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Recommended Citation

Wilson TE. "Progress towards terahertz acoustic phonon generation in doping superlattices." In proceedings of SPIE 6010, Infrared to Terahertz Technologies for Health and the Environment, Belyanin A, Drezek R, Gmachl C, editors, Vol. 6010, 601007, (2005)

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Progress towards terahertz acoustic phonon generation in doping superlattices

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ABSTRACT

Progress is described in experiments to generate coherent terahertz acoustic phonons in silicon doping superlattices by the resonant absorption of nanosecond-pulsed far-infrared laser radiation. Future experiments are proposed that would use the superlattice as a transducer in a terahertz cryogenic acoustic reflection microscope with sub-nanometer resolution.

Keywords: doping superlattice, terahertz, acoustic, phonon, superconducting bolometer, cryogenic, acoustic microscope

1. INTRODUCTION

The optical generation of coherent, monochromatic acoustic phonons has been a long-standing goal in solid state physics. The generation and detection of longitudinal acoustic (LA) phonons with frequency up to 114 gigahertz (GHz) was accomplished through the electromagnetic surface excitation of piezoelectric crystals¹ in completely filled TM cavities. Unfortunately, reported results on the generation of terahertz (THz) transverse acoustic (TA) phonons in quartz through piezoelectric surface excitation with far-infrared laser light have proven not to be repeatable.² More recently however, progress has been made using the elegant technique of picosecond ultrasonics (PU) to generate and detect coherent LA phonons, with frequencies exceeding 400 GHz, acoustic intensities exceeding 100 W/cm² with corresponding strain amplitudes on the order of 10⁻⁴, in solid thin films near room temperature.³ Furthermore, it has also been reported that it is possible to generate coherent pulses of longitudinal acoustic phonons in a gallium arsenide/aluminum arsenide compositional superlattice by femtosecond laser excitation when the excitation energy matches the E1-HH1 transition in the superlattice⁴. We are currently investigating a complementary technique⁵, that of the direct electromagnetic generation of coherent high-frequency monochromatic acoustic phonons in silicon doping superlattices (DSL) by a high peak-power, cavity-dumped, far-infrared (FIR) laser radiation. The latter has the potential to produce intense pulses of high-frequency narrow-bandwidth coherent acoustic phonons of either polarization.

Future applications include using the phonon-generating superlattice as a terahertz acoustic transducer in a cryogenic reflection acoustic microscope and with low-temperature helium-4 as the coupling fluid. State-of-the-art acoustic microscopes have a maximum resolution in the range of 20-nm and use sound waves with frequencies as high as 15-GHz⁶. We propose to improve this resolution to less than a nanometer by using the terahertz frequencies of the resonantly excited doping superlattice. Terahertz acoustic imaging with sub-nanometer resolution, by providing an additional image contrast mechanism (elastic properties), could be expected to provide a tool for the characterization of nanomaterials and nanoelectronic devices, and potentially for acoustic cryo-microscopy of biological samples.

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2. THEORY

Modulation-doped compositional superlattices and *nipi* doping superlattices have been the objects of intense theoretical and experimental study in the past several decades⁷. A number of authors⁵ have studied the effects, on the lattice dynamical properties of an otherwise homogeneous semiconductor, stemming from impurity charges associated with a microstructured one-dimensional periodic *n* and *p*-doping sequence, a so-called *nipi* doping superlattice. The phonon dispersion relation is nearly unchanged, as one might expect from a concentration of 10^{-3} impurity atoms or even less. The periodic space charge resulting from the doping superstructure, however, is the origin of a unique feature: LA or TA acoustic phonons, with wavevectors corresponding to odd multiples of the smallest reciprocal superlattice vector, may be directly excited by electromagnetic fields of the corresponding frequency with reasonable conversion efficiency. The frequency of the generated phonons is simply given by

$$\nu = s/d \quad ,$$

where *s* and *d* are the phase velocity for LA phonons and the superlattice period, respectively.

LA or TA phonons couple to electric fields normal or parallel to the superlattice layers, respectively. We note that, for our purposes, the *nipi* superlattice is preferred over a modulation-doped compositional superlattice because, in the case of the former, the splittings of the back-folded zone-center frequencies are small. One would therefore expect little conversion of the traveling wave into a standing wave by the Bragg scattering of the folded-zone center phonons.⁸ The conversion efficiency, ξ , defined as the ratio of the generated acoustic energy to the energy of the incident electromagnetic wave, is given by equation (1) (cgs units) below, where *a* is the host lattice constant, $n_D^{(2)}$ is the two-dimensional doping concentration, κ_0 is the dielectric constant, *M* is the atomic mass, *d* is the superlattice period, *c* is the speed of light, *s* is the longitudinal phonon velocity, *N* is the number of superlattice periods, and $r \equiv (d/a)$, is the enlarged unit cell:

$$\xi \cong \left[\frac{(4\pi e^2 a^2 (n_D^{(2)})^2 (adN^2))}{(\kappa_0 Mdr)(cs\sqrt{\kappa_0})} \right] \quad (1)$$

The upper limit to the two-dimensional (donor or acceptor) doping concentration is determined by the condition that there be an effective bandgap. The limiting doping concentration follows from equations (1) and (8) in Dohler⁹, and is given in equation (3) below:

$$n_D^{(2)} \cong \left[\frac{(2E_g \kappa_0)}{(\pi d e^2)} \right] \quad , \quad (2)$$

where E_g is the host bandgap. At this doping level, the thin sheets of acceptors and donors are degenerate and there will be no carrier freeze out at liquid helium temperatures.¹⁰ In its ground state, the sample thus consists of alternately positively and negatively charged sheets of ions. Care must be taken to insure that the sample has a closely balanced dopant concentration.

