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Variations of the elastic modulus of automotive steels after yielding

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# VARIATIONS OF THE ELASTIC MODULUS OF AUTOMOTIVE STEELS AFTER YIELDING

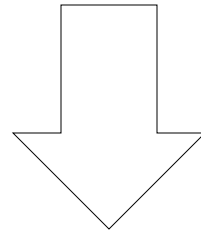
**P. Matteis**, G. Scavino, D. Firrao

Politecnico di Torino – DISMIC  
Torino, Italy

## Overall aim

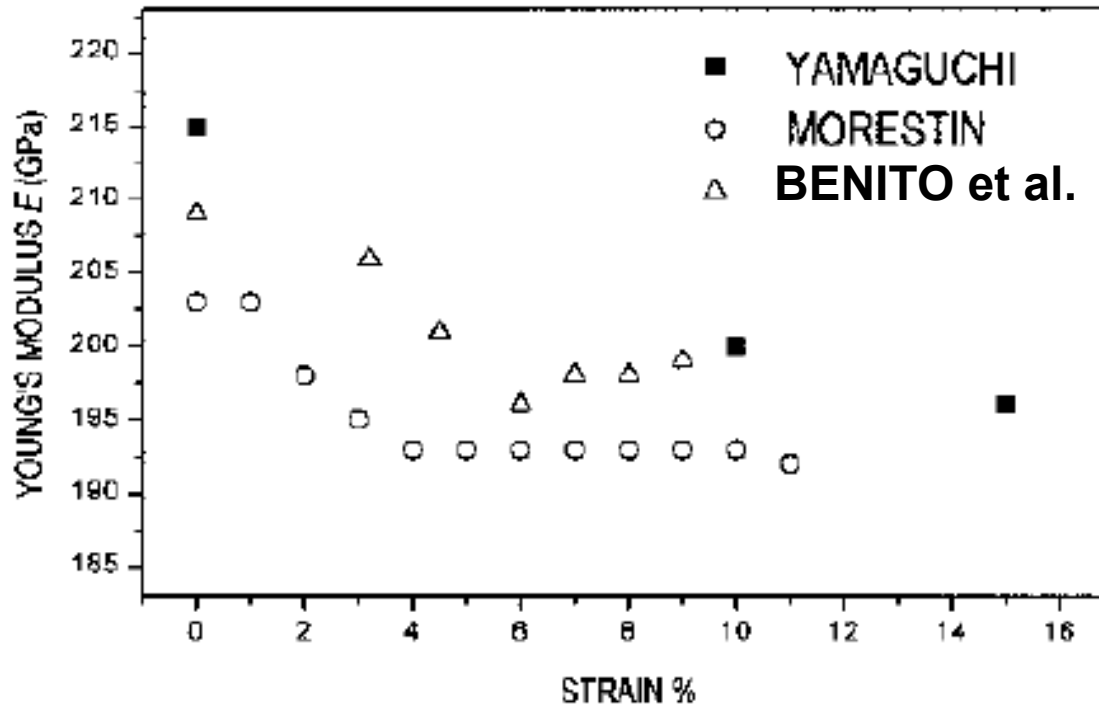
### Accurate simulation of sheet cold forming processes for car body parts

FEM analyses sufficiently accurate to predict springback and to design *compensated* dies requires increasingly accurate material parameters



Accurate measurements of the elastic modulus on both virgin and already deformed steel

# Previous works (1) – pure iron



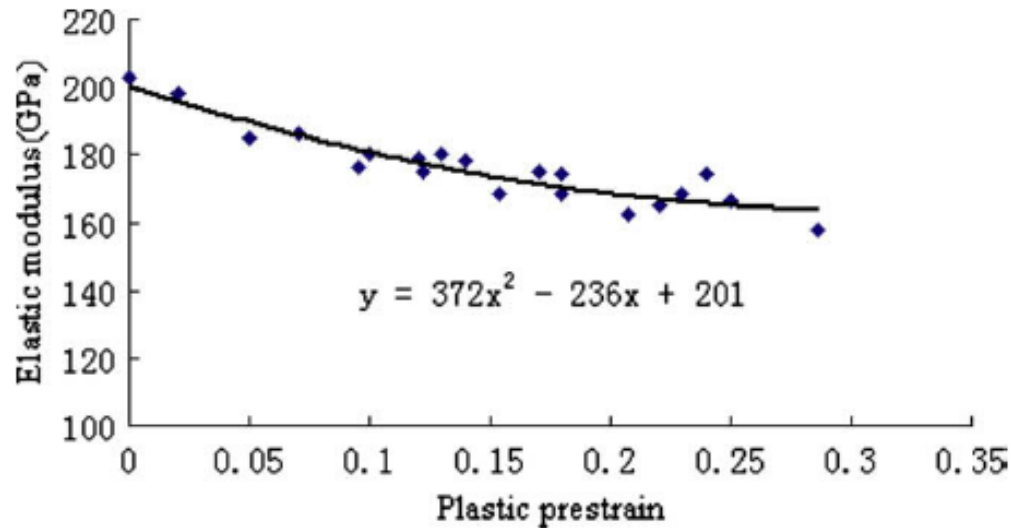
METALLURGICAL AND MATERIALS TRANSACTIONS A

VOLUME 36A, DECEMBER 2005—3317

## Change of Young's Modulus of Cold-Deformed Pure Iron in a Tensile Test

J.A. BENITO, J.M. MANERO, J. JORBA, and A. ROCA

# Previous works (2) – TRIP steel, springback analyses



Materials and Design 30 (2009) 846–850

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Materials and Design

journal homepage: [www.elsevier.com/locate/matdes](http://www.elsevier.com/locate/matdes)

ELSEVIER

Short Communication

Variation of elastic modulus during plastic deformation and its influence on springback

Hai Yan Yu\*

# Tested automotive steel sheets

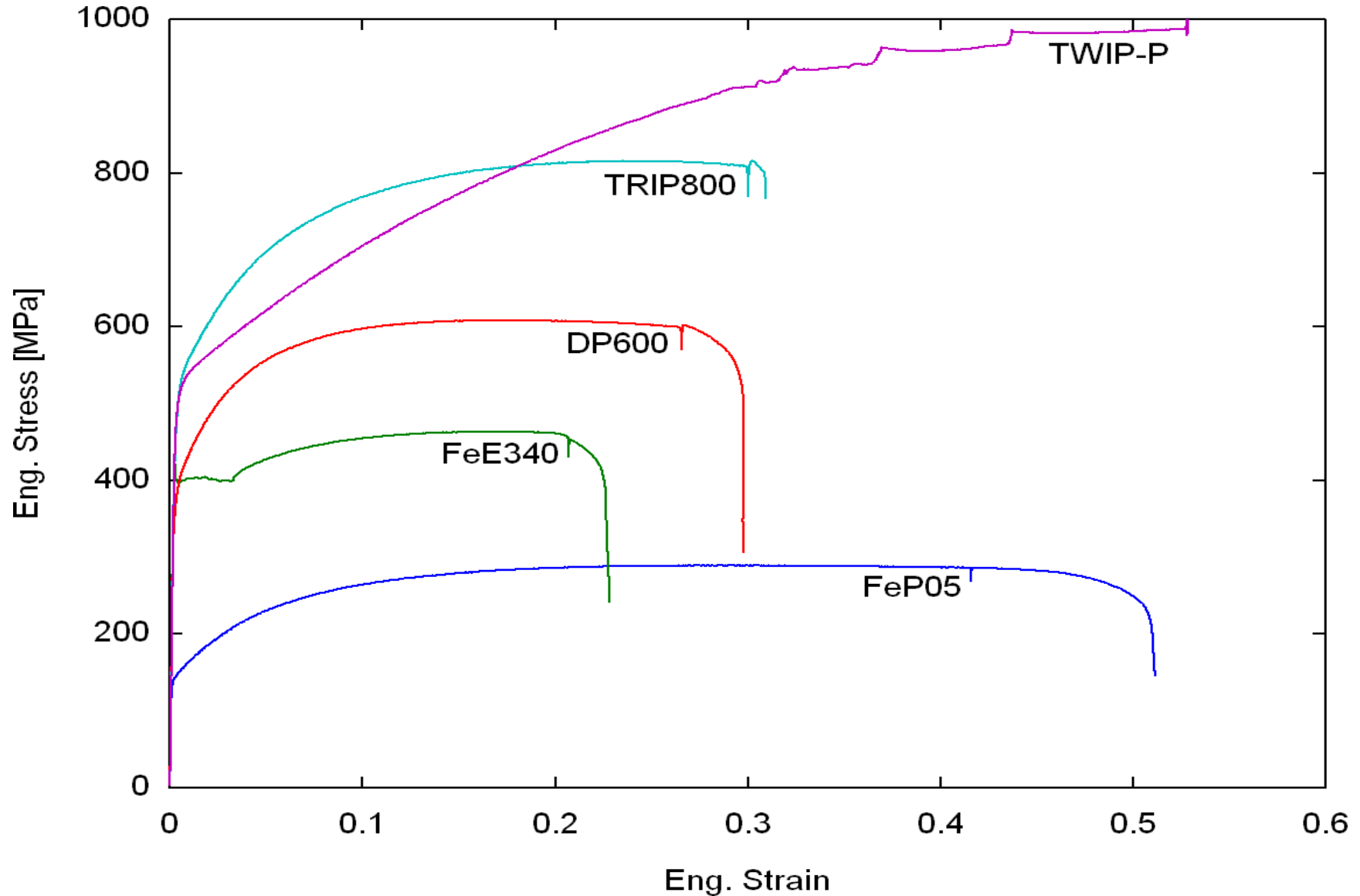
Grade	Thickn. [mm]	YS [MPa]			UTS [MPa]			e <sub>t</sub> [%]		
		T	45	L	T	45	L	T	45	L
<b>FeP05</b> (low carbon)	1	145	154	149	292	300	287	51	50	51
<b>FeE340</b> (microalloyed)	1	433	394	384	476	455	469	23	36	37
<b>DP600</b> (Dual Phase, ferrite & martensite)	1.55	388	387	388	615	610	614	30	21	25
<b>TRIP800</b> (TRAsformation Induced Plasticity)	1	520	511	520	837	830	840	31	27	26
<b>TWIP</b> (18% Mn, 0.65% C, austenitic)	1.45	506	489	484	1010	997	993	53	63	47

As-received (i.e., cold rolled and heat treated) microstructure

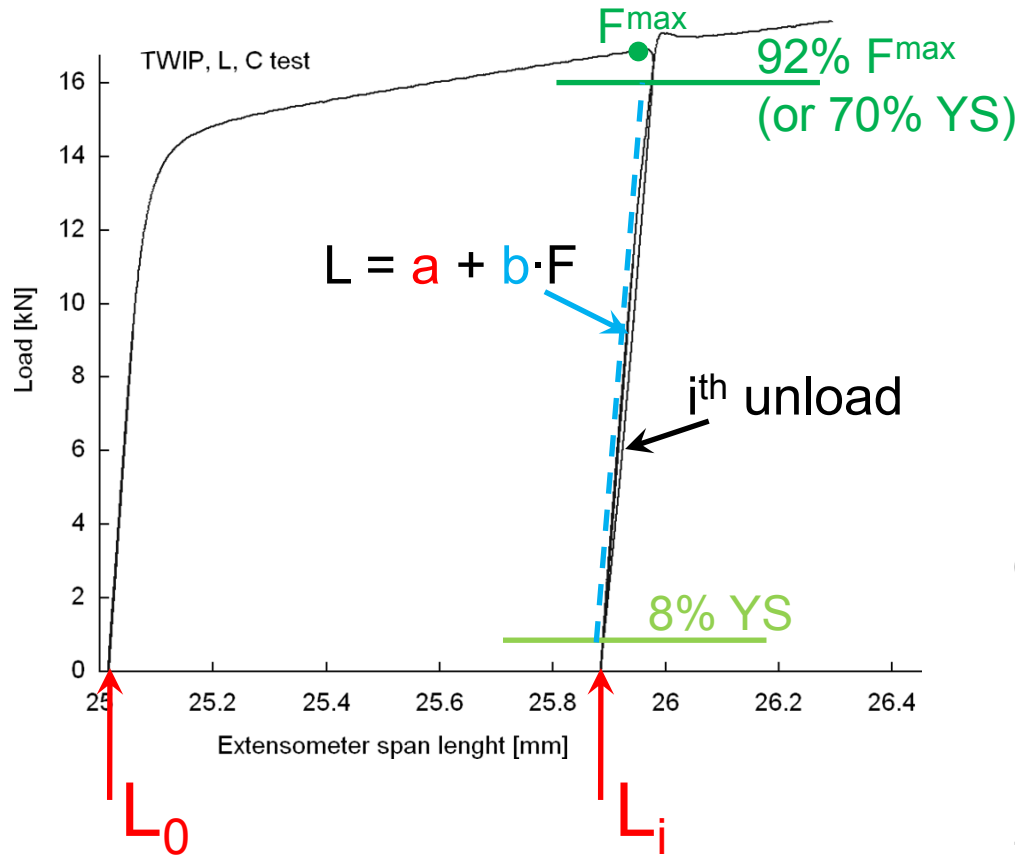
Protective Zn surface layers removed before testing

