

# The Conjugate Refractive-Reflective Homogeniser in a 500X Cassegrain Concentrator: Design and Limits

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**Abstract:** In this study we present the Conjugate Refractive Reflective Homogeniser (CRRH) to be used in a 500X Cassegrain photovoltaic concentrator. The CRRH is a dielectric crossed v-trough lined with a reflective film whilst maintaining an air gap between them. This air gap between the two surfaces helps in trapping the scattered light from the refractive geometry and ensures both total internal reflection (TIR) and standard reflection of the escaped rays. A 10-42% drop in optical efficiency has been shown to occur due to varying the surface roughness of the homogeniser in these ray trace simulations for the Cassegrain set up. The CRRH increased the overall optical efficiency by a maximum of 7.75% in comparison to that of a standard refractive homogeniser simulated within the same concentrator system. The acceptance angle and flux distribution of these homogenisers was also investigated. The simple shape of the CRRH ensures easy manufacturing and produces a relatively uniform irradiance distribution upon the receiver. The theoretical benefit of the CRRH is also validated via practical measurements. Further research is required but a 6.7% power increase was measured under a 1000 W/m<sup>2</sup> solar simulator at normal incidence for the experimental test.

## 1. Introduction

There is a growing interest in concentration photovoltaic (CPV) technologies due to their reduced need for photovoltaic (PV) material and higher potential efficiencies. Not only can CPV systems be the answer to reducing the cost of solar power but they are also more environmentally friendly than regular flat plate PV panels. Two reasons for this are: firstly, CPV technologies use less semiconductor material, and secondly they have a smaller effect on the albedo change in an area than that of flat plate PV panels [1–3]. The Albedo is the percentage of incoming radiation reflected off a surface. Covering surfaces with dark coloured flat plate PV panels results in absorbing and emitting more thermal energy if the original surface was not initially of a similar dark colour (e.g. fields). Due to the relatively low efficiency of flat plate PV panels in comparison to CPV, they convert more of the incoming radiation into heat rather than

25 electricity. This method of PV can change the overall albedo of an area, and contribute to the effect of  
26 ‘urban heat islanding’ [1–3]. Higher efficiency technologies transfer less of the absorbed energy into heat  
27 and do not affect the albedo of an area as significantly as that of flat PV panels [3].

28 As the concentration ratio of an optic is increased, it becomes more difficult to maintain a high  
29 optical efficiency, uniform irradiance distribution, and an acceptable optical tolerance for the system  
30 simultaneously [4]. Matching the output irradiance size and shape to the receiver size and shape effects all  
31 of these factors and non-uniform illumination has a detrimental impact on the solar cell performance [5]. A  
32 secondary optic or homogeniser element improves this and is needed to relax the demand on the system’s  
33 accuracy [6, 7]. Some secondary concentrator optics include the compound parabolic concentrator (CPC)  
34 [8], the dome lens [9], the ball lens [10] and various homogenising light funnel geometries [11–13]. These  
35 typically take on the shape of an inverted cone or pyramid but there are also elliptical and hyperbolic  
36 optics possible [8, 14, 15].

37 One key consideration in all of the above named designs is the material to be used and the resulting  
38 surface quality. The surface roughness of TIR optics causes scattering of incoming light, reducing its  
39 performance from the ideal design.

40 Glass is typically the best choice for high-quality accurate optics, but the strength, flexibility and  
41 light weight of plastics makes polymers such as PMMA the more economic option. PMMA is the most  
42 popular polymer used in CPVs and polyethylene is used widely in other areas but has a short lifetime.  
43 Polyamide, polystyrene, acrylics and polycarbonate (PC) have been investigated but more research is  
44 required [16]. Lenses may be manufactured by hot-embossing, casting, extruding, laminating,  
45 compression-moulding, or injection-moulding thermoplastic PMMA [17]. Reflective optics also depend  
46 greatly on their surface quality. A silvered mirror using smooth glass produces a common mirror with  
47 reflectivity >85% but complex shapes are difficult and expensive. Reflective films are an alternative  
48 simple and effective option for reflective based optics. They are lightweight, typically cheaper than solid  
49 polished metals and films with >90% reflectivity are available. Their application to surfaces, especially 3D  
50 curves, can be difficult however [18]. Polymer mirror films are a more recent low-cost, low weight option  
51 to gain >90% reflective surfaces but require specially designed structures to gain the correct shape [19,  
52 20]. . In terms of mirrors, vacuum metalizing is the current best option but this process, like refractive  
53 lenses, is again highly dependent on the material and surface quality [21, 22].

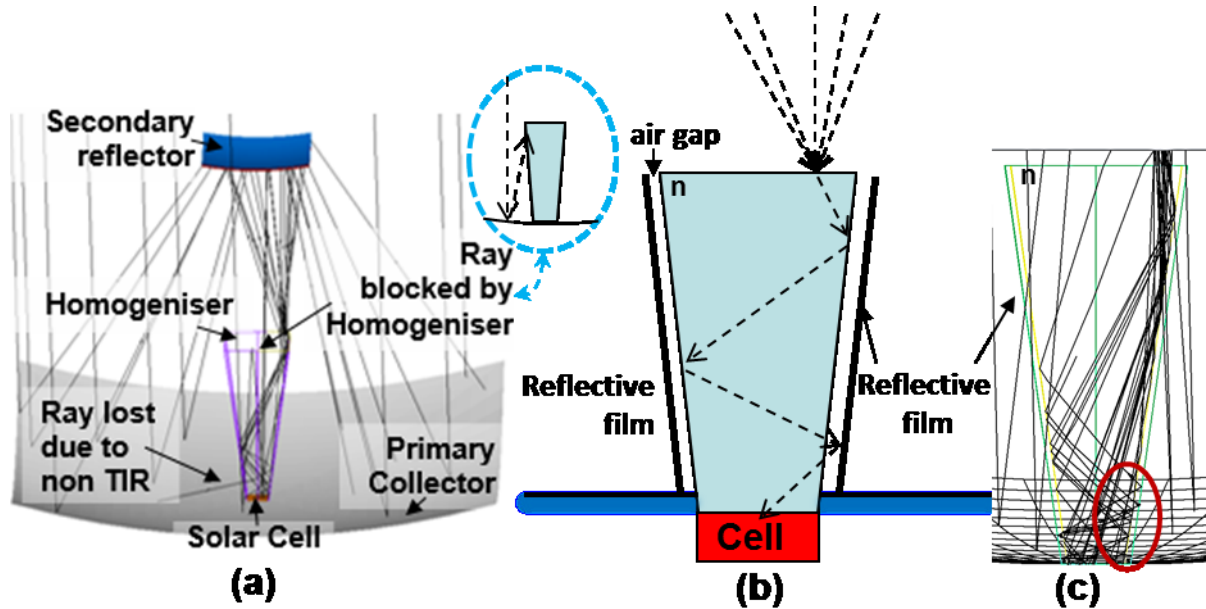
54 The surface structure of an optical element, or the interface between two optical mediums, has a  
55 strong influence on the final direction of the reflected or refracted light. During design simulations, these  
56 optical surfaces are sometimes assumed ideally smooth with no scattered light losses. There is however no

