

Matter Effects in Upward-Going Muons and Sterile Neutrino Oscillations

The MACRO Collaboration

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The angular distribution of upward-going muons produced by atmospheric neutrinos in the rock below the MACRO detector show anomalies in good agreement with two flavor $\nu_\mu \rightarrow \nu_\tau$ oscillations with maximum mixing and Δm^2 around 0.0024 eV^2 . Exploiting the dependence of the magnitude of the matter effect on oscillation channel, and using a set of 809 upward-going muons observed in MACRO, we show that the two flavor $\nu_\mu \rightarrow \nu_s$ oscillation is disfavored with 99% C.L. with respect to $\nu_\mu \rightarrow \nu_\tau$.

PACS 14.60Pq; 14.60Lm

1. INTRODUCTION

Neutrino oscillations[1] were first suggested by B. Pontecorvo in 1957 after the discovery of the $K^0 \leftrightarrow \bar{K}^0$ transitions. Subsequently, evidence for the existence of neutrino oscillation in nature has been provided by the Superkamiokande, Soudan2 and MACRO experiments, each of which has presented data which strongly favor atmospheric neutrino oscillations, in the form of ν_μ disappearance [3].

The two neutrino oscillation probability in vacuum is given by:

$$P(\nu_\ell \rightarrow \nu_{\ell' \neq \ell}) = \sin^2 2\theta \sin^2 \left[1.27 \Delta m^2 \frac{L}{E} \right] \quad (1)$$

where $\Delta m^2 = m_1^2 - m_2^2$ (eV²), L (km), E (GeV), θ is the mixing angle and L is the path length between the neutrino production point and the location at which the neutrino flavor is measured. This simple relation should be modified when a neutrino propagates through matter and when there is a difference in the interactions of the two neutrino flavors with matter [2]. The neutrino weak potential in matter is:

$$V_{\text{weak}} = \pm \frac{G_F n_B}{\sqrt{2}} \times \begin{cases} -Y_n + 2Y_e & \text{for } \nu_e, \\ -Y_n & \text{for } \nu_{\mu, \tau}, \\ 0 & \text{for } \nu_s, \end{cases} \quad (2)$$

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where the upper sign refers to neutrinos, the lower sign to antineutrinos, G_F is the Fermi constant, n_B the baryon density, Y_n the neutron and Y_e the electron number per baryon (both about 1/2 in common matter). The weak potential in matter produces a phase shift that will modify the neutrino oscillation probability if the oscillating neutrinos have different interactions with matter. Therefore, the matter effect could help to discriminate between different neutrino oscillation channels. According to equation, (2) matter effects in the Earth could be important for $\nu_\mu \rightarrow \nu_e$ and for the $\nu_\mu \rightarrow \nu_s$ oscillations, while for $\nu_\mu \rightarrow \nu_\tau$ oscillations there is no matter effect. For particular values of the oscillation parameters the matter effect increases the oscillation probability, leading to 'resonances' (e.g., the MSW effect).

$\nu_\mu \rightarrow \nu_s$ oscillations have been suggested [6] to explain some features of the atmospheric neutrino anomaly. Under most current models, a fourth (sterile) neutrino is necessary to explain all the reported neutrino anomalies (solar, atmospheric and LSND [7]). Matter effects are important [6] when $E_\nu/|\Delta m^2| \geq 10^3$ GeV/eV², therefore in particular for high energy events. The primary purpose of this letter is to compare the MACRO high energy neutrino events sample with the predictions, considering matter effects in the case of $\nu_\mu \rightarrow \nu_s$ oscillations. In MACRO, neutrino oscillation is observed in three different event topologies, having different characteristic ranges of parent neutrino energies. So-called *Up Through* events [4] are associated with muons which penetrate the entire detector. The parent neutrinos in these events have a median neutrino energy around 50 GeV. *Internal Up* events and *Internal Down* events, together with *Up Stop* events, [5] are associated with muons having a track terminus located within the MACRO detector. The parent neutrinos in these events have a significantly lower median energy, of around 4 GeV. In this paper, we focus on the high energy (*Up Through*) data sample. A similar analysis has been recently published by the Superkamiokande collaboration [8].