Tensile tests on 20 mm wide samples, with a 25 mm extensometer

# Tested Materials – tensile curves (Orientation T)



# Elastic modulus calculations



$$L = L_i \cdot (1 + \epsilon) = L_i + L_i \cdot (\sigma / E)$$

$$L = L_i + (L_i \cdot F) / (E \cdot S_i)$$

$$L = L_i + (L_i^2) / (L_0 \cdot S_0 \cdot E) \cdot F$$

(since  $L_0 \cdot S_0 = L_i \cdot S_i$ )

$$L = a + b \cdot F$$

$$\rightarrow L_i = a$$

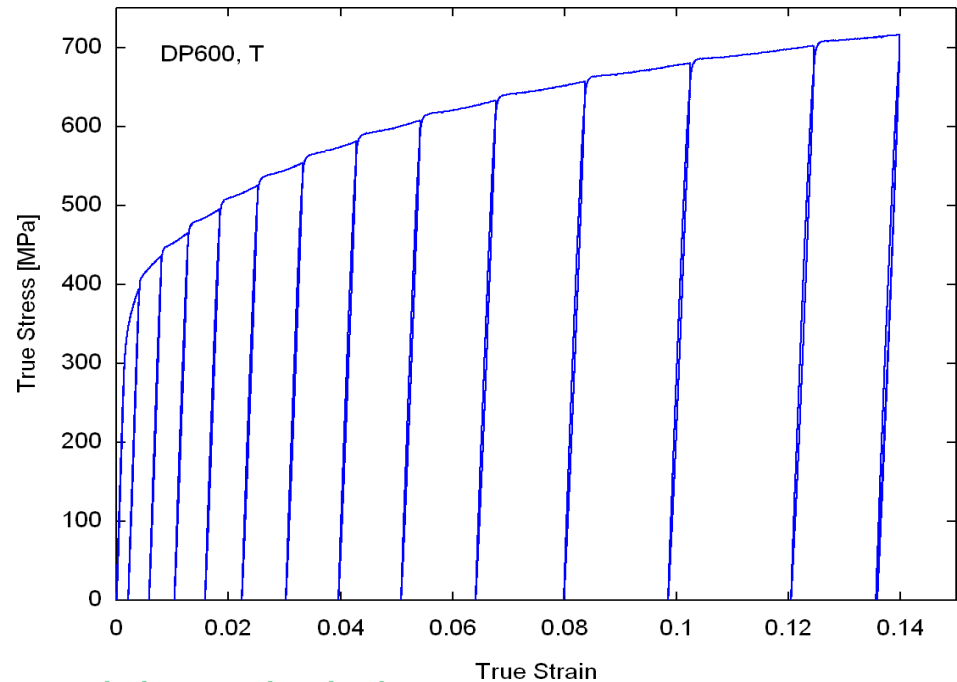
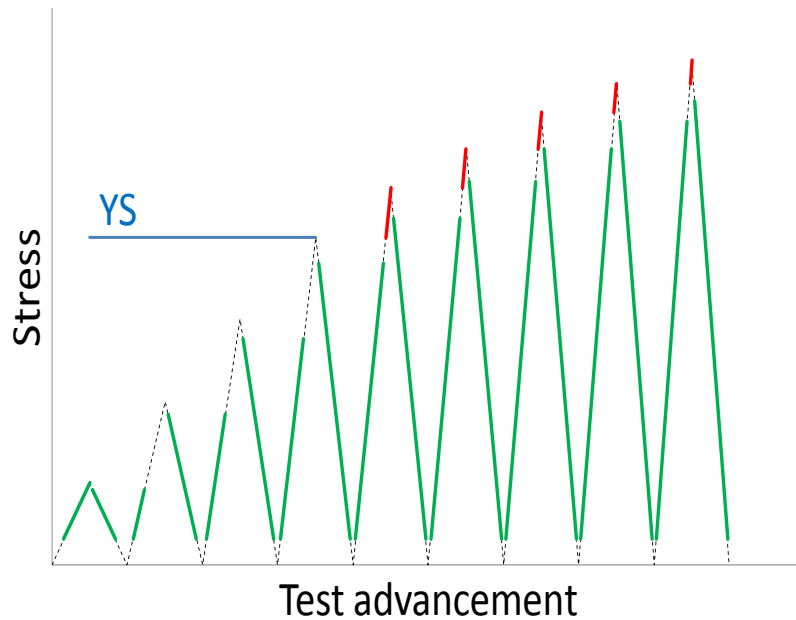
$$\rightarrow \text{Modulus} = E = a^2 / (L_0 \cdot S_0 \cdot b)$$

$$\rightarrow \text{Pre-strain} = \epsilon_i = \ln(L_i / L_0)$$



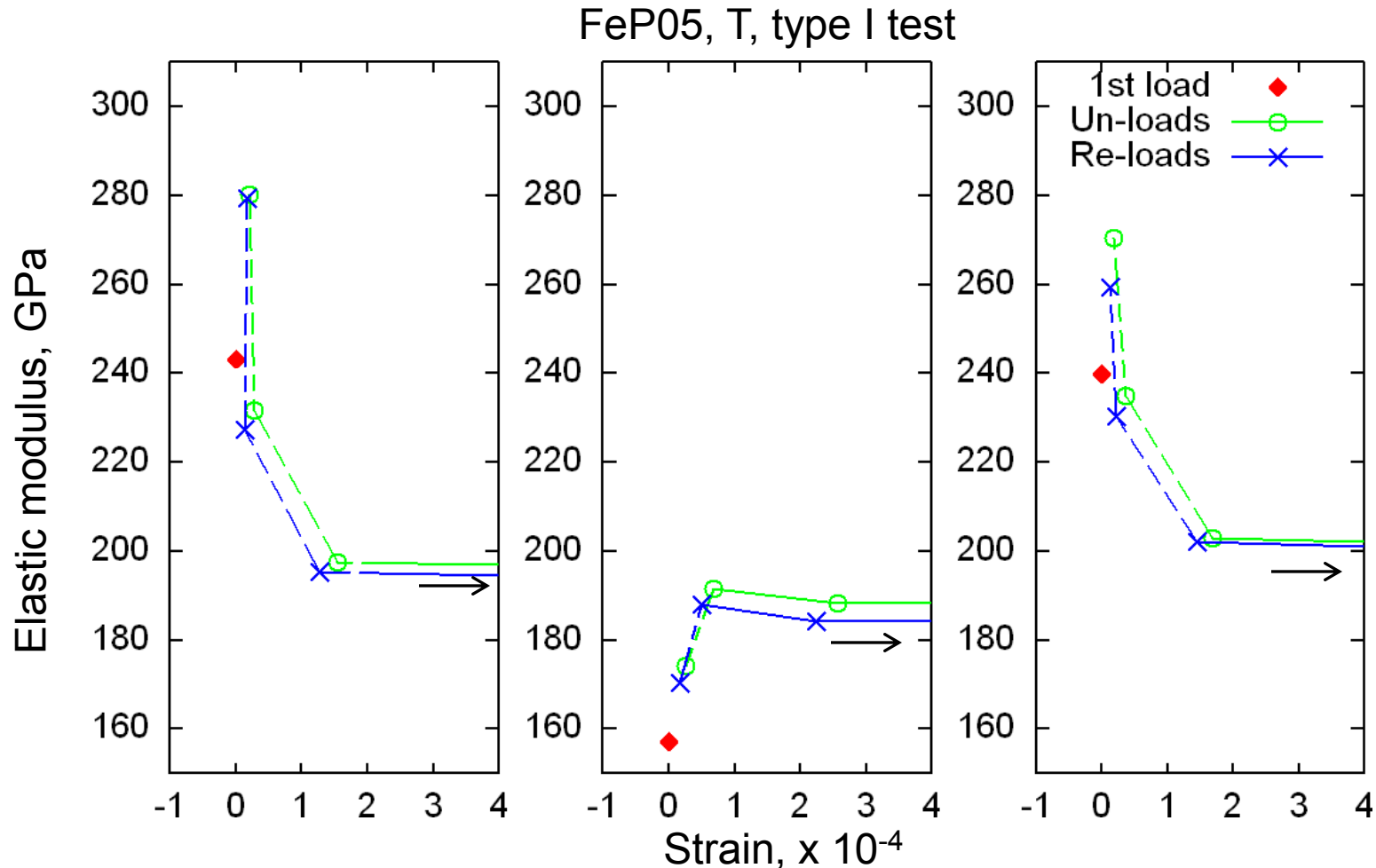
# Type I tests

- unload – reload cycles up to  $\approx 25, 50, 75$  and  $100\%$  of yield stress
- repeated **plastic strain steps**, starting from  $\approx 0.004$  true strain (each  $\approx 20\%$  larger than the previous one)
- one elastic unload-reload cycle after each step (and one final unload)
- elastic strain rate  $\approx 10^{-4} \text{ s}^{-1}$  in all cases



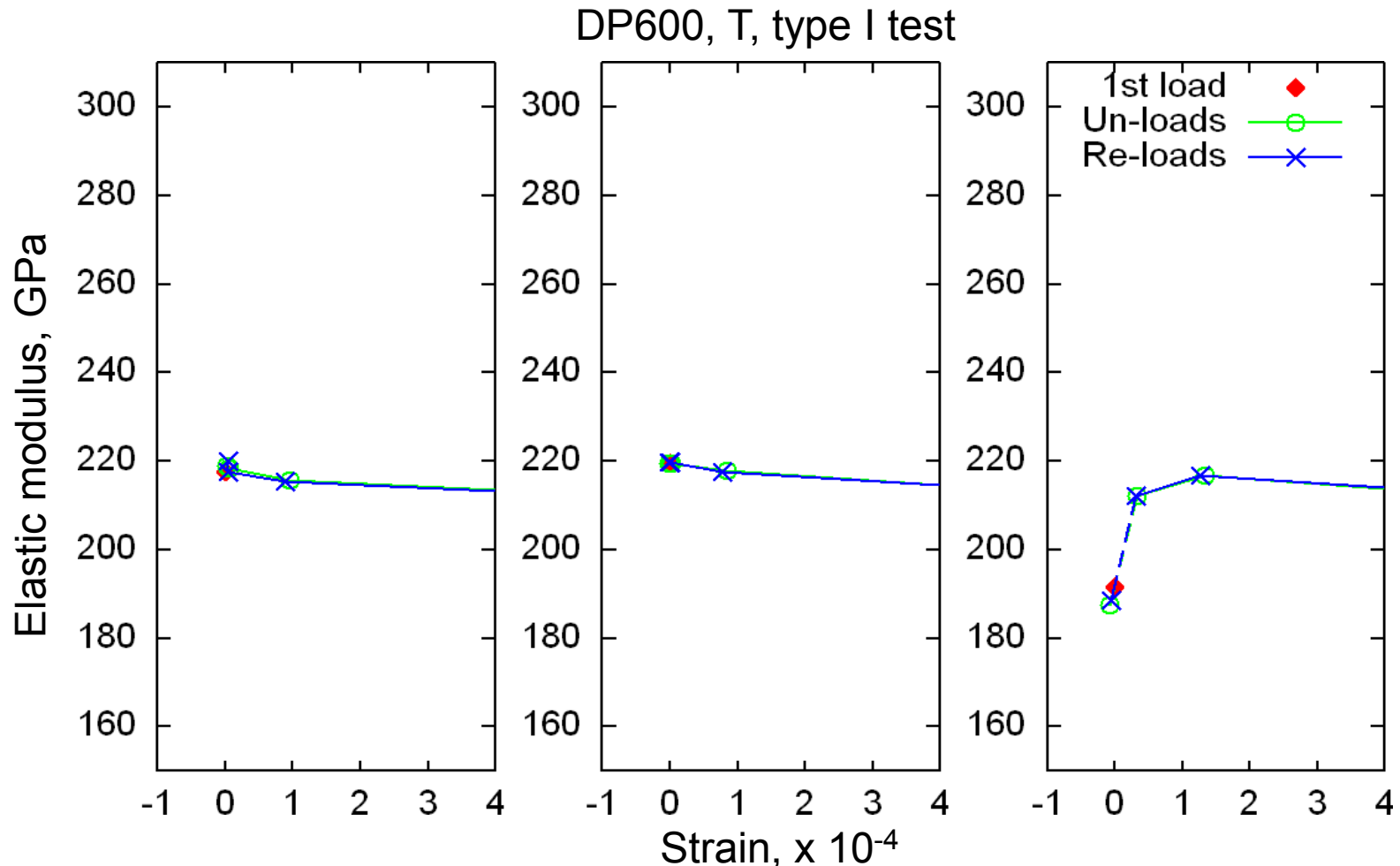
green lines: elastic modulus calculations

**Results (1):** elastic modulus from the 25, 50, 75 and 100% YS unload-reload cycles.



Large variations with increasing maximum stress, below YS, possibly due to **straightening**