57 ideally smooth optical surface for lenses or mirrors and an inherent roughness is always present. The  
58 degree of this surface inhomogeneity depends on the manufacturing process and material used with higher  
59 quality optical finishes and coatings costing more [23]. Manufacturing processes for optics include precise  
60 grinding, milling, polishing, and a variety of coating methods for a smooth finish. Computer-controlled  
61 diamond turning machines, as well as other modern materials and molding techniques, have significantly  
62 improved the design and accuracy of refractive optics such as Fresnel lenses [24]. Similarly, computer-  
63 aided design and machining has improved the quality of reflective optics, but in both cases good-quality  
64 prototyping can be expensive when requiring smooth and accurate geometries. Simple cost effective  
65 methods to improve the optical efficiency of optics are needed, whether the design is in a prototyping or  
66 final installation stage. There are several methods to measure the optical scattering of a surface and hence  
67 various terms associated with its severity [25, 26]. Here we will refer to the bidirectional scattering  
68 distribution Function (BSDF) which is associated with the surface roughness of optical interfaces through  
69 the total integrated scatter (TIS) and dictates how light is transmitted or reflected from it. The BSDF is the  
70 combined function of the bidirectional reflectance distribution function (BRDF) and the bidirectional  
71 transmittance distribution function (BTDF). The BSDF is generally in the form of a mathematical formula,  
72 often encompassing discrete samples of measured data, which approximately models the actual surface  
73 behaviour. The bidirectional scattering distribution function radiometrically characterizes the scatter of  
74 light from a surface as a function of the angular positions of the incident and scattered rays [27].

## 75 **2. Design Considerations**

76 One commonly utilised and widely researched concentrator design is the Cassegrain concentrator  
77 which has the advantages of compactness and having an upward facing receiver [6]. With the receiver  
78 situated in the base of the primary reflector (see fig. 1a), passive cooling methods are more easily  
79 employed and the cell temperature is more manageable. Surface imperfections however will reduce the  
80 optical efficiency at every stage. The primary and secondary dishes shown in figure 1a will have an  
81 associated non-ideal reflectance. A reflective homogeniser optic would similarly suffer, especially if there  
82 are many reflections occurring within. A refractive medium takes advantage of total internal reflection  
83 (TIR) but again, surface roughness, scratches or any form of soiling is subject to refraction losses. This  
84 includes when the rays initially refract into the homogeniser and a small portion of energy is reflected  
85 instead of refracted. A simple but effective method to recover rays which fail TIR at the homogeniser  
86 walls is to use a reflective sleeve with an air gap [28] as shown in figure 1 b & c. Baig et al. [29, 30]  
87 discuss the optical loss caused by the encapsulation medium used in connecting low concentration optics  
88 to solar cells. Light rays incident in this overlap region do not reflect towards the solar cell but continue

89 through the encapsulation medium until lost. Baig et al. overcame the encapsulation issue by adding a strip  
 90 of reflective film to the bottom edge of the 3D cross compound parabolic concentrator designed for  
 91 building integration [29, 30]. We expand on this method by applying reflective film with an air gap to all  
 92 of the TIR active walls of a homogeniser in a high concentration Cassegrain concentrator. Hence, the  
 93 conjugate refractive reflective homogeniser (CRRH) is presented.



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95 **Fig. 1.** (a) Ray Trace Simulation of Cassegrain concentrator at a tracking error of  $\pm 1.75^\circ$ . Lost rays are shown including an  
 96 inlet diagram of how a light ray can be blocked by the homogeniser on route to the secondary reflector. (b) Theoretical  
 97 performance of CRRH with air gap between reflective film. (c) Ray trace diagram confirming that refracted rays can be caught  
 98 by the reflective film (red circle).

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### 2.1. Parameters and Limitations?

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A previous study has been carried out to determine the dimensions of the primary and secondary reflectors as well as the homogeniser dimensions [31]. Overall, the design has a good acceptance angle of  $>1^\circ$ . The homogeniser geometry is set such that a perfect surface should only lose a negligible percentage of energy due to light rays not meeting TIR ( $>0.01\%$ ). When increasing the misalignment with the Sun up to  $2^\circ$  an increase in light loss occurs in this design due to interception by the homogeniser after reflection from the large primary mirror (fig.1a). At  $<0.5^\circ$  misalignment this loss is almost negligible but increases up to  $\sim 1.7\%$  at  $\pm 2^\circ$  solar misalignment. This will limit the air gap and thickness of the reflective sleeve but would not be the case for other designs such as the Fresnel lens. In this study, simulations with an increasing air gap between the refractive homogeniser surface and reflective film surface (figure 1b & c) were carried out. The solar cell size was 1cm x 1cm and the geometrical concentration ratio was 500X.

### 3. Simulation method

Simulations were carried out using Breault's ASAP ray tracing software. The source was set to imitate energy from the sun with  $1000\text{W/m}^2$  and a divergence angle of  $\pm 0.27^\circ$ . The homogeniser material is set as SHOTT BK7, with a dispersion curve as shown in figure 2. This is a commonly used medium and has a higher refractive index than others such as PMMA. The homogeniser will be made out of a material with a similarly stable and high refractive index to SHOTT BK7 (to improve TIR within).

