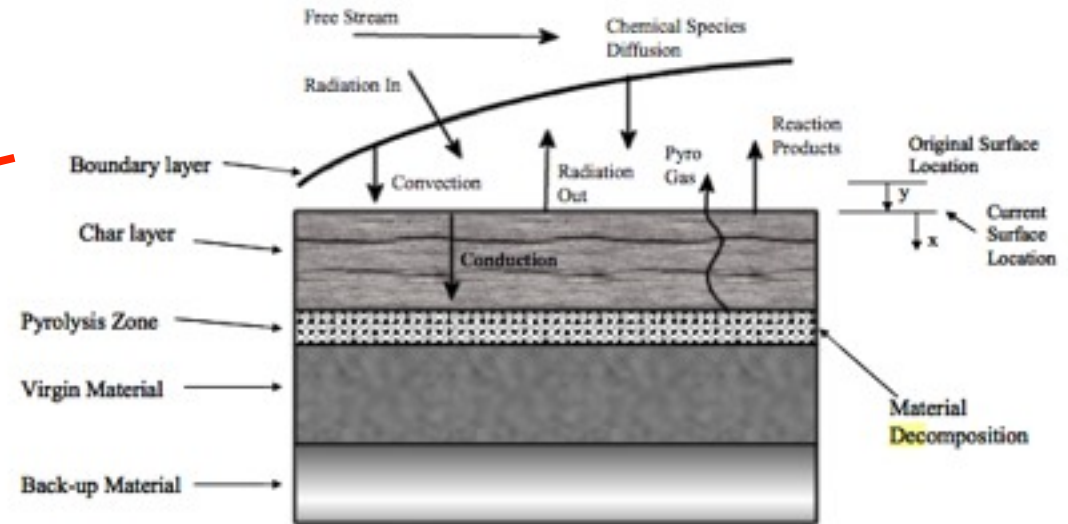

Microscale Modeling of Ablative Thermal Protection System Materials

Eric Stern, Graham Candler, Tom Schwartzentruber,
Ioannis Nompelis, Michael Barnhardt





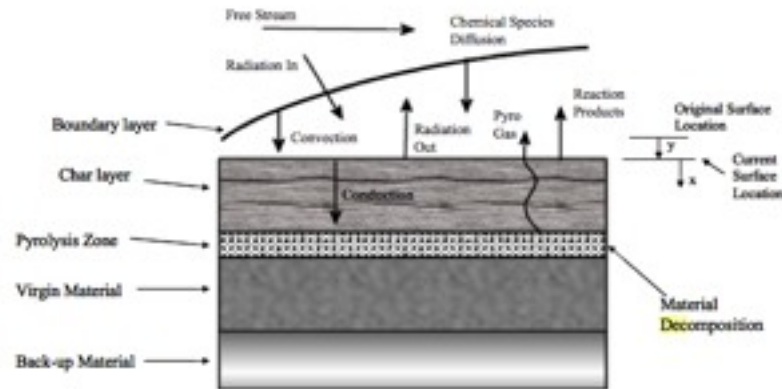
Ablation Modeling



- Engineering material response codes in use today take a macroscopic view of the TPS.
- Typically involve heavy empiricism, and many assumptions



TPS Modeling

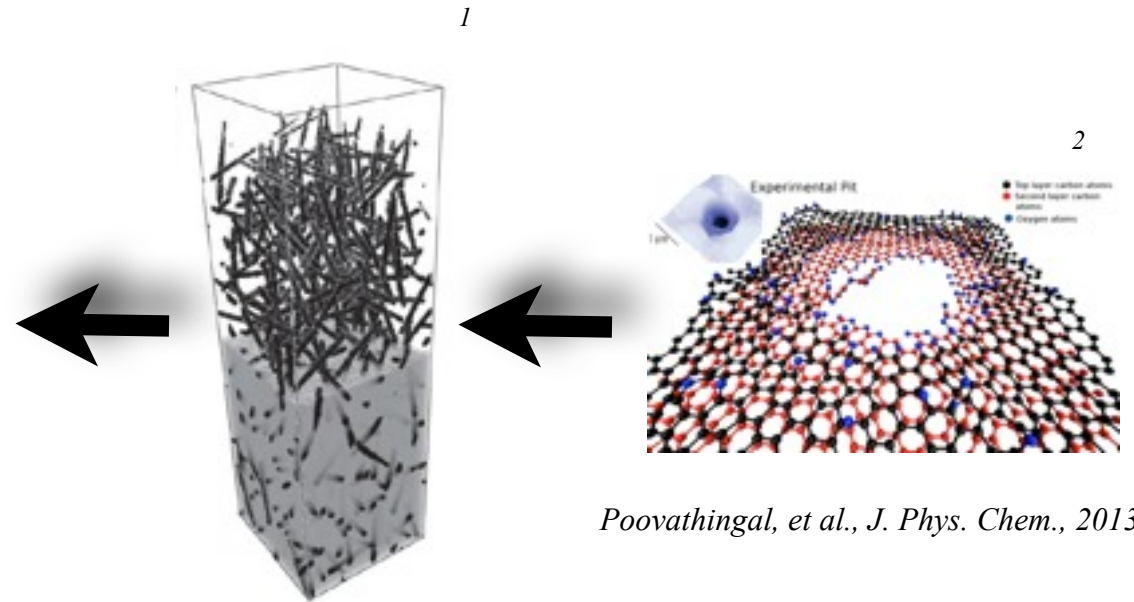
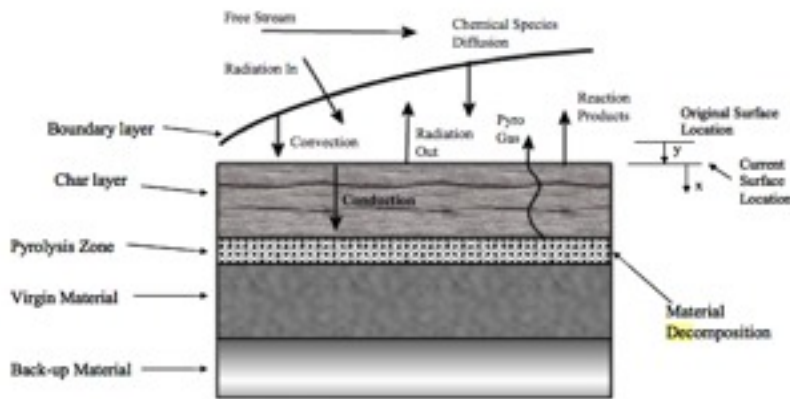


Lachaud, et al., JSR, 2010

- **The goal of this work is to better model processes at the micro-scale to inform macro-scale models.**
 - Volume averaging.
 - Model reduction!
- **This will attempt to build and expand on previous efforts in micro-scale modeling by enabling more physics**



TPS Modeling



Poovathingal, et al., *J. Phys. Chem.*, 2013

Lachaud, et al., *JSR*, 2010

- The goal of this work is to better model processes at the micro-scale to inform macro-scale models.
- ...as well as build a framework where higher fidelity models can be incorporated from the nanoscale



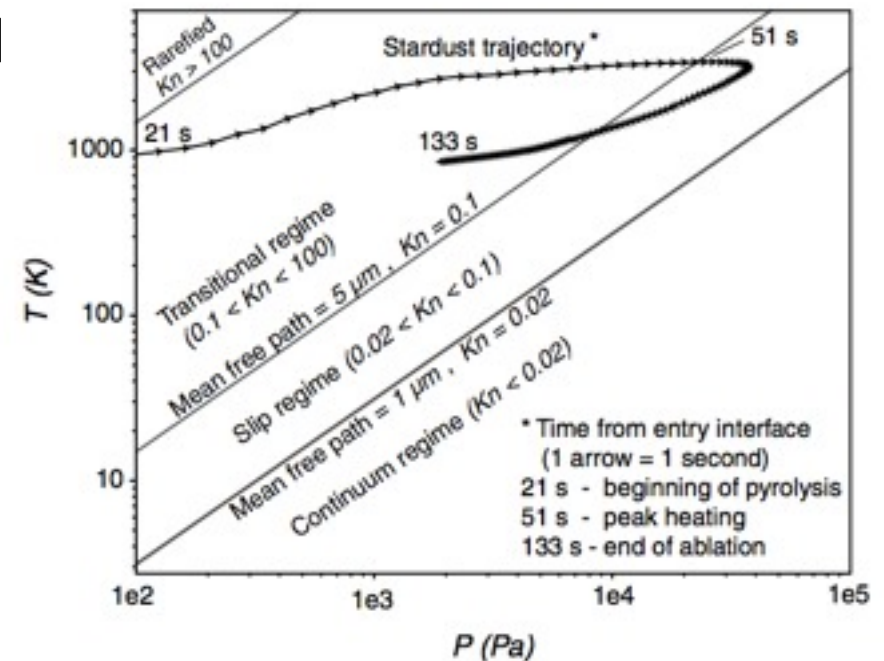
- **Methodology**
 - DSMC
 - Surface Generation and Movement
 - Coupled Ablation
- **Preliminary Validation and Applications**
 - Simplified Darcy Flow
 - Flow-tube Permeability Experiments
- **Future Work**



Why DSMC?

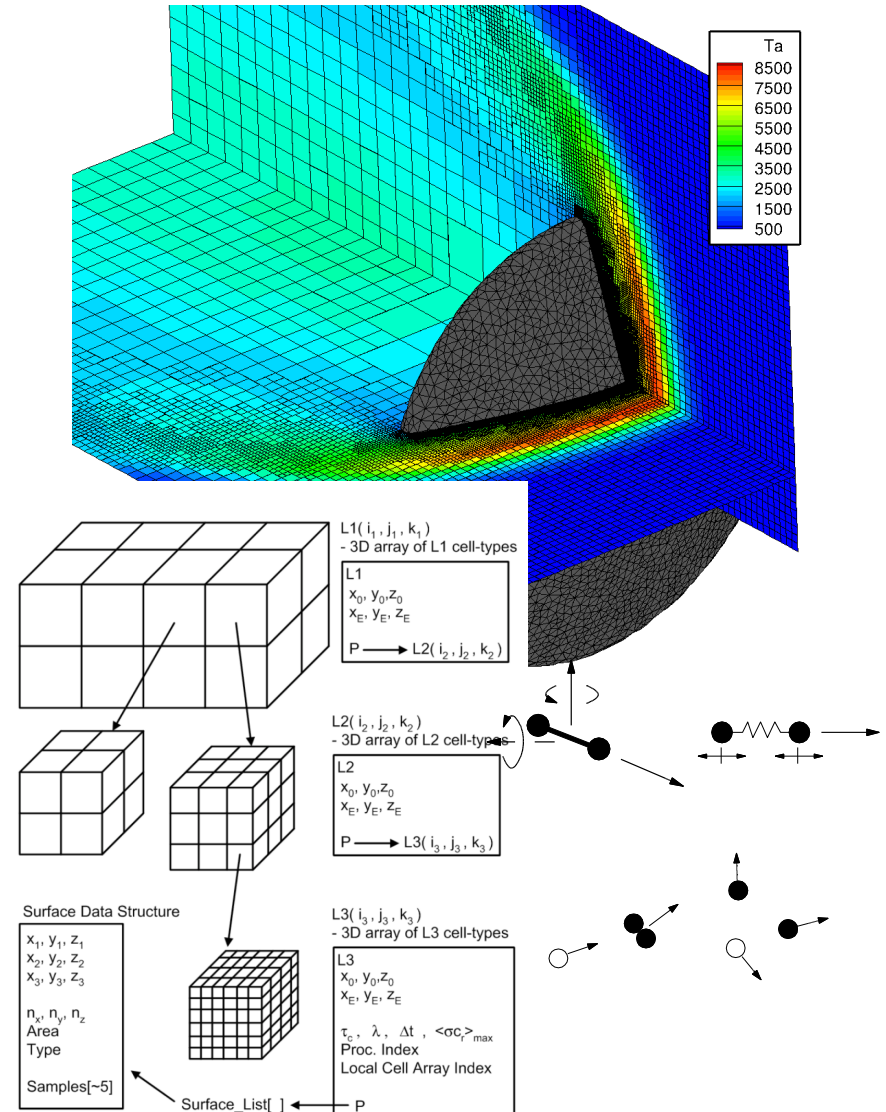


- First: what is DSMC?
- Knudsen numbers in the porous medium range from high-slip to rarefied regimes.
- DSMC can (in principle) simulate all of the relevant physics.
 - Convection
 - Multicomponent Diffusion
 - Gas-phase Kinetics
 - Sophisticated GSI Models
 - Non-equilibrium handled inherently
- DSMC can simulate arbitrarily complex geometries



