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## Prices and Price Dynamics

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# Bard



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Prices and Price Dynamics

by

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I. Introduction.

Simultaneous inflation and unemployment, which has led to the coinage of terms like "stagflation" and "slumpflation," does not seem to be a transitory phenomenon; ~~On the contrary,~~ <sup>deep seated</sup> ~~It~~ seems to be an attribute of today's

capitalism, in the sense that the processes set in motion by the behavior of individuals, firms and governments, <sup>the</sup> within decentralized markets that exist in today's institutional framework, lead to the combination of chronic inflation and unimpressive employment and growth results, ~~that are evoked by the labels~~ <sup>that is labeled</sup> slumpflation and stagflation. The argument that follows implies that the

economic malaise of our times cannot be ~~caused~~ <sup>caused</sup> ~~corrected~~ <sup>changing</sup> by simply ~~correcting~~ monetary and fiscal policies. ~~Improvement will need to be preceded by changes in the~~

~~market power of firms and labor.~~ <sup>It is market power in such power is now</sup> ~~It is market power which lends an~~ "institutional" ~~life of its own to price formation~~

In this paper, we examine output, wage, and price determination in a ~~the~~

system which reflects characteristics of advanced capitalist economies. The structural forces that make stagflation a normal result are ~~firm~~ <sup>administered firm</sup> market powers which ~~leads to~~ administered prices, negotiated wages, and big government.

Administered prices reflect the market power of corporations, <sup>as corporations have used power</sup> ~~derived from the~~ need imposed by financing arrangements to sustain profits flows in an economy where firms with expensive special purpose capital assets and complex liability

structures. Negotiated, or even legislated, wages and wage changes reflect trade union power and the need for comparability of costs for "independent" units that share "market power." <sup>to be comparable</sup> Big government in today's economy mainly operates by way of transfer payments and defense spending. Big government implies a need for high taxes. The combination of government spending and taxing schedules related to income means that the government <sup>surpluses and</sup> ~~deficits~~ <sup>are</sup>

sensitive to income variations. As will be shown below, "big government",

speculation and technical changes that affect market in long run

the market power of firms and labor. It is market power in such power is now exercised that underlies the price dynamic and wage dynamics that leads to the inflation component of current behavior.

need the

which may legislate market power, is of particular importance in that it provides a mechanism that permits the price <sup>that result from the</sup> ~~implication of firms and labor~~ <sup>of firms and labor</sup> market power to be validated in the sense that sales receipts not only cover costs but also generate "ample" profits.

History--the actual path of an economy--results from a combination of systemic and transitory factors. Many explanations of stagflation appeal to transitory and accidental phenomena: the Viet Nam War, the reaction of government economic policy to the social turbulence of 1968-69, the effective oil cartel, and policy errors by <sup>bilateral and</sup> various monetary authorities. Such special events, which are part of the fullness of history, <sup>may</sup> undoubtedly play a significant part in determining the details of what happens. However, there is a core of systemic economic and, because big government is part of the system, political relations that make for a persistence of inflation even as the performance of the economy as measured by unemployment and growth rates deteriorates.

As a result of today's <sup>cash technical</sup> structure, the shape of business cycles has changed. A full-fledged debt deflation, followed by a deep and long depression, cannot occur. This is so because the huge deficit that well-nigh automatically occurs when income turns down sustains prices and profits. This means that the ability of business to fulfill obligations is not compromised <sup>cessions as a result</sup> ~~so that~~ the value of debts and capital assets tend to be sustained.<sup>1</sup> This stabilizing effect of the big government, however, has destabilizing implications for wages and prices. ~~The failure of the conventional theory of the labor market, as embodied in the Phillips curve, to explain rising wages and prices in the face of chronic and worsening unemployment, is one starting point of our analysis.~~ However, our objection goes behind its simple failure. More seriously, the Phillips curve violates the spirit and methodology of modern economic analysis in which interdependent markets determine system

results. The labor market cannot be held responsible in isolation for what happens to wages and prices.

The model that follows is open in that values for investment, tax schedules and endogenously determined parameters that set saving or consumption propensities of classes of income recipients are not discussed. The financial determinants of investment and the systemic interrelations among financial relations and investment which make a debt-deflation process possible have been dealt with by one of the authors in a series of papers. In a similar way in a number of places the other author has discussed the institutional features that lead to market power in labor markets. Our objective in this paper is to understand how the macroeconomics of price determination that follow from a post-Keynesian view of demand determination interacts with the obvious institutional relations in a labor and commodity market which makes the price level a function of past contractual commitments.

## 2. The Analytical Framework

There are two aspects to the price formation model we are examining. One aspect reflects the bargaining process between firms and labor that sets wages and the market power of firms that sets prices given the course of unit labor costs. The second aspect reflects the prices that are derived from aggregate demand and supply. Both the market power/bargaining and the aggregate views of price formation can be interpreted as asserting that prices are a mark-up in unit labor costs, but the substance of the mark-up is different in the two cases.

The bargaining power and market power formulation of price requires both a wage and a price equation. In a general form, they may be represented as:

simple failure. More seriously, the Phillips curve <sup>position of conventional theory</sup> violates the spirit and methodology of modern economic analysis, in which interdependent markets determine system results.

On the other hand, it is possible to show how the monetarists tend to simplify the questions. In our model the influence of the monetary variables is indirect (which does not mean unimportant) and passes through the shifts of ceilings and floors through time.

Our impression is that the economic malaise of our times cannot be eased by simply correcting monetary and fiscal policies.

## 2. The analytical framework.

Let us first consider the bargaining and market power formation of prices. <sup>determination. This</sup> ~~One~~ requires both a wage and a price equation. In a general form, they may be represented as :

$$2.1 \quad P(t) = f(W(t), X(t)) + \alpha P^o(t)$$

$$2.2 \quad W(t) = g(Y(t)) + \beta P^o(t)$$

where  $P(t)$  and  $W(t)$  represent the price and the wage levels at time  $t$ ;  $X(t)$  and  $Y(t)$  stand for a list of real variables (to be identified) and  $P^o(t)$  reflects price expectations.

