

# Raman spectroscopic studies on the ferroelectric soft mode in $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$

著者 (英)	Tsuguhito Nakano, Yu Mikami, Minoru Kobayashi, Yukihiro Kogai, Kohji Abe
journal or publication title	Ferroelectrics
volume	532
number	1
page range	111-120
year	2019-02-11
URL	<a href="http://id.nii.ac.jp/1438/00009294/">http://id.nii.ac.jp/1438/00009294/</a>

doi: 10.1080/00150193.2018.1430427

# Raman spectroscopic studies on the ferroelectric soft mode in $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$

Tsuguhito Nakano<sup>1</sup>, Yu Mikami<sup>2</sup>, Minoru Kobayashi<sup>2</sup>, Yukihiro Kogai<sup>2</sup>, and Kohji Abe<sup>2</sup>

<sup>1</sup>Department of Dentistry, Health Science University of Hokkaido, 1757 Tobetsu-Cho, Ishikari-Gun, Hokkaido, 061-0293 Japan.

<sup>2</sup> Department of Engineering Sciences, The University of Electro-Communications, 1-5-1 Chofugaoka, Chofu-shi, Tokyo, 182-8585 Japan.

[tnakano@hoku-iryo-u.ac.jp](mailto:tnakano@hoku-iryo-u.ac.jp)

## ABSTRACT

The Raman spectra of novel ferroelectric ceramics  $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$  ( $x = 0.1, 0.05$  and  $0.02$ ) were obtained to clarify the mechanism of their ferroelectric phase transitions. Two transverse-optic modes in the ferroelectric phase showed softening toward the ferroelectric transition temperature. A comparison of the spectra obtained for  $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$  with the spectrum of  $\text{Pb}_x\text{Sr}_{1-x}\text{TiO}_3$  facilitated the assignment of the observed modes under the assumption of the ferroelectric phase in  $C_{4v}^1$  symmetry. However, several peaks violating the Raman selection rules were observed, suggesting the emergence and growth of polar regions even in the paraelectric phase.

*Keywords:* Ferroelectricity; Raman scattering;  $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$

## 1. Introduction

Substitution of the A and B sites of  $\text{SrTiO}_3$  (STO) with various elements can induce ferroelectricity and/or change the structural phase-transition temperature. As a result, the tuning of the transition temperature and dielectric properties through appropriate substitutions has been the subject of many previous investigations. [1, 2]

Since STO is a quantum paraelectric crystal, its dielectric permittivity saturates at very high values below  $\sim 4$  K owing to quantum fluctuations. Under these conditions, ferroelectric transition is suppressed. Quantum paraelectricity easily becomes unstable under the effect of external perturbations, as illustrated by the following example: if 0.2% of Sr is replaced with Ca, quantum ferroelectricity is exhibited. [3, 4] Furthermore, when Ba or Pb is substituted for Sr, the crystal structure approaches that

of BaTiO<sub>3</sub> or PbTiO<sub>3</sub>, respectively, and these materials become ferroelectrics. [1, 2] Isotopic effects are also important. The substitution of oxygen with its heavier isotope O<sup>18</sup> suppresses quantum fluctuations and induces ferroelectric behavior. [5]

In 2012, Suzuki et al. reported on the ferroelectricity of Sn<sub>x</sub>Sr<sub>1-x</sub>TiO<sub>3</sub> ceramics (hereafter denoted as SSTO), which are obtained by substituting Sr with Sn in STO.[6] Their work was motivated by a first principles study of pure SnTiO<sub>3</sub>. This study suggested that the spontaneous polarization of SnTiO<sub>3</sub> is larger than that of PbTiO<sub>3</sub> (PTO). [7] The temperature dependence of the dielectric permittivity ( $\epsilon'$ ) of SSTO is described by a broad peak, such that the peak temperature  $T_m$  gradually increases with the concentration of Sn. For SSTO with the highest replacement rate  $x = 0.1$ ,  $T_m$  increases to  $\sim 180$  K. Although this broad peak is characteristic of a relaxor, the frequency dependence of  $\epsilon'$  weakens as the concentration of Sn increases. Below  $T_m$ , a weak  $D$ - $E$  loop is observed. [6] Since SSTO has a high dielectric permittivity and broad peak near room temperature owing to the shift of  $T_m$  due to Sn substitution, it has attracted significant attention as a new lead-free dielectric material.

Several experiments also were performed by Suzuki et. al, in order to investigate the mechanism of ferroelectric transition. [6, 8] X-ray diffraction (XRD) results for SSTO  $x = 0.1$  obtained using a laboratory diffractometer suggest that the lattice constants change at  $T_m$  due to a structural change from a cubic to tetragonal system. [6] The measured values of pyroelectricity show that polarization gradually increases upon cooling from room temperature to  $T_m$ . [6] Spherical-aberration-corrected scanning transmission electron microscopy (Cs-STEM) together with energy-dispersive X-ray spectrometry (EDX) has revealed Sn atoms located at off-centre positions in some lattice sites even at room temperature. [6] Moreover, using piezoresponse force microscopy (PFM), microscale-polar regions distributed inhomogeneously at room temperature have been detected. [8]