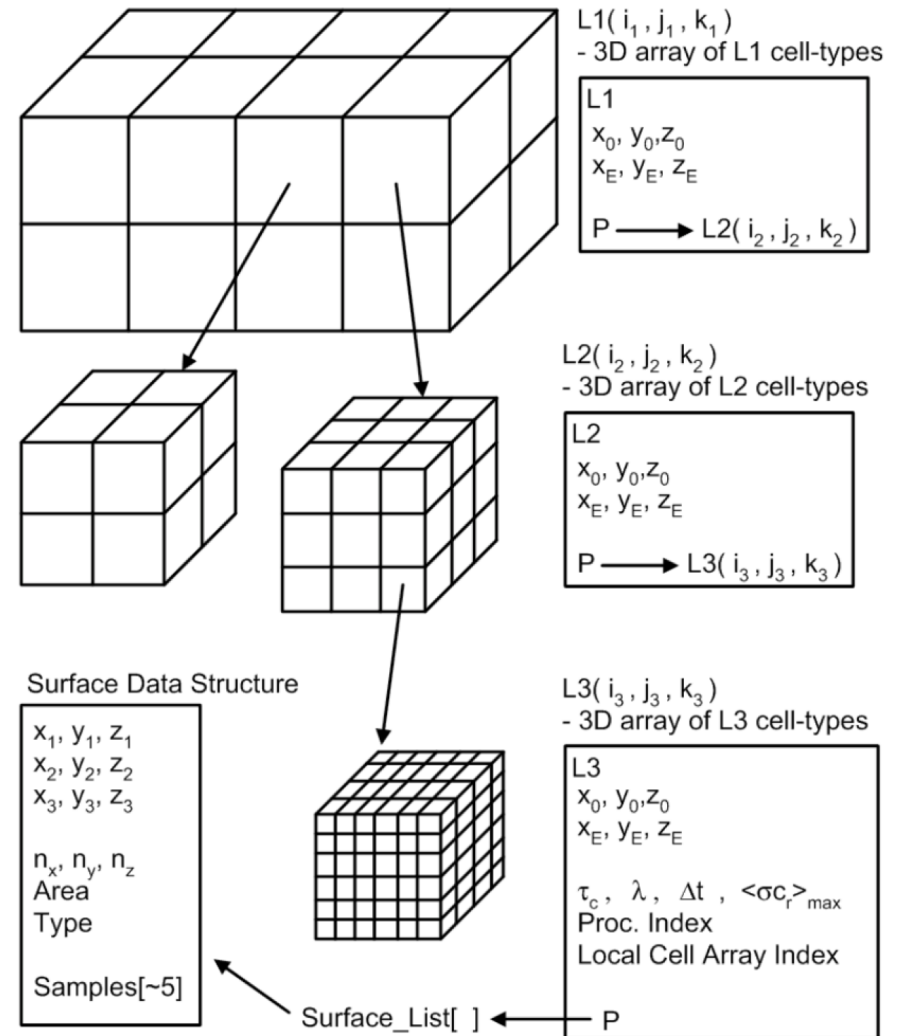
Lachaud, et al., JSR, 2010

- **Parallel implementation of the DSMC method developed at the University of Minnesota.**
 - 3-Level Cartesian Mesh
 - Automated Mesh Refinement
 - Models for dissociation, vibrational/rotational relaxation.



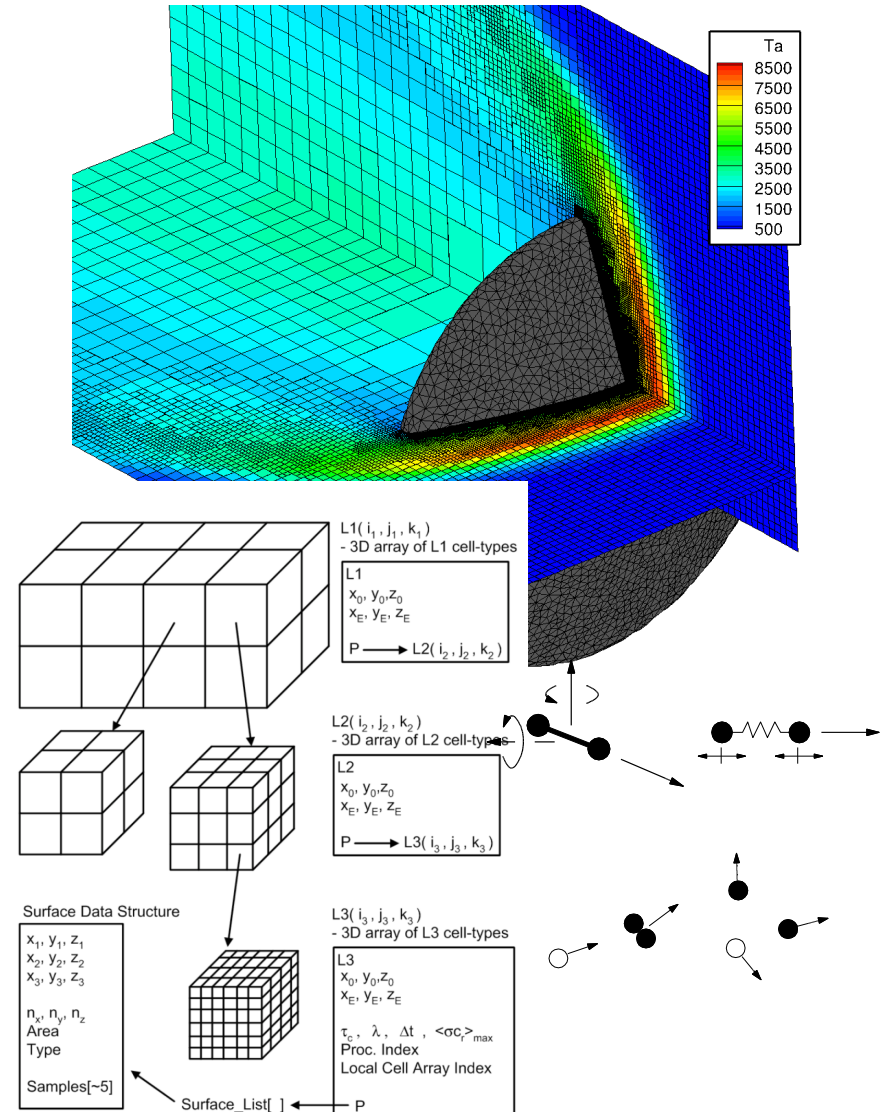
1. Zhang and Schwartzentruber, *Comp. and Fluids*, 2012
2. Nompelis and Schwartzentruber, *AIAA Paper*, 2014