If we substitute 2.2 into <sup>we obtain</sup> 2.1 under particular ~~hypothesis~~ and specifications which are stated below, we ~~obtain~~ a second order difference equation of the type:

$$2.3 \quad P(t) - (C+D)P(t-1) + DP(t-2) = Z$$

<sup>This</sup> which looks like the reduced form of the accelerator-multiplier trade cycle model.<sup>2</sup> It is not necessary to constrain the values of the parameters  $C$  and  $D$  in order to obtain non-explosive <sup>or</sup> results. It is sufficient to posit <sup>dated</sup> transitory limits to actual prices.

In econometric models the values of the parameters of difference equations are constrained so as to avoid explosive results. <sup>or constraints</sup> The ~~assumptions~~ are necessary because <sup>these models assume that</sup> the structure of the economy is kept constant through time. However, if structural changes are taken into account, the range of possible <sup>for dynamic interaction</sup> behavior patterns becomes wider. The hypothesis of ceilings and floors <sup>allows for</sup> which embody structural parameters <sup>to</sup> which change, <sup>Therefore the models</sup> in time ~~allows the~~ incorporation <sup>if unconstrained</sup> of parameter values which generate explosive behavior, <sup>However the time</sup> that cannot be extended in time because <sup>of the structure of the economy</sup> of the structure of the economy. <sup>It leads to new regimes</sup> In fact, <sup>allows for structural changes</sup> it has been shown that otherwise explosive models can be bounded by floors and <sup>such floors and ceiling</sup> ceilings which, by imposing new initial conditions, <sup>rather than they are "attractive"</sup> lead to a realistic outcome from relations that would yield an <sup>or explosive</sup> unstable result. It follows that we have to identify:

- 1) a reasonable set of assumptions which allow us to derive, from equations 2.1 and 2.2, a second order difference equation such as 2.3;

- ii) an economic justification for the presence of ceilings and floors and for their path in time;
- iii) a model which can explain ~~not so much~~ the existence of stagflation <sup>and a few developments of stagflation</sup> as its likely pattern in a medium run perspective.

### 3. The Wage-Price Sub-Model

The price equation 2.1 as set by firms, can be specified as follows:

$$3.1 \quad P(t) = \gamma \frac{W(t)}{a^o(t)} + \alpha P^o(t),$$

$W(t)$  is the money wage rate,  $a^o(t)$  is the entrepreneur expectation of normal labor productivity.  $W(t)/a^o(t)$  can also be written as  $C_L(t)$ , the <sup>normal</sup> unit labor costs of output. The mark-up factor  $\gamma$  reflects a combination of market power, history and the cash payment requirements imposed by the liability structure. There is some minimum ~~achieved~~ mark-up on labor costs which must be achieved if a firm is to fulfill its various payment commitments because of debts.

Equation 3.1 can be rewritten as

$$3.11 \quad P_t = \gamma C_L(t) + \alpha P^o(t).$$

If expectation are extrapulative<sup>3</sup>, we obtain:

$$3.2 \quad P(t) = \gamma \frac{W(t)}{a^o(t)} + \alpha [P(t-1) + \theta(P(t-1) - P(t-2))] \text{ or}$$

$$3.21 \quad P(t) = \gamma C_L(t) + \alpha [P(t-1) + \theta(P(t-1) - P(t-2))]$$

These price equations represent the market power of firms.  $P(t)$  is the index of offer prices which may or may not turn out to be the realized prices.

~~In much of recent literature the course of wages almost always conforms to a Phillips curve, i.e., an inverse relation between the rate of change of money wages and the level of unemployment, perhaps adjusted to reflect recent ad/or anticipated rates of changes of prices. The adjustments have become more complicated and carry more of the econometric explanatory weight as~~



observations from the turbulent years since the middle 1960's gather weight. The Phillips curve of recent literature is a complex reflection of the original formulation. As far as the money wages are concerned,

We live in a world in which trade unions exist and money wages are affected by bargaining or negotiations. The wage function must take this into account. True, unemployment<sup>m</sup> affects the wage bargains that are struck. However, as governments have assumed responsibility for maintaining employment and as catastrophic large and sustained unemployment has been avoided, the effect of today's unemployment rate on today's wage bargains has been attenuated. In this sense, today's unemployment rate may be dropped from the wage equation as an explicit variable, although chronic high unemployment can lead to a fall in the market power of unions that lead to wage dynamics.

We can write equation 2.2 as:

$$3.3 \quad W(t) = g(T_x, a^{\circ}_w) + \beta P^{\circ}(t)$$

where  $T_x$  represents taxation and  $a^{\circ}_w$  stands for an improvement factor achieved by wage bargaining. In other words, we assume that money wages are the result of bargaining processes in which trade unions and employers agree on price adjusted after-tax wages. For the ~~(expected)~~ price component in the wage equation <sup>one can</sup> posit the existence of explicit or implicit full or partial indexation. In that case, <sup>OUC</sup> we obtain:

$$3.4 \quad W(t) = g(T_x, a^{\circ}_w) + \lambda P(t-1)$$

Incomes policy and social contracts introduce limits to the parameters. The typical wage and price freeze or income policy requires workers forego attempts to recoup past losses in the purchasing power of wages in exchange for a promise that ~~no further losses will take place and that henceforth the rise in money wages will exceed the rise in prices.~~ <sup>not full share of</sup> Incomes policy has the effect of institutionalizing expected productivity increases.

both w/d per tendencies & w/d inflation  
 that from decisions looked beyond the  
 market  
 inflation  
 recession

Alternatively,

✓ We may assume the presence of some kind of extrapolative expectations.

