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Observation of D^{0} $\rightarrow \rho^{0}$ and Search for CP Violation in Radiative Charm Decays

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Observation of $D^0 o ho^0 \gamma$ and search for CP violation in radiative charm decays

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We report the first observation of the radiative charm decay $D^0 \to \rho^0 \gamma$ and the first search for CP violation in decays $D^0 \to \rho^0 \gamma$, $\phi \gamma$, and $\overline{K}^{*0}(892)\gamma$, using a data sample of 943 fb⁻¹ collected with the Belle detector at the KEKB asymmetric-energy e^+e^- collider. The branching fraction is measured to be $\mathcal{B}\left(D^0 \to \rho^0 \gamma\right) = (1.77 \pm 0.30 \pm 0.07) \times 10^{-5}$, where the first uncertainty is statistical and the second is systematic. The obtained CP asymmetries, $\mathcal{A}_{CP}\left(D^0 \to \rho^0 \gamma\right) = +0.056 \pm 0.152 \pm 0.006$, $\mathcal{A}_{CP}\left(D^0 \to \phi \gamma\right) = -0.094 \pm 0.066 \pm 0.001$, and $\mathcal{A}_{CP}\left(D^0 \to \overline{K}^{*0}\gamma\right) = -0.003 \pm 0.020 \pm 0.000$, are consistent with no CP violation. We also present an improved measurement of the branching fractions $\mathcal{B}\left(D^0 \to \phi \gamma\right) = (2.76 \pm 0.19 \pm 0.10) \times 10^{-5}$ and $\mathcal{B}\left(D^0 \to \overline{K}^{*0}\gamma\right) = (4.66 \pm 0.21 \pm 0.21) \times 10^{-4}$.

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Within the Standard Model (SM), charge-parity (CP) 109 matrix [1] and is expected to be very small for charmed 107 violation in weak decays of hadrons arises due to a sin- 110 hadrons: up to a few 10^{-3} [2–4]. Observation of CP 108 gle irreducible phase in the Cabibbo-Kobayashi-Maskawa 111 violation above the SM expectation would be an indi-

124 non-perturbative processes that can enhance the branch- 180 We retain candidate ρ^0 , ϕ , or \overline{K}^{*0} resonances if their

branching fraction at 2×10^{-4} [13]. 136 $D^0 \to \rho^0 \gamma$, improved branching fraction measurements of 192 rial background, we restrict the energy released in the $_{137}$ $D^0 \to \phi \gamma$ and $\overline{K}^{*0} \gamma$, as well as the first search for CP vi- $_{193}$ decay, $q \equiv M(D^{*+}) - M(D^0) - m(\pi^+)$, where m is the $_{138}$ olation in all three decays. Inclusion of charge-conjugate $_{194}$ nominal mass, to lie in a $\pm 0.6\,\mathrm{MeV}/c^2$ window around 139 modes is implied unless noted otherwise. The measure- 195 the nominal value [22]. To further reduce the combinatoments are based on 943 fb⁻¹ of data collected at or near 196 rial background contribution, we require the momentum the $\Upsilon(nS)$ resonances (n=2,3,4,5) with the Belle detector of the D^{*+} in the center-of-mass system $[p_{\text{CMS}}(D^{*+})]$ to tor [14, 15], operating at the KEKB asymmetric-energy 198 exceed 2.72, 2.42, and 2.17 GeV/c in the $\rho^0\gamma$, $\phi\gamma$, and $_{143}$ e^+e^- collider [16, 17]. The detector components relevant $_{199}$ $\overline{K}^{*0}\gamma$ modes, respectively. 148 lation counters (TOF) and an array of aerogel threshold 204 signal branching fraction is Cherenkov counters (ACC), and a CsI(Tl) crystal-based electromagnetic calorimeter (ECL). All are located inside a superconducting solenoid coil that provides a 1.5 T magnetic field.