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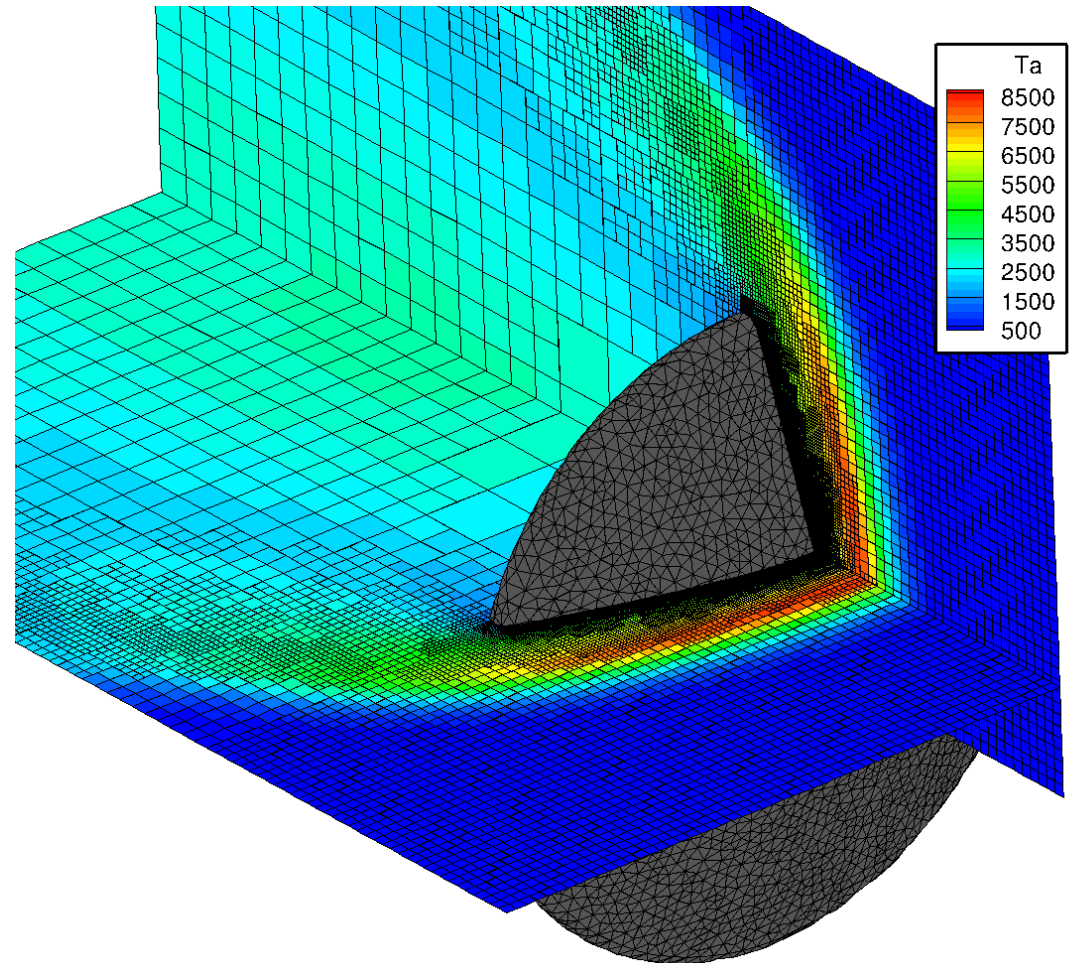
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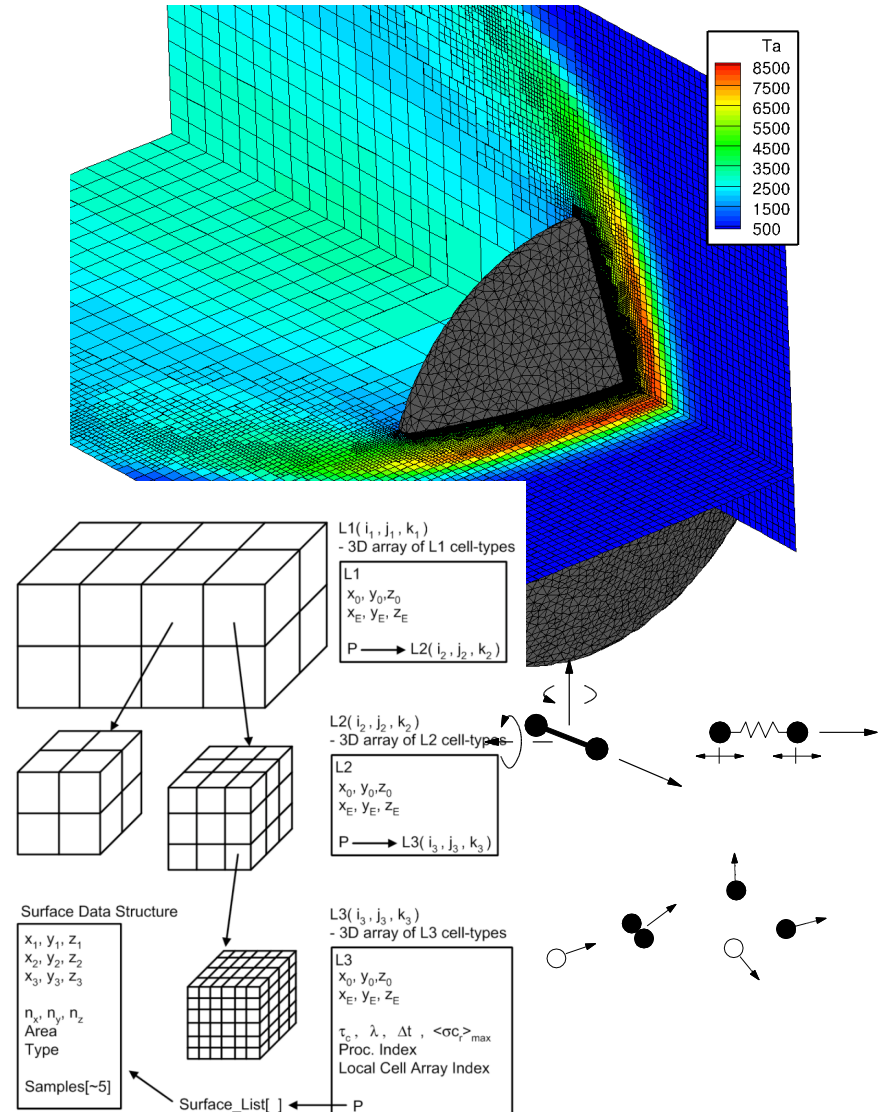
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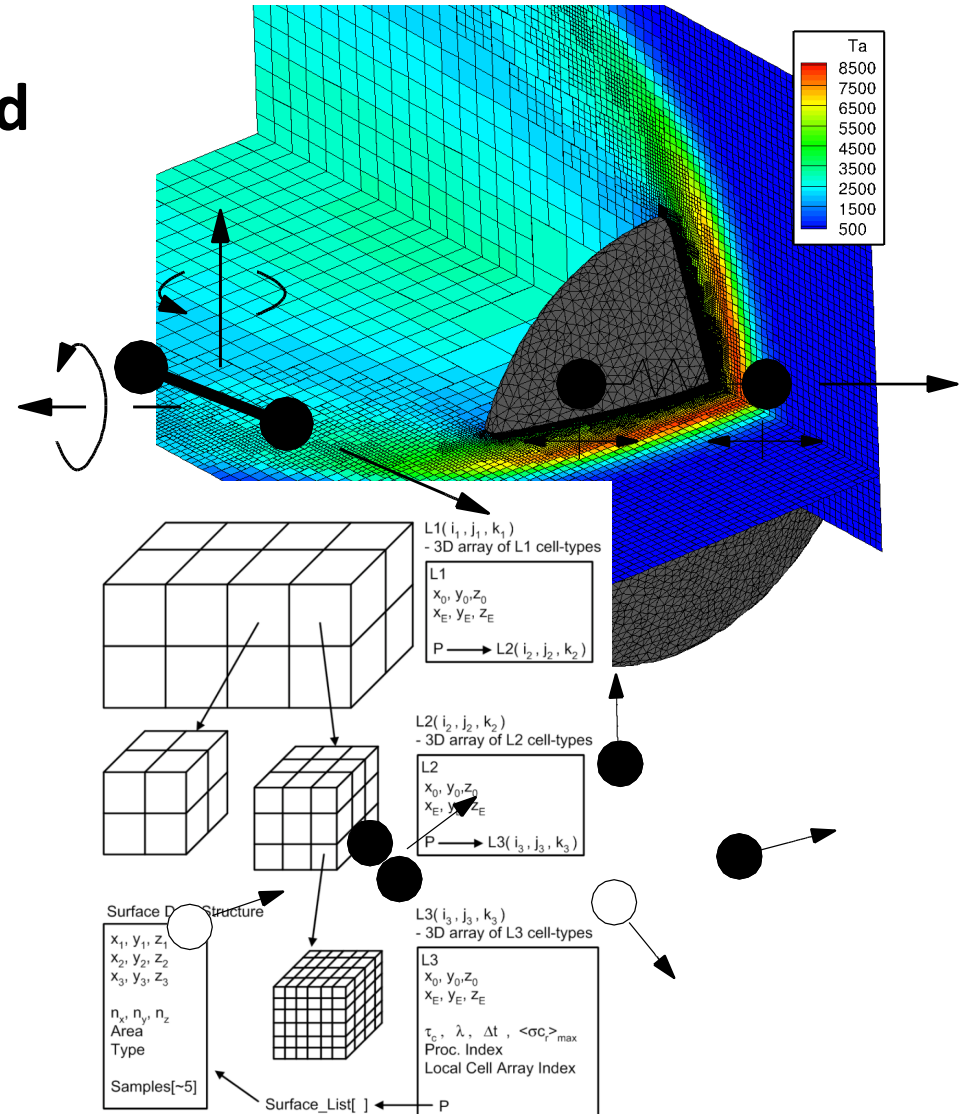
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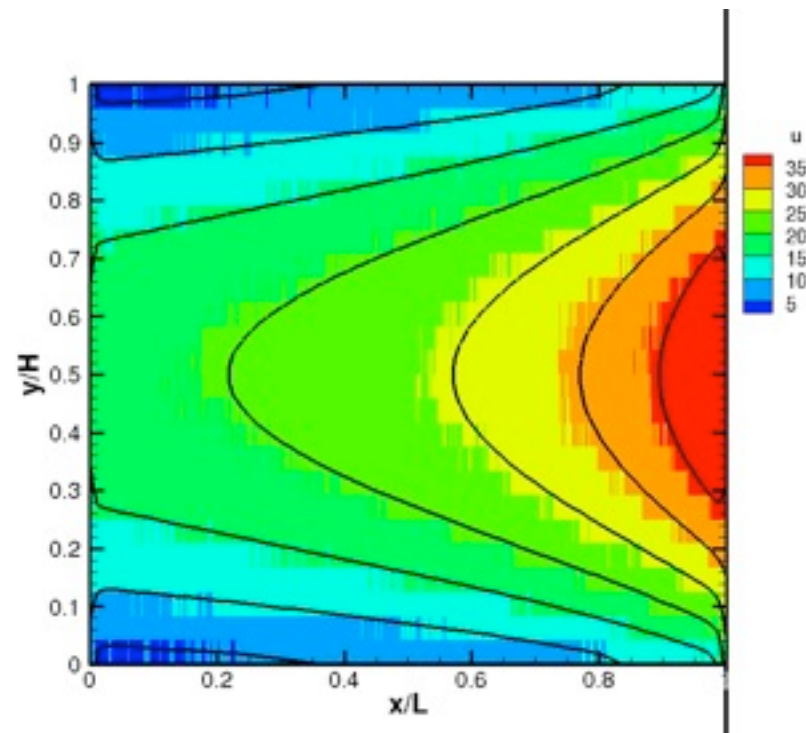
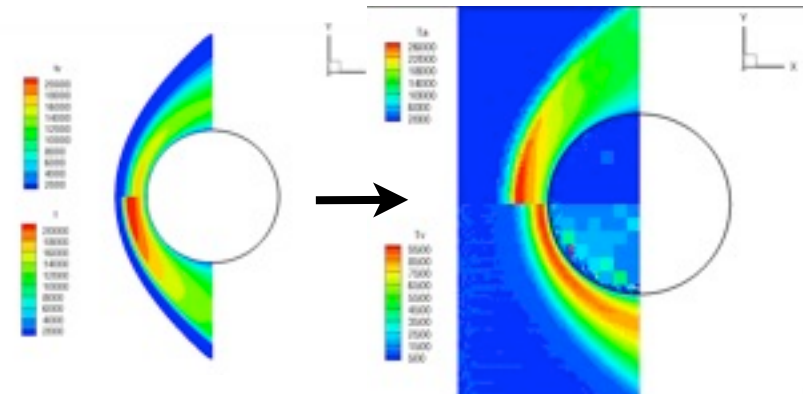
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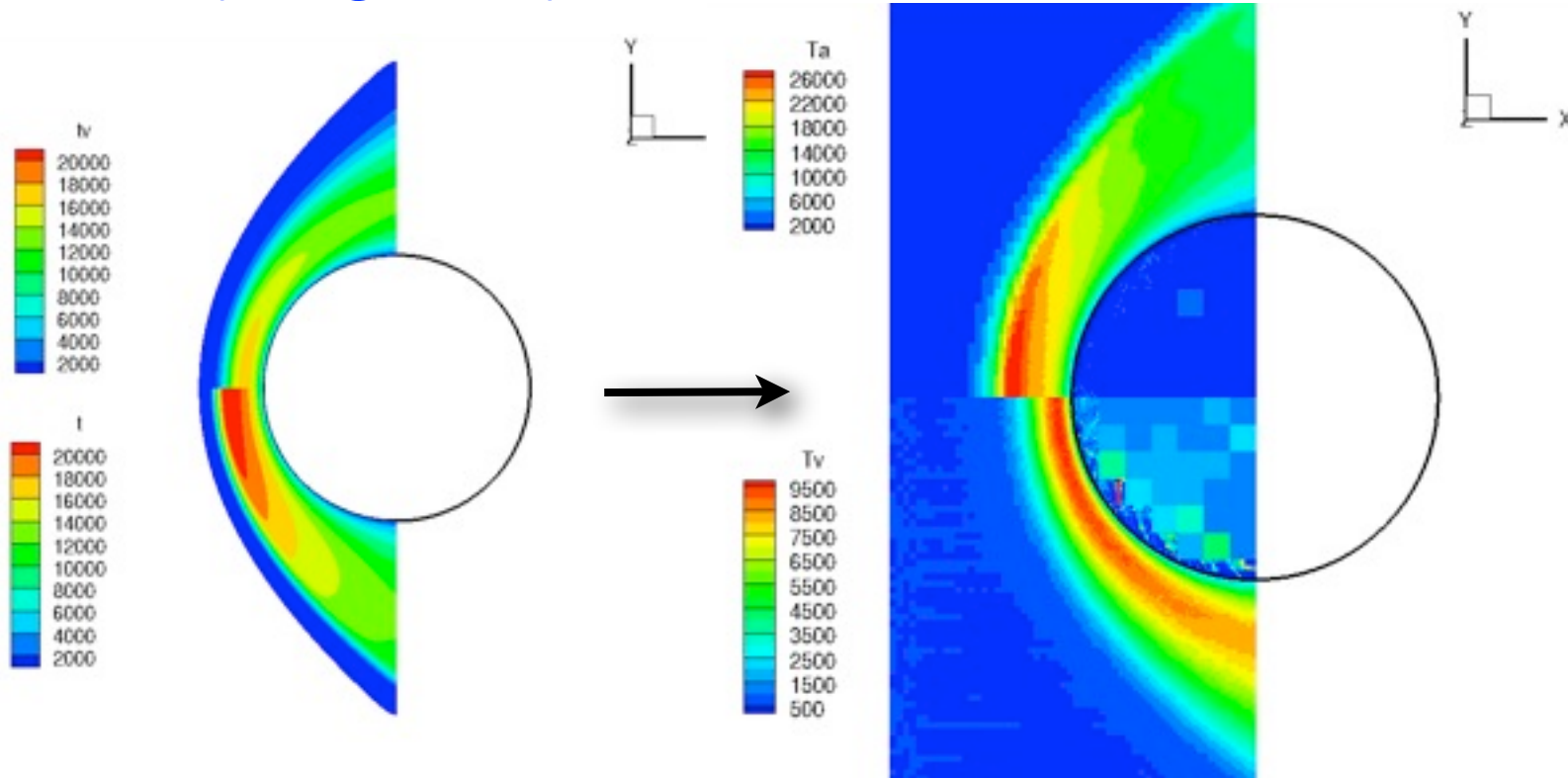
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- **Some additional features have been added to the code specifically for this work.**
 - Initialization of simulation to CFD (using US3D).
 - Subsonic Boundary Conditions
 - Simple gas-surface interaction model
 - Ablation modules

