# A Logistic Regression/Markov Chain Model for NCAA Basketball 

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# A Logistic Regression/Markov Chain Model For NCAA Basketball 

Paul Kvam ${ }^{1}$ and Joel S. Sokol ${ }^{1,2}$


#### Abstract

Each year, more than $\$ 3$ billion is wagered on the NCAA Division I men's basketball tournament. Most of that money is wagered in pools where the object is to correctly predict winners of each game, with emphasis on the last four teams remaining (the Final Four). In this paper, we present a combined logistic regression/Markov chain model for predicting the outcome of NCAA tournament games given only basic input data. Over the past 6 years, our model has been significantly more successful than the other common methods such as tournament seedings, the AP and ESPN/USA Today polls, the RPI, and the Sagarin ratings.


## 1. Introduction

More money is bet on the National Collegiate Athletic Association (NCAA) Division I men's basketball tournament than on any other sporting event in the United States. The FBI estimates that every year, more than $\$ 3$ billion is wagered (legally and illegally) on the tournament's outcome [1]. With so much money on the line, a model that predicts outcomes more effectively that standard ranking and rating systems can be useful, especially if it requires only basic input data. In this paper, we present such a model.

Before describing the model, we provide a short introduction to the NCAA tournament for readers to whom it might not be familiar. At the conclusion of each college basketball season, the NCAA holds a 64-team tournament. The participants are the champions of the 31 conferences in Division I, plus the best remaining teams (as judged by the tournament selection committee). In addition to choosing the teams, the selection committee also seeds them into four regions, each with seeds 1-16. The four teams judged best by the committee are given the \#1 seeds in each region, the next four are given the \#2 seeds, etc. Within each region, the 16 teams play a 4 -round singleelimination tournament with matchups determined by seed ( 1 vs. 16, 2 vs. 15, etc.); the winner of each region goes to the Final Four. The Final Four teams play a 2-round single-elimination tournament to decide the national championship. Throughout all 6 rounds of the tournament, each game is played at a neutral site rather than on the home court of one team or the other.

In most NCAA tournament pools (the primary outlet for tournament wagers), participants predict the winner of each game. All predictions are made before the tournament starts, so it is possible that the predicted winner of a late-round game might not even be a participant, if that team lost in an earlier round.

Pool participants have several sources that can help them make their predictions. The five most common such ranking systems are the Associated Press poll of sportswriters, the ESPN/USA Today poll of coaches, the Ratings Percentage Index (a combination of a team's winning percentage and that of the team's opponents), the

[^0]Sagarin ratings published in USA Today [15], and the tournament selection committee's seedings.

A separate question is, once a ranking or rating system has been selected, how to use the information in a pool setting. Kaplan and Garstka [13] describe a dynamic programming model which, given estimated probabilities of each team beating each other team head-to-head in a tournment game and given point values for each game in the pool, suggests a prediction strategy that can be used to maximize one's pool score. Breiter and Carlin [4] obtain similar (though slower) results via a brute force algorithm. Of course, the quality of the dynamic programming and brute force solutions is dependent on having good probability estimates. Schwertman et al. [10,11] suggest methods for estimating win probabilities based on teams' seedings in the tournament. Carlin [7] suggests methods for estimating win probabilities based on the Sagarin ratings and Las Vegas point spreads; Breiter and Carlin [4] use those methods to illustrate their algorithm. Boulier and Stekler [2] fit a probit model to estimate win probabilities based on seedings in order to maximize the number of games predicted correctly. Caudill [8] uses a maximum score estimator model that is also based on seedings and also tries to maximize the number of correct predictions. Caudill and Godwin [9] use a heterogeneouslyskewed logit model for the same purpose. Kaplan and Garstka [13] propose methods for estimating win probabilities from scoring rates, Sagarin ratings, and Las Vegas point spreads.

Metrick [14] and Clair and Letscher [10] discuss a third relevant question: should one's prediction strategy change based on the number and relative skill of other, competing predictors? They observe that sometimes differentiating one's predictions from the competition yields a higher chance of having the best predictions.

In this paper, we focus on the first question - how to accurately rank (and/or rate) teams using only on basic input data. We present a new model for ranking college basketball teams and estimating win probabilities. Our model uses a logistic regression to populate transition probabilities of a Markov chain. We describe the underlying Markov chain model in Section 2, and in Section 3 we describe the logistic regression model. Section 4 presents our computational results, and in Section 5 we make a conjecture as to why our model is significantly more successful than standard ranking systems when used alone and in the dynamic programming framework. Section 6 summarizes the paper.

## 2. A Markov Chain Model

In this section, we describe a Markov chain model for ranking teams. We begin with a model used to construct NCAA football rankings by Callaghan, Porter, and Mucha [5,6]. The underlying model is a Markov chain with one state for each team. The intuition is that state transitions are like the behavior of a hypothetical voter in one of the two major polls. The current state of the voter corresponds to the team that the voter now believes to be the best. At each time step, the voter reevaluates his judgement in the following way: given that he currently believes team $i$ to be the best, he picks (at random) a game played by team $i$ against some opponent $j$. With probability $p$, the voter moves to the state corresponding to the game's winner; with probability ( $1-p$ ), the voter moves to the losing team's state.

Suppose team $i$ has played a total of $N_{i}$ games, with the $k$ th game ( $k \leq N_{i}$ ) being played against opponent $o_{k}$. Let $I_{i k}$ be an indicator equal to 1 if team $i$ won its $k$ th game, and 0 if team $i$ lost its $k$ th game. Then the transition probabilities $t_{i j}$ from state $i$ in the Markov chain are defined as

$$
\begin{array}{ll}
t_{i j}=\frac{1}{N_{i}} \sum_{k: o_{i k}=j}\left[I_{i k}(1-p)+\left(1-I_{i k}\right) p\right], & \text { for all } j \neq i, \\
t_{i i}=\frac{1}{N_{i}} \sum_{k=1}^{N_{i}}\left[I_{i k} p+\left(1-I_{i k}\right)(1-p)\right] . & \tag{1b}
\end{array}
$$

If we let $W_{i}$ and $L_{i}$ be the number of games that team $i$ has won and lost, and $w_{i j}$ and $l_{i j}$ be the number of games that team $i$ has won and lost against team $j$ specifically, then these transition probabilities can be rewritten in a more intuitive form:

$$
\begin{array}{ll}
t_{i j}=\frac{1}{N_{i}}\left[w_{i j}(1-p)+l_{i j} p\right], & \text { for all } j \neq i, \\
t_{i i}=\frac{1}{N_{i}}\left[W_{i} p+L_{i}(1-p)\right] . & \tag{2b}
\end{array}
$$

As equations (1) and (2) imply, state transitions can be defined as the toss of a fair $N_{i^{-}}$ sided die to select a game, followed by the toss of a weighted coin to determine whether the next state will correspond to the selected game's winner (with probability $p$ ) or loser (with probability $1-p$ ).

