



Physics and Astronomy Faculty Publications

Physics and Astronomy

2-1-2009

Fluorescent Excitation of Balmer Lines in Gaseous Nebulae: Case D

V. Luridiana Instituto de Astrofísica de Andalucía, Spain

S. Simón-Díaz *Observatoire de Paris, France*

M. Cerviño Instituto de Astrofísica de Andalucía, Spain

R. M. González Delgado Instituto de Astrofísica de Andalucía, Spain

R. L. Porter University of Kentucky, rporter@pa.uky.edu

See next page for additional authors

Right click to open a feedback form in a new tab to let us know how this document benefits you.

Follow this and additional works at: https://uknowledge.uky.edu/physastron_facpub Part of the <u>Astrophysics and Astronomy Commons</u>, and the <u>Physics Commons</u>

Repository Citation

Luridiana, V.; Simón-Díaz, S.; Cerviño, M.; González Delgado, R. M.; Porter, R. L.; and Ferland, Gary J., "Fluorescent Excitation of Balmer Lines in Gaseous Nebulae: Case D" (2009). *Physics and Astronomy Faculty Publications*. 79. https://uknowledge.uky.edu/physastron_facpub/79

This Article is brought to you for free and open access by the Physics and Astronomy at UKnowledge. It has been accepted for inclusion in Physics and Astronomy Faculty Publications by an authorized administrator of UKnowledge. For more information, please contact UKnowledge@lsv.uky.edu.

Authors

V. Luridiana, S. Simón-Díaz, M. Cerviño, R. M. González Delgado, R. L. Porter, and Gary J. Ferland

Fluorescent Excitation of Balmer Lines in Gaseous Nebulae: Case D

Notes/Citation Information

Published in *The Astrophysical Journal*, v. 691, no. 2, p. 1712-1728.

© 2009. The American Astronomical Society. All rights reserved. Printed in the U.S.A.

The copyright holder has granted permission for posting the article here.

Digital Object Identifier (DOI)

http://dx.doi.org/10.1088/0004-637X/691/2/1712

FLUORESCENT EXCITATION OF BALMER LINES IN GASEOUS NEBULAE: CASE D

V. LURIDIANA¹, S. SIMÓN-DÍAZ², M. CERVIÑO³, R. M. GONZÁLEZ DELGADO³, R. L. PORTER⁴, AND G. J. FERLAND⁴ ¹Instituto de Astrofísica de Andalucía (CSIC), Camino bajo de Huétor 50, 18008 Granada, Spain; vale@iaa.es

² Observatoire de Genève and LUTH, Observatoire de Paris, Site de Meudon, Meudon, France; sergio.simon-diaz@obs.unige.ch

Instituto de Astrofísica de Andalucía (CSIC), Camino bajo de Huétor 50, 18008 Granada, Spain; mcs@iaa.es, rosa@iaa.es

⁴ Department of Physics, University of Kentucky, Lexington, KY 40506, USA

Received 2008 August 20; accepted 2008 October 6; published 2009 February 9

ABSTRACT

Nonionizing stellar continua are a potential source of photons for continuum pumping in the hydrogen Lyman transitions. In the environments where these transitions are optically thick, de-excitation occurs through higher series lines. As a result, the emitted flux in the affected lines has a fluorescent contribution in addition to the usual recombination one; in particular, Balmer emissivities are systematically enhanced above case B predictions. The effectiveness of such a mechanism in H II regions and the adequacy of photoionization models as a tool to study it are the two main focuses of this work. We find that photoionization models of H II regions illuminated by low-resolution ($\lambda/\delta\lambda \lesssim 1000$) population synthesis models significantly overpredict the fluorescent contribution to the Balmer lines; the bias has typical values of the order of a few hundredths of a dex, with the exact figure depending on the parameters of the specific model and the simulated aperture. Conversely, photoionization models in which the nonionizing part of the continuum is omitted or is not transferred significantly underpredict the fluorescent contribution to the Balmer lines, producing a bias of similar amplitude in the opposite direction. Realistic estimations of the actual fluorescent fraction of the Balmer intensity require photoionization models in which the relevant portion of the stellar continuum is adequately represented, that is, its resolution is high in the region of the Lyman lines. In this paper, we carry out such an estimation and discuss the variations to be expected as the simulated observational setup and the stellar population's parameters are varied. In all the cases explored, we find that fluorescent excitation provides a significant contribution to the total Balmer emissivity. We also show that differential fluorescent enhancement may produce line-of-sight differences in the Balmer decrement, mimicking interstellar extinction. Fluorescent excitation emerges from our study as a small but important mechanism for the enhancement of Balmer lines. As such, we recommend to take it into account in the abundance analysis of photoionized regions, particularly in the case of high-precision applications such as the determination of primordial helium.

Key words: atomic processes – H II regions – ISM: abundances – line: formation – stars: atmospheres

Online-only material: color figures

1. INTRODUCTION

The systematic study of gaseous nebulae started in the decade of 1930s with a long series of papers by Menzel and collaborators (e.g., Menzel 1937; Menzel & Baker 1937; Baker & Menzel 1938, among others). In these papers, the basis was laid for the quantitative analysis of the hydrogen spectrum and the determination of physical conditions in gaseous nebulae. The hydrogen spectrum was recognized to form in the radiative cascade following recombination of H⁺ atoms, and quantitative predictions for the line intensities based on this scenario were made. Two limiting cases were considered, which depend on the optical thickness of the nebula in the Lyman lines. In case A, the nebula is assumed optically thin in all recombination lines, including those of the Lyman series; in case B, the nebula is assumed thick to Lyman radiation, which is consequently scattered until conversion into higher-series photons plus $Ly\alpha$ or $2-\gamma$ continuum emission takes place. Case B was soon shown to be the most appropriate description for most nebulae, both on observational and on theoretical grounds (e.g., Baker & Menzel 1938; Pottasch 1960).

A third scenario, named case C, was also initially introduced to represent the case of optically thin nebulae with stellar continuum pumping as an additional mechanism for the excitation of Ly α . In contrast to cases A and B, however, case C barely had any follow-up in the literature, with very sporadic exceptions (e.g., Chamberlain 1953; Ferland 1999). As pointed out by

Ferland (1999), a reason for this scarce popularity is the a priori assumption of the relative lack of photons at the relevant frequencies due to the absorption features of stellar atmospheres, which would make the mechanism inefficient and imply that case C might be a merely academical scenario with no actual physical applications. (The initial calculation by Baker & Menzel 1938 did not suffer from such limitation, since the stellar source was approximated by a blackbody.)

A further reason for the oblivion of case C is that the scenario it modifies (case A) is inadequate to represent most detectable objects. In other words, the lack of interest toward case C might not have to do with the correction it applies to case A, but rather with case A itself; after all, the fact that nebulae are irradiated by stellar light is beyond doubt. If this is the case, one might wonder why we do not consider the effect of stellar irradiation as a correction to case B, rather than case A. Since case C is the irradiated counterpart to case A, it seems natural to christen the irradiated counterpart to case B as "case D" (Table 1). Note that cases A and B solely depend on the physical conditions in the gas, while cases C and D depend on the illuminating source, so they are not cases in the same "local" sense of cases A and B.

Case D has never been taken, to the best of our knowledge, into consideration. Although this might seem somewhat surprising at first glance, we believe that there are reasons behind it; the arguments developed in this paper will help to understand why, so we defer a discussion of this point to Section 7.2.

 Table 1

 Nomenclature for Different Asymptotic Behaviors ("Cases") of the Hydrogen Spectrum in Gaseous Nebulae

	Thin	Thick
Nonirradiated	А	В
Irradiated	С	D

Note. Column describers specify the optical depth in the Lyman lines and row describers specify whether irradiation by stellar continuum is included or not.

In Section 2, we will argue that case D is a better representation of real nebulae than case B, the difference between the two scenarios being mostly small but substantial by modern standards of accuracy. Curiously enough, case D is implicitly assumed in many (but not all) photoionization models, although in a biased way; the bias can only be eliminated by feeding high-resolution near-UV (NUV) spectra into the models (Section 3). We will also show that the differential fluorescent contribution to the various Balmer lines can also affect the intrinsic Balmer decrement, pushing it toward either the blue or the red (Section 4). The resulting spatial distribution of the Balmer decrement depends on the spatial distribution of stars and the gas around them. A brief discussion of the dependence of fluorescence enhancement on the nebular and the stellar population's parameters and on details of the assumed stellar atmospheres is given in Sections 5 and 6, respectively. The main focus of Section 7 is the comparison of fluorescence enhancement with the other major deviation to case B, namely collisional excitation of H⁰. Finally, a short summary of the paper is given in Section 8.

2. THE MECHANISM

The abundance analysis of gaseous nebulae is based on a very simple principle. The intensity of a line with respect to, for example, $H\beta$ is given by the abundance of the emitting ion relative to H⁺ times a mathematical expression describing the physical mechanisms of line formation involved. If such mechanisms are known and all the parameters they depend on (such as the electronic temperature T_e) can be determined, then the observed value of a line ratio can be used to measure the ionic abundance relative to hydrogen.

The specific mechanisms involved depend on the ion and the regime considered. To mention but a few examples, it is known that He I lines in H II regions mainly form in the recombination cascade of He⁺, plus a density-dependent contribution by collisional excitation from the metastable level 2^{3} S, which mainly affects the triplet lines (Osterbrock & Ferland 2006). He II lines form in the recombination cascade of He⁺⁺. Heavy element lines mainly form through collisional excitation from the ground state of abundant ionic stages. Finally, H I lines—a standard reference for the intensity of the other lines in the optical range—mostly form in the radiative cascade following recombination of H⁺ under case B conditions.

It is also known that case B is only a limiting case and not the exact description of conditions in H II regions; strictly speaking, it is not even self-consistent, as it provides no mechanism to depopulate the 2p level (see, e.g., Burgess 1958). However, the predictions made by assuming case B have generally proved to be accurate, and only in recent times, it has become possible (and relevant) to point out exceptions to it. One such exception is the occurrence of collisional excitation from the ground state,

which has recently been rediscovered and closely studied as a consequence of the increasing need for accuracy in abundance determinations (V. Luridiana 2009, in preparation; Stasińska & Izotov 2001; Luridiana et al. 2003; Peimbert et al. 2007). A further way in which hydrogen may deviate from case B behavior, which is the subject of this paper, is continuum pumping in the Lyman lines and the related Balmer fluorescent enhancement.

