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REMOTE ESTIMATION OF TARGET HEIGHT USING UNMANNED AIR VEHICLES (UAVs)

Andrea Tonini

Dissertation presented as partial requirement for obtaining
the Master's degree in Information Management

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by

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Dissertation presented as partial requirement for obtaining the Master's degree in Information Management, with a specialization in Business Intelligence and Knowledge Management

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DEDICATION

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1 Article

2 REMOTE ESTIMATION OF TARGET HEIGHT 3 USING UNMANNED AIR VEHICLES (UAVs)

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9 **Abstract:** estimation of target height from videos is used for several applications, such as
10 monitoring agricultural plants growth or, within surveillance scenarios, supporting the
11 identification of persons of interest. Several studies have been conducted in this domain but, in
12 almost all the cases, only fixed cameras were considered. Nowadays, lightweight UAVs are often
13 employed for remote monitoring and surveillance activities due to their mobility capacity and
14 freedom for camera orientation. This paper focuses on how the height could be swiftly performed
15 with a gimballed camera installed into a UAV using a pinhole camera model after camera
16 calibration and image distortion compensation. The model is tailored for UAV applications
17 outdoor and generalized for any camera orientations defined by Euler angles. The procedure was
18 tested with real data collected with a regular-market lightweight quad-copter. The data collected
19 was also used to make an uncertainty analysis associated with the estimation. Finally, since the
20 height of a person who is not standing perfectly vertical can be derived by relationships between
21 body parts or human face features ratio, this paper proposes to retrieve the pixel spacing measured
22 along the vertical target, called here Vertical Sample Distance (VSD), to quickly measure vertical
23 sub-portions of the target.

24 **Keywords:** remote surveillance, target height, UAV, pinhole model, image distortion
25 compensation, Vertical Sample Distance (VSD)

26

27 1. Introduction

28 Unmanned Air Vehicles have been employed for more than two decades for military activities
29 [1] but, nowadays, they are also widely used for civil applications. In particular, non-coaxial
30 multi-rotors with weight below 4 kg [2] are often used to complement or, in some cases, even replace
31 fixed video cameras for monitoring and surveillance activities [3]. In fact, UAVs can bring a very
32 relevant added value compared with static installations: the possibility to transport and orient the
33 camera as needed, allowing to perform pre-established survey paths or even follow a specific target,
34 if needed [4].

35 Remote surveillance or monitoring activities may often require estimating the height of a target
36 via image analysis. The target could be a tree for example, in order to monitor its growing for
37 agricultural purposes [4], or a building, to follow contraction developments, or animals, to track
38 cattle growing [5]. However, as we may expect, remote height estimation from image analysis is
39 very often needed to define the exact stature of human beings. This is required to support the
40 identification of a person of interest [6], health care purposes [7] or even for marketing [8]. There is a
41 significant amount of studies in the literature dedicated to obtaining a person's body height from a
42 video but, almost the totality of them considered data collected by static surveillance cameras. On
43 the other hand, UAVs have been mainly used for estimating features' height for topographic or
44 urban mapping using Photogrammetry and LIDAR (Laser Imaging Detection and Ranging)

45 techniques (see for example [9], [10] and [11]). Photogrammetric techniques require having either a
46 double camera pointing at the same target or acquiring two images from different orientations of a
47 (static) feature. LIDAR data needs to be acquired by sophisticated devices installed in aircrafts
48 specifically designated for this kind of survey technique. In some studies [12], human height
49 estimation was performed with UAV using a machine learning approach. However, this approach
50 requires a quite intensive elaboration and it cannot be always performed in near real-time.

51 This paper focuses on how the height of a feature standing vertically from the ground can be
52 measured with a “regular” payload for lightweight UAVs, which is daylight Electro-Optical camera
53 installed into steerable gimbals. The goal is to estimate the height using a single image in a swift
54 fashion, possibly in near real-time, without the need for intense processing rapid situational
55 evaluation and quick decision making during the UAV flight. Moreover, we need to take into the
56 account that the UAV may operate outdoor, where topography and scene content may rapidly
57 change and the target may be a static feature, like a tree, or dynamic, like humans or animals.

58 A widely used approach for height estimation from video footages requires to identify, when
59 possible, vanishing lines in the scene (see for example [13], [14] and [15]). However, this approach
60 has relevant setbacks: defining vanishing lines may not be always possible in an image [16] and a
61 reference height in the scene is required to define the height of the target. Other authors have more
62 recently proposed to estimate the height of a person standing on a floor considering a pinhole
63 camera model after camera calibration and image distortion compensation [17]. A similar approach
64 was also used in [18] in combination with person body height estimation using interpupillary
65 distance, the comparison of these two methods showed that they are comparable and accurate.

66 It is here proposed an approach that foresees camera calibration and lens distortion correction
67 before calculating geometrically the height of the target using the pinhole camera model. This
68 procedure requires just a single image, or video frame, acquired with a camera fitted on-board of a
69 lightweight UAV. The correction for lens distortion allows generating an image as it was acquired by
70 a perfect pinhole system [19], which can be used for the mapping of a 3D scene to a 2D image.
71 However, the correction of an entire image may be very time-consuming. The approach here
72 described requires correcting just a very limited number of pixels, in order to reduce the elaboration
73 time for near real-time applications. On the other hand, the camera calibration [20] requires intrinsic
74 camera parameters, such as the focal length, and extrinsic parameters, such as camera position and
75 orientation. This paper analyzes how these parameters can be defined when dealing with UAVs, for
76 example the position of the camera is given by positional systems, like GPS.
77 The procedure was tested with real data collected with a regular-market lightweight quad-copter. A
78 measuring pole of known length standing vertically from the ground was used as a target for the
79 acquisition of several still images taken from different positions. For each shot, the height of the
80 target was calculated considering the procedure described above and compared with the real height
81 of the pole to assess the accuracy of the estimations. An analysis of the uncertainty was conducted to
82 analyze how the error associated with the camera-to-target distance can influence the accuracy of the
83 estimation.

84 The last part of this paper focuses on how estimating the vertical length of the target’s subparts,
85 which is particularly useful to define the exact human body height. In fact, the exact human stature
86 can be estimated in a video if the subject is standing vertically from the ground in a fully straight
87 pose. If the person has a different pose, such as standing relaxed with feet further apart and weight
88 on both feet standing relaxed with weight on one leg, we would manage to estimate just the height
89 of the body in that specific pose, see [6] and [21], not the real stature of the subject. In literature is
90 well known the relationship between the height of a person its body parts obtained via experimental
91 measures [22]. Therefore, the height a person who is not standing perfectly vertical can be derived
92 by relationships between body parts or and human face features ratio [23] face of the person is well
93 visible in the scene. It is here proposed to use the pixel spacing measured along the vertical target to
94 quickly estimate the length of body parts or face portions. The spacing in the vertical direction is
95 here called Vertical Sample Distance (VSD), which can be calculated as the GSD (Ground Sample
96 Distance, [24]) but perpendicular to the ground (vertical axis).

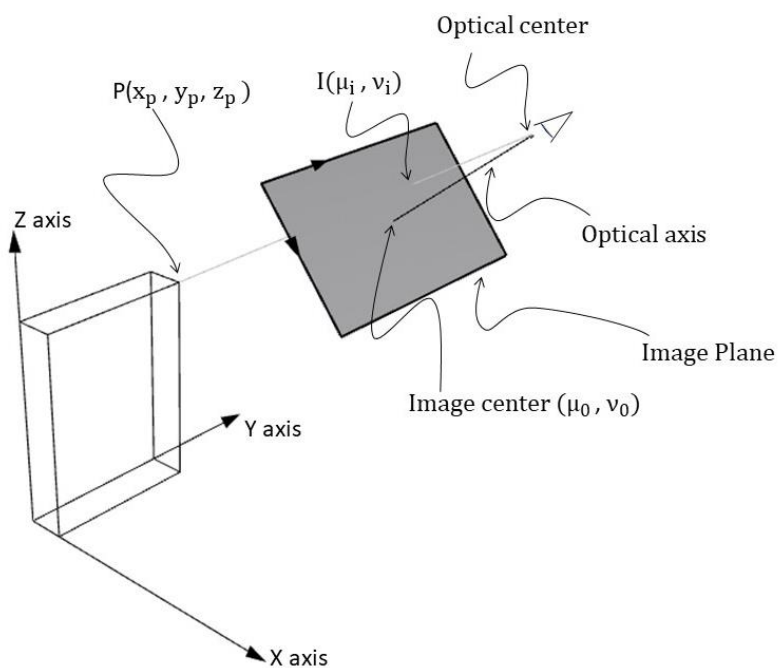
97 2. Methods

98 The first part of this section describes the basic principles of the pinhole model for computer
 99 vision and processes for lens distortion compensation. After that, it is analyzed how computer vision
 100 can be performed when dealing with cameras installed into UAVs. The last part of this section
 101 presents and describe the method to estimate the height from still images or video frames acquired
 102 with cameras installed into UAVs.

103 2.1. Pinhole camera model and computer vision

104 In computer vision, cameras are usually modelled with the pinhole camera model [28]. The
 105 model is inspired by the simplest camera, where the light from an object enters through a small hole
 106 (the pinhole). This model considers a central projection, using the optical center of the camera and an
 107 image plane (that is perpendicular to the camera's optical axis, see **Figure 1**). In the physical camera,
 108 a mirror image is formed behind the camera center but, often, the image plane is represented in front
 109 of the camera center. The pinhole camera model represents every 3D world point P (expressed by
 110 world coordinates x_p, y_p, z_p) with by the intersection between the image plane and the camera ray
 111 line that connects the optical center with the world point P (this intersection is called the image
 112 point, noted with I in **Figure 1**).

113



114

115 **Figure 1.** Graphical representation a 3D world point P is projected onto a 2D Image Plane.

116 The pinhole camera projection can be described by the following linear model

117

$$\begin{bmatrix} \mu_i \\ \nu_i \\ 1 \end{bmatrix} = K[RT] \begin{bmatrix} X_p \\ Y_p \\ Z_p \\ 1 \end{bmatrix} \quad (1)$$

118

119 Where K is the calibration matrix, defined as follow:

120

$$K = \begin{bmatrix} \alpha_\mu & \gamma & \mu_0 \\ 0 & \alpha_\nu & \nu_0 \\ 0 & 0 & 1 \end{bmatrix} \quad (2)$$

121

122

123

124

α_μ and α_ν represent the focal length expressed in pixels. μ_0 and ν_0 are the coordinates of the image center expressed in pixels, with origin in the upper left corner (see *Figure 1*). γ is the skew coefficient between the x and y axis, this latter parameter is very often 0.

125

126

127

128

The focal lengths, (which can be here considered as the distance between the image plane and optical center) can be also expressed in terms of distance (e.g. mm instead of pixels) considering the following expressions:

$$F_x = \alpha_\mu \frac{W_\mu}{w_\mu} \quad (3)$$

$$F_y = \alpha_\nu \frac{W_\nu}{w_\nu} \quad (4)$$

129

130

131

132

133

134

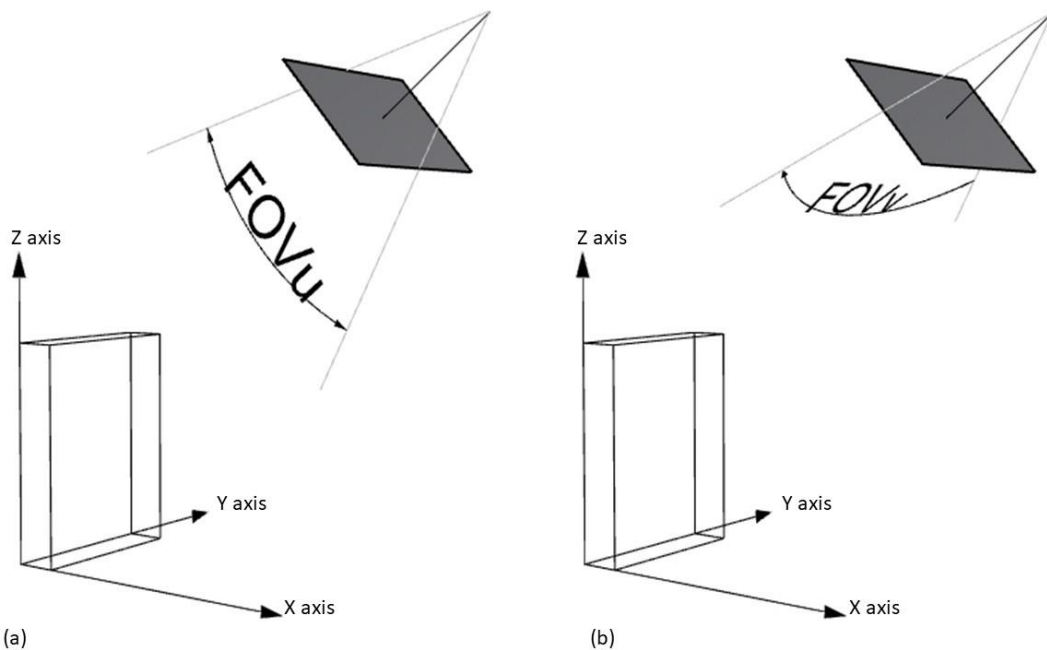
135

136

137

138

Where w_μ and w_ν are, respectively, the image (or video frame) width and length, W_μ is the width and W_ν the length of the camera sensor expressed in world units (e.g. mm). Usually, F_μ and F_ν have the same value, although they may differ due to several reasons such as flaws in the digital camera sensor or when the lens compresses a widescreen scene into a standard-sized sensor. The focal length F (assumed here for simplicity that $F = F_\nu = F_\mu$), W_μ and W_ν can be also used to calculate another important element, the Field of View (FOV) of the camera, which is the angular extent of the observable world that is seen at any given moment and it may be different in μ and ν directions (see *Figure 2*).



139

140

Figure 2 Graphical representation of the Field of View in the μ (a) and ν (b) directions

141

FOV_μ and FOV_ν can be calculated as follow:

$$FOV_\mu = 2 \tan^{-1} \frac{W_\mu}{2F} \quad (5)$$

$$FOV_v = 2 \tan^{-1} \frac{W_v}{2F} \quad (6)$$

142 R and T in (1) are the respectively rotation and translation of the camera. These are the extrinsic
143 parameters which define the so called “camera pose”.

