.

2. The standard design of the quadruped robot must be symmetrical in both longitudinal body direction and

lateral body direction. This point is also applied to the legs structure leads to a less mechanical complexity.

3. When the quadruped robot has a regular shape and symmetric, the vertical projection of COG of the robot body is located at the center of the supporting polygon that is resulted from the legs tips on the ground.

The quadruped robot is design in Fig.(1), based on the above three criteria. In this research the walking direction assumed that the quadruped robot is walking foreword along the X-axis only. This means that there is no motion in the Y-axis stride .So the stride of every leg is a line. These stride lines are situated in the longitudinal body direction to meet the condition of forward walking.
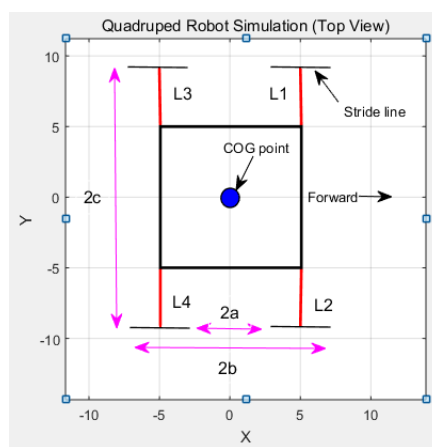

Figure 1: Quadruped robot (top view) illustrate the length (2b) and the width (2c) and the COG point

As seen in Fig.(1), (2a) is the distance between the minimum point limit of the front leg stride line to the maximum point limit of the back leg. (2b) is the distance between the maximum point limit of the front leg stride line to the maximum point limit of the back leg. (2c) is the distance from front/back left leg stride line to the right leg stride line. So the definition of the leg stride line is [13]:

Stride line = b – a   (1)

Along these considerations, the largest stride of the reachable area for a quadruped robot can be calculated from Equ. 1. Most of quadruped robots have the value of length equals to 2b and the value of width equals to 2c. Henceforth, the ratio between the length and width is equal to c/b.

In this paper, the simulation design the quadruped robot leg shown that it has three joints named as the biological of the nature insects as (Coxa joint, Femur joint, Tibia joint) this make each leg has three DOF (degree of freedom). For all legs, hence, the total numbers DOFs equal to 12. The quadruped robot structure is showing in Fig.(2). In Fig.(2-a) shows the quadruped robot main parts that is mimic the natural anatomy of insects and labeling of each leg. In Fig.(2-b) shows the leg joints and the link name of each joint in the quadruped leg. Leg1 is the right front (RF) side and leg3 is the right rear (RR) side and leg2 is the left front (LF)

side and Leg4 is the left rear (LR) side. And as mentioned before, the forward direction of motion of the quadruped robot, in case of the forward direction of motion is set to be with the X-axis direction and the lateral motion of the quadruped robot will be in Y-axis. The quadruped body has a symmetrical dimension in X and Y axes. Which giving the robot better stability during the walking and making it statically stable.
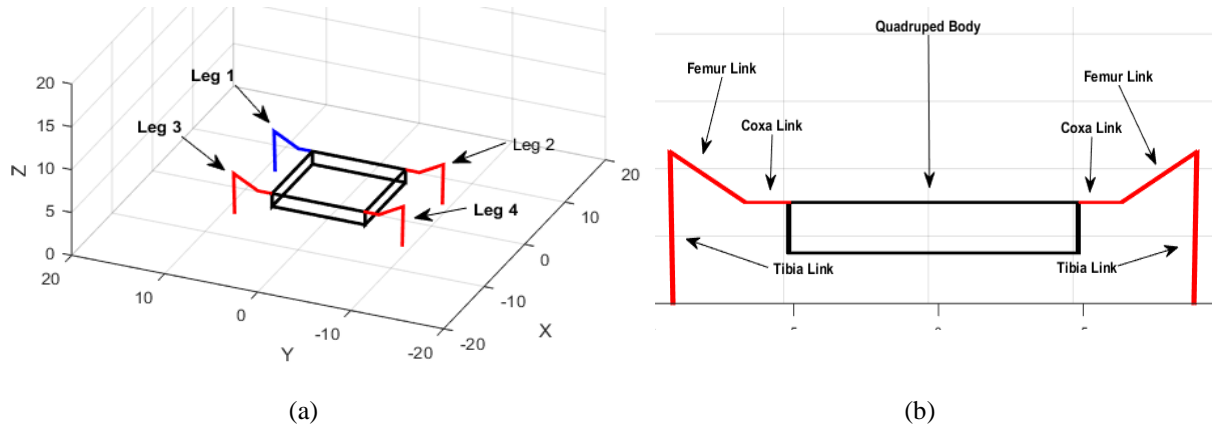

(a)   (b)

Figure 2: Quadruped Robot Simulation Using Matlab (a) quadruped robot with four legs labeling (b) showing the three joints (Coxa, Femur, and Tibia) in each legs.