Continuum pumping is the excitation of a transition by means of the absorption of a stellar continuum photon of the appropriate wavelength. Such excitation is followed by a radiative cascade which, in optically thick environments such as those of H II regions, ends up producing a Balmer series photon plus either Ly α or 2- γ continuum. In such a way, a Ly β absorption at 1026 Å can lead to the emission of an H α photon, a Ly γ absorption at 973 Å can lead to the emission of either H β or Pa α plus H α , and so on. These Balmer photons appear independent of, and in addition to, Balmer photons formed in the recombination cascade of H⁺, so these two contributions add up in the total spectrum. As for Ly α photons, they are scattered and gradually shifted in frequency until they escape the nebula, or are absorbed by dust; in dustless nebulae, a significant fraction of Ly α photons is converted into 2- γ continuum. Dust can also destroy higher Lyman photons, thus inhibiting pumping; this possibility will be briefly discussed in Section 7.

It must be stressed that this Balmer enhancement mechanism is triggered by pumping at the Lyman-line wavelengths, that is, it depends on the shape of the nonionizing stellar field. This runs counter to the common wisdom that, in a photoionized object, only the ionizing part of the stellar field matters; after all, the ionization structure is governed by the ionizing radiation, and the temperature structure is determined by the balance between heating due to photoionization and cooling due to collisional excitation of abundant metals and, in less metal-rich environments, Ly α emission. As a consequence, in photoionization modeling, the effect of nonionizing stellar radiation on the nebula is generally neglected. Yet, the emission spectrum of an H II region can be altered by continuum pumping even if this mechanism has no other effect on the structure of the nebula. In the next section, we will justify this statement by discussing the role of stellar continuum pumping in case C nebulae, referring in particular to Ferland's (1999) results. The following sections will be dedicated to the role of stellar pumping in the optically thick case, which we have labeled above "case D." In particular, we will estimate the contribution of stellar pumping⁵ on Balmer intensities and show that it cannot be neglected.

2.1. Case C

A good starting point to case D is case C, which applies to nebulae optically thin in the Lyman lines irradiated by a stellar continuum. In an optically thin environment, stellar continuum pumping results in a significant enhancement of Ly α emission, sufficient to bring the Ly α /H β ratio well above the case B value, rather than below it as predicted for case A. Ferland (1999) explained this by showing that, in the vicinity of the star (i.e., before stellar Lyman-line photons have been substantially absorbed), continuum pumping provides a source of Balmer

 $[\]frac{1}{5}$ A note on nomenclature: although continuum pumping and fluorescent excitation are different processes (the former referring to level excitation, the latter to line emission), they are linked together, so we will use the two terms interchangeably whenever appropriate.

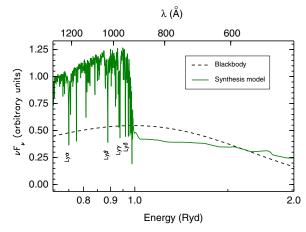


Figure 1. Comparison between the SEDs of a population synthesis model and a blackbody at $T_{\text{eff}} = 40$ k K, normalized to the same number of ionizing photons. The position of the first four Lyman lines is also shown.

photons comparable with recombination. If the gas slab is optically thin, recombination and fluorescence act concurrently in the whole volume, so the total emissivity in Ly α is largely enhanced by the latter mechanism.

This argument anticipates one reason why case D has never been taken into consideration: if the gas thickness is large (i.e., the optical depth is large in the Lyman continuum), Lymanline photons are used up much earlier than Lyman-continuum photons, so that the relative effect of continuum pumping on the total emitted spectrum is diluted; the larger the optical depth, the more diluted the effect, until it possibly becomes negligible altogether. If this were always the case, case D would not have any actual applications. There are, however, three possible exceptions to this conclusion: (a) a high accuracy in abundance analysis is required; (b) the nebular region affected by fluorescence has an unusually large weight in the observation, due to aperture effects; and (c) the balance between the Lymanline photons and the Lyman-continuum photons is more in favor of the former than in the case considered by Ferland (1999).

The first circumstance is certainly met in primordial helium abundance determinations, a goal that requires knowing the line-formation mechanism of H and He lines with an accuracy better than 1%. The second circumstance is met in spatiallyresolved observations sampling small regions in the vicinity of the ionizing cluster; observations of this kind are more and more common as technology improves. The third circumstance does not seem at first glance very probable when considering that the input spectrum of Ferland (1999) is a blackbody; one may be tempted to conclude that these results overestimate rather than underestimate the amount of continuum pumping, since a blackbody has no absorption features. Although this is true, it must be considered that a blackbody has no Lyman jump either, so the Lyman line-to-continuum flux of Ferland (1999) might actually be an underestimate. To demonstrate this point, in Figure 1, we compare the $T_{\rm eff} = 40,000$ K blackbody of that paper with the synthetic spectrum of a t = 3 Myr population emitting the same rate of ionizing photons (i.e., with the same potential to produce H α photons by recombination; more details on this spectrum will be given in Section 2.2). The figure shows that the blackbody does not lie above the synthesis spectrum; rather, it crosses the near-bottom of the relevant absorption lines, thus underestimating the number of photons capable of continuum pumping.

 Table 2

 Elementary Chemical Abundances in the Reference Model, Given as

 $12 + \log(X/H)$

Element	Abundance
He	10.89
С	7.62
N	6.38
0	7.87
Ne	7.15
S	6.47
Cl	4.48
Ar	5.50
Fe	5.81

Note. Remaining elements have not been included in the calculation since they are quite unimportant.

Concluding, we see that there is no a priori reason to discard the relevance of case D. In the following section, we will quantify in a specific case the correction represented by case D with respect to case B, and discuss how this result is expected to depend on the relevant H II region's parameters.

2.2. Case D

The upper panel of Figure 2 shows the physical conditions in a model giant H II region, named M1, computed with Cloudy (version C08.00; Ferland et al. 1998; R. L. Porter et al. 2009, in preparation). This version of the code includes a full model of the hydrogen atom with strong radiation field physics (R. L. Porter et al. 2009, in preparation; Ferland & Rees 1988; Ferguson & Ferland 1997; and Appendix A of this paper). For the sake of simplicity, we assumed a dustless nebula with a simple spherical geometry, with starting radius $R_{in} = 1$ pc, hydrogen number density $N_{\rm H} = 100 \text{ cm}^{-3}$, and filling factor $\epsilon = 0.01$. Although a blister model would be more appropriate to represent many, if not most, H II regions, we prefer to stick to the simplest possible case. The volume-integrated predictions presented in this paper do not depend on the assumed geometry, while the spatially resolved predictions do; it is, therefore, impossible to give figures suitable for any geometry and any line of sight (LOS), so the reader is warned that our spatially resolved predictions are given more as a rough indication of the magnitude of the effect than as a definitive estimate. The model's total metallicity is $Z_{gas} = 0.001$, and the detailed elementary abundances are given in Table 2; dust is not important at such low metallicities. Thermal line widths are assumed; the influence of a nonthermal contribution is discussed in Section 5.4. The ionizing source is the spectral energy distribution (SED) of a t = 3 Myr stellar population, emitting ionizing photons at a rate $\log Q(\mathrm{H}^0) =$ 52.09 s^{-1} . The SED has been computed with Sed@ (Cerviño & Luridiana 2006, and references therein), and does not include stellar winds. The effect of stellar winds on the predictions is discussed in Section 6.

Assuming that the model's emission is described by case B, a fairly constant H α emissivity profile is expected, given the shallow temperature gradient. This, however, is not the case: two exceptions to case B behavior can be seen in the H α profile (Figure 2, bottom panel).

In the external part ($r \gtrsim 70$ pc), there is a small bump in the emissivity profile: this bump is caused by collisional excitation of neutral hydrogen, a mechanism ignored in case B and which only becomes effective in the outer part, thanks to the drop in the hydrogen ionization fraction. A very low metallicity gas, which

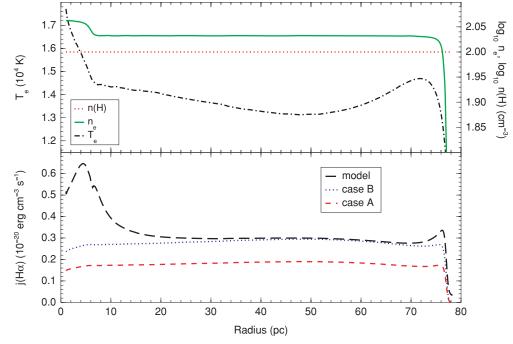


Figure 2. Upper panel: physical conditions in a model low-metallicity giant H II region ionized by a 3 Myr stellar population (see Section 2 for details). Lower panel: normalized H α emissivity profile of the model, compared with case A and B predictions. (A color version of this figure is available in the online journal.)

we consider here, will have a high kinetic temperature, so these collisional processes are especially important; more details on this can be found in V. Luridiana (2009, in preparation).

In the inner part, there is a much larger bump, extending through a substantial fraction of the total radius and whose maximum value more than doubles the expected case B value, which is shown as a dotted line. When the upper and lower panels of Figure 2 are simultaneously considered, it becomes clear that density and temperature cannot be responsible for the excess emissivity, as one can find pairs of points with the same $T_{\rm e}$ and $n_{\rm e}$ values but very different emissivities. In other words, the cause of this behavior cannot be sought in the gas: this leaves the radiation field as the only alternative. Indeed, the excess emissivity is caused by fluorescent excitement of H α by continuum pumping of Lyman photons (mainly $Ly\beta$). This is consistent with the position of the bump, close to the ionizing source (note that this bump has nothing to do with the breaks in the $n_{\rm e}$ and $T_{\rm eff}$ gradients seen at 6 pc, which are caused by the recombination of He^{++} and O^{3+}).

In the following sections, we will discuss whether the behavior of this model is representative of real nebulae and what its consequences are for the analysis of H II regions, considering several specific issues. We will start by considering a simple model of a spherical H II region, ionized by a population synthesis model (Section 3), and show the effect of continuum pumping on the Balmer intensities and ratios. In the following sections, we will complicate this basic scenario by discussing the effect of dust, turbulence, geometry, or a different metallicity (Section 5). Since the amount of continuum pumping depends on the detailed shape of the spectrum, we will also discuss the effect of assuming stellar atmospheres with shocked stellar winds. Since no high-resolution synthesis models are available with shocked winds, we will consider the case of a model H II region ionized by individual stars (Section 6). Sections 7 and 8 will be devoted to the discussion and conclusions, respectively.

