# Matter-Antimatter : An Accentuation-Attrition Model 

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#### Abstract

A system of matter dissipating antimatter and parallel system of antimatter that contribute to the dissipation of the velocity of production of matter is investigated. It is shown that the time independence of the contributions portrays another system by itself and constitutes the equilibrium solution of the original time independent system. With the methodology reinforced with the explanations, we write the governing equations with the nomenclature for the systems in the foregoing, by concatenation process, ipso facto. We discuss following systems in all its predicational anteriorities, character consonations, ontological consonances, primordial exactitude, accolytish representation, differential relations, and concomitant contiguous similarities. (1) Antimatter as an integral part of the electromagnetic phenomena. (2) Electricity consists of the flow of electrons and positrons in opposite directions along a conductor (not only of electrons, as current accepted knowledge describes), induced by the crossing of a magnetic field through the conductor. (3) When a charged particle passes through matter at rest it will cause the production of electron pairs, that is, electrons and positrons, but if nothing separates them by force, they will reunite after the passing of the charged particle, nullifying each other, and the atoms of matter will be back at rest. (4) In order to preserve the law of conservation of energy, the amount of energy required to break free the electron and the positron from a bielectron (a theoretical dual particle containing an electron and a positron) must be equal to the amount of energy released by a matter-antimatter encounter of the same particles. (5) When a conductor is at rest all the bielectrons are located at their respective orbits in the conductor's atoms, generating no electric charge. (6) When a conductor is placed under a moving magnetic field, its otherwise stable bielectrons will break apart into electrons and positrons, which will flow in opposite directions along the conductor. At the closing of the circuit, electrons and positrons, attracted to each other by their opposite charge, reunite into bielectrons releasing an equal amount of energy as initially required to separate them. (7) Matter gormandizes antimatter (Antimatter has to pre-exist to be able to appear in a collision of particles. We are not creating antimatter; antimatter is there, intermingled with matter. Particle collisions do not "produce" antimatter; they separate antimatter from the particles of which it is part). (8) We assume that should there be another force in physics: the force of attraction between matter and antimatter and give a model. We shall call it Bundeswehr (German for "Federal Defense"). So Bundeswehr binds matter and antimatter. (9) At the closing of the circuit the free electrons and positrons, pushed forward by their own "pressure", are irresistibly pulled by the attraction of their antimatter counterpart. It is this process of mutual attraction and continuous reunification into bielectrons which causes the flow of electrons and positrons along the conductors. Paper answers, not wholly or in full measure, but substantially the relationship between dark matter and antimatter and speculates in epiphenomena and phenomenological form the circumspective jurisprudence of consideration of the antimatter as dark matter. This also answers the long standing question in cosmology that why matter is prevalent in the universe in contrast to antimatter. The paper seems to confirm antimatter as an intrinsic constituent of ordinary matter; antimatter as an integral part of the electromagnetic phenomena; the existence of a new particle namely bielectron, consisting of an electron and a positron joined together within the atom; that matter and antimatter preceded the big-bang and their violent encounter may have been the actual cause of the big-bang itself; that matter and antimatter have a pacific coexistence in today's universe, after the big-bang; the possible existence of a new force in physics namely Bundeswehr, which would recombine and keep matter and antimatter particles together.


Keywords: matter-antimatter, where antimatter is, dark-matter, theory of electricity, bielectron, Big-Bang, origin of the Universe.

## 1. INTRODUCTION—VARIABLES USED

Classification of the protagonist or antagonist laws based on the characteristics and penchance, predilection, proclivity and propensities of the systems under investigation:
Quintessential, bastion, pillar post, stylobate and sentinel characteristics are determined by the pattern of organization of the system. For instance illustrational delineation is determined by the pattern of the organization of the system. Autopoietic system is one which can be stated in unmistakable terms the structure of the matter in
question namely the dipole state and tin particular the binding energies of the systems in general.
One example from evolutionary biology and is the cell nucleus that contains the generic material namely the DNA molecules carrying generic information and RNA molecules deliver instructions to the production centres. Coming back to brass tacks of our system the elemental endowment and positive results and disastrous consequences, detrimental ramifications, deleterious implications allegorical, analytical, annotative, critical, declarative, demonstrative around us appears to be "matter", but we routinely produce antimatter in small quantities in high energy accelerator experiments. When a matter particle meets its antimatter particle they destroy each other completely (the technical term is "annihilation"), releasing the equivalent of their rest masses in the form of pure energy (according to the Einstein $E=\mathrm{mc}^{2}$ relation). For example, when an electron meets an antielectron, the two annihilate and produce a burst of light having the energy corresponding to the masses of the two particles.
Because the properties of matter and antimatter parallel each other, we believe that the physics and chemistry of a galaxy made entirely from antimatter would closely parallel that of our matter galaxy. Thus, is conceivable that life built on antimatter could have evolved at other places in the Universe, just as life based on matter has evolved here. (But if your antimatter twin should show up some day, we would advise against shaking hands--remember that matter and antimatter annihilate each other!) However, we have no evidence thus far for large concentrations of antimatter anywhere in the Universe. Everything that we see so far seems to be matter. If true, this is something of a mystery, because naively there are reasons from fundamental physics to believe that the Universe should have produced about as much matter as antimatter.
Solutional behaviour of the systems enumerated in the following bears ample testimony, infallible observatory and impeccable demonstration to the fact that there do exist Antimatter which could be Dark matter in the general term for matter that we cannot see to this point with our telescopes, but that we know must be there because we see its gravitational influence on the rest of the Universe. Many different experiments indicate that there is probably 10 times more matter in the Universe (because we see its gravitational influence) than the matter that we see. Thus, dark matter is basically what the Universe is made out of, but we don't yet know what it is!
As one simple example of the evidence for dark matter, the velocity of rotation for spiral galaxies depends on the amount of mass contained in them. The outer parts of our own spiral galaxy, the Milky Way, are rotating much too fast to be consistent with the amount of matter that we can detect; in fact the data indicates that there must be about 10 times as much matter as we can see distributed in some diffuse halo of our galaxy to account for its rotation. The same is true for most other spiral galaxies where the velocities can be measured.
There are various candidates for the dark matter, ranging from ordinary matter that we just can't see because it isn't bright enough (for example, ordinary matter bound up in black holes, or very faint stars, or large planet-like objects like Jupiter) to more exotic particles that have yet to be discovered. There are some fairly strong arguments based on the production of the light elements in the Big Bang indicating that the majority of the dark matter cannot be ordinary matter or antimatter (which physicists call "baryonic matter"), and thus that the majority of the mass of the Universe is in a form very different from the matter that makes up us and the world around us (physicists call this "non-baryonic matter"). If that is true, then the matter that we are made of (baryonic matter) is but a small impurity compared to the dominant matter in the universe (non-baryonic matter). As someone has put it, "not only are we not the center of the Universe, we aren't even made of the right stuff!"
The nature of the dark matter is perhaps the most fundamental unsolved problem in modern astronomy.
Stability analysis and Solutional behaviour raises a dialectic deliberation, polemical conversation, argumentative confabulation and conjugation confatalia whether it is conceivable that the dark matter (or at least part of it) could be antimatter, but there are very strong experimental reasons to doubt this. For example, if the dark matter out there were antimatter, we would expect it to annihilate with matter whenever it meets up with it, releasing bursts of energy primarily in the form of light. We see no evidence in careful observations for that, which leads most scientists to believe that whatever the dark matter is, it is not antimatter.
In the eventuality of the fact such a predicational territoriality, character constitution, ontological consonance and primordial exactitude arises, we can think of the antimatter itself as a time independent system of the accentuation corroboratory, augmentation and momentary and fortification Dark matter system and the model could be applied with the progression leading to a very clobbered cuff, flailed jolt, knock, pounding pummel, push, rap of the dark matter systems dissipating the antimatter system. This may also provide an elucidation, expatiation and explication of the fact that there exists more matter in the universe than antimatter. This is of paramount importance and solves the most important puzzle as to what the antimatter is all about and what dark matter is made of.
Towards the end of classificational consummation, consolidation, corporation and concatenation we take the characteristics of the systems, the predicational interiorities, ontological consonance and primordial exactitude, accolytish representations, functional topology, apocryphal aneurism and atrophied asseveration event at
contracted points, and other parameters as the bastion and stylobate of the stratification purposes. Such totalistic entities would have easy paradigm of relational content, differentiated system of expressly oriented actions with primary focus and locus of homologues receptiveness and differentially instrumental activity, variable universalism and particularism, imperative compatibilities and structural variabilities, interactional dynamical orientation, institutionalization and internalization of pattern variables (Parsons) common attitudinal orientation of constituionalization of internalized dispositions, and a qualitative gradient of structural differentiation and ascribed particularistic solidarity abstraction or interactional dynamics, internal differentiation, structural morphology, comparative variability, normative aspect of expectational prediction, projection and prognostication. There are different superfield formalism and Curci-Ferrari type restrictions for different investigating systems. Equational realization, consummation and concatenation and consubstantiation are of primal and cardinal and seminal importance Accolytish representation and other parametricization could also be taken in to consideration. There is no sacrosanct rule for this. It is to be remembered that there are many investigatable systems in the world and the equations these theories specify is applicable to them. Another example is about Off shell nil potency; Three Cf type conditions; 3-form Abelian theory; One Cf condition; 1form non abelian Theory $\mathrm{B}+\mathrm{B} 9 \mathrm{bar})=\mathrm{I}(\mathrm{CX} \mathrm{C9bar})$; absolute anticommutivity are other properties that is found in many systems. Systemic characteristics thus play a primordial role in the development of the theory be it theoretical or empirical. So their characteristics could form the sentinel for the consubstantiation of the disintegrational purposes which is orderly in case of constants we talk about total invariants like the total Schrödinger function, albeit we have reservations about Everett's syndrome, like for example Total gravity in the universe. However it is to be stated in unmistakable terms that Universal function is not acceptable to the authors, while instead one could talk of the various investigating systems with different conditionalities notwithstanding the fact that say a Non Linear Schrödinger Equation holds good and the equality holds. The same is true in the Newtonian case of Total gravity extant in the world. Universal wave function calls for the conditionalities and functionalities of the investigating agencies and investigating systems so that those could also be taken in to consideration in the stratification scheme. Neutrinos or the protons are the same, but the source and the time factor and the space factor are also to be taken in to attribution and ascription and assignment. Two examples that could be cited are: Personality type refers to the psychological classification of different types of individuals. Personality types are sometimes distinguished from personality traits, with the latter embodying a smaller grouping of behavioral tendencies. Types are sometimes said to involve qualitative differences between people, whereas traits might be construed as quantitative differences According to type theories, for example, introverts and extraverts are two fundamentally different categories of people. According to trait theories, introversion and extraversion are part of a continuous dimension, with many people in the middle. Myers-Briggs Type Indicator (MBTI) assessment is a psychometric questionnaire designed to measure psychological preferences in how people perceive the world and make decisions. These preferences were extrapolated from the typological theories proposed by Carl Gustav Jung and first published in his 1921 book Psychological Types (English edition, 1923). Jung theorized that there are four principal psychological functions by which we experience the world: sensation, intuition, feeling, and thinking. One of these four functions is dominant most of the time. Equational satisfaction and consummation is of paramount and cardinal importance. We have studied discrete Schrodinger equations, NLSE, and Einstein Field equations on the same basis which must provide frame work for further analysis In the case of Super symmetric Yang Mills Theory integrable systems could be taken in to consideration) The Coulomb branch of $\mathrm{N}=2$ supersymmetric gauge theories in four dimensions is described in general by an integrable Hamiltonian system in the holomorphic sense. A natural construction of such systems comes from two-dimensional gauge theory and spectral curves. Ground state at the critical value of the trapping potential two entanglement measures is another example. Notwithstanding the constant ground states the characteristics of the investigating systems form the bastion and stylobate of the situation. Starting from this point of view, we propose an integrable system relevant to the $\mathrm{N}=2 \mathrm{SU}(\mathrm{n})$ gauge theory with a hypermultiplet in the adjoint representation, and offer much evidence that it is correct. The model has an S-duality group (with the central element -1 of acting as charge conjugation); permutes the Higgs, confining, and oblique confining phases in the expected fashion. Hegel also argues strongly against the epistemological emphasis of modern philosophy from Descartes through Kant, which he describes as having to first establish the nature and criteria of knowledge prior to actually knowing anything, because this would imply an infinite regress, a foundationalism that Hegel maintains is self-contradictory and impossible. Rather, he maintains, we must examine actual knowing as it occurs in real knowledge processes. This is why Hegel uses the term "phenomenology". "Phenomenology" comes from the Greek word for "to appear", and the phenomenology of mind is thus the study of how consciousness or mind appears to itself. In Hegel's dynamic system, it is the study of the successive appearances of the mind to itself, because on examination each one dissolves into a later, more comprehensive and integrated form or structure of mind. We also study more exotic phases. Supersymmetric Yang-Mills theory and integrable systems Ron Donagia, 1, Edward Wittenb, 2 Kind attention is also drawn to the Boltzmann arrow
of time and Everett's many worlds different past and future. [Whitehead's philosophy] is provisionally the last great Anglo- American philosophy, just before the disciples of Wittgenstein spread their mists, their sufficiency and their terror. An event is not only 'a man is crushed': the great pyramid is an event, and its duration for an hour, 30 minutes, 5 minutes ..., a passage of Nature, a view of God. What are the conditions for an event so that all is event? The event produces itself in a chaos, in a chaotic multiplicity, under the condition that a sort of sieve intervenes. A global methodology is assumed here. There is Total energy and Total gravity. Contextually reflexivity and context justification is most alluded coefficient here. As Geroch puts it: Theories consist of enormous number of ideas, arguments, hunches, vague feelings, all arranged in a configuration equivocation. It is the entire body of the material that is the "Theory'. (Written from memory: See Geroch 1978). Dreyfus and Dreyfus regard ceteris paribus condition as the universal restriction on rule systems. Classificational rules constitute prevent the regression of prevarication of such axiomatic predications and postulation alcovishness, and is a paradigmatic statement in the salient feature which does not disregard the cause effect definition and other scientific heuristic explanations. Such congressional enterprise is necessary for the totalistic view of the problem. Part of jurisprudence could be considered part of the law itself. Constitutive rules could be disregarded when the priority of the used rules are properly understood. Paradigms guide research even in the conspicuous absence of rules. Characterization is at the heart of naturalization. Stratification methodologies are much more vintage and montage than any other fait accompli mutatis mutandis desideratum. Manifest world in its entirety is a holographic projection of information embodied in its boundary. Here we are talking of the entire manifest world. But the information obtained is only for a piece of the world for which we have access. Nature's general Ledger is to be down loaded from Neuron DNA. Another factor that is taken in to consideration is Lancan paradox and sense, expression and event: proposition and the attribute of the state of affairs, individualistic denotation, institutionalized generalization, personalized manifestation, organizational individuation, and corporate signification of the systems in general. According to Schrodinger actualization means to extend over a series of ordinary points, to be selected according to the rule of convergence, to be incarnated in a body, to become a state of body, and to be renewed locally namely particle coming back to its original position for the sake of limited new actualizations and extensions. It is in this sense that actualization is collective and individual, internal and external. Geometrical interpretation of the theory of differential equations clearly places in evidence two absolutely distinct realities: (a) there is a field of directions and (b) topological accidents which may suddenly crop up in it, as for example the existence of the plane of "singular points" to which no direction has been attached and there are integral curves with the form they take on in the vicinity of singularities of the field of directions...... The existence and distribution of singularities are notions relative to the field of vectors defined by the differential equation. The form of the integral curves is relative to the solution of this equation. The forms are assuredly complementary, since the nature of the field is defined by the form of integral curves in its vicinity. But it is no less true that the field of vectors on one hand and integral curves on the other are two essentially distinct mathematical realities. In this connection of classificational process of the universal theory, it is necessary to recall what Kant had proved. Kant proves that sum of all possibilities excludes all but originary predicates and in this way constitute the completely determined concept of an individual being or objectification being. For only in this case, is a concept is equivalent to a thing. A thing completely determined in and through itself and known as the representation of an individual or a system under consideration. Thus the Universal Theory is but the form of communication in thought between the cosmic consciousnesses, namely the nature's general ledger, and the finite individualities, namely the histories of individual debits' and credits. It must therefore be entangled with the play of internationalities and pure retentions. Thus the universal theory has a totality. For example total gravity. Individual systems have characteristics for which say a Non Linear Schrodinger's equation holds, and such a consummation and consolidation of the equation is built up on the corporation and actualization of the equations in simplistic and individual cases. Compose is to make up; the parts that compose the whole. The notion of compossibility is thus defined as a continuum of the individual systems that are actualized in accord with the reductionist view which is held dearly in all subjects in this measurement world. In the Saussurean system, potential returns in language as the nonlocalizable excess of signifier over signified that accompanies the local realization of a conventional signifier-signified coupling. This excess is ensconced in the "vertical" dimension of the process (understood very differently than in the present context: as a "synchrony" rather than a temporal disparity, the disparity that is the empty form of time). It constitutes the immanent generative surplus from which the "horizontal" relay to the next linguistic realization is drawn ("diachrony": also different from the "horizontal" lines of encounter at issue here, in that diachrony is not essentially differentiating; the system remains the same across its realizations). An analogous surplus figures in Lévi-Strauss's anthropology as "mana" and its structural equivalents, which constitute the specifically cultural presentation of the staying power of processual remainder (the reserve of potential) in many societies. It is in excess-as-remainder that a reconciling of Deleuze and Guattari's thought and structuralisms of signification might be found ("mana" converts into Deleuze's "dark precursor" or "object $=x$ "; 1979, 315-324; 1990, 113-115;

1994, 119-123). The deleuzo-guattarian conversion of structuralism entails the signifier and signified generating an excess by escaping down a "line of flight" away from the "despotism" (self-sameness across its variations) of the signifying regime--rather than the excess regenerating signifier-signified following the chain of conventional linguistic realizations. This amounts to an autonomization of signified-signifier coupling as a pure, "postsignifying" form in which the matter of content melds with the manner of expression. It is the melding that takes the lead, as an "abstract machine" of autonomized, depersonalized expression (Deleuze/Guattari 1986, 3-8; Deleuze/Guattari 1987, 129-135, 189-191; Haghighi. The triad thesis, antithesis, synthesis is often used to describe the thought of German philosopher Georg Wilhelm Friedrich Hegel. Hegel never used the term himself, and almost all of his biographers have been eager to discredit it. The triad is usually described in the following way: The thesis is an intellectual proposition. The antithesis is simply the negation of the thesis, a reaction to the proposition. The synthesis solves the conflict between the thesis and antithesis by reconciling their common truths and forming a new thesis, starting the process over. According to Walter Kaufmann, although the triad is often thought to form part of an analysis of historical and philosophical progress called the Hegelian dialectic, the assumption is erroneous. Hegel used this classification only once, and he attributed the terminology to Immanuel Kant. The terminology was largely developed earlier by the neo-Kantian Johann Gottlieb Fichte, also an advocate of the philosophy identified as German idealism. The triad thesis, antithesis, synthesis is often used to describe the thought of German philosopher Georg Wilhelm Friedrich Hegel. Hegel stresses the paradoxical nature of consciousness; he knows that the mind wants to know the whole truth, but that it cannot think without drawing a distinction. Unfortunately, every distinction has two terms, every argument has a counter-argument, and consciousness can only focus on one of these at a time. So it fixes first on the one, then under pressure fixes second on the other, until it finally comes to rest on the distinction itself. Hegel refers to this process of alternation and rest as dialectic. In other words, the dialectical method involves the notion that the form of historical movement, process or progress, is the result of conflicting opposites. Thus this area of Hegel's thought has been broken down in terms of the categories of thesis, antithesis, and synthesis. Hegel's philosophy of history embraces the concept that a conflict of opposites is a struggle between actual and potential worlds. Kant's first Critique concerns itself with determining the structure of the objects of experience. His transcendental logic allows an empirical manifold, or multiplicity, to be grasped as a unified object, but only insofar as its unity is provided by the subject (via apperception). The transcendental ego synthesizes manifolds that remain distinct in kind from it, and thus its logic can only provide the a priori conditions for possible experiences, not the generative conditions for actual ones. "Kant's main preoccupation is therefore with the validity of propositions given in advance of our enquiry", for it merely seeks the conditions for subjective knowledge of an object, which are presumed to be identical with the conditions of objects themselves. Limited to schematic overviews, brief asides or even dismissive caricatures these philosophies muster enough strength stride by stride with present day theories( Henry Somers-Hall, Hegel, Deleuze, and the Critique of Representation: Dialectics of Negation and Difference, State University of New York Press, 2012, 289pp., (hbk), ISBN 9781438440095 . Reviewed by Jim Vernon, York University) Hegel shows how the various categories of logic sublate each other, turning contradiction into the motor that drives, rather than the problematic limit that haunts, representational thinking. The extended physical and biological theory is not just a multidimensional consciousness theory, but it is, after and above all, a philosophical theory. But their connection is not hierarchical. The self-created structural and structure less system of the multi-theoretical components is necessarily (in reality and symbolically also, a multicentred, in- and out- infinitely expanded, multi-layered spherical) logical and logical spacetime theory. But to fully unfold this concept, neither physics, nor any other partial theory is capable in itself. So, the different unified theories together are cannot be other than the wholeness theory, the unified top theory or the philosophical metatheory, but is this not just to give a name, to explain something, would this be the Creation/Non-creation itself? On Quantum's Universality: Posted on 5/19/2004 by Dave Bacon (The Quantum Pontiff): Often when I am thinking about the foundations of quantum theory, I am struck by the universality of the theory. Quantum theory (or its related cousin, quantum field theory) applies generically to all physical systems (disregarding the transition to some "classical" theory and of course, difficulties with both QCD and gravity.) Thus we apply quantum theory to our basic theories of physics, electromagnetism, the weak force, the strong force, but we also apply quantum theory to simple atoms and complex molecules, to single electrons and electron gases in metals, etc. Quantum theory is the universal language we use to describe any physical process. If we are thinking about ways to explain quantum theory, then this universality is a bit mysterious: the explanation had better apply to all of these different physical systems and that seems like a lot of work! Of course, this reasoning is flawed: it seems the universality is an illusion. The reason we can describe a complex molecule by quantum theory is that the fundamental constituents of that molecule obey quantum theory. Separation of different energy scales (and other scales, like localibility) allow us to ignore some of the constituents details, and the complex system behaves like a quantum system. So really any explanation of quantum theory need only apply to some basic level of physics (where this level is I refuse to speculate.) While quantum theory appears mysteriously universal, this is an
illusion for those pursuing understanding the mystery of the quantum. Whitehead was a mathematician as well as philosopher. Metaphysics was his main interest. He said it is the task of philosophy "to frame a coherent, logical, necessary system of general ideas in terms of which every element of our experience can be interpreted. Parson's theory of social action is based on his concept of the society. Parsons is known in the field of sociology mostly for his theory of social action. Action is a process in the actor-situation system which has motivational significance to the individual actor or in the case of collectively, its component individuals.
On the basis of this definition it may be said that the processes of action are related to and influenced by the attainment of the gratification or the avoidance of deprivations of the correlative actor, whatever they concretely be in the light of the relative personal structures that there may be. All social actions proceed from mechanism which is their ultimate source. It does not mean that these actions are solely connected with organism. They are also connected with actor's relations with other persons' social situations and culture.

### 1.1 Systems of social action (Observers in natural sciences: an analogy)

Social actions are guided by the following three systems which may also be called as three aspects of the systems of social action Personality system: This aspect of the system of social action is responsible for the needs for fulfillment of which the man makes effort and performs certain actions. But once man makes efforts he has to meet certain conditions. These situations have definite meaning and they are distinguished by various symbols and symptoms. Various elements of the situation come to have several meanings for ego as signs or symbols which become relevant to the organization of his expectation system.
Cultural system: Once the process of the social action develops the symbols and the signs acquire general meaning. They also develop as a result of systematized system and ultimately when different actors under a particular cultural system perform various social interactions, special situation develops.
Social System: A social system consists in a plurity of individual actor's interacting with each other in a situation which has at least a physical or environmental aspect actors are motivated in terms of tendency to the optimization of gratification and whose relations to the situation including each other is defined and motivated in terms of system of culturally structured and shaped symbols.
In Parson's view each of the three main type of social action systems-culture, personality and social systems has a distinctive coordinative role in the action process and therefore has some degree of causal autonomy. Thus personalities organize the total set of learned needs, demands and action choices of individual actors, no two of whom are alike.
Every social system is confronted with 4 functional problems. These problems are those of pattern maintenance, integration, goal attainment and adaptation. Pattern maintenance refers to the need to maintain and reinforce the basic values of the social system and to resolve tensions that emerge from continuous commitment to these values. Integration refers to the allocation of rights and obligations, rewards and facilities to ensure the harmony of relations between members of the social system. Goal attainment involves the necessity of mobilizing actors and resources in organized ways for the attainment of specific goals. Adaptation refers to the need for the production or acquisition of generalized facilities or resources that can be employed in the attainment of various specific goals. Social systems tend to differentiate these problems so as to increase the functional capabilities of the system. Such differentiation whether through the temporal specialization of a structurally undifferentiated unit or through the emergence of two or more structurally distinct units from one undifferentiated unit is held to constitute a major verification of the fourfold functionalist schema. It also provides the framework within which are examined the plural interchanges that occur between structurally differentiated units to provide them with the inputs they require in the performance of their functions and to enable them to dispose of the outputs they produce.

### 1.2 Pattern Variables

Affectivity vs affectivity neutrality: The pattern is affective when an organized action system emphasizes gratification that is when an actor tries to avoid pain and to maximize pleasure; the pattern is affectively neutral when it imposes discipline and renouncement or deferment of some gratifications in favour of other interests. Self-orientation vs collectivity orientation: This dichotomy depends on social norms or shared expectations which define as legitimate the pursuit of the actor's private interests or obligate him to act in the interests of the group. Particularism vs universalism: The former refers to standards determined by an actor's particular relations with particular relations with a particular object; the latter refers to value standards that are highly generalized. Quality vs performance: The choice between modalities of the social object. This is the dilemma of according primary treatment to an object on the basis of what it is in itself an inborn quality or what it does and quality of its performance. The former involves defining people on the basis of certain attributes such as age, sex, color, nationality etc; the latter defines people on the basis of their abilities. Diffusion vs specificity: This is the dilemma of defining the relations borne by object to actor (observer) as indefinitely wide in scope, infinitely broad in involvement morally obligating and significant in pluralistic situations or specifically limited in scope and involvement.

Continental philosophy includes the following movements: German idealism, phenomenology, existentialism (and its antecedents, such as the thought of Kierkegaard and Nietzsche), hermeneutics, structuralism, poststructuralism, French feminism, psychoanalytic theory, and the critical theory of the Frankfurt School and related branches of Western Marxism. It is difficult to identify non-trivial claims that would be common to all the preceding philosophical movements. The term "continental philosophy", like "analytic philosophy", lacks clear definition and may mark merely a family resemblance across disparate philosophical views. Simon Glendinning has suggested that the term was originally more pejorative than descriptive, functioning as a label for types of western philosophy rejected or disliked by analytic philosophers Babette Babich emphasizes the political basis of the distinction, still an issue when it comes to appointments and book contracts. Nonetheless, Michael E. Rosen has ventured to identify common themes that typically characterize continental philosophy. First, continental philosophers generally reject scientism, the view that the natural sciences are the only or most accurate way of understanding phenomena. This contrasts with analytic philosophers, many of whom have considered their inquiries as continuous with, or subordinate to, those of the natural sciences. Continental philosophers often argue that science depends upon a "pre-theoretical substrate of experience" (a version of the Kantian conditions of possible experience or the phenomenological concept of the "lifeworld") and that scientific methods are inadequate to fully understand such conditions of intelligibility. Second, continental philosophy usually considers these conditions of possible experience as variable: determined at least partly by factors such as context, space and time, language, culture, or history. Thus continental philosophy tends toward historicism. Where analytic philosophy tends to treat philosophy in terms of discrete problems, capable of being analyzed apart from their historical origins (much as scientists consider the history of science inessential to scientific inquiry), continental philosophy typically suggests that "philosophical argument cannot be divorced from the textual and contextual conditions of its historical emergence". Third, continental philosophy typically holds that conscious human agency can change these conditions of possible experience: "if human experience is a contingent creation, then it can be recreated in other ways". Thus continental philosophers tend to take a strong interest in the unity of theory and practice, and tend to see their philosophical inquiries as closely related to personal, moral, or political transformation. This tendency is very clear in the Marxist tradition ("philosophers have only interpreted the world, in various ways; the point, however, is to change it"), but is also central in existentialism and post-structuralism. A final characteristic trait of continental philosophy is an emphasis on metaphilosophy. In the wake of the development and success of the natural sciences, continental philosophers have often sought to redefine the method and nature of philosophy. In some cases (such as German idealism or phenomenology), this manifests as a renovation of the traditional view that philosophy is the first, foundational, a priori science. In other cases (such as hermeneutics, critical theory, or structuralism), it is held that philosophy investigates a domain that is irreducibly cultural or practical. And some continental philosophers (such as Kierkegaard, Nietzsche, the later Heidegger, or Derrida) doubt whether any conception of philosophy can coherently achieve its stated goals.(Source: Wikipedia and Stanford encyclopedia)
The triad is often said to have been extended and adopted by Karl Marx and Friedrich Engels, however, Marx referred to them in The Poverty of Philosophy as speaking Greek and "Wooden trichotomies" .The classic empiricist presentation of this approach is William James's Essays in Radical Empiricism: "There is no general stuff of which appearance is made. It is made of that, or just what appears (26-27) ... what I call 'pure experience' [is] only virtually or potentially either object or subject as yet. For the time being, it is plain, unqualified actuality, a simple that (23) ... experience as a whole is self-containing and leans on nothing (193) ... object and subject fuse in the fact of 'presentation' or sense-perception (197) ... knower and object exist as so many ultimate thats or facts of being" (196). As the last phrase suggests, James's "that" (or "this-that": to signal a differential, or incipient difference) is Francis Bacon's "fact," which can in turn be understood in terms of Whitehead's definition of fact as the "undifferentiated terminus of sense-awareness," the inexhaustible unthought from which thought "diversifies" and to which it "demonstratively" returns, as to its "ideal limit" (6-10, 13-15. On the "univocity" of the coming to expression of the multiple, see Deleuze 1990, 177-180; 1994, 35-42, 303-304. Can the nature of thinking be uncovered by thinking alone? (Cf consciousness) "My dialectical method is, in its foundations, not only different from the Hegelian, but exactly opposite to it. For Hegel, the process of thinking, which he even transforms into an independent subject, under the name of 'the idea ', is the creator of the real world, and the real world is only the external appearance of the idea. With me, the reverse is true: the ideal is nothing but the material world reflected in the mind of man, and translated into forms of thought. "Karl Marx, Capital, vol. 1, Preface to the Second Edition. (P.102) (See Ideal / Real) For Aristotle, Thinking is the one specific activity of the Human Soul Which is Capable of Independent Existence and separate from any connection to the Body. A Strenuous counterargument has been made, precisely for body thinking. Deleuze and Guattari for, "Becoming Animal" and "Becoming intense" are Modes of resistance to abstract Thinking. Alain Badiou FOLLOWS Aristotle in using thinking to define specifically the Human, as Opposed to Interest. For Badiou, "the capacity which is specifically human is that of thought, and thought is nothing other than that by
which the path of a truth seizes and traverses the human animal." (Infinite Thought, p. 71) In HIS Essay "Does Consciousness Exist?" William James Pointed out That Consciousness is a Process, and not a substance. (Unlike Descartes, who claimed the existence of a res cogitans?) In The Principles of Psychology, James described five properties of what he called "thought." Every thought, he wrote, tends to be part of personal consciousness. We write this despite the definition that has been held for the consciousness as a storage room and mind anagrammatically acting upon it. Concomitant quantum channeling like synapses and neuron firing might take place in the brain. And that falls under the subterranean realm and ceratoid dualism of Neurology. Thought is always changing, is sensibly continuous, and appears to deal with objects independent of it. In addition, thought focuses on some objects to the exclusion of others. In other words, it involves attention. Alfred North Whitehead claimed that, with this Inquiry, James was to the Twentieth century What Descartes was to the Seventeenth. Louis Sullivan describes "Real Thinking," Thinking in the present tense, as Organic Thought. "It is in the present, only, that you really live, therefore it is in the present, only that you can really think. And in this sense you think organically. Pseudo-thinking is inorganic. The one is living, the other dead. The present is the organic moment, the living moment. "(Kindergarten Chats, "Thought.") Thinking is a form of Computation? Emergence Refers to the appearance of Patterns of Organization and is one of the Key concepts of Complexity and a -life. It is sometimes referred to as a situation where the whole is greater than the sum of the parts, because it cannot be analyzed by taking the parts apart and examining them separately. One reason for this is that in a complex phenomenon showing emergent properties, the parts become a determining context for each other, and these patterns of feedback contribute to the appearance of the emergent phenomenon. For Michael Polanyi, "Evolution can be understood only as a feat of emergence." For Goethe, the Whole Living was Also More than the Sum of ITS parts. "Das Lebendige ist zwar in Elemente zerlegt, aber man kann es aus diesen nicht wieder zusammenstellen und beleben." Goethe quoted in d'Arcy Thompson, On Growth and Form. (P.41) But for most contemporary scientists, Goethe's meaning of emergence was a mystical one. For Francis Crick, the scientific meaning of emergent assumes that while the whole cannot be the simple sum of the separate parts, its behavior can, at least in principle, be understood from the nature and behavior of its parts plus the knowledge of how all these parts interact. (The Astonishing Hypothesis, P.11) (Assuming IT's Possible to have That Laplacian Knowledge) Stuart Kauffman Suggests That many Properties of Organisms May be Probable emergent Collective Properties of Their constituents. (This is precisely Kant's definition of the organic - as the result of internal interactions instead of an assembly of preexisting parts. (See Mechanism / Vitalism) "The problem of origins requires an understanding of how new levels of order emerge from complex patterns of interactions and what the properties of these emergent structures are in terms of their robustness to perturbation and their capacities for self-maintenance "(Brian Goodwin, How the Leopard Changed its Spots, p. 181.) Luc Steels Offers Useful definitions of emergence in Artificial Life half. He distinguishes between first order emergence, defined as a property not explicitly programmed in, and second-order emergence, defined as an emergent behavior that adds additional functionality in the system. In general a-life researchers try to create second -order emergence, then the system for use CANS ITS own emergent Properties to create an upward Spiral of Continuing evolution and emergent behaviors. For a Critique of emergence, See Peter Cariani, "Emergence and adaptivity in Organisms and Devices," World Fudtures 32 (1991):111-32. C. Lloyd Morgan's Descriptions of emergence as a Qualitative Change in direction closely resemble the definitions of bifurcations. HIS In Emergent Evolution, of 1923, he writes, "The emergent step, although it may seem more or less saltatory, is best Regarded as a Qualitative Change of direction, or Critical turning-Point, in the Course of events. " Daniel Stern describes the Infant's sense of Self between Birth and two months as the "emergent Self." (See subject). It is a sense of the Coming-into-Being of Organization and Remains active for the rest of life. But IT is not an overarching schema About Integrating the Self, but rather an Experience of Process. (cf Molar / Molecular) In Gestalt Perception terms, emergence refers to our ability to perceive forms that cannot be reduced to the addition of the "atomic" parts of a pattern. Ego superimposing two squares diagonally displaced allows for readings of an emergent square at their overlap, two emergent L-shapes in the non-Intersecting area, in addition to the two Squares. (cf. Figure / Ground) A Fundamental property of Open Systems is that they stabilize any improbability which Serves to elicit them. Being / Becoming ---------------------- According to Ernst Cassirer, Plato's Philosophy recognizes two Contrary Forms of representation, one of Which is Valid for the Realm of Being and the Other for the Realm of Becoming. (Individual and Cosmos, p.125) For Cassirer, "Form Thinking" Belongs to Being, while "causal Thinking" Belongs to Becoming. But strict Knowledge is Only Possible of the Always-Being. Becoming that which is CAN only be described, if at All, in the language of myth. Or rather, myth is already familiar with both the question of the "what" and the question of the "whence." "It sees everything that it grasps (the world as well as the gods) under this double aspect."(The Problem of Form and the Problem of Cause, in The Logic of the Cultural Sciences, p. 87) Socrates first Discovered the Concept, or Eidos as the relation Between the Particular and the General and as a germ of a new meaning of the general question concerning being. This meaning emerged in its full purity when the Socratic eidos went on to unfold into the (transcendental) Platonic "Idea."
(See transcendence / immanence) For Plato, the soul is an intermediary between being and Becoming. The Aristotelian system seemed to Promise a Different reconciliation of the Opposition between Being and Becoming. Unlike Plato and the thinkers of pure form, Aristotle wanted to restore to Becoming ITS rightful Place, Because He was convinced That Only in this way Could Philosophy be Transformed from a Mere Theory of concepts into a Theory of Reality. Form and Matter, Being and Becoming, must become correlative. Peculiarly Aristotelian the Concept of the formal Cause originates from this fusion. (Cassirer) "In Nature We May Search for successfully something that endures, and in nature we may regard becoming as if any phase of it were the "reason" of a later phase and the "consequence" of an earlier one. We may even go so far as to say: Nature is the one mediate object that obeys the postulates of the rational theory of becoming. "Hans Driesch, History and Theory of Vitalism, p. 193. We are grateful to the Russian Blog that was available on Google search and Wikipedia in the consolidation and consummation of the above facts. Gilles Deluze is another person whose Pure Immanence and The Logic of sense has been helpful. Part of it expatiated and enucleated from blog Интернет версия данной статьи находится по адресу: http://www.situation.ru/app/j_art_1041.htm Copyright (c) Альманах "Восток"

One might compare Hegel's point here to that expressed by Kant in his well known claim that without concepts, those singular and immediate mental representations he calls "intuitions" are "blind." In more recent terminology one might talk of the "concept-" or "theory-ladenness" of all experience, and the lessons of this chapter have been likened to that of Wilfred Sellars's famous criticism of the "myth of the given" (Sellars 1997). Hegel has insisted on quarantining his defensible ideas from it (e.g., Wood 1990). However, rather than be understood as a treatise in formal (or "general") logic, it is perhaps best understood as a version of what Kant had called "transcendental logic," and in this sense thought of as a successor to Kant's "transcendental deduction of the categories" in the Critique of Pure Reason in which Kant attempted to "deduce" a list of those non-empirical concepts, the "categories," which he believed to be presupposed by all empirical judgments made by finite, discursive thinkers. However, whereas the latter's is largely etymologically oriented and given to exploiting semantic ambiguities, traces and aporias, Deleuze's strategy is more geared towards conceptual and functional differentiation, exploring the horizons of Ideas (in the Kantian sense) and bringing forth the machinic and operative features of the philosophies with which he engages. hile, for Lacan, Truth is this shattering experience of the Void - a sudden insight into the abyss of Being, "not a process so much as a brief traumatic encounter, or illuminating shock, in the midst of common reality" -, for Badiou, Truth is what comes afterward: the long arduous work of fidelity, of enforcing a new law onto the situation. 5 The choice is thus: "whether a vanishing apparition of the real as absent cause (for Lacan) or a forceful transformation of the real into a consistent truth. doctrine is precisely that, while never ceasing to be dialectical in pinpointing the absent cause and its divisive effects on the whole, it nevertheless remains tied to this whole itself and is thus unable to account for the latter's possible transformation. /.../ Surely anchored in the real as a lack of being, a truth procedure is that which gives being to this very lack. Pinpointing the absent cause or constitutive outside of a situation, in other words, remains a dialectical yet idealist tactic, unless this evanescent point of the real is forced, distorted, and extended, in order to give consistency to the real as a new generic truth. Bosteels describes the modality of the truth-procedure: Setting out from the void which prior to the event remains indiscernible in the language of established knowledge, a subjective intervention names the event which disappears no sooner than it appears; /it/ faithfully connects as many elements of the situation as possible to this name which is the only trace of the vanished event, and subsequently forces the extended situation from the bias of the new truth as if the latter were indeed already generally applicable. Bosteels basic reproach, according to which, psychoanalysis collapses into an instantaneous act what is in reality an ongoing and impure procedure, which from a singular event leads to a generic truth by way of a forced return upon the initial situation. Whereas for Zizek, the empty place of the real that is impossible to symbolize is somehow already the act of truth itself, for Badiou a truth comes about only by forcing the real and by displacing the empty place, so as to make the impossible possible. 'Every truth is post-evental,' Badiou writes. An example is Descartes' celebrated phrase at the beginning of the Discourse on the Method: Good sense is the most evenly shared thing in the world. . the capacity to judge correctly and to distinguish the true from the false, which is properly what one calls common sense or reason, is naturally equal in all men . . For Deleuze, is an image of thought? Although images of thought take the common form of an 'Everybody knows . . .' (DR 130), they are not essentially conscious. Rather, they operate on the level of the social and the unconscious, and function, "all the more effectively in silence." (DR 167). Relationship of philosophy to thought must have two correlative aspects, Deleuze argues: an attack on the traditional moral image of thought, but also a movement towards understanding thought as self-engendering, an act of creation, not just of what is thought, but of thought itself, within thought (DR 147). he thought which is born in thought, the act of thinking which is neither given by innateness nor presupposed by reminiscence but engendered in its genitality, is a thought without image. But what is such a thought, and how does it operate in the world? (DR 167; cf. 132) Durkheim's concepts of the collective representation and the process of universalization, then, correspond to Kantian concepts, and

Durkheim acknowledges the relevance of Kantian philosophy to his epistemological and moral considerations (1965: 494). It is to be noted and stated in unmistakable and unequivocal words that the singularities and the events constitute a life coexist with the accidents of life that corresponds to it, but they are neither grouped nor divided in the same way. They connect in a manner entirely different from how individuals connect by virtue of which classification takes place. A singular life might do without any individuality, without any other concomitant that individualizes it. Individual life or that of insentient life remains inseparable from empirical determinations. On the other hand, the indefinite as such is the mark of not an empirical indetermination but of a determination by immanence or a transcendental determinability. (Pure Immanence Gilles Deluze: Page number 30). It is to be realized that a phenomenon which we think out is engaged in process of actualization following the plane that gives it its particular reality. Plane of immanence therefore is actualization, as long as the events that populate them are localized by a law or other theorem tic corollary. Another vehement and trenchant example of classification is Hegelianism and teleology thereof. Hegelianism is a collective term for schools of thought following or referring to G. W. F. Hegel's philosophy which can be summed up by the dictum that "the rational alone is real", which means that all reality is capable of being expressed in rational categories. His goal was to reduce reality to a more synthetic unity within the system of transcendental idealism. Hegel's method in philosophy consists of the triadic development (Entwicklung) in each concept and each thing. Thus, he hopes, philosophy will not contradict experience, but will give data of experience to the philosophical, which is the ultimately true explanation. If, for instance, we wish to know what liberty is, we take that concept where we first find it - the unrestrained action of the savage, who does not feel the need of repressing any thought, feeling, or tendency to act. Next, we find that the savage has given up this freedom in exchange for its opposite, the restraint, or, as he considers it, the tyranny, of civilization and law. Finally, in the citizen under the rule of law, we find the third stage of development, namely liberty in a higher and a fuller sense than how the savage possessed it-the liberty to do, say, and think many things beyond the power of the savage. In this triadic process, the second stage is the direct opposite, the annihilation, or at least the sublation, of the first. The third stage is the first returned to itself in a higher, truer, richer, and fuller form. The three stages are, therefore, styled:
In itself (An-sich)
Out of itself (Anderssein)
In and for itself (An-und-für-sich).
These three stages are found succeeding one another throughout the whole realm of thought and being, from the most abstract logical process up to the most complicated concrete activity of organized mind in the succession of states or the production of systems of philosophy.
Deleuze uses the introduction to clarify the term "repetition." Deleuze's repetition can be understood by contrasting it to generality. Both words describe events that have some underlying connections. Generality refers to events that are connected through cycles, equalities, and laws. Most phenomena that can be directly described by science are generalities. Seemingly isolated events will occur in the same way over and over again because they are governed by the same laws. Water will flow downhill and sunlight will create warmth because of principles that apply broadly. In the human realm, behavior that accords with norms and laws counts as generality for similar reasons. Science deals mostly with generalities because it seeks to predict reality using reduction and equivalence. Repetition, for Deleuze, can only describe a unique series of things or events. The Borges story in which Pierre Menard reproduces the exact text of Don Quixote is a quintessential repetition: the repetition of Cervantes in Menard takes on a magical quality by virtue of its translation into a different time and place. Art is often a source of repetition because no artistic use of an element is ever truly equivalent to other uses. (Pop Art pushes this quality to a certain limit by bringing production near the level of capitalism.) For humans, repetition is inherently Transgressive. As in Coldness and Cruelty, Deleuze identifies humor and irony as lines of escape from the generalities of society. Humor and irony are in league with repetition because they create distance from laws and norms even while re-enacting them. Deleuze describes repetition as a shared value of an otherwise rather disparate trio: Kierkegaard, Nietzsche, and Péguy. He also connects the idea to Freud's death drive. He goes on to define repetition as "difference without a concept". Repetition is thus reliant on difference more deeply than it is opposed. Further, profound repetition will be characterized by profound difference.

### 1.3 Difference in Itself

Deleuze paints a picture of philosophical history in which difference has long been subordinated to four pillars of reason: identity, opposition, analogy, and resemblance. He argues that difference has been treated as a secondary characteristic which emerges when one compares pre-existing things; these things can then be said to have differences. This network of direct relations between identities roughly overlays a much more subtle and involuted network of real differences: gradients, intensities, overlaps, and so forth .The chapter contains a discussion of how various philosophers have treated the emergence of difference within Being. This section uses Duns Scotus, Spinoza, and others to make the case that "there has only ever been one ontological proposition:

Being is univocal. ... A single voice raises the clamor of being". One then tries to understand the nature of differences that arise within Being. Deleuze describes how Hegel took contradiction-pure opposition-to be the principle underlying all difference and consequently to be the explanatory principle of the entire world's texture. He accuses this conception of having a theological and metaphysical slant.
Deleuze's geophilosophy is a "surface topology". (109) Hence, we can use topology to construct and deconstruct the structure of the event. If we take one singularity, one knot, one red dot in the Pascal diagram, and spread it out over a "line of ordinary points," we get the labyrinth, the pulsed string, vibrating like a wave at a frequency in tune with its number. The singularity takes this shape of extension over an "ordinary" line in the actualization of the event. (110) "A world already envelops an infinite system of singularities selected through convergence." (109) this idea of convergence is important to Deleuze. Elsewhere, he writes on hylomorphism. The preindividual transcendental field of singularities is self-organizing. This is how a shape or structure takes its shape, its form, "to be incarnated in a body; to become the state of the body." (110) Deleuze says, "An individual is always in a world as a circle of convergence." To be a circle implies that the circle is the result of an event, a convergence that results not in a knot, or some other kind of shape, but in a circle. I visualize two series coming together, two Pascal triangles, the tips of which are interlocking in some kind of dragon-chasing-its-tail kind of shape, a yin-yang whose sum total is something like a circle, which also represents the GCD of the two series. The two Pascal triangles intersect and produce a new gyre, and because it has been lifted up into another dimension, we see the cross-section -- the circle. The circle is the stable shape of this event, and as such associated with the individual. Hegel also diagrammed the world as a series of interlocking concentric circles. Different theory, similar diagram. If you can imagine the Pascal triangle as a 3-D gyre, when the event occurs, the potential energy in the system "falls to its lowest level" -- gets pulled to the tip of the triangle (like a tornado). This idea of energy falling to its lowest level is similar to how we referenced the pachinko game earlier. Deleuze wrote extensively on Leibniz, quoting him here that "each individual monad expresses the world." Each monad would be like a singularity, and in discovering all the frequencies of that singularity (e.g. all the factors of a huge number), we gain a perspective on every other singularity. This is very similar to Borges' aleph, a point in space that reflects all the other points by which one can see everything in the universe. Page 112: Deleuze distinguished between zones of clarity and obscurity in the singularity. In other works, this implies "consistency" and "inconsistency". Here, we can think in terms of sense and nonsense. Sense is the ability for the snowflake, crystalline form to incarnate an event. The nonsense is all the other unformed points (non-red dots). Page 114: "Incompossible" worlds (e.g. a world in which Adam is a sinner and a world in which Adam is not a sinner; not a contradiction but a mutual exclusivity) imply that there must be an "ambiguous sign" or aleatory point constructing the difference between the two worlds. This aleatory point, or shifter, is the key, or machine by which the different actualizations are realized. In the case of Adam, the shifter would be something like, "to sin." Worlds are "overthrown from within by paradox", by this aleatory point or ambiguous sign, this moment of becoming and revolution. This is an exemplary case of what Deleuze deploys in the crucial pages of his Difference and Repetition: while it may seem that the two presents are successive, at a variable distance apart in the series of reals, in fact they form, rather, two real series which coexist in relation to a virtual object of another kind, one which constantly circulates and is displaced in them /.../. Repetition is constituted not from one present to another, but between the two coexistent series that these presents form in function of the virtual object (object $=x$ ). (DR-104-105) Neither the problem nor the question is a subjective determination marking a moment of insufficiency in knowledge. Problematic structure is part of objects themselves, allowing them to be grasped as signs (DR-63-4)
Hegelian counter-argument would have been: is then the "pure" virtual difference not the very name for actual self-identity? Is it not CONSTITUTIVE of actual identity? More precisely, in the terms of Deleuze's transcendental empiricism, pure difference is the virtual support/condition of actual identity: an entity is perceived as "(self-) identical" when (and only when) its virtual support is reduced to a pure difference. In Lacanese, pure difference concerns the supplement of the virtual object (Lacan's objet a); its most plastic experience is that of a sudden change in (our perception of) an object which, with regard to its positive qualities, remains the same: "although nothing changes, the thing all of a sudden seemed totally different" - as Deleuze would have put it, it is the thing's intensity which changes. Lacan himself is here not beyond reproach, since he gets sometimes seduced by the rhizomatic wealth of language beyond (or, rather, beneath) the formal structure that sustains it. It is in this sense that, in the last decade of his teaching, he deployed the notion of lalangue (sometimes simply translated as "language") which stands for language as the space of illicit pleasures that defy any normativity: the chaotic multitude of homonymies, word-plays, "irregular" metaphoric links and resonances... Productive as this notion is, one should be aware of its limitations. Many commentators have noted that Lacan's last great literary reading, that of Joyce to whom his late seminar (XXIII: Le sinthome is dedicated, is not at the level of his previous great readings (Hamlet, Antigone, and Claudel's Coufontaine-trilogy). T (For Lacan, the theoretical problem/task is here to distinguish between the Master-Signifier and objet at which both
refer to the abyssal X in the object beyond its positive properties.) As such, pure difference is closer to antagonism than to the difference between two positive social groups one of which is to be annihilated. The universalism that sustains an antagonistic struggle is not exclusive of anyone, which is why the highest triumph of the antagonistic struggle is not the destruction of the enemy, but the explosion of the "universal brotherhood" in which agents of the opposite camp change sides and join us (recall the proverbial scenes of police or military units joining the demonstrators). It is in such explosion of enthusiastic all-encompassing brotherhood from which no one is in principle excluded, that the difference between "us" and "enemy" as positive agents is reduced to a PURE formal difference. I never pretended that one can insert reality into the past and thus work backwards in time. However, one can without any doubt inserts there the possible, or, rather, at every moment, the possible insert itself there. Insofar as unpredictable and new reality creates itself, its image reflects itself behind itself in the indefinite past: this new reality finds itself all the time having been possible; but it is only at the precise moment of its actual emergence that it begins to always have been, and this is why I say that its possibility, which does not precede its reality, will have preceded it once this reality emerges.
Subjectification (French: subjectivation) is a philosophical concept coined by Michel Foucault and elaborated by Gilles Deleuze and Félix Guattari. It refers to the construction of the individual subject. The concept has been often used in critical theory, sometimes with Louis Althusser's concept of interpellation. In Gilbert Simondon's theory of individuation, subjectification precedes the subject in the same way as the process of individuation precedes the creation of the individual. While the classical notion of a subject considers it as a term, Foucault considered the process of subjectification to have an ontological pre-eminence on the subject as a term.
For Deleuze, the presentation of absolute difference is 'an immediate and adequate expression of an absolute Being that comprises in it all beings.' To cite a phrase Deleuze uses elsewhere, it involves a 'static genesis' of the structure of the absolute. Hegel's Science of Logic, on the other hand, performs a 'dynamic genesis' of 'the logicity of being' in such a way that 'it says its own sense' (accounts for itself through the concepts it has generated) through the very movement of thought presented step-by-step in the book itself. The Logic therefore enacts the complete and immanent interpenetration of the logic of being with the logic of thought. For instance, the movement from being to nothingness and then to becoming at the start of the Logic is simultaneously a movement of thought in which the bare thought of being reveals itself to be nothing determinate. Moreover, it is also through this approach that Hegel completes his response to the Kantian critique of the ontological argument: by arguing that the notion of bare 'existence' or 'being' cannot be conceived without introducing some determinacy into it: to be is to be something. Now Hegel's articulation of the logicity of being is of course only made possible by the claim that difference must be fundamentally understood as negation. We know that Deleuze disagrees with this, but is the necessary consequence of this disagreement that he also has to give up on a determinate and genetic account of the development of thought? If so, then he will have concomitant problems defending his account of immanence against Hegel's. Hegel manages to generate a lot of determinate possibilities out of the structure of negation: it is hard to see what determinate possibilities can be strictly generated from 'difference in itself'. In the Spinozist account, there is no direct movement from the real distinction of the attributes to the position that thought and extensions are two of these attributes. The Vertigo of Philosophy: Deleuze and the Problem of Immanence Christian Kerslake
Deleuze proposes (citing Leibniz) that difference is better understood through the use of dx, the differential. A derivative, dy/dx, determines the structure of a curve while nonetheless existing just outside the curve itself; that is, by describing a virtual tangent. Deleuze argues that difference should fundamentally be the object of affirmation and not negation. As per Nietzsche, negation becomes secondary and epiphenomenal in relation to this primary force. Repetition for Itself: The chapter describes three different levels of time within which repetition occurs. Deleuze takes as axiomatic the notion that there is no time but the present, which contains past and future. These layers describe different ways in which past and future can be inscribed in a present. As this inscription grows more complicated, the status of the present itself becomes more abstract. Basic processes of the universe have a momentum that they carry into each present moment. A 'contraction' of reality refers to the collection of a diffuse ongoing force into the present. Prior thought and behavior, all substance performs contraction. "We are made of contracted water, earth, light, and air...Every organism, in its receptive and perceptual elements, but also in its viscera, is a sum of contractions, of retentions and expectations. Passive synthesis is exemplified by habit. Habit incarnates the past (and gestures to the future) in the present by transforming the weight of experience into an urgency. Habit creates a multitude of "larval selves," each of which functions like a small ego with desires and satisfactions. In Freudian discourse, this is the domain of bound excitations associated with the pleasure principle. Deleuze cites Hume and Bergson as relevant to his understanding of the passive synthesis. Active synthesis: The second level of time is organized by the active force of memory, which introduces discontinuity into the passage of time by sustaining relationships between more distant events. A discussion of destiny makes clear how memory transforms time and enacts a more profound form of repetition: Destiny never consists in step-by-step deterministic relations between presents
which succeed one another according to the order of a represented time. Rather, it implies between successive presents non-localizable connections, actions at a distance, systems of replay, resonance and echoes, objective chances, signs, signals, and roles which transcend spatial locations and temporal successions. Relative to the passive synthesis of habit, memory is virtual and vertical. It deals with events in their depth and structure rather than in their contiguity in time. Where passive syntheses created a field of 'me's,' active synthesis is performed by 'I.' In the Freudian register, this synthesis describes the displaced energy of Eros, which becomes a searching and problematizing force rather than a simple stimulus to gratification.

### 1.4 Empty time

The third layer of time still exists in the present, but it does so in a way that breaks free from the simple repetition of time. This level refers to an ultimate event so powerful that it becomes omnipresent. It is a great symbolic event, like the murder to be committed by Oedipus or Hamlet. Upon rising to this level, an actor effaces herself as such and joins the abstract realm of eternal return. The me and the I give way to "the man without name, without family, without qualities, without self or I...the already-Overman whose scattered members gravitate around the sublime image" Empty time is associated with Thanatos, a desexualized energy that runs through all matter and supersedes the particularity of an individual psychic system. Deleuze is careful to point out that there is no reason for Thanatos to produce a specifically destructive impulse or 'death instinct' in the subject; he conceives of Thanatos as simply indifferent.

### 1.5 Lars Marcussen on Deleuze's philosophy of space and singularities

When the nomad/State opposition is applied to space, the basic principle is that nomad space is 'smooth' and heterogeneous, while State space is 'striated' and homogeneous. Deleuze illustrates these concepts with an example from technology: woven fabric is striated, that is, with the threads of warp and woof; felt is smooth, as it consists of entangled fibres; it is no accident, Deleuze comments, that the Mongolian nomads excel in using felt for their tents, clothing and even armoury. In psychogenetic terms, the difference between metrics and projection is that the straight line is mastered in two different ways: as a 'base line' that structures metric space, and as a 'line of sight' that structures projective space. In the most elementary psychological sense, the straight line of metrics is the line that connects and denotes the distance between two points. When one notes the shortest distance by means of an actual movement, one acquires the idea of the straight line as something that denotes a fixed distance. Eventually, this experience is encoded as a general mental scheme that works automatically in all situations. When we move things around in our imagination so that their relative positions are changed in a regular manner, while their metric identities remain unchanged, the idea gradually emerges of a system of coordinates as a regular frame of reference for a metric space that can be expanded to include bigger and bigger entities. As a matter of fact, the very spaces inhabited by nomads - steppes and deserts - are smooth, and the same is true of the ice desert inhabited by Eskimos, and of the sea roamed by seafaring peoples. In these spaces orientations, landmarks and linkages are in continuous variation, Deleuze observes, and goes on: "there is no line separating earth and sky; there is no intermediate distance, no perspective or contour; visibility is limited; and yet there is an extraordinarily fine topology that relies not on points or objects, but rather on haecceities, on sets of relations (winds, undulations of snow or sand, the song of the sand, the creaking of the ice, the tactile qualities of both)." In contrast to this fluid state, the spaces inhabited by sedentary peoples - which are State spaces - are striated with walls, enclosures and roads that exhibit constancy of orientation and metric regularity. Deleuze designates this state of affairs as 'the actual', and he wants to show that although the actual is indeed a part of reality, it is also a kind of illusion that conceals or 'covers up' another realm of reality, which he calls 'the virtual'. In order to grasp the virtual, we should think of everything as 'individuals', each of which has its own history. The word 'individual' is used here in an extended sense. In biology, for instance, species and genera as well as organisms are defined as individuals. On another spatio-temporal scale, ecological environments in which species are embedded and evolve are individuals, and at the opposite end of the scale each molecule and atom is an individual. In every case individuals are meshed together in fuzzy aggregates without distinct borders, and are in an incessant state of 'becoming' in a sense that escapes our perception of actual processes and states of affairs (Lars Marcussen on Deleuze's philosophy of space and singularities)
To utilize and expand on the possibilities offered by differential calculus, Deleuze proposes an Idea in the Kantian sense insofar as it arises from and regulates its field immanently (Deleuze, Difference and Repetition, 177). "Already Leibniz had shown that calculus ... expressed problems which could not hitherto be solved or, indeed, even posed (transcendent problems)," problems such as the complete determination of a species of curve, or problems characterized by the paradox of Achilles and the tortoise (Deleuze, Difference and Repetition, 177). But what about determinations beyond a single curve? Is there a means to make "a complete determination with regard to the existence and distribution of ... [regular and singular] points which depends upon a completely different instance," an instance characterized in terms of a field of vectors (Devlin 44)? The goal here is to explicitly link differential equations and vector fields. A vector field is defined, by Deleuze, as the complete determination of a problem given in terms of the existence, number and distribution of points that are its
condition. This corresponds fairly well to the more or less standard mathematical definition where a vector field is defined as associating a vector to every point in the field space (Deleuze, Difference and Repetition, 177). Vector fields are used in physics to model observations, such as the movement of a fluid, which include a direction for each point of the observed space. This is particularly important for Deleuze who claims that nature is a vector field. This is what Deleuze calls a plane of immanence. Referring back to the above quote from What is Philosophy?, concepts are singular points on that vector field. They are called attractors. Deleuze and Guattari claim that they attract affects, percepts, functives, and prospects, which are their components and which constitute them, but never absolutely, since such forces only ever approach singularities infinitely without ever being identical to them. Trajectories are the movements of affects, percepts, functives, and prospects as they pass back and forth (forward and backward in time) on this plane of immanence. This is where the speed of light enters the picture (33). How do those affects, percepts, functives, and prospects escape the concepts that attract them? Ideally, they exceed the speed of light and thereby they escape the pull of the singularity. Reflections on Time and Politics (Nathan Widder, Reflections on Time and Politics, Pennsylvania State University Press, 2008)

### 1.6 The Image of Thought

This chapter takes aim at an "image of thought" that permeates both popular and philosophical discourse. According to this image, thinking naturally gravitates towards truth. Thought is divided easily into categories of truth and error. The model for thought comes from the educational institution, in which a master sets a problem and the pupil produces a solution which is either true or false. This image of the subject supposes that there are different faculties, each of which ideally grasps the particular domain of reality to which it is most suited. In philosophy, this conception results in discourses predicated on the argument that "Everybody knows..." the truth of some basic idea. Descartes, for example, appeals to the idea that everyone can at least think and therefore exists. Deleuze points out that philosophy of this type attempts to eliminate all objective presuppositions while maintaining subjective ones. Deleuze maintains, with Artaud, that real thinking is one of the most difficult challenges there is. Thinking requires a confrontation with stupidity, the state of being formlessly human without engaging any real problems. One discovers that the real path to truth is through the production of sense: the creation of a texture for thought that relates it to its object. Sense is the membrane that relates thought to its other. Accordingly, learning is not the memorization of facts but the coordination of thought with a reality. "As a result, 'learning' always takes place in and through the unconscious, thereby establishing the bond of a profound complicity between nature and mind". Deleuze's alternate image of thought is based on difference, which creates a dynamism that traverses individual faculties and conceptions. This thought is fundamentally energetic and asignifying: if it produces propositions, these are wholly secondary to its development.
At the end of the chapter, Deleuze sums up the image of thought he critiques with eight attributes: the postulate of the principle, or the Cogitatio natural universalis (good will of the thinker and good nature of thought); the postulate of the ideal, or common sense (common sense as the concordia facultatum and good sense as the distribution which guarantees this concord); the postulate of the model, or of recognition (recognition inviting all the faculties to exercise themselves upon an object supposedly the same, and the consequent possibility of error in the distribution when one faculty confuses one of its objects with a different object of another faculty); the postulate of the element or of representation (when difference is subordinated to the complimentary dimensions of the Same and the Similar, the Analogous and the Opposed; the postulate of the negative, or of error (in which error expresses everything which can go wrong in thought, but only as the product of external mechanisms); the postulate of logical function, or the proposition (designation is taken to be the locus of truth, sense being no more than the neutralized double or the infinite doubling of the proposition); the postulate of modality, or solutions (problems being materially traced from propositions or indeed, formally defined by the possibility of their being solved); the postulate of the end, or result, the postulate of knowledge (the subordination of learning to knowledge, and of culture to method.
It is to be stated that we are here reproducing the following for the bastion and stylobatishness of the necessity of classificational procedural formalities and I do not believe in whatever that has been stated. Nor is it meant as propaganda. It is purely definitional with axiomatic predications and doctrinal manifestations. In Vedas and Upanishads the classification processual formalities of Universal action is undertaken thus with a mention that the proportion of the ones mentioned would be different in different individuals and individuals themselves are investigating systems notwithstanding a wider classification which is nothing but more than a Universal Law. Manduka Upanishad divides all knowledge into two categories. The knowledge that leads to Self Realization is called Para Vidya (Great or Divine Knowledge) and everything else is called Apara Vidya or Knowledge of Material world (worldly knowledge). Shaunaka approaches sage Angiras and asks "Revered Sir, by knowing what everything will be known?" Angiras replies that two know ledges should be known, one is Para Vidya and other is Apara Vidya. Knowledge of worldly things is Apara Vidya and that by which Eternal Truth or Akshara is obtained is Para Vidya. Though Apara Vidya enables one to earn ones bread and helps one to understand each object of universe separately, it does not show the Ultimate Reality (Akshara) or Root Cause of this universe.

While Para Vidya doesn't teach objects of this universe but enables one to understand underlying fabric of it. Like by knowing gold all the gold ornaments could be known, by knowing Akshara, it's another manifestation, the universe is known. This Upanishad expounds the greatness of Para. To think whether a certain thing may be eaten is a thought-form of the mind; "It is good. It is not good. It can be eaten. It cannot be eaten", discriminating notions like these constitute the discriminative intellect. Because the mind alone constitutes the root-principle manifesting as the individual, God and the world, its absorption or submergence and dissolution in the Self as pure Consciousness is the final emancipation known as Kaivalya and in the Supreme Spirit, the Brahman.(Ramana maharishi and Wikipedia). Tamas (Darkness): Complete delusion, ignorance, illiberality, indecision in respect of action, sleep, haughtiness, fear, cupidity, grief, censure of good acts, loss of memory, unripeness of judgment, absence of faith, violation of all rules of conduct, want of discrimination, blindness, vileness of behaviour, boastful assertions of performance when there has been no performance, presumption of knowledge in ignorance, unfriendliness (or hostility), evilness of disposition, absence of faith, stupid reasoning, crookedness, incapacity for association, sinful action, senselessness, stolidity, lassitude, absence of self-control, degradation, - all these qualities are known as belonging to Darkness (Tamas). Whatever other states of mind connected with delusion exist in the world, all appertain to Darkness. Frequent ill-speaking of other people, censuring the deities and the Brahmanas (priests), illiberality, vanity, delusion, wrath, unforgiveness, hostility towards all creatures, are regarded as the characteristics of Darkness. Whatever undertakings exist that are unmeritorious (in consequence of their being vain or useless), what gifts there are that are unmeritorious (in consequence of the unworthiness of the done, the unreasonableness of the time, the impropriety of the object, etc.), vain eating, - these also appertain to Darknesss (Tamas). Indulgence in calumny, unforgiveness, animosity, vanity, and absence of faith are also said to be characteristics of Darkness. Whatever men there are in this world who are characterized by these and other faults of a similar kind, and who break through the restraints provided by the scriptures, are all regarded as belonging to the quality of Darkness. Here Rishis and Munis (Seers and sages), and deities become deluded, desirous of pleasure. Darkness, delusion, the great delusion, the great obscurity called wrath, and death, that blinding obscurity (these are the five great afflictions). As regards wrath, that is the great obscurity (and not aversion or hatred as is sometimes included in the list). With respect then to its colour (nature), its characteristics, and its source, I have, ye learned Brahmanas, declared to you, accurately and in due order, everything about the quality of Darkness (Tamas). Who is there that truly understands it? Who is there that truly sees it? That, indeed, is the characteristic of Darkness, viz., the beholding of reality in what is not real. The qualities of Darkness have been declared to you in various ways.
Rajas (Passion): Injuring others, beauty, toil, pleasure and pain, cold and heat, lordship (or power), war, peace, arguments, dissatisfaction, endurance, might, valour, pride, wrath, exertion, quarrel, jealousy, desire, malice, battle, the sense of meum or mineness, protection of others, slaughter, bonds, and affliction, buying and selling, lopping off, cutting, piercing and cutting off the coat of mail that another has worn, fierceness, cruelty, vilifying, pointing out the faults of others, thoughts entirely devoted to worldly affairs, anxiety, animosity, reviling of others, false speech, false or vain gifts, hesitancy or doubts, boastfulness of speech, praise and criticisms, laudation, prowess, defiance, attendance (as on the weak and the sick), obedience (to the commands of preceptors and parents), service or ministrations, harbouring of thirst or desire, cleverness or dexterity of conduct, policy heedlessness, contumely, possessions, and diverse decorations that prevail in the world among men, women, animals, inanimate things, houses, grief, incredulousness, vows and regulations, actions with expectation (of good result), diverse acts of public charity, the rites in respect of Swaha salutations, rites of Swadha and Vashat, officiating at the sacrifices of others, imparting of instruction, performance of sacrifices, study, making of gifts, acceptance of gifts, rites of expiation, auspicious acts, the wish to have this and that, affection generated by the merits of the object for which or whom it is felt, treachery, deception, disrespect and respect, theft, killing, desire of concealment, vexation, wakefulness, ostentation, haughtiness, attachment, devotion, contentment, exultation, gambling, indulgence in scandal, all relations arising out of women, attachment to dancing, instrumental music and songs - all these qualities have been said to belong to the quality of Passion (Rajas). Those men on earth who meditate on the past, present and the future, who are devoted to the aggregate of the three viz., Religion, Wealth and Pleasure, who acting from impulse of desire, exult on attaining to affluence in respect of every desire, are said to be enveloped by Passion (Rajas). These men have downward courses. Repeatedly reborn in this world, they give themselves up to pleasure. They covet what belongs to the world as also all those fruits that belong to the world hereafter. They make gifts, accept gifts, offer oblations to the Pitris, and pour libations on the sacrificial fire.
Sattwa (Goodness): Brahma (the Grandsire Prajapati) said: Sattwa is beneficial to all creatures in the world, and unblamable, and constitutes the conduct of those that are good. Joy, satisfaction, nobility, enlightenment, and happiness, absence of stinginess, absence of fear, contentment, disposition for faith, forgiveness, courage, abstention from injuring any creature, equability, truth, straightforwardness, absence of wrath, absence of malice, purity, cleverness, prowess- these appertain to the quality of Goodness (Sattwa). He who is devoted to the duty
of Yoga, regarding knowledge to be vain, conduct to be vain, service to be vain, and mode of life to be vain, attains to what is highest in the world hereafter. Freedom from the idea of meum (mineness), freedom from egoism, freedom from expectations, looking upon all with an equal eye, and freedom from desire, - these constitute the eternal religion of the good. Confidence, modesty, forgiveness, renunciation, purity, absence of laziness, absence of cruelty, absence of delusion, compassion to all creatures, absence of the disposition to calumniate, exultation, satisfaction, rapture, humility, good behaviour, purity in all acts having for their object the attainment of tranquility, righteous understanding, emancipation from attachments, indifference, Brahmacharya (celibacy), complete renunciation, freedom from the idea of meum, freedom from expectations, unbroken observance of righteousness, beliefs that gifts are vain, sacrifices are vain, study is vain, vows are vain, acceptance of gifts is vain, observance of duties is vain, and penances are vain - those Brahmanas (priests) in this world, whose conduct is marked by these virtues, who adhere to righteousness, who abide in the Vedas, are said to be wise and possessed of correctness of vision. [Note: Compare from The Mahabharata, Aswamedha Parva, and Sec.XLIV): Brahma said: The Unmanifest is the source of all the worlds as, indeed, that is the end of everything. Days end with the sun's setting and Nights with the sun's rising. The end of pleasure is always sorrow, and the end of sorrow is always pleasure. All accumulations have exhaustion for their end, and all ascents have falls for their end. All associations have dissociations for their end, and life has death for its end. All action ends in destruction and all that is born is certain to meet with death. Every mobile and immobile thing in this world is transient. Sacrifice, gift, penances, study, vows, observances, - all these have destruction for their end. Of Knowledge, there is no end. Hence, one that is possessed of a tranquil soul, that has subjugated his senses, that is freed from the sense of meum (mineness), that is devoid of egoism, is released from all sins by pure knowledge.] Casting off all sins and freed from grief, those men possessed of wisdom attain to Heaven and create diverse bodies for themselves. Attaining the power of governing everything, self-restraint, minuteness, and these high-souled ones make operations of their own mind, like the gods themselves dwelling in Heaven. Such men are said to have their courses directed upwards. They are veritable gods capable of modifying all things. Attaining to Heaven they modify all things by their very nature. They get whatever objects they desire and enjoy them. Thus have I, ye foremost of regenerate ones, described to you what that conduct is which appertains to the quality of Goodness (Sattwa). Understanding this duly, one acquires whatever objects one desire. The qualities that appertain to Goodness have been declared particularly. The conduct which those qualities constitute has also been properly set forth. That man, who always understands these qualities, succeeds in enjoying the qualities without being attached to them. Sattwa, Rajas \& Tamas Whatever object exists in this world, everything in it is fraught with the three qualities.
It is to be noted that the primary focus and locus of homologous repetitiveness and differentially instrumental activity we are talking about is the application of some certain Universal laws should not be mistaken for the Universalistic laws and particularistic laws themselves. All we are talking about is the application of paradigmatic relational content to specific investigating systems under consideration. On the other hand there certainly exist Universalistic Laws and Particularistic Laws. We are not in from any point of view talking about the imperative compatibilities and structural variabilities of the two different forms of laws but the application of say Einstein's Law of mass energy equivalence to some certain galaxy which is under investigation. Following essay allays and ameliorates the vestiges of doubt in the eventuality of confoundment between the two schools of thought we have essayed. It is simple application systems that are also investigatory and conforms and congruential with the given Einsteinian Theory. This universalism which is not one Linda M. G. Zerilli From: Diacritics Volume 28, Number 2, summer 1998 pp. 3-20 | 10.1353/dia.1998.0013 In lieu of an abstract, here is a brief excerpt of the content: Diacritics 28.2 (1998) 3-20 Review Essay Ernesto Laclau. Emancipation(s). London: Verso, 1996. Judging from the recent spate of publications devoted to the question of the universal, it appears that, in the view of some critics, we are witnessing a reevaluation of its dismantling in twentieth-century thought. One of the many oddities about this "return of the universal" is the idea that contemporary engagements with it are more or less of a piece, and that they reflect a growing consensus that poststructuralist political theories are incapable of generating a viable alternative to the collective fragmentation that characterizes late modernity. The putative return to the universal marks, on this view, both a homecoming to Enlightenment ideals -- purified of their more poisonous elements, of course -- and a reconciliation of sorts between those who refuted these ideals and those who sought to realize them. Now that "we" all know and agree that post structuralism is critically valuable but politically bankrupt; now that we all know and agree that the "old universal" was indeed a "pseudouniversal," so the homecoming narrative goes; we can get on with the project of constructing a "new universal." This authentic universal would really be inclusive of all people, regardless of race, class, gender, sexuality, ethnicity, nationality, and whatever else attaches to the "embarrassing etcetera" that, as Judith Butler reminds us, inevitably accompanies such gestures of acknowledging human diversity.
Before signing on to this felicitous agreement about "the necessity of universalism," we may wish to know whether we have anything like a minimal agreement in language, that is, whether we who speak of this universal
are even speaking about the same thing. Apart from the not insignificant problem of translating from a philosophical to a political idiom, the whole question of this agreement is virtually occluded by the rush to rescue politics from the virulent particularisms that admit no common ground or sense of collective belonging. Presented in terms of the familiar binary couple, the choice between universalism and particularism seems settled by merely pointing to global and domestic political realities. Universalism is the only alternative to social fragmentation, wild child of the collapse of communism, the rise of deadly nationalisms, and the multiculturalist romance with particularism. To invoke the name of the universal in any affirmative sense is already to sign on to the political diagnosis and its solution. One of the many virtues of Ernesto Laclau's Emancipation(s) is that it offers both an alternative to the binarisms spawned by the "return" to the universal (for example, false universalism/true universalism) and a trenchant critique of the original binary couple itself (universalism/ particularism). Demonstrating the imbrications of the universal and the particular, Laclau shows why it is a matter not of choosing one over the other but of articulating, in a scrupulously political sense, the relation between the two. He thus explicitly rejects the notion that this relation is one of mutual exclusion, and shows that the tendency to see it as just that has led to the impasse of the contemporary debate, an impasse that is glossed over in some highly visible academic cases by proclaiming the necessary return to the universal. Although the language of universalism as spoken by Laclau searches for some common ground between particularists and Universalists, it is more by way of articulating their mutual contamination, that is, how each is rendered impure by the irreducible presence of the other. Aristotle assumes that there is a plurality of individual things (substances) that are characterized by intrinsic properties (forms) each. David Lewis, an analytical philosopher, provided the thesis of Humean supervenience: at the basic level of the world, there are only local qualities in the sense of intrinsic properties instantiated by space-time points or point-sized particles or field sources at spacetime points. Space-time points can qualify as individual things in the above mentioned sense. Everything there is in a world like ours supervenes on the distribution of basic intrinsic properties over all space-time points. Whether really everything supervenes on that distribution is not relevant to the present paper. What is important here is the claim that, except for spatio-temporal relations, all the relations between the things at the basic level supervene on their intrinsic properties. We can apply the fundamental principles of mathematical proofs to locate to the True form of nature natural things: Through the systematic observation and analysis (breaking down and classification) of the natural world, in combination with rigorous logic we can make True statements about the natural world and understand: 1) The nature of essences (what something is) 2) The nature of causes (why things occur) Unlike Plato, Aristotle also believes that the other arts are very useful for helping us understand things. Relevant to our course is that he believes argument -- or dialectic -- is a key ingredient for people reaching understandings: by arguing over issues the truth and falsity of the claims becomes increasingly apparent, where Plato might have believed that honing such rhetorical arts only confuses the matter. Entities are not separately determinate individuals but rather inseparable parts of a single phenomenon. In particular, there are no preexisting-individually-determinate-entities-with-determinate-spatial-positions-communicating-
instantaneously-at-some-remove-from-one-another outside of a phenomenon that determinately resolves the boundaries and properties of the entangled components in a way that gives meaning to the notion of individual. Indeed, "individual" is ontologically and semantically indeterminate in the absence of an apparatus that resolves the inherent indeterminacy in a way that makes this notion intelligible (Barad: 316)".
Deleuze's subrepresentational self-differentiation is superior to Hegel's infinite representational selfdifferentiation in solving the problems those self-identity causes in Kant's and Aristotle's (likewise Russell's) representational systems.
Self-identity in representational systems leads to problems in explaining the highest part, the lowest part, and the compositional principle of Kant's, Aristotle's (and Russell's) representational systems. Hegel's and Deleuze's principles of self-difference can solve them. Hegel's productive self-contradiction and sublation suffices logically but not in application to evolution. Deleuze's non-oppositional subrepresentational difference however does suffice in this regard.
A strict view of logical identity leads to problems in Kant's and Aristotle's representational systems. The unities of and between concept and intuition that enable our subject-predicate judgments of the world for Kant are based on the unity of a transcendental self. But Sartre shows this is merely a convenient assumption, because for him the unity of consciousness of the object is based on the continuous unity of the object's givenness. For Deleuze the grounds for our judgments are based on neither the unity of the subject, of the concept, nor of the object, but rather on the unity of incompossible undetermined predicates implying a subject with virtual variations. As it is made of the integration of incompossibilities, it lacks the coherence of self-unity necessary for representation. Another question regards the representational nature of the categories we use for judgment. Aristotle and Russell have hierarchies, but because they exclude self-reference and excluded middle, the very foundations (largest parts), compositions of individuals (smallest parts), and method of composition (division/class inclusion) of their representational systems are problematic and irrepresentable within the systems themselves. Hegel and Deleuze
have different ways of solving this by incorporating self-difference into their systems. Hegel's productive selfopposition creates a genetic line of sublated categories. Deleuze's Bergsonian continuously integrated heterogeneous multiplicity allows a plurality of differentially related incompossible actualizations to coexist virtually. Hegel's and Deleuze's interpretations of differential calculus show us that for Hegel there are ultimately determinate parts that are not finite but make finite values when differentially related; where for Deleuze there are ultimate undetermined parts that are nonetheless determinable as extensive finite values when differentially related. For Hegel the unconditioned (dialectic) and the conditioned (categories it creates) are on the same ontological plane, but for Deleuze the unconditioned (genesis of virtual differentials) and the conditioned (actualization of extensities) are on two different planes, the virtual and the actual, so they cannot succumb to Hegel's system by being sublated. However, Hegel's dialectic can be seen within Deleuze's system as a secondary movement to the genesis of difference. Hegel's theory cannot explain the creation of variation needed in evolutionary, but Deleuze's can.
Deleuze and Hegel offer solutions to the problems of representational systems, which are philosophical systems based on self-unity, identity, and the law of excluded middle. For Kant, our judgments of things have a subjectpredicate structure that is parallel to the subject-predicate structure of concepts and intuitive objects (having the subject-property structure). What unifies each them and all with each other is the a priori unity of a transcendental self. Sartre thinks the unity of objects precedes that of the self. Deleuze's transcendental empiricism posits neither the unity of the self nor of the object; things obtain something like a subject-predicate form from incompossibilities being various and indeterminate, but the thing taking these possible predicates is the subject of the judgments. A strict adherence to the principle of identity and the law of excluded middle causes problems in Aristotle's and Russell's logical systems of classification. For Aristotle, the highest genus is being or unity. But, as it has no genus above it, it cannot be defined according to the structure of this system of division (the problem of the large) and yet all beings under it are characterized by this irrepresentable classification. The species gives the essence, and under the species is the individual, which is distinguished from other individuals not by essential but by accidental traits. But in moments of change, something with one essence has contradictory accidents, and also we don't know until after the change what was essential and what was accidental. So the individual cannot be represented properly in this system (the problem of the small). Also there are cases in the natural world, ring species, which cannot be classified using Aristotle's system of division (the problem of division). Russell also has the problem of the large. He must ban self-reference from his system of set classifications so to avoid the paradox of the set of all non-self-including sets. Yet self-reference is needed to establish identity. Hegel's dialectic and Deleuze's philosophy of difference are competing solutions to these problems with representational systems. Deleuze's system is based on Bergson's continuously integrated heterogeneous multiplicity. We can understand it using Riemann topographical space. Deleuze's virtual/actual relation is like topographical phase space portraits, where we can see all possible actual ways a system can behave. All the incompossible actualizations are differentially related yet are continuously integrated. Hegel's internal dialectic makes use of productive contradiction: from out of a concept arises its contradiction, and from out of that opposition arises a new concept not implied in the first ones. So contraries are located within one another, and there is a genetic chain of production of the categories of understanding. Finite thought like that used in Kant's and Aristotle's systems would find such contradiction unthinkable, but Hegel's infinite thought can think these contradictions. Hegel's and Deleuze's interpretations of the differential calculus help us elaborate their positions. For Hegel, the differential is a relation between vanishing values; they are caught in the act of the sublation of the finite and infinite: the values are vanishing and hence are not finite, but their differential ratio is a finite value; and each is constitutive of the other. For Deleuze, the differential values are not determinate, yet they are determinable in differential relation to one another. For, they are subrepresentational, meaning that they are on a level where parts are not externally exclusive like in extensity, so they are not self-identifiable. The important distinction is that for Hegel the terms are represent able and determinate, but are only thinkable using infinite thought. In examining Kant's antimony of the beginning or beginningless of the world, we see that for Kant, we have this antinomy because we mistakenly think the unconditioned is among the conditioned, when in fact it is noumenal; for Hegel the antinomy indicates the sublation of finite (the necessity for a limit) and infinite (the necessity for all limits to be surpassed), and for him the conditioned and unconditioned are on the same level; yet for Deleuze, the conditioned (actual) is on a different level than the unconditioned (virtual) but the virtual is not outside our knowledge, rather it is only knowable outside representational thinking. Hegel could subsume Deleuze's virtual and actual by sublating them, but that would fail since they are two tendencies of the real and are not really opposites. Deleuze could subsume Hegel's dialectic by saying it is a secondary movement to genesis of pure difference that happens on the level of actuality and representation. But Hegel could say that from the perspective of logic there is no such thing as Deleuze's difference. So we test them by seeing how their theories of the composition of the organism suffice in evolutionary theory. Hegel is like Cuvier in thinking that the organism's parts are matters of how they function in service of the whole (teleological); organ and organism,
individual and species are like sublated opposing terms. But this means that deformations are deteriorations in structure and thus cause deficiencies in functionality. But evolutionary theory depends on a positive account of anatomical variations; natural selection needs to pick the best from a variety of mutations. Geoffrey's and Deleuze's view sees variations as different actualizations of a transcendental model, so their view is more compatible with evolutionary theory. Because Hegel's anatomy is representational, we can see one superiority in Deleuze's subrepresentational response to representational philosophies as opposed to Hegel's infinite representational approach.
Henry Somers-Hall will examine how Deleuze and Hegel respond to the shared problematic of representation in philosophy. He then pits them against one another, and applies them to the role of the structure of the organism in evolution, to evaluate them with respect to one another.
In the first part, we begin by seeing how the history of philosophy contains tendencies toward building theories and systems on the basis of representation. This means that they make use of principles of self-unity, identity, and the law of excluded middle. There are problems with these approaches. Deleuze and Hegel offer solutions. There are two cases under investigation. The first is the transcendental grounds of our knowledge, specifically, what principle allows us to make judgments of the world? Kant offers a representational theory. It is representational, because it is based on a self-identical a priori unified self that is represented in all inner acts, in their accompanying 'I think'. This unity unifies the empirical world into things with a subject-property structure, it unifies our concepts into subject-predicate structure, and it unifies our concepts and our intuitions into represent able judgments with the subject-predicate structure. Sartre's critical stance would say that it is really the unity of objects, and not subjects, that comes first and the unity of the self comes secondly. For Deleuze, a unity neither of consciousness, of self, nor of the objects, is what grounds our subject-predicate knowledge of things. Rather, each moment, events can go many different ways, so the same subject now has many various undetermined predicates, and they are incompossible. Because they are contradictory, the predication of a subject is not representable, even though the subject-predicate structure is there. This is Deleuze's transcendental empiricism. Another case of representation in the history of philosophy is the use of the principle of identity and excluded middle in Aristotle's and Russell's theories of classification. For Aristotle, we define species on the basis of their differences. But the highest genus, being or unity, has nothing to differentiate from, no genus above it or species beside it, so it is indeterminate. However, it is the basic principle saying that all beings are selfunified and have identities (and thus also the system is thoroughly representational). The very representational basis of his system is not itself representational. Russell's theory of class inclusion is also representational. Things are strictly categorized and defined by their groupings. There cannot be contradiction in the system or instances when something's identity contradicts its classification. So it cannot have the paradoxical class of all non-self-inclusive classes. Such a class is meaningless; it cannot be represented in the system. And yet, such a class is based on the same notion of inclusion as all the others. Hence class inclusion, as a universal concept that forms the basis of all instances of classification in his system, is not represent able in this system. So somehow the nature of inclusion for each level is distinguishable, when in fact it is the same sort of inclusion each time. Also, identities and essences are representable, but moments of self-contradiction do not fit into such representable systems. This means that when something is changing, we cannot represent what is happening in the phase of transition when contradictory properties are coincident (like being both wood and fire in the action of ignition). Hegel's solution is to make contradiction productive, using internal dialectic, where some concept brings about its own self-contradiction, and out of it comes a new concept not implied in the first. For Deleuze, this solution still has the problems of representation, as we will later see. Deleuze's solution is a nonoppositional concept of difference.
In the second part, we formulate Deleuze's and Hegel's alternate proposals. Deleuze's is based on Bergson's duration, which is a continuously-integrated heterogeneous multiplicity, unlike the discrete multiplicity of externally related extensive parts characterizing homogeneous space. Bergson's heterogeneous multiplicity better explains living systems.
Deleuze then uses Bergson's continuously integrated heterogeneous multiplicity to characterize the Idea, the problem, and the concept. In all cases, they are terrains of virtual differential incompossibly-actualizeable paths of developmental explication. We can understand them with the model of topographical phase space portraits. They indicate all the tendencies for a system's development using terrain features. This describes the system's behavior on a whole, but in each instantiation only one possible line of development indicated in the map is actualized, because all the lines are incompossible yet coincident in this virtual form. They explicate into extensity. And any one actualization implicates the totality of the whole 'problematic'.
Hegel's dialectical movement brings contraries within one another, and also unites them on the basis of their genetic productions of one another. This allows him to go beyond Kant's finite thought, and also to have totality to his system and an account of change, which is lacking in Aristotle's system. Kant cannot go beyond finite thought, because it cannot think contraries together, like Hegel's infinite thought can. And because Hegel's
concepts are united genetically, differences are inherently linked, and thus he can have totality to a system of differences without the need of some generic category to encompass them all, which was a source of a problem for Aristotle. Rather, their genetic process of unfolding is the glue uniting the differences. Thus Hegel can also explain the process of change, as he has accounted for the process that generates and unites the diverse contradictory changes when something alters.
Now in this final part, we examine how Deleuze and Hegel propose theories that try to overcome the problems of representational theories like the ones we saw in the first part, and we pit the theories against one another and apply them to evolution so to better evaluation them. First we examined how Deleuze's and Hegel's responses to classical representationalist philosophical can be compared on the basis of their different interpretations of differential calculus and Kant's antinomies. We found that for Deleuze we have an unconditioned ground of sensible and intelligible things that is subrepresentational, and for Hegel it is representable, using infinite thought. The calculus differential determines the varying relation between variables that vary with respect to one another. Leibniz saw it as the relation between infinitesimal magnitudes but there are formal problems with this. Newton saw it in terms of vanishing values. Hegel regards the vanishing values as being determinate values that combine finite and infinite, and being and nothingness. This contradiction is only thinkable with infinite thought. For Deleuze the terms of the differential relation are undetermined and subrepresentational, but they are determinable in relation to one another and are the unconditioned condition of conditioned actual determinations. Kant thinks we arrive at antinomous theories regarding whether there is a temporal beginning to the world because our understanding is unable to grasp the unconditioned, the thing in itself, with its categories. Hegel thinks the antinomies go together. Together they express the genuine infinite, because they affirm both that there is a limit and also that it is surpassed. For Hegel the unconditioned, the dialectical contradiction, is representable with infinite thought. Deleuze thinks that the unconditioned is thinkable but not using representational thought but rather using the logic of incompossibility.
We then saw how Deleuze's philosophy of difference is more resilient to attack than Hegel's, when both are pitted against one another. If Hegel wanted to critique Deleuze's philosophy of difference, he would show how Deleuze's virtual and actual as contraries dialectically sublate, which collapses the basic distinction of Deleuze's ontology. However, because Deleuze's virtual and actual are two tendencies of the real and not contraries, such a Hegelian critique would not hold. From a Deleuzean perspective, Hegel's dialectic could be viewed as a false movement, with Deleuze's genesis of difference being the real movement. Yet Hegel purely from a logical standpoint might say that Deleuze's difference does not exist.
So we then applied Deleuze's and Hegel's responses to representation to evolutionary theory to see which one is more compatible and also to see if Deleuze's three criticisms of Hegel still hold: Hegel's is a false movement, Hegel's logic revolves around a single center, and Hegel's dialectic does not provide enough precision for characterizing the world. For Hegel, nature is the one totality and it externalizes into multiplicity, but these form unified systems where parts and their whole are reciprocally determining. Hegel's dialectic is not temporal, so it does not describe an evolutionary progress through time. The structure of the organism is the reciprocally determining relation between organism and organs, which are opposing dialectical pairs like the one and the many. Individuals and species bear this organ/organism relation too for Hegel. Hegel's structure of the organism is more closely tied to Cuvier's anatomy, which is functional and teleological, meaning that organisms' anatomical structures can be understood in terms of their functional purposes. Geoffrey's homological theory of the unity of composition does not identify anatomical parts on the basis of their functions. Rather, he looks to see if the relations between the parts are isomorphic to a transcendental model which is so abstract that it can actualize in a wide variety of forms, such that a fin can be identified with an arm. This is compatible with Deleuze's transcendental empiricism and theory of the virtual, which sees there being a transcendental level that is actualized in various ways. Cuvier's and Hegel's theories, as teleological, regard deformations or mutations in negative terms, as degradations of the organism's structure and thus functioning as well. But evolutionary theory needs a positive view of aberrations. Geoffrey's and Deleuze's theories see variation positively, because variations are considered novel actualizations of the virtual model. Thus Deleuze's response to the problems of representational theories is better than Hegel's at least with regard to its application in evolutionary theory. We also see that Deleuze's three criticism's hold, because Hegel's movement is a matter of (infinite) representation, but because it cannot explain novel evolutionary variations, there is no real evolutionary movement involved. Hegel's structure of the organism has a teleological unity, and so there is a 'monocentering of circles' [around the organic unity of the organism.] Hegel's account is not precise enough. Because it understands the differentiation in the natural world in terms of determinate oppositions, Hegel's dialectic too strongly divides the world rather than seeing the blur rings of boundary that allow for evolutionary variation. Somers-Hall, Henry (2012) Hegel, Deleuze, and the Critique of Representation. Dialectics of Negation and Difference. Albany: SUNY. Emphasis mine