We use Monte Carlo (MC) events, generated using 154 EVTGEN [18], JETSET [19] and PHOTOS [20], followed with a GEANT3 [21] based detector simulation, repre-156 senting six times the data luminosity, to devise selection criteria and investigate possible sources of background. The selection optimization is performed by maximizing $S/\sqrt{S+B}$, where S (B) is the number of signal (back-160 ground) events in a signal window of the reconstructed 209 depends not only on the CP asymmetry, $\mathcal{A}_{CP}=161\ D^0$ invariant mass $1.8\ {\rm GeV}/c^2 < M(D^0) < 1.9\ {\rm GeV}/c^2.$ 210 $[\mathcal{B}(D^0 \to f) - \mathcal{B}(\overline{D}^0 \to \overline{f})]/[\mathcal{B}(D^0 \to f) + \mathcal{B}(\overline{D}^0 \to \overline{f})],$ simulations in accordance with Ref. [7], while the branch- 212 production asymmetry (A_{FB}) [23–25] and the asymmetry world-average values [22].

 $_{167}$ a \overline{K}^{*0} with a photon. The vector resonances are formed $_{216}$ imation assuming all terms to be small. The last two

112 cation of new physics. This phenomenon in the charm 168 from $\pi^+\pi^-$ (ρ^0), K^+K^- (ϕ), and $K^-\pi^+$ (\overline{K}^{*0}) combinasector has been extensively probed in the past decade 169 tions. Charged particles are reconstructed in the tracking in many different decays [5], reaching a sensitivity below 170 system. A likelihood ratio for a given track to be a kaon 0.1% in some cases [6]. The search for CP violation in $_{171}$ or pion is obtained by utilizing specific ionization in the radiative charm decays is complementary to the searches 172 CDC, light yield from the ACC, and information from that have been exclusively performed in hadronic or lep- 173 the TOF. Photons are detected with the ECL and retonic decays. Theoretical calculations [7, 8] show that, 174 quired to have energies of at least 540 MeV. To suppress in SM extensions with chromomagnetic dipole operators, $_{175}$ events with two daughter photons from a π^0 decay formsizable CP asymmetries can be expected in $\bar{D^0} \to \phi \gamma$ 176 ing a merged cluster, we restrict the ratio of the energy and $\rho^0 \gamma$ decays. No experimental results exist to date 177 deposited in a 3 × 3 array of ECL crystals (E₉) and that regarding CP violation in any of the radiative D decays. 178 in the enclosing 5×5 array (E_{25}) to be above 0.94. About Radiative charm decays are dominated by long-range 179 63% of merged clusters are rejected by this requirement. ing fractions up to 10^{-4} , whereas short-range interactions 181 invariant masses are within 150, 11, or $60 \,\mathrm{MeV}/c^2$ of are predicted to yield rates at the level of 10^{-8} [9, 10]. 182 their nominal masses [22], respectively. The D^0 mesons Measurements of branching fractions of these decays can 183 are required to originate from $D^{*+} \to D^0 \pi^+$ in order to therefore be used to test the QCD-based calculations of 184 identify the D^0 flavor and to suppress the combinatolong-distance dynamics. The radiative decay $D^0 \to \phi \gamma$ 185 rial background. The associated track must satisfy the was first observed by Belle [11] and later measured with 186 aforementioned pion-hypothesis requirement. The D^0 131 increased precision by BABAR [12]. In the same study, 187 daughters are refitted to a common vertex, and the re- 132 BABAR made the observation of $D^0 \to \overline{K}^{*0}(892)\gamma$. As 138 sulting D^0 and the slow pion candidate from D^{*+} decay ₁₃₃ for $D^0 \to \rho^0 \gamma$, CLEO II has set an upper limit on its ₁₈₉ are constrained to originate from a common point within 190 the interaction point region. Confidence levels exceeding In this Letter, we present the first observation of 191 10⁻³ are required for both fits. To suppress combinato-