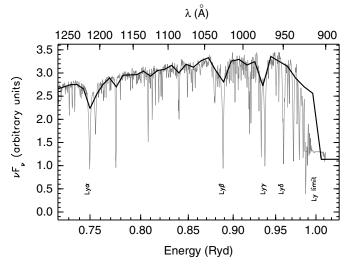


Figure 3. UV SED of a 3 Myr, Z = 0.001 stellar population, in low resolution (thick black line, spectral sampling = 10 Å) and high resolution (thin gray line, spectral sampling = 0.3 Å). Also shown are the first four Lyman lines, from Ly α at $\lambda = 1215$ Å (which does not produce any Balmer photon) through Ly δ at 950 Å.

3. HYDROGEN FLUORESCENT EXCITATION PREDICTED WITH POPULATION SYNTHESIS MODELS

The black thick curve in Figure 3 shows the NUV portion of the SED fed into the model described in Section 2.2; we again stress that this SED, as all the synthesis models used in this work, has been computed with stellar spectra with no emission lines. In this wavelength range, the spectral sampling of this SED is $\Delta \lambda = 10$ Å; this value is determined by the grid of stellar libraries used, that is, it does not depend on the way in which population synthesis is carried out; any synthesis model using the same stellar library would have the same resolution (this is the case, e.g., of Starburst99 models; Leitherer et al. 1999). At such resolution, stellar absorption lines are smoothed out, so that the number of Lyman photons in the spectrum is overestimated. Since the mechanism studied in this work directly depends on the number of Lyman-line photons emitted, it is important to establish whether fluorescent enhancement of H α can actually occur in H II regions or it is just an artifact of low-resolution synthesis models. The only way to answer this question is by feeding a high-resolution SED into the photoionization code.

3.1. Photoionization Models with High-Resolution SEDs

To address the issue mentioned in the previous section, we computed a new photoionization model, labeled M2, identical to M1 in all respects except for the stellar source, which has been replaced with a high-resolution SED in the 900–2000 Å range. This SED represents a population of the same stellar parameters (age and metallicity) as those of the original SED, but has a much better spectral sampling $\Delta \lambda = 0.3$ Å in the NUV range; a portion of this spectrum is shown in Figure 3 (thin gray curve). The SED is taken from a library of highresolution synthesis models computed with the code Sed@ (Cerviño & Luridiana 2006) to carry out this work. The library has been computed with the nonrotating tracks of the Geneva group (Schaller et al. 1992; Schaerer et al. 1993a, 1993b; Charbonnel et al. 1993), including standard mass-loss rates computed at five metallicities: Z = 0.040, 0.020, 0.008, 0.004,and 0.001, respectively. The isochrones are calculated by means of a parabolic interpolation between the tracks (log M, log t_k) in the Hertzsprung-Russell (H-R) diagram on a variable mass grid as prescribed in Cerviño et al. (2001). The isochrones were generated at specific ages with a time step of $\Delta t = 1$ Myr for 1-10 Myr. We have assumed a power-law initial mass function (IMF), with slope $\alpha = -2.35$ (Salpeter 1955) and low- and highmass cutoffs $M_{\rm low} = 0.1 M_{\odot}$ and $M_{\rm up} = 120 M_{\odot}$, respectively.

To model the SED, we have combined two different sets of atmosphere models, with low and high resolutions, respectively. Low-resolution atmosphere models are standard Kurucz local thermodynamic equilibrium (LTE) atmospheres. Highresolution atmosphere models cover the wavelength range from 900 to 2000 Å, and have been computed using the same atmospheres as those described in Martins et al. (2005) and González Delgado et al. (2005), but in the UV domain. Hot stars (27, 500 $\leq T_{\text{eff}} \leq 55,000$ K) are modeled as lineblanketed, non-LTE, plane-parallel, hydrostatic atmospheres (Lanz & Hubeny 2003), and stars with $8000 \leq T_{\text{eff}} \leq 27,000$ K are modeled with Kurucz LTE atmospheres (Kurucz 1993). We have assumed no contribution in the UV from stars with lower temperatures. The high-resolution synthetic spectra were obtained with the program SYNTHE by Hubeny et al. (1995).

The portions of the SED shortward of 900 Å and longward of 2000 Å are equal in the low- and high-resolution models, respectively. The main features of these models are given in Table 3, together with those of the models presented in the remainder of the paper.

A summary of the difference between M1 and M2 from the point of view of the fluorescent contribution to H α is given in Table 4. The three rows in the table correspond to different ways of integrating the emissivity along the shell structure of the model: in the one-dimensional (1D) integration, the emissivity of each shell is weighted by the thickness of the shell dr; in the two-dimensional (2D) integration, it is weighted by the ring surface $2\pi r dr$; and in the three-dimensional (3D) integration, it is weighted by the shell volume $4\pi r^2 dr$. Observationally,

 Table 3

 Main Features of the Photoionization Models Used in this Work

Model	Wav	Wavelength Range (Å)		Nebular Boundary		citat chan	
	> 2000	2000-900	< 900		F	R	CE
M1	LR	LR	LR	Radiation bounded	+	=	=
M2	LR	HR ^b	LR	Radiation bounded	=	=	=
M3	LR	Suppressed ^c	LR	Radiation bounded	=	=	=
M4	LR	HR ^b	LR	Density bounded	=	=	-
M5	LR	Suppressed ^c	LR	Density bounded	-	=	-

Notes.

^a F=fluorescence; R=recombination; CE=collisional excitation; the symbols "+", "=," and "-" denote that the mechanism is overestimated, properly included, and underestimated, respectively.

^b Sampled to $\Delta\lambda/\lambda = 0.0005$ (see Section 3.1).

^c In the 910–1030 Å range.

	Т	able	4		
	_			 	

Bias in the Total Hα Intensity Predicted with a Low-Resolution Stellar Continuum

Integration	$\frac{I(\mathrm{H}\alpha)_{\mathrm{M1}}}{I(\mathrm{H}\alpha)_{\mathrm{M2}}} - 1$
1D	0.09
2D	0.03
3D	0.02

Note. The meaning of labels 1D, 2D, and 3D is explained in Section 3.1.

the three cases correspond to a beam-like aperture, a narrow slit, and an aperture including the whole object, respectively. Since fluorescent excitation takes place in the inner part of the nebula, we expect that the effect on integrated luminosities of differences in the local emissivity is amplified in 1D integrations with respect to 3D integrations. As expected, Table 4 shows that H α is spuriously enhanced in M1 with respect to M2 as a consequence of the poor resolution of its input spectrum, which partially suppresses stellar absorption lines. The bias amounts to as much as 0.04 dex (9%) in the case of a beamlike simulated aperture, relative to the total H α intensity.

Since predicting Balmer line intensities is not a common application of photoionization models, which is the reason for pointing out this bias? The main reason to do it is estimating the amount of fluorescent excitation in real objects so that it can be taken into account when chemical abundances are determined. The exercise realized in this section provides a necessary piece of information in order to know whether such estimation can be carried out with low-resolution models, or high-resolution models are instead needed. The above results indicate that the bias in H α introduced by low-resolution models is substantial if compared with our best possible guess of the total emitted H α intensity, which is given by M2. Therefore, the results of Table 4 indicate that low-resolution synthesis spectra are not suitable to study the effect of fluorescence and that highresolution spectra are instead needed; they also indicate that the predicted spatially resolved line ratios relative to H β predicted are grossly overestimated in the direction of the center. This must be taken into account when photoionization models are used to fit spatially resolved spectroscopic data, as done, for example, in Luridiana & Peimbert (2001).

Note that Cloudy automatically rebins any input spectrum, so that in order to take advantage of the larger spectral resolution, it is necessary to increase Cloudy's default continuum mesh, as explained in the code's documentation (Hazy, part 3,

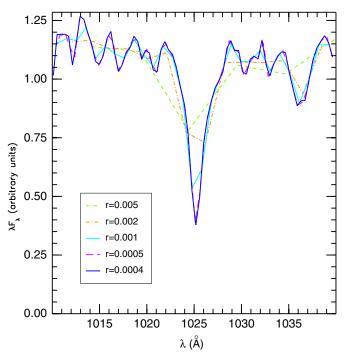


Figure 4. HR synthesis model rebinned by Cloudy to different values of the spectral resolution $r = \Delta \lambda / \lambda$.

p. 410: http://www.nublado.org). We carried out several different experiments in this direction exploring the resolution range $0.005 \le \Delta \lambda/\lambda \le 0.0004$, corresponding to spectral samplings $5 \text{ Å} \ge \Delta \lambda \ge 0.4 \text{ Å}$ at $\lambda = 1000 \text{ Å}$. Some of the spectra used internally by Cloudy after such rebinning are shown in Figure 4 in the Ly β wavelength region. We found no significant differences in the emission-line spectrum below $\Delta \lambda/\lambda \lesssim 0.0005$.

As a final comment, we note that, since real massive stars may develop P-Cygni line profiles due to the presence of strong stellar winds, at very high spectral resolution, one would also need to consider both the detailed line profile and the relative velocities of the star and the nebula, which determine the part of the spectrum that falls at relevant wavelengths.

3.2. Net Contribution of Fluorescent Excitation to Balmer Lines

Having established that low-resolution spectra are unsuitable to compute the fluorescent contribution to Balmer lines, we go on to address this problem by means of high-resolution spectra, considering the specific case of model M2. The fluorescent intensities in M2 can be estimated by computing a new model M3, identical to M2 in all respects except for fluorescent excitation, which is suppressed by setting the relevant portion of the continuum to zero (but it can also be switched off by the Cloudy command "no induced processes"). The fluorescent enhancement of M2 is computed as the difference between the Balmer line intensities of M2 and M3 (Table 5). For reasons explained in Section 3.1, the enhancement is particularly large in the beamlike integration: specifically, in our models, as much as 10% of the total intensity in H α and 14% in H β seen in the direction of the nebular center is caused by fluorescence rather than recombination. For completeness, we have also computed the fluorescent enhancement of Balmer lines of model M1, to quantify the fraction of emissivity that would-erroneously-be

 Table 5

 Fraction of Total Intensity Contributed by Fluorescent Excitation in Models M2 and M1

Integration	$1 - \frac{I(\lambda)_{M3}}{I(\lambda)_{M2}}^{a}$		$1 - \frac{I(\lambda)_{M3}}{I(\lambda)_{M1}}^{b}$			
	Ηα	$H\beta$	$H\gamma$	Ηα	$H\beta$	Hγ
1D	0.10	0.14	0.14	0.17	0.21	0.26
2D	0.03	0.04	0.05	0.06	0.06	0.09
3D	0.02	0.02	0.02	0.04	0.03	0.04

Notes. Total intensities include fluorescence, recombination, and collisional excitation.

