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Recommended Citation

et al., C. Beleño; Joffe, D.; and Kulasiri, Ratnappuli L., "Measurement of the decays $B \rightarrow \eta \ell \nu \ell$ and $B \rightarrow \eta' \ell \nu \ell$ in fully reconstructed events at Belle" (2017). *Faculty Publications*. 4206.
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Measurement of the Decays $B \rightarrow \eta \ell \nu_\ell$ and $B \rightarrow \eta' \ell \nu_\ell$ in Fully Reconstructed Events at Belle

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We report branching fraction measurements of the decays $B^+ \rightarrow \eta \ell^+ \nu_\ell$ and $B^+ \rightarrow \eta' \ell^+ \nu_\ell$ based on 711 fb^{-1} of data collected near the $\Upsilon(4S)$ resonance with the Belle experiment at the KEKB asymmetric-energy e^+e^- collider. This data sample contains 772 million $B\bar{B}$ events. One of the two B mesons is fully reconstructed in a hadronic decay mode. Among the remaining (“signal- B ”) daughters, we search for the η meson in two decay channels, $\eta \rightarrow \gamma\gamma$ and $\eta \rightarrow \pi^+\pi^-\pi^0$, and reconstruct the η' meson in $\eta' \rightarrow \eta\pi^+\pi^-$ with subsequent decay of the η into $\gamma\gamma$. Combining the two η modes and using an extended maximum likelihood, the $B^+ \rightarrow \eta \ell^+ \nu_\ell$ branching fraction is measured to be $(4.2 \pm 1.1(\text{stat.}) \pm 0.3(\text{syst.})) \times 10^{-5}$. For $B^+ \rightarrow \eta' \ell^+ \nu_\ell$, we observe no significant signal and set an upper limit of 0.72×10^{-4} at 90% confidence level.

PACS numbers: 13.20.He, 14.40.Nd

The magnitude of the Cabibbo-Kobayashi-Maskawa matrix element $|V_{ub}|$ [1, 2] can be determined by *inclusive* measurements sensitive to the entire $b \rightarrow u\ell\nu_\ell$ rate in a given region of phase space, or by *exclusive* mea-

surements of specific $b \rightarrow u$ decays such as $B \rightarrow \pi\ell\nu_\ell$. As both experimental and theoretical uncertainties differ in the two approaches, consistency between the inclusive and exclusive determinations of $|V_{ub}|$ is a crucial cross-

check of our understanding of the CKM mechanism. At present, inclusive and exclusive measurements of $|V_{ub}|$ disagree by about three standard deviations [3]. Precise measurements of $B \rightarrow \eta \ell \nu_\ell$ and $B \rightarrow \eta' \ell \nu_\ell$ rates will improve the inclusive signal modelling, since the lack of knowledge on all exclusive $b \rightarrow u \ell \nu$ decays is one of the contributions to the systematic uncertainty [4]. Also, a measurement of the ratio $\mathcal{B}(B \rightarrow \eta \ell \nu_\ell)/\mathcal{B}(B \rightarrow \eta' \ell \nu_\ell)$ determines the $\eta - \eta'$ mixing angle and the $F_+^{B \rightarrow \eta^{(\prime)}}$ form factor [5, 6] by constraining the gluonic singlet contribution to this form factor in the LCSR calculation [4]. In this paper, we report measurements of the branching fractions $\mathcal{B}(B^+ \rightarrow \eta \ell^+ \nu_\ell)$ and $\mathcal{B}(B^+ \rightarrow \eta' \ell^+ \nu_\ell)$ [7], where ℓ stands for either an electron or a muon. These are the first measurements of these decays based on the Belle data sample. The modes have been studied previously by CLEO [8, 9] and BaBar [10–13].

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect K_L^0 mesons and to identify muons (KLM). The detector is described in detail elsewhere [14].

In this analysis, we use the entire Belle data sample of 711 fb^{-1} collected at the KEKB asymmetric-energy e^+e^- collider [15] at the center-of-mass (c.m.) energy of the $\Upsilon(4S)$ resonance. The sample contains $(772 \pm 11) \times 10^6$ $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ events. Two inner detector configurations were used in the course of the experiment. A 2.0 cm beampipe and a 3-layer silicon vertex detector were used for the first sample of 152×10^6 $B\bar{B}$ pairs, while a 1.5 cm beampipe, a 4-layer silicon detector, and a small-cell inner drift chamber were used to record the remaining 620×10^6 $B\bar{B}$ pairs [16].