144 for our study are: a tracking system comprising a sili- 200 We measure the branching fractions and CP asym-145 con vertex detector and a 50-layer central drift chamber 201 metries of aforementioned radiative decays relative to $_{146}$ (CDC), a particle identification (PID) system that con- $_{202}$ well-measured hadronic D^0 decays to $\pi^+\pi^-$, K^+K^- , and sists of a barrel-like arrangement of time-of-flight scintil- $203~K^-\pi^+$ for the ρ^0 , ϕ , and \overline{K}^{*0} mode, respectively. The

$$\mathcal{B}_{\text{sig}} = \mathcal{B}_{\text{norm}} \times \frac{N_{\text{sig}}}{N_{\text{norm}}} \times \frac{\varepsilon_{\text{norm}}}{\varepsilon_{\text{sig}}} \quad ,$$
 (1)

where N is the extracted yield, ε the reconstruction effi- $_{206}$ ciency, and \mathcal{B} the branching fraction for the correspond- $_{207}$ ing mode. The raw asymmetry in decays of D^0 mesons 208 to a specific final state f,

$$A_{\text{raw}} = \frac{N(D^0 \to f) - N(\overline{D}^0 \to \overline{f})}{N(D^0 \to f) + N(\overline{D}^0 \to \overline{f})},\tag{2}$$

The branching fraction of $D^0 \to \rho^0 \gamma$ is set to 3×10^{-5} in ₂₁₁ but also on the contributions from the forward-backward ing fractions of the other two decay modes are set to their 213 try due to different reconstruction efficiencies for pos-214 itively and negatively charged particles (A_{ε}^{\pm}) : $A_{\text{raw}} =$ We reconstruct D^0 mesons by combining a ρ^0 , ϕ , or $_{215}$ $\mathcal{A}_{CP} + A_{FB} + A_{\varepsilon}^{\pm}$. Here, we have used a linear approx-

$$\mathcal{A}_{CP}^{\text{sig}} = A_{\text{raw}}^{\text{sig}} - A_{\text{raw}}^{\text{norm}} + \mathcal{A}_{CP}^{\text{norm}}, \tag{3}$$

the normalization mode [5].

232 network. The final criterion on the veto variable rejects 288 in the ρ^0 and \overline{K}^{*0} modes. All parameters describing the $_{233}$ about $60\,\%$ of background while retaining $85\,\%$ of signal. $_{289}$ combinatorial background are allowed to vary in the fit. 235 the same signal efficiency as compared to the veto used 291 gible, except for the $\overline{K}^{*0}\pi^0$ and $K^-\rho^+$ backgrounds in 236 in previous Belle analyses [27]. A similar veto is con- 292 the \overline{K}^{*0} mode that are accomodated with an additional $_{237}$ sidered for background from $\eta \to \gamma \gamma$, but is found to $_{293}$ Gaussian in the mass PDF whose relative contribution is $_{238}$ be ineffective due to the larger η mass, which shifts the $_{294}$ a function of $\cos\theta_{H}.$ background further away from the signal peak.

²⁴¹ a simultaneous unbinned extended maximum likelihood ²⁹⁷ den decay $D^0 \to K_S^0 \gamma$, which yields mostly background ²⁴² fit of D^0 and \overline{D}^0 samples to the invariant mass of the ²⁹⁸ from $D^0 \to K_S^0 \pi^0$ and $D^0 \to K_S^0 \eta$. The same PID cri- 243 D^0 candidates and the cosine of the helicity angle θ_H . 299 teria as for signal decays are applied, along with the q 244 The latter is the angle between the momenta of the D^0 300 and $p_{\rm CMS}(D^{*+})$ requirements as determined for the ϕ and the $\pi^+, K^+, \text{ or } K^-$ in the rest frame of the ρ^0, ϕ, ∞ mode. The $K_S^0 \to \pi^+\pi^-$ candidates in a $\pm 9\,\mathrm{MeV}/c^2$ \overline{K}^{*0} , respectively. By angular momentum conserva- 302 window around the nominal mass are accepted. To cal-247 tion, the signal $\cos \theta_H$ distribution depicts a $1-\cos^2 \theta_H$ 303 ibrate the distribution, the simulated shape is smeared dependence; no background contribution is expected to 304 with a Gaussian function of width $(7\pm1)\,\mathrm{MeV}/c^2$ and exhibit a similar shape. For the ρ^0 and \overline{K}^{*0} modes, we 305 an offset $(-1.33 \pm 0.25)\,\mathrm{MeV}/c^2$. restrict the helicity angle range to $-0.8 < \cos \theta_H < 0.4$ to 306 The $\cos \theta_H$ signal distribution is parametrized as 1- $2.06 \,\mathrm{GeV}/c^2$ for all three signal channels.

