Mathematical Theory and Modeling ISSN 2224-5804 (Paper) ISSN 2225-0522 (Online) Vol.4, No.8, 2014



Common Random Fixed Point Theorems of Contractions in Partial Cone Metric Spaces over Non normal Cones

PIYUSH M. PATEL⁽¹⁾ Research Scholar of Sainath University,Ranchi(Jarkhand). pmpatel551986@gmail.com

RAMAKANT BHARDWAJ⁽²⁾ Associate Professor in Truba Institute of Engineering & Information Technology, Bhopal (M.P). <u>drrkbhardwaj100@gmail.com</u>

SABHAKANT DWIVEDI⁽³⁾

Department of Mathematics, Institute for Excellence in higher education Bhopal

1. ABSTRACT: The purpose of this paper is to prove existence of common random fixed point in the setting of partial cone metric space over the non-normal cones.

Key wards: common fixed point, cone metric space, random variable

2. INTRODUCTION AND PRELIMINARIES

Random nonlinear analysis is an important mathematical discipline which is mainly concerned with the study of random nonlinear operators and their properties and is needed for the study of various classes of random equations. The study of random fixed point theory was initiated by the Prague school of Probabilities in the 1950s [4, 13, and 14]. Common random fixed point theorems are stochastic generalization of classical common fixed point theorems. The machinery of random fixed point theory provides a convenient way of modeling many problems arising from economic theory and references mentioned therein. Random methods have revolutionized the financial markets. The survey article by Bharucha-Reid [1] attracted the attention of several mathematicians and gave wings to the theory. Itoh [18] extended Spacek's and Hans's theorem to multivalued contraction mappings. Now this theory has become the full edged research area and various ideas associated with random fixed point theory are used to obtain the solution of nonlinear random system (see [2,3,7,8,9]). Papageorgiou [11, 12], Beg [5,6] studied common random fixed points and random coincidence points of a pair of compatible random and proved fixed point theorems for contractive random operators in Polish spaces.

In 2007, Huang and Zhang [9] introduced the concept of cone metric space and establish some fixed point theorems for contractive mappings in normal cone metric spaces. Subsequently, several other authors [10, 17,] studied the existence of fixed points and common fixed points of pings satisfying contractive type condition on a normal cone metric space. In 2008, Rezapour and Hamlbarani [17] omitted the assumption of normality in cone metric space, which is a milestone in developing fixed point theory in cone metric space. In this paper we prove existence of common random fixed point in the setting of cone random metric spaces under weak contractive condition. Recently, Dhagat et al. [19] introduced the concept of cone random metric space and proved an existence of random fixed point under weak contraction condition in the setting of cone random metric spaces. The purpose of this paper to find common random fixed point theorems of contractions in partial cone metric spaces.

Definition 2.1. Let *X* be a nonempty set and let *P* be a cone of a topological vector space *E*. A partial cone metric on *X* is a mapping $p: \Omega \times X \times X \rightarrow P$ such that, for each $f(t), g(t), h(t) \in X$, $t \in \Omega$,

 $\begin{array}{ll} (p1) & p(f(t),g(t)) = p(f(t),f(t)) = p(g(t),g(t)) \Leftrightarrow f(t) = g(t), \\ (p2) & p(f(t),g(t)) = p(g(t),f(t)) \\ (p3) & p(f(t),f(t)) \leq p(f(t),g(t)) \\ (p3) & p(f(t),g(t)) \leq p(f(t),h(t)) + p(h(t),g(t)) - p(h(t),h(t)) \\ \forall t \in \Omega \end{array}$

The pair (X, p) is called a partial cone metric space over *P*.

Definition 2.2. A function f: $\Omega \to C$ is said to be measurable if $f^{-1}(B \cap C) \in \Sigma$ for every Borel subset B of H.