^a True fluorescent enhancement.

^b Biased fluorescent enhancement.

attributed to fluorescence enhancement, had we used model M1 to this aim; in that case, the estimated fluorescent enhancement is almost twice as large as in the unbiased case (Table 5). As anticipated in Section 3.1, this demonstrates that inputting low-resolution spectra to photoionization models grossly biases the estimated fluorescence contribution.

Thus, the first general result is that fluorescence does indeed has a sizeable influence on the emitted Balmer spectrum. In the remainder of this section, we will discuss the implications of such influence. In the following sections, we will briefly discuss how our results depend on the model's parameters, such as the geometrical assumptions on the nebular distribution and the parameters that define the stellar populations.

3.2.1. Effect of Fluorescent Enhancement on Abundance Determinations

The results listed in Table 5 have important implications for abundance determinations. When a beam aperture is applied to the center of model M3, at least 10% of the total Balmer intensity comes from fluorescent excitation. If model M3 were a real object analyzed under the assumption of case B emissivity, and assuming that no fluorescent excitation takes place in other ions, the inferred abundances of helium and heavy elements would be underestimated by up to 0.06 dex. Even in the most favorable case, the large aperture corresponding to a 3D integration, a 0.01 dex (2%) bias would be introduced; although this is negligible for most abundance measurements, it would be crucially large for high-precision applications, such as the determination of primordial helium. Although helium lines might also be affected by fluorescent excitation, line ratios will, in general, be different from what was predicted when neglecting fluorescent excitation.

3.2.2. Effect of Fluorescent Enhancement on the Balmer Decrement

A second implication concerns extinction measurements. The upper panel of Figure 5 shows the local H α /H β radial profile of model M2. In the innermost 20 pc and the outermost 20 pc, this ratio considerably differs from the value expected under case B. The deviation in the external region is caused by collisional excitation: H α /H β sharply rises because collisional excitation is more effective for H α than for H β (V. Luridiana 2009, in preparation). The deviation in the internal region is caused by fluorescence, as can be shown by an analysis of the pattern it follows. Fluorescent excitation of H α and H β is mainly triggered by Ly β and Ly γ photons, respectively; the optical depth in Ly β is larger than that in Ly γ , so that H α peaks at a smaller radius than H β (Figure 5, bottom panel). As a consequence, the H α /H β ratio initially increases, then it decreases as Ly β photons become

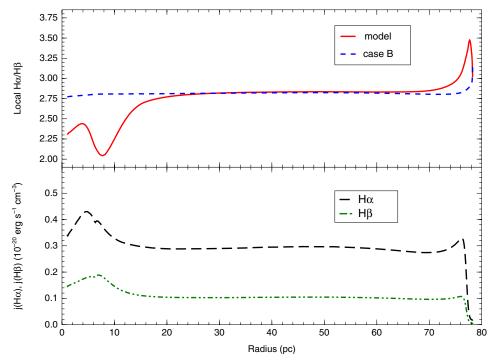


Figure 5. Top panel: local H α /H β intensity ratio as a function of radius in model M2, compared with the case B value at the model's local temperature. Bottom panel: normalized H α and H β emissivity profiles.

exhausted and Ly γ photons are still available, and eventually again increases to approach case B as both Ly β and Ly γ photons are exhausted. This behavior is to be expected no matter what the initial proportion of Ly β and Ly γ photons is, as it only depends on the optical depth at the two wavelengths. A spectrum with a larger flux in Ly β might produce an H α /H β ratio larger than the case B, but the succession between increasing and decreasing stretches would persist.

This interpretation of the H α /H β behavior has been independently verified by running models identical in all respects to model M1 except for the stellar continuum, in which small wavelength ranges around the Lyman-line wavelengths have been selectively suppressed. For example, in the model with no continuum between 1000 and 1050 Å, the H α /H β enhancement completely disappears, leaving only an H α /H β depression around $r \sim 10$ pc. For brevity, the detailed description of these models has been omitted.

The difference in fluorescent enhancement of different lines is shown in Table 5 for H α , H β , and H γ . These differences are model specific and depend on the number of photons available to excite the various Lyman lines (which in turn depends on the precise shape of the spectrum and, in a real nebula, on line broadening and Doppler shifts), and on the electron distribution among different sublevels of a given level, which influences the downward radiative paths available and depends on the local gas density (*l*-mixing is quite ineffective at such low densities). We cannot say whether current synthesis models are accurate enough for these differences to be real, but, if we take them at face value, the straightforward consequence of this differential enhancement is a change in the intrinsic Balmer decrement with respect to its case B value.

Table 6 quantifies this effect for model M2, by comparing its $H\alpha/H\beta$ values with those of model M3. The case B value for these models' temperature is 2.81; the differences between such a value and the numbers in the table are determined

 Table 6

 Dependence of Predicted $H\alpha/H\beta$ Ratios on Fluorescent and Collisional Excitation

$H\alpha/H\beta$					
M2	M3	M4	M5		
2.70	2.84	2.68	2.83		
2.82	2.85	2.80	2.83		
2.86	2.86	2.82	2.83		
	2.70 2.82	M2 M3 2.70 2.84 2.82 2.85	M2 M3 M4 2.70 2.84 2.68 2.82 2.85 2.80		

by a competition among the three factors. On one hand, fluorescent excitation enhances H β more than H α (Table 5); this tends to *decrease* the Balmer decrement. On the other hand, collisional excitation enhances H α more than H β (V. Luridiana 2008, in preparation), tending to *increase* the Balmer decrement. Finally, fluorescent excitation takes place in the center and is, therefore, favored in 1D integrations, whereas collisional excitation takes place in the external part of the model and is favored in 3D integrations. These dependences explain the patterns seen in the table: in model M2 (with a "normal" amount of continuum pumping), fluorescence blueing dominates over collisional reddening in the 1D aperture, while collisional reddening dominates in the 3D aperture; in model M3 (where continuum pumping has been suppressed), fluorescence is quenched, so all the ratios are larger than the case B decrement, and the difference increases proportionally to the weight given to external regions due to the increasing role of collisional excitations. The consistency of this interpretation has been verified by computing density-bounded versions of models M2 and M3, labeled M4 and M5, respectively. In M4 and M5, the nebula is truncated at a radius of 70 pc, so that the region of collisional excitation is not included in the computation; as a result, the H $\alpha/H\beta$ ratios are either lower than (M4, density-bounded variant of M2) or close to (M5, densitybounded variant of M3) the case B value.

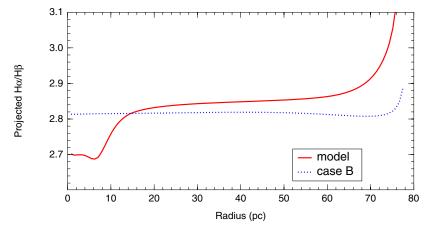


Figure 6. Solid line: $H\alpha/H\beta$ projected profile along the nebular midplane. Dotted line: $H\alpha/H\beta$ projected profile computed assuming case B emission. (A color version of this figure is available in the online journal.)

3.2.3. Observational Implications of Gradients in the Balmer Decrement

We can go a bit further by again recalling that the optical depth is different for different Lyman-line photons, in such a way that they are selectively absorbed at different depths into the nebula. Note that this is true no matter what the initial proportion of Lyman-line photons is, so that no role is played here by the caveat of Section 3.2.2 regarding the accuracy of the spectrum. As by-products of the absorption of Lyman photons, different Balmer lines are also produced in different proportions at different depths into the nebula (Figure 5, bottom); as a consequence, the purely fluorescent $H\alpha/H\beta$ ratio is expected to vary as a function of depth, being in general different from the case B value (Figure 5, top). Therefore, the projected $H\alpha/H\beta$ ratio also depends on the particular direction considered, as it depends on the proportion of fluorescence-excited atoms intercepted along the particular LOS and, therefore, on the distance from the exciting stars. Of course, the amplitude and scale length of this variation depend on the scale of the fluorescence zone, which depends on nebular geometry and is probably very thin in most objects; specifically, this will be shown in Section 5.2.1 that the more plane-parallel the gas distribution, the thinner the fluorescence zone. But in regions with thicker geometries, such dependence may lie above the spatial resolving power and be misinterpreted as a spatial variation of interstellar extinction.

There are numerous observations reporting systematic changes in the Balmer decrement along different LOSs and attributing them to differences in dust extinction (see, e.g., Maíz-Apellániz et al. 1998; Cannon et al. 2002; Kehrig et al. 2008). To investigate the possible role of continuum pumping in such differences, we simulate spatially resolved observations by plotting the predicted H α /H β ratio along a simulated narrow slit (Figure 6). Note that this is not the same as the 2D integration, which describes the *integrated* emission of a narrow slit. Figure 6 shows that, with fluorescent excitation properly taken into account, the H α /H β ratio actually increases from a minimum value near the center to a maximum in the outskirts. With no other observations available, this pattern could be interpreted as a variation in true extinction and bias the dust distribution inferred from the H α /H β ratio.

We believe that, for the most part and in most cases, the observed $H\alpha/H\beta$ gradient does indeed reflect the dust distribution; furthermore, it makes physical sense that such distribution is correlated to the spatial position of massive stars. However, we wish to call attention to the fact that a part of the gradient might also be intrinsic, arising as a consequence of the spatial segregation of fluorescent enhancement and collisional excitation of H⁰. Even adopting a conservative stance, the evidence presented in this section should be interpreted as a measure of the minimum uncertainty affecting interstellar extinction measurements. A rough estimate based on model M2 situates such uncertainty around ± 0.02 dex in H α /H β or ± 0.05 dex in $C(H\beta)$.

