Edward Timko Indiana University Bloomington

On polynomial n-tuples of commuting isometries

Abstract

We extend some of the results of Agler, Knese, and McCarthy concerning pairs of commuting shifts to the case of n-tuples of commuting isometries, where n>2. Let $V=(V_1,\ldots,V_n)$ be an n-tuple of commuting isometries on a Hilbert space and let $\mathrm{Ann}(V)$ denote the set of all n-variable polynomials p such that p(V)=0. When $\mathrm{Ann}(V)$ defines an affine algebraic variety of dimension 1 and V is completely non-unitary, we show that V decomposes as a direct of n-tuples (W_1,\ldots,W_n) with the property that, for each i, W_i is either a shift or a scalar multiple of the identity. If V is a cyclic n-tuple of commuting shifts, then we show that V is determined by $\mathrm{Ann}(V)$ up to near unitary equivalence.

Talk time: 2016-07-18 05:00 PM— 2016-07-18 05:20 PM Talk location: Cupples I Room 207