In that case, we have:

$$3.5 \quad W(t) = g(T_x, a_w^\circ) + \beta [P(t-1)] + \lambda (P(t-1) - P(t-2))$$

In the short run  $T_x$  and  $a_w^\circ$  can be assumed to be constant. The same may be true for  $a^\circ$  (the normal productivity according to entrepreneurs). If we normalize  $a^\circ$  (i.e., we put it equal to 1) and if we insert equation 3.5 into equation 3.2, we get:

~~$$3.5 \quad W(t) = g(T_x, a_w^\circ) + \beta [P(t-1)] + \lambda (P(t-1) - P(t-2))$$~~

~~In the short run  $T_x$  and  $a_w^\circ$  can be assumed to be constant. The same may be true for  $a^\circ$  (the normal productivity according to entrepreneurs). If we normalize  $a^\circ$  (i.e., we put it equal to 1) and if we insert equation 3.5 into equation 3.2, we get:~~

$$3.6 \quad P(t) - ((\alpha + \gamma\beta) + (\beta\gamma\lambda + \alpha\theta)) \underline{P(t-1)} + (\beta\gamma\lambda + \alpha\theta) \underline{P(t-2)} = Z$$

where  $\frac{Z}{X}$  incorporates the productivity,  $x$  improvement and tax parameters that go into determining wages.

#### 4. Ceilings and Floors: The Workings of an Explosive Second Order Dynamic Interaction

~~The~~ Equation 3.6 can be written in the following way:

$$4.1 \quad P(t) - (C+D) P(t-1) + D P(t-2) = Z$$

C being equal to  $\alpha + \gamma\beta$  and D being equal to  $\beta\gamma\lambda + \alpha\theta$ .

The ~~weight~~ of the various parameters may differ in the various countries and in the same country from time to time according to the political and economic situation. In periods of inflation they generally become bigger. If this happens, the mechanism transmitting inflation in the economy becomes stronger. So 3.2 and 3.5 are not the only specification which can give rise to a reduced form of the 4.1 kind.

The general solution to the second order difference equation is given by:

$$4.2 \quad P(t) = A_1 \mu_1^t + A_2 \mu_2^t + h_0$$

where the roots  $\mu_1$  and  $\mu_2$  depend upon the value of the parameters C and D *of eqn 4.1* while  $A_1$  and  $A_2$  are determined by initial conditions.

If we assume that the parameters *of eqn 4.1* are constant, so are  $\mu_1$  and  $\mu_2$ . These *two roots of the solution equation* parameters *besides C and D, and M* may assume values greater than one. In that case the model will tend to explode unless ceilings and floors force an oscillatory pattern, **5** around the particular solution to the difference equation which is given by  $h_0$ .

*change for 3 hrs*  
The ~~nature~~ of the time path of the variable generated by the model depends upon whether the rate of growth of the ceiling is greater than, equal to, or less than the minor root of the solution equation. If one assumes that the larger root of the solution equation is greater than the rate of growth of the ceiling, so that in time the ceiling becomes effective, the problem then is to ascertain whether, once the ceiling becomes effective, the variable will bounce off the ceiling, yielding an upper turning point, or will continue to press against the ceiling, resulting in a state of steady inflation.

As is shown in the appendix, if the rate of growth of the ceiling (c) is equal to or greater than the minor root of the solution equation

$$\mu_1 > c > \mu_2 > 1$$

then the particular solution equation will continuously press against the ceiling so that a steady inflation will take place. If, on the contrary, the rate of growth of the ceiling is smaller than the minor root:

$$\mu_1 > \mu_2 > \overset{c}{1}$$

then the variable will bounce off the ceiling and a turning point will be generated. A succession of such bounces between the ceiling and the floor generates a cycle.

In periods of inflation, the reaction by both firms and trade unions may be such to justify parameters greater than one. In this case, then, we have to look for a meaningful ceiling which at least for a time imposes a pattern of wages and prices other than those given by the market power and bargaining relations embodied in these wage and price equations.

Solution equations like 4.2 are summaries describing the time path of a recursive process such as is given by equations like 3.2. If the two most recent values of prices are given then an equation like 3.2 will generate a current price. If this current price becomes the  $t-1$  price and the previous price becomes the  $t-2$  price, a value of  $P(t+1)$  will be generated. This can be carried out through time and generate a time series of prices.

In a solution equation such as 4.2 the initial conditions determine the  $A_1$  and  $A_2$ . The value for  $P(t)$ ,  $P(t-1)$ , etc., obtained from the difference equation and that obtained from the solution equation are exactly the same.

If in the course of events a realized value differs from the value generated by the recursive formula or the solution equation then a new dynamic process is set in motion with new initial conditions. Thus, as long as the parameter values of the recursive equation are unchanged, the  $\mu_1$  and  $\mu_2$  are unchanged, but any time the realized differs from the computed value the dynamic process continues with a new set of values  $A_1$  and  $A_2$ .

If the ratio of the initial conditions,  $\eta$ , is  $\mu_1 > \eta > \mu_2$ , then the two roots will be weighted by  $A_1$  and  $A_2$  so that the average equals  $\eta$ . However, because of the power of raising to a power the rate of increase of the computed value will increase to  $\mu_1$ .

On the other hand, if  $\mu_1 > \mu_2 > \eta$  and the average of  $\mu_1$  and  $\mu_2$  must equal  $\eta$ , then one of the coefficients in the averaging process must be negative: as  $\eta$  is closer to the smaller positive root, this is achieved by having a small

negative coefficient to the larger root. This means that the unconstrained motion set in process by these initial conditions in time will have the system move more rapidly in the opposite direction from the thrust given by the initial conditions. If the initial condition were set by a ceiling then the free movement of the extrapolative market power pricing funds will fall away from a constant rate of growth ceiling. One exposure to a limitation of growth leads to a rapid dynamic movement away from a ceiling.

### 5. Macroeconomic Determinants of Prices

In equation 3.2 we posited that prices are set according to a mark-up convention, where the unit labor costs that are marked up reflect normal output and productivity; the price formula included a factor allowing for price anticipation.

Firms are not always successful in attaining their price, quantity and profit objectives. There are situations in which they cannot impose prices and achieve output or profit targets. It is the macroeconomic conditions that determine whether the aggregate firms achieve their price, output and profit objectives.