2. DATA ANALYSIS

The MACRO detector [9]. is located in the Hall B of the Gran Sasso Laboratory, with a minimum rock overburden of 3150 hg/cm^2 . It is in the general form of a large rectangular box, $76.6 \text{ m} \times 12 \text{ m} \times 9.3 \text{ m}$, divided longitudinally into six supermodules, and vertically into a lower part (4.8 m high) and an upper part (4.5 m high). The active detection elements are planes of streamer tubes for tracking and of liquid scintillators for fast timing. The lower half of the detector is filled with trays of crushed rock absorbers alternating with streamer tube planes, while the upper part is open and contains electronics racks and work areas.

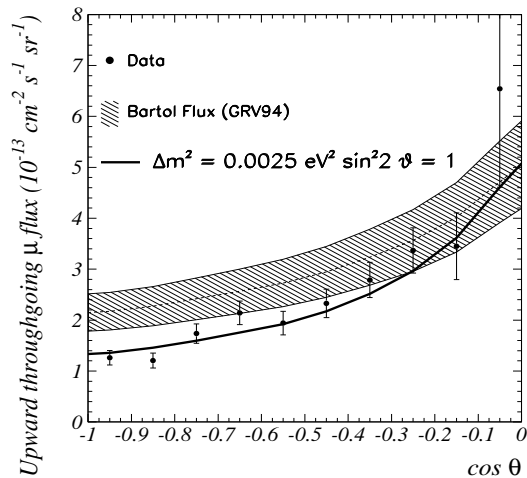


Figure 1. Zenith distribution of the flux of upgoing muons with energy greater than 1 GeV for the combined MACRO data. The shaded region shows the expectation for no oscillations with the 17% normalization uncertainty. The lower line shows the prediction for an oscillated flux with $\sin^2 2\theta = 1$ and $\Delta m^2 = 0.0024 \text{ eV}^2$.

The *Up Through* muon tracks we focus on in this study come from ν_μ interactions in the

rock below MACRO. In these events, the muon crosses the entire detector requiring that $E_\mu > 1 \text{ GeV}$. The time information provided by the scintillator counters determines the flight direction of the muon, allowing *Up Through* events to be distinguished from the much more common down-going muons. The measured muon velocity is calculated with the convention that down going muons have $\beta = \text{velocity}/c = +1$ while up going muons have $\beta = -1$. In the *Up Through* event sample, almost 50% of the tracks intercept 3 scintillator planes. In this case, there is redundancy in the time measurement, and β is calculated from a linear fit of the times as a function of the path length. Tracks with a poor fit are rejected. Upward going muons are selected by requiring that the measured velocity lie in the range $-1.25 \leq 1/\beta \leq -0.75$.

The data used in this study have been collected in three periods, with different detector configurations, starting in 1989. The statistics is largely dominated by the full detector run, started in May 1994 and ended in December 2000 (live time 5.51 years). The total live time, normalized to the full detector configuration, is 6.17 years.

Several cuts are imposed on the data to remove backgrounds caused by radioactivity or showering events which may result in bad time reconstruction. The primary data selection in this regard requires that the position of a muon hit in each scintillator, as determined from the timing within the scintillator counter, agrees within $\pm 70 \text{ cm}$ with the position indicated by the streamer tube track. This eliminates events with significant errors in timing. In addition, downgoing muons which pass near or through MACRO may produce low-energy, upgoing particles, which could appear to be neutrino-induced upward throughgoing muons if the down-going muon misses the detector [10]. In order to reduce this background, we impose a cut requiring that each upgoing muon must cross at least 200 g/cm^2 of material in the bottom half of the detector. Finally, a large number of nearly horizontal ($\cos \theta > -0.1$), but upgoing muons have been observed coming from azimuth angles (in local coordinates) from -30° to 120° . In this direction the overburden is insufficient to remove nearly horizontal, downgoing muons which have

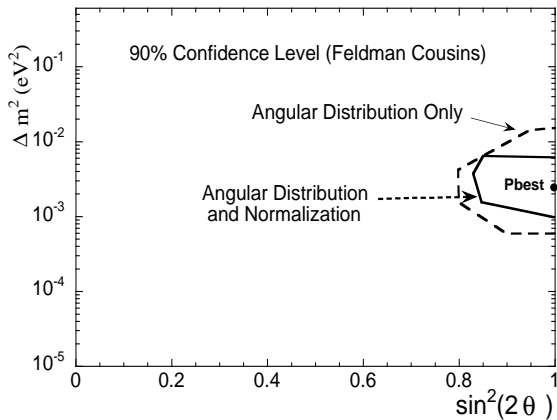


Figure 2. The MACRO 90% confidence level regions computed using the angular distribution only (dashed line) and the angular distribution combined with the normalization (continuous line).

scattered in the mountain and appear as upgoing. We exclude this region from our data.