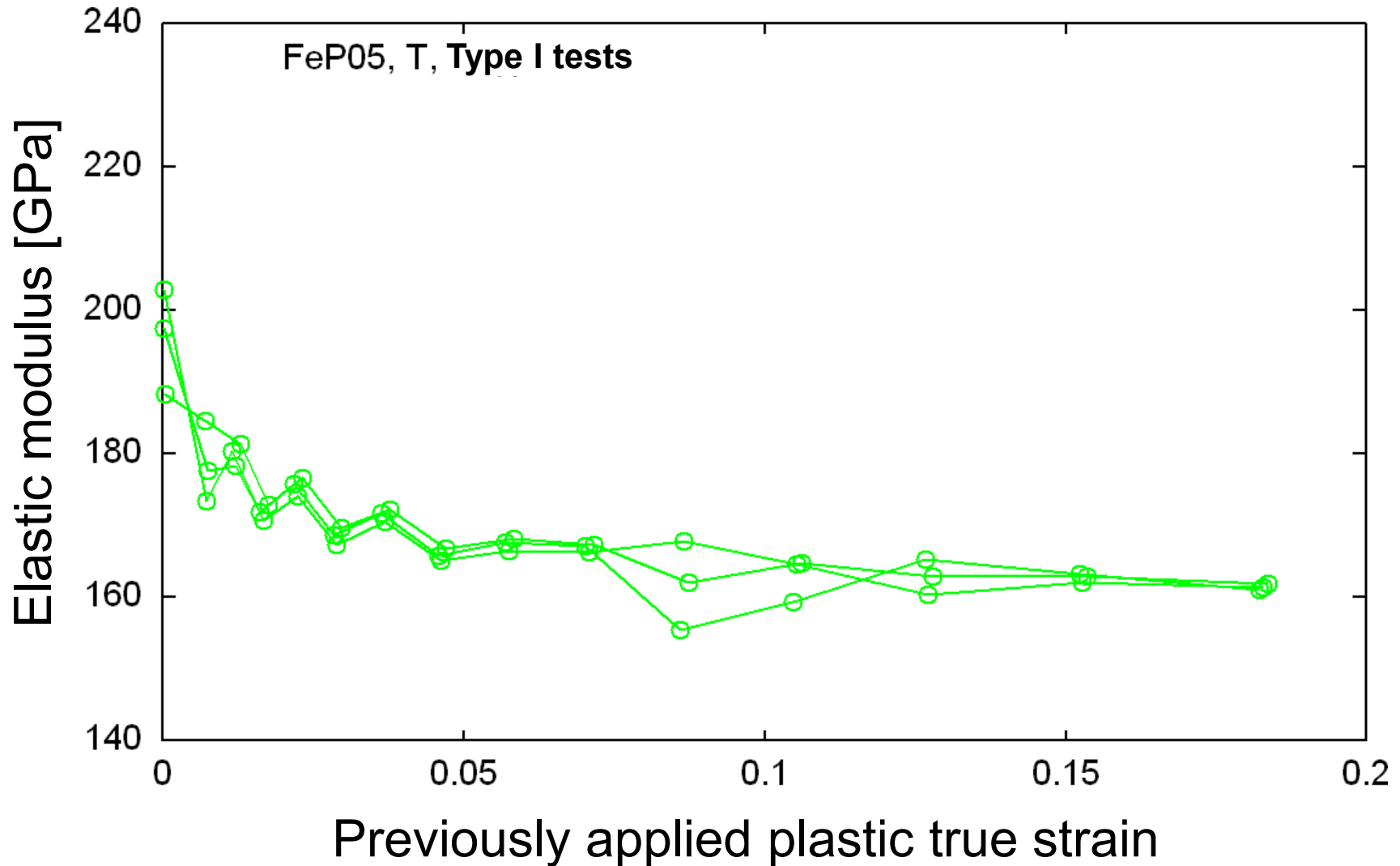
**Results (1):** elastic modulus from the 25, 50, 75 and 100% YS unload-reload cycles.



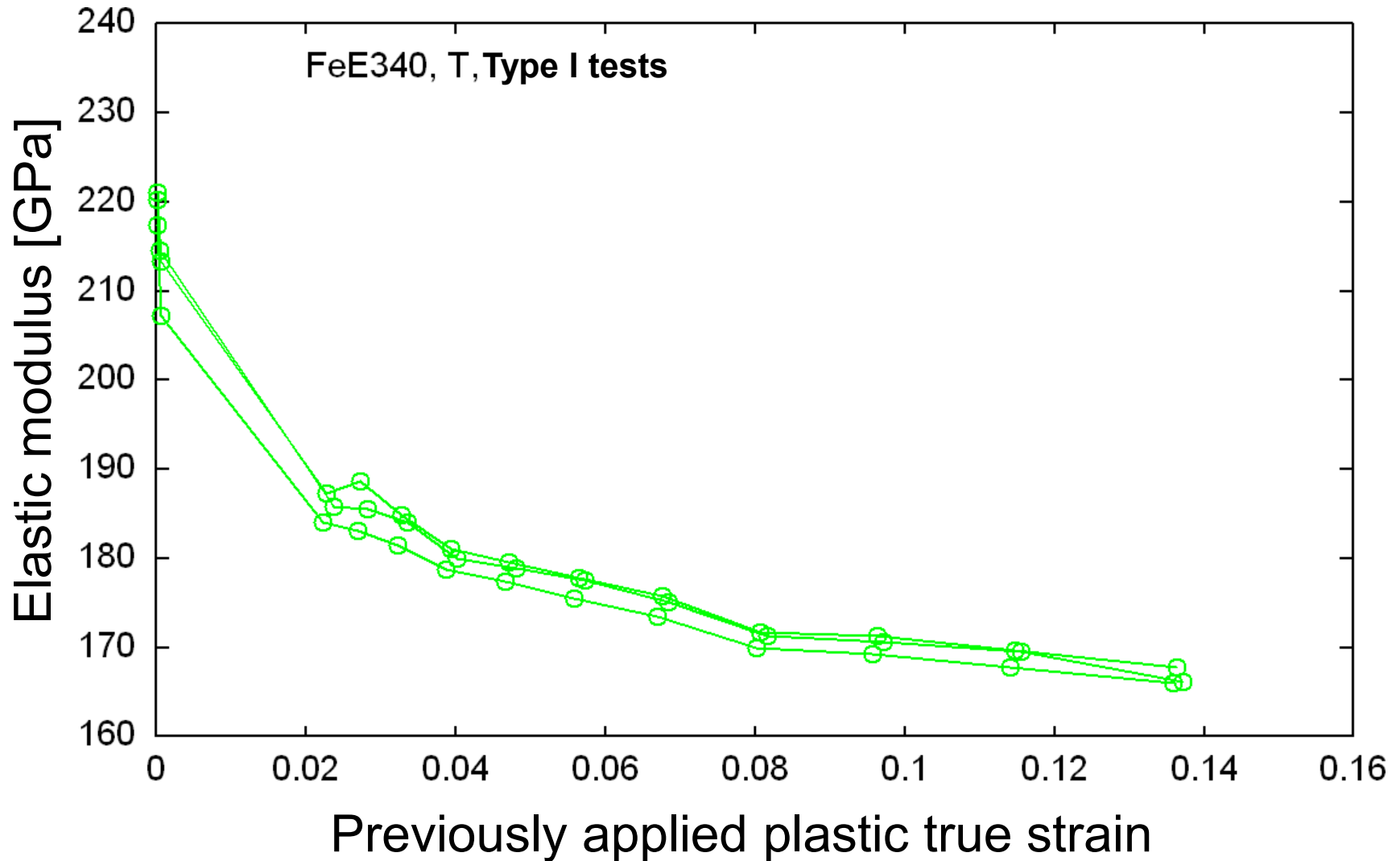
... but not in all cases.

The 0% strain modulus reported below will generally be for about 70% YS loading

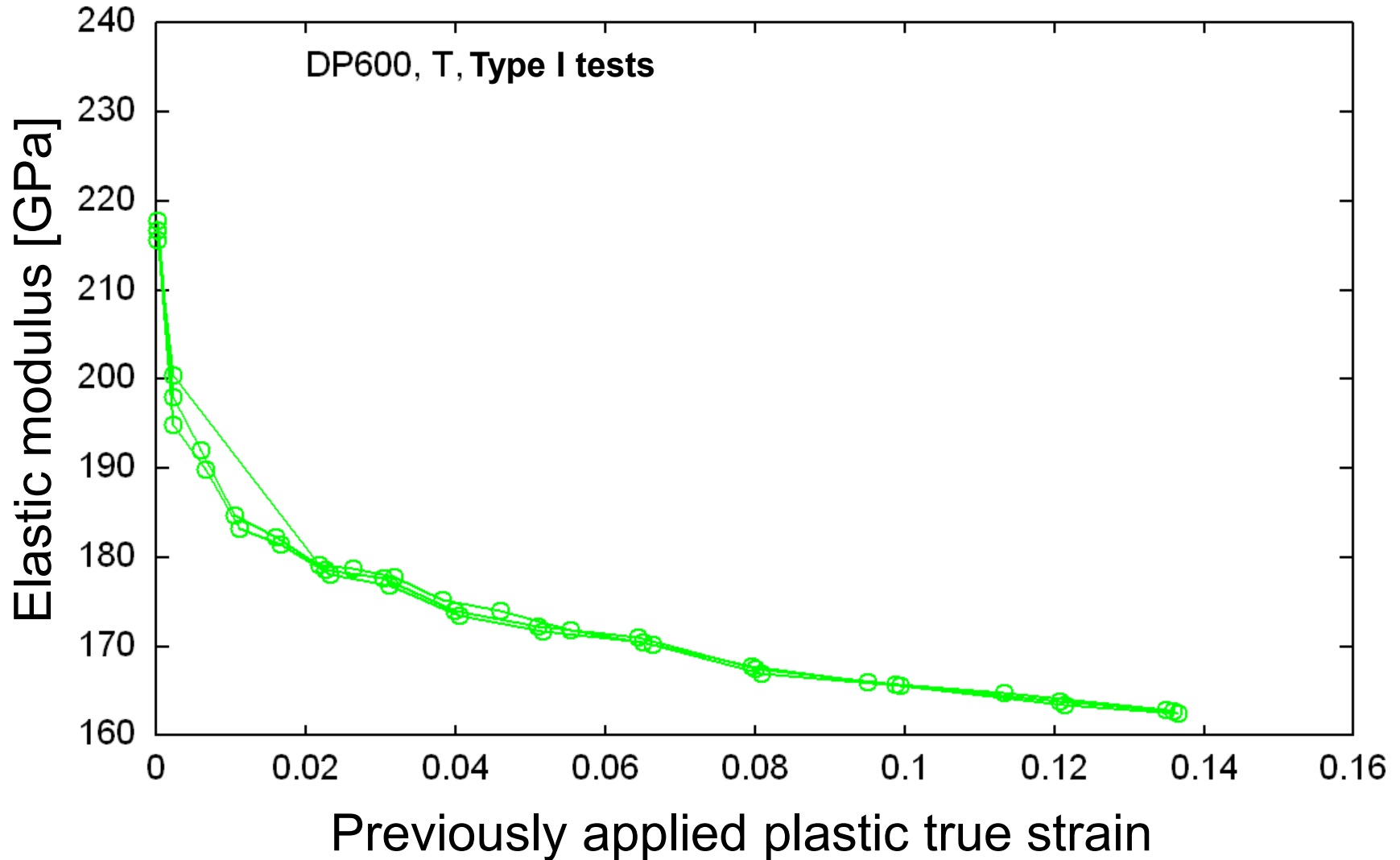
## Results (2): elastic modulus of the 1<sup>st</sup> unload after the plastic prestrain (3 samples)



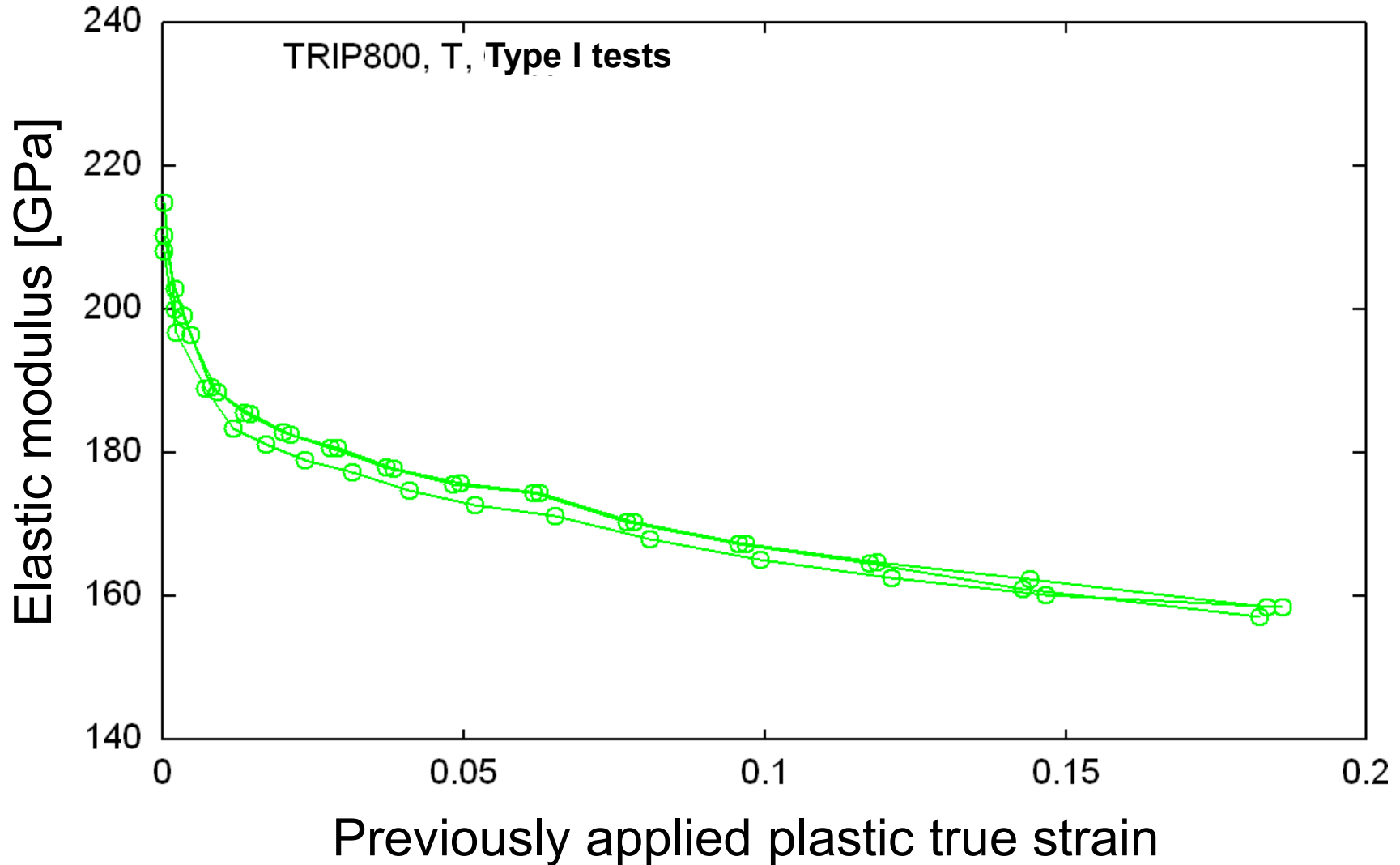
## Results (2): elastic modulus of the 1<sup>st</sup> unload after the plastic prestrain (3 samples)