144 R is defined by the axis of rotation and the angle that describes the amount of rotation. In the
145 case of rotation around the X axis by an angle θ_x , the rotation matrix R_x is given by [19]:
146

$$R_x = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos(\theta_x) & -\sin(\theta_x) \\ 0 & \sin(\theta_x) & \cos(\theta_x) \end{bmatrix} \quad (7)$$

147

148 Rotations by θ_y and θ_z about the Y and Z axes can be written as:
149

$$R_y = \begin{bmatrix} \cos(\theta_y) & 0 & \sin(\theta_y) \\ 0 & 1 & 0 \\ -\sin(\theta_y) & 0 & \cos(\theta_y) \end{bmatrix} \quad (8)$$

150

$$R_z = \begin{bmatrix} \cos(\theta_z) & -\sin(\theta_z) & 0 \\ \sin(\theta_z) & \cos(\theta_z) & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (9)$$

151

152 A rotation R about any arbitrary axis can be written in terms of successive rotations about the Z,
153 Y and finally X axes using the matrix multiplication shown below:

$$R = R_z R_y R_x \quad (10)$$

154 In this formulation θ_x , θ_y and θ_z are the Euler angles.

155 T is expressed by a 3-dimensional vector which defines the position of the camera against the
156 origin of the world coordinate system. GPS coordinates (Latitude, Longitude) and elevation, for
157 example, can define T. Scaling does not take place in the definition of the camera pose. Enlarging the
158 focal length or detector size would provide the scaling.

159 The next paragraph describes how the lens distortion effects and procedures for their
160 correction.

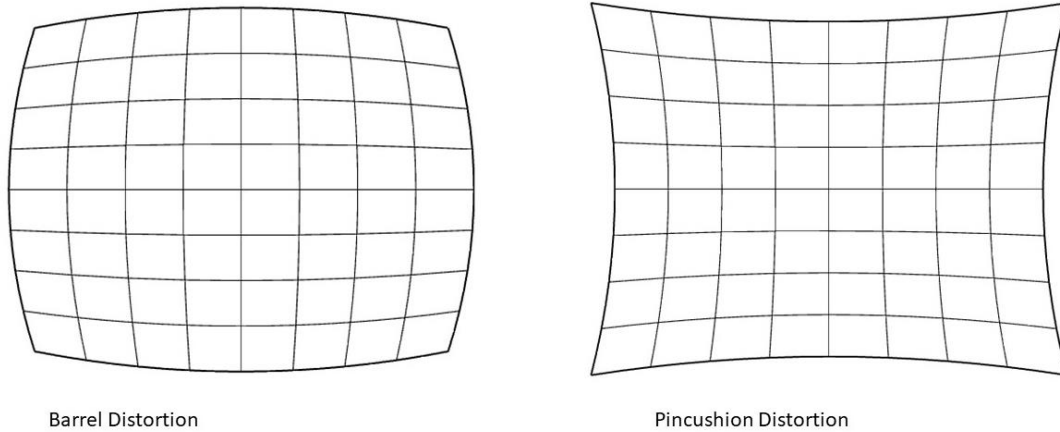
161

162 2.2. Lens distortion and compensation

163

164 The pinhole model does not consider that real lenses may produce several different non-linear
165 distortions. The major defects in cameras are the radial distortion, caused by the spherical shape of
166 the lens. Other distortions, like the tangential distortion, which is generated when the lens is not
167 parallel to the imaging sensor, have minor relevance and will not be considered in this study. The
168 radial distortions can usually be classified as either barrel distortions or pincushion distortions
169 (**Figure 3**), are quadratic, meaning they increase as the square of the distance from the center.
170

171



172

173 **Figure 3** Effect of barrel and pincushion distortions.

174 Removing a distortion means obtaining an undistorted image point, which can be considered as
 175 projected by an ideal pinhole camera, from a distorted image point. The simplest way to model the
 176 radial distortion is with a shift to the pixel coordinates. The radial shift of coordinates modifies only
 177 the distance of every pixel from the image center. Let r represents the observed distance (distorted
 178 image coordinates from the center) and r_{corr} the distance of the undistorted image coordinates from
 179 the center. The observed distance for a point in the image plane I of μ_i and v_i coordinates (see
 180 **Figure 1**) can be calculated as follow:

$$r = \sqrt{(\mu_i - \mu_0)^2 + (v_i - v_0)^2} \quad (11)$$

181

With these notations the function that can be used to remove lens distortion is:

$$r_{corr} = f(r) \quad (12)$$

182

183 However, before applying the compensation function $f(r)$ we need to underline that the
 184 model would be useless if images with the same distortion, but different resolutions would have
 185 different distortion parameters. Therefore, all pixels should be normalized to a dimensionless frame,
 186 where the image resolution is not important. In the dimensionless frame, the diagonal radius of the
 186 image is always 1, and the lens center is (0; 0) [25].

187

The formula to transform the pixel coordinates to dimensionless coordinates is the following:

188

$$\begin{pmatrix} p_\mu \\ p_v \end{pmatrix} = \begin{pmatrix} (\mu_i - \mu_0) / \sqrt{\left(\frac{w_\mu}{2}\right)^2 + \left(\frac{w_v}{2}\right)^2} \\ (v_i - v_0) / \sqrt{\left(\frac{w_\mu}{2}\right)^2 + \left(\frac{w_v}{2}\right)^2} \end{pmatrix} \quad (13)$$

189

190 Where p_μ and p_v are the dimensionless pixel coordinates and w_μ, w_v are the image width
 191 and height in pixels.

192

193 The dimensionless coordinates defined in (13) can be used to calculate a normalized distance r_p
 194 considering the formula given in (11). r_p can be then used to approximate the a normalized r_{corr}
 195 with its Taylor expansion [25]:

195

$$r_{corr} = r_p + \kappa_1 r_p^3 + \kappa_2 r_p^5 + \kappa_3 r_p^7 \quad (14)$$

196 where κ_i are the radial distortion coefficients. The “perfect” approximation would be a
197 polynomial of infinite degree; however, this precision is not needed. Several studies, such as [26],
198 confirmed that for average camera lenses the first order is enough, while more coefficients are
199 required for fish-eye lenses.

200 r_{corr} calculated with (14) needs to be denormalized to obtain the undistorted μ_{i-corr} and
201 v_{i-corr} image coordinates for the image under study.

202

203 2.3. Elements to consider when dealing with cameras installed into UAVs operating outdoor

204

205 Several elements need to be taken in due consideration when operating outdoor with cameras
206 installed into UAVs:

207 • The camera is usually fitted into steerable gimbals, which may have the freedom to move
208 along one, two or even three axes (which would be formalistically called one-gimbal,
209 two-gimbal or three-gimbal configurations, [1]). In those cases where the gimbal has
210 limited degrees of freedom, further steering capacity for the camera must be provided by
211 the UAV itself via flight rotations.

212 • The parameters required for the transformation from world coordinate system to camera
213 coordinate (extrinsic parameters) are given by GPS measurements (latitude, longitude, and
214 elevation) and Euler angles (yaw, pitch, and roll). Regular GPS receivers, which are not
215 subject of enhancements such as Differential GPS, may be affected by a relevant positional
216 error, especially in elevation. On the other hand, the orientation angles are measured by
217 sensitive gyroscopes, which usually have very good accuracy [27].

218 • The parameters for the projective transformation from the 3-D camera’s coordinates into
219 the 2-D image coordinates (intrinsic parameters) must be known. For those cases where the
220 UAV camera specs are not available, the intrinsic parameters (image principal point, focal
221 length, and skew) can be retrieved using calibration procedure provided, for example, by
222 computer vision open libraries such as OpenCV [28].

223 • The UAV can orient the camera to have the target centered in the image plane. Besides
224 being a common practice in UAV operations for tracking, is a mandatory requirement for
225 the calculation of height.

226 • The camera is usually oriented in such a way to have the feature of interest centered in the
227 image plane. Tracking algorithms [28] can be used to automatically kept the camera
228 pointed toward the target.

229 • Each video frame or still image acquired by the UAV is usually accompanied by a set of
230 camera and UAV flight information, stored as metadata. The amount of information
231 actually stored varies from system to system. Advanced imaging equipment may provide
232 a complete set of metadata in KLV (Key-Length-Value) format in accordance with MISB
233 (Motion Imagery Standards Board) standards [29]. Lightweight UAV available in the
234 regular market are not always fitted with such advanced devices but, very often, are
235 capable to store a minimum set of metadata which includes on-board GPS coordinates,
236 flight orientation and camera orientation.

237 • Advanced UAV imaging systems are also fitted with laser range finders, which are capable
238 to measure the instantaneous camera-to-target distance and store this information as
239 metadata. The following paragraph describes in details the pinhole model for computer
240 vision analysis and its parameters.

241

242 2.4. Computer vision with cameras installed into UAVs

243

244 The actual camera pose of a “gimballed” optical sensor can be determined through a sequence
245 of homogeneous matrixes defining a number of transformations [30] that can be briefly summarized
246 as follow:

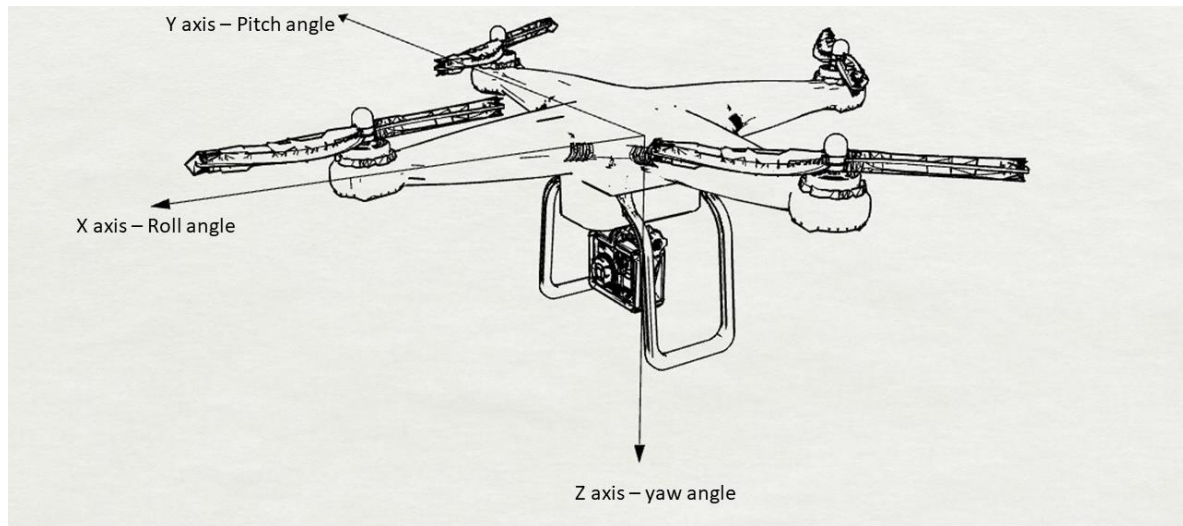
- 247 • Transformation from Inertial frame to UAV Vehicle Frame. The UAV vehicle frame is
248 identical to the inertial frame, only translated to the UAV position. This transformation
249 requires a translation which only depends on the UAV's GPS location and barometric
250 altitude measurements.
- 251 • Transformation from UAV Vehicle Frame to UAV Body frame: this transformation consists
252 of a single rotation R , based on measurements of Euler angles that define the orientation of
253 the UAV. In aeronautics the Euler angles are usually expressed through the yaw (or
254 heading), pitch and roll.
- 255 • Transformation from UAV Body to Gimbal frame (where the origin of the gimbal frame is
256 the center of the gimbal): this requires a translation which depends on the location of the
257 UAV's center of mass with respect to the gimbal's rotation center and a rotation to aligns
258 the gimbal's coordinates frame with the UAV's body frame.
- 259 • Transformation from Gimbal to Camera frame (origin at the camera's center): this
260 transformation depends on the vector that describes the location of the gimbal's rotation
261 center relative to the camera center and it is resolved in the camera's coordinate frame. It
262 also depends on a simple rotation that aligns the camera's coordinate frame with that of
263 the gimbal.

264 Large UAVs, which are also called MALEs (Medium Altitude Long Endurance, [31]), are
265 usually fitted with three-gimbaled advanced imaging systems and accurate positioning systems,
266 such as differential GPS. These systems are capable to calculate all the above-mentioned
267 transformation in real-time and embed the instantaneous camera pose, and other information such
268 as FOV and image footprint on ground, into the acquired video stream using the KLV
269 (Key-Length-Value) encoding protocols [29], in accordance to military standards [32].

270 On the other hand, non-military lightweight UAVs available in the regular market are not
271 always fitted with advanced imaging systems and very accurate GPS. For example, the DJI Phantom
272 4 PRO (a widely diffused multi-rotor platform of 1.388 kg, used to collect data for the testing of the
273 approach described in this paper, see Paragraph 3. Results). is not capable to generate KLV
274 embedded metadata but it can generate ancillary tags in Exchangeable Image File Format (EXIF) of
275 still images which provide, among other information, GPS position of the aircraft, aircraft
276 orientation and camera orientation at the moment of the acquisition of the still image. DJI Phantom 4
277 PRO has a GPS/GLONASS positioning system [33]. The actual accuracy of this positioning system is
278 not specifically indicated by the UAV manufacturer, but it can be roughly assumed between 1m and
279 3m in the condition of good satellite signal [34]. Moreover, it is necessary to underline that the
280 accuracy in altitude of the GPS readings is much lower than the accuracy on the horizontal plane
281 (Latitude, Longitude). The camera of this UAV has a pivoted support (one-gimbal) with a single
282 degree of movement along the Y axis (pitch angle, see **Figure 4**). Angular values are measured with
283 an accuracy of $\pm 0.02^\circ$ [33]. Although not specified in any available technical documentation but,
284 considering the available information of this UAV, it is here assumed that the transformation
285 employed to provide the information in the EXIF tags are the following: a) the translation defined by
286 the GPS coordinate of the UAV body, b) rotation based on Euler angles of the body followed by c) a
287 1D rotation of the camera (pitch angle). Therefore, the position of the camera when dealing with DJI
288 Phantom 4 PRO can be defined by UAV body positional location (GPS coordinates) while the
289 orientation is given by a yaw angle defined by flight orientation, a pitch angle defined by camera
290 orientation and a roll angle defined by flight orientation.