After applying the data selections described in the previous paragraph, we observe 863 events with measured velocities in the range $-1.25 < 1/\beta < -0.75$. Based on events outside the upgoing muon peak, we estimate that there are 22.5 background events in this data sample. In addition, we estimate that there are 14.2 events which result from upgoing charged particles produced by downgoing muons in the rock near MACRO. Finally, it is estimated that 17 events are the result of interactions of neutrinos in the bottom layer of MACRO scintillators. After subtracting these backgrounds to the *UpThrough* data set, the number of upgoing throughgoing muons integrated over all zenith angles is 809.

In the simulation of our upgoing muon data, we have used the neutrino flux computed by the Bartol group [11], and the GRV94 [12] parton distribution set, which increases the upgoing muon flux by +1% with respect to the S_1 [13] parton distribution that we have used in the past. For low energy channels (quasi-elastic and 1 pion production) we have used the cross section in [14]. The propagation of muons to the detector has

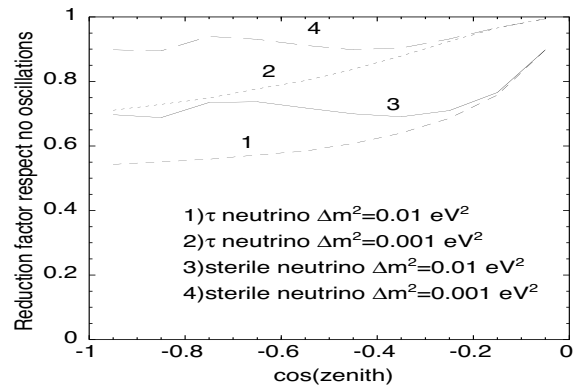


Figure 3. Reduction factor for $\sin^2 2\theta = 1$, two values of Δm^2 and $\nu_\mu \rightarrow \nu_s$ or $\nu_\mu \rightarrow \nu_\tau$

been done using the energy loss calculation by Lohmann et al. [15] for standard rock. The total systematic uncertainty in the predicted flux of upgoing muons, adding in quadrature the errors from the Bartol neutrino flux, the neutrino cross-section, and muon propagation, is estimated to be $\pm 17\%$. This theoretical error in the predicted flux is mainly a scale error that does not change the shape of the angular distribution. Assuming no oscillations, the number of expected events integrated over all zenith angles is 1122, giving a ratio of the observed number of events to the expectation of $0.72 \pm 0.026(\text{stat}) \pm 0.043(\text{systematic}) \pm 0.12(\text{theoretical})$.

Figure 1 shows the zenith angle distribution of the measured flux of upgoing muons with energy greater than 1 GeV for our full upgoing data sample, compared to the Monte Carlo expectation for no oscillations, and with a $\nu_\mu \rightarrow \nu_\tau$ oscillated flux with maximum mixing and $\Delta m^2 = 0.0025 \text{ eV}^2$. The shape of the angular distribution has been tested with the hypothesis of no oscillations, normalizing the total predicted flux to that observed. The χ^2 is 25.9 for 9 degrees of freedom ($P=0.2\%$). Under the hypothesis of $\nu_\mu \rightarrow \nu_\tau$ oscillation, the best χ^2 is 7.1 and is outside the physical region. The best χ^2 in the physical region of the oscillation parameters is 9.7 ($P=37\%$) for Δm^2 of 0.0025 eV^2 and maximum mixing. Combining informa-

tion from the angular distribution and the total number of events according to the procedure described in [16], we obtain a peak probability of 66% for oscillations with Δm^2 of $0.0024 eV^2$ and maximum mixing, while the probability for no oscillations is 0.2%.

The 90% confidence level regions of the MACRO upgoing events are shown in Figure 2. The limits are computed using the Feldman-Cousins procedure [17]. Figure 2 shows the results obtained using the angular distribution alone, and the angular distribution together with the information due to the overall normalization. The 90% confidence level regions are smaller than the regions obtained by SuperKamiokande [18] and Kamiokande [19] for the upgoing muon events. This can be accounted for through the following effects: the different energy threshold (Superkamiokande has an average energy threshold of about 7 GeV, MACRO has 1.5 GeV), the use of the Feldman-Cousins procedure, and the fact that our best point is outside the physical region.