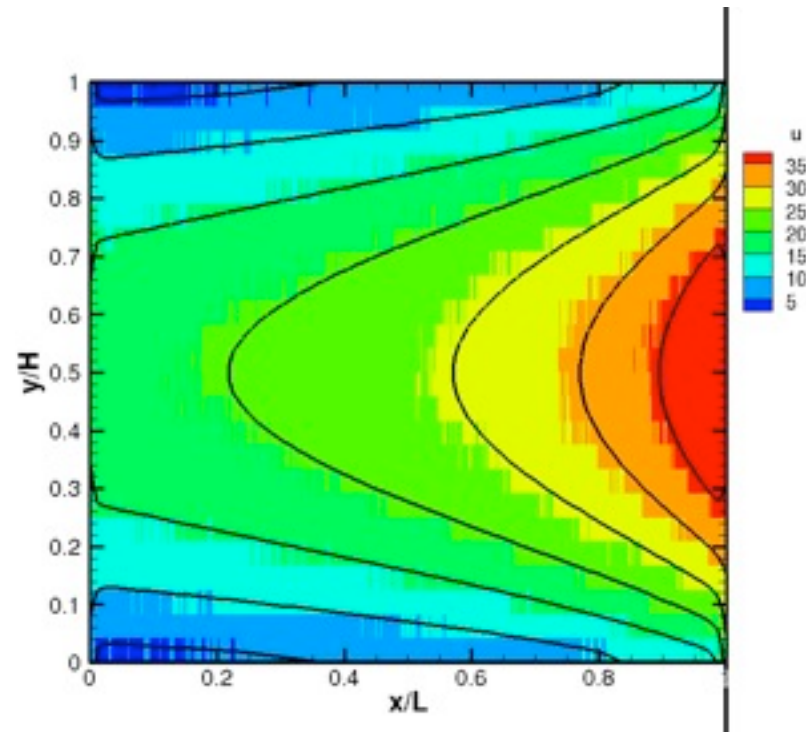
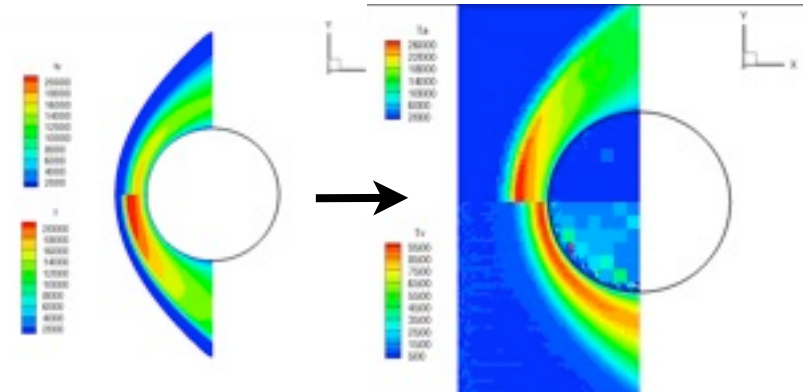




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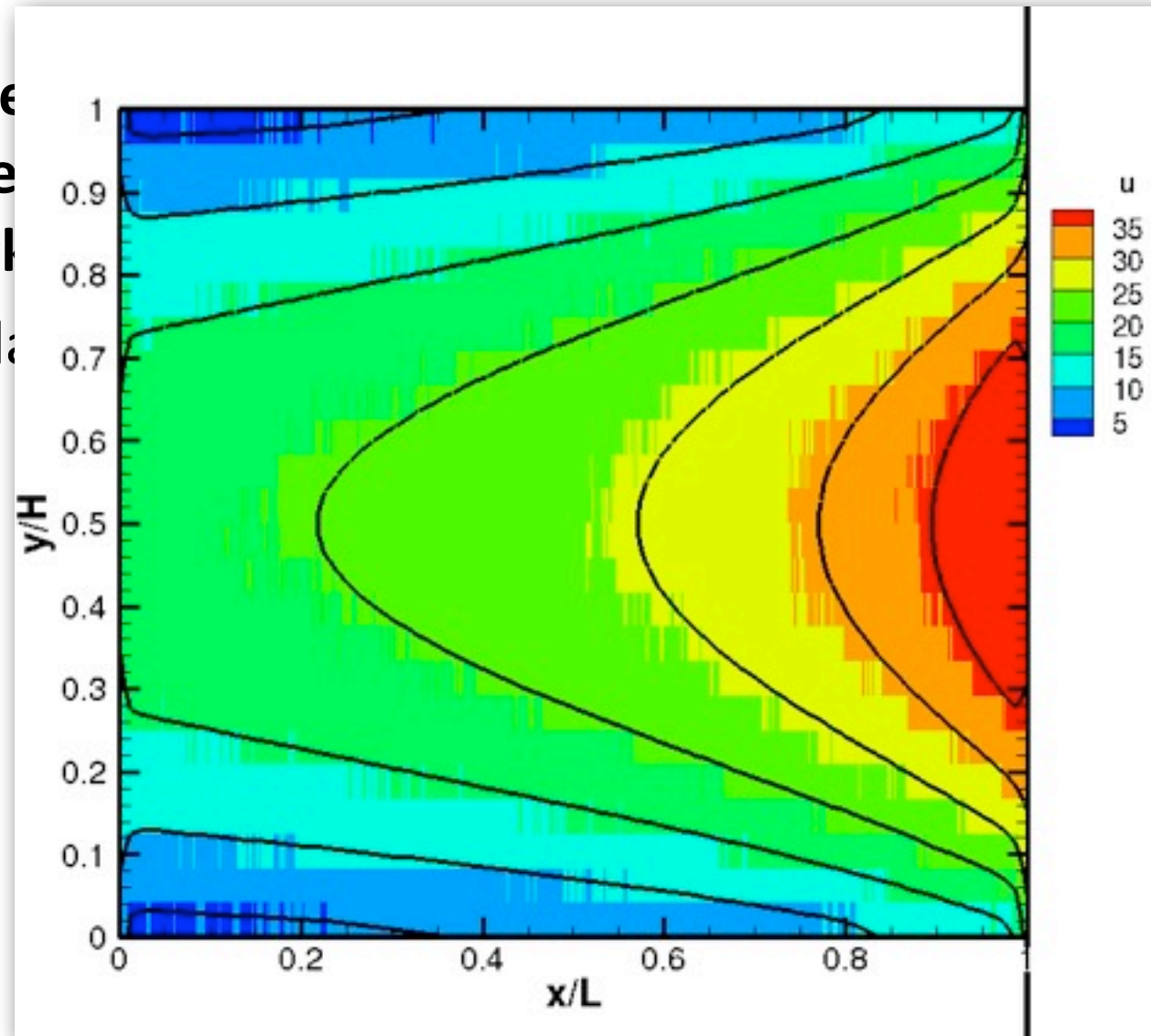


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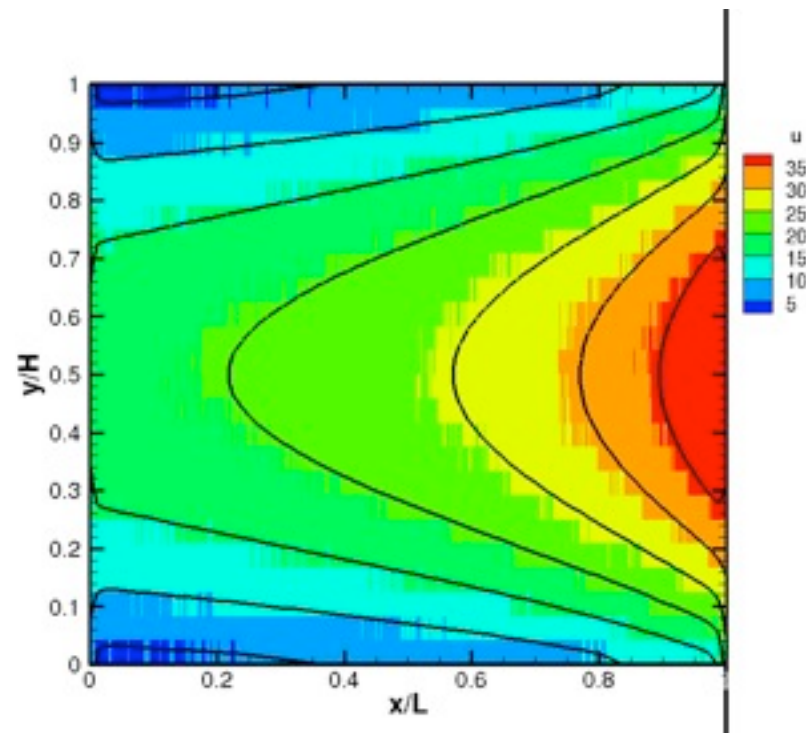
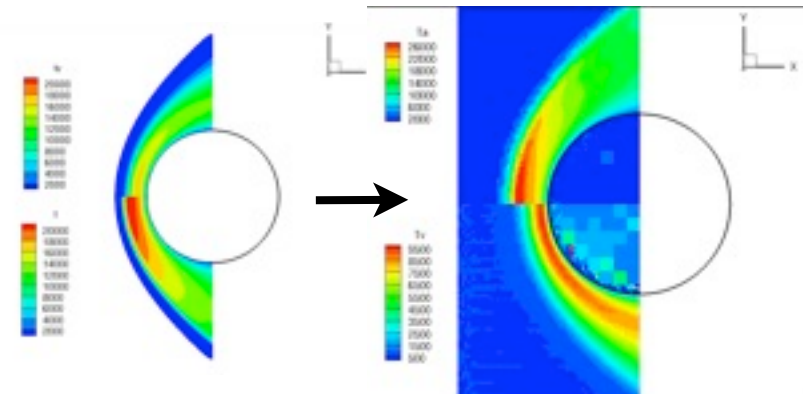




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- **Methodology**
 - DSMC
 - Surface Generation and Movement
 - Coupled Ablation
- **Preliminary Validation and Applications**
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 - Flow-tube Permeability Experiments
- **Future Work**



- **The objective is to develop a tool that is able to generate triangulated surface meshes of random arrays of “fibers” to use in microscale simulations.**
- **We have developed FiberGen with the following features:**
 - It can generate 2D and 3D, random and non-random arrays of cylindrical fibers.
 - The user specifies a box size to fill with fibers, and a target porosity.
 - The user can prescribe properties such as nominal fiber diameter, fiber length, angular biases (i.e. orthotropy), as well as variance and distribution in each.
 - Triangulated surface is output in STL format.
 - It also includes a post-processor for analyzing the geometry.



FiberGen

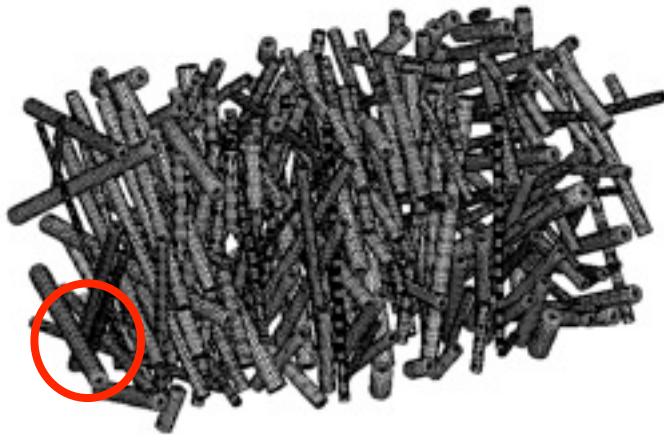
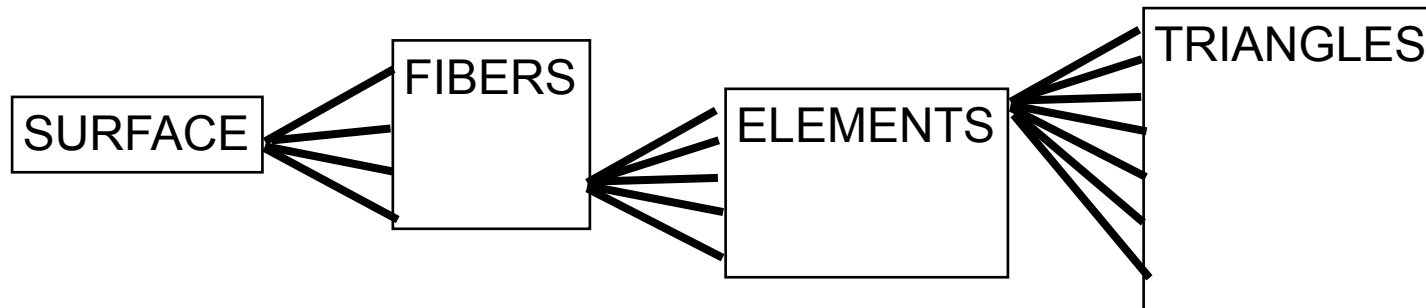


- Additionally, the code creates data structures for the mesh which are used for evolving the surface.
- Fiber data structures are written to HDF5 format for efficient I/O in massively parallel applications.