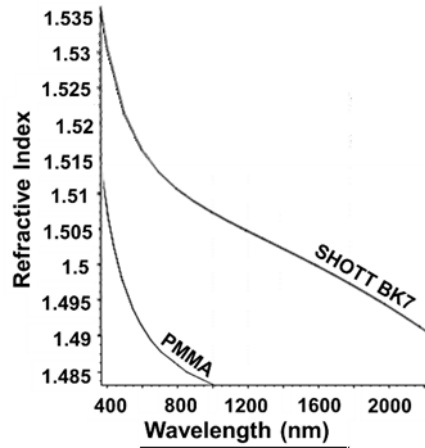


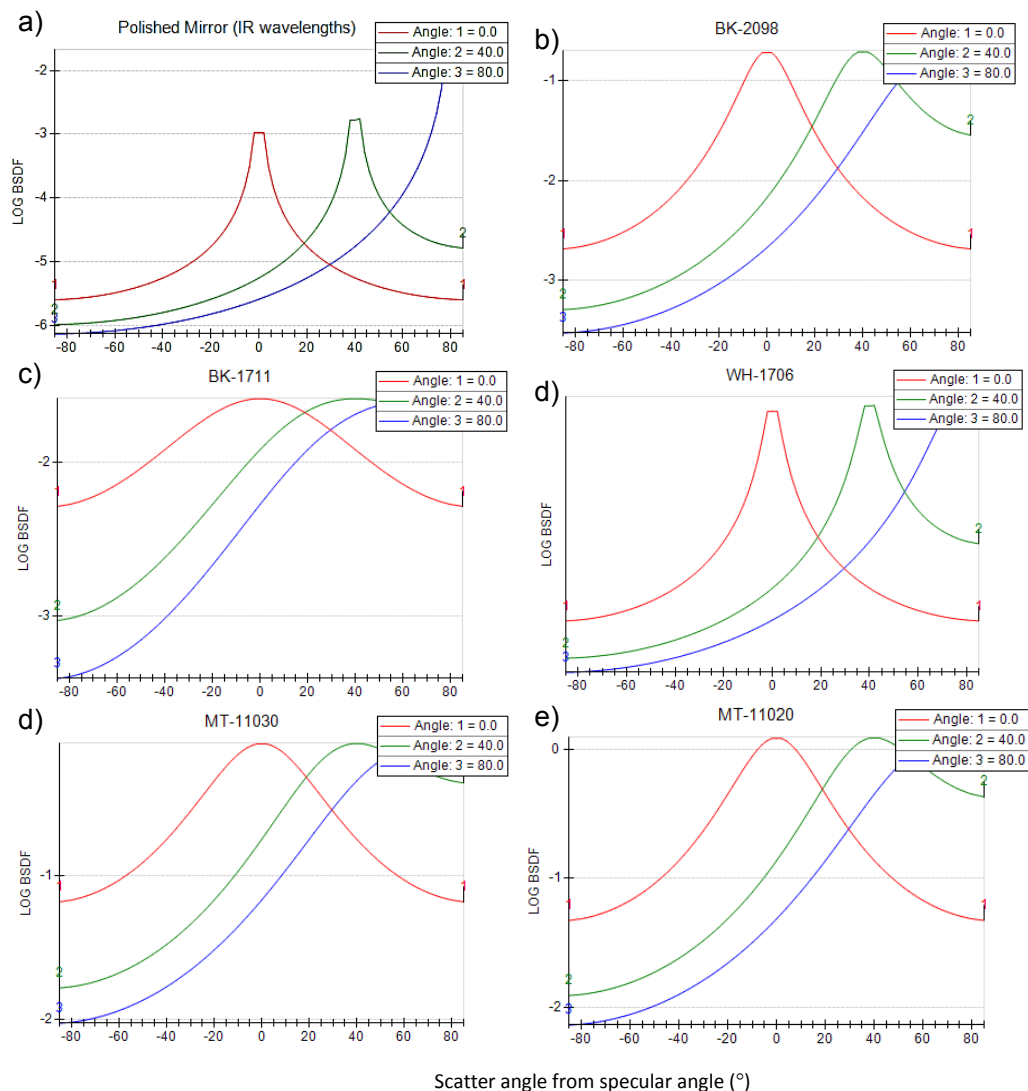
Fig. 2. Dispersion functions of PMMA and SHOTT BK7.

For measurements of the air gap thickness, the BSDF of the homogeniser was chosen to be similar to that of standard polished aluminium, following the Harvey model. This model was chosen as the homogeniser will be molded from an aluminium casing with polished inner surfaces.

Simulations were carried out assuming first the scenario of perfect surface qualities and 100% reflectance for reflectors and 0% absorbance for the homogeniser.  $\sim 10\%$  reflectance loss is then assumed for the two reflective dishes assuming their surfaces follow the polished mirror BSDF (figure 3a). The losses incurred when the light rays refract into the homogenisers entry aperture and are absorbed are included next and finally a surface roughness is added to the homogeniser material. A selection of BSDFs were used in the simulations for this investigation, their plots are given in figure 3 and all taken from the breault software ASAP scattering library [32]. For these simulations a modified Harvey model was used with the selected BSDFs and although the BSDF cannot fully be shown with any 2D or 3D graph the curves in figure 3 are given as some indication of the light scattering profile. The graphs show the log BSDF vs. the scattering angle (with respects to the specular angle) for 3 different incidence angles. All the scatter profiles follow the rule that most of the scattered light should be equal to the angle of incidence (the peaks shown in the graphs in figure 3). Differences can be seen in how the remainder of the light is

distributed at non specular angles (scattered). [27, 32]. The effects and contributions of these imperfect optical elements on optical efficiency and acceptance angle are given in figures 4 and 5.

Simulations were then carried out with the addition of a reflective film sleeve to the homogeniser at increasing air gap widths to investigate its advantages.



**Fig. 3.** LOG BSDF vs. scatter angle from specular of a) polished mirror; b) BK-2098, c) BK-1711, d) WH-1706, e) MT-11030, f) MT-11020. 3 plots are shown in each graph for an incidence angle of 0°, 40° and 80°. The BSDFs beginning with MT are representative of moulded optics surface profiles and those beginning with BK and WH are associated with specific materials available from lens providers. All plots were taken from the breault ASAP scattering library [32].