In 2014, the authors reported the tentative assignment of the Raman spectra of SSTO ceramics. [9] As the structural change in SSTO was not decided at that time, we assumed that the freezing of  $R_{25}$  mode accompanied by the change of symmetry from  $O_h$  into  $D_{4h}$  causes the observed structural phase transition. However, synchrotron-radiation XRD and x-ray absorption fine structure (XAFS), [10] and neutron diffraction [11] analyses have shown that the structural change at  $T_m$  is associated with the displacement of the B site atom and the octahedral oxygen in the opposite direction along the c-axis. This is similar to the ferroelectric transition of PTO in that the space group changes from  $Pm\bar{3}m$  ( $O_h^1$ )

to  $P4mm$  ( $C_{4v}^1$ ). This is also consistent with the displacement predicted by the first-principles calculations performed for  $\text{SnTiO}_3$ . [7] These studies also show that the local distorted structures around Sn atoms exist in the paraelectric phase. [10, 11]

Since these results contradict the model that was originally proposed by the authors, [9] the Raman spectra of ferroelectric  $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$  were measured again in the present study in order to fully determine mode assignments. In Ref [9], two soft transverse optic modes were assigned as  $A_{1g}$  and  $E_g$  in  $D_{4h}^{18}$  which are related to the structural soft mode  $R_{25}$ . In this paper, it was found that those two modes are associated with the  $F_{1u}(\text{TO1})$  ferroelectric soft mode at  $\Gamma$ -point. The assignments of other modes were reconsidered based on the spectra of  $\text{PbTiO}_3$  and  $\text{Pb}_x\text{Sr}_{1-x}\text{TiO}_3$ . [12, 13] Spectra were recorded at temperature higher than the room temperature for SSTO  $x = 0.1$  in order to investigate the origin of the pyroelectricity in the paraelectric phase.

## 2. EXPERIMENTAL PROCEDURES

Ceramic samples of  $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$  ( $x = 0.1, 0.05, \text{ and } 0.02$ ) and  $\text{Pb}_{0.15}\text{Sr}_{0.85}\text{TiO}_3$  (PSTO  $x = 0.15$ ) were prepared by Suzuki at Murata Manufacturing Co. Ltd. [6,14] The samples had a typical size of  $3 \times 3 \times 1 \text{ mm}^3$  and an average grain size of approximately 200–500 nm. They were cooled in a helium flow-type cryostat. The micro-Raman technique was employed using a long-working-distance objective lens (BD Plan Apo10  $\times$ , Mitsutoyo, NA = 0.28, WD = 33 mm). An  $\text{Ar}^+$  laser (wavelength = 514.5 nm) was used as the excitation light source, and backscattered light was collected by the objective lens without a polarizer. The laser power was carefully adjusted in order to prevent local heating of the sample. To obtain spectra over the frequency range of 200–700  $\text{cm}^{-1}$ , a single spectrometer (Spectra Pro275, Acton Research with a resolution equal to 4.0  $\text{cm}^{-1}$ ) with an intensified CCD (ICCD-1152MG-E, Princeton Instruments) was used. For the very-low-frequency region 5–80  $\text{cm}^{-1}$ , a double monochromator (U1000, Jobin-Yvon) was employed. The spectral resolution was set to 1.8  $\text{cm}^{-1}$ . To measure the SSTO  $x = 0.1$  spectra over the temperature range of 120–500 K, the sample was set to a temperature-controlled stage. Scattered light was analyzed using a spectrometer (NR-1800, JASCO, resolution = 1.4  $\text{cm}^{-1}$ ) with an ultralong-working-distance objective lens (ULWD CDPlan40, Olympus, NA = 0.5, WD = 13 mm). When the temperature was raised above room temperature, the sample room was purged with nitrogen to prevent deterioration of the sample surface.

### 3. RESULTS AND DISCUSSION

#### 3.1 Spectra of SSTO in very-low-frequency region

Figure 1(a) shows the temperature dependence of the Raman spectra of SSTO with  $x = 0.02$ ,  $0.05$ , and  $0.1$  in the frequency range of  $5\text{--}80\text{ cm}^{-1}$ . To clearly determine the behavior of these modes, the reduced Raman spectra  $\text{Im}\chi(\omega) = I(\omega)[1 + n(\omega)]^{-1}$  are shown in Figure 1(b), where  $I(\omega)$  is the Raman intensity and  $n(\omega)$  is the Bose factor. For  $x = 0.1$ , three Raman peaks, two peaks are observed at  $\sim 26$  and  $\sim 44\text{ cm}^{-1}$  with a further large peak at  $\sim 77\text{ cm}^{-1}$ , are observed at 20 K. The latter peak illustrates the softening with a decrease in temperature and overlaps with the former two peaks for low Sn concentrations. For all values of Sn concentration, the following behavior is observed: as the temperature decreases from 300 K, the area intensity of the spectrum in the low-frequency range increases and two peaks appear near  $T_m$ . (The values of  $T_m$  for SSTO  $x = 0.1$ ,  $0.05$ , and  $0.02$  are 180, 150 and 90 K, respectively). Below  $T_m$ , the frequencies of these peak increase to  $\sim 26$  and  $\sim 44\text{ cm}^{-1}$ . Since the temperatures at which these peaks appear are in agreement with the  $T_m$  for the corresponding Sn concentration, these two modes are considered as the ferroelectric soft modes.