The main point to ensure the stable walking in the statically stable gait, the quadruped legs positions are playing an important role during the walking of the stability calculations. The legs tips positions should be found by driving the forward kinematics and inverse kinematics for the quadruped robot.

3. Creeping Gait Analysis and Sequence Description

The quadruped robots have three main gaits. This gaits are classified according to its duty factor (β_i) of each leg, where i=1,,,4. These gaits are named from the biological natural gaits of animals such as crawl gait, running gait, and the galloping gait. The quadruped robot locomotion has any type from these gaits according to its duty factor (β_i) which is defined as the ratio of the time periods between the leg period of swinging to the period that the same leg is contact with the ground. When the quadruped robot walks using creeping gait, the value of the duty factor will equals to 0.75. When the quadruped robot is running, it will have duty factor ranged between 0.5-0.75. Finally when the quadruped robot is galloping, it will have duty factor less than 0.5. These main gaits in the robotics field have also been given a name, these names are called: creeping gait, trotting gait and the bounding gait [15]. Hence, these gaits have been used by mammals. For example, cats are using the creeping gait for a very slow walking. Creeping gait has some advantages, this gait is ensure the statically stable movement which is used with the range of low-speed walking. The sequence condition of the creeping gait is need a three legs at least are contact with the ground when the fourth leg are swing to translate to new position. This sequence condition is needed to ensure the statically stable gait. The quadruped robot creeping gait sequence has six types of legs arrangement. In this paper, quadruped robot leg sequence is (RR, RF, LR, and LF) where (R: right, L: left, R: rear, F: front). From the labeling Fig.(2)-a, it can be seen that RR is leg4, RF is leg2, LR is leg3, and LF is leg1. The advantage of choosing this leg sequence arrangement to have a safety walking which is ensure that the robot is body moving forward at the instance time[12]. There are two Cartesian

reference frames coordinate when talking about the quadruped structure, the first coordinate frame is located at the coxa joint and the second coordinate frame is located on the ground. In this Cartesian coordinate the X-axis is referred to the front side direction of the quadruped body, and Y-axis is referred to the left side of the quadruped body. So, these coordinates are very important in the analyzing and ensuring that vertical projection of COG have been located inside the supporting polygon [13].

4. Kinematics Model of a Quadruped Robot

4.1 Forward Kinematics

The quadruped robot is depending on the configuration of each leg, because its represent as the physical constraints of the robot walking. In this paper, the robot leg has three-revolute joints which are labeled in the kinematical chain as (θ_1, θ_2 and θ_3). Every leg has a mechanism that is choosing according to these revolute joints. Modeling of the leg structure is to mimic the biological structures for animals and insects. To drive the geometrical model to each leg which is related to the robot center body, thus forward kinematics must be applied to find the position and orientation for each leg tip which is here named as (xi, yi, zi), i=1,2,3,and 4. In the Fig.(3) the kinematical chains for any leg is showing.
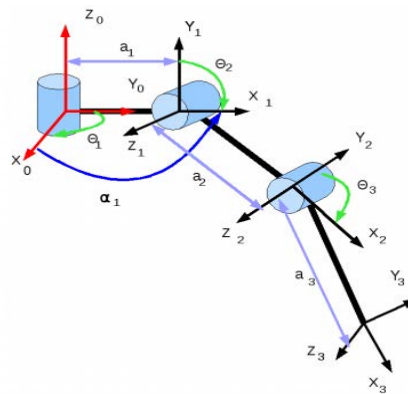

Figure 3: Coordinate frames for one leg of Quadruped Robot

Forward kinematics is depending on the D-H (Denavit-Hartenberg) parameters of the leg structure design; these parameters are showing in Table 1.

