

# Investigation of Conventional and AI Techniques for Online Application to Solve ELD, MED and CEED Problems

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#### **Abstact**

In this paper, one conventional and two AI techniques are investigated to find their suitability for ON-LINE application to solve Economic Load Dispatch (ELD), Minimum Emission Dispatch (MED) and Combined Economic and Emission Dispatch (CEED) problem. In this paper, three techniques, Classical Lambda Iteration method, Particle Swarm Optimization (PSO) and Hopfield Neural Network (HNN) are applied to obtain ELD, MED and CEED problem solutions for three, six and fifteen unit test systems. The results obtained show the superiority of HNN technique over the other two techniques. The solutions obtained are quite encouraging. The algorithm and simulations are carried out using MATLAB software.

**Keywords:** ELD, MED, CEED, Conventional Lambda Technique, Particle Swarm Optimization (PSO), Hopfield Neural Network (HNN), Price Penalty Factor-PPF.

# I. Introduction

One of the most important problems in electric power systems is the operation of power system at minimum cost. This problem, known as Economic Load Dispatch (ELD), minimizes system cost by properly allocating the real power demand amongst the online generating units. Economic load dispatch is one of the principal functions of energy management systems.

The main objective of the ELD problem is to determine the optimum combination of power outputs of all generating units which minimizes the total fuel cost while satisfying the system constraints. The objective of Emission Dispatch problem is to minimize the total environmental degradation of the power system while satisfying the system constraints. Both the objectives of Economic Dispatch and Emission Dispatch problems are considerably different, as the ELD problem deals with minimizing the total fuel cost at an increased emission level whereas MED deals with minimizing the emission level at an increased system operating cost. Therefore, there should be an operating point that strikes a balance between the cost and emission. This is achieved by Combined Economic and Emission Dispatch (CEED) problem.

The objective of CEED problem is to minimize the total operating cost of the power system while satisfying demand and generating limit constraints. The bi-objective CEED is converted into a single optimization problem by introducing a term called Price Penalty Factor.

The proposed techniques are applied to obtain ELD, MED and CEED solutions of three test systems (3-Gen., 6-Gen. and 15-Gen. Unit Test Systems). Investigation of these three techniques is carried out w.r.t Total Operating Cost, Total Emission, Minimum Emission, System Losses and Computation-Time.

### II. Problem Formulation

## A. Economic Dispatch Formulation

Consider a power generation system with 'i' generators. The ELD problem is to find the optimal combination of power generation that minimizes the total cost while satisfying the total demand. The cost function of ELD which is to be optimized is defined as follows:

$$F = \sum f_i(P) = (a_i P_i^2 + b_i P_i + c_i)$$
 (1)

where F is the total fuel cost in Rs/hr,  $f_i$  (P<sub>i</sub>) is the cost of the  $i^{th}$  generator in Rs/hr; P<sub>i</sub> the power output of generator i in MW;  $a_i$ ,  $b_i$  and  $c_i$  are the cost coefficients of the  $i^{th}$  generator.

# B. Emission Dispatch Problem

The total emission of atmospheric pollutants caused by fossils-fuelled thermal units can be expressed as  $E = \sum_{i} (\alpha_{i} P_{i}^{2} + \beta_{i} P_{i} + \gamma_{i}) \tag{2}$ 

where E is the total emission level in Kg/hr,  $\alpha_i$ ,  $\beta_i$  and  $\gamma_i$  are the emission coefficients of the  $i^{th}$  generator.



## C. Problem Constraints

For stable operation of power system, the power output of each generator is restricted within its lower and upper limits, i.e.,

$$P_{i \min} \le P_i \le P_{i \max} \tag{3}$$

And the total active power generation must balance the predicted load demand plus losses, at each time interval over the scheduling time horizon.

$$\sum P_{i} = P_{D} + P_{L} \tag{4}$$

## D. Combined Economic and Emission Dispatch Problem

The bi-objective CEED problem, which minimizes the total operating cost, is converted into single optimization problem by introducing Price Penalty Factor, h. The price penalty factor is the ratio between the maximum fuel cost and maximum emission of the corresponding generator.