4. INFLUENCE OF THE SPATIAL DISTRIBUTION OF STARS

Assuming that the synthesis model used in this work is a good approximation to an actual SED, the effect of continuum pumping is inescapable. However, a natural objection to this conclusion is that it would cause apparent abundance gradients of appreciable amplitude, which would have hardly gone unnoticed. Existing evidence is not conclusive: for example, in the works by Izotov et al. (2006) and Kehrig et al. (2008), radial gradients in the inferred abundance can neither be confirmed nor dismissed. There may be several causes for this. First of all, the error bar in the derived abundances is of the same order of the effect we are concerned with. Second, we consider here a spherical geometry, whereas there are observational evidences of a blister geometry in some resolved H II regions; in such a case, the region affected by fluorescence enhancement would be compressed in a thin shell. Finally, the spatial distribution of stars is not always centrally concentrated as in our naive, highly idealized model. This comment mainly concerns giant H II regions, in which the scale of the system exceeds the Strömgren radius of individual stars. In such cases, we can expect a complex geometry, which cannot be represented by our simple model. In the extreme case of homogeneously distributed sources, local predictions would approach the volume-averaged result of a centrally concentrated source.

5. DEPENDENCE OF FLUORESCENT INTENSITY ON THE MODEL'S PARAMETERS

5.1. Dependence on Stellar Population's Parameters

In this section, we will briefly discuss how fluorescent excitation, whose effectiveness is a function of the Lyman-line photons available in the exciting spectrum, is affected by the stellar population's parameters. Only a qualitative description of the input synthesis models will be used to this aim. The

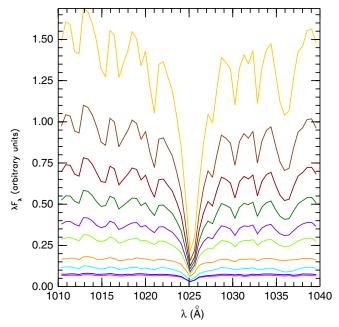


Figure 7. SEDs around $Ly\beta$ of a sequence of synthesis models with increasing ages, normalized to the number of ionizing photons. From the bottom up: 2, 1, 3, 4, 5, 6, 7, 8, 9, and 10 Myr.

discussion below is based on models with Z = 0.02 and Z = 0.001 and ages between 1 and 15 Myr.

The outcome of a comparison between different SEDs depends on the variables that are held fixed. In the present case, the comparison must be carried out at fixed $Q(H^0)$, because we wish to compare the Balmer line intensity due to fluorescent excitation with the intensity due to recombination, which is determined by $Q(H^0)$.

5.1.1. Age of the Burst

The fraction of H α provided by fluorescent excitation monotonically increases as age increases, amounting to, for example, 3%, 4%, and 6% at t = 4, 6, and 10 Myr, respectively. Note that this increase is triggered by the progressive decrease in the number of ionizing photons, which declines with age; this is only partially offset by the increase in the absolute value of the equivalent width of the Lyman α absorption line taking place after 3 Myr. This can be seen in Figure 7, which shows a sequence of SEDs in the age range 1–10 Myr normalized to the number of ionizing photons.

5.1.2. Metallicity

Comparison of models spanning a wide metallicity range $(Z_{\text{gas}}, Z_* = 0.001-0.02)$ suggests that metallicity has no effect in very young objects, and only a slight effect in older objects, in the sense of larger fluorescent contributions at larger metallicities. Our predictions for the 3D integration of models with ages in the 1–5 Myr range are listed in Table 7. Relative contributions for other apertures might be estimated on the basis of these.

5.2. Dependence on Gas Distribution

5.2.1. Nebular Geometry

By "nebular geometry," we exclusively refer to the distinction between thick (spherical) and thin (plane-parallel) models. The volume-integrated fluorescent contribution does not depend on

Ζ		t (Myr)	
	1	3	5
0.001	0.02	0.02	0.03
0.004	0.02	0.02	0.04
0.008	0.02	0.03	0.04
0.02	0.02	0.03	0.04

geometry; roughly speaking, the relative excitation rates depend on the number of photons available for each process (ionizing photons in the case of recombination, Lyman-line photons in the case of fluorescent excitation). However, the beam-integrated fluorescent contribution does depend on nebular geometry: the more plane-parallel the model, the closer its beam- and volumeintegrated line intensities. Asymptotically, the intensities seen through different integrations coincide.

5.2.2. Nebular Boundedness

Density-bounded models differ from ionization-bounded models in that the outermost part is missing. The fraction of fluorescent excitation in these models increases proportionally to the extension of the missing part, until the slab becomes so thin that it falls under case C.

5.3. The Effect of Dust

Our simulations so far have assumed a dustless nebula. This is not a realistic assumption in most nebulae, and the difference may be relevant in the context of this research since dust grains absorb UV photons. To understand this issue, we have computed a series of dusty models with varying metal abundances and dust content. Our models, which span the metallicity range $0.004 \leq Z_{gas} \leq 0.016$, show no dependence of the relative fluorescent contribution on dust content (although, of course, absolute fluxes are altered). The reason for this behavior is the approximate constancy of dust opacity in the relevant range, which roughly goes from the energy of $Ly\beta$ to a few Rydbergs. The grains used in these models are Oriontype, which is relatively large; using ISM-type grains, with a distribution extending to smaller wavelengths, UV photons would be more effectively blocked, resulting in smaller and dimmer nebulae. However, the fluorescent relative contribution would stay constant. This is a consequence of the small relative variation of dust opacity in the relevant range, which goes from Ly β to $\lambda \sim 400$ Å (this range encloses more than 90% of the total number of ionizing photons); see, for example, Figure 19 of Baldwin et al. (1991), which shows that the total variation of the absorption coefficient in the relevant range is within a factor of 2 that defines the maximum bias that might affect our dustless results.

5.4. The Effect of Nonthermal Line Widths

The line widths of actual H II regions are larger than the expected thermal width. The origin of this nonthermal contribution is currently unknown, although it has been suggested that it might be turbulence (Rozas et al. 1998; Relaño et al. 2005). Whatever its cause, the effect of an increased line width is to make continuum pumping more efficient by increasing the line flux available (see, e.g., Ferland 1992). Since our models so far have been computed under the assumption of thermal line width,

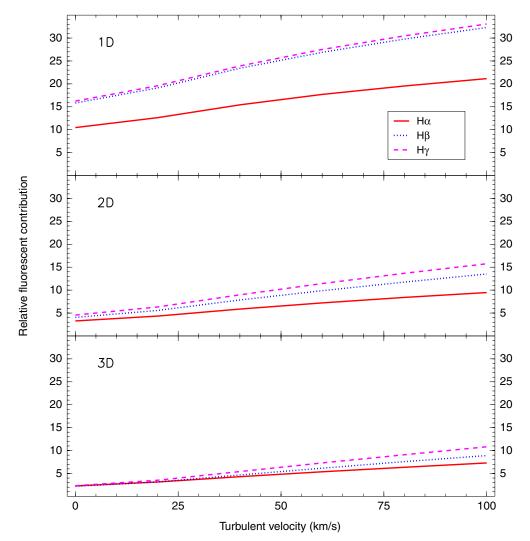


Figure 8. Relative contribution of fluorescent excitation to the intensities in $H\alpha$, $H\beta$, and $H\gamma$ as a function of microturbulent velocity. (A color version of this figure is available in the online journal.)

we will discuss here the consequences of assuming increasing line widths that are caused by turbulence.

Figure 8 illustrates the effect of turbulence on our reference model M2 at different values of the microturbulent velocity, which is assumed Gaussian. The fluorescent component increases linearly with the turbulent velocity in all the range explored; specifically, from 0 to 100 km s⁻¹, it doubles in 1D integrations and triples in 2D integrations, whereas the increase in 3D integrations is even larger. This gives an indication of how this paper's estimates should be increased in order to take turbulence into account. At even larger velocities, the effect would continue to increase.

6. DEPENDENCE OF H FLUORESCENT EXCITATION ON THE STELLAR ATMOSPHERE DETAILS

In this section, we will consider the case of H II regions around individual stars to discuss how our results depend on the details of the stellar atmosphere. In Section 2.1, we mentioned two stellar spectral features, not present in blackbodies, that may affect the balance between the Lyman-line photons and the Lyman-continuum photons, and, hence, the relative importance of fluorescent enhancement in Balmer lines: the Lyman jump and the stellar absorption lines. These two features affect continuum pumping in opposite directions. On one hand, the ratio of nonionizing-to-ionizing photons depends on the size of the Lyman jump; hydrogen continuum pumping has a greater relative importance in a stellar atmosphere with a Lyman jump than in a blackbody case. On the other hand, absorption lines at the Lyman frequencies decrease the number of continuum photons available to pump, thus quenching continuum pumping. Both features depend on the characteristics of the star, that is, on its spectral type and luminosity class, metallicity, and strength of the stellar wind; for example, the size of the Lyman jump is larger in an O9 V star than in an O3 V star.

The stellar flux emitted by massive stars in the spectral range between the Lyman jump and 1200 Å has never been studied in terms of its effect on the surrounding nebular material; usually, only the ionizing part of the stellar fluxes is considered to be important. However, the arguments of Section 2 showed the importance of the nonionizing part. Fortunately, our knowledge of the characteristics of the stellar flux in this spectral range has enormously improved in the last few decades, thanks to the far-UV (FUV) spectroscopic observations provided by space telescopes (mainly *Copernicus* and *Far Ultraviolet Spectroscopic Explorer (FUSE*): see, e.g., Walborn et al. 2002; Pellerin et al. 2002) and the development of stellar atmosphere codes for massive stars (e.g., Hillier & Miller 1998; Pauldrach

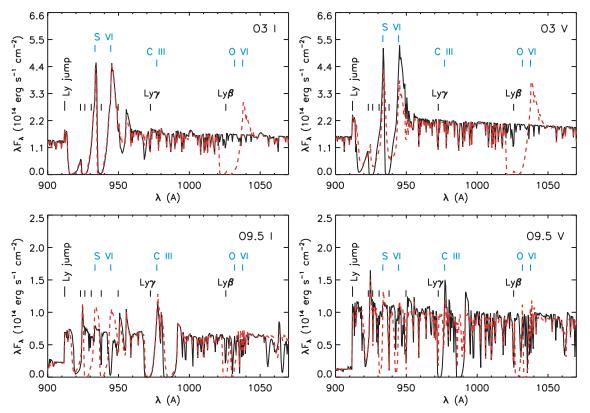


Figure 9. WM-basic models for stars of different spectral types and luminosity classes (see Table 8 for the main models' properties). Black solid lines: models with a smooth wind-velocity law; light dashed lines: shocked-wind models. The main stellar spectral features that may affect case D predictions are indicated. (A color version of this figure is available in the online journal.)

et al. 2001). We review these characteristics here and give examples of how they may affect the behavior of photoionization models including continuum pumping.