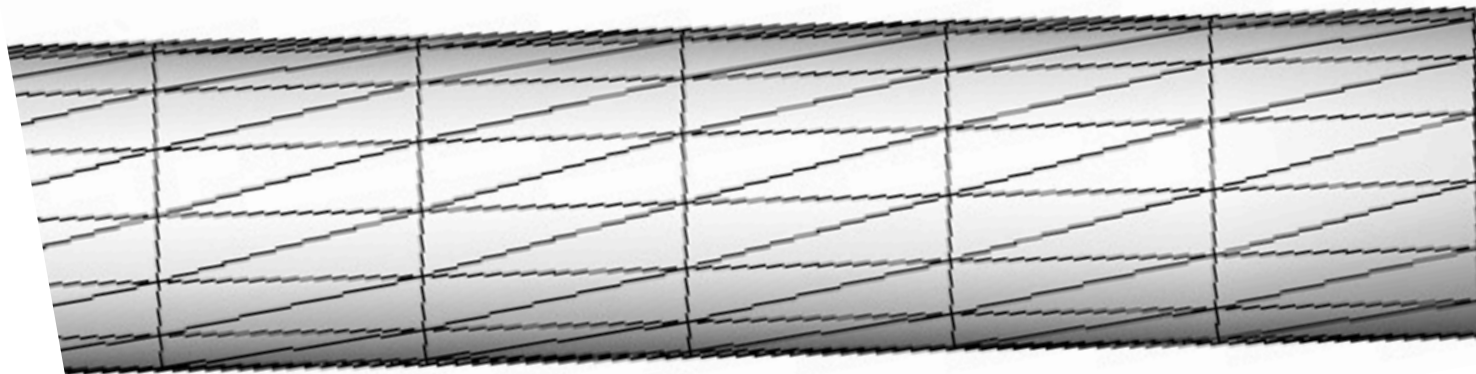
Example geometry having porosity of 0.85, and nominal fiber radius of 6 micron. The figure on the right is of the same geometry after having undergone a prescribed “ablation.”



Surface Data Structure



- The surface is composed of many *fibers*
- Each fiber is composed of discrete *elements* along the axis.
- Each element contains many *triangles* on their surface

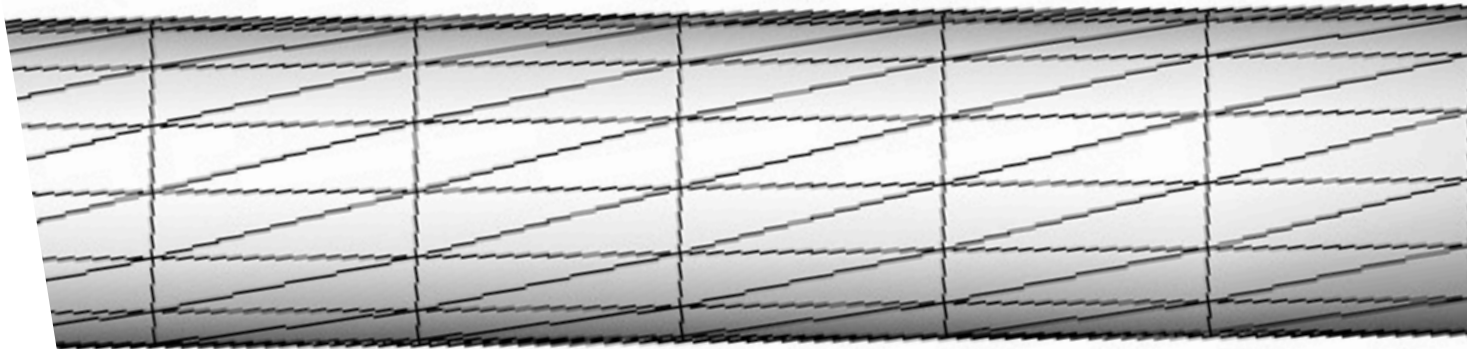




Surface Movement



- Now we would like to leverage this framework to develop an efficient method for evolving the surface under the influence of surface reactions (*ablation*)

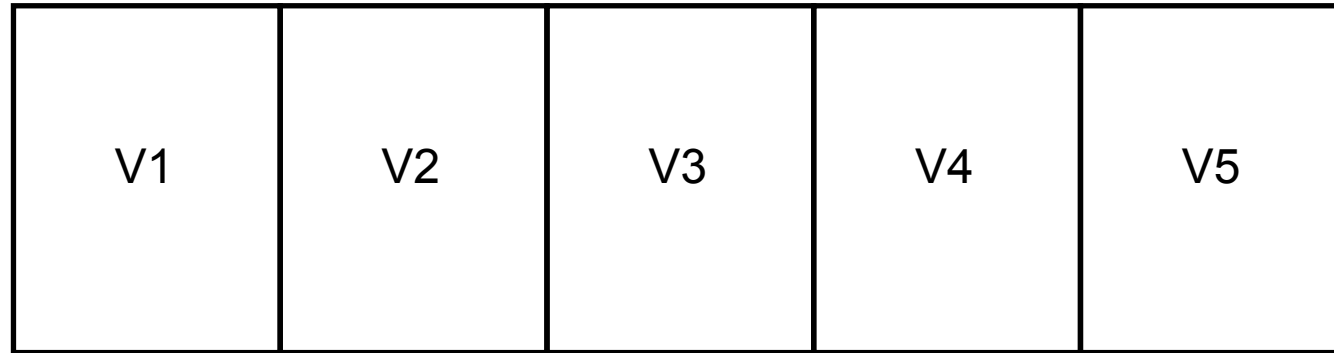


- We begin by computing and storing the volume of each *element* for each fiber.

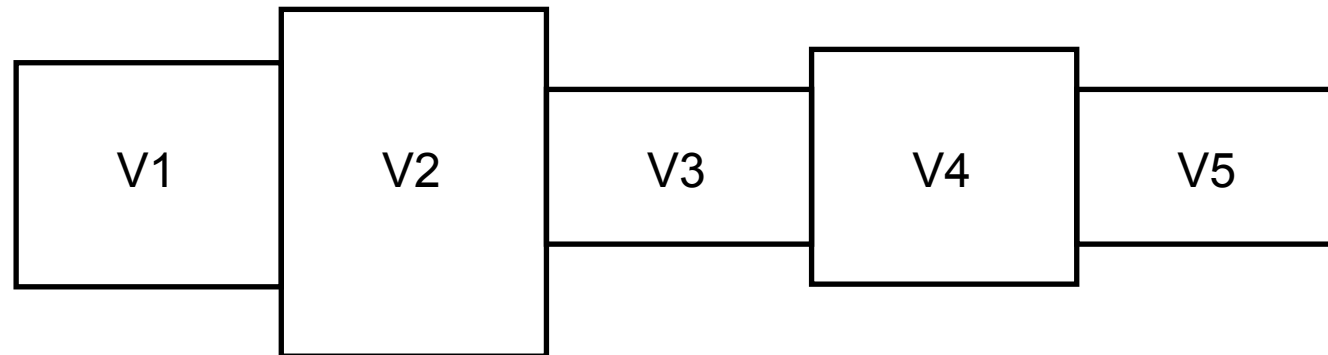
V1	V2	V3	V4	V5
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Surface Movement



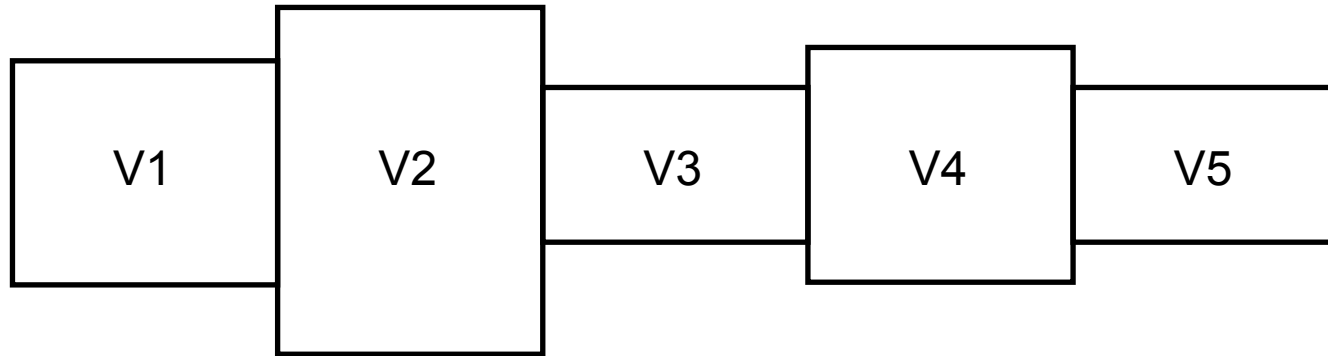
- We then update the *element* volumes as the simulation progresses, and reactions on the *triangles* remove material from the fibers.



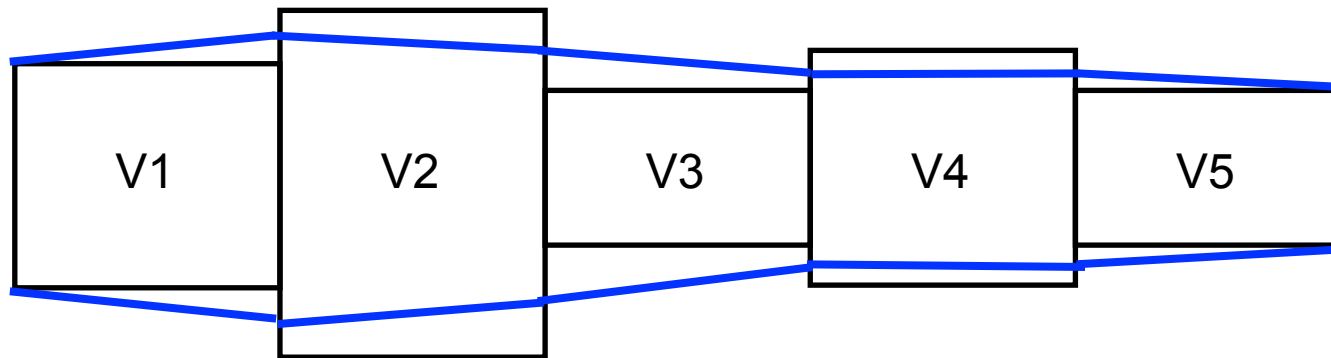
- An effective radius that yields a straight cylinder of the same volume is computed for each *element*.



Surface Movement



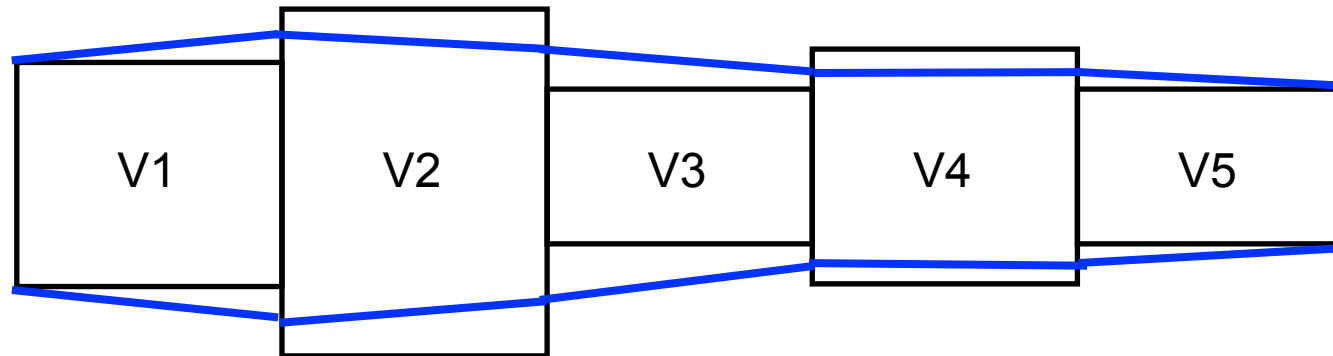
- The radius on each side of each element is then defined as the average between it and its neighbor.