Definition 2.3. A function $F: \Omega \times C \to C$ is said to be a random operator if $F(., x): \Omega \to C$ is measurable for every $x \in C$

Definition 2.4. A measurable $g: \Omega \to C$ is said to be a random fixed point of the random operator $F: \Omega \times C \to C$ if F(t, g(t)) = g(t) for all $t \in \Omega$

Definition 2.5. A random operator F: $\Omega \times C \to C$ is said to be continuous if for fixed $t \in \Omega$, $F(t,.): C \to C$ is continuous.

Lemma:2.6 Let P be solid cone of a topological vector space E and $\{f_n(t)\}, \{g_n(t)\}, \{h_n(t)\} \subset E$. if $f_n(t) \leq h_n(t) \leq g_n(t) \forall n$, and there exists some $\omega(t) \in E$ Such that $f_n(t) \xrightarrow{\omega} \omega(t)$ and $g_n(t) \xrightarrow{\omega} \omega(t)$ then $h_n(t) \xrightarrow{\omega} \omega(t)$

Lemma:2.7 Let P be solid cone of a normed vector space $(E, \|\cdot\|)$ then for each sequence $\{f_n(t)\} \subset E$. $f_n(t) \xrightarrow{\|\cdot\|} \omega(t) \text{ implies } f_n(t) \xrightarrow{\omega} \omega(t) \text{ moreover if P is normal, then } f_n(t) \xrightarrow{\omega} \omega(t)$ implies $f_n(t) \xrightarrow{\|\cdot\|} \omega(t)$

Lemma:2.8 Let P be solid cone of a normed vector space $(E, \|\cdot\|), \{K_n\} \subset \zeta$ and $\{f_n(t)\} \subset P$. $f_n(t) \xrightarrow{\omega} \theta$ and $\sup_n \|K_n\| < +\infty$, then $K_n f_n(t) \xrightarrow{\omega} \theta$.

Theorem 2.9 Let $(X \times \Omega, p)$ be partial cone metric space. The mapping $T, S : X \times \Omega \to X$ are called contractions restricted with variable positive linear bounded mappings if there exist $L_i : X \times X \to \zeta$ (i = 1,2,3,4) such that $p(T(f(t),t)) \leq L_1(f(t),g(t))p(f(t),g(t)) + L_2(f(t),g(t))p(f(t),T(f(t),t))$ $+ L_3(f(t),g(t))p(g(t),S(g(t),t))$ $+ L_4(f(t),g(t))p(f(t),S(g(t),t) + p(g(t),T(f(t),t)))$ $f(t),g(t) \in X ---(*)$

In particular if (*) is holds with

 $L_i(f(t), g(t)) \equiv A_i \text{ and } A_i \in \zeta \ (i = 1, 2, 3, 4)$

then T and S are called contractions restricted with positive linear bounded mappings

3. Main Result:

www.iiste.org

Theorem 3.1. Let (X, p) be a θ -complete partial cone metric space over a solid cone P of a normed vector space $(E, \|\cdot\|)$ and let $T, S : X \times \Omega \to X$ be contractions restricted with variable positive linear bounded random mappings. If $p(L_3(f(t), g(t)) + L_4(f(t), g(t))) < 1$ and $p(L_2(f(t), g(t)) + L_4(f(t), g(t))) < 1$

 $\forall f(t), g(t) \in X \qquad ------(1)$

 $l_1 l_2 < 1$ and $l_3 < \infty$, where p(.) denotes the spectral radius of linear bounded mappings,

$$l_{1} = \sup_{f(t),g(t)\in\mathbf{X}} \left\| K_{1}(f(t),g(t)) \right\|$$

$$l_{2} = \sup_{f(t),g(t)\in\mathbf{X}} \left\| K_{2}(f(t),g(t)) \right\|$$

$$l_{3} = \sup_{f(t),g(t)\in\mathbf{X}} \left\| K_{3}(f(t),g(t)) \right\|, ------(2)$$

 $h_n(t) \in X, h_n(t) \xrightarrow{\tau_p} h(t) \text{ where } h_n(t) \text{ is defined by}$ $h_{n+1}(t) = \begin{cases} T(h_n(t), t) \text{ ; n is even number} \\ S(h_n(t), t) \text{ ; n is odd number} \end{cases} -----(5)$

Proof. For each $x, y \in X$ by (1), the inverse of $1 - L_3(f(t), g(t)) - L_4(f(t), g(t))$ and $1 - L_2(f(t), g(t)) - L_4(f(t), g(t))$ exist. then, it is clear that $\overline{L_1}$ and $\overline{L_2}$ are meaningful and K_1, K_2, K_3 are well defined.