Table 1: The Denavit-Hartenberg parameters table for one leg in our quadruped robot

Link No.	Link name	α_i (deg)	a_i (cm)	d_i (cm)	θ_i (deg)
1	Coxa	90	a_1	0	θ_1
2	Femur	0	a_2	0	θ_2
3	Tibia	0	a_3	0	θ_3

Where the links parameter: $a_1 = 2.5$ cm $a_2 = 5$ cm, and $a_3 = 9$ cm. a_i are the lengths of the leg links. The leg structure is symmetric on the coordinate axis and the walking is set towards the X-axis. The transformation matrix used to translate from one link named i to another link named i-1 by using the D-H parameters table. Equ. 2, the general matrix is given:

$$T_i^{i-1} = \begin{bmatrix} cos\theta_i & -sin\theta_i cos\alpha_i & sin\theta_i sin\alpha_i & a_i cos\theta_i \\ sin\theta_i & cos\theta_i cos\alpha_i & -cos\theta_i sin\alpha_i & a_i sin\theta_i \\ 0 & sin\alpha_i & cos\alpha_i & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

(2)

By multiplying each joint transformation matrix, the overall transformation matrix can be obtained as the following Eq. 3:

$$T_{coxa}^{base} = T_{coxa}^{femur} * T_{femur}^{tibia}$$ (3)

The transformation matrix for each joint in the quadruped robot leg is given by the following equations:

$$T_1^0 = \begin{bmatrix} c_1 & 0 & s_1 & a_1 c_1 \\ s_1 & 0 & -c_1 & a_1 s_1 \\ 0 & 1 & 0 & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$ (4)

$$T_2^1 = \begin{bmatrix} c_2 & -s_2 & 0 & a_2 c_2 \\ s_2 & c_2 & 0 & a_2 s_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$ (5)

$$T_3^2 = \begin{bmatrix} c_3 & -s_3 & 0 & a_3 c_3 \\ s_3 & c_3 & 0 & a_3 s_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$ (6)

Multiplications of these matrixes produce the final matrix that it used to describe the leg-tip position and orientation. This matrix is given as the following:

$$\begin{bmatrix} c_1(c_{2+3}) & -c_1 s_{2-3} & s_1 & a_3 c_1(c_{2+3}) + c_1(a_2 c_{2+} a_1) \\ s_1(c_{2+3}) & -s_1(s_{2-3}) & -c_1 & a_3 s_1(c_{2+3}) + s_1(a_2 c_{2+} a_1) \\ s_{2+3} & (c_{2+3}) & 0 & a_3(s_{2-3}) + a_2 s_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$ (7)

Where:

$c_i = cos\theta_i$ and $s_i = sin\theta_i$, for i=1,2, and 3.

$(c_{2+3})= \cos(\theta_2 + \theta_3)$

$(s_{2-3})= \sin(\theta_2 - \theta_3)$

Thus, the final position of the leg tip can be obtained as:

$$x_i = a_1 c_1 + a_2 c_1 c_2 + a_3 c_1 \qquad (8)$$

$$y_i = a_1 s_1 + a_2 s_1 c_2 + a_3 s_1 c_{2+3} \qquad (9)$$

$$z_i = a_2 s_2 + a_3 s_{2-3} \qquad (10)$$

Where: (x_i, y_i, z_i) is the leg-tip coordinates, i=1…4.

4.2 Inverse Kinematics

The inverse kinematics is used to formulate and achieve the joint angles from the leg tip position and orientation which has been calculated from the forward kinematics [14]. In this paper, the goal of inverse kinematics is to find joint angles of each leg, θ_1, θ_2 and θ_3, from the leg position. The leg configuration assumed to be similar with the natural biological insect as illustrated in Fig.(4).
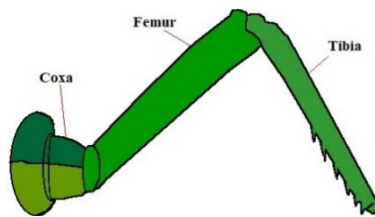
Figure 4: Shows one leg of insect and its links (Coxa, Femur, Tibia) [16]

To solve inverse kinematics for every legs, its need to use the geometrical methods. Firstly, its need to simple the geometrical figure of the leg from (3D) views to (2D) view. Secondly, finding each joint angle by using the geometrical analysis to find (θ_1, θ_2 and θ_3) as shown in Fig.(5).
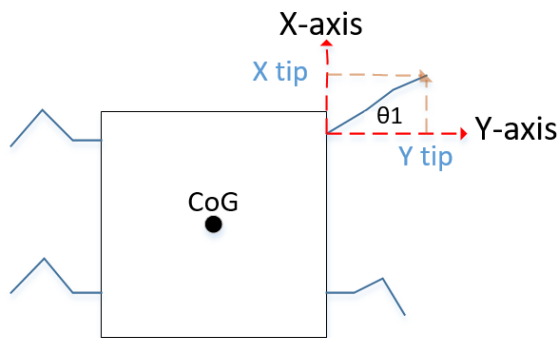

Figure 5: quadruped top view showing leg angle θ_1

θ_1 Can be directly calculated as:

$$\theta_1 = tan^{-1}(\frac{X\ tip}{Y\ tip})$$ (11)

After finding θ_1, the other angelsθ_2 and θ_3 are in the same (Y-Z) plane. Firstly, finding θ_2 by dividing it into two parts $\alpha_1$and α_2 to simplify the problem. From Fig.(6), it can be seen that α_1 is depending on the distance L which equals to:

$$L = \sqrt[2]{z_{offset}^2 + (L_1 - c)^2}$$ (12)

Where: c is the length of Coxa link.