### 1.7 Avoiding the Void

Poets on Poets (Romantic Circles) Saltines and Ginger Ale (Annotated minutes of Yale's Using Theory lunch series) Stanford Encyclopedia of Philosophy Saturday, July 28, 2007
Dread in Kierkegaard
Dread or anxiety has a specific structure for Kierkegaard, a structure Heidegger is correct in elaborating as thrown-ness in Being and Time: in other words, Heidegger's reading of Kierkegaard (and in a footnote Heidegger indeed acknowledges that he is indebted to Kierkegaard as well as to Christian theology: "The man who has gone farthest in analyzing the phenomenon of anxiety--and again in the theological context of a 'psychological' exposition of the problem of original sin--is Soren Kierkegaard") is exact. Let's see how. The structure of dread is outlined by Kierkegaard in the following passage, taking Adam's fall into sin as its concrete instance:
...When it is related in Genesis that God said to Adam, "Only of the tree of the knowledge of good and evil thou shalt not eat," it is a matter of course that Adam did not understand this word [i.e. that he was "innocent"]. For how could he have understood the difference between good and evil, seeing that this distinction was in fact consequent upon the enjoyment of the fruit?
When one assumes that the prohibition awakens the desire, one posits knowledge instead of ignorance; for Adam would have had to have knowledge of freedom, since his desire was to ["freely"] use it [i.e. the distinction between good and evil]. The explanation therefore anticipates what was subsequent. The prohibition alarms Adam [or induces a state of dread] because the prohibition awakens in him the possibility of freedom... [And yet this freedom] is a nothing, the alarming possibility of being able... Thus innocence is brought to its last extremity. -The Concept of Dread, in Existentialism from Dostoevsky to Sartre, 103-104.
Kierkegaard is saying that dread is fundamentally what allows innocence--exemplified in Adam before he ate of the tree of knowledge--to be "brought to its last extremity," or, in other words, to fall into the state of sin, whose essence, Kierkegaard later says, is guilt. Let's represent this structure in this way:
Innocence $\rightarrow$ dread $\rightarrow$ guilt
In this passage Kierkegaard points out explicitly that this structure bypasses the concept of prohibition as we normally understand it completely. Thus he also implicitly indicates fundamentally that prohibition is what is reevaluated or revalued throughout his analysis of dread's engendering guilt. Indeed, Christian theology has often focused on this particular issue (prohibition) primarily when it comes to Adam's fall in Genesis. What is prohibited for Kierkegaard, however, in contrast to this Christian tradition, is not eating of the tree, and therefore something like the desire to know. We'll specify exactly what Kierkegaard thinks is prohibited by God in this statement later, and thus what he conceives of as desire. But for now, with this brought up, the first question to put to ourselves is why he wants to bypass the issue of prohibition in this traditional way? How will looking at dread as the origin of guilt require us to revalue the concept of prohibition?
Because the key to understanding dread is to understand it as also bound up with knowledge. As Kierkegaard says, "when one assumes that the prohibition awakens the desire, one posits a knowledge instead of ignorance.", and this covers up the essential phenomenon of how guilt arises. Essentially, understanding prohibition as the thing that awakens desire covers up the fundamental ignorant innocence that is constitutive for the act of eating of the tree--the ignorance that is precisely what makes the story (like the story of Job) so extremely disturbing to us. Why would God punish what essentially is an act done without our ability to know that it was wrong? Positing that Adam was focused on the prohibition itself when he ate of the tree requires that he know what the tree will do when he eats of it--in short, if the prohibition awakens the desire, it is precisely because Adam would know beforehand why what is prohibited is prohibited. Obviously this is untenable: how could Adam know beforehand what the tree would give him? No, the whole instance proceeded in complete ignorance. But how, then, could Adam have become guilty of trespassing against God's word? That is where dread comes in.
Dread is what, for Kierkegaard, leads us out of innocence and ignorance and into guilt, instead of knowledge. Knowledge is not what causes the fall of Adam, but dread, and with it, freedom. Thus to the structure we outlined above, there would seem to correspond a structure that looks like this:
Ignorance $\rightarrow$ dread $\rightarrow$ knowledge
But because we do not know how dread begets knowledge, this statement as yet is empty. Furthermore, if we were to try and tie freedom into this structure by representing it as the following we would be fundamentally wrong:
Ignorance $\rightarrow$ dread $\rightarrow$ knowledge, freedom
Freedom is not a consequence of dread for Kierkegaard, but rather underlies it as what dread itself activates or actualizes in dread's becoming actual. Thus, we must ask, how does dread lead us out of innocence and ignorance by way of being connected with freedom for Kierkegaard?
It should be noted that all the foregoing has done is to outline the interconnected nature of two structures, the structure of innocence and guilt, and the structure of ignorance and knowledge, which we can represent by
combining our previous representations:
Innocence $\rightarrow$ dread $\rightarrow$ guilt
Ignorance $\rightarrow$ dread $\rightarrow$ knowledge
It is also clear from the foregoing that two concepts remain to be connected to this nexus: prohibition and, most essentially, freedom. But it is not by specifying what either of these are for Kierkegaard that we get a handle on what he means by them and dread more generally. Rather, it is by proceeding with the structures that we already have outlined that we can specify their nature. In other words, though Kierkegaard has a specific nature of freedom, he does not specify what freedom is concretely and then derive his analysis of dread (not to mention his reading of Scripture) from it--this would be too abstract for him. Rather he sticks close to what he already knows and what Scripture already tells him about the transition between ignorance and innocence and guilt and knowledge. We'll do the same. Indeed, it should be obvious by bringing the two structures we have outlined that, if we posit some other term--dread--instead of the prohibition itself as the thing that leads us out of ignorance and innocence, that this third term--dread--will be responsible for relating both ignorance and innocence. In other words, from what we have already seen Kierkegaard say, it should be obvious that dread leads us out of innocence ignorantly, and that dread leads us out of ignorance innocently. It is by analyzing these relations that Kierkegaard sticks close to what he already knows and does not give in to a pressure to cover up the disturbing nature of Adam's fall--not to mention the fall of anyone innocently or ignorantly into guilt and knowledge.
Now, if one is led out of innocence, or, as we normally call it, is guilty for some reason, and yet is led out of innocence ignorantly, he still seems innocent: indeed, this is why Kierkegaard says "he who... becomes guilty is innocent" (102)--that is, if they become guilty ignorantly. Why should this be the case? Why do we normally make this provision for guilt? Or, put differently, how can one who is guilty be innocent at the same time if they are ignorant? By our normal reasoning, we say that if an innocent person is lead to guilt ignorantly, it is something other than effectuates the guilt, not the person who was lead into guilt. "They didn't really mean it," we say, "it wasn't really their fault." Guilt must be tied up with this "something other," then. Kierkegaard simply names this "something other," "dread." That is, instead of pursuing the issue of guilt by making an exception of the case in which someone is led to guilt ignorantly, as we usually do, he analyzes it as a positive phenomenon. In other words, he is not excluding this instance from the rest of our codified ways of assigning guilt, making of it a case where the "rules don't apply in the same way:" rather, he will eventually conclude that this instance is the exemplary instance of the way guilt arises.
But let us continue--how could one be led into guilt ignorantly, if guilt essentially lies in knowingly doing something? Where is the knowledge located in this instance? If someone is guilty innocently because of ignorance, and thus has become guilty by "something other" than her or himself, and if this "something other" is dread, then we might say that it is precisely dread that effectuates the guilt knowingly. In other words, if the innocent person is still innocent after being made guilty through dread, it is not the person who is responsible for this guilty status: for how could he have known--being ignorant--whatever it was that rendered him guilty? Dread knows, somehow, or has some relationship to the knowledge of which the person is ignorant, and thus Kierkegaard continues the sentence just quoted ("he who through dread becomes guilty is innocent") by saying "for it was not he himself but dread, an alien power which laid hold of him" in the transition between innocence and guilt (102). Thus by specifying the relationship of dread to knowledge we get a handle on exactly the way someone innocent and ignorant can be led to guilt. If they are seized by dread, they are seized by something that has a relationship to a knowledge that they do not know. We might represent this the following way before we go on to analyze this relationship:
Innocence/ignorance $\rightarrow$ (dread $\leftarrow$ knowledge $) \rightarrow$ guilt
Notice that this gets rid of our previous schema where knowledge was somehow a product of the dread of an innocent person along with guilt, which was represented this way:
Ignorance $\rightarrow$ dread $\rightarrow$ knowledge
Knowledge is intimately connected with dread, and not with ignorance. Thus it does not directly oppose and obviate ignorance itself; knowledge does not suddenly come along and wipe out innocence because it wipes out ignorance. Rather, knowledge has a direct relationship to dread, and only can effect ignorance through this mediation.
We can specify the relationship of knowledge to dread by asking what must necessarily be the essence of a knowledge that preserves ignorance. The answer to this is that it must be a fantasy, something that is not real in content but is real in its ability or possibility to be real. As Kierkegaard says, at the center of dread is that which in an innocent act could have been, that which in an act was that person's particular "I can" (104), in the sense of an ignorant "I can do this which I currently fantasize about" at the moment of one's fantasizing. This is why Kierkegaard specifies dread as a "dreaming" of the spirit: the moment at which a subject dreads is the moment in which that subject indeed "projects its own reality" even though "this reality is nothing" and "this nothing constantly sees innocence outside of it" . The reality it projects is precisely its own ability to do whatever it is

## that it projects.

Now it should be obvious that by "seeing innocence outside of it," Kierkegaard means that in the particular moment of dread, what is, is only that which is for someone who is ignorant, or does not know reality, and is therefore innocent in the way we determined before. Let's penetrate deeper into this phenomenon. What is real in the moment of dread is nothing, and dread itself is thus dread "about nothing" as we usually say. But this nothing is not really nothing, as Kierkegaard says. It is only nothing insofar as what the dread is about in reality is nothing. In reality, whatever is dreaded has the constitution of a dream, a wish. But the fact that the dread occurs and is about something that is not real does not make the act of dreading itself disappear. The act of dreading is precisely everything, it is so much not anything--it is and remains one of the keenest and most real psychological feelings possible. We thus might represent dread as the following, making a distinction between the act of dread and what is dreaded.
Dread $\rightarrow$ content, what is dreaded $\rightarrow$ nothing, dream
$\downarrow$
Form, the act of dreading
$\downarrow$
Real, reality
More appropriately, we might call the act of dread a desire, since a desire is precisely a relationship to something that is, as of yet, nothing. Indeed, if we are going to call this act a wish or a dream as well this seems legitimate. But in recharacterizing this act this way, we can see desire come into play--and it should be quite clear now that it is precisely not the desire of some particular bit of knowledge like the distinction between good and evil. What is dreaded, what is desired is something that is not, and since the act of dread or desire occurs anyway, we are left to conclude that that which it is really about is precisely unrealized possibility itself, in other words, the reality of nothing--the reality of something that, as of yet, is not real and is therefore nothing. Put differently (and perhaps more clearly), what the desire is about is (in Freudian/Lacanian terms) really the drive, the act of desiring alone. Similarly, what is dreaded is really only the possibility of the individual to realize that particular thing one dreads. Thus the above relationship can be redrawn like this:
Dread $\rightarrow$ desire, what is dreaded $\rightarrow$ nothing, dream
$\downarrow$
Drive, what is really dreaded
$\downarrow$
Real, reality
This continual play on the word "nothing" Kierkegaard uses (and which we are merely reduplicating) he uses perhaps to curb the impact of the radical thesis he is putting forth here. What he is saying is that what dread is drive itself, the desire for the realization of what is unrealized and, as the desire of someone who is ignorant, is the desire of something that is not known. Desire, as dread and therefore as drive, is desire for that of which one is ignorant, that which is nothing currently. As such, it is not fundamentally that thing that is desired, but (because one does not really know that thing, the act one could have done), it is really the possibility of the realization of that thing. This is what is meant by us saying desire is desire of "the reality of nothing:" it is fundamentally the desire for the possibility to realize what nothing, the desire of drive is now. Furthermore, as a dream or wish or desire, one possesses already in dread this possibility--it is there in one's desiring of that which does not exist. This is why it is, as Kierkegaard implies, the greatest inner possibility of a subject.
Let's sum this up to be a little clearer. What is desired in dread is precisely that of which one is completely ignorant--to the subject it appears as nothing, making him say characteristically when asked what he is worried about, "it's nothing." Thus, what is desired is precisely not knowledge, because what is desired is precisely that of which one as of yet cannot actually know. However, desiring (and we should mention that we do not even know of this desire--desire is not like a willing)--desiring that of which one is ignorant is indeed desiring the possibility of knowing that which is not known--this is, as it were, the side effect of desiring precisely that which one cannot know. In desiring non-knowledge, as we might put it, we precisely desire the possibility not of knowing the non-knowledge itself, but of knowing our own possibility to know, our own possibility to not be as ignorant as we are now. This side-effect we call drive, or the reality of the act of dread. We might represent this structure of knowledge thusly:
Dread/desire $\rightarrow$ (desire as such) that of which one is ignorant
$\downarrow$ (drive)
Possibility of knowing
It should be obvious that this is just a condensed version of what we have already specified. It is this downward arrow that is active: the desire for that of which one is ignorant opens up a general, indeterminate possibility of knowing anything-i.e. not just that of which one is ignorant. Rightly, Kierkegaard does not speak of this indeterminate result as genuine knowledge yet: dread brings into view only "a nothing in lively communication
with the innocence of ignorance". It is "lively communication" only that is really going on here, since what is being known is precisely only the reality of the possibility of knowing (drive). Thus, one can still speak of this knowledge of a possibility of knowing as ignorance, and we will indeed do so. It is ignorance in lively communication with only the possibility of knowing, and as such, it produces no knowledge and continues to preserve ignorance itself. We can represent this thus within the larger structure of dread:
Ignorance $\rightarrow$ \{dread $\leftarrow([$ desire $\rightarrow$ that of which one is ignorant $] \rightarrow$ possibility of knowing (drive)/ignorance ] ) $\} \rightarrow$ guilt
This specified, we can show exactly what this type of ignorance is and does. It should be noted that grasping the role of desire has allowed us to specify the role of prohibition, but we will put this off to later when the whole phenomenon of dread comes fully into view. Now, this particular type of ignorance, this knowledge only of an open-ended possibility of knowledge this "I can," this result of a desire based in dread, Kierkegaard names "freedom." As Kierkegaard puts it, "dread is the reality of freedom as possibility anterior to possibility". By "possibility anterior to possibility" Kierkegaard means that freedom is the reality of possibility itself as the reality of possibility in the nothing, in the unrealized, in that of which the subject is and remains ignorant. Thus we might rewrite our above structure as the following, having it retains the same meaning:
Ignorance $\rightarrow$ (dread $\leftarrow$ freedom $) \rightarrow$ guilt
Now, it is obviously this freedom that brings one from innocence into guilt. How does this occur according to Kierkegaard--especially if it is not really knowledge still? I'll save this answer for another post.
Posted by Mike Johnduff
What is written about: Being and Time, Heidegger, Kierkegaard

## 3 comments:

Sean said...
Do you side with Kaufmann or Dreyfus? To what degree is Heidegger indebted to Kierkegaard? Does it really stop at thrown-ness? Or, can you trace all of Heidegger's existentialism back to 'Religiousness A' (a secularized version)? Isn't the real distinction exactly what anxiety reveals, is it the value of finite existence, or does is reveal an infinite - a sort of flipside to finite existence - as well? Also, hello I'm Sean.
February 10, 2008 at 10:48 PM
Mike said...
The relationship of Heidegger to religion is a tricky one. This precludes it being any mere "secularized version" of a text of Kierkegaard. Furthermore, this would have to deal with how, for Heidegger, Kierkegaard relates to the Aristotelian structure of being-in-the-world and the rereading of Aristotle more generally that occurs in Being and Time, which is not an easy relation to figure out. In "The Hermeneutics of Facticity," a pretty early course (1924) Heidegger is outlining much of what will become Being and Time in its basic approach to interpretation, and he there cites Kierkegaard as prominent in the sense that it inspires his hermeneutical or interpretative task or way of getting at being. I think revisiting this nexus would probably give us some directions in conceiving *exactly how* Heidegger is thinking about Kierkegaard: one could say that the interpretative method that Husserl phenomenology gets modified into would have to be conceived as more Kierkegaard. In other words, it is obvious Heidegger is indebted to Kierkegaard massively--the real question is how. This is all one possibility--I'm really saying that I have no clue, and thus your question opens up a great avenue to pursue. Do you have any idea? As to Kaufmann or Dreyfus, I'm not so familiar with the arguments of the former relating to Kierkegaard and their opposition to Dreyfus' readings: I think Dreyfus has a great interpretation of Kierkegaard though, and though I haven't listened yet to his lectures on death, guilt, and resoluteness in the Heidegger course this semester, I plan to--they should localize at least some of these problems within the Heidegger. I will say that I think Dreyfus is a little too quick perhaps to characterize Kierkegaard as merely the "existential" influence of Heidegger, as if all of Heidegger's concern with death and guilt were to stem from a concern that is able to be distinctly separated from his more Aristotelian concern in Division I. I'm not the first to criticize him in this way though: Blattner is the best at it, though perhaps going too far in the other direction and making the concerns of temporality and finitude (finitude being really what death is all about for Heidegger), the sole organizing theme of the book. Heidegger sees being as finite, and this is probably one of the central theses of the book: furthermore, he sees Aristotle saying the same thing long ago. He must elaborate how this is able to be so--and so that leads him to posit a Division I that will merge with the concern of Division II, death etc. Kierkegaard figures there also because he breaks with Hegel--that should be noted. Hegel is Heidegger's archenemy--so anyone able to say that there is a nothingness and a freedom in nothingness, a possibility for a finite subject to relate to infinite possibility (whether God or not), possibility en abyme (as Derrida likes to say) or, conceived probably less rigorously, as drive and repetition of desire (which Lacan says and this is how I formulate it above), would not escape him in his reading of Aristotle. A great helpful book on this is actually Levinas' God, Death and Time--it is really clear and outlines certain concerns
about infinity and finiteness in Heidegger and elsewhere that you touched on. Whatever you think of him, too, reading the section on Kierkegaard in The Gift of Death by Derrida is helpful, because he outlines pretty much a standard reading of the suspension of the ethical in relationship to death and shows how at this point one can relate it to concerns of finiteness and infinity. But I'm talking too much--what do you think? One more thing... with regard to thrown-ness... of course it doesn't stop there, but I think that's the structure that is the best to think about with all this Kierkegaard stuff (as I say in later posts, though unsuccessfully--I stopped all this because it was getting too tough to think)... the real question is how this possibility beyond possibility that is experienced in the dread of nothingness *already exists or is factical* in Dasein. How possibility or futurity (to talk about it in temporal terms) is already within Dasein so that Dasein is thrown back upon it in its existence, so that it is thrown back upon its factical existentiality in its being-existential or projecting itself forward into nothingness, how projecting oneself forward into nothingness is throwing oneself back to the fact of one's nothingness (this all takes place in some remarks on nothingness that are really weird in Being and Time and have a lot to do with Hegel)--this relay, when conceived with respect to its facticity, is the real tough thing to think. Projection is easy--thinking facticity is the real tough stuff. And to Dreyfus' immense credit (I don't know how many people congratulate him on this--but everyone taking his course or exposed to his writings probably should, it is so vital for understanding anything in Being and Time), this is what he thinks best and why he lays so much emphasis on Division I: it's there that we get a structure that is somehow, in its being structured that way, already there (da), albeit falling and distracted, etc. I'll post this as a separate new post, so it might be easier to find--and also so that others can perhaps get in on what you asked!
February 11, 2008 at 10:14 PM
Mike said..
Also I thought of this afterwards with respect to what I was saying towards the end of my comment on the importance of facticity:
This might answer your last question--why I actually don't think that it is so much about the what anxiety reveals. It is about the nature of this revealing as such that is the key for Heidegger. Others like Levinas will change what is revealed and then go back and read it into the structure of Dasein that Heidegger elaborates and show how it cannot be that way (this is what he does in the book I referred you to--but of course not with the rest of his philosophy, which is much more thought out [precisely with regard to what facticity would then have to be] than this one lecture). But for Heidegger, finitude or infinitude would have to announce itself before it is revealed in the revealing itself--the real trick is not deciding then whether revealing that is done in Dasein is finite or infinite, but by trying to let Dasein itself point the way towards answering this, which only then will take us to what is revealed. This leads, however, to the hermeneutic circle Heidegger points out famously. (From Google search, Wikipedia, Text books, and other author's pages)

## 2. MATTER-ANTIMATTER CICLE OF ELECTROMAGNETISM - THEORIES AND CONCEPTS

Sept. 4th, 2012
Posted by Alberto Molina-Martinez, physics researcher at the Molina Institute for Photon Physics Research, Cambridge, Massachusetts, USA.

## "Where did all the anti-matter go?

Answer: nowhere, everywhere, because antimatter is an intrinsic constituent of ordinary matter.
The question "Where did all the antimatter go?" has puzzled physicists for a long time. Many theories have been explored, but still the mystery remains.

## Background

It was by September of 1999 when the author first envisioned a new theory of electricity, which incorporated the concept of antimatter as an integral part of the electromagnetic phenomena.
The concept was published as a conceptual part in a United States patent application of 2004/2005; explored in the website "givetheplanetachance.com" from 2006 to date; discussed in several documents and in at least one new-physics blog, all by the author. The concept, however, remains theoretical to the date of this publication.
This theory suggests that "electricity consists of the flow of electrons and positrons in opposite directions along a conductor (not only of electrons, as current accepted knowledge describes), induced by the crossing of a magnetic field through the conductor. At the closing of the circuit, both, electrons and positrons, flow to their mutual encounter by the attraction of opposites, nullifying each other, annihilating each other, since each one is the antimatter of the other".
If electrons can flow along a conductor by the influence of a moving magnetic field, why wouldn't the positrons be able to do the same, being identical, with just an opposite charge?
[This question of course would not make any sense if atoms had only negatively charged electrons orbiting the
nucleus, because the electrons would interact with the positrons, stopping them. The question would only make sense for the case electrons and positrons could share the same orbits in the form of a dual neutral particle containing both, the electron and the positron, as we'll see further on. In that case, both, electrons and positrons, would be able to flow freely along a conductor under the influence of a moving magnetic field.]*
At the time, however, the author did not realize the implications that this new theory of electricity could have in the search for the antimatter apparently lost in the universe. But, suddenly, in the early morning hours of August 19, 2012, it became clear for the first time that for the new theory of electricity to be correct, the electron and the positron had to pre-exist in the atom.
When a charged particle passes through matter at rest it will cause the production of electron pairs, that is electrons and positrons, but if nothing separates them by force, they will reunite after the passing of the charged particle, nullifying each other, and the atoms of matter will be back at rest.
Where was the positron and where did it go after the passing of the charged particle? The electron and the positron had to pre-exist in the atoms of matter for them to separate and reunite at the passing of a charged particle. A positron cannot just appear when a charged particle passes, only to disappear when it has passed. It must be there, as an integral part of the atom.
On the other hand, since two identical particles, but with opposite charge, could not be around each other in the atom without being attracted to each other, the only way for them to exist would be as part of a common and dual particle that we can call the "bielectron".
This "bielectron" may contain the electron and positron as distinct entities bonded together by their mutual attraction, as shown in Fig. 2, or it may constitute an independent entity in itself that will dissociate into an electron pair under proper circumstances and/or reconstitute itself from a free electron and positron pair close enough to attract each other.
The photovoltaic effect may hold a key to elucidate the existence of the "bielectron". The diagram below is a very common conception of the photovoltaic effect. An incident photon will cause the dissociation of an electron pair, this is, an electron and a positron, but because of the prejudice that an electron and a positron cannot be together, for being the antimatter of each other, we had to invent a "traveling hole" to be able to give it a positive charge.
According to the new conception, it is from the bielectron from where they both, the electron and the positron, emanate.


Fig. 1 - Common conception of the photovoltaic effect. Because of the prejudice that an electron and a positron cannot be together, for being the antimatter of each other, we had to invent a "traveling hole" to be able to give it a positive charge. According to the new conception, it is the positrons coming from the dissociation of bielectrons which travel with positive charge along the conductors.
Now, for a bonding between an electron and a positron to exist there must be a force involved. The energy of a single electron or positron is very small, comparatively, for which it may seem that their bonding may not imply the existence of a very powerful force, but considering that the electron and the positron are the antimatter of each other, this force may have deep physical implications.

In order to preserve the law of conservation of energy the amount of energy required to break free the electron and the positron from a bielectron must be equal to the amount of energy released by a matter-antimatter encounter of the same particles.


Fig. 2 - Conductor at rest. When a conductor is at rest all the bielectrons are located at their respective orbits in the conductor's atoms, not generating any electric charge.

Electrons and positrons, being as they are the antimatter of each other, are part of the same atoms, molecules, planets and stars that form the physical universe.

## Matter-antimatter cycle of electromagnetism

A charged particle passing through matter at rest is carrying with it a fast moving electromagnetic field, a phenomenon not essentially different from a magnetic field passing through a conductor to generate electricity.
When a magnetic field crosses through an electrical conductor, it does the same; it forces the division and separation of the bielectron into its constituents, the electron and the positron. The stronger the magnetic field passing through, the larger the number of bielectrons that will dissociate into electron-pairs (one electron, one positron), separating them in opposite directions.
As equal charges repel each other, both, the negative and the positive free electrons, will physically occupy all the available space in their respective segment of the conductor, being the electrical potential or voltage the concentration or density of free electrons and free positrons occupying said available space. The more electrons and positrons repelling their equals are present in the volume of their respective segment of the conductor, the more the "pressure" (voltage) will grow.
At the closing of the circuit the free electrons and positrons, pushed forward by their own "pressure", are irresistibly pulled by the attraction of their antimatter counterpart. It is this process of mutual attraction and continuous reunification into bielectrons which causes the flow of electrons and positrons along the conductors.
The conductor thus becomes the "battlefield" where electrons and positrons collide with each other, while releasing energy proportional to the amount of particles involved in these matter-antimatter collisions. At low "pressure" or voltage, the only perceptible consequence is the release of energy in the form of heat, but at higher "pressure" or voltage the matter-antimatter encounters can manifest more violently, as expected from antimatter reactions, to the point of melting metals in fractions of a second.


Fig. 3 - Matter-antimatter cycle of electromagnetism. When a conductor is placed under a moving magnetic field, its otherwise stable bielectrons will break apart into electrons and positrons, which will flow in opposite directions along the conductor. At the closing of the circuit (shown here as a closed loop), electrons and positrons, attracted to each other by their opposite charge, reunite into bielectrons, releasing an equal amount of energy as initially required to separate them.

This flow of electrons and positrons along the conductors, in opposite directions, is what allows us to use the electromagnetic phenomena for the production of heat, light, movement, etc.
Should the moving magnetic field stop, and all the electron-pairs just separated will reunite, electrically nullifying themselves (turning back into bielectrons), and matter will be back at rest. This is the reason why electricity disappears when the magnetic field stops moving or goes off in an electrical generator.

Electricity is a matter-antimatter phenomenon, at the electron level.

## Where antimatter is

In the same way that for the production of electron-pairs, an electron and a positron have to pre-exist in the atom, for antimatter to "appear" in any type of particle collisions, antimatter must pre-exist within the collided particles, in one way or another.
For a person to be able to get milk from the refrigerator, the conditio sine qua non is that there is milk in the refrigerator in the first place. But, if that's not the case we cannot expect that the cabbage or the carrots we have there will transform into milk for us.
Antimatter has to pre-exist to be able to appear in a collision of particles. We are not creating antimatter; antimatter is there, intermingled with matter. Particle collisions do not "produce" antimatter; they separate antimatter from the particles of which it is part.
Too many types of particle collisions can generate antimatter particles, as it has been profusely established in the big particle accelerators around the world. It has been recently discovered at NASA that thunderstorms "create" antimatter in the form of positron jets expelled to space through the atmosphere. Even photon-photon collisions release quarks and antiquarks, which are fundamental particles with no known constituents, showing that antimatter is everywhere, as an intrinsic component of physical matter.
Now, in the same way as the electron can coexist with its antimatter particle, the positron, in a bonded state, any other particle in existence must be able to coexist with its antimatter counterpart, either in a bonded state, like in the proposed bielectron, or intermingled with matter, forming other particles.
For this to happen, a large force has to be at play, a force of attraction that does not allow matter particles to separate from antimatter particles.

But, why wouldn't they explode then, releasing a vast amount of energy as predicted for matter-antimatter encounters? They did, and they released that vast amount of energy, at the beginning, when matter first formed. In a matter-antimatter encounter, while the initial reaction converts $100 \%$ of mass into energy, a big portion of it immediately recombines to form matter particles. It is there where matter and antimatter unite to form ordinary matter. Separation is the anomaly, not the rule.
There must have been a primordial-matter or seed-matter, wherever it came from, from where both, matter and antimatter emanated, just prior to the big-bang. Matter and antimatter then joined together in a monumental release of energy, very probably, the cause of the big-bang itself. It was from the subsequent recombination that physical matter came into existence.
The amount of energy required to separate matter and antimatter must be proportional to the amount of energy released initially to form the bonding, as discussed above. This is the reason why it takes so much energy to separate antimatter from ordinary matter. And later on, when matter and antimatter reunite, they must release back the same amount of energy required to separate the particles.
SHOULD THERE BE ANOTHER FORCE IN PHYSICS: THE FORCE OF ATTRACTION BETWEEN MATTER AND ANTIMATTER? It would be the force that keeps particles of matter and antimatter together. In electromagnetism, it manifests as the magnetic attraction among electrons and positrons; but on a larger scale, with all those particles vastly larger than the electron, could it also be the carrier particle of electromagnetism, the photon?
It might be, or might not be. For now, what matters is that we now know it is there. As such, it must be the strongest of all forces, since it keeps half the matter of the observable universe coupled to the other half in a very strong way.
All that has been said here should be relatively easy to prove in Physics. If we can demonstrate the new theory of electricity to start with, we are demonstrating, by extension, that antimatter is an intrinsic constituent of matter. So, where is all the antimatter?
Antimatter is there, as an intrinsic constituent of all the matter in the universe. Antimatter did not go anywhere after the big-bang, it did not disappear; it has been there all along, all of it, as an intrinsic component of ordinary matter."
Last review, June 7, 2013. (Ref. 1)
*Note of the authors.
The possibility of matter and antimatter particles coexisting in ordinary matter is central to the theories presented here. Too many types of particles collisions result in the "production" of antimatter particles for us to be able to ignore that antimatter can certainly be an intrinsic component of ordinary matter.
While matter-antimatter encounters first explode releasing a vast amount of energy, this energy not just dissipates, it immediately recombines into other particles containing matter and antimatter particles!
This has been beautifully described in The Particle Adventure from Particle Data Group, Lawrence Berkeley National Laboratory, as follows:
"In the collision of an electron and a positron at high energy, they first annihilate in a tremendous bust of energy, in the form of a photon or a Z particle, both of which may be virtual force carrier particles; then a charm quark and a charm antiquark emerge from the virtual force carrier particle; these quark and antiquark begin moving apart stretching the color force field (a gluon field for the case); the quarks move apart, further spreading their force field; the energy in the force field increases with the separation between the quarks. When there is sufficient energy in the force field, the energy is converted into a quark and an anti-quark, according to $\mathrm{E}=\mathrm{mc}^{2}$; the quarks separate into distinct, color-neutral particles: the $\mathrm{D}^{+}$(a charm and anti-down quark) and $\mathrm{D}^{-}$(an anticharm and down quark) mesons".
Quarks and antiquarks, as fundamental particles as they seem to be, cannot have a separate existence and quickly recombine to form other particles, as described above, where matter and antimatter coexist.


Fig. 4 - Collision of an electron and a positron at high energy. Note that while the initial encounter converts the whole electrons' masses into pure energy, the ultimate particles formed from of the collision have both antimatter components! From: The Particle Adventure, Particle Data Group, Lawrence Berkeley National Laboratory.
Similarly, "when a quark (from within a proton) and an antiquark (from an antiproton) collide a high energy, they annihilate into a tremendous burst of energy to form virtual gluons; a top and an antitop quark emerge from the gluon cloud; these quarks begin moving apart, stretching the color force field (gluon field) between them; before the top quark and the antiquark have moved very far, they decay into a bottom and antibottom quark (respectively) with the emission of W force carrier particles; the new bottom quark and antibottom quark rebound away from the emitted W force carrier particles; an electron and neutrino emerge from the virtual $\mathrm{W}^{-}$ boson, and an up quark and down antiquark emerge from the virtual $\mathrm{W}^{+}$boson; the bottom quark and bottom antiquark, electron, neutrino, up quark, and down antiquark all move away from one another", just to form new particles made of matter and antimatter as described above for the collision of an electron and a positron.
Matter and antimatter collisions convert $100 \%$ of the mass of the particles into energy but it does not remain in that state; a big portion of it, if not all, immediately recombines to form new particles in which matter and antimatter are intrinsic components!
If it happened that the existence of matter and antimatter preceded the Big-Bang as proposed in "Where did all the antimatter go?", referred above, it seems very probable that their mutual encounter was actually the cause of the monumental explosion that gave birth to the physical universe as we know it today, where now matter and antimatter have a pacific coexistence.
Now, what forces are involved in the joining of matter and antimatter particles to form ordinary matter? Those forces can perfectly be the $\mathrm{W}^{+}, \mathrm{W}^{-}, \mathrm{Z}^{0}$, the photon and gluon that we know of today, or even the theoretical Graviton, but it could also be a new force of which we do not know yet.
In the paper we explore the possibility of a new force in physics, the force of attraction between matter and antimatter particles which would bind them together in a very strong way, such, that it keeps half of the matter in the observable universe coupled to the other half, the antimatter.

## 3. POSTULATES FOR EVALUATION

(1) Antimatter as an integral part of the electromagnetic phenomena.
(2) Electricity consists of the flow of electrons and positrons in opposite directions along a conductor (not only of electrons, as current accepted knowledge describes), induced by the crossing of a magnetic field through the conductor.
(3) When a charged particle passes through matter at rest it will cause the production of electron pairs, that is, electrons and positrons, but if nothing separates them by force, they will reunite after the passing of the charged particle, nullifying each other, and the atoms of matter will be back at rest.
(4) In order to preserve the law of conservation of energy, the amount of energy required to break free the electron and the positron from a bielectron (a theoretical dual particle containing an electron and a positron) must be equal to the amount of energy released by a matter-antimatter encounter of the same particles.
(5) When a conductor is at rest all the bielectrons are located at their respective orbits in the conductor's atoms, generating no electric charge.
(6) When a conductor is placed under a moving magnetic field, its otherwise stable bielectrons will break apart into electrons and positrons, which will flow in opposite directions along the conductor. At the closing of the circuit (shown here as a closed loop), electrons and positrons, attracted to each other by their opposite charge, reunite into bielectrons, releasing an equal amount of energy as initially required to separate them.
(7) Matter gormandizes antimatter (Antimatter has to pre-exist to be able to appear in a collision of particles. We are not creating antimatter; antimatter is there, intermingled with matter. Particle collisions do not "produce" antimatter; they separate antimatter from the particles of which it is part).
(8) We assume that should there be another force in physics: the force of attraction between matter and antimatter and give a model. We shall call it Bundeswehr (German for "Federal Defense"). So Bundeswehr binds matter and antimatter.
(9) At the closing of the circuit the free electrons and positrons, pushed forward by their own "pressure", are irresistibly pulled by the attraction of their antimatter counterpart. It is this process of mutual attraction and continuous reunification into bielectrons which causes the flow of electrons and positrons along the conductors.

## 4. NOTATION

## Module One

$G_{13}$ : Category one of electromagnetic phenomena (Characteristics of the universal investigating systems are taken into consideration in the classification processual formalities and procedural regularities. Kindly refer detailed study in the introduction)
$G_{14}$ : Category two of electromagnetic phenomena
$G_{15}$ : Category three of electromagnetic phenomena
$T_{13}$ : Category one of Antimatter Based on the observable universe and other universes
$T_{14}$ : Category two of Antimatter
$T_{15}$ : Category three of Antimatter

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Module Two
\(G_{16}\) : Category one of crossing of a magnetic field through the conductor(there are many systems investigatable)
\(G_{17}\) : Category two of crossing of a magnetic field through the conductor
\(G_{18}\) : Category three of crossing of a magnetic field through the conductor
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$T_{16}$ : Category one of Electricity consists of the flow of electrons and positrons in opposite directions along a conductor (not only of electrons, as current accepted knowledge describes),
$T_{17}$ : Category two of Electricity consists of the flow of electrons and positrons in opposite directions along a conductor (not only of electrons, as current accepted knowledge describes),
$T_{18}$ : Category three of Electricity consists of the flow of electrons and positrons in opposite directions along a conductor (not only of electrons, as current accepted knowledge describes),

## Module three

$G_{20}$ : Category one of charged particle passes through matter at rest
$G_{21}$ : Category two of charged particle passes through matter at rest
$G_{22}$ : Category three of charged particle passes through matter at rest
$T_{20}$ : Category one of production of electron pairs, that is, electrons and positrons, but if nothing separates them by force, they will reunite after the passing of the charged particle, nullifying each other, and the atoms of matter will be back at rest
$T_{21}$ : Category two of production of electron pairs, that is, electrons and positrons, but if nothing separates them by force, they will reunite after the passing of the charged particle, nullifying each other, and the atoms of matter will be back at rest
$T_{22}$ : Category three of production of electron pairs, that is, electrons and positrons, but if nothing separates them by force, they will reunite after the passing of the charged particle, nullifying each other, and the atoms of matter will be back at rest

## Module four(Conservation of law of energy)

$G_{24}$ : Category one of amount of energy required to break free the electron and the positron from a bielectron (there are lot of systems and classification is based on the systemic characteristics. For details please see introduction).
$G_{25}$ : Category two of amount of energy required to break free the electron and the positron from a bielectron
$G_{26}$ : Category three of amount of energy required to break free the electron and the positron from a bielectron
$T_{24}$ : Category one of amount of energy released by a matter-antimatter encounter of the same particles.
$T_{25}$ : Category two of amount of energy released by a matter-antimatter encounter of the same particles.
$T_{26}$ : Category three of amount of energy released by a matter-antimatter encounter of the same particles.

## Module five

$G_{28}$ : Category one of conductor at rest and all the bielectrons are located at their respective orbits in the conductor's atoms (there are lot of conductors. Classification salient features are given in the introduction and kindly refer to it. This holds good for the entire monograph)
$G_{29}$ : Category two of conductor at rest and all the bielectrons are located at their respective orbits in the conductor's atoms
$G_{30}$ : Category three of conductor at rest and all the bielectrons are located at their respective orbits in the conductor's atoms
$T_{28}$ : Category one of non generation of electric charge concomitant and corresponding to the classification above
$T_{29}$ : Category two of non generation of electric charge concomitant and corresponding to the classification above
$\mathrm{T}_{30}$ : Category three of non generation of electric charge concomitant and corresponding to the classification above

## Module six

$G_{32}$ : Category one of conductor placed under a moving magnetic field, its otherwise stable bielectrons will break apart into electrons and positrons, which will flow in opposite directions along the conductor; at the closing of the circuit (shown here as a closed loop), electrons and positrons, attracted to each other by their opposite charge, reunite into bielectrons
$G_{33}$ : Category two of conductor placed under a moving magnetic field, its otherwise stable bielectrons will break apart into electrons and positrons, which will flow in opposite directions along the conductor; at the closing of the circuit (shown here as a closed loop), electrons and positrons, attracted to each other by their opposite charge, reunite into bielectrons
$G_{34}$ : Category three of conductor placed under a moving magnetic field, its otherwise stable bielectrons will break apart into electrons and positrons, which will flow in opposite directions along the conductor; at the closing of the circuit (shown here as a closed loop), electrons and positrons, attracted to each other by their opposite charge, reunite into bielectrons
$\mathrm{T}_{32}$ : Category one of equal amount of energy as initially required to separate them.
$T_{33}$ : Category two of equal amount of energy as initially required to separate them.
$T_{34}$ : Category three of equal amount of energy as initially required to separate them.

## Module seven

$G_{36}$ : Category one of antimatter
$G_{37}$ : Category two of antimatter
$G_{38}$ : Category three of antimatter
$\mathrm{T}_{36}$ : Category one of Matter
$T_{37}$ : Category two of Matter
$T_{38}$ : Category three of Matter

## Module eight

$G_{40}$ : Category one of Bundeswehr. Note again the classification is based on the characteristics and parametricization of the investigating systems; there is matter and concomitant antimatter in some region of
space and corresponding consummation force that binds
$G_{41}$ : Category two of Bundeswehr
$G_{42}$ : Category three of Bundeswehr
$\mathrm{T}_{40}$ : Category one of matter and antimatter
$T_{41}$ : Category two of matter and antimatter
$T_{42}$ : Category three of matter and antimatter

## Module Nine

$G_{44}$ : Category one of process of mutual attraction and continuous reunification into bielectrons
$G_{45}$ : Category two of process of mutual attraction and continuous reunification into bielectrons
$G_{46}$ : Category three of process of mutual attraction and continuous reunification into bielectrons
$\mathrm{T}_{44}$ : Category one of flow of electrons and positrons along the conductors.
$T_{45}$ : Category two of flow of electrons and positrons along the conductors.
$T_{46}$ : Category three of flow of electrons and positrons along the conductors.

$$
\begin{aligned}
& \left(a_{15}\right)^{(1)}, \quad\left(b_{13}\right)^{(1)},\left(b_{14}\right)^{(1)},\left(b_{15}\right)^{(1)} \quad\left(a_{16}\right)^{(2)},\left(a_{17}\right)^{(2)},\left(a_{18}\right)^{(2)} \quad\left(b_{16}\right)^{(2)},\left(b_{17}\right)^{(2)},\left(b_{18}\right)^{(2)}: \\
& \left(a_{20}\right)^{(3)},\left(a_{21}\right)^{(3)},\left(a_{22}\right)^{(3)},\left(b_{20}\right)^{(3)},\left(b_{21}\right)^{(3)},\left(b_{22}\right)^{(3)} \\
& \left(a_{24}\right)^{(4)},\left(a_{25}\right)^{(4)},\left(a_{26}\right)^{(4)},\left(b_{24}\right)^{(4)},\left(b_{25}\right)^{(4)},\left(b_{26}\right)^{(4)},\left(b_{28}\right)^{(5)},\left(b_{29}\right)^{(5)},\left(b_{30}\right)^{(5)} \\
& \left(a_{28}\right)^{(5)},\left(a_{29}\right)^{(5)},\left(a_{30}\right)^{(5)},\left(a_{32}\right)^{(6)},\left(a_{33}\right)^{(6)},\left(a_{34}\right)^{(6)},\left(b_{32}\right)^{(6)},\left(b_{33}\right)^{(6)},\left(b_{34}\right)^{(6)} \\
& \left(a_{36}\right)^{(7)},\left(a_{37}\right)^{(7)},\left(a_{38}\right)^{(7)},\left(b_{36}\right)^{(7)},\left(b_{37}\right)^{(7)},\left(b_{38}\right)^{(7)} \\
& \left(a_{40}\right)^{(8)},\left(a_{41}\right)^{(8)},\left(a_{42}\right)^{(8)},\left(b_{40}\right)^{(8)},\left(b_{41}\right)^{(8)},\left(b_{42}\right)^{(8)} \\
& \left(a_{44}\right)^{(9)},\left(a_{45}\right)^{(9)},\left(a_{46}\right)^{(9)},\left(b_{44}\right)^{(9)},\left(b_{45}\right)^{(9)},\left(b_{46}\right)^{(9)}
\end{aligned}
$$

are Accentuation coefficients

$$
\begin{aligned}
& \left(a_{13}^{\prime}\right)^{(1)},\left(a_{14}^{\prime}\right)^{(1)},\left(a_{15}^{\prime}\right)^{(1)}, \quad\left(a_{13}^{\prime}\right)^{(1)},\left(b_{14}^{\prime}\right)^{(1)},\left(b_{15}^{\prime}\right)^{(1)},\left(a_{17}^{\prime}\right)^{(2)},\left(a_{18}^{\prime}\right)^{(2)}, \\
& \left(b_{16}^{\prime}\right)^{(2)},\left(b_{17}^{\prime}\right)^{(2)},\left(b_{18}^{\prime}\right)^{(2)} \quad,\left(a_{20}^{\prime}\right)^{(3)},\left(a_{21}^{\prime}\right)^{(3)},\left(a_{22}^{\prime}\right)^{(3)},\left(b_{20}^{\prime}\right)^{(3)},\left(b_{21}^{\prime}\right)^{(3)},\left(b_{22}^{\prime}\right)^{(3)} \\
& \left(a_{24}^{\prime}\right)^{(4)},\left(a_{25}^{\prime}\right)^{(4)},\left(a_{26}^{\prime}\right)^{(4)},\left(b_{24}^{\prime}\right)^{(4)},\left(b_{25}^{\prime}\right)^{(4)},\left(b_{26}^{\prime}\right)^{(4)},\left(b_{28}^{\prime}\right)^{(5)},\left(b_{29}^{\prime}\right)^{(5)},\left(b_{30}^{\prime}\right)^{(5)} \\
& \left(a_{28}^{\prime}\right)^{(5)},\left(a_{29}^{\prime}\right)^{(5)},\left(a_{30}^{\prime}\right)^{(5)},\left(a_{32}^{\prime}\right)^{(6)},\left(a_{33}^{\prime}\right)^{(6)},\left(a_{34}^{\prime}\right)^{(6)},\left(b_{32}^{\prime}\right)^{(6)},\left(b_{33}^{\prime}\right)^{(6)},\left(b_{34}^{\prime}\right)^{(6)} \\
& \left(a_{36}^{\prime}\right)^{(7)},\left(a_{37}^{\prime}\right)^{(7)},\left(a_{38}^{\prime}\right)^{(7)},\left(b_{36}^{\prime}\right)^{(7)},\left(b_{37}^{\prime}\right)^{(7)},\left(b_{38}^{\prime}\right)^{(7)}, \\
& \left(a_{40}^{\prime}\right)^{(8)},\left(a_{41}^{\prime}\right)^{(8)},\left(a_{42}^{\prime}\right)^{(8)},\left(b_{40}^{\prime}\right)^{(8)},\left(b_{41}^{\prime}\right)^{(8)},\left(b_{42}^{\prime}\right)^{(8)}, \\
& \left(a_{44}^{\prime}\right)^{(9)},\left(a_{45}^{\prime}\right)^{(9)},\left(a_{46}^{\prime}\right)^{(9)},\left(b_{44}^{\prime}\right)^{(9)},\left(b_{45}^{\prime}\right)^{(9)},\left(b_{46}^{\prime}\right)^{(9)},
\end{aligned}
$$

are Dissipation coefficients

## Module Numbered One

The differential system of this model is now (Module Numbered one)

$$
\begin{aligned}
& \frac{d G_{13}}{d t}=\left(a_{13}\right)^{(1)} G_{14}-\left[\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)\right] G_{13} \\
& \frac{d G_{14}}{d t}=\left(a_{14}\right)^{(1)} G_{13}-\left[\left(a_{14}^{\prime}\right)^{(1)}+\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)\right] G_{14} \\
& \frac{d G_{15}}{d t}=\left(a_{15}\right)^{(1)} G_{14}-\left[\left(a_{15}^{\prime}\right)^{(1)}+\left(a_{15}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)\right] G_{15}
\end{aligned}
$$

$\frac{d T_{13}}{d t}=\left(b_{13}\right)^{(1)} T_{14}-\left[\left(b_{13}^{\prime}\right)^{(1)}-\left(b_{13}^{\prime \prime}\right)^{(1)}(G, t)\right] T_{13}$
$\frac{d T_{14}}{d t}=\left(b_{14}\right)^{(1)} T_{13}-\left[\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{14}^{\prime \prime}\right)^{(1)}(G, t)\right] T_{14}$
$\frac{d T_{15}}{d t}=\left(b_{15}\right)^{(1)} T_{14}-\left[\left(b_{15}^{\prime}\right)^{(1)}-\left(b_{15}^{\prime \prime}\right)^{(1)}(G, t)\right] T_{15}$
$+\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)=$ First augmentation factor
$-\left(b_{13}^{\prime \prime}\right)^{(1)}(G, t)=$ First detritions factor

## Module Numbered Two

The differential system of this model is now (Module numbered two)
$\frac{d G_{16}}{d t}=\left(a_{16}\right)^{(2)} G_{17}-\left[\left(a_{16}^{\prime}\right)^{(2)}+\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)\right] G_{16}$
$\frac{d G_{17}}{d t}=\left(a_{17}\right)^{(2)} G_{16}-\left[\left(a_{17}^{\prime}\right)^{(2)}+\left(a_{17}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)\right] G_{17}$
$\frac{d G_{18}}{d t}=\left(a_{18}\right)^{(2)} G_{17}-\left[\left(a_{18}^{\prime}\right)^{(2)}+\left(a_{18}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)\right] G_{18}$
$\frac{d T_{16}}{d t}=\left(b_{16}\right)^{(2)} T_{17}-\left[\left(b_{16}^{\prime}\right)^{(2)}-\left(b_{16}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right)\right] T_{16}$
$\frac{d T_{17}}{d t}=\left(b_{17}\right)^{(2)} T_{16}-\left[\left(b_{17}^{\prime}\right)^{(2)}-\left(b_{17}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right)\right] T_{17}$
$\frac{d T_{18}}{d t}=\left(b_{18}\right)^{(2)} T_{17}-\left[\left(b_{18}^{\prime}\right)^{(2)}-\left(b_{18}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right)\right] T_{18}$
$+\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)=$ First augmentation factor
$-\left(b_{16}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right)=$ First detritions factor

## Module Numbered Three

The differential system of this model is now (Module numbered three)
$\frac{d G_{20}}{d t}=\left(a_{20}\right)^{(3)} G_{21}-\left[\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)\right] G_{20}$
$\frac{d G_{21}}{d t}=\left(a_{21}\right)^{(3)} G_{20}-\left[\left(a_{21}^{\prime}\right)^{(3)}+\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)\right] G_{21}$
$\frac{d G_{22}}{d t}=\left(a_{22}\right)^{(3)} G_{21}-\left[\left(a_{22}^{\prime}\right)^{(3)}+\left(a_{22}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)\right] G_{22}$
$\frac{d T_{20}}{d t}=\left(b_{20}\right)^{(3)} T_{21}-\left[\left(b_{20}^{\prime}\right)^{(3)}-\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right)\right] T_{20}$
$\frac{d T_{21}}{d t}=\left(b_{21}\right)^{(3)} T_{20}-\left[\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{21}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right)\right] T_{21}$
$\frac{d T_{22}}{d t}=\left(b_{22}\right)^{(3)} T_{21}-\left[\left(b_{22}^{\prime}\right)^{(3)}-\left(b_{22}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right)\right] T_{22}$
$+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)=$ First augmentation factor
$-\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right)=$ First detritions factor

## Module Numbered Four

The differential system of this model is now (Module numbered Four)
$\frac{d G_{24}}{d t}=\left(a_{24}\right)^{(4)} G_{25}-\left[\left(a_{24}^{\prime}\right)^{(4)}+\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)\right] G_{24}$
$\frac{d G_{25}}{d t}=\left(a_{25}\right)^{(4)} G_{24}-\left[\left(a_{25}^{\prime}\right)^{(4)}+\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)\right] G_{25}$
$\frac{d G_{26}}{d t}=\left(a_{26}\right)^{(4)} G_{25}-\left[\left(a_{26}^{\prime}\right)^{(4)}+\left(a_{26}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)\right] G_{26}$
$\frac{d T_{24}}{d t}=\left(b_{24}\right)^{(4)} T_{25}-\left[\left(b_{24}^{\prime}\right)^{(4)}-\left(b_{24}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right)\right] T_{24}$
$\frac{d T_{25}}{d t}=\left(b_{25}\right)^{(4)} T_{24}-\left[\left(b_{25}^{\prime}\right)^{(4)}-\left(b_{25}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right)\right] T_{25}$
$\frac{d T_{26}}{d t}=\left(b_{26}\right)^{(4)} T_{25}-\left[\left(b_{26}^{\prime}\right)^{(4)}-\left(b_{26}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right)\right] T_{26}$
$+\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)=$ First augmentation factor
$-\left(b_{24}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right)=$ First detritions factor

## Module Numbered Five:

The differential system of this model is now (Module number five)
$\frac{d G_{28}}{d t}=\left(a_{28}\right)^{(5)} G_{29}-\left[\left(a_{28}^{\prime}\right)^{(5)}+\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)\right] G_{28}$
$\frac{d G_{29}}{d t}=\left(a_{29}\right)^{(5)} G_{28}-\left[\left(a_{29}^{\prime}\right)^{(5)}+\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)\right] G_{29}$
$\frac{d G_{30}}{d t}=\left(a_{30}\right)^{(5)} G_{29}-\left[\left(a_{30}^{\prime}\right)^{(5)}+\left(a_{30}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)\right] G_{30}$
$\frac{d T_{28}}{d t}=\left(b_{28}\right)^{(5)} T_{29}-\left[\left(b_{28}^{\prime}\right)^{(5)}-\left(b_{28}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right)\right] T_{28}$
$\frac{d T_{29}}{d t}=\left(b_{29}\right)^{(5)} T_{28}-\left[\left(b_{29}^{\prime}\right)^{(5)}-\left(b_{29}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right)\right] T_{29}$
$\frac{d T_{30}}{d t}=\left(b_{30}\right)^{(5)} T_{29}-\left[\left(b_{30}^{\prime}\right)^{(5)}-\left(b_{30}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right)\right] T_{30}$
$+\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)=$ First augmentation factor
$-\left(b_{28}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right)=$ First detritions factor

## Module Numbered Six

The differential system of this model is now (Module numbered Six)
$\frac{d G_{32}}{d t}=\left(a_{32}\right)^{(6)} G_{33}-\left[\left(a_{32}^{\prime}\right)^{(6)}+\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)\right] G_{32}$
$\frac{d G_{33}}{d t}=\left(a_{33}\right)^{(6)} G_{32}-\left[\left(a_{33}^{\prime}\right)^{(6)}+\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)\right] G_{33}$
$\frac{d G_{34}}{d t}=\left(a_{34}\right)^{(6)} G_{33}-\left[\left(a_{34}^{\prime}\right)^{(6)}+\left(a_{34}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)\right] G_{34}$
$\frac{d T_{32}}{d t}=\left(b_{32}\right)^{(6)} T_{33}-\left[\left(b_{32}^{\prime}\right)^{(6)}-\left(b_{32}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right)\right] T_{32}$
$\frac{d T_{33}}{d t}=\left(b_{33}\right)^{(6)} T_{32}-\left[\left(b_{33}^{\prime}\right)^{(6)}-\left(b_{33}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right)\right] T_{33}$
$\frac{d T_{34}}{d t}=\left(b_{34}\right)^{(6)} T_{33}-\left[\left(b_{34}^{\prime}\right)^{(6)}-\left(b_{34}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right)\right] T_{34}$
$+\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)=$ First augmentation factor

## Module Numbered Seven:

The differential system of this model is now (SEVENTH MODULE)
$\frac{d G_{36}}{d t}=\left(a_{36}\right)^{(7)} G_{37}-\left[\left(a_{36}^{\prime}\right)^{(7)}+\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)\right] G_{36}$
$\frac{d G_{37}}{d t}=\left(a_{37}\right)^{(7)} G_{36}-\left[\left(a_{37}^{\prime}\right)^{(7)}+\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)\right] G_{37}$
$\frac{d G_{38}}{d t}=\left(a_{38}\right)^{(7)} G_{37}-\left[\left(a_{38}^{\prime}\right)^{(7)}+\left(a_{38}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)\right] G_{38}$
$\frac{d T_{36}}{d t}=\left(b_{36}\right)^{(7)} T_{37}-\left[\left(b_{36}^{\prime}\right)^{(7)}-\left(b_{36}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right), t\right)\right] T_{36}$
$\frac{d T_{37}}{d t}=\left(b_{37}\right)^{(7)} T_{36}-\left[\left(b_{37}^{\prime}\right)^{(7)}-\left(b_{37}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right), t\right)\right] T_{37}$
$+\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)=$ First augmentation factor

## Module Numbered Eight GOVERNING EQUATIONS:

The differential system of this model is now
$\frac{d G_{40}}{d t}=\left(a_{40}\right)^{(8)} G_{41}-\left[\left(a_{40}^{\prime}\right)^{(8)}+\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)\right] G_{40}$
$\frac{d G_{41}}{d t}=\left(a_{41}\right)^{(8)} G_{40}-\left[\left(a_{41}^{\prime}\right)^{(8)}+\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)\right] G_{41}$
$\frac{d G_{42}}{d t}=\left(a_{42}\right)^{(8)} G_{41}-\left[\left(a_{42}^{\prime}\right)^{(8)}+\left(a_{42}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)\right] G_{42}$
$\frac{d T_{40}}{d t}=\left(b_{40}\right)^{(8)} T_{41}-\left[\left(b_{40}^{\prime}\right)^{(8)}-\left(b_{40}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right)\right] T_{40}$
$\frac{d T_{41}}{d t}=\left(b_{41}\right)^{(8)} T_{40}-\left[\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{41}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right)\right] T_{41}$
$\frac{d T_{42}}{d t}=\left(b_{42}\right)^{(8)} T_{41}-\left[\left(b_{42}^{\prime}\right)^{(8)}-\left(b_{42}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right)\right] T_{42}$

## Module Numbered Nine

## GOVERNING EQUATIONS:

The differential system of this model is now
$\frac{d G_{44}}{d t}=\left(a_{44}\right)^{(9)} G_{45}-\left[\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)\right] G_{44}$
$\frac{d G_{45}}{d t}=\left(a_{45}\right)^{(9)} G_{44}-\left[\left(a_{45}^{\prime}\right)^{(9)}+\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)\right] G_{45}$
$\frac{d G_{46}}{d t}=\left(a_{46}\right)^{(9)} G_{45}-\left[\left(a_{46}^{\prime}\right)^{(9)}+\left(a_{46}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)\right] G_{46}$
$\frac{d T_{44}}{d t}=\left(b_{44}\right)^{(9)} T_{45}-\left[\left(b_{44}^{\prime}\right)^{(9)}-\left(b_{44}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right), t\right)\right] T_{44}$
$\frac{d T_{45}}{d t}=\left(b_{45}\right)^{(9)} T_{44}-\left[\left(b_{45}^{\prime}\right)^{(9)}-\left(b_{45}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right), t\right)\right] T_{45}$
$\frac{d T_{46}}{d t}=\left(b_{46}\right)^{(9)} T_{45}-\left[\left(b_{46}^{\prime}\right)^{(9)}-\left(b_{46}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right), t\right)\right] T_{46}$
$+\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)=$ First augmentation factor $-\left(b_{44}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right), t\right)=$ First detritions factor

$$
\frac{d G_{13}}{d t}=\left(a_{13}\right)^{(1)} G_{14}-\left[\begin{array}{c}
\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)+\left(a_{16}^{\prime \prime}\right)^{(2,2,)}\left(T_{17}, t\right)+\left(a_{20}^{\prime \prime}\right)^{(3,3)}\left(T_{21}, t\right) \\
+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,)}\left(T_{25}, t\right)+\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,)}\left(T_{29}, t\right)+\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,)}\left(T_{33}, t\right) \\
+\left(a_{36}^{\prime \prime}\right)^{(7,7)}\left(T_{37}, t\right)+\left(a_{40}^{\prime \prime}\right)^{(8,8)}\left(T_{41}, t\right)+\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)
\end{array}\right] G_{13}
$$