However, owing to the strong intensity of Rayleigh scattering and the strong anharmonicity of the soft modes, it is difficult to determine whether the soft mode freezes or not. At temperatures higher than  $T_m$ , it seems that the intensity of the overdamped mode increases toward  $T_m$ . We assumed that this behavior is indicative of the relaxation mode. Further analysis of the low-frequency region using other models will be performed in future work by taking into account the coupling of soft modes and the effects of the ferroelectric microregion (FMR). [15]

#### 3.2 SSTO $x=0.1$ and PSTO $x=0.15$ in wide spectral range

Figure 2(a) shows the Raman spectra of SSTO  $x = 0.1$  in the frequency range of  $15\text{--}700\text{ cm}^{-1}$ . At  $T = 300\text{ K}$ , broad peaks at  $\sim 120$  and  $\sim 545\text{ cm}^{-1}$  and an asymmetric peak at  $\sim 173\text{ cm}^{-1}$  are observed. In addition to these modes, a broad peak at  $\sim 120\text{ cm}^{-1}$  ( $T = 300\text{ K}$ ) splits into two peaks at  $T \sim T_m$  upon cooling. Of these peaks, the lower-frequency component decreases to  $77\text{ cm}^{-1}$ . Below  $T_m$ , the peaks at  $\sim 267$  and  $\sim 444\text{ cm}^{-1}$  become clearer. Two modes that appear below  $50\text{ cm}^{-1}$  are the ferroelectric soft modes, as was shown in Figure 1.

For comparison with SSTO, Raman spectra of displacive-type ferroelectrics  $\text{Pb}_{0.15}\text{Sr}_{0.85}\text{TiO}_3$  (PSTO  $x = 0.15$ ) are shown in Figure 2(b). PSTO  $x=0.15$  undergoes the ferroelectric transition at  $T_c=170$  K with the symmetry changes from  $Pm\bar{3}m$  ( $O_h^1$ ) to  $P4mm$  ( $C_{4v}^1$ ). [1,2] This symmetry change is the same as that observed in SSTO with the neutron scattering. [11] The overall spectral structure of PSTO  $x = 0.15$  is very similar to that of SSTO, except that no peaks appear above  $T_c$  and their line widths are relatively narrow.

### 3.3 Mode Assignment

The mode assignment of the PSTO  $x=0.15$  spectra in Figure 2(b) was obtained with reference to the Raman-scattering studies on PTO single crystal [12] and PSTO  $x=0.2$  and  $0.3$  ceramics. [13] In ref. [13], the large splitting of  $E$ -mode with lowest frequencies was attributed to the symmetry breaking by the A-site cation. [16, 17] However, since it is not clear whether the effect of A-site cation is same in the case of Sn substitution as the Pb case, for the assignment of the spectra below  $\sim 100$   $\text{cm}^{-1}$ , we referred to the PTO single crystal spectra in ref. [12].

In the paraelectric phase, no peaks are observed as expected from Raman selection rules. Below  $T_c$  (170K), several peaks are observed owing to the reduction in symmetry. A couple of peaks at  $\sim 27$  and  $\sim 50$   $\text{cm}^{-1}$  at 20 K (shown by the arrows in the inset of Figure 2(b)) are assigned as the ferroelectric soft mode  $E$  and  $A_1$  mode in  $C_{4v}^1$  originate from  $F_{1u}(\text{TO1})$  in  $O_h^1$ . [12] Then, two peaks split at about  $80$   $\text{cm}^{-1}$  and  $120$   $\text{cm}^{-1}$  which are from the single peak at  $\sim 95$   $\text{cm}^{-1}$  are the corresponding LO modes, namely  $E(\text{LO1})$  and  $A_1(\text{LO1})$ . [12] LO components are observable in the backscatter geometry because the sample is ceramic. [13] A tiny peak at  $\sim 470$   $\text{cm}^{-1}$ , which is clearly seen in the spectra of PSTO  $x \geq 0.2$ , is also an LO component, namely  $A_1+E$  from  $F_{1u}(\text{LO2})$ . [13]

From the comparison with the spectrum of PSTO allows the peaks at approximately 26, 44, 77 and  $120$   $\text{cm}^{-1}$  in the spectra of SSTO are assigned to be  $E(\text{TO1})$ ,  $A_1(\text{TO1})$ ,  $E(\text{LO1})$ , and  $A_1(\text{LO1})$  in  $C_{4v}^1$ , respectively. They originate from  $F_{1u}(\text{TO1})$  and  $F_{1u}(\text{LO1})$  in  $O_h$  symmetry. The remaining peaks in the spectra of SSTO were assigned in the similar way and the results are summarized in Table 1.

We note that in contrast to the PSTO spectrum, the peaks at  $\sim 120$   $\text{cm}^{-1}$  (LO1),  $\sim 173$   $\text{cm}^{-1}$  (TO2) and  $\sim 555$   $\text{cm}^{-1}$  (TO4) are found in the paraelectric phase in the SSTO spectra. In  $\text{ABO}_3$  cubic perovskite compounds, four triply degenerate optical modes  $3F_{1u} + F_{2u}$  are Raman-forbidden. Therefore, these

peaks violate the Raman selection rules. The appearance of these peaks is considered due to the existence of local polarizations. Such effects are found also in the Raman spectra of STO ceramics, films, and nanocubes. [18-20] Moreover, since the grain sizes of the PSTO and SSTO samples are approximately the same, Sn doping may be the reason for the breaking of the local centrosymmetry. This is consistent with studies that reported Sn atoms located at off-centered positions using Cs-STEM [6].