So α_1 can be calculated as:

$$\alpha_1 = cos^{-1}(\frac{z_{offset}}{L})$$ (13)

From the cosine rules and from Fig.(6), $\alpha_2$will be found as:

$$T^2 = F^2 + L^2 - (2 * F * L)cos(\alpha_2)$$

Thus:

$$\alpha_2 = cos^{-1}\left(\frac{F^2+L^2-T^2}{2*F*L}\right)$$ (14)

Where: F is the Femur link length and T is the Tibia Link length.
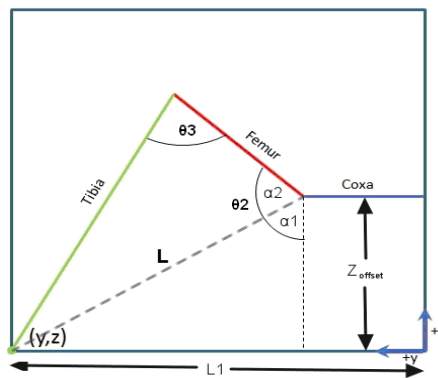
Figure 6: Quadruped robot leg and its links (Coxa, Femur, Tibia), θ_2 andθ_3 [14]

From Fig.(6),θ_2 equals to:

$$\theta_2 = \alpha_1 + \alpha_2$$

$$\theta_2 = cos^{-1}\left(\frac{z_{offset}}{L}\right) + cos^{-1}\left(\frac{F^2+L^2-T^2}{2*F*L}\right) \qquad (15)$$

By the same method, θ_3 is calculated as:

$$\theta_3 = cos^{-1}\left(\frac{F^2+T^2-L^2}{2*F*T}\right) \qquad (16)$$

5. Stability Margins Analysis for Quadruped Robot Creeping Gait

The quadruped robot walks with a specific goal to have a statically stable movement. During the robot walking the vertical projection of COG on the ground must be inside the supporting polygon. This is the main criterion which is conditioned for the statically stable walking. The quadruped robot is stable and will not turn down when it satisfied these conditions of the statically stable walking. The main advantage of the quadruped robot walking in periodically repeated locomotion is to produce a constant speed. This property is leading to the fact that the accelerations on the robot body are equal to zero, and the disturbances on the legs will be reduced. When the quadruped robot walking using creeping gait, the static stability walking is depending on the stability margins. These margins are defined as shortest distance between the vertical projection of COG to the boundaries of the supporting pattern [13]. The next figures are showing and explaining the quadruped robot model, and the stability margins mathematically analysis to find and calculate the stability margins as the following cases:
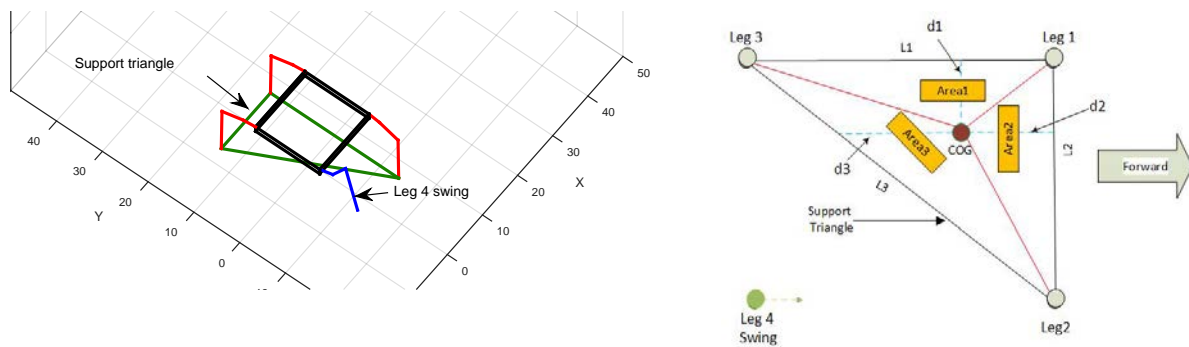

Figure 7: Quadruped robot (top-view) showing the support triangle when leg4 is swinging and other legs are fixed on the ground