$\frac{d G_{14}}{d t}=\left(a_{14}\right)^{(1)} G_{13}-\left[\begin{array}{c|c|}\left(a_{14}^{\prime}\right)^{(1)}+\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right) & +\left(a_{17}^{\prime \prime}\right)^{(2,2,)}\left(T_{17}, t\right) \\ +\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(a_{21}^{\prime \prime}\right)^{(3,3,)}\left(T_{21}, t\right) \\ +\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,)}\left(T_{33}, t\right) \\ +\left(a_{37}^{\prime \prime}\right)^{(7,7)}\left(T_{37}, t\right) & +\left(a_{41}^{\prime \prime}\right)^{(8,8)}\left(T_{41}, t\right)+\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)\end{array}\right] G_{14}$
$\frac{d G_{15}}{d t}=\left(a_{15}\right)^{(1)} G_{14}-\left[\begin{array}{l}\left(a_{15}^{\prime}\right)^{(1)}+\left(a_{15}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)+\left(a_{18}^{\prime \prime}\right)^{(2,2,)}\left(T_{17}, t\right)+\left(a_{22}^{\prime \prime}\right)^{(3,3,)}\left(T_{21}, t\right) \\ +\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(T_{25}, t\right)+\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,)}\left(T_{29}, t\right)+\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6}\left(T_{33}, t\right) \\ +\left(a_{38}^{\prime \prime}\right)^{(7,7)}\left(T_{37}, t\right)+\left(a_{42}^{\prime \prime}\right)^{(8,8)}\left(T_{41}, t\right)+\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)\end{array}\right] G_{15}$
Where $\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right),\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right),\left(a_{15}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)$ are first augmentation coefficients for category 1,2 and 3
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2,2,)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2,2,)}\left(T_{17}, t\right)$ are second augmentation coefficient for category 1,2 and 3
$+\left(a_{20}^{\prime \prime}\right)^{(3,3,)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3,3,)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3,3,)}\left(T_{21}, t\right)$ are third augmentation coefficient for category 1,2 and 3
$+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,)}\left(T_{25}, t\right),+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,)}\left(T_{25}, t\right)$ are fourth augmentation coefficient for category 1,2 and 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,)}\left(T_{29}, t\right)$ are fifth augmentation coefficient for category 1,2 and 3
$+\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,)}\left(T_{33}, t\right)$ are sixth augmentation coefficient for category 1,2 and 3
$+\left(a_{38}^{\prime \prime}\right)^{(7,7)}\left(T_{37}, t\right)+\left(a_{37}^{\prime \prime}\right)^{(7,7)}\left(T_{37}, t\right)+\left(a_{36}^{\prime \prime}\right)^{(7,7)}\left(T_{37}, t\right)$ are seventh augmentation coefficient for 1,2,3
$+\left(a_{40}^{\prime \prime}\right)^{(8,8)}\left(T_{41}, t\right)+\left(a_{41}^{\prime \prime}\right)^{(8,8)}\left(T_{41}, t\right)+\left(a_{42}^{\prime \prime}\right)^{(8,8)}\left(T_{41}, t\right)$ are eight augmentation coefficient for $1,2,3$ $+\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right),+\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)$ are ninth augmentation coefficient for $1,2,3$
$\frac{d T_{13}}{d t}=\left(b_{13}\right)^{(1)} T_{14}-\left[\begin{array}{cc}\left(b_{13}^{\prime}\right)^{(1)}-\left(b_{13}^{\prime \prime}\right)^{(1)}(G, t) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,)}\left(G_{19}, t\right) \\ -\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,)}\left(G_{27}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(3,5,5,5,5,)}\left(G_{31}, t\right) \\ -\left(b_{23}^{\prime \prime}, t\right) \\ -(6,6,6,6,) \\ \hline & \\ -\left(b_{36}^{\prime \prime}\right)^{(7,7,)}\left(G_{39}, t\right) & -\left(b_{40}^{\prime \prime}\right)^{(8,8)}\left(G_{43}, t\right) \\ \hline-\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{13}$
$\frac{d T_{14}}{d t}=\left(b_{14}\right)^{(1)} T_{13}-\left[\begin{array}{ccc|}\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{14}^{\prime \prime}\right)^{(1)}(G, t) & -\left(b_{17}^{\prime \prime}\right)^{(2,2,)}\left(G_{19}, t\right) & -\left(b_{21}^{\prime \prime}\right)^{(3,3,)}\left(G_{23}, t\right) \\ -\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,)}\left(G_{27}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,)}\left(G_{31}, t\right) & -\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{37}^{\prime \prime}\right)^{(7,7,)}\left(G_{39}, t\right) & -\left(b_{41}^{\prime \prime}\right)^{(8,8)}\left(G_{43}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{14}$
$\frac{d T_{15}}{d t}=\left(b_{15}\right)^{(1)} T_{14}-\left[\begin{array}{c|c|c|}\left(b_{15}^{\prime}\right)^{(1)}-\left(b_{15}^{\prime \prime}\right)^{(1)}(G, t) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,)}\left(G_{19}, t\right) & -\left(b_{22}^{\prime \prime}\right)^{(3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4}\left(G_{27}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,)}\left(G_{31}, t\right) & -\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,9}\left(G_{35}, t\right) \\ -\left(b_{38}^{\prime \prime}\right)^{(7,7,)}\left(G_{39}, t\right) & -\left(b_{42}^{\prime \prime}\right)^{(8,8)}\left(G_{43}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{15}$
Where $-\left(b_{13}^{\prime \prime}\right)^{(1)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1)}(G, t),-\left(b_{15}^{\prime \prime}\right)^{(1)}(G, t)$ are first detrition coefficients for category 1 , 2 and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,)}\left(G_{19}, t\right),-\left(b_{17}^{\prime \prime}\right)^{(2,2,)}\left(G_{19}, t\right),-\left(b_{18}^{\prime \prime}\right)^{(2,2,)}\left(G_{19}, t\right)$ are second detrition coefficients for category 1,2 and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3)}\left(G_{23}, t\right)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,)}\left(G_{27}, t\right)$ are fourth detrition coefficients for category 1,2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,)}\left(G_{31}, t\right)$ are fifth detrition coefficients for category 1,2 and 3
$-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(G_{35}, t\right)$ are sixth detrition coefficients for category 1,2 and 3
$-\left(b_{37}^{\prime \prime}\right)^{(7,7,)}\left(G_{39}, t\right),-\left(b_{36}^{\prime \prime}\right)^{(7,7,)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7,7,)}\left(G_{39}, t\right)$ are seventh detrition coefficients for category 1,2 and 3
$-\left(b_{40}^{\prime \prime}\right)^{(8,8)}\left(G_{43}, t\right)-\left(b_{41}^{\prime \prime}\right)^{(8,8)}\left(G_{43}, t\right)-\left(b_{42}^{\prime \prime}\right)^{(8,8)}\left(G_{43}, t\right)$ are eight detrition coefficients for category 1,2 and 3
$-\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)$ are ninth
detrition coefficients for category 1,2 and 3
$\frac{d G_{16}}{d t}=\left(a_{16}\right)^{(2)} G_{17}-\left[\begin{array}{c|c|c}\left(a_{16}^{\prime}\right)^{(2)}+\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right) & +\left(a_{13}^{\prime \prime}\right)^{(1,1)}\left(T_{14}, t\right) & +\left(a_{20}^{\prime \prime}\right)^{(3,3,3)}\left(T_{21}, t\right) \\ \hline+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(T_{33}, t\right) \\ \hdashline+\left(a_{36}^{\prime \prime}\right)^{(7,7,7)}\left(T_{37}, t\right) & +\left(a_{40}^{\prime \prime}\right)^{(8,8,8)}\left(T_{41}, t\right) & +\left(a_{44}^{\prime \prime}\right)^{(9,9)}\left(T_{45}, t\right)\end{array}\right] G_{16}$
$\frac{d G_{17}}{d t}=\left(a_{17}\right)^{(2)} G_{16}-\left[\begin{array}{ccc|c}\left(a_{17}^{\prime}\right)^{(2)}+\left(a_{17}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right) & +\left(a_{14}^{\prime \prime}\right)^{(1,1,)}\left(T_{14}, t\right) & +\left(a_{21}^{\prime \prime}\right)^{(3,3,3)}\left(T_{21}, t\right) \\ +\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(T_{33}, t\right) \\ \hdashline+\left(a_{37}^{\prime \prime}\right)^{(7,7,7)}\left(T_{37}, t\right) & +\left(a_{41}^{\prime \prime}\right)^{(8,8,8)}\left(T_{41}, t\right) & +\left(a_{45}^{\prime \prime}\right)^{(9,9)}\left(T_{45}, t\right)\end{array}\right] G_{17}$
$\frac{d G_{18}}{d t}=\left(a_{18}\right)^{(2)} G_{17}-\left[\begin{array}{cc|c}\left(a_{18}^{\prime}\right)^{(2)}+\left(a_{18}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right) & +\left(a_{15}^{\prime \prime}\right)^{(1,1)}\left(T_{14}, t\right) & +\left(a_{22}^{\prime \prime}\right)^{(3,3,3)}\left(T_{21}, t\right) \\ +\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(T_{33}, t\right) \\ \hdashline+\left(a_{38}^{\prime \prime}\right)^{(7,7,7)}\left(T_{37}, t\right) & +\left(a_{42}^{\prime \prime}\right)^{(8,8,8)}\left(T_{41}, t\right) & +\left(a_{46}^{\prime \prime}\right)^{(9,9)}\left(T_{45}, t\right)\end{array}\right] G_{18}$
Where $+\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)$ are first augmentation coefficients for category 1, 2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1)}\left(T_{14}, t\right),+\left(a_{14}^{\prime \prime}\right)^{(1,1,)}\left(T_{14}, t\right),+\left(a_{15}^{\prime \prime}\right)^{(1,1,)}\left(T_{14}, t\right)$ are second augmentation coefficient for category 1,2 and 3
$+\left(a_{20}^{\prime \prime}\right)^{(3,3,3)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3,3,3)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3,3,3)}\left(T_{21}, t\right)$ are third augmentation coefficient for category 1,2 and 3
$+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(T_{25}, t\right)$ are fourth augmentation coefficient for category 1,2 and 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(T_{29}, t\right)$ are fifth augmentation coefficient for category 1,2 and 3
$+\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(T_{33}, t\right)$ are sixth augmentation coefficient for category 1,2 and 3
$+\left(a_{36}^{\prime \prime}\right)^{(7,7,7)}\left(T_{37}, t\right),+\left(a_{37}^{\prime \prime}\right)^{(7,7,7)}\left(T_{37}, t\right),+\left(a_{38}^{\prime \prime}\right)^{(7,7,7)}\left(T_{37}, t\right)$ are seventh augmentation coefficient for category 1,2 and 3
$+\left(a_{40}^{\prime \prime}\right)^{(8,8,8)}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8,8,8)}\left(T_{41}, t\right),+\left(a_{42}^{\prime \prime}\right)^{(8,8,8)}\left(T_{41}, t\right)$ are eight augmentation coefficient for category 1,2 and 3
$+\left(a_{44}^{\prime \prime}\right)^{(9,9)}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9,9)}\left(T_{45}, t\right),+\left(a_{46}^{\prime \prime}\right)^{(9,9)}\left(T_{45}, t\right)$ are ninth augmentation coefficient for category 1, 2 and 3
$\frac{d T_{16}}{d t}=\left(b_{16}\right)^{(2)} T_{17}-\left[\begin{array}{c|c|c|}\left(b_{16}^{\prime}\right)^{(2)} & -\left(b_{16}^{\prime \prime}\right)^{(2)}\left(G_{19}, t\right) & -\left(b_{13}^{\prime \prime}\right)^{(1,1,)}(G, t) \\ \hline-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(G_{27}^{\prime \prime}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(G_{23}, t\right) \\ \hline-\left(b_{36}^{\prime \prime}\right)^{(7,7,7)}\left(G_{39}, t\right) & -\left(b_{40}^{\prime \prime}\right)^{(8,8,8)}\left(G_{43}, t\right) & -\left(b_{44}^{\prime \prime}\right)^{(9,9)}\left(G_{47}, t\right)\end{array}\right] T_{16}$
$\frac{d T_{17}}{d t}=\left(b_{17}\right)^{(2)} T_{16}-\left[\begin{array}{c|c|c}\left(b_{17}^{\prime}\right)^{(2)} & -\left(b_{17}^{\prime \prime}\right)^{(2)}\left(G_{19}, t\right) & -\left(b_{14}^{\prime \prime}\right)^{(1,1)}(G, t) \\ \hline-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{33}^{\prime \prime}\right)^{(6,3,3,6,6,6,6)}\left(G_{23}, t\right) \\ \hline-\left(G_{35}^{\prime \prime}, t\right) \\ \hline-\left(b_{37}\right)^{(7,7,7)}\left(G_{39}, t\right) & -\left(b_{41}^{\prime \prime}\right)^{(8,8,8)}\left(G_{43}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9)}\left(G_{47}, t\right)\end{array}\right] T_{17}$
$\frac{d T_{18}}{d t}=\left(b_{18}\right)^{(2)} T_{17}-\left[\begin{array}{c|c|c|c}\left(b_{18}^{\prime}\right)^{(2)} & -\left(b_{18}^{\prime \prime}\right)^{(2)}\left(G_{19}, t\right) & -\left(b_{15}^{\prime \prime}\right)^{(1,1,)}(G, t) & -\left(b_{22}^{\prime \prime}\right)^{(3,3,3,)}\left(G_{23}, t\right) \\ \hline-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(G_{35}, t\right) \\ \hline-\left(b_{38}^{\prime \prime}\right)^{(7,7,7)}\left(G_{39}, t\right) & -\left(b_{42}^{\prime \prime}\right)^{(8,8,8)}\left(G_{43}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9)}\left(G_{47}, t\right)\end{array}\right] T_{18}$
where $-\left(\mathrm{b}_{16}^{\prime \prime}\right)^{(2)}\left(\mathrm{G}_{19}, \mathrm{t}\right),-\left(\mathrm{b}_{17}^{\prime \prime}\right)^{(2)}\left(\mathrm{G}_{19}, \mathrm{t}\right),-\left(\mathrm{b}_{18}^{\prime \prime}\right)^{(2)}\left(\mathrm{G}_{19}, \mathrm{t}\right)$ are first detrition coefficients for category 1,2 and 3
$-\left(b_{13}^{\prime \prime}\right)^{(1,1,)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1,1,)}(G, t),-\left(b_{15}^{\prime \prime}\right)^{(1,1,)}(G, t)$ are second detrition coefficients for category
1,2 and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,3,)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3,3,)}\left(G_{23}, t\right)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4)}\left(G_{27}, t\right)$ are fourth detrition coefficients for category 1,2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5)}\left(G_{31}, t\right)$ are fifth detrition coefficients for category 1,2 and 3
$-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6)}\left(G_{35}, t\right)$ are sixth detrition coefficients for category 1,2 and 3
$-\left(b_{36}^{\prime \prime}\right)^{(7,7,7)}\left(G_{39}, t\right),-\left(b_{37}^{\prime \prime}\right)^{(7,7,7)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7,7,7)}\left(G_{39}, t\right)$ are seventh detrition coefficients for category 1,2 and 3
$-\left(b_{40}^{\prime \prime}\right)^{(8,8,8)}\left(G_{43}, t\right),-\left(b_{41}^{\prime \prime}\right)^{(8,8,8)}\left(G_{43}, t\right),-\left(b_{42}^{\prime \prime}\right)^{(8,8,8)}\left(G_{43}, t\right)$ are eight detrition coefficients for category 1,2 and 3
$-\left(b_{44}^{\prime \prime}\right)^{(9,9)}\left(G_{47}, t\right),-\left(b_{46}^{\prime \prime}\right)^{(9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9)}\left(G_{47}, t\right)$ are ninth detrition coefficients for category 1,2 and 3

$$
\begin{aligned}
& \frac{d G_{20}}{d t}= \\
& \left(a_{20}\right)^{(3)} G_{21}-\left[\begin{array}{c|c|c}
\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right) & +\left(a_{16}^{\prime \prime}\right)^{(2,2,2)}\left(T_{17}, t\right) & +\left(a_{13}^{\prime \prime}\right)^{(1,1,1,)}\left(T_{14}, t\right) \\
+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(T_{33}, t\right) \\
\hdashline+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{44}^{\prime \prime}\right)^{(9,9,9)}\left(T_{45}, t\right)
\end{array}\right] G_{20}
\end{aligned}
$$

$$
\begin{aligned}
& \frac{d G_{22}}{d t}=\left(a_{22}\right)^{(3)} G_{21}-\left[\begin{array}{c|c|c|c}
\left(a_{22}^{\prime}\right)^{(3)}+\left(a_{22}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right) & +\left(a_{18}^{\prime \prime}\right)^{(2,2,2)}\left(T_{17}, t\right) & +\left(a_{15}^{\prime \prime}\right)^{(1,1,1,)}\left(T_{14}, t\right) \\
\hline+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(T_{33}, t\right) \\
\hline+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{46}^{\prime \prime}\right)^{(9,9,9)}\left(T_{45}, t\right)
\end{array}\right] G_{22}
\end{aligned}
$$

$+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)$ are first augmentation coefficients for category 1,2 and 3
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,2)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2,2,2)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2,2,2)}\left(T_{17}, t\right)$ are second augmentation coefficients for category 1,2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1,1)}\left(T_{14}, t\right),+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,)}\left(T_{14}, t\right),+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,)}\left(T_{14}, t\right)$ are third augmentation coefficients for category 1,2 and 3
$+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(T_{25}, t\right)$ are fourth augmentation coefficients for category 1,2 and 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(T_{29}, t\right)$ are fifth augmentation coefficients for category 1,2 and 3
$+\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(T_{33}, t\right)$ are sixth augmentation coefficients for category 1,2 and 3
$+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7)}\left(T_{37}, t\right),+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7)}\left(T_{37}, t\right),+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7)}\left(T_{37}, t\right)$ are seventh augmentation coefficients for category 1,2 and 3
$+\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8)}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8)}\left(T_{41}, t\right),+\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8)}\left(T_{41}, t\right)$ are eight augmentation coefficients for category 1,2 and 3
$+\left(a_{44}^{\prime \prime}\right)^{(9,9,9)}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9,9,9)}\left(T_{45}, t\right),+\left(a_{46}^{\prime \prime}\right)^{(9,9,9)}\left(T_{45}, t\right)$ are ninth augmentation coefficients for category 1,2 and 3

$$
\begin{aligned}
& \frac{d T_{20}}{d t}=\left(b_{20}\right)^{(3)} T_{21}-\left[\begin{array}{c|c|}
\left(b_{20}^{\prime}\right)^{(3)}-\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,2)}\left(G_{19}, t\right) \\
-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,)}(G, t) \\
-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(G_{31}, t\right) \\
\hline-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(G_{35}, t\right) \\
-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8)}\left(G_{43}, t\right) \\
\hline-\left(b_{44}^{\prime \prime}\right)^{(9,9,9)}\left(G_{47}, t\right)
\end{array}\right] T_{20} \\
& \frac{d T_{21}}{d t}=\left(b_{21}\right)^{(3)} T_{20}-\left[\begin{array}{ccc}
\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{21}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right) & -\left(b_{17}^{\prime \prime}\right)^{(2,2,2)}\left(G_{19}, t\right) & -\left(b_{14}^{\prime \prime}\right)^{(1,1,1,)}(G, t) \\
-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(G_{35}, t\right) \\
\hdashline-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9,9)}\left(G_{47}, t\right)
\end{array}\right] T_{21} \\
& \frac{d T_{22}}{d t}=\left(b_{22}\right)^{(3)} T_{21}-\left[\begin{array}{c|c|c|}
\left(b_{22}^{\prime}\right)^{(3)} & -\left(b_{22}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,2)}\left(G_{19}, t\right) \\
\hline-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(G_{27}^{\prime \prime}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(1,1,5,5,5,5,5,5)}(G, t) \\
\hline-\left(G_{31}, t\right) & -\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(G_{35}, t\right) \\
\hline-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9,9)}\left(G_{47}, t\right)
\end{array}\right] T_{22}
\end{aligned}
$$

$-\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right)$ are first detrition coefficients for category 1, 2 and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,2)}\left(G_{19}, t\right),-\left(b_{17}^{\prime \prime}\right)^{(2,2,2)}\left(G_{19}, t\right),-\left(b_{18}^{\prime \prime}\right)^{(2,2,2)}\left(G_{19}, t\right)$ are second detrition coefficients for category 1, 2 and 3
$-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,)}(G, t),-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,)}(G, t)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(G_{27}, t\right)$ are fourth detrition coefficients for category 1, 2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(G_{31}, t\right)$ are fifth detrition coefficients for category 1, 2 and 3
$-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6)}\left(G_{35}, t\right)$ are sixth detrition coefficients for category 1,2 and 3
$-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7)}\left(G_{39}, t\right),-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7)}\left(G_{39}, t\right)-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7)}\left(G_{39}, t\right)$ are seventh detrition coefficients for category 1,2 and 3
$-\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8)}\left(G_{43}, t\right),-\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8)}\left(G_{43}, t\right),-\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8)}\left(G_{43}, t\right)$ are eight detrition coefficients for category 1, 2 and 3
$-\left(b_{46}^{\prime \prime}\right)^{(9,9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9,9)}\left(G_{47}, t\right),-\left(b_{44}^{\prime \prime}\right)^{(9,9,9)}\left(G_{47}, t\right)$ are ninth detrition coefficients for category 1, 2 and 3
$\frac{d G_{24}}{d t}=\left(a_{24}\right)^{(4)} G_{25}-\left[\begin{array}{cc|c|c|}\left(a_{24}^{\prime}\right)^{(4)} & +\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right) & +\left(a_{28}^{\prime \prime}\right)^{(5,5,)}\left(T_{29}, t\right) & +\left(a_{32}^{\prime \prime}\right)^{(6,6,)}\left(T_{33}, t\right) \\ \hline+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3)}\left(T_{21}, t\right) \\ \hline+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9)}\left(T_{45}, t\right)\end{array} G_{24}\right.$
$\frac{d G_{25}}{d t}=\left(a_{25}\right)^{(4)} G_{24}-\left[\begin{array}{cc|c|c}\left(a_{25}^{\prime}\right)^{(4)}+\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right) & +\left(a_{29}^{\prime \prime}\right)^{(5,5)}\left(T_{29}, t\right) & +\left(a_{33}^{\prime \prime}\right)^{(6,6)}\left(T_{33}, t\right) \\ +\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3)}\left(T_{21}, t\right) \\ \hline+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{41}^{\prime \prime}\right)^{(,, 8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9)}\left(T_{45}, t\right)\end{array}\right\} G_{25}$
$\frac{d G_{26}}{d t}=\left(a_{26}\right)^{(4)} G_{25}-\left[\begin{array}{ccc|c|}\left(a_{26}^{\prime}\right)^{(4)}+\left(a_{26}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right) & +\left(a_{30}^{\prime \prime}\right)^{(5,5,)}\left(T_{29}, t\right) & +\left(a_{34}^{\prime \prime}\right)^{(6,6,)}\left(T_{33}, t\right) \\ +\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3)}\left(T_{21}, t\right) \\ \hline+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9)}\left(T_{45}, t\right)\end{array}\right] G_{26}$
$\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right),\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right),\left(a_{26}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)$ are first augmentation coefficients category 1,2 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,)}\left(T_{29}, t\right)$ are second augmentation coefficient for category 1,2 and 3
$+\left(a_{32}^{\prime \prime}\right)^{(6,6,)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,)}\left(T_{33}, t\right)$ are third augmentation
coefficient for category 1,2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1)}\left(T_{14}, t\right),+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1)}\left(T_{14}, t\right),+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1)}\left(T_{14}, t\right)$
are fourth augmentation coefficients for category 1,2 and 3
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2)}\left(T_{17}, t\right) \quad, \quad+\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2)}\left(T_{17}, t\right)$
are fifth augmentation coefficients for category 1,2 and 3
$+\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3)}\left(T_{21}, t\right) \quad, \quad+\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3)}\left(T_{21}, t\right) \quad, \quad+\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3)}\left(T_{21}, t\right)$
are sixth augmentation coefficients for category 1,2 and 3
$+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(T_{37}, t\right) \quad, \quad+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(T_{37}, t\right) \quad+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(T_{37}, t\right)$
are seventh augmentation coefficients for category 1,2 and 3
$+\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(T_{41}, t\right)$
are eighth augmentation coefficients for category 1, 2 and 3
$+\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9)}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9)}\left(T_{45}, t\right),+\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9)}\left(T_{45}, t\right)$ are ninth detrition coefficients for category 123
$\frac{d T_{24}}{d t}=\left(b_{24}\right)^{(4)} T_{25}-\left[\begin{array}{cc|c|c|}\left(b_{24}^{\prime}\right)^{(4)} & -\left(b_{24}^{\prime \prime}\right)^{(4)}\left(G_{27}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(5,5)}\left(G_{31}, t\right) & -\left(b_{32}^{\prime \prime}\right)^{(6,6,)}\left(G_{35}, t\right) \\ -\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1)}(G, t) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3)}\left(G_{23}, t\right) \\ \hline-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{24}$
$\frac{d T_{25}}{d t}=\left(b_{25}\right)^{(4)} T_{24}-\left[\begin{array}{cc|c|c|c|}\left(b_{25}^{\prime}\right)^{(4)} & -\left(b_{25}^{\prime \prime}\right)^{(4)}\left(G_{27}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5)}\left(G_{31}, t\right) & -\left(b_{33}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1)}(G, t) & -\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3)}\left(G_{23}, t\right) \\ \hline-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{25}$
$\frac{d T_{26}}{d t}=\left(b_{26}\right)^{(4)} T_{25}-\left[\begin{array}{ccc|c}\left(b_{26}^{\prime}\right)^{(4)}-\left(b_{26}^{\prime \prime}\right)^{(4)}\left(G_{27}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(5,5,)}\left(G_{31}, t\right) & -\left(b_{34}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1)}(G, t) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{26}$
Where $-\left(b_{24}^{\prime \prime}\right)^{(4)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4)}\left(G_{27}, t\right)$ are first detrition coefficients for category 1,2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5)}\left(G_{31}, t\right)$ are second detrition coefficients for category 1,2 and 3 $-\left(b_{32}^{\prime \prime}\right)^{(6,6,)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6,6)}\left(G_{35}, t\right)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1)}(G, t)$
$-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1)}(G, t)$
are fourth detrition coefficients for category 1,2 and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2)}\left(G_{19}, t\right) \quad, \quad-\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2)}\left(G_{19}, t\right) \quad, \quad-\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2)}\left(G_{19}, t\right)$
are fifth detrition coefficients for category 1,2 and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3)}\left(G_{23}, t\right)$
are sixth detrition coefficients for category 1,2 and 3

$$
-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(G_{39}, t\right) \quad, \quad-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7)}\left(G_{39}, t\right) \quad, \quad-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7)}\left(G_{39}, t\right)
$$

are seventh detrition coefficients for category 1,2 and 3
$-\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8)}\left(G_{43}, t\right)$
are eighth detrition coefficients for category 1,2 and 3
$-\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9)}\left(G_{47}, t\right),-\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9)}\left(G_{47}, t\right)$ are ninth detrition coefficients for category 123

$$
\begin{aligned}
& \frac{d G_{29}}{d t}=\left(a_{29}\right)^{(5)} G_{28}-\left[\begin{array}{cc|c}
\left(a_{29}^{\prime}\right)^{(5)}+\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right) & +\left(a_{25}^{\prime \prime}\right)^{(4,4)}\left(T_{25}, t\right) & +\left(a_{33}^{\prime \prime}\right)^{(6,6,6)}\left(T_{33}, t\right) \\
+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(T_{21}, t\right) \\
+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(T_{45}, t\right)
\end{array}\right] G_{29} \\
& \frac{d G_{30}}{d t}=\left(a_{30}\right)^{(5)} G_{29}-\left[\begin{array}{ccc}
\left(a_{30}^{\prime}\right)^{(5)}+\left(a_{30}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right) & +\left(a_{26}^{\prime \prime}\right)^{(4,4)}\left(T_{25}, t\right) & +\left(a_{34}^{\prime \prime}\right)^{(6,6,6)}\left(T_{33}, t\right) \\
+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(T_{21}, t\right) \\
+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9}\left(T_{45}, t\right)
\end{array}\right] G_{30}
\end{aligned}
$$

Where $+\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)$ are first augmentation coefficients for category 1,2 and 3
And $+\left(a_{24}^{\prime \prime}\right)^{(4,4)}\left(T_{25}, t\right),+\left(a_{25}^{\prime \prime}\right)^{(4,4)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4)}\left(T_{25}, t\right)$ are second augmentation
coefficient for category 1,2 and 3
$+\left(a_{32}^{\prime \prime}\right)^{(6,6,6)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,6)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,6)}\left(T_{33}, t\right)$ are third augmentation
coefficient for category 1,2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1)}\left(T_{14}, t\right)$ are fourth augmentation coefficients for category 1,2 , and 3
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(T_{17}, t\right) \quad$ are $\quad$ fifth augmentation coefficients for category 1,2 , and 3
$+\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(T_{21}, t\right)$ are sixth augmentation coefficients for category $1,2,3$
$+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(T_{37}, t\right), \quad+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(T_{37}, t\right) \quad, \quad+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(T_{37}, t\right) \quad$ are seventh augmentation coefficients for category 1,2,3
$+\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(T_{41}, t\right)$ are eighth augmentation coefficients for category $1,2,3$
$+\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(T_{45}, t\right),+\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(T_{45}, t\right)$ are ninth augmentation coefficients for category $1,2,3$
$\frac{d T_{28}}{d t}=\left(b_{28}\right)^{(5)} T_{29}-\left[\begin{array}{c|c|c|c|}\left(b_{28}^{\prime}\right)^{(5)} & -\left(b_{28}^{\prime \prime}\right)^{(5)}\left(G_{31}, t\right) & -\left(b_{24}^{\prime \prime}\right)^{(4,4)}\left(G_{27}, t\right) & -\left(b_{32}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1)}(G, t) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(G_{23}, t\right) \\ \hline-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(G_{47}, t\right) \\ \hline\end{array}\right.$
$\frac{d T_{29}}{d t}=\left(b_{29}\right)^{(5)} T_{28}-\left[\begin{array}{cc|c}\left(b_{29}^{\prime}\right)^{(5)} & -\left(b_{29}^{\prime \prime}\right)^{(5)}\left(G_{31}, t\right) & -\left(b_{25}^{\prime \prime}\right)^{(4,4,)}\left(G_{27}, t\right) \\ -\left(b_{33}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{14}^{(1,1,1,1,1)}(G, t)\right. & -\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(G_{47}, t\right)\end{array} T_{29}\right.$
$\frac{d T_{30}}{d t}=\left(b_{30}\right)^{(5)} T_{29}-\left[\begin{array}{cc|c|c|}\left(b_{30}^{\prime}\right)^{(5)}-\left(b_{30}^{\prime \prime}\right)^{(5)}\left(G_{31}, t\right) & -\left(b_{26}^{\prime \prime}\right)^{(4,4)}\left(G_{27}, t\right) & -\left(b_{34}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,)}(G, t) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(G_{23}, t\right) \\ \hline-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(G_{47}, t\right) \\ \hline\end{array}\right] T_{30}$
where $-\left(b_{28}^{\prime \prime}\right)^{(5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5)}\left(G_{31}, t\right)$
are first detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,)}\left(G_{27}, t\right)$ are second detrition coefficients for category 1,2 and 3
$-\left(b_{32}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6,6,6)}\left(G_{35}, t\right)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1)}(G, t),-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,)}(G, t)$ are fourth detrition coefficients for category 1,2 , and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2)}\left(G_{19}, t\right)$ are fifth detrition coefficients for category 1,2 , and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3)}\left(G_{23}, t\right)$ are sixth detrition coefficients for category 1,2 , and 3 $-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right),-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right)$ are seventh detrition coefficients for category 1,2 , and 3
$-\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(G_{43}, t\right)$ are eighth detrition coefficients for category 1,2 , and 3
$-\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9)}\left(G_{47}, t\right)$ are ninth detrition coefficients
for category 1,2 , and 3
$\frac{d G_{32}}{d t}$

$\frac{d G_{33}}{d t}$
$=\left(a_{33}\right)^{(6)} G_{32}-\left[\begin{array}{cc|c|c|}\left(a_{33}^{\prime}\right)^{(6)}+\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right) & +\left(a_{29}^{\prime \prime}\right)^{(5,5,5)}\left(T_{29}, t\right) & +\left(a_{25}^{\prime \prime}\right)^{(4,4,4)}\left(T_{25}, t\right) \\ +\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(T_{21}, t\right) \\ +\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(T_{45}, t\right)\end{array}\right] G_{33}$
$\frac{d G_{34}}{d t}$
$=\left(a_{34}\right)^{(6)} G_{33}-\left[\begin{array}{cc|c|c|}\left(a_{34}^{\prime}\right)^{(6)}+\left(a_{34}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right) & +\left(a_{30}^{\prime \prime}\right)^{(5,5,5)}\left(T_{29}, t\right) & +\left(a_{26}^{\prime \prime}\right)^{(4,4,4,)}\left(T_{25}, t\right) \\ +\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(T_{21}, t\right) \\ +\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(T_{45}, t\right)\end{array}\right] G_{34}$ $+\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)$ are first augmentation coefficients for category 1,2 and 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,5)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5,5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,5)}\left(T_{29}, t\right)$ are second augmentation
coefficients for category 1,2 and 3
$+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,)}\left(T_{25}, t\right),+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,)}\left(T_{25}, t\right)$ are third augmentation
coefficients for category 1,2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1)}\left(T_{14}, t\right)$ - are fourth augmentation coefficients
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(T_{17}, t\right) \quad$ - fifth augmentation coefficients
$+\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(T_{21}, t\right) \quad$ sixth augmentation coefficients
$+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(T_{37}, t\right) \quad, \quad+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(T_{37}, t\right) \quad, \quad+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(T_{37}, t\right)$
seventh augmentation coefficients

$$
+\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(T_{41}, t\right)
$$

Eighth augmentation coefficients
$+\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(T_{45}, t\right),+\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(T_{45}, t\right)$ ninth augmentation coefficients
$\frac{d T_{32}}{d t}$
$=\left(b_{32}\right)^{(6)} T_{33}-\left[\begin{array}{c|c|c|c}\left(b_{32}^{\prime}\right)^{(6)} & -\left(b_{32}^{\prime \prime}\right)^{(6)}\left(G_{35}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(5,5,5)}\left(G_{31}, t\right) & -\left(b_{24}^{\prime \prime}\right)^{(4,4,4,)}\left(G_{27}, t\right) \\ -\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1)}(G, t) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right) \\ \hline-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{32}$
$\frac{d T_{33}}{d t}$
$=\left(b_{33}\right)^{(6)} T_{32}-\left[\begin{array}{cc|c}\left(b_{33}^{\prime}\right)^{(6)} & -\left(b_{33}^{\prime \prime}\right)^{(6)}\left(G_{35}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5,5)}\left(G_{31}, t\right) \\ -\left(b_{25}^{\prime \prime}\right)^{(4,4,4)}\left(G_{27}, t\right) \\ -\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1)}(G, t) & -\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{33}$
$\frac{d T_{34}}{d t}$
$=\left(b_{34}\right)^{(6)} T_{33}-\left[\begin{array}{cc|c|c|}\left(b_{34}^{\prime}\right)^{(6)} & -\left(b_{34}^{\prime \prime}\right)^{(6)}\left(G_{35}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(5,5,5)}\left(G_{31}, t\right) & -\left(b_{26}^{\prime \prime}\right)^{(4,4,4)}\left(G_{27}, t\right) \\ -\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1)}(G, t) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{34}$
$-\left(b_{32}^{\prime \prime}\right)^{(6)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6)}\left(G_{35}, t\right)$ are first detrition coefficients
for category 1,2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5,5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5,5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5,5)}\left(G_{31}, t\right)$ are second detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,)}\left(G_{27}, t\right)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1)}(G, t),-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1)}(G, t) \quad$ are fourth detrition coefficients for category 1,2 , and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2)}\left(G_{19}, t\right) \quad$ are fifth detrition coefficients for category 1,2 , and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right)$ are sixth detrition coefficients for category 1,2 , and 3
$-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right),-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7)}\left(G_{39}, t\right)$ are seventh detrition coefficients for category 1,2 , and 3
$-\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8)}\left(G_{43}, t\right)$
are eighth detrition coefficients for category 1,2 , and 3
$-\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9)}\left(G_{47}, t\right)$ are ninth detrition coefficients for category 1,2 , and 3

$$
\begin{aligned}
& \frac{d G_{36}}{d t} \\
& =\left(a_{36}\right)^{(7)} G_{37} \\
& -\left[\begin{array}{c|c|c}
\left(a_{36}^{\prime}\right)^{(7)} & +\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right) & +\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(T_{17}, t\right) \\
-+\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right) \\
++\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6}\left(T_{33}, t\right) \\
\hline+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)
\end{array}\right] G_{13} \\
& \frac{d G_{37}}{d t} \\
& =\left(a_{37}\right)^{(7)} G_{36} \\
& -\left[\begin{array}{ccc|}
\begin{array}{cc}
\left(a_{37}^{\prime}\right)^{(7)} & +\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right) \\
\hline+\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right) \\
\hline+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) \\
\hline+\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6}\left(T_{33}, t\right) \\
\hline+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(T_{41}, t\right) \\
\hline & +\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)
\end{array}
\end{array}\right] G_{14}
\end{aligned}
$$

$\frac{d G_{38}}{d t}$
$=\left(a_{38}\right)^{(7)} G_{37}$
$-\left[\begin{array}{ccc:c}\left(a_{38}^{\prime}\right)^{(7)} & +\left(a_{38}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right) & +\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right) \\ ++\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(T_{33}, t\right) \\ \hline+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(T_{41}, t\right) & +\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)\end{array}\right] G_{15}$
Where $\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right),\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right),\left(a_{38}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)$ are first augmentation coefficients for category 1,2 and 3
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(T_{17}, t\right) \quad, \quad+\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(T_{17}, t\right)$ are second augmentation coefficient for category 1,2 and 3 $+\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right) \quad$ are third augmentation coefficient for category 1,2 and 3
$+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(T_{25}, t\right) \quad+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(T_{25}, t\right)$ are fourth augmentation coefficient for category 1,2 and 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5)}\left(T_{29}, t\right) \quad$ are $\quad$ fift augmentation coefficient for category 1,2 and 3
$+\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(T_{33}, t\right) \quad$ are sixth augmentation coefficient for category 1,2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1)}\left(T_{14}, t\right) \quad$ are seventh augmentation coefficient for category 1,2 and 3

$$
+\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(T_{41}, t\right)
$$

are eighth augmentation coefficient for $1,2,3$
$+\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(T_{45}, t\right) \cdot+\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(T_{45}, t\right)$ are ninth augmentation coefficient for $1,2,3$

$$
\begin{aligned}
& \frac{d T_{36}}{d t}= \\
& \left(b_{36}\right)^{(7)} T_{37}-\left[\begin{array}{c|c|c|}
\left(b_{36}^{\prime}\right)^{(7)} & -\left(b_{36}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(G_{19}, t\right) \\
-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(5,3,3,3,3,3,3,3,5,5,5,5)}\left(G_{23}, t\right) \\
\hline & & -\left(G_{31}^{\prime \prime}, t\right) \\
\hline-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(G_{35}, t\right) \\
\hline & & \\
\hline
\end{array}\right. \\
& \frac{d T_{37}}{d t}= \\
& \left(b_{37}\right)^{(7)} T_{36}-\left[\begin{array}{ccc|}
\left(b_{37}^{\prime}\right)^{(7)} & -\left(b_{37}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right) & -\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(G_{19}, t\right) \\
-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(G_{23}, t\right) \\
-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(G_{35}, t\right) \\
-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(G_{43}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)
\end{array}\right] T_{14} \\
& \frac{d T_{38}}{d t}= \\
& \left(b_{38}\right)^{(7)} T_{37}-\left[\begin{array}{c|c|c|}
\left(b_{38}^{\prime}\right)^{(7)} & -\left(b_{38}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(G_{19}, t\right) \\
\hline-\left(b_{26}^{\prime \prime}\right)^{\prime \prime}(4,4,4,4,4,4,4) & \left(G_{27}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(5,3,5,5,5,5,5,5,5)}\left(G_{31}, t\right) \\
\hline-\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(G_{35}, t\right) \\
\hline-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8}\left(G_{43}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(G_{47}, t\right) \\
\hline-4 &
\end{array}\right] T_{15}
\end{aligned}
$$

Where $-\left(b_{36}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right),-\left(b_{37}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right)$ are first detrition coefficients for category 1,2 and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2)}\left(G_{19}, t\right)$ are second detrition coefficients for category 1,2 and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3)}\left(G_{23}, t\right)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(G_{27}, t\right)$ are fourth detrition coefficients for category 1,2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5)}\left(G_{31}, t\right)$ are fifth detrition coefficients for category 1,2 and 3
$-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(G_{35}, t\right)$ are sixth detrition coefficients for category 1,2 and 3
$-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t),-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1)}(G, t)$
are seventh detrition coefficients for category 1,2 and 3
$-\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8)}\left(G_{43}, t\right)$ are eighth detrition coefficients for category 1,2 and 3
$-\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9)}\left(G_{47}, t\right)$ are ninth detrition
coefficients for category 1,2 and 3

$$
\begin{aligned}
& \frac{d G_{40}}{d t} \\
& =\left(a_{40}\right)^{(8)} G_{41}
\end{aligned}
$$

$$
\begin{aligned}
& \frac{d G_{41}}{d t} \\
& =\left(a_{41}\right)^{(8)} G_{40} \\
& -\left[\begin{array}{cccc}
\left(a_{41}^{\prime}\right)^{(8)} & +\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right) & +\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(T_{21}, t\right) \\
\hline+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right) \\
\hline+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)
\end{array}\right] G_{14} \\
& \frac{d G_{42}}{d t} \\
& =\left(a_{42}\right)^{(8)} G_{41} \\
& -\left[\begin{array}{ccc|c}
\left(a_{42}^{\prime}\right)^{(8)}+\left(a_{42}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right) & +\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{22}^{\prime \prime}\right)(3,3,3,3,3,3,3,3) \\
\hline+\left(a_{21}^{\prime \prime}, t\right) \\
\hline+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6}\left(T_{33}, t\right) \\
\hline+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)
\end{array}\right] G_{15}
\end{aligned}
$$

Where $+\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right),+\left(a_{42}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)$ are first augmentation coefficients for category 1,2 and 3
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2)}\left(T_{17}, t\right)$ are second augmentation coefficient for category 1,2 and 3 $+\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(T_{21}, t\right) \quad$ are third augmentation coefficient for category 1,2 and 3
$+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(T_{25}, t\right)$ are fourth augmentation coefficient for category 1,2 and 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) \quad$ are $\quad$ fift augmentation coefficient for category 1,2 and 3

$$
+\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right) \quad \text { are sixth }
$$

augmentation coefficient for category 1,2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) \quad+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) \quad+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}\left(T_{14}, t\right)$ are seventh augmentation coefficient for 1,2,3
$+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(T_{37}, t\right),+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(T_{37}, t\right),+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(T_{37}, t\right)$ are eighth augmentation coefficient for $1,2,3$
$+\left(a_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(T_{45}, t\right) \quad, \quad+\left(a_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(T_{45}, t\right) \quad,+\left(a_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(T_{45}, t\right)$ are ninth augmentation coefficient for $1,2,3$
$\frac{d T_{40}}{d t}=$
$\left(b_{40}\right)^{(8)} T_{41}-$
$\left[\begin{array}{cccc|}\left(b_{40}^{\prime}\right)^{(8)}-\left(b_{40}^{\prime \prime}\right)^{(8)}\left(G_{43}, t\right) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(G_{35}, t\right) \\ --\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right) \\ \hline & & \end{array}\right] T_{13}$
$\frac{d T_{41}}{d t}=$
$\left(b_{41}\right)^{(8)} T_{40}-$
$\left[\begin{array}{cccc}\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{41}^{\prime \prime}\right)^{(8)}\left(G_{43}, t\right) & -\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{14}$
$\frac{d T_{42}}{d t}=$
$\left(b_{42}\right)^{(8)} T_{41}-$
$\left[\begin{array}{cccc}\left(b_{42}^{\prime}\right)^{(8)}-\left(b_{42}^{\prime \prime}\right)^{(8)}\left(G_{43}, t\right) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(G_{35}, t\right) \\ -\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)\end{array}\right] T_{15}$
Where $-\left(b_{36}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right),-\left(b_{37}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right)$ are first detrition coefficients for category 1,2 and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(G_{19}, t\right) \quad$ are second detrition coefficients for category 1,2 and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right)$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right)$ are fourth detrition coefficients for category 1,2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right)$ are fifth detrition coefficients for category 1,2 and 3
$-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,)}\left(G_{35}, t\right),-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t)$ are sixth detrition coefficients for category 1, 2 and 3
$-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t) \quad,-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t),-\left(b_{38}^{\prime \prime}\right)^{(7,7,)}\left(G_{39}, t\right)$ are seventh detrition coefficients for category 1,2 and 3
$-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right),-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right)$ are eighth detrition coefficients for category 1,2 and 3
$-\left(b_{44}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(G_{47}, t\right),-\left(b_{46}^{\prime \prime}\right)^{(9,9,9,9,9,9,9,9)}\left(G_{47}, t\right)$ are ninth detrition coefficients for category 1,2 and 3
$\frac{d G_{44}}{d t}$
$=\left(a_{44}\right)^{(9)} G_{45}$
$-\left[\begin{array}{c|c|c}\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{44}^{\prime \prime}\right)(9)\left(T_{45}, t\right) & +\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3,3)}\left(T_{21}, t\right) \\ +\left(a_{24}^{\prime \prime}(4,4,4,4,4,4,4,4,4)\right. \\ \hline+\left(T_{25}, t\right) & +\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5,5}\left(T_{29}, t\right) & +\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right) \\ \hline+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8,8)}\left(T_{41}, t\right)\end{array}\right] G_{13}$
$\frac{d G_{45}}{d t}$
$=\left(a_{45}\right)^{(9)} G_{44}$
$-\left[\begin{array}{ccc}\left(a_{45}^{\prime}\right)^{(9)}+\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right) & +\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2,2)}\left(T_{17}, t\right) & +\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3,3)}\left(T_{21}, t\right) \\ +\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right) \\ \hline+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(T_{41}, t\right)\end{array}\right] G_{14}$
$\frac{d G_{46}}{d t}$
$=\left(a_{46}\right)^{(9)} G_{45}$
$-\left[\begin{array}{ccc|}\left(a_{46}^{\prime}\right)^{(9)}+\left(a_{46}^{\prime \prime}\right)^{(9)}\left(T_{37}, t\right) & +\left(a_{18}^{\prime \prime}{ }^{(2,2,2,2,2,2,2,2,2)}\left(T_{17}, t\right)\right. & +\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3,3)}\left(T_{21}, t\right) \\ ++\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4,4,4)}\left(T_{25}, t\right) & +\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5,5)}\left(T_{29}, t\right) & +\left(a_{34}^{\prime \prime}{ }^{(6,6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right)\right. \\ \hline+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right) & +\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7,7)}\left(T_{37}, t\right) & +\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8,8}\left(T_{41}, t\right)\end{array}\right] G_{15}$
Where $+\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right),+\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right),+\left(a_{46}^{\prime \prime}\right)^{(9)}\left(T_{37}, t\right)$ are first augmentation coefficients for category 1,2 and 3
$+\left(a_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2,2)}\left(T_{17}, t\right),+\left(a_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2,2)}\left(T_{17}, t\right)$ are second augmentation coefficient for category 1,2 and 3 $+\left(a_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3,3)}\left(T_{21}, t\right),+\left(a_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3,3)}\left(T_{21}, t\right)$ are third augmentation coefficient for category 1,2 and 3
$+\left(a_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4,4,4}\left(T_{25}, t\right),+\left(a_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4,4)}\left(T_{25}, t\right),+\left(a_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4,4)}\left(T_{25}, t\right)$ are fourth augmentation coefficient for category 1, 2 and 3
$+\left(a_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5)}\left(T_{29}, t\right),+\left(a_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5)}\left(T_{29}, t\right)$ are fifth augmentation coefficient for category 1,2 and 3
$+\left(a_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right),+\left(a_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(T_{33}, t\right)$ are sixth augmentation coefficient for category 1,2 and 3
$+\left(a_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right),+\left(a_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1,1)}\left(T_{14}, t\right)$ are Seventh augmentation coefficient for category 1,2 and 3
$+\left(a_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(T_{37}, t\right) \quad+\left(a_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(T_{37}, t\right) \quad+\left(a_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(T_{37}, t\right)$ are eighth augmentation coefficient for 1,2,3
$+\left(a_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(T_{41}, t\right),+\left(a_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(T_{41}, t\right)$ are ninth augmentation coefficient for $1,2,3$
$\frac{d T_{44}}{d t}=$
$\left(b_{44}\right)^{(9)} T_{45}-$
$\left[\begin{array}{cccc}\left(b_{44}^{\prime}\right)^{(9)} & -\left(b_{44}^{\prime \prime}\right)^{(9)}\left(G_{47}, t\right) & -\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6,6)}\left(G_{35}, t\right) \\ & -\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8,8)}\left(G_{43}, t\right)\end{array}\right] T_{13}$
$\frac{d T_{45}}{d t}=$
$\left(b_{45}\right)^{(9)} T_{44}-$
$\left[\begin{array}{ccc|c}\left(b_{45}^{\prime}\right)^{(9)} & -\left(b_{45}^{\prime \prime}\right)^{(9)}\left(G_{47}, t\right) & -\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right) \\ -\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5)}\left(G_{31}, t\right) & -\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6}\left(G_{35}, t\right) \\ \hline-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(G_{43}, t\right)\end{array}\right] T_{14}$
$\frac{d T_{46}}{d t}=$
${ }_{\left(b_{46}\right)}{ }^{(9)} T_{45}-$
$\left[\begin{array}{ccc|c}\left(b_{46}^{\prime}\right)^{(9)}-\left(b_{46}^{\prime \prime}\right)^{(9)}\left(G_{47}, t\right) & -\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2)}\left(G_{19}, t\right) & -\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3,3)}\left(G_{23}, t\right) \\ \hline-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) & -\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5,5)}\left(G_{31}, t\right) & \left.-\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6}\right)\left(G_{35}, t\right) \\ \hline-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1)}(G, t) & -\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7,7)}\left(G_{39}, t\right) & -\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(G_{43}, t\right)\end{array}\right] T_{15}$
Where $-\left(b_{44}^{\prime \prime}\right)^{(9)}\left(G_{47}, t\right),-\left(b_{45}^{\prime \prime}\right)^{(9)}\left(G_{47}, t\right),-\left(b_{46}^{\prime \prime}\right)^{(9)}\left(G_{47}, t\right)$ are first detrition coefficients for category 1,2 and 3
$-\left(b_{16}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{17}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2,2)}\left(G_{19}, t\right),-\left(b_{18}^{\prime \prime}\right)^{(2,2,2,2,2,2,2,2,2)}\left(G_{19}, t\right)$ are second detrition coefficients for category 1,2 and 3
$-\left(b_{20}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{21}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(G_{23}, t\right),-\left(b_{22}^{\prime \prime}\right)^{(3,3,3,3,3,3,3)}\left(G_{23}, t\right) \quad$ are third detrition coefficients for category 1,2 and 3
$-\left(b_{24}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{25}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right),-\left(b_{26}^{\prime \prime}\right)^{(4,4,4,4,4,4,4,4)}\left(G_{27}, t\right) \quad$ are $\quad$ fourth
detrition coefficients for category 1,2 and 3
$-\left(b_{28}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{29}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right),-\left(b_{30}^{\prime \prime}\right)^{(5,5,5,5,5,5,5,5)}\left(G_{31}, t\right)$ are fift detrition coefficients for category 1,2 and 3
$-\left(b_{32}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{33}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(G_{35}, t\right),-\left(b_{34}^{\prime \prime}\right)^{(6,6,6,6,6,6,6,6,6)}\left(G_{35}, t\right)$ are sixth detrition coefficients for category 1,2 and 3
$-\left(b_{15}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t),-\left(b_{14}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1)}(G, t),-\left(b_{13}^{\prime \prime}\right)^{(1,1,1,1,1,1,1,1,1)}(G, t)$ are seventh detrition coefficients for category 1,2 and 3
$-\left(b_{37}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(G_{39}, t\right) \quad,-\left(b_{36}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(G_{39}, t\right),-\left(b_{38}^{\prime \prime}\right)^{(7,7,7,7,7,7,7)}\left(G_{39}, t\right)$ are eighth detrition coefficients for category 1,2 and 3
$-\left(b_{42}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{41}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(G_{43}, t\right),-\left(b_{40}^{\prime \prime}\right)^{(8,8,8,8,8,8,8,8,8)}\left(G_{43}, t\right)$ are ninth detrition coefficients for category 1,2 and 3

Where we suppose
(A) $\quad\left(a_{i}\right)^{(1)},\left(a_{i}^{\prime}\right)^{(1)},\left(a_{i}^{\prime \prime}\right)^{(1)},\left(b_{i}\right)^{(1)},\left(b_{i}^{\prime}\right)^{(1)},\left(b_{i}^{\prime \prime}\right)^{(1)}>0$,
$i, j=13,14,15$
(B) The functions $\left(a_{i}^{\prime \prime}\right)^{(1)},\left(b_{i}^{\prime \prime}\right)^{(1)}$ are positive continuous increasing and bounded.

Definition of $\left(p_{i}\right)^{(1)},\left(r_{i}\right)^{(1)}$ :
$\left(a_{i}^{\prime}\right)^{(1)}\left(T_{14}, t\right) \leq\left(p_{i}\right)^{(1)} \leq\left(\hat{A}_{13}\right)^{(1)}$
$\left(b_{i}^{\prime \prime}\right)^{(1)}(G, t) \leq\left(r_{i}\right)^{(1)} \leq\left(b_{i}^{\prime}\right)^{(1)} \leq\left(\hat{B}_{13}\right)^{(1)}$
(C) $\quad \lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)=\left(p_{i}\right)^{(1)}$

$$
\lim _{\mathrm{G} \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(1)}(G, t)=\left(r_{i}\right)^{(1)}
$$

Definition of $\left(\hat{A}_{13}\right)^{(1)},\left(\hat{B}_{13}\right)^{(1)}$ :
Where $\left(\hat{A}_{13}\right)^{(1)},\left(\hat{B}_{13}\right)^{(1)},\left(p_{i}\right)^{(1)},\left(r_{i}\right)^{(1)}$ are positive constants and $i=13,14,15$
They satisfy Lipschitz condition:
$\left|\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)\right| \leq\left(\hat{k}_{13}\right)^{(1)}\left|T_{14}-T_{14}^{\prime}\right| e^{-\left(\hat{M}_{13}\right)^{(1)} t}$
$\left|\left(b_{i}^{\prime \prime}\right)^{(1)}\left(G^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(1)}(G, t)\right|<\left(\hat{k}_{13}\right)^{(1)}| | G-G^{\prime}| | e^{-\left(\hat{M}_{13}\right)^{(1)} t}$
With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}^{\prime}, t\right)$ and $\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right) \cdot\left(T_{14}^{\prime}, t\right)$ and $\left(T_{14}, t\right)$ are points belonging to the interval $\left[\left(\hat{k}_{13}\right)^{(1)},\left(\widehat{M}_{13}\right)^{(1)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{13}\right)^{(1)}=1$ then the function $\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.
Definition of $\left(\widehat{M}_{13}\right)^{(1)},\left(\widehat{k}_{13}\right)^{(1)}$ :
(D) $\quad\left(\widehat{M}_{13}\right)^{(1)},\left(\hat{k}_{13}\right)^{(1)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(1)}}{\left(\widehat{M}_{13}\right)^{(1)}}, \frac{\left(b_{i}\right)^{(1)}}{\left(\widehat{M}_{13}\right)^{(1)}}<1
$$

Definition of $\left(\hat{P}_{13}\right)^{(1)},\left(\hat{Q}_{13}\right)^{(1)}$ :
(E) There exists two constants $\left(\hat{P}_{13}\right)^{(1)}$ and $\left(\hat{Q}_{13}\right)^{(1)}$ which together with $\left(\widehat{M}_{13}\right)^{(1)},\left(\hat{k}_{13}\right)^{(1)},\left(\hat{A}_{13}\right)^{(1)} \quad$ and $\quad\left(\hat{B}_{13}\right)^{(1)}$ and the constants $\left(a_{i}\right)^{(1)},\left(a_{i}^{\prime}\right)^{(1)},\left(b_{i}\right)^{(1)},\left(b_{i}^{\prime}\right)^{(1)},\left(p_{i}\right)^{(1)},\left(r_{i}\right)^{(1)}, i=13,14,15$, satisfy the inequalities

$$
\begin{aligned}
& \frac{1}{\left(\hat{M}_{13}\right)^{(1)}}\left[\left(a_{i}\right)^{(1)}+\left(a_{i}^{\prime}\right)^{(1)}+\left(\hat{A}_{13}\right)^{(1)}+\left(\hat{P}_{13}\right)^{(1)}\left(\hat{k}_{13}\right)^{(1)}\right]<1 \\
& \frac{1}{\left(M_{13}\right)^{(1)}}\left[\left(b_{i}\right)^{(1)}+\left(b_{i}^{\prime}\right)^{(1)}+\left(\hat{B}_{13}\right)^{(1)}+\left(\hat{Q}_{13}\right)^{(1)}\left(\hat{k}_{13}\right)^{(1)}\right]<1
\end{aligned}
$$

Where we suppose

$$
\begin{equation*}
\left(a_{i}\right)^{(2)},\left(a_{i}^{\prime}\right)^{(2)},\left(a_{i}^{\prime \prime}\right)^{(2)},\left(b_{i}\right)^{(2)},\left(b_{i}^{\prime}\right)^{(2)},\left(b_{i}^{\prime \prime}\right)^{(2)}>0, \quad i, j=16,17,18 \tag{F}
\end{equation*}
$$

(G) The functions $\left(a_{i}^{\prime \prime}\right)^{(2)},\left(b_{i}^{\prime \prime}\right)^{(2)}$ are positive continuous increasing and bounded.

Definition of $\left(\mathrm{p}_{\mathrm{i}}\right)^{(2)},\left(\mathrm{r}_{\mathrm{i}}\right)^{(2)}$ :

$$
\begin{aligned}
& \left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right) \leq\left(p_{i}\right)^{(2)} \leq\left(\hat{A}_{16}\right)^{(2)} \\
& \left(b_{i}^{\prime \prime}\right)^{(2)}\left(G_{19}, t\right) \leq\left(r_{i}\right)^{(2)} \leq\left(b_{i}^{\prime}\right)^{(2)} \leq\left(\hat{B}_{16}\right)^{(2)}
\end{aligned}
$$

$$
\begin{equation*}
\lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)=\left(p_{i}\right)^{(2)} \tag{H}
\end{equation*}
$$

Definition of $\left(\hat{A}_{16}\right)^{(2)},\left(\hat{B}_{16}\right)^{(2)}$ :

$$
\lim _{G \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right)=\left(r_{i}\right)^{(2)}
$$

Where $\left(\hat{A}_{16}\right)^{(2)},\left(\hat{B}_{16}\right)^{(2)},\left(p_{i}\right)^{(2)},\left(r_{i}\right)^{(2)}$ are positive constants and $i=16,17,18$
They satisfy Lipschitz condition:
$\left|\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)\right| \leq\left(\hat{k}_{16}\right)^{(2)}\left|T_{17}-T_{17}^{\prime}\right| e^{-\left(\widehat{M}_{16}\right)^{(2)} t}$
$\left|\left(b_{i}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right)^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right)\right|<\left(\widehat{k}_{16}\right)^{(2)}| |\left(G_{19}\right)-\left(G_{19}\right)^{\prime}| | e^{-\left(\widehat{M}_{16}\right)^{(2)} t}$
With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}^{\prime}, t\right)$ $\operatorname{and}\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right) \cdot\left(T_{17}^{\prime}, t\right)$ and $\left(T_{17}, t\right)$ are points belonging to the interval $\left[\left(\widehat{k}_{16}\right)^{(2)},\left(\widehat{M}_{16}\right)^{(2)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{16}\right)^{(2)}=$ 1 then the function $\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.
Definition of $\left(\widehat{M}_{16}\right)^{(2)},\left(\widehat{k}_{16}\right)^{(2)}$ :
(I) $\quad\left(\widehat{M}_{16}\right)^{(2)},\left(\hat{k}_{16}\right)^{(2)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(2)}}{\left(\widetilde{M}_{16}\right)^{(2)}}, \frac{\left(b_{i}\right)^{(2)}}{\left(\widetilde{M}_{16}\right)^{(2)}}<1
$$

Definition of $\left(\hat{P}_{13}\right)^{(2)},\left(\hat{Q}_{13}\right)^{(2)}$ :
There exists two constants $\left(\hat{P}_{16}\right)^{(2)}$ and $\left(\hat{Q}_{16}\right)^{(2)}$ which together with $\quad\left(\widehat{M}_{16}\right)^{(2)},\left(\hat{k}_{16}\right)^{(2)},\left(\hat{A}_{16}\right)^{(2)}$ and $\left(\widehat{B}_{16}\right)^{(2)}$ and the constants $\left(a_{i}\right)^{(2)},\left(a_{i}^{\prime}\right)^{(2)},\left(b_{i}\right)^{(2)},\left(b_{i}^{\prime}\right)^{(2)},\left(p_{i}\right)^{(2)},\left(r_{i}\right)^{(2)}, i=16,17,18$, satisfy the inequalities
$\frac{1}{\left(\widehat{M}_{16}\right)^{(2)}}\left[\left(a_{i}\right)^{(2)}+\left(a_{i}^{\prime}\right)^{(2)}+\left(\hat{A}_{16}\right)^{(2)}+\left(\hat{P}_{16}\right)^{(2)}\left(\hat{k}_{16}\right)^{(2)}\right]<1$
$\frac{1}{\left(\hat{M}_{16}\right)^{(2)}}\left[\left(b_{i}\right)^{(2)}+\left(b_{i}^{\prime}\right)^{(2)}+\left(\hat{B}_{16}\right)^{(2)}+\left(\hat{Q}_{16}\right)^{(2)}\left(\hat{k}_{16}\right)^{(2)}\right]<1$
Where we suppose
(J)

$$
\left(a_{i}\right)^{(3)},\left(a_{i}^{\prime}\right)^{(3)},\left(a_{i}^{\prime \prime}\right)^{(3)},\left(b_{i}\right)^{(3)},\left(b_{i}^{\prime}\right)^{(3)},\left(b_{i}^{\prime \prime}\right)^{(3)}>0, \quad i, j=20,21,22
$$

The functions $\left(a_{i}^{\prime \prime}\right)^{(3)},\left(b_{i}^{\prime \prime}\right)^{(3)}$ are positive continuous increasing and bounded.
Definition of $\left(p_{i}\right)^{(3)},\left(\mathrm{r}_{\mathrm{i}}\right)^{(3)}$ :

$$
\begin{gathered}
\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right) \leq\left(p_{i}\right)^{(3)} \leq\left(\hat{A}_{20}\right)^{(3)} \\
\left(b_{i}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right) \leq\left(r_{i}\right)^{(3)} \leq\left(b_{i}^{\prime}\right)^{(3)} \leq\left(\hat{B}_{20}\right)^{(3)} \\
\lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)=\left(p_{i}\right)^{(3)} \\
\lim _{\mathrm{G} \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right)=\left(r_{i}\right)^{(3)}
\end{gathered}
$$

Definition of $\left(\hat{A}_{20}\right)^{(3)},\left(\hat{B}_{20}\right)^{(3)}$ :
Where $\left(\hat{A}_{20}\right)^{(3)},\left(\hat{B}_{20}\right)^{(3)},\left(p_{i}\right)^{(3)},\left(r_{i}\right)^{(3)}$ are positive constants and $i=20,21,22$
They satisfy Lipschitz condition:
$\left|\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)\right| \leq\left(\hat{k}_{20}\right)^{(3)}\left|T_{21}-T_{21}^{\prime}\right| e^{-\left(\widehat{M}_{20}\right)^{(3)} t}$
$\left|\left(b_{i}^{\prime \prime}\right)^{(3)}\left(G_{23}^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(3)}\left(G_{23}, t\right)\right|<\left(\hat{k}_{20}\right)^{(3)}| | G_{23}-G_{23}| | e^{-\left(\hat{M}_{20}\right)^{(3)} t}$
With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}^{\prime}, t\right)$ $\operatorname{and}\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right) .\left(T_{21}^{\prime}, t\right)$ And $\left(T_{21}, t\right)$ are points belonging to the interval $\left[\left(\hat{k}_{20}\right)^{(3)},\left(\widehat{M}_{20}\right)^{(3)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{20}\right)^{(3)}=$ 1 then the function $\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.
Definition of $\left(\widehat{M}_{20}\right)^{(3)},\left(\widehat{k}_{20}\right)^{(3)}$ :
(K) $\quad\left(\widehat{M}_{20}\right)^{(3)},\left(\hat{k}_{20}\right)^{(3)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(3)}}{\left(\bar{M}_{20}\right)^{(3)}}, \frac{\left(b_{i}\right)^{(3)}}{\left(\hat{M}_{20}\right)^{(3)}}<1
$$

There exists two constants There exists two constants $\left(\hat{P}_{20}\right)^{(3)}$ and $\left(\hat{Q}_{20}\right)^{(3)}$ which together with
$\left(\widehat{M}_{20}\right)^{(3)},\left(\hat{k}_{20}\right)^{(3)},\left(\hat{A}_{20}\right)^{(3)}$ and $\left(\hat{B}_{20}\right)^{(3)}$ and the constants
$\left(a_{i}\right)^{(3)},\left(a_{i}^{\prime}\right)^{(3)},\left(b_{i}\right)^{(3)},\left(b_{i}^{\prime}\right)^{(3)},\left(p_{i}\right)^{(3)},\left(r_{i}\right)^{(3)}, i=20,21,22$,
satisfy the inequalities
$\frac{1}{\left(\widehat{M}_{20}\right)^{(3)}}\left[\left(a_{i}\right)^{(3)}+\left(a_{i}^{\prime}\right)^{(3)}+\left(\hat{A}_{20}\right)^{(3)}+\left(\hat{P}_{20}\right)^{(3)}\left(\hat{k}_{20}\right)^{(3)}\right]<1$
$\frac{1}{\left(\hat{M}_{20}\right)^{(3)}}\left[\left(b_{i}\right)^{(3)}+\left(b_{i}^{\prime}\right)^{(3)}+\left(\hat{B}_{20}\right)^{(3)}+\left(\hat{Q}_{20}\right)^{(3)}\left(\hat{k}_{20}\right)^{(3)}\right]<1$

Where we suppose
$\left(a_{i}\right)^{(4)},\left(a_{i}^{\prime}\right)^{(4)},\left(a_{i}^{\prime \prime}\right)^{(4)},\left(b_{i}\right)^{(4)},\left(b_{i}^{\prime}\right)^{(4)},\left(b_{i}^{\prime \prime}\right)^{(4)}>0, \quad i, j=24,25,26$
(L) The functions $\left(a_{i}^{\prime \prime}\right)^{(4)},\left(b_{i}^{\prime \prime}\right)^{(4)}$ are positive continuous increasing and bounded.

Definition of $\left(p_{i}\right)^{(4)},\left(r_{i}\right)^{(4)}$ :

$$
\begin{aligned}
& \left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right) \leq\left(p_{i}\right)^{(4)} \leq\left(\hat{A}_{24}\right)^{(4)} \\
& \left(b_{i}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right) \leq\left(r_{i}\right)^{(4)} \leq\left(b_{i}^{\prime}\right)^{(4)} \leq\left(\hat{B}_{24}\right)^{(4)}
\end{aligned}
$$

(M)

$$
\begin{aligned}
& \lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)=\left(p_{i}\right)^{(4)} \\
& \lim _{G \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right)=\left(r_{i}\right)^{(4)}
\end{aligned}
$$

Definition of $\left(\hat{A}_{24}\right)^{(4)},\left(\hat{B}_{24}\right)^{(4)}$ :
Where $\left(\hat{A}_{24}\right)^{(4)},\left(\hat{B}_{24}\right)^{(4)},\left(p_{i}\right)^{(4)},\left(r_{i}\right)^{(4)}$ are positive constants and $i=24,25,26$
They satisfy Lipschitz condition:
$\left|\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)\right| \leq\left(\hat{k}_{24}\right)^{(4)}\left|T_{25}-T_{25}^{\prime}\right| e^{-\left(\widehat{M}_{24}\right)^{(4)} t}$
$\left|\left(b_{i}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right)\right|<\left(\hat{k}_{24}\right)^{(4)}\left\|\left(G_{27}\right)-\left(G_{27}\right)^{\prime}\right\| e^{-\left(\widehat{M}_{24}\right)^{(4)} t}$
With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}^{\prime}, t\right)$ $\operatorname{and}\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right) .\left(T_{25}^{\prime}, t\right)$ and $\left(T_{25}, t\right)$ are points belonging to the interval $\left[\left(\hat{k}_{24}\right)^{(4)},\left(\widehat{M}_{24}\right)^{(4)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{24}\right)^{(4)}=$ 4 then the function $\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.
Definition of $\left(\widehat{M}_{24}\right)^{(4)},\left(\widehat{k}_{24}\right)^{(4)}$ :
$\left(\widehat{M}_{24}\right)^{(4)},\left(\hat{k}_{24}\right)^{(4)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(4)}}{\left(\hat{M}_{24}\right)^{(4)}}, \frac{\left(b_{i}\right)^{(4)}}{\left(\widehat{M}_{24}\right)^{(4)}}<1
$$

Definition of $\left(\hat{P}_{24}\right)^{(4)},\left(\hat{Q}_{24}\right)^{(4)}$ :
$(\mathrm{N}) \quad$ There exists two constants $\left(\hat{P}_{24}\right)^{(4)}$ and $\left(\hat{Q}_{24}\right)^{(4)}$ which together with $\left(\widehat{M}_{24}\right)^{(4)},\left(\hat{k}_{24}\right)^{(4)},\left(\hat{A}_{24}\right)^{(4)}$ and $\left(\widehat{B}_{24}\right)^{(4)}$ and the constants $\left(a_{i}\right)^{(4)},\left(a_{i}^{\prime}\right)^{(4)},\left(b_{i}\right)^{(4)},\left(b_{i}^{\prime}\right)^{(4)},\left(p_{i}\right)^{(4)},\left(r_{i}\right)^{(4)}, i=24,25,26$, satisfy the inequalities
$\frac{1}{\left(\widehat{M}_{24}\right)^{(4)}}\left[\left(a_{i}\right)^{(4)}+\left(a_{i}^{\prime}\right)^{(4)}+\left(\hat{A}_{24}\right)^{(4)}+\left(\hat{P}_{24}\right)^{(4)}\left(\hat{k}_{24}\right)^{(4)}\right]<1$

$$
\begin{equation*}
\frac{1}{\left(\hat{M}_{24}\right)^{(4)}}\left[\left(b_{i}\right)^{(4)}+\left(b_{i}^{\prime}\right)^{(4)}+\left(\hat{B}_{24}\right)^{(4)}+\left(\hat{Q}_{24}\right)^{(4)}\left(\hat{k}_{24}\right)^{(4)}\right]<1 \tag{122}
\end{equation*}
$$

Where we suppose
$\left(a_{i}\right)^{(5)},\left(a_{i}^{\prime}\right)^{(5)},\left(a_{i}^{\prime \prime}\right)^{(5)},\left(b_{i}\right)^{(5)},\left(b_{i}^{\prime}\right)^{(5)},\left(b_{i}^{\prime \prime}\right)^{(5)}>0, \quad i, j=28,29,30$
(O) The functions $\left(a_{i}^{\prime \prime}\right)^{(5)},\left(b_{i}^{\prime \prime}\right)^{(5)}$ are positive continuous increasing and bounded.

Definition of $\left(p_{i}\right)^{(5)},\left(r_{i}\right)^{(5)}$ :

$$
\begin{align*}
& \left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right) \leq\left(p_{i}\right)^{(5)} \leq\left(\hat{A}_{28}\right)^{(5)} \\
& \left(b_{i}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right) \leq\left(r_{i}\right)^{(5)} \leq\left(b_{i}^{\prime}\right)^{(5)} \leq\left(\hat{B}_{28}\right)^{(5)} \tag{123}
\end{align*}
$$

(P)

$$
\begin{gathered}
\lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)=\left(p_{i}\right)^{(5)} \\
\lim _{G \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(5)}\left(G_{31}, t\right)=\left(r_{i}\right)^{(5)}
\end{gathered}
$$

Definition of $\left(\hat{A}_{28}\right)^{(5)},\left(\hat{B}_{28}\right)^{(5)}$ :
Where $\left(\hat{A}_{28}\right)^{(5)},\left(\hat{B}_{28}\right)^{(5)},\left(p_{i}\right)^{(5)},\left(r_{i}\right)^{(5)}$ are positive constants and $i=28,29,30$
They satisfy Lipschitz condition:
$\left|\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)\right| \leq\left(\hat{k}_{28}\right)^{(5)}\left|T_{29}-T_{29}^{\prime}\right| e^{-\left(\widehat{M}_{28}\right)^{(5)} t}$
$\left|\left(b_{i}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right)^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right)\right|<\left(\hat{k}_{28}\right)^{(5)}\left\|\left(G_{31}\right)-\left(G_{31}\right)^{\prime}\right\| e^{-\left(\left(_{28}\right)^{(5)} t\right.}$
With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}^{\prime}, t\right)$ $\operatorname{and}\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right) \cdot\left(T_{29}^{\prime}, t\right)$ and $\left(T_{29}, t\right)$ are points belonging to the interval $\left[\left(\hat{k}_{28}\right)^{(5)},\left(\widehat{M}_{28}\right)^{(5)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{28}\right)^{(5)}=$ 5 then the function $\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.
Definition of $\left(\widehat{M}_{28}\right)^{(5)},\left(\hat{k}_{28}\right)^{(5)}$ :
$\left(\widehat{M}_{28}\right)^{(5)},\left(\hat{k}_{28}\right)^{(5)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(5)}}{\left(\widetilde{M}_{28}\right)^{(5)}}, \frac{\left(b_{i}\right)^{(5)}}{\left(\widetilde{M}_{28}\right)^{(5)}}<1
$$

Definition of $\left(\hat{P}_{28}\right)^{(5)},\left(\hat{Q}_{28}\right)^{(5)}$ :
There exists two constants $\left(\hat{P}_{28}\right)^{(5)}$ and $\left(\hat{Q}_{28}\right)^{(5)}$ which together with $\left(\widehat{M}_{28}\right)^{(5)},\left(\hat{k}_{28}\right)^{(5)},\left(\hat{A}_{28}\right)^{(5)}$ and $\left(\hat{B}_{28}\right)^{(5)}$ and the constants $\left(a_{i}\right)^{(5)},\left(a_{i}^{\prime}\right)^{(5)},\left(b_{i}\right)^{(5)},\left(b_{i}^{\prime}\right)^{(5)},\left(p_{i}\right)^{(5)},\left(r_{i}\right)^{(5)}, i=28,29,30, \quad$ satisfy the inequalities
$\frac{1}{\left(\hat{M}_{28}\right)^{(5)}}\left[\left(a_{i}\right)^{(5)}+\left(a_{i}^{\prime}\right)^{(5)}+\left(\hat{A}_{28}\right)^{(5)}+\left(\hat{P}_{28}\right)^{(5)}\left(\hat{k}_{28}\right)^{(5)}\right]<1$
$\frac{1}{\left(\hat{M}_{28}\right)^{(5)}}\left[\left(b_{i}\right)^{(5)}+\left(b_{i}^{\prime}\right)^{(5)}+\left(\hat{B}_{28}\right)^{(5)}+\left(\hat{Q}_{28}\right)^{(5)}\left(\hat{k}_{28}\right)^{(5)}\right]<1$
Where we suppose
$\left(a_{i}\right)^{(6)},\left(a_{i}^{\prime}\right)^{(6)},\left(a_{i}^{\prime \prime}\right)^{(6)},\left(b_{i}\right)^{(6)},\left(b_{i}^{\prime}\right)^{(6)},\left(b_{i}^{\prime \prime}\right)^{(6)}>0, \quad i, j=32,33,34$
(Q) The functions $\left(a_{i}^{\prime \prime}\right)^{(6)},\left(b_{i}^{\prime \prime}\right)^{(6)}$ are positive continuous increasing and bounded.

Definition of $\left(p_{i}\right)^{(6)},\left(r_{i}\right)^{(6)}$ :
$\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right) \leq\left(p_{i}\right)^{(6)} \leq\left(\hat{A}_{32}\right)^{(6)}$
$\left(b_{i}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right) \leq\left(r_{i}\right)^{(6)} \leq\left(b_{i}^{\prime}\right)^{(6)} \leq\left(\hat{B}_{32}\right)^{(6)}$
(R) $\quad \lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)=\left(p_{i}\right)^{(6)}$

$$
\lim _{\mathrm{G} \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right)=\left(r_{i}\right)^{(6)}
$$

Definition of $\left(\hat{A}_{32}\right)^{(6)},\left(\hat{B}_{32}\right)^{(6)}$ :

$$
\text { Where }\left(\hat{A}_{32}\right)^{(6)},\left(\hat{B}_{32}\right)^{(6)},\left(p_{i}\right)^{(6)},\left(r_{i}\right)^{(6)} \text { are positive constants and } i=32,33,34
$$

They satisfy Lipschitz condition:
$\left|\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)\right| \leq\left(\hat{k}_{32}\right)^{(6)}\left|T_{33}-T_{33}^{\prime}\right| e^{-\left(\widehat{M}_{32}\right)^{(6)} t}$
$\left|\left(b_{i}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right)^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right)\right|<\left(\hat{k}_{32}\right)^{(6)}\left\|\left(G_{35}\right)-\left(G_{35}\right)^{\prime}\right\| e^{-\left(\tilde{M}_{32}\right)^{(6)} t}$
With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}^{\prime}, t\right)$ $\operatorname{and}\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right) .\left(T_{33}^{\prime}, t\right)$ and $\left(T_{33}, t\right)$ are points belonging to the interval $\left[\left(\widehat{k}_{32}\right)^{(6)},\left(\widehat{M}_{32}\right)^{(6)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{32}\right)^{(6)}=$ 6 then the function $\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.
Definition of $\left(\widehat{M}_{32}\right)^{(6)},\left(\widehat{k}_{32}\right)^{(6)}$ :
$\left(\widehat{M}_{32}\right)^{(6)},\left(\hat{k}_{32}\right)^{(6)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(6)}}{\left(\widehat{M}_{32}\right)^{(6)}}, \frac{\left(b_{i}\right)^{(6)}}{\left(\widehat{M}_{32}\right)^{(6)}}<1
$$

Definition of $\left(\hat{P}_{32}\right)^{(6)},\left(\hat{Q}_{32}\right)^{(6)}$ :
There exists two constants $\left(\hat{P}_{32}\right)^{(6)}$ and $\left(\hat{Q}_{32}\right)^{(6)}$ which together with $\left(\widehat{M}_{32}\right)^{(6)},\left(\hat{k}_{32}\right)^{(6)},\left(\hat{A}_{32}\right)^{(6)}$ and $\left(\hat{B}_{32}\right)^{(6)}$ and the constants
$\left(a_{i}\right)^{(6)},\left(a_{i}^{\prime}\right)^{(6)},\left(b_{i}\right)^{(6)},\left(b_{i}^{\prime}\right)^{(6)},\left(p_{i}\right)^{(6)},\left(r_{i}\right)^{(6)}, i=32,33,34$,
satisfy the inequalities
$\frac{1}{\left(\widehat{M}_{32}\right)^{(6)}}\left[\left(a_{i}\right)^{(6)}+\left(a_{i}^{\prime}\right)^{(6)}+\left(\hat{A}_{32}\right)^{(6)}+\left(\hat{P}_{32}\right)^{(6)}\left(\hat{k}_{32}\right)^{(6)}\right]<1$
$\frac{1}{\left(\hat{M}_{32}\right)^{(6)}}\left[\left(b_{i}\right)^{(6)}+\left(b_{i}^{\prime}\right)^{(6)}+\left(\hat{B}_{32}\right)^{(6)}+\left(\hat{Q}_{32}\right)^{(6)}\left(\hat{k}_{32}\right)^{(6)}\right]<1$
Where we suppose

$$
\begin{aligned}
& \left(a_{i}\right)^{(7)},\left(a_{i}^{\prime}\right)^{(7)},\left(a_{i}^{\prime \prime}\right)^{(7)},\left(b_{i}\right)^{(7)},\left(b_{i}^{\prime}\right)^{(7)},\left(b_{i}^{\prime \prime}\right)^{(7)}>0 \\
& \quad i, j=36,37,38
\end{aligned}
$$

The functions $\left(a_{i}^{\prime \prime}\right)^{(7)},\left(b_{i}^{\prime \prime}\right)^{(7)}$ are positive continuous increasing and bounded.
Definition of $\left(p_{i}\right)^{(7)},\left(r_{i}\right)^{(7)}$ :

$$
\begin{aligned}
& \left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right) \leq\left(p_{i}\right)^{(7)} \leq\left(\hat{A}_{36}\right)^{(7)} \\
& \quad\left(b_{i}^{\prime \prime}\right)^{(7)}\left(G_{39}, t\right) \leq\left(r_{i}\right)^{(7)} \leq\left(b_{i}^{\prime}\right)^{(7)} \leq\left(\hat{B}_{36}\right)^{(7)} \\
& \lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)=\left(p_{i}\right)^{(7)} \\
& \lim _{\mathrm{G} \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right), t\right)=\left(r_{i}\right)^{(7)}
\end{aligned}
$$

Definition of $\left(\hat{A}_{36}\right)^{(7)},\left(\hat{B}_{36}\right)^{(7)}$ :
Where $\quad\left(\hat{A}_{36}\right)^{(7)},\left(\hat{B}_{36}\right)^{(7)},\left(p_{i}\right)^{(7)},\left(r_{i}\right)^{(7)}$ are positive constants and $i=36,37,38$

They satisfy Lipschitz condition:

$$
\begin{aligned}
& \left|\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)\right| \leq\left(\hat{k}_{36}\right)^{(7)}\left|T_{37}-T_{37}^{\prime}\right| e^{-\left(\widehat{M}_{36}\right)^{(7)} t} \\
& \left|\left(b_{i}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right)^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right), t\right)\right|<\left(\hat{k}_{36}\right)^{(7)}| |\left(G_{39}\right)-\left(G_{39}\right)^{\prime} \| e^{-\left(\widehat{M}_{36}\right)^{(7)} t}
\end{aligned}
$$

With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}^{\prime}, t\right)$ $\operatorname{and}\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right) .\left(T_{37}^{\prime}, t\right)$ and $\left(T_{37}, t\right)$ are points belonging to the interval $\left[\left(\widehat{k}_{36}\right)^{(7)},\left(\widehat{M}_{36}\right)^{(7)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{36}\right)^{(7)}=$ 7 then the function $\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.

## Definition of $\left(\widehat{M}_{36}\right)^{(7)},\left(\hat{k}_{36}\right)^{(7)}$ :

$\left(\widehat{M}_{36}\right)^{(7)},\left(\hat{k}_{36}\right)^{(7)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(7)}}{\left(M_{36}\right)^{(7)}}, \frac{\left(b_{i}\right)^{(7)}}{\left(M_{36}\right)^{(7)}}<1
$$

## Definition of $\left(\hat{P}_{36}\right)^{(7)},\left(\hat{Q}_{36}\right)^{(7)}$ :

There exists two constants $\left(\hat{P}_{36}\right)^{(7)}$ and $\left(\hat{Q}_{36}\right)^{(7)}$ which together with $\left(\widehat{M}_{36}\right)^{(7)},\left(\hat{k}_{36}\right)^{(7)},\left(\hat{A}_{36}\right)^{(7)}$ and $\left(\hat{B}_{36}\right)^{(7)}$ and the constants $\left(a_{i}\right)^{(7)},\left(a_{i}^{\prime}\right)^{(7)},\left(b_{i}\right)^{(7)},\left(b_{i}^{\prime}\right)^{(7)},\left(p_{i}\right)^{(7)},\left(r_{i}\right)^{(7)}, i=36,37,38$, satisfy the inequalities
$\frac{1}{\left(\widehat{M}_{36}\right)^{(7)}}\left[\left(a_{i}\right)^{(7)}+\left(a_{i}^{\prime}\right)^{(7)}+\left(\hat{A}_{36}\right)^{(7)}+\left(\hat{P}_{36}\right)^{(7)}\left(\hat{k}_{36}\right)^{(7)}\right]<1$
$\frac{1}{\left(\widehat{M}_{36}\right)^{(7)}}\left[\left(b_{i}\right)^{(7)}+\left(b_{i}^{\prime}\right)^{(7)}+\left(\hat{B}_{36}\right)^{(7)}+\left(\hat{Q}_{36}\right)^{(7)}\left(\hat{k}_{36}\right)^{(7)}\right]<1$
Where we suppose
A. $\left(a_{i}\right)^{(8)},\left(a_{i}^{\prime}\right)^{(8)},\left(a_{i}^{\prime \prime}\right)^{(8)},\left(b_{i}\right)^{(8)},\left(b_{i}^{\prime}\right)^{(8)},\left(b_{i}^{\prime \prime}\right)^{(8)}>0, \quad i, j=40,41,42$
B. The functions $\left(a_{i}^{\prime \prime}\right)^{(8)},\left(b_{i}^{\prime \prime}\right)^{(8)}$ are positive continuous increasing and bounded

Definition of $\left(p_{i}\right)^{(8)},\left(r_{i}\right)^{(8)}$ :
$\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right) \leq\left(p_{i}\right)^{(8)} \leq\left(\hat{A}_{40}\right)^{(8)}$
$\left(b_{i}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right) \leq\left(r_{i}\right)^{(8)} \leq\left(b_{i}^{\prime}\right)^{(8)} \leq\left(\hat{B}_{40}\right)^{(8)}$
C. $\lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)=\left(p_{i}\right)^{(8)}$
$\lim _{G \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right)=\left(r_{i}\right)^{(8)}$
Definition of $\left(\hat{A}_{40}\right)^{(8)},\left(\hat{B}_{40}\right)^{(8)}$ :
Where $\left(\hat{A}_{40}\right)^{(8)},\left(\hat{B}_{40}\right)^{(8)},\left(p_{i}\right)^{(8)},\left(r_{i}\right)^{(8)}$ are positive constants and $i=40,41,42$

They satisfy Lipschitz condition:
$\left|\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)\right| \leq\left(\hat{k}_{40}\right)^{(8)}\left|T_{41}-T_{41}^{\prime}\right| e^{-\left(\widehat{M}_{40}\right)^{(8)} t}$
$\left|\left(b_{i}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right)^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right)\right|<\left(\hat{k}_{40}\right)^{(8)}\left\|\left(G_{43}\right)-\left(G_{43}\right)^{\prime}\right\| e^{-\left(\widehat{M}_{40}\right)^{(8)} t}$
With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}^{\prime}, t\right)$ and $\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right) .\left(T_{41}^{\prime}, t\right)$ and $\left(T_{41}, t\right)$ are points belonging to the interval $\left[\left(\hat{k}_{40}\right)^{(8)},\left(\widehat{M}_{40}\right)^{(8)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{40}\right)^{(8)}=8$ then the function $\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.