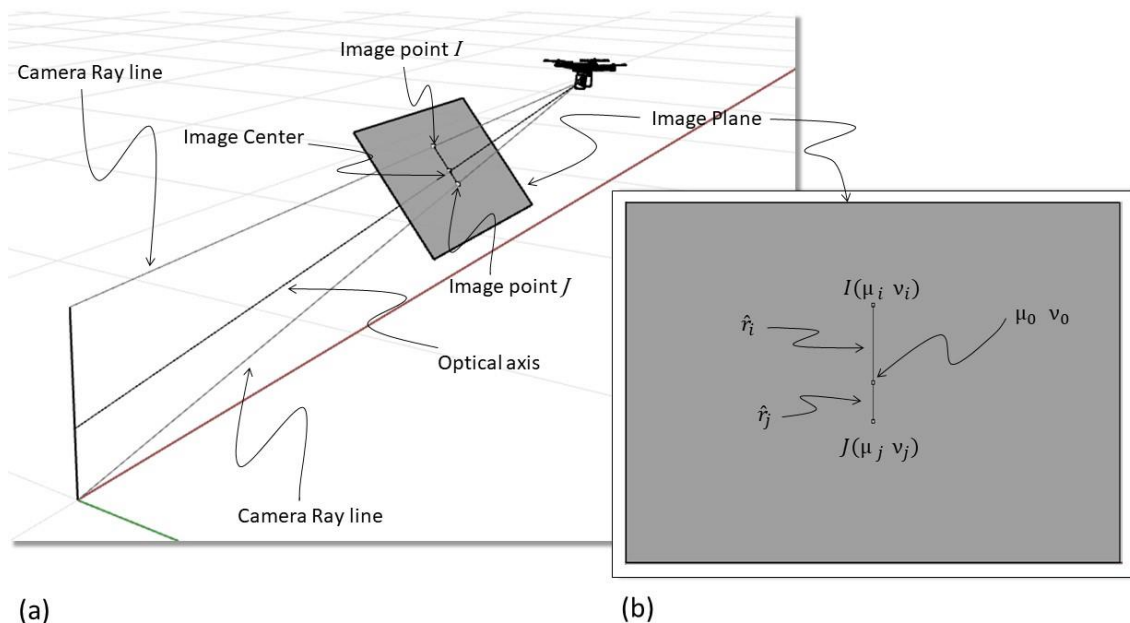
291 The camera sensor is a CMOS of 20M effective pixels with 5472×3648 resolution and $13.2 \times$
292 8.8mm size, lens focal length of 8.8mm with no optical zoom and FOV of 84° .

293



294
295 **Figure 4** Axis and Euler angles for the case of DJI Phantom 4 PRO.

296 Let's now assume to have a lightweight UAV, like the one described in **Figure 4**, and a feature
297 standing vertically on the ground, for example a pole. Let's also assume that the UAV has a heading
298 (Yaw angle) and pitch angle appropriate to pointing to the target as graphically represented in
299 **Figure 5**. Let's also assume that the roll angle is equal to zero.
300



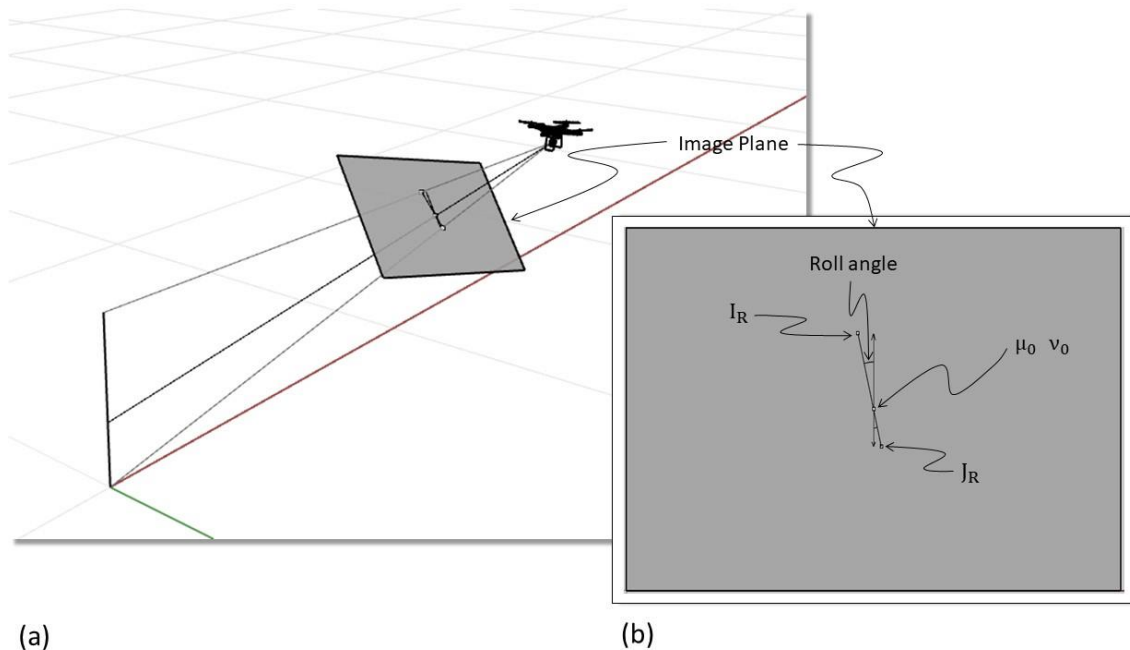
301 (a) (b)
302 **Figure 5** graphical representation of a lightweight UAV pointing to a vertical pole (a) with Roll angle equal to
303 zero. In (b) the image plane is represented in orthogonal view (as it would appear on screen).

304 Point μ_0, ν_0 in **Figure 5b** is the camera center, which is obtained, as already described, by the
305 interception between the image plane and the optical axis (see **Figure 5a**). The optical axis is centered
306 to the target, not necessarily the midpoint but any point of the pole. The Image Point I is given by the
307 interception of the camera ray line that connects the tip (highest point) of the pole with the camera
308 center. This point is expressed by the image coordinate μ_i, ν_i while \hat{r}_i represents the distance from
309 the image center. Moreover, \hat{r}_i is a distorted value that needs to be compensated to obtain the
310 distance r_{i-corr} of the ideal undistorted image. The procedure to obtain such undistorted distance
311 was already discussed in the previous paragraph (see (14)). Similarly, the Image Point J is the
312 interception of the image plane with the ray line that connects the bottom of the pole (lowest point)

313 with the camera center. The point is expressed by the image coordinate μ_j, v_j while \hat{r}_j represents the
 314 distance from the image center that needs to be compensated to get r_{j-corr} , the undistorted distance
 315 from the center of the ideal undistorted image. The line I-J in the image plane is the height of pole
 316 expressed in pixels in the image plane.

317 Let's now consider the same case when the Roll angle is different than zero, as graphically
 318 represented in **Figure 6**.

319



320

321 **Figure 6** graphical representation of a lightweight UAV pointing to a vertical pole (a) with Roll angle different
 322 than zero. Orthogonal view of the image plane (b) with the representation of the pole and indication of the Roll
 323 angle.

324 When the Roll angle is different than zero, the line I_R - J_R , which is the representation of the pole
 325 in the image plane, will not appear as parallel to the v axes, as in the case before, but rotated of an
 326 angle equal to the Roll angle itself, as it possible to infer from (7). As mentioned above, the observed
 327 distances (respectively \hat{r}_{Ri} and \hat{r}_{Rj}) must be compensated to obtain the distances $r_{Ri-corr}$ and
 328 $r_{Rj-corr}$ of the ideal undistorted image.

329 The next paragraph describes how to estimate the height of a target standing vertically (pole)
 330 considering the elements discussed so far in this paper. It is used, as an example, a lightweight UAV
 331 like the DJI Phantom 4 PRO but the approach can be extended to any imaging system installed in
 332 steerable moving platforms.

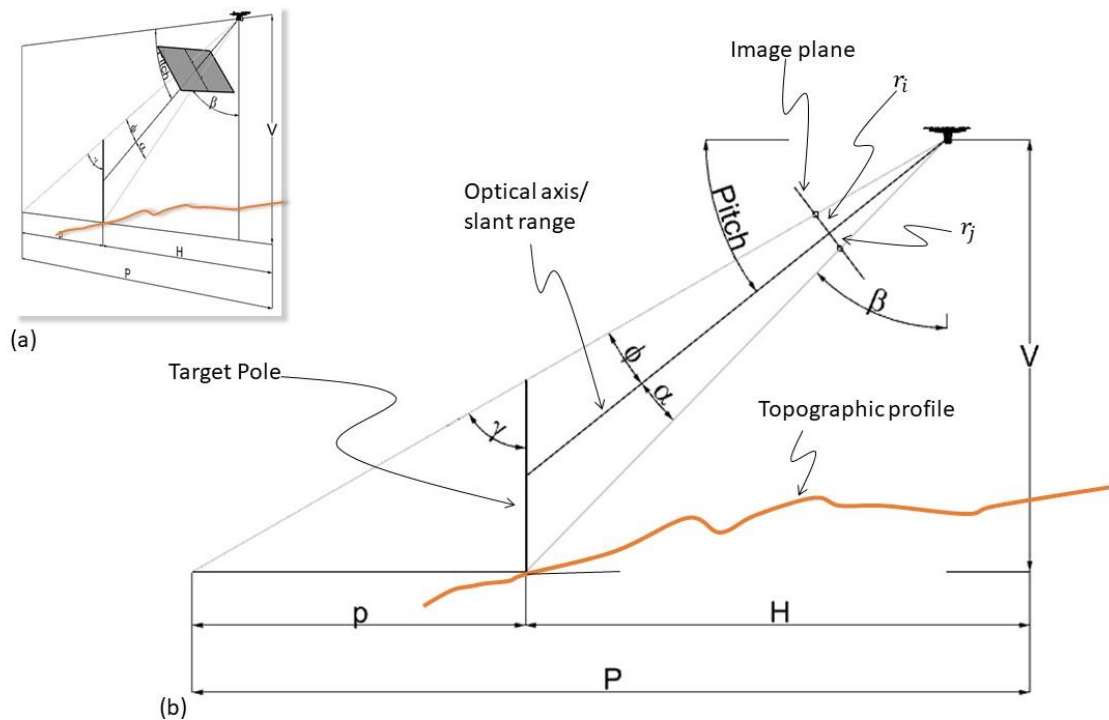
333 2.5. Estimating target height with camera fitted into UAVs

334 The approach proposed in this study for the estimation of target height using camera fitted into
 335 UAVs foresees the UAV pointing at the target as depicted in **Figure 5** and **Figure 6**. Let's get started
 336 with the case when the roll is zero (see **Figure 7**).

337

338

339



340

341

342

Figure 7 Perspective view of a lightweight UAV pointing to a vertical target (pole) (a). Orthogonal view of the same scene with descriptions (b).

343

344

345

The pitch angle, which can be also identified with θ_y , see (9) is a known value, while the angles α , β , ϕ , γ are not originally known but they can be retrieved using simple trigonometric calculations:

$$\alpha = \tan^{-1}\left(\frac{r_{j-corr}}{F}\right) \quad (15)$$

$$\beta = 90 - (\theta_y + \alpha) \quad (16)$$

$$\phi = \tan^{-1}\left(\frac{r_{i-corr}}{F}\right) \quad (17)$$

$$\gamma = (\phi + \beta + \alpha) \quad (18)$$

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Where r_{i-corr} can be calculated considering (14) in the previous paragraph starting from the observed r_i in the image plane (see **Figure 7**). Similarly, r_{j-corr} refers to the point J (see also **Figure 5**). F is the focal length, which was defined by (3) and (4) (assumed here for simplicity that $F = F_v = F_u$).

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V in **Figure 7** is the vertical distance between the base of the target and the camera center, while H is the horizontal distance between the target and the camera center. To be underlined H and V are not related at all to the topography, as it is possible to infer in **Figure 7**. If the coordinates of the target are known, then H and V are also known since the GPS coordinate of the camera are available (see Paragraph 2.3. Cameras installed into UAVs). The accuracy of the GPS and how it will impact the estimation of the target height will be treated later in this paper, but, since the accuracy of altitude in the GPS readings is much lower than the accuracy on the horizontal plane (Latitude, Longitude), V is always calculated in function of H , as defined in (19) below.

$$V = H \tan(90 - \beta) \quad (19)$$

358 the angles α , β , ϕ , γ are now known, as well as the pitch angle, V and H . These elements can
 359 be used to calculate the height of the target using the triangles similarity theorem. In fact, P (see
 360 **Figure 7**) can be calculated as follow:

$$P = V \tan(\alpha + \beta + \phi) \quad (20)$$

361 p is which is the horizontal distance between the base of the target and the camera ray that
 362 passes thought the tip (highest point) of the target, which can be calculated as follow:

$$p = P - H \quad (21)$$

363 Finally, the height of the target can be calculated:

$$\text{Height of the Target} = p \tan(90 - \gamma) \quad (22)$$

364 As already mentioned, the horizontal distance between the target and the camera center can be
 365 determined if the coordinates of the target are known. In practice, this could be the case only when
 366 dealing with immobile features like trees or buildings. If the position of the target is not known, as it
 367 may happen for moving targets like humans, vehicles, etc., laser range finder devices can be used to
 368 measure the instantaneous camera-to-target distance (slant range). As already mentioned, advanced
 369 imaging systems are very often fitted with such devices [1] and the instantaneous distance
 370 measurements can be stored in the KLV metadata set [31].

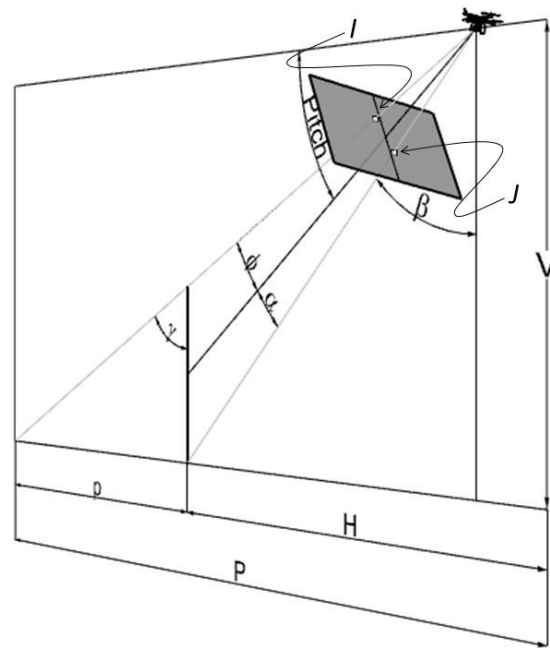
371 Slant Range values are distance is aligned to the optical axis of the camera (see **Figure 7**) and
 372 used to calculate the horizontal distance H using the following formula:

$$H = \text{Slant Range Distance} * \sin(90 - \text{Pitch angle}) \quad (23)$$

373 To be underlined that also the Slant Range distances measured by laser range finders are
 374 affected by a certain error that should duly be considered during the estimation of target height.
 375
 376

377 Let's now analyze the case when the roll angle is different than zero. In this case, as already
 378 discussed (see **Figure 6**) the points I and J are not located along the v axis passing on the center of the
 379 image. In other words, a vertical feature will appear as "tilted" in the image on an angle equal to
 380 Roll. However, as it possible to infer from (10) and as graphically represented in **Figure 8**, I and J are
 381 in the same (vertical) plane than Pitch angle. In other words, the approach presented in this paper
 382 does not need to consider the Roll angle for the calculation of target height. Also, in this case it is
 383 necessary to perform distortion correction to obtain r_{i-corr} and r_{j-corr} and use these parameters in
 384 the formulas previously described (see (15) and (17)).