Monte Carlo (MC) simulated samples are generated using the EvtGen [17] package and the response of the detector is modeled using GEANT3 [18]. MC samples equivalent to about five times the integrated luminosity are produced for $\Upsilon(4S) \rightarrow B\bar{B}$ events and $e^+e^- \rightarrow q\bar{q}$ continuum events, where q stands for a u, d, s or c quark. Simulated samples containing the decay $b \rightarrow u \ell \nu$ equivalent to 20 times the integrated luminosity are used in this analysis. In these samples, the decays $B^+ \rightarrow \eta \ell^+ \nu_\ell$ and $B^+ \rightarrow \eta' \ell^+ \nu_\ell$ have been generated according to the ISWG2 [19] calculation of the form factors.

After selecting hadronic events ($\Upsilon(4S) \rightarrow B\bar{B}$, $e^+e^- \rightarrow q\bar{q}$) based on the charged track multiplicity and the total visible energy [20], we reconstruct one B meson (B_{tag}) of the $B\bar{B}$ pair in a hadronic decay mode using the Belle full reconstruction software [21] based on the

NeuroBayes neural-network package [22]. A total of 1104 exclusive decay channels to charm mesons and 71 neural networks were employed to reconstruct B_{tag} whose quality is characterized by the NeuroBayes classifier (O_{NB}), which ranges from 0 to 1. We require that $\ln O_{NB} > -8$ to ensure good quality of B_{tag} . B_{tag} is identified using the beam-constrained mass, $M_{\text{bc}} = \sqrt{E_{\text{beam}}^*{}^2 - |\vec{p}_{B_{\text{tag}}}^*|^2}$, and the energy difference, $\Delta E = E_{B_{\text{tag}}}^* - E_{\text{beam}}^*$, where E_{beam}^* is the energy of the colliding beam particles in the c.m. frame and $E_{B_{\text{tag}}}^*$ and $\vec{p}_{B_{\text{tag}}}^*$ are the reconstructed energy and three-momentum of the B_{tag} candidate in the same reference system [23]. For well-reconstructed candidates, ΔE peaks at zero and M_{bc} peaks at the nominal B mass; we retain events that satisfy $-0.1 \text{ GeV} < \Delta E < 0.05 \text{ GeV}$ and $5.27 \text{ GeV} < M_{\text{bc}} < 5.29 \text{ GeV}$. Finally, we select only the charged B_{tag} candidates since the signal mode only involves charged B mesons.

The other B meson in the event, B_{sig} , is reconstructed using all charged particles and neutral clusters not associated with the B_{tag} candidate. Low-momentum particles, which spiral inside the CDC and pass close to the interaction point, can lead to multiple reconstruction of the same particle. Duplicate tracks are identified as pairs of tracks with momenta transverse to the beam direction below 275 MeV, with a momentum difference below 100 MeV, and with an opening angle either below 15° or above 165° . Whenever such pair is found, we select the track passing closer to the interaction point.

Charged hadrons are identified using the ionization energy loss dE/dx in the CDC, the time-of-flight information provided by the TOF, and the response of the ACC [24]. Pions used in this analysis are identified with an efficiency of 98% and a kaon fake rate of 30%. Electron candidates are identified using the ratio of the energy detected in the ECL to the track momentum, the ECL shower shape, the position matching between the track and the ECL cluster, the energy loss in the CDC, and the response of the ACC. Muons are identified based on their penetration range and transverse scattering in the KLM detector. In the momentum region relevant to this analysis, charged leptons are identified with an efficiency of about 90% and the probability to misidentify a pion as an electron (muon) is 0.25% (1.4%) [25, 26]. We veto charged leptons from photon conversion and J/ψ decay if the lepton candidate, when combined with an oppositely charged particle, gives an invariant mass below 100 MeV or within ± 4.9 MeV around the nominal J/ψ mass. Only events with a single charged lepton candidate on the signal side are considered in this analysis.

Photons are reconstructed from clusters in the ECL not matched to a track. Beam-related background is removed by rejecting clusters with an energy below 50 MeV. Higher thresholds of 100 MeV and 150 MeV are applied in the forward ($17^\circ < \theta < 32^\circ$) and backward ($130^\circ < \theta < 150^\circ$) regions, respectively, where θ is the

laboratory-frame polar angle with respect to the opposite of the positron beam direction. Neutral pion candidates are reconstructed by combining two photons, requiring their invariant mass to lie between 120 and 150 MeV. The c.m. momentum of the π^0 candidate must exceed 200 MeV.