$$h_i = F(P_{i max}) / E(P_{i max}) i=1,2...n$$
 (5)

# III. Particle Swarm Optimization (PSO)

In 1965, Kennedy and Eberhart [1995] first introduced the Particle Swarm Optimization (PSO) method, motivated by social behavior of organisms such as fish schooling and bird flocking. PSO, as an optimization tool, provides a population – based search procedure in which individuals called particles change their positions (states) with time. In a PSO system particles lie around in a multidimensional search space. During flight, each particle adjusts its position according to its own experience, and the experience of neighboring particles, making use of the best position encountered by itself and its neighbors. The swarm direction of a particle is defined by the set of particles neighboring the particle and its history experience.

# PSO Algorithm

Step1: Initial Swarm and velocities of each particle/agent are randomly generated within the allowable search range. The current searching point is set to pbest (particle best) for each agent. The best evaluated value of pbest is set to gbest (global best).

Step2: The objective function value is calculated for each agent/particle. If the current value is better than previous poest of the particle, then the poest value is replaced by the current value. If the best value of poest is better than the previous gbest, the gbest is replaced by the current gbest value.

Step3: The current searching point of each agent/particle is changed using 
$$v_{ij}^{r+1} = w^* v_{ij}^r + C_1^* R_1^* (Pb_{ij}^r - P_{ij}^r) + C_2^* R_2^* (G_j^r - P_{ij}^r)$$
(6) 
$$i = 1, 2, \dots, NP;$$
$$j = 1, 2, \dots, NG.$$
$$P_{ij}^{r+1} = P_{ij}^r + v_{ij}^{r+1}$$
(7)

In general, the inertia weight w is set according to the following equation:

$$w = w^{max} - \underline{w^{max} - w^{min} *} IT$$

$$IT^{max}$$
 (8)

where,

IT<sup>max</sup> is the maximum number of iterations (generations), and IT is the current number of iterations.

Step4: Check the Stopping Criterion.

## **Modified Hopfield Neural Network**

In this paper, a Modified Hopfield Neural Network Method is employed with Linear Input-Output Function. The Power mismatch (Pm), can be predetermined at any small value one expects such that the dynamic equation of a neuron has the merit that it is not related to any other neurons. Consequently, each neurons dynamic performance can be simply described using a first order differential equation.

To solve the CEED problem without Losses using Modified HNN Method, energy function including

both power mismatch (
$$P_m$$
), and total operating cost  $F_t$  is defined as follows: 
$$E = (D/2)[(P_D + P_L) - \sum P_i]^2 + (G/2) \sum (A_i P_i^2 + B_i P_i + C_i)$$

$$E = (D/2)P_m^2 + (G/2) \phi$$
 (9) where,  $A_i = a_i + h\alpha_i$ 

$$B_i = b_i + h\beta_i \qquad \text{and} \qquad C_i = c_i + h\gamma_i$$

$$\frac{d\phi(P_i)}{dP_i} = 2A_i P_i + B_i$$
 (10)

D and G are positive weighting factors. By comparing (9) with the energy function of the conventional HNN, we



get

$$T_{ii} = -D - GC_i \tag{11}$$

$$T_{ij} = -D \tag{12}$$

$$I_i = DP_D - GB_i/2 \tag{13}$$

The dynamic equation of a neuron is given as

$$\frac{dU_i}{dt} = \sum_j T_{ij} P_j + I_i \tag{14}$$

Substituting (11), (12) and (13) into (14) the dynamic equation becomes

$$dU_i / dt = DP_m - (G/2)(d\phi_i / dP_i)$$
(15)

The dynamic equation is obtained by substituting eq.10 into eq. 15

 $dUi/dt = DP_m - (G/2) [B_i + 2A_i(K_{1i}U_i + K_{2i})]$ 

$$=K_{3i} U_i + K_{4i}$$
 (16)

where

$$K_{3i} = -GC_i K_{1i} = -GA_i(P_{imax} - P_{imin}) / (U_{max} - U_{min})$$

 $K_{4i} = DP_m - (G/2) B_i - GA_i K_{2i}$ 

Here,  $K_{3i}$  has relation to decaying speed, and its value is negative. Solving (16), the neurons input function,  $U_i(t)$  is obtained as

$$U_{i}(t) = [U_{i}(0) + (K_{4i}/K_{3i})]e^{K3it} + (-K_{4i}/K_{3i})$$
(17)

