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Coexistence of ferromagnetism and unconventional spin-glass freezing in the site-disordered kagome ferrite SrSn₂Fe₄O₁₁

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Single-crystal x-ray diffraction refinements indicate $SrSn_2Fe_4O_{11}$ crystallizes in the hexagonal *R*-type ferrite structure with noncentrosymmetric space group $P6_3mc$ and lattice parameters a = 5.9541(2) Å, c = 13.5761(5) Å, Z = 2 (R(F) = 0.034). Octahedrally coordinated 2a [M(1) and M(1a)] and 6c sites [M(2)] have random, mixed occupation by Sn and Fe; whereas the tetrahedrally coordinated 2b sites [Fe(3) and Fe(3a)] are exclusively occupied by Fe, whose displacement from the ideal position with trigonal-bipyramidal coordination causes the loss of inversion symmetry. Our dc and ac magnetization data indicate $SrSn_2Fe_4O_{11}$ single crystals undergo a ferro- or ferri-magnetic transition below a temperature $T_C = 630$ K with very low coercive fields $\mu_0 H_{c\perp} = 0.27$ Oe and $\mu_0 H_{c\parallel} = 1.5$ Oe at 300 K, for applied field perpendicular and parallel to the c axis, respectively. The value for T_C is exceptionally high, and the coercive fields exceptionally low, among the known R-type ferrites. Time-dependent dc magnetization and frequency-dependent ac magnetization data indicate the onset of short-range, spin-glass freezing below $T_f = 35.8$ K, which results from crystallographic disorder of magnetic relaxation behavior in the short-range-ordered state differs from that of conventional spin glasses. Optical measurements in the ultraviolet to visible frequency range in a diffuse reflectance geometry indicate an overall optical band gap of 0.8 eV, consistent with observed semiconducting properties.

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I. INTRODUCTION

The *R*-type ferrite (RTF) family of ternary oxides includes a range of compositions (Ba, Sr) $M_{2\pm x}M'_{4\mp x}O_{11}$ (M = Mn, Fe, Co, Ni, Cu, Zn; M' = Ru, Ti) [1–8] that exhibit a spectrum of fundamental condensed matter physics phenomena. This broad stability range of known RTF compositions retains only small variations of a hexagonal structure type that features edge-connected $M(2)O_6$ octahedra that form Kagome layers that are prone to magnetic frustration (Fig. 1). In spite of their structural and compositional similarities, members of the (Ba,Sr) $M_{2\pm x}Ru_{4\mp x}O_{11}$ subfamily of ruthenates exhibit a remarkable variety of electrical transport and magnetic properties that can be tuned by chemical substitution among 3d and 4d transition elements, or by simply varying the relative concentration of the 3d elements and 4d Ru within established homogeneity ranges [1,2].

Atomic disorder has profound effects on the behavior of RTF. On the one hand, the metallic compounds BaZnRu₅O₁₁ and BaNiRu₅O₁₁ form highly ordered Kagome planes of Ru moments that resist any transition to magnetic order at temperatures below 1 K [5–7]. On the other hand, Fe-bearing RTF exhibit atomically disordered Kagome planes and long-range, collinear ferrimagnetic order below remarkably high Curie temperatures (e.g., $T_C \sim 490$ K) [1,3,4].

It is indeed noteworthy that the room-temperature resistivities of the Ba- and Sr-based Fe RTF lie in the range of In contrast, the Mn- or Co-bearing Ru ferrites are bad metals with temperature- and field-dependent, noncollinear magnetic structures [1–4]. The AHE of these compounds is enhanced above the values expected for a conventional ferromagnet by virtue of a coupling between conduction electrons and a nontrivial spin texture on the Kagome sublattice. The spin chirality of noncollinear spin textures in the presence of geometrical frustration introduces a Berry phase in the itinerant electron states, which leads to an anomalous Hall effect of topological origin (THE) [3,11–13]. A THE controlled by spin chirality is of great current interest in condensed matter physics, not only for its fundamental scientific importance, but also because of its potential applications in semiconductor spintronics.

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typical narrow-gap semiconductors (0.001–100 Ω cm), and are accompanied by high carrier concentrations and practical carrier mobilities [1]. These characteristics make them promising candidates for spin-based, multifunctional materials, since they can optimize spin injection and detection efficiencies across a doped-semiconductor/ferromagnetic semiconductor interface. Moreover, the magnetic 3d and 4d ions of these compounds tend to populate distinct sublattices, which differs from dilute magnetic semiconductors such as (Ga,Mn)As and (Zn,Co)O, which suffer from electrical and magnetic inhomogeneities due to clustering of dilute 3d dopants among randomly occupied sites [9]. Further, a very large room-temperature anomalous Hall effect (AHE) with a transverse resistivity $\rho_{xy} = 77 \,\mu\Omega$ -cm has been observed for BaFe_{3.4}Ru_{2.6}O₁₁, which makes this material very attractive for Hall sensor applications [10].

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FIG. 1. Crystal structure of $SrSn_2Fe_4O_{11}$. The unit cell shown is extended by the oxide coordination of the metal atoms. Dark ellipsoids represent Sr. Small, dark ellipsoids represent mixed occupation by Fe/Sn in octahedral coordination, or Fe in tetrahedral coordination. Light spheres represent O. Atoms are depicted with displacement ellipsoids with 90% probability.

Atomic disorder can strongly influence the physical properties of magnetically frustrated lattices [5,14-16]. We have investigated the magnetic properties of $SrSn_2Fe_4O_{11}$ as an RTF with relatively strong magnetic interactions among atomically disordered sites, which results in a high ordering temperature. The influence of spin-orbit interactions is also not expected to be decisive in this *3d*-electron material, which should produce distinct differences from the complex behaviors observed for 4*d* (e.g., Ru) and 5*d* (e.g., Ir) oxides [17].

