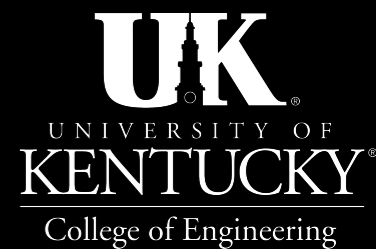


Overview of ablation test-cases

Dr. Alexandre Martin (U. of Kentucky)
Dr. Jean Lachaud (UC Santa Cruz/NASA Ames)
Mr. Tom van Eekelen (LMS-Siemens)
Dr. Ioana Cozmuta (Space Portal/NASA Ames)
Dr. Michael Wright (NASA Ames)
Dr. Nagi Mansour (NASA Ames)
Dr. Daniele Bianchi (U. of Roma "La Sapienza")



- Motivation
 - Why did we start this? -> pure curiosity
 - How do codes compare? – if same model.
 - How do models compare? – if different physics implemented.
- Goal
 - propose problems of increasing complexity until it is agreed that the most-elaborated well-defined problem is formulated
- Method to design a test case
 - census on problems of interest
 - census on code capabilities
 - draft a proposition of test case (necessarily a compromise)
 - iterate with the community until the test-case definition is clear and complete
- We try our best to propose **SOFT** test-cases
 - Simple, Open, Focused, Trouble-free

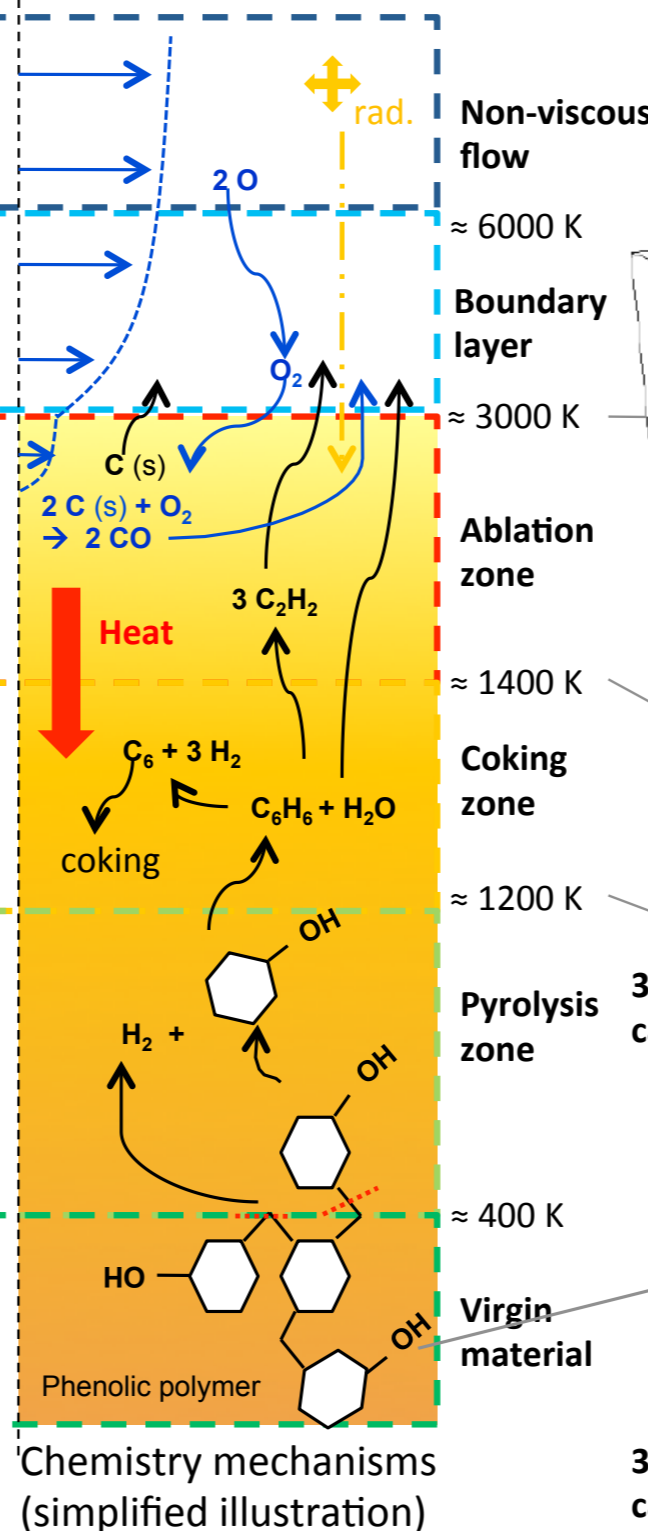
- 0 – TACOT: Theoretical Ablative Composite for Open Testing created from literature data. It is a low-density carbon/phenolic.
- 1st test-case (2011) : 15 participants / 25 codes in the open literature. Mostly a simple heat transfer problem chosen for its simplicity
- 2nd test-case series (2012) – progress: convective boundary condition & recession
 - 2.1 - bridge between 1st and 2.2 (non-physical but useful for code developers)
 - 2.2 - 1D state-of-the art design level – low heat-flux
 - 2.3 - 1D state-of-the art design level – high heat-flux
 - 2.4 - Comparison of methods to compute recession rates (e.g. B' tables)
- 3rd test-case series:
 - Initial version (2012): 5th Ablation Workshop, Lexington, KY
 - First complete version (2013): Gordon Research Conference, Ventura, CA