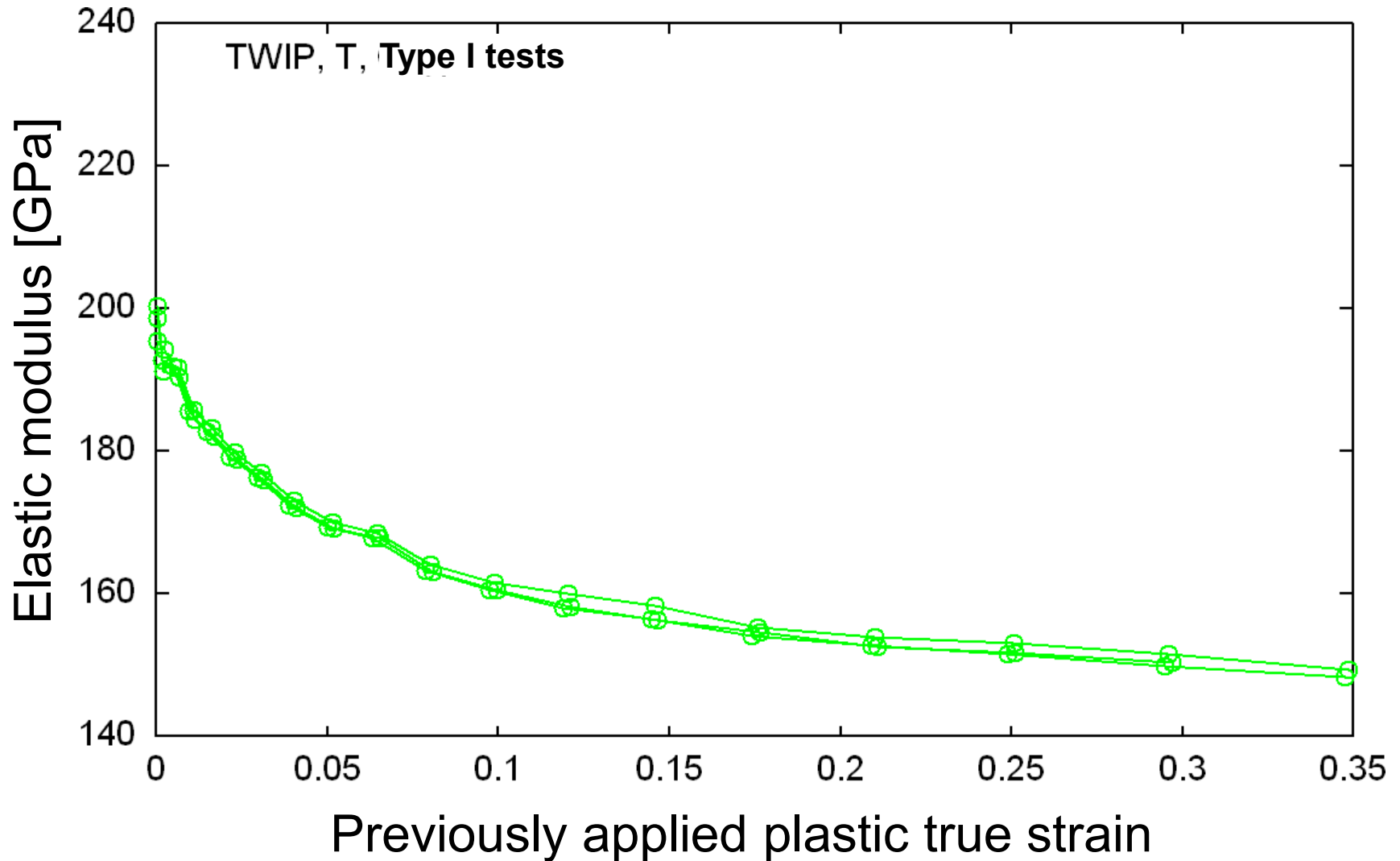
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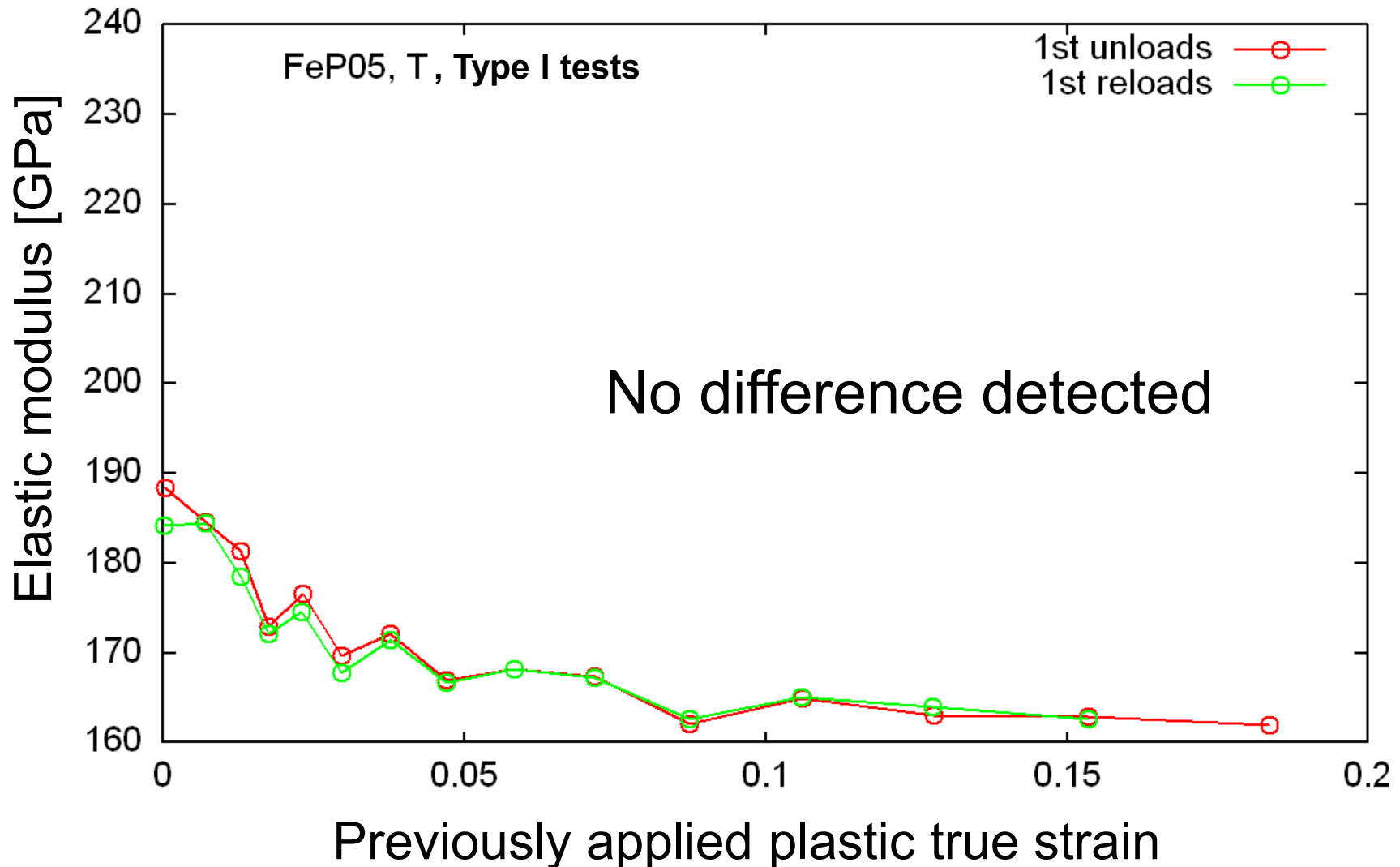


## Results (2): elastic modulus of the 1<sup>st</sup> unload after the plastic prestrain (3 samples)

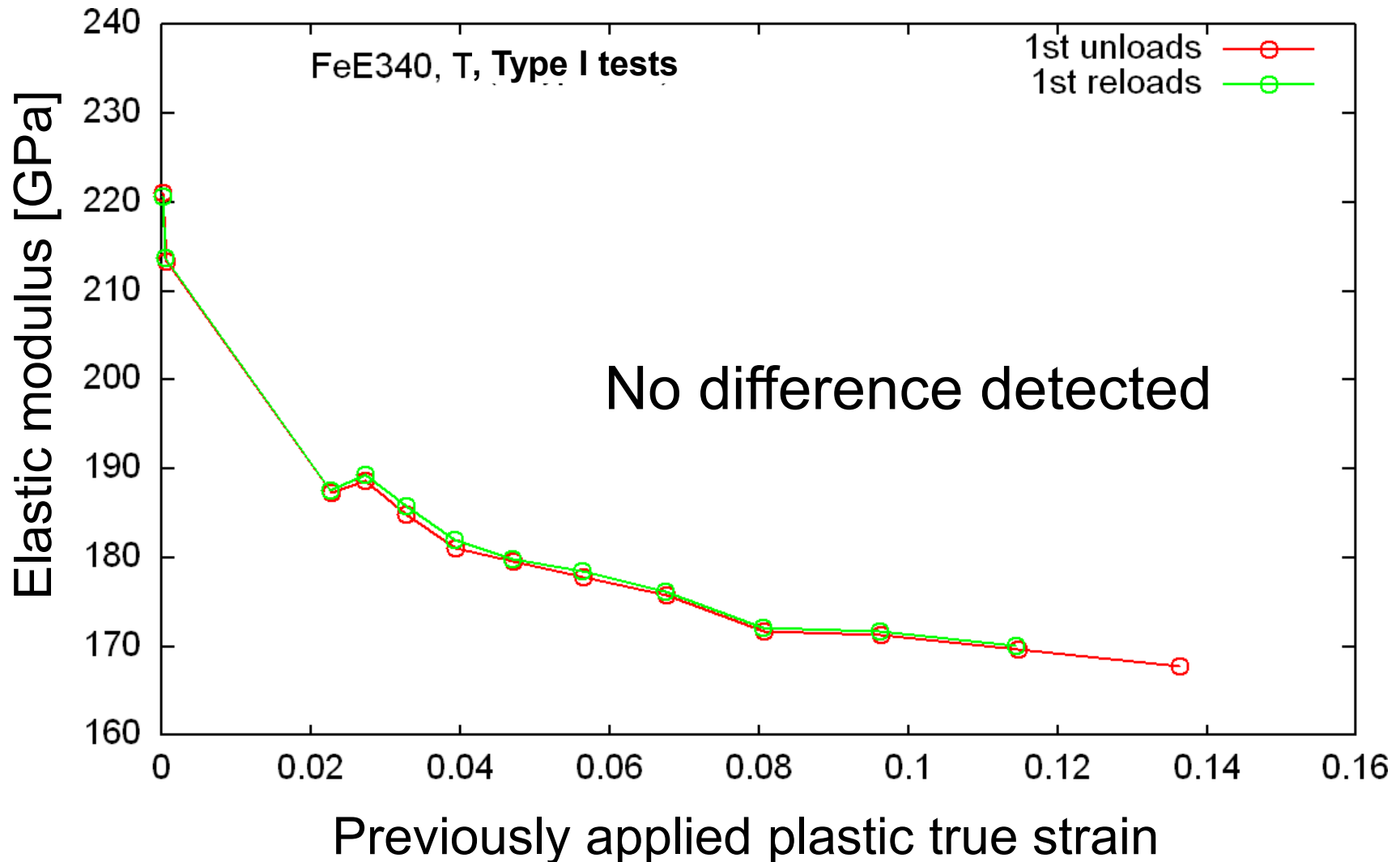




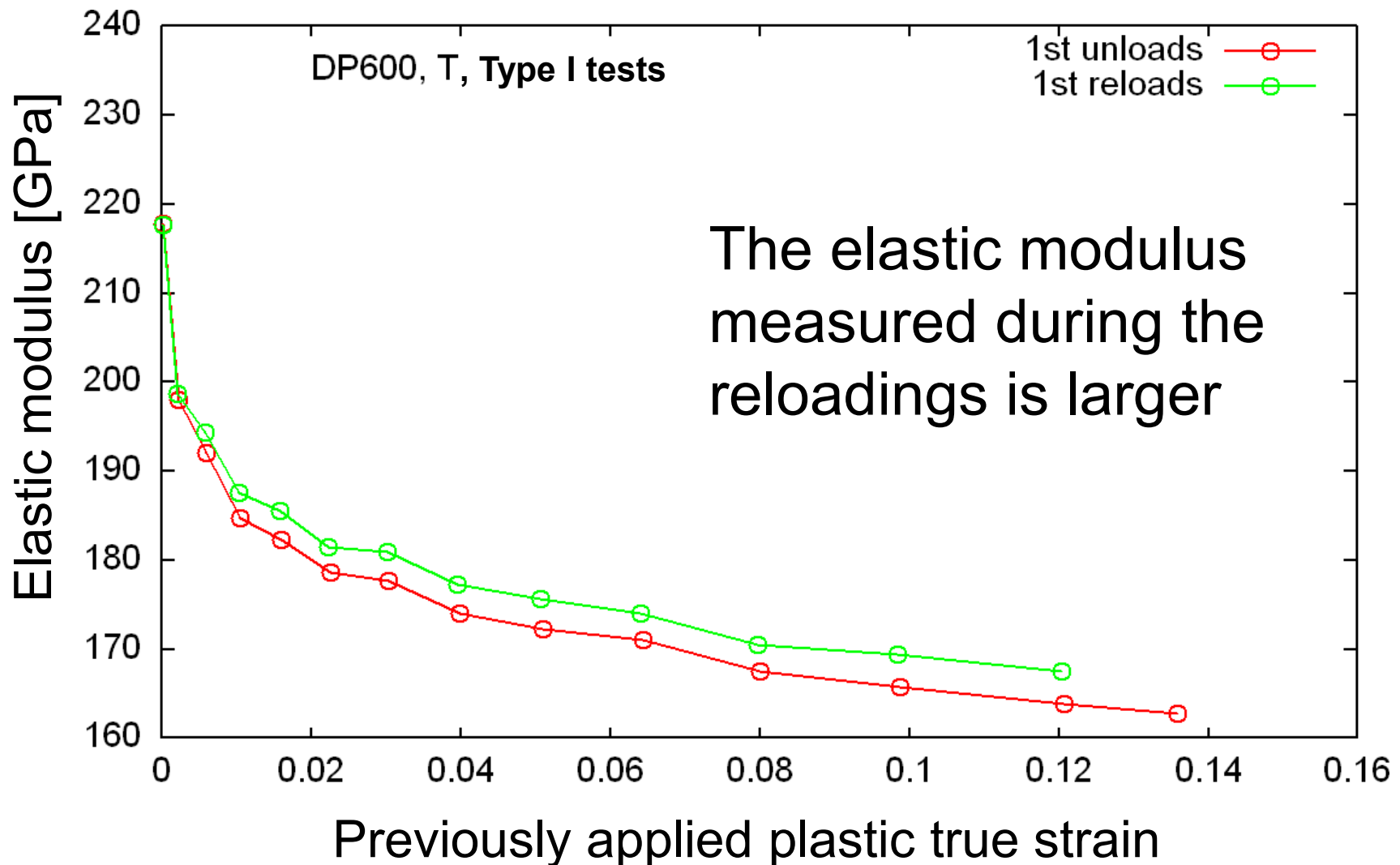
**Results (3):** elastic modulus obtained from the 1<sup>st</sup> unload after the plastic strain, or from the successive (1<sup>st</sup>) reload