Given the state transition probabilities $T=\left[t_{i j}\right]$ defined in (2a) and (2b), Callaghan, Porter, and Mucha use the standard equations $\pi T=\pi, \Sigma_{i} \pi_{i}=1$ to calculate the steady-state probabilities of each team's node. The teams are ranked in order of their steady-state probability - the team with the highest steady-state probability is ranked first, etc.

A nice characteristic of Callaghan, Porter, and Mucha’s Markov chain model is that it can be implemented simply, without much data. Specifically, daily on-line scoreboards such as [19] provide all the necessary data for the model; no additional team or individual statistics are required. When extending their model to college basketball, one of our goals was to preserve this basic simplicity. Therefore, our model also requires no more data than daily scoreboards provide.

### 2.1. Alternative Transition Probabilities

The transition parameter $p$ can be interpreted in a very intuitive way: the value of $p$ is the model's answer to the question "Given that team A beat team B, what is the probability that A is a better team than B?" However, daily scoreboards give additional useful information that can refine these probability estimates. It is well-known in many of the major team sports, including baseball, basketball, soccer, football, and ice hockey, that teams playing at home have an advantage. Another factor that is often considered when evaluating teams is "margin of victory," defined as the difference between the
winning and losing teams' scores. A team that wins its games by wide margins is generally thought to be better than a team that wins its games by narrow margins.

In the context of this model, we would like to find transition probabilities that answer the question, "Given that Team A beat Team B by $x$ points at home (or on the road), what is the probability that A is a better team than $B$ ?"

Let $r_{x}^{H}$ be the probability that a team that wins a game at home by $x$ points is better than its opponent, and $r_{x}^{R}=1-r_{-x}^{H}$ be the probability that a team that wins a game on the road by $x$ points is better than its opponent. (Note that $x$ can be negative to indicate that the team in question lost the game.) If we denote each game by an ordered pair ( $i, j$ ) of teams with the visiting team listed first, and let $x(g)$ be the difference between the home team's score and the visiting team's score in game $g$, then we can write the state transition probabilities as

$$
\begin{array}{ll}
t_{i j}=\frac{1}{N_{i}}\left[\sum_{g=(i, j)}\left(1-r_{x(g)}^{R}\right)+\sum_{g=(i, i)}\left(1-r_{-x(g)}^{H}\right)\right], & \text { for all } j \neq i, \\
t_{i i}=\frac{1}{N_{i}}\left[\sum_{j} \sum_{g=(i, j)} r_{x(g)}^{R}+\sum_{j} \sum_{g=(i, i)} r_{-x(g)}^{H}\right] . & \tag{3b}
\end{array}
$$

Wins, losses, locations, and margins of victory are easy to observe; the difficulty with using this model is in estimating values of $r_{x}^{H}$ and $r_{x}^{R}$ for each $x$. In Section 3, we present a logistic regression model that exploits the basketball schedule's structure to answer this question.

### 2.2. Relation to Standard Methods

Standard methods that are used to evaluate college basketball teams take into account a team's record of winning games and its strength of schedule (i.e., the quality of the teams it played against when compiling that record). In fact, the pre-2005 RPI formula considered these factors explicitly: it took the weighted average a team's winning percentage and its opponents' winning percentage. In this section, we show how the Markov chain steady-state probabilities can be viewed as a combination of these same two factors.

The steady-state probability $\pi_{i}$ of being in the state of team $i$ can be expressed as the product of two terms, the expected time to leave a state and the expected number of entries to that state, divided by an appropriate time constant. The expected time $T_{i}$ to leave state $i$ satisfies the equation $T_{i}=1+t_{i i} T_{i}$, so

$$
\begin{equation*}
T_{i}=\frac{1}{1-\frac{1}{N_{i}}\left[\sum_{j} \sum_{g=(i, j)} r_{(g)}^{R}+\sum_{j} \sum_{g=(i, i)} r_{-x(g)}^{H}\right]} . \tag{4}
\end{equation*}
$$

Similarly, the expected number of entries $E_{i}$ to state $i$ is

$$
\begin{equation*}
E_{i}=\sum_{j} \pi_{j} t_{j i}=\sum_{j} \pi_{j} \frac{1}{N_{j}}\left[\sum_{g=(j, i)}\left(1-r_{x(g)}^{R}\right)+\sum_{g=(i, j)}\left(1-r_{-\chi(g)}^{H}\right)\right] . \tag{5}
\end{equation*}
$$

Notice that in (4), $T_{i}$ is a function only of team i's performance in the games it played. In (5), $E_{i}$ is a function of team $i$ 's performance against each team $j$, weighted by $\pi_{j}$, which is our measure of team $j$ 's strength. Therefore, we can see that our method is fundamentally similar to the RPI in that it combines a team's performance with the strength of its opponents. The team's performance dictates how long the system remains in the team's state each time it enters, and the team's strength-of-schedule dictates how often the system enters the team's state.

## 3. A Logistic Regression Model for Calculating Transition Probabilities

In this section, we describe a method for estimating the values of $r_{x}^{H}$, the probability that a team with a margin of victory of $x$ points at home is better than its opponent. (Note that we need only determine $r_{x}^{H}$ since $r_{x}^{R}=1-r_{-x}^{H}$.) Estimating $r_{x}^{H}$ is difficult because, while the input (margin of victory $x$ ) is easily observable, the response - whether one team is better than another - is hard to determine. (In fact, if we knew that information a priori or were able to directly observe it, there would be no need for the predictive model presented in this paper.)

To estimate $r_{x}^{H}$, we exploit the structure of NCAA basketball schedules. Almost every one of the 327 Division I teams is a member of a basketball conference. Conferences each play a home-and-home round robin schedule in which members $i$ and $j$ of a conference play each other twice each year, once on $i$ 's home court and once on $j$ 's home court. Smaller conferences play full home-and-home round robin schedules, where each pair of teams in the conference plays each other twice. However, some conferences are too large; scheduling restrictions make it impossible for them to play enough games to fulfill the full home-and-home requirements. These conferences play a partial home-and-home round robin, in which most teams play each other twice while a few pairs of teams play each other only once.