The neurons output function,  $P_i(t)$ , is obtained as

$$P_{i}(t) = (K_{1i} U_{i}(0) + K_{2i} - [(2K_{AB}P_{m} - B_{i})/(2A_{i})])e^{k3it} + [(2K_{AB}P_{m} - B_{i})/(2A_{i})]$$
(18)

where  $K_{AB} = A/B$ .

Because of  $K_{3i}$ < 0 the exponential term on the right side of the above Eqn. (8.11) is of transient existence. This term decays exponentially and finally becomes vanishingly small eventually setting t= $\infty$  for (18) then

$$P_{i}(\infty) = (2K_{AB}P_{m} - B_{i})/2A_{i}$$

$$\tag{19}$$

Here  $P_i(\infty)$  represents the optimal generation level for unit i. The power mismatch  $P_m$  which is defined as the power demand less the total generating power is expressed as

$$P_{m} = [P_{D} + (1/2)\sum(B_{i}/A_{i})] / [K_{AB}\sum(1/A_{i})+1]$$

Appropriately selecting KAB, we have

 $K_{AB} \sum (1/A_i) >> 1$ 

Finally, an useful approximate formula for  $P_{\text{m}}$  can be written as

$$P_{\rm m} = [P_{\rm D} + (1/2)\sum(B_{\rm i}/A_{\rm i})] / [K_{\rm AB}\sum(1/A_{\rm i})]$$

# V. Results and Analysis

**Case1:** 3-Generating Unit Test System

The 3-Gen. Unit Test System consists of three generators with a load demand of 500 MW [16]. Owing to the limit of space, the parameters of the units and the B loss coefficients matrix cannot be listed.

Table 1: Results of ELD without Losses for a Power Demand of 500 MW

P <sub>D</sub> (MW)	Description	A method	l PSO	HNN		
500	Total Cost (Rs./hr)	24924.126	3 24580.1364	24924.1218		
	Computation-Time in Seconds					
Conventional Lambda Method			0.047506			
Particle Swarm Optimization			0.23164			
Hopfield Neural Network			0.007342			

	P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method	PSO	HNN
		$P_{G1}$	97.2251	92.5867	97.22505
	500	$P_{G2}$	210.159	236.4381	210.1589
		$P_{G3}$	192.616	181.643	192.6159



Table 2: Results of ELD with Losses for a Power Demand of 500 MW

P <sub>D</sub> (MW)	Description	λ-Me	thod	PSO	HNN		
500	Total Cost (Rs./hr)	25467.3289		23074.777	25465.4307		
300	Loss (MW)	11.9933		8.8139	11.9143		
	Computation-Time in Seconds						
Conver	Conventional Lambda Method			0.049058			
Particle Swarm Optimization			0.564688				
Hopfield Neural Network			0.038041				

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	99.80379	83.086	105.8804
500	$P_{G2}$	214.4906	297.73	212.7289
	$P_{G3}$	197.6889	137.62	193.3042

Table 3: Results of MED without Losses for a Power Demand of 500MW

$P_{D}$ (MW) Description $\lambda$ -1		λ-Me	thod	PSO	HNN		
500	Total Emission (Kg/hr)	296.8	3268	300.0031	296.7952		
	Computation-Time in Seconds						
Con	Conventional Lambda Method			0.0605			
Particle Swarm Optimization			0.2387				
Hopfield Neural Network			0.0163				

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	129.8752	126.7495	128.0191
500	$P_{G2}$	185.0624	196.8482	185.9904
	$P_{G3}$	185.0624	178.7558	185.9904