 $x, y \in X$, which is together with $L_i: X \times X \to \zeta$ (i = 2,3,4) implies that $L_i: X \times X \to \zeta$ (i = 1,2)and hence $K_i: X \times X \to \zeta$ (i = 1,2,3).by(*),(5), (p4) $L_4: X \times X \to \zeta$

$$\begin{split} p(f_{2k+1}(t), f_{2k+2}(t)) &= p(T(f_{2k}(t), t), S(f_{2k+1}(t), t)) \\ &\leq L_1(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+1}(t)) \\ &+ L_2(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+1}(t)) \\ &+ L_3(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+2}(t)) \\ &+ L_4(f_{2k}(t), f_{2k+1}(t)) [p(f_{2k}(t), f_{2k+2}(t)) + p(f_{2k+1}(t), f_{2k+1}(t))] \\ &\leq L_1(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+1}(t)) \\ &+ L_2(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+1}(t)) \\ &+ L_3(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+1}(t)) + p(f_{2k+1}(t), f_{2k+2}(t))] \\ &+ L_4(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+1}(t)) + p(f_{2k+1}(t), f_{2k+2}(t))] \\ &+ L_4(f_{2k}(t), f_{2k+1}(t)) [p(f_{2k}(t), f_{2k+1}(t)) + p(f_{2k+1}(t), f_{2k+2}(t))]] \\ \forall k \in N \\ &- - - - - (7) \\ \begin{bmatrix} I - L_2(f_{2k}(t), f_{2k+1}(t)) - L_4(f_{2k}(t), f_{2k+1}(t)) \end{bmatrix} p(f_{2k+1}(t), f_{2k+2}(t)) \\ &+ L_4(f_{2k}(t), f_{2k+1}(t)) + L_2(f_{2k}(t), f_{2k+1}(t)) \end{bmatrix} p(f_{2k}(t), f_{2k+1}(t)) \\ \end{bmatrix} p(f_{2k}(t), f_{2k+1}(t)) \end{bmatrix} \\ d so \qquad \leq \begin{bmatrix} L_1(f_{2k}(t), f_{2k+1}(t)) + L_2(f_{2k}(t), f_{2k+1}(t)) \\ &+ L_4(f_{2k}(t), f_{2k+1}(t)) \end{bmatrix} p(f_{2k}(t), f_{2k+1}(t)) \end{bmatrix} p(f_{2k}(t), f_{2k+1}(t)) \\ \end{bmatrix} p(f_{2k}(t), f_{2k+1}(t)) \end{bmatrix} d'k \in N \\ &- - - - - (8) \\ \end{bmatrix}$$

An

Act the above inequality with $\overline{L_1}(f_{2k}(t), f_{2k+1}(t))$; then, $\overline{L_1}: X \times X \to \zeta$, $p(f_{2k+1}(t), f_{2k+2}(t)) \le K_1(f_{2k}(t), f_{2k+1}(t)) p(f_{2k}(t), f_{2k+1}(t)), \forall k \in \mathbb{N}$

