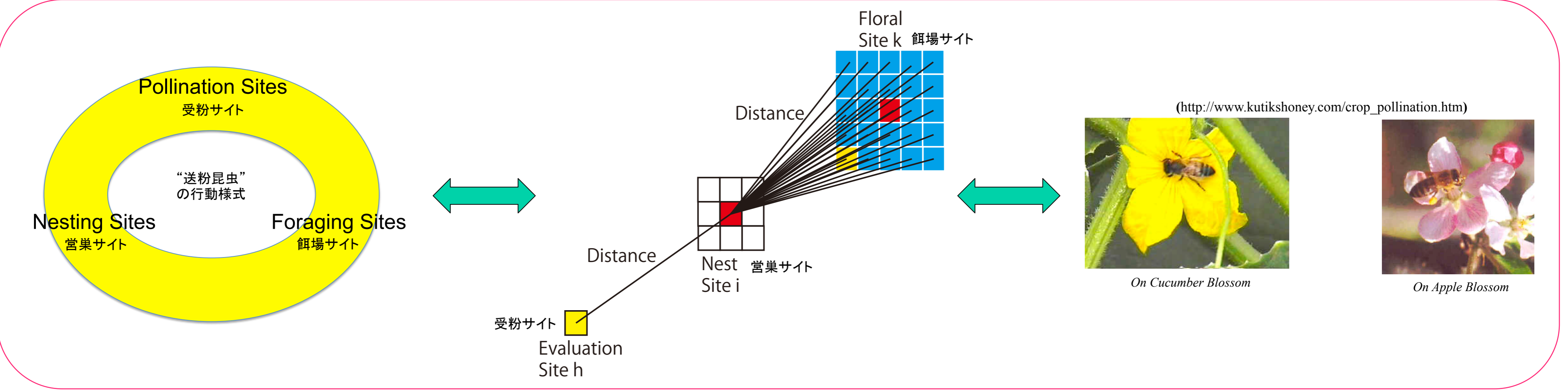


空間的非線形評価を伴う受粉サービスに対する離散最適化

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【受粉サービス】

受粉を必要とする農作物の生産では、ミツバチなど“送粉昆虫”の果たす役割は生態系がもたらす重要な“生態系サービス”の一つである。ミツバチが蜜・花粉を求めて飛び回る際、体毛に花粉が付着し、雌しべの先につくことにより受粉が完了する。また、閉鎖環境のハウスなどにおいても、野生の送粉昆虫による受粉ではないものの、花の開花時期に合わせて花粉交配専用の飼養ミツバチを導入し、ハウス内に巣箱を設置することによりミツバチの飛翔を促し、受粉が完了する。



【研究目的】

本研究では、土地利用の改変に伴う効率的な花粉交配を念頭に蜂場・蜜源の最適配置を探索できる離散最適化システムの構築を目指し、限られた送粉昆虫資源に対し受粉サービスの効率的・効果的な供給を可能にする土地利用管理を探索する。

【受粉スコア(Pollination Score by Landsdorf et al., Ann. Bot., 2009)】

“Since pollinator abundance is limited by both nesting and floral resources, the pollinator score on a parcel is simply **the product of foraging and nesting**. This score represents the location and relative abundance of pollinators available for crop pollination from a parcel.”

$$\text{Pollination Score} = \text{Habitat Suitability for Nesting} \times \text{Habitat Suitability for Foraging}$$

Habitat suitability for Nesting by a pollinator at k -parcel

$$HN_k = \sum_{j=1}^J N_j p_{jk} = \sum_{j=1}^J \nu_k(j)$$

j : j -habitat (land use) J : the number of habitats for a parcel
 k : k -parcel
 N_j : Compatibility of j -habitat for a pollinator's nesting
 p_{jk} : Proportion by j -habitat at k -parcel