We focus on pairs of teams (from both smaller and larger conferences) that play each other twice per season as part of either a full or a partial home-and-home round robin schedule. Our method consists of two steps:

1. Using home-and-home conference data, estimate an answer to the following question: "Given that Team A had a margin of victory of $x$ points at home against Team B, what is the probability that Team A beat Team B in their other game, on the road?"
2. Given these road-win probabilities, deduce $r_{x}^{H}$, the probability that the home team is the better team, i.e., "Given that Team A had a margin of victory of $x$ points at home against Team B, what is the probability $r_{x}^{H}$ that Team A is better than Team B, i.e., that Team A would beat Team B on a neutral court?"

We use four years of NCAA data (the 1999-2000 through 2002-2003 seasons) to estimate these probabilities. In those four seasons, we found all matched pairs of teams that had played once on each of their home courts. For each of those games we recorded the home team, the visiting team, and the point differential at the end of regulation time ${ }^{3}$. We note that on very rare occasions, conference games might be played on a neutral court; this data was not available, and we do not believe its inclusion would significantly impact our results.


Figure 1. Number of home-and-home games by home team victory margin
Figure 1 displays the number of games in which the home team won by various margins. As one might expect, the frequency decreases as the absolute value of the point spread increases; there are very few games decided by 50 or 60 points.

Figure 2 shows the observed win probabilities $s_{x}^{H}$, where $s_{x}^{H}$ answers the following question: "Given that Team A beat Team B by $x$ points on A's home court, what is the probability that A beat B on B's home court?" (Notice that this is not quite the question we would like to answer; in Section 3.1 we discuss how to deduce $r_{x}^{H}$ from $s_{x}^{H}$.)

For each margin of victory (or loss) by a home team $i$ against an opponent $j$, Figure 2 shows the fraction of times that team $i$ beat the same opponent $j$ on $j$ 's home court. For example, $50 \%$ of teams that lost by 36 points on their home court beat that same opponent on the opponent's home court. Although this seems improbable, Figure 1 shows the reason; the sample size is only two games. Similar improbable results caused by small sample sizes can be found at the other extreme. For example, $0 \%$ of teams that won by 54 points at home also won the road matchup; in this case, there was only one observation of a 54 -point win.

To obtain a better, smoother estimate of win probability, we use a logistic regression model to find a good fit. The logistic regression helps linearize the nonlinear

[^1]function by estimating parameters $a$ and $b$ to fit $\ln \frac{s_{x}^{H}}{1-s_{x}^{H}}=a x+b$. Rearranging terms yields an expression for the probability that a team with an $x$-point margin at home will win the road matchup: $s_{x}^{H}=\frac{e^{-(a x+b)}}{1+e^{-(a x+b)}}$.


Figure 2. Observed probability of a home team winning its road game against the same opponent, given margin of victory in the home game.

The best-fit parameters using the matched-pair games from the 1999-2000 through 2002-2003 seasons are $(a, b)=(-0.6228,0.0292)$ with standard errors ( $0.0231,0.0017$ ). Figure 3 shows the logistic regression estimate of $s_{x}^{H}$ superimposed on the observed probability chart.


Figure 3. Observed values and logistic regression estimates for $S_{x}^{H}$

### 3.1. Deducing Neutral-Court Probabilities

The logistic regression model presented in Section 3 estimates $s_{x}^{H}$, the probability that Team A will beat Team B on B's court given that A beat B by $x$ points on A's court. However, in order to populate the transition matrix for our Markov chain model, we need an estimate of $r_{x}^{H}$, the probability that Team A will beat Team B on a neutral site given that A beat $B$ by $x$ points on A's court. In this section, we describe how we deduce $r_{x}^{H}$ from $s_{x}^{H}$.

The key to finding $r_{x}^{H}$ is to consider the case in which the game on B's home court is an even matchup ( $s_{x}^{H}=0.5$ ). We make one significant assumption, that the effect of home court advantage is additive. In other words, we assume that playing at home increases a team's expected point spread by $h>0$; in such a model (also implicitly used by [15] and others), $h$ is called the home-court advantage.

Given that home teams have some expected advantage $h$, we also assume that a game between A and B on B's home court is an even matchup if the expected point spread between the two teams is zero ${ }^{4}$. If the expected point spread on B's home court is zero, then the home-court advantage $h$ must exactly cancel A's inherent advantage over B ; the two have equal magnitude. Therefore, we expect that the game between A and B on A's home court would be decided by $2 h$, since A would have both its inherent advantage and the home-court advantage.

In the case of a neutral-court game, a team that wins by $x$ points at home would be expected to win by $x-h$ at the neutral site (due to losing their home-court advantage). Since $s_{x}^{H}$ denotes the probability of winning when the expected point spread is $x-2 h$, we can deduce that the probability of winning when the expected point spread is $x-h$ must be $r_{x}^{H}=s_{x+h}^{H}$.

### 3.2. Team vs. Team Win Probabilities

The probabilities $r_{x}^{H}$ can be used to seed the Markov chain transition matrix, as described in Section 2. The resulting steady-state probabilities $\pi$ give a natural ranking of teams: the team with the highest steady-state probability is highest-ranked, the team with the second-highest steady-state probability is ranked second, etc. These rankings can be used to predict tournament outcomes, under the assumption that it is best to always pick the higher-ranked team to win a game.

As Breiter and Carlin [4] and Kaplan and Garstka [13] pointed out, picking the highest-ranked available team might not always be the best strategy. Their models require estimates of team-vs.-team win probabilities in order to find a pool strategy. Therefore, we would like to use our logistic regression/Markov chain model to determine estimates for these team-vs.-team win probabilities.

Carlin [7], Breiter and Carlin [4], and Kaplan and Garstka [13] use a simple method for determining team-vs.-team win probabilities. Given an estimated point

[^2]difference $x$ between the two teams (i.e., given that team $i$ is expected to score $x$ more points than team $j$ in a head-to-head matchup) and a standard error $\sigma$ of the difference in score, they estimate the probability of $i$ beating $j$ as $p_{i j}=\Phi(x / \sigma)$. This probability estimate can be used with any model that predicts a head-to-head scoring difference, such as Sagarin ratings [4,7,13], Poisson scoring-rate models [13], and Las Vegas betting lines [7,13]; therefore, all we require is a way to estimate scoring difference from our steadystate probabilities $\pi$.