Similarly ,by (*),(p3), (p4) and $L_4: X \times X \to \zeta$

$$\begin{split} p(f_{2k+2}(t), f_{2k+3}(t)) &= p(f_{2k+3}(t), f_{2k+2}(t)) \\ &= p(T(f_{2k+2}(t), t), S(f_{2k+1}(t), t)) \\ &\leq L_1(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+1}(t)) \\ &+ L_2(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+3}(t)) \\ &+ L_3(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+2}(t)) \\ &+ L_4(f_{2k+2}(t), f_{2k+1}(t)) [p(f_{2k+2}(t), f_{2k+2}(t)) + p(f_{2k+1}(t), f_{2k+3}(t))] \\ &\leq L_1(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+1}(t)) \\ &+ L_2(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+3}(t)) \\ &+ L_3(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+3}(t)) \\ &+ L_4(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+3}(t)) \\ &+ L_4(f_{2k+2}(t), f_{2k+1}(t)) p(f_{2k+2}(t), f_{2k+3}(t)) \\ &+ L_4(f_{2k+2}(t), f_{2k+1}(t)) [p(f_{2k+2}(t), f_{2k+3}(t)) + p(f_{2k+2}(t), f_{2k+3}(t))] \quad \forall k \in N \\ &------(10) \end{split}$$

And so

Act the above inequality with $\overline{L_2}(f_{2k+2}(t), f_{2k+1}(t))$; then, by: $\overline{L_2}: X \times X \to \zeta$, $p(f_{2k+2}(t), f_{2k+1}(t) \le K_2(f_{2k+2}(t), f_{2k+1}(t))p \ (f_{2k+1}(t), f_{2k+2}(t)), \forall k \in \mathbb{N}.$ ------(12) Moreover $K_1, K_2: X \times X \to \zeta$, $p(f_{2k+1}(t), f_{2k+2}(t)) \le K_1(f_{2k}(t), f_{2k+1}(t)) \times K_2(f_{2k}(t), f_{2k-1}(t))......$ $\dots K_1(f_0(t), f_1(t))p(f_0(t), f_1(t)), \forall k \in \mathbb{N}.$ ------(13)

In the following, we will prove that

 $p(f_n(t), f_m(t)) \xrightarrow{\omega} \theta$ ------(14) For m>n, we have four cases

(1) m = 2p + 1, n = 2q + 1; (2) m = 2p + 1, n = 2q (3) m = 2p, n = 2q + 1 (4) m = 2p, n = 2qWhere p and q are two non negative integers such that p > q. We only show that (14) holds for

case (1) the proof of three cases is similar. It follows for (p4) and (13) that

$$\begin{aligned} \theta &\leq p(f_n(t), f_m(t)) \\ &= p(f_{2q+1}(t), f_{2p+1}(t)) \\ &\leq p(f_{2q+1}(t), f_{2q+2}(t)) + p(f_{2q+2}(t), f_{2q+3}(t)) + \dots + p(f_{2p-1}(t), f_{2p}(t)) + p(f_{2p}(t), f_{2p+1}(t)) \\ &\leq pK_1K_2(f_0(t), f_1(t)) \\ &= K_1(f_{2q}(t), f_{2q+1}(t)) \times K_2(f_{2q}(t), f_{2q-1}(t)) \dots K_1(f_0(t), f_1(t)) p(f_0(t), f_1(t)) p(f_0(t), f_1(t)) p(f_0(t), f_1(t)) + \dots \\ &+ K_1(f_{2q-2}(t), f_{2q+1}(t)) \times K_2(f_{2p-2}(t), f_{2p-3}(t)) \dots K_1(f_0(t), f_1(t)) p(f_0(t), f_1(t)) p(f_0(t), f_1(t)) + \dots \\ &+ K_1(f_{2p}(t), f_{2q-1}(t)) \times K_2(f_{2p-2}(t), f_{2p-1}(t)) \dots K_1(f_0(t), f_1(t)) p(f_0(t), f_1(t)) p(f_0(t), f_1(t)) \\ &+ K_2(f_{2p}(t), f_{2q-1}(t)) \times K_1(f_{2p-2}(t), f_{2p-1}(t)) \dots K_1(f_0(t), f_1(t)) p(f_0(t), f_1(t)) \forall p > q \\ &- \dots - \dots - (15) \end{aligned}$$