Definition of $\left(\widehat{M}_{40}\right)^{(8)},\left(\hat{k}_{40}\right)^{(8)}$ :
D. $\left(\widehat{M}_{40}\right)^{(8)},\left(\hat{k}_{40}\right)^{(8)}$, are positive constants
$\frac{\left(a_{i}\right)^{(8)}}{\left(\widehat{M}_{40}\right)^{(8)}}, \frac{\left(b_{i}\right)^{(8)}}{\left(\widehat{M}_{40}\right)^{(8)}}<1$
Definition of $\left(\hat{P}_{40}\right)^{(8)},\left(\hat{Q}_{40}\right)^{(8)}$ :
E. There exists two constants $\left(\hat{P}_{40}\right)^{(8)}$ and $\left(\hat{Q}_{40}\right)^{(8)}$ which together with $\left(\widehat{M}_{40}\right)^{(8)},\left(\hat{k}_{40}\right)^{(8)},\left(\hat{A}_{40}\right)^{(8)}$ $\left(\hat{B}_{40}\right)^{(8)}$ and the constants $\left(a_{i}\right)^{(8)},\left(a_{i}^{\prime}\right)^{(8)},\left(b_{i}\right)^{(8)},\left(b_{i}^{\prime}\right)^{(8)},\left(p_{i}\right)^{(8)},\left(r_{i}\right)^{(8)}, i=40,41,42$, Satisfy the inequalities
$\frac{1}{\left(\widehat{M}_{40}\right)^{(8)}}\left[\left(a_{i}\right)^{(8)}+\left(a_{i}^{\prime}\right)^{(8)}+\left(\hat{A}_{40}\right)^{(8)}+\left(\hat{P}_{40}\right)^{(8)}\left(\hat{k}_{40}\right)^{(8)}\right]<1$
$\frac{1}{\left(\widehat{M}_{40}\right)^{(8)}}\left[\left(b_{i}\right)^{(8)}+\left(b_{i}^{\prime}\right)^{(8)}+\left(\hat{B}_{40}\right)^{(8)}+\left(\widehat{Q}_{40}\right)^{(8)}\left(\hat{k}_{40}\right)^{(8)}\right]<1$
Where we suppose
(X) $\quad\left(a_{i}\right)^{(9)},\left(a_{i}^{\prime}\right)^{(9)},\left(a_{i}^{\prime \prime}\right)^{(9)},\left(b_{i}\right)^{(9)},\left(b_{i}^{\prime}\right)^{(9)},\left(b_{i}^{\prime \prime}\right)^{(9)}>0$,
(Y) The functions $\left(a_{i}^{\prime \prime}\right)^{(9)},\left(b_{i}^{\prime \prime}\right)^{(9)}$ are positive continuous increasing and bounded.

Definition of $\left(p_{i}\right)^{(9)},\left(r_{i}\right)^{(9)}$ :
$\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right) \leq\left(p_{i}\right)^{(9)} \leq\left(\hat{A}_{44}\right)^{(9)}$
$\left(b_{i}^{\prime \prime}\right)^{(9)}(G, t) \leq\left(r_{i}\right)^{(9)} \leq\left(b_{i}^{\prime}\right)^{(9)} \leq\left(\widehat{B}_{44}\right)^{(9)}$
(Z) $\quad \lim _{T_{2} \rightarrow \infty}\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)=\left(p_{i}\right)^{(9)}$
$\lim _{G \rightarrow \infty}\left(b_{i}^{\prime \prime}\right)^{(9)}(G, t)=\left(r_{i}\right)^{(9)}$
Definition of $\left(\hat{A}_{44}\right)^{(9)},\left(\widehat{B}_{44}\right)^{(9)}$ :
Where $\quad\left(\hat{A}_{44}\right)^{(9)},\left(\hat{B}_{44}\right)^{(9)},\left(p_{i}\right)^{(9)},\left(r_{i}\right)^{(9)}$ are positive constants and $i=44,45,46$

They satisfy Lipschitz condition:

$$
\begin{aligned}
& \left|\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}^{\prime}, t\right)-\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)\right| \leq\left(\hat{k}_{44}\right)^{(9)}\left|T_{45}-T_{45}^{\prime}\right| e^{-\left(\widehat{M}_{44}\right)^{(9)} t} \\
& \left|\left(b_{i}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right)^{\prime}, t\right)-\left(b_{i}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right), t\right)\right|<\left(\hat{k}_{44}\right)^{(9)}| |\left(G_{47}\right)-\left(G_{47}\right)^{\prime}| | e^{-\left(\widehat{M}_{44}\right)^{(9)} t}
\end{aligned}
$$

With the Lipschitz condition, we place a restriction on the behavior of functions $\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}^{\prime}, t\right)$ $\operatorname{and}\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right) \cdot\left(T_{45}^{\prime}, t\right)$ and $\left(T_{45}, t\right)$ are points belonging to the interval $\left[\left(\hat{k}_{44}\right)^{(9)},\left(\widehat{M}_{44}\right)^{(9)}\right]$. It is to be noted that $\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)$ is uniformly continuous. In the eventuality of the fact, that if $\left(\widehat{M}_{44}\right)^{(9)}=$ 1 then the function $\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)$, the first augmentation coefficient attributable to terrestrial organisms, would be absolutely continuous.

Definition of $\left(\widehat{M}_{44}\right)^{(9)},\left(\hat{k}_{44}\right)^{(9)}$ :
(AA) $\quad\left(\widehat{M}_{44}\right)^{(9)},\left(\hat{k}_{44}\right)^{(9)}$, are positive constants

$$
\frac{\left(a_{i}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}, \frac{\left(b_{i}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}<1
$$

Definition of $\left(\hat{P}_{44}\right)^{(9)},\left(\hat{Q}_{44}\right)^{(9)}$ :
(BB) There exists two constants $\left(\hat{P}_{44}\right)^{(9)}$ and $\left(\hat{Q}_{44}\right)^{(9)}$ which together with $\left(\widehat{M}_{44}\right)^{(9)},\left(\hat{k}_{44}\right)^{(9)},\left(\hat{A}_{44}\right)^{(9)}$ and $\left(\widehat{B}_{44}\right)^{(9)}$ and the constants $\left(a_{i}\right)^{(9)},\left(a_{i}^{\prime}\right)^{(9)},\left(b_{i}\right)^{(9)},\left(b_{i}^{\prime}\right)^{(9)},\left(p_{i}\right)^{(9)},\left(r_{i}\right)^{(9)}, i=44,45,46$, satisfy the inequalities

$$
\begin{aligned}
& \frac{1}{\left(\widehat{M}_{44}\right)^{(9)}}\left[\left(a_{i}\right)^{(9)}+\left(a_{i}^{\prime}\right)^{(9)}+\left(\hat{A}_{44}\right)^{(9)}+\left(\hat{P}_{44}\right)^{(9)}\left(\hat{k}_{44}\right)^{(9)}\right]<1 \\
& \frac{1}{\left(\widehat{M}_{44}\right)^{(9)}}\left[\left(b_{i}\right)^{(9)}+\left(b_{i}^{\prime}\right)^{(9)}+\left(\hat{B}_{44}\right)^{(9)}+\left(\widehat{Q}_{44}\right)^{(9)}\left(\hat{k}_{44}\right)^{(9)}\right]<1
\end{aligned}
$$

Theorem 1: if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0)$ :
$\begin{array}{ll}G_{i}(t) \leq\left(\hat{P}_{13}\right)^{(1)} e^{\left(\widehat{M}_{13}\right)^{(1)} t}, & G_{i}(0)=G_{i}^{0}>0 \\ T_{i}(t) \leq\left(\widehat{Q}_{13}\right)^{(1)} e^{\left(\widehat{M}_{13}\right)^{(1)} t}, & T_{i}(0)=T_{i}^{0}>0\end{array}$

Theorem 2: if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0)$
$G_{i}(t) \leq\left(\hat{P}_{16}\right)^{(2)} e^{\left(\hat{M}_{16}\right)^{(2)} t}, \quad G_{i}(0)=G_{i}^{0}>0$
$T_{i}(t) \leq\left(\widehat{Q}_{16}\right)^{(2)} e^{\left(\widehat{M}_{16}\right)^{(2)} t} \quad, \quad T_{i}(0)=T_{i}^{0}>0$
Theorem 3 : if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
$G_{i}(t) \leq\left(\hat{P}_{20}\right)^{(3)} e^{\left(\widehat{M}_{20}\right)^{(3)} t}, \quad G_{i}(0)=G_{i}^{0}>0$
$T_{i}(t) \leq\left(\hat{Q}_{20}\right)^{(3)} e^{\left(M_{20}\right)^{(3)} t} \quad, \quad T_{i}(0)=T_{i}^{0}>0$
Theorem 4 : if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0)$ :
$G_{i}(t) \leq\left(\hat{P}_{24}\right)^{(4)} e^{\left(\widehat{M}_{24}\right)^{(4)} t}, G_{i}(0)=G_{i}^{0}>0$
$T_{i}(t) \leq\left(\widehat{Q}_{24}\right)^{(4)} e^{\left(M_{24}\right)^{(4)} t}, \quad T_{i}(0)=T_{i}^{0}>0$
Theorem 5 : if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0)$ :
$G_{i}(t) \leq\left(\hat{P}_{28}\right)^{(5)} e^{\left(\widehat{M}_{28}\right)^{(5)} t}, \quad G_{i}(0)=G_{i}^{0}>0$
$T_{i}(t) \leq\left(\widehat{Q}_{28}\right)^{(5)} e^{\left(\widehat{M}_{28}\right)^{(5)} t} \quad, \quad T_{i}(0)=T_{i}^{0}>0$
Theorem 6 : if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0)$ :
$\begin{array}{ll}G_{i}(t) \leq\left(\widehat{P}_{32}\right)^{(6)} e^{\left(\widehat{M}_{32}\right)^{(6)} t}, G_{i}(0)=G_{i}^{0}>0 \\ T_{i}(t) \leq\left(\hat{Q}_{32}\right)^{(6)} e^{\left(\widehat{(M}_{32}\right)^{(6)} t} & , \quad T_{i}(0)=T_{i}^{0}>0\end{array}$
Theorem 7: if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0):$

$$
\begin{array}{ll}
G_{i}(t) \leq\left(\hat{P}_{36}\right)^{(7)} e^{\left(\widehat{M}_{36}\right)^{(7)} t}, & G_{i}(0)=G_{i}^{0}>0 \\
T_{i}(t) \leq\left(\widehat{Q}_{36}\right)^{(7)} e^{\left(\widehat{M}_{36}\right)^{(7)} t} & , \quad T_{i}(0)=T_{i}^{0}>0
\end{array}
$$

Theorem 8: if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0):$
$G_{i}(t) \leq\left(\hat{P}_{40}\right)^{(8)} e^{\left(\widehat{M}_{40}\right)^{(8)} t}, \quad G_{i}(0)=G_{i}^{0}>0$
$T_{i}(t) \leq\left(\hat{Q}_{40}\right)^{(8)} e^{\left(\widehat{M}_{40}\right)^{(8)} t} \quad, T_{i}(0)=T_{i}^{0}>0$
Theorem 9: if the conditions (A)-(E) above are fulfilled, there exists a solution satisfying the conditions
Definition of $G_{i}(0), T_{i}(0)$ :
$\begin{array}{ll}G_{i}(t) \leq\left(\hat{P}_{44}\right)^{(9)} e^{\left(\widehat{M}_{44}\right)^{(9)} t}, \quad G_{i}(0)=G_{i}^{0}>0 \\ T_{i}(t) \leq\left(\widehat{Q}_{44}\right)^{(9)} e^{\left(\widehat{(M 44 ~}^{(9)} t\right.}, & T_{i}(0)=T_{i}^{0}>0\end{array}$
Proof: Consider operator $\mathcal{A}^{(1)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow$ $\mathbb{R}_{+}$which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{13}\right)^{(1)}, T_{i}^{0} \leq\left(\hat{Q}_{13}\right)^{(1)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{13}\right)^{(1)} e^{\left(\widehat{M}_{13}\right)^{(1)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\widehat{Q}_{13}\right)^{(1)} e^{\left(\widehat{M}_{13}\right)^{(1)} t}$
By
$\left.\bar{G}_{13}(t)=G_{13}^{0}+\int_{0}^{t}\left[\left(a_{13}\right)^{(1)} G_{14}\left(s_{(13)}\right)-\left(\left(a_{13}^{\prime}\right)^{(1)}+a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}\left(s_{(13)}\right), s_{(13)}\right)\right) G_{13}\left(s_{(13)}\right)\right] d s_{(13)}$
$\bar{G}_{14}(t)=G_{14}^{0}+\int_{0}^{t}\left[\left(a_{14}\right)^{(1)} G_{13}\left(s_{(13)}\right)-\left(\left(a_{14}^{\prime}\right)^{(1)}+\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}\left(s_{(13)}\right), s_{(13)}\right)\right) G_{14}\left(s_{(13)}\right)\right] d s_{(13)}$
$\bar{G}_{15}(t)=G_{15}^{0}+\int_{0}^{t}\left[\left(a_{15}\right)^{(1)} G_{14}\left(s_{(13)}\right)-\left(\left(a_{15}^{\prime}\right)^{(1)}+\left(a_{15}^{\prime \prime}\right)^{(1)}\left(T_{14}\left(s_{(13)}\right), s_{(13)}\right)\right) G_{15}\left(s_{(13)}\right)\right] d s_{(13)}$
$\bar{T}_{13}(t)=T_{13}^{0}+\int_{0}^{t}\left[\left(b_{13}\right)^{(1)} T_{14}\left(s_{(13)}\right)-\left(\left(b_{13}^{\prime}\right)^{(1)}-\left(b_{13}^{\prime \prime}\right)^{(1)}\left(G\left(s_{(13)}\right), s_{(13)}\right)\right) T_{13}\left(s_{(13)}\right)\right] d s_{(13)}$
$\bar{T}_{14}(t)=T_{14}^{0}+\int_{0}^{t}\left[\left(b_{14}\right)^{(1)} T_{13}\left(s_{(13)}\right)-\left(\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{14}^{\prime \prime}\right)^{(1)}\left(G\left(s_{(13)}\right), s_{(13)}\right)\right) T_{14}\left(s_{(13)}\right)\right] d s_{(13)}$
$\overline{\mathrm{T}}_{15}(\mathrm{t})=\mathrm{T}_{15}^{0}+\int_{0}^{t}\left[\left(b_{15}\right)^{(1)} T_{14}\left(s_{(13)}\right)-\left(\left(b_{15}^{\prime}\right)^{(1)}-\left(b_{15}^{\prime \prime}\right)^{(1)}\left(G\left(s_{(13)}\right), s_{(13)}\right)\right) T_{15}\left(s_{(13)}\right)\right] d s_{(13)}$
Where $s_{(13)}$ is the integrand that is integrated over an interval $(0, t)$

## Proof:

Consider operator $\mathcal{A}^{(2)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$ which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{16}\right)^{(2)}, T_{i}^{0} \leq\left(\hat{Q}_{16}\right)^{(2)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{16}\right)^{(2)} e^{\left(\widehat{M}_{16}\right)^{(2)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\widehat{Q}_{16}\right)^{(2)} e^{\left(\widehat{M}_{16}\right)^{(2)} t}$
By
$\left.\bar{G}_{16}(t)=G_{16}^{0}+\int_{0}^{t}\left[\left(a_{16}\right)^{(2)} G_{17}\left(s_{(16)}\right)-\left(\left(a_{16}^{\prime}\right)^{(2)}+a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}\left(s_{(16)}\right), s_{(16)}\right)\right) G_{16}\left(s_{(16)}\right)\right] d s_{(16)}$
$\bar{G}_{17}(t)=G_{17}^{0}+\int_{0}^{t}\left[\left(a_{17}\right)^{(2)} G_{16}\left(s_{(16)}\right)-\left(\left(a_{17}^{\prime}\right)^{(2)}+\left(a_{17}^{\prime \prime}\right)^{(2)}\left(T_{17}\left(s_{(16)}\right), s_{(17)}\right)\right) G_{17}\left(s_{(16)}\right)\right] d s_{(16)}$
$\bar{G}_{18}(t)=G_{18}^{0}+\int_{0}^{t}\left[\left(a_{18}\right)^{(2)} G_{17}\left(s_{(16)}\right)-\left(\left(a_{18}^{\prime}\right)^{(2)}+\left(a_{18}^{\prime \prime}\right)^{(2)}\left(T_{17}\left(s_{(16)}\right), s_{(16)}\right)\right) G_{18}\left(s_{(16)}\right)\right] d s_{(16)}$
$\bar{T}_{16}(t)=T_{16}^{0}+\int_{0}^{t}\left[\left(b_{16}\right)^{(2)} T_{17}\left(s_{(16)}\right)-\left(\left(b_{16}^{\prime}\right)^{(2)}-\left(b_{16}^{\prime \prime}\right)^{(2)}\left(G\left(s_{(16)}\right), s_{(16)}\right)\right) T_{16}\left(s_{(16)}\right)\right] d s_{(16)}$
$\bar{T}_{17}(t)=T_{17}^{0}+\int_{0}^{t}\left[\left(b_{17}\right)^{(2)} T_{16}\left(s_{(16)}\right)-\left(\left(b_{17}^{\prime}\right)^{(2)}-\left(b_{17}^{\prime \prime}\right)^{(2)}\left(G\left(s_{(16)}\right), s_{(16)}\right)\right) T_{17}\left(s_{(16)}\right)\right] d s_{(16)}$
$\bar{T}_{18}(t)=T_{18}^{0}+\int_{0}^{t}\left[\left(b_{18}\right)^{(2)} T_{17}\left(s_{(16)}\right)-\left(\left(b_{18}^{\prime}\right)^{(2)}-\left(b_{18}^{\prime \prime}\right)^{(2)}\left(G\left(s_{(16)}\right), s_{(16)}\right)\right) T_{18}\left(s_{(16)}\right)\right] d s_{(16)}$
Where $s_{(16)}$ is the integrand that is integrated over an interval $(0, t)$

## Proof:

Consider operator $\mathcal{A}^{(3)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$ which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{20}\right)^{(3)}, T_{i}^{0} \leq\left(\hat{Q}_{20}\right)^{(3)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{20}\right)^{(3)} e^{\left(\widehat{M}_{20}\right)^{(3)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\hat{Q}_{20}\right)^{(3)} e^{\left(\widehat{M}_{20}\right)^{(3)} t}$
By
$\left.\bar{G}_{20}(t)=G_{20}^{0}+\int_{0}^{t}\left[\left(a_{20}\right)^{(3)} G_{21}\left(s_{(20)}\right)-\left(\left(a_{20}^{\prime}\right)^{(3)}+a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}\left(s_{(20)}\right), s_{(20)}\right)\right) G_{20}\left(s_{(20)}\right)\right] d s_{(20)}$
$\bar{G}_{21}(t)=G_{21}^{0}+\int_{0}^{t}\left[\left(a_{21}\right)^{(3)} G_{20}\left(s_{(20)}\right)-\left(\left(a_{21}^{\prime}\right)^{(3)}+\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}\left(s_{(20)}\right), s_{(20)}\right)\right) G_{21}\left(s_{(20)}\right)\right] d s_{(20)}$
$\bar{G}_{22}(t)=G_{22}^{0}+\int_{0}^{t}\left[\left(a_{22}\right)^{(3)} G_{21}\left(s_{(20)}\right)-\left(\left(a_{22}^{\prime}\right)^{(3)}+\left(a_{22}^{\prime \prime}\right)^{(3)}\left(T_{21}\left(s_{(20)}\right), s_{(20)}\right)\right) G_{22}\left(s_{(20)}\right)\right] d s_{(20)}$
$\bar{T}_{20}(t)=T_{20}^{0}+\int_{0}^{t}\left[\left(b_{20}\right)^{(3)} T_{21}\left(s_{(20)}\right)-\left(\left(b_{20}^{\prime}\right)^{(3)}-\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G\left(s_{(20)}\right), s_{(20)}\right)\right) T_{20}\left(s_{(20)}\right)\right] d s_{(20)}$
$\bar{T}_{21}(t)=T_{21}^{0}+\int_{0}^{t}\left[\left(b_{21}\right)^{(3)} T_{20}\left(s_{(20)}\right)-\left(\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{21}^{\prime \prime}\right)^{(3)}\left(G\left(s_{(20)}\right), s_{(20)}\right)\right) T_{21}\left(s_{(20)}\right)\right] d s_{(20)}$
$\overline{\mathrm{T}}_{22}(\mathrm{t})=\mathrm{T}_{22}^{0}+\int_{0}^{t}\left[\left(b_{22}\right)^{(3)} T_{21}\left(s_{(20)}\right)-\left(\left(b_{22}^{\prime}\right)^{(3)}-\left(b_{22}^{\prime \prime}\right)^{(3)}\left(G\left(s_{(20)}\right), s_{(20)}\right)\right) T_{22}\left(s_{(20)}\right)\right] d s_{(20)}$
Where $s_{(20)}$ is the integrand that is integrated over an interval $(0, t)$
Proof: Consider operator $\mathcal{A}^{(4)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow$ $\mathbb{R}_{+}$which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{24}\right)^{(4)}, T_{i}^{0} \leq\left(\hat{Q}_{24}\right)^{(4)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{24}\right)^{(4)} e^{\left(\widehat{M}_{24}\right)^{(4)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\hat{Q}_{24}\right)^{(4)} e^{\left(\widehat{M}_{24}\right)^{(4)} t}$
By
$\left.\bar{G}_{24}(t)=G_{24}^{0}+\int_{0}^{t}\left[\left(a_{24}\right)^{(4)} G_{25}\left(s_{(24)}\right)-\left(\left(a_{24}^{\prime}\right)^{(4)}+a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}\left(s_{(24)}\right), s_{(24)}\right)\right) G_{24}\left(s_{(24)}\right)\right] d s_{(24)}$
$\bar{G}_{25}(t)=G_{25}^{0}+\int_{0}^{t}\left[\left(a_{25}\right)^{(4)} G_{24}\left(s_{(24)}\right)-\left(\left(a_{25}^{\prime}\right)^{(4)}+\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}\left(s_{(24)}\right), s_{(24)}\right)\right) G_{25}\left(s_{(24)}\right)\right] d s_{(24)}$
$\bar{G}_{26}(t)=G_{26}^{0}+\int_{0}^{t}\left[\left(a_{26}\right)^{(4)} G_{25}\left(s_{(24)}\right)-\left(\left(a_{26}^{\prime}\right)^{(4)}+\left(a_{26}^{\prime \prime}\right)^{(4)}\left(T_{25}\left(s_{(24)}\right), s_{(24)}\right)\right) G_{26}\left(s_{(24)}\right)\right] d s_{(24)}$
$\bar{T}_{24}(t)=T_{24}^{0}+\int_{0}^{t}\left[\left(b_{24}\right)^{(4)} T_{25}\left(s_{(24)}\right)-\left(\left(b_{24}^{\prime}\right)^{(4)}-\left(b_{24}^{\prime \prime}\right)^{(4)}\left(G\left(s_{(24)}\right), s_{(24)}\right)\right) T_{24}\left(s_{(24)}\right)\right] d s_{(24)}$
$\bar{T}_{25}(t)=T_{25}^{0}+\int_{0}^{t}\left[\left(b_{25}\right)^{(4)} T_{24}\left(s_{(24)}\right)-\left(\left(b_{25}^{\prime}\right)^{(4)}-\left(b_{25}^{\prime \prime}\right)^{(4)}\left(G\left(s_{(24)}\right), s_{(24)}\right)\right) T_{25}\left(s_{(24)}\right)\right] d s_{(24)}$
$\overline{\mathrm{T}}_{26}(\mathrm{t})=\mathrm{T}_{26}^{0}+\int_{0}^{t}\left[\left(b_{26}\right)^{(4)} T_{25}\left(s_{(24)}\right)-\left(\left(b_{26}^{\prime}\right)^{(4)}-\left(b_{26}^{\prime \prime}\right)^{(4)}\left(G\left(s_{(24)}\right), s_{(24)}\right)\right) T_{26}\left(s_{(24)}\right)\right] d s_{(24)}$
Where $s_{(24)}$ is the integrand that is integrated over an interval $(0, t)$
Proof: Consider operator $\mathcal{A}^{(5)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow$ $\mathbb{R}_{+}$which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{28}\right)^{(5)}, T_{i}^{0} \leq\left(\hat{Q}_{28}\right)^{(5)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{28}\right)^{(5)} e^{\left(\widehat{M}_{28}\right)^{(5)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\hat{Q}_{28}\right)^{(5)} e^{\left(\widehat{M}_{28}\right)^{(5)} t}$
By
$\left.\bar{G}_{28}(t)=G_{28}^{0}+\int_{0}^{t}\left[\left(a_{28}\right)^{(5)} G_{29}\left(s_{(28)}\right)-\left(\left(a_{28}^{\prime}\right)^{(5)}+a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}\left(s_{(28)}\right), s_{(28)}\right)\right) G_{28}\left(s_{(28)}\right)\right] d s_{(28)}$
$\bar{G}_{29}(t)=G_{29}^{0}+\int_{0}^{t}\left[\left(a_{29}\right)^{(5)} G_{28}\left(s_{(28)}\right)-\left(\left(a_{29}^{\prime}\right)^{(5)}+\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}\left(s_{(28)}\right), s_{(28)}\right)\right) G_{29}\left(s_{(28)}\right)\right] d s_{(28)}$
$\bar{G}_{30}(t)=G_{30}^{0}+\int_{0}^{t}\left[\left(a_{30}\right)^{(5)} G_{29}\left(s_{(28)}\right)-\left(\left(a_{30}^{\prime}\right)^{(5)}+\left(a_{30}^{\prime \prime}\right)^{(5)}\left(T_{29}\left(s_{(28)}\right), s_{(28)}\right)\right) G_{30}\left(s_{(28)}\right)\right] d s_{(28)}$
$\bar{T}_{28}(t)=T_{28}^{0}+\int_{0}^{t}\left[\left(b_{28}\right)^{(5)} T_{29}\left(s_{(28)}\right)-\left(\left(b_{28}^{\prime}\right)^{(5)}-\left(b_{28}^{\prime \prime}\right)^{(5)}\left(G\left(s_{(28)}\right), s_{(28)}\right)\right) T_{28}\left(s_{(28)}\right)\right] d s_{(28)}$
$\bar{T}_{29}(t)=T_{29}^{0}+\int_{0}^{t}\left[\left(b_{29}\right)^{(5)} T_{28}\left(s_{(28)}\right)-\left(\left(b_{29}^{\prime}\right)^{(5)}-\left(b_{29}^{\prime \prime}\right)^{(5)}\left(G\left(s_{(28)}\right), s_{(28)}\right)\right) T_{29}\left(s_{(28)}\right)\right] d s_{(28)}$
$\overline{\mathrm{T}}_{30}(\mathrm{t})=\mathrm{T}_{30}^{0}+\int_{0}^{t}\left[\left(b_{30}\right)^{(5)} T_{29}\left(s_{(28)}\right)-\left(\left(b_{30}^{\prime}\right)^{(5)}-\left(b_{30}^{\prime \prime}\right)^{(5)}\left(G\left(s_{(28)}\right), s_{(28)}\right)\right) T_{30}\left(s_{(28)}\right)\right] d s_{(28)}$
Where $s_{(28)}$ is the integrand that is integrated over an interval $(0, t)$

## Proof:

Consider operator $\mathcal{A}^{(6)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$ which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{32}\right)^{(6)}, T_{i}^{0} \leq\left(\hat{Q}_{32}\right)^{(6)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{32}\right)^{(6)} e^{\left(\hat{M}_{32}\right)^{(6)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\widehat{Q}_{32}\right)^{(6)} e^{\left(\widehat{M}_{32}\right)^{(6)} t}$
By
$\left.\bar{G}_{32}(t)=G_{32}^{0}+\int_{0}^{t}\left[\left(a_{32}\right)^{(6)} G_{33}\left(s_{(32)}\right)-\left(\left(a_{32}^{\prime}\right)^{(6)}+a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}\left(s_{(32)}\right), s_{(32)}\right)\right) G_{32}\left(s_{(32)}\right)\right] d s_{(32)}$
$\bar{G}_{33}(t)=G_{33}^{0}+\int_{0}^{t}\left[\left(a_{33}\right)^{(6)} G_{32}\left(s_{(32)}\right)-\left(\left(a_{33}^{\prime}\right)^{(6)}+\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}\left(s_{(32)}\right), s_{(32)}\right)\right) G_{33}\left(s_{(32)}\right)\right] d s_{(32)}$
$\bar{G}_{34}(t)=G_{34}^{0}+\int_{0}^{t}\left[\left(a_{34}\right)^{(6)} G_{33}\left(s_{(32)}\right)-\left(\left(a_{34}^{\prime}\right)^{(6)}+\left(a_{34}^{\prime \prime}\right)^{(6)}\left(T_{33}\left(s_{(32)}\right), s_{(32)}\right)\right) G_{34}\left(s_{(32)}\right)\right] d s_{(32)}$
$\bar{T}_{32}(t)=T_{32}^{0}+\int_{0}^{t}\left[\left(b_{32}\right)^{(6)} T_{33}\left(s_{(32)}\right)-\left(\left(b_{32}^{\prime}\right)^{(6)}-\left(b_{32}^{\prime \prime}\right)^{(6)}\left(G\left(s_{(32)}\right), s_{(32)}\right)\right) T_{32}\left(s_{(32)}\right)\right] d s_{(32)}$
$\bar{T}_{33}(t)=T_{33}^{0}+\int_{0}^{t}\left[\left(b_{33}\right)^{(6)} T_{32}\left(s_{(32)}\right)-\left(\left(b_{33}^{\prime}\right)^{(6)}-\left(b_{33}^{\prime \prime}\right)^{(6)}\left(G\left(s_{(32)}\right), s_{(32)}\right)\right) T_{33}\left(s_{(32)}\right)\right] d s_{(32)}$
$\overline{\mathrm{T}}_{34}(\mathrm{t})=\mathrm{T}_{34}^{0}+\int_{0}^{t}\left[\left(b_{34}\right)^{(6)} T_{33}\left(s_{(32)}\right)-\left(\left(b_{34}^{\prime}\right)^{(6)}-\left(b_{34}^{\prime \prime}\right)^{(6)}\left(G\left(s_{(32)}\right), s_{(32)}\right)\right) T_{34}\left(s_{(32)}\right)\right] d s_{(32)}$
Where $s_{(32)}$ is the integrand that is integrated over an interval $(0, t)$

## Proof:

Consider operator $\mathcal{A}^{(7)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$ which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{36}\right)^{(7)}, T_{i}^{0} \leq\left(\widehat{Q}_{36}\right)^{(7)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{36}\right)^{(7)} e^{\left(\widehat{M}_{36}\right)^{(7)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\widehat{Q}_{36}\right)^{(7)} e^{\left(\widehat{M}_{36}\right)^{(7)} t}$

By
$\left.\bar{G}_{36}(t)=G_{36}^{0}+\int_{0}^{t}\left[\left(a_{36}\right)^{(7)} G_{37}\left(s_{(36)}\right)-\left(\left(a_{36}^{\prime}\right)^{(7)}+a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}\left(s_{(36)}\right), s_{(36)}\right)\right) G_{36}\left(s_{(36)}\right)\right] d s_{(36)}$
$\bar{G}_{37}(t)=G_{37}^{0}+\int_{0}^{t}\left[\left(a_{37}\right)^{(7)} G_{36}\left(s_{(36)}\right)-\left(\left(a_{37}^{\prime}\right)^{(7)}+\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}\left(s_{(36)}\right), s_{(36)}\right)\right) G_{37}\left(s_{(36)}\right)\right] d s_{(36)}$
$\bar{G}_{38}(t)=G_{38}^{0}+\int_{0}^{t}\left[\left(a_{38}\right)^{(7)} G_{37}\left(s_{(36)}\right)-\left(\left(a_{38}^{\prime}\right)^{(7)}+\left(a_{38}^{\prime \prime}\right)^{(7)}\left(T_{37}\left(s_{(36)}\right), s_{(36)}\right)\right) G_{38}\left(s_{(36)}\right)\right] d s_{(36)}$
$\bar{T}_{36}(t)=T_{36}^{0}+\int_{0}^{t}\left[\left(b_{36}\right)^{(7)} T_{37}\left(s_{(36)}\right)-\left(\left(b_{36}^{\prime}\right)^{(7)}-\left(b_{36}^{\prime \prime}\right)^{(7)}\left(G\left(s_{(36)}\right), s_{(36)}\right)\right) T_{36}\left(s_{(36)}\right)\right] d s_{(36)}$
$\bar{T}_{37}(t)=T_{37}^{0}+\int_{0}^{t}\left[\left(b_{37}\right)^{(7)} T_{36}\left(s_{(36)}\right)-\left(\left(b_{37}^{\prime}\right)^{(7)}-\left(b_{37}^{\prime \prime}\right)^{(7)}\left(G\left(s_{(36)}\right), s_{(36)}\right)\right) T_{37}\left(s_{(36)}\right)\right] d s_{(36)}$
$\overline{\mathrm{T}}_{38}(\mathrm{t})=\mathrm{T}_{38}^{0}+\int_{0}^{t}\left[\left(b_{38}\right)^{(7)} T_{37}\left(s_{(36)}\right)-\left(\left(b_{38}^{\prime}\right)^{(7)}-\left(b_{38}^{\prime \prime}\right)^{(7)}\left(G\left(s_{(36)}\right), s_{(36)}\right)\right) T_{38}\left(s_{(36)}\right)\right] d s_{(36)}$
Where $s_{(36)}$ is the integrand that is integrated over an interval $(0, t)$

## Proof:

Consider operator $\mathcal{A}^{(8)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$ which satisfy
$G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{40}\right)^{(8)}, T_{i}^{0} \leq\left(\hat{Q}_{40}\right)^{(8)}$,
$0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{40}\right)^{(8)} e^{\left(\widehat{M}_{40}\right)^{(8)} t}$
$0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\widehat{Q}_{40}\right)^{(8)} e^{\left(\widehat{M}_{40}\right)^{(8)} t}$
By
$\left.\bar{G}_{40}(t)=G_{40}^{0}+\int_{0}^{t}\left[\left(a_{40}\right)^{(8)} G_{41}\left(s_{(40)}\right)-\left(\left(a_{40}^{\prime}\right)^{(8)}+a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}\left(s_{(40)}\right), s_{(40)}\right)\right) G_{40}\left(s_{(40)}\right)\right] d s_{(40)}$
$\bar{G}_{41}(t)=G_{41}^{0}+\int_{0}^{t}\left[\left(a_{41}\right)^{(8)} G_{40}\left(s_{(40)}\right)-\left(\left(a_{41}^{\prime}\right)^{(8)}+\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}\left(s_{(40)}\right), s_{(40)}\right)\right) G_{41}\left(s_{(40)}\right)\right] d s_{(40)}$
$\bar{G}_{42}(t)=G_{42}^{0}+\int_{0}^{t}\left[\left(a_{42}\right)^{(8)} G_{41}\left(s_{(40)}\right)-\left(\left(a_{42}^{\prime}\right)^{(8)}+\left(a_{42}^{\prime \prime}\right)^{(8)}\left(T_{41}\left(s_{(40)}\right), s_{(40)}\right)\right) G_{42}\left(s_{(40)}\right)\right] d s_{(40)}$
$\bar{T}_{40}(t)=T_{40}^{0}+\int_{0}^{t}\left[\left(b_{40}\right)^{(8)} T_{41}\left(s_{(40)}\right)-\left(\left(b_{40}^{\prime}\right)^{(8)}-\left(b_{40}^{\prime \prime}\right)^{(8)}\left(G\left(s_{(40)}\right), s_{(40)}\right)\right) T_{40}\left(s_{(40)}\right)\right] d s_{(40)}$
$\bar{T}_{41}(t)=T_{41}^{0}+\int_{0}^{t}\left[\left(b_{41}\right)^{(8)} T_{40}\left(s_{(40)}\right)-\left(\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{41}^{\prime \prime}\right)^{(8)}\left(G\left(s_{(40)}\right), s_{(40)}\right)\right) T_{41}\left(s_{(40)}\right)\right] d s_{(40)}$
$\overline{\mathrm{T}}_{42}(\mathrm{t})=\mathrm{T}_{42}^{0}+\int_{0}^{t}\left[\left(b_{42}\right)^{(8)} T_{41}\left(s_{(40)}\right)-\left(\left(b_{42}^{\prime}\right)^{(8)}-\left(b_{42}^{\prime \prime}\right)^{(8)}\left(G\left(s_{(40)}\right), s_{(40)}\right)\right) T_{42}\left(s_{(40)}\right)\right] d s_{(40)}$
Where $S_{(40)}$ is the integrand that is integrated over an interval $(0, t)$

## Proof:

Consider operator $\mathcal{A}^{(9)}$ defined on the space of sextuples of continuous functions $G_{i}, T_{i}: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$A which satisfy

$$
\begin{aligned}
& G_{i}(0)=G_{i}^{0}, T_{i}(0)=T_{i}^{0}, G_{i}^{0} \leq\left(\hat{P}_{44}\right)^{(9)}, T_{i}^{0} \leq\left(\widehat{Q}_{44}\right)^{(9)}, \\
& 0 \leq G_{i}(t)-G_{i}^{0} \leq\left(\hat{P}_{44}\right)^{(9)} e^{\left(\widehat{M}_{44}\right)^{(9)} t} \\
& 0 \leq T_{i}(t)-T_{i}^{0} \leq\left(\hat{Q}_{44}\right)^{(9)} e^{\left(\widehat{M}_{44}\right)^{(9)} t} \\
& \text { By } \\
& \left.\bar{G}_{44}(t)=G_{44}^{0}+\int_{0}^{t}\left[\left(a_{44}\right)^{(9)} G_{45}\left(s_{(44)}\right)-\left(\left(a_{44}^{\prime}\right)^{(9)}+a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}\left(s_{(44)}\right), s_{(44)}\right)\right) G_{44}\left(s_{(44)}\right)\right] d s_{(44)}
\end{aligned}
$$

$$
\begin{aligned}
& \bar{G}_{45}(t)=G_{45}^{0}+\int_{0}^{t}\left[\left(a_{45}\right)^{(9)} G_{44}\left(s_{(44)}\right)-\left(\left(a_{45}^{\prime}\right)^{(9)}+\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}\left(s_{(44)}\right), s_{(44)}\right)\right) G_{45}\left(s_{(44)}\right)\right] d s_{(44)} \\
& \bar{G}_{46}(t)=G_{46}^{0}+\int_{0}^{t}\left[\left(a_{46}\right)^{(9)} G_{45}\left(s_{(44)}\right)-\left(\left(a_{46}^{\prime}\right)^{(9)}+\left(a_{46}^{\prime \prime}\right)^{(9)}\left(T_{45}\left(s_{(44)}\right), s_{(44)}\right)\right) G_{46}\left(s_{(44)}\right)\right] d s_{(44)} \\
& \bar{T}_{44}(t)=T_{44}^{0}+\int_{0}^{t}\left[\left(b_{44}\right)^{(9)} T_{45}\left(s_{(44)}\right)-\left(\left(b_{44}^{\prime}\right)^{(9)}-\left(b_{44}^{\prime \prime}\right)^{(9)}\left(G\left(s_{(44)}\right), s_{(44)}\right)\right) T_{44}\left(s_{(44)}\right)\right] d s_{(44)} \\
& \bar{T}_{45}(t)=T_{45}^{0}+\int_{0}^{t}\left[\left(b_{45}\right)^{(9)} T_{44}\left(s_{(44)}\right)-\left(\left(b_{45}^{\prime}\right)^{(9)}-\left(b_{45}^{\prime \prime}\right)^{(9)}\left(G\left(s_{(44)}\right), s_{(44)}\right)\right) T_{45}\left(s_{(44)}\right)\right] d s_{(44)}
\end{aligned}
$$

$$
\overline{\mathrm{T}}_{46}(\mathrm{t})=\mathrm{T}_{46}^{0}+\int_{0}^{t}\left[\left(b_{46}\right)^{(9)} T_{45}\left(s_{(44)}\right)-\left(\left(b_{46}^{\prime}\right)^{(9)}-\left(b_{46}^{\prime \prime}\right)^{(9)}\left(G\left(s_{(44)}\right), s_{(44)}\right)\right) T_{46}\left(s_{(44)}\right)\right] d s_{(44)}
$$

Where $s_{(44)}$ is the integrand that is integrated over an interval $(0, t)$

The operator $\mathcal{A}^{(1)}$ maps the space of functions satisfying Equations into itself.Indeed it is obvious that

$$
\begin{aligned}
G_{13}(t) \leq & G_{13}^{0}+\int_{0}^{t}\left[\left(a_{13}\right)^{(1)}\left(G_{14}^{0}+\left(\hat{P}_{13}\right)^{(1)} e^{\left.\left(\widehat{M}_{13}\right)^{(1)} s_{(13)}\right)}\right)\right] d s_{(13)}= \\
& \left(1+\left(a_{13}\right)^{(1)} t\right) G_{14}^{0}+\frac{\left(a_{13}\right)^{(1)}\left(\hat{P}_{13}\right)^{(1)}}{\left(\widehat{M}_{13}\right)^{(1)}}\left(e^{\left(\widehat{M}_{13}\right)^{(1)} t}-1\right)
\end{aligned}
$$

From which it follows that
$\left(G_{13}(t)-G_{13}^{0}\right) e^{-\left(\widehat{M}_{13}\right)^{(1)} t} \leq \frac{\left(a_{13}\right)^{(1)}}{\left(\widehat{M}_{13}\right)^{(1)}}\left[\left(\left(\hat{P}_{13}\right)^{(1)}+G_{14}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{13}\right)^{(1)}+G_{14}^{0}}{G_{14}^{0}}\right)}+\left(\hat{P}_{13}\right)^{(1)}\right]$
$\left(G_{i}^{0}\right)$ is as defined in the statement of theorem 1
Analogous inequalities hold also for $G_{14}, G_{15}, T_{13}, T_{14}, T_{15}$
The operator $\mathcal{A}^{(2)}$ maps the space of functions satisfying Equations into itself .Indeed it is obvious that
$G_{16}(t) \leq G_{16}^{0}+\int_{0}^{t}\left[\left(a_{16}\right)^{(2)}\left(G_{17}^{0}+\left(\hat{P}_{16}\right)^{(6)} e^{\left(M_{16}\right)^{(2)} s_{(16)}}\right)\right] d s_{(16)}=\left(1+\left(a_{16}\right)^{(2)} t\right) G_{17}^{0}+$
$\frac{\left(a_{16}\right)^{(2)}\left(\hat{P}_{16}\right)^{(2)}}{\left(\widehat{M}_{16}\right)^{(2)}}\left(e^{\left(\widehat{M}_{16}\right)^{(2)} t}-1\right)$
From which it follows that
$\left(G_{16}(t)-G_{16}^{0}\right) e^{-\left(\widehat{M}_{16}\right)^{(2)} t} \leq \frac{\left(a_{16}\right)^{(2)}}{\left(\bar{M}_{16}\right)^{(2)}}\left[\left(\left(\hat{P}_{16}\right)^{(2)}+G_{17}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{16}\right)^{(2)}+G_{17}^{0}}{G_{17}^{0}}\right)}+\left(\hat{P}_{16}\right)^{(2)}\right]$
Analogous inequalities hold also for $G_{17}, G_{18}, T_{16}, T_{17}, T_{18}$
The operator $\mathcal{A}^{(3)}$ maps the space of functions satisfying Equations into itself .Indeed it is obvious
that

$$
\begin{aligned}
G_{20}(t) \leq & G_{20}^{0}+\int_{0}^{t}\left[\left(a_{20}\right)^{(3)}\left(G_{21}^{0}+\left(\hat{P}_{20}\right)^{(3)} e^{\left.\left(\widehat{M}_{20}\right)^{(3)} s_{(20)}\right)}\right)\right] d s_{(20)}= \\
& \left(1+\left(a_{20}\right)^{(3)} t\right) G_{21}^{0}+\frac{\left(a_{20}\right)^{(3)}\left(\hat{P}_{20}\right)^{(3)}}{\left(\hat{M}_{20}\right)^{(3)}}\left(e^{\left(\widehat{M}_{20}\right)^{(3)} t}-1\right)
\end{aligned}
$$

From which it follows that
$\left(G_{20}(t)-G_{20}^{0}\right) e^{-\left(\hat{M}_{20}\right)^{(3)} t} \leq \frac{\left(a_{20}\right)^{(3)}}{\left(\widehat{M}_{20}\right)^{(3)}}\left[\left(\left(\hat{P}_{20}\right)^{(3)}+G_{21}^{0}\right) e^{\left(-\frac{\left(\hat{P}_{20}\right)^{(3)}+G_{21}^{0}}{G_{21}^{0}}\right)}+\left(\hat{P}_{20}\right)^{(3)}\right]$
Analogous inequalities hold also for $G_{21}, G_{22}, T_{20}, T_{21}, T_{22}$
The operator $\mathcal{A}^{(4)}$ maps the space of functions satisfying into itself .Indeed it is obvious that

$$
\begin{gathered}
G_{24}(t) \leq G_{24}^{0}+\int_{0}^{t}\left[\left(a_{24}\right)^{(4)}\left(G_{25}^{0}+\left(\hat{P}_{24}\right)^{(4)} e^{\left.\left(\hat{M}_{24}\right)^{(4)} s_{(24)}\right)}\right)\right] d s_{(24)}= \\
\left(1+\left(a_{24}\right)^{(4)} t\right) G_{25}^{0}+\frac{\left(a_{24}\right)^{(4)}\left(\hat{P}_{24}\right)^{(4)}}{\left(\widehat{M}_{24}\right)^{(4)}}\left(e^{\left(\tilde{M}_{24}\right)^{(4)} t}-1\right)
\end{gathered}
$$

From which it follows that
$\left(G_{24}(t)-G_{24}^{0}\right) e^{-\left(\widehat{M}_{24}\right)^{(4)} t} \leq \frac{\left(a_{24}\right)^{(4)}}{\left(\widehat{M}_{24}\right)^{(4)}}\left[\left(\left(\hat{P}_{24}\right)^{(4)}+G_{25}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{24}\right)^{(4)}+G_{25}^{0}}{G_{25}^{0}}\right)}+\left(\hat{P}_{24}\right)^{(4)}\right]$
$\left(G_{i}^{0}\right)$ is as defined in the statement of theorem 4
The operator $\mathcal{A}^{(5)}$ maps the space of functions satisfying Equations into itself .Indeed it is obvious that

$$
\begin{aligned}
G_{28}(t) \leq & G_{28}^{0}+\int_{0}^{t}\left[\left(a_{28}\right)^{(5)}\left(G_{29}^{0}+\left(\hat{P}_{28}\right)^{(5)} e^{\left.\left(\widehat{M}_{28}\right)^{(5)} s_{(28)}\right)}\right)\right] d s_{(28)}= \\
& \left(1+\left(a_{28}\right)^{(5)} t\right) G_{29}^{0}+\frac{\left(a_{28}\right)^{(5)}\left(\hat{P}_{28}\right)^{(5)}}{\left(\hat{M}_{28}\right)^{(5)}}\left(e^{\left(\widehat{M}_{28}\right)^{(5)} t}-1\right)
\end{aligned}
$$

From which it follows that
$\left(G_{28}(t)-G_{28}^{0}\right) e^{-\left(\hat{M}_{28}\right)^{(5)} t} \leq \frac{\left(a_{28}\right)^{(5)}}{\left(\widehat{M}_{28}\right)^{(5)}}\left[\left(\left(\hat{P}_{28}\right)^{(5)}+G_{29}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{28}\right)^{(5)}+G_{29}^{0}}{G_{29}^{0}}\right)}+\left(\hat{P}_{28}\right)^{(5)}\right]$
$\left(G_{i}^{0}\right)$ is as defined in the statement of theorem 5
The operator $\mathcal{A}^{(6)}$ maps the space of functions satisfying Equations into itself .Indeed it is obvious that

$$
\begin{aligned}
G_{32}(t) \leq & G_{32}^{0}+\int_{0}^{t}\left[\left(a_{32}\right)^{(6)}\left(G_{33}^{0}+\left(\hat{P}_{32}\right)^{(6)} e^{\left.\left(\tilde{M}_{32}\right)^{(6)} s_{(32)}\right)}\right)\right] d s_{(32)}= \\
& \left(1+\left(a_{32}\right)^{(6)} t\right) G_{33}^{0}+\frac{\left(a_{32}\right)^{(6)}\left(\hat{P}_{32}\right)^{(6)}}{\left(\widehat{M}_{32}\right)^{(6)}}\left(e^{\left(\widehat{M}_{32}\right)^{(6)} t}-1\right)
\end{aligned}
$$

From which it follows that
$\left(G_{32}(t)-G_{32}^{0}\right) e^{-\left(\widehat{M}_{32}\right)^{(6)} t} \leq \frac{\left(a_{32}\right)^{(6)}}{\left(\widehat{M}_{32}\right)^{(6)}}\left[\left(\left(\hat{P}_{32}\right)^{(6)}+G_{33}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{32}\right)^{(6)}+G_{33}^{0}}{G_{33}^{0}}\right)}+\left(\hat{P}_{32}\right)^{(6)}\right]$
$\left(G_{i}^{0}\right)$ is as defined in the statement of theorem 6
Analogous inequalities hold also for $G_{25}, G_{26}, T_{24}, T_{25}, T_{26}$
The operator $\mathcal{A}^{(7)}$ maps the space of functions satisfying Equations into itself .Indeed it is obvious that

$$
\begin{aligned}
& G_{36}(t) \leq G_{36}^{0}+\int_{0}^{t}\left[\left(a_{36}\right)^{(7)}\left(G_{37}^{0}+\left(\hat{P}_{36}\right)^{(7)} e^{\left.\left(\widehat{M}_{36}\right)^{(7)} s_{(36)}\right)}\right)\right] d s_{(36)}= \\
& \quad\left(1+\left(a_{36}\right)^{(7)} t\right) G_{37}^{0}+\frac{\left(a_{36}\right)^{(7)}\left(\hat{P}_{36}\right)^{(7)}}{\left(\bar{M}_{36}\right)^{(7)}}\left(e^{\left(\widehat{M}_{36}\right)^{(7)} t}-1\right)
\end{aligned}
$$

From which it follows that
$\left(G_{36}(t)-G_{36}^{0}\right) e^{-\left(\widehat{M}_{36}\right)^{(7)} t} \leq \frac{\left(a_{36}\right)^{(7)}}{\left(\widehat{M}_{36}\right)^{(7)}}\left[\left(\left(\hat{P}_{36}\right)^{(7)}+G_{37}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{36}\right)^{(7)}+G_{37}^{0}}{G_{37}^{0}}\right)}+\left(\hat{P}_{36}\right)^{(7)}\right]$
$\left(G_{i}^{0}\right)$ is as defined in the statement of theorem 7

The operator $\mathcal{A}^{(8)}$ maps the space of functions satisfying Equations into itself. Indeed it is obvious that

$$
\begin{equation*}
G_{40}(t) \leq G_{40}^{0}+\int_{0}^{t}\left[\left(a_{40}\right)^{(8)}\left(G_{41}^{0}+\left(\hat{P}_{40}\right)^{(8)} e^{\left.\left(\hat{M}_{40}\right)^{(8)} s_{(40)}\right)}\right)\right] d s_{(40)}= \tag{180}
\end{equation*}
$$

$$
\left(1+\left(a_{40}\right)^{(8)} t\right) G_{41}^{0}+\frac{\left(a_{40}\right)^{(8)}\left(\hat{P}_{40}\right)^{(8)}}{\left(\widehat{M}_{40}\right)^{(8)}}\left(e^{\left(\widehat{M}_{40}\right)^{(8)} t}-1\right)
$$

From which it follows that
$\left(G_{40}(t)-G_{40}^{0}\right) e^{-\left(\widehat{M}_{40}\right)^{(8)} t} \leq \frac{\left(a_{40}\right)^{(8)}}{\left(\widehat{M}_{40}\right)^{(8)}}\left[\left(\left(\hat{P}_{40}\right)^{(8)}+G_{41}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{40}\right)^{(8)}+G_{41}^{0}}{G_{41}^{0}}\right)}+\left(\hat{P}_{40}\right)^{(8)}\right]$
$\left(G_{i}^{0}\right)$ is as defined in the statement of theorem 8
Analogous inequalities hold also for $G_{41}, G_{42}, T_{40}, T_{41}, T_{42}$
(b) The operator $\mathcal{A}^{(9)}$ maps the space of functions satisfying $34,35,36$ into itself. Indeed it is obvious that
$G_{44}(t) \leq G_{44}^{0}+\int_{0}^{t}\left[\left(a_{44}\right)^{(9)}\left(G_{45}^{0}+\left(\hat{P}_{44}\right)^{(9)} e^{\left.\left(\widehat{M}_{44}\right)^{(9)} s_{(44)}\right)}\right)\right] d s_{(44)}=$

$$
\left(1+\left(a_{44}\right)^{(9)} t\right) G_{45}^{0}+\frac{\left(a_{44}\right)^{(9)}\left(\hat{P}_{44}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}\left(e^{\left(\widehat{M}_{44}\right)^{(9)} t}-1\right)
$$

From which it follows that
$\left(G_{44}(t)-G_{44}^{0}\right) e^{-\left(\widehat{M}_{44}\right)^{(9)} t} \leq \frac{\left(a_{44}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}\left[\left(\left(\widehat{P}_{44}\right)^{(9)}+G_{45}^{0}\right) e^{\left(-\frac{\left(\widehat{P}_{44}\right)^{(9)}+G_{45}^{0}}{G_{45}^{0}}\right)}+\left(\hat{P}_{44}\right)^{(9)}\right]$
$\left(G_{i}^{0}\right)$ is as defined in the statement of theorem 9
Analogous inequalities hold also for $G_{45}, G_{46}, T_{44}, T_{45}, T_{46}$
It is now sufficient to take $\frac{\left(a_{i}\right)^{(1)}}{\left(\widehat{M}_{13}\right)^{(1)}}, \frac{\left(b_{i}\right)^{(1)}}{\left(\widehat{M}_{13}\right)^{(1)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{13}\right)^{(1)}$ and $\left(\widehat{\mathrm{Q}}_{13}\right)^{(1)}$ large to have
$\frac{\left(a_{i}\right)^{(1)}}{\left(\bar{M}_{13}\right)^{(1)}}\left[\left(\widehat{P}_{13}\right)^{(1)}+\left(\left(\hat{P}_{13}\right)^{(1)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{13}\right)^{(1)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{13}\right)^{(1)}$
$\frac{\left(b_{i}\right)^{(1)}}{\left(\hat{M}_{13}\right)^{(1)}}\left[\left(\left(\hat{Q}_{13}\right)^{(1)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\hat{Q}_{13}\right)^{(1)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\hat{Q}_{13}\right)^{(1)}\right] \leq\left(\hat{Q}_{13}\right)^{(1)}$
In order that the operator $\mathcal{A}^{(1)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations into itself
The operator $\mathcal{A}^{(1)}$ is a contraction with respect to the metric
$d\left(\left(G^{(1)}, T^{(1)}\right),\left(G^{(2)}, T^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{13}\right)^{(1)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{13}\right)^{(1)} t}\right\}$
Indeed if we denote
Definition of $\tilde{G}, \tilde{T}:(\tilde{G}, \tilde{T})=\mathcal{A}^{(1)}(G, T)$
It results
$\left|\tilde{G}_{13}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{13}\right)^{(1)}\left|G_{14}^{(1)}-G_{14}^{(2)}\right| e^{-\left(\widehat{M}_{13}\right)^{(1)} s_{(13)}} e^{\left(\widehat{M}_{13}\right)^{(1)} s_{(13)}} d s_{(13)}+$
$\int_{0}^{t}\left\{\left(a_{13}^{\prime}\right)^{(1)}\left|G_{13}^{(1)}-G_{13}^{(2)}\right| e^{-\left(\widehat{M}_{13}\right)^{(1)} s_{(13)}} e^{-\left(\widehat{M}_{13}\right)^{(1)} s_{(13)}}+\right.$
$\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}^{(1)}, s_{(13)}\right)\left|G_{13}^{(1)}-G_{13}^{(2)}\right| e^{-\left(\bar{M}_{13}\right)^{(1)} s_{(13)}} e^{\left(\bar{M}_{13}\right)^{(1)} s_{(13)}}+$
$\left.G_{13}^{(2)}\left|\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}^{(1)}, s_{(13)}\right)-\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}^{(2)}, s_{(13)}\right)\right| e^{-\left(\bar{M}_{13}\right)^{(1)} s_{(13)}} e^{\left(\widehat{M}_{13}\right)^{(1)} s_{(13)}}\right\} d s_{(13)}$
Where $s_{(13)}$ represents integrand that is integrated over the interval [ $0, \mathrm{t}$ ]
From the hypotheses it follows
$\left|G^{(1)}-G^{(2)}\right| e^{-\left(\widehat{M}_{13}\right)^{(1)} t} \leq$
$\frac{1}{\left(\widetilde{M}_{13}\right)^{(1)}}\left(\left(a_{13}\right)^{(1)}+\left(a_{13}^{\prime}\right)^{(1)}+\left(\widehat{A}_{13}\right)^{(1)}+\left(\widehat{P}_{13}\right)^{(1)}\left(\widehat{k}_{13}\right)^{(1)}\right) d\left(\left(G^{(1)}, T^{(1)} ; G^{(2)}, T^{(2)}\right)\right)$
And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis the result follows
Remark 1: The fact that we supposed $\left(a_{13}^{\prime \prime}\right)^{(1)}$ and $\left(b_{13}^{\prime \prime}\right)^{(1)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis, in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{13}\right)^{(1)} e^{\left(\bar{M}_{13}\right)^{(1)} t}$ and $\left(\widehat{Q}_{13}\right)^{(1)} e^{\left(\bar{M}_{13}\right)^{(1)} t}$ respectively of $\mathbb{R}_{+}$.
If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(1)}$ and $\left(b_{i}^{\prime \prime}\right)^{(1)}, i=13,14,15$ depend only on $\mathrm{T}_{14}$ and respectively on $G$ (and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.
Remark 2: There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
From 19 to 24 it results
$G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(1)}-\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}\left(s_{(13)}\right), s_{(13)}\right)\right\} d s_{(13)}\right]} \geq 0$
$T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(1)} t\right)}>0 \quad$ for $\mathrm{t}>0$
Definition of $\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{1},\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{2}$ and $\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{3}$ :
Remark 3: if $G_{13}$ is bounded, the same property have also $G_{14}$ and $G_{15}$. indeed if $G_{13}<\left(\widehat{M}_{13}\right)^{(1)}$ it follows $\frac{d G_{14}}{d t} \leq\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{1}-\left(a_{14}^{\prime}\right)^{(1)} G_{14}$ and by integrating
$G_{14} \leq\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{2}=G_{14}^{0}+2\left(a_{14}\right)^{(1)}\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{1} /\left(a_{14}^{\prime}\right)^{(1)}$

In the same way, one can obtain
$G_{15} \leq\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{3}=G_{15}^{0}+2\left(a_{15}\right)^{(1)}\left(\left(\widehat{M}_{13}\right)^{(1)}\right)_{2} /\left(a_{15}^{\prime}\right)^{(1)}$
If $G_{14}$ or $G_{15}$ is bounded, the same property follows for $G_{13}, G_{15}$ and $G_{13}, G_{14}$ respectively.
Remark 4: If $G_{13}$ is bounded, from below, the same property holds for $G_{14}$ and $G_{15}$. The proof is
analogous with the preceding one. An analogous property is true if $G_{14}$ is bounded from below.
Remark 5: If $\mathrm{T}_{13}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(1)}(G(t), t)\right)=\left(b_{14}^{\prime}\right)^{(1)}$ then $T_{14} \rightarrow \infty$.
Definition of $(m)^{(1)}$ and $\varepsilon_{1}$ :
Indeed let $t_{1}$ be so that for $t>t_{1}$
$\left(b_{14}\right)^{(1)}-\left(b_{i}^{\prime \prime}\right)^{(1)}(G(t), t)<\varepsilon_{1}, T_{13}(t)>(m)^{(1)}$
Then $\frac{d T_{14}}{d t} \geq\left(a_{14}\right)^{(1)}(m)^{(1)}-\varepsilon_{1} T_{14}$ which leads to
$T_{14} \geq\left(\frac{\left(a_{14}\right)^{(1)}(m)^{(1)}}{\varepsilon_{1}}\right)\left(1-e^{-\varepsilon_{1} t}\right)+T_{14}^{0} e^{-\varepsilon_{1} t}$ If we take $t$ such that $e^{-\varepsilon_{1} t}=\frac{1}{2}$ it results
$T_{14} \geq\left(\frac{\left(a_{14}\right)^{(1)}(m)^{(1)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{1}}$ By taking now $\varepsilon_{1}$ sufficiently small one sees that $\mathrm{T}_{14}$ is unbounded.
The same property holds for $T_{15}$ if $\lim _{t \rightarrow \infty}\left(b_{15}^{\prime \prime}\right)^{(1)}(G(t), t)=\left(b_{15}^{\prime}\right)^{(1)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations
It is now sufficient to take $\frac{\left(a_{i}\right)^{(2)}}{\left(\widehat{M}_{16}\right)^{(2)}}, \frac{\left(b_{i}\right)^{(2)}}{\left(\widehat{M}_{16}\right)^{(2)}}<1$ and to choose
$\left(\hat{P}_{16}\right)^{(2)}$ and $\left(\hat{Q}_{16}\right)^{(2)}$ large to have
$\frac{\left(a_{i}\right)^{(2)}}{\left(\widehat{M}_{16}\right)^{(2)}}\left[\left(\widehat{P}_{16}\right)^{(2)}+\left(\left(\hat{P}_{16}\right)^{(2)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{16}\right)^{(2)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{16}\right)^{(2)}$
$\frac{\left(b_{i}\right)^{(2)}}{\left(\hat{M}_{16}\right)^{(2)}}\left[\left(\left(\hat{Q}_{16}\right)^{(2)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\hat{Q}_{16}\right)^{(2)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\hat{Q}_{16}\right)^{(2)}\right] \leq\left(\hat{Q}_{16}\right)^{(2)}$
In order that the operator $\mathcal{A}^{(2)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations
into itself
The operator $\mathcal{A}^{(2)}$ is a contraction with respect to the metric
$d\left(\left(\left(G_{19}\right)^{(1)},\left(T_{19}\right)^{(1)}\right),\left(\left(G_{19}\right)^{(2)},\left(T_{19}\right)^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\mathbb{M}_{16}\right)^{(2)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(M_{16}\right)^{(2)} t}\right\}$
Indeed if we denote
Definition of $\widetilde{G_{19}}, \widetilde{T_{19}}:\left(\widetilde{G_{19}}, \widetilde{T_{19}}\right)=\mathcal{A}^{(2)}\left(G_{19}, T_{19}\right)$
It results
$\left|\tilde{G}_{16}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{16}\right)^{(2)}\left|G_{17}^{(1)}-G_{17}^{(2)}\right| e^{-\left(\bar{M}_{16}\right)^{(2)} s_{(16)}} e^{\left(\bar{M}_{16}\right)^{(2)} s_{(16)}} d s_{(16)}+$
$\int_{0}^{t}\left\{\left(a_{16}^{\prime}\right)^{(2)}\left|G_{16}^{(1)}-G_{16}^{(2)}\right| e^{-\left(\bar{M}_{16}\right)^{(2)} s_{(16)}} e^{-\left(\widehat{M}_{16}\right)^{(2)} s_{(16)}}+\right.$
$\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}^{(1)}, s_{(16)}\right)\left|G_{16}^{(1)}-G_{16}^{(2)}\right| e^{-\left(\widehat{M}_{16}\right)^{(2)} s_{(16)}} e^{\left(\widehat{M}_{16}\right)^{(2)} s_{(16)}}+$
$\left.G_{16}^{(2)}\left|\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}^{(1)}, s_{(16)}\right)-\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}^{(2)}, s_{(16)}\right)\right| e^{-\left(\widehat{M}_{16}\right)^{(2)} s_{(16)}} e^{\left.\left(\widehat{M}_{16}\right)^{(2)} s_{(16)}\right\}}\right\} s_{(16)}$
Where $s_{(16)}$ represents integrand that is integrated over the interval $[0, t]$
From the hypotheses it follows
$\left|\left(G_{19}\right)^{(1)}-\left(G_{19}\right)^{(2)}\right| \mathrm{e}^{-\left(\overline{\mathrm{M}}_{16}\right)^{(2)} \mathrm{t}} \leq$
$\frac{1}{\left(\overline{\mathrm{M}}_{16}\right)^{(2)}}\left(\left(a_{16}\right)^{(2)}+\left(a_{16}^{\prime}\right)^{(2)}+\left(\widehat{\mathrm{A}}_{16}\right)^{(2)}+\left(\widehat{\mathrm{P}}_{16}\right)^{(2)}\left(\widehat{k}_{16}\right)^{(2)}\right) \mathrm{d}\left(\left(\left(G_{19}\right)^{(1)},\left(T_{19}\right)^{(1)} ;\left(G_{19}\right)^{(2)},\left(T_{19}\right)^{(2)}\right)\right)$
And analogous inequalities for $\mathrm{G}_{i}$ and $\mathrm{T}_{i}$. Taking into account the hypothesis the result follows
Remark 6: The fact that we supposed $\left(a_{16}^{\prime \prime}\right)^{(2)}$ and $\left(b_{16}^{\prime \prime}\right)^{(2)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis, in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{\mathrm{P}}_{16}\right)^{(2)} \mathrm{e}^{\left(\widehat{\mathrm{M}}_{16}\right)^{(2)} \mathrm{t}}$ and $\left(\widehat{\mathrm{Q}}_{16}\right)^{(2)} \mathrm{e}^{\left(\widehat{\mathrm{M}}_{16}\right)^{(2)} \mathrm{t}}$ respectively of $\mathbb{R}_{+}$.
If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(2)}$ and $\left(b_{i}^{\prime \prime}\right)^{(2)}, i=16,17,18$ depend only on $\mathrm{T}_{17}$ and respectively on $\left(G_{19}\right)$ (and not on t ) and hypothesis can replaced by a usual Lipschitz condition.
Remark 7: There does not exist any t where $\mathrm{G}_{i}(\mathrm{t})=0$ and $\mathrm{T}_{i}(\mathrm{t})=0$
$\mathrm{G}_{i}(\mathrm{t}) \geq \mathrm{G}_{i}^{0} \mathrm{e}^{\left[-\int_{0}^{\mathrm{t}}\left(\left(a_{i}^{\prime}\right)^{(2)}-\left(a_{i}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}\left(s_{(16)}\right), s_{(16)}\right)\right) \mathrm{ds} s_{(16)}\right]} \geq 0$
$\mathrm{T}_{i}(\mathrm{t}) \geq \mathrm{T}_{i}^{0} \mathrm{e}^{\left(-\left(b_{i}^{\prime}\right)^{(2)} \mathrm{t}\right)}>0$ for $\mathrm{t}>0$
Definition of $\left(\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}\right)_{1^{\prime}}\left(\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}\right)_{2}$ and $\left(\left(\overline{\mathrm{M}}_{16}\right)^{(2)}\right)_{3}$ :
Remark 8: if $\mathrm{G}_{16}$ is bounded, the same property have also $\mathrm{G}_{17}$ and $\mathrm{G}_{18}$. Indeed if
$\mathrm{G}_{16}<\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}$ it follows $\frac{\mathrm{dG}_{17}}{\mathrm{dt}} \leq\left(\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}\right)_{1}-\left(a_{17}^{\prime}\right)^{(2)} \mathrm{G}_{17}$ and by integrating
$\mathrm{G}_{17} \leq\left(\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}\right)_{2}=\mathrm{G}_{17}^{0}+2\left(a_{17}\right)^{(2)}\left(\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}\right)_{1} /\left(a_{17}^{\prime}\right)^{(2)}$
In the same way, one can obtain
$\mathrm{G}_{18} \leq\left(\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}\right)_{3}=\mathrm{G}_{18}^{0}+2\left(a_{18}\right)^{(2)}\left(\left(\widehat{\mathrm{M}}_{16}\right)^{(2)}\right)_{2} /\left(a_{18}^{\prime}\right)^{(2)}$
If $\mathrm{G}_{17}$ or $\mathrm{G}_{18}$ is bounded, the same property follows for $\mathrm{G}_{16}, \mathrm{G}_{18}$ and $\mathrm{G}_{16}, \mathrm{G}_{17}$ respectively.
Remark 9: If $G_{16}$ is bounded, from below, the same property holds for $G_{17}$ and $G_{18}$. The proof is
analogous with the preceding one. An analogous property is true if $\mathrm{G}_{17}$ is bounded from below.
Remark 10: If $\mathrm{T}_{16}$ is bounded from below and $\lim _{\mathrm{t} \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right)(\mathrm{t}), \mathrm{t}\right)\right)=\left(b_{17}^{\prime}\right)^{(2)}$ then $\mathrm{T}_{17} \rightarrow \infty$.
Definition of $(m)^{(2)}$ and $\varepsilon_{2}$ :
Indeed let $\mathrm{t}_{2}$ be so that for $\mathrm{t}>\mathrm{t}_{2}$
$\left(b_{17}\right)^{(2)}-\left(b_{i}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right)(\mathrm{t}), \mathrm{t}\right)<\varepsilon_{2}, \mathrm{~T}_{16}(\mathrm{t})>(m)^{(2)}$
Then $\frac{\mathrm{dT}_{17}}{\mathrm{dt}} \geq\left(a_{17}\right)^{(2)}(m)^{(2)}-\varepsilon_{2} \mathrm{~T}_{17}$ which leads to
$\mathrm{T}_{17} \geq\left(\frac{\left(a_{17}\right)^{(2)}(m)^{(2)}}{\varepsilon_{2}}\right)\left(1-\mathrm{e}^{-\varepsilon_{2} \mathrm{t}}\right)+\mathrm{T}_{17}^{0} \mathrm{e}^{-\varepsilon_{2} \mathrm{t}}$ If we take t such that $\mathrm{e}^{-\varepsilon_{2} \mathrm{t}}=\frac{1}{2}$ it results
$\mathrm{T}_{17} \geq\left(\frac{\left(a_{17}\right)^{(2)}(m)^{(2)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{2}}$ By taking now $\varepsilon_{2}$ sufficiently small one sees that $\mathrm{T}_{17}$ is unbounded.
The same property holds for $\mathrm{T}_{18}$ if $\lim _{t \rightarrow \infty}\left(b_{18}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right)(\mathrm{t}), \mathrm{t}\right)=\left(b_{18}^{\prime}\right)^{(2)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations
It is now sufficient to take $\frac{\left(a_{i}\right)^{(3)}}{\left(\widehat{M}_{20}\right)^{(3)}}, \frac{\left(b_{i}\right)^{(3)}}{\left(\widehat{M}_{20}\right)^{(3)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{20}\right)^{(3)}$ and $\left(\widehat{\mathrm{Q}}_{20}\right)^{(3)}$ large to have
$\frac{\left(a_{i}\right)^{(3)}}{\left(\widehat{M}_{20}\right)^{(3)}}\left[\left(\widehat{P}_{20}\right)^{(3)}+\left(\left(\widehat{P}_{20}\right)^{(3)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{20}\right)^{(3)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{20}\right)^{(3)}$
$\frac{\left(b_{i}\right)^{(3)}}{\left(\hat{M}_{20}\right)^{(3)}}\left[\left(\left(\hat{Q}_{20}\right)^{(3)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\hat{Q}_{20}\right)^{(3)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\hat{Q}_{20}\right)^{(3)}\right] \leq\left(\hat{Q}_{20}\right)^{(3)}$
In order that the operator $\mathcal{A}^{(3)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations
into itself
The operator $\mathcal{A}^{(3)}$ is a contraction with respect to the metric
$d\left(\left(\left(G_{23}\right)^{(1)},\left(T_{23}\right)^{(1)}\right),\left(\left(G_{23}\right)^{(2)},\left(T_{23}\right)^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\hat{M}_{20}\right)^{(3)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\hat{M}_{20}\right)^{(3)} t}\right\}$

Indeed if we denote
Definition of $\widetilde{G_{23}}, \widetilde{T_{23}}:\left(\widetilde{\left(G_{23}\right)}, \widetilde{\left(T_{23}\right)}\right)=\mathcal{A}^{(3)}\left(\left(G_{23}\right),\left(T_{23}\right)\right)$

It results
$\left|\tilde{G}_{20}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{20}\right)^{(3)}\left|G_{21}^{(1)}-G_{21}^{(2)}\right| e^{-\left(\bar{M}_{20}\right)^{(3)} s_{(20)}} e^{\left(\bar{M}_{20}\right)^{(3)} s_{(20)}} d s_{(20)}+$
$\int_{0}^{t}\left\{\left(a_{20}^{\prime}\right)^{(3)}\left|G_{20}^{(1)}-G_{20}^{(2)}\right| e^{-\left(\bar{M}_{20}\right)^{(3)} s(20)} e^{-\left(\bar{M}_{20}\right)^{(3)} s(20)}+\right.$
$\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}^{(1)}, s_{(20)}\right)\left|G_{20}^{(1)}-G_{20}^{(2)}\right| e^{-\left(\bar{M}_{20}\right)^{(3)} s_{(20)}} e^{\left(\bar{M}_{20}\right)^{(3)} s_{(20)}}+$
$G_{20}^{(2)}\left|\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}^{(1)}, s_{(20)}\right)-\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}^{(2)}, s_{(20)}\right)\right| e^{-\left(\bar{M}_{20}\right)^{(3)} s_{(20)}} e^{\left.\left(\bar{M}_{20}\right)^{(3)} s_{(20)}\right\} d s_{(20)}}$
Where $s_{(20)}$ represents integrand that is integrated over the interval [ $0, \mathrm{t}$ ]
From the hypotheses it follows

$$
\begin{aligned}
& \left|G^{(1)}-G^{(2)}\right| e^{-\left(\widehat{M}_{20}\right)^{(3)} t} \leq \\
& \frac{1}{\left(\widehat{M}_{20}\right)^{(3)}}\left(\left(a_{20}\right)^{(3)}+\left(a_{20}^{\prime}\right)^{(3)}+\left(\widehat{A}_{20}\right)^{(3)}+\left(\widehat{P}_{20}\right)^{(3)}\left(\widehat{k}_{20}\right)^{(3)}\right) d\left(\left(\left(G_{23}\right)^{(1)},\left(T_{23}\right)^{(1)} ;\left(G_{23}\right)^{(2)},\left(T_{23}\right)^{(2)}\right)\right)
\end{aligned}
$$

And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis the result follows
Remark 11: The fact that we supposed $\left(a_{20}^{\prime \prime}\right)^{(3)}$ and $\left(b_{20}^{\prime \prime}\right)^{(3)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis ,in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{20}\right)^{(3)} e^{\left(\widehat{M}_{20}\right)^{(3)} t}$ and $\left(\widehat{Q}_{20}\right)^{(3)} e^{\left(\bar{M}_{20}\right)^{(3)} t}$ respectively of $\mathbb{R}_{+}$.
If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(3)}$ and $\left(b_{i}^{\prime \prime}\right)^{(3)}, i=20,21,22$ depend only on $\mathrm{T}_{21}$ and respectively on $\left(G_{23}\right)$ (and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.
Remark 12: There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
it results
$G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(3)}-\left(a_{i}^{\prime \prime}\right)^{(3)}\left(T_{21}\left(s_{(20)}\right), s_{(20)}\right)\right\} d s_{(20)}\right]} \geq 0$
$T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(3)} t\right)}>0$ for $\mathrm{t}>0$
Definition of $\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{1},\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{2}$ and $\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{3}$ :
Remark 13: if $G_{20}$ is bounded, the same property have also $G_{21}$ and $G_{22}$. indeed if
$G_{20}<\left(\widehat{M}_{20}\right)^{(3)}$ it follows $\frac{d G_{21}}{d t} \leq\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{1}-\left(a_{21}^{\prime}\right)^{(3)} G_{21}$ and by integrating
$G_{21} \leq\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{2}=G_{21}^{0}+2\left(a_{21}\right)^{(3)}\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{1} /\left(a_{21}^{\prime}\right)^{(3)}$
In the same way, one can obtain
$G_{22} \leq\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{3}=G_{22}^{0}+2\left(a_{22}\right)^{(3)}\left(\left(\widehat{M}_{20}\right)^{(3)}\right)_{2} /\left(a_{22}^{\prime}\right)^{(3)}$
If $G_{21}$ or $G_{22}$ is bounded, the same property follows for $G_{20}, G_{22}$ and $G_{20}, G_{21}$ respectively.
Remark 14: If $G_{20}$ is bounded, from below, the same property holds for $G_{21}$ and $G_{22}$. The proof is
analogous with the preceding one. An analogous property is true if $G_{21}$ is bounded from below.
Remark 15: If $\mathrm{T}_{20}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(3)}\left(\left(G_{23}\right)(t), t\right)\right)=\left(b_{21}^{\prime}\right)^{(3)}$ then $T_{21} \rightarrow$ $\infty$.
Definition of $(m)^{(3)}$ and $\varepsilon_{3}$ :
Indeed let $t_{3}$ be so that for $t>t_{3}$
$\left(b_{21}\right)^{(3)}-\left(b_{i}^{\prime \prime}\right)^{(3)}\left(\left(G_{23}\right)(t), t\right)<\varepsilon_{3}, T_{20}(t)>(m)^{(3)}$
Then $\frac{d T_{21}}{d t} \geq\left(a_{21}\right)^{(3)}(m)^{(3)}-\varepsilon_{3} T_{21}$ which leads to
$T_{21} \geq\left(\frac{\left(a_{21}\right)^{(3)}(m)^{(3)}}{\varepsilon_{3}}\right)\left(1-e^{-\varepsilon_{3} t}\right)+T_{21}^{0} e^{-\varepsilon_{3} t}$ If we take t such that $e^{-\varepsilon_{3} t}=\frac{1}{2}$ it results
$T_{21} \geq\left(\frac{\left(a_{21}\right)^{(3)}(m)^{(3)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{3}}$ By taking now $\varepsilon_{3}$ sufficiently small one sees that $\mathrm{T}_{21}$ is unbounded.
The same property holds for $T_{22}$ if $\lim _{t \rightarrow \infty}\left(b_{22}^{\prime \prime}\right)^{(3)}\left(\left(G_{23}\right)(t), t\right)=\left(b_{22}^{\prime}\right)^{(3)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations
It is now sufficient to take $\frac{\left(a_{i}\right)^{(4)}}{\left(\widehat{M}_{24}\right)^{(4)}}, \frac{\left(b_{i}\right)^{(4)}}{\left(\widehat{M}_{24}\right)^{(4)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{24}\right)^{(4)}$ and $\left(\widehat{\mathrm{Q}}_{24}\right)^{(4)}$ large to have
$\frac{\left(a_{i}\right)^{(4)}}{\left(\widehat{M}_{24}\right)^{(4)}}\left[\left(\widehat{P}_{24}\right)^{(4)}+\left(\left(\widehat{P}_{24}\right)^{(4)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{24}\right)^{(4)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{24}\right)^{(4)}$
$\frac{\left(b_{i}\right)^{(4)}}{\left(\hat{M}_{24}\right)^{(4)}}\left[\left(\left(\hat{Q}_{24}\right)^{(4)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{Q}_{24}\right)^{(4)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\hat{Q}_{24}\right)^{(4)}\right] \leq\left(\hat{Q}_{24}\right)^{(4)}$
In order that the operator $\mathcal{A}^{(4)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations
into itself
The operator $\mathcal{A}^{(4)}$ is a contraction with respect to the metric
$d\left(\left(\left(G_{27}\right)^{(1)},\left(T_{27}\right)^{(1)}\right),\left(\left(G_{27}\right)^{(2)},\left(T_{27}\right)^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{24}\right)^{(4)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{24}\right)^{(4)} t}\right\}$
Indeed if we denote
Definition of $\left(\widetilde{\left(G_{27}\right)}, \widetilde{\left(T_{27}\right)}: \quad\left(\widetilde{\left(G_{27}\right)}, \widetilde{\left(T_{27}\right)}\right)=\mathcal{A}^{(4)}\left(\left(G_{27}\right),\left(T_{27}\right)\right)\right.$