Then, η mesons are reconstructed in the decays $\eta \rightarrow \gamma\gamma$ and $\eta \rightarrow \pi^+\pi^-\pi^0$. Candidates are selected in the intervals $0.506 \text{ GeV} < M_{\gamma\gamma} < 0.584 \text{ GeV}$ and $0.535 \text{ GeV} < M_{\pi^+\pi^-\pi^0} < 0.560 \text{ GeV}$, determined by signal-to-background optimization on MC simulated events. We reconstruct η' candidates in the $\eta' \rightarrow \eta\pi^+\pi^-$ channel with $\eta \rightarrow \gamma\gamma$ and require $0.926 \text{ GeV} < M_{\eta\pi^+\pi^-} < 0.986 \text{ GeV}$. The aforementioned mass requirements correspond to 3σ windows around the nominal mass of the mesons. The fraction of events with multiple meson candidates after the signal selection corresponds to 17.5% for $\eta \rightarrow \gamma\gamma$, 7.4% for $\eta \rightarrow \pi^+\pi^-\pi^0$ and 36% for $\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$. If more than one $\eta^{(\prime)}$ candidate is found on the signal side, we select the one closer to the nominal $\eta^{(\prime)}$ mass [27]. For modes involving charged pions, we also use information on the signal vertex quality, and choose the candidate with the smallest χ_{tot}^2 defined as $\chi_{\text{mass}}^2 + \chi_{\text{vertex}}^2$.

After selecting the single charged lepton and the $\eta^{(\prime)}$ candidate, the remaining particles on the signal side are considered further to reduce background. We require no remaining charged particles. The sum of the energies of neutral clusters associated with neither B_{tag} nor B_{sig} must be below 0.5 GeV. To reject charged leptons inconsistent with the signal decay, the charge of the lepton must be opposite to that of the B_{tag} meson. Since the $\eta \rightarrow \gamma\gamma$ mode has a larger background than the $\eta \rightarrow \pi^+\pi^-\pi^0$ mode, we remove any events in the former channel that contain one or more neutral pions on the signal side. This π^0 veto is not applied to the $\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$ channel.

The $B \rightarrow \eta^{(\prime)}\ell\nu_\ell$ yield is extracted from the distribution of the missing mass squared, defined as $M_{\text{miss}}^2 = (p_{B_{\text{tag}}} - p_{\eta^{(\prime)}} - p_\ell)^2$, where $p_{B_{\text{tag}}}$, $p_{\eta^{(\prime)}}$ and p_ℓ are the four-momenta of the B_{tag} , $\eta^{(\prime)}$, and charged lepton candidates, respectively. For well-reconstructed signal decays, we expect M_{miss}^2 to peak at zero, as the only remaining particle in the event is the neutrino. We determine the yields of the signal, $b \rightarrow u\ell\nu_\ell$, $b \rightarrow c\ell\nu_\ell$ and continuum backgrounds from an extended binned maximum likelihood fit to the M_{miss}^2 distribution between -1.6 and 5.0 GeV^2 (with a bin width of 0.2 GeV^2). The shapes of the fit components are taken from MC simulation and the fitting algorithm accounts for statistical fluctuations in both the real data and the MC simulated samples [28]. As continuum is a small component, we fix it to the MC expected yield. The contributions from secondary and fake leptons are negligible and thus not taken into account as additional fit components. For $B^+ \rightarrow \eta\ell\nu_\ell$, the fit incorporates both η modes. As a cross-check, we

also determine the fit results for the individual η modes. In addition, we include also fit results for the regions of $q^2 = (p_\ell + p_{\nu_\ell})^2$ below and above 12 GeV^2 . These fit results are quoted in Table I and shown in Fig. 1. We carried out 10000 toy MC to validate the fit procedure. The distributions of signal and background in each ensemble are generated according to their measured values in data, and then the fit procedure is executed. The statistical uncertainties estimated by the nominal fit are consistent with the size of the uncertainties evaluated by the toy MC technique. However, given that in some channels the pull distribution exhibits a non-Gaussian shape, we do not apply a correction to the central value of the signal yields. Instead, we assign a systematic uncertainty associated with the fit procedure with values between 2% and 10% depending on the reconstructed channel.