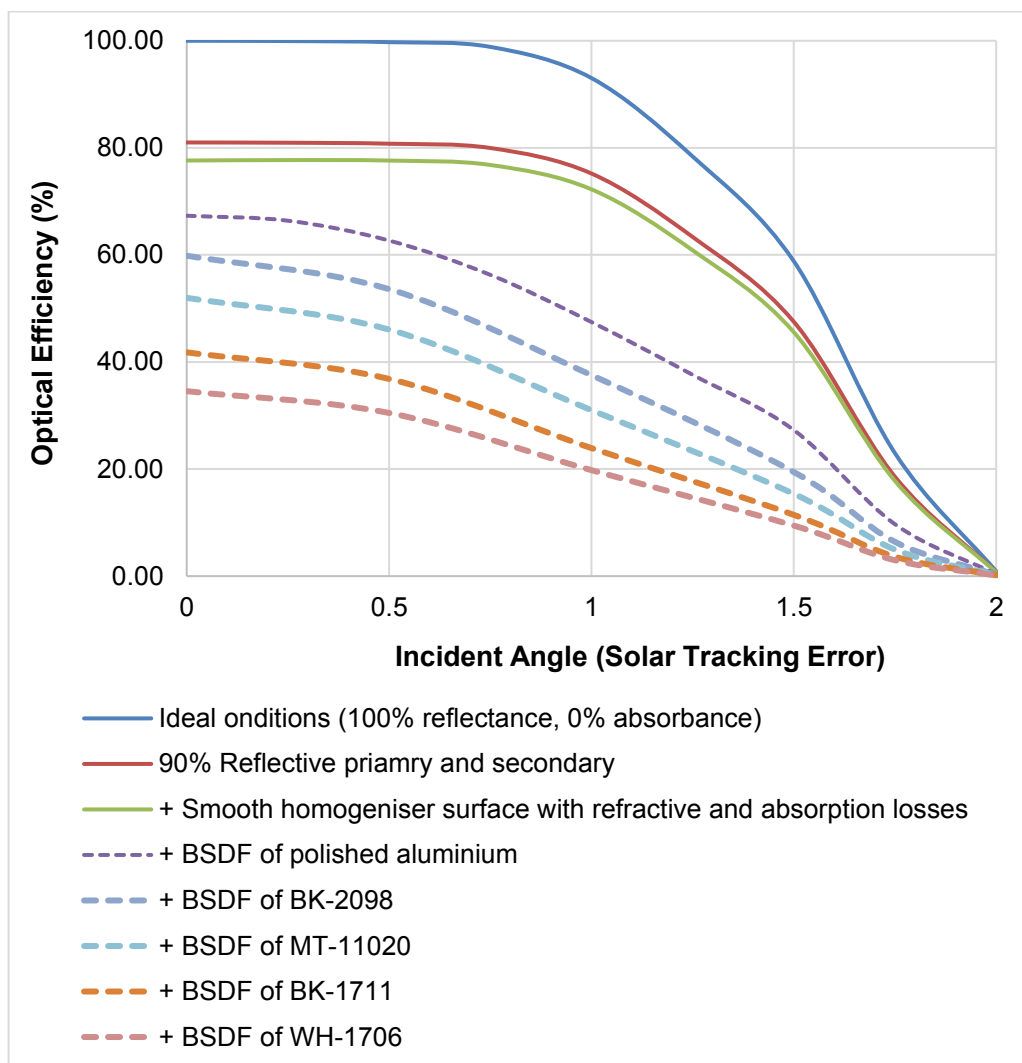
## 4. Results and discussion

### 4.1. Optical efficiency decrease in realistic system

Figure 4 confirms that no light rays are lost within the system at normal incidence as shown by the 'ideal' scenario results.

As can be seen from figures 4 and 5, the addition of a 10% reflection loss on both dishes causes a significant drop in optical efficiency. There are materials and coatings with improved reflectance [33] such as silver (~97% reflectance) but degradation and/or expense are common problems with such high quality reflective materials. All following simulations hence consider a 90% reflective primary and secondary dish so as final results are more realistic.

There is a small loss of energy due to when the light refracts into the homogeniser and some portion of the rays is reflected away. This can be improved with antireflection coatings and special textures of the homogeniser surface but again this is expensive [34, 35].



**Fig. 4.** Practical losses summary. Optical efficiency decreases as surface losses are added in stages. The dashed lines represent possible surface finishes of the homogeniser depending on which material and manufacturing process is employed.

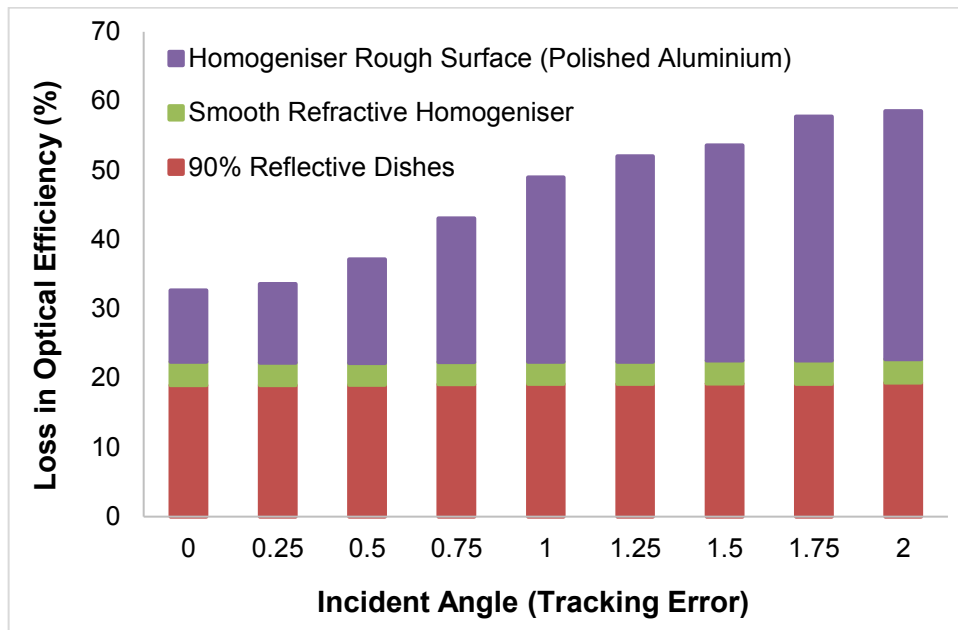


Fig. 5. Contribution of optical losses from different imperfect surface considerations.