To this aim, we considered two sources of information: the FUV spectral atlases, compiled by Walborn et al. (2002) and Pellerin et al. (2002), and the predictions of WM-basic models (Pauldrach et al. 2001). Below, we describe the main stellar spectral features that may affect case D predictions. In particular, we are interested in the Lyman jump and those spectral features affecting the stellar flux emitted at the Lyman wavelengths.

In Figure 9, we show the spectra of WM-basic models corresponding to four different spectral type-luminosity class combinations, in the wavelength range 900–1070 Å, which includes the Lyman jump, the relevant H Lyman lines, and other stellar features of interest. Only this range is represented because we are only interested in those lines that can produce Balmer lines through continuum pumping, that is, $Ly\beta$ and Lyman lines of shorter wavelengths. Two types of WM-basic models were computed and included in the figure (also see Table 8): black solid lines represent models with a smooth wind-velocity law and light dashed lines represent models including the effect of shocks in the wind. This second type of models is necessary to reproduce some of the lines observed in the FUV spectra of massive stars, such as O vI lines (see below).

6.1. The Lyman Jump

This feature, located at $\lambda = 911$ Å, is the limit between the ionizing and the nonionizing parts of the stellar flux. It is produced by the presence of a sharp limit in the ionization cross section for the ground level of H I. Therefore, its size depends on the amount of neutral H I atoms in the atmosphere,

 Table 8

 Parameters of the WM-Basic Models Used in This Work

SpT	T _{eff} (K)	$\log g$ (cm s ⁻²)	R	$\log \dot{M}$	$\frac{v_{\infty}}{(\mathrm{km}\mathrm{s}^{-1})}$
031	42233	3.73	$\frac{(R_{\odot})}{18.6}$	$(M_{\odot} yr^{-1})$ -5.15	2800
O9.5 I	30463	3.19	22.1	-5.67	2200
03 V	44852	3.92	13.8	-5.77	2800
03 V 09.5 V	31884	3.92	7.2	-6.89	130

Note. For those models including a shocked wind, the X-ray luminosity is $L_{\rm X} = 10^{-6.5} L_{\rm bol}$. The parameters are based on the observational $T_{\rm eff}$ scales by Martins et al. (2005; their Table 4).

which is determined by the temperature and density in the region of the stellar atmosphere where the stellar continuum at this wavelength is formed. Generally speaking, the Lyman jump will be larger at lower effective temperatures and larger gravities (since in these cases, hydrogen is expected to be more recombined). Note, however, that the size of the Lyman jump may also be affected by other features of massive stars' winds (see, e.g., Gabler et al. 1989; Najarro et al. 1996).

Since practically no observations of the Lyman jump exist (the nonionizing part of the stellar flux is generally not accessible to direct observations), we have to rely on stellar atmosphere models. As already mentioned, the Lyman jump is larger in stars with larger gravities (dwarf stars) and later spectral types (Figure 9).

6.2. Stellar Lines

Both observations and models show that the stellar flux at the Lyman wavelengths may be affected not only by the H Lyman

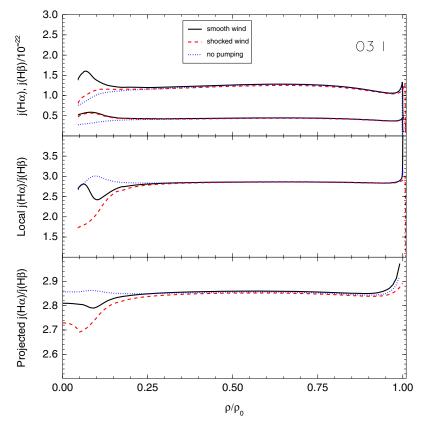


Figure 10. Local emissivities, local Balmer line ratios, and projected Balmer line ratios of photoionization models illuminated by WM-basic models of an O3 I star, with a smooth wind-velocity law (solid) and a shocked wind (dashed), compared with those of a model with no fluorescent excitation (dotted). Emissivities are in units of erg s⁻¹ cm⁻². The distances to the stars are normalized to the maximum nebular radius in each case. (A color version of this figure is available in the online journal.)

lines, but also by resonant lines of heavy elements at different wavelengths that may develop P-Cygni profiles if the characteristics of the stellar wind are appropriate. If the P-Cygni profile is completely developed and the wind terminal velocity is large enough, the saturated blueshifted absorption may reach blueward the wavelength of the closest H Lyman line (see Figure 9).

As illustrative examples, we discuss here the behavior of the O vI $\lambda\lambda$ 1032, 1038 doublet and the C III λ 979 lines as a function of the spectral type, luminosity class, and wind characteristics, respectively. Figure 9 also shows the location of the S vI lines, which may affect other H Lyman lines. However, this is only given for information and its behavior is not discussed here.

The O VI $\lambda\lambda$ 1032, 1038 lines may affect the spectral region of Ly β . The spectroscopic catalogues by Pellerin et al. (2002) and Walborn et al. (2002) show that these lines exhibit a single P-Cygni wind profile in early-type O stars, both in dwarfs and supergiants. In later O-type spectra, two distinct blueshifted absorption features are often visible and, in the case of supergiants, O vI lines are still visible in B1 I stars. These lines depend only weakly on the temperature, luminosity, and metallicity of the star, and can still be seen even at metallicities as low as in the Small Magellanic Cloud (SMC).

The presence of lines of this "superionization" species in the spectrum of OB stars has been commonly attributed to the effect of shock-produced X-rays on the ionization distribution in hot star winds (see, e.g., Macfarlane et al. 1993, for a discussion concerning the origin of this exotic species). In fact, only stellar atmosphere models including shocks in the stellar wind can produce the O vI lines.

Figure 9 shows the synthetic UV spectra of WM-basic models with and without shocks. In the case of O3 stars, strong O vI P-Cygni profiles are only developed if shocks are included in the models. Something similar occurs in the O9.5 models where, although a P-Cygni profile is not developed, we can still find strong extended blueshifted absorptions. In all the cases, the presence of the O vI lines totally quenches the stellar continuum flux in Ly β . This only happens if the terminal velocity of the wind is above ~ 1700 km s⁻¹.

Our second example is the C III λ 979 line. Pellerin et al. (2002) showed that, in supergiants, this line appears as a broad P-Cygni profile with a broad absorption component in spectral types from O6 to O9.7, while a broad absorption feature is detectable in subtypes from O9.5 to B3 V. However, Walborn et al. (2002) showed that in SMC supergiants, the line saturates despite the lower abundances, and does not appear weaker than in their Large Magellanic Cloud (LMC) counterparts. Figure 9 shows the behavior of this line as predicted by WM-basic models for the stellar cases considered. In both O9.5 models, the C III line develops a P-Cygni profile whose blue absorption affects the flux in Ly γ . Interestingly, in the O9.5V star, this line is inhibited by the inclusion of shocks.

6.3. Implications of the Nonionizing Stellar SED on Case D Predictions

In this section, we discuss how the spectral features considered above make ionized nebulae deviate from case B to case D. To this aim, we constructed a set of spherical, dustless, constant density photoionization models with Cloudy. The internal radius and density of the models were $R_i = 1$ pc and $n_H = 200$ cm⁻³,

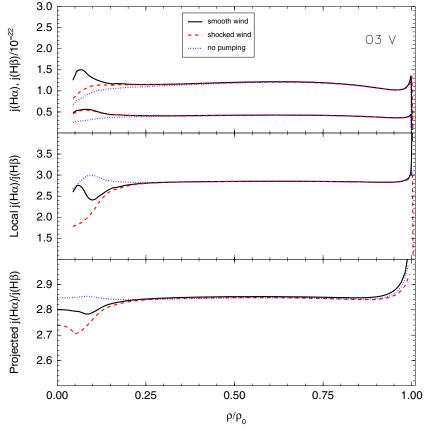


Figure 11. As in Figure 10, for the case of an O3 V star. (A color version of this figure is available in the online journal.)

respectively, and no turbulent line widening was assumed. The SEDs predicted by WM-basic for the stellar models summarized in Table 8 were included as input in these Cloudy models, normalized to log $Q(H^0) = 52.09 \text{ s}^{-1}$.

Figures 10–13 show the predicted H α and H β emissivities and the H α /H β ratio for different stellar cases: similar to Figure 9, dashed and solid lines indicate results obtained with or without shocks, respectively, with full inclusion of fluorescent excitation, while dotted lines are results obtained by switching off the fluorescent excitation. The behavior of ratios can be easily understood by considering the spectral features of each model as a function of its properties.

In O3 stars, we see that while the behavior of the H α /H β line ratio is very close to case B predictions when a smooth stellar wind-velocity law is assumed, it is decreased with respect to case B predictions when a shocked wind stellar model is considered. In the case of a smooth wind law, even though the Lyman jump is small and the stellar continuum flux at the Ly β and Ly γ wavelengths is diminished, the local H α and H β emissivities are noticeably affected by stellar continuum pumping in the region close to the stars, resulting in a strong deviation from case B predictions. However, the H α and H β variations are similar in such a way that their ratio is close to case B predictions. However, in the shocked-wind stellar atmosphere models, the presence of the O vI P-Cygni line (see Figure 9) leaves no Ly β photons, and hence the fluorescent contribution to H α is negligible. Since the fluorescent excitation of H β is similar to the previous case, the combined effect is a lower $H\alpha/H\beta$ ratio in the inner part of the nebula as compared to case B predictions.

A similar line of reasoning can be followed to understand the other stellar cases represented in Figures 10–13. For example, the large H α /H β line ratio predicted in the O9.5 I case when a smooth wind law is used in the stellar atmosphere model calculation is a consequence of the large flux in Ly β (which triggers a large fluorescent contribution to H α) and the small flux in Ly γ , due to the presence of the C III line (which quenches the fluorescent contribution to H β). (Note that in this case, the Lyman jump is larger.) This large deviation from case B vanishes when the shocked-wind stellar atmosphere model is considered, due to the development of a broad absorption feature in the O vI lines that affects Ly β . In this case, the continuum pumping at Ly β and Ly γ is zero (note, however, that the H α and H β emissivities slightly deviate from case B; this is produced by pumping in Ly δ).