As an example, we consider a silicon (Si) superlattice consisting of N periods, with a period of length $d = 3.45 \times 10^{-6}$ cm, and with individual layers having a two-dimensional doping concentration $n_D^{(2)} = 1.7 \times 10^{13} \text{ cm}^{-2}$. The conversion efficiency ξ of this superlattice, in terms of the number of superlattice periods N , is readily found from Equation (1): $\xi = 4.75 \times 10^{-11} N^2$. For instance, for a structure consisting of 500 periods, $\xi = 1.2 \times 10^{-5}$. The period chosen matches the LA phonon wavelength in silicon for 245.5-GHz (1.22-mm), a particularly strong far-infrared laser line produced by the $^{13}\text{CH}_3\text{F}$ gain medium (below). The corresponding phonon strain amplitude is on the order 10^{-6} .

In order to protect the sensitive superconducting bolometer detector from the intense FIR laser radiation, we use a small-period metallic grating coupler¹¹; i.e., heat pulse generation in bolometers exposed to intense FIR laser pulses has been observed previously². Broadband phonon generation might also be expected, in the absence of such a grating-coupling scheme, to result both from multi-phonon¹² and defect-induced¹³ absorption in the substrate. The grating coupler has drawn considerable interest in recent years since it has been shown to significantly improve the intersubband absorption in multiple quantum-well infrared photodetectors under normally incident illumination.¹¹ The grating coupler converts normally incident plane wave radiation, into an evanescent surface wave with a large electric field component perpendicular to the interface. The decay length δ of the first-order diffracted evanescent ($p/(\lambda/n) < 1$) field of the grating-coupler is given by Equation (7) of Reference 11:

$$\delta \cong \left[\frac{p}{2\pi \sqrt{1 - (np/\lambda)^2}} \right], \quad (3)$$

where p is the grating period and λ/n is the optical wavelength of the FIR in the DSL. For a given δ , equation (3) may be inverted to find the optimum grating period p . Ideally, one would choose the decay length to match the DSL thickness; in our case, the overall DSL thickness (14 layers \times 34.5-nm period) corresponds to a $\delta \sim 0.5\text{-}\mu\text{m}$. However, we have used a grating period of $p \sim 10\text{-}\mu\text{m}$, resulting in a decay length of $\delta \sim 1.6\text{-}\mu\text{m}$, slightly larger than the overall superlattice thickness. The larger p was chosen due to constraints imposed by our photolithography system. ($n = 3.41$ for silicon at 246-GHz). Niobium was used as the grating material because of its small surface resistance (i.e., low FIR absorption) below its superconducting transition temperature¹⁴.

The spectral and polarization characteristics of the generated coherent acoustic phonons will be studied using Si:B piezo phonon spectroscopy¹⁵. The phonons, generated in the DSL, will propagate ballistically through a lightly boron-doped Si substrate and will be detected by a granular aluminum superconducting bolometer¹⁶ located on the rear sample face. The sample, cooled by immersion in liquid helium by means of a cryostat with optical access, is uniformly stressed at levels up to several kBar by a stress apparatus suitable for use in low-temperature cryostats¹⁷. Along symmetry directions in Si:B, the stress-dependent energy level splitting of the boron acceptor's ground-state Kramer's doublets is known. The bolometer signal will drop sharply when the energy difference between the stress-split levels matches the phonon energy. Measurements of the phonon transmission as a function of the applied stress will yield the phonon spectrum. Furthermore, the spectral content of TA and LA phonons may be studied independently by gating the detector signal at the corresponding phonon time-of-flight across the substrate. The spectrometer resolution, under the conditions of the proposed experimental arrangement, is typically 5 GHz; this is of the same order as the predicted phonon linewidth resulting from a 100-period thick DSL. The temporal resolution, determined by the bolometer response, is typically of order 10 ns (Figure 4). We will generate and detect phonons at a number of discrete frequencies, ranging

from 0.25 to 1.0 THz, by using samples with different DSL period and corresponding FIR laser excitation wavelength. Measurements of the phonon spectral width and the relative conversion efficiency of electromagnetic to acoustic power will be compared to theory.