The signal branching fractions are calculated as

$$\mathcal{B}(B^+ \rightarrow \eta^{(\prime)}\ell^+\nu_\ell) = \frac{1}{2} \frac{N_{\text{signal}}}{N_{B\bar{B}}\mathcal{B}(\eta^{(\prime)})\epsilon}, \quad (1)$$

where N_{signal} is the fitted signal yield from Table I, $N_{B\bar{B}}$ is the number of $B\bar{B}$ pairs in the Belle data, $\mathcal{B}(\eta^{(\prime)})$ is the world average value of the $\eta^{(\prime)}$ sub-decay branching fraction [27, 29] and ϵ is the signal efficiency including B_{tag} reconstruction, calibrated as described in Ref. [30]. The factor of 2 in the denominator indicates an average over lepton flavor. The combined and separate $B^+ \rightarrow \eta\ell^+\nu_\ell$ branching fractions are quoted in Table II. Our result for the $B^+ \rightarrow \eta\ell^+\nu_\ell$ branching fraction is $(4.2 \pm 1.1(\text{stat}) \pm 0.3(\text{syst.})) \times 10^{-5}$. The significance of the observed signal [31, 32] is calculated as $S = \sqrt{-2\Delta \ln(\mathcal{L})}$ with $\Delta \ln(\mathcal{L}) = \ln(\mathcal{L}_B) - \ln(\mathcal{L}_{S+B})$, where $\ln(\mathcal{L}_{S+B})$ is the maximized log-likelihood assuming a signal plus background hypothesis and $\ln(\mathcal{L}_B)$ is the maximized log-likelihood with background only. Systematic uncertainties are included by convolving \mathcal{L} with a Gaussian function of width corresponding to the systematic uncertainty in the number of signal events. The signal significance in the combined η mode sample is found to be $S = 3.7$, including systematic uncertainties related to the signal yield.

For $B^+ \rightarrow \eta'\ell^+\nu_\ell$, we calculate a branching fraction of $(3.6 \pm 2.7(\text{stat.})_{-0.4}^{+0.3}(\text{syst.})) \times 10^{-5}$ and a significance (including systematics) of $S = 1.6$. Given the low value of S , we convert this result into an upper limit on $\mathcal{B}(B^+ \rightarrow \eta'\ell^+\nu_\ell)$. Using the frequentist calculator from the RooStats package [33], we obtain a 90% confidence level upper limit of 11.6 events on the $B^+ \rightarrow \eta'\ell^+\nu_\ell$ signal yield or 0.72×10^{-4} on the branching fraction. For the $B^+ \rightarrow \eta\ell^+\nu_\ell$ channel this upper limit is of 51.2 events, corresponding an upper bound on the branching ratio of 0.55×10^{-4} .

We also determine the ratio $\mathcal{B}(B^+ \rightarrow \eta'\ell^+\nu_\ell)/\mathcal{B}(B^+ \rightarrow \eta\ell^+\nu_\ell)$ to be $0.86 \pm 0.68(\text{stat.}) \pm 0.09(\text{syst.})$, which is important to constraint the gluonic singlet contribution [4]. A 90% confidence level upper limit to the latter quantity