Habitat suitability for Foraging for a pollinator at k -parcel

$$HF_k = \frac{\sum_{m=1}^M \sum_{j=1}^J F_j p_{jm} \exp(-D_{mk} / \alpha)}{\sum_{m=1}^M \exp(-D_{mk} / \alpha)} = \frac{\sum_{m=1}^M \sum_{j=1}^J \varphi_m(j) \exp(-D_{mk} / \alpha)}{\sum_{m=1}^M \exp(-D_{mk} / \alpha)}$$

D_{mk} : Distance from k -parcel to m -parcel
 F_j : Compatibility of j -habitat for a pollinator
 α : Expected pollinator foraging distance
 M : The number of parcels

Pollination Score induced by a pollinator at k -parcel $\rightarrow P_k = HN_k \cdot HF_k$
 Pollination Service at h -parcel by a pollinator $\rightarrow PS_h = \left\{ \sum_{k=1}^M P_k \exp(-D_{hk} / \alpha) \right\} / \sum_{k=1}^M \exp(-D_{hk} / \alpha)$

Decision variables: Land use selection for a parcel

$$x_{ij} = \begin{cases} 1 & \text{if the } j\text{-th habitat is selected for the } i\text{-th parcel} \\ 0 & \text{otherwise} \end{cases}, \sum_{j=1}^J x_{ij} = 1 \quad \forall i$$

Nonlinearity to linearity by a new variable

$$Y = X \otimes X, \quad y_{M(i-1)+k, J(j-1)+l} = x_{ij} \cdot x_{kl} = x_{kl} \cdot x_{ij} = y_{M(k-1)+i, J(l-1)+j}$$

Constraints among variables from habitat nest
 If $x_{ij} = 0 \Rightarrow x_{ij} \cdot X = 0_m$, $\sum_{i=1}^M y_{M(i-1)+k, J(j-1)+l} = 0 \quad (k=1, 2, \dots, M)$
 If $x_{ij} = 1 \Rightarrow x_{ij} \cdot X = 1_m$, $\sum_{i=1}^M y_{M(i-1)+k, J(j-1)+l} = 1 \quad (k=1, 2, \dots, M)$

Constraints among variables from habitat floral site
 If $x_{kl} = 0 \Rightarrow X \cdot x_{kl} = 0_M$, $\sum_{j=1}^J y_{M(k-1)+i, J(l-1)+j} = 0 \quad (i=1, 2, \dots, M)$
 If $x_{kl} = 1 \Rightarrow X \cdot x_{kl} = 1_M$, $\sum_{j=1}^J y_{M(k-1)+i, J(l-1)+j} = 1 \quad (i=1, 2, \dots, M)$

Pollination Score expressed by decision variables

$$P_k = \sum_{m=1}^M \sum_{l=1}^J \sum_{j=1}^J \nu_l x_{kl} \varphi_j x_{mj} \exp(-D_{mk} / \alpha) / \sum_{m=1}^M \exp(-D_{mk} / \alpha)$$

$\nu_l(l) = \nu_l x_{kl}$: Nesting score for l -habitat at k -parcel
 $\varphi_m(j) = \varphi_j x_{mj}$: Foraging score for j -habitat at m -parcel

【モデリングと結果】

Example

25 parcels

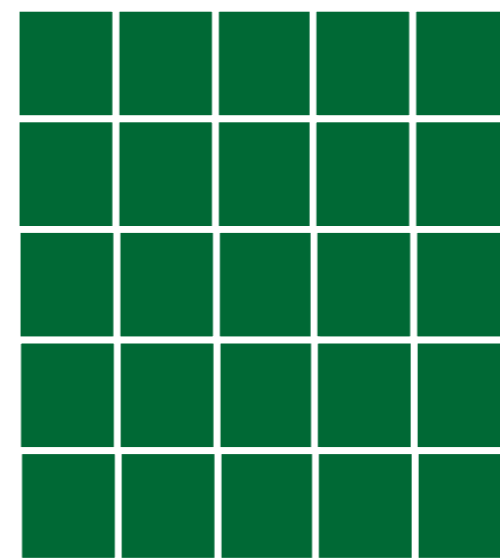
5	21	22	23	24	25
4	16	17	18	19	20
3	11	12	13	14	15
2	6	7	8	9	10
1	1	2	3	4	5
1	2	3	4	5	