Although SrSn₂Fe₄O₁₁ was first synthesized by Cadee and Ijdo [18] in 1984, little is known about this material beyond Sn Mössbauer spectroscopy data that characterize local environments in polycrystalline samples [19]. As previously found for the Ba-isotypes [18], RTF generally crystallize in a hexagonal structure that is typically identified as the centrosymmetric $P6_3/mmc$ space group, which contains a Kagome substructure formed by edge-sharing $M(2)O_6$ octahedra located within the *ab*-plane (Fig. 1). These Kagome planes are connected along [001] by face-sharing $M(1)O_6$ octahedra and $M(3)O_5$ trigonal bipyramids. There is a mixing of magnetic 3d and 4d ions on the M(1) and M(2) crystallographic sites, while 3d elements exclusively occupy the trigonal-bipyramidalcoordinated M(3) positions (Fig. 2). Note that the Ru 4d ions have been completely replaced with nonmagnetic Sn or magnetic Fe ions in the isostructural SrSn₂Fe₄O₁₁ compound. Therefore, atomic disorder in SrSn₂Fe₄O₁₁ stems from the random distribution of magnetic Fe³⁺ and nonmagnetic Sn⁴⁺ within both the Kagome substructure, and inside the facesharing $M(1)O_6$ octahedra. This spatial distribution of strongly magnetic Fe³⁺ results in an inhomogeneous local environment for individual spins.

Our x-ray crystal structure refinements of $SrSn_2Fe_4O_{11}$ indicate the Fe³⁺ ions randomly occupy 84% of the M(2) sites within the Kagome planes, but occupy only 30% of the M(1)and M(1a) sites located in face-sharing octahedra connecting adjacent Kagome planes. Although the M(3) sites in the



FIG. 2. Section of the crystal structure of $SrSn_2Fe_4O_{11}$. Sr is coordinated by twelve oxygen atoms that define a nearly ideal anticuboctahedrom. Face-sharing octahedral sites have mixed occupation by Sn/Fe atoms with different ratios (M(1) by 86% Sn, M(1a) by 54% Sn). Face-sharing tetrahedra are occupied to a different extent: Fe(3) to 19%, Fe(3a) to 81%, which corresponds to a shift of the Fe(3a) atoms by about 0.2 Å off the ideal center position along [001] in the trigonal bipyramidal void. Atoms are depicted with displacement ellipsoids with 90% probability.

bipyramids are exclusively occupied by Fe³⁺, the higher degree of substitution of nonmagnetic Sn⁴⁺ for magnetic Fe³⁺ ions in M(1) sites located between the Kagome planes should weaken the interlayer coupling and reduce the effective dimensionality of the magnetic lattice, which could alter the cooperative behavior of the compound. Previously, it was shown that magnetic dilution, even at low level, has a significant impact on geometrically frustrated systems with antiferromagnetic nearest-neighbor interactions such as $SrGa_{12-x}Cr_xO_{19}$ (0 \leq x < 1), whose spin-glass transition temperature is strongly reduced with increasing Ga content [16]. On the other hand, a study of spin freezing in the diluted spin-ice compounds $Dy_{2-x}Y_{x}Ti_{2}O_{7}$ ($0 \le x \le 0.4$), where ferromagnetic interactions are frustrated on the pyrochlore lattice, suggests that their freezing temperature is essentially unchanged by dilution [14]. These results indicate different mechanisms of glassy behavior exist in frustrated, site-disordered magnets.

In this work we have investigated the magnetic properties of single crystals of the site-disordered Kagome compound $SrSn_2Fe_4O_{11}$ using dc and ac magnetization measurements. Our results contain evidence of a complex magnetic ground state in which long-range FM order (existing below $T_C =$ 630 K) coexists with a short-range, spin-glass state below 36 K. The short-range-ordered state exhibits anomalous behavior of the ac susceptibility and thermomagnetic relaxation data which differ from those of conventional spin glasses.

II. EXPERIMENTAL DETAILS

To realize single-crystal growth of $SrSn_2Fe_4O_{11}$, initial amounts of 2.9 mmol SnO_2 , 3.1 mmol Fe_2O_3 , and 3.2 mmol $SrCl_2$ were mixed and then pressed into a pellet that was heated to 1330 °C and kept at this temperature for several days; the furnace was then slowly cooled to room temperature. Black hexagonal platelets of maximum size 1.5 mm with thicknesses 0.07–0.08 mm were obtained. Small hexagonal platelets were selected for x-ray diffraction at ambient temperature using a four-circle diffractometer (NONIUS- κ -CCD, Bruker AXS GmbH) with monochromatic Mo K_{α} radiation. An absorption correction based on symmetry-equivalent reflections was applied (program X-SHAPE). The structure was solved using

TABLE I. Crystal structure data for SrSn₂Fe₄O₁₁.

Formula	SrSn _{1.89(5)} Fe _{4.11} O ₁₁
Crystal system	Hexagonal
Space group	$P6_3mc$
<i>a</i> , Å	5.9541(2)
<i>c</i> , Å	13.5761(5)
$V, \text{\AA}^3$	416.8
Ζ	2
$D_{ m calcd}, { m g} { m cm}^{-3}$	5.77
$\mu(\mathrm{Mo}K_{\alpha}),\mathrm{mm}^{-1}$	19.1
<i>F</i> (000), e	660
hkl range	$\pm 7, \pm 7, \pm 18$
$2\theta_{\rm max}$, deg	56.22
Refl. measured	6574
Refl. unique	428
R _{int}	0.077
Param. refined	41
$R(F)/wR(F^2)$ (all reflections)	0.034/0.070
$GoF(F^2)$	1.196
BASF ^{a)}	0.47(4)
$\Delta \rho_{\rm fin}$ (max/min), e Å ⁻³	0.76

^{a)}Inversion twinning of single crystals.

direct methods, and refined (program SHELXS-97-2, SHELXL-97-2 [20]), yielding a composition $SrSn_{1.89(5)}Fe_{4.11}O_{11}$. Oxygen atoms were restricted to isotropic displacement parameters in the refinements, due to a limited number of unique intensity data. Details of the data collection and results of the structural refinements are collected in Tables I and II; additional information regarding the crystal structure investigations may be obtained from [21].