Table 4: Results of MED with Losses for a Power Demand of 500MW

P <sub>D</sub> (MW)	Description	λ-Me	thod	PSO	HNN	
500	Total Emission (Kg/hr)	311.	.082	308.7924	311.0773	
300	Loss (MW)	11.6	787	9.0963	11.6727	
Computation-Time in Seconds						
Conventional Lambda Method				0.0589	)	
Particle Swarm Optimization			0.6011			
Hopfield Neural Network			0.043			

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	130.9659	84.6997	131.5437
500	$P_{G2}$	190.3562	186.9572	190.264
	$P_{G3}$	190.3562	243.671	189.864

 Table 5: Results of CEED without Losses for a Power Demand of 500MW

$P_{D}(MW)$	PPF (h) in Rs./Kg	Description	λ-Method	PSO	HNN		
500	44.806	Total Cost (Rs./hr)	38264.488	37655.0977	38264.478		
	Computation-Time in Seconds						
	Conventional Lambda Method			0.038223			
Particle Swarm Optimization			0.346507				
Hopfield Neural Network				0.004942			

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	124.9274	133.5104	124.9274
500	$P_{G2}$	188.3903	170.663	188.3902
	$P_{G3}$	186.6823	197.802	186.6823



Table 6: Results of CEED with Losses for a Power Demand of 500MW

P <sub>D</sub> (MW)	PPF (h) in Rs./Kg	Description	λ-Method	PSO	HNN		
500	44.806	Total Cost(Rs./hr)	39436.9253	39479.9062	39436.0592		
300	44.806	Loss (MW)	11.7035	11.7043	11.6935		
	Computation-Time in Seconds						
	Conventional Lambda Method			0.03883			
Particle Swarm Optimization			0.396325				
Hopfield Neural Network			0.039649				

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	127.8382	129.91	128.8256
500	$P_{G2}$	192.7562	192.30	192.5791
	$P_{G3}$	191.109	189.90	190.2853

**Analysis**: From case 1, it is observed that PSO technique provides better result in terms of total cost, reduced losses when compared to other two techniques for ELD, MED problems. In case of MED, PSO provides better emission than PSO and Conventional Lambda technique. For practical application HNN technique provides a better result in terms of total cost, reduced system losses as well as computationally fast.

Case 2: 6- Generating Unit Test System

An IEEE-30 bus system is considered, which consists of 6 generators for a Power Demand of 900MW. The system parameters, Loss Coefficients are presented in [17].

Table7: Results of ELD without Losses for a Power Demand of 900 MW

P <sub>D</sub> (MW)	Description	λ-Method		PSO	HNN		
900	Total Cost(Rs./hr)	45464.157		45399.9543	45464.1521		
	Computation-Time in Seconds						
Conver	Conventional Lambda Method			0.032178			
Particle Swarm Optimization			0.315269				
Hopfield Neural Network				0.00985	3		

$P_{D}$ (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	32.4969	41.449	32.4969
	$P_{G2}$	10.81598	20.947	10.81597
900	$P_{G3}$	143.6467	224.3	143.6467
900	$P_{G4}$	143.0317	136.45	143.0316
	$P_{G5}$	287.1036	275.31	287.1036
	$P_{G6}$	282.9051	209.94	282.9051

Table 8: Results of ELD with Losses for a Power Demand of 900 MW

Table 6. Iteland of EED Will Eddeed for all over Demand of 200 111 V							
P <sub>D</sub> (MW)	Description	λ-Method	PSO	HNN			
900	Total Cost (Rs./hr)	47065.5716	44982.3142	47035.1907			
900	Loss (MW)	32.931	29.4422	31.7216			
Computation-Time in Seconds							
Conventional Lambda Method 0.04087			7				
Particle Swarm Optimization			0.754222				
Hopfield Neural Network			0.038594				

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	33.67818	41.666	38.34618
	$P_{G2}$	12.51721	24.937	21.38999
900	$P_{G3}$	150.0723	161.65	163.4752
900	$P_{G4}$	148.1109	124.32	152.8626
	$P_{G5}$	295.6356	314.34	283.5868
	$P_{G6}$	292.9168	309.89	272.0664