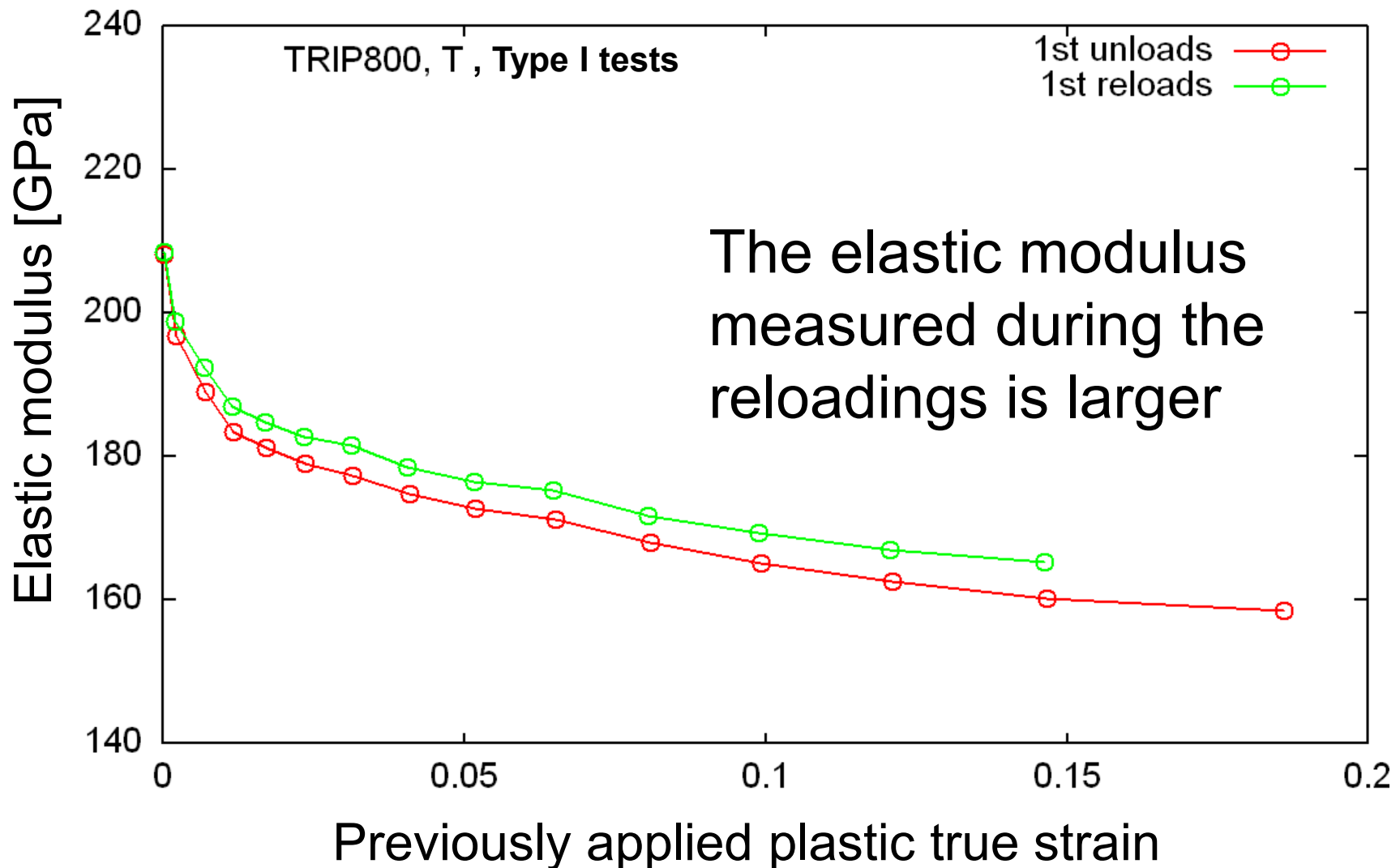
**Results (3):** elastic modulus obtained from the 1<sup>st</sup> unload after the plastic strain, or from the successive (1<sup>st</sup>) reload



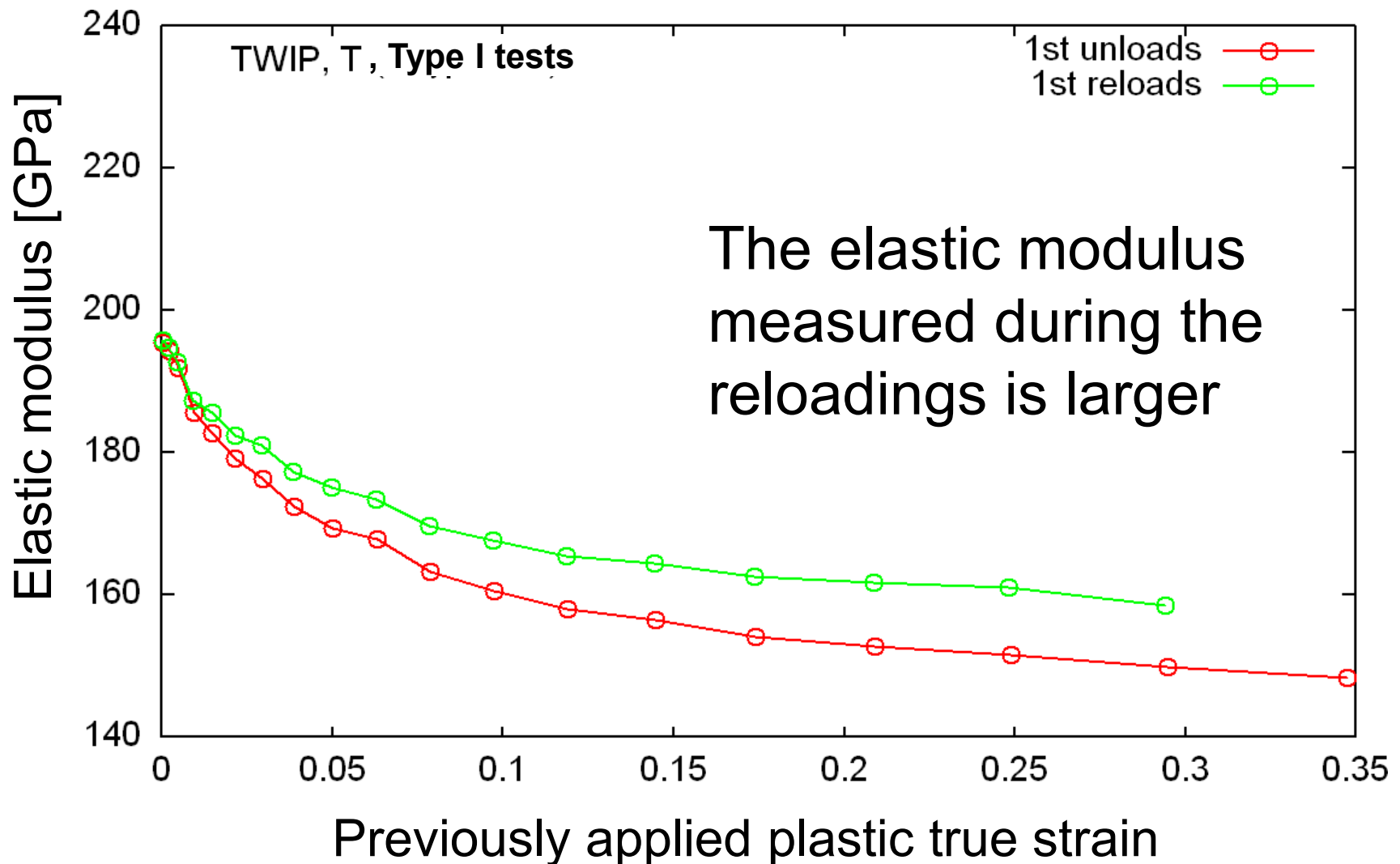
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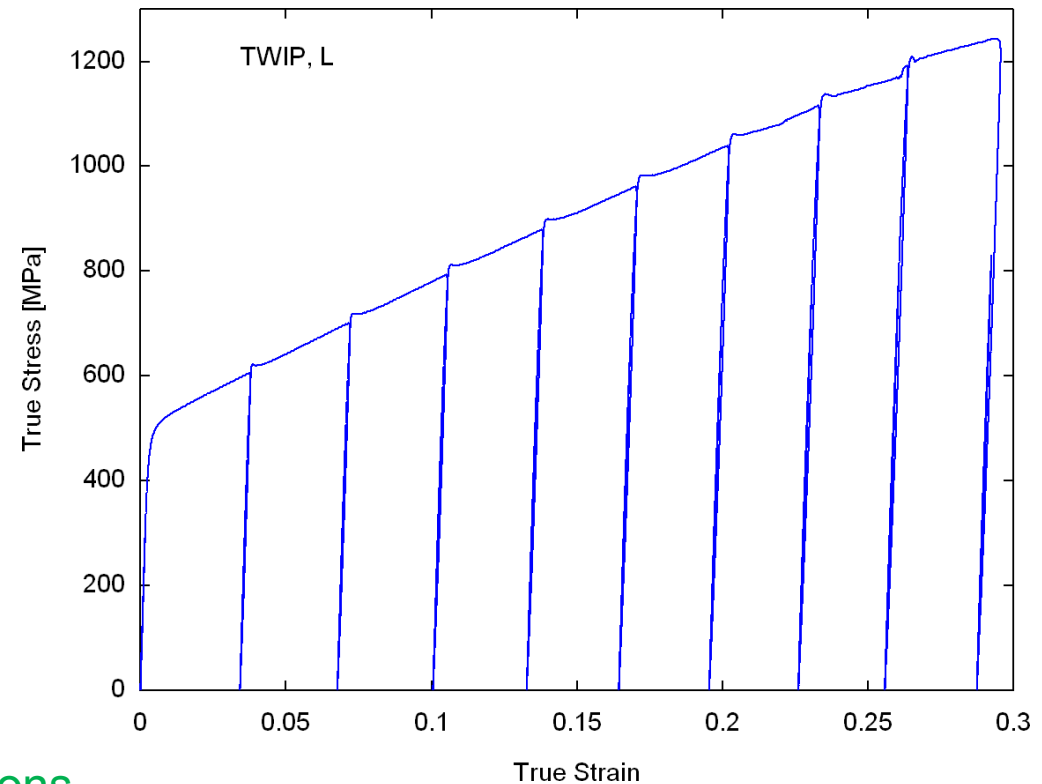
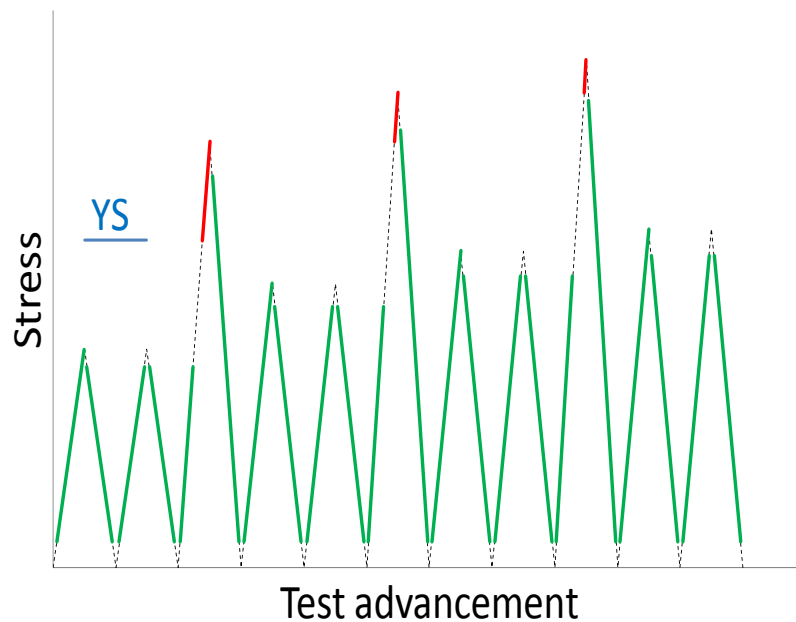