Surprisingly, the scoring difference between two teams appears to be fairly wellestimated by a simple linear function of the difference in steady-state probabilities. Specifically, using 1999-2003 regular-season data we find a good estimate to be

$$
\begin{equation*}
x_{i j}=9180\left(\pi_{i}-\pi_{j}\right) . \tag{4}
\end{equation*}
$$

Adding nonlinear (including logarithmic) factors does not improve the fit of the model; even simply allowing for different coefficients of $\pi_{i}$ and $\pi_{j}$ does not yield an improvement - the two coefficients are nearly identical (modulo their signs), and each is well within the standard error of the other. Overall, the simple one-parameter model in equation (4) has a standard error of 10.9 points; by comparison, Breiter and Carlin [4] use a standard error of 11 points when dealing with Las Vegas betting lines and Sagarin ratings. The standard error of the coefficient 9180 in our model is 71.5.

We also attempt to predict team-vs.-team win probabilities directly from steadystate probabilities (i.e., without using scoring difference as an intermediate step). A logistic regression model is appropriate, since the outcomes are binary (wins and losses). Figure 4 shows the relative frequency of steady-state-probability differences between teams that played each other.


Figure 4. Number of games by steady-state probability differences $\times 10^{-4}$
Figure 5 shows the observed probability that the home team wins a game with a certain steady-state probability difference.


Figure 5. Observed win probability by steady state difference x $10^{-4}$
The best-fit logistic regression model (obtained using Minitab) is

$$
\begin{equation*}
\hat{p}_{i j}=1-\frac{e^{-1834.72\left(\pi_{i}-\pi_{j}\right)-0.6716}}{1+e^{-1834.72\left(\pi_{i}-\pi_{j}\right)-0.6716}} . \tag{5}
\end{equation*}
$$

However, this data implicitly includes a home court advantage. The constant term 0.6716 in the exponential can be thought of as the home-court effect; on a neutral court, the probabilities translate to

$$
\begin{equation*}
p_{i j}=1-\frac{e^{-1834.72\left(\pi_{i}-\pi_{j}\right)}}{1+e^{-1834.72\left(\pi_{i}-\pi_{j}\right)}} . \tag{6}
\end{equation*}
$$

## 4. Computational Results

To test the models developed in Section 3, we analyze their predictions of NCAA Tournament games. The NCAA tournament schedules all of its games on neutral courts, thus eliminating home-court advantage. Consequently, our transition probabilities, each of which estimates the probability of one team being better than another, are valid for attempting to predict the winners of neutral-court NCAA Tournament games.

We test our model in two different ways: as a stand-alone predictor (where the better team is always predicted to win) and as the source of probability estimates for Kaplan and Garstka’s [13] dynamic programming model. By comparing our model's success with the success of other ranking and rating systems, we hope to determine both how good a ranking system it is compared to other common methods, as well as its compatibility (again, compared to other methods) with the dynamic programming framework.

### 4.1. Best-team-wins (Ranking) Results

We compare our logistic regression/Markov chain (LR/MC) model to the five most commonly-used NCAA basketball ranking systems: the Associated Press poll of sportswriters (AP), the ESPN/USA Today poll of coaches (Coach), the Ratings Percentage Index (RPI), the Sagarin ratings (Sagarin) [15], and the tournament seeds assigned by the NCAA selection committee (Seed).

For each of the models tested, we use the final pre-tournament ranking of teams. We obtained ranking data for the pre-tournament polls ${ }^{5}$, RPI, seedings, and Sagarin ratings from [18]. Note that for the 2004-2005 season, the NCAA changed the mathematical formula for RPI; the 2004-2005 predictions using the new formula were almost exactly the same as using the old formula, so we report only the old RPI formula here. We obtained RPI data from [11]. For the LR/MC model, we used all of the game data (home team, visiting team, margin of victory) from the beginning of the season until just before the start of the tournament; we obtained this data, as well as tournament results, on line from [19]. We note that neutral-site non-tournament games were unknown in our data set; the team listed as "home" on the scoreboard was considered the home team in our data.

In addition to these ranking systems, we also tested the a set of rankings derived by Kaplan and Garstka [13] from Las Vegas betting lines. Given the Las Vegas line that team $i$ is a $f_{i j}$-point favorite over team $j$ and the over-under (the expected number of points scored in the game) is $g_{i j}$, Kaplan and Garstka [13] deduce an implicit rating $\lambda_{i}$ and $\lambda_{j}$ for each of the two teams: $\left(\lambda_{i}+\lambda_{j}\right)=g_{i j}$ and $\left(\lambda_{i}-\lambda_{j}\right)=f_{i j}$, so $\lambda_{i}=\left(f_{i j}+g_{i j}\right) / 2$ and $\lambda_{j}=\left(g_{i j}-\right.$ $f_{i j} / 2$. We obtained these betting lines for first-round NCAA tournament games from [12,18]; since all of the other methods use only pre-tournament data, we used the rankings implied by these pre-tournament betting lines to predict all tournament outcomes; for each game, we assume that the higher-rated team (the team with the higher $\lambda$ ) is predicted to win.

Based on the pre-tournament rankings from each source, we evaluated each model based on its ability to predict outcomes of tournament games. We first tested pure "best team wins" predictions, and counted (1) the number of games for which the source predicted the correct winner, (2) the number of games in which the higher-ranked team won. These two counts were different because of the possibility of multiple upsets. For example, if two second-round opponents were both upset winners in the first round, then metric (1) would give a score of zero but metric (2) could give a score of 1 if the secondround winner was the higher of the two upset-winners. We report the results of both metrics because they both give information regarding the quality of the ranking system.

Table 1 shows the performance of the seven rankings according to the two metrics, based on their performance over six seasons: 1999-2000 through 2004-2005. The LR/MC model was more successful at picking the winners of tournament games than any of the other rankings. Note that fractional results indicate the presence of ties in the ranking (for example, when two \#1 seeds play each other each is considered to be $1 / 2$ of the predicted seeding-method winner).

|  | AP | Coach | RPI | Seed | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Games won by predicted winner | 236 | $2351 / 2$ | 229 | $2351 / 4$ | 229 | $231 / 2$ | 248 |
| Games won by higher-ranked team | 263 | $2631 / 2$ | 259 | 262 | 260 | 260 | 273 |

Table 1. Performance of models on two metrics of prediction quality, 1999-2000 through 2004-2005 seasons (378 total games).