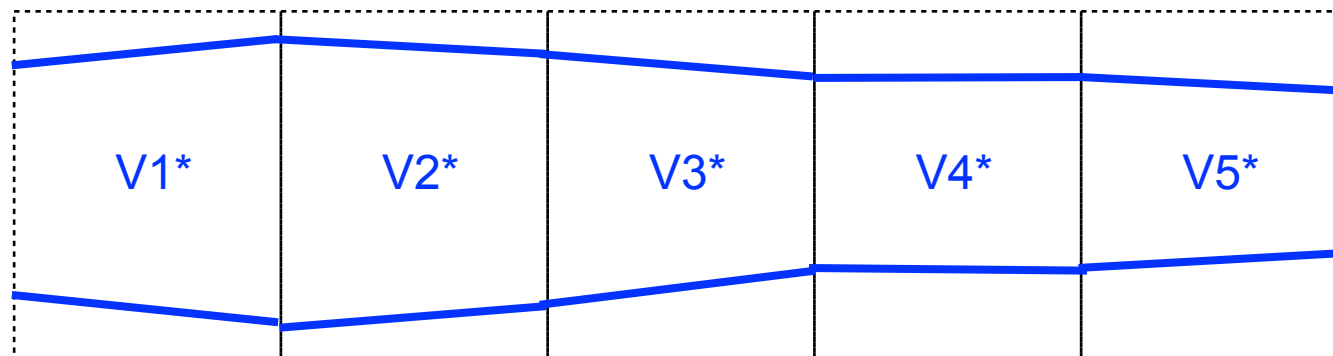
- The surface is then reconstructed from conical frustum segments.



Surface Movement



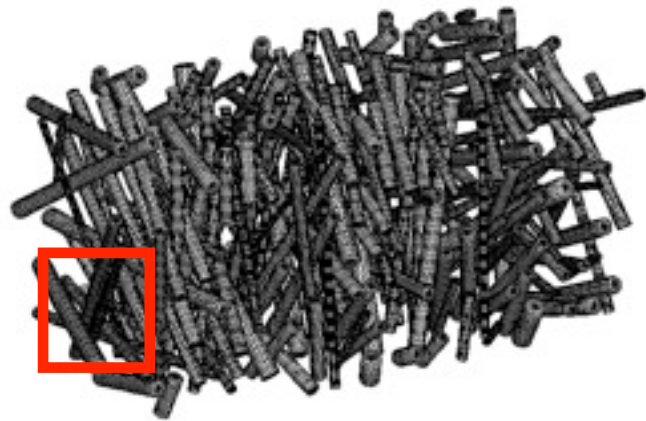
- The surface is then reconstructed from conical frustum segments.



- Note: there is error in the volume of the reconstruction, however we always track and operate on the *actual* volume, so mass is conserved.

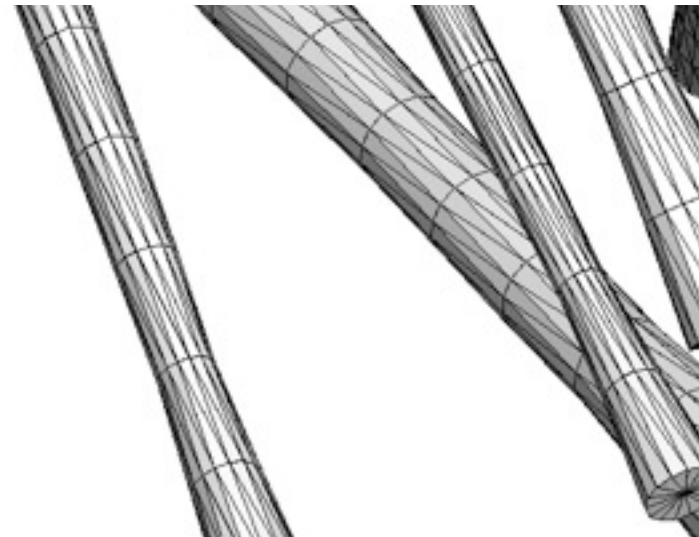
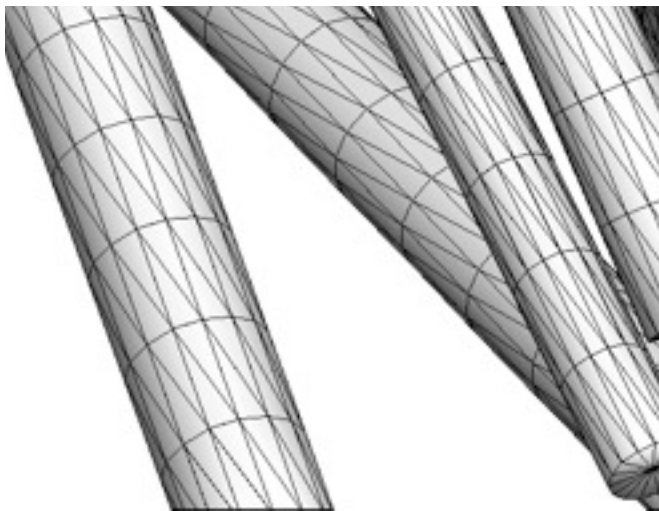


Surface Movement



This treatment is able to replicate some of the dominant morphologies we observe at the micro-scale.

- non-uniform thinning
- "needling"





Surface Movement



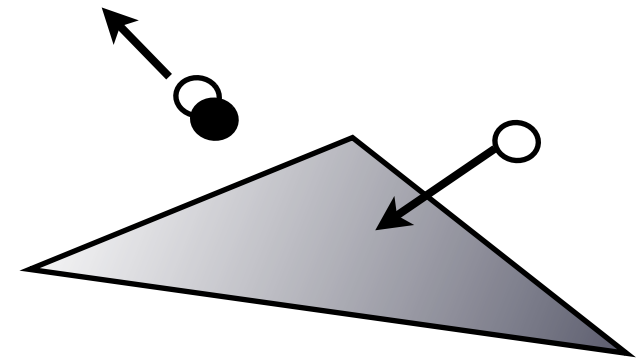
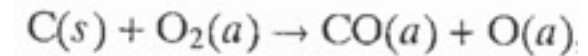
- This reconstruction method could be thought of as a **Axisymmetric Volume of Fluid (VoF) approach**.
- **Benefits:**
 - Relatively easy to implement
 - Error in volume is small and bounded for our work (<1%)
 - Extending code to modeling fiber material response would be (fairly) straightforward (i.e. solving the heat conduction equation is quasi-1D).
 - Surface reconstruction is *very* fast
- **Limitations:**
 - Limited to axisymmetric shapes
 - Not easily extensible to tomography-generated surfaces



- **Methodology**
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- **Conclusions**



- In DSMC, the gas surface interaction is modeled by determining the probability that a gas particle will react if it strikes a surface
- For our current analysis, we use a temperature dependent probability for carbon oxidation given by Park.
- Devising more sophisticated treatments for the GSI is an active area of research.

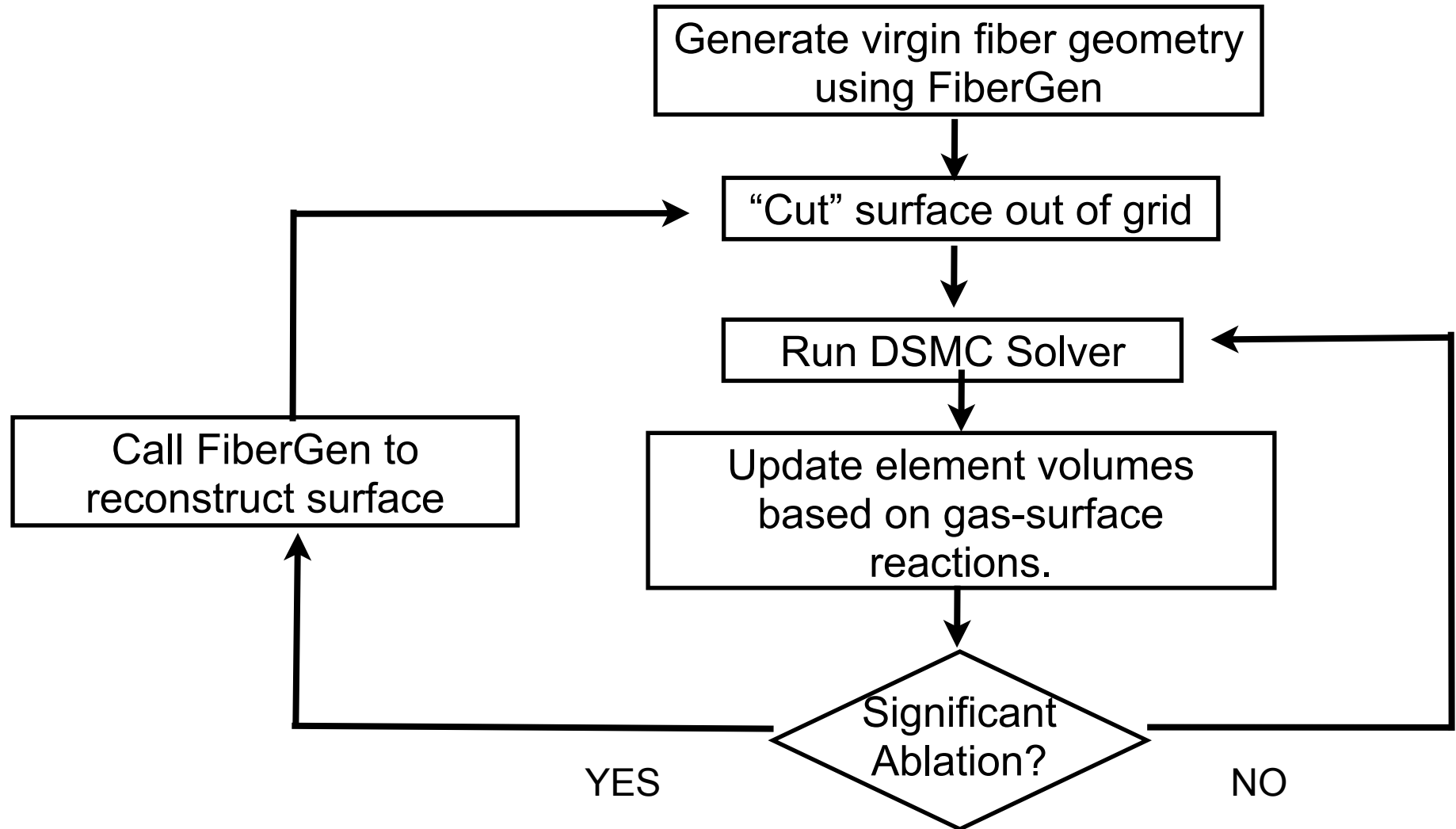


$$\alpha = \frac{1.43 \times 10^{-3} + 0.01 \exp(-1450/T)}{1 + 2 \times 10^{-4} \exp(13,000/T)}$$

Park, Nonequilibrium Hypersonic Aerothermodynamics, 1991



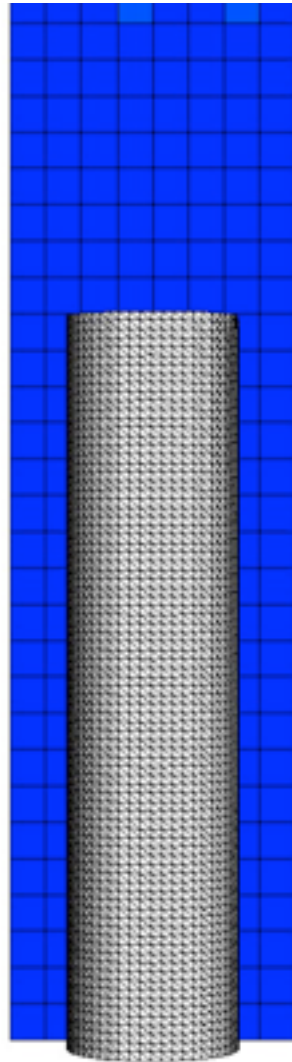
Coupled Ablation



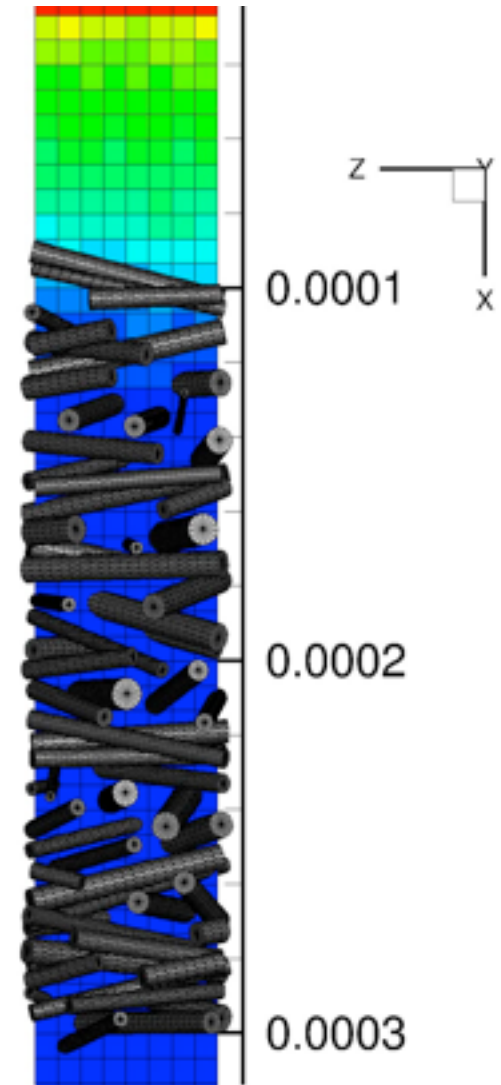
- We have found (so far) that the surface update is generally very fast, therefore we update fairly frequently since there is little to no penalty