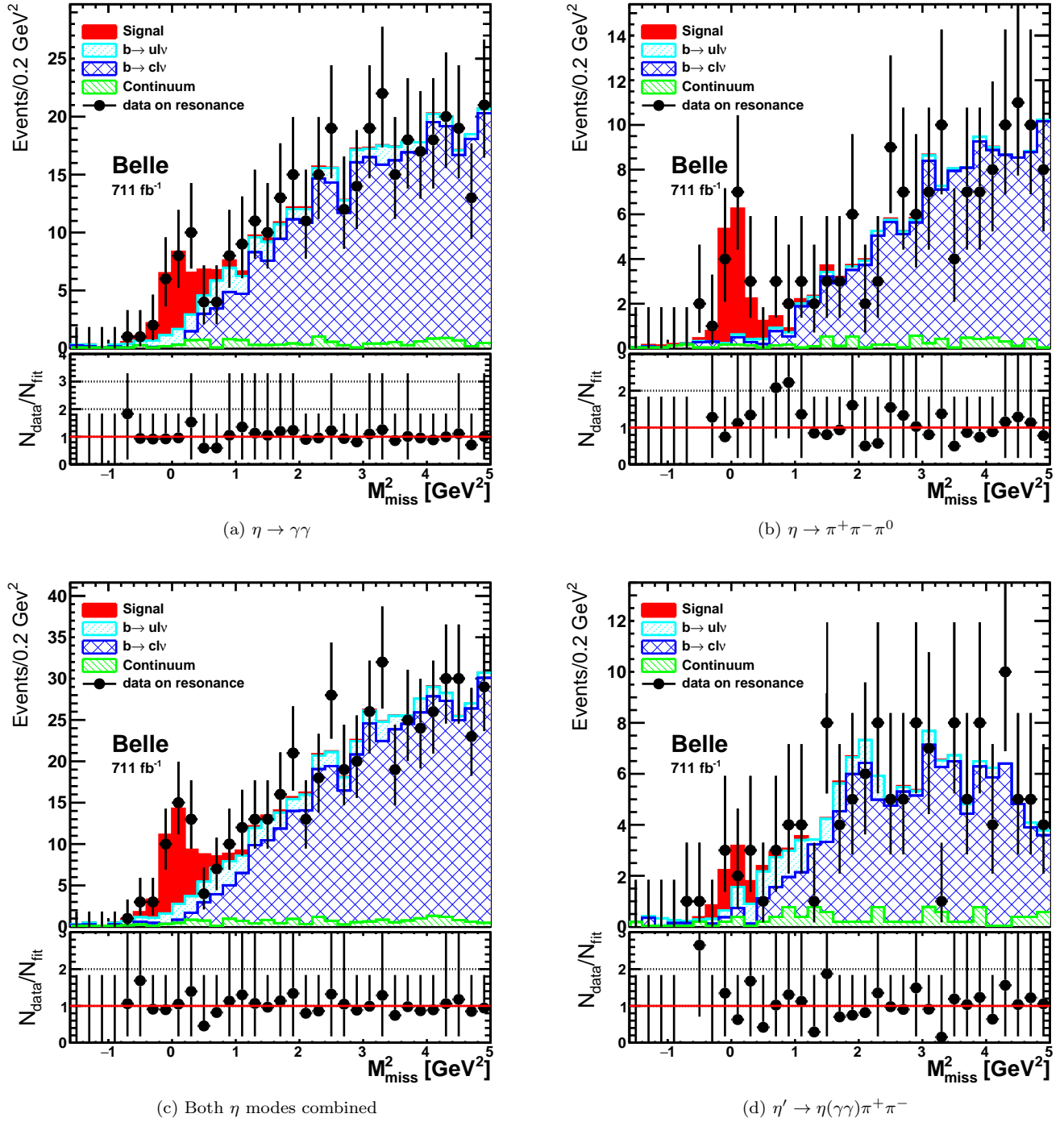


FIG. 1: Distribution of M_{miss}^2 (points with error bars) for: (a) $\eta \rightarrow \gamma\gamma$, (b) $\eta \rightarrow \pi^+\pi^-\pi^0$, (c) both η modes combined, and (d) $\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$. The fit results with the different components are shown as the colored histograms. The ratio of data to the sum of the fitted yields is shown below each plot.

is calculated to be $\mathcal{B}(B^+ \rightarrow \eta' \ell^+ \nu_\ell) / \mathcal{B}(B^+ \rightarrow \eta \ell^+ \nu_\ell) < 1.31$.

We compute the CKM matrix element $|V_{ub}|$ from our measurement of $\mathcal{B}(B^+ \rightarrow \eta \ell^+ \nu_\ell)$ in the region $q^2 < 12 \text{ GeV}^2$ using the light-cone sum rule (LCSR) calculation

of the form factor $f_+(q^2)$ in Ref. [4]. For that purpose we use the relation:

TABLE I: Fit results in regions of $q^2 = (p_\ell + p_{\nu_\ell})^2$ for the different modes. “Raw yield” denotes the number of events seen in the data; “signal”, “ $b \rightarrow ul\nu_\ell$ ”, “ $b \rightarrow cl\nu_\ell$ ” and “continuum” are the fitted yields. The continuum component is fixed and hence no fit errors are quoted. Only statistical uncertainties are shown.

Channel	$B^+ \rightarrow \eta l \nu_\ell$						$B^+ \rightarrow \eta' l \nu_\ell$			
	$\eta \rightarrow \gamma\gamma$			$\eta \rightarrow \pi^+ \pi^- \pi^0$			Both modes combined			$\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$
q^2 [GeV ²]	All	< 12	> 12	All	< 12	> 12	All	< 12	> 12	All
Raw yield	355	261	94	148	98	50	503	359	144	129
Signal	23.6±8.7	15.7±7.3	9.0±5.3	16.0±5.3	12.2±4.1	4.0±2.5	38.8±10.1	27.9±8.7	12.9±6.1	5.7±4.4
$b \rightarrow ul\nu_\ell$	32±25	22±27	10±13	4±21	1±5	4±8	46±29	30±29	14±18	15±13
$b \rightarrow cl\nu_\ell$	287±27	212±28	73±13	122±17	79±10	41±10	399±31	285±30	114±18	99±14
Continuum	12.7	10.4	2.3	6.2	5.2	0.9	18	15.7	3.2	9.7
ϵ [10 ⁻³]	1.21	1.28	0.99	0.53	0.57	0.44	0.96	1.02	0.79	0.61
χ^2/ndf	12.0/29	11.5/29	35.2/29	18.8/29	30.5/29	19.4/29	18.0/29	20.1/29	35.5/29	24.4/29
Probability[%]	99.8	99.8	19.0	92.5	39.1	91.1	94.4	88.8	18.9	70.9