257 eled with a Crystal-Ball probability density function [28] 313 and nonresonant amplitudes. For other background cate-Crystal-Ball and two Gaussians for the \overline{K}^{*0} mode. To 315 based on MC predictions. obtained values are applied to the other two modes.

₂₆₈ type backgrounds are $\rho^0\pi^0$, $\rho^{\pm}\pi^{\mp}$ and $K^-\rho^+$ with the ₃₂₄ The same is done for backgrounds with a photon from kaon being misidentified as pion. For the ϕ mode, the 325 FSR or radiative ρ decay in the ρ^0 and \overline{K}^{*0} modes. All

217 terms can be eliminated using the same normalization 271 the \overline{K}^{*0} mode, the π^{0} - and η -type backgrounds are the mode as used in the branching fraction measurements: 272 decays $D^0 \to \overline{K}^{*0}\pi^0$, $K^-\rho^+$, $K_0^*(1430)^-\pi^+$, $K^{*-}\pi^+$, (3) nonresonant $K^-\pi^+\pi^0$, $\overline{K}^{*0}\eta$ and nonresonant $K^-\pi^+\eta$. In all three signal modes, the 'other- D^0 ' background comwhere $\mathcal{A}_{CP}^{\text{norm}}$ is the nominal value of CP asymmetry of 275 prises all other decays wherein the D^0 is reconstructed ₂₇₆ from the majority of daughter particles. In the ρ^0 The dominant background arises from $D^0 \to f^+ f^- \pi^0$ 277 (\overline{K}^{*0}) mode, there are two additional small backgrounds: decays, with the π^0 subsequently decaying to a pair of 278 $\pi^+\pi^-(K^-\pi^+)$ with the photon being emitted as final photons, e.g., $D^0 \to \phi \pi^0 (\to \gamma \gamma)$. If one of the daughter 279 state radiation (FSR), and $K^- \rho^+$ with the photon arisphotons is missed in the reconstruction, the final state 280 ing from the radiative decay of the charged ρ meson. As mimics the signal decay. Such events are suppressed with 281 there are no missing particles, these decays exhibit the a dedicated π^0 veto in the form of a neural network [26] 282 same $M(D^0)$ distribution as the signal decays. We jointly constructed from two mass-veto variables, described be- 283 denote them as irreducible background. Their yields are low. The signal photon is paired for the first (second) 284 fixed to MC expectations and the known branching fractime with all other photons in the event having an en- 285 tions [22]. The remaining combinatorial background is ergy greater than 30 (75) MeV. The pair in each set whose 286 parametrized in $M(D^0)$ with an exponential function in diphoton invariant mass lies closest to $m(\pi^0)$ is fed to the 287 the ϕ mode and a second-order Chebyshev polynomial With this method, we reject 13% more background at 290 Possible correlations among the fit variables are negli-