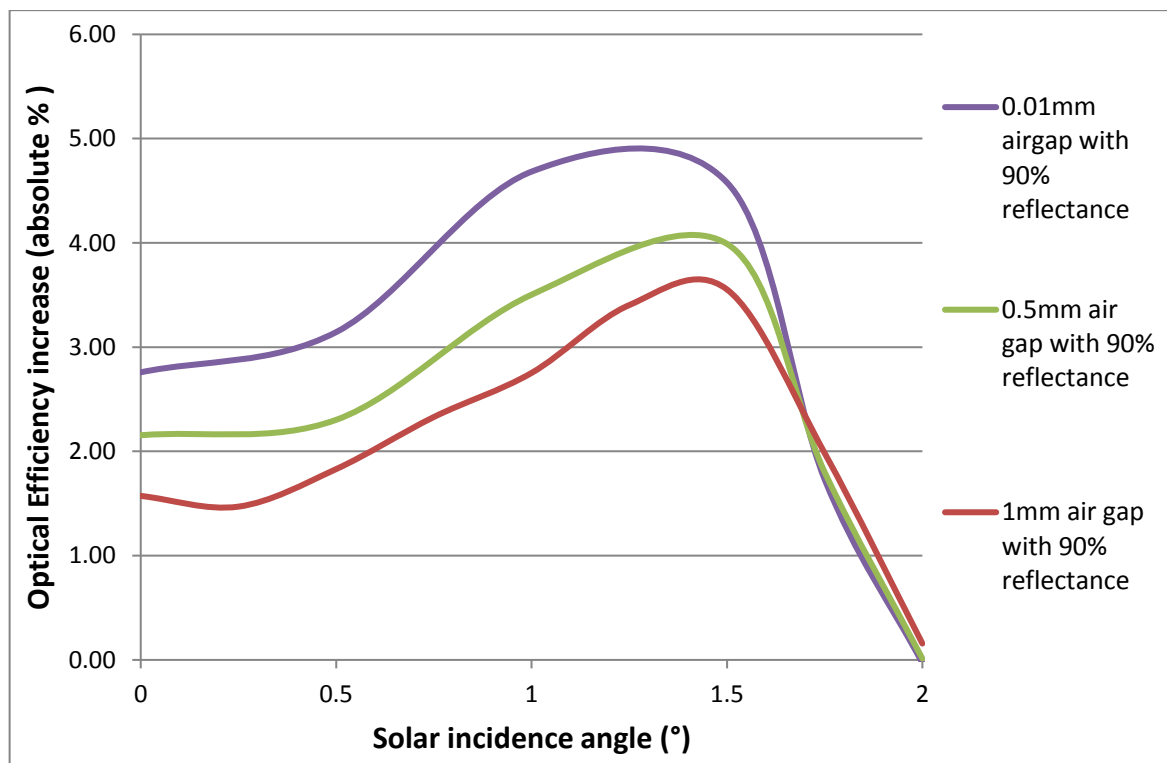
The surface roughness is a main factor causing a drop in optical efficiency and lowering the acceptance angle (fig. 4 & 5). There is a severe drop especially for the BSDF's related to poorer surface finishes as shown in figure 4. These BSDF's were selected from a database of expected BSDF's of optical finishes available from companies. The BSDF's were chosen simply to give a good range. Typical surface quality would be expected to be in the upper region of these samples. Their effect is shown more clearly in figure 5 for the BSDF of polished aluminium, which although has the smallest drop in optical efficiency in figure 4, still contributes significantly to the total optical loss in figure 5. Due to the increase in the solar misalignment angles, the rays reflect more within the homogeniser against the rough surfaced walls and are more likely to scatter instead of undergoing TIR. This causes the greater loss at  $>0.75^\circ$  solar incident angles in figure 5. More accurate solar trackers and accurately built systems would not suffer as significantly if within  $\pm 0.5^\circ$  accuracy but these incur further expense as well.

#### 4.2. Impact of CRRH and air gap

Using first the lowest effecting BSDF (that of a standard polished aluminium) for the homogeniser surface and the added reflective film surface, an increase in optical efficiency was measured as shown in figure 6. The conjugate refractive-reflective homogeniser improves optical efficiency most between the 1 and 1.5 degree range of misalignment due to the increased incidence angle. When considering realistic conditions (90% reflectance from primary dishes and reflective film), the optical efficiency is increased by 2.8% (absolute value) at normal incidence and as high as 4.7% over the 1 and 1.5 degree region as shown



187 in figure 6. Although this is a significant gain, it should be noted that other manufacturing methods can  
 188 result in smoother surface finishes with less light loss. The optical efficiency of any previous stage optics  
 189 will also have an effect on the light saved by using the CRRH. If there is more energy going into the  
 190 homogeniser there is a greater portion of energy that can be trapped. The reflectance of the reflective film  
 191 itself will alter results as well. If the CRRH with 0.01mm air gap had 100% reflectance for the primary  
 192 dishes and reflective film the maximum optical efficiency gain would be ~7% for these simulations of a  
 193 500X Cassegrain system.



194 **Fig. 6.** Increase in optical efficiency with the addition of the reflective sleeve under different conditions. Here the base optical  
 195 efficiency is that of the refractive homogeniser with the same dimensions and no reflective sleeve.  
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198 The thickness of the air gap was found to have very little effect on the efficiency with which  
 199 refracted light rays are caught as shown in figure 7, though there is a significant difference without an air  
 200 gap. Figure 7 shows the optimum air gap to be 0.01mm in these investigations, this would be nearly  
 201 impossible to cost effectively implement due to manufacturing limitations but it can be assumed as small  
 202 an air gap as is feasible considering manufacturing and cost would have the highest benefit.

203 Figure 7 shows that with no air gap (0mm), TIR is lost and all rays are reflected with specular losses  
 204 (10%) in energy due to the 90% reflectance of the reflective film. As soon as there is an air gap, even as  
 205 small as 0.01mm in these simulations, the optical efficiency sharply increases as shown in figure 7. This  
 206 increase in optical efficiency indicates how many reflections are experienced by the light rays and hence

the benefit TIR provides. The larger the increase in optical efficiency between the 0 and 0.01 air gap marks in figure 7, the more reflections occurring within the homogeniser which will benefit from TIR. This is why larger misalignment angles (except for 2 degrees misalignment where most rays completely miss the homogeniser) have a more significant optical efficiency gain (vertical incline from 0mm to 0.01mm) in figure 7, because there are more reflections occurring.