Chemical microprobe analyses yielded very consistent compositions for all crystals investigated, with inferred atomic density ratios $n(Sr)/n(Sn)/n(Fe) = 0.9 \pm 0.2 : 2.0 \pm$

 $0.1: 4.0 \pm 0.1$ (the oxygen content could not be quantified with this technique), in excellent agreement with the composition inferred from x-ray diffraction data, and with no additional elements detected. The x-ray refinement and microprobe results indicate the crystals examined were single phase and of excellent quality.

The magnetization data for separate, oriented single crystals were acquired over a temperature range $1.8 \text{ K} \leq T \leq 300 \text{ K}$ in applied magnetic fields $0 \leq \mu_0 H \leq 5 \text{ T}$ using a Quantum Design MPMS7 SQUID Magnetometer. AC magnetic susceptibility data were taken using a 5.0 Oe RMS drive applied in the hexagonal basal plane.

Diffuse reflectance spectra were measured on a J&M TIDAS UV-vis-NIR Spectrophotometer equipped with a reflection measuring head. BaSO₄ was used as a white standard. The Kubelka-Munk function was applied to convert reflectance into absorbance and obtain electronic band gap information.

III. RESULTS AND DISCUSSION

A. Crystal structure and composition

There has been considerable work done on the structure of $BaSn_2Fe_4O_{11}$, which was originally described in the hexagonal space group $P6_3/mmc$ from powder neutron diffraction at ambient temperatures [18]. Shortly thereafter, Sn–Fe ordering within the Kagome net was proposed, resulting in orthorhombic symmetry with space group *Cmcm* (direct subgroup of $P6_3/mmc$), based on powder neutron diffraction data acquired at 10 and 240 K [22–24]. However, later studies carried out on single crystals grown from $BaCl_2/B_2O_3$ flux indicated a hexagonal symmetry was the correct choice [25]. Finally, diffraction experiments using synchrotron radiation performed on microcrystalline powder gave no indication for any deviation from hexagonal symmetry [26]. However, the single-crystal XRD results, together with Mössbauer spectroscopic

Atom	Site	x	у	Z	$U_{ m eq}/{ m \AA}^2$	
Sr	2 <i>b</i>	1/3	2/3	0.2487(5)	0.0163(7)	
$M(1)^{*}$	2a	0	0	0.14349(8)	0.009(1)	
$M(1a)^*$	2a	0	0	0.3575(1)	0.003(1)	
$M(2)^{*}$	6 <i>c</i>	0.5003(2)	0.0006(4)	0.0001(5)	0.0065(4)	
$\operatorname{Fe}(3)^*$	2b	2/3	1/3	0.222(3)	0.008(1)	
$Fe(3a)^*$	2b	2/3	1/3	0.2620(5)	$U_{eq}(Fe(3))$	
$O(1)^{+}$	6 <i>c</i>	0.172(1)	2x	0.0797(7)	0.009(1)	
$O(1a)^{+}$	6 <i>c</i>	0.179(1)	2 x	0.4157(7)	0.007(2)	
$O(2)^{+}$	6 <i>c</i>	0.301(1)	1/2 x	0.2472(9)	0.011(1)	
$O(3)^{+}$	2b	2/3	1/3	0.414(1)	0.008(3)	
O(3a) ⁺	2b	2/3	1/3	0.076(1)	0.011(4)	
Atom	U_{11}	U_{22}	U_{33}	U_{23}	U_{13}	U_{12}
Sr	0.0149(6)	U_{11}	0.019(1)	0	0	$1/2 U_{11}$
<i>M</i> (1)	0.008(2)	U_{11}	0.011(1)	0	0	$1/2 U_{11}$
<i>M</i> (1a)	0.001(2)	U_{11}	0.005(2)	0	0	$1/2 U_{11}$
M(2)	0.0059(4)	0.0045(5)	0.0086(5)	0.0005(4)	$1/2 U_{23}$	$1/2 U_{22}$
Fe(3)/Fe(3a)	0.006(1)	U_{11}	0.013(4)	0	0	$1/2 U_{11}$

TABLE II. Crystal structure parameters of SrSn₂Fe₄O₁₁.

⁺Refined with isotropic displacements parameters.

 $^{*}M(1) = 0.86(2)$ Sn, 0.14 Fe; M(1a) = 0.54(2) Sn, 0.46 Fe; M(2) = 0.161(6) Sn, 0.839 Fe; Fe(3) = 0.19(2) Fe; Fe(3a) = 0.81 Fe.

TABLE III. Selected distances (Å) for $SrSn_2Fe_4O_{11}$ with estimated standard deviations in parentheses.