### 3.4 Sn-concentration dependence

Raman spectra of SSTO for  $x = 0.05$  and  $x = 0.02$  are shown in Figure 3. Although no great differences are observed between the spectral features and temperature dependence among the three samples, we note that the relative intensity of TO4 at  $545 \text{ cm}^{-1}$  to the background  $\sim 620 \text{ cm}^{-1}$  in the paraelectric phase is much weaker for  $x=0.02$  than  $x=0.1$ . This result would be related to the existence of local polarization caused by Sn doping since the symmetry changes in SSTO  $x = 0.05$  and  $0.02$  would be the same as that observed in SSTO  $x = 0.1$ . However, the reason for the lack of peak at  $\sim 444 \text{ cm}^{-1}$  only for  $x=0.05$  is unknown and requires further investigation.

Since PSTO  $x \sim 0.025$  retains the structural phase transition due to the condensation of the  $R_{25}$  mode at  $\sim 90 \text{ K}$  as was shown in ref. [1, 2], the effect of Sn doping on the structure is considered to be relatively strong. The strong suppression of the structural phase transition and promotion of the ferroelectric phase transition owing to Sn-substitution could be closely related to the ionic radius as well as the position of Sn within the structure. The Shannon–Prewitt ionic radii of 12-coordinated  $\text{Sr}^{2+}$  and  $\text{Pb}^{2+}$  are  $1.44$ , and  $1.49 \text{ \AA}$ , respectively, [21] whereas that of  $\text{Sn}^{2+}$  is estimated to be  $1.35 \text{ \AA}$ . [22] The large difference in the ionic radii together with the off-center position of Sn would tilt the oxygen octahedron from the crystal axes, resulting in the suppression of the structural phase transition, which is triggered by the freezing of the  $R_{25}$  mode associated with the collective antiphase rotation of the octahedral oxygen about the c-axis.

### 3.5 Temperature dependence of the intensity of TO4 mode

In a further step, the temperature dependence of the intensity of the TO4 mode,  $I_{\text{TO4}}$ , at  $\sim 555 \text{ cm}^{-1}$  for SSTO  $x = 0.1$  was investigated in the range of  $120\text{--}510 \text{ K}$ . To accurately measure the change in the intensity, the spectra are recorded at a point on the sample surface by monitoring the position using a

microscope. The beam-spot size is approximately  $2 \mu\text{m}$ , which is larger than the average grain size. Figure 4 (a) shows the obtained Raman spectra. The values of  $I_{\text{TO4}}$  obtained by fitting to a damped harmonic oscillator (DHO) are plotted as a function of temperature in Figure 4(b). Upon cooling,  $I_{\text{TO4}}$  emerges at  $\sim 400$  K and gradually increases. A rapid increase in  $I_{\text{TO4}}$  is observed for temperatures slightly higher than  $T_m$ . This behavior is similar to the temperature dependence of the polarization measured by Suzuki et al. and is shown in Figure 4(c). [6] Assuming that  $I_{\text{TO4}}$  in the paraelectric phase reflects the distribution of the local polarizations, this result suggests that local polar regions are expected to emerge below  $\sim 400$  K and increase in volume as the temperature decreases. The discrepancy between the temperature dependence of  $I_{\text{TO4}}$  and that of the polarization shown in Figure 4(c) is attributed to the fact that Raman intensity is not associated with polarization but with electronic polarizability. Currently, the origin of such polar regions is not well-understood. Some explanations on this behavior would be possible, e.g., the effect of stress at the ceramic grain boundaries due to thermal expansion; percolation of local polarizations caused by the off-center position of the Sn atom; and the formation of polar nanoregions (PNRs), as observed in  $\text{Pb}(\text{Mn}_{1/3}\text{Nb}_{2/3})\text{O}_3$  (PMN). [23] The Raman spectra in the low-frequency region, obtained at high temperatures using a powder sample, will aid the understanding of the origin of the polar regions and their influence on the ferroelectric phase transition and the peculiar dielectric responses observed. [24]

#### 4 SUMMARY

Raman spectra were studied in the frequency range of  $5\text{--}700 \text{ cm}^{-1}$  in order to investigate the ferroelectric transition mechanism of  $\text{Sn}_x\text{Sr}_{1-x}\text{TiO}_3$   $x = 0.02\text{--}0.1$ . Assuming that the symmetry of the ferroelectric phase in  $C_{4v}^1$  symmetry as proposed by a recent neutron scattering study, the Raman peaks observed at  $\sim 26$ ,  $44$ ,  $77$ , and  $120 \text{ cm}^{-1}$  at  $20 \text{ K}$  were assigned to  $E$  (TO1),  $A_1$  (TO1),  $E$  (LO1), and  $A_1$  (LO1), respectively. The frequencies of the two TO1 modes decreased to considerably low frequencies in the region of their ferroelectric transition temperatures.

Raman spectra observed at higher temperatures revealed that polar local regions induced by the Sn atom emerge at  $\sim 400 \text{ K}$  and grow as the temperature decreases. The increase in the spectral intensities around the zero frequency suggests the existence of a relaxation mode. Further analysis of the



spectra in the low-frequency region will lead to a thorough understanding of the influence of these polar regions on phase transitions and peculiar dielectric permittivity.

## **ACKNOWLEDGMENTS**

Authors are grateful to Dr. S. Suzuki and Dr. A. Ando at Murata Manufacturing Co. Ltd. for providing us SSTO and PSTO samples and for stimulating discussions. T. N. thanks Assoc. Prof. T. Nezu at Health Science University of Hokkaido (HSUH) for his support in arranging experimental equipment. Parts of the experiments were performed at the High-Tech research center at HSHU.

