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Additional results for "Joint entropy of continuously differentiable ultrasonic waveforms" [J. Acoust. Soc. Am. 133(1), 283–300 (2013)] (L)

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Previous results on the use of joint entropy for detection of targeted nanoparticles accumulating in the neovasculature of MDA435 tumors [Fig. 7 of M. S. Hughes *et al.*, J. Acoust. Soc. Am. **133**, 283–300 (2013)] are extended, with sensitivity improving by nearly another factor of 2. This result is obtained using a "quasi-optimal" reference waveform in the computation of the joint entropy imaging technique used to image the accumulating nanoparticles.

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[KGS] Pages: 501–501

In this Comment we report on a further improvement in sensitivity of ultrasonic detection of targeted nanoparticle contrast agents *in vivo* beyond that reported in Fig. 7 of a recent publication in this journal. These results were obtained using the joint entropy, $H_{f,g}$ [Eq. (4) of Ref. 1], of the backscattered radio frequency ultrasound and a reflection of the insonifying pulse, g(t), as a reference waveform.

A theoretical analysis of average performance of this type of signal processing in the presence of Gaussian noise leads to a general strategy for finding a much better choice of reference in many experimental circumstances.² This search requires extensive computer time but results in a further 2.5-fold increase in sensitivity as quantified by the statistical confidence of the measurements means and standard deviations [Eq. (6) of Ref. 1].

All data acquisition and analysis parameters are the same as described previously. The new feature of the analysis presented here is the use of a more nearly optimum reference waveform, g(t), for the computation of joint entropy, $H_{t,g}$.

The reference, g(t), was found by searching for the maximum confidence obtained using step-like functions having jumps at the extrema of the reflection of the transducer insonifying pulse from a stainless steel-reflector. These functions are specified by location of jumps, low-value, and high-value. The search spanned the following parameter ranges. Shift values: from -0.02 to 0.10 in increments of 0.01, high-values: from 100.0 to 10000.0 in decades, low-values: from 0.01 to 0.001 in decades values.

FIG. 1. Confidence, **c**, panels for $\Delta H_{f,g}$ for all groups used in our study. (A) MDA 435-implanted mice injected with $\alpha_v \beta_3$ -targeted nanoparticles (N=5); (B) MDA 435-implanted mice injected with non-targeted nanoparticles (N=5); (C) MDA 435-implanted mice injected with saline (N=5); (D),(E),(F) same injections into N=5 tumor-free mice.

The color lookup table of Fig. 1 is chosen to be the same as that of Fig. 7 published previously. However, the confidence values in the panels cover the range -7.7 to 30.1 so that the upper range of values, which appear on the upper right of panel (A) are actually saturated. These are roughly twice the magnitude of the largest confidences (-16) obtained previously. I

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A $\alpha_v \beta_3$ -Targeted N.P. MDA-435-Implanted

B Non-Targeted N.P. MDA-435-Implanted

C Saline MDA-435-Implanted

D $\alpha_v \beta_3$ -Targeted N.P. Non-Implanted

E Non-Targeted N.P. Non-Implanted

F Saline Non-Implanted

¹M. Hughes, J. McCarthy, J. Marsh, and S. Wickline, "Joint entropy of continuously differentiable ultrasonic waveforms," J. Acoust. Soc. Am. **133**(1), 283–300 (2013).

²M. Hughes, J. McCarthy, J. Marsh, and S. Wickline, "Entropic vs. energy waveform processing: A comparison based on the heat equation," in Proceedings of the Fall 2014 Acoustical Society Meeting, 2014.

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