Movies



Ablation of a single fiber



Ablation of a porous geometry



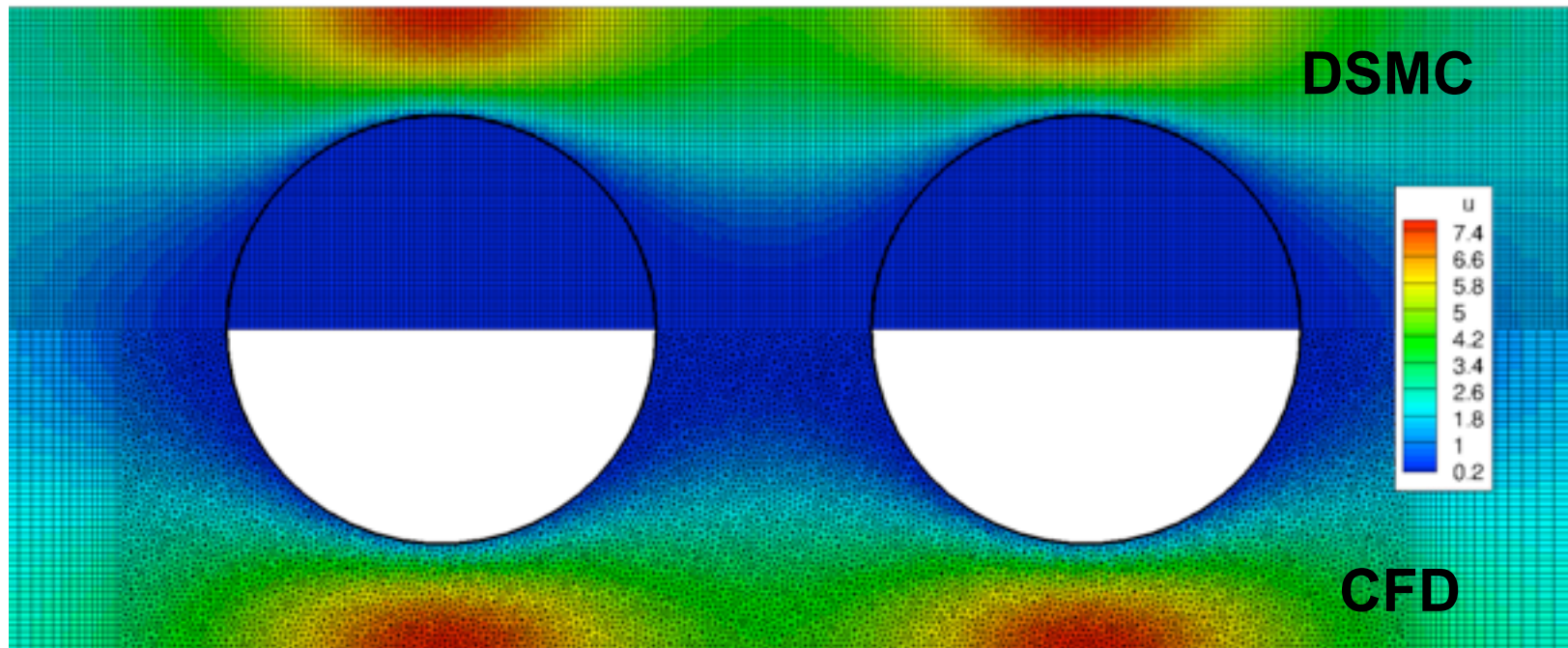
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Simple Darcy Flow



- To begin, we seek to validate the approach for simple Stoke's flow through idealized porous medium.
 - We compare to both CFD, and models (analytical and empirical) in the literature
 - CFD augmented with Maxwell slip model



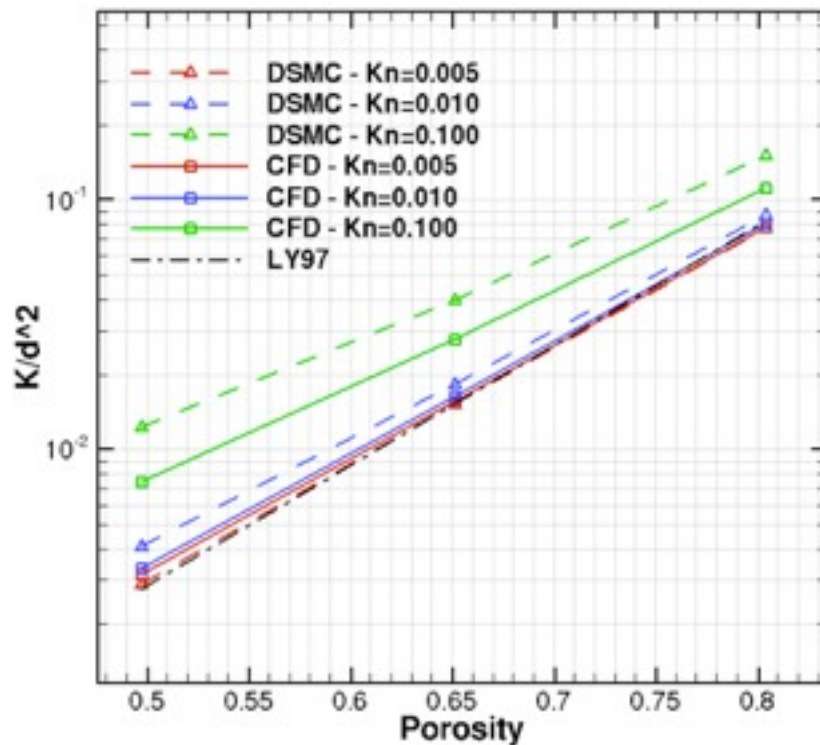


Simple Darcy Flow

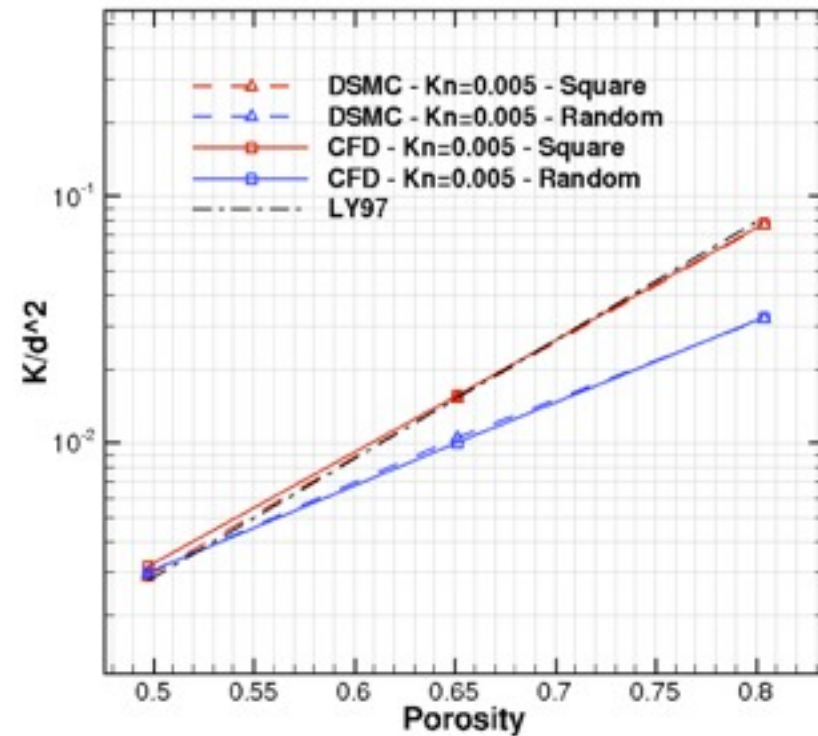


- Results show good agreement with literature.
- ...as well as intuitive departures due to Knudsen number effects, as well as microstructure changes

$$\frac{\partial p}{\partial x} = -\frac{\mu}{K} v'_g$$



Regular Array of Cylinders



Random Array of Cylinders

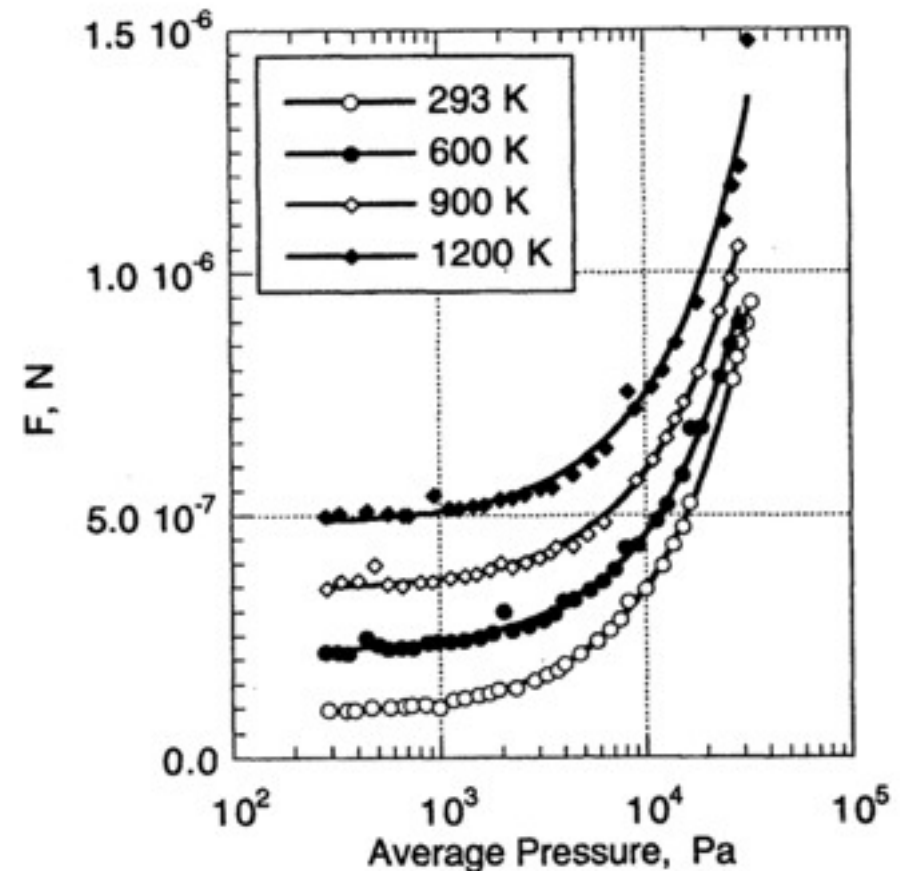


FiberForm Permeability



- Now we want to look at more relevant geometries and conditions.
- Flow-tube experiments performed at NASA Ames.
- Experimental data well-fit by Klinkenberg form of Darcy equation.
- Material permeability tested at various pressures and temperatures
- Significant variation in permeability observed due to rarefied effects.