From Kalecki we know that aggregate profits for a closed economy are given by:

$$5.0 \quad \Pi = I + Df + C_{\Pi} - SW, \quad S_w$$

where  $\Pi$  = profits,  $I$  = investment,  $Df$  = the deficit,  $C_{\Pi}$  = consumption out of profits and  $SW$  = savings out of wages. Aggregate profits equals profits in consumption production,  $\Pi_c$ , and profits in investment production,  $\Pi_I$ . We therefore have:

$$5.1 \quad \Pi_c = W_I N_I + Df + C_{\Pi} - SW \quad \text{and}$$

$$5.11 \quad \Pi_I = \Pi_I.$$

Total revenues in the production of consumer goods equals total expenditure on

consumption goods. Total revenues in consumption goods production equals the expenditure financed by wage income in the products of consumer goods and the profits earned in consumer goods production.

$$5.2 \quad P_C Q_C = W_C N_C + \Pi_C$$

$$5.21 \quad P_C Q_C = W_C N_C + W_I N_I + Df + C\cancel{I} - S\cancel{W}$$

We therefore have

$$5.3 \quad P_C Q_C = W_C N_C \left( 1 + \frac{W_I N_I + Df + C\cancel{I} - S\cancel{W}}{W_C N_C} \right)$$

Inasmuch as the <sup>biggest</sup> price level is a factor affecting wages, the relevant price level for wage dynamics is that of consumer goods. The demand or realized price level of investment goods is quite different in its conception than the price level of investment goods. If  $W_I N_I$  are the wage costs in the production of investment goods and  $\rho$  is the interest rate or costs imposed by eternal financing terms and the producer's margin of safety we have that

$$P_I Q_I = W_I N_I (1 + \rho).$$

$Q_I$  of investment will take place at price  $P_I$  only as long as business people and their bankers can come up with  $W_I N_I (1 + \rho)$  of take out financing either from internal funds (gross retainment profits) or from new issues of appropriate debts or equities. The wage rate in investment output is determined by the same considerations as the wage rate in consumption output.

The aggregate price level at any period is compounded out the determinants of the movement of consumer goods prices and investment goods prices.

The realized price level for consumer goods becomes

$$5.4 \quad P_C = \frac{W_C N_C}{Q_C} \left( 1 + \frac{W_I N_I + Df + C\cancel{I} + S\cancel{W}}{W_C N_C} \right)$$

The price level for investment goods is

$$P_C Q_C = W_C N_C + \Pi_C$$

$$P_C Q_C = W_C N_C + W_I N_I$$

$$P_I = \frac{W_I N_I}{Q_I} (1+\phi) - \frac{W_I}{R_I}$$

where P reflects financing terms and  $W_I N_I$  reflects the financing that must be obtained.

Let us write  $Q_C^o$  for the normal output consumer goods and  $Q_C$  for the actual output; the ratio of actual to normal output is

$$k_C = Q_C / Q_C^o$$

If we write  $a_C^o = Q_C^o / N_C$  as the normal productivity of labor in the production of consumer goods then 5.4 becomes

$$5.51 \quad P_C = \frac{W_C N_C}{W_C} \cdot \frac{Q_C}{Q_C^o} \left( 1 + \frac{W_I N_I + Df + C_I + SW}{W_C N_C} \right)$$

$$5.52 \quad P_C = \frac{W_L}{a_C^o} \cdot \frac{Q_C}{Q_C^o} \left( 1 + \frac{W_I N_I + Df + C_I + SW}{W_C N_C} \right)$$

$$5.53 \quad P_C = \frac{W_C}{a_C^o} \cdot \frac{1}{k_C} \left( 1 + \frac{W_I N_I + Df + C_I + SW}{W_C N_C} \right)$$

Equation 5.53 can be written as

$$5.54 \quad P_C = \frac{C_L}{k} \cdot (1+M)$$

for  $\frac{W_L}{a_L}$  is the unit labor costs  $C_L$ ,  $k$  is the ratio of output to target output

and  $M$  is the ratio of demand for consumer goods financed by other than the wage bill in consumer goods to the wage bill in consumer goods. Equations 5.51 through 5.54 are macroeconomic price equations. This is not quite a precise statement of  $M$  for  $SW$  represents savings out of wage income. We assume that prices are as in the market power and bargaining equations as long

*if really want the true market output*  
 $P_C = \frac{C_L}{k} (1+M)$   
 $P_C = \frac{C_L}{k} (1+M)$   
 $P = \frac{W_C N_C + Df + C_I + SW}{W_C N_C}$   
 $= \frac{W_C N_C}{W_C N_C} + \frac{Df + C_I + SW}{W_C N_C}$

## 5. Macroeconomic determinants of prices.

In equation 3.2 we posited that prices are set according to a mark-up convention, where the unit labour costs that are marked up reflect normal output and productivity; the price formula included a factor allowing for price anticipations.

Firms are not always successful in attaining their price, quantity and profits objectives. There are situations in which they cannot impose prices and achieve output or profit targets. It is the macroeconomic conditions that determine whether in the aggregate firms achieve their objectives.

From Kalecky we know that aggregate profits for a closed economy are given by : (6)

$$5.1 \quad \pi = I + Df + C_{\pi} - S_w$$

where  $\pi$  are profits,  $I$  investment,  $Df$  deficit,  $C_{\pi}$  consumption out of profits and  $S_w$ , savings out of wages.