Sr	-O(1a)	2.77(1)	3×
	-O(1)	2.83(1)	6×
	-O(2)	2.9817(4)	6×
<i>M</i> (1)	-M(1a)	2.905(1)	1×
	-O(1)	1.97(1)	3×
	-O(2)	2.096(9)	3×
<i>M</i> (1a)	-M(1)	2.905(1)	$1 \times$
	-O(1a)	2.01(1)	3×
	-O(2)	2.157(9)	3×
M(2)	-O(3a)	1.999(9)	1×
	-O(1)	2.010(9)	$2 \times$
	-O(1a)	2.013(8)	$2 \times$
	-O(3)	2.08(1)	1×
	-M(2)	2.971(3)	$2 \times$
	-M(2)	2.983(3)	1×
Fe(3)	-Fe(3a)	0.54(3)	1×
	-O(2)	1.914(9)	3×
	-O(3a)	1.99(4)	1×
Fe(3a)	-Fe(3)	0.54(3)	1×
	-O(2)	1.895(6)	3×
	-O(3)	2.07(2)	1×

studies, indicate the Fe/Sn occupation for both octahedrally coordinated metal sites has some dependence on thermal history (i.e., preparation conditions) [19]. Mössbauer spectroscopy also revealed a preference for Fe to be located in tetrahedral rather than trigonal bipyramidal coordination, with 50% probability for each of the two tetrahedral sites [18].

We have determined that SrSn₂Fe₄O₁₁ crystallizes in the hexagonal RTF structure consisting of layers of edge-sharing $M(2)O_6$ octahedra interconnected by face-sharing double octahedra $O_3 M(1)O_3 M(1a)O_3$ and trigonal bipyramids Fe(3)O₅. Our crystal structure refinement for SrSn₂Fe₄O₁₁ was first carried out in the centrosymmetric space group $P6_3/mmc$; however, a strong elongation for displacements of Sr in the [001] direction was obtained, proximate to the expected elongation of Fe located in trigonal bipyramidal coordination [Fe(3)]. This led us to consider a refinement in the noncentrosymmetric structure $P6_3mc$, which is known to be the correct space group assignment for the ambient temperature modifications of PbV₆O₁₁ and SrV₆O₁₁ [27,28], and BaV₆O₁₁ below 250 K [29]. The M(2) metal sites themselves lie on a nearly ideal Kagome net randomly occupied by 84% Fe and 16% Sn with only small distortions and interatomic metal-metal distances slightly below 3 Å. Selected interatomic distances are gathered in Table III. The centers of the double octahedra have mixed occupation by Sn and Fe with a slight excess of Sn [54(2)% Sn, 46% Fe], while the trigonal bipyramid is centered exclusively by Fe. The lack of centrosymmetry leads to slight displacements of most atoms along [001] and lifts the equivalency of the two metal sites in the face-sharing double octahedra-one being occupied to a larger extent by Sn [M(1), 86%] than the second [M(1a), 54%]. Additionally, the two face-sharing tetrahedra that form the trigonal-bipyramidal void are occupied to a different extent—the Fe(3) site to only 19%, whereas the Fe(3a) site to about 81%. The displacement of Fe(3a) corre-



FIG. 3. Temperature dependence of the FC dc magnetic susceptibility $\chi(T)$ of a SrSn₂Fe₄O₁₁ single crystal for $H \perp c$ and $H \parallel c$ in applied magnetic field $\mu_0 H = 0.1$ T. Arrows designate the hightemperature onset of long-range magnetic order, and the much lower onset temperature of spin-glass order at $T_f = 35.8$ K.

300

200

100

Ó

sponds to a shift of about 0.2 Å along the [001] direction with respect to the ideal center position in the trigonal bipyramidal void. The M(1) and M(1a) sites are significantly displaced from the ideal position at the octahedra centers towards the terminal faces of the edge-sharing $O_3M(1)O_3M(1a)O_3$ double octahedra, due to Coulomb repulsion between the positive metal ions.

The only crystal structure data for $SrSn_2Fe_4O_{11}$ in the current literature are (1) unit cell parameters obtained from powder samples [18], which are in good agreement with our values (a = 5.9558(9) Å, c = 13.5429(21) Å versus a = 5.9541(2) Å, c = 13.5761(5) Å); and (2) an analysis of Sn and Fe distribution over the three possible sites in $P6_3/mmc$ symmetry obtained from Mössbauer spectroscopy [19] on a sample quenched from 1423 K (no Sn in trigonal coordination, 28% Sn in face-sharing octahedra and 72% Sn in Kagome nets). This analysis of site occupancies in BaSn₂Fe₄O₁₁ differs from our structure refinements; however, it is important to note that the Mössbauer sample was annealed at 1423 K. In this regard, we note that the distributions of Ti and Fe over these two distinct octahedrally coordinated positions invert in BaTi₂Fe₄O₁₁ if it is annealed at 973 K [19].

B. Static magnetic properties

Figure 3 shows the temperature dependence of the fieldcooled (FC) magnetic susceptibility of a $SrSn_2Fe_4O_{11}$ single crystal measured in a 0.1 T magnetic field applied either parallel or perpendicular to the *c* axis. All investigated samples undergo a FM phase transition at $T_C = 630$ K to an ordered state with a finite spontaneous magnetization. The observed Curie temperature is significantly higher than that of other RTF (Ba,Sr) $M_{2\pm x}M'_{4\mp x}O_{11}$ (M = Mn, Fe, Co; M' = Ru, Ti) [1–6]. To our knowledge, $SrSn_2Fe_4O_{11}$ has the highest T_C reported among all known members of the RTF family. It should be noted that a much lower $T_C = 180$ K was reported

500

600

700

800

400

T (K)



FIG. 4. Coercive field $H_{C\perp}$ for dc field applied perpendicular to the *c*-axis, versus temperature *T* for a SrSn₂Fe₄O₁₁ single crystal. The dashed line is a fit to Eq. (1) (see text for details) using parameters $H_{CO} = 5.06$ Oe, $T_1 = 4.60$ K, $H_{C1} = 391$ Oe, $T_2 = 37.9$ K, and $H_{C2} = 58.1$ Oe. Inset: The low-temperature dependence of the ZFC and FC dc magnetic moment of a SrSn₂Fe₄O₁₁ single crystal for applied field *H* parallel and perpendicular to the *c*-axis. Arrow designates the spin-glass transition temperature $T_f = 35.8$ K.