Table 9: Results of MED without Losses for a Power Demand of 900 MW

P <sub>D</sub> (MW)	Description	λ-Method F		PSO	HNN
900	Total Emission (lb/hr)	698.5438		701.046	646.1284
Computation-Time in Seconds					
Conv	rentional Lambda Method		0.03446		
Particle Swarm Optimization			0.32018		
Hopfield Neural Network			0.00902		

$P_{D}(MW)$	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	55.58136	105.32	116.9927
	$P_{G2}$	55.58136	128.39	116.9927
900	$P_{G3}$	161.9423	120.82	135.6939
900	$P_{G4}$	161.9423	126.47	135.6939
	$P_{G5}$	232.4763	181.2	197.3133
	$P_{G6}$	232.4763	268.28	197.3133

Table 10: Results of MED with Losses for a Power Demand of 900 MW

P <sub>D</sub> (MW)	Description	λ-Me	thod	PSO	HNN		
900	Total Emission (lb/hr)	679.0766		717.6656	678.9358		
900	Loss (MW)	24.7979		26.3243	24.5913		
	Computation-Time in Seconds						
Conv	Conventional Lambda Method			0.035832			
Particle Swarm Optimization			0.71995				
Hopfield Neural Network			0.034848				

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	121.9083	13.421	124.1611
	$P_{G2}$	121.9083	62.089	125.1892
900	$P_{G3}$	138.7095	200.47	138.99
900	$P_{G4}$	138.7095	207.2	138.1487
	$P_{G5}$	201.7811	256.87	199.3437
	$P_{G6}$	201.7811	189.43	198.7581

Table 11: Results of CEED without Losses for a Power Demand of 900 MW

P <sub>D</sub> (MW)	PPF(h) in Rs./Kg	Descr	iption	λ-Method	PSO	HNN
900	47.822	Total Cos	st (Rs./hr)	78208.674	78050.8478	78208.6623
Computation-Time in Seconds						
Conventional Lambda Method				0.0	064037	
Particle Swarm Optimization				0.5	514841	
Hopfield Neural Network				0.0	005864	

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	88.63243	92.342	88.63242
	$P_{G2}$	P <sub>G2</sub> 89.67917		89.67915
000	$P_{G3}$	144.4325	75.32	144.4325
900	$P_{G4}$	144.3562	115.30	144.3562
	$P_{G5}$	217.0664	221.18	217.0664
	$P_{G6}$	215.8333	302.77	215.8332



Table 12: Results of CEED with Losses for a Power Demand of 900 MW

$P_{D}$ (MW)	PPF (h) in Rs./Kg	Description	λ-Method	PSO	HNN		
900	47.822	Total Cost (Rs./hr)	81354.4119	81355.726	81333.9164		
		Loss (MW)	26.6391	26.6398	26.3069		
	Computation-Time in Seconds						
Cor	Conventional Lambda Method			0.046405			
Particle Swarm Optimization			0.600675				
Hopfield Neural Network			0.043807				

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	92.40464	92.405	95.39424
	$P_{G2}$	94.02537	94.025	98.86849
900	$P_{G3}$	148.1855	148.19	149.1057
900	$P_{G4}$	148.0321	148.03	147.5048
	$P_{G5}$	222.5762	222.58	218.8518
	$P_{G6}$	221.4151	221.42	216.5777

**Analysis:** From case 2, i.e., 6 Gen. Unit Test System for a power demand of 900 MW, it is observed that PSO technique provides a better cost, reduced system losses when compared to other two techniques for an ELD problem. In case of MED, HNN technique provides better emission than other two techniques. For CEED problem, HNN technique gives better result in terms of total operating cost, minimum emission, reduced losses as well as computationally fast.

Case 3: 15 Generating Unit Test System

15- Generating Unit Test System consists of 15 generators for a Power Demand of 2630 MW.