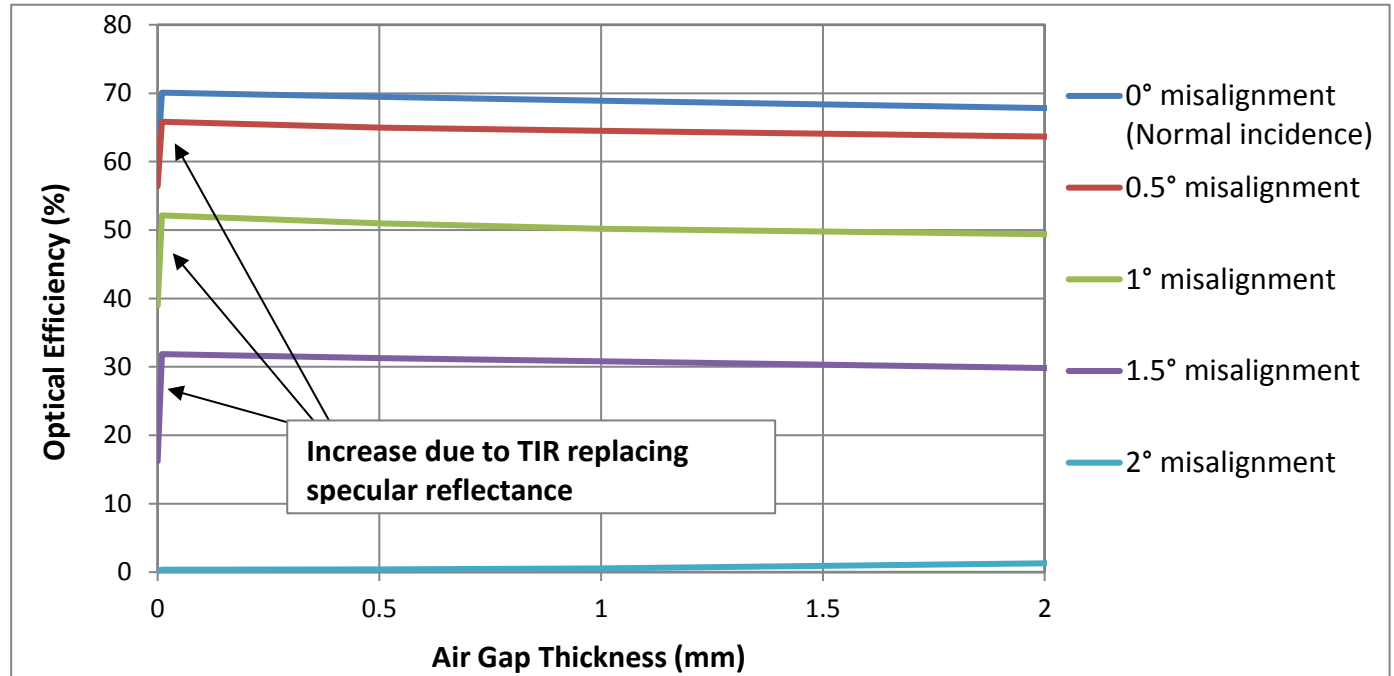
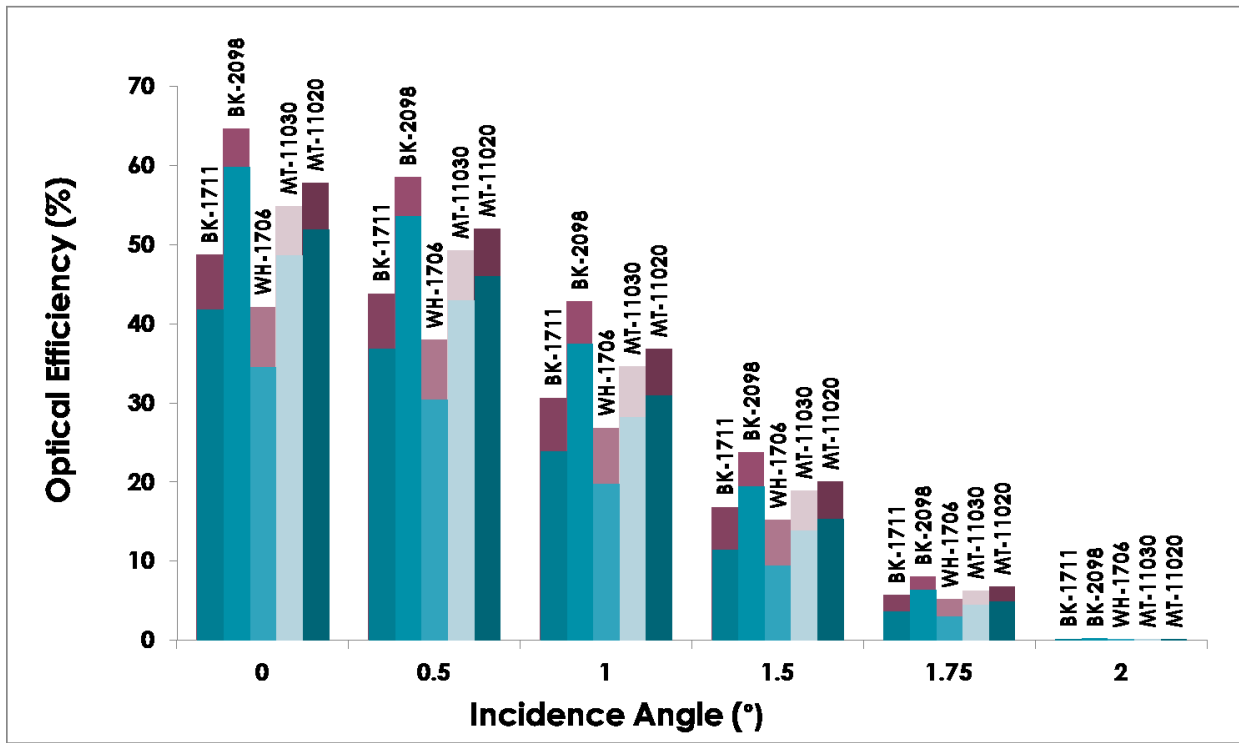


Fig. 7. Graph of optical efficiency vs. air gap thickness for different solar misalignment angles.