[18] for isostructural $BaSn_2Fe_4O_{11}$, which may be related to differences in the ionic size between Ba^{2+} and Sr^{2+} and/or to a strong influence of the preparation procedure on the cation distribution in $BaSn_2Fe_4O_{11}$ [19,23–26].

Upon further cooling, the dc susceptibility exhibits an anomaly for applied field in both crystallographic directions at $T_f = 35.8 \text{ K}$ (inset in Fig. 4). There is a distinct irreversibility between the ZFC and FC magnetization below T_f , which is a typical signature of the metastable magnetic state commonly found in short-range-ordered materials such as spin glasses [15]. Note that our sample presents two essential microscopic ingredients of spin-glass freezing-that is, Fe³⁺/Sn⁴⁺ site disorder and a geometrically frustrated Kagome lattice. Structural disorder due to the random replacement of magnetic Fe^{3+} by nonmagnetic Sn^{4+} on the Kagome net of $SrSn_2Fe_4O_{11}$ may cause an additional "reentrant spin-glass" transition at temperatures below either a long-range ferromagnetic or antiferromagnetic transition [30–32]. The high-temperature, longrange-ordered state is frustrated due to the increasing strength of random ferromagnetic or antiferromagnetic interactions with decreasing temperature; consequently, a reentrant spinglass transition occurs with further cooling. However, the divergence between the ZFC and FC magnetizations cannot unambiguously prove the onset of a spin-glass state, since this behavior might also be attributed to irreversible domain wall dynamics within the ferromagnetic state, which are reflected in field-dependent, isothermal magnetization data.

Indeed, the dc magnetic hysteresis loops of $SrSn_2Fe_4O_{11}$ exhibit unusual behavior, as shown in Figs. 5 and 6 for T = 4.5 and 300 K, respectively, and two crystallographic orientations. At room temperature, m(*H*) exhibits weak anisotropy and varies almost linearly with magnetic field above 1.2 T. The low-temperature behavior of m(*H*) is similar for T = 4.5 K,



FIG. 5. Magnetic moment *m* vs. applied field $H \perp c$ for temperatures T = 300 K (solid line) and T = 4.5 K (dashed lines) for a SrSn₂Fe₄O₁₁ single crystal. Note the lack of saturation for T = 4.5 K, and the very small hysteresis for dc applied field swept back and forth between ± 5 T. Note also the very similar behavior of these data and those of Fig. 6 for $H \parallel c$.

except for its relatively large overall magnitude. The magnetic moment m as a function of $\mu_0 H$ at T = 4.5 K (50 K) yields coercive field values $\mu_0 H_{c\perp} = 200$ Oe (20 Oe) and $\mu_0 H_{c\parallel} =$ 270 Oe (25 Oe). Very small coercive fields $\mu_0 H_{c\perp} = 0.27$ Oe and $\mu_0 H_{c\parallel} = 1.5$ Oe are observed for T = 300 K, classifying this material as an extremely soft magnet. The value $\mu_0 H_{c\perp} =$ 0.27 Oe is, to our knowledge, the lowest value of coercive field ever reported for ferrites, and is smaller than the coercive fields of Ni_{0.8}Fe_{0.2} (permalloy) thin films, a material widely used in technological applications. Materials dominated by 3*d* magnetism tend to have low magnetic anisotropy and often exhibit soft magnetic behavior. However, the coincidence of such very



FIG. 6. Magnetic moment *m* vs. applied field $H \parallel c$ for temperatures T = 300 K (solid line) and T = 4.5 K (dashed lines) for a SrSn₂Fe₄O₁₁ single crystal. Note the lack of saturation for T = 4.5 K, and the very small hysteresis for dc applied field swept back and forth between ± 5 T. Note also the very similar behavior of these data and those of Fig. 5 for $H \perp c$.

small coercive fields with nonsaturating magnetization, which we observe for $T \ll T_C$, is unusual.

The temperature dependence of the coercive field of $SrSn_2Fe_4O_{11}$ is shown in Fig. 4. The coercivity of $SrSn_2Fe_4O_{11}$ appears to decrease exponentially with temperature, similar to that observed for the frustrated cluster glass Dy_5Pd_2 [33]. However, fits of $H_C(T)$ to a simple exponential behavior failed; nevertheless, an expression that includes two activation mechanisms (reflected in two characteristic temperature scales, T_1 and T_2), did provide a satisfactory fit (dashed line in Fig. 4):

$$H_C(T) = H_{C0} + H_{C1}\exp(-T/T_1) + H_{C2}\exp(-T/T_2).$$
 (1)

The best-fit parameters appropriate to Fig. 4 are $H_{CO} = 5.057$ Oe, $H_{C1} = 391.2$ Oe, $T_1 = 4.600$ K, $H_{C2} = 58.09$ Oe, and $T_2 = 37.86$ K.

Exponential dependences of $H_C(T)$ are not universal in spin glasses; for example, the following power law has also been predicted and observed for isotropic spin glasses [34]:

$$H_C(T) \propto (1 - T/T_f)^{1/2}$$
. (2)

A rapid increase of m(*H*) with increasing *H* at low fields, followed by a nearly linear variation of m(*H*) for $\mu_0 H >$ 1.1 T, and the failure of m(*H*) to saturate at high fields, are typical of either a canted antiferromagnetic or ferrimagnetic state [3,8,13,35]. Geometrical frustration within the Kagome plane can be accompanied by spin canting along (001) [3,13], induced by antisymmetric Dzyaloshinsky-Moriya (DM) interactions [36,37] appropriate for spins in the noncentrosymmetric structure of SrSn₂Fe₄O₁₁. Nonzero spin canting gives rise to finite scalar spin chirality and an anomalous Hall effect of topological origin, as observed in the related RTF, BaMn_{2,49}Ru_{3,51}O₁₁ [3]. Additional neutron diffraction studies of powders and/or larger single crystals are needed to determine the mechanism of the anomalous behavior of m(*H*).