$$\begin{split} &l_{1}l_{2} < 1, \\ &\|pK_{1}K_{2}(f_{0}(t), f_{1}(t))\| \\ \leq &l_{1}^{q+1}l_{2}^{q} + l_{1}^{q+1}l_{2}^{q+1} + \dots + l_{1}^{p+1}l_{2}^{p} + l_{1}^{p}l_{2}^{p} \|p(f_{0}(t), f_{1}(t))\| \\ = & \left(l_{1}\sum_{i=q}^{p} (l_{1}l_{2})^{i} + l_{1}\sum_{i=q+1}^{p} (l_{1}l_{2})^{i} + \right) \|p(f_{0}(t), f_{1}(t))\| \\ \leq & \frac{(l_{1}+l_{1}l_{2})(l_{1}l_{2})^{q} \|p(f_{0}(t), f_{1}(t))\|}{1-l_{1}l_{2}} \quad \forall \ p > q, \ ------(16) \end{split}$$

Which implies that $p(f_n(t), f_m(t)) \xrightarrow{\parallel} \theta$, and hence $p(f_n(t), f_m(t)) \xrightarrow{\omega} \theta$ by lemma(2.7) Thus by (15) and lemma (2.6) $p(f_n(t), f_m(t)) \xrightarrow{\omega} \theta$; that is (14) holds. It is prove that $\{f_n(t)\}$ is a θ Cauchy sequence in (X, p), and so by the θ completeness of (X, p), there exits $h(t) \in X$ such that $f_n(t) \xrightarrow{\tau_p} h(t)$ and $p(h(t), h(t)) = \theta$; that is, $p(f_n(t), h(t)) \xrightarrow{\omega} \theta \longrightarrow \theta \longrightarrow (17)$

For all $k \in N$, by (*) and (p4),

$$\begin{split} p\big(T(h(t),t),h(t)\big) &\leq p\big(T(h(t),t),h(t),f_{2k}(t)\big) + p(f_{2k}(t),h(t)) \\ &= p\big(T\big(h(t),t\big),S\big(f_{2k-1}(t),t\big)\big) + p(f_{2k}(t),h(t)) \\ &\leq L_1(h(t),f_{2k-1}(t))p(h(t),f_{2k-1}(t)) \\ &+ L_2(h(t),f_{2k-1}(t))p\big(h(t),T(h(t),t)\big) \\ &+ L_3(h(t),f_{2k-1}(t))p(f_{2k-1}(t),f_{2k}(t)) \\ &+ L_4(h(t),f_{2k-1}(t))\big[p(h(t),f_{2k}(t)) + p\big(f_{2k-1}(t),T(h(t),t)\big)\big] \\ &+ p(f_{2k}(t),h(t)) \end{split}$$

And so

$$\begin{bmatrix} I - L_2(h(t), f_{2k-1}(t)) - L_4(h(t), f_{2k-1}(t)) \end{bmatrix} p(T(h(t), t), h(t))$$

$$\leq \begin{bmatrix} L_1(h(t), f_{2k-1}(t)) + L_3(h(t), f_{2k-1}(t)) + L_4(h(t), f_{2k-1}(t)) \end{bmatrix} p(h(t), f_{2k-1}(t))$$

$$+ \begin{bmatrix} I + L_3(h(t), f_{2k-1}(t)) + L_4(h(t), f_{2k-1}(t)) \end{bmatrix} p(f_{2k}(t), h(t)) \forall k \in N$$
------(19)

Act the above inequality with $\overline{L_2}(h(t), f_{2k-1}(t))$; then, $\overline{L_1}: X \times X \to \zeta$, $\theta \le p(T(h(t), t, h(t)) \le K_{2, 2k-1} p(h(t), f_{2k-1}(t) + K_{3, 2k-1} p(f_{2k}(t), h(t))) \forall k \in \mathbb{N} - ---(20)$