Under reasonable assumptions, we may write for a closed and integrated economy :

$$5.2 \quad PQ = WN + I + Df + C_{\pi} - S_w$$

since we have defined profits as the difference between the value of output ( $PQ$ ) and the wage bill ( $WN$ ),  $N$  being the amount of employment.

$$\begin{aligned}
 PQ &= W_e N_e + W_e N_s + \pi_e + L_e - S_w \\
 &= W_e N_e + \pi_e \\
 &= W_e N_e + \pi_e + L_e - S_w \\
 &= W_e N_e + \pi_e + L_e - S_w
 \end{aligned}$$



Or we may write :

$$5.3 \quad PQ = WN \left( 1 + \frac{I + Df + C_{\pi} - S_w}{WN} \right)$$

The realized price level becomes :

$$5.4 \quad P = \frac{WN}{Q} \left( 1 + \frac{I + Df + C_{\pi} - S_w}{WN} \right)$$

Let us write  $Q^{\circ}$  for normal output and  $Q$  for actual output. The ratio between the second and the first one becomes: (7)

$$k = \frac{Q}{Q^{\circ}}$$

If we define  $a^{\circ} = Q^{\circ} / N$

as the normal productivity of labour, then 5.4 becomes (8):

$$5.5.1 \quad P = \frac{WN}{Q} \frac{Q^{\circ}}{Q^{\circ}} \left( 1 + \frac{I + Df + C_{\pi} - S_w}{WN} \right)$$

or

$$5.5.2 \quad P = \frac{W}{a^{\circ}} \frac{Q^{\circ}}{Q} \left( 1 + \frac{I + Df + C_{\pi} - S_w}{WN} \right)$$

$$5.5.3 \quad P = \frac{W}{a^{\circ}} \frac{1}{k} \left( 1 + \frac{I + Df + C_{\pi} - S_w}{WN} \right)$$

Equation 5.5.3 can be written as :

$$5.5.4 \quad P = \frac{c_l}{k} (1 + M)$$

where  $c_l$  is  $W/a^0$  i.e. the normalized labour cost,  $k$  is the ratio of output to target output and  $M$  is the mark up, given by the ratio of exogenous expenditure to the wage bill:

$$5.6 \quad M = \frac{I + Df + \frac{C}{\pi} - \frac{S}{w}}{WN}$$

Given the exogenous variables, the equations 3.2, 3.5, 5.5.4 and 5.6 determine  $P(t)$ ,  $W(t)$ ,  $k$  and  $M$ .

Equations 5.5 are macroeconomic price equations. We assume that prices are as in the market power and bargaining equations as long as the macroeconomic price equation can equal that level for a given mark up by adjusting  $k$ , the ratio of employed to employable resources.

as the macroeconomic price equation can equal that level for a given mark-up by adjusting  $k$ , the ratio of employed to employable results.

## 6. The Path of Prices

There are two price level equations and they represent different aspects of the workings of the economy. One price equation represents the market power of firms and the bargaining process in wages. This equation can be interpreted as yielding the supply price. The second price equation represents the aggregate demand conditions. In this second price equation the mark-up on unit costs is determined by the ratio to the wage bill ~~in~~ ~~consumption goods~~ of investment, the government deficit, the balance of trade and the consumption propensities of wage earners and profit receivers.

In both equations prices are mark-ups on unit labor costs which is the ratio of money wages to the productivity of labor. The course of money wages reflects bargaining and political processes.

The market power/bargaining power price equation becomes a second order difference equation

$$3.6 \quad P(t) - \left( \frac{\alpha}{\gamma + \gamma\beta} + (\beta\gamma\lambda + \alpha\theta) \right) P(t-1) + (\beta\gamma\lambda + \alpha\theta) P(t-2) = Z$$

or

$$3.21 \quad P(t) = \gamma C(t) + \alpha [P(t-1)] + \theta [P(t-1) - P(t-2)]$$

The macroeconomic price equation is:

$$5.53 \quad P(t) = \frac{C_L(t)}{k(t)} (1 + M(t))$$

The actual path of prices depends upon the interaction between the market power price equation and the aggregate demand price equation. We need a reconciliation process, which means we need parameters that will adjust when the prices determined by the two equations differ. One parameter of reconciliation is the level of output relative to normal output,  $k$ , which can

just as well be interpreted as the unemployment rate.

If the unit labor costs in the two formulas are the same, then the reconciliation of the two price levels can be considered to take place by way of output and employment.

$$( ) \quad m_t \quad \frac{C_L(t)}{k(t)} (1+M_t) \stackrel{\text{If } \gamma C_L(t) +}{=} \gamma C_L(t) + \alpha \theta (P_{t-1} - P_{t-2})$$

then  $k$  changes so that equality is achieved. This means that if the aggregate demand price equation for a given  $k$  is higher than the market power price equation, then  $k(t)$  will increase (unemployment will decrease). Similarly, <sup>if the</sup> aggregate demand price equation yields a lower price level <sup>for a given  $k(t)$</sup>  than the bargaining power / market power price equation output will fall, unemployment will increase. That is, if

$$\frac{C_L(t)}{k(t)} (1+M_t) < \gamma C_L(t) + \alpha P_{t-1} + \alpha \theta (k_{t-1} - P_{t-2})$$

then  $k_t$  falls, output falls and unemployment rises.

*The above result is that*

If prices as set by market power are too great for demand then aggregate output falls. Too great a rise in prices <sup>due to</sup> by the exercises of market power implies unemployment. Stagflation is no mystery. <sup>is the</sup> It results from an inconsistency of prices as set by market power and prices as determined by spending patterns ~~of the economy~~. This inconsistency can be reconciled by paying the prices as set by market power but purchasing less. The adjustment comes through unemployment.

If  $\frac{C_L(t)}{k(t)} (1+M_t) > \gamma C_L(t) + \alpha P_{t-1} + \alpha \theta (P_{t-1} - P_{t-2})$ , then  $k_t$  will rise. Thus

prices will be as the market power dynamics would indicate unless  $k_t$  cannot change.

*or no other*

In both cases equality of the market power and macroeconomic price formulas is achieved by adjustment of the ratio of output to target output.

~~Employment and output adjust.~~ Price moderation by units that have market power is good for employment whereas price aggressiveness is bad. <sup>Any accretion of</sup> ~~We have~~ market power will lead to price/wage increases being associated with declines in output and employment. ~~achieved the inverse of the Phillips curve.~~ <sup>as</sup> ~~Inasmuch as~~ fixing unemployment and sluggish expansion of output is <sup>a</sup> ~~one~~ repercussion of increases in prices <sup>price</sup> beyond that which can be sustained by macroeconomic determinants, <sup>by process determined</sup> ~~the result~~ can properly be labeled stagflation.