3. EXPERIMENT / PRELIMINARY RESULTS

3.1 The far-infrared laser

Strong pulsed lasing action at 1.22-mm was first reported by Hacker *et al*¹⁸ in a ¹³CH₃F mirrorless waveguide laser., optically-pumped by the 9P32 line of a TEA CO₂ laser. As a source of intense ultrashort (~nanosecond) pulses of far-infrared laser radiation suitable for this experiment, we use our¹⁹ cavity-dumped optical laser resonator, modified for use at 1.22-mm. The laser resonator schematic diagram is depicted in Figure 1.

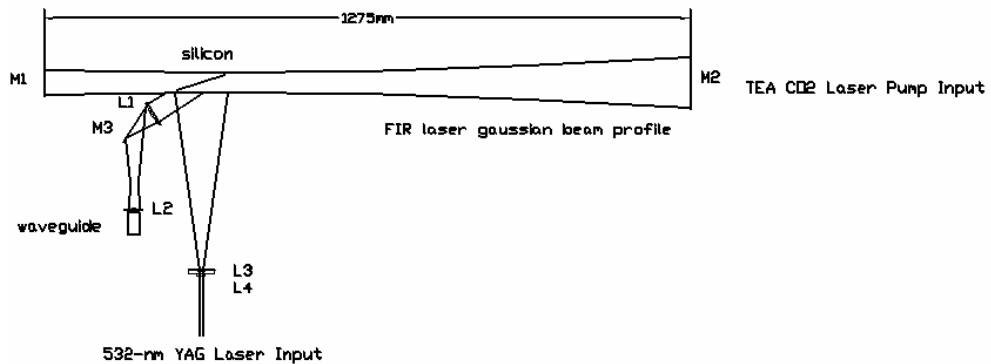
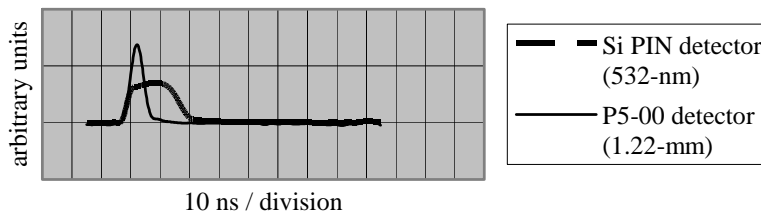


Figure 1. FIR laser resonator schematic diagram. *M1*: 10-cm diameter Au-coated concave copper mirror, radius of curvature 845 mm; *M2*: 10-cm diameter Au-coated concave copper mirror, radius of curvature 1275 mm; *Silicon*: {100} float-zone, double-sided polished, 100-mm diameter x 0.5 mm, 7000 Ohm-cm resistivity; *L1*, *L2*, plano-convex TPX lens, 159-mm and 105-mm focal length, respectively; *M3*: 75-mm diameter flat Au-coated Pyrex mirror; *L3*: 50-mm diameter, -100 mm focal length plano-concave BK7 spherical lens, visible AR coating; *L4*: -40 mm focal length cylindrical BK7 lens. Not shown: modified *Gentec DD-250* TEA CO₂ pumping laser (focused TEA laser radiation enters through 2-mm coupling hole in *M2*), *Spectra-Physics GCR-150* frequency-doubled YAG laser output entering through *L4*. The FIR laser output is coupled into a segmented 246-GHz corrugated waveguide.

Our technique for cavity-dumping by the optical-switching of an intra-cavity intrinsic silicon wafer, oriented at the Brewster angle to the circulating p-polarized far-infrared radiation, through the absorption of above bandgap radiation, has also been used elsewhere²⁰. The risetime of the output pulse is typically on the order of a nanosecond and the pulsewidth corresponds to the roundtrip time of the circulating far-infrared radiation. Recent improvements to the laser have included: (1) an in-situ mode-matching Newtonian telescope, employing custom TPX lens, to couple the output into a 246-GHz corrugated waveguide²¹ for beam transport (2) a recycling cryogenic absorption pump for the isotopic methyl fluoride gain medium. The laser routinely produces single-longitudinal mode pulsed output in peak powers of 25-kW (measured by a *Coherent Molectron*²² *J25* pyroelectric joulemeter), 6-ns pulsewidth (measured by a *Coherent*

Figure 2. 1.22-mm cavity-dumped FIR (25kW) output and 532-nm switching radiation



Molelectron P5-00 pyroelectric detector) at a 10 pps repetition rate. FIR laser output is also available at other wavelengths, for instance at 496-micron, in CH_3F pumped by the 9P20 line. A typical output pulse is shown in Figure 2.