## REFERENCES

- [1] V. V Lemanov, Phys. Solid State. **39** (1997) 1468–1473.
- [2] V. V. Lemanov, Ferroelectrics. **226** (1999) 133–146.
- [3] J.G. Bednorz, K.A. Muller, Phys. Rev. Lett. **52** (1984) 2289–2292.
- [4] U. Bianchi, W. Kleemann, J.G. Bednorz, J. Phys. Condens. Matter. **6** (1994) 1229–1238.
- [5] M. Itoh, R. Wang, Y. Inaguma, T. Yamaguchi, Y.J. Shan, T. Nakamura, Phys. Rev. Lett. **82** (1999) 3540–3543.
- [6] S. Suzuki, A. Honda, N. Iwaji, S. Higai, A. Ando, H. Takagi, H. Kasatani, K. Deguchi, Phys.Rev.B**86** (2012) 060102(R).
- [7] Y. Uratani, T. Shishidou, T. Oguchi, Jpn. J. Appl. Phys. **47** (2008) 7735–7739.
- [8] S. Suzuki, A. Honda, K. Suzuki, S. Higai, A. Ando, K. Niwa, M. Hasegawa, Jpn. J. Appl. Phys. **52** (2013) 52–54.
- [9] T. Nakano, Y. Mikami, K. Abe, S. Suzuki, K. Akiyama, A. Ando, Ferroelectrics. **464** (2014) 72–79.
- [10] H. Kasatani, S. Suzuki, A. Ando, E. Magome, C. Moriyoshi, Y. Kuroiwa and K. Deguchi, Acta Cryst. (2014). A**70**, C61.
- [11] G. Laurita, R. Seshadri, Phys. Rev. B**92** (2015)214109.
- [12] G. Burns, B.A. Scott, Phys. Rev. B **7** (1973) 3088–3101.
- [13] M. Jain, Y.I. Yuzyuk, R.S. Katiyar, Y. Somiya, A.S. Bhalla, J. Appl. Phys. **98** (2005) 24116.
- [14] S. Suzuki, T. Takeda, A. Ando, H. Takagi, Appl. Phys. Lett. **96** (2010) 132903.
- [15] H. Uwe, K. B. Lyons, H. L. Carter, and P. A. Fleury, Phys. Rev. B**33** (1986) 6436-6440.
- [16] J. Frantti, V. Lantto, S. Nishio, and M. Kakihana, Phys. Rev. B**59** (1999) 12-15.
- [17] S. M. Cho, J. H. Park, and H. M. Jang, J. Appl. Phys. **94** (2003) 1948-1953.
- [18] J. Petzelt, T. Ostapchuk, I. Gregora, I. Rychetský, S. Hoffmann-Eifert, A. V Pronin, Y. Yuzyuk, B.P. Gorshunov, S. Kamba, V. Bovtun, J. Pokorný, M. Savinov, V. Porokhonsky, D. Rafaja, P. Vaněk, A. Almeida, M.R. Chaves, A.A. Volkov, M. Dressel, R. Waser, Dielectric, Phys. Rev. B. **64** (2001) 184111.
- [19] A.A. Sirenko, C. Bernhard, A. Golnik, A.M. Clark, J. Hao, W. Si, X.X. Xi, Nature. **404** (2000) 373–376.
- [20] S. Banerjee, D. Kim, R.D. Robinson, I.P. Herman, Y. Mao, S.S. Wong, Appl. Phys. Lett. **89** (2006) 223130.
- [21] R.D. Shannon, Acta Crystallogr. Sect. A. **32** (1976) 751–767.
- [22] J.W. Bennett, I. Grinberg, P.K. Davies, A.M. Rappe, Phys. Rev. B. **83** (2011) 144112.
- [23] G. Burns, B.A. Scott, Solid State Commun. **13** (1973) 423–426.
- [24] J. Petzelt, S. Kamba, J. Hlinka, Ferroelectric soft modes in ceramics and films, chapter in the book *New*

**Figure captions**

## Figure 1

(a) Raman spectra and (b) reduced Raman spectra  $\text{Im}\chi(\omega)$  of SSTO for  $x = 0.1, 0.05,$  and  $0.02$  in the frequency range of  $5\text{--}80\text{ cm}^{-1}$ .

## Figure 2

(a) Raman spectra of SSTO  $x = 0.1$  in the frequency range of  $15\text{--}700\text{ cm}^{-1}$  and (b) Raman spectra of PSTO  $x = 0.15$  in the frequency range of  $15\text{--}700\text{ cm}^{-1}$ . The inset is the spectra at  $20\text{ K}$  in the range of  $15\text{--}150\text{ cm}^{-1}$ . The shape of spectra below  $20\text{ cm}^{-1}$  at  $250\text{ K}$  for PSTO  $x=0.15$  is artifact with the optical filter protecting CCD from the Rayleigh line.

## Table 1

Mode assignment for SSTO  $x = 0.1$  determined by referring to the Raman spectra of PSTO. The frequencies are approximate values, and all values are expressed in  $\text{cm}^{-1}$ .

## Figure 3

Raman spectra of (a) SSTO  $x = 0.05$  and (b) SSTO  $x = 0.02$  in the frequency range of  $15\text{--}700\text{ cm}^{-1}$ .

## Figure 4

Raman spectra of SSTO  $x = 0.1$  in the temperature range of  $120\text{--}510\text{ K}$ . (b) Peak intensities of the TO4 mode as a function of temperature. Open circles represent the data measured using another experimental set-up. (c) The temperature dependence of the polarization of SSTO  $x = 0.1$  reported by Suzuki et al. [6].