However, ~~we can posit that~~ the output adjustment process has a limit, <sup>as the constant</sup> that is, there is a  $k_{min}$  and a  $k_{max}$  beyond which  $k$  is not allowed to move:

$k_{min} \leq k^x(t) \leq k_{max}$  <sup>if we work with  $P_c$  then  $k_{min} + k_{max}$</sup>   
 ~~$k_{min}$  is~~ the lowest level of employment policy can tolerate and  ~~$k_{max}$  is~~ some full employment level of output. <sup>is  $k_{min}$</sup>  <sup>as a transfer</sup>

If, with employment at a maximum, <sup>is</sup> prices, as determined by aggregate demand, exceed prices as given by market power, ~~the~~ <sup>lead to</sup> output shortages will ~~make~~ actual prices exceed <sup>represented by</sup> the prices as determined by the market dynamics as given in equation 3.2. This is a case of pure demand inflation and might be likened to the inflation that accompanied the escalated entry into Viet Nam.

With actual  $p(t)$  greater than anticipated  $p(t)$ , <sup>as generally wage price dynamics means</sup> new initial conditions determining a new  $A_1$  and  $A_2$  for the solution equation are set in motion. <sup>the initial conditions for future human price has changed. for those dynamics</sup> This new equation will make for a more rapid rate of growth of the market power/bargaining <sup>prices and wages</sup> wage rate.

When the market power price equation leads to prices that are greater than the macroeconomic price formula allows, then output falls, <sup>and</sup> unemployment rises even as prices rise. This process continues until the minimum accepted employment level is achieved. <sup>OR the market power wage setting and price setting limits are both</sup> At that point two routes to policy are open.

Fiscal policy can increase the deficit along some path, thus increasing the mark-up on labor costs that aggregate demand can sustain. <sup>is consistent with acceptable employment level</sup> This path would lead to rising prices at a faster rate than earlier.

Alternatively, a fight inflation program can be adopted which constrains <sup>increase</sup> the rise in the components of the mark-up. If the prices implicit in this program fall very fast then the reaction through the unemployment level may not be appreciable, <sup>prices achieved will</sup> ~~prices achieved will~~ fall <sup>will break</sup> below the market power ~~relation.~~

If prices are not as the market power equation indicates, ~~the~~ new initial conditions become the basis for a new ruling dynamical <sup>process</sup> ~~equation~~ that lowers the weight of the dominant root--it may even be negative so that a rapid price deflation begins.

The economy is not a mechanical interaction among price determining equations: the economy's actual price path reflects market processes. A break in the price path that market power and bargaining would determine indicates that there has been a change in the effective market power of firms. If there was no firm market power then prices would be as the aggregate demand equation indicates with the k parameter set at some approximation to full employment.

~~If~~ stagflation is the result of firms' market power, <sup>wage determining</sup> the bargaining process, ~~and~~ accomodating monetary/fiscal policies, along with a policy commitment to investment <sup>and</sup> ~~combined with~~ an unwillingness of the authorities to tolerate unemployment above some threshold, ~~then~~ stagflation can be eliminated ~~only~~ if market power, bargaining <sup>are</sup> or the commitment to investment are reduced. ~~Allowing unemployment to increase--forcing a serious depression--~~ <sup>is one way to decrease market power and the impact of bargaining.</sup> ~~is one way to decrease market power and the impact of bargaining.~~

<sup>is one way to decrease market power and the impact of bargaining.</sup> The alternative to a deep depression <sup>is to</sup> ~~is~~ eliminate <sup>inflationary</sup> the impact of market power and bargaining upon prices: <sup>can</sup> to lower the major root of the solution equation for the market power price equation, <sup>level</sup> ~~This can be done in two ways:~~ <sup>be lowered some other way</sup> legislation that truly forces competitive labor and product markets or an

incomes policy which effectively constrains the ability of units with market power to affect prices and wages. *an alternative to a deep depression*

The market and bargaining powers that force the hand of macroeconomic policy <sup>so that it</sup> to validate inflation are themselves the product of the success of <sup>the</sup> macroeconomic demand management in maintaining a close approximation to full employment over an extended period of time. ~~The~~ successful macroeconomic policies reduced the potential penalty for exercising market power by assuring that <sup>the</sup> profit flows will be sustained. Assured profits meant that the use of resources to gain market power by firms along with an acquiescence by firms in the exercise of limited <sup>bargaining</sup> market power by unions led to the development of an institutional structure which gave price and wage determination an "uncontrolled" dynamic of its own. ~~An effective incomes policy must be based~~ <sup>on</sup> upon recognition that the ~~basic cause of the~~ transformation of macroeconomic stabilization policy into an engine of inflation was the growth in market power and an increase in the willingness of those with market power to use their <sup>need under a</sup> power. For incomes policy to enjoy more than a transitory success it must be joined to industrial and labor market policies that aim at constraining and reducing market power. Demand management <sup>is successful as</sup> is successful as output and employment <sup>management</sup> as it works within a structure of competitive markets in which market power is limited.

~~It is not surprising that incomes policy, in the sense of policies that~~ <sup>actively impose the results that would rule in competitive markets where</sup> actively impose the results that would rule in competitive markets where competitive do not exist, is a necessary adjunct to successful monetary and fiscal policy.

## 7. Final Remarks

~~The success of the Phillips curve in explaining wage and price behavior in the sixties led to the diffusion of a trade-off philosophy: more unemployment~~

is necessary if there is to be less inflation. In fact, in the years that followed, increases in unemployment have been tolerated because less inflation was to result. In the seventies, even as the trade-off view dominated policy, we have had more inflation with more unemployment.

An implication of the present work is that unemployment and inflation are both results of the processes by which prices are set and then <sup>validated</sup> "determined" by the structure of income. Unemployment is not a variable that checks inflation as long as the tolerable range of unemployment is slight. The success of the Phillips curve explaining prices and wages in the sixties was more the result of the underlying pattern of the economy than the result of how prices are formed in the labor market.

To understand the new reality of stagflation, one has:

- a) to have a suitable analytical framework;
- b) to identify the main historical changes.