3.2 Granular aluminum bolometer and thin film patterning

The resonantly excited phonons not scattered by the boron acceptors will ordinarily propagate ballistically across the Si:B substrate and be detected on the opposite face by a superconducting granular aluminum bolometer²³. Superconducting bolometers of this ilk typically have a phonon power detection threshold on the order of $\sim 10^{-8}$ W without integration². Our bolometers are 100-nm thick, 10 micron x 20 micron granular aluminum links that span the gap between millimeter-square chromium/gold contact pads. We fabricate the granular aluminum bolometers and niobium grating couplers, at the University of Delaware ECE Cleanroom, using a lift-off process with image-reversal lithography employing *AZ 5214 E* photoresist and *AZ Developer*, as partially described in the literature²⁴. (The overall image-reversal process recipe characterization is nearly completed.) We have found it imperative to use *AZ Developer* since, unlike most positive photoresist developers; it does not etch aluminum (see Figure 5). We expose the silicon die on a *Karl Suss MJB3* mask aligner through chromium soda-lime photomasks, supplied by *Adtek Photomasks, Inc.*, and designed with *L-Edit* software²⁵. We use a *Discovery 18* load-lock dual-target DC-magnetron sputter deposition system²⁶ retrofitted with an oxygen lecture bottle and a precision leak valve arrangement. Starting from a base pressure of 1 microTorr, granular aluminum is sputtered for 80-seconds at 400-W in an 8.5 mTorr argon plasma with an oxygen partial pressure of 170 microTorr. To prevent oxidation of the granular aluminum surface during subsequent processing, a thin (5-nm) palladium film is sputtered, from a second target, on top of the granular aluminum, prior to breaking vacuum. Under these deposition conditions, it is found that that the granular aluminum/palladium bilayer possesses a room temperature resistivity in the range of 25 to 50 microOhm-cm and a corresponding superconducting transition temperature near 1.76-K. Furthermore, the palladium coating consistently results in reliable electrical connection to the overlying chromium/gold contacts – a new finding. The bolometer is cooled by immersion in He II by means of a cryostat with optical access. A constant temperature is maintained through pumping on the helium and controlling its vapor pressure with a regulator. This technique allows the selection of a fixed temperature from 1.4 K to 2.2 K with a constancy of better than 0.002 K, much less than the width of the superconducting transition. Figure 3 displays a recent four-point probe measurement of the superconducting transition of a U-Delaware fabricated granular aluminum/palladium bilayer. Figure 4 shows the recent test of a larger granular aluminum bolometer, fabricated earlier by shadow-mask evaporation in the laboratory of Dr. Werner Dietsche at MPI-Stuttgart. Figure 4 displays the arrival of a

heat pulse generated by on the front surface of a Si:B sample (with no doping superlattice), at the expected time-of-flight for LA phonons.

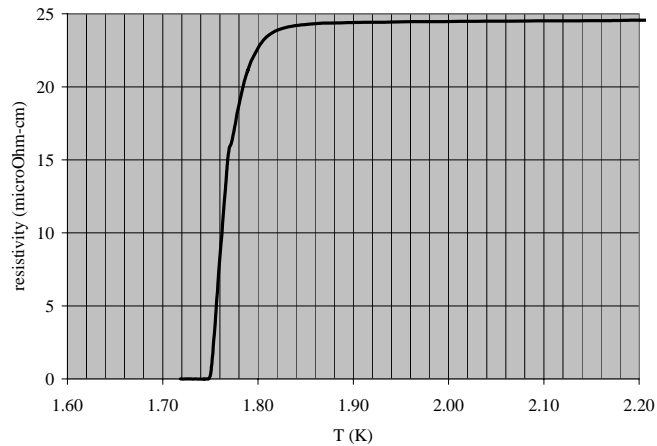


Figure 3: Four-point probe measurement of resistivity versus temperature for a sputtered granular aluminum/palladium bilayer. Temperature computed via helium vapour pressure according to the International Temperature Scale of 1990²⁷.

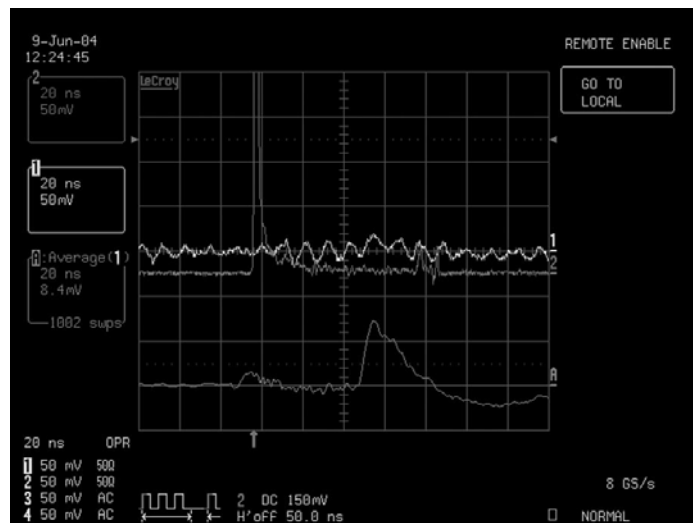


Figure 4: Granular aluminum bolometer response (second pulse on lowest trace) to heat pulse produced on front surface of an aluminum-coated {100} Si:B sample by 300-W mini-YAG laser irradiation (upper trace). The first pulse on the lowest trace corresponds to scattered light striking the bolometer. The second pulse on the lowest trace

corresponds to the time-of-flight (60-ns) for LA phonons in 0.5-mm thick silicon. A broadband impedance mini-transformer (16:1) positioned near the sample in the helium bath was used to match the 3-Ohm bolometer to 50-Ohm miniature coaxial cable.