Case one: when the quadruped robot leg4 is swing and the other legs (1, 2, and 3) are fixed on the ground as showing in Fig. (7). The supporting area will be divided into three areas called (Area1, Area2, and Area3). The blue lines are the lines of the stability margins which are needed to be the minimum from the vertical projection of COG to the supporting lines (L1, L2, and L3). These blue lines are denoted as (T1, T2, and T3). After this method is applied, the stability margins will be found as:

$$Area_1 = \frac{1}{2}\begin{bmatrix} 1 & 1 & 1 \\ x_{cog} & x_1 & x_3 \\ y_{cog} & y_1 & y_3 \end{bmatrix}$$

Where, (x_{cog}, y_{cog}) is the center of gravity coordinate of the quadruped robot on the ground. (x_1, y_1) is the leg1

coordinate of tip position. (x_3, y_3) is the leg3 coordinate of tip position. By expanding and simplify this matrix $Area_1$ can be calculated as the following:

$$Area_1 = \frac{1}{2}\{(x_1 - x_{cog})(y_3 - y_{cog}) - (x_3 - x_{cog})(y_1 - y_{cog})\}$$

$$L_1 = \sqrt{(x_1 - x_3)^2 + (y_1 - y_3)^2}$$

$$d_1 = 2 * (\frac{Area_1}{L_1}) \tag{17}$$

By the same way, $Area_2$ and $Area_3$ will be found as:

$$Area_2 = \frac{1}{2}\{(x_1 - x_{cog})(y_2 - y_{cog}) - (x_2 - x_{cog})(y_1 - y_{cog})\}$$

$$L_2 = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$d_2 = 2 * (\frac{Area_2}{L_2}) \tag{18}$$

$$Area_2 = \frac{1}{2}\{(x_2 - x_{cog})(y_3 - y_{cog}) - (x_2 - x_{cog})(y_3 - y_{cog})\}$$

$$L_3 = \sqrt{(x_2 - x_3)^2 + (y_2 - y_3)^2}$$

$$d_3 = 2 * (\frac{Area_3}{L_3}) \tag{19}$$

Finally, the first stability margin sm_1 is the minimum distance from these three margins:

$$sm_1 = min(d_1, d_2, d_3) \tag{20}$$

The other stability margins have been calculated in each period when the other legs are swinging respectively. As sm_1 analyzed, the other margins are equals to:

$$sm_2 = min(d_4, d_5, d_6) \tag{21}$$

$$sm_3 = min(d_7, d_8, d_9) \tag{22}$$
$$sm_4 = min(d_{10}, d_{11}, d_{12}) \tag{23}$$

Where $(sm_2, sm_3, and\ sm_4)$ have been calculated corresponding to the other cases when the legs are swinging sequence during the robot creeping gait. And d_i (i=4,...,12) are the distances between the robot center and the legs tips, when all the legs had been swing as leg_2, leg_3, and leg_1 respectively.

6. Stability Margins Optimization using PSO

The stability margins of each leg sequence when the quadruped robot walking with creeping gait is analyzed. These margins are varying between a range of values, and its need to achieving the optimal value of each stability margin. In this section an optimization method called Particle Swarm Optimization is used to optimize the stability margins to have the best stability margin during the quadruped robot walking using creeping gait locomotion.

The PSO optimization algorithm is based on some features such as:

1- The cost function: this is the main function of the problem that it needs to be optimized. In this paper, the main parameters that will pass to the cost function are the robot body center in X-axis and Y-axis and the leg tips which are presented as the constraint of the cost function.

2- The minimum and maximum values of variables: in this paper, the stability margin limiting values are presented as VARmin and VARmax

3- Number of iteration: in this paper the number of iteration is: 500 iteration

4- Number of population: in this paper the number of population equals to 5.

5- The initial weight : in this paper the initial weight $W_{initial} = 1$, and the damping weight $W_{damp} = 0.99$

6- The constant values C_1 and C_2: in this paper $C_1 = 3.999$ and $C_2 = 0.0001$.

All these parameters are playing a very important role for enhancement the optimization method working. The PSO optimization results of the stability margins are showing in section 7.

