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Letter to the Editor

The mathematics of drug dose individualization should be built with random effects linear models

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Sir,

We are delighted at the publication of Holford and Buclin's article¹, which proposes a general theoretical framework for the clinical problem of individualizing drug doses. The essence of their proposal is that a careful assessment of between-patient and within-patient variability in the pharmacokinetic or pharmacodynamic response of interest should be made to decide whether a target concentration intervention (TCI) is appropriate, and should be made prior to formulating a TCI. Although Holford and Buclin do not give details about how these variabilities should be computationally combined with a particular patient's drug plasma concentrations and covariate values in order to implement a TCI in practice, their description of criteria to determine whether or not a TCI is necessary is an important contribution. Another reason for our enthusiasm is that Holford and Buclin's framework is conceptually equivalent to a rigorous mathematical formulation of dose individualization that we developed in several prior publications.^{2,3,4} In fact, we can say that if a pharmacologist is willing to *computationally* implement Holford and Buclin's ideas in a TCI by using standard statistical software, or to rigorously derive further *practical* and *methodological* consequences of these ideas for therapeutic drug monitoring (TDM), then he/she may want to read our publications as a next step.^{2,3,4}

Each and every pharmacokinetic concept described in Holford and Buclin's article has a corresponding and equivalently defined concept in our mathematical formulation. Table 1 describes the equivalence between Holford and Buclin's concepts and some of our concepts. We hope that this table serves as a guideline for those who want to proceed to read our more mathematically demanding papers.^{2,3} A friendly introduction for clinicians and pharmacologists, and epistemological consequences of the approach are in reference 4. Our mathematical formulation of dose individualization is based on random effects linear models, a family of statistical models that is well known and widely used by professional statisticians, but that, unfortunately, is not well known by pharmacologists. We celebrate that Holford and Buclin seem to have been inspired by random-effects ideas. This is suggested by the fact that they cite a work from the Sheiner School in their paper,⁵ a school that for decades have advocated the use of random-effects models (also called mixed regression models) for developing dose individualization methods. The Sheiner School, however, places emphasis on random-effects nonlinear models, not linear models, which is a reason to consider Holford and Buclin's ideas a significant conceptual jump.

The fact that other authors have independently developed ideas about dose individualization that are essentially equivalent to ours confirms that random effects linear models are the natural mathematical language of a pharmacological theory and practice of dose individualization.⁴ Our mathematical formulation based on these models provides answers to important questions that are not addressed in Holford and Buclin's article. For instance, 1) How can we compute an optimal dose for a particular patient, that is, what is the *optimal* way of combining steady-state concentrations from an individual patient with his/her demographic, clinical or genetic covariates in order to obtain an appropriate dose for the patient?; 2) What is the minimum number of blood samples at steady state that are needed from a patient in order to compute an *optimal* dose for that patient?; and 3) Do dose individualization methods currently used in TDM produce *optimal* doses?. After laying out the term "optimal dose" with

a concept that we have called omega-optimality, we have demonstrated through both decisiontheoretical arguments and computer simulations that a traditional TDM method of dose individualization that is advocated in many pharmacology textbooks does not produce optimal doses (see also footnote h to Table 1).³ Also, we have computed a table that provides the minimum number of blood samples that are needed from individual patients in order to obtain an omega-optimum dose for a high percentage of the patients in the population.² Finally, the basic tenet of the Sheiner School, that an empirical Bayesian approach should be used to amalgamate all the available information from a patient with prior population information in order to search for an optimum dose for the patient, can be shown to be particularly valid (and easy to implement computationally) when random effects linear models are used.^{2,3}

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Table 1. List of concepts that Holford and Buclin¹ use to build their approach to dose individualization, and the conceptually equivalent concepts that Diaz et al.^{2,3} use to build their statistical model and clinical algorithm for target concentration intervention.

Holford and Buclin's ¹ concept	Symbol used ^a	Diaz et al.'s ^{2,3} equivalent concept ^b	<u>Symbol(s) used^c</u>
Target concentration	тс	Target concentration ^d	C ₀
Safe and effective concentration range	SECR	Target concentration range (TCR)	(l_1, l_2)
Unpredictable between-subject variability	BSVu	Between-subjects variance ^e	σ_{lpha}^2
Unpredictable within-subject variability	WSVu	Intra-individual random error	σ_{ϵ}^2
Unpredictable variability	PPVu	Total variance of log of steady-state plasma concentrations	$\sigma_{\alpha}^2 + \sigma_{\epsilon}^2$
Predictable variability	PPV _P	Combination of fixed effects and covariates ^f	$\mu_{\alpha} + \boldsymbol{\beta}^T \boldsymbol{X}$
Safe and effective variability	SEV	Fraction of maximum attainable probability	$\omega imes m$, $\omega \approx 1$
		that patient reaches TCR ^g	
Individual target dose	ITD	Dose computed at second step of individualization algorithm ^h	<i>D</i> ₂
Clearance	CL	Patient's concentration-to-dose ratio at steady state ⁱ	$e^{\alpha+\boldsymbol{\beta}^T\boldsymbol{X}}$

^aSymbol used in Holford and Buclin's paper.¹

^bSome of the concepts used by Diaz et al.^{2,3} are standard concepts from the statistical literature on random effects linear models.

^cSymbol(s) or formula used in Diaz et al.'s paper.²

^dDiaz et al.^{2,3} also computed an optimal target concentration, symbolized by C_0^* , when it is desired to reach a particular target concentration range. However, any desired target concentration can be input into their dose individualization algorithm, including the TC suggested in formula (1) of Holford and Buclin.¹

^eThis is the variance of the random intercept,² or in general, the compounded variances of the random effects in a more general formulation given in reference 3.

^fIn the general mathematical formulation given in reference 3, covariates that have random effects on plasma concentrations also contribute to the predictable variability.

^gSimilarly to the SEV concept of Holford and Buclin,¹ the maximum attainable probability of a patient reaching the TCR (symbolized with *m* by Diaz et al.^{2,3}) is essentially a function of both the SECR and WSV_U or, equivalently, of (l_1, l_2) and σ_{ϵ}^2 . Under a TCI, the exact relationship between $\omega \times m$ and SEV is $\omega \times m = 1 - 2\Phi(-(\log \sqrt{l_2/l_1})/\text{SEV})$, where Φ is the standard normal cumulative distribution function.

^hA limitation of Holford and Buclin¹ paper is they do not specifically describe how to compute the ITD from a particular patient's drug plasma concentration. However, they describe that the ITD is usually computed with a concentration produced in the patient by a group therapy dose (GTD). If an empirical Bayesian approach such as that proposed by Diaz et al.^{2,3} were used to carry out this computation, the ITD would correspond to D_2 , the dose computed at the second step of Diaz et al.'s individualization algorithm. Depending on the particular values of BSV_u and WSV_u, and of SECR, this dose may or may not be optimal according to the omega-optimality criterion of Diaz et al.^{2,3} If it is not optimal, additional algorithm steps are needed to obtain optimality. In general, depending on both how the ITD is computed and the patient population characteristics, the ITD may or may not be optimal in the sense that the probability that a particular patient reaches the SER with such dose may or may not be as high as possible.

ⁱDiaz et al.^{3,4} describe empirical and theoretical evidence from them and other authors demonstrating that their statistical model is essentially a model of clearance when the log of steady-state drug plasma concentrations is used as the dependent variable and the drug follows linear pharmacokinetics.