We estimate the expected signal-to-noise ratio for the DSL phonon generation experiment as follows. For a DLS sample with 14 periods (one of our samples), the conversion efficiency ξ is 9.2×10^{-9} . The grating coupling efficiency, defined as the ratio of the total energy density associated with the component of the electric field of the FIR evanescent wave normal to the surface, to the energy density of the linearly polarized incident FIR wave, is estimated as 0.80. If one assumes 10-kW of FIR laser power incident upon the DSL, the expected phonon power arriving at the bolometer is 7.4×10^{-5} W, well above the threshold of detection.

The experiment awaits further bolometer fabrication development. It was observed that *AZ 351* developer etched the granular aluminum/palladium bilayer during the subsequent deposition of the contact pads. Work is in progress to develop an image-reversal process (for more consistent lift-off results) using the *AZ Developer* instead of the *AZ 351*.

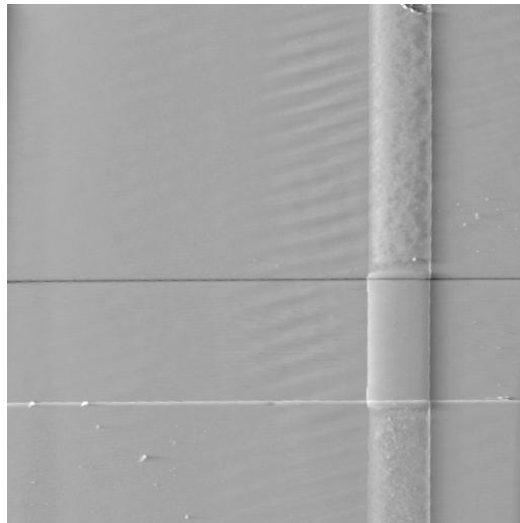


Figure 5: An atomic force microscope image of a 10 micron x 20 micron x 80-nm thick granular aluminum/palladium bilayer (spanning two larger chromium/gold contacts). Notice the roughness as a result of the etching of the aluminum (under the contacts) from the use of *AZ 351* developer during the subsequent processing of the contacts. Such etching prevents the bolometer from becoming superconducting.

3.3 Piezo phonon spectroscopy

The experimental method to be used for measuring phonon emission spectra using the Si:B spectrometer is described in the literature²⁸. In the Si:B piezo phonon spectrometer, the boron acceptor ground state, consisting of a quartet, is split into two Kramers doublets by applied stress. Phonons are resonantly scattered by the acceptors when the phonon energy matches the difference in the energy levels of the doublets. For stress applied along the [100], [110] and [111]

directions, the energy level splitting in Si:B, as a function of stress, is known. For example, the ground state splitting energy E as a function of stress X along a [100] direction is given by:

$$E = (392 \text{ GHz/kBar}) X \quad (4)$$

The resonant scattering rate and linewidth, as a function of the splitting energy, acceptor concentration and temperature, are also known. For instance, near 250 GHz, the linewidth is ~5 GHz. The spectrum of any TA or LA phonons generated by the superlattice can be obtained by monitoring the transmitted phonon signal, received at the bolometer at the back face of the sample, as a function of stress applied in a direction normal to the propagating phonons. A significant drop in transmission should occur when the phonon energy matches the stress-split level separation. In addition, the spectral content of TA and LA phonons may be analyzed separately by gating the detector at the corresponding phonon time of flight. The time-dependent bolometer voltage can be numerically de-convoluted to obtain the time-dependent absorbed phonon flux.¹⁶

To prepare die for the stress apparatus, the wafer is first diced into 12-mm x 16-mm platelets and the thin films are patterned on a 2 x 2 array and then subsequently diced into 5-mm x 7-mm samples. The top and bottom

Resonant Longitudinal Acoustic Phonon Generation in Si Doping Superlattice by Pulsed Millimeter-Wave Laser Radiation