We presented a first target. Two are the elements essential to the working of the model: the parameters of the reduced form of the system that sets ex ante prices are such as to generate an explosive inflation, while the presence of a ceiling to prices due to the limit on the mark-up that can be realized tends to generate unemployment,  $k$  falls when  $P_{ex\text{-}ante} > P_{ex\text{-}post}$ . When  $P_{ex\text{-}ante}$  has to adjust to  $P_{ex\text{-}post}$ , the new initial condition is the  $P_{ex\text{-}ante}$  determining relation can lead to a downturn in prices. The model does not belong to either the cost push or to the monetarist variant of neo-classical thinking. The aspects typically characterising cost push models of inflation are incorporated in to the reduced form, while monetary or financial factors influence the ceiling by affecting financial investment.

The model is open not only because it does not explain the behavior of important variables (for instance, investment or productivity), but also



because it does not pretend to explain the inflation process in its historical experience. <sup>but</sup>

However, as has been pointed out, it is just this openness that makes it more useful for research on a concrete historical experience. The fact that the parameters have changed in such a way as to produce an accelerating inflation is not an explanation of inflation but it is rather an expression of it. ~~The same holds true for the shifts of the ceiling in time.~~

The only way to face a crisis in the process of accumulation and to prevent a deep and lasting depression is to increase the government deficit. This stimulates profits even if it is not sufficient to check unemployment. The inflation of the years since the middle '60's in the United States is a side effect of this medicine (not only huge deficits but also effective lender of last resort intervention which has not been pursued in the present paper). It has taken place in spite of rising unemployment and a weakened labor movement. Other reasons why the ceiling has shifted come from the international links of each economy.

Not only can the present model incorporate the main shocks that have occurred at an international level, but it can be reshaped in such a way as to deal with the inflation explosion in reference to the international system itself.

## 7. Final remarks.

To understand the new reality of stagflation, one has :

- a) to identify the main historical changes;
- b) to have a suitable analytical framework.

We tried to reach the second target. Although many factors contribute to history, we have looked for some systemic factors that makes stagflation a possible result.

Two ~~are the~~ <sup>are</sup> elements essential to the working of the model : 1) the parameters of the reduced form of the system that express what we called as the market power /bargaining process and 2) the macro-economic conditions that set a limit to the <sup>adjustment</sup> mark up that can be realized.

The ~~working of the~~ model can produce a variety of results that cannot be found in those models insisting exclusively either on cost-push aspects or on monetary factors.

The fact that the parameters can change in such a way as to produce an accelerating inflation which does not necessarily explode thanks to the working of a ceiling is not an explanation of inflation but it is rather an expression of it. The same holds true for the shifts of the ceiling in time.

As has been said, a positive aspect of the present model is that it is open to many extensions. For instance, not only the present model can incorporate the main shocks that have occurred at an international level, but it can be reshaped in such a way as to deal with the inflation explosion referred to the international system itself.

## Notes

<sup>1</sup>For these aspects, see Minsky (1980).

<sup>2</sup>See Minsky (1959). In this aggregate model we shall not consider the structure of prices and hence we shall make the assumption that wages depend on prices

~~For a discussion on this point, see Ferri (1973).~~ in general.

<sup>5</sup> $\mu_1$  and  $\mu_2$  are the roots of the characteristic equation:

$$f(x) = x^2 - (C+D)x + D$$

to the second order equation. The roots are determined by setting  $f(x) = 0$ . From elementary algebra, it turns out that if:

$$(C+D)^2 - 4D > 0; C+D > 2 \text{ and } D < 1, \text{ then we have that } \mu_1 \text{ and } \mu_2 > 1.$$

The particular solution is equal to  $h_0 = \frac{Z}{1-C}$ , where  $1-C > 0$ .

<sup>6</sup>See Kalecki (1971).

(3) For a discussion on the meaning of expectations and a criticism to the rational expectations theory, see Tobin (1980). It is worth stressing that in our model the expectations are not fixed once for all but may be changed according to the macroeconomic conditions. See paragraph 6.

(2) In the literature, the nature of wages almost always conforms to a Phillips curve, i.e. an inverse relation between the rate of change of money wages and the level of unemployment, perhaps adjusted to reflect recent and/or anticipated rates of changes of prices. The adjustments have become more complicated and carry more of the econometric explanatory weight as observations from the turbulent years since the middle 1960's gather weight. Phillips curve of recent literature is a complex reflection of the original formulation. A discussion on the origin, the meaning, the changes and the implications of the Phillips

...

is beyond the scope of the present work. For an analysis, see Ferri (1978). Suffice it to stress some points.

i) The relation between wages and unemployment, that was initially stated by Phelps Brown and Phillips, was taken to be an aggregate law of price formulation, i.e.; that the rate of change of the price of a product is an increasing function of the excess demand in its own market.

ii) Afterwards, the researches have taken two routes. On one hand, many authors have tried to find a theoretical paradigm capable of generating the results. Neo-classical frameworks of the various kinds (Walrasian, Pigouvian or the so-called micro-foundations) have been the favourite choice above all in the Anglo-Saxon world. The roots in the Ricardo-Marx tradition has been stressed in the Italian tradition: see, for instance, Sylos Labini<sup>(1976)</sup>. On the other hand, estimates have been carry out in order to quantify the importance of the independent variables and, primarily, the role of the prices which was negligible in the pioniering works. The importance of these studies lies in the attempt to draw economic policy conclusions: if the parameters of the prices is equal to one no trade-off between unemployment and prices is possible.

Three kinds of observations are worth stressing.

First of all, it is important to say that the success of the Phillips curve in the sixties was more the result of the underlying pattern of the economy than the result of how prices are formed in the labour market.

In the second place, it is true, as the rational expectationists claim (but according to Tobin (1980), pag. 29 this is not controversial), that Phillips curves did not survive when economic policy attempted, whether purposefully or not, to purchase lower unemployment with the predicted increment of inflation.

Finally, it is not true, as Friedman claims, that the differences among economists are of empirical nature about the value of the parameters. On the contrary there are important theoretical questions at issue. For instance, how are expectations formed outside a steady-state world? Which are the peculiarities of the labour market? (The developing theory of contracts tries, for instance, to unveil the forces governing institutional arrangements even if <sup>with</sup> many ambiguities), while the marxists stress the relation between wages and the nature of the process of production in a capitalistic world.) Finally, one should ask in which sense the literature on the Phillips curve conceived as a trade-off instrument violates the methodological principle according to which interdependent markets determine system results.