TABLE II: Branching fraction of the decay $B^+ \rightarrow \eta l^+ \nu_\ell$ (in units of 10⁻⁵) calculated for the different samples and regions of q^2 . The first error is statistical and the second is systematic. The main result is the lower right value (Combined, All q^2). The values in the “Sum” row provide a cross-check.

	$\eta \rightarrow \gamma\gamma$	$\eta \rightarrow \pi^+ \pi^- \pi^0$	Combined
$q^2 < 12$ GeV ²	2.0 ± 0.9 ± 0.2	6.0 ± 2.0 ± 0.6	2.8 ± 0.9 ± 0.2
$q^2 > 12$ GeV ²	1.5 ± 0.9 ± 0.1	2.6 ± 1.6 ± 0.3	1.7 ± 0.8 ± 0.1
Sum	3.5 ± 1.3 ± 0.3	8.6 ± 2.6 ± 0.7	4.5 ± 1.2 ± 0.3
All q^2	3.4 ± 1.2 ± 0.3	8.5 ± 2.8 ^{+0.7} _{-0.8}	4.2 ± 1.1 ± 0.3

$$|V_{ub}| = \sqrt{\frac{C_v \Delta \mathcal{B}}{\tau_B \Delta \zeta}}, \quad (2)$$

where $C_v = 2$ for B^+ decays, $\Delta \mathcal{B}$ is the measured partial branching ratio for $q^2 < 12$ GeV², $\tau_B = 1.638(4)$ ps [27] is the lifetime of the B^+ meson and $\Delta \zeta$ is the decay rate provided by theory [4]. We determine $\Delta \zeta$ to be $(2.65^{+0.43}_{-0.47}) \times 10^{12}$ s⁻¹ and consequently $|V_{ub}| = (3.59 \pm 0.58(\text{stat.}) \pm 0.13(\text{syst.})^{+0.29}_{-0.32}(\text{theo.})) \times 10^{-3}$, which is in agreement with previous exclusive measurements [3].

The systematic uncertainties considered for the branching fractions are summarized in Table III and fall into two groups: those related to detector performance and those in the signal and background modeling. Uncertainties related to detector performance are derived from dedicated studies of control samples within the Belle experiment to measure the tracking efficiency of charged particles, the photon and neutral-pion reconstruction efficiency, and the charged-lepton and pion-identification efficiency. Systematic uncertainties related to the signal and background model are estimated by varying the

respective parameter in the simulation within its uncertainty or by reweighting MC samples. The deviation of the result from the nominal fit is taken as the uncertainty.

Uncertainties in the signal form factors are estimated by comparing the Ball-Zwicky model [34] to the ISGW2 model [19]. The form factor parameters of the former are taken from Ref. [4]. The HQET-based form factors of the decays $B \rightarrow D^{(*)} l \nu_\ell$ in the MC simulation are adjusted to the recent world average values [3]. The branching fractions of $B \rightarrow (D^{(*)}, \pi, \rho, \omega) l \nu_\ell$ have been corrected [27]. The hadronic branching fractions on the tag side are adjusted by the B_{tag} calibration and its uncertainty is taken from Ref. [30]. We vary the branching fractions of the $b \rightarrow ul\nu_\ell$ and $b \rightarrow cl\nu_\ell$ decay modes within ± 1 standard deviation of their world average values. We consider the form-factor uncertainties in the decays $B \rightarrow D^* l \nu_\ell$, $B \rightarrow D^0 l \nu_\ell$, $B \rightarrow \pi l \nu_\ell$, and $B \rightarrow \omega l \nu_\ell$, and uncertainties in the shape-function parameters of the inclusive $b \rightarrow ul\nu_\ell$ model. We further assign an uncertainty due to the branching fraction uncertainty in the $\eta^{(\prime)}$ sub-decay modes. The systematic error components in which a weight factor is applied include uncertainties due to secondary and fake leptons and the continuum.