This example illustrates how deviation from case B to case D depends on the spectral features appearing in the spectral region considered. Generally speaking, we can conclude that the characteristics of the wind have a sizeable effect on the predicted Balmer line ratios. Models with shocked winds have lower H α /H β wih respect to models with smooth wind-velocity laws.

6.4. The Effect of the Lyman-Line Profile

The discussion above has made clear that the amount of Lyman-continuum pumping in a nebula is crucially dependent on the line profiles. These depend on both the wind structure and the relative motion between the stellar source and the gas, so the case should be considered in which the Lyman lines in the stellar continuum are in emission rather than absorption; in such

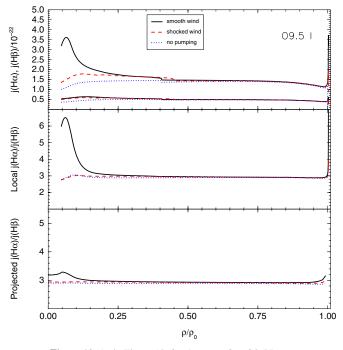


Figure 12. As in Figure 10, for the case of an O9.5 I star. (A color version of this figure is available in the online journal.)

a case, the nebula could produce more excitation than expected. We have taken such possibility into account by computing a sequence of models with varying blocking factors, whose effect is to amplify the amount of continuum pumping by a given factor, which can be either smaller or larger than 1 (see Appendix A in Pellegrini et al. 2007).

The result is illustrated by Figure 14, which shows the ratio of the total H β emission to the case B H β emission as a function of the blocking factor in a radiation-bounded spherical model ionized by a stellar continuum (solid line, left-hand scale). In the same figure, we have plotted the predictions for the first zone of the same models, a case corresponding to classical case C. In either case, a blocking factor larger than 1 implies that pumping is amplified with respect to the predicted value. It can be seen that increasing values of pumping trigger H β intensities well above predictions, particularly under case C conditions.

7. DISCUSSION

7.1. Comparison with Collisional Excitation

In this section, we highlight the differences between fluorescent and collisional excitation, in order to provide some useful guidelines to minimize their impact on observations aimed at abundance determinations. Both mechanisms provide channels to increase the intensity of Balmer lines, but they act with different effectiveness depending on the location within the nebula and the physical conditions' regime. The following is a quick summary of such analogies and differences.

7.1.1. Why Fluorescent Excitation Might be More Important than Collisional Excitation

Along any given LOS, fluorescent excitation takes place in the nebular region, which lies closest to the illuminating stars. Collisional excitation, in contrast, preferentially takes place in the recombination zone that marks the outer limit of the

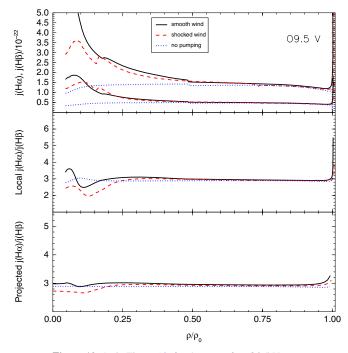


Figure 13. As in Figure 10, for the case of an O9.5 V star. (A color version of this figure is available in the online journal.)

H II region. Such a region may be lacking totally or in part if the nebula is density-bounded, whereas a fluorescent region always exists. A further consequence of the different positions in the nebula is that the relative contribution of fluorescence is enhanced in slit observations. Finally, fluorescence appears to be happening in all kinds of nebulae, with no strong preferences for metallicities and with a tendency to increase at increasing ages, whereas collisional excitation is effective only in hot, young nebulae. All in all, fluorescence then appears to be a more ubiquitous process.

7.1.2. Comparison Between the Uncertainties Affecting Either Process

The *integrated* value of fluorescent excitation does not depend on the geometrical distribution of the gas neither does the *integrated* value of collisional excitation, provided the region is radiation bounded. Therefore, the two processes are pretty much geometry-free as long as the whole nebula is integrated, and detailed knowledge of geometry is not necessary.

Fluorescent excitation might depend much more than collisional excitation on the distribution of stars in the case of spatially resolved observations. This circumstance is further complicated by the fact that it is not necessarily dominated by the hottest stars, as are recombination and, probably, collisional excitation.

Both processes also depend on the illuminating SED, but collisional excitation depends on it in a much weaker way than fluorescent excitation. The dependence of collisional excitation on the SED arises on the heating power of the ionizing photons: the harder the average photon, the hotter the gas, so younger clusters are more collisionally excited than older clusters. However, rough knowledge of the cluster's age and its SED is usually sufficient to this aim. However, fluorescent excitation crucially depends on the SED and specifically on the detailed profile of the relevant spectral features, which determine the proportion of photons available to excite the various Lyman lines. Theoretically, such a shape depends on the stellar mix,

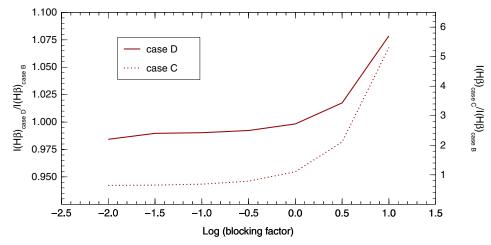


Figure 14. $H\beta_{tot}/H\beta_{caseB}$ as a function of the blocking factor, for a model nebula ionized by a stellar model with a smooth wind law. Solid line, left-hand scale: radiation-bounded model (case B conditions). Dotted line, right-hand scale: predictions for the innermost zone (case C conditions). Note that the ratio is, in case C, much larger than 1. Also see Ferland (1999).

the metallicity, and details of the atmosphere. Examples of this are given in Section 6 and in González Delgado et al. (1997), where it is shown how the stellar Ly β flux may be affected by a neighboring O vI line. This extreme dependence implies that moderate nebular motions might drastically change the result by Doppler-shifting the line photons seen by the gas. In sum, uncertainties related to the SED affect the estimation of fluorescent excitation, while they have a much smaller impact on the evaluation of collisional excitation.

As for the $H\alpha/H\beta$ ratio, it can only be increased by collisions, while it can either be increased or decreased by fluorescence, depending on the details of the SED and the spatial position considered.

7.2. Literature on Case D

As noticed in Section 1, not much has been written on the subject of optically thick nebulae illuminated by stellar radiation, which we have called "case D." There are several specific reasons for this, at first surprising, fact. One of them has already been mentioned earlier in this section: absorption lines in stellar continua are expected to quench continuum pumping. Even if the hypothesis is made such that enough photons survive, a quantitative analysis must by necessity rely on a detailed model spectrum; if this ingredient is lacking, it becomes difficult even to make qualitative assessments (see, e.g., Section 2.1). High-resolution stellar libraries and synthesis spectra have only recently become available, making this kind of study possible. From this point of view, the forthcoming publication of high-resolution spectral synthesis models will be a giant leap forward.

For lines of other ions, fluorescence is a well-known excitation mechanism (see, e.g., Seaton 1968; Ferland 1992; Lucy 1995). Its effect on the helium spectrum has been recently discussed by Benjamin et al. (2002). In the case of hydrogen, though, fluorescence only provides a small fraction of the total intensity, and until recently neither theory nor observations were accurate enough to justify an analysis at that level of precision. As an extreme example, consider that at the time of publication of the Baker and collaborators' series of papers, Gaunt factors equal to 1 were still considered a reasonable approximation, and in 1959, errors on Gaunt factors as great as 20% were still acceptable (Seaton 1959).

A final point is brought about by improvements in technology, and in particular by the increasingly better spatial resolution. Since fluorescent contribution is the largest in beamlike observations close to the stars, the availability of spatially resolved information might actually signify a worsening in accuracy. This is analogous to what happens in population synthesis, where the straightforward modelization of stellar populations is made difficult by the poor sampling associated with small observing elements, in such a way that a probabilistic treatment becomes imperative (i.e., Cerviño & Luridiana 2006).

8. SUMMARY AND CONCLUSIONS

Case D is the theoretical scenario describing optically thick nebulae irradiated by stellar continua. In these objects, the Balmer spectrum has a fluorescent component superposed to the recombination component: while the ionizing part of the stellar continuum is responsible for the recombination component, the nonionizing part produces a generally small but non-negligible fluorescent component. In the same way as collisional excitation of H^0 , which is discussed in various papers cited in this work, this mechanism represents an additive correction to recombination, and as such it must be taken into account in abundance analysis to avoid biased results.

Case D represents a correction to the more famous case B, but, as case B, it is a limiting scenario that only asymptotically describes the behavior of real nebulae. The label "case D" has been given for symmetry with case C, but cases C and D are inherently different from cases A and B in that they are not descriptions of intrinsic gas properties, but rather descriptions of complex systems that depend as much on the intrinsic properties of hydrogen as on the "boundary conditions" represented by the stellar pumping.

To estimate the fluorescent contribution predicted under case D, it is necessary to understand how it depends on the object's physical parameters and how it is affected by the observational conditions. With respect to the first point, our bottom line in this work is that proper modeling requires inputting high-resolution synthesis models into the photoionization code. Even this might be only a rough approximation as Doppler shifts and various line-broadening mechanisms might be acting in real nebulae, thus altering the pattern of photons absorption, but at least it is a physically based approximation and a good starting point for further explorations.

Regarding the influence of observational conditions, we have shown that the relative fluorescent intensity observed depends on the aperture. Such dependence is straightforward in the case of a centrally concentrated cluster, but it becomes nontrivial as more complicated spatial configurations are considered. 3D models including continuum transfer and photoionized by highresolution SEDs might help in these cases, but even these could be insufficient to account for actual complexities, as a substantial fraction of the fluorescent component might come from stars of stellar type later than O. When large apertures are considered, geometrical features bear no influence.

A comparison with the other major deviation from pure recombination, collisional excitation, is interesting both to clarify both mechanisms and to devise observational strategies to deal with them, which usually means trying to minimize them. Our study suggests that fluorescence might be much more important than collisional excitation in two important ways: it may contribute a larger fraction of the intensity and it is predicted to virtually affect any H II region, whereas collisional excitation is effective only in hot, young, metal-poor, radiation-bounded H II regions. One important difference between the two is that while collisional excitation takes place in the outer parts of H II regions, fluorescent excitation takes place in the vicinity of stars; the observer willing to minimize its contribution on the total intensity is thus placed before a dilemma, as the former mechanism is minimized by spatially resolved observations, while the latter is minimized by observations of the complete nebula. Finally, collisional excitations always produce reddening in the spectrum, whereas fluorescence might produce both blueing and reddening at different points in the nebula. Both mechanisms must be taken into account when optical spectra are used to study the dust distribution of observed objects, as they can introduce small biases in spatially resolved extinction measurements.