(7) On this point see also Badhuri-Robinson (1980)

(8) We could define normal productivity theratio between normal output  $Q^0$  and optimum employment  $N^0$ , i.e  $a^0 = Q^0/N^0$ . In this case the equation 5.5.3' would become:

$$5.5.3' P(t) = \frac{W}{a^0} \frac{N}{N^0} \frac{1}{k} \left( 1 + \frac{I+Df + C_{\pi} - S_w}{WN} \right)$$

(9) If one wants to emphasize the employment aspects ,one should consider the equation 5.5.3' of <sup>footnote</sup> paragraph 8 and not the equation 5.5.3. In such a case one should consider  $N$  as a variable and one needs one more equation:  $Q = F( N)$  could be a candidate. In such a case the working of the model becomes a little more complicated (  $N$  influences the denominator of  $M$  ).

Appendix.

In order to understand the functioning of the model, one must distinguish between actual prices  $(P(t))^{(a)}$ , prices generated by a particular solution equation  $(P(t))^{(c)}$ , ceiling  $(P(t))^{(c)}$  and floor  $(P(t))^{(f)}$  price levels, identified by superscripts. <sup>(1)</sup>

Since in the present model ceilings will be interpreted as imposing new initial conditions, we take account of these intermittently imposed initial conditions in our notation by writing the date of the initial conditions in parenthesis after  $P(t)$ ,  $A_1$  and  $A_2$  and subtracting the date of the first initial conditions from the solution equation.

In these sections, it will be mathematically convenient to measure the variables  $P$  as deviation from  $h_0$ . A lower case  $p$  will be used when the level of prices is so measured.

Let us start from the determination of  $A_1$  and  $A_2$ .

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(i) A detailed description of these demonstrations are contained in Minsky(1959)

Determination of  $A_1$  and  $A_2$

To determine  $A_1$  and  $A_2$  it is necessary to know the actual level of prices of two dates,  $P(0)$  and  $P(1)$  / We have :

$$\begin{aligned}
 p^{(a)}(0) - P^{(a)}(0) - h_0 &= A_1 (0,1) + A_2 (0,1) \\
 p^{(a)}(1) - P^{(a)}(1) - h_0 &= A_1 (0,1) \mu_1 + A_2 (0,1) \mu_2
 \end{aligned}$$

Assuming  $h_0$  is known and that  $p(1) = \bar{\mu} p(0)$  we have

$$A_1 (0,1) = \frac{\bar{\mu} - \mu_1}{\mu_1 - \mu_2} p(0) \quad (a)$$

$$A_2 (0,1) = \frac{\mu_1 - \bar{\mu}}{\mu_1 - \mu_2} p(0) \quad (a)$$

If  $\bar{p}(1) > p(0) > 0$

and  $\mu_1 > \bar{\mu} > \mu_2$

then  $A_1 (0,1)$  and  $A_2 (0,1)$  are both positive and the price changes generated by this particular solution equation will be positive and the rate of growth of prices will increase, approaching  $\mu_1$  as a limit.

On the other hand, if  $\mu_2 > \bar{\mu}$ ,  $A_1 (0,1)$  is negative. Therefore if  $p(1) > p(0)$  but  $p(1) < \mu_2 p(0)$

$A_1 (0,1)$ , the coefficient of the dominant root will be negative.

This particular equation, with roots large enough to generate an explosive time series, will in fact have one upper turning point. If instead of  $\bar{m}$  we introduce  $c$ , the rate of growth of the ceiling, we obtain the results previously stated.

### The ceiling to prices

In time, say at the  $n$ th date, the rate of growth of prices generated by the particular solution equation will become greater than the ceiling

$$p(n) = A_1(0,1)\mu_1^m + A_2(0,1)\mu_2^m > c^n p(0)^{(c)}$$

where  $c$  is a constant rate of growth of the ceiling.

Whenever a particular solution equation tends to generate a price rate of change inconsistent with the constraint, the actual rate of change will be equal to the ceiling rate of change. And whenever actual rate of change of prices is determined by a constraint, it will be interpreted as imposing new initial conditions.

As  $p'(n)^{(a)}$  and  $p(n+1)^{(a)}$  are both ceiling rate of change,

$$\frac{p(n+1)^{(a)}}{p(n)} = c$$

so that a negative  $A_1(n,n+1)$  coefficient will be determined. As long as  $\mu_1 > \mu_2 > c$

this new particular solution equation

$$p(t)^{(a)}_{n,n+1} = A_1(n,n+1)\mu_1^{t-m} + A_2(n,n+1)\mu_2^{t-m}$$

will generate future rates of change of prices smaller than the ceiling



rates of the respective dates.

Therefore the ceiling will no longer be an effective constraint. The variable will bounce off the ceiling and, unless constrained by a floor, the solution equation will in time generate an income that approaches  $-\infty$  at a rate determined by  $\mu_1$ . (2)

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(2) Mutatis mutandis, we can apply the same kind of technique in the presence of a floor which can be represented by a price equation incorporating some minimum level of mark up. However, as Hicks pointed out "it is harder to demonstrate the necessity of a floor than to demonstrate the necessity of a ceiling". See Hicks(1949)

On the other hand, if  $\mu_1 > c$ ,  $\mu_2 > 1$

a steady solution will be generated. In fact, let us suppose that the  $n$ th and  $(n+1)$ st date are ceiling level of prices. A particular solution equation determined by using these dates' prices as initial conditions will have positive  $A_1$  and  $A_2$  (see A.1 and A.2). This particular equation will yield only positive and increasing prices and  $p(n+2)$  generated by this equation will be greater than  $p^{(c)}(n+2)$ . As a result of  $p(n+2)$  being determined by a ceiling constraint rather than by the solution equation, new initial conditions are effective. This will be repeated as long as the ceiling level of prices is the effective determinant. A steady solution will be generated.