Previous studies of the (Sr,Ba)(Fe,Ru)₆O₁₁ RTF systems indicate that the ratio of the number of 3*d* and 4*d* magnetic ions plays an important role in determining the magnetic anisotropy [1,2]: A higher Ru/Fe ratio correlates with higher anisotropy [1], which originates from spin-orbit interactions and an incompletely quenched orbital angular momentum of the relatively large 4*d* orbitals [17]. Moreover, the strong decrease in magnetic anisotropy observed for larger substitutions of 3*d* Fe for 4*d* Ru suggests that an increasing Fe/Ru ratio reduces the spin-orbit interaction responsible for the anisotropy [1]. Therefore, it is reasonable to associate the very soft magnetic behavior observed in SrSn₂Fe₄O₁₁ with a complete substitution of Ru³⁺/Ru⁵⁺ by Fe³⁺ and nonmagnetic Sn⁴⁺.

C. Dynamic magnetic properties

To obtain further evidence of a spin-glass state below 36 K, the dynamic properties of SrSn₂Fe₄O₁₁ were investigated by ac susceptibility measurements at low temperatures. Figure 7 shows the temperature dependence of the ac susceptibility taken in zero dc applied magnetic field. As temperature decreases, the real part of the ac susceptibility, $\chi'(T)$, exhibits a pronounced kink at $T = T_k = 35$ K, which is often used to define the freezing temperature T_f in spin glasses; and an observable frequency dependence of T_k usually signals a transition into a true spin-glass state [15]. On the other hand, the



FIG. 7. Temperature and frequency dependences of the (a) real, χ' , and (b) imaginary, χ'' , parts of the ac susceptibility of a SrSn₂Fe₄O₁₁ single crystal for applied ac magnetic field $h \perp c$, with RMS magnitude 5.0 Oe. The vertical dashed line in (a) indicates the frequency-independent temperature T_k of a kink in χ' , which corresponds well with the proposed freezing temperature, $T_f =$ 35.8 K (see Fig. 3).

magnitude of χ' decreases as frequency increases [Fig. 7(a)], and for temperatures above and well below T_k , the $\chi'(T)$ curves for different frequencies remain separated. Furthermore, the $\chi'(T)$ curves converge to a nonzero, frequency-independent value in the zero-temperature limit, which is a behavior often seen in spin-glass materials [38,39]. In contrast, the imaginary part of the ac susceptibility, $\chi''(T)$, exhibits a well-defined peak at $T = T_p$ for each frequency investigated [Fig. 7(b)]; this peak increases in magnitude, broadens and shifts upward by as much as 20 K on increasing the frequency from 0.1 to 1000 Hz, which is also typical of spin glasses [15,40–42].

A careful comparison of Figs. 7(a) and 7(b) reveals an inflection point in $\chi'(T)$ at $T = T_i$, which is well below the kink temperature T_k , but lies slightly below, and tracks the temperature of the peak in $\chi''(T)$ at T_p , as shown in Fig. 8. Therefore, we will use the more robust peak in $\chi''(T)$ to estimate the spin-glass freezing point T_f in the following discussion. The magnitude of the frequency dependence of $\chi''(T)$, quantified by $p \equiv \{\Delta T_f/T_f\}\Delta(\log f) \approx 0.12$, is much higher than that of canonical spin glasses (e.g., p = 0.01 [15]), but is an order of magnitude lower than that of superparamagnets (e.g., $p \approx 3$ [15]), and is comparable to values observed for dilute dipole glasses [42] and geometrically frustrated magnets (e.g., $p \approx 0.18$ [43]).



FIG. 8. Dependence of the anomaly temperatures T_k , T_p , and T_i on the ac measuring frequency f from the ac moment data of Fig. 7.

The onset of a broad temperature interval with strong frequency dependence distinctly below an initial peak in $\chi'(T)$, which has no frequency dependence, resembles the ac susceptibility data for the reentrant spin-glass Fe_{0.62}Mn_{0.38}TiO₃ [44]. On the other hand, $\chi'(T)$ for Fe_{0.62}Mn_{0.38}TiO₃ exhibits no frequency dependence near and well above the kink temperature, which differs from the $\chi'(T)$ data shown for SrSn₂Fe₄O₁₁ in Fig. 7(a). The overall behavior of the ac susceptibility, including a large frequency shift in the peak in $\chi''(T)$ resembles that of a spin-glass like state. In contrast, the absence of a frequency dependence of the kink in $\chi'(T)$, accompanied by a strong frequency-dependence across a wide temperature interval surrounding the kink, indicate that the frozen spin state in SrFe₂Sn₄O₁₁ differs from that of conventional spin-glass materials.

A change in the sign of χ'' from positive to negative with decreasing temperture $T \leq 8$ K is seen in Fig. 7(b) for frequency f = 1000 Hz, and can be extrapolated from the 700 Hz data. We mention his curious behavior because it violates simple linear response theory (where χ'' is a measure of energy dissipation in the sample); and a negative $\chi''(T)$ has also been observed in the Na_{0.85}CoO₂ cobaltate [45], and in the BiFeO₃ ferrite, where it was attributed to a modulated magnetic structure [38]. Such a sign change has not been reported previously for RTF materials; verification/clarification of this phenomenon will require more detailed magnetothermal measurements at variable frequency.