The $M(D^0)$ PDF shape for the $\pi^0(\eta)$ -type background, We extract the signal yield and CP asymmetry via 296 obtained from MC samples, is calibrated using the forbid-

suppress backgrounds that peak at the edges of the dis- $307 \cos^2 \theta_H$ for all three modes. For the $V\pi^0$ and $V\eta$ (V=tribution. For the ϕ mode, where the background levels ρ^0 , ϕ , \overline{K}^{*0} categories, the shape is close to $\cos^2\theta_H$ and are lower overall, the entire $\cos \theta_H$ range is used. The D^0 309 described with a second- (ρ^0 and ϕ mode) or third-order candidate mass is restricted to $1.67\,\mathrm{GeV}/c^2 < M(D^0) < 310$ (\overline{K}^{*0} mode) Chebyshev polynomial. In the ϕ mode, a $_{311}$ linear term in $\cos \theta_H$ is added with a free coefficient to The invariant mass distribution of signal events is mod- 312 take into account possible interference between resonant (PDF) for the ρ^0 and ϕ modes, and with the sum of a 314 gories, the distributions are modeled using suitable PDFs

take into account possible differences between MC and $_{316}$ Apart from normalizations, the asymmetries A_{raw} of data, a free offset and scale factor are implemented for 317 signal and background modes are left free in the fit. All the mean and width of the \overline{K}^{*0} PDF, respectively. The 318 PDF shapes are fixed to MC values, unless previously 319 stated otherwise.

The π^0 - and η -type background $M(D^0)$ distributions 320 In the \overline{K}^{*0} mode, the yields (and A_{raw}) of certain are described with a pure Crystal-Ball or the sum of ei- 321 backgrounds that contain a small number of events (one ther a Crystal-Ball or logarithmic Gaussian [29] and up 322 or two orders of magnitude less than signal) are fixed: to two additional Gaussians. For the ρ^0 mode, the π^0 - 323 $K_0^*(1430)^-\pi^+$, $K^{*-}\pi^+$, and the 'other- D^0 ' background. 270 only π^0 -type background is the decay $D^0 \to \phi \pi^0$. For 326 fixed yields are scaled by the ratio between reconstructed

Table I. Efficiencies, extracted yields and A_{raw} values for all signal and normalization modes. The uncertainties are statis-

	Efficiency [%]	Yield	A_{raw}
$\rho^0 \gamma$	6.77 ± 0.09	500 ± 85	$+0.064 \pm 0.152$
$\phi\gamma$	9.77 ± 0.10	524 ± 35	-0.091 ± 0.066
$\overline{K}^{*0}\gamma$	7.81 ± 0.03	9104 ± 396	-0.002 ± 0.020
$\pi^+\pi^-$	21.4 ± 0.12	$(1.28 \pm 0.01) \times 10^5$	
K^+K^-	22.7 ± 0.12	$(3.62 \pm 0.01) \times 10^5$	$(2.2 \pm 1.7) \times 10^{-3}$
$K^-\pi^+$	27.0 ± 0.13	$(4.02 \pm 0.02) \times 10^6$	$(1.3 \pm 0.5) \times 10^{-3}$

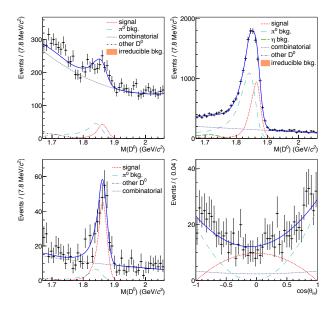


Figure 1. Top two panels are signal-enhanced projections of the combined $M(D^0)$ distribution for $D^0 \to \rho^0 \gamma$ (left) and $\overline{K}^{*0}\gamma$ (right). Bottom two panels are the signal-enhanced $M(D^0)$ (left) and $\cos \theta_H$ (right) distributions for $D^0 \to \phi \gamma$. Fit results are superimposed, with the fit components identified in the panel legend.

327 signal events in data and simulation of the normalization modes. We impose an additional constraint in the \overline{K}^{*0} η -type backgrounds, respectively. Since all are Cabibbofavored decays, \mathcal{A}_{CP} is expected to be zero, while other with the same final-state particles.