[^3]In addition to counting statistics, we also tracked the rankings of the eventual Final Four teams. The six seasons’ Final Four teams had very different characteristics. There were three "surprise" teams in 1999-2000, including two (Wisconsin and North Carolina) that did not get even one vote in the coaches' poll. On the other hand, in 20002001 and 2001-2002, three of the four teams were considered favorites to reach the Final Four.

Table 2 shows each method's rankings of each season's Final Four teams. In five of the six test seasons, the LR/MC model had the Final Four teams collectively ranked higher than any of the other ranking systems. Of the 24 teams, 16 were ranked in the top five by the LR/MC model, and 21 were ranked in the top 10 . Collectively, the 24 Final Four teams had a LR/MC total ranking of 152, much better than the total for Sagarin (198), AP ( $\geq 236$ ), ESPN ( $\geq 242$ ), and RPI (264). The Seeding total ranged from 192 to 264, spanning the range of Sagarin, AP, ESPN, and RPI, but still clearly worse than LR/MC. The Vegas model finished last, with a total of 296 (though they did have one significant success, ranking North Carolina as \#8 in 2000). We therefore conclude that our LR/MC model appears to be significantly better at identifying potential Final Four teams than any of these other rankings.

Conventional wisdom is that there have been "surprise" teams in the Final Four every year, but there is no standard definition of "surprise". If we define a surprise team as one outside the top 10, Table 2 demonstrates that there have been only 3 teams to surprise our model in the past 6 years, including two in one season. By contrast, the Sagarin ratings have been surprised 6 times, the selection committee has been surprised 6-10 times, the RPI 9 times, the AP pollsters 8 times, the coaches 9 times, and the Vegas model 12 times. In most cases, teams that were surprises to other rating systems were well-predicted by ours; moreover, although the two biggest surprises (Wisconsin and North Carolina, both in 1999-2000) also surprised our ranking system, we had the two teams in question ranked higher in total than each of the other systems. Only with one team, Marquette in 2002-2003, did our ranking system perform significantly worse than a majority of the others.

|  | 1999－2000 |  |  |  | 2000－2001 |  |  |  | 2001－2002 |  |  |  | 2002－2003 |  |  |  | 2003－2004 |  |  |  | 2004－2005 |  |  |  | Totals |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3 3 0 0. 0 0 0 0 0 |  | $\begin{aligned} & \sum_{n}^{n} \\ & 0 \\ & 0 \\ & 0 . \end{aligned}$ | $\begin{aligned} & \text { z } \\ & \text { 兰 } \\ & 0 \\ & 0 \\ & 0 \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { E } \\ & \text { 会 } \end{aligned}$ |  |  |  | त्त्0 敬 | $\begin{aligned} & \text { 을 } \\ & \text { 音 } \\ & \text { 曾 } \end{aligned}$ | 3 3 2 0 | 启 |  | $\begin{aligned} & \text { त्रि } \\ & \text { 馬 } \end{aligned}$ | $\begin{aligned} & \text { 3 } \\ & \text { 苞 } \\ & \frac{0}{0} \\ & \stackrel{0}{0} \end{aligned}$ |  | Oklahoma State | $\begin{aligned} & \text { O} \\ & \text { 总 } \end{aligned}$ | $\begin{aligned} & \text { O} \\ & \text { 訁 } \\ & \text { た } \\ & \stackrel{\rightharpoonup}{2} \\ & = \end{aligned}$ |  | 曾 |  |  |  |  |
| AP | 2 | 13 | 37 | ＊ | 1 | 3 | 5 | 11 | 2 | 3 | 4 | 26 | 5 | 6 | 9 | 13 | 4 | 6 | 7 | 14 | 1 | 4 | 2 | 15 | $\geq 236$ |
| Coach | 2 | 11 | ＊ | ＊ | 1 | 3 | 4 | 11 | 2 | 3 | 4 | 27 | 5 | 6 | 11 | 12 | 3 | 6 | 7 | 15 | 1 | 4 | 3 | 15 | $\geq 242$ |
| RPI | 13 | 18 | 32 | 41 | 1 | 3 | 8 | 22 | 1 | 5 | 3 | 20 | 4 | 6 | 10 | 9 | 6 | 1 | 5 | 16 | 2 | 11 | 5 | 22 | 264 |
| Seed ${ }^{6}$ | 1－4 | 17－20 | 29－32 | 29－32 | 1－4 | 1－4 | 5－8 | 9－12 | 1－4 | 1－4 | 5－8 | 17－20 | 1－4 | 5－8 | 9－12 | 9－12 | 5－8 | 1－4 | 5－8 | 9－12 | 1－4 | 13－16 | 1－4 | 17－20 | $\begin{aligned} & 192- \\ & 264 \end{aligned}$ |
| Sagarin | 4 | 10 | 25 | 31 | 1 | 3 | 4 | 10 | 3 | 4 | 5 | 21 | 5 | 4 | 14 | 12 | 5 | 1 | 7 | 8 | 1 | 7 | 2 | 11 | 198 |
| Vegas | 11 | 19 | 38 | 8 | 1 | 7 | 2 | 10 | 3 | 11 | 2 | 49 | 1 | 16 | 25 | 14 | 15 | 2 | 13 | 16 | 5 | 6 | 1 | 21 | 296 |
| LR／MC | 3 | 5 | 19 | 26 | 1 | 5 | 4 | 3 | 3 | 5 | 2 | 10 | 7 | 1 | 19 | 10 | 5 | 1 | 2 | 4 | 2 | 6 | 1 | 8 | 152 |

Table 2．Final Four teams’ rankings．＊denotes that a team was unranked；both polls had 42 ranked teams just before the 1999－2000 NCAA Tournament，so these teams were ranked no higher than $43^{\text {rd }}$ ．

[^4]
### 4.2. Dynamic-programming-based Ranking Results

In addition to testing the ranking systems, we also tested the effectiveness of the ranking systems in the framework of Kaplan and Garstka's [13] dynamic programming model.