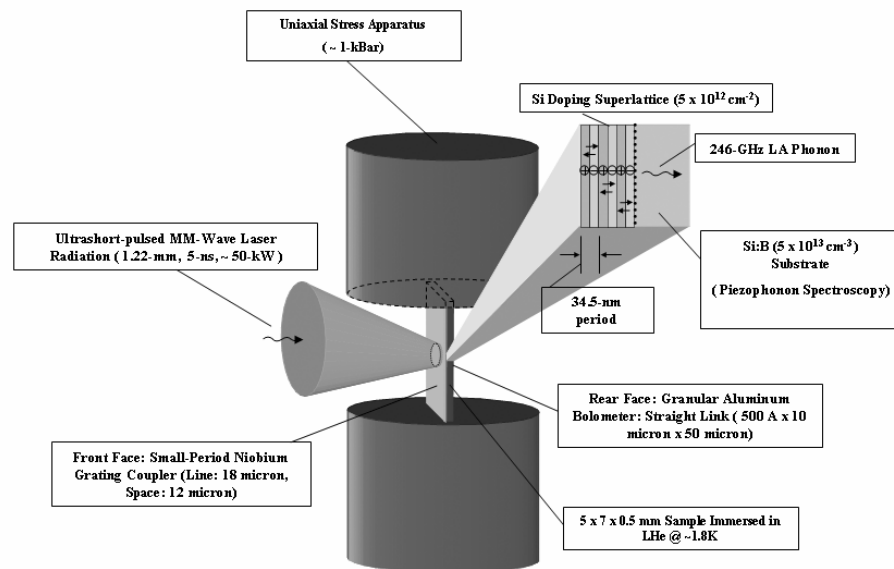


Figure 6: Schematic Diagram for Experimental Arrangement for Phonon Generation in Silicon Doping Superlattice by Pulsed Far-Infrared Laser Radiation

surfaces of the samples are lapped parallel to one another on a glass plate using a custom lapping fixture²⁹. Flatness can be verified using an optical test jig based upon a design by Viertl³⁰. The pistons of the stress apparatus are similarly

lapped and adjusted for parallelism. Parallel alignment of the pistons is accomplished by placing a small commercial gauge block between the pistons and then tightening the piston's alignment screws with a small torque wrench. Parallelism is readily verified by viewing, with crossed polarizers, the strain field of one of an identically-lapped (using the same lapping jig) fused quartz platelet, positioned between the pistons of the apparatus. When the pistons are parallel, the strain field of the quartz is uniform.

3.4 Summary

To summarize, the unique source of intense ultra-short pulsed THz (and sub-THz) laser radiation including corrugated-waveguide output coupling for convenient beam transport, the doping superlattice samples, a vapour-pressure regulated liquid helium cryostat, the uniaxial stress apparatus, and the bolometer signal recovery electronics, are all available and functional. The only remaining task before beginning the phonon generation experiment is to complete the bolometer fabrication work on the rear face of the DSL samples using image-reversal lithography with *AZ5214 E* photoresist and *AZ Developer*. The phonon generation experiments will follow immediately thereafter. Figure 6 shows the overall experimental arrangement.

4. FUTURE APPLICATION – THZ CRYOGENIC ACOUSTIC MICROSCOPE

4.1 Background

After phonon generation by our technique is established, we would like to pursue the development of a cryogenic THz acoustic microscope by the following experiments: (1) the coherent detection of an electromagnetic echo produced in the superlattice from a specularly reflected phonon pulse at the rear surface of the substrate, immersed in 2-K liquid helium (2) the coherent detection of an electromagnetic echo produced in the superlattice from returning coherent phonons that have first propagated across the silicon interface into low temperature (0.150-K) liquid helium-4, and then reflect from a piezomotor-driven sapphire³¹ phonon mirror also immersed in the liquid helium bath (3) the fabrication of an acoustic microlens coated with the phonon anti-reflection multilayer in order to focus the phonon beam in the liquid helium bath to a nanometer beamwaist.

The previous highest operating transducer frequency for a cryogenic acoustic microscope has been near 15 GHz. In this frequency regime (15-GHz), three-phonon decay processes have been shown to result in a depletion of the focused beam and to severely impact the signal to noise ratio.³² However, above 209 GHz, sound attenuation and nonlinearity in low-temperature (<150 mK) helium do not appear to be limiting factors and mean free paths on the order of cm have been measured³³. An acoustic microscope operating above 209 GHz, with a fast acoustic lens impedance-matched to liquid helium-4 (using a ³He one-shot cryostat or a dilution refrigerator) as the coupling fluid, could be expected to possess a resolution of less than a nanometer – a major advance.

4.2 Coherent detection of electromagnetic echo

As the first experiment along the path to the development of a THz cryogenic acoustic microscope, the coherent nature of the generated phonons could be verified in a pulse-echo experiment with phonons remaining within the DSL

substrate immersed in a simple 2-K liquid helium cryostat. A phonon pulse, upon returning to the DSL after undergoing specular reflection (see discussion below) at the rear sample face, will generate an electromagnetic echo pulse which will be coherently detected. The coherence of the phonons in this context refers to the phonons, in the small volume, having a common propagation velocity, wavevector, and phase. For an optimal detection signal in the pulse-echo experiment, incident acoustic waves must have a wavefront parallel within a part of a wavelength to the DSL surface in order to get no phase cancellation in the mean value of the produced electric field. The thick, superpolished rear face of the substrate will satisfy parallelism and flatness conditions³⁴ for an acoustic wavelength on the order of tens of nanometers. The echo pulse would be coherently detected and captured on a fast (1-GHz bandwidth) digitizing oscilloscope. The phonon linewidth would be extracted by deconvolving the instrumental linewidth from the Fourier transform of the digitized echo pulse.