7. Simulation and Results

In this section, the quadruped robot walking according to the creeping gait sequence locomotion is shown. Each gait has its stability margin is varying between a range of values according to which leg is swing in the air. After finding the stability margin of each gait, applying the PSO optimization algorithm to achieve the best stability margin which gives the best stability that it used to balance the quadruped robot at the period when it walks with creeping gait locomotion. As shown in the following figures.
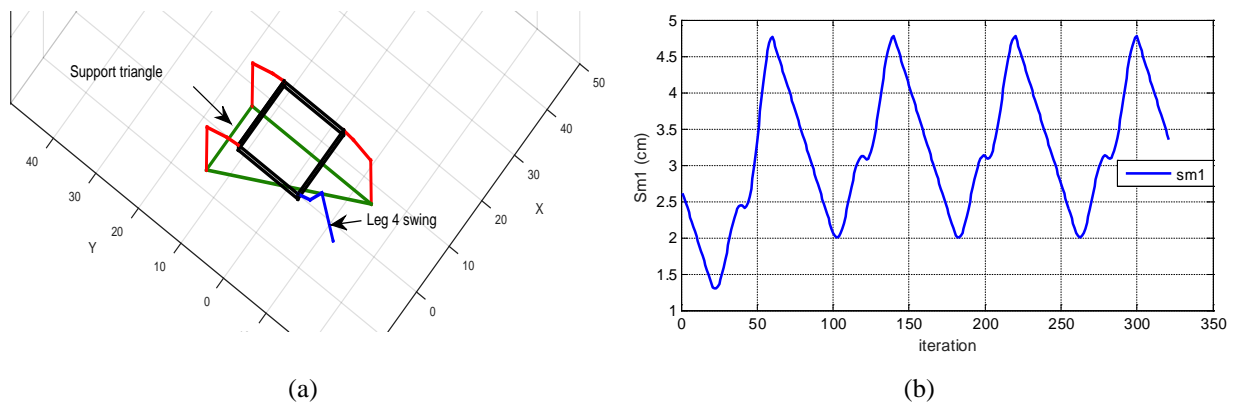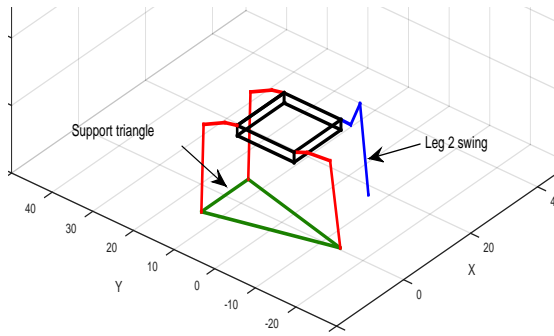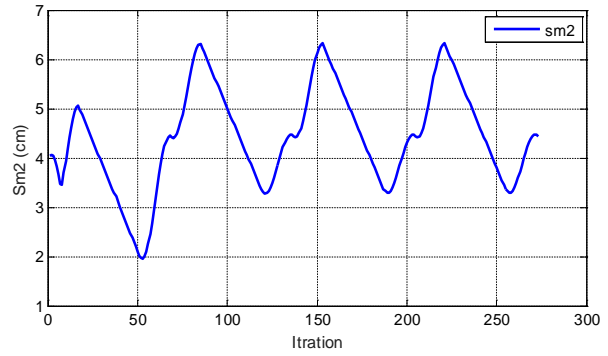

(a) (b)

Figure 8: (a) Leg 4 in swinging phase (b) The stability margin Sm_1(cm) when leg4 is swing.

(a)   (b)

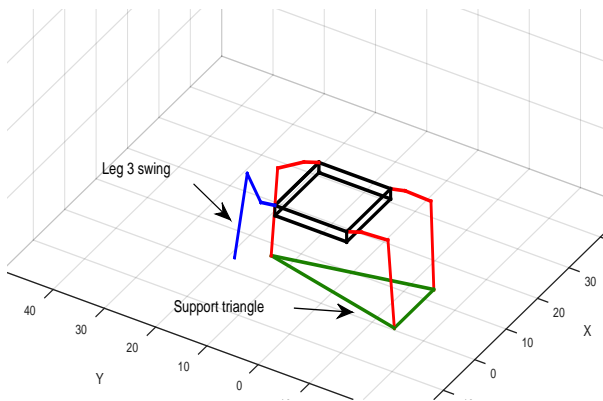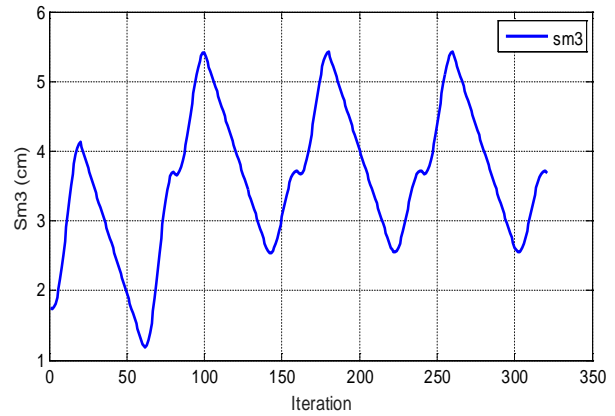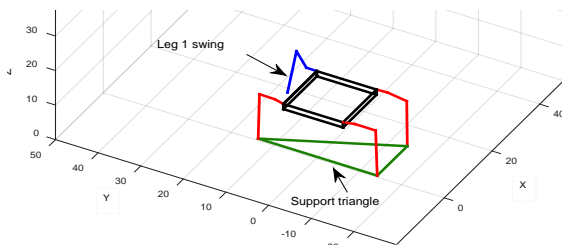**Figure 9:** (a) Leg 2 in swinging phase. (b) The stability margin Sm_2(cm) when leg2 is swing.
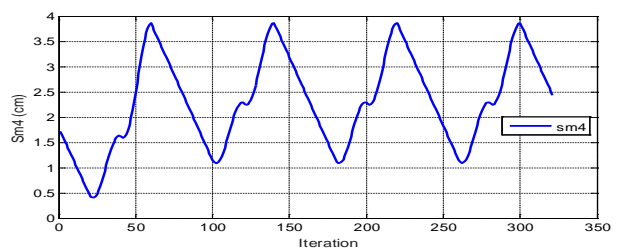