To clarify the low-temperature dynamics of the spin-glass state of SrFe₂Sn₄O₁₁, we first applied a simple Arrhenius law to describe the frequency dependence of $T_p \equiv T_f$, as has been done for conventional spin glasses composed of isolated clusters (superparamagnets), where

$$f = f_0 \exp(-E_a/k_B T_f).$$
(3)

Here, E_a and f_0 are the energy barrier and characteristic frequency of a superparamagnet, respectively. The temperatures of the peaks observed in $\chi''(T)$ appear to follow such an



FIG. 9. Logarithm (base-10) of the measuring frequency log f versus the inverse of the peak temperature in $\chi''(T)$, $1/T_p$ [see Fig. 7(b)], for a SrSn₂Fe₄O₁₁ single crystal. The solid line is a fit of the data to the Arrhenius law [Eq. (3)] with $E_a/k_B = 138$ K and log(f_0) = 6.7134, corresponding to $f_0 = 5.169 \times 10^6$ Hz. Note the appreciable deviations from the fit below 20 K.

Arrhenius law with parameters $E_a/k_B = 138$ K and $\log_{10}(f_0) = 6.7134$, corresponding to $f_0 = 5.169 \times 10^6$ Hz only for T > 20 K (see Fig. 9). Below 20 K, a clear deviation from the Arrhenius law is observed. Application of a Vogel-Fulcher law $f = f_0 \exp[E_a/k_B(T_f - T_0)]$, proposed for magnetically interacting clusters, does not significantly improve the fits.

We tentatively concluded that a nonthermal relaxation process is active in SrSn₂Fe₄O₁₁ below about 20 K, recalling the quantum spin relaxations observed in the dilute Ising spin system LiHo_{1-x}Y_xF₄ [40] and the geometrically frustrated spin-ice D₂Ti₂O₇ [46]. We therefore measured the frequency dependence of the ac susceptibility of SrSn₂Fe₄O₁₁ at various temperatures below $T_f \approx 36$ K, and found $\chi''(f)$ indeed exhibits a double-peak structure (see Fig. 10) that indicates the presence of multiple relaxation processes. A double-peak



FIG. 10. Frequency dependence of the imaginary part of the ac susceptibility, $\chi''(f)$, at different temperatures (see online for color key).

structure was previously found in the temperature dependence of χ'' of Fe_{0.62}Mn_{0.38}TiO₃ [44], where it was attributed to the competition between the weakening of long-range antiferromagnetic order and growth of a reentrant spin-glass phase with decreasing temperature. Double-peaks in the *frequency* dependence of χ'' are rarely reported or discussed in the literature, and could reflect the existence of two different types of dynamics driven by thermally activated, or quantum relaxation processes. The higher-frequency peaks clearly show a decrease in the peak frequency as temperature decreases from 31 to 25 K, as expected for thermally-induced spin relaxation. In contrast, additional lower-frequency peaks can be identified at approximately the same frequency ($\approx 10 \text{ Hz}$) in the temperature range, $T \ge 22$ K, as expected for quantum spin relaxation. When the temperature is decreased below 25 K, magnetic relaxation becomes very slow, and the position of the dominant peak shifts to lower frequencies. Apparently, the peak structure is gradually transformed as the temperature is lowered, and only a single broad peak is visible at 20 K.

Based on our preliminary analyses of the frequencydependent ac susceptibility, we conclude that the magnetic dynamics of $SrSn_2Fe_4O_{11}$ are not well described by either the exponential or power law behaviors that are typical for canonical spin-glass materials. The mechanism underlying two-peak behavior of $\chi''(f)$ is not clear at present, and detailed investigations of the magnetic structure and dynamics are required to clarify these issues.

A typical signature of complex spin dynamics in spin glasses is a time-dependent magnetization below T_f . We therefore measured the thermomagnetic relaxation of a SrSn₂Fe₄O₁₁ sample that was initially field-cooled to 25 K in an applied field $H_{FC} = 500$ Oe, which was then removed. The magnetization was then measured as a function of time after waiting a certain time t_w . The results for a waiting time $t_w = 1000$ s are presented in Fig. 11. Thermomagnetic



FIG. 11. Time dependence of the magnetic moment *m* of a SrSn₂Fe₄O₁₁ single crystal at T = 25 K (see text for experimental protocol). Dotted line corresponds to power law fit [Eq. (6)] with parameters: $M_0 = 6.8 \times 10^{-3}$ emu/mol, $\gamma = 0.18$. Dashed line corresponds to stretched exponential fit [Eq. (4)] with parameters: $M_0 = 2.6 \times 10^{-2}$ emu/mol, $\tau = 255$ s, n = 0.1. Solid line corresponds to Eq. (7) with parameters $M_0 = 6.8 \times 10^{-3}$ emu/mol, $\gamma = 0.18$, $M_1 = 2.6 \times 10^{-2}$ emu/mol, $\tau = 255$ s, and n = 0.1.

magnetization data are typically analyzed using a stretched exponential form based on a phenomenological description of relaxation in disordered systems [47]:

$$M(t) = M_0 \exp[-(t/\tau)^{1-n}].$$
 (4)

Here, $M_0 = M$ (t = 0) and τ is the relaxation time. However, fits to Eq. (4) yielded very poor results (see dashed line in Fig. 11). Alternatively, we attempted to fit the data to a logarithmic dependence used to describe relaxation processes in systems with long-range magnetic order [41]:

$$M(t) = M_0 - C\ln(t).$$
⁽⁵⁾

Here M_0 is the initial value of the remanent magnetization and *C* is a constant that depends on the field, temperature, and material. Fits using Eq. (5) were also unsuccessful.