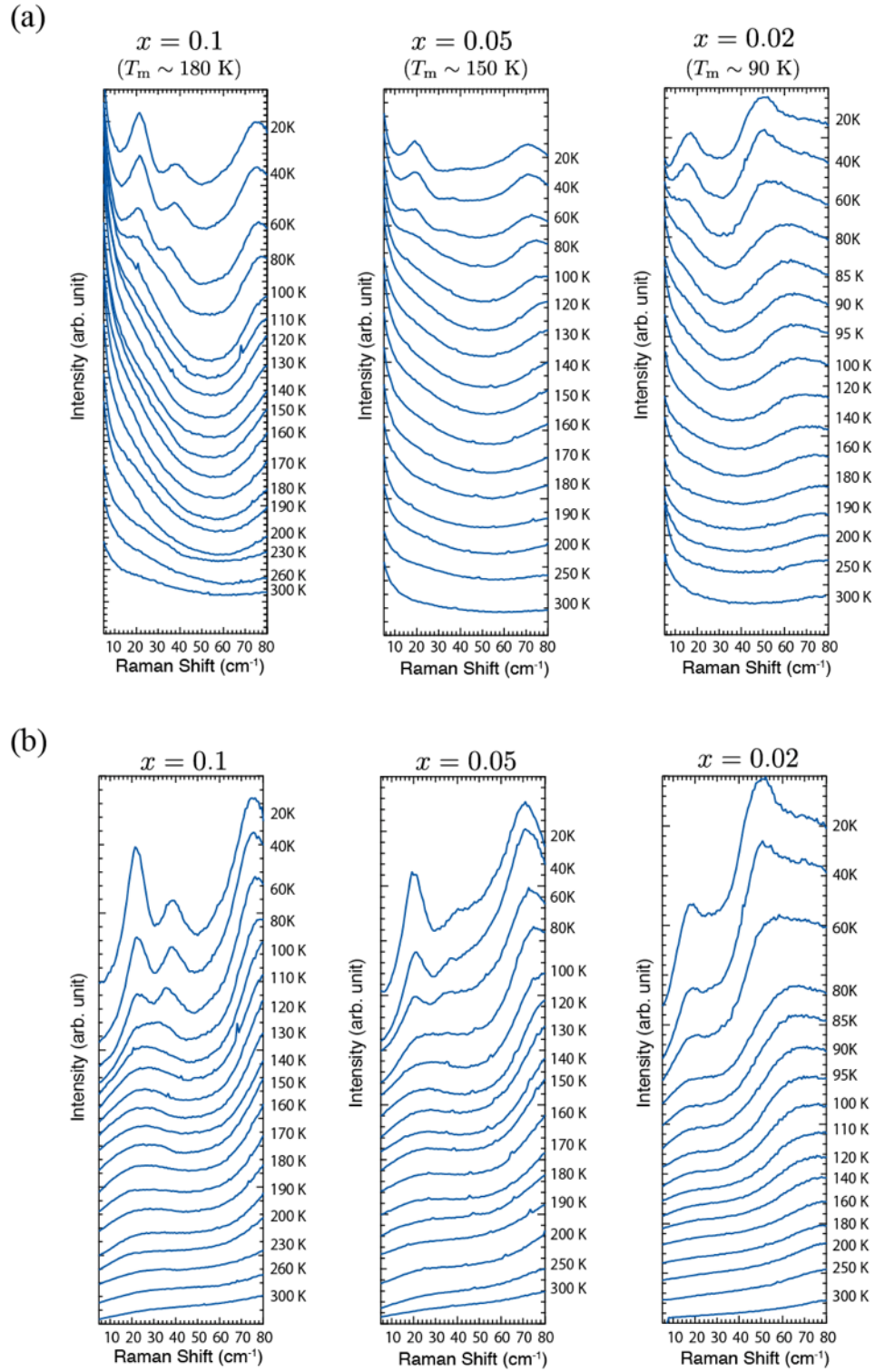


Figure 1

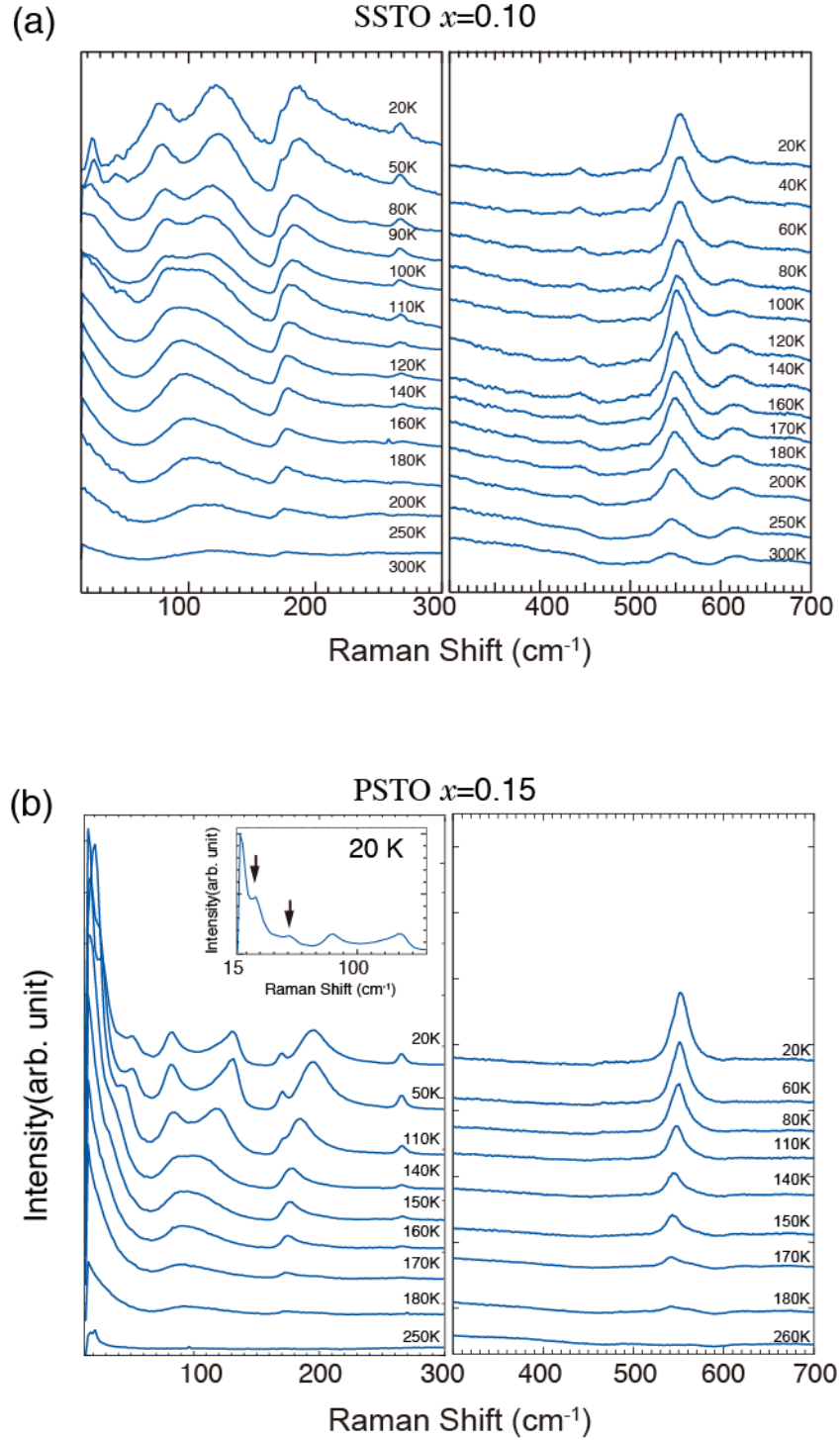


Figure 2

SSTO  $x = 0.1$ 

Paraelectric phase (300 K)		Ferroelectric phase (20 K)		
$Pm\bar{3}m (O_h^1)$		$P4mm (C_{4v}^1)$		
$F_{1u}(\text{TO1})$	—	$E$	26	
		$A_1$	44	
$F_{1u}(\text{LO1})$	$\sim 120$	$E$	77	
		$A_1$	120	
$F_{1u}(\text{TO2})$	$\sim 173$	$E$	173	
		$A_1$	176	assymmetric
$F_{2u}(\text{TO3})$	—	$B_1 + E$	267	
$F_{1u}(\text{LO2})$	—	$A_1 + E$	444	
$F_{1u}(\text{TO4})$	545	$E$	555	