(a)   (b)

Figure 10: (a) Leg 3 in swinging phase. (b) The stability margin Sm_3(cm) when leg3 is swing.

(a)   (b)

Figure 11: (a) Leg 1 in swinging phase. (b) The stability margin Sm_4(cm) when leg1 is swing.

From above figures it can be seen the following:

1. In Fig.(8): leg4 tip is swinging and the stability margin Sm_1(cm) equals to (1.71) cm.

2. In Fig.(9): leg2 swinging and the stability margin Sm_2(cm) equals to (1.35) cm.

3. In Fig.(10): leg3 swinging and the stability margin Sm_3(cm) equals to (2.3) cm.

4. In Fig.(11): leg1 swinging and the stability margin Sm_4(cm) equals to (1.95) cm.

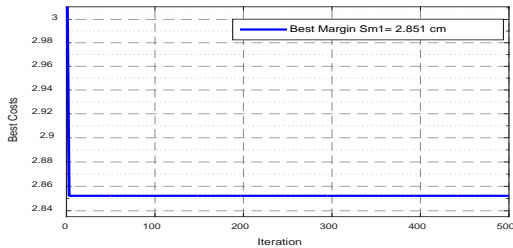The best stability margins achieving from the PSO optimization algorithm are showing in the following figures

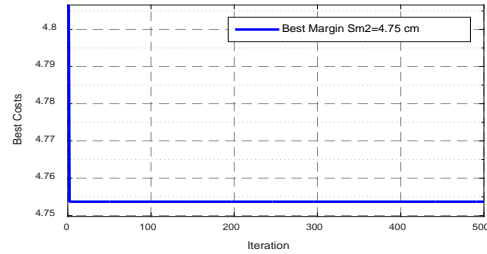**Figure 12:** Best cost for the stability margin Sm_1

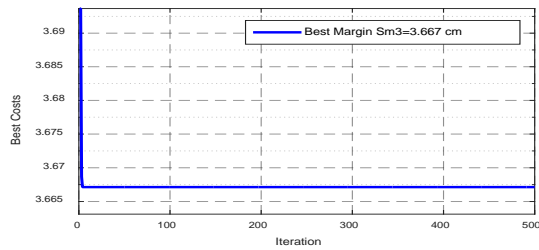**Figure 13:** Best cost for the stability margin Sm_2

Figure 14: Best cost for the stability margin Sm_3
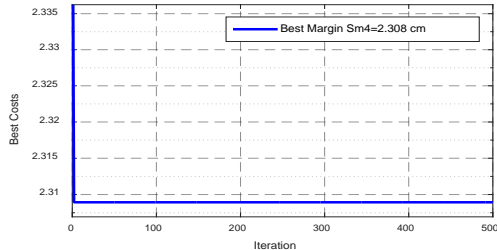

Figure 15: Best cost for the stability margin Sm_4

The following Table (2) is a comparison between the classical stability margins analysis and proposed optimization using PSO algorithm method used in this paper.