Table 13: Results of ELD without Losses for a Power Demand of 2630MW

P <sub>D</sub> (MW)	Description	λ-Method	PSO	HNN	
2630	Fuel Cost (Rs./hr)	32257	31792	32257	
	Run-Time Con	nparison in S	Seconds		
Conventional Lambda Method			0.03334		
Particl	e Swarm Optimization	n	0.6573		
Hopf	ield Neural Network		0.0409	)	

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	455	438.04	455
	$P_{G2}$	455	300.67	455
	$P_{G3}$	130	106.85	130
	$P_{G4}$	130	30.115	130
	$P_{G5}$	271.18	434.06	271.18
	$P_{G6}$	460	459.76	460
	$P_{G7}$	465	417.99	465
2630	$P_{G8}$	60	68.283	60
	$P_{G9}$	25	80.735	25
	$P_{G10}$	25	33.768	25
	$P_{G11}$	43.389	79.987	43.3887
	$P_{G12}$	55.431	40.21	55.4311
	$P_{G13}$	25	35.601	25
	$P_{G14}$	15	50.241	15
	$P_{G15}$	15	54.454	15



**Table 14**: Results of ELD with Losses for a Power Demand of 2630 MW

P <sub>D</sub> (MW)	Description	λ-Method PSO HN			
2620	Fuel Cost (Rs./hr)	32560	32832	32670.6254	
2630	Loss (MW)	28.835	38.615	28.777	
	Run-Ti	me Comparison in Seco	nds		
Conve	entional Lambda Met	thod	0.78400		
Particle Swarm Optimization		tion	1.4167		
Hoj	pfield Neural Networ	·k	0.0395		

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	455	275.47	150
	$P_{G2}$	455	437.72	455
	$P_{G3}$	130	101.69	130
	$P_{G4}$	130	118.38	130
	$P_{G5}$	297.53	440.73	470
	$P_{G6}$	460	322.53	460
	$P_{G7}$	465	399.32	465
2630	$P_{G8}$	60	166.85	60
	$P_{G9}$	25	136.98	25
	$P_{G10}$	25	37.663	98.7769
	$P_{G11}$	44.895	54.414	80
	$P_{G12}$	56.411	72.638	80
	$P_{G13}$	25	76.121	25
	$P_{G14}$	15	32.54	15
	$P_{G15}$	15	16.364	15

Table 15: Results of MED without Losses for a Power Demand of 2630 MW

$P_{D}$ (MW)	Description	λ-Method	d PSO	HNN		
2630	Total Emission (lb/hr)	3427.2905	7933.3166	3427.2902		
	Run-Time Comparison in Seconds					
Conv	Conventional Lambda Method			0.039347		
Particle	Swarm Optimization (PS	<b>5O</b> )	0.682377			
Hopfie	ld Neural Network (HNN	0)	0.029945			

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	455	434.8853	455
	$P_{G2}$	368.6461	434.3304	368.646
	$P_{G3}$	45.15943	78.4912	45.15943
	$P_{G4}$	130	124.2692	130
	$P_{G5}$	130	344.487	150
	$P_{G6}$	150	438.4005	135
	$P_{G7}$	135	293.1891	369.1944
2630	$P_{G8}$	369.1945	204.263	300
	$P_{G9}$	300	30.4301	162
	$P_{G10}$	162	156.2781	160
	$P_{G11}$	160	55.7061	80
	$P_{G12}$	80	78.8129	80
	$P_{G13}$	80	62.4025	85
	$P_{G14}$	85	41.4214	55
	$P_{G15}$	55	42.4821	55



Table 16: Results of MED with Losses for a Power Demand of 2630 MW

P <sub>D</sub> (MW)	Description	λ-Metho		od	PSO	HNN
2630	Total Emission (lb	/hr)	5770	.7112	9058.7713	4384.4285
2030	Loss (MW)		388.	4587	54.2608	387.761
	Run-Time Comparison				conds	
Convo	Conventional Lambda Method		]	0.823596		
Particle Swarm Optimization (PSO)			1.4679			
Hopfield Neural Network (HNN)		0.041687				

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	455	263.191	455
	$P_{G2}$	455	420.6357	455
	$P_{G3}$	130	70.4227	130
	$P_{G4}$	130	108.5654	130
	$P_{G5}$	191.0303	313.6179	150
	$P_{G6}$	215.2773	363.6523	135
	$P_{G7}$	465	457.4283	465
2630	$P_{G8}$	300	291.6469	300
	$P_{G9}$	162	123.9988	162
	$P_{G10}$	160	134.1981	160
	$P_{G11}$	80	36.8355	80
	$P_{G12}$	80	76.6688	80
	$P_{G13}$	85	28.615	85
	$P_{G14}$	55	43.9092	55
	$P_{G15}$	55	16.1217	55