Macroscopic phenomenology

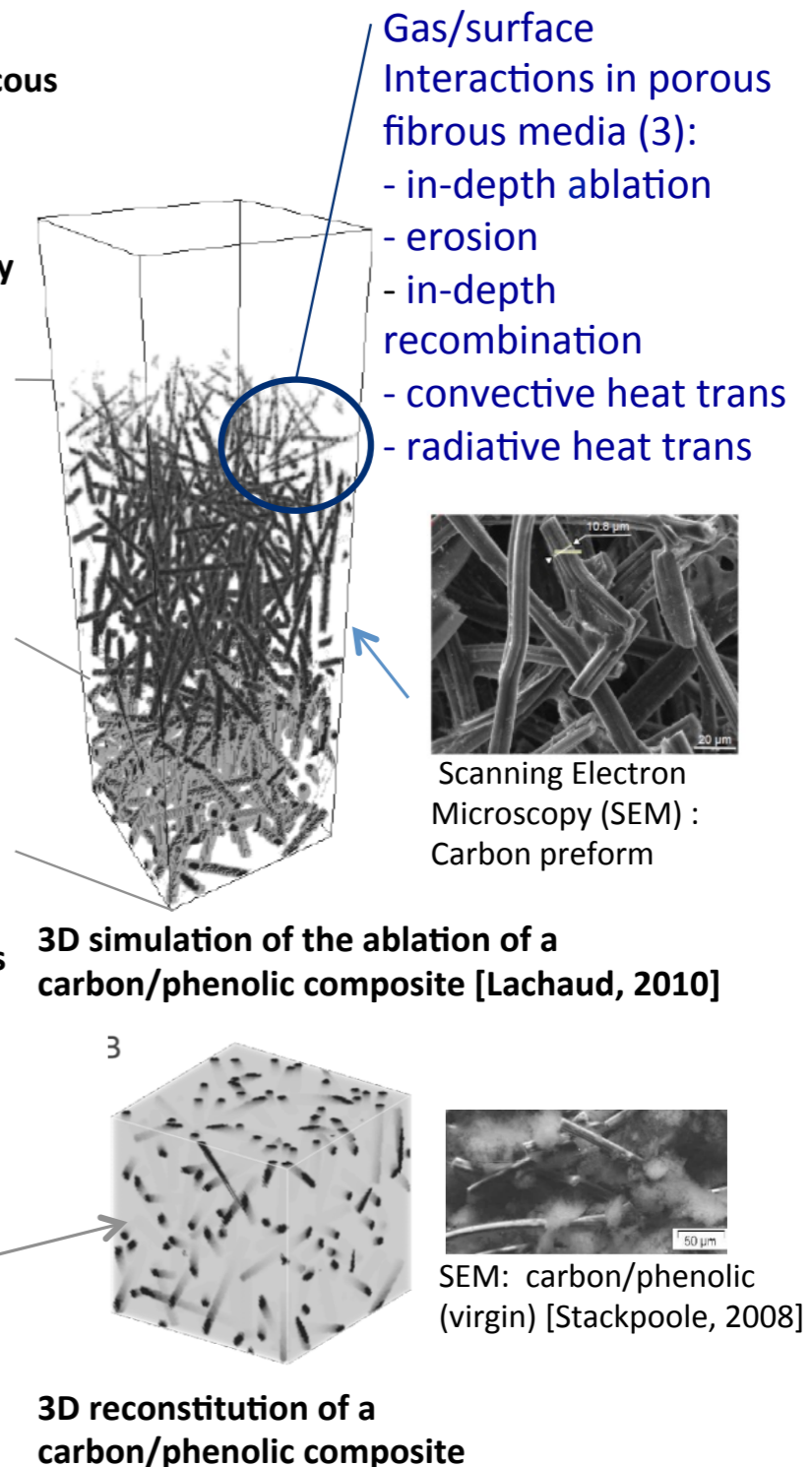
- Long distance effects
 - Radiation
- Material/flow coupling
 - Boundary layer transfers (heat and mass)
 - Recombination/catalicity
 - Ablation (oxidation, sublimation, spallation)
- Interface phenomena: Heat and mass balance (1), Subsurface phenomena
 - In-depth ablation (3)
 - Penetration of radiation (3)
 - Gas flow entering into the material (3)
- Conduction heat transfer (1)
 - Radiation heat transfer (empirical: 1, modeled: 3)
 - Finite-rate chemistry of the pyrolysis gases (3)
 - Coking (3)
- Multi-component diffusion (3)
 - Convective transport (Darcy: 2, Klinkenberg: 3)
 - Charring process (evolution of the density: 1, porosity: 2, tortuosity: 3, permeability: 2, effective conductivity: 1, effective surface area: 3)
- Phenolic-decomposition product (3)
 - Phenolic-decomposition rate (1)

