

**Abstract:**

We report some results concerning spectral asymptotics of fractal Laplacians defined one-dimensional self-similar measures with overlaps. We also discuss some applications of the theory, including heat kernel estimates and wave propagation speed. Part of this work is joint with Qingsong Gu, Jiaxin Hu, Wei Tang and Yuanyuan Xie.