It results

$$
\begin{aligned}
& \left|\tilde{G}_{24}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{24}\right)^{(4)}\left|G_{25}^{(1)}-G_{25}^{(2)}\right| e^{-\left(\bar{M}_{24}\right)^{(4)} s_{(24)}} e^{\left(\widehat{M}_{24}\right)^{(4)} s_{(24)}} d s_{(24)}+ \\
& \int_{0}^{t}\left\{\left(a_{24}^{\prime}\right)^{(4)}\left|G_{24}^{(1)}-G_{24}^{(2)}\right| e^{-\left(\bar{M}_{24}\right)^{(4)} s_{(24)}} e^{-\left(\bar{M}_{24}\right)^{(4)} s_{(24)}}+\right. \\
& \left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}^{(1)}, s_{(24)}\right)\left|G_{24}^{(1)}-G_{24}^{(2)}\right| e^{-\left(\widehat{M}_{24}\right)^{(4)} s_{(24)} e^{\left(\widehat{M}_{24}\right)^{(4)} s_{(24)}}+} \\
& \quad G_{24}^{(2)}\left|\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}^{(1)}, s_{(24)}\right)-\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}^{(2)}, s_{(24)}\right)\right| e^{-\left(\widehat{M}_{24}\right)^{(4)} s_{(24)}} e^{\left.\left(\widehat{M}_{24}\right)^{(4)} s_{(24)}\right\}} d s_{(24)}
\end{aligned}
$$

Where $s_{(24)}$ represents integrand that is integrated over the interval [ $0, \mathrm{t}$ ]
From the hypotheses on Equations it follows
$\left|\left(G_{27}\right)^{(1)}-\left(G_{27}\right)^{(2)}\right| e^{-\left(\widehat{M}_{24}\right)^{(4)} t} \leq$
$\frac{1}{\left(\widehat{M}_{24}\right)^{(4)}}\left(\left(a_{24}\right)^{(4)}+\left(a_{24}^{\prime}\right)^{(4)}+\left(\widehat{A}_{24}\right)^{(4)}+\left(\widehat{P}_{24}\right)^{(4)}\left(\widehat{k}_{24}\right)^{(4)}\right) d\left(\left(\left(G_{27}\right)^{(1)},\left(T_{27}\right)^{(1)} ;\left(G_{27}\right)^{(2)},\left(T_{27}\right)^{(2)}\right)\right)$
And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis the result follows
Remark 16: The fact that we supposed $\left(a_{24}^{\prime \prime}\right)^{(4)}$ and $\left(b_{24}^{\prime \prime}\right)^{(4)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis, in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{24}\right)^{(4)} e^{\left(\widehat{M}_{24}\right)^{(4)} t}$ and $\left(\widehat{Q}_{24}\right)^{(4)} e^{\left(\bar{M}_{24}\right)^{(4)} t}$ respectively of $\mathbb{R}_{+}$.
If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(4)}$ and $\left(b_{i}^{\prime \prime}\right)^{(4)}, i=24,25,26$ depend only on $\mathrm{T}_{25}$ and respectively on $\left(G_{27}\right)$ (and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.
Remark 17: There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
it results
$G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(4)}-\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}\left(s_{(24)}\right), s_{(24)}\right)\right\} d s_{(24)}\right]} \geq 0$
$T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(4)} t\right)}>0 \quad$ for $t>0$
Definition of $\left.\left(\left(\widehat{M}_{24}\right)^{(4)}\right)_{1^{\prime}},\left(\widehat{M}_{24}\right)^{(4)}\right)_{2}$ and $\left(\left(\widehat{M}_{24}\right)^{(4)}\right)_{3}$ :
Remark 18: if $G_{24}$ is bounded, the same property have also $G_{25}$ and $G_{26}$. Indeed if
$G_{24}<\left(\widehat{M}_{24}\right)^{(4)}$ it follows $\frac{d G_{25}}{d t} \leq\left(\left(\widehat{M}_{24}\right)^{(4)}\right)_{1}-\left(a_{25}^{\prime}\right)^{(4)} G_{25}$ and by integrating
$G_{25} \leq\left(\left(\widehat{M}_{24}\right)^{(4)}\right)_{2}=G_{25}^{0}+2\left(a_{25}\right)^{(4)}\left(\left(\widehat{M}_{24}\right)^{(4)}\right)_{1} /\left(a_{25}^{\prime}\right)^{(4)}$
In the same way, one can obtain
$G_{26} \leq\left(\left(\widehat{M}_{24}\right)^{(4)}\right)_{3}=G_{26}^{0}+2\left(a_{26}\right)^{(4)}\left(\left(\widehat{M}_{24}\right)^{(4)}\right)_{2} /\left(a_{26}^{\prime}\right)^{(4)}$
If $G_{25}$ or $G_{26}$ is bounded, the same property follows for $G_{24}, G_{26}$ and $G_{24}, G_{25}$ respectively.
Remark 19: If $G_{24}$ is bounded, from below, the same property holds for $G_{25}$ and $G_{26}$. The proof is
analogous with the preceding one. An analogous property is true if $G_{25}$ is bounded from below.
Remark 20: If $\mathrm{T}_{24}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)(t), t\right)\right)=\left(b_{25}^{\prime}\right)^{(4)}$ then $T_{25} \rightarrow \infty$.
Definition of $(m)^{(4)}$ and $\varepsilon_{4}$ :
Indeed let $t_{4}$ be so that for $t>t_{4}$
$\left(b_{25}\right)^{(4)}-\left(b_{i}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)(t), t\right)<\varepsilon_{4}, T_{24}(t)>(m)^{(4)}$
Then $\frac{d T_{25}}{d t} \geq\left(a_{25}\right)^{(4)}(m)^{(4)}-\varepsilon_{4} T_{25}$ which leads to
$T_{25} \geq\left(\frac{\left(a_{25}\right)^{(4)}(m)^{(4)}}{\varepsilon_{4}}\right)\left(1-e^{-\varepsilon_{4} t}\right)+T_{25}^{0} e^{-\varepsilon_{4} t}$ If we take $t$ such that $e^{-\varepsilon_{4} t}=\frac{1}{2}$ it results
$T_{25} \geq\left(\frac{\left(a_{25}\right)^{(4)}(m)^{(4)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{4}}$ By taking now $\varepsilon_{4}$ sufficiently small one sees that $\mathrm{T}_{25}$ is unbounded.
The same property holds for $T_{26}$ if $\lim _{t \rightarrow \infty}\left(b_{26}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)(t), t\right)=\left(b_{26}^{\prime}\right)^{(4)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations 37 to 42
Analogous inequalities hold also for $G_{29}, G_{30}, T_{28}, T_{29}, T_{30}$
It is now sufficient to take $\frac{\left(a_{i}\right)^{(5)}}{\left(\widehat{M}_{28}\right)^{(5)}}, \frac{\left(b_{i}\right)^{(5)}}{\left(\bar{M}_{28}\right)^{(5)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{28}\right)^{(5)}$ and $\left(\widehat{\mathrm{Q}}_{28}\right)^{(5)}$ large to have
$\frac{\left(a_{i}\right)^{(5)}}{\left(\hat{M}_{28}\right)^{(5)}}\left[\left(\widehat{P}_{28}\right)^{(5)}+\left(\left(\widehat{P}_{28}\right)^{(5)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{28}\right)^{(5)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{28}\right)^{(5)}$
$\frac{\left(b_{i}\right)^{(5)}}{\left(\hat{M}_{28}\right)^{(5)}}\left[\left(\left(\hat{Q}_{28}\right)^{(5)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\hat{Q}_{28}\right)^{(5)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\hat{Q}_{28}\right)^{(5)}\right] \leq\left(\hat{Q}_{28}\right)^{(5)}$
In order that the operator $\mathcal{A}^{(5)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations into itself
The operator $\mathcal{A}^{(5)}$ is a contraction with respect to the metric
$d\left(\left(\left(G_{31}\right)^{(1)},\left(T_{31}\right)^{(1)}\right),\left(\left(G_{31}\right)^{(2)},\left(T_{31}\right)^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\hat{M}_{28}\right)^{(5)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\hat{M}_{28}\right)^{(5)} t}\right\}$
Indeed if we denote
Definition of $\left(\widetilde{G_{31}}\right), \widetilde{\left(T_{31}\right)}: \quad\left(\widetilde{\left(G_{31}\right)}, \widetilde{\left(T_{31}\right)}\right)=\mathcal{A}^{(5)}\left(\left(G_{31}\right),\left(T_{31}\right)\right)$
It results
$\left|\tilde{G}_{28}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{28}\right)^{(5)}\left|G_{29}^{(1)}-G_{29}^{(2)}\right| e^{-\left(\widehat{M}_{28}\right)^{(5)} s_{(28)}} e^{\left(\widehat{M}_{28}\right)^{(5)} s_{(28)}} d s_{(28)}+$
$\int_{0}^{t}\left\{\left(a_{28}^{\prime}\right)^{(5)}\left|G_{28}^{(1)}-G_{28}^{(2)}\right| e^{-\left(\bar{M}_{28}\right)^{(5)} s(28)} e^{-\left(\bar{M}_{28}\right)^{(5)} s(28)}+\right.$
$\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}^{(1)}, s_{(28)}\right)\left|G_{28}^{(1)}-G_{28}^{(2)}\right| e^{-\left(\widehat{M}_{28}\right)^{(5)} s_{(28)}} e^{\left(\widehat{M}_{28}\right)^{(5)} s_{(28)}}+$
$G_{28}^{(2)}\left|\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}^{(1)}, s_{(28)}\right)-\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}^{(2)}, s_{(28)}\right)\right| e^{-\left(\widehat{M}_{28}\right)^{(5)} s_{(28)}} e^{\left.\left(\widehat{M}_{28}\right)^{(5)} s_{(28)}\right\} d s_{(28)}}$
Where $s_{(28)}$ represents integrand that is integrated over the interval [ $0, \mathrm{t}$ ]
From the hypotheses on it follows
$\left|\left(G_{31}\right)^{(1)}-\left(G_{31}\right)^{(2)}\right| e^{-\left(\widehat{M}_{28}\right)^{(5)} t} \leq$
$\frac{1}{\left(\widehat{M}_{28}\right)^{(5)}}\left(\left(a_{28}\right)^{(5)}+\left(a_{28}^{\prime}\right)^{(5)}+\left(\widehat{A}_{28}\right)^{(5)}+\left(\widehat{P}_{28}\right)^{(5)}\left(\widehat{k}_{28}\right)^{(5)}\right) d\left(\left(\left(G_{31}\right)^{(1)},\left(T_{31}\right)^{(1)} ;\left(G_{31}\right)^{(2)},\left(T_{31}\right)^{(2)}\right)\right)$
And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis the result follows
Remark 21: The fact that we supposed $\left(a_{28}^{\prime \prime}\right)^{(5)}$ and $\left(b_{28}^{\prime \prime}\right)^{(5)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis, in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{28}\right)^{(5)} e^{\left(\widehat{M}_{28}\right)^{(5)} t}$ and $\left(\widehat{Q}_{28}\right)^{(5)} e^{\left(\widehat{M}_{28}\right)^{(5)} t}$ respectively of $\mathbb{R}_{+}$.
If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(5)}$ and $\left(b_{i}^{\prime \prime}\right)^{(5)}, i=28,29,30$ depend only on $\mathrm{T}_{29}$ and respectively on $\left(G_{31}\right)$ (and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.
Remark 22: There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
it results
$G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(5)}-\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}\left(s_{(28)}\right), s_{(28)}\right)\right\} d s_{(28)}\right]} \geq 0$
$T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(5)} t\right)}>0 \quad$ for $\mathrm{t}>0$
Definition of $\left.\left(\left(\widehat{M}_{28}\right)^{(5)}\right)_{1^{\prime}},\left(\widehat{M}_{28}\right)^{(5)}\right)_{2}$ and $\left(\left(\widehat{M}_{28}\right)^{(5)}\right)_{3}$ :
Remark 23: if $G_{28}$ is bounded, the same property have also $G_{29}$ and $G_{30}$. indeed if
$G_{28}<\left(\widehat{M}_{28}\right)^{(5)}$ it follows $\frac{d G_{29}}{d t} \leq\left(\left(\widehat{M}_{28}\right)^{(5)}\right)_{1}-\left(a_{29}^{\prime}\right)^{(5)} G_{29}$ and by integrating
$G_{29} \leq\left(\left(\widehat{M}_{28}\right)^{(5)}\right)_{2}=G_{29}^{0}+2\left(a_{29}\right)^{(5)}\left(\left(\widehat{M}_{28}\right)^{(5)}\right)_{1} /\left(a_{29}^{\prime}\right)^{(5)}$
In the same way, one can obtain
$G_{30} \leq\left(\left(\widehat{M}_{28}\right)^{(5)}\right)_{3}=G_{30}^{0}+2\left(a_{30}\right)^{(5)}\left(\left(\widehat{M}_{28}\right)^{(5)}\right)_{2} /\left(a_{30}^{\prime}\right)^{(5)}$
If $G_{29}$ or $G_{30}$ is bounded, the same property follows for $G_{28}, G_{30}$ and $G_{28}, G_{29}$ respectively.
Remark 24: If $G_{28}$ is bounded, from below, the same property holds for $G_{29}$ and $G_{30}$. The proof is
analogous with the preceding one. An analogous property is true if $G_{29}$ is bounded from below.
Remark 25: If $\mathrm{T}_{28}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right)(t), t\right)\right)=\left(b_{29}^{\prime}\right)^{(5)}$ then $T_{29} \rightarrow \infty$.
Definition of $(m)^{(5)}$ and $\varepsilon_{5}$ :
Indeed let $t_{5}$ be so that for $t>t_{5}$
$\left(b_{29}\right)^{(5)}-\left(b_{i}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right)(t), t\right)<\varepsilon_{5}, T_{28}(t)>(m)^{(5)}$
Then $\frac{d T_{29}}{d t} \geq\left(a_{29}\right)^{(5)}(m)^{(5)}-\varepsilon_{5} T_{29}$ which leads to
$T_{29} \geq\left(\frac{\left(a_{29}\right)^{(5)}(m)^{(5)}}{\varepsilon_{5}}\right)\left(1-e^{-\varepsilon_{5} t}\right)+T_{29}^{0} e^{-\varepsilon_{5} t}$ If we take t such that $e^{-\varepsilon_{5} t}=\frac{1}{2}$ it results
$T_{29} \geq\left(\frac{\left(a_{29}\right)^{(5)}(m)^{(5)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{5}}$ By taking now $\varepsilon_{5}$ sufficiently small one sees that $\mathrm{T}_{29}$ is unbounded.

The same property holds for $T_{30}$ if $\lim _{t \rightarrow \infty}\left(b_{30}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right)(t), t\right)=\left(b_{30}^{\prime}\right)^{(5)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations
Analogous inequalities hold also for $G_{33}, G_{34}, T_{32}, T_{33}, T_{34}$
It is now sufficient to take $\frac{\left(a_{i}\right)^{(6)}}{\left(\bar{M}_{32}\right)^{(6)}}, \frac{\left(b_{i}\right)^{(6)}}{\left(\mathcal{M}_{32}\right)^{(6)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{32}\right)^{(6)}$ and $\left(\widehat{\mathrm{Q}}_{32}\right)^{(6)}$ large to have
$\frac{\left(a_{i}\right)^{(6)}}{\left(\widehat{M}_{32}\right)^{(6)}}\left[\left(\widehat{P}_{32}\right)^{(6)}+\left(\left(\widehat{P}_{32}\right)^{(6)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{32}\right)^{(6)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{32}\right)^{(6)}$
$\frac{\left(b_{i}\right)^{(6)}}{\left(\widehat{M}_{32}\right)^{(6)}}\left[\left(\left(\widehat{Q}_{32}\right)^{(6)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{Q}_{32}\right)^{(6)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\widehat{Q}_{32}\right)^{(6)}\right] \leq\left(\hat{Q}_{32}\right)^{(6)}$
In order that the operator $\mathcal{A}^{(6)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations into itself
The operator $\mathcal{A}^{(6)}$ is a contraction with respect to the metric
$d\left(\left(\left(G_{35}\right)^{(1)},\left(T_{35}\right)^{(1)}\right),\left(\left(G_{35}\right)^{(2)},\left(T_{35}\right)^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\bar{M}_{32}\right)^{(6)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\bar{M}_{32}\right)^{(6)} t}\right\}$
Indeed if we denote
Definition of $\left(\widetilde{\left(G_{35}\right)}, \widetilde{\left(T_{35}\right)}: \quad\left(\widetilde{\left(G_{35}\right)}, \widetilde{\left(T_{35}\right)}\right)=\mathcal{A}^{(6)}\left(\left(G_{35}\right),\left(T_{35}\right)\right)\right.$

## It results

$\left|\tilde{G}_{32}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{32}\right)^{(6)}\left|G_{33}^{(1)}-G_{33}^{(2)}\right| e^{-\left(\widehat{M}_{32}\right)^{(6)} s_{(32)}} e^{\left(\widehat{M}_{32}\right)^{(6)} s_{(32)}} d s_{(32)}+$
$\int_{0}^{t}\left\{\left(a_{32}^{\prime}\right)^{(6)}\left|G_{32}^{(1)}-G_{32}^{(2)}\right| e^{-\left(\widehat{M}_{32}\right)^{(6)} s_{(32)}} e^{-\left(\widehat{M}_{32}\right)^{(6)} s_{(32)}}+\right.$
$\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}^{(1)}, s_{(32)}\right)\left|G_{32}^{(1)}-G_{32}^{(2)}\right| e^{-\left(\widehat{M}_{32}\right)^{(6)} s_{(32)}} e^{\left(\widehat{M}_{32}\right)^{(6)} s_{(32)}}+$
$\left.G_{32}^{(2)}\left|\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}^{(1)}, s_{(32)}\right)-\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}^{(2)}, s_{(32)}\right)\right| e^{-\left(\bar{M}_{32}\right)^{(6)} s_{(32)}} e^{\left.\left(\bar{M}_{32}\right)^{(6)} s_{(32)}\right\}}\right\} d s_{(32)}$
Where $s_{(32)}$ represents integrand that is integrated over the interval [ $0, \mathrm{t}$ ]
From the hypotheses it follows
$\left|\left(G_{35}\right)^{(1)}-\left(G_{35}\right)^{(2)}\right| e^{-\left(\bar{M}_{32}\right)^{(6)} t} \leq$
$\frac{1}{\left(\widehat{M}_{32}\right)^{(6)}}\left(\left(a_{32}\right)^{(6)}+\left(a_{32}^{\prime}\right)^{(6)}+\left(\widehat{A}_{32}\right)^{(6)}+\left(\widehat{P}_{32}\right)^{(6)}\left(\widehat{k}_{32}\right)^{(6)}\right) d\left(\left(\left(G_{35}\right)^{(1)},\left(T_{35}\right)^{(1)} ;\left(G_{35}\right)^{(2)},\left(T_{35}\right)^{(2)}\right)\right)$
And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis the result follows
Remark 26: The fact that we supposed $\left(a_{32}^{\prime \prime}\right)^{(6)}$ and $\left(b_{32}^{\prime \prime}\right)^{(6)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis, in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{32}\right)^{(6)} e^{\left(\widehat{M}_{32}\right)^{(6)} t}$ and $\left(\widehat{Q}_{32}\right)^{(6)} e^{\left(\widehat{M}_{32}\right)^{(6)} t}$ respectively of $\mathbb{R}_{+}$.
If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(6)}$ and $\left(b_{i}^{\prime \prime}\right)^{(6)}, i=32,33,34$ depend only on $\mathrm{T}_{33}$ and respectively on $\left(G_{35}\right)$ (and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.
Remark 27: There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
it results
$G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(6)}-\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}\left(s_{(32)}\right), s_{(32)}\right)\right\} d s_{(32)}\right]} \geq 0$
$T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(6)} t\right)}>0 \quad$ for $\mathrm{t}>0$
Definition of $\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{1^{\prime}}\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{2}$ and $\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{3}$ :
Remark 28: if $G_{32}$ is bounded, the same property have also $G_{33}$ and $G_{34}$. indeed if
$\overline{G_{32}<\left(\widehat{M}_{32}\right)^{(6)}}$ it follows $\frac{d G_{33}}{d t} \leq\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{1}-\left(a_{33}^{\prime}\right)^{(6)} G_{33}$ and by integrating
$G_{33} \leq\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{2}=G_{33}^{0}+2\left(a_{33}\right)^{(6)}\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{1} /\left(a_{33}^{\prime}\right)^{(6)}$
In the same way, one can obtain
$G_{34} \leq\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{3}=G_{34}^{0}+2\left(a_{34}\right)^{(6)}\left(\left(\widehat{M}_{32}\right)^{(6)}\right)_{2} /\left(a_{34}^{\prime}\right)^{(6)}$
If $G_{33}$ or $G_{34}$ is bounded, the same property follows for $G_{32}, G_{34}$ and $G_{32}, G_{33}$ respectively.
Remark 29: If $G_{32}$ is bounded, from below, the same property holds for $G_{33}$ and $G_{34}$. The proof is
analogous with the preceding one. An analogous property is true if $G_{33}$ is bounded from below.

Remark 30: If $T_{32}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right)(t), t\right)\right)=\left(b_{33}^{\prime}\right)^{(6)}$ then $T_{33} \rightarrow \infty$.
Definition of $(\mathrm{m})^{(6)}$ and $\varepsilon_{6}$ :
Indeed let $t_{6}$ be so that for $t>t_{6}$
$\left(b_{33}\right)^{(6)}-\left(b_{i}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right)(t), t\right)<\varepsilon_{6}, T_{32}(t)>(m)^{(6)}$
Then $\frac{d T_{33}}{d t} \geq\left(a_{33}\right)^{(6)}(m)^{(6)}-\varepsilon_{6} T_{33}$ which leads to
$T_{33} \geq\left(\frac{\left(a_{33}\right)^{(6)}(m)^{(6)}}{\varepsilon_{6}}\right)\left(1-e^{-\varepsilon_{6} t}\right)+T_{33}^{0} e^{-\varepsilon_{6} t}$ If we take t such that $e^{-\varepsilon_{6} t}=\frac{1}{2}$ it results
$T_{33} \geq\left(\frac{\left(a_{33}\right)^{(6)}(m)^{(6)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{6}}$ By taking now $\varepsilon_{6}$ sufficiently small one sees that $\mathrm{T}_{33}$ is unbounded.
The same property holds for $T_{34}$ if $\lim _{t \rightarrow \infty}\left(b_{34}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right)(t), t(t), t\right)=\left(b_{34}^{\prime}\right)^{(6)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations
Analogous inequalities hold also for $G_{37}, G_{38}, T_{36}, T_{37}, T_{38}$
It is now sufficient to take $\frac{\left(a_{i}\right)^{(7)}}{\left(\widehat{M}_{36}\right)^{(7)}}, \frac{\left(b_{i}\right)^{(7)}}{\left(\widehat{M}_{36}\right)^{(7)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{36}\right)^{(7)}$ and $\left(\widehat{\mathrm{Q}}_{36}\right)^{(7)}$ large to have
$\frac{\left(a_{i}\right)^{(7)}}{\left(M_{36}\right)^{(7)}}\left[\left(\widehat{P}_{36}\right)^{(7)}+\left(\left(\widehat{P}_{36}\right)^{(7)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{36}\right)^{(7)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{36}\right)^{(7)}$
$\frac{\left(b_{i}\right)^{(7)}}{\left(\widehat{M}_{36}\right)^{(7)}}\left[\left(\left(\widehat{Q}_{36}\right)^{(7)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{Q}_{36}\right)^{(7)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\widehat{Q}_{36}\right)^{(7)}\right] \leq\left(\hat{Q}_{36}\right)^{(7)}$
In order that the operator $\mathcal{A}^{(7)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations into itself
The operator $\mathcal{A}^{(7)}$ is a contraction with respect to the metric
$d\left(\left(\left(G_{39}\right)^{(1)},\left(T_{39}\right)^{(1)}\right),\left(\left(G_{39}\right)^{(2)},\left(T_{39}\right)^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\mathbb{M}_{36}\right)^{(7)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\mathbb{M}_{36}\right)^{(7)} t}\right\}$

Indeed if we denote
Definition of $\left(\widetilde{\left(G_{39}\right)}, \widetilde{\left(T_{39}\right)}:\left(\widetilde{\left(G_{39}\right)}, \widetilde{\left(T_{39}\right)}\right)=\mathcal{A}^{(7)}\left(\left(G_{39}\right),\left(T_{39}\right)\right)\right.$
It results
$\left|\tilde{G}_{36}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{36}\right)^{(7)}\left|G_{37}^{(1)}-G_{37}^{(2)}\right| e^{-\left(\widehat{M}_{36}\right)^{(7)} s_{(36)}} e^{\left(\widehat{M}_{36}\right)^{(7)} s_{(36)}} d s_{(36)}+$
$\int_{0}^{t}\left\{\left(a_{36}^{\prime}\right)^{(7)}\left|G_{36}^{(1)}-G_{36}^{(2)}\right| e^{-\left(\widehat{M}_{36}\right)^{(7)} s_{(36)}} e^{-\left(\widehat{M}_{36}\right)^{(7)} s_{(36)}}+\right.$
$\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}^{(1)}, s_{(36)}\right)\left|G_{36}^{(1)}-G_{36}^{(2)}\right| e^{-\left(\bar{M}_{36}\right)^{(7)} s_{(36)}} e^{\left(\bar{M}_{36}\right)^{(7)} s_{(36)}}+$
$\left.G_{36}^{(2)}\left|\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}^{(1)}, s_{(36)}\right)-\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}^{(2)}, s_{(36)}\right)\right| e^{-\left(\widehat{M}_{36}\right)^{(7)} s_{(36)}} e^{\left.\left(\widehat{M}_{36}\right)^{(7)} s_{(36)}\right\}}\right\} d s_{(36)}$
Where $s_{(36)}$ represents integrand that is integrated over the interval $[0, \mathrm{t}]$
From the hypotheses on it follows
$\left|\left(G_{39}\right)^{(1)}-\left(G_{39}\right)^{(2)}\right| e^{-\left(\widehat{M}_{36}\right)^{(7)} t} \leq$
$\frac{1}{\left(\bar{M}_{36}\right)^{(7)}}\left(\left(a_{36}\right)^{(7)}+\left(a_{36}^{\prime}\right)^{(7)}+\left(\widehat{A}_{36}\right)^{(7)}+\left(\widehat{P}_{36}\right)^{(7)}\left(\widehat{k}_{36}\right)^{(7)}\right) d\left(\left(\left(G_{39}\right)^{(1)},\left(T_{39}\right)^{(1)} ;\left(G_{39}\right)^{(2)},\left(T_{39}\right)^{(2)}\right)\right)$
And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis the result follows

Remark 31: The fact that we supposed $\left(a_{36}^{\prime \prime}\right)^{(7)}$ and $\left(b_{36}^{\prime \prime}\right)^{(7)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis, in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{36}\right)^{(7)} e^{\left(\widehat{M}_{36}\right)^{(7)} t}$ and $\left(\widehat{Q}_{36}\right)^{(7)} e^{\left(\widehat{M}_{36}\right)^{(7)} t}$ respectively of $\mathbb{R}_{+}$.

If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(7)}$ and $\left(b_{i}^{\prime \prime}\right)^{(7)}, i=36,37,38$ depend only on $\mathrm{T}_{37}$ and respectively on $\left(G_{39}\right)($ and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.

Remark 32: There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
it results
$G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(7)}-\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}\left(s_{(36)}\right), s_{(36)}\right)\right\} d s_{(36)}\right]} \geq 0$
$T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(7)} t\right)}>0 \quad$ for $\mathrm{t}>0$
Definition of $\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{1^{\prime}}\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{2}$ and $\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{3}$ :
Remark 33: if $G_{36}$ is bounded, the same property have also $G_{37}$ and $G_{38}$. Indeed if
$G_{36}<\left(\widehat{M}_{36}\right)^{(7)}$ it follows $\frac{d G_{37}}{d t} \leq\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{1}-\left(a_{37}^{\prime}\right)^{(7)} G_{37}$ and by integrating
$G_{37} \leq\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{2}=G_{37}^{0}+2\left(a_{37}\right)^{(7)}\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{1} /\left(a_{37}^{\prime}\right)^{(7)}$
In the same way, one can obtain
$G_{38} \leq\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{3}=G_{38}^{0}+2\left(a_{38}\right)^{(7)}\left(\left(\widehat{M}_{36}\right)^{(7)}\right)_{2} /\left(a_{38}^{\prime}\right)^{(7)}$
If $G_{37}$ or $G_{38}$ is bounded, the same property follows for $G_{36}, G_{38}$ and $G_{36}, G_{37}$ respectively.
Remark 34: If $G_{36}$ is bounded, from below, the same property holds for $G_{37}$ and $G_{38}$. The proof is analogous with the preceding one. An analogous property is true if $G_{37}$ is bounded from below.

Remark 35: If $\mathrm{T}_{36}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right)(t), t\right)\right)=\left(b_{37}^{\prime}\right)^{(7)}$ then $T_{37} \rightarrow \infty$.
Definition of $(m)^{(7)}$ and $\varepsilon_{7}$ :
Indeed let $t_{7}$ be so that for $t>t_{7}$
$\left(b_{37}\right)^{(7)}-\left(b_{i}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right)(t), t\right)<\varepsilon_{7}, T_{36}(t)>(m)^{(7)}$
Then $\frac{d T_{37}}{d t} \geq\left(a_{37}\right)^{(7)}(m)^{(7)}-\varepsilon_{7} T_{37}$ which leads to
$T_{37} \geq\left(\frac{\left(a_{37}\right)^{(7)}(m)^{(7)}}{\varepsilon_{7}}\right)\left(1-e^{-\varepsilon_{7} t}\right)+T_{37}^{0} e^{-\varepsilon_{7} t}$ If we take t such that $e^{-\varepsilon_{7} t}=\frac{1}{2}$ it results
$T_{37} \geq\left(\frac{\left(a_{37}\right)^{(7)}(m)^{(7)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{7}}$ By taking now $\varepsilon_{7}$ sufficiently small one sees that $\mathrm{T}_{37}$ is unbounded.
The same property holds for $T_{38}$ if $\lim _{t \rightarrow \infty}\left(b_{38}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right)(t), t\right)=\left(b_{38}^{\prime}\right)^{(7)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations
It is now sufficient to take $\frac{\left(a_{i}\right)^{(8)}}{\left(\bar{M}_{40}\right)^{(8)}}, \frac{\left(b_{i}\right)^{(8)}}{\left(\bar{M}_{40}\right)^{(8)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{40}\right)^{(8)}$ and $\left(\widehat{\mathrm{Q}}_{40}\right)^{(8)}$ large to have
$\frac{\left(a_{i}\right)^{(8)}}{\left(\widehat{M}_{40}\right)^{(8)}}\left[\left(\widehat{P}_{40}\right)^{(8)}+\left(\left(\hat{P}_{40}\right)^{(8)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{40}\right)^{(8)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{40}\right)^{(8)}$
$\frac{\left(b_{i}\right)^{(8)}}{\left(\hat{M}_{40}\right)^{(8)}}\left[\left(\left(\hat{Q}_{40}\right)^{(8)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\hat{Q}_{40}\right)^{(8)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\hat{Q}_{40}\right)^{(8)}\right] \leq\left(\hat{Q}_{40}\right)^{(8)}$
In order that the operator $\mathcal{A}^{(8)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying Equations into itself
The operator $\mathcal{A}^{(8)}$ is a contraction with respect to the metric
$d\left(\left(\left(G_{43}\right)^{(1)},\left(T_{43}\right)^{(1)}\right),\left(\left(G_{43}\right)^{(2)},\left(T_{43}\right)^{(2)}\right)\right)=$
$\sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{40}\right)^{(8)} t}, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{40}\right)^{(8)} t}\right\}$

Indeed if we denote
Definition of $\widetilde{\left(G_{43}\right)}, \widetilde{\left(T_{43}\right)} \quad: \quad\left(\widetilde{\left(G_{43}\right)}, \widetilde{\left(T_{43}\right)}\right)=\mathcal{A}^{(8)}\left(\left(G_{43}\right),\left(T_{43}\right)\right)$

It results
$\left|\tilde{G}_{40}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{40}\right)^{(8)}\left|G_{41}^{(1)}-G_{41}^{(2)}\right| e^{-\left(\bar{M}_{40}\right)^{(8)} s_{(40)}} e^{\left(\widehat{M}_{40}\right)^{(8)} s_{(40)}} d s_{(40)}+$
$\int_{0}^{t}\left\{\left(a_{40}^{\prime}\right)^{(8)}\left|G_{40}^{(1)}-G_{40}^{(2)}\right| e^{-\left(\widehat{M}_{40}\right)^{(8)} s_{(40)}} e^{-\left(\widehat{M}_{40}\right)^{(8)} s_{(40)}}+\right.$
$\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}^{(1)}, s_{(40)}\right)\left|G_{40}^{(1)}-G_{40}^{(2)}\right| e^{-\left(\widehat{M}_{40}\right)^{(8)} s_{(40)}} e^{\left(\widehat{M}_{40}\right)^{(8)} s_{(40)}}+$
$\left.G_{40}^{(2)}\left|\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}^{(1)}, s_{(40)}\right)-\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}^{(2)}, s_{(40)}\right)\right| e^{-\left(\widehat{M}_{40}\right)^{(8)} s_{(40)}} e^{\left(\widehat{M}_{40}\right)^{(8)} s_{(40)}}\right\} d s_{(40)}$
Where $s_{(40)}$ represents integrand that is integrated over the interval $[0, \mathrm{t}]$
From the hypotheses it follows
$\left|\left(G_{43}\right)^{(1)}-\left(G_{43}\right)^{(2)}\right| e^{-\left(\widehat{M}_{40}\right)^{(8)} t} \leq$
$\frac{1}{\left(\bar{M}_{40}\right)^{(8)}}\left(\left(a_{40}\right)^{(8)}+\left(a_{40}^{\prime}\right)^{(8)}+\left(\widehat{A}_{40}\right)^{(8)}+\left(\widehat{P}_{40}\right)^{(8)}\left(\widehat{k}_{40}\right)^{(8)}\right) d\left(\left(\left(G_{43}\right)^{(1)},\left(T_{43}\right)^{(1)} ;\left(G_{43}\right)^{(2)},\left(T_{43}\right)^{(2)}\right)\right)$
And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis the result follows
Remark 36: The fact that we supposed $\left(a_{40}^{\prime \prime}\right)^{(8)}$ and $\left(b_{40}^{\prime \prime}\right)^{(8)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis , in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{40}\right)^{(8)} e^{\left(\widehat{M}_{40}\right)^{(8)} t}$ and $\left(\widehat{Q}_{40}\right)^{(8)} e^{\left(\widehat{M}_{40}\right)^{(8)} t}$ respectively of $\mathbb{R}_{+}$.

If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(8)}$ and $\left(b_{i}^{\prime \prime}\right)^{(8)}, i=40,41,42$ depend only on $\mathrm{T}_{41}$ and respectively on $\left(G_{43}\right)$ (and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.
$\underline{\text { Remark } 37}$ There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
it results
$G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(8)}-\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}\left(s_{(40)}\right), s_{(40)}\right)\right\} d s_{(40)}\right]} \geq 0$
$T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(8)} t\right)}>0 \quad$ for $\mathrm{t}>0$
Definition of $\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{1^{\prime}},\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{2}$ and $\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{3}$ :
Remark 38: if $G_{40}$ is bounded, the same property have also $G_{41}$ and $G_{42}$. Indeed if
$G_{40}<\left(\widehat{M}_{40}\right)^{(8)}$ it follows $\frac{d G_{41}}{d t} \leq\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{1}-\left(a_{41}^{\prime}\right)^{(8)} G_{41}$ and by integrating
$G_{41} \leq\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{2}=G_{41}^{0}+2\left(a_{41}\right)^{(8)}\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{1} /\left(a_{41}^{\prime}\right)^{(8)}$
In the same way, one can obtain
$G_{42} \leq\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{3}=G_{42}^{0}+2\left(a_{42}\right)^{(8)}\left(\left(\widehat{M}_{40}\right)^{(8)}\right)_{2} /\left(a_{42}^{\prime}\right)^{(8)}$
If $G_{41}$ or $G_{42}$ is bounded, the same property follows for $G_{40}, G_{42}$ and $G_{40}, G_{41}$ respectively.
Remark 39: If $G_{40}$ is bounded, from below, the same property holds for $G_{41}$ and $G_{42}$. The proof is analogous with the preceding one. An analogous property is true if $G_{41}$ is bounded from below.

Remark 40: If $\mathrm{T}_{40}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right)(t), t\right)\right)=\left(b_{41}^{\prime}\right)^{(8)}$ then $T_{41} \rightarrow \infty$.
Definition of $(m)^{(8)}$ and $\varepsilon_{8}$ :
Indeed let $t_{8}$ be so that for $t>t_{8}$

$$
\left(b_{41}\right)^{(8)}-\left(b_{i}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right)(t), t\right)<\varepsilon_{8}, T_{40}(t)>(m)^{(8)}
$$

Then $\frac{d T_{41}}{d t} \geq\left(a_{41}\right)^{(8)}(m)^{(8)}-\varepsilon_{8} T_{41}$ which leads to
$T_{41} \geq\left(\frac{\left(a_{41}\right)^{(8)}(m)^{(8)}}{\varepsilon_{8}}\right)\left(1-e^{-\varepsilon_{8} t}\right)+T_{41}^{0} e^{-\varepsilon_{8} t}$ If we take t such that $e^{-\varepsilon_{8} t}=\frac{1}{2}$ it results
$T_{41} \geq\left(\frac{\left(a_{41}\right)^{(8)}(m)^{(8)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{8}}$ By taking now $\varepsilon_{8}$ sufficiently small one sees that $\mathrm{T}_{41}$ is unbounded.
The same property holds for $T_{42}$ if $\lim _{t \rightarrow \infty}\left(b_{42}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right)(t), t(t), t\right)=\left(b_{42}^{\prime}\right)^{(8)}$

It is now sufficient to take $\frac{\left(a_{i}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}, \frac{\left(b_{i}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}<1$ and to choose
$\left(\widehat{\mathrm{P}}_{44}\right)^{(9)}$ and $\left(\widehat{\mathrm{Q}}_{44}\right)^{(9)}$ large to have
$\frac{\left(a_{i}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}\left[\left(\widehat{P}_{44}\right)^{(9)}+\left(\left(\widehat{P}_{44}\right)^{(9)}+G_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{P}_{44}\right)^{(9)}+G_{j}^{0}}{G_{j}^{0}}\right)}\right] \leq\left(\hat{P}_{44}\right)^{(9)}$
$\frac{\left(b_{i}\right)^{(9)}}{\left(\widehat{M}_{44}\right)^{(9)}}\left[\left(\left(\widehat{Q}_{44}\right)^{(9)}+T_{j}^{0}\right) e^{-\left(\frac{\left(\widehat{Q}_{44}\right)^{(9)}+T_{j}^{0}}{T_{j}^{0}}\right)}+\left(\widehat{Q}_{44}\right)^{(9)}\right] \leq\left(\widehat{Q}_{44}\right)^{(9)}$
In order that the operator $\mathcal{A}^{(9)}$ transforms the space of sextuples of functions $G_{i}, T_{i}$ satisfying 39,35,36 into itsel

The operator $\mathcal{A}^{(9)}$ is a contraction with respect to the metric

$$
\begin{aligned}
& d\left(\left(\left(G_{47}\right)^{(1)},\left(T_{47}\right)^{(1)}\right),\left(\left(G_{47}\right)^{(2)},\left(T_{47}\right)^{(2)}\right)\right)= \\
& \sup _{i}\left\{\max _{t \in \mathbb{R}_{+}}\left|G_{i}^{(1)}(t)-G_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{44}\right)^{(9)}} t, \max _{t \in \mathbb{R}_{+}}\left|T_{i}^{(1)}(t)-T_{i}^{(2)}(t)\right| e^{-\left(\widehat{M}_{44}\right)^{(9)} t}\right\}
\end{aligned}
$$

## Indeed if we denote

Definition of $\widetilde{\left(G_{47}\right)}, \widetilde{\left(T_{47}\right)}:\left(\widetilde{\left(G_{47}\right)}, \widetilde{\left(T_{47}\right)}\right)=\mathcal{A}^{(9)}\left(\left(G_{47}\right),\left(T_{47}\right)\right)$
It results

$$
\begin{aligned}
& \left|\tilde{G}_{44}^{(1)}-\tilde{G}_{i}^{(2)}\right| \leq \int_{0}^{t}\left(a_{44}\right)^{(9)}\left|G_{45}^{(1)}-G_{45}^{(2)}\right| e^{-\left(\widetilde{M}_{44}\right)^{(9)} s_{(44)}} e^{\left(\widetilde{M}_{44}{ }^{(9)} s_{(44)}\right.} d s_{(44)}+ \\
& \int_{0}^{t}\left\{\left(a_{44}^{\prime}\right)^{(9)}\left|G_{44}^{(1)}-G_{44}^{(2)}\right| e^{-\left(\widehat{M}_{44}\right)^{(9)} s_{(44)}} e^{-\left(\widehat{M}_{44}\right)^{(9)} s_{(44)}}+\right. \\
& \left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}^{(1)}, s_{(44)}\right)\left|G_{44}^{(1)}-G_{44}^{(2)}\right| e^{-\left(\widehat{M}_{44}\right)^{(9)} s_{(44)}} e^{\left(\widehat{M}_{44}\right)^{(9)} s_{(44)}}+ \\
& G_{44}^{(2)}\left|\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}^{(1)}, s_{(44)}\right)-\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}^{(2)}, s_{(44)}\right)\right| e^{\left.-\left(\widehat{M}_{44}\right)^{(9)} s_{(44)} e^{\left.\left(\widetilde{M}_{44}\right)^{(9)} s_{(44)}\right)}\right\} d s_{(44)}, ~}
\end{aligned}
$$

Where $s_{(44)}$ represents integrand that is integrated over the interval $[0, \mathrm{t}]$
From the hypotheses on $45,46,47,28$ and 29 it follows

```
\(\left|\left(G_{47}\right)^{(1)}-G^{(2)}\right| e^{-\left(\widehat{M}_{44}\right)^{(9)} t} \leq\)
\(\frac{1}{\left(\widehat{M}_{44}\right)^{(9)}}\left(\left(a_{44}\right)^{(9)}+\left(a_{44}^{\prime}\right)^{(9)}+\left(\widehat{A}_{44}\right)^{(9)}+\right.\)
(P44)9(k44)9dG471,T471; G472,T472
```

And analogous inequalities for $G_{i}$ and $T_{i}$. Taking into account the hypothesis $(39,35,36)$ the result follows

Remark 41: The fact that we supposed $\left(a_{44}^{\prime \prime}\right)^{(9)}$ and $\left(b_{44}^{\prime \prime}\right)^{(9)}$ depending also on $t$ can be considered as not conformal with the reality, however we have put this hypothesis ,in order that we can postulate condition necessary to prove the uniqueness of the solution bounded by $\left(\widehat{P}_{44}\right)^{(9)} e^{\left(\widehat{M}_{44}\right)^{(9)} t}$ and $\left(\widehat{Q}_{44}\right)^{(9)} e^{\left(\widehat{M}_{44}\right)^{(9)} t}$ respectively of $\mathbb{R}_{+}$.

If instead of proving the existence of the solution on $\mathbb{R}_{+}$, we have to prove it only on a compact then it suffices to consider that $\left(a_{i}^{\prime \prime}\right)^{(9)}$ and $\left(b_{i}^{\prime \prime}\right)^{(9)}, i=44,45,46$ depend only on $\mathrm{T}_{45}$ and respectively on $\left(G_{47}\right)$ (and not on $t$ ) and hypothesis can replaced by a usual Lipschitz condition.

Remark 42: There does not exist any $t$ where $G_{i}(t)=0$ and $T_{i}(t)=0$
From 99 to 44 it results

$$
\begin{aligned}
& G_{i}(t) \geq G_{i}^{0} e^{\left[-\int_{0}^{t}\left\{\left(a_{i}^{\prime}\right)^{(9)}-\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}\left(s_{(44)}\right), s_{(44)}\right)\right\} d s_{(44)}\right]} \geq 0 \\
& T_{i}(t) \geq T_{i}^{0} e^{\left(-\left(b_{i}^{\prime}\right)^{(9)} t\right)}>0 \text { for } \mathrm{t}>0
\end{aligned}
$$

Definition of $\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{1},\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{2}$ and $\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{3}$ :
Remark 43: if $G_{44}$ is bounded, the same property have also $G_{45}$ and $G_{46}$. Indeed if
$G_{44}<\left(\widehat{M}_{44}\right)^{(9)}$ it follows $\frac{d G_{45}}{d t} \leq\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{1}-\left(a_{45}^{\prime}\right)^{(9)} G_{45}$ and by integrating
$G_{45} \leq\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{2}=G_{45}^{0}+2\left(a_{45}\right)^{(9)}\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{1} /\left(a_{45}^{\prime}\right)^{(9)}$
In the same way, one can obtain
$G_{46} \leq\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{3}=G_{46}^{0}+2\left(a_{46}\right)^{(9)}\left(\left(\widehat{M}_{44}\right)^{(9)}\right)_{2} /\left(a_{46}^{\prime}\right)^{(9)}$
If $G_{45}$ or $G_{46}$ is bounded, the same property follows for $G_{44}, G_{46}$ and $G_{44}, G_{45}$ respectively.
Remark 44: If $G_{44}$ is bounded, from below, the same property holds for $G_{45}$ and $G_{46}$. The proof is analogous with the preceding one. An analogous property is true if $G_{45}$ is bounded from below.

Remark 45: If $\mathrm{T}_{44}$ is bounded from below and $\lim _{t \rightarrow \infty}\left(\left(b_{i}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right)(t), t\right)\right)=\left(b_{45}^{\prime}\right)^{(9)}$ then $T_{45} \rightarrow \infty$.
Definition of $(m)^{(9)}$ and $\varepsilon_{9}$ :
Indeed let $t_{9}$ be so that for $t>t_{9}$

$$
\left(b_{45}\right)^{(9)}-\left(b_{i}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right)(t), t\right)<\varepsilon_{9}, T_{44}(t)>(m)^{(9)}
$$

Then $\frac{d T_{45}}{d t} \geq\left(a_{45}\right)^{(9)}(m)^{(9)}-\varepsilon_{9} T_{45}$ which leads to
$T_{45} \geq\left(\frac{\left(a_{45}\right)^{(9)}(m)^{(9)}}{\varepsilon_{9}}\right)\left(1-e^{-\varepsilon_{9} t}\right)+T_{45}^{0} e^{-\varepsilon_{9} t}$ If we take t such that $e^{-\varepsilon_{9} t}=\frac{1}{2}$ it results
$T_{45} \geq\left(\frac{\left(a_{45}\right)^{(9)}(m)^{(9)}}{2}\right), \quad t=\log \frac{2}{\varepsilon_{9}}$ By taking now $\varepsilon_{9}$ sufficiently small one sees that $\mathrm{T}_{45}$ is unbounded. The same property holds for $T_{46}$ if $\lim _{t \rightarrow \infty}\left(b_{46}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right)(t), t\right)=\left(b_{46}^{\prime}\right)^{(9)}$
We now state a more precise theorem about the behaviors at infinity of the solutions of equations 37 to 92

## Behavior of the solutions of equation

## Theorem If we denote and define

Definition of $\left(\sigma_{1}\right)^{(1)},\left(\sigma_{2}\right)^{(1)},\left(\tau_{1}\right)^{(1)},\left(\tau_{2}\right)^{(1)}$ :
(a) $\left.\sigma_{1}\right)^{(1)},\left(\sigma_{2}\right)^{(1)},\left(\tau_{1}\right)^{(1)},\left(\tau_{2}\right)^{(1)}$ four constants satisfying $-\left(\sigma_{2}\right)^{(1)} \leq-\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{14}^{\prime}\right)^{(1)}-\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)+\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right) \leq-\left(\sigma_{1}\right)^{(1)}$
$-\left(\tau_{2}\right)^{(1)} \leq-\left(b_{13}^{\prime}\right)^{(1)}+\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{13}^{\prime \prime}\right)^{(1)}(G, t)-\left(b_{14}^{\prime \prime}\right)^{(1)}(G, t) \leq-\left(\tau_{1}\right)^{(1)}$
Definition of $\left(v_{1}\right)^{(1)},\left(v_{2}\right)^{(1)},\left(u_{1}\right)^{(1)},\left(u_{2}\right)^{(1)}, v^{(1)}, u^{(1)}$ :
(b) By $\left(v_{1}\right)^{(1)}>0,\left(v_{2}\right)^{(1)}<0$ and respectively $\left(u_{1}\right)^{(1)}>0,\left(u_{2}\right)^{(1)}<0$ the roots of the equations $\left(a_{14}\right)^{(1)}\left(v^{(1)}\right)^{2}+\left(\sigma_{1}\right)^{(1)} v^{(1)}-\left(a_{13}\right)^{(1)}=0$ and $\left(b_{14}\right)^{(1)}\left(u^{(1)}\right)^{2}+\left(\tau_{1}\right)^{(1)} u^{(1)}-\left(b_{13}\right)^{(1)}=0$
Definition of $\left(\bar{v}_{1}\right)^{(1)},,\left(\bar{v}_{2}\right)^{(1)},\left(\bar{u}_{1}\right)^{(1)},\left(\bar{u}_{2}\right)^{(1)}$ :
By $\left(\bar{v}_{1}\right)^{(1)}>0,\left(\bar{v}_{2}\right)^{(1)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(1)}>0,\left(\bar{u}_{2}\right)^{(1)}<0$ the roots of the equations $\left(a_{14}\right)^{(1)}\left(v^{(1)}\right)^{2}+\left(\sigma_{2}\right)^{(1)} v^{(1)}-\left(a_{13}\right)^{(1)}=0$ and $\left(b_{14}\right)^{(1)}\left(u^{(1)}\right)^{2}+\left(\tau_{2}\right)^{(1)} u^{(1)}-\left(b_{13}\right)^{(1)}=0$
Definition of $\left(m_{1}\right)^{(1)},\left(m_{2}\right)^{(1)},\left(\mu_{1}\right)^{(1)},\left(\mu_{2}\right)^{(1)},\left(v_{0}\right)^{(1)}:-$
(c) If we define $\left(m_{1}\right)^{(1)},\left(m_{2}\right)^{(1)},\left(\mu_{1}\right)^{(1)},\left(\mu_{2}\right)^{(1)}$ by

$$
\begin{aligned}
& \left(m_{2}\right)^{(1)}=\left(v_{0}\right)^{(1)},\left(m_{1}\right)^{(1)}=\left(v_{1}\right)^{(1)} \text {, if }\left(v_{0}\right)^{(1)}<\left(v_{1}\right)^{(1)} \\
& \left(m_{2}\right)^{(1)}=\left(v_{1}\right)^{(1)},\left(m_{1}\right)^{(1)}=\left(\bar{v}_{1}\right)^{(1)} \text {, if }\left(v_{1}\right)^{(1)}<\left(v_{0}\right)^{(1)}<\left(\bar{v}_{1}\right)^{(1)}, \\
& \text { and }\left(v_{0}\right)^{(1)}=\frac{G_{13}^{0}}{G_{14}^{0}} \\
& \left(m_{2}\right)^{(1)}=\left(v_{1}\right)^{(1)},\left(m_{1}\right)^{(1)}=\left(v_{0}\right)^{(1)} \text {, if }\left(\bar{v}_{1}\right)^{(1)}<\left(v_{0}\right)^{(1)}
\end{aligned}
$$

and analogously
$\left(\mu_{2}\right)^{(1)}=\left(u_{0}\right)^{(1)},\left(\mu_{1}\right)^{(1)}=\left(u_{1}\right)^{(1)}$, if $\left(u_{0}\right)^{(1)}<\left(u_{1}\right)^{(1)}$
$\left(\mu_{2}\right)^{(1)}=\left(u_{1}\right)^{(1)},\left(\mu_{1}\right)^{(1)}=\left(\bar{u}_{1}\right)^{(1)}$, if $\left(u_{1}\right)^{(1)}<\left(u_{0}\right)^{(1)}<\left(\bar{u}_{1}\right)^{(1)}$,
and $\left(u_{0}\right)^{(1)}=\frac{T_{13}^{0}}{T_{14}^{0}}$
$\left(\mu_{2}\right)^{(1)}=\left(u_{1}\right)^{(1)},\left(\mu_{1}\right)^{(1)}=\left(u_{0}\right)^{(1)}$, if $\left(\bar{u}_{1}\right)^{(1)}<\left(u_{0}\right)^{(1)}$ where $\left(u_{1}\right)^{(1)},\left(\bar{u}_{1}\right)^{(1)}$
are defined
Then the solution of global equations satisfies the inequalities
$G_{13}^{0} e^{\left(\left(S_{1}\right)^{(1)}-\left(p_{13}\right)^{(1)}\right) t} \leq G_{13}(t) \leq G_{13}^{0} e^{\left(S_{1}\right)^{(1)} t}$
where $\left(p_{i}\right)^{(1)}$ is defined by equation
$\frac{1}{\left(m_{1}\right)^{(1)}} G_{13}^{0} e^{\left(\left(S_{1}\right)^{(1)}-\left(p_{13}\right)^{(1)}\right) t} \leq G_{14}(t) \leq \frac{1}{\left(m_{2}\right)^{(1)}} G_{13}^{0} e^{\left(S_{1}\right)^{(1)} t}$
$\left(\frac{\left(a_{15}\right)^{(1)} G_{13}^{0}}{\left(m_{1}\right)^{(1)}\left(\left(S_{1}\right)^{(1)}-\left(p_{13}\right)^{(1)}-\left(S_{2}\right)^{(1)}\right)}\left[e^{\left(\left(S_{1}\right)^{(1)}-\left(p_{13}\right)^{(1)}\right) t}-e^{-\left(S_{2}\right)^{(1)} t}\right]+G_{15}^{0} e^{-\left(S_{2}\right)^{(1)} t} \leq G_{15}(t) \leq\right.$
$\left.\frac{\left(a_{15}\right)^{(1)} G_{13}^{0}}{\left(m_{2}\right)^{(1)}\left(\left(S_{1}\right)^{(1)}-\left(a_{15}^{\prime}\right)^{(1)}\right)}\left[e^{\left(S_{1}\right)^{(1)} t}-e^{-\left(a_{15}^{\prime}\right)^{(1)} t}\right]+G_{15}^{0} e^{-\left(a_{15}^{\prime}\right)^{(1)} t}\right)$
$T_{13}^{0} e^{\left(R_{1}\right)^{(1)} t} \leq T_{13}(t) \leq T_{13}^{0} e^{\left(\left(R_{1}\right)^{(1)}+\left(r_{13}\right)^{(1)}\right) t}$
$\frac{1}{\left(\mu_{1}\right)^{(1)}} T_{13}^{0} e^{\left(R_{1}\right)^{(1)} t} \leq T_{13}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(1)}} T_{13}^{0} e^{\left(\left(R_{1}\right)^{(1)}+\left(r_{13}\right)^{(1)}\right) t}$
$\frac{\left(b_{15}\right)^{(1)} T_{13}^{0}}{\left(\mu_{1}\right)^{(1)}\left(\left(_{1}\right)^{(1)}-\left(b_{15}^{\prime}\right)^{(1)}\right)}\left[e^{\left(R_{1}\right)^{(1)} t}-e^{-\left(b_{15}^{\prime}\right)^{(1)} t}\right]+T_{15}^{0} e^{-\left(b_{15}^{\prime}\right)^{(1)} t} \leq T_{15}(t) \leq$
$\frac{\left(a_{15}\right)^{(1)} T_{13}^{0}}{\left(\mu_{2}\right)^{(1)}\left(\left(R_{1}\right)^{(1)}+\left(r_{13}\right)^{\left.(1)+\left(R_{2}\right)^{(1)}\right)}\right.}\left[e^{\left(\left(R_{1}\right)^{(1)}+\left(r_{13}\right)^{(1)}\right) t}-e^{-\left(R_{2}\right)^{(1)} t}\right]+T_{15}^{0} e^{-\left(R_{2}\right)^{(1)} t}$
Definition of $\left(S_{1}\right)^{(1)},\left(S_{2}\right)^{(1)},\left(R_{1}\right)^{(1)},\left(R_{2}\right)^{(1)}$ :-
Where $\left(S_{1}\right)^{(1)}=\left(a_{13}\right)^{(1)}\left(m_{2}\right)^{(1)}-\left(a_{13}^{\prime}\right)^{(1)}$

$$
\begin{aligned}
& \left(S_{2}\right)^{(1)}=\left(a_{15}\right)^{(1)}-\left(p_{15}\right)^{(1)} \\
& \left(R_{1}\right)^{(1)}=\left(b_{13}\right)^{(1)}\left(\mu_{2}\right)^{(1)}-\left(b_{13}^{\prime}\right)^{(1)} \\
& \left(R_{2}\right)^{(1)}=\left(b_{15}^{\prime}\right)^{(1)}-\left(r_{15}\right)^{(1)}
\end{aligned}
$$

Behavior of the solutions of equation
Theorem 2: If we denote and define
Definition of $\left(\sigma_{1}\right)^{(2)},\left(\sigma_{2}\right)^{(2)},\left(\tau_{1}\right)^{(2)},\left(\tau_{2}\right)^{(2)}$ :
(d) $\left.\sigma_{1}\right)^{(2)},\left(\sigma_{2}\right)^{(2)},\left(\tau_{1}\right)^{(2)},\left(\tau_{2}\right)^{(2)}$ four constants satisfying
$-\left(\sigma_{2}\right)^{(2)} \leq-\left(a_{16}^{\prime}\right)^{(2)}+\left(a_{17}^{\prime}\right)^{(2)}-\left(a_{16}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}, t\right)+\left(a_{17}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}, t\right) \leq-\left(\sigma_{1}\right)^{(2)}$
$-\left(\tau_{2}\right)^{(2)} \leq-\left(b_{16}^{\prime}\right)^{(2)}+\left(b_{17}^{\prime}\right)^{(2)}-\left(b_{16}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right)-\left(b_{17}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right), t\right) \leq-\left(\tau_{1}\right)^{(2)} 294$
Definition of $\left(v_{1}\right)^{(2)},\left(v_{2}\right)^{(2)},\left(u_{1}\right)^{(2)},\left(u_{2}\right)^{(2)}$ :
By $\left(v_{1}\right)^{(2)}>0,\left(v_{2}\right)^{(2)}<0$ and respectively $\left(u_{1}\right)^{(2)}>0,\left(u_{2}\right)^{(2)}<0$ the roots
(e) of the equations $\left(a_{17}\right)^{(2)}\left(v^{(2)}\right)^{2}+\left(\sigma_{1}\right)^{(2)} v^{(2)}-\left(a_{16}\right)^{(2)}=0 \quad 297$
and $\left(b_{14}\right)^{(2)}\left(u^{(2)}\right)^{2}+\left(\tau_{1}\right)^{(2)} u^{(2)}-\left(b_{16}\right)^{(2)}=0$ and
Definition of $\left(\bar{v}_{1}\right)^{(2)},,\left(\bar{v}_{2}\right)^{(2)},\left(\bar{u}_{1}\right)^{(2)},\left(\bar{u}_{2}\right)^{(2)}$ :
299
By $\left(\bar{v}_{1}\right)^{(2)}>0,\left(\bar{v}_{2}\right)^{(2)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(2)}>0,\left(\bar{u}_{2}\right)^{(2)}<0$ the 300
roots of the equations $\left(a_{17}\right)^{(2)}\left(v^{(2)}\right)^{2}+\left(\sigma_{2}\right)^{(2)} v^{(2)}-\left(a_{16}\right)^{(2)}=0$
and $\left(b_{17}\right)^{(2)}\left(u^{(2)}\right)^{2}+\left(\tau_{2}\right)^{(2)} u^{(2)}-\left(b_{16}\right)^{(2)}=0$
Definition of $\left(m_{1}\right)^{(2)},\left(m_{2}\right)^{(2)},\left(\mu_{1}\right)^{(2)},\left(\mu_{2}\right)^{(2)}:-$
(f) If we define $\left(m_{1}\right)^{(2)},\left(m_{2}\right)^{(2)},\left(\mu_{1}\right)^{(2)},\left(\mu_{2}\right)^{(2)}$ by 304
$\left(m_{2}\right)^{(2)}=\left(v_{0}\right)^{(2)},\left(m_{1}\right)^{(2)}=\left(v_{1}\right)^{(2)}$, if $\left(v_{0}\right)^{(2)}<\left(v_{1}\right)^{(2)} \quad 305$
$\left(m_{2}\right)^{(2)}=\left(v_{1}\right)^{(2)},\left(m_{1}\right)^{(2)}=\left(\bar{v}_{1}\right)^{(2)}$, if $\left(v_{1}\right)^{(2)}<\left(v_{0}\right)^{(2)}<\left(\bar{v}_{1}\right)^{(2)}$,
and $\left(v_{0}\right)^{(2)}=\frac{\mathrm{G}_{16}^{0}}{\mathrm{G}_{17}^{0}}$
$\left(m_{2}\right)^{(2)}=\left(v_{1}\right)^{(2)},\left(m_{1}\right)^{(2)}=\left(v_{0}\right)^{(2)}$, if $\left(\bar{v}_{1}\right)^{(2)}<\left(v_{0}\right)^{(2)}$
and analogously
$\left(\mu_{2}\right)^{(2)}=\left(u_{0}\right)^{(2)},\left(\mu_{1}\right)^{(2)}=\left(u_{1}\right)^{(2)}$, if $\left(u_{0}\right)^{(2)}<\left(u_{1}\right)^{(2)}$
$\left(\mu_{2}\right)^{(2)}=\left(u_{1}\right)^{(2)},\left(\mu_{1}\right)^{(2)}=\left(\bar{u}_{1}\right)^{(2)}$, if $\left(u_{1}\right)^{(2)}<\left(u_{0}\right)^{(2)}<\left(\bar{u}_{1}\right)^{(2)}$,
and $\left(u_{0}\right)^{(2)}=\frac{\mathrm{T}_{16}^{0}}{\mathrm{~T}_{17}^{0}}$
$\left(\mu_{2}\right)^{(2)}=\left(u_{1}\right)^{(2)},\left(\mu_{1}\right)^{(2)}=\left(u_{0}\right)^{(2)}$, if $\left(\bar{u}_{1}\right)^{(2)}<\left(u_{0}\right)^{(2)}$
Then the solution of global equations satisfies the inequalities

$$
\mathrm{G}_{16}^{0} \mathrm{e}^{\left(\left(\mathrm{S}_{1}\right)^{(2)}-\left(p_{16}\right)^{(2)}\right) \mathrm{t}} \leq G_{16}(t) \leq \mathrm{G}_{16}^{0} \mathrm{e}^{\left(\mathrm{S}_{1}\right)^{(2)} \mathrm{t}}
$$

$\left(p_{i}\right)^{(2)}$ is defined by equation

$$
\frac{1}{\left(m_{1}\right)^{(2)}} \mathrm{G}_{16}^{0} \mathrm{e}^{\left(\left(\mathrm{S}_{1}\right)^{(2)}-\left(p_{16}\right)^{(2)}\right) \mathrm{t}} \leq G_{17}(t) \leq \frac{1}{\left(m_{2}\right)^{(2)}} \mathrm{G}_{16}^{0} \mathrm{e}^{\left(\mathrm{S}_{1}\right)^{(2)} \mathrm{t}}
$$

$$
\left(\frac{\left(a_{18}\right)^{(2)} \mathrm{G}_{16}^{0}}{\left(m_{1}\right)^{(2)}\left(\left(\mathrm{S}_{1}\right)^{(2)}-\left(p_{16}\right)^{(2)}-\left(\mathrm{S}_{2}\right)^{(2)}\right)}\left[\mathrm{e}^{\left(\left(\mathrm{S}_{1}\right)^{(2)}-\left(p_{16}\right)^{(2)}\right) \mathrm{t}}-\mathrm{e}^{-\left(\mathrm{S}_{2}\right)^{(2)} \mathrm{t}}\right]+\mathrm{G}_{18}^{0} \mathrm{e}^{-\left(\mathrm{S}_{2}\right)^{(2)} \mathrm{t}} \leq \mathrm{G}_{18}(t) \leq\right.
$$

$$
\left.\frac{\left(a_{18}\right)^{(2)} \mathrm{G}_{16}^{0}}{\left(m_{2}\right)^{(2)}\left(\left(\mathrm{s}_{1}\right)^{(2)}-\left(a_{18}^{\prime}\right)^{(2)}\right)}\left[\mathrm{e}^{\left(\mathrm{S}_{1}\right)^{(2)} \mathrm{t}}-\mathrm{e}^{-\left(a_{18}^{\prime}\right)^{(2)}} \mathrm{t}\right]+\mathrm{G}_{18}^{0} \mathrm{e}^{-\left(a_{18}^{\prime}\right)^{(2)} \mathrm{t}}\right)
$$

$$
\mathrm{T}_{16}^{0} \mathrm{e}^{\left(\mathrm{R}_{1}\right)^{(2)} t} \leq T_{16}(t) \leq \mathrm{T}_{16}^{0} \mathrm{e}^{\left.\left(\mathrm{R}_{1}\right)^{(2)}+\left(r_{16}\right)^{(2)}\right) t}
$$

$$
\frac{\left(a_{18}\right)^{(2)} \mathrm{T}_{16}^{0}}{\left(\mu_{2}\right)^{(2)}\left(\left(\mathrm{R}_{1}\right)^{(2)}+\left(r_{16}\right)^{(2)}+\left(\mathrm{R}_{2}\right)^{(2)}\right)}\left[\mathrm{e}^{\left(\left(\mathrm{R}_{1}\right)^{(2)}+\left(r_{16}\right)^{(2)}\right) t}-\mathrm{e}^{-\left(\mathrm{R}_{2}\right)^{(2)} t}\right]+\mathrm{T}_{18}^{0} \mathrm{e}^{-\left(\mathrm{R}_{2}\right)^{(2)} t}
$$

$$
\begin{aligned}
& \left(\mathrm{S}_{2}\right)^{(2)}=\left(a_{18}\right)^{(2)}-\left(p_{18}\right)^{(2)} \\
& \left(R_{1}\right)^{(2)}=\left(b_{16}\right)^{(2)}\left(\mu_{2}\right)^{(1)}-\left(b_{16}^{\prime}\right)^{(2)} \\
& \left(\mathrm{R}_{2}\right)^{(2)}=\left(b_{18}^{\prime}\right)^{(2)}-\left(r_{18}\right)^{(2)}
\end{aligned}
$$

## Behavior of the solutions

$$
\frac{1}{\left(\mu_{1}\right)^{(2)}} \mathrm{T}_{16}^{0} \mathrm{e}^{\left(\mathrm{R}_{1}\right)^{(2)} t} \leq T_{16}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(2)}} \mathrm{T}_{16}^{0} \mathrm{e}^{\left(\left(\mathrm{R}_{1}\right)^{(2)}+\left(r_{16}\right)^{(2)}\right) t}
$$

$$
\frac{\left(b_{18}\right)^{(2)} \mathrm{T}_{16}^{0}}{\left(\mu_{1}\right)^{(2)}\left(\left(\mathrm{R}_{1}\right)^{(2)}-\left(b_{18}^{\prime}\right)^{(2)}\right)}\left[\mathrm{e}^{\left(\mathrm{R}_{1}\right)^{(2)} t}-\mathrm{e}^{-\left(b_{18}^{\prime}\right)^{(2)} t}\right]+\mathrm{T}_{18}^{0} \mathrm{e}^{-\left(b_{18}^{\prime}\right)^{(2)} t} \leq T_{18}(t) \leq
$$

$$
\text { Definition of }\left(\mathrm{S}_{1}\right)^{(2)},\left(\mathrm{S}_{2}\right)^{(2)},\left(\mathrm{R}_{1}\right)^{(2)},\left(\mathrm{R}_{2}\right)^{(2)} \text { :- }
$$

$$
\text { Where }\left(\mathrm{S}_{1}\right)^{(2)}=\left(a_{16}\right)^{(2)}\left(m_{2}\right)^{(2)}-\left(a_{16}^{\prime}\right)^{(2)}
$$

## Theorem 3: If we denote and define

## Definition of $\left(\sigma_{1}\right)^{(3)},\left(\sigma_{2}\right)^{(3)},\left(\tau_{1}\right)^{(3)},\left(\tau_{2}\right)^{(3)}$ :

(a) $\left.\sigma_{1}\right)^{(3)},\left(\sigma_{2}\right)^{(3)},\left(\tau_{1}\right)^{(3)},\left(\tau_{2}\right)^{(3)}$ four constants satisfying

$$
\begin{aligned}
& -\left(\sigma_{2}\right)^{(3)} \leq-\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{21}^{\prime}\right)^{(3)}-\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)+\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right) \leq-\left(\sigma_{1}\right)^{(3)} \\
& -\left(\tau_{2}\right)^{(3)} \leq-\left(b_{20}^{\prime}\right)^{(3)}+\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{20}^{\prime \prime}\right)^{(3)}(G, t)-\left(b_{21}^{\prime \prime}\right)^{(3)}\left(\left(G_{23}\right), t\right) \leq-\left(\tau_{1}\right)^{(3)}
\end{aligned}
$$

Definition of $\left(v_{1}\right)^{(3)},\left(v_{2}\right)^{(3)},\left(u_{1}\right)^{(3)},\left(u_{2}\right)^{(3)}$ :
(b) By $\left(v_{1}\right)^{(3)}>0,\left(v_{2}\right)^{(3)}<0$ and respectively $\left(u_{1}\right)^{(3)}>0,\left(u_{2}\right)^{(3)}<0$ the roots of the equations $\left(a_{21}\right)^{(3)}\left(v^{(3)}\right)^{2}+\left(\sigma_{1}\right)^{(3)} v^{(3)}-\left(a_{20}\right)^{(3)}=0$
and $\left(b_{21}\right)^{(3)}\left(u^{(3)}\right)^{2}+\left(\tau_{1}\right)^{(3)} u^{(3)}-\left(b_{20}\right)^{(3)}=0$ and
By $\left(\bar{v}_{1}\right)^{(3)}>0,\left(\bar{v}_{2}\right)^{(3)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(3)}>0,\left(\bar{u}_{2}\right)^{(3)}<0$ the
roots of the equations $\left(a_{21}\right)^{(3)}\left(v^{(3)}\right)^{2}+\left(\sigma_{2}\right)^{(3)} v^{(3)}-\left(a_{20}\right)^{(3)}=0$
and $\left(b_{21}\right)^{(3)}\left(u^{(3)}\right)^{2}+\left(\tau_{2}\right)^{(3)} u^{(3)}-\left(b_{20}\right)^{(3)}=0$
Definition of $\left(m_{1}\right)^{(3)},\left(m_{2}\right)^{(3)},\left(\mu_{1}\right)^{(3)},\left(\mu_{2}\right)^{(3)}:-$
(c) If we define $\left(m_{1}\right)^{(3)},\left(m_{2}\right)^{(3)},\left(\mu_{1}\right)^{(3)},\left(\mu_{2}\right)^{(3)}$ by

$$
\left(m_{2}\right)^{(3)}=\left(v_{0}\right)^{(3)},\left(m_{1}\right)^{(3)}=\left(v_{1}\right)^{(3)}, \text { if }\left(v_{0}\right)^{(3)}<\left(v_{1}\right)^{(3)}
$$

$$
\left(m_{2}\right)^{(3)}=\left(v_{1}\right)^{(3)},\left(m_{1}\right)^{(3)}=\left(\bar{v}_{1}\right)^{(3)}, \text { if }\left(v_{1}\right)^{(3)}<\left(v_{0}\right)^{(3)}<\left(\bar{v}_{1}\right)^{(3)} \text {, }
$$

$$
\text { and }\left(v_{0}\right)^{(3)}=\frac{G_{20}^{0}}{G_{21}^{0}}
$$

$$
\left(m_{2}\right)^{(3)}=\left(v_{1}\right)^{(3)},\left(m_{1}\right)^{(3)}=\left(v_{0}\right)^{(3)}, \text { if }\left(\bar{v}_{1}\right)^{(3)}<\left(v_{0}\right)^{(3)}
$$

and analogously

$$
\begin{aligned}
& \left(\mu_{2}\right)^{(3)}=\left(u_{0}\right)^{(3)},\left(\mu_{1}\right)^{(3)}=\left(u_{1}\right)^{(3)}, \text { if }\left(u_{0}\right)^{(3)}<\left(u_{1}\right)^{(3)} \\
& \left(\mu_{2}\right)^{(3)}=\left(u_{1}\right)^{(3)},\left(\mu_{1}\right)^{(3)}=\left(\bar{u}_{1}\right)^{(3)}, \text { if }\left(u_{1}\right)^{(3)}<\left(u_{0}\right)^{(3)}<\left(\bar{u}_{1}\right)^{(3)}, \quad \text { and }\left(u_{0}\right)^{(3)}=\frac{T_{20}^{0}}{T_{21}^{0}} \\
& \left(\mu_{2}\right)^{(3)}=\left(u_{1}\right)^{(3)},\left(\mu_{1}\right)^{(3)}=\left(u_{0}\right)^{(3)}, \text { if }\left(\bar{u}_{1}\right)^{(3)}<\left(u_{0}\right)^{(3)}
\end{aligned}
$$

$$
\text { Definition of }\left(S_{1}\right)^{(3)},\left(S_{2}\right)^{(3)},\left(R_{1}\right)^{(3)},\left(R_{2}\right)^{(3)} \text { :- }
$$

Where $\left(S_{1}\right)^{(3)}=\left(a_{20}\right)^{(3)}\left(m_{2}\right)^{(3)}-\left(a_{20}^{\prime}\right)^{(3)}$

$$
\begin{aligned}
& \left(S_{2}\right)^{(3)}=\left(a_{22}\right)^{(3)}-\left(p_{22}\right)^{(3)} \\
& \left(R_{1}\right)^{(3)}=\left(b_{20}\right)^{(3)}\left(\mu_{2}\right)^{(3)}-\left(b_{20}^{\prime}\right)^{(3)} \\
& \left(R_{2}\right)^{(3)}=\left(b_{22}^{\prime}\right)^{(3)}-\left(r_{22}\right)^{(3)}
\end{aligned}
$$

## Behavior of the solutions of equation

Theorem: If we denote and define
Definition of $\left(\sigma_{1}\right)^{(4)},\left(\sigma_{2}\right)^{(4)},\left(\tau_{1}\right)^{(4)},\left(\tau_{2}\right)^{(4)}$ :
(d) $\left(\sigma_{1}\right)^{(4)},\left(\sigma_{2}\right)^{(4)},\left(\tau_{1}\right)^{(4)},\left(\tau_{2}\right)^{(4)}$ four constants satisfying

$$
\begin{aligned}
& -\left(\sigma_{2}\right)^{(4)} \leq-\left(a_{24}^{\prime}\right)^{(4)}+\left(a_{25}^{\prime}\right)^{(4)}-\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)+\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right) \leq-\left(\sigma_{1}\right)^{(4)} \\
& -\left(\tau_{2}\right)^{(4)} \leq-\left(b_{24}^{\prime}\right)^{(4)}+\left(b_{25}^{\prime}\right)^{(4)}-\left(b_{24}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right)-\left(b_{25}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right), t\right) \leq-\left(\tau_{1}\right)^{(4)}
\end{aligned}
$$

Definition of $\left(v_{1}\right)^{(4)},\left(v_{2}\right)^{(4)},\left(u_{1}\right)^{(4)},\left(u_{2}\right)^{(4)}, v^{(4)}, u^{(4)}$ :
(e) By $\left(v_{1}\right)^{(4)}>0,\left(v_{2}\right)^{(4)}<0$ and respectively $\left(u_{1}\right)^{(4)}>0,\left(u_{2}\right)^{(4)}<0$ the roots of the equations $\left(a_{25}\right)^{(4)}\left(v^{(4)}\right)^{2}+\left(\sigma_{1}\right)^{(4)} v^{(4)}-\left(a_{24}\right)^{(4)}=0$
and $\left(b_{25}\right)^{(4)}\left(u^{(4)}\right)^{2}+\left(\tau_{1}\right)^{(4)} u^{(4)}-\left(b_{24}\right)^{(4)}=0$ and
Definition of $\left(\bar{v}_{1}\right)^{(4)},\left(\bar{v}_{2}\right)^{(4)},\left(\bar{u}_{1}\right)^{(4)},\left(\bar{u}_{2}\right)^{(4)}$ :
By $\left(\bar{v}_{1}\right)^{(4)}>0,\left(\bar{v}_{2}\right)^{(4)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(4)}>0,\left(\bar{u}_{2}\right)^{(4)}<0$ the roots of the equations $\left(a_{25}\right)^{(4)}\left(v^{(4)}\right)^{2}+\left(\sigma_{2}\right)^{(4)} v^{(4)}-\left(a_{24}\right)^{(4)}=0$

$$
\text { and }\left(b_{25}\right)^{(4)}\left(u^{(4)}\right)^{2}+\left(\tau_{2}\right)^{(4)} u^{(4)}-\left(b_{24}\right)^{(4)}=0
$$

Definition of $\left(m_{1}\right)^{(4)},\left(m_{2}\right)^{(4)},\left(\mu_{1}\right)^{(4)},\left(\mu_{2}\right)^{(4)},\left(v_{0}\right)^{(4)}:-$
(f) If we define $\left(m_{1}\right)^{(4)},\left(m_{2}\right)^{(4)},\left(\mu_{1}\right)^{(4)},\left(\mu_{2}\right)^{(4)}$ by

$$
\left(m_{2}\right)^{(4)}=\left(v_{0}\right)^{(4)},\left(m_{1}\right)^{(4)}=\left(v_{1}\right)^{(4)}, \text { if }\left(v_{0}\right)^{(4)}<\left(v_{1}\right)^{(4)}
$$