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Figure 8 Perspective view of the image plane with visualization of the I and J, representing respectively the top and the bottom of the pole in the image plane.

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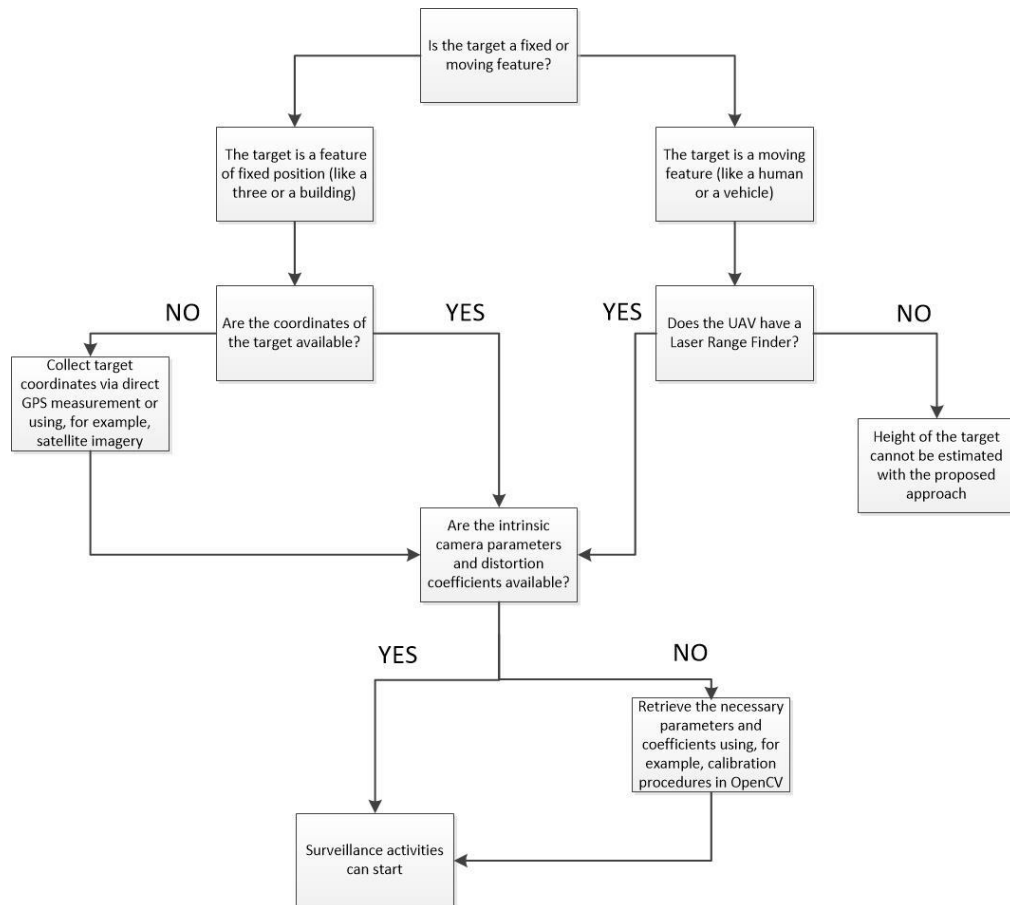
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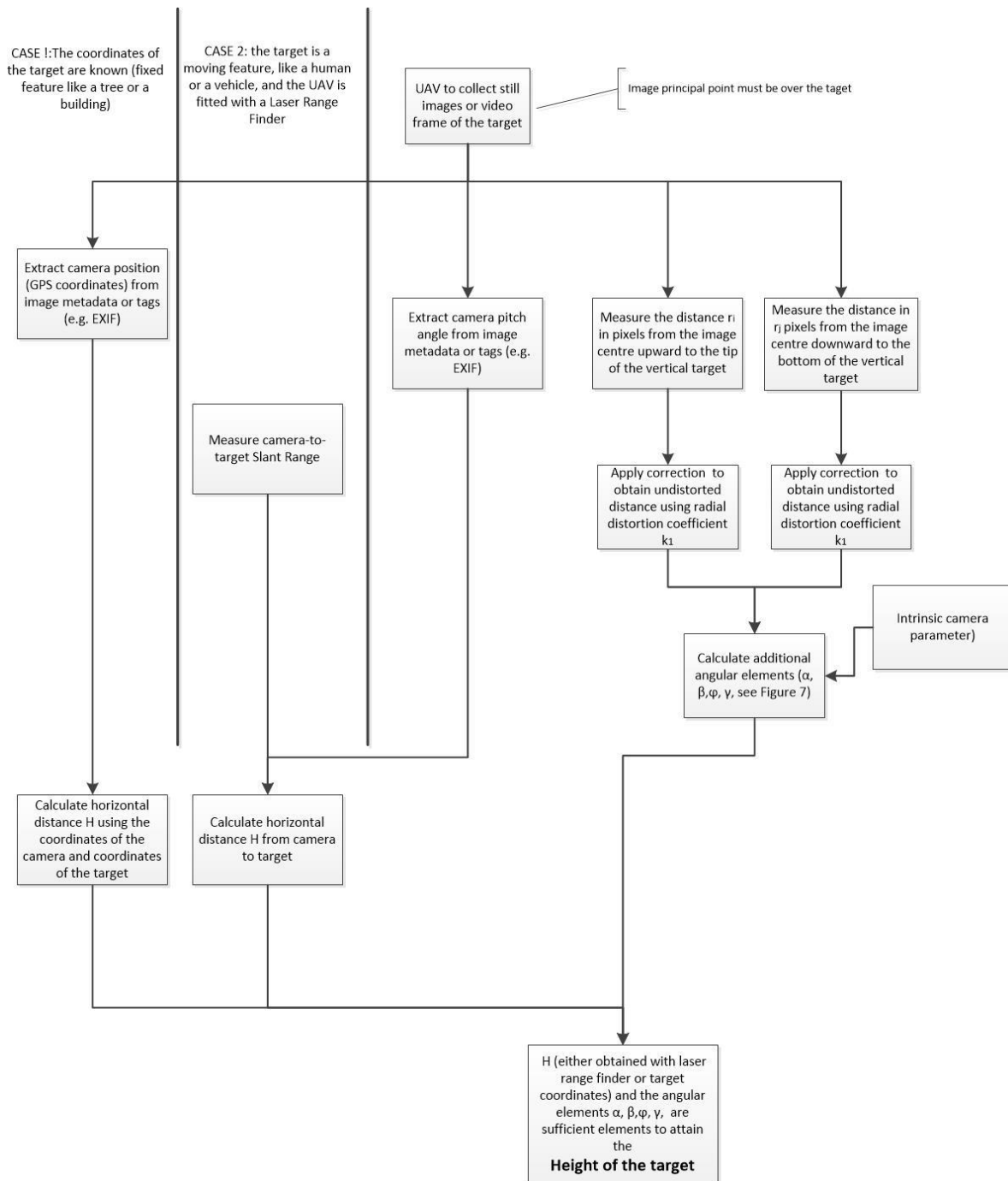
2.6. Workflows for target height estimation

The approach described in the following paragraphs is here summarized through workflows which are intended to be of practical use. The first workflow in **Figure 9** should be considered during the planning phase prior to initiate a surveillance campaign to define if all the condition to estimate the height of the target feature are in place. It is necessary to underline that if the target is a moving feature and the UAV is not equipped with a laser range finder, it would not be possible to estimate the height of the target with the proposed procedure. This is relevant limitation should be addressed in future studies. The second workflow (**Figure 10**) describes the actions to perform during the UAV flight to obtain all the information needed to calculate feature height.



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Figure 9 Workflow to verify if all the conditions to estimate the height of the target feature are in place. This analysis should be done during the planning phase prior to initiate a surveillance campaign.

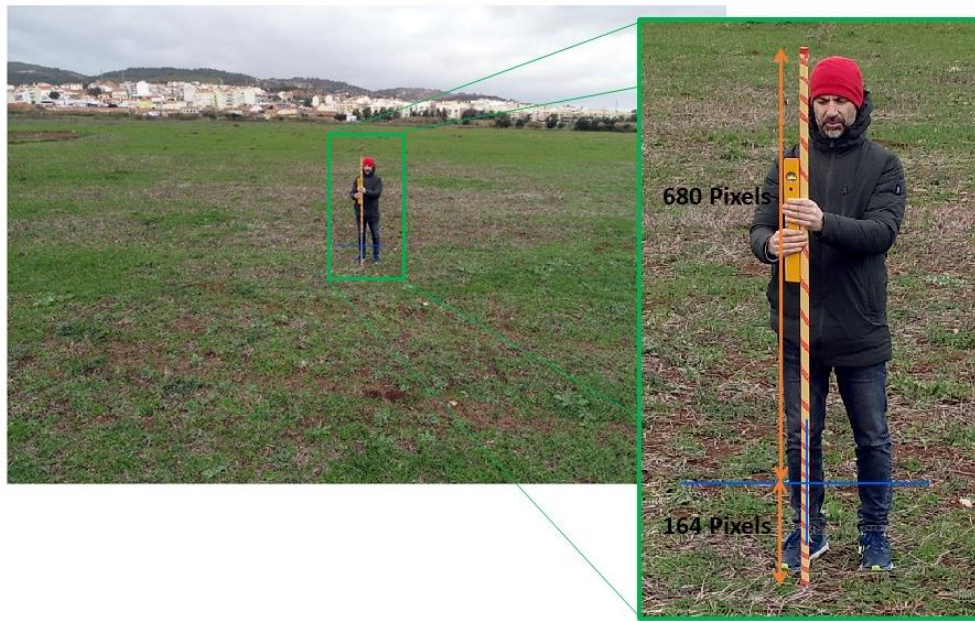


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 406 **Figure 10** Workflow describing the actions to perform during the UAV flight to obtain all the information
 407 needed to calculate feature's height.

408 3. Results

409 The procedure to estimate target height described in the previous section was tested using real
 410 data acquired with a DJI Phantom 4 PRO (see Paragraph 2.3. Cameras installed into UAVs for
 411 technical details regarding this device and camera used). In this field test it was used as target a
 412 wooden pole of 180 cm standing vertically from ground located in a position of known coordinates.
 413 32 still images were acquired with different camera poses and, in each acquired image, the principal
 414 point was always oriented over the pole (any point along pole as defined in **Figure 6**). Images not
 415 properly oriented (principal point not located over the pole) were discarded and not used in this
 416 study. The images were acquired in an open space with good visibility to satellites.

417 GPS readings (position of the UAV in WGS84 geographic coordinates) and camera pitch angle
 418 of each image were extracted from EXIF tags while the number of pixels spanning upward from
 419 image principal point (r_i) and downward (r_j) were measured manually on screen (see also **Figure**
 420 **11**). The Lat-Long coordinates of each image were plotted into a GIS environment along with the
 421 position of the reference pole to measure horizontal distance (H values, as graphically described in
 422 **Figure 7**). The first part of the **Table 1** and **Table 2** provides the above-discussed data for all the
 423 acquired images.
 424



425 **Figure 11** Still image acquired with DJI Phantom 4 PRO with image principal point (visualized in the picture
 426 with a blue cross) located over the pole. The number of pixels spanning upward (680) and downward (164)
 427 from the image principal point were measured manually on screen. A level of 0.4m length was kept tight and
 428 alight to the pole to maintain it vertical during the acquisition of each shot.
 429

430 As mentioned in the previous paragraph, the GPS readings have an accuracy between 1 to 3m.
 431 An accuracy of 1m means that the real position of the UAV is not known, but it must be located (with
 432 a probability of 95%) within a circle of 0.5 radius around the GPS readings given in the EXIF tag.
 433 Therefore, the distance of the UAV from the pole could be any value within $H+0.50\text{m}$ and $H-0.50\text{m}$.
 434 In **Table 1** and **Table 2** this element has been reported as $H+\text{GPS Err}$ and $H-\text{GPS Err}$ for each image.
 435 The accuracy of the angular measurement is $\pm 0.02^\circ$ (see Paragraph 2.3. Cameras installed into
 436 UAVs), which is neglectable for the purpose of this study.

437 In the paragraph 2.2 it was described the procedure to obtain a corrected distance from image
 438 center. Such a procedure was applied to each image obtaining the r_{i-corr} (number of corrected
 439 pixels from image center upward to pole's top point) and r_{j-corr} (number of corrected pixels from
 440 image center downward to pole's bottom). These values, as well as the total number of pixels
 441 spanning the entire pole, are reported in **Table 1** and **Table 2**. The Distortion Coefficient to be used
 442 for the correction was retrieved through camera calibration techniques [20] developed with OpenCV
 443 via Python programming.

444 The calculation of the target height (pole) was performed in accordance with the procedure
 445 described in the Paragraph 2.4. *Target height (NO GPS err)* in **Table 1** and **Table 2** indicates the
 446 estimated height of the pole considering the Horizontal distance considering the camera position
 447 indicated in the EXIF tags. On the other hand, *Target height (when H+ GPS err)* and *Target height (when*
 448 *H- GPS err)* in **Table 1** and **Table 2** provide the calculated height of the pole considering a GPS error
 449 of $\pm 0.5\text{m}$.

450 The field called *Height Uncertainty* in **Table 1** and **Table 2** represents the arithmetical difference
451 between *Target height (when H+ GPS err)* and *Target height (when H- GPS err)*.
452

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Table 1 data and results for the first 16 still images acquired with the lightweight UAV.