1 : in all material response models (type 1)
 2 : in SOA material response models (type 2)
 3 : in future material response models (type 3)

Macroscopic illustration



Microscopic illustration



Gas species mass conservation

$$\underbrace{\partial_t(\epsilon_g \rho_g y_i)}_{\text{gas content}} + \underbrace{\partial_{\mathbf{x}} \cdot (\epsilon_g \rho_g y_i \mathbf{v}_g)}_{\text{convective flux}} + \underbrace{\partial_{\mathbf{x}} \cdot \mathcal{F}_i}_{\text{diffusive flux}} = \underbrace{\pi_i M_i}_{\text{heterogeneous reaction source}} + \underbrace{\epsilon_g \omega_i M_i}_{\text{homogeneous reaction source}}$$

Solid species mass conservation

$$\underbrace{\partial_t(\epsilon_s \rho_s)}_{\text{solid content}} = \underbrace{\partial_t(\epsilon_m \rho_m)}_{\text{resin}} + \underbrace{\partial_t(\epsilon_f \rho_f)}_{\text{fibers}} = -\Pi + \sum_{i \in s} \underbrace{\epsilon_g \omega_i M_i}_{\text{heterogeneous reaction source}} + \sum_{i \in s} \underbrace{\tau_i M_i}_{\text{fiber erosion}}$$

coking

Momentum conservation

$$\mathbf{v}_g = -\frac{1}{\epsilon_g \mu} \frac{1 + \beta/p}{1 + Fo} \underline{\underline{\mathbf{K}}} \cdot \partial_{\mathbf{x}} p$$