Fig. 1 shows the signal-enhanced $M(D^0)$ projections of $_{390}$ along with reconstruction efficiencies. The background $_{396}$ 0.23% for E_9/E_{25} and 1.15% for E_γ . raw asymmetries are consistent with zero.

344 teria as for signal modes for PID, vertex fit, q and 400 Wigner function. In the signal window, we compare the

 $p_{\text{CMS}}(D^{*+})$ are applied. The signal yield is extracted by subtracting the background in a signal window of $M(D^0)$, 347 where the background is estimated from a symmetrical 348 upper and lower sideband. The signal window and side-- 349 bands for the $\pi^+\pi^-$ mode are $\pm 15~{\rm MeV}/c^2$ and $\pm (20-35)$ 350 MeV/ c^2 around the nominal value [22], respectively. For the K^+K^- mode, the signal window is $\pm 14~{\rm MeV}/c^2$ and 352 sidebands are $\pm (31\text{-}45) \text{ MeV}/c^2$, whereas for the $K^-\pi^+$ mode, the signal window is $\pm 16.2~{
m MeV}/c^2$ and sidebands are $\pm (28.8-45.0) \text{ MeV}/c^2$. The obtained signal yields and raw asymmetries are also listed in Table I.

The systematic uncertainties are listed in Table II. All uncertainties are simultaneously estimated for \mathcal{B} and \mathcal{A}_{CP} , unless stated otherwise. There are two main sources: those due to the selection criteria and those arising from the signal extraction method, both for signal and normalization modes. Some of the uncertainties from the first group cancel if they are common to the signal and respective normalization mode, such as those related to PID, vertex fit, and the requirement on $p_{\text{CMS}}(D^{*+})$. A 2.2% uncertainty is ascribed to photon reconstruction efficiency [32]. Due to the presence of the photon in the signal modes, the resolution of the q distribution is worse than in the normalization modes. Thus, the related uncertainties cannot be assumed to cancel completely. We separately estimate the uncertainty due to the q requirement using the control channel $D^0 \to \overline{K}^{*0} \pi^0$. For both MC and data, the efficiency is $_{373}$ estimated by calculating the ratio R of the signal yield, $_{374}$ extracted with and without the requirement on q. Then, $_{375}$ the double ratio $R_{
m MC}/R_{
m data}$ is calculated to assess the possible difference between simulation and data. We ob- $_{377} an R_{\rm MC}/R_{\rm data}(q) = 1.0100 \pm 0.0016$. We do not correct 378 the efficiency by the central value; instead, we assign a 379 systematic uncertainty of 1.16%.

The double-ratio method is also used to estimate the $_{^{381}}$ uncertainty due to the $\pi^0\text{-veto}$ requirement on the control ₃₈₂ channel $D^0 \to K_S^0 \pi^0$. The veto is calculated by pairing 383 the first daughter photon (the more energetic one) of the π^0 with all others, but for the second daughter. The ratio mode by assigning two common $A_{\rm raw}$ variables to π^0 - and $_{385}$ R of so-discarded events is calculated for MC and data, $_{386}$ with all other selection criteria applied. The obtained ₃₈₇ double ratio is $R_{\rm MC}/R_{\rm data}(\pi^0 \text{ veto}) = 1.002 \pm 0.005$. The asymmetries contributing to $A_{\rm raw}$ are the same for decays $_{388}$ error directly translates to the systematic uncertainty of 389 the efficiency.

