

# **Fully Invariant and Characteristic Interval-Valued**

# **Intuitionistic Fuzzy Dual Ideals of BF-algebras**

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#### Abstract

The notion of interval-valued intuitionistic fuzzy sets was first introduced by Atanassov and Gargov as a generalization of both interval-valued fuzzy sets and intuitionistic fuzzy sets. Satyanarayana et. al., applied the concept of interval-valued intuitionistic fuzzy ideals and interval-valued intuitionistic fuzzy dual ideals to BF-algebras. In this paper, we introduce the notion of fully invariant and characteristic interval-valued intuitionistic fuzzy dual ideals of BF-algebras and investigate some of its properties.

### 1. Introduction and preliminaries

For the first time Zadeh (1965) introduced the concept of fuzzy sets and also Zadeh (1975) introduced the concept of an interval-valued fuzzy sets, which is an extension of the concept of fuzzy set. <u>Atanassov and Gargov, 1989</u>) introduced the notion of interval-valued intuitionistic fuzzy sets, which is a generalization of both intuitionistic fuzzy sets and interval-valued fuzzy sets. <u>Meng and Jun (1993)</u> introduced fuzzy dual ideals in BCK-algebras. On other hand, <u>Satyanarayana et al., (2010)</u> and (2011) applied the concept of interval-valued intuitionistic fuzzy ideals and interval-valued intuitionistic fuzzy dual ideals to BF-algebras. In this paper we introduce the notion of fully invariant and characteristic interval-valued intuitionistic fuzzy dual ideals of BF-algebras and investigate some of its properties.

By a BF-algebra we mean an algebra satisfying the axioms:

(1). x \* x = 0,

(2). x \* 0 = x,

(3). 0 \* (x \* y) = y \* x, for all  $x, y \in X$ 

Throughout this paper, X is a BF-algebra. If there is an element 1 of X satisfying  $x \le 1$ , for all  $x \in X$ , then the element 1 is called unit of X. A BF-algebra with unit is called bounded. In a bounded

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**Definition 1.1** (Satyanarayana et al., 2011) A nonempty subset D in a BF-algebra X is said to be a dual ideal of X if it satisfies:

 $(D_1) 1 \in D$ ,

 $(D_2)$  N(Nx \* Ny)  $\in$  D and y  $\in$  D imply x  $\in$  D, for any x, y  $\in$  X.

**Definition 1.2** Let X be a set. A fuzzy set in X is a function  $\mu: X \to [0,1]$ .

**Definition 1.3** (Meng and Jun (1993) A fuzzy subset of X is said to be a fuzzy dual ideal of X if it satisfies

(FDI 1)  $\mu(1) \ge \mu(x)$ 

(FDI 2)  $\mu(x) \ge \min\{\mu(N(Nx * Ny)), \mu(y)\}$  for all x, y in X.

We now review some fuzzy logic concepts. For fuzzy sets  $\mu$  and  $\lambda$  of X and s, t  $\in [0,1]$ , the set

 $U(\mu; t) = \{x \in X : \mu(x) \ge t\}$  is called upper t-level cut of  $\mu$  and the set

 $L(\mu; t) = \{x \in X : \lambda(x) \le s\}$  is called lower s-level cut of  $\lambda$ . The fuzzy set  $\mu$  in X is called a

fuzzy dual sub algebra of X, if  $\mu(N(Nx * Ny)) \ge \min\{\mu(x), \mu(y)\}$ , for all  $x, y \in X$ .

Intuitionistic fuzzy sets: (Fatemi 2011 and Wang et. al., 2011) An intuitionistic fuzzy set (shortly IFS) in a non-empty set X is an object having the form  $A = \{(x, \mu_A(x), \lambda_A(x)) : x \in X\}$ , where the functions  $\mu_A : X \to [0,1]$  and  $\lambda_A : X \to [0,1]$  denote the degree of membership (namely  $\mu_A(x)$ ) and the degree of non membership (namely  $\lambda_A(x)$ ) of each element  $x \in X$  to the set A respectively such that for any  $x \in X$ .  $0 \le \mu_A(x) + \lambda_A(x) \le 1$ . For the sake of simplicity we use the symbol form  $A = (\mu_A, \lambda_A)$  or  $A = (X, \mu_A, \lambda_A)$ .