Coherent detection of the electromagnetic echo would be employed using a room-temperature Schottky-barrier diode mixer, with an NEP of 10^{-19} W/Hz^{1/2}, in a waveguide-based monolithic heterodyne receiver using the tripled output of a Gunn oscillator as the local oscillator (LO). The LO could provide up to 2 mW of cw power. A complete waveguide-based receiver at 245.5 GHz, containing a conventional mixer, the LO and the IF processing electronics, is commercially available.³⁵ We estimate the expected SNR as follows. The one-way conversion efficiency ξ of a DSL with period 34.5-nm and a maximum two-dimensional doping concentration of $n_D^{(2)} = 1.7 \times 10^{13}$ cm², expressed in terms of the number of periods N , is $4.7 \times 10^{-11} N^2$. Assuming a 50% grating coupling efficiency, a 50% beamsplitter for the laser radiation, and a 10 kW laser pulse at 246 GHz, the electromagnetic power generated by the acoustic echo and arriving at the detector is $1.4 \times 10^{-18} N^4$ W. The electromagnetic power at the detector would exist in a bandwidth determined by the finite number of superlattice periods given by $\Delta f = \sqrt{2}(246)/N$ GHz. For this bandwidth, the Schottky sensitivity is $3.5 \times 10^{-8}/N$ W. In terms of the number of periods; the expected SNR is $4 \times 10^{-11} N^5$. For example, one would need to use a superlattice containing approximately 500 periods, corresponding to a bandwidth of 0.70 GHz, in order to achieve a SNR of 30 dB. If necessary, the SNR could be increased by the integration of successive pulses.

4.2 Ensuring specular reflection at DSL/liquid helium interface

A technical challenge would exist in producing specular reflection at the rear silicon/liquid helium interface. Specular scattering does not normally occur at ordinary (imperfect) interfaces in the case of phonons with wavelengths of a few hundred angstroms or less; instead, the scattering becomes diffusive. A strong connection exists between the defect-induced diffuse scattering of high-frequency phonons at a solid/liquid helium interface and the Kapitza effect³⁶ (The Kapitza effect refers to the anomalously low interfacial thermal resistance that exists between solids and liquid helium at these frequencies compared to the predictions of the acoustic impedance mismatch model.) However, work on the polarization dependence of the Kapitza effect for nearly normally incident phonons provides strong evidence that, for properly *ex situ* prepared surfaces, only the transverse modes behave anomalously.³⁷ For instance, a specialized wafer polishing technique, HF spin-etching, has been demonstrated to eliminate diffusive scattering for normally incident LA phonons of somewhat longer wavelength (46 GHz). The spin-etch removed the native oxide layer in such a way that the resulting surface consists of large, atomically smooth, H-terminated silicon terraces. Smooth, clean surfaces produced in this manner were reported to result in a reduction in the anomalous Kapitza transmission by a factor of 20 for 200 GHz TA phonons, compared to more conventional *ex situ* cleaning techniques, employing only detergents and/or organic solvents. In addition, laser annealing has been shown to eliminate diffusive phonon scattering at a silicon-liquid helium interface³⁸. These techniques for eliminating diffusive scattering are expected to hold for higher frequency phonons as

well, provided that $q_{\perp}d \ll 1$, where d is the thickness of the surface defect layer, including the mean amplitude of any surface roughness, and q_{\perp} is the component of the phonon wavevector normal to the surface. With increasing q_{\perp} , the defects extend beyond the phonon amplitude node at the surface and begin to feel the strain field. For 246 GHz LA phonons in Si, $q_{\perp} = 0.018 \text{ \AA}^{-1}$. Any surface roughness, contaminants, defects and/or subsurface damage should therefore have a characteristic thickness much less than 50 Å in order for the Kapitza anomaly to become extinguished. With recent improvements in superpolishing³⁴ and these surface preparation techniques, this constraint may be able to be satisfied.

4.3 Anti-reflection multilayer for terahertz LA phonons

After successful pulse-echo experiments within the crystalline substrate are completed, the next step would be to successfully transmit a coherent phonon beam into low-temperature liquid helium-4, the coupling fluid for a reflection acoustic microscope application. It would be also necessary to apply a phonon anti-reflection coating after excimer laser-annealing rear surface of the DSL substrate for efficient and coherent phonon transmission into the liquid helium bath.