**Results (3):** elastic modulus obtained from the 1<sup>st</sup> unload after the plastic strain, or from the successive (1<sup>st</sup>) reload



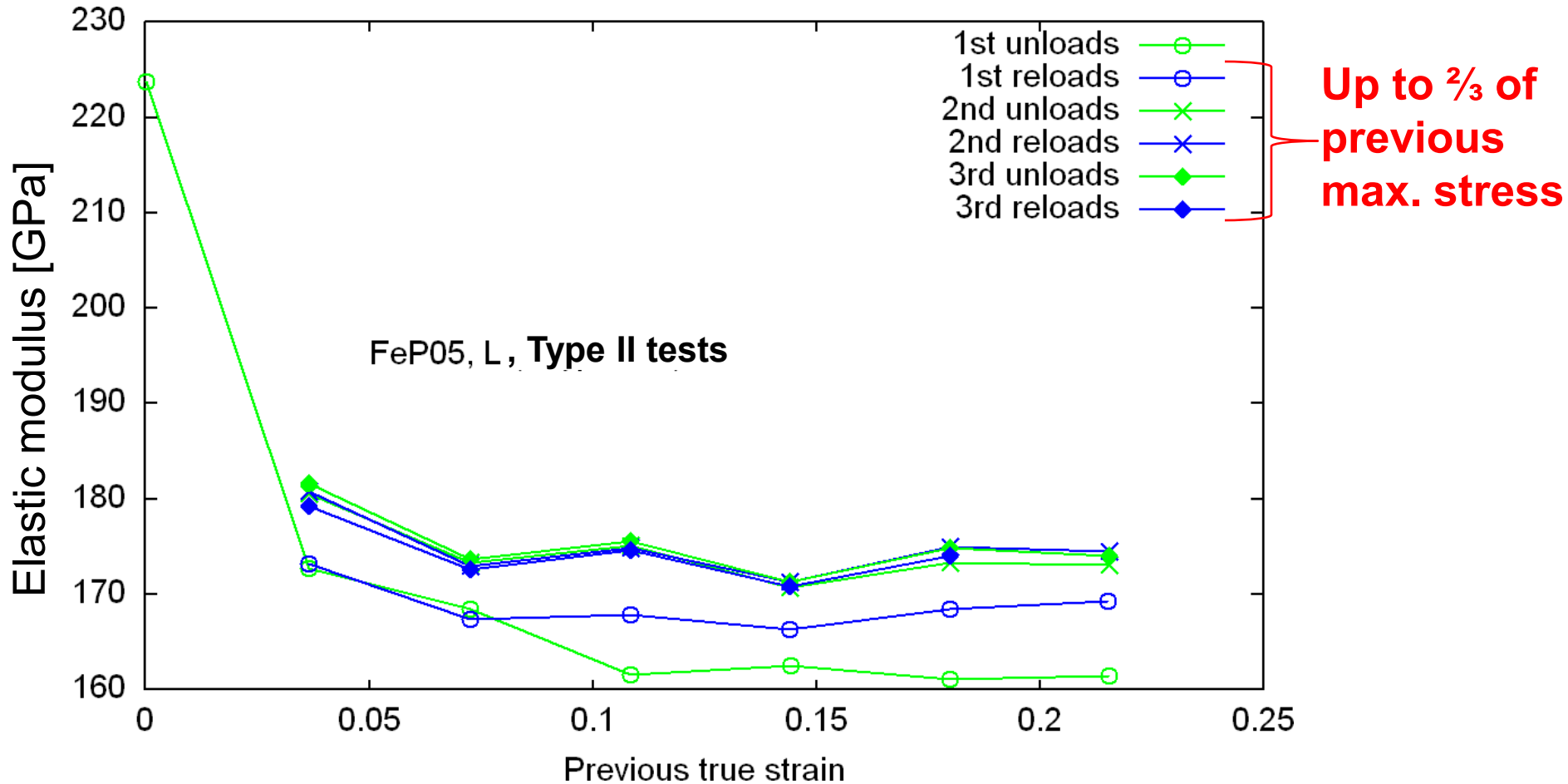
# Type II tests

- repeated  $\approx 3\%$  true **plastic strain steps**  
(elastic strain rate: loading  $\approx 10^{-3} \text{ s}^{-1}$ , unloading  $\approx 10^{-4} \text{ s}^{-1}$ )
- 2 elastic unload-reload cycles at test start and after each plastic step, up to  $\frac{2}{3}$  of YS or  $\frac{2}{3}$  of previous maximum stress (strain rate  $\approx 10^{-4} \text{ s}^{-1}$ )



green lines: elastic modulus calculations

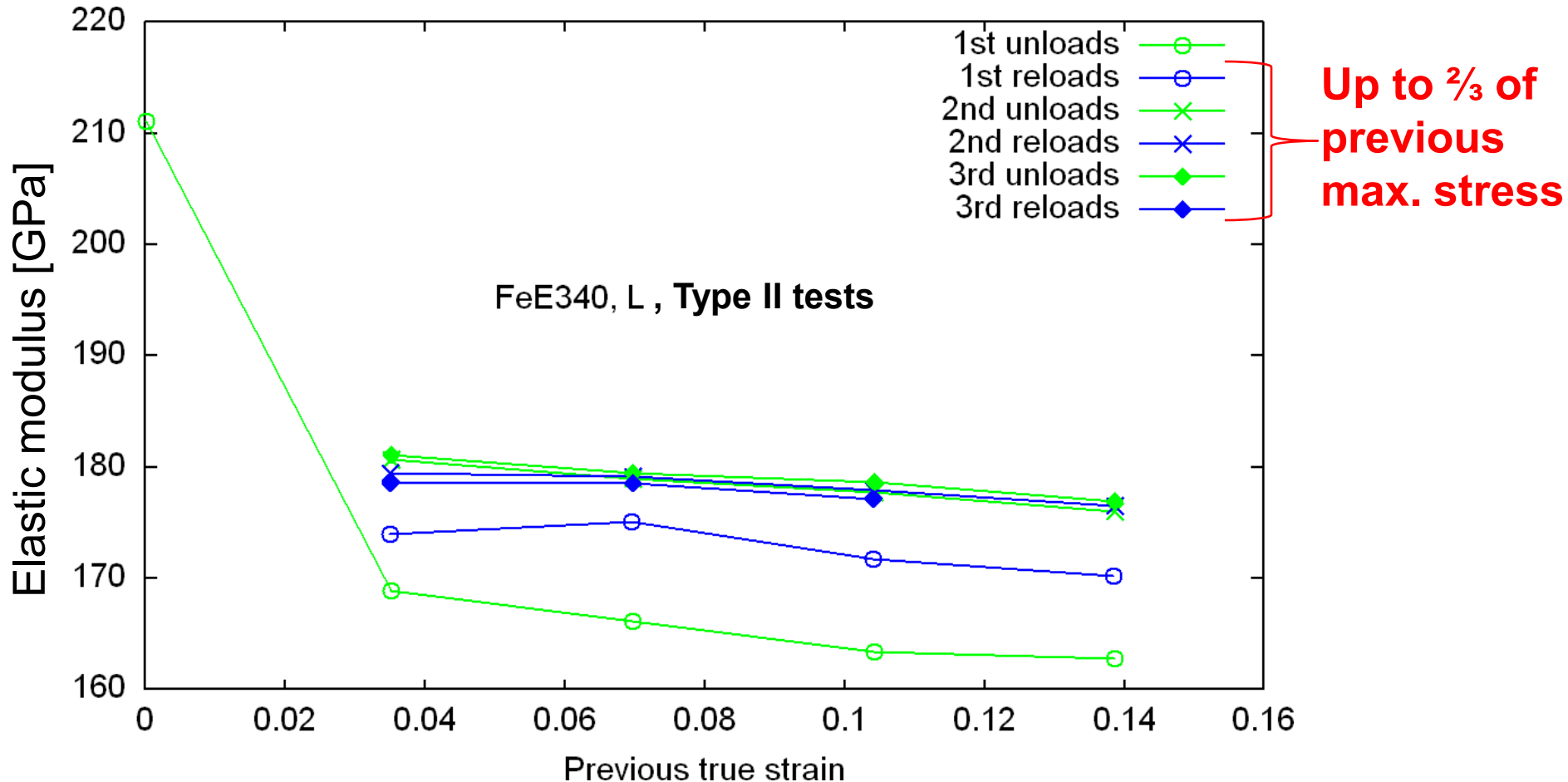
## Results (4): elastic modulus measured upon successive unloads and reloads after the plastic strain



Differences are slightly broader than in type I tests, probably due to the lower reloading max. stress.

After the 2nd unload-reload cycle, an asymptote is reached

## Results (4): elastic modulus measured upon successive unloads and reloads after the plastic strain



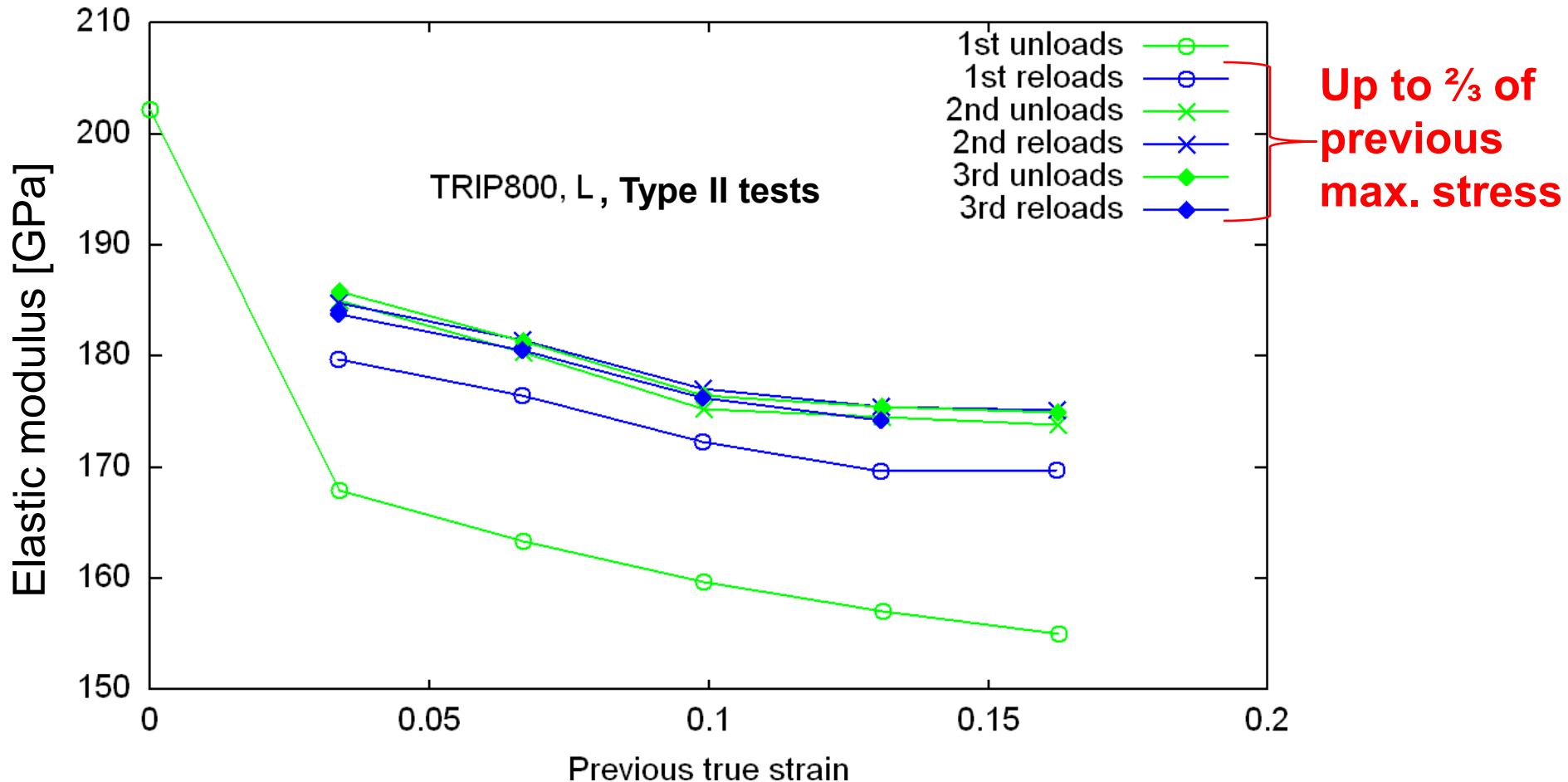
Up to  $\frac{2}{3}$  of previous max. stress

Differences are slightly broader than in type I tests, probably due to the lower reloading max. stress.