$\left(m_{2}\right)^{(4)}=\left(v_{1}\right)^{(4)},\left(m_{1}\right)^{(4)}=\left(\bar{v}_{1}\right)^{(4)}$, if $\left(v_{4}\right)^{(4)}<\left(v_{0}\right)^{(4)}<\left(\bar{v}_{1}\right)^{(4)}$,
and $\left(v_{0}\right)^{(4)}=\frac{G_{24}^{0}}{G_{25}^{0}}$

$$
\left(m_{2}\right)^{(4)}=\left(v_{4}\right)^{(4)},\left(m_{1}\right)^{(4)}=\left(v_{0}\right)^{(4)}, \text { if }\left(\bar{v}_{4}\right)^{(4)}<\left(v_{0}\right)^{(4)}
$$

and analogously

$$
\begin{aligned}
& \left(\mu_{2}\right)^{(4)}=\left(u_{0}\right)^{(4)},\left(\mu_{1}\right)^{(4)}=\left(u_{1}\right)^{(4)}, \text { if }\left(u_{0}\right)^{(4)}<\left(u_{1}\right)^{(4)} \\
& \left(\mu_{2}\right)^{(4)}=\left(u_{1}\right)^{(4)},\left(\mu_{1}\right)^{(4)}=\left(\bar{u}_{1}\right)^{(4)}, \text { if }\left(u_{1}\right)^{(4)}<\left(u_{0}\right)^{(4)}<\left(\bar{u}_{1}\right)^{(4)}
\end{aligned}
$$

$$
\begin{aligned}
& \begin{array}{l}
T_{20}^{0} e^{\left(R_{1}\right)^{(3)} t} \leq T_{20}(t) \leq T_{20}^{0} e^{\left.\left(R_{1}\right)^{(3)}+\left(r_{20}\right)^{(3)}\right) t} \\
\frac{1}{\left(\mu_{1}\right)^{(3)}} T_{20}^{0} e^{\left(R_{1}\right)^{(3)} t} \leq T_{20}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(3)}} T_{20}^{0} e^{\left.\left(R_{1}\right)^{(3)}+\left(r_{20}\right)^{(3)}\right) t}
\end{array} \\
& \frac{\left(b_{22}\right)^{(3)} T_{20}^{0}}{\left.\left(\mu_{1}\right)^{(3)}\left(R_{1}\right)^{(3)}-\left(b_{22}^{\prime}\right)^{(3)}\right)}\left[e^{\left(R_{1}\right)^{(3)} t}-e^{-\left(b_{22}^{\prime}\right)^{(3)} t}\right]+T_{22}^{0} e^{-\left(b_{22}^{\prime}\right)^{(3)} t} \leq T_{22}(t) \leq \\
& \frac{\left(a_{22}\right)^{(3)} T_{20}^{0}}{\left(\mu_{2}\right)^{(3)}\left(\left(R_{1}\right)^{(3)}+\left(r_{20}\right)^{(3)}+\left(R_{2}\right)^{(3)}\right)}\left[e^{\left(\left(R_{1}\right)^{(3)}+\left(r_{20}\right)^{(3)}\right) t}-e^{-\left(R_{2}\right)^{(3)} t}\right]+T_{22}^{0} e^{-\left(R_{2}\right)^{(3)} t}
\end{aligned}
$$

$$
\text { and }\left(u_{0}\right)^{(4)}=\frac{T_{24}^{0}}{T_{25}^{0}}
$$

$$
\left(\mu_{2}\right)^{(4)}=\left(u_{1}\right)^{(4)},\left(\mu_{1}\right)^{(4)}=\left(u_{0}\right)^{(4)}, \text { if }\left(\bar{u}_{1}\right)^{(4)}<\left(u_{0}\right)^{(4)} \text { where }\left(u_{1}\right)^{(4)},\left(\bar{u}_{1}\right)^{(4)}
$$

Then the solution of global equations satisfies the inequalities

$$
G_{24}^{0} e^{\left(\left(S_{1}\right)^{(4)}-\left(p_{24}\right)^{(4)}\right) t} \leq G_{24}(t) \leq G_{24}^{0} e^{\left(S_{1}\right)^{(4)} t}
$$

where $\left(p_{i}\right)^{(4)}$ is defined by equation
$\frac{1}{\left(m_{1}\right)^{(4)}} G_{24}^{0} e^{\left(\left(S_{1}\right)^{(4)}-\left(p_{24}\right)^{(4)}\right) t} \leq G_{25}(t) \leq \frac{1}{\left(m_{2}\right)^{(4)}} G_{24}^{0} e^{\left(S_{1}\right)^{(4)} t}$
$\left(\frac{\left(a_{26}\right)^{(4)} G_{24}^{0}}{\left(m_{1}\right)^{(4)}\left(\left(S_{1}\right)^{(4)}-\left(p_{24}\right)^{(4)}-\left(S_{2}\right)^{(4)}\right)}\left[e^{\left(\left(S_{1}\right)^{(4)}-\left(p_{24}\right)^{(4)}\right) t}-e^{-\left(S_{2}\right)^{(4)} t}\right]+G_{26}^{0} e^{-\left(S_{2}\right)^{(4)} t} \leq G_{26}(t) \leq\right.$
(a26)4G240(m2)4(S1)4-(a26')4e(S1)4t-e-(a26')4t+G260e-(a26')4t
$T_{24}^{0} e^{\left(R_{1}\right)^{(4)} t} \leq T_{24}(t) \leq T_{24}^{0} e^{\left(\left(R_{1}\right)^{(4)}+\left(r_{24}\right)^{(4)}\right) t}$
$\frac{1}{\left(\mu_{1}\right)^{(4)}} T_{24}^{0} e^{\left(R_{1}\right)^{(4)} t} \leq T_{24}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(4)}} T_{24}^{0} e^{\left(\left(R_{1}\right)^{(4)}+\left(r_{24}\right)^{(4)}\right) t}$
$\frac{\left(b_{26}\right)^{(4)} T_{24}^{0}}{\left(\mu_{1}\right)^{(4)}\left(\left(R_{1}\right)^{(4)}-\left(b_{26}^{\prime}\right)^{(4)}\right)}\left[e^{\left(R_{1}\right)^{(4)} t}-e^{-\left(b_{26}^{\prime}\right)^{(4)} t}\right]+T_{26}^{0} e^{-\left(b_{26}^{\prime}\right)^{(4)} t} \leq T_{26}(t) \leq$
$\frac{\left(a_{26}\right)^{(4)} T_{24}^{0}}{\left(\mu_{2}\right)^{(4)}\left(\left(R_{1}\right)^{(4)}+\left(r_{24}\right)^{(4)}+\left(R_{2}\right)^{(4)}\right)}\left[e^{\left(\left(R_{1}\right)^{(4)}+\left(r_{24}\right)^{(4)}\right) t}-e^{-\left(R_{2}\right)^{(4)} t}\right]+T_{26}^{0} e^{-\left(R_{2}\right)^{(4)} t}$
Definition of $\left(S_{1}\right)^{(4)},\left(S_{2}\right)^{(4)},\left(R_{1}\right)^{(4)},\left(R_{2}\right)^{(4)}$ :-
Where $\left(S_{1}\right)^{(4)}=\left(a_{24}\right)^{(4)}\left(m_{2}\right)^{(4)}-\left(a_{24}^{\prime}\right)^{(4)}$

$$
\begin{aligned}
& \left(S_{2}\right)^{(4)}=\left(a_{26}\right)^{(4)}-\left(p_{26}\right)^{(4)} \\
& \quad\left(R_{1}\right)^{(4)}=\left(b_{24}\right)^{(4)}\left(\mu_{2}\right)^{(4)}-\left(b_{24}^{\prime}\right)^{(4)} \\
& \left(R_{2}\right)^{(4)}=\left(b_{26}^{\prime}\right)^{(4)}-\left(r_{26}\right)^{(4)}
\end{aligned}
$$

## Behavior of the solutions of equation

Theorem 2: If we denote and define
Definition of $\left(\sigma_{1}\right)^{(5)},\left(\sigma_{2}\right)^{(5)},\left(\tau_{1}\right)^{(5)},\left(\tau_{2}\right)^{(5)}$ :
(g) $\left(\sigma_{1}\right)^{(5)},\left(\sigma_{2}\right)^{(5)},\left(\tau_{1}\right)^{(5)},\left(\tau_{2}\right)^{(5)}$ four constants satisfying
$-\left(\sigma_{2}\right)^{(5)} \leq-\left(a_{28}^{\prime}\right)^{(5)}+\left(a_{29}^{\prime}\right)^{(5)}-\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)+\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right) \leq-\left(\sigma_{1}\right)^{(5)}$
$-\left(\tau_{2}\right)^{(5)} \leq-\left(b_{28}^{\prime}\right)^{(5)}+\left(b_{29}^{\prime}\right)^{(5)}-\left(b_{28}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right)-\left(b_{29}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right), t\right) \leq-\left(\tau_{1}\right)^{(5)}$
Definition of $\left(v_{1}\right)^{(5)},\left(v_{2}\right)^{(5)},\left(u_{1}\right)^{(5)},\left(u_{2}\right)^{(5)}, v^{(5)}, u^{(5)}$ :
(h) By $\left(v_{1}\right)^{(5)}>0,\left(v_{2}\right)^{(5)}<0$ and respectively $\left(u_{1}\right)^{(5)}>0,\left(u_{2}\right)^{(5)}<0$ the roots of the equations $\left(a_{29}\right)^{(5)}\left(v^{(5)}\right)^{2}+\left(\sigma_{1}\right)^{(5)} v^{(5)}-\left(a_{28}\right)^{(5)}=0$
and $\left(b_{29}\right)^{(5)}\left(u^{(5)}\right)^{2}+\left(\tau_{1}\right)^{(5)} u^{(5)}-\left(b_{28}\right)^{(5)}=0$ and
Definition of $\left(\bar{v}_{1}\right)^{(5)},\left(\bar{v}_{2}\right)^{(5)},\left(\bar{u}_{1}\right)^{(5)},\left(\bar{u}_{2}\right)^{(5)}$ :
By $\left(\bar{v}_{1}\right)^{(5)}>0,\left(\bar{v}_{2}\right)^{(5)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(5)}>0,\left(\bar{u}_{2}\right)^{(5)}<0$ the roots of the equations $\left(a_{29}\right)^{(5)}\left(v^{(5)}\right)^{2}+\left(\sigma_{2}\right)^{(5)} v^{(5)}-\left(a_{28}\right)^{(5)}=0$ and $\left(b_{29}\right)^{(5)}\left(u^{(5)}\right)^{2}+\left(\tau_{2}\right)^{(5)} u^{(5)}-\left(b_{28}\right)^{(5)}=0$
Definition of $\left(m_{1}\right)^{(5)},\left(m_{2}\right)^{(5)},\left(\mu_{1}\right)^{(5)},\left(\mu_{2}\right)^{(5)},\left(v_{0}\right)^{(5)}:-$
(i) If we define $\left(m_{1}\right)^{(5)},\left(m_{2}\right)^{(5)},\left(\mu_{1}\right)^{(5)},\left(\mu_{2}\right)^{(5)}$ by

$$
\begin{aligned}
& \left(m_{2}\right)^{(5)}=\left(v_{0}\right)^{(5)},\left(m_{1}\right)^{(5)}=\left(v_{1}\right)^{(5)}, \text { if }\left(v_{0}\right)^{(5)}<\left(v_{1}\right)^{(5)} \\
& \left(m_{2}\right)^{(5)}=\left(v_{1}\right)^{(5)},\left(m_{1}\right)^{(5)}=\left(\bar{v}_{1}\right)^{(5)}, \text { if }\left(v_{1}\right)^{(5)}<\left(v_{0}\right)^{(5)}<\left(\bar{v}_{1}\right)^{(5)}, \\
& \text { and }\left(v_{0}\right)^{(5)}=\frac{G_{28}^{0}}{G_{29}^{0}} \\
& \left(m_{2}\right)^{(5)}=\left(v_{1}\right)^{(5)},\left(m_{1}\right)^{(5)}=\left(v_{0}\right)^{(5)}, \text { if }\left(\bar{v}_{1}\right)^{(5)}<\left(v_{0}\right)^{(5)}
\end{aligned}
$$

and analogously

$$
\begin{aligned}
& \left(\mu_{2}\right)^{(5)}=\left(u_{0}\right)^{(5)},\left(\mu_{1}\right)^{(5)}=\left(u_{1}\right)^{(5)}, \text { if }\left(u_{0}\right)^{(5)}<\left(u_{1}\right)^{(5)} \\
& \left(\mu_{2}\right)^{(5)}=\left(u_{1}\right)^{(5)},\left(\mu_{1}\right)^{(5)}=\left(\bar{u}_{1}\right)^{(5)}, \text { if }\left(u_{1}\right)^{(5)}<\left(u_{0}\right)^{(5)}<\left(\bar{u}_{1}\right)^{(5)}, \\
& \text { and }\left(u_{0}\right)^{(5)}=\frac{T_{28}^{0}}{T_{29}^{0}} \\
& \left(\mu_{2}\right)^{(5)}=\left(u_{1}\right)^{(5)},\left(\mu_{1}\right)^{(5)}=\left(u_{0}\right)^{(5)}, \text { if }\left(\bar{u}_{1}\right)^{(5)}<\left(u_{0}\right)^{(5)} \text { where }\left(u_{1}\right)^{(5)},\left(\bar{u}_{1}\right)^{(5)}
\end{aligned}
$$

Then the solution of global equations satisfies the inequalities
$G_{28}^{0} e^{\left(\left(S_{1}\right)^{(5)}-\left(p_{28}\right)^{(5)}\right) t} \leq G_{28}(t) \leq G_{28}^{0} e^{\left(S_{1}\right)^{(5)} t}$
where $\left(p_{i}\right)^{(5)}$ is defined by equation
$\frac{1}{\left(m_{5}\right)^{(5)}} G_{28}^{0} e^{\left(\left(S_{1}\right)^{(5)}-\left(p_{28}\right)^{(5)}\right) t} \leq G_{29}(t) \leq \frac{1}{\left(m_{2}\right)^{(5)}} G_{28}^{0} e^{\left(S_{1}\right)^{(5)} t}$
$\left(\frac{\left(a_{30}\right)^{(5)} G_{28}^{0}}{\left(m_{1}\right)^{(5)}\left(\left(S_{1}\right)^{(5)}-\left(p_{28}\right)^{(5)}-\left(S_{2}\right)^{(5)}\right)}\left[e^{\left(\left(S_{1}\right)^{(5)}-\left(p_{28}\right)^{(5)}\right) t}-e^{-\left(S_{2}\right)^{(5)} t}\right]+G_{30}^{0} e^{-\left(S_{2}\right)^{(5)} t} \leq G_{30}(t) \leq\right.$
(a30)5G280(m2)5(S1)5-(a30')5e(S1)5t-e-(a30')5t+G300e-(a30')5t
$T_{28}^{0} e^{\left(R_{1}\right)^{(5)} t} \leq T_{28}(t) \leq T_{28}^{0} e^{\left(\left(R_{1}\right)^{(5)}+\left(r_{28}\right)^{(5)}\right) t}$
$\frac{1}{\left(\mu_{1}\right)^{(5)}} T_{28}^{0} e^{\left(R_{1}\right)^{(5)} t} \leq T_{28}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(5)}} T_{28}^{0} e^{\left(\left(R_{1}\right)^{(5)}+\left(r_{28}\right)^{(5)}\right) t}$
$\frac{\left(b_{30}\right)^{(5)} T_{28}^{0}}{\left(\mu_{1}\right)^{(5)}\left(\left(R_{1}\right)^{(5)}-\left(b_{30}^{\prime}\right)^{(5)}\right)}\left[e^{\left(R_{1}\right)^{(5)} t}-e^{-\left(b_{30}^{\prime}\right)^{(5)} t}\right]+T_{30}^{0} e^{-\left(b_{30}^{\prime}\right)^{(5)} t} \leq T_{30}(t) \leq$
$\frac{\left(a_{30}\right)^{(5)} T_{28}^{0}}{\left(\mu_{2}\right)^{(5)}\left(\left(R_{1}\right)^{(5)}+\left(r_{28}\right)^{(5)}+\left(R_{2}\right)^{(5)}\right)}\left[e^{\left(\left(R_{1}\right)^{(5)}+\left(r_{28}\right)^{(5)}\right) t}-e^{-\left(R_{2}\right)^{(5)} t}\right]+T_{30}^{0} e^{-\left(R_{2}\right)^{(5)} t}$
Definition of $\left(S_{1}\right)^{(5)},\left(S_{2}\right)^{(5)},\left(R_{1}\right)^{(5)},\left(R_{2}\right)^{(5)}$ :-

Where $\left(S_{1}\right)^{(5)}=\left(a_{28}\right)^{(5)}\left(m_{2}\right)^{(5)}-\left(a_{28}^{\prime}\right)^{(5)}$

$$
\begin{aligned}
& \left(S_{2}\right)^{(5)}=\left(a_{30}\right)^{(5)}-\left(p_{30}\right)^{(5)} \\
& \left(R_{1}\right)^{(5)}=\left(b_{28}\right)^{(5)}\left(\mu_{2}\right)^{(5)}-\left(b_{28}^{\prime}\right)^{(5)} \\
& \left(R_{2}\right)^{(5)}=\left(b_{30}^{\prime}\right)^{(5)}-\left(r_{30}\right)^{(5)}
\end{aligned}
$$

## Behavior of the solutions of equation

Theorem 2: If we denote and define
Definition of $\left(\sigma_{1}\right)^{(6)},\left(\sigma_{2}\right)^{(6)},\left(\tau_{1}\right)^{(6)},\left(\tau_{2}\right)^{(6)}$ :
(j) $\left(\sigma_{1}\right)^{(6)},\left(\sigma_{2}\right)^{(6)},\left(\tau_{1}\right)^{(6)},\left(\tau_{2}\right)^{(6)}$ four constants satisfying
$-\left(\sigma_{2}\right)^{(6)} \leq-\left(a_{32}^{\prime}\right)^{(6)}+\left(a_{33}^{\prime}\right)^{(6)}-\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)+\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right) \leq-\left(\sigma_{1}\right)^{(6)}$
$-\left(\tau_{2}\right)^{(6)} \leq-\left(b_{32}^{\prime}\right)^{(6)}+\left(b_{33}^{\prime}\right)^{(6)}-\left(b_{32}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right)-\left(b_{33}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right), t\right) \leq-\left(\tau_{1}\right)^{(6)}$
Definition of $\left(v_{1}\right)^{(6)},\left(v_{2}\right)^{(6)},\left(u_{1}\right)^{(6)},\left(u_{2}\right)^{(6)}, v^{(6)}, u^{(6)}$ :
(k) By $\left(v_{1}\right)^{(6)}>0,\left(v_{2}\right)^{(6)}<0$ and respectively $\left(u_{1}\right)^{(6)}>0,\left(u_{2}\right)^{(6)}<0$ the roots of the equations $\left(a_{33}\right)^{(6)}\left(v^{(6)}\right)^{2}+\left(\sigma_{1}\right)^{(6)} v^{(6)}-\left(a_{32}\right)^{(6)}=0$ and $\left(b_{33}\right)^{(6)}\left(u^{(6)}\right)^{2}+\left(\tau_{1}\right)^{(6)} u^{(6)}-\left(b_{32}\right)^{(6)}=0$ and

Definition of $\left(\bar{v}_{1}\right)^{(6)},,\left(\bar{v}_{2}\right)^{(6)},\left(\bar{u}_{1}\right)^{(6)},\left(\bar{u}_{2}\right)^{(6)}$ :
By $\left(\bar{v}_{1}\right)^{(6)}>0,\left(\bar{v}_{2}\right)^{(6)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(6)}>0,\left(\bar{u}_{2}\right)^{(6)}<0$ the roots of the equations $\left(a_{33}\right)^{(6)}\left(v^{(6)}\right)^{2}+\left(\sigma_{2}\right)^{(6)} v^{(6)}-\left(a_{32}\right)^{(6)}=0$ and $\left(b_{33}\right)^{(6)}\left(u^{(6)}\right)^{2}+\left(\tau_{2}\right)^{(6)} u^{(6)}-\left(b_{32}\right)^{(6)}=0$
Definition of $\left(m_{1}\right)^{(6)},\left(m_{2}\right)^{(6)},\left(\mu_{1}\right)^{(6)},\left(\mu_{2}\right)^{(6)},\left(v_{0}\right)^{(6)}:-$
(l) If we define $\left(m_{1}\right)^{(6)},\left(m_{2}\right)^{(6)},\left(\mu_{1}\right)^{(6)},\left(\mu_{2}\right)^{(6)}$ by
$\left(m_{2}\right)^{(6)}=\left(v_{0}\right)^{(6)},\left(m_{1}\right)^{(6)}=\left(v_{1}\right)^{(6)}$, if $\left(v_{0}\right)^{(6)}<\left(v_{1}\right)^{(6)}$
$\left(m_{2}\right)^{(6)}=\left(v_{1}\right)^{(6)},\left(m_{1}\right)^{(6)}=\left(\bar{v}_{6}\right)^{(6)}$, if $\left(v_{1}\right)^{(6)}<\left(v_{0}\right)^{(6)}<\left(\bar{v}_{1}\right)^{(6)}$,
and $\left(v_{0}\right)^{(6)}=\frac{G_{32}^{0}}{G_{33}^{0}}$
$\left(m_{2}\right)^{(6)}=\left(v_{1}\right)^{(6)},\left(m_{1}\right)^{(6)}=\left(v_{0}\right)^{(6)}$, if $\left(\bar{v}_{1}\right)^{(6)}<\left(v_{0}\right)^{(6)}$
and analogously

$$
\begin{aligned}
& \quad\left(\mu_{2}\right)^{(6)}=\left(u_{0}\right)^{(6)},\left(\mu_{1}\right)^{(6)}=\left(u_{1}\right)^{(6)}, \text { if }\left(u_{0}\right)^{(6)}<\left(u_{1}\right)^{(6)} \\
& \left(\mu_{2}\right)^{(6)}=\left(u_{1}\right)^{(6)},\left(\mu_{1}\right)^{(6)}=\left(\bar{u}_{1}\right)^{(6)}, \text { if }\left(u_{1}\right)^{(6)}<\left(u_{0}\right)^{(6)}<\left(\bar{u}_{1}\right)^{(6)}, \\
& \text { and }\left(u_{0}\right)^{(6)}=\frac{T_{32}^{0}}{T_{33}^{0}}
\end{aligned}
$$

$$
\left(\mu_{2}\right)^{(6)}=\left(u_{1}\right)^{(6)},\left(\mu_{1}\right)^{(6)}=\left(u_{0}\right)^{(6)}, \text { if }\left(\bar{u}_{1}\right)^{(6)}<\left(u_{0}\right)^{(6)} \text { where }\left(u_{1}\right)^{(6)},\left(\bar{u}_{1}\right)^{(6)}
$$

Then the solution of global equations satisfies the inequalities

$$
G_{32}^{0} e^{\left(\left(S_{1}\right)^{(6)}-\left(p_{32}\right)^{(6)}\right) t} \leq G_{32}(t) \leq G_{32}^{0} e^{\left(S_{1}\right)^{(6)} t}
$$

where $\left(p_{i}\right)^{(6)}$ is defined by equation
$\frac{1}{\left(m_{1}\right)^{(6)}} G_{32}^{0} e^{\left(\left(S_{1}\right)^{(6)}-\left(p_{32}\right)^{(6)}\right) t} \leq G_{33}(t) \leq \frac{1}{\left(m_{2}\right)^{(6)}} G_{32}^{0} e^{\left(S_{1}\right)^{(6)} t}$
$\left(\frac{\left(a_{34}\right)^{(6)} G_{32}^{0}}{\left(m_{1}\right)^{(6)}\left(\left(S_{1}\right)^{(6)}-\left(p_{32}\right)^{(6)}-\left(S_{2}\right)^{(6)}\right)}\left[e^{\left(\left(S_{1}\right)^{(6)}-\left(p_{32}\right)^{(6)}\right) t}-e^{-\left(S_{2}\right)^{(6)} t}\right]+G_{34}^{0} e^{-\left(S_{2}\right)^{(6)} t} \leq G_{34}(t) \leq\right.$
(a34) $6 G 320(m 2) 6(S 1) 6-\left(a 344^{\prime}\right) 6 e(S 1) 6 t-e-\left(a 34^{\prime}\right) 6 t+G 340 e-\left(a 34^{\prime}\right) 6 t$
$T_{32}^{0} e^{\left(R_{1}\right)^{(6)} t} \leq T_{32}(t) \leq T_{32}^{0} e^{\left.\left(R_{1}\right)^{(6)}+\left(r_{32}\right)^{(6)}\right) t}$
$\frac{1}{\left(\mu_{1}\right)^{(6)}} T_{32}^{0} e^{\left(R_{1}\right)^{(6)} t} \leq T_{32}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(6)}} T_{32}^{0} e^{\left(\left(R_{1}\right)^{(6)}+\left(r_{32}\right)^{(6)}\right) t}$
$\frac{\left(b_{34}\right)^{(6)} T_{32}^{0}}{\left(\mu_{1}\right)^{(6)}\left(\left(R_{1}\right)^{(6)}-\left(b_{34}^{\prime}\right)^{(6)}\right)}\left[e^{\left(R_{1}\right)^{(6)} t}-e^{-\left(b_{34}^{\prime}\right)^{(6)} t}\right]+T_{34}^{0} e^{-\left(b_{34}^{\prime}\right)^{(6)} t} \leq T_{34}(t) \leq$
$\frac{\left(a_{34}\right)^{(6)} T_{32}^{0}}{\left(\mu_{2}\right)^{(6)}\left(\left(R_{1}\right)^{(6)}+\left(r_{32}\right)^{(6)}+\left(R_{2}\right)^{(6)}\right)}\left[e^{\left(\left(R_{1}\right)^{(6)}+\left(r_{32}\right)^{(6)}\right) t}-e^{-\left(R_{2}\right)^{(6)} t}\right]+T_{34}^{0} e^{-\left(R_{2}\right)^{(6)} t}$
Definition of $\left(S_{1}\right)^{(6)},\left(S_{2}\right)^{(6)},\left(R_{1}\right)^{(6)},\left(R_{2}\right)^{(6)}$ :-
Where $\left(S_{1}\right)^{(6)}=\left(a_{32}\right)^{(6)}\left(m_{2}\right)^{(6)}-\left(a_{32}^{\prime}\right)^{(6)}$

$$
\begin{aligned}
& \left(S_{2}\right)^{(6)}=\left(a_{34}\right)^{(6)}-\left(p_{34}\right)^{(6)} \\
& \left(R_{1}\right)^{(6)}=\left(b_{32}\right)^{(6)}\left(\mu_{2}\right)^{(6)}-\left(b_{32}^{\prime}\right)^{(6)} \\
& \left(R_{2}\right)^{(6)}=\left(b_{34}^{\prime}\right)^{(6)}-\left(r_{34}\right)^{(6)}
\end{aligned}
$$

## Behavior of the solutions of equation

Theorem 2: If we denote and define
Definition of $\left(\sigma_{1}\right)^{(7)},\left(\sigma_{2}\right)^{(7)},\left(\tau_{1}\right)^{(7)},\left(\tau_{2}\right)^{(7)}$ :
$\left(\sigma_{1}\right)^{(7)},\left(\sigma_{2}\right)^{(7)},\left(\tau_{1}\right)^{(7)},\left(\tau_{2}\right)^{(7)}$ four constants satisfying
$-\left(\sigma_{2}\right)^{(7)} \leq-\left(a_{36}^{\prime}\right)^{(7)}+\left(a_{37}^{\prime}\right)^{(7)}-\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)+\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right) \leq-\left(\sigma_{1}\right)^{(7)}$
$-\left(\tau_{2}\right)^{(7)} \leq-\left(b_{36}^{\prime}\right)^{(7)}+\left(b_{37}^{\prime}\right)^{(7)}-\left(b_{36}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right), t\right)-\left(b_{37}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right), t\right) \leq-\left(\tau_{1}\right)^{(7)}$
Definition of $\left(v_{1}\right)^{(7)},\left(v_{2}\right)^{(7)},\left(u_{1}\right)^{(7)},\left(u_{2}\right)^{(7)}, v^{(7)}, u^{(7)}$ :
By $\left(v_{1}\right)^{(7)}>0,\left(v_{2}\right)^{(7)}<0$ and respectively $\left(u_{1}\right)^{(7)}>0,\left(u_{2}\right)^{(7)}<0$ the roots of the equations $\left(a_{37}\right)^{(7)}\left(v^{(7)}\right)^{2}+\left(\sigma_{1}\right)^{(7)} v^{(7)}-\left(a_{36}\right)^{(7)}=0$ and $\left(b_{37}\right)^{(7)}\left(u^{(7)}\right)^{2}+\left(\tau_{1}\right)^{(7)} u^{(7)}-\left(b_{36}\right)^{(7)}=0$ and

Definition of $\left(\bar{v}_{1}\right)^{(7)},\left(\bar{v}_{2}\right)^{(7)},\left(\bar{u}_{1}\right)^{(7)},\left(\bar{u}_{2}\right)^{(7)}$ :
$\operatorname{By}\left(\bar{v}_{1}\right)^{(7)}>0,\left(\bar{v}_{2}\right)^{(7)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(7)}>0,\left(\bar{u}_{2}\right)^{(7)}<0$ the
roots of the equations $\left(a_{37}\right)^{(7)}\left(v^{(7)}\right)^{2}+\left(\sigma_{2}\right)^{(7)} v^{(7)}-\left(a_{36}\right)^{(7)}=0$

$$
\text { and }\left(b_{37}\right)^{(7)}\left(u^{(7)}\right)^{2}+\left(\tau_{2}\right)^{(7)} u^{(7)}-\left(b_{36}\right)^{(7)}=0
$$

Definition of $\left(m_{1}\right)^{(7)},\left(m_{2}\right)^{(7)},\left(\mu_{1}\right)^{(7)},\left(\mu_{2}\right)^{(7)},\left(v_{0}\right)^{(7)}:-$
If we define $\left(m_{1}\right)^{(7)},\left(m_{2}\right)^{(7)},\left(\mu_{1}\right)^{(7)},\left(\mu_{2}\right)^{(7)}$ by

$$
\left.\begin{array}{l}
\left(m_{2}\right)^{(7)}=\left(v_{0}\right)^{(7)},\left(m_{1}\right)^{(7)}=\left(v_{1}\right)^{(7)}, \text { if }\left(v_{0}\right)^{(7)}<\left(v_{1}\right)^{(7)} \\
\quad\left(m_{2}\right)^{(7)}=\left(v_{1}\right)^{(7)},\left(m_{1}\right)^{(7)}=\left(\bar{v}_{1}\right)^{(7)}, \text { if }\left(v_{1}\right)^{(7)}<\left(v_{0}\right)^{(7)}<\left(\bar{v}_{1}\right)^{(7)}, \\
\text { and }\left(v_{0}\right)^{(7)}=\frac{G_{36}^{0}}{G_{37}^{0}}
\end{array}\right] \begin{aligned}
& \left(m_{2}\right)^{(7)}=\left(v_{1}\right)^{(7)},\left(m_{1}\right)^{(7)}=\left(v_{0}\right)^{(7), \text { if }\left(\bar{v}_{1}\right)^{(7)}<\left(v_{0}\right)^{(7)}}
\end{aligned}
$$

and analogously

$$
\begin{aligned}
& \quad\left(\mu_{2}\right)^{(7)}=\left(u_{0}\right)^{(7)},\left(\mu_{1}\right)^{(7)}=\left(u_{1}\right)^{(7)}, \text { if }\left(u_{0}\right)^{(7)}<\left(u_{1}\right)^{(7)} \\
& \left(\mu_{2}\right)^{(7)}=\left(u_{1}\right)^{(7)},\left(\mu_{1}\right)^{(7)}=\left(\bar{u}_{1}\right)^{(7)}, \text { if }\left(u_{1}\right)^{(7)}<\left(u_{0}\right)^{(7)}<\left(\bar{u}_{1}\right)^{(7)}, \\
& \text { and }\left(u_{0}\right)^{(7)}=\frac{T_{36}^{0}}{T_{37}^{0}}
\end{aligned}
$$

$$
\left(\mu_{2}\right)^{(7)}=\left(u_{1}\right)^{(7)},\left(\mu_{1}\right)^{(7)}=\left(u_{0}\right)^{(7)} \text {, if }\left(\bar{u}_{1}\right)^{(7)}<\left(u_{0}\right)^{(7)} \text { where }\left(u_{1}\right)^{(7)},\left(\bar{u}_{1}\right)^{(7)}
$$

Then the solution of global equations satisfies the inequalities

$$
G_{36}^{0} e^{\left(\left(S_{1}\right)^{(7)}-\left(p_{36}\right)^{(7)}\right) t} \leq G_{36}(t) \leq G_{36}^{0} e^{\left(S_{1}\right)^{(7)} t}
$$

where $\left(p_{i}\right)^{(7)}$ is defined by equation
$\frac{1}{\left(m_{7}\right)^{(7)}} G_{36}^{0} e^{\left(\left(S_{1}\right)^{(7)}-\left(p_{36}\right)^{(7)}\right) t} \leq G_{37}(t) \leq \frac{1}{\left(m_{2}\right)^{(7)}} G_{36}^{0} e^{\left(S_{1}\right)^{(7)} t}$
$\frac{\left(a_{38}\right)^{(7)} G_{36}^{0}}{\left.\left(m_{1}\right)^{(7)}\left(S_{1}\right)^{(7)}-\left(p_{36}\right)^{(7)}-\left(S_{2}\right)^{(7)}\right)}\left[e^{\left(\left(s_{1}\right)^{(7)}-\left(p_{36}\right)^{(7)}\right) t}-e^{-\left(s_{2}\right)^{(7)} t}\right]+G_{38}^{0} e^{-\left(S_{2}\right)^{(7)} t} \leq G_{38}(t) \leq$
$\left.\frac{\left(a_{38}\right)^{(7)} G_{36}^{0}}{\left(m_{2}\right)^{(7)}\left((S S 1)^{(7)}-\left(a_{38}^{\prime}\right)^{(7)}\right)}\left[e^{\left(S_{1}\right)^{(7)} t}-e^{-\left(a_{38}^{\prime}\right)^{(7)} t}\right]+G_{38}^{0} e^{-\left(a_{38}^{\prime}\right)^{(7)} t}\right)$
$T_{36}^{0} e^{\left(R_{1}\right)^{(7)} t} \leq T_{36}(t) \leq T_{36}^{0} e^{\left(\left(R_{1}\right)^{(7)}+\left(r_{36}\right)^{(7)}\right) t}$
$\frac{1}{\left(\mu_{1}\right)^{(7)}} T_{36}^{0} e^{\left(R_{1}\right)^{(7)} t} \leq T_{36}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(7)}} T_{36}^{0} e^{\left(\left(R_{1}\right)^{(7)}+\left(r_{36}\right)^{(7)}\right) t}$
$\frac{\left(b_{38}\right)^{(7)} T_{36}^{0}}{\left(\mu_{1}\right)^{(7)}\left({\left(R_{1}\right)}^{(7)}-\left(b_{38}^{\prime}\right)^{(7)}\right)}\left[e^{\left(R_{1}\right)^{(7)} t}-e^{-\left(b_{38}^{\prime}\right)^{(7)} t}\right]+T_{38}^{0} e^{-\left(b_{38}^{\prime}\right)^{(7)} t} \leq T_{38}(t) \leq$
$\frac{\left(a_{38}\right)^{(7)} T_{36}^{0}}{\left(\mu_{2}\right)^{(7)}\left(\left(R_{1}\right)^{(7)}+\left(r_{36}\right)^{(7)}+\left(R_{2}\right)^{(7)}\right)}\left[e^{\left(\left(R_{1}\right)^{(7)}+\left(r_{36}\right)^{(7)}\right) t}-e^{-\left(R_{2}\right)^{(7)} t}\right]+T_{38}^{0} e^{-\left(R_{2}\right)^{(7)} t}$
Definition of $\left(S_{1}\right)^{(7)},\left(S_{2}\right)^{(7)},\left(R_{1}\right)^{(7)},\left(R_{2}\right)^{(7)}$ :-
Where $\left(S_{1}\right)^{(7)}=\left(a_{36}\right)^{(7)}\left(m_{2}\right)^{(7)}-\left(a_{36}^{\prime}\right)^{(7)}$

$$
\left(S_{2}\right)^{(7)}=\left(a_{38}\right)^{(7)}-\left(p_{38}\right)^{(7)}
$$

$$
\begin{aligned}
& \left(R_{1}\right)^{(7)}=\left(b_{36}\right)^{(7)}\left(\mu_{2}\right)^{(7)}-\left(b_{36}^{\prime}\right)^{(7)} \\
& \left(R_{2}\right)^{(7)}=\left(b_{38}^{\prime}\right)^{(7)}-\left(r_{38}\right)^{(7)}
\end{aligned}
$$

## Behavior of the solutions of equation

Theorem 2: If we denote and define
Definition of $\left(\sigma_{1}\right)^{(8)},\left(\sigma_{2}\right)^{(8)},\left(\tau_{1}\right)^{(8)},\left(\tau_{2}\right)^{(8)}$ :
(m) $\quad\left(\sigma_{1}\right)^{(8)},\left(\sigma_{2}\right)^{(8)},\left(\tau_{1}\right)^{(8)},\left(\tau_{2}\right)^{(8)}$ four constants satisfying
$-\left(\sigma_{2}\right)^{(8)} \leq-\left(a_{40}^{\prime}\right)^{(8)}+\left(a_{41}^{\prime}\right)^{(8)}-\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)+\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right) \leq-\left(\sigma_{1}\right)^{(8)}$
$-\left(\tau_{2}\right)^{(8)} \leq-\left(b_{40}^{\prime}\right)^{(8)}+\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{40}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right)-\left(b_{41}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right), t\right) \leq-\left(\tau_{1}\right)^{(8)}$
Definition of $\left(v_{1}\right)^{(8)},\left(v_{2}\right)^{(8)},\left(u_{1}\right)^{(8)},\left(u_{2}\right)^{(8)}, v^{(8)}, u^{(8)}$ :
(n) By $\left(v_{1}\right)^{(8)}>0,\left(v_{2}\right)^{(8)}<0$ and respectively $\left(u_{1}\right)^{(8)}>0,\left(u_{2}\right)^{(8)}<0$ the roots of the equations $\left(a_{41}\right)^{(8)}\left(v^{(8)}\right)^{2}+\left(\sigma_{1}\right)^{(8)} v^{(8)}-\left(a_{40}\right)^{(8)}=0$
and $\left(b_{41}\right)^{(8)}\left(u^{(8)}\right)^{2}+\left(\tau_{1}\right)^{(8)} u^{(8)}-\left(b_{40}\right)^{(8)}=0$ and
Definition of $\left(\bar{v}_{1}\right)^{(8)},\left(\bar{v}_{2}\right)^{(8)},\left(\bar{u}_{1}\right)^{(8)},\left(\bar{u}_{2}\right)^{(8)}$ :
By $\left(\bar{v}_{1}\right)^{(8)}>0,\left(\bar{v}_{2}\right)^{(8)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(8)}>0,\left(\bar{u}_{2}\right)^{(8)}<0$ the roots of the equations $\left(a_{41}\right)^{(8)}\left(v^{(8)}\right)^{2}+\left(\sigma_{2}\right)^{(8)} v^{(8)}-\left(a_{40}\right)^{(8)}=0$
and $\left(b_{41}\right)^{(8)}\left(u^{(8)}\right)^{2}+\left(\tau_{2}\right)^{(8)} u^{(8)}-\left(b_{40}\right)^{(8)}=0$
Definition of $\left(m_{1}\right)^{(8)},\left(m_{2}\right)^{(8)},\left(\mu_{1}\right)^{(8)},\left(\mu_{2}\right)^{(8)},\left(\nu_{0}\right)^{(8)}:-$
(o) If we define $\left(m_{1}\right)^{(8)},\left(m_{2}\right)^{(8)},\left(\mu_{1}\right)^{(8)},\left(\mu_{2}\right)^{(8)} \quad$ by

$$
\left(m_{2}\right)^{(8)}=\left(v_{0}\right)^{(8)},\left(m_{1}\right)^{(8)}=\left(v_{1}\right)^{(8)}, \text { if }\left(v_{0}\right)^{(8)}<\left(v_{1}\right)^{(8)}
$$

$\left(m_{2}\right)^{(8)}=\left(v_{1}\right)^{(8)},\left(m_{1}\right)^{(8)}=\left(\bar{v}_{1}\right)^{(8)}$, if $\left(v_{1}\right)^{(8)}<\left(v_{0}\right)^{(8)}<\left(\bar{v}_{1}\right)^{(8)}$,
and $\left(v_{0}\right)^{(8)}=\frac{G_{40}^{0}}{G_{41}^{0}}$

$$
\left(m_{2}\right)^{(8)}=\left(v_{1}\right)^{(8)},\left(m_{1}\right)^{(8)}=\left(v_{0}\right)^{(8)}, \text { if }\left(\bar{v}_{1}\right)^{(8)}<\left(v_{0}\right)^{(8)}
$$

and analogously
$\left(\mu_{2}\right)^{(8)}=\left(u_{0}\right)^{(8)},\left(\mu_{1}\right)^{(8)}=\left(u_{1}\right)^{(8)}$, if $\left(u_{0}\right)^{(8)}<\left(u_{1}\right)^{(8)}$
$\left(\mu_{2}\right)^{(8)}=\left(u_{1}\right)^{(8)},\left(\mu_{1}\right)^{(8)}=\left(\bar{u}_{1}\right)^{(8)}$, if $\left(u_{1}\right)^{(8)}<\left(u_{0}\right)^{(8)}<\left(\bar{u}_{1}\right)^{(8)}$,
and $\left(u_{0}\right)^{(8)}=\frac{T_{40}^{0}}{T_{41}^{0}}$
$\left(\mu_{2}\right)^{(8)}=\left(u_{1}\right)^{(8)},\left(\mu_{1}\right)^{(8)}=\left(u_{0}\right)^{(8)}$, if $\left(\bar{u}_{1}\right)^{(8)}<\left(u_{0}\right)^{(8)}$ where $\left(u_{1}\right)^{(8)},\left(\bar{u}_{1}\right)^{(8)}$

Then the solution of global equations satisfies the inequalities

$$
G_{40}^{0} e^{\left(\left(S_{1}\right)^{(8)}-\left(p_{40}\right)^{(8)}\right) t} \leq G_{40}(t) \leq G_{40}^{0} e^{\left(S_{1}\right)^{(8)} t}
$$

where $\left(p_{i}\right)^{(8)}$ is defined by equation
$\frac{1}{\left(m_{1}\right)^{(8)}} G_{40}^{0} e^{\left(\left(S_{1}\right)^{(8)}-\left(p_{40}\right)^{(8)}\right) t} \leq G_{41}(t) \leq \frac{1}{\left(m_{2}\right)^{(8)}} G_{40}^{0} e^{\left(S_{1}\right)^{(8)} t}$
$\left(\frac{\left(a_{42}\right)^{(8)} G_{40}^{0}}{\left(m_{1}\right)^{(8)}\left(\left(S_{1}\right)^{(8)}-\left(p_{40}\right)^{(8)}-\left(S_{2}\right)^{(8)}\right)}\left[e^{\left(\left(S_{1}\right)^{(8)}-\left(p_{40}\right)^{(8)}\right) t}-e^{-\left(S_{2}\right)^{(8)} t}\right]+G_{42}^{0} e^{-\left(S_{2}\right)^{(8)} t} \leq G_{42}(t) \leq\right.$
$\left.\frac{\left(a_{42}\right)^{(8)} G_{40}^{0}}{\left(m_{2}\right)^{(8)}\left(\left(S_{1}\right)^{(8)}-\left(a_{42}^{\prime}\right)^{(8)}\right)}\left[e^{\left(S_{1}\right)^{(8)} t}-e^{-\left(a_{42}^{\prime}\right)^{(8)} t}\right]+G_{42}^{0} e^{-\left(a_{42}^{\prime}\right)^{(8)} t}\right)$
$T_{40}^{0} e^{\left(R_{1}\right)^{(8)} t} \leq T_{40}(t) \leq T_{40}^{0} e^{\left(\left(R_{1}\right)^{(8)}+\left(r_{40}\right)^{(8)}\right) t}$
$\frac{1}{\left(\mu_{1}\right)^{(8)}} T_{40}^{0} e^{\left(R_{1}\right)^{(8)} t} \leq T_{40}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(8)}} T_{40}^{0} e^{\left(\left(R_{1}\right)^{(8)}+\left(r_{40}\right)^{(8)}\right) t}$
$\frac{\left(b_{42}\right)^{(8)} T_{40}^{0}}{\left(\mu_{1}\right)^{(8)}\left(\left(R_{1}\right)^{(8)}-\left(b_{42}^{\prime}\right)^{(8)}\right)}\left[e^{\left(R_{1}\right)^{(8)} t}-e^{-\left(b_{42}^{\prime}\right)^{(8)} t}\right]+T_{42}^{0} e^{-\left(b_{42}^{\prime}\right)^{(8)} t} \leq T_{42}(t) \leq$
$\frac{\left(a_{42}\right)^{(8)} T_{40}^{0}}{\left(\mu_{2}\right)^{(8)}\left(\left(R_{1}\right)^{(8)}+\left(r_{40}\right)^{(8)}+\left(R_{2}\right)^{(8)}\right)}\left[e^{\left(\left(R_{1}\right)^{(8)}+\left(r_{40}\right)^{(8)}\right) t}-e^{-\left(R_{2}\right)^{(8)} t}\right]+T_{42}^{0} e^{-\left(R_{2}\right)^{(8)} t}$
Definition of $\left(S_{1}\right)^{(8)},\left(S_{2}\right)^{(8)},\left(R_{1}\right)^{(8)},\left(R_{2}\right)^{(8)}$ :-
Where $\left(S_{1}\right)^{(8)}=\left(a_{40}\right)^{(8)}\left(m_{2}\right)^{(8)}-\left(a_{40}^{\prime}\right)^{(8)}$

$$
\begin{aligned}
& \left(S_{2}\right)^{(8)}=\left(a_{42}\right)^{(8)}-\left(p_{42}\right)^{(8)} \\
& \left(R_{1}\right)^{(8)}=\left(b_{40}\right)^{(8)}\left(\mu_{2}\right)^{(8)}-\left(b_{40}^{\prime}\right)^{(8)} \\
& \left(R_{2}\right)^{(8)}=\left(b_{42}^{\prime}\right)^{(8)}-\left(r_{42}\right)^{(8)}
\end{aligned}
$$

Behavior of the solutions of equation 37 to 92
Theorem 2: If we denote and define
Definition of $\left(\sigma_{1}\right)^{(9)},\left(\sigma_{2}\right)^{(9)},\left(\tau_{1}\right)^{(9)},\left(\tau_{2}\right)^{(9)}$ :
(p) $\left.\sigma_{1}\right)^{(9)},\left(\sigma_{2}\right)^{(9)},\left(\tau_{1}\right)^{(9)},\left(\tau_{2}\right)^{(9)}$ four constants satisfying

$$
\begin{aligned}
& -\left(\sigma_{2}\right)^{(9)} \leq-\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{45}^{\prime}\right)^{(9)}-\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)+\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right) \leq-\left(\sigma_{1}\right)^{(9)} \\
& -\left(\tau_{2}\right)^{(9)} \leq-\left(b_{44}^{\prime}\right)^{(9)}+\left(b_{45}^{\prime}\right)^{(9)}-\left(b_{44}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right), t\right)-\left(b_{45}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right), t\right) \leq-\left(\tau_{1}\right)^{(9)}
\end{aligned}
$$

Definition of $\left(v_{1}\right)^{(9)},\left(v_{2}\right)^{(9)},\left(u_{1}\right)^{(9)},\left(u_{2}\right)^{(9)}, v^{(9)}, u^{(9)}$ :
(q) By $\left(v_{1}\right)^{(9)}>0,\left(v_{2}\right)^{(9)}<0$ and respectively $\left(u_{1}\right)^{(9)}>0,\left(u_{2}\right)^{(9)}<0$ the roots of the equations $\left(a_{45}\right)^{(9)}\left(v^{(9)}\right)^{2}+\left(\sigma_{1}\right)^{(9)} v^{(9)}-\left(a_{44}\right)^{(9)}=0$
and $\left(b_{45}\right)^{(9)}\left(u^{(9)}\right)^{2}+\left(\tau_{1}\right)^{(9)} u^{(9)}-\left(b_{44}\right)^{(9)}=0$ and
Definition of $\left(\bar{v}_{1}\right)^{(9)}$, $,\left(\bar{v}_{2}\right)^{(9)},\left(\bar{u}_{1}\right)^{(9)},\left(\bar{u}_{2}\right)^{(9)}$ :
By $\left(\bar{v}_{1}\right)^{(9)}>0,\left(\bar{v}_{2}\right)^{(9)}<0$ and respectively $\left(\bar{u}_{1}\right)^{(9)}>0,\left(\bar{u}_{2}\right)^{(9)}<0$ the
roots of the equations $\left(a_{45}\right)^{(9)}\left(v^{(9)}\right)^{2}+\left(\sigma_{2}\right)^{(9)} v^{(9)}-\left(a_{44}\right)^{(9)}=0$
and $\left(b_{45}\right)^{(9)}\left(u^{(9)}\right)^{2}+\left(\tau_{2}\right)^{(9)} u^{(9)}-\left(b_{44}\right)^{(9)}=0$
Definition of $\left(m_{1}\right)^{(9)},\left(m_{2}\right)^{(9)},\left(\mu_{1}\right)^{(9)},\left(\mu_{2}\right)^{(9)},\left(v_{0}\right)^{(9)}:-$
(r) If we define $\left(m_{1}\right)^{(9)},\left(m_{2}\right)^{(9)},\left(\mu_{1}\right)^{(9)},\left(\mu_{2}\right)^{(9)}$ by

$$
\left(m_{2}\right)^{(9)}=\left(v_{0}\right)^{(9)},\left(m_{1}\right)^{(9)}=\left(v_{1}\right)^{(9)}, \text { if }\left(v_{0}\right)^{(9)}<\left(v_{1}\right)^{(9)}
$$

$$
\left(m_{2}\right)^{(9)}=\left(v_{1}\right)^{(9)},\left(m_{1}\right)^{(9)}=\left(\bar{v}_{1}\right)^{(9)}, \text { if }\left(v_{1}\right)^{(9)}<\left(v_{0}\right)^{(9)}<\left(\bar{v}_{1}\right)^{(9)},
$$

$$
\text { and }\left(v_{0}\right)^{(9)}=\frac{G_{44}^{0}}{G_{45}^{0}}
$$

$$
\left(m_{2}\right)^{(9)}=\left(v_{1}\right)^{(9)},\left(m_{1}\right)^{(9)}=\left(v_{0}\right)^{(9)}, \text { if }\left(\bar{v}_{1}\right)^{(9)}<\left(v_{0}\right)^{(9)}
$$

and analogously

$$
\begin{aligned}
& \quad\left(\mu_{2}\right)^{(9)}=\left(u_{0}\right)^{(9)},\left(\mu_{1}\right)^{(9)}=\left(u_{1}\right)^{(9)}, \text { if }\left(u_{0}\right)^{(9)}<\left(u_{1}\right)^{(9)} \\
& \left(\mu_{2}\right)^{(9)}=\left(u_{1}\right)^{(9)},\left(\mu_{1}\right)^{(9)}=\left(\bar{u}_{1}\right)^{(9)}, \text { if }\left(u_{1}\right)^{(9)}<\left(u_{0}\right)^{(9)}<\left(\bar{u}_{1}\right)^{(9)}, \\
& \text { and }\left(u_{0}\right)^{(9)}=\frac{T_{44}^{0}}{T_{45}}
\end{aligned}
$$

$\left(\mu_{2}\right)^{(9)}=\left(u_{1}\right)^{(9)},\left(\mu_{1}\right)^{(9)}=\left(u_{0}\right)^{(9)}$, if $\left(\bar{u}_{1}\right)^{(9)}<\left(u_{0}\right)^{(9)}$ where $\left(u_{1}\right)^{(9)},\left(\bar{u}_{1}\right)^{(9)}$
are defined by 59 and 69 respectively
Then the solution of $99,20,44,22,23$ and 44 satisfies the inequalities

$$
G_{44}^{0} e^{\left(\left(S_{1}\right)^{(9)}-\left(p_{44}\right)^{(9)}\right) t} \leq G_{44}(t) \leq G_{44}^{0} e^{\left(S_{1}\right)^{(9)} t}
$$

where $\left(p_{i}\right)^{(9)}$ is defined by equation 45

$$
\frac{1}{\left(m_{9}\right)^{(9)}} G_{44}^{0} e^{\left(\left(S_{1}\right)^{(9)}-\left(p_{44}\right)^{(9)}\right) t} \leq G_{45}(t) \leq \frac{1}{\left(m_{2}\right)^{(9)}} G_{44}^{0} e^{\left(S_{1}\right)^{(9)} t}
$$

$$
\left(\frac{\left(a_{46}\right)^{(9)} G_{44}^{0}}{\left(m_{1}\right)^{(9)}\left(\left(S_{1}\right)^{(9)}-\left(p_{44}\right)^{(9)}-\left(S_{2}\right)^{(9)}\right)}\left[e^{\left(\left(S_{1}\right)^{(9)}-\left(p_{44}\right)^{(9)}\right) t}-e^{-\left(S_{2}\right)^{(9)} t}\right]+G_{46}^{0} e^{-\left(S_{2}\right)^{(9)} t} \leq G_{46}(t) \leq\right.
$$

$$
\left.\frac{\left(a_{46}\right)^{(9)} G_{44}^{0}}{\left(m_{2}\right)^{(9)}\left(\left(s_{1}\right)^{(9)}-\left(a_{46}^{\prime}\right)^{(9)}\right)}\left[e^{\left(s_{1}\right)^{(9)} t}-e^{-\left(a_{46}^{\prime}\right)^{(9)} t}\right]+G_{46}^{0} e^{-\left(a_{46}^{\prime}\right)^{(9)} t}\right)
$$

$$
T_{44}^{0} e^{\left(R_{1}\right)^{(9)} t} \leq T_{44}(t) \leq T_{44}^{0} e^{\left(\left(R_{1}\right)^{(9)}+\left(r_{44}\right)^{(9)}\right) t}
$$

$$
\frac{1}{\left(\mu_{1}\right)^{(9)}} T_{44}^{0} e^{\left(R_{1}\right)^{(9)} t} \leq T_{44}(t) \leq \frac{1}{\left(\mu_{2}\right)^{(9)}} T_{44}^{0} e^{\left(\left(R_{1}\right)^{(9)}+\left(r_{44}\right)^{(9)}\right) t}
$$

$$
\frac{\left(b_{46}\right)^{(9)} T_{44}^{0}}{\left(\mu_{1}\right)^{(9)}\left(\left(R_{1}\right)^{(9)}-\left(b_{46}^{\prime}\right)^{(9)}\right)}\left[e^{\left(R_{1}\right)^{(9)} t}-e^{-\left(b_{46}^{\prime}\right)^{(9)} t}\right]+T_{46}^{0} e^{-\left(b_{46}^{\prime}\right)^{(9)} t} \leq T_{46}(t) \leq
$$

$$
\frac{\left(a_{46}\right)^{(9)} T_{44}^{0}}{\left(\mu_{2}\right)^{(9)}\left(\left(R_{1}\right)^{(9)}+\left(r_{44}\right)^{(9)}+\left(R_{2}\right)^{(9)}\right)}\left[e^{\left(\left(R_{1}\right)^{(9)}+\left(r_{44}\right)^{(9)}\right) t}-e^{-\left(R_{2}\right)^{(9)} t}\right]+T_{46}^{0} e^{-\left(R_{2}\right)^{(9)} t}
$$

Definition of $\left(S_{1}\right)^{(9)},\left(S_{2}\right)^{(9)},\left(R_{1}\right)^{(9)},\left(R_{2}\right)^{(9)}$ :-
Where $\left(S_{1}\right)^{(9)}=\left(a_{44}\right)^{(9)}\left(m_{2}\right)^{(9)}-\left(a_{44}^{\prime}\right)^{(9)}$

$$
\left(S_{2}\right)^{(9)}=\left(a_{46}\right)^{(9)}-\left(p_{46}\right)^{(9)}
$$

$$
\begin{aligned}
& \left(R_{1}\right)^{(9)}=\left(b_{44}\right)^{(9)}\left(\mu_{2}\right)^{(9)}-\left(b_{44}^{\prime}\right)^{(9)} \\
& \left(R_{2}\right)^{(9)}=\left(b_{46}^{\prime}\right)^{(9)}-\left(r_{46}\right)^{(9)}
\end{aligned}
$$

Proof: From global equations we obtain
$\frac{d v^{(1)}}{d t}=\left(a_{13}\right)^{(1)}-\left(\left(a_{13}^{\prime}\right)^{(1)}-\left(a_{14}^{\prime}\right)^{(1)}+\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right)\right)-\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}, t\right) v^{(1)}-\left(a_{14}\right)^{(1)} v^{(1)}$
Definition of $v^{(1)}: \quad v^{(1)}=\frac{G_{13}}{G_{14}}$
It follows

$$
-\left(\left(a_{14}\right)^{(1)}\left(v^{(1)}\right)^{2}+\left(\sigma_{2}\right)^{(1)} v^{(1)}-\left(a_{13}\right)^{(1)}\right) \leq \frac{d v^{(1)}}{d t} \leq-\left(\left(a_{14}\right)^{(1)}\left(v^{(1)}\right)^{2}+\left(\sigma_{1}\right)^{(1)} v^{(1)}-\left(a_{13}\right)^{(1)}\right)
$$

## From which one obtains

Definition of $\left(\bar{v}_{1}\right)^{(1)},\left(v_{0}\right)^{(1)}$ :-
(a) For $0<\left(v_{0}\right)^{(1)}=\frac{G_{13}^{0}}{G_{14}^{0}}<\left(v_{1}\right)^{(1)}<\left(\bar{v}_{1}\right)^{(1)}$

$$
\begin{gathered}
v^{(1)}(t) \geq \frac{\left(v_{1}\right)^{(1)}+(C)^{(1)}\left(v_{2}\right)^{(1)} e^{\left[-\left(a_{14}\right)^{(1)}\left(\left(v_{1}\right)^{(1)}-\left(v_{0}\right)^{(1)}\right) t\right]}}{1+(C)^{(1)} e^{\left[-\left(a_{14}\right)^{(1)}\left(\left(v_{1}\right)^{(1)}-\left(v_{0}\right)^{(1)}\right) t\right]}}, \quad(C)^{(1)}=\frac{\left(v_{1}\right)^{(1)}-\left(v_{0}\right)^{(1)}}{\left(v_{0}\right)^{(1)}-\left(v_{2}\right)^{(1)}} \\
\text { it follows }\left(v_{0}\right)^{(1)} \leq v^{(1)}(t) \leq\left(v_{1}\right)^{(1)}
\end{gathered}
$$

In the same manner, we get

From which we deduce $\left(v_{0}\right)^{(1)} \leq v^{(1)}(t) \leq\left(\bar{v}_{1}\right)^{(1)}$
(b) If $0<\left(v_{1}\right)^{(1)}<\left(v_{0}\right)^{(1)}=\frac{G_{13}^{0}}{G_{14}^{0}}<\left(\bar{v}_{1}\right)^{(1)}$ we find like in the previous case,

$$
\begin{aligned}
& \left(v_{1}\right)^{(1)} \leq \frac{\left(v_{1}\right)^{(1)}+(C)^{(1)}\left(v_{2}\right)^{(1)} e^{\left.\left.\left[-\left(a_{14}\right)^{(1)}\right)\left(v_{1}\right)^{(1)}-\left(v_{2}\right)^{(1)}\right) t\right]}}{1+(C)^{(1)} e^{\left[\left(a_{14}\right)^{(1)}\left(\left(v_{1}\right)^{(1)}-\left(v_{2}\right)^{(1)}\right) t\right]} \leq v^{(1)}(t) \leq} \\
& \frac{\left(\bar{v}_{1}\right)^{(1)}+(\bar{C})^{(1)}\left(\bar{v}_{2}\right)^{(1)} e^{\left.\left[-\left(a_{14}\right)^{(1)}\left(\bar{v}_{1}\right)^{(1)}-\left(\bar{v}_{2}\right)^{(1)}\right) t\right]}}{1+(\bar{C})^{(1)} e^{\left[-\left(a_{14}\right)^{(1)}\left(\left(\bar{v}_{1}\right)^{(1)}-\left(\bar{v}_{2}\right)^{(1)}\right) t\right]} \leq\left(\bar{v}_{1}\right)^{(1)}}
\end{aligned}
$$

(c) If $0<\left(v_{1}\right)^{(1)} \leq\left(\bar{v}_{1}\right)^{(1)} \leq\left(v_{0}\right)^{(1)}=\frac{G_{13}^{0}}{G_{14}^{0}}$, we obtain

$$
\left(v_{1}\right)^{(1)} \leq v^{(1)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(1)}+(\bar{C})^{(1)}\left(\bar{v}_{2}\right)^{(1)} e^{\left.\left[-\left(a_{14}\right)^{(1)}\left(\bar{v}_{1}\right)^{(1)}-\left(\bar{v}_{2}\right)^{(1)}\right) t\right]}}{1+(\bar{C})^{(1)} e^{\left.-\left(a_{14}\right)^{(1)}\left(\left(\bar{v}_{1}\right)^{(1)}-\left(\bar{v}_{2}\right)^{(1)}\right) t\right]}} \leq\left(v_{0}\right)^{(1)}
$$

And so with the notation of the first part of condition (c), we have
Definition of $\boldsymbol{v}^{(1)}(t)$ :-
$\left(m_{2}\right)^{(1)} \leq v^{(1)}(t) \leq\left(m_{1}\right)^{(1)}, \quad v^{(1)}(t)=\frac{G_{13}(t)}{G_{14}(t)}$
In a completely analogous way, we obtain
Definition of $u^{(1)}(t)$ :-
$\left(\mu_{2}\right)^{(1)} \leq u^{(1)}(t) \leq\left(\mu_{1}\right)^{(1)}, \quad u^{(1)}(t)=\frac{T_{13}(t)}{T_{14}(t)}$
Now, using this result and replacing it in global equations we get easily the result stated in the theorem.
Particular case:
If $\left(a_{13}^{\prime \prime}\right)^{(1)}=\left(a_{14}^{\prime \prime}\right)^{(1)}$, then $\left(\sigma_{1}\right)^{(1)}=\left(\sigma_{2}\right)^{(1)}$ and in this case $\left(v_{1}\right)^{(1)}=\left(\bar{v}_{1}\right)^{(1)}$ if in addition $\left(v_{0}\right)^{(1)}=$ $\left(v_{1}\right)^{(1)}$ then $v^{(1)}(t)=\left(v_{0}\right)^{(1)}$ and as a consequence $G_{13}(t)=\left(v_{0}\right)^{(1)} G_{14}(t)$ this also defines $\left(v_{0}\right)^{(1)}$ for the special case
Analogously if $\left(b_{13}^{\prime \prime}\right)^{(1)}=\left(b_{14}^{\prime \prime}\right)^{(1)}$, then $\left(\tau_{1}\right)^{(1)}=\left(\tau_{2}\right)^{(1)}$ and then
$\left(u_{1}\right)^{(1)}=\left(\bar{u}_{1}\right)^{(1)}$ if in addition $\left(u_{0}\right)^{(1)}=\left(u_{1}\right)^{(1)}$ then $T_{13}(t)=\left(u_{0}\right)^{(1)} T_{14}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(1)}$ and $\left(\bar{v}_{1}\right)^{(1)}$, and definition of $\left(u_{0}\right)^{(1)}$.

Proof: From global equations we obtain
$\frac{\mathrm{d} v^{(2)}}{\mathrm{dt}}=\left(a_{16}\right)^{(2)}-\left(\left(a_{16}^{\prime}\right)^{(2)}-\left(a_{17}^{\prime}\right)^{(2)}+\left(a_{16}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}, \mathrm{t}\right)\right)-\left(a_{17}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}, \mathrm{t}\right) v^{(2)}-\left(a_{17}\right)^{(2)} v^{(2)}$
Definition of $v^{(2)}: \quad v^{(2)}=\frac{\mathrm{G}_{16}}{\mathrm{G}_{17}}$
It follows
$-\left(\left(a_{17}\right)^{(2)}\left(v^{(2)}\right)^{2}+\left(\sigma_{2}\right)^{(2)} v^{(2)}-\left(a_{16}\right)^{(2)}\right) \leq \frac{\mathrm{d} v^{(2)}}{\mathrm{dt}} \leq-\left(\left(a_{17}\right)^{(2)}\left(v^{(2)}\right)^{2}+\left(\sigma_{1}\right)^{(2)} v^{(2)}-\left(a_{16}\right)^{(2)}\right)$
From which one obtains
Definition of $\left(\bar{v}_{1}\right)^{(2)},\left(v_{0}\right)^{(2)}:-$
(d) For $0<\left(v_{0}\right)^{(2)}=\frac{\mathrm{G}_{16}^{0}}{\mathrm{G}_{17}^{0}}<\left(v_{1}\right)^{(2)}<\left(\bar{v}_{1}\right)^{(2)}$

$$
v^{(2)}(t) \geq \frac{\left(v_{1}\right)^{(2)}+(\mathrm{C})^{(2)}\left(v_{2}\right)^{(2)} e^{\left[-\left(a_{17}\right)^{(2)}\left(\left(v_{1}\right)^{(2)}-\left(v_{0}\right)^{(2)}\right) t\right]}}{1+(\mathrm{C})^{(2)} e^{\left[-\left(a_{17}\right)^{(2)}\left(\left(v_{1}\right)^{(2)}-\left(v_{0}\right)^{(2)}\right) t\right]}} \quad, \quad(\mathrm{C})^{(2)}=\frac{\left(v_{1}\right)^{(2)}-\left(v_{0}\right)^{(2)}}{\left(v_{0}\right)^{(2)}-\left(v_{2}\right)^{(2)}}
$$

it follows $\left(v_{0}\right)^{(2)} \leq v^{(2)}(t) \leq\left(v_{1}\right)^{(2)}$
In the same manner, we get
$v^{(2)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(2)}+(\overline{\mathrm{C}})^{(2)}\left(\bar{v}_{2}\right)^{(2)} e^{\left.\left[-\left(a_{17}\right)^{(2)}\left(\bar{v}_{1}\right)^{(2)}-\left(\bar{v}_{2}\right)^{(2)}\right) t\right]}}{1+(\overline{\mathrm{C}})^{(2)} e^{\left[-\left(a_{17}\right)^{(2)}\left(\bar{v}_{1}\right)^{(2)}-\left(\bar{v}_{2}\right)^{(2)}\right) t}} \quad, \quad(\overline{\mathrm{C}})^{(2)}=\frac{\left(\bar{v}_{1}\right)^{(2)}-\left(v_{0}\right)^{(2)}}{\left(v_{0}\right)^{(2)}-\left(\bar{v}_{2}\right)^{(2)}}$
From which we deduce $\left(v_{0}\right)^{(2)} \leq v^{(2)}(t) \leq\left(\bar{v}_{1}\right)^{(2)}$
(e) If $0<\left(v_{1}\right)^{(2)}<\left(v_{0}\right)^{(2)}=\frac{\mathrm{G}_{16}^{0}}{\mathrm{G}_{17}^{0}}<\left(\bar{v}_{1}\right)^{(2)}$ we find like in the previous case,
$\left(v_{1}\right)^{(2)} \leq \frac{\left(v_{1}\right)^{(2)}+(\mathrm{C})^{(2)}\left(v_{2}\right)^{(2)} e^{\left.\left[-\left(a_{17}\right)^{(2)}\left(v_{1}\right)^{(2)}-\left(v_{2}\right)^{(2)}\right) t\right]}}{1+(\mathrm{C})^{(2)} e^{\left[-\left(a_{17}\right)^{(2)}\left(\left(_{1}\right)^{(2)}-\left(v_{2}\right)^{(2)}\right) t\right]}} \leq v^{(2)}(t) \leq$

$$
\frac{\left(\bar{v}_{1}\right)^{(2)}+(\overline{\mathrm{C}})^{(2)}\left(\bar{v}_{2}\right)^{(2)} e^{\left.\left[-\left(a_{17}\right)\right)^{(2)}\left(\left(\bar{v}_{1}\right)^{(2)}-\left(\bar{v}_{2}\right)^{(2)}\right) t\right]}}{1+(\overline{\mathrm{C}})^{(2)} e^{\left.\left.\left[-\left(a_{17}\right)\right)^{(2)}\left(\bar{v}_{1}\right)^{(2)}-\left(\bar{v}_{2}\right)^{(2)}\right) t\right]}} \leq\left(\bar{v}_{1}\right)^{(2)}
$$

(f) If $0<\left(v_{1}\right)^{(2)} \leq\left(\bar{v}_{1}\right)^{(2)} \leq\left(v_{0}\right)^{(2)}=\frac{\mathrm{G}_{16}^{0}}{\mathrm{G}_{17}^{0}}$, we obtain
$\left(v_{1}\right)^{(2)} \leq v^{(2)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(2)}+(\overline{\mathrm{C}})^{(2)}\left(\bar{v}_{2}\right)^{(2)} e^{\left.\left[-\left(a_{17}\right)^{(2)}\left(\bar{v}_{1}\right)^{(2)}-\left(\bar{v}_{2}\right)^{(2)}\right) t\right]}}{1+(\bar{C})^{(2)} e^{\left.\left[-\left(a_{17}\right)^{(2)}\left(\bar{v}_{1}\right)^{(2)}-\left(\bar{v}_{2}\right)^{(2)}\right) t\right]}} \leq\left(v_{0}\right)^{(2)}$
And so with the notation of the first part of condition (c), we have
Definition of $\boldsymbol{v}^{(2)}(t)$ :-
$\left(m_{2}\right)^{(2)} \leq v^{(2)}(t) \leq\left(m_{1}\right)^{(2)}, \quad v^{(2)}(t)=\frac{G_{16}(t)}{G_{17}(t)}$
In a completely analogous way, we obtain
Definition of $u^{(2)}(t)$ :-
$\left(\mu_{2}\right)^{(2)} \leq u^{(2)}(t) \leq\left(\mu_{1}\right)^{(2)}, \quad u^{(2)}(t)=\frac{T_{16}(t)}{T_{17}(t)}$
Now, using this result and replacing it in global equations we get easily the result stated in the theorem.

## Particular case :

If $\left(a_{16}^{\prime \prime}\right)^{(2)}=\left(a_{17}^{\prime \prime}\right)^{(2)}$, then $\left(\sigma_{1}\right)^{(2)}=\left(\sigma_{2}\right)^{(2)}$ and in this case $\left(v_{1}\right)^{(2)}=\left(\bar{v}_{1}\right)^{(2)}$ if in addition $\left(v_{0}\right)^{(2)}=$ $\left(v_{1}\right)^{(2)}$ then $v^{(2)}(t)=\left(v_{0}\right)^{(2)}$ and as a consequence $G_{16}(t)=\left(v_{0}\right)^{(2)} G_{17}(t)$
Analogously if $\left(b_{16}^{\prime \prime}\right)^{(2)}=\left(b_{17}^{\prime \prime}\right)^{(2)}$, then $\left(\tau_{1}\right)^{(2)}=\left(\tau_{2}\right)^{(2)}$ and then
$\left(u_{1}\right)^{(2)}=\left(\bar{u}_{1}\right)^{(2)}$ if in addition $\left(u_{0}\right)^{(2)}=\left(u_{1}\right)^{(2)}$ then $T_{16}(t)=\left(u_{0}\right)^{(2)} T_{17}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(2)}$ and $\left(\bar{v}_{1}\right)^{(2)}$
Proof: From global equations we obtain
$\frac{d v^{(3)}}{d t}=\left(a_{20}\right)^{(3)}-\left(\left(a_{20}^{\prime}\right)^{(3)}-\left(a_{21}^{\prime}\right)^{(3)}+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right)\right)-\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}, t\right) v^{(3)}-\left(a_{21}\right)^{(3)} v^{(3)}$
Definition of $v^{(3)}:-\quad v^{(3)}=\frac{G_{20}}{G_{21}}$
It follows

$$
-\left(\left(a_{21}\right)^{(3)}\left(v^{(3)}\right)^{2}+\left(\sigma_{2}\right)^{(3)} v^{(3)}-\left(a_{20}\right)^{(3)}\right) \leq \frac{d v^{(3)}}{d t} \leq-\left(\left(a_{21}\right)^{(3)}\left(v^{(3)}\right)^{2}+\left(\sigma_{1}\right)^{(3)} v^{(3)}-\left(a_{20}\right)^{(3)}\right)
$$

From which one obtains
(a) For $0<\left(v_{0}\right)^{(3)}=\frac{G_{20}^{0}}{G_{21}^{0}}<\left(v_{1}\right)^{(3)}<\left(\bar{v}_{1}\right)^{(3)}$
it follows $\left(v_{0}\right)^{(3)} \leq v^{(3)}(t) \leq\left(v_{1}\right)^{(3)}$
In the same manner, we get
$v^{(3)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(3)}+\left(\bar{C}{ }^{(3)}\left(\bar{v}_{2}\right)^{(3)} e^{\left.\left[-\left(a_{21}\right)^{(3)}\left(\bar{v}_{1}\right)^{(3)}-\left(\bar{v}_{2}\right)^{(3)}\right) t\right]}\right.}{1+(\bar{C})^{(3)} e^{\left.\left[-\left(a_{21}\right)^{(3)}\left(\bar{v}_{1}\right)^{(3)}-\left(\bar{v}_{2}\right)^{(3)}\right) t\right]} \quad, \quad(\bar{C})^{(3)}=\frac{\left(\bar{v}_{1}\right)^{(3)}-\left(v_{0}\right)^{(3)}}{\left(v_{0}\right)^{(3)}-\left(\bar{v}_{2}\right)^{(3)}}}$
Definition of $\left(\bar{v}_{1}\right)^{(3)}$ :-
From which we deduce $\left(v_{0}\right)^{(3)} \leq v^{(3)}(t) \leq\left(\bar{v}_{1}\right)^{(3)}$
(b) If $0<\left(v_{1}\right)^{(3)}<\left(v_{0}\right)^{(3)}=\frac{G_{20}^{0}}{G_{21}^{0}}<\left(\bar{v}_{1}\right)^{(3)}$ we find like in the previous case,

$$
\begin{aligned}
& \left(v_{1}\right)^{(3)} \leq \frac{\left(v_{1}\right)^{(3)}+(C)^{(3)}\left(v_{2}\right)^{(3)} e^{\left[-\left(a_{21}\right)^{(3)}\left(\left(v_{1}\right)^{(3)}-\left(v_{2}\right)^{(3)}\right) t\right]}}{1+(C)^{(3)} e^{\left[-\left(a_{21}\right)^{(3)}\left(\left(v_{1}\right)^{(3)}-\left(v_{2}\right)^{(3)}\right) t\right]} \leq v^{(3)}(t) \leq} \\
& \frac{\left(\bar{v}_{1}\right)^{(3)}+(\bar{C})^{(3)}\left(\bar{v}_{2}\right)^{(3)} e^{\left.\left.\left[-\left(a_{21}\right)^{(3)}\left(\bar{v}_{1}\right)^{(3)}-\bar{v}_{2}\right)^{(3)}\right) t\right]}}{1+(\bar{C})^{(3)} e^{\left[-\left(a_{21}\right)^{(3)}\left(\left(\bar{v}_{1}\right)^{(3)}-\left(\bar{v}_{2}\right)^{(3)}\right) t\right]} \leq\left(\bar{v}_{1}\right)^{(3)}}
\end{aligned}
$$

(c) If $0<\left(v_{1}\right)^{(3)} \leq\left(\bar{v}_{1}\right)^{(3)} \leq\left(v_{0}\right)^{(3)}=\frac{G_{20}^{0}}{G_{21}^{0}}$, we obtain

And so with the notation of the first part of condition (c), we have
Definition of $v^{(3)}(t)$ :-
$\left(m_{2}\right)^{(3)} \leq v^{(3)}(t) \leq\left(m_{1}\right)^{(3)}, \quad v^{(3)}(t)=\frac{G_{20}(t)}{G_{21}(t)}$
In a completely analogous way, we obtain
Definition of $u^{(3)}(t)$ :-
$\left(\mu_{2}\right)^{(3)} \leq u^{(3)}(t) \leq\left(\mu_{1}\right)^{(3)}, \quad u^{(3)}(t)=\frac{T_{20}(t)}{T_{21}(t)}$
Now, using this result and replacing it in global equations we get easily the result stated in the theorem.
Particular case:
If $\left(a_{20}^{\prime \prime}\right)^{(3)}=\left(a_{21}^{\prime \prime}\right)^{(3)}$, then $\left(\sigma_{1}\right)^{(3)}=\left(\sigma_{2}\right)^{(3)}$ and in this case $\left(v_{1}\right)^{(3)}=\left(\bar{v}_{1}\right)^{(3)}$ if in addition $\left(v_{0}\right)^{(3)}=$ $\left(v_{1}\right)^{(3)}$ then $v^{(3)}(t)=\left(v_{0}\right)^{(3)}$ and as a consequence $G_{20}(t)=\left(v_{0}\right)^{(3)} G_{21}(t)$
Analogously if $\left(b_{20}^{\prime \prime}\right)^{(3)}=\left(b_{21}^{\prime \prime}\right)^{(3)}$, then $\left(\tau_{1}\right)^{(3)}=\left(\tau_{2}\right)^{(3)}$ and then
$\left(u_{1}\right)^{(3)}=\left(\bar{u}_{1}\right)^{(3)}$ if in addition $\left(u_{0}\right)^{(3)}=\left(u_{1}\right)^{(3)}$ then $T_{20}(t)=\left(u_{0}\right)^{(3)} T_{21}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(3)}$ and $\left(\bar{v}_{1}\right)^{(3)}$

Proof: From global equations we obtain

$$
\frac{d v^{(4)}}{d t}=\left(a_{24}\right)^{(4)}-\left(\left(a_{24}^{\prime}\right)^{(4)}-\left(a_{25}^{\prime}\right)^{(4)}+\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right)\right)-\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}, t\right) v^{(4)}-\left(a_{25}\right)^{(4)} v^{(4)}
$$

Definition of $v^{(4)}: \quad v^{(4)}=\frac{G_{24}}{G_{25}}$
It follows

$$
-\left(\left(a_{25}\right)^{(4)}\left(v^{(4)}\right)^{2}+\left(\sigma_{2}\right)^{(4)} v^{(4)}-\left(a_{24}\right)^{(4)}\right) \leq \frac{d v^{(4)}}{d t} \leq-\left(\left(a_{25}\right)^{(4)}\left(v^{(4)}\right)^{2}+\left(\sigma_{4}\right)^{(4)} v^{(4)}-\left(a_{24}\right)^{(4)}\right)
$$

From which one obtains
Definition of $\left(\bar{v}_{1}\right)^{(4)},\left(v_{0}\right)^{(4)}:-$
(d) For $0<\left(v_{0}\right)^{(4)}=\frac{G_{24}^{0}}{G_{25}^{0}}<\left(v_{1}\right)^{(4)}<\left(\bar{v}_{1}\right)^{(4)}$

$$
v^{(4)}(t) \geq \frac{\left(v_{1}\right)^{(4)}+(C)^{(4)}\left(v_{2}\right)^{(4)} e^{\left[-\left(a_{25}\right)^{(4)}\left(\left(v_{1}\right)^{(4)}-\left(v_{0}\right)^{(4)}\right) t\right]}}{4+(C)^{(4)} e^{\left[-\left(a_{25}\right)^{(4)}\left(\left(v_{1}\right)^{(4)}-\left(v_{0}\right)^{(4)}\right) t\right]}} \quad, \quad(C)^{(4)}=\frac{\left(v_{1}\right)^{(4)}-\left(v_{0}\right)^{(4)}}{\left(v_{0}\right)^{(4)}-\left(v_{2}\right)^{(4)}}
$$

it follows $\left(v_{0}\right)^{(4)} \leq v^{(4)}(t) \leq\left(v_{1}\right)^{(4)}$
In the same manner, we get
$v^{(4)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(4)}+(\bar{C})^{(4)}\left(\bar{v}_{2}\right)^{(4)} e^{\left.\left[-\left(a_{25}\right)^{(4)}\left(\bar{v}_{1}\right)^{(4)}-\left(\bar{v}_{2}\right)^{(4)}\right) t\right]}}{4+(\bar{C})^{(4)} e^{\left[\left(a_{25}\right)^{(4)}\left(\left(\bar{v}_{1}\right)^{(4)}-\left(\bar{v}_{2}\right)^{(4)}\right) t\right]} \quad, \quad(\bar{C})^{(4)}=\frac{\left(\bar{v}_{1}\right)^{(4)}-\left(v_{0}\right)^{(4)}}{\left(v_{0}\right)^{(4)}-\left(\bar{v}_{2}\right)^{(4)}}}$
From which we deduce $\left(v_{0}\right)^{(4)} \leq v^{(4)}(t) \leq\left(\bar{v}_{1}\right)^{(4)}$
(e) If $0<\left(v_{1}\right)^{(4)}<\left(v_{0}\right)^{(4)}=\frac{G_{24}^{0}}{G_{25}^{0}}<\left(\bar{v}_{1}\right)^{(4)}$ we find like in the previous case,

$$
\begin{aligned}
& \left(v_{1}\right)^{(4)} \leq \frac{\left(v_{1}\right)^{(4)}+(C)^{(4)}\left(v_{2}\right)^{(4)} e^{\left[-\left(a_{25}\right)^{(4)}\left(\left(v_{1}\right)^{(4)}-\left(v_{2}\right)^{(4)}\right) t\right]}}{1+(C)^{(4)} e^{\left.\left.-\left(a_{25}\right)^{(4)}\left(v_{1}\right)^{(4)}-\left(v_{2}\right)^{(4)}\right) t\right]} \leq v^{(4)}(t) \leq} \\
& \frac{\left(\bar{v}_{1}\right)^{(4)}+(\bar{C})^{(4)}\left(\bar{v}_{2}\right)^{(4)} e^{\left[-\left(a_{25}\right)^{(4)}\left(\left(\bar{v}_{1}\right){ }^{(4)}-\left(\bar{v}_{2}\right)^{(4)}\right) t\right]}}{1+(\bar{C})^{(4)} e^{\left[-\left(a_{25}\right)^{(4)}\left(\left(\bar{v}_{1}\right)^{(4)}-\left(\bar{v}_{2}\right)^{(4)}\right) t\right]} \leq\left(\bar{v}_{1}\right)^{(4)}}
\end{aligned}
$$

(f) If $0<\left(v_{1}\right)^{(4)} \leq\left(\bar{v}_{1}\right)^{(4)} \leq\left(v_{0}\right)^{(4)}=\frac{G_{24}^{0}}{G_{25}^{0}}$, we obtain

And so with the notation of the first part of condition (c), we have

## Definition of $v^{(4)}(t)$ :-

$\left(m_{2}\right)^{(4)} \leq v^{(4)}(t) \leq\left(m_{1}\right)^{(4)}, \quad v^{(4)}(t)=\frac{G_{24}(t)}{G_{25}(t)}$
In a completely analogous way, we obtain
Definition of $u^{(4)}(t)$ :-
$\left(\mu_{2}\right)^{(4)} \leq u^{(4)}(t) \leq\left(\mu_{1}\right)^{(4)}, \quad u^{(4)}(t)=\frac{T_{24}(t)}{T_{25}(t)}$
Now, using this result and replacing it in global equations we get easily the result stated in the theorem.