The contribution of the secondary leptons is adjusted to the measured $b \rightarrow c \rightarrow \ell$ branching fraction. The contribution of events in which a lepton has been misidentified as a hadron is corrected using the fake rate measured in a kinematically selected $D^{*+} \rightarrow D^0(K^-\pi^+)\pi^+$ sample. Since the expected number of continuum events is small after signal selection, a comparison with off-resonance data is not carried out. Instead, we rely on MC simulation to estimate the systematic uncertainty associated with continuum normalization by varying the number of events by 20% and examining the effect on the fit. The deviation from the nominal fit is taken as the uncertainty. The uncertainty on the number of produced B -meson pairs is 1.4%.

In summary, we have measured the branching fraction of the decay $B^+ \rightarrow \eta \ell^+ \nu_\ell$ to be $(4.2 \pm 1.1 \pm 0.3) \times 10^{-5}$, where the first error is statistical and the second systematic. For the branching fraction of $B^+ \rightarrow \eta' \ell^+ \nu_\ell$, we determine a 90% confidence level upper limit of 0.72×10^{-4} . The measurements are compatible with previous analyses performed by CLEO and BaBar [8–13]. Our measurement is limited by the size of the Belle data sample. Significant improvements can thus be expected from the Belle II/SuperKEKB super flavor factory.

We thank the KEKB group for the excellent operation of the accelerator; the KEK cryogenics group for the efficient operation of the solenoid; and the KEK computer group, the National Institute of Informatics, and the PNNL/EMSL computing group for valuable computing and SINET5 network support. We acknowledge support from the Ministry of Education, Culture, Sports, Science, and Technology (MEXT) of Japan, the Japan Society for the Promotion of Science (JSPS), and the Tau-Lepton Physics Research Center of Nagoya University; the Australian Research Council; Austrian Science Fund under Grant No. P 26794-N20; the National Natural Science Foundation of China under Contracts No. 10575109, No. 10775142, No. 10875115, No. 11175187, No. 11475187, No. 11521505 and No. 11575017; the Chinese Academy of Science Center for Excellence in Particle Physics; the Ministry of Education, Youth and Sports of the Czech Republic under Contract No. LG14034; the Carl Zeiss Foundation, the Deutsche Forschungsgemeinschaft, the Excellence Cluster Universe, and the VolkswagenStiftung; the Department of Science and Technology of India; the Istituto Nazionale di Fisica Nucleare of Italy; the WCU program of the Ministry of Education, National Research Foundation (NRF) of Korea Grants No. 2011-0029457, No. 2012-0008143, No. 2014R1A2A2A01005286, No. 2014R1A2A2A01002734, No. 2015R1A2A2A01003280, No. 2015H1A2A1033649, No. 2016R1D1A1B01010135, No. 2016K1A3A7A09005603, No. 2016K1A3A7A09005604, No. 2016R1D1A1B02012900,

No. 2016K1A3A7A09005606, No. NRF-2013K1A3A7A06056592; the Brain Korea 21-Plus program and Radiation Science Research Institute; the Polish Ministry of Science and Higher Education and the National Science Center; the Ministry of Education and Science of the Russian Federation and the Russian Foundation for Basic Research; the Slovenian Research Agency; Ikerbasque, Basque Foundation for Science and the Euskal Herriko Unibertsitatea (UPV/EHU) under program UFI 11/55 (Spain); the Swiss National Science Foundation; the Ministry of Education and the Ministry of Science and Technology of Taiwan; and the U.S. Department of Energy and the National Science Foundation.

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TABLE III: Relative systematic uncertainties in the signal yield in per cent for the fits to the two η -mode samples and in the different q^2 regions.