	DJI31	DJI32	DJI34	DJI41	DJ09	DJI12	DJI13	DJI15	DJI17	DJI18	DJI33	DJI35	DJI36	DJI37	DJI42	DJI_125	DJI42
Number of pixels upwards (r_i)	355	680	172	151	1358	1352	942	931	592	363	678	150	334	344	156	154	156
Number of pixels downwards (r_j)	1150	164	204	142	49	69	82	92	48	61	160	216	203	514	141	297	141
Gimbal pitch angle (degrees)	13.7	13.7	5.6	14.8	38.7	38.7	26.4	26.4	16	10.1	13.7	12	17.9	30.6	14.8	26.7	14.8
Flight roll angle (degrees)	1.8	0.9	4.2	5.2	0.4	0.8	0.5	0	0.6	0.3	1.2	2.9	3.3	0.8	1.3	3.6	1.3
Horizontal distance (H) (m)	4.2	7.9	17.1	21.28	3.6	3.64	6.04	6.17	10.28	14.96	7.95	17.38	11.62	6.04	21.12	11.78	21.12
H+ GPS err (m)	4.7	8.4	17.6	21.78	4.1	4.14	6.54	6.67	10.78	15.46	8.45	17.88	12.12	6.54	21.62	12.28	21.62
H- GPS err (m)	3.7	7.4	16.6	20.78	3.1	3.14	5.54	5.67	9.78	14.46	7.45	16.88	11.12	5.54	20.62	11.28	20.62
r_{i-corr} (upward) in pixels	355	679	172	151	1352	1346	940	929	591	363	677	150	334	344	156	154	156
r_{j-corr} (downward) in pixels	1146	164	204	142	49	69	82	92	48	61	160	216	203	514	141	297	141
Total number of pixels	1501	843	376	293	1401	1415	1022	1021	639	424	837	366	537	858	297	451	297
Target height (NO GPS err) (m)	1.94	1.87	1.78	1.83	1.77	1.82	1.89	1.93	1.87	1.77	1.87	1.83	1.87	1.98	1.84	1.87	1.84
Target height (when H+ GPS err)	2.17	1.99	1.84	1.88	2.01	2.07	2.05	2.09	1.96	1.83	1.99	1.88	1.95	2.14	1.88	1.94	1.88
Target height (when H- GPS err)	1.71	1.75	1.73	1.79	1.52	1.57	1.73	1.78	1.78	1.71	1.75	1.78	1.79	1.82	1.79	1.79	1.79
Uncertainty (m)	0.46	0.24	0.10	0.09	0.49	0.50	0.31	0.31	0.18	0.12	0.23	0.11	0.16	0.33	0.09	0.16	0.19

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Table 2 data and results for the remaining 16 still images acquired with the lightweight UAV (continuation of **Table 1**).

	DJI143	DJI144	DJI148	DJI149	DJI150	DJI151	DJI152	DJI153	DJI154	DJI155	DJI156	DJI157	DJI40	DJI43	DJI137
Number of pixels upwards (r_i)	207	359	32	83	68	112	241	156	307	339	573	902	254	114	136
Number of pixels downwards (r_j)	208	75	86	26	102	90	145	78	304	280	559	211	180	161	33
Gimbal pitch angle (degrees)	38.5	39.4	6.9	16.6	30.4	47.3	20.7	10.7	34.4	34.4	34.5	41.7	22.9	22.4	15.5
Flight roll angle (degrees)	9.6	8.5	5.5	8.6	3.1	3	3.8	5.2	3.3	4.2	2.8	7.1	1.9	1.1	5.6
Horizontal distance (H) (m)	9.51	9.71	54.24	54.49	28.33	15.33	14.85	26.68	7.43	7.3	4.22	4.13	13.38	21.08	37.12
H+ GPS err (m)	10.01	10.21	54.74	54.99	28.83	15.83	15.35	27.18	7.93	7.8	4.72	4.63	13.88	21.58	37.62
H- GPS err (m)	9.01	9.21	53.74	53.99	27.83	14.83	14.35	26.18	6.93	6.8	3.72	3.63	12.88	20.58	36.62
r_{i-corr} (upward) in pixels	207	359	29	83	68	112	241	156	307	339	573	900	254	114	136
r_{j-corr} (downward) in pixels	208	75	84	26	102	90	145	78	304	280	559	211	180	161	33
Total number of pixels	415	434	118	109	170	202	386	234	611	619	1132	1111	434	275	169
Target height (NO GPS err) (m)	1.79	1.84	1.79	1.78	1.79	1.84	1.78	1.77	1.83	1.81	1.95	1.96	1.86	1.87	1.85
Target height (when H+ GPS err)	1.89	1.93	1.81	1.80	1.82	1.90	1.84	1.80	1.96	1.93	2.18	2.20	1.93	1.91	1.87
Target height (when H- GPS err)	1.70	1.75	1.77	1.77	1.75	1.78	1.72	1.74	1.71	1.69	1.72	1.73	1.79	1.82	1.82
Uncertainty (m)	0.19	0.19	0.03	0.03	0.06	0.12	0.12	0.07	0.25	0.25	0.46	0.48	0.14	0.09	0.05

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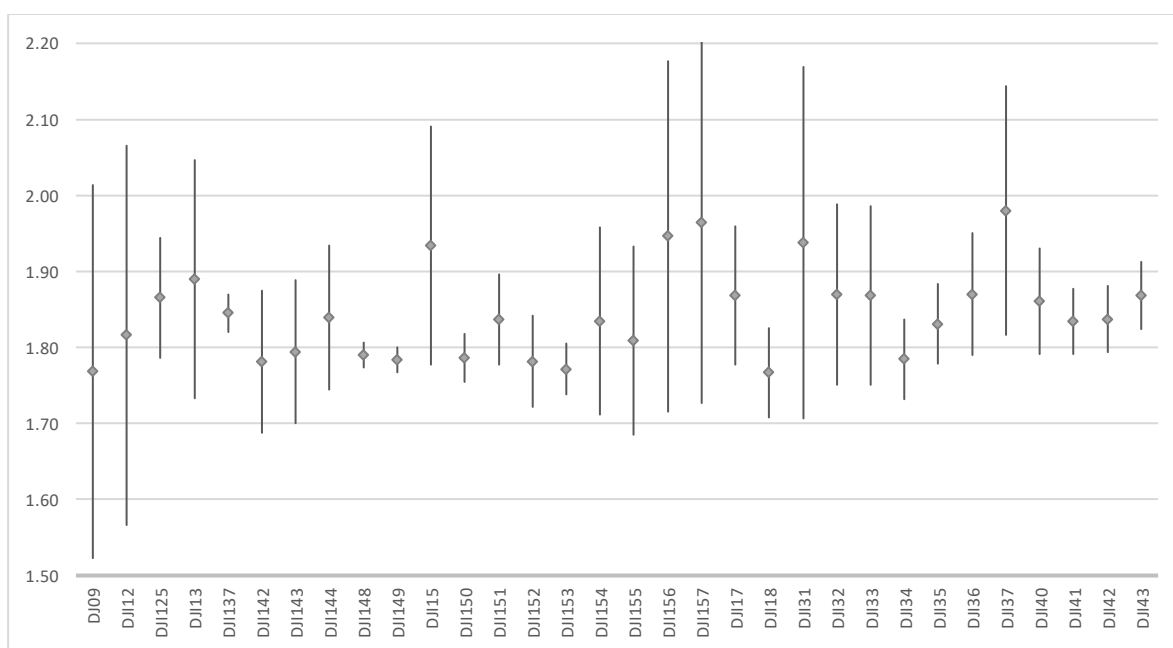
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467 Looking at *Target height (NO GPS err)* in **Table 1** and **Table 2**, the results clearly indicate that in
 468 almost no image the correct height (180cm) is obtained. However, considering *Target height when H+*
 469 *GPS err* and *Target height (when H- GPS err)*, which give interval from the highest and lowest possible
 470 height value considering the GPS error, we can see that 180cm is (almost) always within the range of
 471 each image. This can be also visualized in **Figure 12**. Only the images DJI137, DJI43 and DJI137 don't
 472 include the real value (1.80m) within their range, assuming a GPS error of +/- 0.5m.

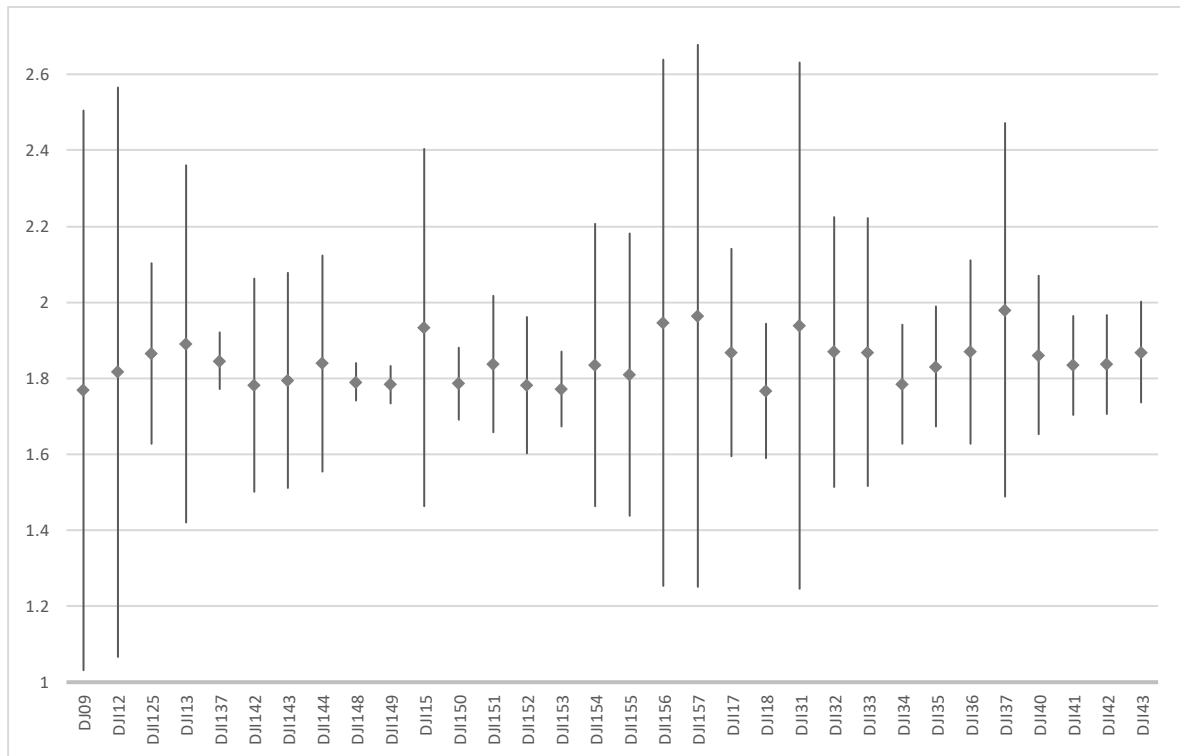
473 In other words, the accuracy in the estimation of target height depends on the error associated
 474 to the horizontal distance H. In a real case scenario, taking for example the case of the image DJI143
 475 (first column on **Table 2**), we could only say that the real height of the target has a value included
 476 between 1.70m and 1.89m (0.19m interval).
 477



478 **Figure 12** Grey rhombus represent the target height calculated considering GPS reading extracted from the
 479 EXIF tags for each acquired image, while the vertical lines represent the uncertainty when GPS error is 1m.
 480

481 Let's now analyze the case when GPS is assumed to be 3m (the results of this analysis are not
 482 ere reported in a tabular format but only graphically in **Figure 13**). The first element to notice is that
 483 the accuracy intervals have greatly increased, for example for DJI143 the real value may range
 484 from 1.51m to 2.08m (0.57m interval), three times bigger than the interval obtained when the
 485 horizontal accuracy was assumed to be 1m. The second element to underline is that all the images
 486 have the real height value (1.80m) included in their interval. Even those images that did not have the
 487 right height within their interval assuming a positional accuracy of 1m (DJI137, DJI43 and DJI137).
 488 This simply means that the positional accuracy of those three images is more than 1m and below 3m.

489 In the case here under discussion the horizontal distance was calculated considering the
 490 coordinates of the target and UAV. A similar approach should be also considered when dealing with
 491 slant-range measurements obtained with laser range finders installed into UAVs. These devices may
 492 measure distances with a certain error that, taking into the account (23), generate uncertainty in the
 493 correct estimation of target height, as seen for the case above.
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Figure 13 Grey rhombus represent the target height calculated considering GPS reading extracted from the EXIF tags for each acquired image, while the vertical lines represent the uncertainty when GPS error is 3m.

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We should also notice in **Figure 12** and **Figure 13** that the uncertainty is not constant, but it rather changes substantially from image to image. An uncertainty analysis can be conducted using the data described in Table 1 and Table 2 to verify how the parameters involved in the calculations are affecting the uncertainty.

The first parameter to consider is the Pitch angle. However, this parameter may depend on which part of the vertical target the camera is pointing to (see **Figure 7**). To avoid this issue, it is preferable to consider the Pitch angle plus α angle, in this way we always refereeing to the bottom point of the pole in every image. In **Figure 14** the angles obtained by the Pitch angle plus the α angle are plotted against the Height Uncertainty values of the images described in Table 1 and Table 2 (horizontal accuracy of 1m). The data distribution looks quite sparse although we may say that the uncertainty is generally growing when the Pitch angles are higher, as the best linear fit and its coefficient of determination can also attest.

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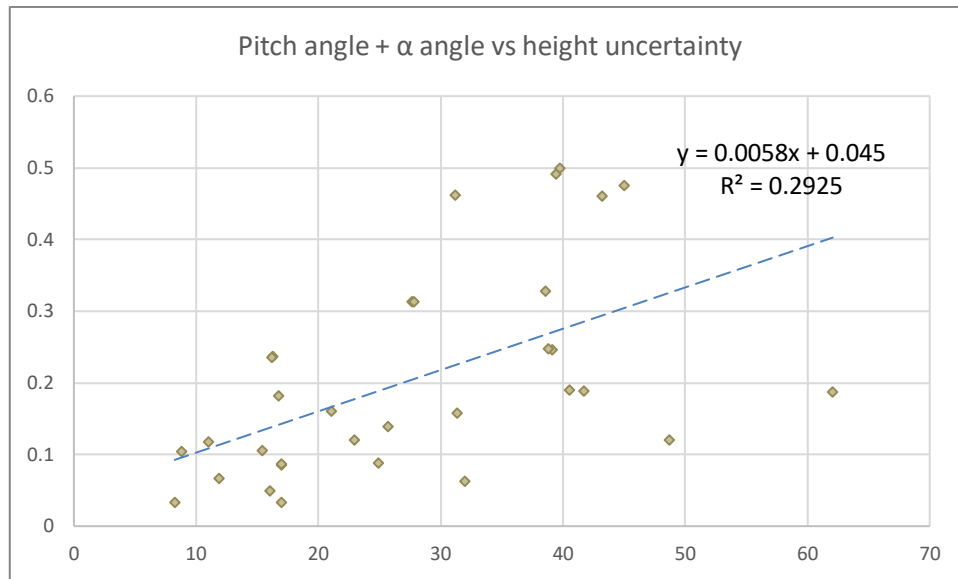
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The second parameter to consider is the camera-to-target horizontal distance H . If we plot in a graph the uncertainty against the horizontal distance, we can notice a clear relationship between them (see **Figure 15**). They are related by an exponential relationship which tells us that the accuracy is lower when the horizontal distance is higher. In **Figure 15** it is reported the equation of the curve that best fits when the horizontal accuracy of 1m.