Where $K_{2,2k-1} = K_2 p(h(t), f_{2k-1}(t))$ and $K_{3,2k-1} = K_2 p(h(t), f_{2k-1}(t))$. It is clear that $\{K_{2,2k-1}\}, \{K_{3,2k-1}\}$ subsets of ζ and $\sup_k ||K_{2,2k-1}|| < +\infty, \sup_k ||K_{3,2k-1}|| < +\infty$ by $l_1 l_2 < 1$ and $l_3 < +\infty$.then its follows from the lemma (3) and (17) that

$$K_{2,2k-1}p(h(t), f_{2k-1}(t) + K_{3,2k-1}p(h(t), f_{2k-1}(t) \xrightarrow{\omega} \theta, \quad ------(21)$$

Which together with lemma (2.6) and (20) implies that $p(h(t), T(h(t), t)) = \theta$

Therefore T(h(t),t) = h(t) by (p1) and (p3).similarly we can show that S(h(t),t) = h(t).

Hence h(t) is common random fixed point of T and

Now we show the uniqueness of fixed point. Let f(t) and h(t) be two common random fixed point of T and S then by (*) and (p3) $L_i: X \times X \to \zeta$ (i = 2,3)

$$\begin{split} p(h(t), f(t)) &= p(T(h(t), t)), S(f(t), t)) \\ &\leq L_1(h(t), f(t)) p(h(t), f(t),) + L_2(h(t), f(t)) p(h(t), T(h(t), t) + L_3(h(t), f(t)) p(f(t), S(f(t), t))) \\ &+ L_4(h(t), f(t)) \Big[p(h(t), S(f(t), t)) + p(f(t), T(h(t), t)) \Big] \\ &= \Big[L_1(h(t), f(t)) + 2L_4(h(t), f(t)) \Big] p(h(t), f(t)) \\ &+ L_2(h(t), f(t)) p(h(t), h(t)) + L_3(h(t), f(t)) p(f(t), f(t)) \\ &\leq \Big[L_1(h(t), f(t)) + L_2(h(t), f(t)) + L_3(h(t), f(t)) + 2L_4(h(t), f(t)) \Big] p(h(t), f(t)), -----(22) \end{split}$$

And so

$$[I - L_1(h(t), f(t)) - L_2(h(t), f(t)) - L_3(h(t), f(t)) - 2L_4(h(t), f(t))]p(h(t), f(t)), ----(23)$$

It follow from (3) that the inverse of

$$\begin{bmatrix} I - L_1(h(t), f(t)) - L_2(h(t), f(t)) - L_3(h(t), f(t)) - 2L_4(h(t), f(t)) \end{bmatrix} \text{ exists(denoted by)}$$

$$\begin{bmatrix} I - L_1(h(t), f(t)) - L_2(h(t), f(t)) - L_3(h(t), f(t)) - 2L_4(h(t), f(t)) \end{bmatrix}^{-1} \text{ and}$$

$$\begin{bmatrix} I - L_1(h(t), f(t)) - L_2(h(t), f(t)) - L_3(h(t), f(t)) - 2L_4(h(t), f(t)) \end{bmatrix}^{-1} \in \zeta \text{ by Neumann's formula}$$
with $\begin{bmatrix} I - L_1(h(t), f(t)) - L_2(h(t), f(t)) - L_3(h(t), f(t)) - 2L_4(h(t), f(t)) \end{bmatrix}^{-1}$; then $p(h(t), f(t)) = \theta$
and hence $h(t) = f(t)$ by (p1) and (p3) the proof is completed.

REFERENCES:

1. A.T. Bharucha-Reid, Random Integral equations, Mathematics in Science and Engineering, vol. 96, Academic Press, New York(1972).