3. TWO FLAVORS STERILE NEUTRINO OSCILLATIONS AND TAU NEUTRINO OSCILLATIONS

In the $\nu_\mu - \nu_s$ oscillation scenario, the matter effect changes the shape of the angular distribution and the total number of events with respect to vacuum oscillations. Large matter effects are expected for neutrinos near vertical incidence, due to the large neutrino path length in this case, and to the increase in the density of the Earth near its core. Assuming maximal mixing, as suggested by all available data, the matter effect produces a reduction of the oscillation effect, and results in an upgoing muon flux closer to that predicted by the no oscillation scenario. This effect would be most pronounced for directions near the vertical [6]. Figure 3 shows the reduction with respect to no oscillations for maximal mixing for $\nu_\mu \rightarrow \nu_s$ and $\nu_\mu \rightarrow \nu_\tau$ oscillations, with $\Delta m^2 = 0.001 eV^2$ and $\Delta m^2 = 0.01 eV^2$. We have tested the shape of the observed upgoing muon angular distribution against the hypothesis of $\nu_\mu - \nu_s$ oscillations with maximum mixing. The best χ^2 is 20.1 with 9 degrees of freedom. Combining the information

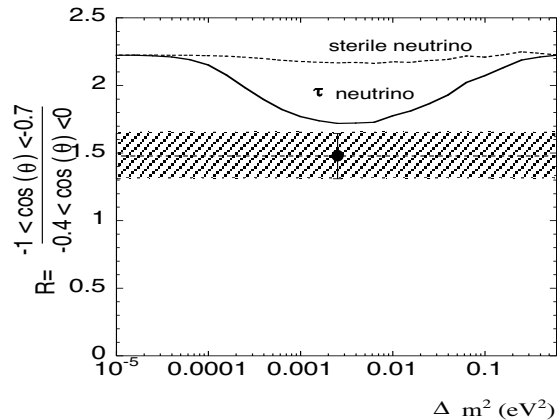


Figure 4. The ratio between the data in two bins (dashed line) and the comparison with the ν_s and ν_τ oscillations with $\sin^2 2\theta = 1$. The error bar includes statistical and systematical error.

obtained from the angular distribution and the normalization the highest probability obtained is 8% for maximum mixing and $\Delta m^2 = 0.006 eV^2$. A statistically more powerful test is based on the ratio between the number of events in the two angular regions $\cos(\theta) \geq 0.7$ and $\cos(\theta) \leq 0.4$ as shown in Figure 4. This quantity is statistically more powerful than the χ^2 in 10 bins because data are binned to maximize the difference between the two hypotheses to be tested and because the ratio is sensitive to the sign of the variation (while the χ^2 is not). In addition, this ratio is insensitive to most of the errors in the theoretical prediction of the ν flux and cross section. The primary disadvantage of this statistic is the loss of some features of the angular distribution. We have chosen slightly different angular regions than suggested in the original proposal for this statistic, presented in ref [20]. In our study, the angular regions used are based on a Montecarlo study of the intervals providing the maximum discrimination between the $\nu_\mu \rightarrow \nu_s$ and the $\nu_\mu \rightarrow \nu_\tau$ oscillation hypotheses.

The ratio of the flux of upgoing muons in two angular intervals is insensitive to uncertainties in the overall ν flux and cross section, as pointed out

in the last paragraph. Several effects do, however, lead to systematic errors in this ratio. For example, uncertainties in the K,π fraction in atmospheric air showers, and the different angular distributions of neutrinos produced by these parents, leads to approximately a 3% systematic error[21] in the predicted value for this ratio. Another theoretical error, at the level of approximately 2% for MACRO, results from uncertainties in the neutrino cross sections, and the different energy distributions of neutrinos arriving from the horizontal and vertical directions. A final source of systematic error in the prediction of the flux ratio results from the seasonal variations of the atmosphere's density profile, and the fact that the neutrino flux is computed for the standard United States atmosphere [11] not taking into account variations of the density profile with latitude. Seasonal variation of the high energy muon flux has been observed by MACRO[22] at 42° North latitude, where a 3% difference was observed between summer and winter. At more extreme latitudes, Amanda[23], which operates near the South Pole, observes a 20% difference between winter and summer. A precise estimate of the seasonal variation of the high energy neutrino flux is rather difficult to obtain because it requires knowing the density profile of the atmosphere over the entire Earth. We have performed a simplified estimate of the size of this effect based on an analytic neutrino flux calculation [24] and the CIRA-86 atmosphere tables [25]. According to this calculation the amplitude of the seasonal variations of the ratio of the vertical to horizontal neutrino flux is of the order of $\pm 2.6\%$. Assuming a sinusoidal variation during the year, this amplitude corresponds to a root mean square value of about 1.3%. Dividing the MACRO data into a winter set (including the months from November up to April) and a summer set (the remaining months), we observe a difference in the ratio of the flux in the two angular bins of $19\% \pm 17\%$ between the two data sets, with a smaller value in the summer as expected for the seasonal variation, compatible inside the large errors with the expectations. We include in our estimate of the total systematical error in the predicted flux ratio a 1.3% contribution due to seasonal variations.