Thicker air gaps result in a longer path length of the non TIR rays. This means rays will re-enter into the refractive medium at a lower position close to the solar cell and in theory possibly increase the optical efficiency of the system. However, in this cassegrain design, a thicker air gap also blocks more rays traveling towards the secondary from the primary dish as mentioned earlier and shown in figure 3. This would explain why there is a slight decrease in optical efficiency as the air gap thickness is increased in figure 7.

#### 4.3. Impact of BSDF value

From the above results, it can be concluded that as small an airgap as possible is preferred. An air gap of 0.01mm was hence used to investigate the effect of different BSDFs such as those already given in figures 3 and 4.



**Fig. 8.** Increase in optical efficiency (purple shades) due to the addition of the reflective sleeve to the refractive homogeniser with an air gap of 0.01mm for increasing BSKDF's. The incidence angle of the light is also increased up to 2 degrees to show the effect misalignment has on the benefit of the CRRH in comparison to the performance of a refractive homogeniser (blue shades).

As can be seen from figure 8, the CRRH consistently improves the optical efficiency in comparison to a standard refractive homogeniser of this type for a range of surface scattering profiles. The maximum improvement is 7.75% with the BSKDF of WH-1701 at normal incidence. Contrary to initial expectations however, this improvement did not increase with larger solar misalignment angles. At increased incident angles the benefit of the CRRH decreased until negligible at 2 degrees incidence angle as shown in figure 8 where the optical efficiency of the standard refractive homogeniser is almost zero. Misalignment with the sun causes less light to reach the input surface of the homogeniser which can explain why the benefit of the CRRH decreases with increasing incidence angle. Also, if too many reflections occur within the homogeniser (due to the increased initial incidence angle), some light rays, despite being trapped at the CCRH walls, can still be reflected back out the entry aperture of the CRRH.

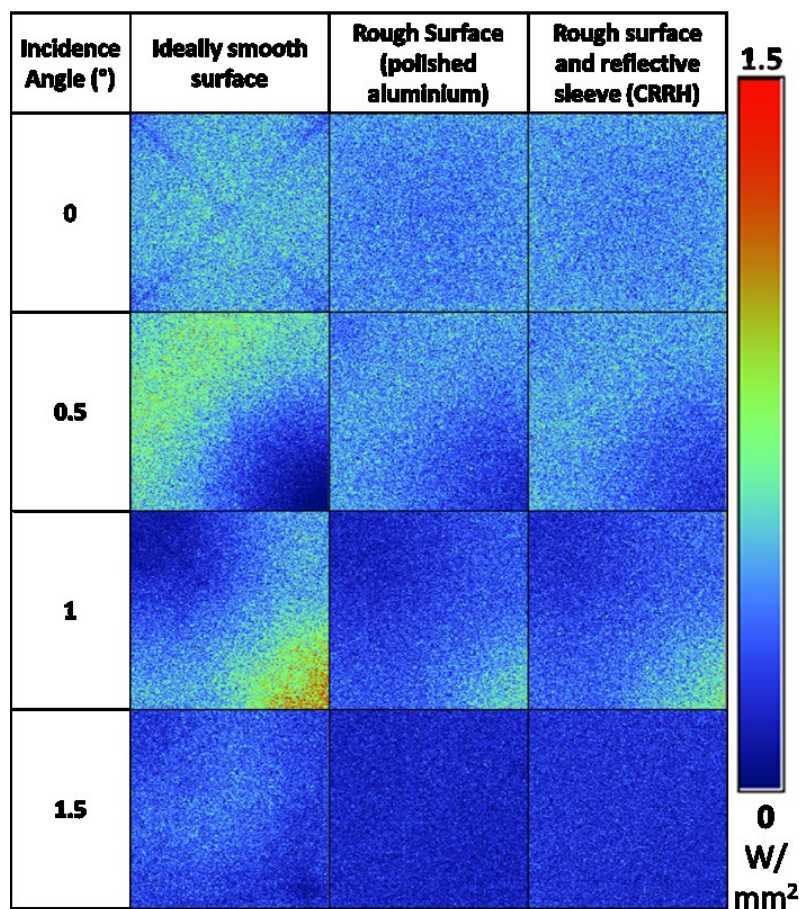
It can be drawn from these results that as long as there is some percentage (>2%) of light reaching the solar cell for the standard refractive homogeniser case, the CRRH will improve the optical efficiency by a non-negligible amount (as shown for the case of 1.75° incidence angle in figure 8). At normal incidence the smallest optical efficiency improvement by the CRRH was 4.82% with a BSKDF of BK-2098. These results confirm that the more efficient a purely refractive optic is to begin with (BK-2098 had the

highest original optical efficiency shown in figure 8), the less the addition of a reflective sleeve will improve the optical efficiency.

It should be noted that other manufacturing methods can result in smoother surface finishes with less light loss. The BSDFs beginning with MT in figures 3, 4 and 8 are representative of moulded optics surface profiles and those beginning with BK and WH are associated with specific materials available from lens providers.

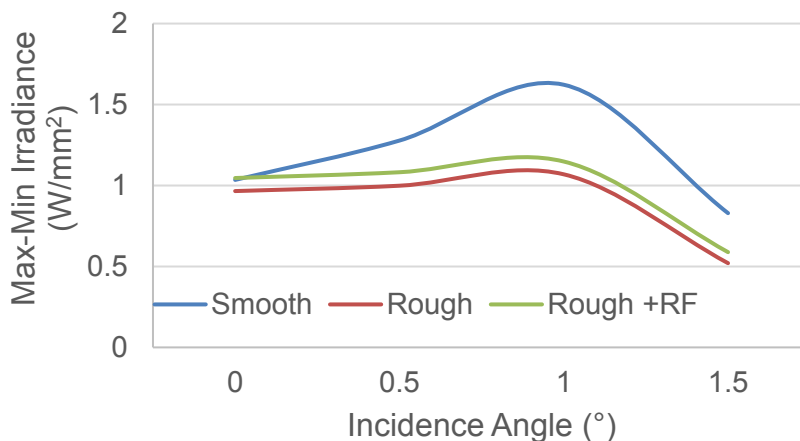
#### 4.4. Effect on irradiance distribution

The irradiance distribution upon the solar cell is also affected by the surface roughness of the homogeniser as shown in figure 9.