- 2. A.T. Bharucha-Reid, Fixed point theorems in Probabilistic analysis Bulletin of the American Mathematical Society, 82(5) (1976), 641-657.
- 3. C.J. Himmelberg, Measurable relations, Fundamenta Mathematicae, 87 (1975), 53-72.
- 4. D.H. Wagner, Survey of measurable selection theorem, SIAM Journal on Control and Optimization, 15(5) (1977), 859-903
- 5. I. Beg, Random fixed points of random operators satisfying semi contractivity conditions Mathematics Japonica, 46(1) (1997), 151-155.
- I. Beg, Approximation of random fixed points in normed spaces Nonlinear Analysis 51(8) (2002), 1363-1372.
- 7. I. Beg and M. Abbas, Equivalence and stability of random fixed point iterative procedures Journal of Applied Mathematics and Stochastic Analysis, (2006), 19 pages
- 8. I. Beg and M. Abbas, Iterative procedures for solutions of random operator equations in Banach spaces,
- Journal of Mathematical Analysis and Applications, 315(1) (2006), 181-201.
- 9. L.-G. Huang and X. Zhang, Cone metric spaces and fixed point theorems of contractive mappings, J. Math. Anal. Appl., 332(2) (2007), 1468-1476
- 10. M. Abbas and G. Jungck, Common fixed point results for non commuting mappings continuity in cone metric spaces, J. Math. Anal. Appl., 341 (2008), 416-420.
- 11. N.S. Papageorgiou, Random fixed point theorems for measurable multifunctions in Banach spaces, Proceedings of the American Mathematical Society, 97(3) (1986),507-514.
- N.S. Papageorgiou, On measurable multifunctions with stochastic domain, Journal of Australian Mathematical Society. Series A, 45(2) (1988), 204-216.
 O. Hone Bedrarder and Statistical Learning Conductive Mathematical Learning
 - O. Hans, Reduzierende zufallige transformationen, Czechoslovak Mathematical Journal (82) (1957), 154-1587.

14. O. Hans, Random operator equations, Proceeding of the 4th Berkeley Symposium on Mathematical Statistics and Probability, Vol. II, University of California Press, California, (1961), 185-202.
15. R. Penaloza, A characterization of renegotiation proof contracts via random fixed points in Banach spaces, working paper 269, Department of Economics, University of Brasilia, Brasilia, December (2002).

. 16 Sh. Rezapour, A review on topological properties of cone metric spaces, in Proceedings of the International Conference on Analysis, Topology and Appl. (ATA 08), Vrinjacka

Banja, Serbia, May-June (2008).

17. Sh. Rezapour and R. Hamlbarani, Some notes on the paper "Cone metric spaces and fixed point theorems of contractive mappings", J. Math. Anal. Appl., 345(2) (2008), 719-724.

18. S. Itoh, Random fixed point theorems with an application to random differential equations in Banach spaces, Journal of Mathematical Analysis and Applications, 67(2) (1979), 261-273.

19. V.B. Dhagat, R. Shrivastav and V. Patel, Fixed point theorems in cone random metric spaces, Advances in Fixed Point Theory, 2(3) (2012), 357-363.

20.V.M. Sehgal and S.P. Singh, On random approximations and a random fixed point theorem for set valued mappings, Proceedings of the American Mathematical Society, 95(1) (1985), 91-94.

The IISTE is a pioneer in the Open-Access hosting service and academic event management. The aim of the firm is Accelerating Global Knowledge Sharing.

More information about the firm can be found on the homepage: <u>http://www.iiste.org</u>

CALL FOR JOURNAL PAPERS

There are more than 30 peer-reviewed academic journals hosted under the hosting platform.

Prospective authors of journals can find the submission instruction on the following page: <u>http://www.iiste.org/journals/</u> All the journals articles are available online to the readers all over the world without financial, legal, or technical barriers other than those inseparable from gaining access to the internet itself. Paper version of the journals is also available upon request of readers and authors.

MORE RESOURCES

Book publication information: <u>http://www.iiste.org/book/</u>

IISTE Knowledge Sharing Partners

EBSCO, Index Copernicus, Ulrich's Periodicals Directory, JournalTOCS, PKP Open Archives Harvester, Bielefeld Academic Search Engine, Elektronische Zeitschriftenbibliothek EZB, Open J-Gate, OCLC WorldCat, Universe Digtial Library, NewJour, Google Scholar