The anti-reflection multilayer for LA phonons will be fabricated using an amorphous (*a*-) silicon dioxide/silicon superlattice (ASL); the ASL has been reported by Koblinger *et al*³⁹. For phonons propagating along a crystal symmetry direction and arriving at normal incidence upon a flat ASL, the anisotropy of the elastic constants may be ignored. In this case, the characteristic matrix method of stratified media⁴⁰ of classical optics may be used to compute the phonon transmissivity, provided one substitutes for the impedance of the electromagnetic wave, the acoustic impedance $Z_i = \rho v_i$ of the individual layers of the ASL with density ρ , and phonon velocity v_i . The speed of 246 GHz phonons in helium-4 is 189 m/s and the density at 150-mK is 0.145 g/cm^3 ⁴¹. The corresponding acoustic impedance of helium-4 at this temperature becomes $2.74 \times 10^3 \text{ g/(cm}^2\text{-s)}$. The ASL would be fabricated in an ultrahigh-vacuum, electron beam evaporation system as was done by Koblinger. In general, the elastic constants for amorphous materials depend upon the growth technique. However, for films grown in an ultrahigh vacuum ($<10^{-8}$ Torr) electron beam evaporation system, the impedances are known. The longitudinal phonon velocity⁴², in this frequency regime, in *a*:SiO₂, is 5840 m/s. The density of *a*:SiO₂ is 2.3 g/cm^3 , yielding an acoustic impedance of 1.34×10^6 , in the above units. For *a*:Si, the longitudinal phonon velocity can be found from the TA phonon velocity, given by Koblinger, when one makes use of the simplifying assumption⁴³ that the TA and LA phonon velocities scale by a common factor $r = v_{\text{TA}}/v_{\text{LA}} = 0.62$. For *a*:Si in the units above, the acoustic impedance for longitudinal phonons becomes 1.64×10^6 . Using these parameters, a simple calculation, employing the characteristic matrix method of stratified media⁴⁴, predicts a phonon transmissivity greater than 99% for a multilayer stack consisting of 32 alternating quarter-wave layers of *a*:SiO₂ and *a*:Si of thickness' 5.0 and 8.6 nanometers, respectively. The layer thickness can be controlled to better than 3% using *in situ* atomic absorption techniques during thin film deposition⁴⁵.

To obtain a smooth silicon/ASL interface, the *ex situ* spin-etch surface cleaning and passivation technique would be done on the superpolished and excimer laser-annealed substrate within one hour prior to the growth of the ASL. In addition, one would spin-etch the ASL surface, just prior to sample insertion into the low temperature cryostat, in order to remove a protective capping *a*:SiO₂ layer grown during ASL fabrication. After the capping layer had been removed, the top *a*-Si layer of the ASL would be smooth and clean⁴⁶. By these techniques, it might be possible to eliminate the

diffusive scattering of nearly-normal incident LA phonons at the ASL/liquid helium interface and, therefore, preserve the spatial coherence of the phonon pulse as it is transmitted into the He II bath.

Santos *et al.*⁴⁷ have reported that phonons with a frequency as high as 600 GHz can easily traverse a large number (>200) of layers and interfaces of amorphous Si:H and Si:N_x without noticeable degradation. This implies that the coherence length of the phonons far exceeded the superlattice thickness (~1 μm) used by Santos. Since the ASL reported by Koblinger *et al.* has sharper filter characteristics than similar superlattices formed of amorphous Si:H and Si:N_x, one may conclude that the thickness of an amorphous Si/SiO₂ superlattice consisting of 32 layers should be much less than the coherence length of 246 GHz LA phonons.

In this step in the development of the THz cryogenic acoustic microscope, at some distance from the substrate in the helium-4 bath, the propagating phonon pulse would arrive normally incident upon a polished sapphire surface and undergo specular reflection³¹. A piezomotor-driven positioner specifically designed for use in low temperature applications⁴⁸ would drive the sapphire phonon mirror. It may be most prudent to perform this experiment at the University of California-Santa Barbara *Center for Terahertz Science and Technology* (available resources include a free electron laser as a tunable source of intense pulsed THz radiation (~10-KW peak power with 40-ns pulsewidth), a dilution refrigerator and fast THz detectors).

4.4 Acoustic lens

The final experiment to demonstrate the feasibility of a terahertz cryogenic acoustic microscope would be to fabricate a high-quality acoustic microlens on the rear silicon substrate and to apply the phonon anti-reflection coating as described above, to focus the phonon beam to a nanometer waist in the low-temperature helium-4. Acoustic lenses suitable for operation at a lower frequency of 1-GHz have been fabricated by an isotropic chemical etch⁴⁹. However at terahertz frequencies, advanced dry etching techniques would be used to fabricate the precision acoustic microlens. For instance, MEMS Optical Inc. (<http://www.memsoptical.com>) can fabricate mm-diameter hemispherical acoustic lens with ~mm focal lengths, using gray scale technology and deep reactive ion etching, with a spherical error under 15 nm rms and a surface roughness of ~2-8 nm. Alternatively, one could attempt the fabrication of the acoustic microlens in single crystal silicon using ultra-precision lathe single-point diamond turning (Corning NetOptix, Inc., <http://www.corningnetoptix.com/>). Prior to the application of the phonon AR coating upon the lens surface, an excimer laser anneal⁵⁰ to remove any subsurface amorphous regions, would also be performed.

In order to accurately predict the profile of the acoustic beam waist at the focus, one would first need to calculate the spatial distribution of the transmitted phonon intensity across the surface of the AR-coated acoustic lens. The [100] phonons, propagating in the silicon substrate, will arrive at oblique angles to the convex surface of the ASL forming the AR-coating and consequently, will undergo mode conversion at the ASL interfaces. However, the calculation should be possible using recent techniques.⁵¹

ACKNOWLEDGEMENTS

This work has been generously supported by the US Army Research Office: Program of *Theoretical Physics and Nonlinear Phenomena*, under contract numbers DAAD19-01-1-0466 and DAAHO4-96-1-0401.

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