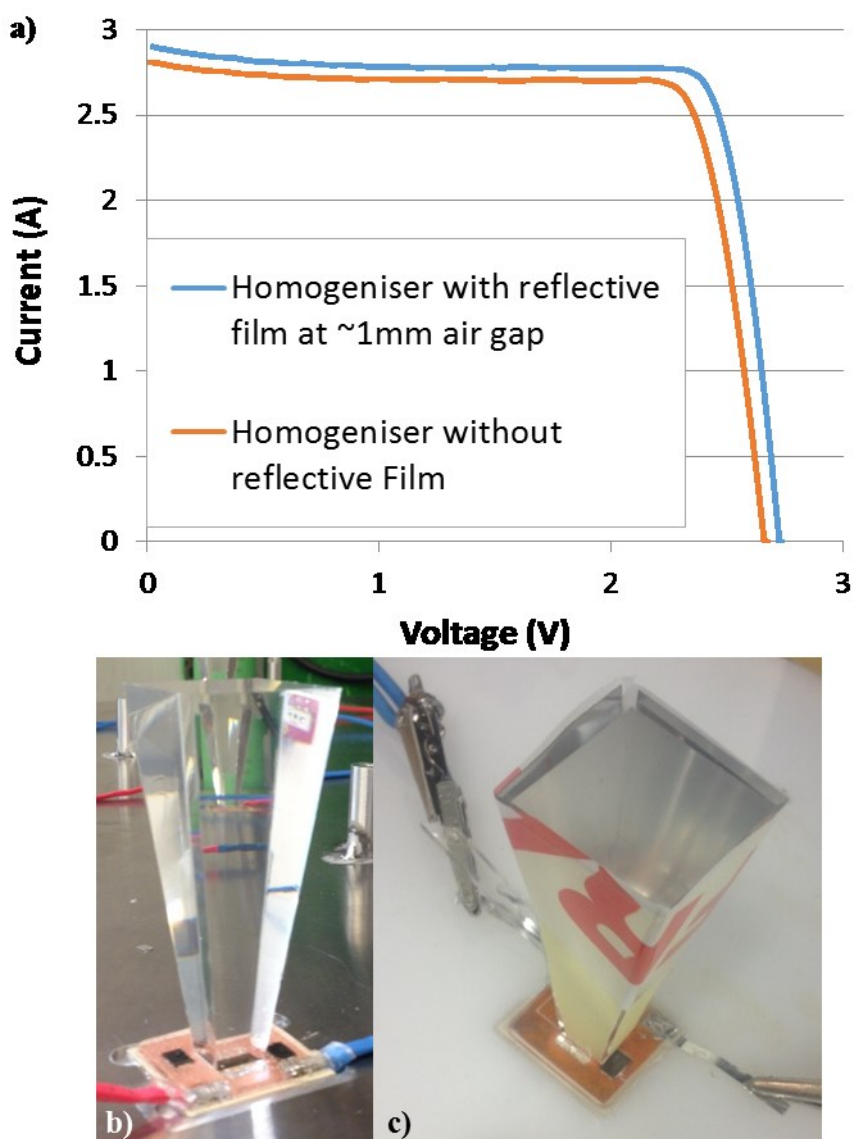


**Fig. 9.** Irradiance distribution upon solar cell with increasing solar incidence angle (increasing tracking error). Column 1: Solar Incidence angle upon full Cassegrain system. Column 2: the case of 100% reflective dishes and a refractive homogeniser with an ideal surface finish. Column 3: Results after the addition of a rough surface finish upon the homogeniser. Column 4: Same conditions as previous but with the reflective sleeve in place. The tracking error is set for both axes, hence the diagonal focusing.

266 The irradiance distribution is improved due to the slight diffusion of the rays from the rough surface  
 267 of the homogeniser. In the case of the conjugate refractive reflective homogeniser, when the reflective  
 268 sleeve is added, the irradiance distribution is negligibly different to that without the reflective sleeve. The  
 269 difference between the maximum and minimum irradiance values are given in figure 10. This shows a  
 270 purely smooth and ideal optic to have the least homogeneous distribution, the addition of the rough surface  
 271 modelling has the most homogeneous irradiance distribution, and the CRRH has slightly less evenly  
 272 distributed irradiance upon the cell. As expected, with a higher misalignment angle, the distribution is less  
 273 even, especially at 1°, before falling lower due to less total light being focused successfully to the solar  
 274 cell.



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 276 **Fig. 10.** Irradiance range (max-min) upon the solar cell with increasing solar incidence angle (increasing tracking error) for  
 277 the smooth refractive homogeniser, the realistically rough refractive homogeniser and CRRH.  
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**Fig. 11.** a) I-V trace for the refractive homogeniser with and without the reflective sleeve and air gap. Refractive homogeniser without reflective sleeve shown in b) and with reflective sleeve to make prototype CRRH in c).

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The measurements shown in figure 11a gave a 3.5% current increase and a 6.7% power increase. When adding the reflective film to the refractive homogeniser (figures 11 b and c), care was taken that the film did not optically stick to the refractive medium and prevent TIR. It was also ensured that the primary optic (Fresnel lens) only focused to the centre of the homogeniser for both tests and the same concentration ratio was maintained. With higher efficiency primary optics and higher concentration levels, the final stage optic gains more influence on the overall optical efficiency and performance. These practical measurements confirm the advantage of the CRRH over a plane refractive homogeniser.

## 5. Conclusion

The Conjugate Refractive Reflective Homogeniser has been presented within the Cassegrain concentrator design. The CRRH has been shown to improve the optical efficiency by a maximum of 7.75% when considering a realistic surface roughness upon the homogeniser and reflective optics within the Cassegrain concentrator system. The benefits of the CRRH are limited by the Cassegrain concentrator geometry and by the magnitude of surface roughness upon the homogeniser. A high quality homogenising optic with almost ideal surface smoothness would not benefit from the addition of a reflective sleeve but this is rarely the case due to difficult geometries and expense. Experimental tests confirmed the ray trace simulation analysis and a 6.7% performance improvement with the CRRH in comparison to the original refractive homogenizer was measured. Future work is required to fully understand the benefit conjugate refractive reflective optics can have for solar concentrator technologies.

## 6. Acknowledgments

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