Mode q^2 [GeV ²]	$\eta \rightarrow \gamma\gamma$			$\eta \rightarrow \pi^+\pi^-\pi^0$			Both η modes			$\eta' \rightarrow \eta(\gamma\gamma)\pi^+\pi^-$
	All	< 12	> 12	All	< 12	> 12	All	< 12	> 12	All
Track finding	± 0.35	± 0.35	± 0.35	± 1.05	± 1.05	± 1.05	± 0.5	± 0.5	± 0.5	± 1.05
Photon finding	± 4.0	± 4.0	± 4.0	± 0.0	± 0.0	± 0.0	± 3.1	± 3.1	± 3.1	± 4.0
π^0 reconstruction	± 0.0	± 0.0	± 0.0	± 2.5	± 2.5	± 2.5	± 0.5	± 0.5	± 0.5	± 0.0
π^0 veto	± 2.5	± 2.5	± 2.5	± 0.0	± 0.0	± 0.0	± 2.0	± 2.0	± 2.0	± 0.0
Pion ID	± 0.0	± 0.0	± 0.0	± 1.0	± 1.0	± 1.0	± 0.20	± 0.20	± 0.20	± 1.0
Lepton ID	± 2.0	± 2.0	± 2.0	± 2.0	± 2.0	± 2.0	± 2.0	± 2.0	± 2.0	± 2.0
Lepton fake rate	± 0.36	$^{+0.19}_{-0.13}$	± 0.11	$^{+0.46}_{-0.50}$	$^{+0.42}_{-0.47}$	$^{+0.18}_{-0.16}$	$^{+0.47}_{-0.44}$	± 0.51	$^{+0.02}_{-0.07}$	$^{+1.6}_{-1.8}$
Signal model	± 0.83	± 0.75	± 1.0	± 0.50	± 0.70	± 0.46	± 0.88	± 0.71	± 2.0	± 0.28
$b \rightarrow ul\nu_\ell$ form factors	± 1.1	± 0.49	± 0.72	$^{+1.8}_{-2.6}$	$^{+0.14}_{-0.16}$	$^{+0.82}_{-1.4}$	$^{+0.31}_{-0.43}$	$^{+0.73}_{-1.1}$	$^{+0.77}_{-0.70}$	$^{+0.92}_{-0.56}$
$b \rightarrow ul\nu_\ell$ branching fractions	$^{+0.26}_{-0.20}$	± 1.0	$^{+1.4}_{-1.3}$	$^{+0.04}_{-0.05}$	± 0.05	$^{+0.85}_{-0.95}$	$^{+0.50}_{-0.45}$	$^{+1.5}_{-1.8}$	$^{+0.86}_{-1.2}$	$^{+1.9}_{-2.4}$
$b \rightarrow cl\nu_\ell$ form factors	$^{+1.0}_{-0.15}$	$^{+2.3}_{-0.60}$	± 0.0	$^{+0.21}_{-0.06}$	$^{+0.70}_{-0.22}$	± 0.0	$^{+1.1}_{-0.10}$	$^{+1.3}_{-0.24}$	± 0.0	$^{+0.18}_{-0.23}$
$b \rightarrow cl\nu_\ell$ branching fractions	± 0.14	± 0.80	± 0.29	± 0.28	$^{+0.43}_{-0.45}$	$^{+0.18}_{-0.28}$	± 0.13	± 0.64	$^{+0.21}_{-0.27}$	± 0.62
Secondary leptons	$^{+0.00}_{-0.06}$	± 0.12	$^{+0.01}_{-0.03}$	$^{+0.07}_{-0.04}$	$^{+0.15}_{-0.13}$	$^{+0.02}_{-0.12}$	$^{+0.03}_{-0.01}$	± 0.08	$^{+0.06}_{-0.04}$	$^{+0.01}_{-0.00}$
$\mathcal{B}(\eta^{(\prime)})$ [29]	± 0.50	± 0.50	± 0.50	± 1.2	± 1.2	± 1.2	± 0.50	± 0.50	± 0.50	± 1.7
Hadronic tag	± 4.2	± 4.2	± 4.2	± 4.2	± 4.2	± 4.2	± 4.2	± 4.2	± 4.2	± 4.2
$N(B\bar{B})$	± 1.4	± 1.4	± 1.4	± 1.4	± 1.4	± 1.4	± 1.4	± 1.4	± 1.4	± 1.4
Continuum	$^{+0.77}_{-0.80}$	$^{+0.98}_{-0.96}$	$^{+0.24}_{-0.30}$	$^{+0.66}_{-0.64}$	$^{+1.1}_{-1.2}$	$^{+0.71}_{-0.62}$	± 0.47	± 0.83	$^{+1.2}_{-1.3}$	± 3.9
Fit procedure	± 2.9	± 9.8	± 2.0	± 6.3	± 8.7	± 9.6	± 2.2	± 5.6	± 3.2	± 5.2
Total	± 7.6	$^{+12.3}_{-12.1}$	± 7.3	$^{+8.8}_{-9.0}$	± 10.6	$^{+11.3}_{-11.4}$	± 6.7	± 8.7	$^{+7.4}_{-7.5}$	$^{+9.7}_{-9.8}$

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