By an interval number D on [0,1] we mean an interval  $[a^-, a^+]$  where  $0 \le a^- \le a^+ \le 1$ . The set of all closed subintervals of [0,1] is denoted by D[0,1]. For interval numbers  $D_1 = [a_1^-, b_1^+]$ ,

Mathematical Theory and Modeling www.iiste.org ISSN 2224-5804 (Paper) ISSN 2225-0522 (Online) Vol.2, No.3, 2012 IISTF  $D_2 = \left| a_2^-, b_2^+ \right|$ . We define •  $D_1 \cap D_2 = \min(D_1, D_2) = \min(|a_1^-, b_1^+|, |a_2^-, b_2^+|) = [\min\{a_1^-, a_2^-\}, \min\{b_1^+, b_2^+\}]$ •  $D_1 \cup D_2 = \max(D_1, D_2) = \max(|a_1^-, b_1^+|, |a_2^-, b_2^+|) = \max\{a_1^-, a_2^-\} \max\{b_1^+, b_2^+\}$  $D_1 + D_2 = [a_1^- + a_2^- - a_1^- a_2^-, b_1^+ + b_2^+ - b_1^+ b_2^+]$ 

and put

- $D_1 \leq D_2 \Leftrightarrow a_1^- \leq a_2^-$  and  $b_1^+ \leq b_2^+$
- $D_1 = D_2 \Leftrightarrow a_1^- = a_2^- \text{ and } b_1^+ = b_2^+$ ,
- $D_1 < D_2 \Leftrightarrow D_1 \le D_2$  and  $D_1 \ne D_2$
- $mD = m[a_1^-, b_1^+] = [ma_1^-, mb_1^+]$ , where  $0 \le m \le 1$ .

Obviously  $(D[0,1], \leq, \lor, \land)$  form a complete lattice with [0,0] as its least element and [1,1] as its greatest element. We now use D[0, 1] to denote the set of all closed subintervals of the interval [0, 1].

Let L be a given nonempty set. An interval-valued fuzzy set (briefly, i-v fuzzy set) B on L is defined by  $B = \{ (x, [\mu_B^-(x), \mu_B^+(x)]) : x \in L \}$ , where  $\mu_B^-(x)$  and  $\mu_B^+(x)$  are fuzzy sets of L such that  $\mu_B^-(x) \leq \mu_B^+(x)$  for all  $x \in L$ . Let  $\tilde{\mu}_B^-(x) = \left[\mu_B^-(x), \mu_B^+(x)\right]$ , then  $B = \left\{ (x, \widetilde{\mu}_B(x)) : x \in L \right\} \text{ where } \widetilde{\mu}_B : L \to D[0, 1]. \quad \text{A mapping } A = (\widetilde{\mu}_A, \widetilde{\lambda}_A)$ :  $L \rightarrow D[0,1] \times D[0,1]$  is called an interval-valued intuitionistic fuzzy set (i-v IF set, in short) in L if  $0 \le \mu_A^+(x) + \lambda_A^+(x) \le 1$  and  $0 \le \mu_A^-(x) + \lambda_A^-(x) \le 1$  for all  $x \in L$  (that is,  $A^+ = (X, \mu_A^+, \lambda_A^+)$  and  $A^- = (X, \mu_A^-, \lambda_A^-)$  are intuitionistic fuzzy sets), where the mappings  $\widetilde{\mu}_A(x) = [\mu_A^-(x), \mu_A^+(x)] : L \to D[0,1] \text{ and } \widetilde{\lambda}_A(x) = [\lambda_A^-(x), \lambda_A^+(x)] : L \to D[0,1] \text{ denote}$ 



the degree of membership (namely  $\ \widetilde{\mu}_{A}(x)$ ) and degree of non-membership (namely

 $\tilde{\lambda}_A(x)$ ) of each element  $x \in L$  to A respectively.

### 2 Main Result

In this section we introduce fully invariant and characteristic interval–valued intuitionistic fuzzy dual ideals and prove some of its properties.

**Definition 2.1** A dual ideal F of BF-algebra X is said to be a fully invariant dual ideal if  $f(F) \subseteq F$ 

for all  $f \in End(X)$  where End(X) is set of all endomorphisms of BF-algebras X.