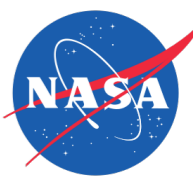
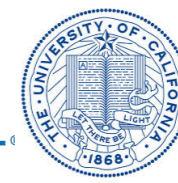
- Darcy's Law
- Forchheimer correction
- Klinkenberg correction

Energy conservation

$$\underbrace{\partial_t \rho_a e_a}_{\text{energy content}} + \underbrace{\partial_{\mathbf{x}} \cdot (\epsilon_g \rho_g h_g \mathbf{v}_g)}_{\text{convective flux}} + \underbrace{\partial_{\mathbf{x}} \cdot \sum_{i=1}^{N_g} (h_i \mathcal{F}_i)}_{\text{diffusive flux}} = \underbrace{\partial_{\mathbf{x}} \cdot (\underline{\underline{\mathbf{k}}} \cdot \partial_{\mathbf{x}} T)}_{\text{conductive flux}} + \underbrace{\mu \epsilon_g^2 (\underline{\underline{\mathbf{K}}}^{-1} \cdot \mathbf{v}) \cdot \mathbf{v}}_{\text{viscous flux}}$$

$$\rho_a e_a = \epsilon_g \rho_g e_g + \epsilon_m \rho_m h_m + \epsilon_f \rho_f h_f$$

Current Codes



Name	Contact	Owner	Users	Applications
Amaryllis	T. van Eekelen	LMS Samtech, Belgium	EADS Astrium, ESA	Design
CAMAC	W.-S. Lin	CSIST, Taiwan	Taiwan Ins. of Sci. Tech.	Unknown
CAT	N. N. Mansour	NASA ARC, USA	NASA ARC	Analysis
CHALEUR	B. Blackwell	SNL, USA	SNL	Design
CHAP	P. Keller	Boeing, USA	Boeing	Design
CHAR	A. Amar	NASA JSC, USA	NASA	Analysis
CMA	R. Beck	Aerotherm, USA	NASA, SNL	Design
CMA/SCMA	C. Park	Tokyo Univ., Japan	JAXA	Design
CMA/KCMA	P. Reynier	ISA, France	ISA/ESA	Analysis
FEAR	J. Dec	NASA LaRC, USA	NASA LaRC	Analysis
FABL	J. Merrifield	Fluid Grav. Eng. Ltd., UK	ISA/ESA/FGE	Analysis
FIAT	Y.-K. Chen	NASA ARC, USA	NASA, SpaceX	Design
3DFIAT	Y.-K. Chen	NASA ARC, USA	NASA ARC	Analysis
HERO	M. E. Ewing	ATK, USA	ATK	Analysis
ITARC	M. E. Ewing	ATK, USA	ATK	Design
libAblation	R. R. Upadhyay	Univ. of Tex. Aust., USA	UTA	Analysis
MIG	S. Roy	Univ. of Flo., USA	Univ. of Florida	Analysis
MOPAR	A. Martin	Univ. of Mich., USA	UKY/Univ. of Michigan	Analysis
NEQAP	J. B. Scoggins	N. Carol. St. Univ., USA	NCSU	Analysis
NIDA	G. C. Cheng	Univ. Alab. Birm., USA	UAB	Analysis
PATO	J. Lachaud	NASA ARC, USA	Univ. Calif. Santa Cruz	Analysis
STAB	B. Remark	NASA JSC, USA	NASA, FGE	Design
TITAN	F. S. Milos	NASA ARC, USA	NASA	Analysis
TMU	A. R. Bahramian	T. Modares Univ., Iran	TMU	Analysis
US3D	G. Candler	Univ. of Minn., USA	UM	Analysis