$$F = \frac{4\mu\dot{m}RTL}{\pi D^2 M \Delta P} = K_0(P_{av} + b)$$



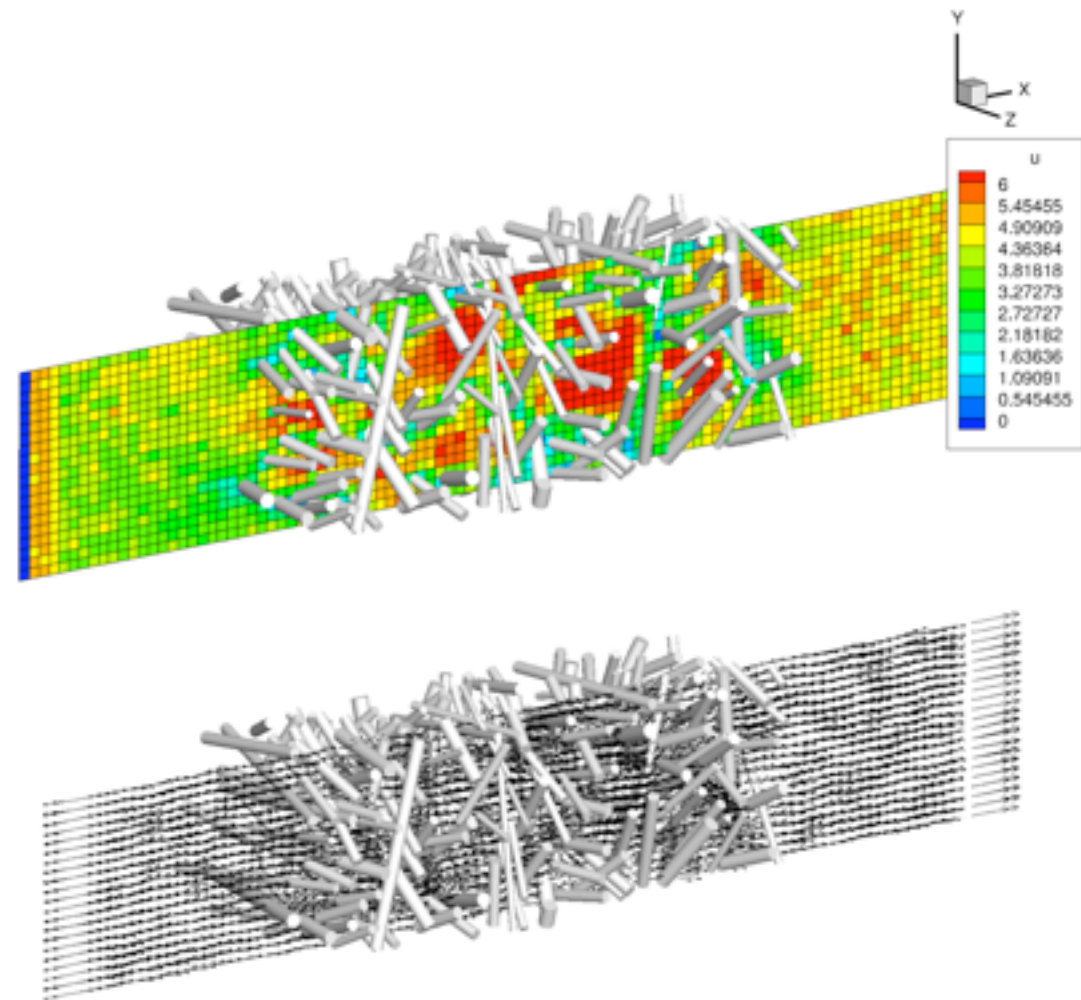
Marschall and Milos, JTHT, 1998



Preliminary Results



- Simulations were performed near the low end of the pressure range ($\sim 1kPa$) of the experiments.
- Gas used was N2 at room temperature.
- Size of volume was 200x50x50 microns with a porosity of ~ 0.85
- Two nominal fiber radii were used
 - 6 micron (*single fiber*)
 - 10 micron (*fiber bundle*)
- Several fiber orientations were simulated

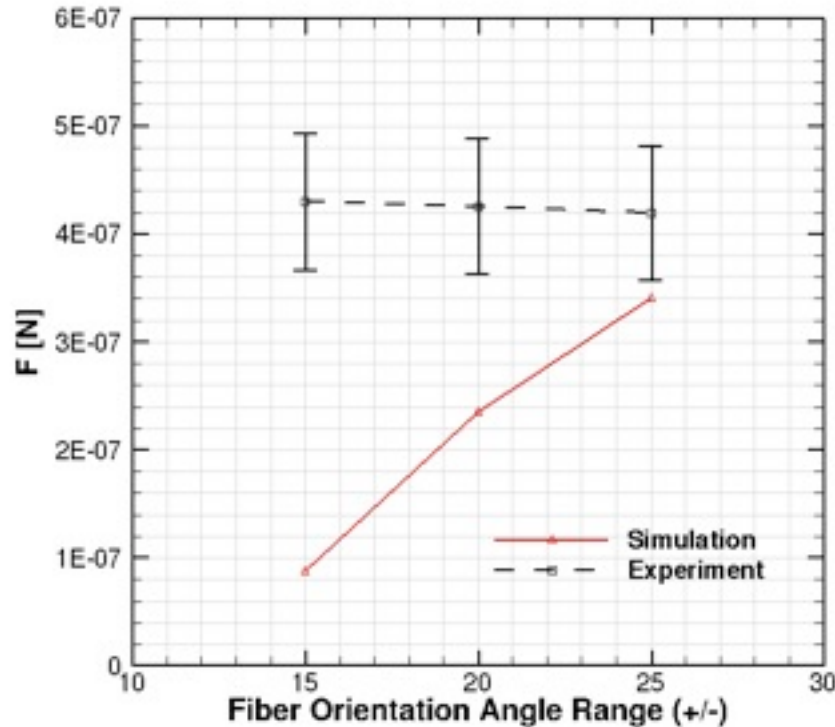




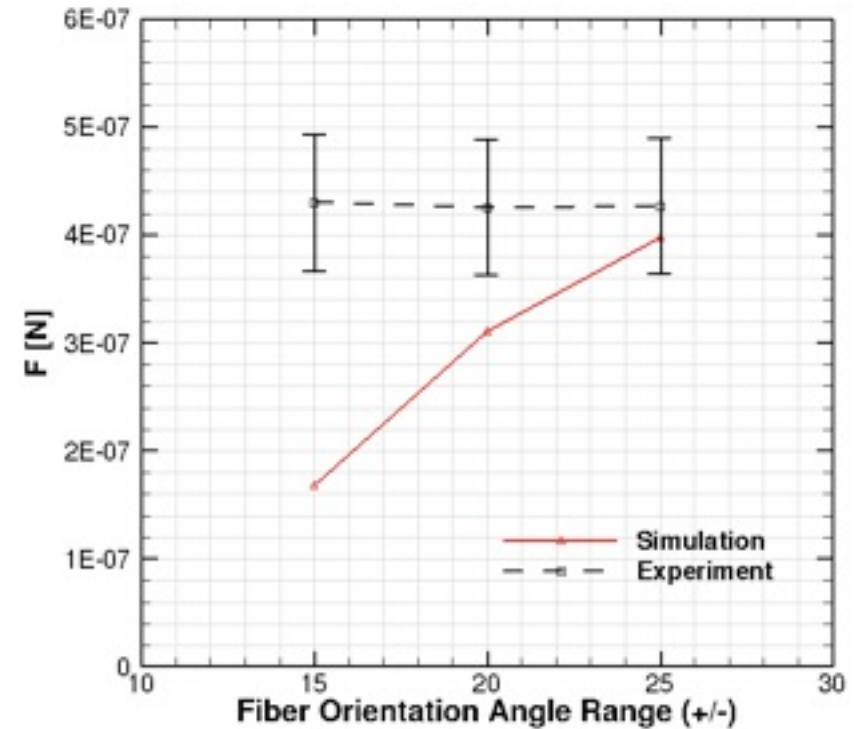
Preliminary Results



$D_f = 6\mu\text{m}$



$D_f = 10\mu\text{m}$



- Fiber orientation is defined as the angle of the fiber with “pressing” plane.
- Error bars are those reported in the paper for *all* runs.



Permeability Results



- **Caveats:**

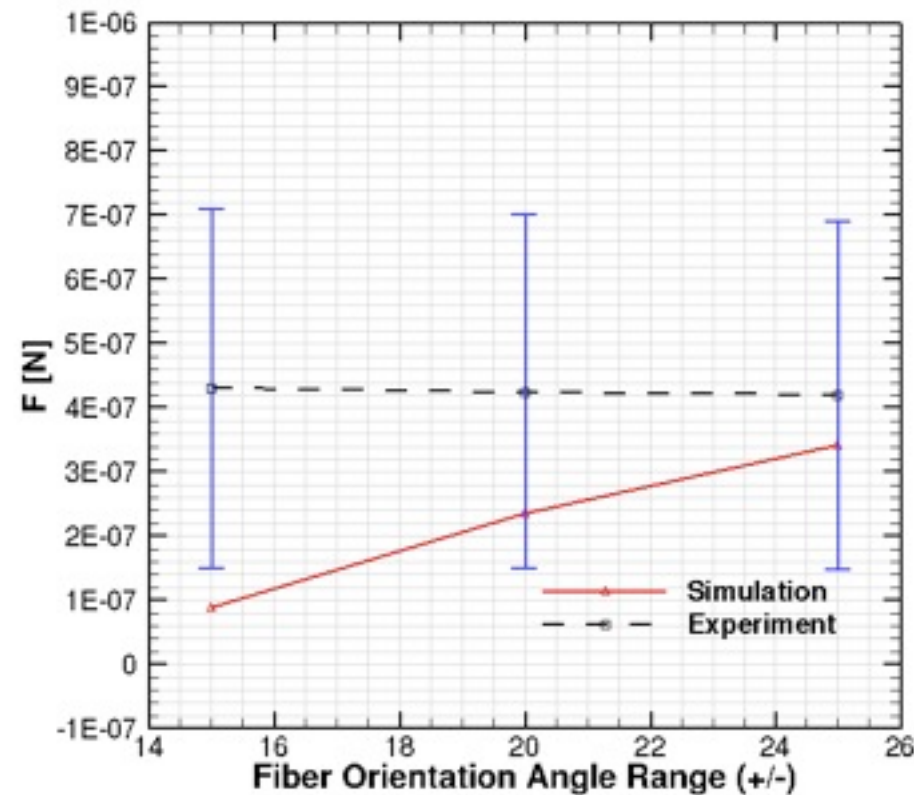
- Seems to be large scatter in the experimental data

FiberForm	145	359	703
	149	323	877
	157	82.3	1100
	161	79.1	1150

- Simulated geometry likely doesn't constitute a "representative volume element"
- Experiment gas was air

- **Takeaways:**

- Microstructure is important
- We're in the ballpark!





Future Work

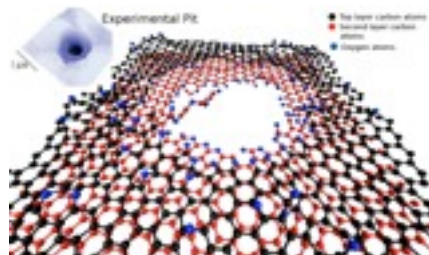


FiberGen

- Add analysis toolbox for computing geometric properties and statistics.
- Woven geometries

Gas-Surface Modeling

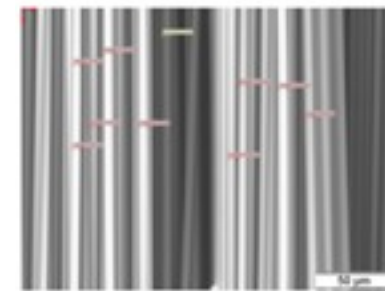
- Develop new gas-surface interaction model that takes better advantage of the improved fidelity of DSMC
 - “Active site” based approach
- Incorporate probabilities from Molecular Dynamics simulations



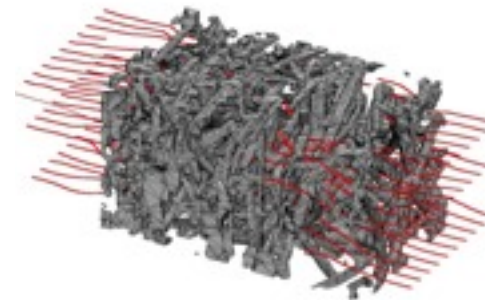
Poovathingal, et al., *J. Phys. Chem.*, 2013

Experimental Validation

- Interested in performing targeted validation experiments in the NASA Flow-tube facility on “simple(r)” microstructure



Simulate Stuff!...(cool stuff)



Stern et. al., *Gordon Research Conf*, 2013



Acknowledgements



- The author would like to thank the NASA Office of the Chief Technologist for supporting this work through the NASA Space Technology Research Fellowship.
- Additionally, the author would like to thank the many researchers at NASA Ames and the U of M who were generous enough to lend their support, and tremendous expertise on this and other topics:

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Nagi Mansour
Francesco Panerai
Steve Sepka
Jim Arnold
et al....

Questions?