**Definition 2.2** An interval-valued IFS  $A = (X, \tilde{\mu}_A, \tilde{\lambda}_A)$  is called interval-valued intuitionistic fuzzy dual ideal (shortly i-v IF dual ideal) of BF-algebra X if satisfies the following inequality

(i-v IF1) 
$$\tilde{\mu}_{A}(1) \ge \tilde{\mu}_{A}(x)$$
 and  $\tilde{\lambda}_{A}(1) \le \tilde{\lambda}_{A}(x)$   
(i-v IF2)  $\tilde{\mu}_{A}(x) \ge \min \left\{ \tilde{\mu}_{A}(N(Nx*Ny)), \tilde{\mu}_{A}(y) \right\}$   
(i-v IF2)  $\tilde{\lambda}_{A}(x) \le \max \left\{ \tilde{\lambda}_{A}(N(Nx*Ny)), \tilde{\lambda}_{A}(y) \right\}$ , for all  $x, y, z \in X$ .

**Example 2.3** Consider a BF-algebra  $X = \{0, 1, 2, 3\}$  with following table.

*	0	1	2	3
0	0	1	2	3
1	1	0	3	2
2	2	3	0	1
3	3	2	1	0

Let A be an interval valued fuzzy set in X defined by  $\tilde{\mu}_A(0) = \tilde{\mu}_A(1) = [0.6, 0.7]$ ,  $\tilde{\mu}_A(2) = \tilde{\mu}_A(3) = [0.2, 0.3]$ ,  $\tilde{\lambda}_A(0) = \tilde{\lambda}_A(1) = [0.1, 0.2]$  and  $\tilde{\lambda}_A(2) = \tilde{\lambda}_A(3) = [0.5, 0.7]$ . It is easy to verify that A is an interval valued intuitionistic fuzzy dual ideal of X.

**Definition 2.4** An interval-valued intuitionistic fuzzy dual ideal  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  of X is called a fully invariant if  $\tilde{\mu}_A^f(x) = \tilde{\mu}_A(f(x)) \le \tilde{\mu}_A(x)$  and  $\tilde{\lambda}_A^f(x) = \tilde{\lambda}_A(f(x)) \le \tilde{\lambda}_A(x)$  for all  $x \in X$  and



 $f \in End(X)$ .

**Theorem 2.5** If  $\{A_i \mid i \in I\}$  is a family of i-v intuitionistic fuzzy fully invariant dual ideals of X,

then  $\bigcap_{i \in I} A_i = (\bigwedge_{i \in I} \widetilde{\mu}_{A_i}, \bigvee_{i \in I} \widetilde{\lambda}_{A_i})$  is an interval-valued intuitionistic fully invariant dual

ideal of X , where

$$\bigwedge_{i\in I} \widetilde{\mu}_{A_{i}}(x) = \inf\{\widetilde{\mu}_{A_{i}}(x) \setminus i \in I, x \in X\} \text{ and } \bigvee_{i\in I} \widetilde{\lambda}_{A_{i}}(x) = \sup\{\widetilde{\lambda}_{A_{i}}(x) \setminus i \in I, x \in X\}.$$

**Theorem 2.6** Let S be nonempty subsets of BF-algebra X and  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  an i-v intuitionistic fuzzy dual ideals defined by

$$\widetilde{\mu}_{A}(\mathbf{x}) = \begin{cases} [s_{2}, t_{2}] & \text{if } \mathbf{x} \in \mathbf{S} \\ [s_{1}, t_{1}] & \text{otherwise,} \end{cases} \text{ and } \widetilde{\lambda}_{A}(\mathbf{x}) = \begin{cases} [\alpha_{2}, \beta_{2}] & \text{if } \mathbf{x} \in \mathbf{S} \\ [\alpha_{1}, \beta_{1}] & \text{otherwise,} \end{cases}$$

Where  $[0,0] \le [s_1,t_1] < [s_2,t_2] \le [1,1], [0,0] \le [\alpha_2,\beta_2] < [\alpha_1,\beta_1] \le [1,1],$ 

 $[0,0] \le [s_i, t_i] + [\alpha_i, \beta_i] \le [1,1]$  for i = 1, 2. If S is an interval-valued intuitionistic fully

invariant dual ideal of X, then  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  is an interval-valued intuitionistic fully invariant dual ideal of X.