— not observed

Table 1

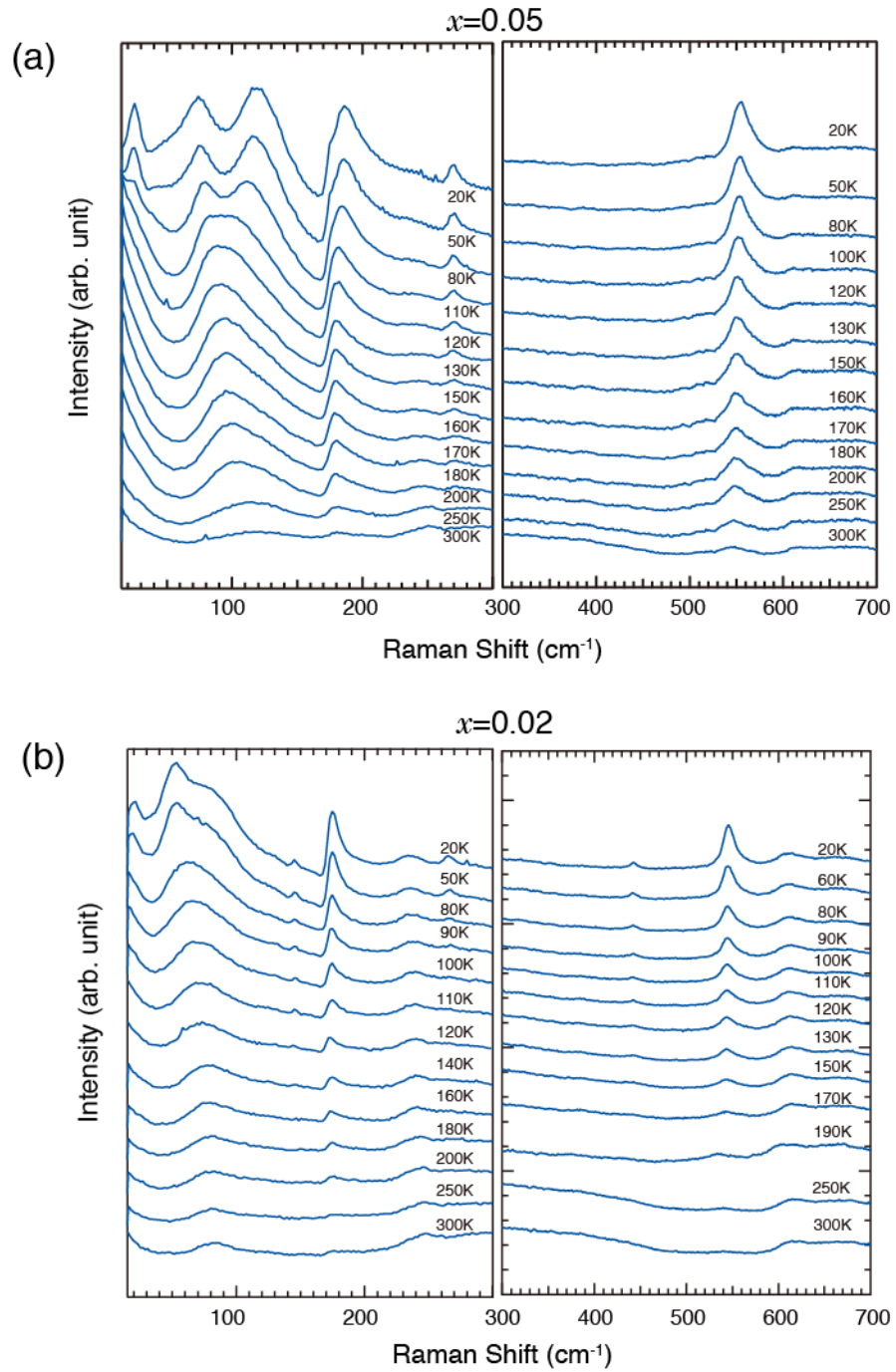


Figure 3

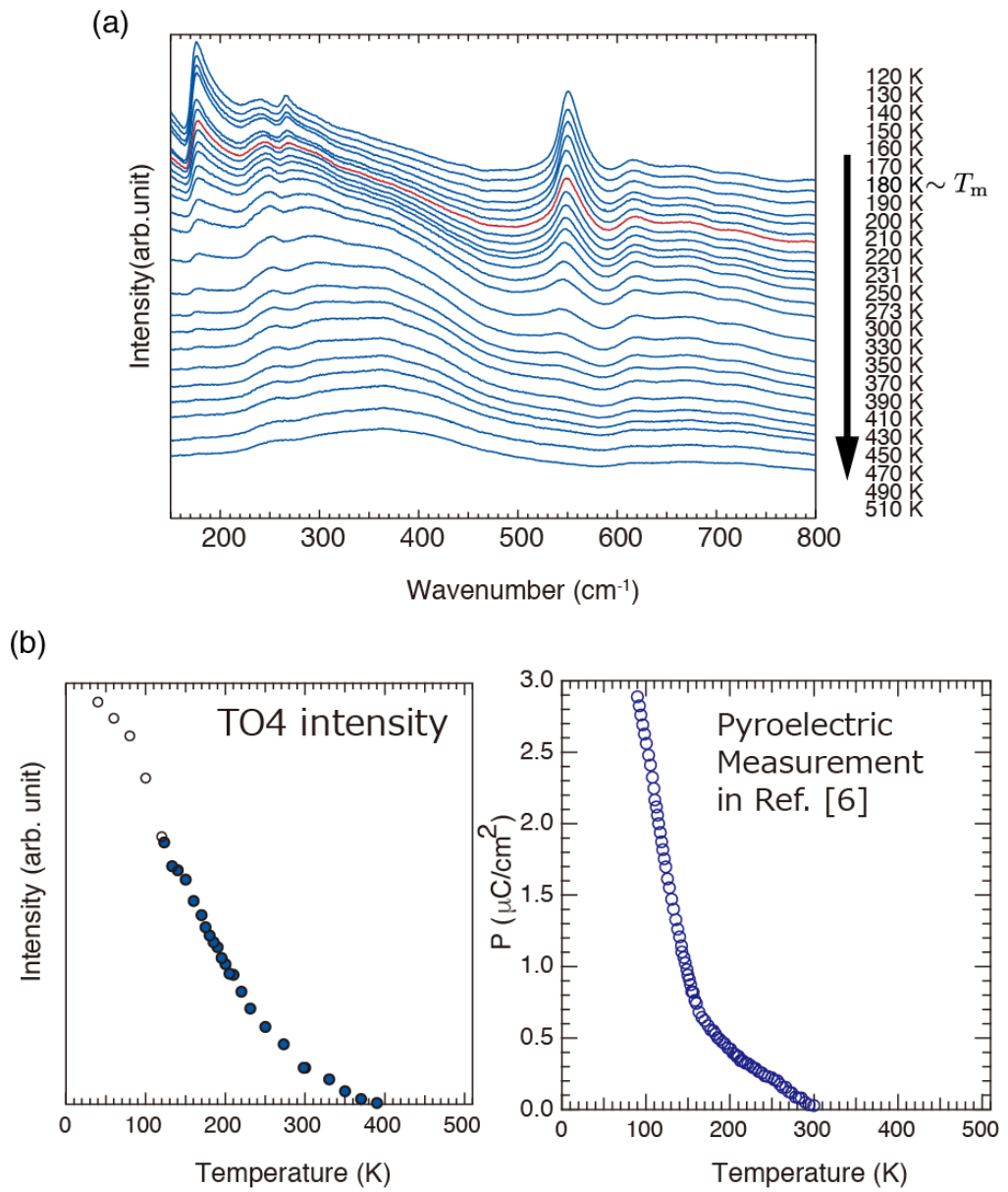


Figure 4