Table 2: Stability margins comparison between the classical analyses and the optimized method

Classical Analysis Method	Proposed Optimization using PSO algorithm
1. When Leg 4 is swing the stability margin Sm_1 ranging between (2 – 4.55) cm.	1. When Leg 4 is swing the best stability margin Sm_1 equals to2.851 cm.
2. When Leg 2 is swing the stability margin Sm_2 ranging between (3 – 6.2) cm.	2. When Leg 2 is swing the best stability margin Sm_2 equals to2.75 cm.
3. When Leg 3 is swing the stability margin Sm_3 ranging between (2.7 – 5.3) cm.	3. When Leg 3 is swing the best stability margin Sm_3 equals to: 3.667 cm.
4. When Leg 1 is swing the stability margin Sm_4 ranging between (1.6 – 3.6) cm.	4. When Leg 1 is swing the best stability margin Sm_4 equals to: 2.308 cm.

From above figures it can be seen that:

1. In Fig.(12): the best cost of the stability margin Sm_1 equals to (1.635) cm.

2. In Fig.(13): the best cost of the stability margin Sm_2 equals to (1.25) cm.

3. In Fig.(14): the best cost of the stability margin Sm_3 equals to (2.173) cm.

4. In Fig.(15): the best cost of the stability margin Sm_4 equals to (2.309) cm.

During the creeping gait sequence, the quadruped robot leg angles are changing. These angles are (θ_1,θ_2 and θ_3) of each leg. This changing is showing in Fig.(19):
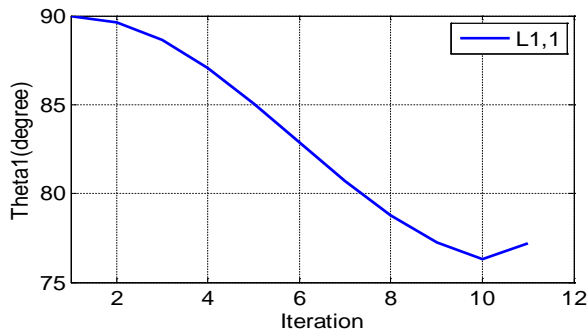

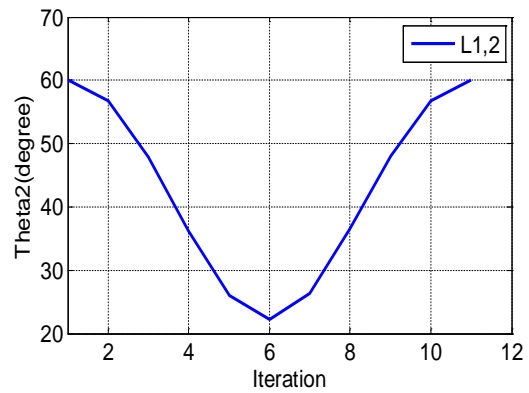**Figure 16:** Changing of Coxa-angle in one step movement

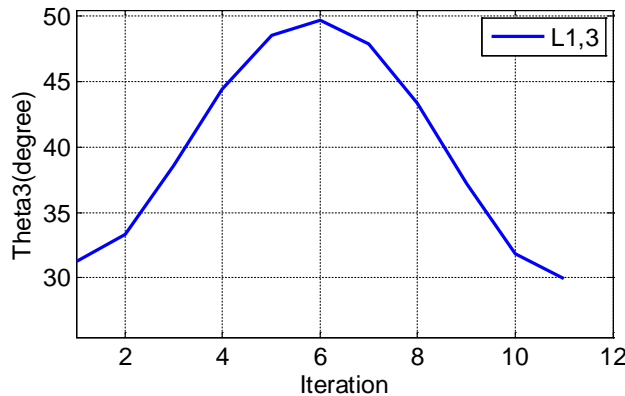**Figure 17:** Changing of Femur-angle in one step movement

Figure 18: Changing of Tibia-angle in one step movement

From above figures it can be seen that:

1. Fig.(16) is the changing of Coxa-angle θ_1. This angle is varying between (90 degree) to (76 degree).

2. Fig.(17) is the changing of Femur-angle θ_2. This angle is varying between (23 degree) to (60 degree).

3. Fig.(18) is the changing of Tibia-angle θ_3. This angle is varying between (30 degree) to (49 degree).

8. Conclusion

Illuminating the basic points of this paper, analyze of the quadruped robot walking of creeping gait and the derivation, emphasize and showed that the quadruped robot is statically stable throughout walking. To access the objective of the work, firstly, the whole forward and inverse kinematics model have been derived and utilized for stability validation of walking steps. So the intersection between sequence of robot creeping gait and the geometric modeling of robot legs-tip which are derived to find the entire static stability margins during walking. The results certainly proved the best of stability margins that own the minimum values with utilizing PSO algorithm to guarantee the robot COG preservation into the supporting triangle via the swing phase for one leg with the rest legs that on the ground. Furthermore, an improvement for future work, it's necessary to analyze and enhance the quadruped robot walking on hard and rough terrain.

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