Name	Numerical method	Spatial accuracy	Temporal accuracy
Amaryllis[22]	Finite-Element	First-order	First order
CAMAC[23]	Unknown	Unknown	Unknown
CAT[24]	Implicit Finite Volume	Second-order	Second-order
CHALEUR[25]	Control Volume Finite-Element	Second-order	First-order
CHAP[26]	Implicit Finite-Difference	First-order	Second-order
CHAR[27]	Galerkin Finite Element	Second-order	Second-order
CMA[28]	Implicit Finite-Difference	First-order ²	First-order
CMA/SCMA[29]	Implicit Finite-Difference	Second-order	First-order
CMA/KCMA[30]	Implicit Finite-Difference	Second-order	First-order
FABL[32]			
FIAT[20]	Implicit Finite-Volume	First-order	First-order
3DFIAT[33]	Implicit Finite-Volume	First-order	First-order
FEAR[31]	Galerkin Finite Element	Second-order ¹	Second-order ¹
HERO[34]	Finite-Element	Second order	First order ³
ITARC[34]	Control Volume	Up to 3rd-order ¹	First order
libAblation[35]	Newton on analy. eq.	First-order in space	No time integration
MIG[36]	Discrete Galerkin	Up to 4th-order	3rd-order
MOPAR[37]	Control Volume Finite-Element	Second-order	First-order
NEQAP[38]	Implicit Finite-Difference	Second order	Second order
NIDA[39]	Finite-Difference	Second order	Unknown
PATO [40]	Implicit Finite-Volume	First-order ¹	First-order ¹
STAB[41]	Implicit Finite-Difference	Second-order	First-order
TITAN[42]	Implicit Finite-Volume	First-order	First-order
TMU[43]	Explicit Finite-Difference	First-order	Unknown
US3D[44]	Implicit Finite-Volume	Second-order	First-order

Codes Capabilities

Code capabilities	A	C	C	C	C	C	C	C	C	F	F	3	H	I	L	M	M	N	N	P	S	T	T	U
Green : verified and available	M	A	A	H	H	M	M	M	O	D	D	B	F	R	I	M	M	N	N	P	S	T	T	U
Yellow : under verification, not in the official version/ release	R	A	T	A	A	A	A	A	D	E	E	L	A	R	B	O	P	Q	D	A	A	A	A	D
Red : in development	Y	C	L	L	P	S	K	-	-	J	L	A	A	C	A	A	A	A	O	B	T	A	N	M
	L		E	E				S	C	A	R	T			B	R	P							O
	I		U	U					C						L									D
	S		R	R											A									M
Summary																								
Model fidelity (1-3)	2	1	3	2	1	1	2	1	2	1	2	1	1	2	2	1	2	2	3	3	1	1	1	1
Code dimensionality (nD= 1-3)	3	1	1	1	1	1	1	1	3	1	1	1	3	3	1	1	1	1	1	3	1	2	1	1
Code maturity level (1-3)	3	1	2	3	3	3	3	2	2	2	2	3	2	2	3	1	1	2	1	1	2	3	2	2
Gas-phase Mass Conservation	In-depth : Eq. 1																							
Storage ($\partial_t \dots$)	Red	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Divergence ($\partial_x \dots$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Pyrolysis production (Π)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Pyrolysis model	In-depth: Eq. 2-7																							
SoA Arrhenius laws ($\rightarrow \Pi$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Species production ($\rightarrow \pi_i$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Gas-species Conservation	In-depth: Eq. 8																							
Storage ($\partial_t \dots$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Divergence ($\partial_x \dots$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Multi-component diffusion ($\partial_x F$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Finite-rate chemistry (π_i, ω_i)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Solid-phase mass conservation	In-depth: Eq. 9-10																							
Pyrolyzing matrix mass loss	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
In-depth ablation/coking	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Momentum conservation	In-depth: Eq. 11																							
Darcy's law	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Klinkenberg	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Forchheimer	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Energy conservation	In-depth: Eq. 12-13																							
Storage ($\partial_t \dots$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Divergence ($\partial_x \dots$)	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Effective conduction	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Viscous dissipation	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Boundary conditions	At the wall: Eq. 14-22																							
Surface energy balance	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Wall chemistry from B' table	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Internal wall chemistry solver	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Other utilities	Integrated libraries																							
Equilibrium chemistry solver	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Integrated boundary layer code	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green
Script-coupling to CFD code	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green