The systematic uncertainties due to the E_9/E_{25} and the combined sample in the region $-0.3 < \cos \theta_H < 0.3$ 391 E_{γ} requirements are estimated on the \overline{K}^{*0} mode by refor all three signal modes, as well as the signal-enhanced 392 peating the fit without any constraint on the variable in $\cos \theta_H$ projection in the 1.85 GeV/ c^2 < $M(D^0)$ < 393 question. The systematic error is the difference between $1.88\,\mathrm{GeV}/c^2$ region for the $\phi\gamma$ mode [30]. The obtained 394 the central value of the ratio $N_\mathrm{sig}/\varepsilon_\mathrm{sig}$ from this fit and signal yields and raw asymmetries are listed in Table I, 395 that of the nominal fit. The obtained uncertainties are

The systematic uncertainties due to the requirement The analysis of the normalization modes relies on the 398 on the mass of the vector meson are estimated using previous analysis by Belle [31]. The same selection cri- 399 the mass distribution, modeled with a relativistic Breit401 integrals of the nominal function and the same modified by the uncertainties on the central value and width. The 403 obtained uncertainties are 0.2% for the ρ^0 mode, 0.1% for the ϕ mode, and 1.7% for the \overline{K}^{*0} mode. All uncertainties described above are summed in quadrature and the final value is listed as 'Efficiency' in Table II. They affect only the branching fraction, as they cancel in Eq. 2.

For the fit procedure, a systematic uncertainty must be ascribed to every parameter that is determined and fixed to MC values but might differ in data. The fit procedure is repeated with each parameter varied by its uncertainty on the positive and negative sides. The larger deviation from the nominal branching fraction or \mathcal{A}_{CP} value is taken as the double-sided systematic error and these are summed in quadrature for all parameters. An uncertainty is assigned to the calibration offset and width of the π^0 -type backgrounds. For the ϕ and ρ^0 modes, the 418 uncertainty is calculated for the width scale factor (and $_{\mbox{\tiny 419}}$ offset) of the signal $M(D^0)$ PDF and $\pi^0\text{-type}$ background 420 varied simultaneously. All these quadratically summed 421 uncertainties are listed as 'Fit parametrization' in Ta-

The values of the fixed yields of some backgrounds in the ρ^0 and \overline{K}^{*0} mode are varied according to the uncertainties of the respective branching fractions [22]. For the category with the FSR photon, a 20% variation is used [33]. As the branching fractions contributing to the 'other- D^0 ' background in the \overline{K}^{*0} mode are unknown, we apply the largest variation from among other categories. The quadratically summed uncertainty is listed as 'Background normalization' in Table II.

For the normalization modes, the procedure is repeated the nominal $m(D^0)$ value. The statistical error from sideband subtraction is taken into account. Since possible differences in the signal shape between simulation and data could also affect the signal yield, a similar proce-438 dure as for the calibration of the π^0 background is performed. A systematic uncertainty is assigned for the case when the MC shape is smeared by a Gaussian of width $1.6 \,\mathrm{MeV}/c^2$. All uncertainties arising from normalization 442 modes are summed in quadrature and listed as 'Normal-443 ization mode' in Table II.

Finally, an uncertainty is assigned by varying the nom-445 inal values of the branching fractions and \mathcal{A}_{CP} of the 446 normalization modes and vector meson sub-decay modes 476 are consistent with no CP violation. Since the unby their respective uncertainties.

449 ing fraction and \mathcal{A}_{CP} in three radiative charm decays 479 ment [36]. 450 $D^0 \to \rho^0 \gamma$, $\phi \gamma$, and $\overline{K}^{*0} \gamma$ using the full dataset recorded 480 We thank the KEKB group for excellent operation 451 by the Belle experiment. We report the first observa- 481 of the accelerator; the KEK cryogenics group for effi-₄₅₂ tion of $D^0 \to \rho^0 \gamma$ with a significance of 5.5 σ , including ₄₈₂ cient solenoid operations; and the KEK computer group, 453 systematic uncertainties. The significance is calculated 483 the NII, and PNNL/EMSL for valuable computing and $_{454}$ as $\sqrt{-2\ln(\mathcal{L}_0/\mathcal{L}_{\max})}$, where \mathcal{L}_0 is the likelihood value $_{484}$ SINET4 network support. We acknowledge support from 455 with the signal yield fixed to zero and \mathcal{L}_{max} is that of 485 MEXT, JSPS and Nagoya's TLPRC (Japan); ARC (Aus-

Table II. Systematic uncertainties for all three signal modes.