Table 17: Results of CEED without Losses for a Power Demand of 2630MW

P <sub>D</sub> (MW)	PPF (h) in Rs./Kg	Description	λ-Method	PSO	HNN	
2630	13.2870	Total Cost(Rs./hr)	78744.81	105045.88	78744.80	
	Computation-Time in Seconds					
	Conventional Lambda Method			0.05658		
Particle Swarm Optimization				0.50986		
	Hopfield Neural Network			0.03197		

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
	$P_{G1}$	454.8143	390.1487	455
	$P_{G2}$	366.6624	379.2113	366.5752
	$P_{G3}$	46.59585	128.8317	46.58659
	$P_{G4}$	130	127.9059	130
	$P_{G5}$	150	174.644	150
	$P_{G6}$	135	269.5435	135
	$P_{G7}$	369.9274	460.3626	369.8381
2630	$P_{G8}$	300	171.8644	300
	$P_{G9}$	162	158.5007	162
	$P_{G10}$	160	152.9686	160
	$P_{G11}$	80	75.5318	80
	$P_{G12}$	80	48.8405	80
	$P_{G13}$	85	50.1766	85
	$P_{G14}$	55	38.7588	55
	$P_{G15}$	55	45.6668	55



P <sub>D</sub> (MW)	PPF (h) in Rs./Kg	Description	λ-Method	PSO	HNN		
2630 13.2870	Total Cost (Rs./hr)	113789.5217	145632.2137	94092.2341			
2030	13.2670	Loss (MW)	388.4787	145.1269	388.4787		
	Run-Time Comparison in Seconds						
Conventional Lambda Method				3.2543			
Particle Swarm Optimization				6.1056			
Hopfield Neural Network				0.05617			

P <sub>D</sub> (MW)	Gen. Unit No.	λ-Method (MW)	PSO (MW)	HNN (MW)
2630	$P_{G1}$	455	330.7868	455
	$P_{G2}$	455	375.7288	455
	$P_{G3}$	130	121.6557	130
	$P_{G4}$	130	109.8083	130
	$P_{G5}$	190.9695	212.6889	150
	$P_{G6}$	215.4891	452.3237	135
	$P_{G7}$	465	433.4686	465
	$P_{G8}$	300	261.3454	300
	$P_{G9}$	162	87.7303	162
	$P_{G10}$	160	56.4719	160
	$P_{G11}$	80	52.4599	80
	$P_{G12}$	80	52.768	80
	$P_{G13}$	85	58.9815	85
	$P_{G14}$	55	47.0678	55
	$P_{G15}$	55	17.7119	55

**Analysis**: From case 3, i.e., 15 Gen. Unit Test System for a power demand of 2630 MW, it is observed that for a pure ELD problem PSO technique gives better solution in terms of cost and reduced losses. But computationally, HNN technique is faster than other two techniques. In case of MED problem, HNN technique provides minimum emission, minimum losses as well as computationally fast. For CEED problem, HNN technique gives a better optimum solution in terms of total operating cost, minimum emission level, reduced system losses and faster computation.

## VI. CONCLUSIONS

From the case studies, it is observed that for pure ELD problem, the Particle Swarm Optimization (PSO) technique provides a better solution in terms of total cost and reduced system losses. But computationally, HNN technique is faster than other two techniques. For MED problem, PSO technique provides minimum emission in case of small generating unit test systems whereas HNN technique gives minimum emission level for large generating unit test systems. In case of CEED problem, HNN technique provides a better solution w.r.t. total operating cost, minimum emission, reduced system losses as well as computationally fast. Hence, Hopfield Neural Network (HNN) technique is suitable for ON-LINE application of power system whereas for pure ELD problem, PSO technique gives better solution in terms of total cost, reduced system losses.

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