After the 2nd unload-reload cycle, an asymptote is reached



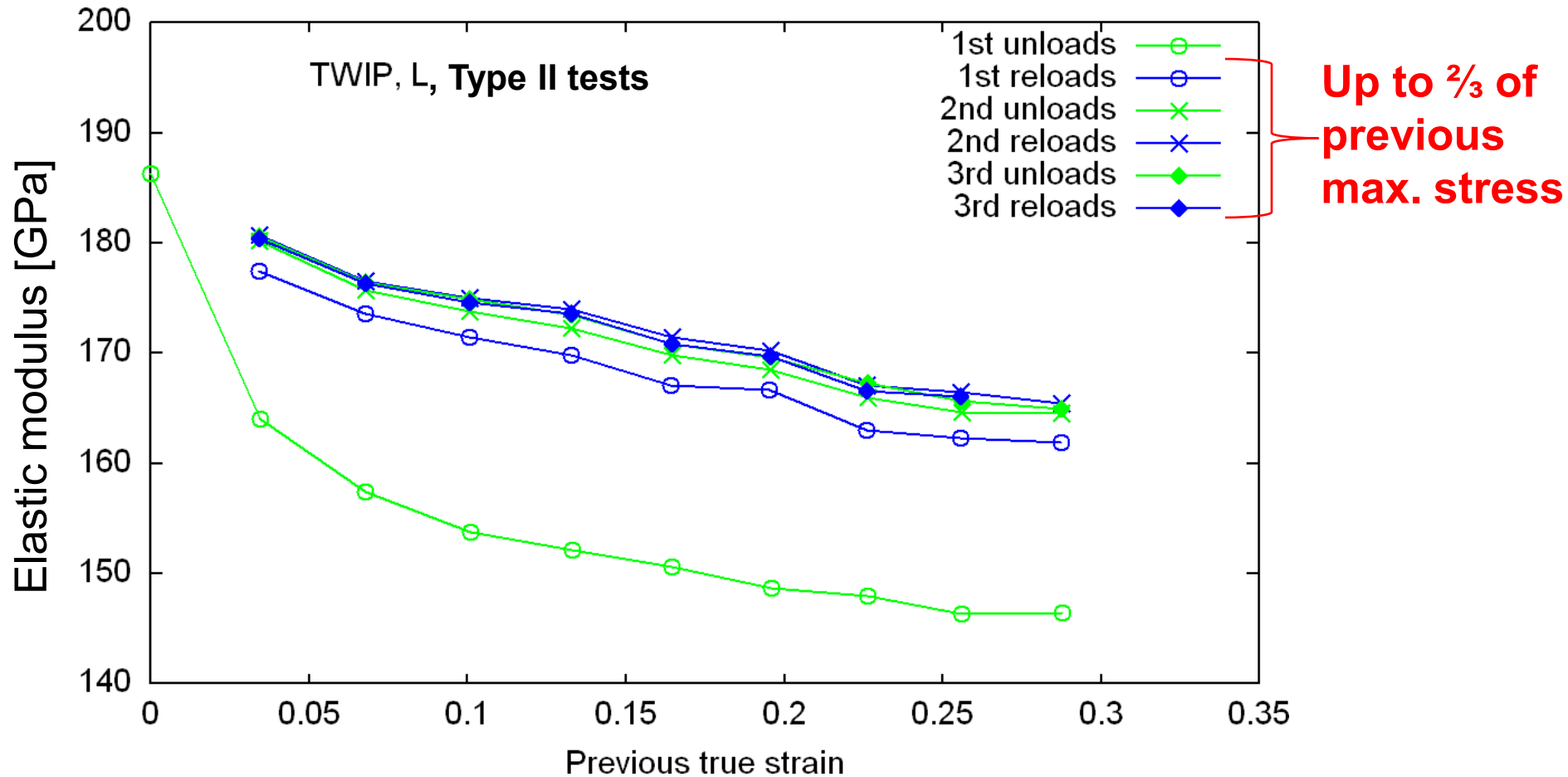
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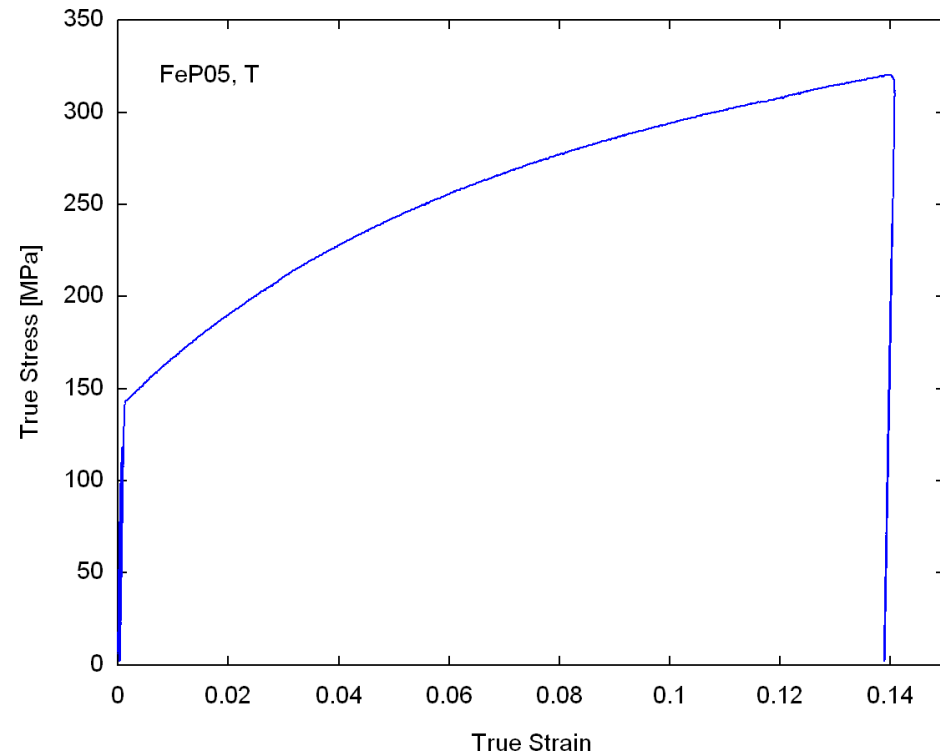
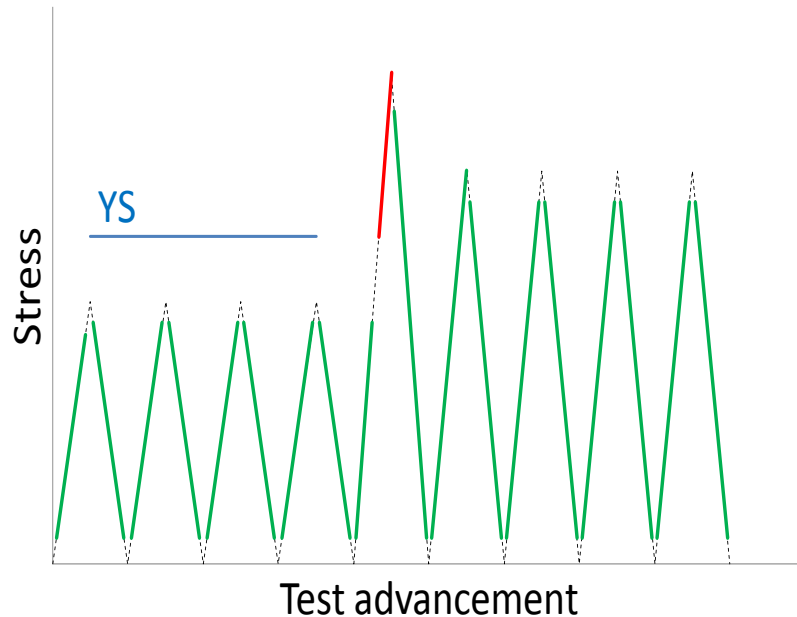


Differences are slightly broader than in type I tests, probably due to the lower reloading max. stress.

After the 2nd unload-reload cycle, an asymptote is reached

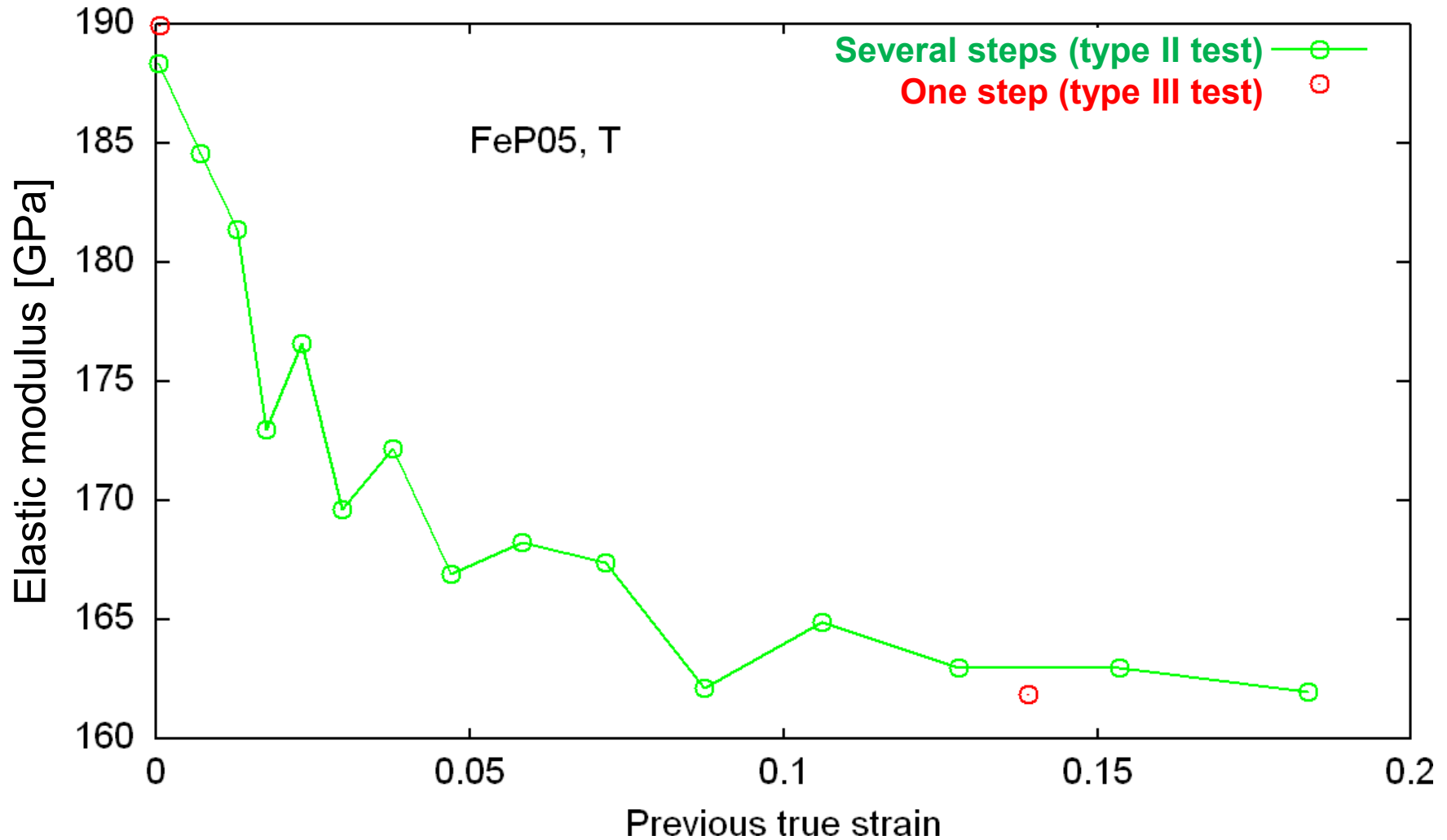
# Type III tests

- one  $\approx 14\%$  true **plastic strain step**  
(elastic strain rate: loading  $\approx 10^{-3} \text{ s}^{-1}$ , unloading  $\approx 10^{-4} \text{ s}^{-1}$ )
- 4 elastic unload-reload cycles at test start, up to 80% YS, and after the plastic strain, up to 80% of maximum stress (strain rate  $\approx 5 \cdot 10^{-5} \text{ s}^{-1}$ )



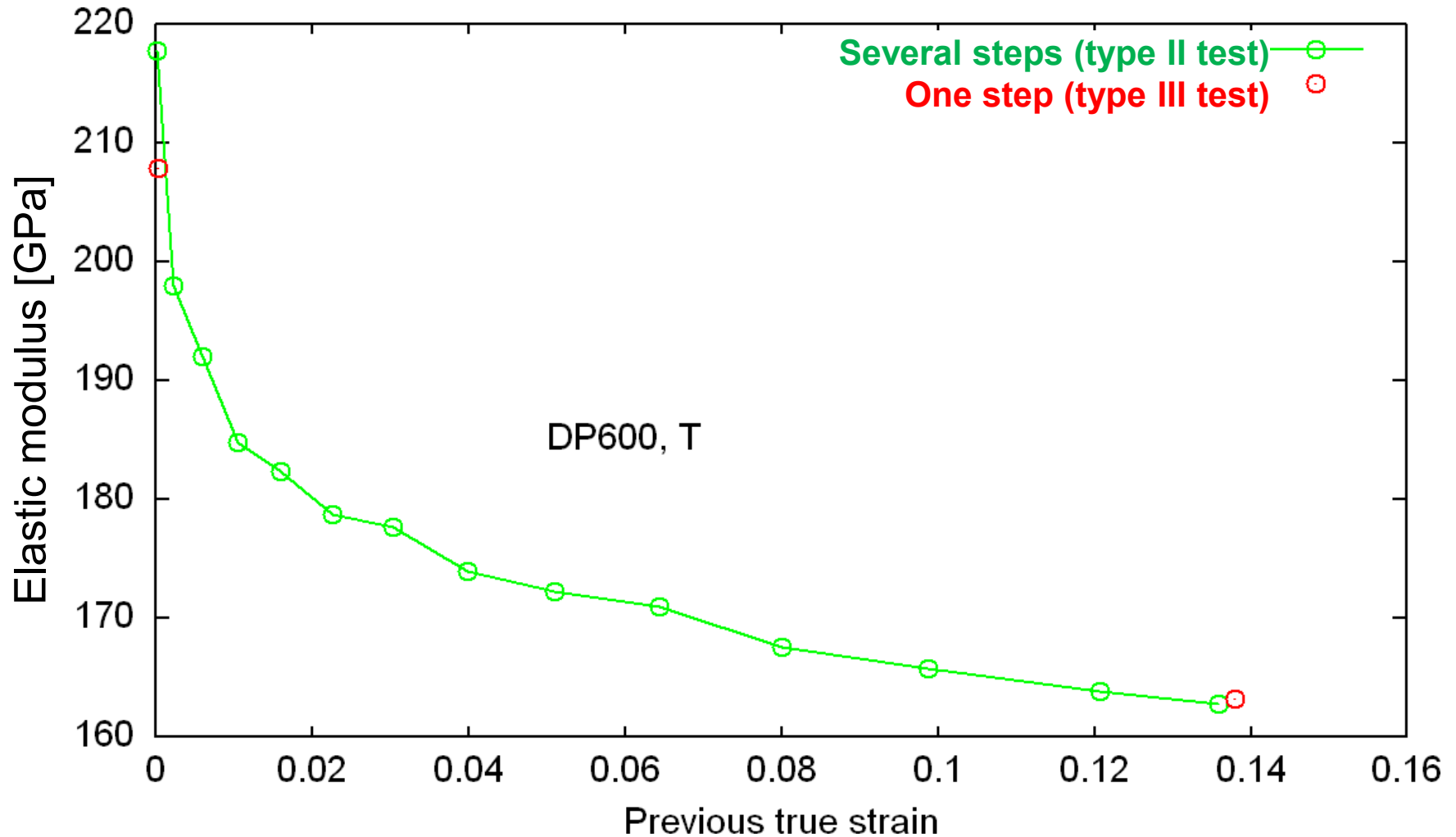
green lines: elastic modulus calculations