Kaplan and Garstka's [13] dynamic program requires team-vs.-team win probabilities for each possible tournament matchup. There are several methods for translating rankings to probabilities suggested in the literature. As before, let $p_{i j}$ be the probability that team $i$ will beat team $j$ on a neutral court. Schwertman, McCready, and Howard [16] suggest the ratio of rankings $p_{i j}=\frac{y_{j}}{y_{i}+y_{j}}$, where $y_{i}$ and $y_{j}$ are the rankings of teams $i$ and $j$. (They initially suggested this calculation for use with tournament seeds, but it is easily extendable to other ranking systems.) Bouler and Stekler [2] suggest a probit model that they fit for tournament seeds only.

Schwertman, McCready, and Howard [16] and Schwertman, Schenk, and Holbrook [17] suggest probabilities based on the assumption that teams' strength is normally distributed. Both sets of researchers propose probabilities of the form $p_{i j}=\alpha_{0}+$ $\alpha_{1}\left(S\left(y_{i}\right)-S\left(y_{j}\right)\right)$, where $S\left(y_{i}\right)$ is the inverse normal cumulative distribution function of team $i$ 's ranking relative to the total. For example, if there were 325 teams and team $i$ was ranked $y_{i}=21^{\text {st }}$, then $S\left(y_{i}\right)$ would be the inverse normal CDF of (325-21)/325. The parameters $\alpha_{0}$ and $\alpha_{1}$ are fit based on regular-season data. In [16], they define $\alpha_{0}=0.5$ (so that teams of equal strength are assigned a $50 \%$ chance of beating each other) and fit $\alpha_{1}$; in [17] they also consider fitting both $\alpha_{0}$ and $\alpha_{1}$. Since this second model might yield $p_{i j}+p_{j i} \neq 1$, we define $p_{j i}=1-p_{i j}$ whenever $i$ is a higher-ranked team than $j$. We also truncate meaningless values of $p_{i j}$; negative values are assigned 0 , and values greater than 1 are reduced to 1 . Schwertman, Schenk, and Holbrook [17] suggest similar one- and two-parameter fits based on an exponential probability function: $p_{i j}=\frac{1}{1+e^{\beta_{0}+\beta_{1}\left(S\left(y_{i}\right)-S\left(y_{j}\right)\right)}}$. In the one-parameter fit, $\beta_{0}=0$ ensures that teams of equal strength are assigned a $50 \%$ chance of beating each other; in the two-parameter fit, we handle out-of-range probabilities and $p_{i j}+p_{j i} \neq 1$ in the same way as before.

The final ranking-based probability system we test is from Carlin [7]. He suggests using a two-parameter fit to calculate an expected point difference $\hat{x}_{i j}=\gamma_{0}+\gamma_{1}\left(y_{j}-y_{i}\right)^{2}$ and then estimating the probability $p_{i j}$ from the cumulative normal distribution, i.e., $p_{i j}=\Phi\left(\frac{\hat{X}_{i j}}{\sigma}\right)$. We use $\sigma=11$, as suggested by [7].

Kaplan and Garstka’s [13] dynamic programming model is designed for use with tournament pools. There are many different pool scoring systems; we tested ours on three common systems, each of which emphasizes additional solution features.

The first type of pool we tested awards one point per correctly-predicted game, regardless of which round the game is in. This type of pool makes the first and second rounds more important than later rounds, simply because more than $3 / 4$ of all tournament games occur in those first two rounds.

The second type of pool we tested awards an exponentially-increasing number of points per correct prediction, based on the round that the game occurs. Specifically, we tested a system where each correct prediction earns $2^{\text {round-1 }}$ points (i.e., 1 point per firstround game, 2 points per second-round game, 4 points per third-round game, etc.). This type of pool makes later-round predictions more important than early predictions; however, later-round predictions are more difficult, because they require the predicted winner to win not just that game, but all of its previous tournament games as well.

The third type of pool we tested follows the exponential increase system, but rewards correct upset predictions. Specifically, base the number of points for each game remains the same ( $2^{\text {round- }}$ ), but is multiplied by the seed of the predicted winning team. For example, in a first-round game between a \#2 seed and a \#15 seed, the base point value of the game is $2^{1-1}=1$ point. Correctly predicting the \#2 seed to win earns $2 \times 1=2$ points, while correctly predicting an upset (the \#15 seed winning) earns $15 \times 1=15$ points. This method rewards not only correct long-term predictions, but also better insight into which lower-seeded teams will be successful.

Before testing any of the dynamic-programming-based predictions, we test the best-team-wins method on each of the three pool types. The previous section's results, which suggested that the LR/MC method picked slightly more winners but was significantly superior at selecting later-round winners (especially those that might be lower-seeded), led us to expect that LR/MC would increase its superiority in exponentially-weighted pools and upset-bonus pools.

In fact, as Table 3 shows, this is exactly what happened. For the one-point-pergame pool, LR/MC was $5 \%$ better than the second-best ranking method, and $6.5 \%$ better than the average of the other six methods. For the exponentially-weighted pool, LR/MC's advantage increased to $17 \%$ over the second-best method, and $23 \%$ over the average of the other six methods. When the upset bonus was included, LR/MC's advantage was even greater, $22 \%$ over the second-best method and $26 \%$ over the average.

| Pool Type | AP | Coach | RPI | Seed | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| One point per game | 236 | $2351 / 2$ | 229 | $2351 / 4$ | 229 | $2311 / 2$ | 248 |
| $2^{\text {round-1 }}$ points | 541 | $5311 / 2$ | 465 | 495 | 520 | 519 | 632 |
| seed $\times 2^{\text {round- }}$ points | $11941 / 2$ | $11921 / 2$ | 1104 | 1115 | 1155 | $11881 / 2$ | 1454 |

Table 3. Total pool score of models using best-team-wins prediction method, 1999-2000 through 20042005 seasons.

In addition to the results reported in Table 3, we also tested the maximum score estimator model of Caudill [8], another deterministic method. Based on seedings, it uses historical data to predict outcomes (so, for example, if $14^{\text {th }}$ seeds beat $3^{\text {rd }}$ seeds more often than vice versa, it will make this prediction instead). Its performance was worse than that of just selecting the higher seeds.