The distance from the image center to top and bottom of the pole measure in pixels after distortion correction (r_{i-corr} and r_{j-corr}) should be also considered. However, as seen for the Pitch angle, also these parameters depend on which part of the vertical target the camera is pointing to. It is therefore preferable to consider the total number of pixels spanning the feature (the pole) for this analysis. In **Figure 16** the Total Number of Pixels for each image was plotted against the Height Uncertainty. The data distribution shows a quite evident linear trend, the equation of the best linear fit and its coefficient of determination are also reported in the figure.

Finally, intrinsic camera parameters should be also considered to analyze how they influence the overall accuracy. This analysis was not performed in this study because all the images were acquired with the same camera configuration.



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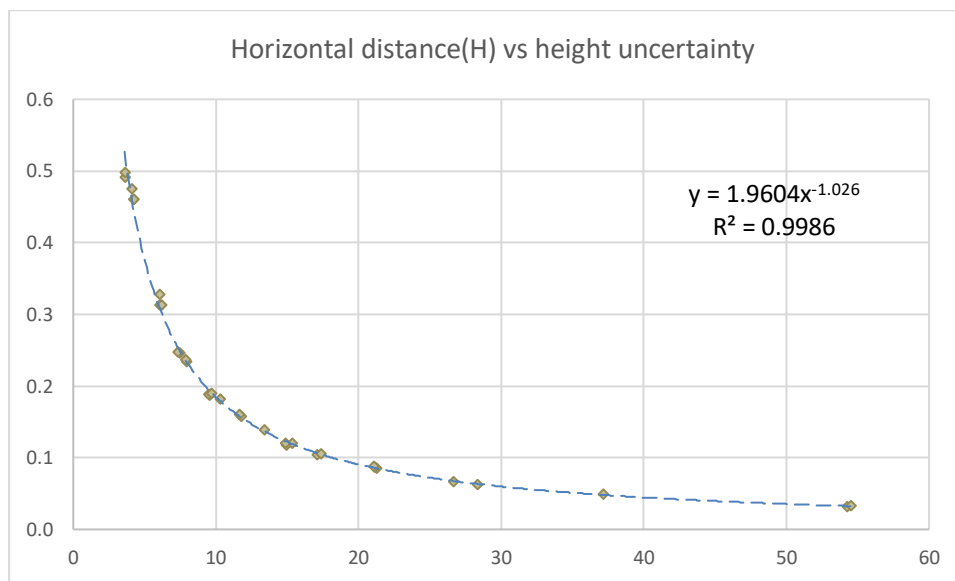
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Figure 14 Pitch angle plus α angle expressed in degrees (y) vs uncertainty values expressed in meters (x) for the images described in Table 1 and Table 2. The equation of the best linear fit and its coefficient of determination are also reported.

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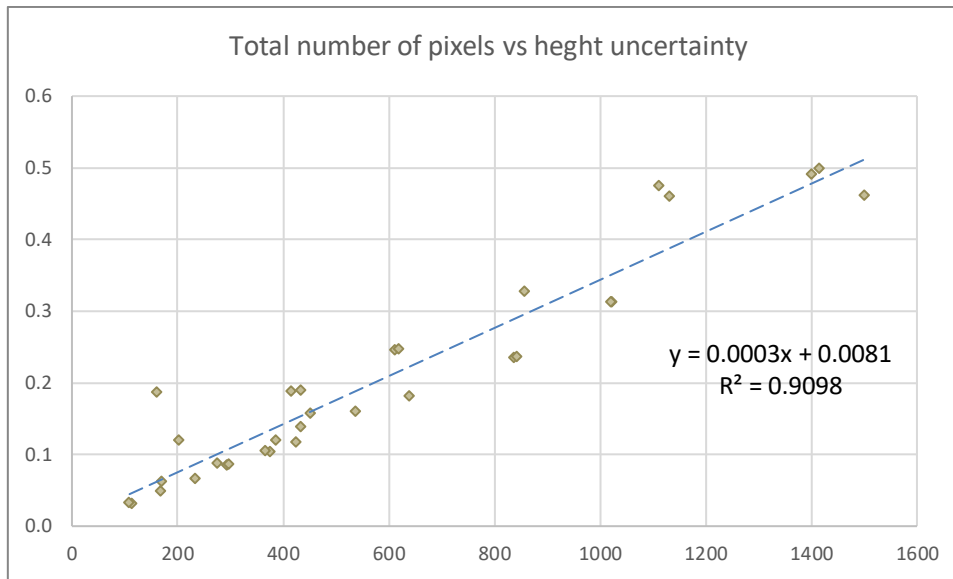
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Figure 15 Horizontal distance expressed in meters (y) vs uncertainty values expressed in meters (x) for the images described in Table 1 and Table 2. The equation of the best exponential fit curve and its coefficient of determination are also reported.



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Figure 16 Total Number of Pixels (y) vs uncertainty values expressed in meters (x). The equation of the best linear fit and its coefficient of determination are also reported.

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The graph in *Figure 15* is particularly interesting. The regression curve has an extremely good coefficient of determination to the data; therefore, the equation of the curve can tell us quite precisely which is the expected accuracy considering a certain distance from the target.

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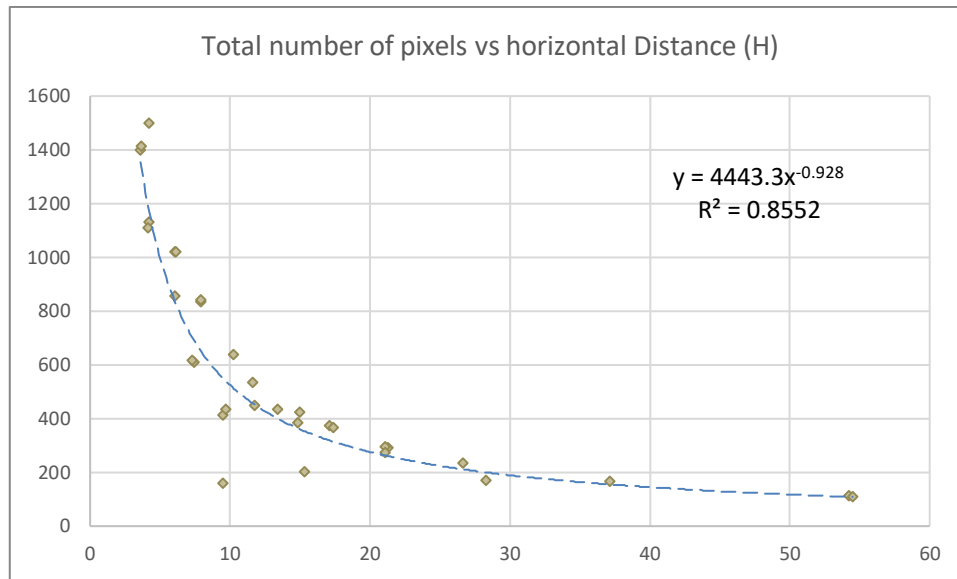
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Although not directly related to uncertainty analysis, it is also interesting to analyze the correlation between Total Number of Pixels and the Horizontal Distance, this is shown in *Figure 17*. The data distribution can be well fitted with a power regression curve, whose equation and coefficient of determination are reported in the graph. This relationship is valid for a target of 1.80m, which was the height of the pole used in this study; further research should be conducted to verify if there is a clear and well predictable relationship also for different target heights. If this is the case, the target-to-target distance could be no longer a required parameter for the calculations. The relationship shown in *Figure 17* also explains the linear correlation between Height Uncertainty and Total Number of Pixels seen in *Figure 16*. On the other hand, there is no evident relationship between pith angle and number of pixels as shown in *Figure 18*.



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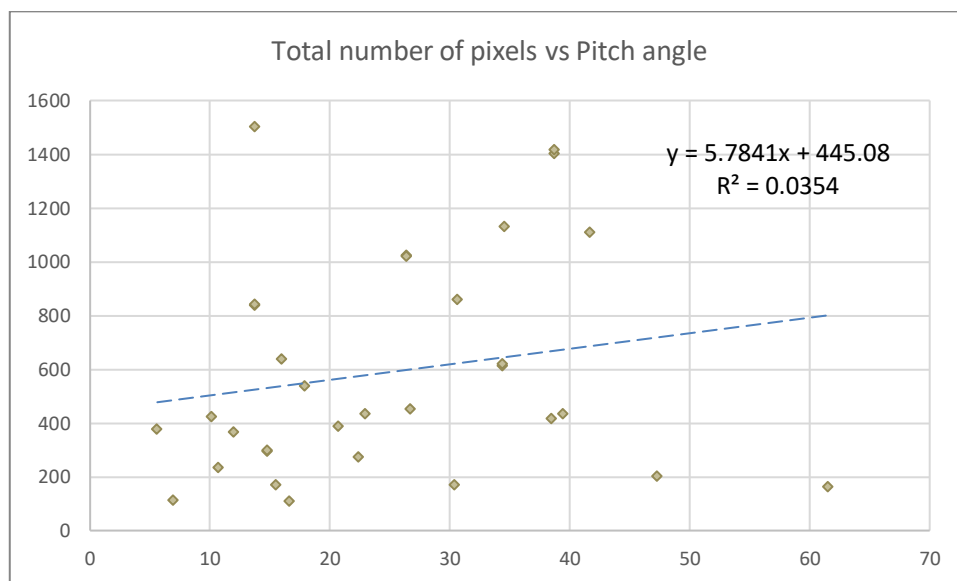
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Figure 17 Total Number of Pixels (y) vs horizontal distance expressed in meters (x) for the images described in Table 1 and Table 2. The equation of the best regression curve and its coefficient of determination are also reported in the figure.

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Figure 18 Total number of pixels (y) vs Pitch angle expressed in degrees (x) for the images described in Table 1 and Table 2. The equation of the best linear fit and its coefficient of determination are also reported.

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Finally, it is interesting to analyze the impact of an inaccurate distortion correction. A non-accurate correction, that may lead to an erroneous value of the distance from the image center measured in pixels. Therefore, it is important to understand how a variation of number of pixels may impact the estimation of the target height. To achieve this goal, 5 pixels were added to the total number of pixels (3 upward and 2 downward, the values were chosen arbitrary) and the height was recalculated to verify the variation. The results are reported in *Table 3*.

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The difference in height varies from 0.005m up to 0.08m, and it increases linearly with the horizontal distance, as we may expect. This analysis demonstrates that a non-accurate distortion correction may lead to an erroneous value of height, which is however much lower than the error associated to the horizontal distance. This statement is anyway true for the camera and UAV system used in this study; other cameras with a different resolution may give different errors.

571

572 **Table 3** The height calculated with the number of pixels measured in each image is compared with height

573 calculated by adding 5 pixels to the original number. The table reports also the difference between the height

574 calculated with the original number the height with when 5 pixels are added.

	Original total number of pixels	Height (m) considering Total number of pixels	Total number of pixels +5	Height (m) considering Total number of pixels +5	Height Difference (m)
DJI31	1501	1.94	1506	1.94	0.006
DJI32	843	1.87	848	1.88	0.011
DJI34	376	1.78	381	1.81	0.023
DJI41	293	1.83	298	1.86	0.031
DJ09	1401	1.77	1406	1.77	0.005
DJI12	1415	1.82	1420	1.82	0.005
DJI13	1022	1.89	1027	1.90	0.008
DJI15	1021	1.93	1026	1.94	0.009
DJI17	639	1.87	644	1.88	0.014
DJI18	424	1.77	429	1.79	0.020
DJI33	837	1.87	842	1.88	0.011
DJI35	366	1.83	371	1.86	0.024
DJI36	537	1.87	542	1.89	0.017
DJI37	858	1.98	863	1.99	0.010
DJI42	297	1.84	302	1.87	0.030
DJI125	451	1.87	456	1.88	0.019
DJI142	161	1.78	166	1.83	0.051
DJI143	415	1.79	420	1.81	0.020
DJI144	434	1.84	439	1.86	0.019
DJI148	118	1.79	123	1.86	0.074
DJI149	109	1.78	114	1.86	0.081
DJI150	170	1.79	175	1.84	0.051
DJI151	202	1.84	207	1.88	0.043
DJI152	386	1.78	391	1.80	0.022
DJI153	234	1.77	239	1.81	0.037
DJI154	611	1.83	616	1.85	0.013
DJI155	619	1.81	624	1.82	0.013
DJI156	1132	1.95	1137	1.95	0.007
DJI157	1111	1.96	1116	1.97	0.007
DJI40	434	1.86	439	1.88	0.020
DJI43	275	1.87	280	1.90	0.033
DJI137	169	1.85	174	1.90	0.054

575

576 4. Estimating the vertical length of target's subparts

577 In several occasions there might be the need to measure the length of subparts of the target. This
 578 is a common situation when the purpose of the surveillance activities is dedicated to estimate
 579 human body height.

580 In fact, the body height is the vertical distance from the bottom of bare feet to the top of the
 581 head, which shall be measured while the person is standing in a straight position [35]. If the person
 582 has a different pose, such as standing relaxed with weight on one leg or watching the telephone
 583 with the head tilted down, we would manage to estimate just the height of the body in that specific
 584 pose, not the real stature of the subject. On the other hand, in literature is well known the
 585 relationship between the height of a person its body parts (arms, hands, legs, etc.) [22] or and
 586 human face features ratio [23] obtained via experimental measures.

587 It is here proposed to determine pixel spacing expressed in length units (e.g. meters) measured
 588 along the vertical target, this pixel spacing can be used to estimate the length of body parts or face
 589 portions by counting the number of pixels spanning these sub-features. This is deemed to be the
 590 most practical approach to swiftly estimate the body stature when the subject does not have a
 591 straight pose in scene.