	$\sigma(\mathcal{B})/\mathcal{B}$ [%]			$A_{CP} \left[\times 10^{-3} \right]$ $\phi \ \overline{K}^{*0} \ \rho^0$		
	ϕ	\overline{K}^{*0}	$ ho^0$	ϕ	\overline{K}^{*0}	$ ho^0$
Efficiency	2.8	3.3	2.8	_	_	_
Fit parametrization	1.0	2.8	2.3	0.1	0.4	5.3
Background normalization	_	0.3	0.6	_	0.2	0.5
Normalization mode	0.0	0.0	0.1	0.5	0.0	0.3
External \mathcal{B} and \mathcal{A}_{CP}	2.0	1.0	1.8	1.2	0.0	1.5
Total	3.6	4.5	4.1	1.3	0.4	5.5

cluded by convolving the statistical likelihood function with a Gaussian of width equal to the systematic uncer-459 tainty that affects the signal yield. The measured ratios 460 of branching fractions to their normalization modes are $\begin{array}{l} \mbox{\tiny 461} \ (1.25\pm0.21\pm0.05)\times 10^{-2}, \, (6.88\pm0.47\pm0.21)\times 10^{-3} \ \mbox{and} \\ \mbox{\tiny 462} \ (1.19\pm0.05\pm0.05)\times 10^{-2} \ \mbox{for} \ D^0 \rightarrow \rho^0 \gamma, \, \phi\gamma, \, \mbox{and} \ \overline{K}^{*0}\gamma, \end{array}$ 463 respectively. The first uncertainty is statistical and the 464 second systematic. Using world-average values for the 465 normalization modes [22], we obtain

$$\mathcal{B}\left(D^{0} \to \rho^{0} \gamma\right) = (1.77 \pm 0.30 \pm 0.07) \times 10^{-5},$$

$$\mathcal{B}\left(D^{0} \to \phi \gamma\right) = (2.76 \pm 0.19 \pm 0.10) \times 10^{-5},$$

$$\mathcal{B}\left(D^{0} \to \overline{K}^{*0} \gamma\right) = (4.66 \pm 0.21 \pm 0.21) \times 10^{-4}.$$

 $_{\mbox{\tiny 466}}$ For the ρ^0 mode, the obtained value is considerably larger 467 than theoretical expectations [34, 35]. The result of the $_{468}$ ϕ mode is improved compared to the previous determi-469 nations by Belle and BABAR, and is consistent with the 470 world average value [22]. Our branching fraction of the with shifted sidebands, starting from $\pm 25\,\mathrm{MeV}/c^2$ from $_{471}^{-1}\,\overline{K}^{*0}$ mode is 3.3σ above the BABAR measurement [12]. Both ϕ and \overline{K}^{*0} results agree with the latest theoretical 473 calculations [10].

> We also report the first measurement of \mathcal{A}_{CP} in these 475 decays. The values, obtained from Eq. 3:

$$\mathcal{A}_{CP} \left(D^0 \to \rho^0 \gamma \right) = +0.056 \pm 0.152 \pm 0.006,$$

 $\mathcal{A}_{CP} \left(D^0 \to \phi \gamma \right) = -0.094 \pm 0.066 \pm 0.001,$
 $\mathcal{A}_{CP} \left(D^0 \to \overline{K}^{*0} \gamma \right) = -0.003 \pm 0.020 \pm 0.000,$

477 certainty is statistically dominated, the sensitivity can We have conducted a measurement of the branch- 478 be greatly enhanced at the upcoming Belle II experi-

456 the nominal fit. The systematic uncertainties are in-486 tralia); FWF (Austria); NSFC and CCEPP (China);

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