A closer inspection of the data set revealed two regimes with different time responses: A rapid initial magnetization relaxation is followed by a slower relaxation for t > 1500 s. For times shorter than 1500 s, we find a power-law behavior predicted by Ulrich *et al.* [48] (see dotted line in Fig. 11):

$$M(t) = M_0 t^{-\gamma}.$$
 (6)

Here, M_0 is related to the intrinsic ferromagnetic component and γ depends on the strength of magnetic interactions. If the measurements are extended for longer times (t > 1500 s), a crossover from the power-law behavior to a stretched exponential decay, $M(t) = M_0 \exp[-(t/\tau)^n]$, is observed. Indeed, the solid line in Fig. 11 shows that the thermomagnetic relaxation data are well described by a supersposition of the power-law and stretched exponential forms:

$$M(t) = M_0 t^{-\gamma} + M_1 [\exp(-t/\tau)^{1-n}].$$
 (7)

The best-fit parameters are $M_0 = 6.8 \times 10^{-3}$ emu/mol, $\gamma = 0.18$, $M_1 = 2.6 \times 10^{-2}$ emu/mol, $\tau = 255$ s, and n = 0.1.

To summarize our analyses of magnetic dynamics, two processes with different characteristic relaxation times are present in $SrSn_2Fe_4O_{11}$, and they merge into a complex relaxation process below 35 K. Possible relaxation processes include the nonexponential relaxation of dynamically correlated ferromagnetic domains [48], while the stretched exponential form might reflect glassy dynamics of a disordered spin structure inside domains [47].

IV. OPTICAL MEASUREMENTS

Previous work [1,2] has shown that the long-range magnetic ordering temperatures of various RTF are strongly correlated with the size of the semiconducting gap in the case of nonmetallic materials, whereas the ordering temperatures are typically near or below 200 K for metallic examples. We therefore measured the diffuse reflectance spectra of $SrSn_2Fe_4O_{11}$ over the ultraviolet-to-visible frequency range to obtain estimates of the optical band gap. The diffuse reflectance was converted into absorption using the Kubelka-Munk approximation [49,50], which relates the absorption coefficient (α) to the diffusion coefficient (S) of the compound. Three steep absorption thresholds appear in the energy range 0.7–3 eV (1750–410 nm) (Fig. 12). The absorption edge energies (E_g), derived from the intersection point of the base line along the energy axis and



FIG. 12. Plot of the Kubelka-Munk function (α /S) against energy. The absorption edge energies are derived from the individual intersection point of the base lines drawn along the energy axis and the extrapolated lines of the linear parts of the threshold.

the extrapolated line of the linear part of the threshold, exhibit values of approximately 0.8 eV, 1.3 eV, and 1.9 eV. We assume that the absorption edge at 0.8 eV can be assigned to the overall optical band gap of the sample as a transition from the valence band to the conduction band, whereas the other two edges observed at 1.3 and 1.9 eV can be assigned to different types of transitions, such as charge transfer or d-d transitions [51–53]. Ligand-to-metal charge transfer (LMCT) from oxide anions towards Fe³⁺ cations can be generally presumed for such transition metal oxides; however, d-d interactions may occur due to crystal field splitting of the 3d orbitals in combination with noncentrosymmetric local environment of the Fe^{3+} ions. The optical thresholds clearly imply that SrSn₂Fe₄O₁₁ is a semiconductor and are consistent with a striking empirical correlation between the magnitudes of the semiconducting gaps and the magnetic ordering temperatures of nonmetallic, Fe/Ru-bearing RTF [1].

V. CONCLUSION

We have found that single crystals of the $SrSn_2Fe_4O_{11}$ RTF are semiconducting, and exhibit long-range FM order well above room temperature (i.e., $T_C = 630$ K), accompanied by very low coercive fields $\mu_0 H_{C\perp} = 0.27$ Oe and $\mu_0 H_{C\parallel} =$ 1.5 Oe at 300 K. Overall, our measurements of static magnetic properties show SrSn₂Fe₄O₁₁ exhibits features typical of longrange FM order, such as finite remanence, and coercivity that decreases exponentially with increasing temperature. These properties make this material attractive for microwave devices and recording media.

Our lower temperature data and analyses provide strong evidence that the magnetic ground state of SrSn₂Fe₄O₁₁ is heterogeneous, due to an apparent coexistence of long-range FM order and an unconventional spin-glass state. Low-temperature magnetic measurements on SrSn₂Fe₄O₁₁ single crystals reveal a distinct spin-glass anomaly at $T_f = 35.8 \text{ K}$, which is very far below the onset temperature of long-range magnetic order at $T_C = 630$ K. The spin-glass state in SrSn₂Fe₄O₁₁ exhibits two regimes of spin-glass freezing. One regime is analogous to the dynamic freezing associated with relaxation over a wide range of length and time scales, as in conventional disordered systems, while the second regime is predominantly associated with a single relaxation mode, as observed, for example, in geometrically frustrated systems. We relate the first mode to the large-scale Fe^{3+}/Sn^{4+} site disorder present in SrSn₂Fe₄O₁₁, while the second mode is a consequence of the geometrical frustration of the Kagome lattice. SrSn₂Fe₄O₁₁ may represent an interesting class of quantum dynamics in a ferromagnet; and further experiments are needed to clarify the nature of the low-temperature spin-glass state, especially the double-peak structure of $\chi''(f)$. The coexistence of long-range and unconventional short-range magnetic orders is unusual, and has been previously observed in only a limited number of materials, including geometrically frustrated magnets (see Ref. [54], and references therein). The appearance of such a complex ground state is consistent with a competition between the inherent topological frustration of the Kagome network and atomic disorder among the Fe^{3+}/Sn^{4+} sites of $SrSn_2Fe_4O_{11}$.

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