592
 593 The spacing in the vertical direction is here proposed to be called Vertical Sample Distance
 594 (VSD), which can be calculated as the GSD (Ground Sample Distance, [24]), but along the vertical
 595 axis perpendicular to the ground. GSD represents the distance between pixel centers measured on
 596 the ground. When the camera is looking vertically to the ground (viewing angle τ equal to zero, see
 597 **Figure 19**), GSD can be calculated as follow [36]:

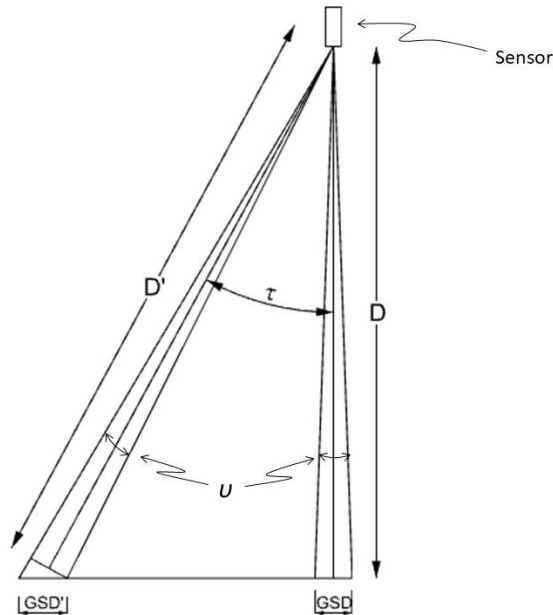
$$\text{GSD} = \frac{d}{F} D \quad (24)$$

598 Where d is the distance between detectors centers (pixel pitch), F is the focal length (see (3) and
 599 (4)) and D is the range. In the camera is not oriented perpendicular to the ground, τ is different than
 600 zero and the GSD must be corrected as follow, obtaining GSD' (see **Figure 19**).

$$\text{GSD}' = \frac{d}{F} D' \frac{1}{\cos \tau} \quad (25)$$

601 When dealing with UAVs, the GSD' is not a static but rather a dynamic parameter [37] since it
 602 changes according to the camera-to-target distance and viewing angle. Genrally speacking, we can
 603 say that each video frame has a specific GSD'.

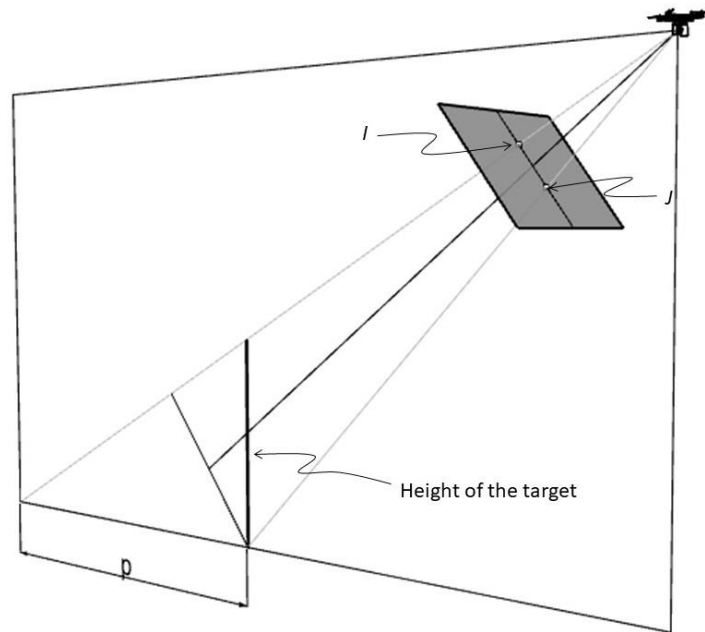
604



605

606 **Figure 19** GSD (when the looking angle τ is zero) and GSD' (when τ is different than zero). u is the Field of View
 607 of a single element (pixel) of the detector.

608 As graphically represented in **Figure 20** and expressed in (26), the sum of all the singles GSD' of
 609 the pixels spanning the vertical target in the image plane (distance from point I to point J) are equal
 610 to the distance p on ground (this distance has been previously mentioned during the calculations to
 611 obtain the height of the target, see (21).



612

613 **Figure 20** The horizontal distance p is the sum of the GSD' of each pixel spanning from the point I and J in the
 614 image plane. In analogy, the height of the target.

$$p = \sum_{n=i}^j GSD'_n \quad (26)$$

615 Dividing the distance p by the number of pixels spanning the feature in the image plane (I-J)
 616 would then give the average value of GSD' s for each pixel within the distance I-J measured on the
 617 image plane.

618 In this paper we propose to follow the same approach to calculate the sample distance on
 619 vertical planes, the Vertical Sample Distance (VSD), which can be calculated as follow considering
 620 **Figure 19**:

$$VSD' = \frac{d}{F} D' \sin \tau \quad (27)$$

621 In analogy to GSD , as graphically represented in **Figure 20** and expressed in (28), VSD of all the
 622 pixels spanning the vertical target are equal to height of the target.

$$\text{Height of the target} = \sum_{n=i}^j VSD'_n \quad (28)$$

623 Dividing the height of the target by the number of pixels spanning the feature in the image
 624 plane (I-J) would then give the average value of VSD' for each pixel spanning the feature in the
 625 image plane (distance I-J in **Figure 20**). As seen for GSD' , also VSD' is not constant, each image has a
 626 specific value that depends on the instantaneous camera-to-target distance and viewing angle.

627 More practically, we can measure the height of human subject using the procedure described in
 628 the previous chapters. If he subject does not have a straight pose, the height of the body in the
 629 specific pose can be anyway used to calculate the average VSD' (estimated target height divided
 630 the number of pixels spanning the target) and multiply this value for the number of pixels

631 spanning subject's subparts, such as face features or body parts, which can be used to retrieve the
632 real stature considering ratios or relationships available in literature.

633 Each pixel has a specific GDS' value and, in analogy to that, each pixel has a specific VDS'
634 value. The next paragraph intends to analyse the error generated by using the average VDS' instead
635 the real VDS of the pixels spanning the target subpart.

636 4.6. Field verification

637 The data acquired with DJI Phantom 4 PRO can be used to verify the error due to using average
638 VSD'. A level of 0.4m was kept tight and alighted to the pole to keep it vertical in each acquired
639 image. The length of this level could be considered, for the sake of this analysis, as a subpart of the
640 pole (see **Figure 11**).

641 For each mage (see **Table 1** and **Table 2**) the VSD was calculated dividing the real length of the
642 pole (1.80m) by the Total Number of pixels spanning the pole. The total number of pixels spanning
643 the level in each image was measured on screen and then corrected for lens distortion. This value
644 was then multiplied for VSD to obtain the estimated length of the level (see **Table 4**).

645

646 **Table 4** Data used to calculate the average VSD' and the estimated length of the level (real level length is 0.4m).

	Total Number of pixels spanning the pole	Average VSD' (m) (height of the pole = 1.80m)	Total Number of pixels spanning the level (after distortion correction)	Estimated length of the Level (m)
DJI31	1501	0.120	342	0.41
DJI32	843	0.214	191	0.41
DJI34	376	0.479	84	0.40
DJI41	293	0.614	66	0.41
DJ09	1401	0.128	320	0.41
DJI12	1415	0.127	324	0.41
DJI13	1022	0.176	230	0.41
DJI15	1021	0.176	228	0.40
DJI17	639	0.282	143	0.40
DJI18	424	0.425	93	0.39
DJI33	837	0.215	188	0.40
DJI35	366	0.492	81	0.40
DJI36	537	0.335	120	0.40
DJI37	858	0.210	194	0.41
DJI42	297	0.606	66	0.40
DJI125	451	0.399	100	0.40
DJI142	161	1.118	35	0.39
DJI143	415	0.434	91	0.39
DJI144	434	0.415	94	0.39

DJI148	118	1.525	26	0.40
DJI149	109	1.651	25	0.41
DJI150	170	1.059	38	0.40
DJI151	202	0.891	44	0.39
DJI152	386	0.466	85	0.40
DJI153	234	0.769	52	0.40
DJI154	611	0.295	133	0.39
DJI155	619	0.291	137	0.40
DJI156	1132	0.159	253	0.40
DJI157	1111	0.162	250	0.41
DJI140	434	0.415	30	0.39
DJI143	275	0.655	91	0.39
DJI137	169	1.065	37	0.39

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The results in **Table 4** show that the length of the level obtained using average VDS' gave a general error of less than 0.01m (real level length is 0.4m) which means that the average value of VDS the pixels involved in the calculation have a good average of the real value. However, this is clearly specific to the conditions analyzed in this study, namely height of the target of 1.80m, subpart of 0.4m, etc.

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5. Discussion: Future developments for an automatic estimation of human body height in near real-time using camera installed into UAVs

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Among all the possible applications of remote target height estimation using camera installed into UAVs, obtaining the real human body height is one of the most relevant. The method described in this paper, although not specifically focused on human target but usable also for other targets like trees or buildings, provides fundamental elements for this purpose.

The presence of human beings can be automatically detected in still images or video frames by computer vision algorithms, such as Histograms of Oriented Gradients (HOG) [38] and Viola Jones Object Detection Framework (Haar Cascades) [39] pre-trained for human detection. Those algorithms usually show the localization of a person via a rectangular boundary surrounding each object (see **Figure 21a**) that, if properly fitted to the human target (see **Figure 21b**), can be used to measure automatically the number of pixels spanning the target upward and downward from the image center. The camera position and orientation (camera pose) can be extracted from metadata embedded in the still images or video (e.g. KLV) to estimate in near real-time the height of the boundary box using the procedure described in this paper. If the person is standing straight in the image, the height of the bounding box could be assuming as the real stature of the subject. Otherwise, the height of the bound box divided the total number of pixels spanning the rectangle would give the average VSD'. Face identification algorithms [40] or other object recognition algorithms trained for body parts detection (such as arms, [41]) can be used to automatically detect subparts and count the number of pixels spanning vertically the face or other body parts. The number of pixels multiplied for average VSD' would give the vertical length of those parts, which

680 can be used to estimate the real stature of the human subject. Finally, we need always to take into the
681 account the accuracy of the estimation to define the range within which the real height would be.

682 However, to achieve a solid automatic estimation of human body height in near real-time
683 several developments still need to be implemented:

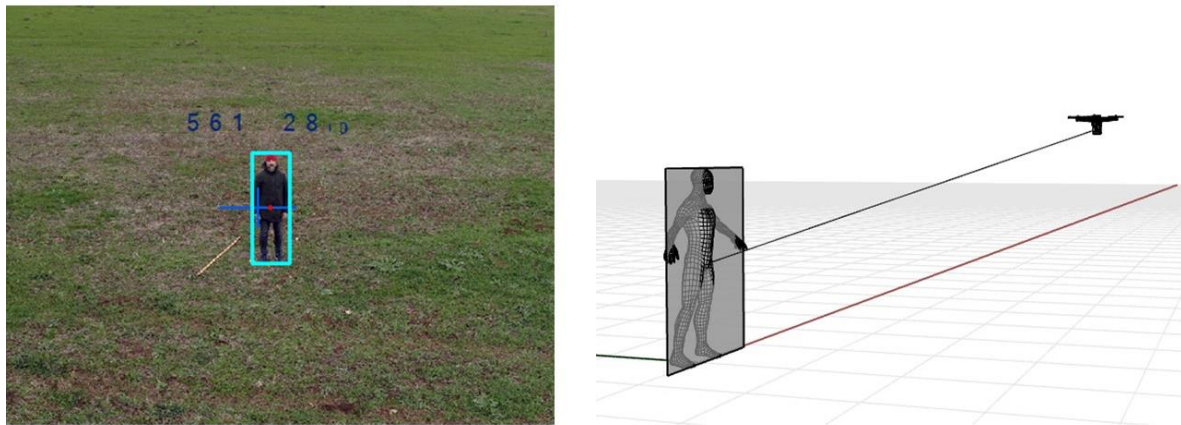
684 • The accuracy analysis associated to height estimation should consider also intrinsic
685 camera parameters. In this study the intrinsic parameters were not considered because
686 all the data (still images) were collected with the same camera.

687 • Algorithms previously trained for human detection available in freely available
688 libraries may have drawbacks such as missed detection, false detections and duplicated
689 detections for the same features. Deep Convolution Neural Networks should be used to
690 develop more robust human detection algorithms specifically dedicated for high angle
691 images usually acquired by UAVs [42].

692 • Generating accurate and consistent boundary rectangles between detections of the
693 same features in subsequent video frames is a key element to estimate real human body
694 height. A robust detection algorithm can only partially solve this issue. In fact, high
695 looking angles may generate non-vertical boundary rectangles (see **Figure 22**) that may
696 introduce an additional error in estimations of human stature. Further studies are
697 required to analysis these issues and identify suitable solutions to compensate for this
698 problem.

699 • VDS can be used to estimate the length of body parts oriented vertically from the
700 ground. However, very often, the body parts may be oriented differently (lets' think
701 about the ordination of the legs while walking, for example). Further studies should be
702 focused on how to measure distances in the vertical plane (see **Figure 21b**)
703 independently from the orientation of the subpart.

704 • Finally, it would be very important to analyse if height can be estimated without the
705 need of the camera-to-target distance. In fact, even a laser range finder, which is
706 mandatory payload device when dealing with moving targets such as people, may not
707 have enough accuracy for precise human height estimations. The graph in **Figure 17**
708 may be of interest in this respect, since it shows a clear relationship between the total
709 number of pixels and the horizontal distance, well describable by a power regression
710 curve. This relationship is valid for a target of 1.80m, which was the height of the pole
711 used in this study. Further studies should be conducted to analyze if there is also a clear
712 and well predictable relationship between the total number of pixels, horizontal distance
713 and the height. If this is the case, the target-to-target distance could be no longer a
714 required parameter for the calculations.