## Results (5): elastic modulus measured after one or several prestrain steps (upon 1<sup>st</sup> unloading)



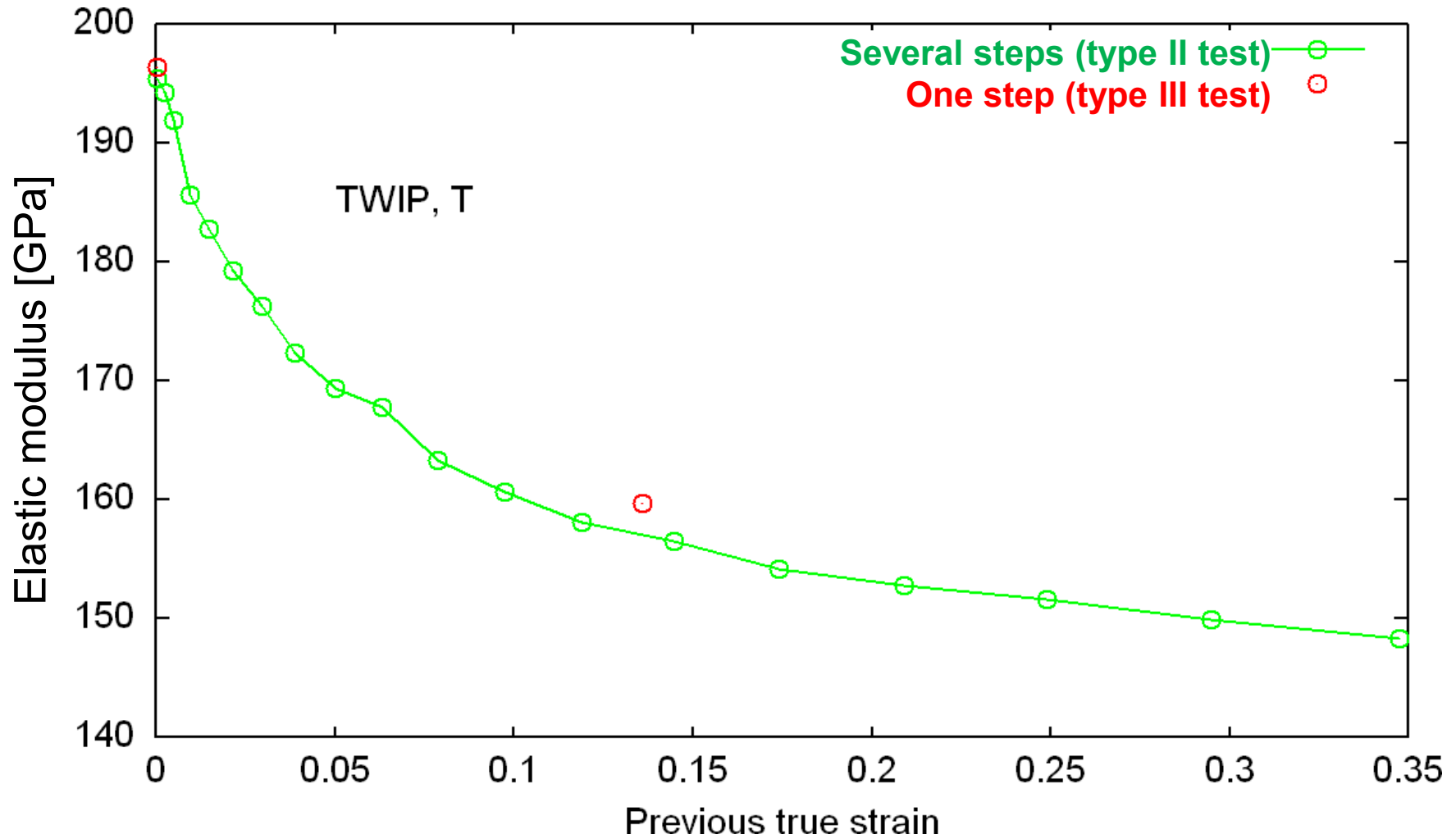
No relevant differences

## Results (5): elastic modulus measured after one or several prestrain steps (upon 1<sup>st</sup> unloading)



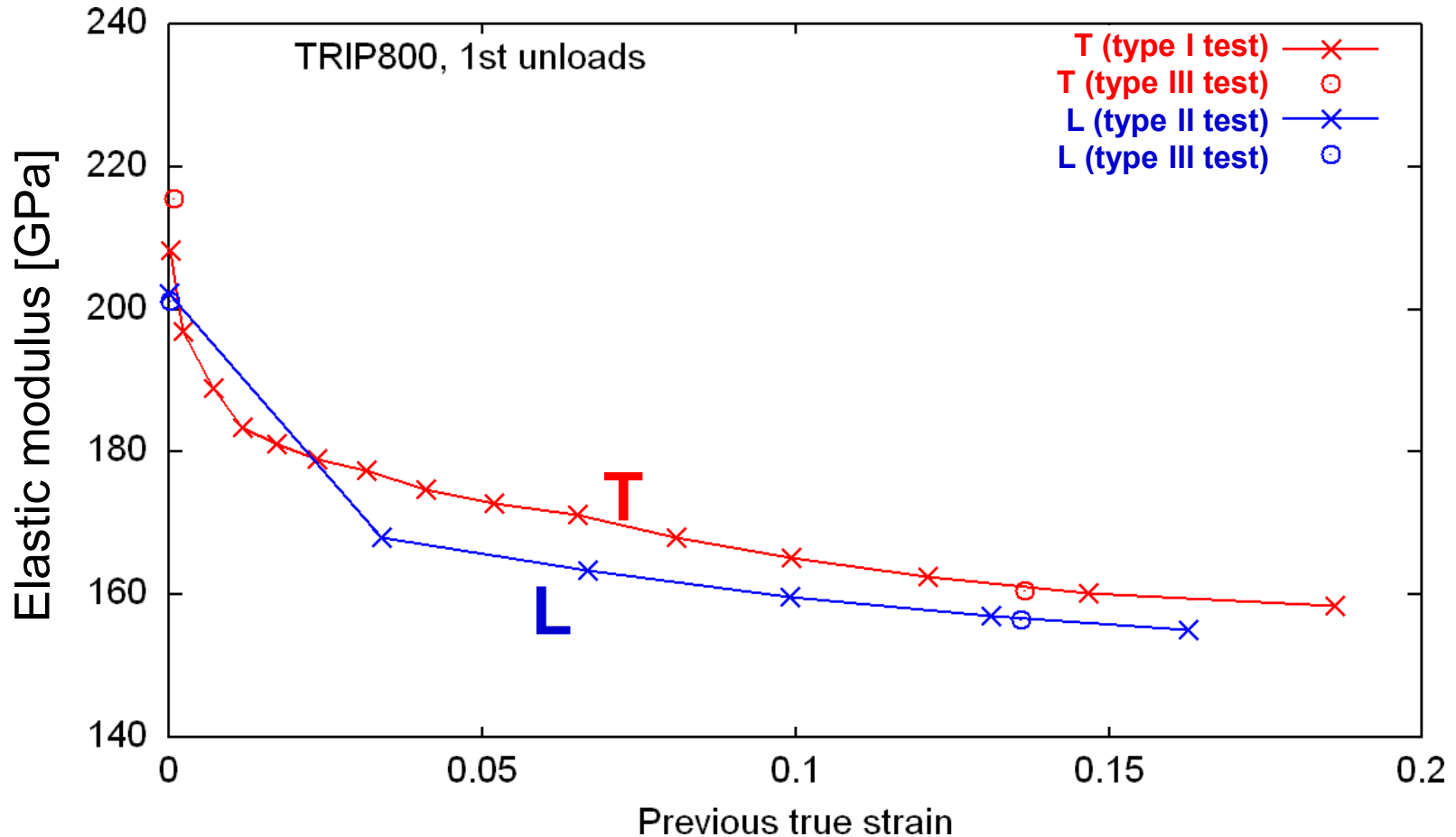
No relevant differences

## Results (5): elastic modulus measured after one or several prestrain steps (upon 1<sup>st</sup> unloading)



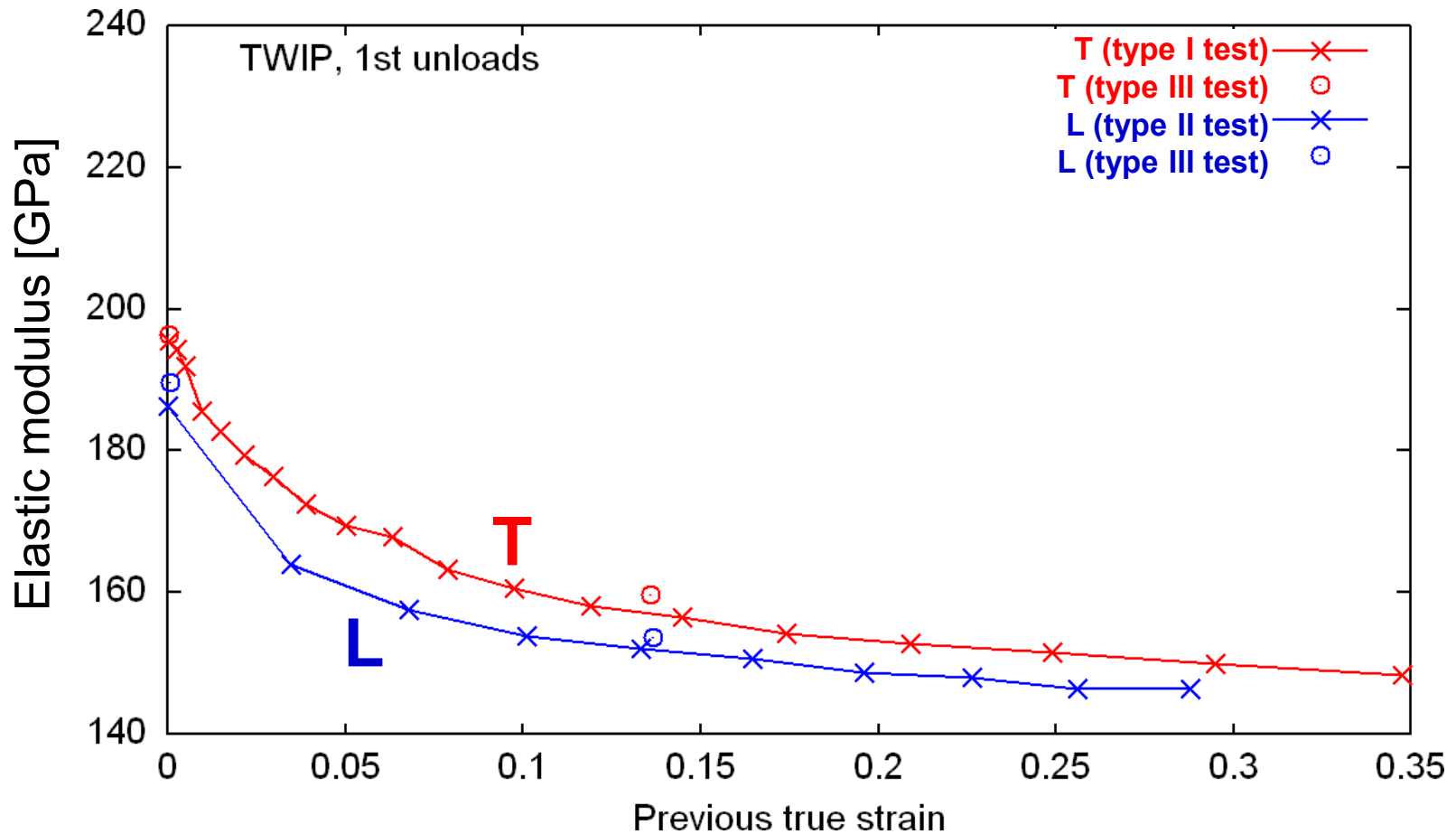
No relevant differences

## Results (5): elastic modulus of specimens with T or L rolling orientations (measured upon 1<sup>st</sup> unloading)



A small difference due to the specimen orientation can be detected in most examined materials

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A small difference due to the specimen orientation can be detected in most examined materials



# Conclusions

- The elastic modulus of the examined automotive steels decreases with increasing previous plastic deformation (done at room temperature)
- If one or more elastic unloading and reloading cycles are performed after a plastic deformation, increasing values of elastic modulus are detected, until an asymptote is reached (which, however, is still lower than the modulus of the undeformed steel)
- No significant differences are detected if the same previous plastic deformation is performed in one or several steps
- Smaller differences are due to the orientation relative to sheet rolling