Tables 4, 5, and 6 compare the dynamic programming-based predictions using each ranking method and each ranking-to-probability formula; the final row of each table show the best-team-wins method for purposes of comparison. Again, the results are clear. Regardless of which method is used to derive probabilities from the rankings, the LR/MC results are superior. In fact, in every case, even the worst LR/MC result (without dynamic programming) is superior to the best result obtained from any of the other
rankings, using any of the probability models, with or without dynamic programming. Thus, we can conclude that, although selecting a good probability model and using dynamic programming both can improve the results (especially as the pool scoring system gets more complex), it is far more important to begin with an accurate ranking system such as LR/MC.

|  | AP | Coach | RPI | Seed | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ratio of rankings [16] | 242 | 240 | 235 | 241 | 238 | 236 | 250 |
| Linear, $\alpha_{0}=0.5$ [16] | 243 | 238 | 235 | 241 | 240 | 236 | 251 |
| Linear, $\alpha_{0}$ and $\alpha_{1}$ fit [17] | 242 | 238 | 236 | 241 | 240 | 235 | 249 |
| Exponential, $\beta_{0}=0$ [17] | 243 | 240 | 236 | 241 | 241 | 237 | 254 |
| Exponential, $\beta_{0}$ and $\beta_{1}$ fit [17] | 241 | 238 | 236 | 241 | 240 | 237 | 251 |
| Normal CDF [7] | 239 | 241 | 232 | 241 | 237 | 238 | 253 |
| Seed probit [2] | --- | -- | --- | 240 | --- | --- | --- |
| Best-team-wins | 236 | $2351 / 2$ | 229 | $2351 / 4$ | 229 | $2311 / 2$ | 248 |

Table 4. Total one-point-per-game pool score of models using ranking-based dynamic programming prediction methods and best-team-wins, 1999-2000 through 2004-2005 seasons.

|  | AP | Coach | RPI | Seed | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ratio of rankings [16] | 546 | 534 | 470 | 520 | 523 | 531 | 625 |
| Linear, $\alpha_{0}=0.5[16]$ | 548 | 528 | 470 | 520 | 543 | 531 | 633 |
| Linear, $\alpha_{0}$ and $\alpha_{1}$ fit [17] | 546 | 528 | 472 | 520 | 541 | 529 | 623 |
| Exponential, $\beta_{0}=0$ [17] | 541 | 530 | 472 | 520 | 545 | 535 | 651 |
| Exponential, $\beta_{0}$ and $\beta_{1}$ fit [17] | 538 | 528 | 472 | 520 | 543 | 535 | 633 |
| Normal CDF [7] | 538 | 580 | 420 | 520 | 521 | 557 | 661 |
| Seed probit [2] | --- | --- | --- | 519 | --- | -- | --- |
| Best-team-wins | 541 | $5311 / 2$ | 465 | 495 | 520 | 519 | 632 |

Table 5. Total $2^{\text {round-1 }}$-points-per-game pool score of models using ranking-based dynamic programming prediction methods and best-team-wins, 1999-2000 through 2004-2005 seasons.

|  | AP | Coach | RPI | Seed | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ratio of rankings [16] | 1300 | 1262 | 1072 | 1139 | 1213 | 1205 | 1654 |
| Linear, $\alpha_{0}=0.5$ [16] | 1294 | 1280 | 990 | 1094 | 1210 | 1147 | 1806 |
| Linear, $\alpha_{0}$ and $\alpha_{1}$ fit [17] | 1208 | 1249 | 1031 | 1120 | 1175 | 1203 | 1832 |
| Exponential, $\beta_{0}=0$ [17] | 1226 | 1186 | 1069 | 1026 | 1146 | 1180 | 1838 |
| Exponential, $\beta_{0}$ and $\beta_{1}$ fit [17] | 1242 | 1229 | 1053 | 1006 | 1192 | 1208 | 1843 |
| Normal CDF [7] | 1210 | 1260 | 1023 | 1139 | 1224 | 1149 | 1611 |
| Seed probit [2] | --- | --- | --- | 1174 | --- | --- | --- |
| Best-team-wins | $11941 / 2$ | $1192^{11 / 2}$ | 1104 | 1115 | 1155 | $11881 / 2$ | 1454 |

Table 6. Total seed $\times 2^{\text {round-1 }}$-points-per-game pool score of models using ranking-based dynamic programming prediction methods and best-team-wins, 1999-2000 through 2004-2005 seasons.

### 4.3. Dynamic-programming-based Rating Results

Three of the ranking methods we have tested, Sagarin, Vegas, and LR/MC, actually give more data than just the relative ranks of teams. All three assign a rating to a
team; the Sagarin and Vegas ratings are meant to be directly translated to point differentials between teams, while in Section 3.2 we have described how to translate LR/MC ratings to estimated point differentials. Carlin [7] and Kaplan and Garstka [13] have discussed ways of using estimated point differentials $\lambda_{i}-\lambda_{j}$ to estimate team-vs.team win probabilities $p_{i j}$. Specifically, Carlin [7] suggests a Normal model using $p_{i j}=$ $\Phi\left(\left(\lambda_{i}-\lambda_{j}\right) / \sigma\right)$, where $\sigma$ is conservatively estimated to be approximately 11. Kaplan and Garstka [13] use a Poisson model to refine the estimate of $\sigma$, suggesting $p_{i j}=$ $\Phi\left(\frac{\lambda_{i}-\lambda_{j}}{\sqrt{\lambda_{i}+\lambda_{j}}}\right)$. These models can be used either with Sagarin ratings or with Kaplan and Garstka's [13] Vegas-based ratings. Carlin [7] also gives a refined probability estimate for Sagarin ratings, noting that teams' observed point difference tends to be slightly underestimated by the Sagarin method. He fits a linear model and obtains the estimate $p_{i j}$ $=\Phi\left(1.165\left(\lambda_{i}-\lambda_{j}\right) / \sigma\right)$ for use with Sagarin ratings. In Section 3.2, we describe two possible methods for translating LR/MC ratings to win probabilities, one based on point differences and one directly fitting a logistic regression model.