## Particular case :

If $\left(a_{24}^{\prime \prime}\right)^{(4)}=\left(a_{25}^{\prime \prime}\right)^{(4)}$, then $\left(\sigma_{1}\right)^{(4)}=\left(\sigma_{2}\right)^{(4)}$ and in this case $\left(v_{1}\right)^{(4)}=\left(\bar{v}_{1}\right)^{(4)}$ if in addition $\left(v_{0}\right)^{(4)}=$ $\left(v_{1}\right)^{(4)}$ then $v^{(4)}(t)=\left(v_{0}\right)^{(4)}$ and as a consequence $G_{24}(t)=\left(v_{0}\right)^{(4)} G_{25}(t)$ this also defines $\left(v_{0}\right)^{(4)}$ for the special case.

Analogously if $\left(b_{24}^{\prime \prime}\right)^{(4)}=\left(b_{25}^{\prime \prime}\right)^{(4)}$, then $\left(\tau_{1}\right)^{(4)}=\left(\tau_{2}\right)^{(4)}$ and then
$\left(u_{1}\right)^{(4)}=\left(\bar{u}_{4}\right)^{(4)}$ if in addition $\left(u_{0}\right)^{(4)}=\left(u_{1}\right)^{(4)}$ then $T_{24}(t)=\left(u_{0}\right)^{(4)} T_{25}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(4)}$ and $\left(\bar{v}_{1}\right)^{(4)}$, and definition of $\left(u_{0}\right)^{(4)}$.

Proof: From global equations we obtain
$\frac{d v^{(5)}}{d t}=\left(a_{28}\right)^{(5)}-\left(\left(a_{28}^{\prime}\right)^{(5)}-\left(a_{29}^{\prime}\right)^{(5)}+\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right)\right)-\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}, t\right) v^{(5)}-\left(a_{29}\right)^{(5)} v^{(5)}$

Definition of $v^{(5)}:-\quad v^{(5)}=\frac{G_{28}}{G_{29}}$
It follows

$$
-\left(\left(a_{29}\right)^{(5)}\left(v^{(5)}\right)^{2}+\left(\sigma_{2}\right)^{(5)} v^{(5)}-\left(a_{28}\right)^{(5)}\right) \leq \frac{d v^{(5)}}{d t} \leq-\left(\left(a_{29}\right)^{(5)}\left(v^{(5)}\right)^{2}+\left(\sigma_{1}\right)^{(5)} v^{(5)}-\left(a_{28}\right)^{(5)}\right)
$$

## From which one obtains

Definition of $\left(\bar{v}_{1}\right)^{(5)},\left(v_{0}\right)^{(5)}$ :-
(g) For $0<\left(v_{0}\right)^{(5)}=\frac{G_{28}^{0}}{G_{22}^{0}}<\left(v_{1}\right)^{(5)}<\left(\bar{v}_{1}\right)^{(5)}$

$$
v^{(5)}(t) \geq \frac{\left(v_{1}\right)^{(5)}+(C)^{(5)}\left(v_{2}\right)^{(5)} e^{\left[-\left(a_{29}\right)^{(5)}\left(\left(v_{1}\right)^{(5)}-\left(v_{0}\right)^{(5)}\right) t\right]}}{5+(C)^{(5)} e^{\left[-\left(a_{29}\right)^{(5)}\left(\left(v_{1}\right)^{(5)}-\left(v_{0}\right)^{(5)}\right) t\right]}} \quad, \quad(C)^{(5)}=\frac{\left(v_{1}\right)^{(5)}-\left(v_{0}\right)^{(5)}}{\left(v_{0}\right)^{(5)}-\left(v_{2}\right)^{(5)}}
$$

it follows $\left(v_{0}\right)^{(5)} \leq v^{(5)}(t) \leq\left(v_{1}\right)^{(5)}$
In the same manner, we get

$$
v^{(5)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(5)}+(\bar{C})^{(5)}\left(\bar{v}_{2}\right)^{(5)} e^{\left[-\left(a_{29}\right)^{(5)}\left(\left(\bar{v}_{1}\right)^{(5)}-\left(\bar{v}_{2}\right)^{(5)}\right) t\right]}}{5+(\bar{C})^{(5)} e^{\left.\left[-\left(a_{29}\right)^{(5)}\left(\bar{v}_{1}\right)^{(5)}-\left(\bar{v}_{2}\right)^{(5)}\right) t\right]} \quad, \quad(\bar{C})^{(5)}=\frac{{\left(\bar{v}_{1}\right)^{(5)}-\left(v_{0}\right)^{(5)}}_{\left(v_{0}\right)^{(5)}-\left(\bar{v}_{2}\right)^{(5)}}}{} . \quad \text {. }}
$$

From which we deduce $\left(v_{0}\right)^{(5)} \leq v^{(5)}(t) \leq\left(\bar{v}_{5}\right)^{(5)}$
(h) If $0<\left(v_{1}\right)^{(5)}<\left(v_{0}\right)^{(5)}=\frac{G_{28}^{0}}{G_{29}^{0}}<\left(\bar{v}_{1}\right)^{(5)}$ we find like in the previous case,

$$
\begin{aligned}
& \left(v_{1}\right)^{(5)} \leq \frac{\left(v_{1}\right)^{(5)}+(C)^{(5)}\left(v_{2}\right)^{(5)} e^{\left[-\left(a_{29}\right)^{(5)}\left(\left(_{1}\right)^{(5)}-\left(v_{2}\right)^{(5)}\right) t\right]}}{1+(C)^{(5)} e^{\left[\left(a_{29}\right)^{(5)}\left({\left(v_{1}\right)}^{(5)}-\left(v_{2}\right)^{(5)}\right) t\right]} \leq v^{(5)}(t) \leq} \\
& \frac{\left(\bar{v}_{1}\right)^{(5)}+(\bar{c})^{(5)}\left(\bar{v}_{2}\right)^{(5)} e^{\left[-\left(a_{29}\right)^{(5)}\left(\left(\bar{v}_{1}\right)^{(5)}-\left(\bar{v}_{2}\right)^{(5)}\right) t\right]}}{1+(\bar{C})^{(5)} e^{\left.\left[-\left(a_{29}\right)^{(5)}\left(\bar{v}_{1}\right)^{(5)}-\left(\bar{v}_{2}\right)^{(5)}\right) t\right]} \leq\left(\bar{v}_{1}\right)^{(5)}}
\end{aligned}
$$

(i) If $0<\left(v_{1}\right)^{(5)} \leq\left(\bar{v}_{1}\right)^{(5)} \leq\left(v_{0}\right)^{(5)}=\frac{G_{28}^{0}}{G_{29}^{0}}$, we obtain

And so with the notation of the first part of condition (c), we have
Definition of $v^{(5)}(t)$ :-
$\left(m_{2}\right)^{(5)} \leq v^{(5)}(t) \leq\left(m_{1}\right)^{(5)}, \quad v^{(5)}(t)=\frac{G_{28}(t)}{G_{29}(t)}$
In a completely analogous way, we obtain
Definition of $u^{(5)}(t)$ :-
$\left(\mu_{2}\right)^{(5)} \leq u^{(5)}(t) \leq\left(\mu_{1}\right)^{(5)}, \quad u^{(5)}(t)=\frac{T_{28}(t)}{T_{29}(t)}$

Now, using this result and replacing it in global equations we get easily the result stated in the theorem.

## Particular case:

If $\left(a_{28}^{\prime \prime}\right)^{(5)}=\left(a_{29}^{\prime \prime}\right)^{(5)}$, then $\left(\sigma_{1}\right)^{(5)}=\left(\sigma_{2}\right)^{(5)}$ and in this case $\left(v_{1}\right)^{(5)}=\left(\bar{v}_{1}\right)^{(5)}$ if in addition $\left(v_{0}\right)^{(5)}=$ $\left(v_{5}\right)^{(5)}$ then $v^{(5)}(t)=\left(v_{0}\right)^{(5)}$ and as a consequence $G_{28}(t)=\left(v_{0}\right)^{(5)} G_{29}(t)$ this also defines $\left(v_{0}\right)^{(5)}$ for the special case.

Analogously if $\left(b_{28}^{\prime \prime}\right)^{(5)}=\left(b_{29}^{\prime \prime}\right)^{(5)}$, then $\left(\tau_{1}\right)^{(5)}=\left(\tau_{2}\right)^{(5)}$ and then
$\left(u_{1}\right)^{(5)}=\left(\bar{u}_{1}\right)^{(5)}$ if in addition $\left(u_{0}\right)^{(5)}=\left(u_{1}\right)^{(5)}$ then $T_{28}(t)=\left(u_{0}\right)^{(5)} T_{29}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(5)}$ and $\left(\bar{v}_{1}\right)^{(5)}$, and definition of $\left(u_{0}\right)^{(5)}$.

Proof: From global equations we obtain
$\frac{d v^{(6)}}{d t}=\left(a_{32}\right)^{(6)}-\left(\left(a_{32}^{\prime}\right)^{(6)}-\left(a_{33}^{\prime}\right)^{(6)}+\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right)\right)-\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}, t\right) v^{(6)}-\left(a_{33}\right)^{(6)} v^{(6)}$

Definition of $v^{(6)}:-\quad v^{(6)}=\frac{G_{32}}{G_{33}}$
It follows

$$
-\left(\left(a_{33}\right)^{(6)}\left(v^{(6)}\right)^{2}+\left(\sigma_{2}\right)^{(6)} v^{(6)}-\left(a_{32}\right)^{(6)}\right) \leq \frac{d v^{(6)}}{d t} \leq-\left(\left(a_{33}\right)^{(6)}\left(v^{(6)}\right)^{2}+\left(\sigma_{1}\right)^{(6)} v^{(6)}-\left(a_{32}\right)^{(6)}\right)
$$

## From which one obtains

$\underline{\text { Definition of }}\left(\bar{v}_{1}\right)^{(6)},\left(v_{0}\right)^{(6)}:-$
(j) For $0<\left(v_{0}\right)^{(6)}=\frac{G_{32}^{0}}{G_{32}^{0}}<\left(v_{1}\right)^{(6)}<\left(\bar{v}_{1}\right)^{(6)}$

$$
v^{(6)}(t) \geq \frac{\left(v_{1}\right)^{(6)}+(C)^{(6)}\left(v_{2}\right)^{(6)} e^{\left[-\left(a_{33}\right)^{(6)}\left(\left(v_{1}\right)^{(6)}-\left(v_{0}\right)^{(6)}\right) t\right]}}{1+(C)^{(6)} e^{\left[-\left(a_{33}\right)^{(6)}\left(\left(v_{1}\right)^{(6)}-\left(v_{0}\right)^{(6)}\right) t\right]} \quad, \quad(C)^{(6)}=\frac{\left(v_{1}\right)^{(6)}-\left(v_{0}\right)^{(6)}}{\left(v_{0}\right)^{(6)}-\left(v_{2}\right)^{(6)}} \text {. }}
$$

it follows $\left(v_{0}\right)^{(6)} \leq v^{(6)}(t) \leq\left(v_{1}\right)^{(6)}$
In the same manner, we get

$$
v^{(6)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(6)}+(\bar{C})^{(6)}\left(\bar{v}_{2}\right)^{(6)} e^{\left.\left.\left[-\left(a_{33}\right)^{(6)}\right)\left(\bar{v}_{1}\right)^{(6)}-\left(\bar{v}_{2}\right)^{(6)}\right) t\right]}}{1+(\bar{C})^{(6)} e^{\left.\left[-\left(a_{33}\right)^{(6)}\left(\bar{v}_{1}\right)^{(6)}-\left(\bar{v}_{2}\right)^{(6)}\right) t\right]} \quad, \quad(\bar{C})^{(6)}=\frac{\left(\bar{v}_{1}\right)^{(6)}-\left(v_{0}\right)^{(6)}}{\left(v_{0}\right)^{(6)}-\left(\bar{v}_{2}\right)^{(6)}}}
$$

From which we deduce $\left(v_{0}\right)^{(6)} \leq v^{(6)}(t) \leq\left(\bar{v}_{1}\right)^{(6)}$
(k) If $0<\left(v_{1}\right)^{(6)}<\left(v_{0}\right)^{(6)}=\frac{G_{32}^{0}}{G_{33}^{0}}<\left(\bar{v}_{1}\right)^{(6)}$ we find like in the previous case,

$$
\frac{\left.\left(\bar{v}_{1}\right)^{(6)}+(\bar{C})^{(6)}\right)\left(\bar{v}_{2}\right)^{(6)} e^{\left.\left[-\left(a_{33}\right)^{(6)}\left(\bar{v}_{1}\right)^{(6)}-\left(\bar{v}_{2}\right)^{(6)}\right) t\right]}}{1+(\bar{C})^{(6)} e^{\left.\left[\left(a_{33}\right)^{(6)}\left(\bar{v}_{1}\right)^{(6)}-\left(\bar{v}_{2}\right)^{(6)}\right) t\right]}} \leq\left(\bar{v}_{1}\right)^{(6)}
$$

(l) If $0<\left(v_{1}\right)^{(6)} \leq\left(\bar{v}_{1}\right)^{(6)} \leq\left(v_{0}\right)^{(6)}=\frac{G_{32}^{0}}{G_{33}^{0}}$, we obtain
$\left(v_{1}\right)^{(6)} \leq v^{(6)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(6)}+(\bar{C})^{(6)}\left(\bar{v}_{2}\right)^{(6)} e^{\left.\left[-\left(a_{33}\right)^{(6)}\left(\bar{v}_{1}\right)^{(6)}-\left(\bar{v}_{2}\right)^{(6)}\right) t\right]}}{1+(\bar{C})^{(6)} e^{\left.\left[-\left(a_{33}\right)^{(6)}\left(\bar{v}_{1}\right)^{(6)}-\left(\bar{v}_{2}\right)^{(6)}\right) t\right]}} \leq\left(v_{0}\right)^{(6)}$
And so with the notation of the first part of condition (c), we have
Definition of $v^{(6)}(t)$ :-

$$
\left(m_{2}\right)^{(6)} \leq v^{(6)}(t) \leq\left(m_{1}\right)^{(6)}, \quad v^{(6)}(t)=\frac{G_{32}(t)}{G_{33}(t)}
$$

In a completely analogous way, we obtain
Definition of $u^{(6)}(t)$ :-

$$
\left(\mu_{2}\right)^{(6)} \leq u^{(6)}(t) \leq\left(\mu_{1}\right)^{(6)}, \quad u^{(6)}(t)=\frac{T_{32}(t)}{T_{33}(t)}
$$

Now, using this result and replacing it in global equations we get easily the result stated in the theorem.

## Particular case:

If $\left(a_{32}^{\prime \prime}\right)^{(6)}=\left(a_{33}^{\prime \prime}\right)^{(6)}$, then $\left(\sigma_{1}\right)^{(6)}=\left(\sigma_{2}\right)^{(6)}$ and in this case $\left(v_{1}\right)^{(6)}=\left(\bar{v}_{1}\right)^{(6)}$ if in addition $\left(v_{0}\right)^{(6)}=$ $\left(v_{1}\right)^{(6)}$ then $v^{(6)}(t)=\left(v_{0}\right)^{(6)}$ and as a consequence $G_{32}(t)=\left(v_{0}\right)^{(6)} G_{33}(t)$ this also defines $\left(v_{0}\right)^{(6)}$ for the special case.
Analogously if $\left(b_{32}^{\prime \prime}\right)^{(6)}=\left(b_{33}^{\prime \prime}\right)^{(6)}$, then $\left(\tau_{1}\right)^{(6)}=\left(\tau_{2}\right)^{(6)}$ and then
$\left(u_{1}\right)^{(6)}=\left(\bar{u}_{1}\right)^{(6)}$ if in addition $\left(u_{0}\right)^{(6)}=\left(u_{1}\right)^{(6)}$ then $T_{32}(t)=\left(u_{0}\right)^{(6)} T_{33}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(6)}$ and $\left(\bar{v}_{1}\right)^{(6)}$, and definition of $\left(u_{0}\right)^{(6)}$.

Proof: From global equations we obtain

$$
\begin{aligned}
& \frac{d v^{(7)}}{d t}=\left(a_{36}\right)^{(7)}-\left(\left(a_{36}^{\prime}\right)^{(7)}-\left(a_{37}^{\prime}\right)^{(7)}+\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right)\right)- \\
& \left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}, t\right) v^{(7)}-\left(a_{37}\right)^{(7)} v^{(7)}
\end{aligned}
$$

Definition of $v^{(7)}: \quad v^{(7)}=\frac{G_{36}}{G_{37}}$
It follows

$$
\begin{aligned}
& -\left(\left(a_{37}\right)^{(7)}\left(v^{(7)}\right)^{2}+\left(\sigma_{2}\right)^{(7)} v^{(7)}-\left(a_{36}\right)^{(7)}\right) \leq \frac{d v^{(7)}}{d t} \leq \\
& \\
& \quad-\left(\left(a_{37}\right)^{(7)}\left(v^{(7)}\right)^{2}+\left(\sigma_{1}\right)^{(7)} v^{(7)}-\left(a_{36}\right)^{(7)}\right)
\end{aligned}
$$

From which one obtains
Definition of $\left(\bar{v}_{1}\right)^{(7)},\left(v_{0}\right)^{(7)}$ :-

$$
\begin{aligned}
& \text { For } 0<\left(v_{0}\right)^{(7)}=\frac{G_{36}^{0}}{G_{37}^{0}}<\left(v_{1}\right)^{(7)}<\left(\bar{v}_{1}\right)^{(7)} \\
& v^{(7)}(t) \geq \frac{\left(v_{1}\right)^{(7)}+(C)^{(7)}\left(v_{2}\right)^{(7)} e^{\left.\left[-\left(a_{37}\right)\right)^{(7)}\left(\left(v_{1}\right)^{(7)}-\left(v_{0}\right)^{(7)}\right) t\right]}}{1+(C)^{(7)} e^{\left[\left(-\left(a_{37}\right)^{(7)}\left((1 v 1)^{(7)}-\left(v_{0}\right)^{(7)}\right) t\right]\right.} \quad, \quad(C)^{(7)}=\frac{\left(v_{1}\right)^{(7)}-\left(v_{0}\right)^{(7)}}{\left(v_{0}\right)^{(7)}-\left(v_{2}\right)^{(7)}}}
\end{aligned}
$$

it follows $\left(v_{0}\right)^{(7)} \leq v^{(7)}(t) \leq\left(v_{1}\right)^{(7)}$
In the same manner, we get

From which we deduce $\left(v_{0}\right)^{(7)} \leq v^{(7)}(t) \leq\left(\bar{v}_{1}\right)^{(7)}$
If $0<\left(v_{1}\right)^{(7)}<\left(v_{0}\right)^{(7)}=\frac{G_{36}^{0}}{G_{37}^{0}}<\left(\bar{v}_{1}\right)^{(7)}$ we find like in the previous case,

$$
\begin{align*}
& \left(v_{1}\right)^{(7)} \leq \frac{\left(v_{1}\right)^{(7)}+(C)^{(7)}\left(v_{2}\right)^{(7)} e^{\left.\left[-\left(a_{37}\right)^{(7)}\left(v_{1}\right)^{(7)}-\left(v_{2}\right)^{(7)}\right) t\right]}}{1+(C)^{(7)} e^{\left[-\left(a_{37}\right)^{(7)}\left(\left(v_{1}\right)^{(7)}-\left(v_{2}\right)^{(7)}\right) t\right]}} \leq v^{(7)}(t) \leq \\
& \frac{\left.\left(\bar{v}_{1}\right)^{(7)}+(\bar{C})^{(7)}\right)_{\left(\bar{v}_{2}\right)}{ }^{(7)} e^{\left.\left[-\left(a_{37}\right)^{(7)}\left(\bar{v}_{1}\right)^{(7)}-\left(\bar{v}_{2}\right)^{(7)}\right) t\right]}}{1+(\bar{C})^{(7)} e^{\left.\left[-\left(a_{37}\right)^{(7)}\left(\bar{v}_{1}\right)^{(7)}-\left(\bar{v}_{2}\right)^{(7)}\right) t\right]}} \leq\left(\bar{v}_{1}\right)^{(7)} \\
& \text { If } 0<\left(v_{1}\right)^{(7)} \leq\left(\bar{v}_{1}\right)^{(7)} \leq\left(v_{0}\right)^{(7)}=\frac{G_{36}^{0}}{G_{37}^{0}} \text {, we obtain }  \tag{419}\\
& \left(v_{1}\right)^{(7)} \leq v^{(7)}(t) \leq \frac{\left.\left(\bar{v}_{1}\right)^{(7)}+(\bar{c})^{(7)}\right)\left(\bar{v}_{2}\right)^{(7)} e^{\left.\left[-\left(a_{37}\right)^{(7)}\left(\bar{v}_{1}\right)^{(7)}-\left(\bar{v}_{2}\right)^{(7)}\right) t\right]}}{1+(\bar{C})^{(7)} e^{\left.\left.-\left(a_{37}\right)^{(7)}\left(\bar{v}_{1}\right)^{(7)}-\left(\bar{v}_{2}\right)^{(7)}\right) t\right]}} \leq\left(v_{0}\right)^{(7)}
\end{align*}
$$

And so with the notation of the first part of condition (c), we have
Definition of $v^{(7)}(t)$ :-
$\left(m_{2}\right)^{(7)} \leq v^{(7)}(t) \leq\left(m_{1}\right)^{(7)}, \quad v^{(7)}(t)=\frac{G_{36}(t)}{G_{37}(t)}$
In a completely analogous way, we obtain
Definition of $u^{(7)}(t)$ :-
$\left(\mu_{2}\right)^{(7)} \leq u^{(7)}(t) \leq\left(\mu_{1}\right)^{(7)}, \quad u^{(7)}(t)=\frac{T_{36}(t)}{T_{37}(t)}$
Now, using this result and replacing it in global equations we get easily the result stated in the theorem.

## Particular case:

If $\left(a_{36}^{\prime \prime}\right)^{(7)}=\left(a_{37}^{\prime \prime}\right)^{(7)}$, then $\left(\sigma_{1}\right)^{(7)}=\left(\sigma_{2}\right)^{(7)}$ and in this case $\left(v_{1}\right)^{(7)}=\left(\bar{v}_{1}\right)^{(7)}$ if in addition $\left(v_{0}\right)^{(7)}=$ $\left(v_{1}\right)^{(7)}$ then $v^{(7)}(t)=\left(v_{0}\right)^{(7)}$ and as a consequence $G_{36}(t)=\left(v_{0}\right)^{(7)} G_{37}(t)$ this also defines $\left(v_{0}\right)^{(7)}$ for the special case.

Analogously if $\left(b_{36}^{\prime \prime}\right)^{(7)}=\left(b_{37}^{\prime \prime}\right)^{(7)}$, then $\left(\tau_{1}\right)^{(7)}=\left(\tau_{2}\right)^{(7)}$ and then $\left(u_{1}\right)^{(7)}=\left(\bar{u}_{1}\right)^{(7)}$ if in addition $\left(u_{0}\right)^{(7)}=\left(u_{1}\right)^{(7)}$ then $T_{36}(t)=\left(u_{0}\right)^{(7)} T_{37}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(7)}$ and $\left(\bar{v}_{1}\right)^{(7)}$, and definition of $\left(u_{0}\right)^{(7)}$.

Proof: From global equations we obtain
$\frac{d v^{(8)}}{d t}=\left(a_{40}\right)^{(8)}-\left(\left(a_{40}^{\prime}\right)^{(8)}-\left(a_{41}^{\prime}\right)^{(8)}+\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right)\right)-\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}, t\right) v^{(8)}-\left(a_{41}\right)^{(8)} v^{(8)}$
$\underline{\text { Definition of } v^{(8)}}$ :-

$$
v^{(8)}=\frac{G_{40}}{G_{41}}
$$

It follows

$$
-\left(\left(a_{41}\right)^{(8)}\left(v^{(8)}\right)^{2}+\left(\sigma_{2}\right)^{(8)} v^{(8)}-\left(a_{40}\right)^{(8)}\right) \leq \frac{d v^{(8)}}{d t} \leq-\left(\left(a_{41}\right)^{(8)}\left(v^{(8)}\right)^{2}+\left(\sigma_{1}\right)^{(8)} v^{(8)}-\left(a_{40}\right)^{(8)}\right)
$$

From which one obtains
Definition of $\left(\bar{v}_{1}\right)^{(8)},\left(v_{0}\right)^{(8)}$ :-
(m) $\quad$ For $0<\left(v_{0}\right)^{(8)}=\frac{G_{40}^{0}}{G_{41}^{0}}<\left(v_{1}\right)^{(8)}<\left(\bar{v}_{1}\right)^{(8)}$
it follows $\left(v_{0}\right)^{(8)} \leq v^{(8)}(t) \leq\left(v_{1}\right)^{(8)}$

In the same manner, we get
$v^{(8)}(t) \leq \frac{{\left.\overline{\left(\bar{v}_{1}\right.}\right)}^{(8)}+(\bar{C})^{(8)}\left(\bar{v}_{2}\right)^{(8)} e^{\left.\left[-\left(a_{41}\right)^{(8)}\left(\bar{v}_{1}\right)^{(8)}-\left(\bar{v}_{2}\right)^{(8)}\right) t\right]}}{1+(\bar{C})^{(8)} e^{\left.\left[-\left(a_{41}\right)^{(8)}\left(\bar{v}_{1}\right)^{(8)}-\left(\bar{v}_{2}\right)^{(8)}\right) t\right]}} \quad, \quad(\bar{C})^{(8)}=\frac{\left(\bar{v}_{1}\right)^{(8)}-\left(v_{0}\right)^{(8)}}{\left(v_{0}\right)^{(8)}-\left(\bar{v}_{2}\right)^{(8)}}$
From which we deduce $\left(v_{0}\right)^{(8)} \leq v^{(8)}(t) \leq\left(\bar{v}_{8}\right)^{(8)}$
(n) If $0<\left(v_{1}\right)^{(8)}<\left(v_{0}\right)^{(8)}=\frac{G_{40}^{0}}{G_{41}^{0}}<\left(\bar{v}_{1}\right)^{(8)}$ we find like in the previous case,

$$
\begin{aligned}
& \left(v_{1}\right)^{(8)} \leq \frac{\left(v_{1}\right)^{(8)}+(C)^{(8)}\left(v_{2}\right)^{(8)} e^{\left[-\left(a_{41}\right)^{(8)}\left(\left(_{1}\right)^{(8)}-\left(v_{2}\right)^{(8)}\right) t\right]}}{1+(C)^{(8)} e^{\left.\left[\left(a_{41}\right)^{(8)}\left(v_{1}\right)^{(8)}-\left(v_{2}\right)^{(8)}\right) t\right]}} \leq v^{(8)}(t) \leq \\
& \frac{\left.\left(\bar{v}_{1}\right)^{(8)}+(\bar{C})^{(8)} \bar{v}_{2}\right)^{(8)} e^{\left.\left[-\left(a_{41}\right)^{(8)}\left(\bar{v}_{1}\right)^{(8)}-\left(\bar{v}_{2}\right)^{(8)}\right) t\right]}}{1+(\bar{C})^{(8)} e^{\left.\left.-\left(a_{41}\right)^{(8)}\left(\bar{v}_{1}\right)^{(8)}-\left(\bar{v}_{2}\right)^{(8)}\right) t\right]}} \leq\left(\bar{v}_{1}\right)^{(8)}
\end{aligned}
$$

(o) If $0<\left(v_{1}\right)^{(8)} \leq\left(\bar{v}_{1}\right)^{(8)} \leq\left(v_{0}\right)^{(8)}=\frac{G_{40}^{0}}{G_{41}^{0}}$, we obtain
$\left(v_{1}\right)^{(8)} \leq v^{(8)}(t) \leq \frac{\left.\left(\bar{v}_{1}\right)^{(8)}+(\bar{c})^{(8)} \bar{v}_{2}\right)^{(8)} e^{\left[-\left(a_{41}\right)^{(8)}\left(\left(\bar{v}_{1}\right)^{(8)}-\left(\bar{v}_{2}\right)^{(8)}\right) t\right]}}{1+(\bar{c})^{(8)} e^{\left.\left[-\left(a_{41}\right)^{(8)}\left(\bar{v}_{1}\right)^{(8)}-\left(\bar{v}_{2}\right)^{(8)}\right) t\right]}} \leq\left(v_{0}\right)^{(8)}$
And so with the notation of the first part of condition (c), we have
Definition of $\boldsymbol{v}^{(8)}(t)$ :-

$$
\left(m_{2}\right)^{(8)} \leq v^{(8)}(t) \leq\left(m_{1}\right)^{(8)}, \quad v^{(8)}(t)=\frac{G_{40}(t)}{G_{41}(t)}
$$

In a completely analogous way, we obtain
Definition of $u^{(8)}(t)$ :-
$\left(\mu_{2}\right)^{(8)} \leq u^{(8)}(t) \leq\left(\mu_{1}\right)^{(8)}, \quad u^{(8)}(t)=\frac{T_{40}(t)}{T_{41}(t)}$

Now, using this result and replacing it in global equations we get easily the result stated in the theorem.

## Particular case :

If $\left(a_{40}^{\prime \prime}\right)^{(8)}=\left(a_{41}^{\prime \prime}\right)^{(8)}$, then $\left(\sigma_{1}\right)^{(8)}=\left(\sigma_{2}\right)^{(8)}$ and in this case $\left(v_{1}\right)^{(8)}=\left(\bar{v}_{1}\right)^{(8)}$ if in addition $\left(v_{0}\right)^{(8)}=$ $\left(v_{1}\right)^{(8)}$ then $v^{(8)}(t)=\left(v_{0}\right)^{(8)}$ and as a consequence $G_{40}(t)=\left(v_{0}\right)^{(8)} G_{41}(t)$ this also defines $\left(v_{0}\right)^{(8)}$ for

## the special case.

Analogously if $\left(b_{40}^{\prime \prime}\right)^{(8)}=\left(b_{41}^{\prime \prime}\right)^{(8)}$, then $\left(\tau_{1}\right)^{(8)}=\left(\tau_{2}\right)^{(8)}$ and then
$\left(u_{1}\right)^{(8)}=\left(\bar{u}_{1}\right)^{(8)}$ if in addition $\left(u_{0}\right)^{(8)}=\left(u_{1}\right)^{(8)}$ then $T_{40}(t)=\left(u_{0}\right)^{(8)} T_{41}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(8)}$ and $\left(\bar{v}_{1}\right)^{(8)}$, and definition of $\left(u_{0}\right)^{(8)}$.

Proof: From 99,20,44,22,23,44 we obtain

$$
\begin{aligned}
& \frac{d v^{(9)}}{d t}=\left(a_{44}\right)^{(9)}-\left(\left(a_{44}^{\prime}\right)^{(9)}-\left(a_{45}^{\prime}\right)^{(9)}+\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right)\right)- \\
& \left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}, t\right) v^{(9)}-\left(a_{45}\right)^{(9)} v^{(9)}
\end{aligned}
$$

$\underline{\text { Definition of } v^{(9)}}$ :-

$$
v^{(9)}=\frac{G_{44}}{G_{45}}
$$

It follows

$$
\begin{aligned}
& -\left(\left(a_{45}\right)^{(9)}\left(v^{(9)}\right)^{2}+\left(\sigma_{2}\right)^{(9)} v^{(9)}-\left(a_{44}\right)^{(9)}\right) \leq \frac{d v^{(9)}}{d t} \leq \\
& -\left(\left(a_{45}\right)^{(9)}\left(v^{(9)}\right)^{2}+\left(\sigma_{1}\right)^{(9)} v^{(9)}-\left(a_{44}\right)^{(9)}\right)
\end{aligned}
$$

## From which one obtains

Definition of $\left(\bar{v}_{1}\right)^{(9)},\left(v_{0}\right)^{(9)}:-$
(p) For $0<\left(v_{0}\right)^{(9)}=\frac{G_{44}^{0}}{G_{45}^{0}}<\left(v_{1}\right)^{(9)}<\left(\bar{v}_{1}\right)^{(9)}$
it follows $\left(v_{0}\right)^{(9)} \leq v^{(9)}(t) \leq\left(v_{9}\right)^{(9)}$
In the same manner, we get

$$
v^{(9)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(9)}+(\bar{C})^{(9)}\left(\bar{v}_{2}\right)^{(9)} e^{\left.\left[-\left(a_{45}\right)^{(9)}\left(\bar{v}_{1}\right)^{(9)}-\left(\bar{v}_{2}\right)^{(9)}\right) t\right]}}{1+(\bar{C})^{(9)} e^{\left.-\left(a_{45}\right)^{(9)}\left(\left(\bar{v}_{1}\right)^{(9)}-\left(\bar{v}_{2}\right)^{(9)}\right) t\right]} \quad, \quad(\bar{C})^{(9)}=\frac{\left(\bar{v}_{1}\right)^{(9)}-\left(v_{0}\right)^{(9)}}{\left(v_{0}\right)^{(9)}-\left(\bar{v}_{2}\right)^{(9)}}}
$$

From which we deduce $\left(v_{0}\right)^{(9)} \leq v^{(9)}(t) \leq\left(\bar{v}_{1}\right)^{(9)}$
(q) If $0<\left(v_{1}\right)^{(9)}<\left(v_{0}\right)^{(9)}=\frac{G_{44}^{0}}{G_{45}^{0}}<\left(\bar{v}_{1}\right)^{(9)}$ we find like in the previous case,

$$
\begin{aligned}
& \left(v_{1}\right)^{(9)} \leq \frac{\left(v_{1}\right)^{(9)}+(C)^{(9)}\left(v_{2}\right)^{(9)} e^{\left[-\left(a_{45}\right)^{(9)}\left({ }^{\left.\left.\left(v_{1}\right)^{(9)}-\left(v_{2}\right)^{(9)}\right) t\right]}\right.\right.}}{1+(C)^{(9)} e^{\left.\left[-\left(a_{45}\right)^{(9)}\left(v_{1}\right)^{(9)}-\left(v_{2}\right)^{(9)}\right) t\right]}} \leq v^{(9)}(t) \leq \\
& \frac{\left.\left(\bar{v}_{1}\right)^{(9)}+(\bar{C})^{(9)}\right)^{\left(\bar{v}_{2}\right)}{ }^{(9)} e^{\left.\left[-\left(a_{45}\right)^{(9)}\left({\left(\bar{v}_{1}\right)}\right)^{(9)}-\left(\bar{v}_{2}\right)^{(9)}\right) t\right]}}{1+(\bar{C})^{(9)} e^{\left.\left.-\left(a_{45}\right)^{(9)}\left(\bar{v}_{1}\right)^{(9)}-\left(\bar{v}_{2}\right)^{(9)}\right) t\right]}} \leq\left(\bar{v}_{1}\right)^{(9)}
\end{aligned}
$$

(r) If $0<\left(v_{1}\right)^{(9)} \leq\left(\bar{v}_{1}\right)^{(9)} \leq\left(v_{0}\right)^{(9)}=\frac{G_{44}^{0}}{G_{45}^{0}}$, we obtain

$$
\left(v_{1}\right)^{(9)} \leq v^{(9)}(t) \leq \frac{\left(\bar{v}_{1}\right)^{(9)}+(\bar{C})^{(9)}\left(\bar{v}_{2}\right)^{(9)} e^{\left.\left[-\left(a_{45}\right)^{(9)}\left(\bar{v}_{1}\right)^{(9)}-\left(\bar{v}_{2}\right)^{(9)}\right) t\right]}}{1+(\bar{C})^{(9)} e^{\left.\left.-\left(a_{45}\right)^{(9)}\left(\left(\bar{v}_{1}\right)^{(9)}\right)-\left(\bar{v}_{2}\right)^{(9)}\right) t\right]}} \leq\left(v_{0}\right)^{(9)}
$$

And so with the notation of the first part of condition (c), we have
Definition of $v^{(9)}(t)$ :-

$$
\left(m_{2}\right)^{(9)} \leq v^{(9)}(t) \leq\left(m_{1}\right)^{(9)}, \quad v^{(9)}(t)=\frac{G_{44}(t)}{G_{45}(t)}
$$

In a completely analogous way, we obtain
Definition of $u^{(9)}(t)$ :-
$\left(\mu_{2}\right)^{(9)} \leq u^{(9)}(t) \leq\left(\mu_{1}\right)^{(9)}, \quad u^{(9)}(t)=\frac{T_{44}(t)}{T_{45}(t)}$
Now, using this result and replacing it in $99,20,44,22,23$, and 44 we get easily the result stated in the theorem.

## Particular case :

If $\left(a_{44}^{\prime \prime}\right)^{(9)}=\left(a_{45}^{\prime \prime}\right)^{(9)}$, then $\left(\sigma_{1}\right)^{(9)}=\left(\sigma_{2}\right)^{(9)}$ and in this case $\left(v_{1}\right)^{(9)}=\left(\bar{v}_{1}\right)^{(9)}$ if in addition $\left(v_{0}\right)^{(9)}=$ $\left(v_{1}\right)^{(9)}$ then $v^{(9)}(t)=\left(v_{0}\right)^{(9)}$ and as a consequence $G_{44}(t)=\left(v_{0}\right)^{(9)} G_{45}(t)$ this also defines $\left(v_{0}\right)^{(9)}$ for the special case.

Analogously if $\left(b_{44}^{\prime \prime}\right)^{(9)}=\left(b_{45}^{\prime \prime}\right)^{(9)}$, then $\left(\tau_{1}\right)^{(9)}=\left(\tau_{2}\right)^{(9)}$ and then
$\left(u_{1}\right)^{(9)}=\left(\bar{u}_{1}\right)^{(9)}$ if in addition $\left(u_{0}\right)^{(9)}=\left(u_{1}\right)^{(9)}$ then $T_{44}(t)=\left(u_{0}\right)^{(9)} T_{45}(t)$ This is an important consequence of the relation between $\left(v_{1}\right)^{(9)}$ and $\left(\bar{v}_{1}\right)^{(9)}$, and definition of $\left(u_{0}\right)^{(9)}$.

We can prove the following
Theorem : If $\left(a_{i}^{\prime \prime}\right)^{(1)}$ and $\left(b_{i}^{\prime \prime}\right)^{(1)}$ are independent on $t$, and the conditions with the notations
$\left(a_{13}^{\prime}\right)^{(1)}\left(a_{14}^{\prime}\right)^{(1)}-\left(a_{13}\right)^{(1)}\left(a_{14}\right)^{(1)}<0$
$\left(a_{13}^{\prime}\right)^{(1)}\left(a_{14}^{\prime}\right)^{(1)}-\left(a_{13}\right)^{(1)}\left(a_{14}\right)^{(1)}+\left(a_{13}\right)^{(1)}\left(p_{13}\right)^{(1)}+\left(a_{14}^{\prime}\right)^{(1)}\left(p_{14}\right)^{(1)}+\left(p_{13}\right)^{(1)}\left(p_{14}\right)^{(1)}>0$
$\left(b_{13}^{\prime}\right)^{(1)}\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{13}\right)^{(1)}\left(b_{14}\right)^{(1)}>0$,
$\left(b_{13}^{\prime}\right)^{(1)}\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{13}\right)^{(1)}\left(b_{14}\right)^{(1)}-\left(b_{13}^{\prime}\right)^{(1)}\left(r_{14}\right)^{(1)}-\left(b_{14}^{\prime}\right)^{(1)}\left(r_{14}\right)^{(1)}+\left(r_{13}\right)^{(1)}\left(r_{14}\right)^{(1)}<0$
with $\left(p_{13}\right)^{(1)},\left(r_{14}\right)^{(1)}$ as defined by equation are satisfied, then the system
Theorem : If $\left(a_{i}^{\prime \prime}\right)^{(2)}$ and $\left(b_{i}^{\prime \prime}\right)^{(2)}$ are independent on $t$, and the conditions with the notations
$\left(a_{16}^{\prime}\right)^{(2)}\left(a_{17}^{\prime}\right)^{(2)}-\left(a_{16}\right)^{(2)}\left(a_{17}\right)^{(2)}<0$
$\left(a_{16}^{\prime}\right)^{(2)}\left(a_{17}^{\prime}\right)^{(2)}-\left(a_{16}\right)^{(2)}\left(a_{17}\right)^{(2)}+\left(a_{16}\right)^{(2)}\left(p_{16}\right)^{(2)}+\left(a_{17}^{\prime}\right)^{(2)}\left(p_{17}\right)^{(2)}+\left(p_{16}\right)^{(2)}\left(p_{17}\right)^{(2)}>0$
$\left(b_{16}^{\prime}\right)^{(2)}\left(b_{17}^{\prime}\right)^{(2)}-\left(b_{16}\right)^{(2)}\left(b_{17}\right)^{(2)}>0$,
$\left(b_{16}^{\prime}\right)^{(2)}\left(b_{17}^{\prime}\right)^{(2)}-\left(b_{16}\right)^{(2)}\left(b_{17}\right)^{(2)}-\left(b_{16}^{\prime}\right)^{(2)}\left(r_{17}\right)^{(2)}-\left(b_{17}^{\prime}\right)^{(2)}\left(r_{17}\right)^{(2)}+\left(r_{16}\right)^{(2)}\left(r_{17}\right)^{(2)}<0$
with $\left(p_{16}\right)^{(2)},\left(r_{17}\right)^{(2)}$ as defined by equation are satisfied, then the system
Theorem : If $\left(a_{i}^{\prime \prime}\right)^{(3)}$ and $\left(b_{i}^{\prime \prime}\right)^{(3)}$ are independent on $t$, and the conditions with the notations
$\left(a_{20}^{\prime}\right)^{(3)}\left(a_{21}^{\prime}\right)^{(3)}-\left(a_{20}\right)^{(3)}\left(a_{21}\right)^{(3)}<0$
$\left(a_{20}^{\prime}\right)^{(3)}\left(a_{21}^{\prime}\right)^{(3)}-\left(a_{20}\right)^{(3)}\left(a_{21}\right)^{(3)}+\left(a_{20}\right)^{(3)}\left(p_{20}\right)^{(3)}+\left(a_{21}^{\prime}\right)^{(3)}\left(p_{21}\right)^{(3)}+\left(p_{20}\right)^{(3)}\left(p_{21}\right)^{(3)}>0$
$\left(b_{20}^{\prime}\right)^{(3)}\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{20}\right)^{(3)}\left(b_{21}\right)^{(3)}>0$,
$\left(b_{20}^{\prime}\right)^{(3)}\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{20}\right)^{(3)}\left(b_{21}\right)^{(3)}-\left(b_{20}^{\prime}\right)^{(3)}\left(r_{21}\right)^{(3)}-\left(b_{21}^{\prime}\right)^{(3)}\left(r_{21}\right)^{(3)}+\left(r_{20}\right)^{(3)}\left(r_{21}\right)^{(3)}<0$
with $\left(p_{20}\right)^{(3)},\left(r_{21}\right)^{(3)}$ as defined by equation are satisfied, then the system
We can prove the following
Theorem : If $\left(a_{i}^{\prime \prime}\right)^{(4)}$ and $\left(b_{i}^{\prime \prime}\right)^{(4)}$ are independent on $t$, and the conditions with the notations $\left(a_{24}^{\prime}\right)^{(4)}\left(a_{25}^{\prime}\right)^{(4)}-\left(a_{24}\right)^{(4)}\left(a_{25}\right)^{(4)}<0$
$\left(a_{24}^{\prime}\right)^{(4)}\left(a_{25}^{\prime}\right)^{(4)}-\left(a_{24}\right)^{(4)}\left(a_{25}\right)^{(4)}+\left(a_{24}\right)^{(4)}\left(p_{24}\right)^{(4)}+\left(a_{25}^{\prime}\right)^{(4)}\left(p_{25}\right)^{(4)}+\left(p_{24}\right)^{(4)}\left(p_{25}\right)^{(4)}>0$
$\left(b_{24}^{\prime}\right)^{(4)}\left(b_{25}^{\prime}\right)^{(4)}-\left(b_{24}\right)^{(4)}\left(b_{25}\right)^{(4)}>0$,
$\left(b_{24}^{\prime}\right)^{(4)}\left(b_{25}^{\prime}\right)^{(4)}-\left(b_{24}\right)^{(4)}\left(b_{25}\right)^{(4)}-\left(b_{24}^{\prime}\right)^{(4)}\left(r_{25}\right)^{(4)}-\left(b_{25}^{\prime}\right)^{(4)}\left(r_{25}\right)^{(4)}+\left(r_{24}\right)^{(4)}\left(r_{25}\right)^{(4)}<0$
with $\left(p_{24}\right)^{(4)},\left(r_{25}\right)^{(4)}$ as defined by equation are satisfied, then the system
Theorem : If $\left(a_{i}^{\prime \prime}\right)^{(5)}$ and $\left(b_{i}^{\prime \prime}\right)^{(5)}$ are independent on $t$, and the conditions with the notations
$\left(a_{28}^{\prime}\right)^{(5)}\left(a_{29}^{\prime}\right)^{(5)}-\left(a_{28}\right)^{(5)}\left(a_{29}\right)^{(5)}<0$
$\left(a_{28}^{\prime}\right)^{(5)}\left(a_{29}^{\prime}\right)^{(5)}-\left(a_{28}\right)^{(5)}\left(a_{29}\right)^{(5)}+\left(a_{28}\right)^{(5)}\left(p_{28}\right)^{(5)}+\left(a_{29}^{\prime}\right)^{(5)}\left(p_{29}\right)^{(5)}+\left(p_{28}\right)^{(5)}\left(p_{29}\right)^{(5)}>0$
$\left(b_{28}^{\prime}\right)^{(5)}\left(b_{29}^{\prime}\right)^{(5)}-\left(b_{28}\right)^{(5)}\left(b_{29}\right)^{(5)}>0$,
$\left(b_{28}^{\prime}\right)^{(5)}\left(b_{29}^{\prime}\right)^{(5)}-\left(b_{28}\right)^{(5)}\left(b_{29}\right)^{(5)}-\left(b_{28}^{\prime}\right)^{(5)}\left(r_{29}\right)^{(5)}-\left(b_{29}^{\prime}\right)^{(5)}\left(r_{29}\right)^{(5)}+\left(r_{28}\right)^{(5)}\left(r_{29}\right)^{(5)}<0$
with $\left(p_{28}\right)^{(5)},\left(r_{29}\right)^{(5)}$ as defined by equation are satisfied, then the system

Theorem If $\left(a_{i}^{\prime \prime}\right)^{(6)}$ and $\left(b_{i}^{\prime \prime}\right)^{(6)}$ are independent on $t$, and the conditions with the notations

$$
\left(a_{32}^{\prime}\right)^{(6)}\left(a_{33}^{\prime}\right)^{(6)}-\left(a_{32}\right)^{(6)}\left(a_{33}\right)^{(6)}+\left(a_{32}\right)^{(6)}\left(p_{32}\right)^{(6)}+\left(a_{33}^{\prime}\right)^{(6)}\left(p_{33}\right)^{(6)}+\left(p_{32}\right)^{(6)}\left(p_{33}\right)^{(6)}>0
$$

$$
\left(b_{32}^{\prime}\right)^{(6)}\left(b_{33}^{\prime}\right)^{(6)}-\left(b_{32}\right)^{(6)}\left(b_{33}\right)^{(6)}>0,
$$

$$
\left(b_{32}^{\prime}\right)^{(6)}\left(b_{33}^{\prime}\right)^{(6)}-\left(b_{32}\right)^{(6)}\left(b_{33}\right)^{(6)}-\left(b_{32}^{\prime}\right)^{(6)}\left(r_{33}\right)^{(6)}-\left(b_{33}^{\prime}\right)^{(6)}\left(r_{33}\right)^{(6)}+\left(r_{32}\right)^{(6)}\left(r_{33}\right)^{(6)}<0
$$

with $\left(p_{32}\right)^{(6)},\left(r_{33}\right)^{(6)}$ as defined by equation are satisfied, then the system
Theorem : If $\left(a_{i}^{\prime \prime}\right)^{(7)}$ and $\left(b_{i}^{\prime \prime}\right)^{(7)}$ are independent on $t$, and the conditions with the notations

$$
\left(a_{36}^{\prime}\right)^{(7)}\left(a_{37}^{\prime}\right)^{(7)}-\left(a_{36}\right)^{(7)}\left(a_{37}\right)^{(7)}<0
$$

$$
\left(a_{36}^{\prime}\right)^{(7)}\left(a_{37}^{\prime}\right)^{(7)}-\left(a_{36}\right)^{(7)}\left(a_{37}\right)^{(7)}+\left(a_{36}\right)^{(7)}\left(p_{36}\right)^{(7)}+\left(a_{37}^{\prime}\right)^{(7)}\left(p_{37}\right)^{(7)}+\left(p_{36}\right)^{(7)}\left(p_{37}\right)^{(7)}>0
$$

$$
\left(b_{36}^{\prime}\right)^{(7)}\left(b_{37}^{\prime}\right)^{(7)}-\left(b_{36}\right)^{(7)}\left(b_{37}\right)^{(7)}>0,
$$

$$
\left(b_{36}^{\prime}\right)^{(7)}\left(b_{37}^{\prime}\right)^{(7)}-\left(b_{36}\right)^{(7)}\left(b_{37}\right)^{(7)}-\left(b_{36}^{\prime}\right)^{(7)}\left(r_{37}\right)^{(7)}-\left(b_{37}^{\prime}\right)^{(7)}\left(r_{37}\right)^{(7)}+\left(r_{36}\right)^{(7)}\left(r_{37}\right)^{(7)}<0
$$

with $\left(p_{36}\right)^{(7)},\left(r_{37}\right)^{(7)}$ as defined by equation are satisfied, then the system
Theorem : If $\left(a_{i}^{\prime \prime}\right)^{(8)}$ and $\left(b_{i}^{\prime \prime}\right)^{(8)}$ are independent on $t$, and the conditions with the notations

$$
\begin{aligned}
& \left(a_{40}^{\prime}\right)^{(8)}\left(a_{41}^{\prime}\right)^{(8)}-\left(a_{40}\right)^{(8)}\left(a_{41}\right)^{(8)}<0 \\
& \left(a_{40}^{\prime}\right)^{(8)}\left(a_{41}^{\prime}\right)^{(8)}-\left(a_{40}\right)^{(8)}\left(a_{41}\right)^{(8)}+\left(a_{40}\right)^{(8)}\left(p_{40}\right)^{(8)}+\left(a_{41}^{\prime}\right)^{(8)}\left(p_{41}\right)^{(8)}+\left(p_{40}\right)^{(8)}\left(p_{41}\right)^{(8)}>0 \\
& \left(b_{40}^{\prime}\right)^{(8)}\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{40}\right)^{(8)}\left(b_{41}\right)^{(8)}>0 \\
& \left(b_{40}^{\prime}\right)^{(8)}\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{40}\right)^{(8)}\left(b_{41}\right)^{(8)}-\left(b_{40}^{\prime}\right)^{(8)}\left(r_{41}\right)^{(8)}-\left(b_{41}^{\prime}\right)^{(8)}\left(r_{41}\right)^{(8)}+\left(r_{40}\right)^{(8)}\left(r_{41}\right)^{(8)}<0
\end{aligned}
$$

with $\left(p_{40}\right)^{(8)},\left(r_{41}\right)^{(8)}$ as defined by equation are satisfied, then the system
$\underline{\text { Theorem }}$ : If $\left(a_{i}^{\prime \prime}\right)^{(9)}$ and $\left(b_{i}^{\prime \prime}\right)^{(9)}$ are independent on $t$, and the conditions (with the notations

$$
\begin{aligned}
& \left(a_{44}^{\prime}\right)^{(9)}\left(a_{45}^{\prime}\right)^{(9)}-\left(a_{44}\right)^{(9)}\left(a_{45}\right)^{(9)}<0 \\
& \left(a_{44}^{\prime}\right)^{(9)}\left(a_{45}^{\prime}\right)^{(9)}-\left(a_{44}\right)^{(9)}\left(a_{45}\right)^{(9)}+\left(a_{44}\right)^{(9)}\left(p_{44}\right)^{(9)}+\left(a_{45}^{\prime}\right)^{(9)}\left(p_{45}\right)^{(9)}+\left(p_{44}\right)^{(9)}\left(p_{45}\right)^{(9)}>0 \\
& \left(b_{44}^{\prime}\right)^{(9)}\left(b_{45}^{\prime}\right)^{(9)}-\left(b_{44}\right)^{(9)}\left(b_{45}\right)^{(9)}>0, \\
& \left(b_{44}^{\prime}\right)^{(9)}\left(b_{45}^{\prime}\right)^{(9)}-\left(b_{44}\right)^{(9)}\left(b_{45}\right)^{(9)}-\left(b_{44}^{\prime}\right)^{(9)}\left(r_{45}\right)^{(9)}-\left(b_{45}^{\prime}\right)^{(9)}\left(r_{45}\right)^{(9)}+\left(r_{44}\right)^{(9)}\left(r_{45}\right)^{(9)}<0
\end{aligned}
$$

$$
\text { with }\left(p_{44}\right)^{(9)},\left(r_{45}\right)^{(9)} \text { as defined by equation } 45 \text { are satisfied, then the system }
$$

$$
\left(a_{13}\right)^{(1)} G_{14}-\left[\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}\right)\right] G_{13}=0
$$

$$
\left(a_{14}\right)^{(1)} G_{13}-\left[\left(a_{14}^{\prime}\right)^{(1)}+\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}\right)\right] G_{14}=0
$$

$\left(b_{13}\right)^{(1)} T_{14}-\left[\left(b_{13}^{\prime}\right)^{(1)}-\left(b_{13}^{\prime \prime}\right)^{(1)}(G)\right] T_{13}=0$
$\left(b_{14}\right)^{(1)} T_{13}-\left[\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{14}^{\prime \prime}\right)^{(1)}(G)\right] T_{14}=0$
$\left(b_{15}\right)^{(1)} T_{14}-\left[\left(b_{15}^{\prime}\right)^{(1)}-\left(b_{15}^{\prime \prime}\right)^{(1)}(G)\right] T_{15}=0$
has a unique positive solution, which is an equilibrium solution for the system
$\left(a_{16}\right)^{(2)} G_{17}-\left[\left(a_{16}^{\prime}\right)^{(2)}+\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)\right] G_{16}=0$
$\left(a_{17}\right)^{(2)} G_{16}-\left[\left(a_{17}^{\prime}\right)^{(2)}+\left(a_{17}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)\right] G_{17}=0$
$\left(a_{18}\right)^{(2)} G_{17}-\left[\left(a_{18}^{\prime}\right)^{(2)}+\left(a_{18}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)\right] G_{18}=0$
$\left(b_{16}\right)^{(2)} T_{17}-\left[\left(b_{16}^{\prime}\right)^{(2)}-\left(b_{16}^{\prime \prime}\right)^{(2)}\left(G_{19}\right)\right] T_{16}=0$
$\left(b_{17}\right)^{(2)} T_{16}-\left[\left(b_{17}^{\prime}\right)^{(2)}-\left(b_{17}^{\prime \prime}\right)^{(2)}\left(G_{19}\right)\right] T_{17}=0$
447
$\left(b_{18}\right)^{(2)} T_{17}-\left[\left(b_{18}^{\prime}\right)^{(2)}-\left(b_{18}^{\prime \prime}\right)^{(2)}\left(G_{19}\right)\right] T_{18}=0 \quad 448$
has a unique positive solution, which is an equilibrium solution
$\left(a_{20}\right)^{(3)} G_{21}-\left[\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}\right)\right] G_{20}=0$
$\left(a_{21}\right)^{(3)} G_{20}-\left[\left(a_{21}^{\prime}\right)^{(3)}+\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}\right)\right] G_{21}=0$
450
$\left(a_{22}\right)^{(3)} G_{21}-\left[\left(a_{22}^{\prime}\right)^{(3)}+\left(a_{22}^{\prime \prime}\right)^{(3)}\left(T_{21}\right)\right] G_{22}=0$

$$
\begin{array}{lc}
\left(b_{20}\right)^{(3)} T_{21}-\left[\left(b_{20}^{\prime}\right)^{(3)}-\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}\right)\right] T_{20}=0 & 452 \\
\left(b_{21}\right)^{(3)} T_{20}-\left[\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{21}^{\prime \prime}\right)^{(3)}\left(G_{23}\right)\right] T_{21}=0 & 453 \\
\left(b_{22}\right)^{(3)} T_{21}-\left[\left(b_{22}^{\prime}\right)^{(3)}-\left(b_{22}^{\prime \prime}\right)^{(3)}\left(G_{23}\right)\right] T_{22}=0 & 454 \\
\text { has a unique positive solution, which is an equilibrium solution } & 455 \\
\left(a_{24}\right)^{(4)} G_{25}-\left[\left(a_{24}^{\prime}\right)^{(4)}+\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)\right] G_{24}=0 & 456 \\
\left(a_{25}\right)^{(4)} G_{24}-\left[\left(a_{25}^{\prime}\right)^{(4)}+\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)\right] G_{25}=0 & 457 \\
\left(a_{26}\right)^{(4)} G_{25}-\left[\left(a_{26}^{\prime}\right)^{(4)}+\left(a_{26}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)\right] G_{26}=0 & 458 \\
\left(b_{24}\right)^{(4)} T_{25}-\left[\left(b_{24}^{\prime}\right)^{(4)}-\left(b_{24}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)\right)\right] T_{24}=0 & 459 \\
\left(b_{25}\right)^{(4)} T_{24}-\left[\left(b_{25}^{\prime}\right)^{(4)}-\left(b_{25}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)\right)\right] T_{25}=0 & 45 \\
\left(b_{26}\right)^{(4)} T_{25}-\left[\left(b_{26}^{\prime}\right)^{(4)}-\left(b_{26}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)\right)\right] T_{26}=0 & 460
\end{array}
$$

has a unique positive solution, which is an equilibrium solution
$\left(a_{28}\right)^{(5)} G_{29}-\left[\left(a_{28}^{\prime}\right)^{(5)}+\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)\right] G_{28}=0$
$\left(a_{29}\right)^{(5)} G_{28}-\left[\left(a_{29}^{\prime}\right)^{(5)}+\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)\right] G_{29}=0$462
$\left(a_{30}\right)^{(5)} G_{29}-\left[\left(a_{30}^{\prime}\right)^{(5)}+\left(a_{30}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)\right] G_{30}=0$463
$\left(b_{28}\right)^{(5)} T_{29}-\left[\left(b_{28}^{\prime}\right)^{(5)}-\left(b_{28}^{\prime \prime}\right)^{(5)}\left(G_{31}\right)\right] T_{28}=0$
$\left(b_{29}\right)^{(5)} T_{28}-\left[\left(b_{29}^{\prime}\right)^{(5)}-\left(b_{29}^{\prime \prime}\right)^{(5)}\left(G_{31}\right)\right] T_{29}=0$465
$\left(b_{30}\right)^{(5)} T_{29}-\left[\left(b_{30}^{\prime}\right)^{(5)}-\left(b_{30}^{\prime \prime}\right)^{(5)}\left(G_{31}\right)\right] T_{30}=0$
has a unique positive solution, which is an equilibrium solution
$\left(a_{32}\right)^{(6)} G_{33}-\left[\left(a_{32}^{\prime}\right)^{(6)}+\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)\right] G_{32}=0$
$\left(a_{33}\right)^{(6)} G_{32}-\left[\left(a_{33}^{\prime}\right)^{(6)}+\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)\right] G_{33}=0$
$\left(a_{34}\right)^{(6)} G_{33}-\left[\left(a_{34}^{\prime}\right)^{(6)}+\left(a_{34}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)\right] G_{34}=0$469
$\left(b_{32}\right)^{(6)} T_{33}-\left[\left(b_{32}^{\prime}\right)^{(6)}-\left(b_{32}^{\prime \prime}\right)^{(6)}\left(G_{35}\right)\right] T_{32}=0$
$\left(b_{33}\right)^{(6)} T_{32}-\left[\left(b_{33}^{\prime}\right)^{(6)}-\left(b_{33}^{\prime \prime}\right)^{(6)}\left(G_{35}\right)\right] T_{33}=0$
$\left(b_{34}\right)^{(6)} T_{33}-\left[\left(b_{34}^{\prime}\right)^{(6)}-\left(b_{34}^{\prime \prime}\right)^{(6)}\left(G_{35}\right)\right] T_{34}=0$
has a unique positive solution, which is an equilibrium solution

$$
\left(a_{36}\right)^{(7)} G_{37}-\left[\left(a_{36}^{\prime}\right)^{(7)}+\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)\right] G_{36}=0
$$

$$
\left(a_{37}\right)^{(7)} G_{36}-\left[\left(a_{37}^{\prime}\right)^{(7)}+\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)\right] G_{37}=0
$$

$\left(a_{38}\right)^{(7)} G_{37}-\left[\left(a_{38}^{\prime}\right)^{(7)}+\left(a_{38}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)\right] G_{38}=0$475
$\left(b_{36}\right)^{(7)} T_{37}-\left[\left(b_{36}^{\prime}\right)^{(7)}-\left(b_{36}^{\prime \prime}\right)^{(7)}\left(G_{39}\right)\right] T_{36}=0$476
$\left(b_{37}\right)^{(7)} T_{36}-\left[\left(b_{37}^{\prime}\right)^{(7)}-\left(b_{37}^{\prime \prime}\right)^{(7)}\left(G_{39}\right)\right] T_{37}=0$
$\left(b_{38}\right)^{(7)} T_{37}-\left[\left(b_{38}^{\prime}\right)^{(7)}-\left(b_{38}^{\prime \prime}\right)^{(7)}\left(G_{39}\right)\right] T_{38}=0$
$\left(a_{40}\right)^{(8)} G_{41}-\left[\left(a_{40}^{\prime}\right)^{(8)}+\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)\right] G_{40}=0$
$\left(a_{41}\right)^{(8)} G_{40}-\left[\left(a_{41}^{\prime}\right)^{(8)}+\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)\right] G_{41}=0$ 480
$\left(a_{42}\right)^{(8)} G_{41}-\left[\left(a_{42}^{\prime}\right)^{(8)}+\left(a_{42}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)\right] G_{42}=0$
$\left(b_{40}\right)^{(8)} T_{41}-\left[\left(b_{40}^{\prime}\right)^{(8)}-\left(b_{40}^{\prime \prime}\right)^{(8)}\left(G_{43}\right)\right] T_{40}=0$482
$\left(b_{41}\right)^{(8)} T_{40}-\left[\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{41}^{\prime \prime}\right)^{(8)}\left(G_{43}\right)\right] T_{41}=0$
$\left(b_{42}\right)^{(8)} T_{41}-\left[\left(b_{42}^{\prime}\right)^{(8)}-\left(b_{42}^{\prime \prime}\right)^{(8)}\left(G_{43}\right)\right] T_{42}=0$
$\left(a_{44}\right)^{(9)} G_{45}-\left[\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)\right] G_{44}=0$
$\left(a_{45}\right)^{(9)} G_{44}-\left[\left(a_{45}^{\prime}\right)^{(9)}+\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)\right] G_{45}=0$
$\left(a_{46}\right)^{(9)} G_{45}-\left[\left(a_{46}^{\prime}\right)^{(9)}+\left(a_{46}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)\right] G_{46}=0$
$\left(b_{44}\right)^{(9)} T_{45}-\left[\left(b_{44}^{\prime}\right)^{(9)}-\left(b_{44}^{\prime \prime}\right)^{(9)}\left(G_{47}\right)\right] T_{44}=0$
$\left(b_{45}\right)^{(9)} T_{44}-\left[\left(b_{45}^{\prime}\right)^{(9)}-\left(b_{45}^{\prime \prime}\right)^{(9)}\left(G_{47}\right)\right] T_{45}=0$
$\left(b_{46}\right)^{(9)} T_{45}-\left[\left(b_{46}^{\prime}\right)^{(9)}-\left(b_{46}^{\prime \prime}\right)^{(9)}\left(G_{47}\right)\right] T_{46}=0$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{13}, G_{14}$ if
$F(T)=\left(a_{13}^{\prime}\right)^{(1)}\left(a_{14}^{\prime}\right)^{(1)}-\left(a_{13}\right)^{(1)}\left(a_{14}\right)^{(1)}+\left(a_{13}^{\prime}\right)^{(1)}\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}\right)+\left(a_{14}^{\prime}\right)^{(1)}\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}\right)+$ $\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}\right)\left(a_{14}^{\prime \prime}\right)^{(1)}\left(T_{14}\right)=0$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{16}, G_{17}$ if
$\mathrm{F}\left(T_{19}\right)=\left(a_{16}^{\prime}\right)^{(2)}\left(a_{17}^{\prime}\right)^{(2)}-\left(a_{16}\right)^{(2)}\left(a_{17}\right)^{(2)}+\left(a_{16}^{\prime}\right)^{(2)}\left(a_{17}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)+\left(a_{17}^{\prime}\right)^{(2)}\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)+$ $\left(a_{16}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)\left(a_{17}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)=0$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{20}, G_{21}$ if

$$
F\left(T_{23}\right)=\left(a_{20}^{\prime}\right)^{(3)}\left(a_{21}^{\prime}\right)^{(3)}-\left(a_{20}\right)^{(3)}\left(a_{21}\right)^{(3)}+\left(a_{20}^{\prime}\right)^{(3)}\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}\right)+\left(a_{21}^{\prime}\right)^{(3)}\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}\right)+
$$

$$
\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}\right)\left(a_{21}^{\prime \prime}\right)^{(3)}\left(T_{21}\right)=0
$$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{24}, G_{25}$ if
$F\left(T_{27}\right)=\left(a_{24}^{\prime}\right)^{(4)}\left(a_{25}^{\prime}\right)^{(4)}-\left(a_{24}\right)^{(4)}\left(a_{25}\right)^{(4)}+\left(a_{24}^{\prime}\right)^{(4)}\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)+\left(a_{25}^{\prime}\right)^{(4)}\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)+$ $\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)\left(a_{25}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)=0$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{28}, G_{29}$ if

$$
\begin{aligned}
& F\left(T_{31}\right)=\left(a_{28}^{\prime}\right)^{(5)}\left(a_{29}^{\prime}\right)^{(5)}-\left(a_{28}\right)^{(5)}\left(a_{29}\right)^{(5)}+\left(a_{28}^{\prime}\right)^{(5)}\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)+\left(a_{29}^{\prime}\right)^{(5)}\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)+ \\
& \left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)\left(a_{29}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)=0
\end{aligned}
$$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{32}, G_{33}$ if
$F\left(T_{35}\right)=\left(a_{32}^{\prime}\right)^{(6)}\left(a_{33}^{\prime}\right)^{(6)}-\left(a_{32}\right)^{(6)}\left(a_{33}\right)^{(6)}+\left(a_{32}^{\prime}\right)^{(6)}\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)+\left(a_{33}^{\prime}\right)^{(6)}\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)+$ $\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)\left(a_{33}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)=0$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{36}, G_{37}$ if
$F\left(T_{39}\right)=\left(a_{36}^{\prime}\right)^{(7)}\left(a_{37}^{\prime}\right)^{(7)}-\left(a_{36}\right)^{(7)}\left(a_{37}\right)^{(7)}+\left(a_{36}^{\prime}\right)^{(7)}\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)+\left(a_{37}^{\prime}\right)^{(7)}\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)+$ $\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)\left(a_{37}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)=0$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{40}, G_{41}$ if

$$
\begin{aligned}
& F\left(T_{43}\right)=\left(a_{40}^{\prime}\right)^{(8)}\left(a_{41}^{\prime}\right)^{(8)}-\left(a_{40}\right)^{(8)}\left(a_{41}\right)^{(8)}+\left(a_{40}^{\prime}\right)^{(8)}\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)+\left(a_{41}^{\prime}\right)^{(8)}\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)+ \\
& \left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)\left(a_{41}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)=0
\end{aligned}
$$

## Proof:

(a) Indeed the first two equations have a nontrivial solution $G_{44}, G_{45}$ if
$F\left(T_{47}\right)=\left(a_{44}^{\prime}\right)^{(9)}\left(a_{45}^{\prime}\right)^{(9)}-\left(a_{44}\right)^{(9)}\left(a_{45}\right)^{(9)}+\left(a_{44}^{\prime}\right)^{(9)}\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)+\left(a_{45}^{\prime}\right)^{(9)}\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)+$ $\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)\left(a_{45}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)=0$
Definition and uniqueness of $\mathrm{T}_{14}^{*}$ :-
After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{14}\right)$ being increasing, it follows that there exists a unique $T_{14}^{*}$ for which $f\left(T_{14}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{13}=\frac{\left(a_{13}\right)^{(1)} G_{14}}{\left[\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}^{*}\right)\right]} \quad, \quad G_{15}=\frac{\left(a_{15}\right)^{(1)} G_{14}}{\left[\left(a_{15}^{\prime}\right)^{(1)}+\left(a_{15}^{\prime \prime}\right)^{(1)}\left(T_{14}^{*}\right)\right]}$
Definition and uniqueness of $\mathrm{T}_{17}^{*}$ :-
After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(2)}\left(T_{17}\right)$ being increasing, it follows that there exists a unique $\mathrm{T}_{17}^{*}$ for which $f\left(\mathrm{~T}_{17}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{16}=\frac{\left(a_{16}\right)^{(2)} \mathrm{G}_{17}}{\left[\left(a_{16}^{\prime}\right)^{(2)}+\left(a_{16}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}^{*}\right)\right]} \quad, \quad G_{18}=\frac{\left(a_{18}\right)^{(2)} \mathrm{G}_{17}}{\left[\left(a_{18}^{\prime}\right)^{(2)}+\left(a_{18}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}^{*}\right)\right]}$
Definition and uniqueness of $\mathrm{T}_{21}^{*}$ :-
After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(1)}\left(T_{21}\right)$ being increasing, it follows that there exists a unique $T_{21}^{*}$ for which $f\left(T_{21}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{20}=\frac{\left(a_{20}\right)^{(3)} G_{21}}{\left[\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}^{*}\right)\right]} \quad, \quad G_{22}=\frac{\left(a_{22}\right)^{(3)} G_{21}}{\left[\left(a_{22}^{\prime}\right)^{(3)}+\left(a_{22}^{\prime \prime}\right)^{(3)}\left(T_{21}^{*}\right)\right]}$
Definition and uniqueness of $\mathrm{T}_{25}^{*}$ :-
After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(4)}\left(T_{25}\right)$ being increasing, it follows that there exists a unique $T_{25}^{*}$ for which $f\left(T_{25}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{24}=\frac{\left(a_{24}\right)^{(4)} G_{25}}{\left[\left(a_{24}^{\prime}\right)^{(4)}+\left(a_{24}^{\prime \prime}\right)^{(4)}\left(T_{25}^{*}\right)\right]} \quad, \quad G_{26}=\frac{\left(a_{26}\right)^{(4)} G_{25}}{\left[\left(a_{26}^{\prime}\right)^{(4)}+\left(a_{26}^{\prime \prime}\right)^{(4)}\left(T_{25}^{*}\right)\right]}$
Definition and uniqueness of $\mathrm{T}_{29}^{*}$ :-
After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(5)}\left(T_{29}\right)$ being increasing, it follows that
there exists a unique $T_{29}^{*}$ for which $f\left(T_{29}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{28}=\frac{\left(a_{28}\right)^{(5)} G_{29}}{\left[\left(a_{28}^{\prime}\right)^{(5)}+\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}^{*}\right)\right]} \quad, \quad G_{30}=\frac{\left(a_{30}\right)^{(5)} G_{29}}{\left[\left(a_{30}^{\prime}\right)^{(5)}+\left(a_{30}^{\prime \prime}\right)^{(5)}\left(T_{29}^{*}\right)\right]}$

## Definition and uniqueness of $\mathrm{T}_{33}^{*}$ :-

After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(6)}\left(T_{33}\right)$ being increasing, it follows that there exists a unique $T_{33}^{*}$ for which $f\left(T_{33}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{32}=\frac{\left(a_{32}\right)^{(6)} G_{33}}{\left[\left(a_{32}^{\prime}\right)^{(6)}+\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}^{*}\right)\right]} \quad, \quad G_{34}=\frac{\left(a_{34}\right)^{(6)} G_{33}}{\left[\left(a_{34}^{\prime}\right)^{(6)}+\left(a_{34}^{\prime \prime}\right)^{(6)}\left(T_{33}^{*}\right)\right]}$
Definition and uniqueness of $\mathrm{T}_{37}^{*}$ :-
After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(7)}\left(T_{37}\right)$ being increasing, it follows that there exists a unique $T_{37}^{*}$ for which $f\left(T_{37}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{36}=\frac{\left(a_{36}\right)^{(7)} G_{37}}{\left[\left(a_{36}^{\prime}\right)^{(7)}+\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}^{*}\right)\right]} \quad, \quad G_{38}=\frac{\left(a_{38}\right)^{(7)} G_{37}}{\left[\left(a_{38}^{\prime}\right)^{(7)}+\left(a_{38}^{\prime \prime}\right)^{(7)}\left(T_{37}^{*}\right)\right]}$

## Definition and uniqueness of $\mathrm{T}_{41}^{*}$ :-

After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(8)}\left(T_{41}\right)$ being increasing, it follows that there exists a unique $T_{41}^{*}$ for which $f\left(T_{41}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{40}=\frac{\left(a_{40}\right)^{(8)} G_{41}}{\left[\left(a_{40}^{\prime}\right)^{(8)}+\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}^{*}\right)\right]} \quad, \quad G_{42}=\frac{\left(a_{42}\right)^{(8)} G_{41}}{\left[\left(a_{42}^{\prime}\right)^{(8)}+\left(a_{42}^{\prime \prime}\right)^{(8)}\left(T_{41}^{*}\right)\right]}$

## Definition and uniqueness of $\mathrm{T}_{45}^{*}$ :-

After hypothesis $f(0)<0, f(\infty)>0$ and the functions $\left(a_{i}^{\prime \prime}\right)^{(9)}\left(T_{45}\right)$ being increasing, it follows that there exists a unique $T_{45}^{*}$ for which $f\left(T_{45}^{*}\right)=0$. With this value, we obtain from the three first equations
$G_{44}=\frac{\left(a_{44}\right)^{(9)} G_{45}}{\left[\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}^{*}\right)\right]} \quad, \quad G_{46}=\frac{\left(a_{46}\right)^{(9)} G_{45}}{\left[\left(a_{46}^{\prime}\right)^{(9)}+\left(a_{46}^{\prime \prime}\right)^{(9)}\left(T_{45}^{*}\right)\right]}$
(c) By the same argument, the equations admit solutions $G_{13}, G_{14}$ if
$\varphi(G)=\left(b_{13}^{\prime}\right)^{(1)}\left(b_{14}^{\prime}\right)^{(1)}-\left(b_{13}\right)^{(1)}\left(b_{14}\right)^{(1)}-$
$\left[\left(b_{13}^{\prime}\right)^{(1)}\left(b_{14}^{\prime}\right)^{(1)}(G)+\left(b_{14}^{\prime}\right)^{(1)}\left(b_{13}^{\prime \prime}\right)^{(1)}(G)\right]+\left(b_{13}^{\prime \prime}\right)^{(1)}(G)\left(b_{14}^{\prime \prime}\right)^{(1)}(G)=0$
Where in $G\left(G_{13}, G_{14}, G_{15}\right), G_{13}, G_{15}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{14}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{14}^{*}$ such that $\varphi\left(G^{*}\right)=0$
(d) By the same argument, the equations admit solutions $G_{16}, G_{17}$ if
$\varphi\left(G_{19}\right)=\left(b_{16}^{\prime}\right)^{(2)}\left(b_{17}^{\prime}\right)^{(2)}-\left(b_{16}\right)^{(2)}\left(b_{17}\right)^{(2)}-$
$\left[\left(b_{16}^{\prime}\right)^{(2)}\left(b_{17}^{\prime \prime}\right)^{(2)}\left(G_{19}\right)+\left(b_{17}^{\prime}\right)^{(2)}\left(b_{16}^{\prime \prime}\right)^{(2)}\left(G_{19}\right)\right]+\left(b_{16}^{\prime \prime}\right)^{(2)}\left(G_{19}\right)\left(b_{17}^{\prime \prime}\right)^{(2)}\left(G_{19}\right)=0$
Where in $\left(G_{19}\right)\left(G_{16}, G_{17}, G_{18}\right), G_{16}, G_{18}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{17}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $\mathrm{G}_{14}^{*}$ such that $\varphi\left(\left(G_{19}\right)^{*}\right)=0$
(a) By the same argument, the equations admit solutions $G_{20}, G_{21}$ if

$$
\begin{aligned}
& \varphi\left(G_{23}\right)=\left(b_{20}^{\prime}\right)^{(3)}\left(b_{21}^{\prime}\right)^{(3)}-\left(b_{20}\right)^{(3)}\left(b_{21}\right)^{(3)}- \\
& {\left[\left(b_{20}^{\prime}\right)^{(3)}\left(b_{21}^{\prime \prime}\right)^{(3)}\left(G_{23}\right)+\left(b_{21}^{\prime}\right)^{(3)}\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}\right)\right]+\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}\right)\left(b_{21}^{\prime \prime}\right)^{(3)}\left(G_{23}\right)=0}
\end{aligned}
$$