Since this is an exploratory paper, we do not attempt to establish here an exhaustive calibration of fluorescent excitation of Balmer lines across the whole H II regions' taxonomy; rather, we aim at pointing out a problem and the tools necessary to solve it. Fluorescent excitation adds a small but non-negligible contribution to the observed Balmer spectra of H II regions and, as such, it should be studied in detail and thoroughly understood since neglecting it might introduce biases in abundance determinations. Such biases might be particularly significant when determining the abundance of primordial helium, where a high accuracy is required. For such application, it is also necessary to take into account the effect of continuum fluorescence on the helium emission lines.

This work has been funded with support from the Spanish Ministerio de Educación y Ciencia through grants AYA2004-63030 and AYA2007-64712, cofinanced with FEDER funds. G.J.F. acknowledges support from NSF (AST 0607028) and NASA (07-ATFP07-0124). S.S.D. acknowledges support by the Spanish MEC/Fullbright postdoctoral fellowship program. The title was inspired by L. B. Lucy's paper (Lucy 1995). The plots have been made with the IDL package *jmaplot* by J. Maíz. Fruitful discussions have been conducted with J. García Rojas, A. Peimbert, M. Peimbert, E. Pérez, G. Stasinska, and

 Table 9

 Comparison of Predictions

Line	Case A	Case C (l-mixed)	Case C (l-resolved)
1216	33.1	146.00	165.00
6563	2.82	4.02	8.02
4861	1.00	1.45	2.35
4340	0.473	0.687	1.00
4102	0.264	0.384	0.523
1.875 m	0.455	0.496	0.807
1.282 m	0.215	0.235	0.347

R. Szczerba. V.L. acknowledges the Instituto de Astronomía-UNAM for hospitality.

APPENDIX

CASE A, B, AND C IN C08

Version C08 of Cloudy has the ability to resolve atoms and ions of the H-like iso-electronic sequence. For most of its history, the code has used the compact model of the H atom originally described by Ferland (1980), Cota & Ferland (1988), and updated by Ferguson & Ferland (1997). This model assumed a well *l*-mixed *n*-configuration as pioneered by Seaton (1959). Under this assumption, the populations of *l*-terms within an *n*configuration are proportional to the statistical weight 2(l+1). Term-averaged transition probabilities, such as those given by NIST, are used.

With the advent of faster processors, it is now possible to resolve the nl-terms within an n-configuration. The number of states that must be considered is substantially larger. For instance, there are 210 terms within the first 20 levels of H⁰, so on most processors, the linear algebra will be roughly 2 dex slower. In the current implementation, it is possible to adjust the number of n-configurations that result into l-terms. These are then supplemented with several additional l-mixed n-configurations to "top off" the model atom. Only lines produced within the nl-resolved levels are reported.

The predictions of the resolved and *l*-mixed models can be different at low densities where the real *l*-terms are not mixed by collisions. Continuum fluorescence, the topic of this paper, has different effects in these two approximations, as stressed by Ferland (1999). The reason is that l-averaged transition probabilities between excited *n*-configurations and the ground n = 1 configuration are dramatically different because only np-1s transitions occur. At low densities, the rate of decay from an excited *n* to ground will be overestimated if the *l*-mixed transition probabilities are used. Another complication is that the relationships between the Einstein A and B coefficients are not correct if the total statistical weight of the upper configuration is used. All of these problems are solved with the *l*-resolved model now used in Cloudy. The current version of Cloudy predicts an H I spectrum in excellent agreement with Storey & Hummer (1995) when the number of resolved levels is made large enough.

Predictions of the fluorescent excitation spectrum can have even greater differences. Table 9 gives a comparison of the fluorescent-excited spectrum for an optically thin cell of pure hydrogen gas with unit density. It is exposed to a 50,000 K blackbody with an ionization parameter of 0.01. The emission would be close to case A if there were no external continuum fluorescing the Lyman lines. It is in the case C limit when continuum excitation is included. The first column gives the wavelength of a few Lyman, Balmer, and Paschen lines. The second column gives the Storey & Hummer (1995) case A intensities relative to their predicted H β . The last two columns give the case C predictions for the *l*-resolved (current Cloudy) and *l*-mixed (versions before C08) cases, respectively.

REFERENCES

- Baker, J. G., & Menzel, D. H. 1938, ApJ, 86, 70
- Baldwin, J. A., Ferland, G. J., Martin, P. G., Corbin, M. R., Cota, S. A., Peterson, B. M., & Slettebak, A. 1991, ApJ, 374, 580
- Benjamin, R. A., Skillman, E. D., & Smits, D. P. 2002, ApJ, 569, 288
- Burgess, A. 1958, MNRAS, 118, 477
- Cannon, J. M., Skillman, E. D., Garnett, D. R., & Dufour, R. J. 2002, ApJ, 565, 931
- Cerviño, M., Gómez-Flechoso, M. A., Castander, F. J., Schaerer, D., Mollá, M., Knödlseder, J., & Luridiana, V. 2001, A&A, 376, 422
- Cerviño, M., & Luridiana, V. 2006, A&A, 451, 475
- Chamberlain, J. W. 1953, ApJ, 117, 399
- Charbonnel, C., Meynet, G., Maeder, A., Schaeller, G., & Schaerer, D. 1993, A&AS, 101, 415
- Cota, S. A., & Ferland, G. J. 1988, ApJ, 326, 889
- Ferguson, J. W., & Ferland, G. J. 1997, ApJ, 479, 363
- Ferland, G. J. 1980, PASP, 92, 596
- Ferland, G. J. 1992, ApJ, 389, L63
- Ferland, G. J. 1999, PASP, 111, 1524
- Ferland, G. J., Korista, K. T., Verner, D. A., Ferguson, J. W., Kingdon, J. B., & Verner, E. M. 1998, PASP, 110, 761
- Ferland, G. J., & Rees, M. J. 1988, ApJ, 332, 141
- Gabler, R., Gabler, A., Kudritzki, R. P., Puls, J., & Pauldrach, A. 1989, A&A, 226, 162
- González Delgado, R. M., Cerviño, M., Martins, L. P., Leitherer, C., & Hauschildt, P. H. 2005, MNRAS, 357, 945
- González Delgado, R. M., Leitherer, C., & Heckman, T. 1997, ApJ, 489, 601
- Hillier, D. J., & Miller, D. L. 1998, ApJ, 496, 407
- Hubeny, I., Lanz, T., & Jeffery, C. S. 1995, SYNSPEC-A Users Guide (http://nova.astro.umd.edu)
- Izotov, Y. I., Schaerer, D., Blecha, A., Royer, F., Guseva, N. G., & North, P. 2006, A&A, 459, 71
- Kehrig, C., Vílchez, J. M., Sánchez, S. F., Telles, E., Pérez-Montero, E., & Martín-Gordón, D. 2008, A&A, 477, 813

- Kurucz, R. L. 1993, Kurucz CD-ROM 13, ATLAS9 Stellar Atmosphere Programs and 2 km/s Grid (Cambridge: SAO)
- Lanz, T., & Hubeny, I. 2003, ApJ, 146, 417
- Leitherer, C., et al. 1999, ApJS, 123, 3
- Lucy, L. B. 1995, A&A, 294, 555
- Luridiana, V., & Peimbert, M. 2001, ApJ, 553, 633
- Luridiana, V., Peimbert, A., Peimbert, M., & Cerviño, M. 2003, ApJ, 592, 846
- Macfarlane, J. J., Waldron, W. L., Corcoran, M. F., Wolff, M. J., Wang, P., & Cassinelli, J. P. 1993, ApJ, 419, 813
- Maíz-Apellániz, J., Mas-Hesse, J. M., Muñoz-Tuñón, C., Vílchez, J. M., & Castañeda, H. O. 1998, A&A, 329, 409
- Martins, F., Schaerer, D., & Hillier, D. J. 2005, A&A, 436, 1049
- Martins, L. P., González Delgado, R. M., Leitherer, C., Cerviño, M., & Hauschildt, P. 2005, MNRAS, 358, 49
- Menzel, D. H. 1937, ApJ, 85, 330 Menzel, D. H., & Baker, J. G. 1937, ApJ, 86, 70
- Najarro, F., Kudritzki, R. P., Cassinelli, J. P., Stahl, O., & Hillier, D. J. 1996, A&A. 306, 892
- Osterbrock, D. E., & Ferland, G. J. 2006, in Astrophysics of Gaseous Nebulae and Active Galactic Nuclei, ed. D. E. Osterbrock & G. J. Ferland (2nd ed.; Sausalito, CA: Univ. Science Books)
- Pauldrach, A. W. A., Hoffmann, T. L., & Lennon, M. 2001, A&A, 375, 161
- Peimbert, M., Luridiana, V., & Peimbert, A. 2007, ApJ, 666, 636
- Pellegrini, E. W., et al. 2007, ApJ, 658, 1119
- Pellerin, A., et al. 2002, ApJS, 143, 159
- Pottasch, S. R. 1960, ApJ, 131, 202
- Relaño, M., Beckman, J. E., Zurita, A., Rozas, M., & Giammanco, C. 2005, A&A, 431, 235
- Rozas, M., Sabalisck, N., Beckman, J. E., & Knapen, J. H. 1998, A&A, 338, 15
- Salpeter, E. E. 1955, ApJ, 121, 161
- Schaerer, D., Charbonnel, C., Meynet, G., Maeder, A., & Schaller, G. 1993a, A&AS, 102, 339
- Schaller, G., Schaerer, D., Meynet, G., & Maeder, A. 1992, A&AS, 96, 269
- Schaerer, D., Meynet, G., Maeder, A., & Schaller, G. 1993b, A&AS, 98, 523
- Seaton, M. J. 1959, MNRAS, 119, 81
- Seaton, M. J. 1968, MNRAS, 139, 129
- Stasińska, G., & Izotov, Y. I. 2001, A&A, 378, 817
- Storey, P. J., & Hummer, D. G. 1995, MNRAS, 272, 41 (on the web at http://adc.gsfc.nasa.gov/adc-cgi/cat.pl?/catalogs/6/6064/)
- Walborn, N. R., Fullerton, A. W., Crowther, P. A., Bianchi, L., Hutchings, J. B., Pellerin, A., Sonneborn, G., & Willis, A. J. 2002, ApJS, 141, 443