Tables 7, 8, and 9 show the performance of each model in the three pool scoring systems. Again, just as with ranking-based methods, LR/MC even without probability models or dynamic programming outperforms all of the other methods in any form. We note, though, that while using ratings instead of rankings helps both the Sagarin and the Vegas methods, the best LR/MC results are obtained from rankings. This suggests that, although the LR/MC model is still clearly the best, we do not yet have a good method for deriving probability estimates from LR/MC ratings. For now, even using slightly unreliable probability estimates is sufficient to outperform the other methods; however, we also point out that this opportunity for future research might yield a method that gives even better results.

|  | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: |
| Normal [7] | 240 | 239 | --- |
| Poisson [13] | 240 | 239 | --- |
| Sagarin fit [7] | 240 | --- | --- |
| LR/MC points | --- | --- | 252 |
| LR/MC direct | --- | --- | 252 |
| Best-team-wins | 229 | $2311 / 2$ | 248 |

Table 7. Total one-point-per-game pool score of models using rating-based dynamic programming prediction methods and best-team-wins, 1999-2000 through 2004-2005 seasons.

|  | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: |
| Normal [7] | 560 | 548 | --- |
| Poisson [13] | 560 | 548 | --- |
| Sagarin fit [7] | 560 | --- | --- |
| LR/MC points | --- | --- | 635 |
| LR/MC direct | --- | -- | 635 |
| Best-team-wins | 520 | 519 | 632 |

Table 8. Total $2^{\text {round-1 }}$-points-per-game pool score of models using rating-based dynamic programming prediction methods and best-team-wins, 1999-2000 through 2004-2005 seasons.

|  | Sagarin | Vegas | LR/MC |
| :--- | :---: | :---: | :---: |
| Normal [7] | 1362 | 1366 | --- |
| Poisson [13] | 1247 | 1322 | --- |
| Sagarin fit [7] | 1292 | --- | --- |
| LR/MC points | --- | --- | 1600 |
| LR/MC direct | --- | -- | 1705 |
| Best-team-wins | 1155 | $11881 / 2$ | 1454 |

Table 9. Total seed $\times 2^{\text {round-1 }}$-points-per-game pool score of models using rating-based dynamic programming prediction methods and best-team-wins, 1999-2000 through 2004-2005 seasons.

## 5. Close Games and Ranking Systems

The logistic regression model described in Section 3.1 and the analysis done in Section 3.2 give rise to an interesting observation about close games. Conventional wisdom, repeated by sportscasters, sportswriters, and fans alike, is that "good teams find a way to win close games." In other words, better teams are frequently able to find some physical or psychological reserves when the outcome of the game is on the line.
[3] has already shown this idea to be untrue in Major League Baseball. A baseball team's record in close games has less correlation with its overall winning percentage; a more accurate statement is that good teams are more likely to win games that are not close. This result is not surprising, given that opposing teams' run-scoring processes are almost entirely independent. If one team is better than another (its offense is likely to score more runs against the other's pitching/defense than vice versa), then it is more likely to win a non-close game than a close one.

On the other hand, opposing teams' point-scoring processes are much less independent in basketball. A good defense can stimulate offensive production by providing turnover-induced fast-break opportunities in which the probability of scoring is much higher than on a normal possession. On the other hand, a good offense can help defensively as well, especially when the team plays a pressing style of defense that is much easier to implement after the team has just scored. Therefore, one might wonder whether the adage "good teams find a way to win close games" could hold true in basketball even though [3] has shown it to be untrue in baseball.

However, our results do not support the validity of the conventional wisdom in college basketball. The data from 1999-2003 shows that of all 791 teams that won a close home matchup (defined as a spread between 1 and 3 points, or at most one basket), approximately $35 \%$ won the road matchup against the same opponent. Of the 713 that lost a close home matchup, approximately $33 \%$ won the road matchup. If the better team really is able to win close games more frequently, one would expect the difference in road success to be much larger. Better teams (the ones who, presumably, had won the close games) would be expected to have a comparatively higher road win rate compared to worse teams (who, presumably, had lost the close games). The logistic regression estimate gives similar results; it predicts road win rates of $36 \%$ and $33 \%$.

Therefore, rather than good teams winning close games, teams that win several close games (perhaps due more to luck than other factors) might tend to be overrated by
fans and the sports media, and teams that lose several close games tend to be underrated. This occurs because an event that might really be a $50 / 50$ (or $35 / 65$ ) coin flip is translated into a binary win/loss result. In fact, this might explain why our combined logistic regression/Markov chain model is more successful than others in selecting potential Final Four participants. Very good teams that lost a few "extra" close games will tend to be ranked lower than they deserve by the polls, RPI, and other methods that treat wins and losses as binary events; our more-continuous model tends to rank those teams more accurately.

## 6. Summary

The annual NCAA Division I basketball tournament is the largest sports gambling event in the United States. With over $\$ 3$ billion wagered each year on the outcome of the tournament, bettors turn to expert rankings of teams for help with predictions. The five most prevalent ranking systems are the two major polls (the Associated Press poll of sportswriters and the ESPN/USA Today poll of coaches), the Ratings Percentage Index, the Sagarin ratings, and the tournament selection committee's seedings; we also tested rankings and ratings derived from Las Vegas betting odds.

In this paper, we describe a logistic regression/Markov chain (LR/MC) model for predicting the outcome of NCAA Division I basketball tournament games. It uses only basic input data, and is able to predict individual game outcomes more accurately than the standard ranking systems. Moreover, it is much better than other rankings at predicting potential Final Four teams. When tested on three common but diverse NCAA tournament pool scoring systems, even the simplest LR/MC approach (selecting the higher-ranked team to win each game) outperforms all other methods, even when those methods are supplemented by other researchers' probability and dynamic programming models. When those models are also used with LR/MC, the performance of LR/MC is even better, especially for more-complex pool scoring systems.

We conjecture that part of the reason for the comparative success of our model is that the other models treat the outcome of games as binary events, wins and losses. In contrast, our model estimates the probability of the winning team being better than the losing team based on the location of the game and the margin of victory and is therefore able to more-accurately assess the outcome of a close game.

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[^1]:    ${ }^{3}$ We treat overtime games as having a zero-point differential; because overtime periods are relatively short, they are played with different strategies that might give a different distribution of point spreads.

[^2]:    ${ }^{4}$ One can imagine scenarios where this is not true, e.g., where one team has a $90 \%$ chance of winning by a single point, while the other team has a $10 \%$ chance of winning by nine points; however, the distribution of observed point spreads shown in Figure 1 suggests that our simple model is a reasonable approximation of reality.

[^3]:    ${ }^{5}$ Only the top 30-40 teams generally get votes in the polls, so all unranked teams were given equal pretournament poll rankings. It was rare that two such teams lasted long enough in the tournament to face each other; those instances were considered tossups when evaluating the polls' predictions.

[^4]:    ${ }^{6}$ Four teams（one from each tournament region）are assigned each seed．Therefore，the four \＃1 seeds are ranked 1－4，the four \＃2 seeds are ranked 5－8，etc．， without specification．