Where in $G_{23}\left(G_{20}, G_{21}, G_{22}\right), G_{20}, G_{22}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{21}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{21}^{*}$ such that $\varphi\left(\left(G_{23}\right)^{*}\right)=0$
(b) By the same argument, the equations admit solutions $G_{24}, G_{25}$ if

$$
\begin{aligned}
& \varphi\left(G_{27}\right)=\left(b_{24}^{\prime}\right)^{(4)}\left(b_{25}^{\prime}\right)^{(4)}-\left(b_{24}\right)^{(4)}\left(b_{25}\right)^{(4)}- \\
& {\left[\left(b_{24}^{\prime}\right)^{(4)}\left(b_{25}^{\prime \prime}\right)^{(4)}\left(G_{27}\right)+\left(b_{25}^{\prime}\right)^{(4)}\left(b_{24}^{\prime \prime}\right)^{(4)}\left(G_{27}\right)\right]+\left(b_{24}^{\prime \prime}\right)^{(4)}\left(G_{27}\right)\left(b_{25}^{\prime \prime}\right)^{(4)}\left(G_{27}\right)=0}
\end{aligned}
$$

Where in $\left(G_{27}\right)\left(G_{24}, G_{25}, G_{26}\right), G_{24}, G_{26}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{25}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{25}^{*}$ such that $\varphi\left(\left(G_{27}\right)^{*}\right)=0$
(c) By the same argument, the equations admit solutions $G_{28}, G_{29}$ if
$\varphi\left(G_{31}\right)=\left(b_{28}^{\prime}\right)^{(5)}\left(b_{29}^{\prime}\right)^{(5)}-\left(b_{28}\right)^{(5)}\left(b_{29}\right)^{(5)}-$
$\left[\left(b_{28}^{\prime}\right)^{(5)}\left(b_{29}^{\prime \prime}\right)^{(5)}\left(G_{31}\right)+\left(b_{29}^{\prime}\right)^{(5)}\left(b_{28}^{\prime \prime}\right)^{(5)}\left(G_{31}\right)\right]+\left(b_{28}^{\prime \prime}\right)^{(5)}\left(G_{31}\right)\left(b_{29}^{\prime \prime}\right)^{(5)}\left(G_{31}\right)=0$
Where in $\left(G_{31}\right)\left(G_{28}, G_{29}, G_{30}\right), G_{28}, G_{30}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{29}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{29}^{*}$ such that $\varphi\left(\left(G_{31}\right)^{*}\right)=0$
(d) By the same argument, the equations admit solutions $G_{32}, G_{33}$ if
$\varphi\left(G_{35}\right)=\left(b_{32}^{\prime}\right)^{(6)}\left(b_{33}^{\prime}\right)^{(6)}-\left(b_{32}\right)^{(6)}\left(b_{33}\right)^{(6)}-$
$\left[\left(b_{32}^{\prime}\right)^{(6)}\left(b_{33}^{\prime \prime}\right)^{(6)}\left(G_{35}\right)+\left(b_{33}^{\prime}\right)^{(6)}\left(b_{32}^{\prime \prime}\right)^{(6)}\left(G_{35}\right)\right]+\left(b_{32}^{\prime \prime}\right)^{(6)}\left(G_{35}\right)\left(b_{33}^{\prime \prime}\right)^{(6)}\left(G_{35}\right)=0$
Where in $\left(G_{35}\right)\left(G_{32}, G_{33}, G_{34}\right), G_{32}, G_{34}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{33}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{33}^{*}$ such that $\varphi\left(G^{*}\right)=0$
(e) By the same argument, the equations admit solutions $G_{36}, G_{37}$ if
$\varphi\left(G_{39}\right)=\left(b_{36}^{\prime}\right)^{(7)}\left(b_{37}^{\prime}\right)^{(7)}-\left(b_{36}\right)^{(7)}\left(b_{37}\right)^{(7)}-$
$\left[\left(b_{36}^{\prime}\right)^{(7)}\left(b_{37}^{\prime \prime}\right)^{(7)}\left(G_{39}\right)+\left(b_{37}^{\prime}\right)^{(7)}\left(b_{36}^{\prime \prime}\right)^{(7)}\left(G_{39}\right)\right]+\left(b_{36}^{\prime \prime}\right)^{(7)}\left(G_{39}\right)\left(b_{37}^{\prime \prime}\right)^{(7)}\left(G_{39}\right)=0$
Where in $\left(G_{39}\right)\left(G_{36}, G_{37}, G_{38}\right), G_{36}, G_{38}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{37}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{37}^{*}$ such that $\varphi\left(G^{*}\right)=0$
(f) By the same argument, the equations admit solutions $G_{40}, G_{41}$ if
$\varphi\left(G_{43}\right)=\left(b_{40}^{\prime}\right)^{(8)}\left(b_{41}^{\prime}\right)^{(8)}-\left(b_{40}\right)^{(8)}\left(b_{41}\right)^{(8)}-$
$\left[\left(b_{40}^{\prime}\right)^{(8)}\left(b_{41}^{\prime \prime}\right)^{(8)}\left(G_{43}\right)+\left(b_{41}^{\prime}\right)^{(8)}\left(b_{40}^{\prime \prime}\right)^{(8)}\left(G_{43}\right)\right]+\left(b_{40}^{\prime \prime}\right)^{(8)}\left(G_{43}\right)\left(b_{41}^{\prime \prime}\right)^{(8)}\left(G_{43}\right)=0$
Where in $\left(G_{43}\right)\left(G_{40}, G_{41}, G_{42}\right), G_{40}, G_{42}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{41}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{41}^{*}$ such that $\varphi\left(G^{*}\right)=0$
(g) By the same argument, the equations 92,93 admit solutions $G_{44}, G_{45}$ if
$\varphi\left(G_{47}\right)=\left(b_{44}^{\prime}\right)^{(9)}\left(b_{45}^{\prime}\right)^{(9)}-\left(b_{44}\right)^{(9)}\left(b_{45}\right)^{(9)}-$
$\left[\left(b_{44}^{\prime}\right)^{(9)}\left(b_{45}^{\prime \prime}\right)^{(9)}\left(G_{47}\right)+\left(b_{45}^{\prime}\right)^{(9)}\left(b_{44}^{\prime \prime}\right)^{(9)}\left(G_{47}\right)\right]+\left(b_{44}^{\prime \prime}\right)^{(9)}\left(G_{47}\right)\left(b_{45}^{\prime \prime}\right)^{(9)}\left(G_{47}\right)=0$
Where in $\left(G_{47}\right)\left(G_{44}, G_{45}, G_{46}\right), G_{44}, G_{46}$ must be replaced by their values from 96 . It is easy to see that $\varphi$ is a decreasing function in $G_{45}$ taking into account the hypothesis $\varphi(0)>0, \varphi(\infty)<0$ it follows that there exists a unique $G_{45}^{*}$ such that $\varphi\left(\left(G_{47}\right)^{*}\right)=0$
Finally we obtain the unique solution
$G_{14}^{*}$ given by $\varphi\left(G^{*}\right)=0, T_{14}^{*}$ given by $f\left(T_{14}^{*}\right)=0$ and
$G_{13}^{*}=\frac{\left(a_{13}\right)^{(1)} G_{14}^{*}}{\left[\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{13}^{\prime \prime}\right)^{(1)}\left(T_{14}^{*}\right)\right]} \quad, \quad G_{15}^{*}=\frac{\left(a_{15}\right)^{(1)} G_{14}^{*}}{\left[\left(a_{15}^{\prime}\right)^{(1)}+\left(a_{15}^{\prime \prime}\right)^{(1)}\left(T_{14}^{*}\right)\right]}$
$T_{13}^{*}=\frac{\left(b_{13}\right)^{(1)} T_{14}^{*}}{\left[\left(b_{13}^{\prime}\right)^{(1)}-\left(b_{13}^{\prime \prime}\right)^{(1)}\left(G^{*}\right)\right]} \quad, \quad T_{15}^{*}=\frac{\left(b_{15}\right)^{(1)} T_{14}^{*}}{\left[\left(b_{15}^{\prime}\right)^{(1)}-\left(b_{15}^{\prime \prime}\right)^{(1)}\left(G^{*}\right)\right]}$
Obviously, these values represent an equilibrium solution
Finally we obtain the unique solution
$\mathrm{G}_{17}^{*}$ given by $\varphi\left(\left(G_{19}\right)^{*}\right)=0, \mathrm{~T}_{17}^{*}$ given by $f\left(\mathrm{~T}_{17}^{*}\right)=0$ and
$\mathrm{G}_{16}^{*}=\frac{\left(\mathrm{a}_{16}{ }^{(2)} \mathrm{G}_{17}^{*}\right.}{\left[\left(\mathrm{a}_{16}^{\prime}\right)^{(2)}+\left(\mathrm{a}_{16}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}^{*}\right)\right]} \quad, \quad \mathrm{G}_{18}^{*}=\frac{\left(\mathrm{a}_{18}{ }^{(2)} \mathrm{G}_{17}^{*}\right.}{\left[\left(\mathrm{a}_{18}^{\prime}\right)^{(2)}+\left(\mathrm{a}_{18}^{\prime \prime}\right)^{(2)}\left(\mathrm{T}_{17}^{*}\right)\right]}$
$\mathrm{T}_{16}^{*}=\frac{\left(\mathrm{b}_{16}{ }^{(2)} \mathrm{T}_{17}^{*}\right.}{\left[\left(\mathrm{b}_{16}^{\prime}\right)^{(2)}-\left(\mathrm{b}_{16}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right)^{*}\right)\right]} \quad, \quad \mathrm{T}_{18}^{*}=\frac{\left(\mathrm{b}_{18}\right)^{(2)} \mathrm{T}_{17}^{*}}{\left[\left(\mathrm{~b}_{18}^{\prime}\right)^{(2)}-\left(\mathrm{b}_{18}^{\prime \prime}\right)^{(2)}\left(\left(G_{19}\right)^{*}\right)\right]}$
Obviously, these values represent an equilibrium solution
Finally we obtain the unique solution
$G_{21}^{*}$ given by $\varphi\left(\left(G_{23}\right)^{*}\right)=0, T_{21}^{*}$ given by $f\left(T_{21}^{*}\right)=0$ and
$G_{20}^{*}=\frac{\left(a_{20}\right)^{(3)} G_{21}^{*}}{\left[\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{20}^{\prime \prime}\right)^{(3)}\left(T_{21}^{*}\right)\right]}, \quad G_{22}^{*}=\frac{\left(a_{22}\right)^{(3)} G_{21}^{*}}{\left[\left(a_{22}^{\prime}\right)^{(3)}+\left(a_{22}^{\prime \prime}\right)^{(3)}\left(T_{21}^{*}\right)\right]}$
$T_{20}^{*}=\frac{\left(b_{20}\right)^{(3)} T_{21}^{*}}{\left[\left(b_{20}^{\prime}\right)^{(3)}-\left(b_{20}^{\prime \prime}\right)^{(3)}\left(G_{23}{ }^{*}\right)\right]} \quad, \quad T_{22}^{*}=\frac{\left(b_{22}\right)^{(3)} T_{21}^{*}}{\left[\left(b_{22}^{\prime}\right)^{(3)}-\left(b_{22}^{\prime \prime}\right)^{(3)}\left(G_{23}{ }^{*}\right)\right]}$
Obviously, these values represent an equilibrium solution of global equations
Finally we obtain the unique solution
$G_{25}^{*}$ given by $\varphi\left(G_{27}\right)=0, T_{25}^{*}$ given by $f\left(T_{25}^{*}\right)=0$ and
$G_{24}^{*}=\frac{\left(a_{24}\right)^{(4)} G_{25}^{*}}{\left.\left[\left(a_{24}^{\prime}\right)^{(4)}+\left(a_{24}^{\prime \prime}\right)\right)^{(4)}\left(T_{25}^{*}\right)\right]} \quad, \quad G_{26}^{*}=\frac{\left(a_{26}\right)^{(4)} G_{25}^{*}}{\left[\left(a_{26}^{\prime}\right)^{(4)}+\left(a_{26}^{\prime \prime}\right)^{(4)}\left(T_{25}^{*}\right)\right]}$
$T_{24}^{*}=\frac{\left(b_{24}{ }^{(4)} T_{25}^{*}\right.}{\left[\left(b_{24}^{\prime}\right)^{(4)}-\left(b_{24}^{\prime \prime}\right)^{(4)}\left(\left(G_{27}\right)^{*}\right)\right]} \quad, \quad T_{26}^{*}=\frac{\left(b_{26}\right)^{(4)} T_{2}^{*}}{\left.\left[\left(b_{26}^{\prime}\right)^{(4)}-\left(b_{26}^{\prime \prime}\right)\right)^{(4)}\left(\left(G_{27}\right)^{*}\right)\right]}$
Obviously, these values represent an equilibrium solution of global equations
Finally we obtain the unique solution
$G_{29}^{*}$ given by $\varphi\left(\left(G_{31}\right)^{*}\right)=0, T_{29}^{*}$ given by $f\left(T_{29}^{*}\right)=0$ and
$G_{28}^{*}=\frac{\left(a_{28}\right)^{(5)} G_{29}^{*}}{\left[\left(a_{28}^{\prime}\right)^{(5)}+\left(a_{28}^{\prime \prime}\right)^{(5)}\left(T_{29}^{*}\right)\right]} \quad, \quad G_{30}^{*}=\frac{\left(a_{30}\right)^{(5)} G_{29}^{*}}{\left[\left(a_{30}^{\prime}\right)^{(5)}+\left(a_{30}^{\prime \prime}\right)^{(5)}\left(T_{29}^{*}\right)\right]}$
$T_{28}^{*}=\frac{\left(b_{28}{ }^{(5)} T_{29}^{*}\right.}{\left[\left(b_{28}^{\prime}\right)^{(5)}-\left(b_{28}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right)^{*}\right)\right]} \quad, \quad T_{30}^{*}=\frac{\left(b_{30}\right)^{(5)} T_{29}^{*}}{\left[\left(b_{30}^{\prime}\right)^{(5)}-\left(b_{30}^{\prime \prime}\right)^{(5)}\left(\left(G_{31}\right)^{*}\right)\right]}$
Obviously, these values represent an equilibrium solution of global equations
Finally we obtain the unique solution
$G_{33}^{*}$ given by $\varphi\left(\left(G_{35}\right)^{*}\right)=0, T_{33}^{*}$ given by $f\left(T_{33}^{*}\right)=0$ and
$G_{32}^{*}=\frac{\left(a_{32}\right)^{(6)} G_{33}^{*}}{\left[\left(a_{32}^{\prime}\right)^{(6)}+\left(a_{32}^{\prime \prime}\right)^{(6)}\left(T_{33}^{*}\right)\right]} \quad, \quad G_{34}^{*}=\frac{\left(a_{34}\right)^{(6)} G_{33}^{*}}{\left[\left(a_{34}^{\prime}\right)^{(6)}+\left(a_{34}^{\prime \prime}\right)^{(6)}\left(T_{33}^{*}\right)\right]}$
$T_{32}^{*}=\frac{\left(b_{32}\right)^{(6)} T_{33}^{*}}{\left[\left(b_{32}^{\prime}\right)^{(6)}-\left(b_{32}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right)^{*}\right)\right]} \quad, \quad T_{34}^{*}=\frac{\left(b_{34}{ }^{(6)} T_{33}^{*}\right.}{\left[\left(b_{34}^{\prime}\right)^{(6)}-\left(b_{34}^{\prime \prime}\right)^{(6)}\left(\left(G_{35}\right)^{*}\right)\right]}$
Obviously, these values represent an equilibrium solution of global equations
Finally we obtain the unique solution
$G_{37}^{*}$ given by $\varphi\left(\left(G_{39}\right)^{*}\right)=0, T_{37}^{*}$ given by $f\left(T_{37}^{*}\right)=0$ and
$G_{36}^{*}=\frac{\left(a_{36}\right)^{(7)} G_{37}^{*}}{\left[\left(a_{36}^{\prime}\right)^{(7)}+\left(a_{36}^{\prime \prime}\right)^{(7)}\left(T_{37}^{*}\right)\right]} \quad, \quad G_{38}^{*}=\frac{\left(a_{38}\right)^{(7)} G_{37}^{*}}{\left[\left(a_{38}^{\prime}\right)^{(7)}+\left(a_{38}^{\prime \prime}\right)^{(7)}\left(T_{37}^{*}\right)\right]}$
$T_{36}^{*}=\frac{\left(b_{36}{ }^{(7)} T_{37}^{*}\right.}{\left[\left(b_{36}^{\prime}\right)^{(7)}-\left(b_{36}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right)^{*}\right)\right]} \quad, \quad T_{38}^{*}=\frac{\left(b_{38}\right)^{(7)} T_{37}^{*}}{\left[\left(b_{38}^{\prime}\right)^{(7)}-\left(b_{38}^{\prime \prime}\right)^{(7)}\left(\left(G_{39}\right)^{*}\right)\right]}$
Finally we obtain the unique solution
$G_{41}^{*}$ given by $\varphi\left(\left(G_{43}\right)^{*}\right)=0, T_{41}^{*}$ given by $f\left(T_{41}^{*}\right)=0$ and
$G_{40}^{*}=\frac{\left(a_{40}\right)^{(8)} G_{41}^{*}}{\left[\left(a_{40}^{\prime}\right)^{(8)}+\left(a_{40}^{\prime \prime}\right)^{(8)}\left(T_{41}^{*}\right)\right]} \quad, \quad G_{42}^{*}=\frac{\left(a_{42}\right)^{(8)} G_{41}^{*}}{\left[\left(a_{42}^{\prime}\right)^{(8)}+\left(a_{42}^{\prime \prime}\right)^{(8)}\left(T_{41}^{*}\right)\right]}$
$T_{40}^{*}=\frac{\left(b_{40}\right)^{(8)} T_{41}^{*}}{\left[\left(b_{40}^{\prime}\right)^{(8)}-\left(b_{40}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right)^{*}\right)\right]} \quad, \quad T_{42}^{*}=\frac{\left(b_{42}\right)^{(8)} T_{41}^{*}}{\left[\left(b_{42}^{\prime}\right)^{(8)}-\left(b_{42}^{\prime \prime}\right)^{(8)}\left(\left(G_{43}\right)^{*}\right)\right]}$
Finally we obtain the unique solution of 89 to 99
$G_{45}^{*}$ given by $\varphi\left(\left(G_{47}\right)^{*}\right)=0, T_{45}^{*}$ given by $f\left(T_{45}^{*}\right)=0$ and
$G_{44}^{*}=\frac{\left(a_{44}\right)^{(9)} G_{45}^{*}}{\left[\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{44}^{\prime \prime}\right)^{(9)}\left(T_{45}^{*}\right)\right]} \quad, \quad G_{46}^{*}=\frac{\left(a_{46}\right)^{(9)} G_{45}^{*}}{\left[\left(a_{46}^{\prime}\right)^{(9)}+\left(a_{46}^{\prime \prime}\right)^{(9)}\left(T_{45}^{*}\right)\right]}$
$T_{44}^{*}=\frac{\left(b_{44}\right)^{(9)} T_{45}^{*}}{\left[\left(b_{44}^{\prime}\right)^{(9)}-\left(b_{44}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right)^{*}\right)\right]} \quad, \quad T_{46}^{*}=\frac{\left(b_{46}\right)^{(9)} T_{45}^{*}}{\left[\left(b_{46}^{\prime}\right)^{(9)}-\left(b_{46}^{\prime \prime}\right)^{(9)}\left(\left(G_{47}\right)^{*}\right)\right]}$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 4: If the conditions of the previous theorem are satisfied and if the functions $\left(a_{i}^{\prime \prime}\right)^{(1)}$ and $\left(b_{i}^{\prime \prime}\right)^{(1)}$ Belong to $C^{(1)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.
Proof:_Denote
Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}$ :-

$$
\begin{align*}
& G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i} \\
& \frac{\partial\left(a_{14}^{\prime \prime}()^{(1)}\right.}{\partial T_{14}}\left(T_{14}^{*}\right)=\left(q_{14}\right)^{(1)}, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(1)}}{\partial G_{j}}\left(G^{*}\right)=s_{i j} \tag{525}
\end{align*}
$$

Then taking into account equations and neglecting the terms of power 2, we obtain
$\frac{d \mathbb{G}_{13}}{d t}=-\left(\left(a_{13}^{\prime}\right)^{(1)}+\left(p_{13}\right)^{(1)}\right) \mathbb{G}_{13}+\left(a_{13}\right)^{(1)} \mathbb{G}_{14}-\left(q_{13}\right)^{(1)} G_{13}^{*} \mathbb{T}_{14}$
$\frac{d \mathbb{G}_{14}}{d t}=-\left(\left(a_{14}^{\prime}\right)^{(1)}+\left(p_{14}\right)^{(1)}\right) \mathbb{G}_{14}+\left(a_{14}\right)^{(1)} \mathbb{G}_{13}-\left(q_{14}\right)^{(1)} G_{14}^{*} \mathbb{T}_{14}$
$\frac{d \mathbb{G}_{15}}{d t}=-\left(\left(a_{15}^{\prime}\right)^{(1)}+\left(p_{15}\right)^{(1)}\right) \mathbb{G}_{15}+\left(a_{15}\right)^{(1)} \mathbb{G}_{14}-\left(q_{15}\right)^{(1)} G_{15}^{*} \mathbb{T}_{14}$
$\frac{d \mathbb{T}_{13}}{d t}=-\left(\left(b_{13}^{\prime}\right)^{(1)}-\left(r_{13}\right)^{(1)}\right) \mathbb{T}_{13}+\left(b_{13}\right)^{(1)} \mathbb{T}_{14}+\sum_{j=13}^{15}\left(s_{(13)(j)} T_{13}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{14}}{d t}=-\left(\left(b_{14}^{\prime}\right)^{(1)}-\left(r_{14}\right)^{(1)}\right) \mathbb{T}_{14}+\left(b_{14}\right)^{(1)} \mathbb{T}_{13}+\sum_{j=13}^{15}\left(s_{(14)(j)} T_{14}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{15}}{d t}=-\left(\left(b_{15}^{\prime}\right)^{(1)}-\left(r_{15}\right)^{(1)}\right) \mathbb{T}_{15}+\left(b_{15}\right)^{(1)} \mathbb{T}_{14}+\sum_{j=13}^{15}\left(s_{(15)(j)} T_{15}^{*} \mathbb{G}_{j}\right)$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 4: If the conditions of the previous theorem are satisfied and if the functions $\left(\mathrm{a}_{i}^{\prime \prime}\right)^{(2)}$ and $\left(\mathrm{b}_{i}^{\prime \prime}\right)^{(2)}$ Belong to $\mathrm{C}^{(2)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable
Proof: Denote
Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}$ :-
$\mathrm{G}_{i}=\mathrm{G}_{i}^{*}+\mathbb{G}_{i} \quad, \mathrm{~T}_{i}=\mathrm{T}_{i}^{*}+\mathbb{T}_{i}$
$\frac{\partial\left(a_{17}^{\prime \prime}\right)^{(2)}}{\partial \mathrm{T}_{17}}\left(\mathrm{~T}_{17}^{*}\right)=\left(q_{17}\right)^{(2)}, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(2)}}{\partial \mathrm{G}_{j}}\left(\left(G_{19}\right)^{*}\right)=s_{i j}$
taking into account equations and neglecting the terms of power 2, we obtain
$\frac{\mathrm{d} \mathbb{G}_{16}}{\mathrm{dt}}=-\left(\left(a_{16}^{\prime}\right)^{(2)}+\left(p_{16}\right)^{(2)}\right) \mathbb{G}_{16}+\left(a_{16}\right)^{(2)} \mathbb{G}_{17}-\left(q_{16}\right)^{(2)} \mathrm{G}_{16}^{*} \mathbb{T}_{17}$
$\frac{\mathrm{d} \mathbb{G}_{17}}{\mathrm{dt}}=-\left(\left(a_{17}^{\prime}\right)^{(2)}+\left(p_{17}\right)^{(2)}\right) \mathbb{G}_{17}+\left(a_{17}\right)^{(2)} \mathbb{G}_{16}-\left(q_{17}\right)^{(2)} \mathrm{G}_{17}^{*} \mathbb{T}_{17}$
$\frac{\mathrm{d} \mathbb{G}_{18}}{\mathrm{dt}}=-\left(\left(a_{18}^{\prime}\right)^{(2)}+\left(p_{18}\right)^{(2)}\right) \mathbb{G}_{18}+\left(a_{18}\right)^{(2)} \mathbb{G}_{17}-\left(q_{18}\right)^{(2)} \mathrm{G}_{18}^{*} \mathbb{T}_{17}$
$\frac{\mathrm{d} \mathbb{T}_{16}}{\mathrm{dt}}=-\left(\left(b_{16}^{\prime}\right)^{(2)}-\left(r_{16}\right)^{(2)}\right) \mathbb{T}_{16}+\left(b_{16}\right)^{(2)} \mathbb{T}_{17}+\sum_{j=16}^{18}\left(s_{(16)(j)} \mathrm{T}_{16}^{*} \mathbb{G}_{j}\right)$
$\frac{\mathrm{d} \mathrm{T}_{17}}{\mathrm{dt}}=-\left(\left(b_{17}^{\prime}\right)^{(2)}-\left(r_{17}\right)^{(2)}\right) \mathbb{T}_{17}+\left(b_{17}\right)^{(2)} \mathbb{T}_{16}+\sum_{j=16}^{18}\left(s_{(17)(j)} \mathrm{T}_{17}^{*} \mathbb{G}_{j}\right)$
$\frac{\mathrm{d} \mathbb{T}_{18}}{\mathrm{dt}}=-\left(\left(b_{18}^{\prime}\right)^{(2)}-\left(r_{18}\right)^{(2)}\right) \mathbb{T}_{18}+\left(b_{18}\right)^{(2)} \mathbb{T}_{17}+\sum_{j=16}^{18}\left(s_{(18)(j)} \mathrm{T}_{18}^{*} \mathbb{G}_{j}\right)$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 4: If the conditions of the previous theorem are satisfied and if the functions $\left(a_{i}^{\prime \prime}\right)^{(3)}$ and $\left(b_{i}^{\prime \prime}\right)^{(3)}$ Belong to $C^{(3)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.
Proof: Denote
Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}:-$

$$
\begin{aligned}
& G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i} \\
& \frac{\partial\left(a_{21}^{\prime \prime}\right)^{(3)}}{\partial T_{21}}\left(T_{21}^{*}\right)=\left(q_{21}\right)^{(3)} \quad, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(3)}}{\partial G_{j}}\left(\left(G_{23}\right)^{*}\right)=s_{i j}
\end{aligned}
$$

Then taking into account equations and neglecting the terms of power 2, we obtain
$\frac{d \mathbb{G}_{20}}{d t}=-\left(\left(a_{20}^{\prime}\right)^{(3)}+\left(p_{20}\right)^{(3)}\right) \mathbb{G}_{20}+\left(a_{20}\right)^{(3)} \mathbb{G}_{21}-\left(q_{20}\right)^{(3)} G_{20}^{*} \mathbb{T}_{21}$
$\frac{d \mathbb{G}_{21}}{d t}=-\left(\left(a_{21}^{\prime}\right)^{(3)}+\left(p_{21}\right)^{(3)}\right) \mathbb{G}_{21}+\left(a_{21}\right)^{(3)} \mathbb{G}_{20}-\left(q_{21}\right)^{(3)} G_{21}^{*} \mathbb{T}_{21}$
$\frac{d \mathbb{G}_{22}}{d t}=-\left(\left(a_{22}^{\prime}\right)^{(3)}+\left(p_{22}\right)^{(3)}\right) \mathbb{G}_{22}+\left(a_{22}\right)^{(3)} \mathbb{G}_{21}-\left(q_{22}\right)^{(3)} G_{22}^{*} \mathbb{T}_{21}$
$\frac{d \mathbb{T}_{20}}{d t}=-\left(\left(b_{20}^{\prime}\right)^{(3)}-\left(r_{20}\right)^{(3)}\right) \mathbb{T}_{20}+\left(b_{20}\right)^{(3)} \mathbb{T}_{21}+\sum_{j=20}^{22}\left(s_{(20)(j)} T_{20}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{21}}{d t}=-\left(\left(b_{21}^{\prime}\right)^{(3)}-\left(r_{21}\right)^{(3)}\right) \mathbb{T}_{21}+\left(b_{21}\right)^{(3)} \mathbb{T}_{20}+\sum_{j=20}^{22}\left(s_{(21)(j)} T_{21}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{22}}{t}=-\left(\left(b_{22}^{\prime}\right)^{(3)}-\left(r_{22}\right)^{(3)}\right) \mathbb{T}_{22}+\left(b_{22}\right)^{(3)} \mathbb{T}_{21}+\sum_{j=20}^{22}\left(s_{(22)(j)} T_{22}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{22}}{d t}=-\left(\left(b_{22}^{\prime}\right)^{(3)}-\left(r_{22}\right)^{(3)}\right) \mathbb{T}_{22}+\left(b_{22}\right)^{(3)} \mathbb{T}_{21}+\sum_{j=20}^{22}\left(s_{(22)(j)} T_{22}^{*} \mathbb{G}_{j}\right)$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 4: If the conditions of the previous theorem are satisfied and if the functions $\left(a_{i}^{\prime \prime}\right)^{(4)}$ and $\left(b_{i}^{\prime \prime}\right)^{(4)}$ Belong to $C^{(4)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.

## Proof: Denote

Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}$ :-
$G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i}$
$\frac{\partial\left(a_{25}^{\prime \prime}\right)^{(4)}}{\partial T_{25}}\left(T_{25}^{*}\right)=\left(q_{25}\right)^{(4)}, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(4)}}{\partial G_{j}}\left(\left(G_{27}\right)^{*}\right)=s_{i j}$
Then taking into account equations and neglecting the terms of power 2, we obtain
$\frac{d \mathbb{G}_{24}}{d t}=-\left(\left(a_{24}^{\prime}\right)^{(4)}+\left(p_{24}\right)^{(4)}\right) \mathbb{G}_{24}+\left(a_{24}\right)^{(4)} \mathbb{G}_{25}-\left(q_{24}\right)^{(4)} G_{24}^{*} \mathbb{T}_{25}$
$\frac{d \mathbb{G}_{25}}{d t}=-\left(\left(a_{25}^{\prime}\right)^{(4)}+\left(p_{25}\right)^{(4)}\right) \mathbb{G}_{25}+\left(a_{25}\right)^{(4)} \mathbb{G}_{24}-\left(q_{25}\right)^{(4)} G_{25}^{*} \mathbb{T}_{25}$
$\frac{d \mathbb{G}_{26}}{d t}=-\left(\left(a_{26}^{\prime}\right)^{(4)}+\left(p_{26}\right)^{(4)}\right) \mathbb{G}_{26}+\left(a_{26}\right)^{(4)} \mathbb{G}_{25}-\left(q_{26}\right)^{(4)} G_{26}^{*} \mathbb{T}_{25}$
$\frac{d \mathbb{T}_{24}}{d t}=-\left(\left(b_{24}^{\prime}\right)^{(4)}-\left(r_{24}\right)^{(4)}\right) \mathbb{T}_{24}+\left(b_{24}\right)^{(4)} \mathbb{T}_{25}+\sum_{j=24}^{26}\left(s_{(24)(j)} T_{24}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{25}}{d t}=-\left(\left(b_{25}^{\prime}\right)^{(4)}-\left(r_{25}\right)^{(4)}\right) \mathbb{T}_{25}+\left(b_{25}\right)^{(4)} \mathbb{T}_{24}+\sum_{j=24}^{26}\left(s_{(25)(j)} T_{25}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{26}}{d t}=-\left(\left(b_{26}^{\prime}\right)^{(4)}-\left(r_{26}\right)^{(4)}\right) \mathbb{T}_{26}+\left(b_{26}\right)^{(4)} \mathbb{T}_{25}+\sum_{j=24}^{26}\left(s_{(26)(j)} T_{26}^{*} \mathbb{G}_{j}\right)$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 5: If the conditions of the previous theorem are satisfied and if the functions $\left(a_{i}^{\prime \prime}\right)^{(5)}$ and $\left(b_{i}^{\prime \prime}\right)^{(5)}$ Belong to $C^{(5)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.
Proof: Denote
Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}$ :-
$G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i}$
$\frac{\partial\left(a_{29}^{\prime \prime}\right)^{(5)}}{\partial T_{29}}\left(T_{29}^{*}\right)=\left(q_{29}\right)^{(5)} \quad, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(5)}}{\partial G_{j}}\left(\left(G_{31}\right)^{*}\right)=s_{i j}$
Then taking into account equations and neglecting the terms of power 2, we obtain
$\frac{d \mathbb{G}_{28}}{d t}=-\left(\left(a_{28}^{\prime}\right)^{(5)}+\left(p_{28}\right)^{(5)}\right) \mathbb{G}_{28}+\left(a_{28}\right)^{(5)} \mathbb{G}_{29}-\left(q_{28}\right)^{(5)} G_{28}^{*} \mathbb{T}_{29}$
$\frac{d \mathbb{G}_{29}}{d t}=-\left(\left(a_{29}^{\prime}\right)^{(5)}+\left(p_{29}\right)^{(5)}\right) \mathbb{G}_{29}+\left(a_{29}\right)^{(5)} \mathbb{G}_{28}-\left(q_{29}\right)^{(5)} G_{29}^{*} \mathbb{T}_{29}$
$\frac{d \mathbb{G}_{30}}{d t}=-\left(\left(a_{30}^{\prime}\right)^{(5)}+\left(p_{30}\right)^{(5)}\right) \mathbb{G}_{30}+\left(a_{30}\right)^{(5)} \mathbb{G}_{29}-\left(q_{30}\right)^{(5)} G_{30}^{*} \mathbb{T}_{29}$
$\frac{d \mathbb{T}_{28}}{d t}=-\left(\left(b_{28}^{\prime}\right)^{(5)}-\left(r_{28}\right)^{(5)}\right) \mathbb{T}_{28}+\left(b_{28}\right)^{(5)} \mathbb{T}_{29}+\sum_{j=28}^{30}\left(s_{(28)(j)} T_{28}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{29}}{d t}=-\left(\left(b_{29}^{\prime}\right)^{(5)}-\left(r_{29}\right)^{(5)}\right) \mathbb{T}_{29}+\left(b_{29}\right)^{(5)} \mathbb{T}_{28}+\sum_{j=28}^{30}\left(s_{(29)(j)} T_{29}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{30}}{d t}=-\left(\left(b_{30}^{\prime}\right)^{(5)}-\left(r_{30}\right)^{(5)}\right) \mathbb{T}_{30}+\left(b_{30}\right)^{(5)} \mathbb{T}_{29}+\sum_{j=28}^{30}\left(s_{(30)(j)} T_{30}^{*} \mathbb{G}_{j}\right)$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 6: If the conditions of the previous theorem are satisfied and if the functions $\left(a_{i}^{\prime \prime}\right)^{(6)}$ and $\left(b_{i}^{\prime \prime}\right)^{(6)}$ Belong to $C^{(6)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.

## Proof: Denote

Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}$ :-

$$
\begin{aligned}
& G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i} \\
& \frac{\partial\left(a_{33}^{\prime \prime}\right)^{(6)}}{\partial T_{33}}\left(T_{33}^{*}\right)=\left(q_{33}\right)^{(6)} \quad, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(6)}}{\partial G_{j}}\left(\left(G_{35}\right)^{*}\right)=s_{i j}
\end{aligned}
$$

Then taking into account equations and neglecting the terms of power 2, we obtain
$\begin{array}{lr}\frac{d \mathbb{G}_{32}}{d t}=-\left(\left(a_{32}^{\prime}\right)^{(6)}+\left(p_{32}\right)^{(6)}\right) \mathbb{G}_{32}+\left(a_{32}\right)^{(6)} \mathbb{G}_{33}-\left(q_{32}\right)^{(6)} G_{32}^{*} \mathbb{T}_{33} & 565 \\ \frac{d \mathbb{G}_{33}}{d t}=-\left(\left(a_{33}^{\prime}\right)^{(6)}+\left(p_{33}\right)^{(6)}\right) \mathbb{G}_{33}+\left(a_{33}\right)^{(6)} \mathbb{G}_{32}-\left(q_{33}\right)^{(6)} G_{33}^{*} \mathbb{T}_{33} & 566 \\ \frac{d \mathbb{G}_{34}}{d t}=-\left(\left(a_{34}^{\prime}\right)^{(6)}+\left(p_{34}\right)^{(6)}\right) \mathbb{G}_{34}+\left(a_{34}\right)^{(6)} \mathbb{G}_{33}-\left(q_{34}\right)^{(6)} G_{34}^{*} \mathbb{T}_{33} & 567 \\ \frac{d \mathbb{T}_{32}}{d t}=-\left(\left(b_{32}^{\prime}\right)^{(6)}-\left(r_{32}\right)^{(6)}\right) \mathbb{T}_{32}+\left(b_{32}\right)^{(6)} \mathbb{T}_{33}+\sum_{j=32}^{34}\left(s_{(32)(j)} T_{32}^{*} \mathbb{G}_{j}\right) & 568 \\ \frac{d \mathbb{T}_{33}}{d t}=-\left(\left(b_{33}^{\prime}\right)^{(6)}-\left(r_{33}\right)^{(6)}\right) \mathbb{T}_{33}+\left(b_{33}\right)^{(6)} \mathbb{T}_{32}+\sum_{j=32}^{34}\left(s_{(33)(j)} T_{33}^{*} \mathbb{G}_{j}\right) & 569 \\ \frac{d \mathbb{T}_{34}}{d t}=-\left(\left(b_{34}^{\prime}\right)^{(6)}-\left(r_{34}\right)^{(6)}\right) \mathbb{T}_{34}+\left(b_{34}\right)^{(6)} \mathbb{T}_{33}+\sum_{j=32}^{34}\left(s_{(34)(j)} T_{34}^{*} \mathbb{G}_{j}\right) & 570\end{array}$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 7: If the conditions of the previous theorem are satisfied and if the functions
$\left(a_{i}^{\prime \prime}\right)^{(7)}$ and $\left(b_{i}^{\prime \prime}\right)^{(7)}$ Belong to $C^{(7)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.
Proof: Denote

## Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}:-$

$$
\begin{aligned}
& G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i} \\
& \frac{\partial\left(a_{37}^{\prime \prime}\right)^{(7)}}{\partial T_{37}}\left(T_{37}^{*}\right)=\left(q_{37}\right)^{(7)}, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(7)}}{\partial G_{j}}\left(\left(G_{39}\right)^{* *}\right)=s_{i j}
\end{aligned}
$$

Then taking into account equations and neglecting the terms of power 2, we obtain from
$\frac{d \mathbb{G}_{36}}{d t}=-\left(\left(a_{36}^{\prime}\right)^{(7)}+\left(p_{36}\right)^{(7)}\right) \mathbb{G}_{36}+\left(a_{36}\right)^{(7)} \mathbb{G}_{37}-\left(q_{36}\right)^{(7)} G_{36}^{*} \mathbb{T}_{37}$
$\frac{d \mathbb{G}_{37}}{d t}=-\left(\left(a_{37}^{\prime}\right)^{(7)}+\left(p_{37}\right)^{(7)}\right) \mathbb{G}_{37}+\left(a_{37}\right)^{(7)} \mathbb{G}_{36}-\left(q_{37}\right)^{(7)} G_{37}^{*} \mathbb{T}_{37}$
$\frac{d \mathbb{G}_{38}}{d t}=-\left(\left(a_{38}^{\prime}\right)^{(7)}+\left(p_{38}\right)^{(7)}\right) \mathbb{G}_{38}+\left(a_{38}\right)^{(7)} \mathbb{G}_{37}-\left(q_{38}\right)^{(7)} G_{38}^{*} \mathbb{T}_{37}$
$\frac{d \mathbb{T}_{36}}{d t}=-\left(\left(b_{36}^{\prime}\right)^{(7)}-\left(r_{36}\right)^{(7)}\right) \mathbb{T}_{36}+\left(b_{36}\right)^{(7)} \mathbb{T}_{37}+\sum_{j=36}^{38}\left(s_{(36)(j)} T_{36}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{37}}{d t}=-\left(\left(b_{37}^{\prime}\right)^{(7)}-\left(r_{37}\right)^{(7)}\right) \mathbb{T}_{37}+\left(b_{37}\right)^{(7)} \mathbb{T}_{36}+\sum_{j=36}^{38}\left(s_{(37)(j)} T_{37}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{38}}{d t}=-\left(\left(b_{38}^{\prime}\right)^{(7)}-\left(r_{38}\right)^{(7)}\right) \mathbb{T}_{38}+\left(b_{38}\right)^{(7)} \mathbb{T}_{37}+\sum_{j=36}^{38}\left(s_{(38)(j)} T_{38}^{*} \mathbb{G}_{j}\right)$
Obviously, these values represent an equilibrium solution

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 8: If the conditions of the previous theorem are satisfied and if the functions $\left(a_{i}^{\prime \prime}\right)^{(8)}$ and $\left(b_{i}^{\prime \prime}\right)^{(8)}$ Belong to $C^{(8)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.

Proof: Denote
Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}:-$

$$
\begin{aligned}
& G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i} \\
& \frac{\partial\left(a_{41}^{\prime \prime}\right)^{(8)}}{\partial T_{41}}\left(T_{41}^{*}\right)=\left(q_{41}\right)^{(8)}, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(8)}}{\partial G_{j}}\left(\left(G_{43}\right)^{*}\right)=s_{i j}
\end{aligned}
$$

Then taking into account equations and neglecting the terms of power 2, we obtain
$\frac{d \mathbb{G}_{40}}{d t}=-\left(\left(a_{40}^{\prime}\right)^{(8)}+\left(p_{40}\right)^{(8)}\right) \mathbb{G}_{40}+\left(a_{40}\right)^{(8)} \mathbb{G}_{41}-\left(q_{40}\right)^{(8)} G_{40}^{*} \mathbb{T}_{41}$
$\frac{d \mathbb{G}_{41}}{d t}=-\left(\left(a_{41}^{\prime}\right)^{(8)}+\left(p_{41}\right)^{(8)}\right) \mathbb{G}_{41}+\left(a_{41}\right)^{(8)} \mathbb{G}_{40}-\left(q_{41}\right)^{(8)} G_{41}^{*} \mathbb{T}_{41}$
$\frac{d \mathbb{G}_{42}}{d t}=-\left(\left(a_{42}^{\prime}\right)^{(8)}+\left(p_{42}\right)^{(8)}\right) \mathbb{G}_{42}+\left(a_{42}\right)^{(8)} \mathbb{G}_{41}-\left(q_{42}\right)^{(8)} G_{42}^{*} \mathbb{T}_{41}$
$\frac{d \mathbb{T}_{40}}{d t}=-\left(\left(b_{40}^{\prime}\right)^{(8)}-\left(r_{40}\right)^{(8)}\right) \mathbb{T}_{40}+\left(b_{40}\right)^{(8)} \mathbb{T}_{41}+\sum_{j=40}^{42}\left(s_{(40)(j)} T_{40}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{41}}{d t}=-\left(\left(b_{41}^{\prime}\right)^{(8)}-\left(r_{41}\right)^{(8)}\right) \mathbb{T}_{41}+\left(b_{41}\right)^{(8)} \mathbb{T}_{40}+\sum_{j=40}^{42}\left(s_{(41)(j)} T_{41}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{42}}{d t}=-\left(\left(b_{42}^{\prime}\right)^{(8)}-\left(r_{42}\right)^{(8)}\right) \mathbb{T}_{42}+\left(b_{42}\right)^{(8)} \mathbb{T}_{41}+\sum_{j=40}^{42}\left(s_{(42)(j)} T_{42}^{*} \mathbb{G}_{j}\right)$

## ASYMPTOTIC STABILITY ANALYSIS

Theorem 9: If the conditions of the previous theorem are satisfied and if the functions $\left(a_{i}^{\prime \prime}\right)^{(9)}$ and $\left(b_{i}^{\prime \prime}\right)^{(9)}$ Belong to $C^{(9)}\left(\mathbb{R}_{+}\right)$then the above equilibrium point is asymptotically stable.

Proof: Denote
Definition of $\mathbb{G}_{i}, \mathbb{T}_{i}:-$

$$
\begin{aligned}
& G_{i}=G_{i}^{*}+\mathbb{G}_{i} \quad, T_{i}=T_{i}^{*}+\mathbb{T}_{i} \\
& \frac{\partial\left(a_{45}^{\prime \prime}\right)^{(9)}}{\partial T_{45}}\left(T_{45}^{*}\right)=\left(q_{45}\right)^{(9)} \quad, \frac{\partial\left(b_{i}^{\prime \prime}\right)^{(9)}}{\partial G_{j}}\left(\left(G_{47}\right)^{*}\right)=s_{i j}
\end{aligned}
$$

Then taking into account equations 89 to 99 and neglecting the terms of power 2, we obtain from 99 to 44
$\frac{d \mathbb{G}_{44}}{d t}=-\left(\left(a_{44}^{\prime}\right)^{(9)}+\left(p_{44}\right)^{(9)}\right) \mathbb{G}_{44}+\left(a_{44}\right)^{(9)} \mathbb{G}_{45}-\left(q_{44}\right)^{(9)} G_{44}^{*} \mathbb{T}_{45}$
$\frac{d \mathbb{G}_{45}}{d t}=-\left(\left(a_{45}^{\prime}\right)^{(9)}+\left(p_{45}\right)^{(9)}\right) \mathbb{G}_{45}+\left(a_{45}\right)^{(9)} \mathbb{G}_{44}-\left(q_{45}\right)^{(9)} G_{45}^{*} \mathbb{T}_{45}$
$\frac{d \mathbb{G}_{46}}{d t}=-\left(\left(a_{46}^{\prime}\right)^{(9)}+\left(p_{46}\right)^{(9)}\right) \mathbb{G}_{46}+\left(a_{46}\right)^{(9)} \mathbb{G}_{45}-\left(q_{46}\right)^{(9)} G_{46}^{*} \mathbb{T}_{45}$
$\frac{d \mathbb{T}_{44}}{d t}=-\left(\left(b_{44}^{\prime}\right)^{(9)}-\left(r_{44}\right)^{(9)}\right) \mathbb{T}_{44}+\left(b_{44}\right)^{(9)} \mathbb{T}_{45}+\sum_{j=44}^{46}\left(s_{(44)(j)} T_{44}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{45}}{d t}=-\left(\left(b_{45}^{\prime}\right)^{(9)}-\left(r_{45}\right)^{(9)}\right) \mathbb{T}_{45}+\left(b_{45}\right)^{(9)} \mathbb{T}_{44}+\sum_{j=44}^{46}\left(s_{(45)(j)} T_{45}^{*} \mathbb{G}_{j}\right)$
$\frac{d \mathbb{T}_{46}}{d t}=-\left(\left(b_{46}^{\prime}\right)^{(9)}-\left(r_{46}\right)^{(9)}\right) \mathbb{T}_{46}+\left(b_{46}\right)^{(9)} \mathbb{T}_{45}+\sum_{j=44}^{46}\left(s_{(46)(j)} T_{46}^{*} \mathbb{G}_{j}\right)$

## The characteristic equation of this system is

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$\left((\lambda)^{(1)}+\left(b_{15}^{\prime}\right)^{(1)}-\left(r_{15}\right)^{(1)}\right)\left\{\left((\lambda)^{(1)}+\left(a_{15}^{\prime}\right)^{(1)}+\left(p_{15}\right)^{(1)}\right)\right.$
$\left[\left(\left((\lambda)^{(1)}+\left(a_{13}^{\prime}\right)^{(1)}+\left(p_{13}\right)^{(1)}\right)\left(q_{14}\right)^{(1)} G_{14}^{*}+\left(a_{14}\right)^{(1)}\left(q_{13}\right)^{(1)} G_{13}^{*}\right)\right]$
$\left(\left((\lambda)^{(1)}+\left(b_{13}^{\prime}\right)^{(1)}-\left(r_{13}\right)^{(1)}\right) s_{(14),(14)} T_{14}^{*}+\left(b_{14}\right)^{(1)} s_{(13),(14)} T_{14}^{*}\right)$
$+\left(\left((\lambda)^{(1)}+\left(a_{14}^{\prime}\right)^{(1)}+\left(p_{14}\right)^{(1)}\right)\left(q_{13}\right)^{(1)} G_{13}^{*}+\left(a_{13}\right)^{(1)}\left(q_{14}\right)^{(1)} G_{14}^{*}\right)$
$\left(\left((\lambda)^{(1)}+\left(b_{13}^{\prime}\right)^{(1)}-\left(r_{13}\right)^{(1)}\right) s_{(14),(13)} T_{14}^{*}+\left(b_{14}\right)^{(1)} s_{(13),(13)} T_{13}^{*}\right)$
$\left(\left((\lambda)^{(1)}\right)^{2}+\left(\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{14}^{\prime}\right)^{(1)}+\left(p_{13}\right)^{(1)}+\left(p_{14}\right)^{(1)}\right)(\lambda)^{(1)}\right)$
$\left(\left((\lambda)^{(1)}\right)^{2}+\left(\left(b_{13}^{\prime}\right)^{(1)}+\left(b_{14}^{\prime}\right)^{(1)}-\left(r_{13}\right)^{(1)}+\left(r_{14}\right)^{(1)}\right)(\lambda)^{(1)}\right)$
$+\left(\left((\lambda)^{(1)}\right)^{2}+\left(\left(a_{13}^{\prime}\right)^{(1)}+\left(a_{14}^{\prime}\right)^{(1)}+\left(p_{13}\right)^{(1)}+\left(p_{14}\right)^{(1)}\right)(\lambda)^{(1)}\right)\left(q_{15}\right)^{(1)} G_{15}$
$+\left((\lambda)^{(1)}+\left(a_{13}^{\prime}\right)^{(1)}+\left(p_{13}\right)^{(1)}\right)\left(\left(a_{15}\right)^{(1)}\left(q_{14}\right)^{(1)} G_{14}^{*}+\left(a_{14}\right)^{(1)}\left(a_{15}\right)^{(1)}\left(q_{13}\right)^{(1)} G_{13}^{*}\right)$
$\left.\left(\left((\lambda)^{(1)}+\left(b_{13}^{\prime}\right)^{(1)}-\left(r_{13}\right)^{(1)}\right) s_{(14),(15)} T_{14}^{*}+\left(b_{14}\right)^{(1)} s_{(13),(15)} T_{13}^{*}\right)\right\}=0$
$+$
$\left((\lambda)^{(2)}+\left(b_{18}^{\prime}\right)^{(2)}-\left(r_{18}\right)^{(2)}\right)\left\{\left((\lambda)^{(2)}+\left(a_{18}^{\prime}\right)^{(2)}+\left(p_{18}\right)^{(2)}\right)\right.$
$\left[\left(\left((\lambda)^{(2)}+\left(a_{16}^{\prime}\right)^{(2)}+\left(p_{16}\right)^{(2)}\right)\left(q_{17}\right)^{(2)} \mathrm{G}_{17}^{*}+\left(a_{17}\right)^{(2)}\left(q_{16}\right)^{(2)} \mathrm{G}_{16}^{*}\right)\right]$
$\left(\left((\lambda)^{(2)}+\left(b_{16}^{\prime}\right)^{(2)}-\left(r_{16}\right)^{(2)}\right) s_{(17),(17)} \mathrm{T}_{17}^{*}+\left(b_{17}\right)^{(2)} s_{(16),(17)} \mathrm{T}_{17}^{*}\right)$

$$
\begin{aligned}
& +\left(\left((\lambda)^{(2)}+\left(a_{17}^{\prime}\right)^{(2)}+\left(p_{17}\right)^{(2)}\right)\left(q_{16}\right)^{(2)} \mathrm{G}_{16}^{*}+\left(a_{16}\right)^{(2)}\left(q_{17}\right)^{(2)} \mathrm{G}_{17}^{*}\right) \\
& \left.\left(\left((\lambda)^{(2)}+\left(b_{16}^{\prime}\right)\right)^{(2)}-\left(r_{16}\right)^{(2)}\right) s_{(17),(16)} \mathrm{T}_{17}^{*}+\left(b_{17}\right)^{(2)} s_{(16),(16)} \mathrm{T}_{16}^{*}\right) \\
& \left(\left((\lambda)^{(2)}\right)^{2}+\left(\left(a_{16}^{\prime}\right)^{(2)}+\left(a_{17}^{\prime}\right)^{(2)}+\left(p_{16}\right)^{(2)}+\left(p_{17}\right)^{(2)}\right)(\lambda)^{(2)}\right) \\
& \left(\left((\lambda)^{(2)}\right)^{2}+\left(\left(b_{16}^{\prime}\right)^{(2)}+\left(b_{17}^{\prime}\right)^{(2)}-\left(r_{16}\right)^{(2)}+\left(r_{17}\right)^{(2)}\right)(\lambda)^{(2)}\right) \\
& +\left(\left((\lambda)^{(2)}\right)^{2}+\left(\left(a_{16}^{\prime}\right)^{(2)}+\left(a_{17}^{\prime}\right)^{(2)}+\left(p_{16}\right)^{(2)}+\left(p_{17}\right)^{(2)}\right)(\lambda)^{(2)}\right)\left(q_{18}\right)^{(2)} \mathrm{G}_{18} \\
& +\left((\lambda)^{(2)}+\left(a_{16}^{\prime}\right)^{(2)}+\left(p_{16}\right)^{(2)}\right)\left(\left(a_{18}\right)^{(2)}\left(q_{17}\right)^{(2)} \mathrm{G}_{17}^{*}+\left(a_{17}\right)^{(2)}\left(a_{18}\right)^{(2)}\left(q_{16}\right)^{(2)} \mathrm{G}_{16}^{*}\right) \\
& \left.\left(\left((\lambda)^{(2)}+\left(b_{16}^{\prime}\right)^{(2)}-\left(r_{16}\right)^{(2)}\right) s_{(17),(18)} \mathrm{T}_{17}^{*}+\left(b_{17}\right)^{(2)} s_{(16),(18))_{16}^{*}}\right)\right\}=0 \\
& \stackrel{+}{\left((\lambda)^{(3)}+\left(b_{22}^{\prime}\right)^{(3)}-\left(r_{22}\right)^{(3)}\right)\left\{\left((\lambda)^{(3)}+\left(a_{22}^{\prime}\right)^{(3)}+\left(p_{22}\right)^{(3)}\right), ~\right.} \\
& {\left[\left(\left((\lambda)^{(3)}+\left(a_{20}^{\prime}\right)^{(3)}+\left(p_{20}\right)^{(3)}\right)\left(q_{21}\right)^{(3)} G_{21}^{*}+\left(a_{21}\right)^{(3)}\left(q_{20}\right)^{(3)} G_{20}^{*}\right)\right]} \\
& \left(\left((\lambda)^{(3)}+\left(b_{20}^{\prime}\right)^{(3)}-\left(r_{20}\right)^{(3)}\right) s_{(21),(21)} T_{21}^{*}+\left(b_{21}\right)^{(3)} s_{(20),(21)} T_{21}^{*}\right) \\
& +\left(\left((\lambda)^{(3)}+\left(a_{21}^{\prime}\right)^{(3)}+\left(p_{21}\right)^{(3)}\right)\left(q_{20}\right)^{(3)} G_{20}^{*}+\left(a_{20}\right)^{(3)}\left(q_{21}\right)^{(1)} G_{21}^{*}\right) \\
& \left(\left((\lambda)^{(3)}+\left(b_{20}^{\prime}\right)^{(3)}-\left(r_{20}\right)^{(3)}\right) s_{(21),(20)} T_{21}^{*}+\left(b_{21}\right)^{(3)} s_{(20),(20)} T_{20}^{*}\right) \\
& \left(\left((\lambda)^{(3)}\right)^{2}+\left(\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{21}^{\prime}\right)^{(3)}+\left(p_{20}\right)^{(3)}+\left(p_{21}\right)^{(3)}\right)(\lambda)^{(3)}\right) \\
& \left(\left((\lambda)^{(3)}\right)^{2}+\left(\left(b_{20}^{\prime}\right)^{(3)}+\left(b_{21}^{\prime}\right)^{(3)}-\left(r_{20}\right)^{(3)}+\left(r_{21}\right)^{(3)}\right)(\lambda)^{(3)}\right) \\
& +\left(\left((\lambda)^{(3)}\right)^{2}+\left(\left(a_{20}^{\prime}\right)^{(3)}+\left(a_{21}^{\prime}\right)^{(3)}+\left(p_{20}\right)^{(3)}+\left(p_{21}\right)^{(3)}\right)(\lambda)^{(3)}\right)\left(q_{22}\right)^{(3)} G_{22} \\
& +\left((\lambda)^{(3)}+\left(a_{20}^{\prime}\right)^{(3)}+\left(p_{20}\right)^{(3)}\right)\left(\left(a_{22}\right)^{(3)}\left(q_{21}\right)^{(3)} G_{21}^{*}+\left(a_{21}\right)^{(3)}\left(a_{22}\right)^{(3)}\left(q_{20}\right)^{(3)} G_{20}^{*}\right) \\
& \left.\left(\left((\lambda)^{(3)}+\left(b_{20}^{\prime}\right)^{(3)}-\left(r_{20}\right)^{(3)}\right) s_{(21),(22)} T_{21}^{*}+\left(b_{21}\right)^{(3)} s_{(20),(22)} T_{20}^{*}\right)\right\}=0 \\
& + \\
& \left((\lambda)^{(4)}+\left(b_{26}^{\prime}\right)^{(4)}-\left(r_{26}\right)^{(4)}\right)\left\{\left((\lambda)^{(4)}+\left(a_{26}^{\prime}\right)^{(4)}+\left(p_{26}\right)^{(4)}\right)\right. \\
& {\left[\left(\left((\lambda)^{(4)}+\left(a_{24}^{\prime}\right)^{(4)}+\left(p_{24}\right)^{(4)}\right)\left(q_{25}\right)^{(4)} G_{25}^{*}+\left(a_{25}\right)^{(4)}\left(q_{24}\right)^{(4)} G_{24}^{*}\right)\right]} \\
& \left(\left((\lambda)^{(4)}+\left(b_{24}^{\prime}\right)^{(4)}-\left(r_{24}\right)^{(4)}\right) s_{(25),(25)} T_{25}^{*}+\left(b_{25}\right)^{(4)} s_{(24),(25)} T_{25}^{*}\right) \\
& +\left(\left((\lambda)^{(4)}+\left(a_{25}^{\prime}\right)^{(4)}+\left(p_{25}\right)^{(4)}\right)\left(q_{24}\right)^{(4)} G_{24}^{*}+\left(a_{24}\right)^{(4)}\left(q_{25}\right)^{(4)} G_{25}^{*}\right) \\
& \left(\left((\lambda)^{(4)}+\left(b_{24}^{\prime}\right)^{(4)}-\left(r_{24}\right)^{(4)}\right) s_{(25),(24)} T_{25}^{*}+\left(b_{25}\right)^{(4)} s_{(24),(24)} T_{24}^{*}\right) \\
& \left(\left((\lambda)^{(4)}\right)^{2}+\left(\left(a_{24}^{\prime}\right)^{(4)}+\left(a_{25}^{\prime}\right)^{(4)}+\left(p_{24}\right)^{(4)}+\left(p_{25}\right)^{(4)}\right)(\lambda)^{(4)}\right) \\
& \left(\left((\lambda)^{(4)}\right)^{2}+\left(\left(b_{24}^{\prime}\right)^{(4)}+\left(b_{25}^{\prime}\right)^{(4)}-\left(r_{24}\right)^{(4)}+\left(r_{25}\right)^{(4)}\right)(\lambda)^{(4)}\right) \\
& +\left(\left((\lambda)^{(4)}\right)^{2}+\left(\left(a_{24}^{\prime}\right)^{(4)}+\left(a_{25}^{\prime}\right)^{(4)}+\left(p_{24}\right)^{(4)}+\left(p_{25}\right)^{(4)}\right)(\lambda)^{(4)}\right)\left(q_{26}\right)^{(4)} G_{26} \\
& +\left((\lambda)^{(4)}+\left(a_{24}^{\prime}\right)^{(4)}+\left(p_{24}\right)^{(4)}\right)\left(\left(a_{26}\right)^{(4)}\left(q_{25}\right)^{(4)} G_{25}^{*}+\left(a_{25}\right)^{(4)}\left(a_{26}\right)^{(4)}\left(q_{24}\right)^{(4)} G_{24}^{*}\right) \\
& \left.\left(\left((\lambda)^{(4)}+\left(b_{24}^{\prime}\right)^{(4)}-\left(r_{24}\right)^{(4)}\right) s_{(25),(26)} T_{25}^{*}+\left(b_{25}\right)^{(4)} s_{(24),(26)} T_{24}^{*}\right)\right\}=0 \\
& + \\
& \begin{array}{l}
\left((\lambda)^{(5)}+\left(b_{30}^{\prime}\right)^{(5)}-\left(r_{30}\right)^{(5)}\right)\left\{\left((\lambda)^{(5)}+\left(a_{30}^{\prime}\right)^{(5)}+\left(p_{30}\right)^{(5)}\right)\right. \\
{\left[\left(\left((\lambda)^{(5)}+\left(a_{28}^{\prime}\right)^{(5)}+\left(p_{28}\right)^{(5)}\right)\left(q_{29}\right)^{(5)} G_{29}^{*}+\left(a_{29}\right)^{(5)}\left(q_{28}\right)^{(5)} G_{28}^{*}\right)\right]} \\
\left(\left((\lambda)^{(5)}+\left(b_{28}^{\prime}\right)^{(5)}-\left(r_{28}\right)^{(5)}\right) s_{(29),(299} T_{29}^{*}+\left(b_{29}\right)^{(5)} s_{(28),(29} T_{29}^{*}\right) \\
+\left(\left((\lambda)^{(5)}+\left(a_{29}^{\prime}\right)^{(5)}+\left(p_{29}\right)^{(5)}\right)\left(q_{28}\right)^{(5)} G_{28}^{*}+\left(a_{28}\right)^{(5)}\left(q_{29}\right)^{(5)} G_{29}^{*}\right) \\
\quad\left(\left((\lambda)^{(5)}+\left(b_{28}^{\prime}\right)^{(5)}-\left(r_{28}\right)^{(5)}\right) s_{(29),(28)} T_{29}^{*}+\left(b_{29}\right)^{(5)} s_{(28),(28)} T_{28}^{*}\right) \\
\left(\left((\lambda)^{(5)}\right)^{2}+\left(\left(a_{28}^{\prime}\right)^{(5)}+\left(a_{29}^{\prime}{ }^{(5)}+\left(p_{28}\right)^{(5)}+\left(p_{29}\right)^{(5)}\right)(\lambda)^{(5)}\right)\right. \\
\left(\left((\lambda)^{(5)}\right)^{2}+\left(\left(b_{28}^{\prime}\right)^{(5)}+\left(b_{29}^{\prime}\right)^{(5)}-\left(r_{28}\right)^{(5)}+\left(r_{29}\right)^{(5)}\right)(\lambda)^{(5)}\right) \\
+\left(\left((\lambda)^{(5)}\right)^{2}+\left(\left(a_{28}^{\prime}\right)^{(5)}+\left(a_{99}^{\prime}\right)^{(5)}+\left(p_{28}^{(5)}+\left(p_{29}\right)^{(5)}\right)(\lambda)^{(5)}\right)\left(q_{30}\right)^{(5)} G_{30}\right. \\
+\left((\lambda)^{(5)}+\left(a_{28}^{\prime}\right)^{(5)}+\left(p_{28}\right)^{(5)}\right)\left(\left(a_{30}\right)^{(5)}\left(q_{29}\right)^{(5)} G_{29}^{*}+\left(a_{29}\right)^{(5)}\left(a_{30}\right)^{(5)}\left(q_{28}\right)^{(5)} G_{28}^{*}\right)
\end{array}
\end{aligned}
$$

$\left.\left(\left((\lambda)^{(5)}+\left(b_{28}^{\prime}\right)^{(5)}-\left(r_{28}\right)^{(5)}\right) s_{(29),(30)} T_{29}^{*}+\left(b_{29}\right)^{(5)} s_{(28),(30)} T_{28}^{*}\right)\right\}=0$
$\left((\lambda)^{(6)}+\left(b_{34}^{\prime}\right)^{(6)}-\left(r_{34}\right)^{(6)}\right)\left\{\left((\lambda)^{(6)}+\left(a_{34}^{\prime}\right)^{(6)}+\left(p_{34}\right)^{(6)}\right)\right.$
$\left[\left(\left((\lambda)^{(6)}+\left(a_{32}^{\prime}\right)^{(6)}+\left(p_{32}\right)^{(6)}\right)\left(q_{33}\right)^{(6)} G_{33}^{*}+\left(a_{33}\right)^{(6)}\left(q_{32}\right)^{(6)} G_{32}^{*}\right)\right]$
$\left(\left((\lambda)^{(6)}+\left(b_{32}^{\prime}\right)^{(6)}-\left(r_{32}\right)^{(6)}\right) s_{(33),(33)} T_{33}^{*}+\left(b_{33}\right)^{(6)} s_{(32),(33)} T_{33}^{*}\right)$
$+\left(\left((\lambda)^{(6)}+\left(a_{33}^{\prime}\right)^{(6)}+\left(p_{33}\right)^{(6)}\right)\left(q_{32}\right)^{(6)} G_{32}^{*}+\left(a_{32}\right)^{(6)}\left(q_{33}\right)^{(6)} G_{33}^{*}\right)$
$\left(\left((\lambda)^{(6)}+\left(b_{32}^{\prime}\right)^{(6)}-\left(r_{32}\right)^{(6)}\right) s_{(33),(32)} T_{33}^{*}+\left(b_{33}\right)^{(6)} s_{(32),(32)} T_{32}^{*}\right)$
$\left(\left((\lambda)^{(6)}\right)^{2}+\left(\left(a_{32}^{\prime}\right)^{(6)}+\left(a_{33}^{\prime}\right)^{(6)}+\left(p_{32}\right)^{(6)}+\left(p_{33}\right)^{(6)}\right)(\lambda)^{(6)}\right)$

$$
\left(\left((\lambda)^{(6)}\right)^{2}+\left(\left(b_{32}^{\prime}\right)^{(6)}+\left(b_{33}^{\prime}\right)^{(6)}-\left(r_{32}\right)^{(6)}+\left(r_{33}\right)^{(6)}\right)(\lambda)^{(6)}\right)
$$

$$
+\left(\left((\lambda)^{(6)}\right)^{2}+\left(\left(a_{32}^{\prime}\right)^{(6)}+\left(a_{33}^{\prime}\right)^{(6)}+\left(p_{32}\right)^{(6)}+\left(p_{33}\right)^{(6)}\right)(\lambda)^{(6)}\right)\left(q_{34}\right)^{(6)} G_{34}
$$

$$
+\left((\lambda)^{(6)}+\left(a_{32}^{\prime}\right)^{(6)}+\left(p_{32}\right)^{(6)}\right)\left(\left(a_{34}\right)^{(6)}\left(q_{33}\right)^{(6)} G_{33}^{*}+\left(a_{33}\right)^{(6)}\left(a_{34}\right)^{(6)}\left(q_{32}\right)^{(6)} G_{32}^{*}\right)
$$

$$
\left.\left(\left((\lambda)^{(6)}+\left(b_{32}^{\prime}\right)^{(6)}-\left(r_{32}\right)^{(6)}\right) s_{(33),(34)} T_{33}^{*}+\left(b_{33}\right)^{(6)} s_{(32),(34)} T_{32}^{*}\right)\right\}=0
$$

+ 

$$
\left((\lambda)^{(7)}+\left(b_{38}^{\prime}\right)^{(7)}-\left(r_{38}\right)^{(7)}\right)\left\{\left((\lambda)^{(7)}+\left(a_{38}^{\prime}\right)^{(7)}+\left(p_{38}\right)^{(7)}\right)\right.
$$

$$
\left[\left(\left((\lambda)^{(7)}+\left(a_{36}^{\prime}\right)^{(7)}+\left(p_{36}\right)^{(7)}\right)\left(q_{37}\right)^{(7)} G_{37}^{*}+\left(a_{37}\right)^{(7)}\left(q_{36}\right)^{(7)} G_{36}^{*}\right)\right]
$$

$$
\left(\left((\lambda)^{(7)}+\left(b_{36}^{\prime}\right)^{(7)}-\left(r_{36}\right)^{(7)}\right) s_{(37),(37)} T_{37}^{*}+\left(b_{37}\right)^{(7)} s_{(36),(37)} T_{37}^{*}\right)
$$

$$
+\left(\left((\lambda)^{(7)}+\left(a_{37}^{\prime}\right)^{(7)}+\left(p_{37}\right)^{(7)}\right)\left(q_{36}\right)^{(7)} G_{36}^{*}+\left(a_{36}\right)^{(7)}\left(q_{37}\right)^{(7)} G_{37}^{*}\right)
$$

$$
\left(\left((\lambda)^{(7)}+\left(b_{36}^{\prime}\right)^{(7)}-\left(r_{36}\right)^{(7)}\right) s_{(37),(36)} T_{37}^{*}+\left(b_{37}\right)^{(7)} s_{(36),(36)} T_{36}^{*}\right)
$$

$$
\left(\left((\lambda)^{(7)}\right)^{2}+\left(\left(a_{36}^{\prime}\right)^{(7)}+\left(a_{37}^{\prime}\right)^{(7)}+\left(p_{36}\right)^{(7)}+\left(p_{37}\right)^{(7)}\right)(\lambda)^{(7)}\right)
$$

$$
\left(\left((\lambda)^{(7)}\right)^{2}+\left(\left(b_{36}^{\prime}\right)^{(7)}+\left(b_{37}^{\prime}\right)^{(7)}-\left(r_{36}\right)^{(7)}+\left(r_{37}\right)^{(7)}\right)(\lambda)^{(7)}\right)
$$

$$
+\left(\left((\lambda)^{(7)}\right)^{2}+\left(\left(a_{36}^{\prime}\right)^{(7)}+\left(a_{37}^{\prime}\right)^{(7)}+\left(p_{36}\right)^{(7)}+\left(p_{37}\right)^{(7)}\right)(\lambda)^{(7)}\right)\left(q_{38}\right)^{(7)} G_{38}
$$

$$
+\left((\lambda)^{(7)}+\left(a_{36}^{\prime}\right)^{(7)}+\left(p_{36}\right)^{(7)}\right)\left(\left(a_{38}\right)^{(7)}\left(q_{37}\right)^{(7)} G_{37}^{*}+\left(a_{37}\right)^{(7)}\left(a_{38}\right)^{(7)}\left(q_{36}\right)^{(7)} G_{36}^{*}\right)
$$

$$
\left.\left(\left((\lambda)^{(7)}+\left(b_{36}^{\prime}\right)^{(7)}-\left(r_{36}\right)^{(7)}\right) s_{(37),(38)} T_{37}^{*}+\left(b_{37}\right)^{(7)} s_{(36),(38)} T_{36}^{*}\right)\right\}=0
$$

$$
\begin{aligned}
& + \\
& \left((\lambda)^{(8)}+\left(b_{42}^{\prime}\right)^{(8)}-\left(r_{42}\right)^{(8)}\right)\left\{\left((\lambda)^{(8)}+\left(a_{42}^{\prime}\right)^{(8)}+\left(p_{42}\right)^{(8)}\right)\right. \\
& {\left[\left(\left((\lambda)^{(8)}+\left(a_{40}^{\prime}\right)^{(8)}+\left(p_{40}\right)^{(8)}\right)\left(q_{41}\right)^{(8)} G_{41}^{*}+\left(a_{41}\right)^{(8)}\left(q_{40}\right)^{(8)} G_{40}^{*}\right)\right]} \\
& \left(\left((\lambda)^{(8)}+\left(b_{40}^{\prime}\right)^{(8)}-\left(r_{40}\right)^{(8)}\right) s_{(41),(41)} T_{41}^{*}+\left(b_{41}\right)^{(8)} s_{(40),(41)} T_{41}^{*}\right) \\
& +\left(\left((\lambda)^{(8)}+\left(a_{41}^{\prime}\right)^{(8)}+\left(p_{41}\right)^{(8)}\right)\left(q_{40}\right)^{(8)} G_{40}^{*}+\left(a_{40}\right)^{(8)}\left(q_{41}\right)^{(8)} G_{41}^{*}\right) \\
& \left(\left((\lambda)^{(8)}+\left(b_{40}^{\prime}\right)^{(8)}-\left(r_{40}\right)^{(8)}\right) s_{(41),(40)} T_{41}^{*}+\left(b_{41}\right)^{(8)} S_{(40),(40)} T_{40}^{*}\right) \\
& \left(\left((\lambda)^{(8)}\right)^{2}+\left(\left(a_{40}^{\prime}\right)^{(8)}+\left(a_{41}^{\prime}\right)^{(8)}+\left(p_{40}\right)^{(8)}+\left(p_{41}\right)^{(8)}\right)(\lambda)^{(8)}\right) \\
& \left(\left((\lambda)^{(8)}\right)^{2}+\left(\left(b_{40}^{\prime}\right)^{(8)}+\left(b_{41}^{\prime}\right)^{(8)}-\left(r_{40}\right)^{(8)}+\left(r_{41}\right)^{(8)}\right)(\lambda)^{(8)}\right) \\
& +\left(\left((\lambda)^{(8)}\right)^{2}+\left(\left(a_{40}^{\prime}\right)^{(8)}+\left(a_{41}^{\prime}\right)^{(8)}+\left(p_{40}\right)^{(8)}+\left(p_{41}\right)^{(8)}\right)(\lambda)^{(8)}\right)\left(q_{42}\right)^{(8)} G_{42} \\
& +\left((\lambda)^{(8)}+\left(a_{40}^{\prime}\right)^{(8)}+\left(p_{40}\right)^{(8)}\right)\left(\left(a_{42}\right)^{(8)}\left(q_{41}\right)^{(8)} G_{41}^{*}+\left(a_{41}\right)^{(8)}\left(a_{42}\right)^{(8)}\left(q_{40}\right)^{(8)} G_{40}^{*}\right) \\
& \left.\left(\left((\lambda)^{(8)}+\left(b_{40}^{\prime}\right)^{(8)}-\left(r_{40}\right)^{(8)}\right) s_{(41),(42)} T_{41}^{*}+\left(b_{41}\right)^{(8)} s_{(40),(42)} T_{40}^{*}\right)\right\}=0 \\
& + \\
& \left((\lambda)^{(9)}+\left(b_{46}^{\prime}\right)^{(9)}-\left(r_{46}\right)^{(9)}\right)\left\{\left((\lambda)^{(9)}+\left(a_{46}^{\prime}\right)^{(9)}+\left(p_{46}\right)^{(9)}\right)\right. \\
& {\left[\left(\left((\lambda)^{(9)}+\left(a_{44}^{\prime}\right)^{(9)}+\left(p_{44}\right)^{(9)}\right)\left(q_{45}\right)^{(9)} G_{45}^{*}+\left(a_{45}\right)^{(9)}\left(q_{44}\right)^{(9)} G_{44}^{*}\right)\right]} \\
& \left(\left((\lambda)^{(9)}+\left(b_{44}^{\prime}\right)^{(9)}-\left(r_{44}\right)^{(9)}\right) s_{(45),(45)} T_{45}^{*}+\left(b_{45}\right)^{(9)} s_{(44),(45)} T_{45}^{*}\right) \\
& +\left(\left((\lambda)^{(9)}+\left(a_{45}^{\prime}\right)^{(9)}+\left(p_{45}\right)^{(9)}\right)\left(q_{44}\right)^{(9)} G_{44}^{*}+\left(a_{44}\right)^{(9)}\left(q_{45}\right)^{(9)} G_{45}^{*}\right)
\end{aligned}
$$

$$
\begin{aligned}
& \quad\left(\left((\lambda)^{(9)}+\left(b_{44}^{\prime}\right)^{(9)}-\left(r_{44}\right)^{(9)}\right) s_{(45),(44)} T_{45}^{*}+\left(b_{45}\right)^{(9)} s_{(44),(44)} T_{44}^{*}\right) \\
& \left(\left((\lambda)^{(9)}\right)^{2}+\left(\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{45}^{\prime}\right)^{(9)}+\left(p_{44}\right)^{(9)}+\left(p_{45}\right)^{(9)}\right)(\lambda)^{(9)}\right) \\
& \quad\left(\left((\lambda)^{(9)}\right)^{2}+\left(\left(b_{44}^{\prime}\right)^{(9)}+\left(b_{45}^{\prime}\right)^{(9)}-\left(r_{44}\right)^{(9)}+\left(r_{45}\right)^{(9)}\right)(\lambda)^{(9)}\right) \\
& +\left(\left((\lambda)^{(9)}\right)^{2}+\left(\left(a_{44}^{\prime}\right)^{(9)}+\left(a_{45}^{\prime}\right)^{(9)}+\left(p_{44}\right)^{(9)}+\left(p_{45}\right)^{(9)}\right)(\lambda)^{(9)}\right)\left(q_{46}\right)^{(9)} G_{46} \\
& +\left((\lambda)^{(9)}+\left(a_{44}^{\prime}\right)^{(9)}+\left(p_{44}\right)^{(9)}\right)\left(\left(a_{46}\right)^{(9)}\left(q_{45}\right)^{(9)} G_{45}^{*}+\left(a_{45}\right)^{(9)}\left(a_{46}\right)^{(9)}\left(q_{44}\right)^{(9)} G_{44}^{*}\right) \\
& \left.\left(\left((\lambda)^{(9)}+\left(b_{44}^{\prime}\right)^{(9)}-\left(r_{44}\right)^{(9)}\right) s_{(45),(46)} T_{45}^{*}+\left(b_{45}\right)^{(9)} s_{(44),(46)} T_{44}^{*}\right)\right\}=0
\end{aligned}
$$

And as one sees, all the coefficients are positive. It follows that all the roots have negative real part, and this proves the theorem.

## 5. CONCLUSIONS

Paper answers, not wholly or in full measure, but substantially the relationship between dark matter and antimatter and speculates in epiphenomena and phenomenological form the circumspective jurisprudence of consideration of the antimatter as dark matter. this also answers the long standing question in cosmology that why matter is prevalent in the universe in contrast to antimatter. for if antimatter is dark matter then it is also invisible and helps critically declaratively, demonstratively, discursive, frighteningly exegetic, explanatory explicative, exposition ally hermeneutic answer for the problem that has cast its shadow over the otherwise chart busting growth of cosmology.
The paper seems to confirm antimatter as an intrinsic constituent of ordinary matter; antimatter as an integral part of the electromagnetic phenomena; the existence of a new particle namely bielectron, consisting of an electron and a positron joined together within the atom; that matter and antimatter preceded the big-bang and their violent encounter may have been the actual cause of the big-bang itself; that matter and antimatter have a pacific coexistence in today's universe, after the big-bang; the possible existence of a new force in physics namely bundeswehr, which would recombine and keep matter and antimatter particles together.

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The introduction is a collection of information from, articles, abstracts of the articles, paper reports, home pages of the authors, textbooks, research papers, and various other sources in the internet including Wikipedia. We acknowledge all authors who have contributed to the same. Should there be any act of omission or commission on the part of the authors in not referring to the author, it is authors' sincere entreat, earnest beseech, and fervent appeal to pardon such lapses as has been done or purported in the foregoing. With great deal of compunction and contrition, the authors beg the pardon of the respective sources. References list is only illustrative and not exhaustive. We have put all concerted efforts and sustained endeavors to incorporate the names of all the sources from which information has been extracted. It is because of such eminent, erudite, and esteemed people allowing us to piggy ride on their backs, we have attempted to see little forward, or so we think.

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