**Proof:** We can easily see that  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  is an i-v intuitionistic fuzzy dual ideal of X. Let  $x \in X$  and  $f \in End(X)$ . If  $x \in S$ , then  $f(x) \in f(S) \subseteq S$ . Thus we have

$$\widetilde{\mu}_{A}^{f}(x) = \widetilde{\mu}_{A}(f(x)) \le \widetilde{\mu}_{A}(x) = [s_{2}, t_{2}] \text{ and } \widetilde{\lambda}_{A}^{f}(x) = \widetilde{\lambda}_{A}(f(x)) \le \widetilde{\lambda}_{A}(x) = [\alpha_{2}, \beta_{2}]. \text{ For if }$$

otherwise, we have

$$\widetilde{\mu}_{A}^{f}(x) = \widetilde{\mu}_{A}(f(x)) \leq \widetilde{\mu}_{A}(x) = [s_{1}, t_{1}] \text{ and } \widetilde{\lambda}_{A}^{f}(x) = \widetilde{\lambda}_{A}(f(x)) \leq \widetilde{\lambda}_{A}(x) = [\alpha_{1}, \beta_{1}].$$

Thus, we have verified that  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  is an interval-valued intuitionistic fully invariant dual ideal of X.

**Definition 2.7** An i-v intuitionistic fuzzy dual ideal  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  of X has the same type as an i-v intuitionistic fuzzy dual ideal  $B = (\tilde{\mu}_B, \tilde{\lambda}_B)$  of X if there exist  $f \in End(X)$  such that



$$A = B \circ f \text{ i. e } \widetilde{\mu}_A(x) \geq \widetilde{\mu}_B(f(x)), \widetilde{\lambda}_A(x) \geq \widetilde{\lambda}_B(f(x)) \text{ for all } x \in X \text{ .}$$

**Theorem 2.8** Interval-valued intuitionistic fuzzy dual ideals of X have same type if and only if they are isomorphic.

**Proof:** We only need to prove the necessity part because the sufficiency part is obvious. If an i-v intuitionistic fuzzy dual ideal  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  of X has the same type as  $B = (\tilde{\mu}_B, \tilde{\lambda}_B)$ , then there exist  $\phi \in End(X)$  such that  $\tilde{\mu}_A(x) \ge \tilde{\mu}_B(\phi(x)), \tilde{\lambda}_A(x) \ge \tilde{\lambda}_B(\phi(x))$  for all  $x \in X$ . Let  $f : A(X) \rightarrow B(X)$  be a mapping defined by  $f(A(x) = B(\phi(x)))$  for all  $x \in X$ , i.e,  $f(\tilde{\mu}_A(x)) = \tilde{\mu}_B(\phi(x)), f(\tilde{\lambda}_A(x)) = \tilde{\lambda}_B(\phi(x))$  for  $x \in X$ . Then, it is clear that f is a surjective homomorphism. Also, f is injective because  $f(\tilde{\mu}_A(x)) = f(\tilde{\mu}_A(y))$  for all  $x, y \in X$  implies  $\tilde{\mu}_B(\phi(x)) = \tilde{\mu}_B(\phi(y))$ . Hence  $\tilde{\mu}_A(x) = \tilde{\mu}_B(y)$ . Likewise, from  $f(\tilde{\lambda}_A(x)) = f(\tilde{\lambda}_A(y))$  we conclude  $\tilde{\lambda}_A(x) = \tilde{\lambda}_B(y)$  for all  $x \in X$ . Hence  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  is

isomorphic to  $\mathbf{B} = (\widetilde{\mu}_{B}, \widetilde{\lambda}_{B})$  . This completes the proof.

**Definition 2.9** An ideal C of X is said to be characteristic if f(C) = C for all  $f \in Aut(X)$ where Aut(x) is the set of all automorphisms of X. An i-v intuitionistic fuzzy dual ideal  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  of X is called characteristic if  $\tilde{\mu}_A(f(x) = \tilde{\mu}_A(x)$  and  $\tilde{\lambda}_A(f(x)) = \tilde{\lambda}_A(x)$  for all  $x \in X$  and  $f \in Aut(X)$ .

**Lemma 2.10** Let  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  be an i-v intuitionistic fuzzy dual ideal of X and let  $x \in X$ . Then  $\tilde{\mu}_A(x) = \tilde{t}$ ,  $\tilde{\lambda}_A(x) = \tilde{s}$  if and only if  $x \in U(\tilde{\mu}_A; \tilde{t})$ ,  $x \notin U(\tilde{\mu}_A; \tilde{s})$  and  $x \in L(\tilde{\lambda}_A; \tilde{s})$ ,  $x \notin L(\tilde{\lambda}_A; \tilde{t})$  for all  $\tilde{s} > \tilde{t}$ .