- Forest
- Coffee
- Cane
- Pasture/Grass
- Scrub
- Bare
- Built

1. Maximize pollination service only

$$J = \max \sum_{h=1}^M PS_h = \sum_{h=1}^M \sum_{k=1}^M \sum_{j=1}^J \nu_k(j) \varphi_j x_{hj} \exp(-D_{hk} / \alpha) / \sum_{k=1}^M \exp(-D_{hk} / \alpha)$$

subject to
 $Z = Y(I_j \otimes \text{diag}(\varphi_1, \varphi_2, \dots, \varphi_J)) \{ \text{diag}(\nu_1, \nu_2, \dots, \nu_J) \otimes I_J \}$
 $x_i X \mathbf{1}_J = x_i \mathbf{1}_M \quad (i=1, 2, \dots, M, j=1, 2, \dots, J)$
 $(X x_k) \mathbf{1}_J = x_k \mathbf{1}_M \quad (k=1, 2, \dots, M, l=1, 2, \dots, J)$
 $\sum_i x_i = 1 \quad \forall i$



2. Maximize pollination service subject to limit for pollination service

$$J = \max \sum_{h=1}^M PS_h = \sum_{h=1}^M \sum_{k=1}^M \sum_{j=1}^J \nu_k(j) \varphi_j x_{hj} \exp(-D_{hk} / \alpha) / \sum_{k=1}^M \exp(-D_{hk} / \alpha)$$

subject to
 $\sum_{h=1}^M \sum_{k=1}^M \sum_{j=1}^J \nu_k(j) \varphi_j x_{hj} \exp(-D_{hk} / \alpha) \leq 5$
 $Z = Y(I_j \otimes \text{diag}(\varphi_1, \varphi_2, \dots, \varphi_J)) \{ \text{diag}(\nu_1, \nu_2, \dots, \nu_J) \otimes I_J \}$
 $x_i X \mathbf{1}_J = x_i \mathbf{1}_M \quad (i=1, 2, \dots, M, j=1, 2, \dots, J)$
 $(X x_k) \mathbf{1}_J = x_k \mathbf{1}_M \quad (k=1, 2, \dots, M, l=1, 2, \dots, J)$
 $\sum_i x_i = 1 \quad \forall i$



3. Maximize benefits from land use subject to limit for pollination service

$$J = \max \sum_{h=1}^M \sum_{k=1}^M \sum_{j=1}^J b_j x_{hj} \exp(-D_{hk} / \alpha) / \sum_{k=1}^M \exp(-D_{hk} / \alpha)$$

subject to
 $\sum_{h=1}^M \sum_{k=1}^M \sum_{j=1}^J \nu_k(j) \varphi_j x_{hj} \exp(-D_{hk} / \alpha) \leq 5$
 $Z = Y(I_j \otimes \text{diag}(\varphi_1, \varphi_2, \dots, \varphi_J)) \{ \text{diag}(\nu_1, \nu_2, \dots, \nu_J) \otimes I_J \}$
 $x_i X \mathbf{1}_J = x_i \mathbf{1}_M \quad (i=1, 2, \dots, M, j=1, 2, \dots, J)$
 $(X x_k) \mathbf{1}_J = x_k \mathbf{1}_M \quad (k=1, 2, \dots, M, l=1, 2, \dots, J)$
 $\sum_i x_i = 1 \quad \forall i$

b_j		
1	Forest	0.3
2	Coffee	1
3	Cane	1.2
4	Pasture/grass	0.7
5	Scrub	0.1
6	Bare	0
7	Built	0