The systematic error due to the fact that the neutrino flux is calculated using the standard United States atmosphere has been estimated to be less than 1%. Accounting for all contributions to the systematic error, we estimate that the total uncertainty in the predicted value for the flux ratio is 4%.

The total systematic error in the measured value of the flux ratio has been estimated to be 4.6%. This error is due to uncertainties in the efficiency of the analysis cuts and detector efficiencies; it could be reduced in the future with a reprocessing of the data to correct for the change of the apparatus operating conditions with time. Combining in quadrature the theoretical error and the experimental error we obtain a total error in the ratio of about 6%.

In the full upgoing muon data set, there are 305 events with $\cos(\theta) \leq -0.7$, and 206 events with $\cos(\theta) \geq -0.4$, giving a value for the flux ratio of $R_{exp} = 1.48 \pm 0.13_{stat} \pm 0.10_{syst}$. This measured value can be compared with $R_{\tau_{min}}=1.72$ and $R_{sterile_{min}}=2.16$, which are the minimum possible values of R for $\nu_\mu \rightarrow \nu_\tau$ and $\nu_\mu - \nu_s$ oscillations respectively, for maximum mixing and Δm^2 of $0.0025 eV^2$. For values of $\sin^2 2\theta \leq 1$ the value of R is larger than R_{min} both for $\nu_\mu - \nu_s$ and $\nu_\mu \rightarrow \nu_\tau$. We note that this ratio does not have a gaussian distribution - the errors are reported only to give a crude estimate of the statistical significance. The corresponding one sided probability P_{best_τ} of measuring a value smaller than R_{exp} , assuming a true value for the ratio of $R_{\tau_{min}}$, is 8.4%. For $\nu_\mu - \nu_s$ the probability $P_{best_{ster}}$ is 0.033%. The ratio of the probabilities $P_{best_\tau} / P_{best_{ster}}$ is 254. This implies that $\nu_\mu - \nu_s$ oscillation (with any mixing) is excluded at about 99% C.L. compared with $\nu_\mu \rightarrow \nu_\tau$ oscillation with maximum mixing. In calculating these confidence limits we have considered correctly the non gaussian distribution of the ratio.

Additional information could be derived from the total number of events, at the expense of larger theoretical uncertainties. For the best value of Δm^2 for sterile neutrino oscillation we expect a flux reduction of $R_{flux} = 0.83$ for $\nu_\mu \rightarrow \nu_s$ and $\Delta m^2 = 0.0025 eV^2$, to be compared with the measured value 0.72. However, due to the

large theoretical uncertainty, the total number of events was not used in the statistical analysis presented here.

It should be noted that this analysis has been carried out for the two neutrino mixing case. A more complicated oscillation scenario, with 3 or more neutrinos [26], or the scenario with large extra dimensions [27] cannot be excluded.

In conclusion, using the improved statistics afforded by the full MACRO data set, the test of the shape of the angular distribution of upgoing muons is in good agreement with $\nu_\mu \rightarrow \nu_\tau$ oscillation, and maximal mixing. The best χ^2 is 9.7 for 9 degrees of freedom. Based on the ratio test, the $\nu_\mu \rightarrow \nu_s$ oscillation hypothesis has a 0.033% probability of agreeing with the data, and is disfavored at more than 99% C.L. with respect to the best fit point of $\nu_\mu \rightarrow \nu_\tau$ oscillation.

We thank T. Kajita for useful discussions to compare our data to those of Superkamiokande. We acknowledge the staff of the *Laboratori Nazionali del Gran Sasso* and the invaluable assistance of the technical staffs of all the participating Institutions. For generous financial contributions we thank the U.S. Department of Energy, the National Science Foundation, and the Italian *Istituto Nazionale di Fisica Nucleare*: both for direct support and for FAI grants awarded to non-Italian MACRO collaborators.

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