715

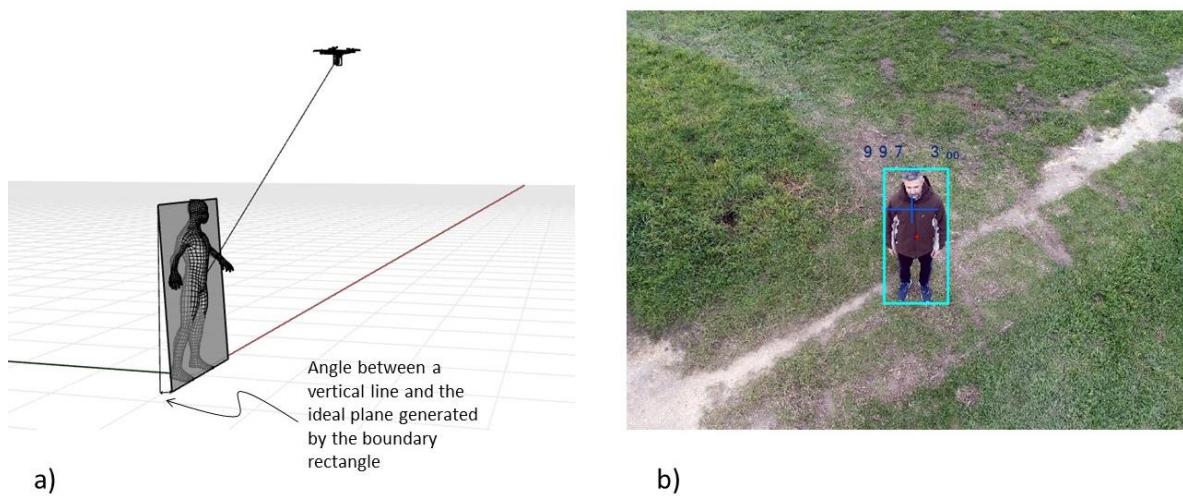
a)

b)

716

717 **Figure 21** a) human detection algorithms usually show the presence of person with a boundary rectangle (light
 718 blue, the red dot represents the center of the rectangle, blue cross indicates the center of the image, the number
 719 in the rectangle's top left corner indicates the total number of pixels spanning the rectangle, while the other
 720 number indicates the number of pixels from image center to the top of the rectangle). b) if the rectangle is
 721 properly fitted to the person, it can be used to measure the number of pixels spanning the target.

721



722

a)

b)

723

724 **Figure 22** a) Boundary rectangles generated by high looking angles may be not vertical. b) example of boundary
 725 rectangle in a real picture.

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5. Conclusions

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This paper described a procedure for the remote estimation of target height using gimbaled camera installed into a UAV. The procedure foresees the camera calibration and image distortion compensation before using a pinhole model to calculate geometrically the vertical length of a feature. The main strengths of this approach are the simplicity and rapidness. In fact, height estimation does not require special equipment or double cameras, a single still image or video frame acquired with an optical camera is sufficient. Moreover, no vanishing lines or objects of reference height are required to be present in the scene. Finally, just few parameters are required: intrinsic camera parameters, which are usually provided by manufacturer but they can also retrieved via computer vision analysis, camera pitch angle, usually available in metadata associated to the acquired images or video data, number of pixels spanning the feature, which can be measured either

736 manually or automatically using feature detection algorithms, and, finally, the distance between the
737 camera and target, which can be obtained using coordinates if the position of the target is known or
738 using devices to measure distances, such as laser range finders. These parameters are involved in
739 simple trigonometric calculations that can be very rapidly performed for near real-time applications.
740 Also, the processing for lens distortion compensation, which may be very time-consuming if
741 performed for the entire image, is very swift because it involves only a very little number of pixels.

742 On the other hand, the weakness of this procedure is related to the uncertainty of the
743 estimation, which is mainly linked to the error associated to the camera-to-target distance. Also,
744 inaccurate lens distortion correction procedures may introduce some error, but this study confirmed
745 that they are very minor compared to camera-to-sensor distance error. This distance, either acquired
746 via coordinates difference of measured via laser range finders, is always affected by a certain error
747 that generates an uncertainty in the height estimation. This paper has also analyzed how extrinsic
748 camera parameters are affecting the overall uncertainty, identifying interesting relationships that
749 may be used to define in advance the expected accuracy during surveillance activities. However, this
750 analysis did not take into consideration how intrinsic camera parameters are concurring to the
751 uncertainty, future studies should be dedicated to further develop this aspect. Future studies should
752 be also dedicated on how the height can be estimated without the need of the camera-to-target
753 distance. Along this line, this paper has shown a very well predictable relationship between the
754 number of pixels and the camera-to-target distance, additional studies should be conducted to
755 analyze if there is also a clear and well predictable relationship between the total number of pixels,
756 horizontal distance and the height. If this is the case, the target-to-target distance could be no longer
757 a required parameter for the calculations.

758 Another important element treated in this paper was the Vertical Sample Distance (VSD). The
759 height a person who is not standing perfectly vertical can be derived by relationships between body
760 parts or human face features ratio VDS can be used to estimate the length of body parts oriented
761 vertically from the ground. However, very often, the body parts may be oriented differently (lets'
762 think about the ordination of the legs while walking, for example). Further studies should be
763 focused on how to measure distances in the vertical plane (see Figure 21b) independently from the
764 orientation of the subpart.

765 Finally, the method described in this paper, although not specifically focused on human target
766 but usable also for other targets like trees or buildings, provides fundamental elements for an
767 automatic estimation of human body height in near real-time using camera installed into UAVs.

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778 References

- 779 1. Fahlstrom, P.G.; Gleason, T.J. *Introduction to UAV systems*; Aerospace series; 4th ed.; John Wiley & Sons:
780 Chichester, West Sussex, 2012; ISBN 978-1-119-97866-4.
- 781 2. European Aviation Safety Agency Introduction of a regulatory framework for the operation of drones 2017.

- 782 3. Jung, J.; Yoo, S.; La, W.; Lee, D.; Bae, M.; Kim, H. AVSS: Airborne Video Surveillance System. *Sensors* **2018**, *18*,
783 1939.
- 784 4. Cai, J.; Walker, R. Height estimation from monocular image sequences using dynamic programming with explicit
785 occlusions. *IET Computer Vision* **2010**, *4*, 149.
- 786 5. Negretti, P.; Bianconi, G.; Bartocci, S.; Terramocchia, S. Lateral Trunk Surface as a new parameter to estimate live
787 body weight by Visual Image Analysis. *Italian Journal of Animal Science* **2007**, *6*, 1223–1225.
- 788 6. Kim, M.-G.; Moon, H.-M.; Chung, Y.; Pan, S.B. A Survey and Proposed Framework on the Soft Biometrics Technique
789 for Human Identification in Intelligent Video Surveillance System. *Journal of Biomedicine and Biotechnology* **2012**,
790 *2012*, 1–7.
- 791 7. Ramstrand, N.; Ramstrand, S.; Brolund, P.; Norell, K.; Bergström, P. Relative effects of posture and activity on human
792 height estimation from surveillance footage. *Forensic Science International* **2011**, *212*, 27–31.
- 793 8. Rues, D.; Manthey, K.; Reulke, R. An accurate 3D feature tracking system with wide-baseline stereo smart cameras. In
794 Proceedings of the 2011 Fifth ACM/IEEE International Conference on Distributed Smart Cameras; IEEE: Ghent,
795 Belgium, 2011; pp. 1–6.
- 796 9. Cali, M.; Ambu, R. Advanced 3D Photogrammetric Surface Reconstruction of Extensive Objects by UAV Camera
797 Image Acquisition. *Sensors* **2018**, *18*, 2815.
- 798 10. Azevedo, F.; Dias, A.; Almeida, J.; Oliveira, A.; Ferreira, A.; Santos, T.; Martins, A.; Silva, E. LiDAR-Based
799 Real-Time Detection and Modeling of Power Lines for Unmanned Aerial Vehicles. *Sensors* **2019**, *19*, 1812.
- 800 11. Christiansen, M.; Laursen, M.; Jørgensen, R.; Skovsen, S.; Gislum, R. Designing and Testing a UAV Mapping System
801 for Agricultural Field Surveying. *Sensors* **2017**, *17*, 2703.
- 802 12. Aguilar, W.G.; Luna, M.A.; Moya, J.F.; Abad, V.; Parra, H.; Ruiz, H. Pedestrian Detection for UAVs Using Cascade
803 Classifiers with MeanShift. In Proceedings of the 2017 IEEE 11th International Conference on Semantic Computing
804 (ICSC); IEEE: San Diego, CA, USA, 2017; pp. 509–514.
- 805 13. Criminisi, A.; Reid, I.; Zisserman, A. Single view metrology. In Proceedings of the Proceedings of the Seventh IEEE
806 International Conference on Computer Vision; IEEE: Kerkyra, Greece, 1999; pp. 434–441 vol.1.
- 807 14. Hartley, R.; Zisserman, A. *Multiple view geometry in computer vision*; 2nd ed.; Cambridge University Press:
808 Cambridge, UK; New York, 2003; ISBN 978-0-521-54051-3.
- 809 15. Pears, N.; Liang, B.; Chen, Z. Mobile Robot Visual Navigation Using Multiple Features. *EURASIP Journal on*
810 *Advances in Signal Processing* **2005**, *2005*.
- 811 16. Li, S.; Nguyen, V.H.; Ma, M.; Jin, C.-B.; Do, T.D.; Kim, H. A simplified nonlinear regression method for human
812 height estimation in video surveillance. *EURASIP Journal on Image and Video Processing* **2015**, *2015*.
- 813 17. Jeges, E.; Kispal, I.; Hornak, Z. Measuring human height using calibrated cameras. In Proceedings of the 2008
814 Conference on Human System Interactions; IEEE: Krakow, Poland, 2008; pp. 755–760.
- 815 18. Fabián, J. Person Body Height Measurement by Using Surveillance Cameras. Master's Thesis, Czech Technical
816 University in Prague: Prague, Hungary, 2015.
- 817 19. Sturm, P. Pinhole Camera Model. In *Computer Vision*; Ikeuchi, K., Ed.; Springer US: Boston, MA, 2014; pp. 610–613
818 ISBN 978-0-387-30771-8.
- 819 20. Zhang, Z. A flexible new technique for camera calibration. *IEEE Transactions on Pattern Analysis and Machine*
820 *Intelligence* **2000**, *22*, 1330–1334.
- 821 21. Criminisi, A.; Zisserman, A.; Van Gool, L.J.; Bramble, S.K.; Compton, D. New approach to obtain height
822 measurements from video.; Higgins, K., Ed.; Boston, MA, 1999; pp. 227–238.
- 823 22. Winter, D.A. *Biomechanics and motor control of human movement*; 4th ed.; Wiley: Hoboken, NJ, 2009; ISBN
824 978-0-470-39818-0.

- 825 23. Guan, Y.-P. Unsupervised human height estimation from a single image. *Journal of Biomedical Science and*
826 *Engineering* **2009**, *02*, 425–430.
- 827 24. *Encyclopedia of optical engineering*; Driggers, R.G., Ed.; Marcel Dekker: New York, 2003; ISBN
828 978-0-8247-4250-8.
- 829 25. Vass, G.; Perlaki, T. Applying and removing lens distortion in post production.; 2003; pp. 9–16.
- 830 26. Basu, A.; Licardie, S. Alternative models for fish-eye lenses. *Pattern Recognition Letters* **1995**, *16*, 433–441.
- 831 27. Padhy, R.P.; Verma, S.; Ahmad, S.; Choudhury, S.K.; Sa, P.K. Deep Neural Network for Autonomous UAV
832 Navigation in Indoor Corridor Environments. *Procedia Computer Science* **2018**, *133*, 643–650.
- 833 28. Minichino, J.; Howse, J. *Learning OpenCV 3 computer vision with Python: Unleash the power of computer vision with*
834 *Python using OpenCV*; Second edition.; Packt Publishing: Birmingham, UK, 2015; ISBN 978-1-78528-384-0.
- 835 29. Motion Imagery Standards Board Motion Imagery Sensor Minimum Metadata Set 2018.
- 836 30. Redding, J.D.; McLain, T.W.; Beard, R.W.; Taylor, C.N. Vision-based target localization from a fixed-wing miniature
837 air vehicle. In Proceedings of the 2006 American Control Conference; IEEE: Minneapolis, MN, USA, 2006; p. 6 pp.
- 838 31. Grant, B.G. *Getting started with UAV imaging systems: a radiometric guide*; SPIE Press: Bellingham, Washington,
839 2016; ISBN 978-1-5106-0183-3.
- 840 32. Marques, M.M. STANAG 4586: Standard Interfaces of UAV Control System (UCS) for NATO UAV Interoperability
841 2012.
- 842 33. DJI Phantom 4 PRO/PRO+ User Manual 2017.
- 843 34. Li, X.; Ge, M.; Dai, X.; Ren, X.; Fritsche, M.; Wickert, J.; Schuh, H. Accuracy and reliability of multi-GNSS real-time
844 precise positioning: GPS, GLONASS, BeiDou, and Galileo. *Journal of Geodesy* **2015**, *89*, 607–635.
- 845 35. Vester, J. Estimating the Height of an Unknown Object in a 2D Image. Master Thesis, Royal Institute of Technology:
846 Stockholm, Sweden, 2012.
- 847 36. Leachtenauer, J.C.; Driggers, R.G. *Surveillance and reconnaissance imaging systems: modeling and performance*
848 *prediction*; Artech House optoelectronics library; Artech House: Boston, 2001; ISBN 978-1-58053-132-0.
- 849 37. Lazreg, N.; Bouchiha, R.; Besbes, K. Registration and correction techniques in Cubesat remote sensing images. In
850 Proceedings of the 2017 International Conference on Engineering & MIS (ICEMIS); IEEE: Monastir, 2017; pp. 1–7.
- 851 38. Dalal, N.; Triggs, B. Histograms of Oriented Gradients for Human Detection. In Proceedings of the 2005 IEEE
852 Computer Society Conference on Computer Vision and Pattern Recognition (CVPR'05); IEEE: San Diego, CA, USA,
853 2005; Vol. 1, pp. 886–893.
- 854 39. Jia, H.-X.; Zhang, Y.-J. Fast Human Detection by Boosting Histograms of Oriented Gradients. In Proceedings of the
855 Fourth International Conference on Image and Graphics (ICIG 2007); IEEE: Chengdu, Sichuan, China, 2007; pp. 683–
856 688.
- 857 40. Passalis, N.; Tefas, A. Concept detection and face pose estimation using lightweight convolutional neural networks for
858 steering drone video shooting. In Proceedings of the 2017 25th European Signal Processing Conference (EUSIPCO);
859 IEEE: Kos, Greece, 2017; pp. 71–75.
- 860 41. Bk, S.; Corvee, E.; Bremond, F.; Thonnat, M. Person Re-identification Using Spatial Covariance Regions of Human
861 Body Parts. In Proceedings of the 2010 7th IEEE International Conference on Advanced Video and Signal Based
862 Surveillance; IEEE: Boston, MA, USA, 2010; pp. 435–440.
- 863 42. Bejiga, M.; Zeggada, A.; Nouffidj, A.; Melgani, F. A Convolutional Neural Network Approach for Assisting
864 Avalanche Search and Rescue Operations with UAV Imagery. *Remote Sensing* **2017**, *9*, 100.
- 865



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