#### **Proof:** Straight forward

**Theorem 2.11** An i-v intuitionistic fuzzy dual ideal is characteristic if and only if each its level set is a characteristic dual ideal.



**Proof:** Let an i-v intuitionistic fuzzy dual ideal  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  be characteristic,

$$\begin{split} \widetilde{t} &\in Im(\widetilde{\mu}_A), f \in Aut(X), x \in U(\widetilde{\mu}_A; \widetilde{t}). \quad \text{Then} \, \widetilde{\mu}_A(f(x)) = \widetilde{\mu}_A(x) \geq \widetilde{t} \text{ , which means that} \\ f(x) &\in U(\widetilde{\mu}_A; \widetilde{t}). \quad \text{Thus} \, f(U(\widetilde{\mu}_A; \widetilde{t})) \subseteq U(\widetilde{\mu}_A; \widetilde{t}). \text{ Since for each} \quad x \in U(\widetilde{\mu}_A; \widetilde{t}) \text{ there exist} \\ y &\in X \text{ such that } f(y) = x \text{ we have } \widetilde{\mu}_A(y) = \widetilde{\mu}_A(f(y)) = \widetilde{\mu}_A(x) \geq \widetilde{t} \text{ , hence we conclude} \\ y &\in U(\widetilde{\mu}_A; \widetilde{t}). \end{split}$$

 $\text{Consequently, } x = f(y) \in f(U(\widetilde{\mu}_A; \widetilde{t}). \quad \text{Hence } f(U(\widetilde{\mu}_A; \widetilde{t}) = U(\widetilde{\mu}_A; \widetilde{t}).$ 

Similarly,  $f(L(\tilde{\lambda}_A; \tilde{s})) = L(\tilde{\lambda}_A; \tilde{s})$ . This proves that  $U(\tilde{\mu}_A; \tilde{t})$  and  $L(\tilde{\lambda}_A; \tilde{s})$  are characteristic.

Conversely, if all levels of  $A = (\tilde{\mu}_A, \tilde{\lambda}_A)$  are characteristic dual ideals of X, then for  $x \in X$ ,

 $f \in Aut(X)$  and  $\tilde{\mu}_A(x) = \tilde{t} < \tilde{s} = \tilde{\lambda}_A(x)$ , by lemma 2.10, we have  $x \in U(\tilde{\mu}_A; \tilde{t}), x \notin U(\tilde{\mu}_A; \tilde{s})$ 

and 
$$x \in L(\lambda_A; \tilde{s}), x \notin L(\lambda_A; \tilde{t})$$
. Thus  $f(x) \in f(U(\tilde{\mu}_A; \tilde{t})) = U(\tilde{\mu}_A; \tilde{t})$  and

$$f(x) \in f(L(\widetilde{\lambda}_A; \widetilde{s}) = L(\widetilde{\lambda}_A; \widetilde{s}) \text{ , i.e. } \widetilde{\mu}_A(f(x)) \geq \widetilde{t} \text{ and } \widetilde{\lambda}_A(f(x)) \leq \widetilde{s} \text{ . For } \widetilde{\mu}_A(f(x)) = \widetilde{t}_l > \widetilde{t} \text{ , }$$

$$\widetilde{\lambda}_A(f(x)) = \widetilde{s}_l < \widetilde{s} \;. \quad \text{We have } f(x) \in U(\widetilde{\mu}_A; \widetilde{t}_l) = f(U(\widetilde{\mu}_A; \widetilde{t}_l), \;\; f(x) \in L(\widetilde{\lambda}_A; \widetilde{s}_l) = f(L(\widetilde{\lambda}_A; \widetilde{s}_l)) \;.$$

Hence  $x \in U(\widetilde{\mu}_A; \widetilde{t}_1)$ ,  $x \in L(\widetilde{\lambda}_A; \widetilde{s}_1)$  this is a contradiction. Thus  $\widetilde{\mu}_A(f(x)) = \widetilde{\mu}_A(x)$  and

 $\widetilde{\lambda}_{A}(f(x)) = \widetilde{\lambda}_{A}(x)$ .So,  $A = (\widetilde{\mu}_{A}, \widetilde{\lambda}_{A})$  is characteristic.

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