## List of symbols

Number sets and vector spaces  $\mathbf{N}, \mathbf{Z}, \mathbf{Q}, \mathbf{R}, \mathbf{C}$ 

	complex numbers
$\mathbf{R}^n$	set of all real $n$ -tuples
$\mathbf{S}^{n-1}$	unit sphere of $\mathbf{R}^n$
$\mathbf{R}^n_+$	$\mathbf{R}^n \cap \{x_n \ge 0\}$
$\mathbf{C}^n$	set of all complex $n$ -tuples
$a \wedge b, a \vee b$	minimum and maximum of $a$ and $b$
$ \alpha $	the length of the multi-index $\alpha$ , i.e.
	$ \alpha  = \alpha_1 + \dots + \alpha_n$
$\operatorname{Re}\lambda,\operatorname{Im}\lambda$	real and imaginary part of $\lambda \in \mathbf{C}$
#E	the cardinality of the set E
Topological and metric space notation	
$\overline{E}$	topological closure of $E$
$\partial E$	topological boundary of $E$
$E^c$	the complementary set of $E$ in a domain
	$\Omega$ or in $\mathbf{R}^n$
$E \subset \subset F$	$\overline{E} \subset F, \overline{E}$ compact
$B(x_0,r)$	open ball with center $x$ and radius $r$
$B^{+}(0,r)$	$B(0,r) \cap \mathbf{R}^n_+$
$\mathcal{L}(X,Y)$	set of bounded and linear operators
	from $X$ to $Y$
$\mathcal{L}(X)$	$\mathcal{L}(X,X)$
X'	dual space of the Banach space $X$

set of natural, integer, rational, real and

Matrix and linear algebra T the identity matrix  ${\rm det}B$ the determinant of the matrix B*i*-th vector of the canonical basis of  $\mathbf{R}^n$  $e_i$  ${\rm Tr}B$ the trace of the matrix Bthe Euclidean norm of the matrix B, i.e.  $||B||_{\infty}$  $(\sum_{i,j=1}^{n} b_{ij}^{2})^{1/2} \\ (\sum_{i,j,h=1}^{n} |D_h b_{ij}|^2)^{1/2} \\ (\sum_{i,j,h=1}^{n} |D_h b_{ij}|^2)^{1/2}$  $||B||_{1,\infty}$  $(\sum_{i,j,h,k=1}^{n} |D_{hk}b_{ij}|^2)^{1/2}$  $||B||_{2,\infty}$  $\langle \cdot, \cdot \rangle$  or  $x \cdot y$ the Euclidean inner product between the vectors  $x, y \in \mathbf{R}^n$ Function spaces: let  $f: X \to Y$  $f \sqsubseteq E$  or  $f_{|E}$ restriction of f to  $E \subset X$ closure of  $\{x \in X : f(x) \neq 0\}$  $\operatorname{supp} f$ characteristic function of the set E $\chi_E$ partial derivative with respect to t $u_t$ partial derivative with respect to  $x_i$  $D_i$  $D_{ij}$  $D_i D_j$ Duspace gradient of a real-valued function u $D^2 u$ Hessian matrix of a real-valued function u $\operatorname{Tr}(D^2 u)$  $\Delta u$ C(X,Y)space of continuous functions from X into Y $C(\Omega)$ space of continuous functions valued in  $\mathbf{R}$  or  $\mathbf{C}$  $C_c(\Omega)$ functions in  $C(\Omega)$  with compact support in  $\Omega$  $C_0(\Omega)$ closure in the sup norm of  $C_c(\Omega)$  $UC_b(\Omega)$ space of the uniformly continuous and bounded functions on  $\Omega$  $C_{h}^{k}(\overline{\Omega})$ space of k-times differentiable functions with  $D^m f$ for  $|m| \leq k$  bounded and continuous up to the boundary  $C^{\alpha}(\Omega)$ space of  $\alpha$ -Hölder continuous functions,  $\alpha \in (0, 1)$  $C^{k,\alpha}(\Omega)$ space of  $f \in C^k(\Omega)$  with  $D^m f \in C^{\alpha}(\Omega)$  for  $|m| \leq k$  and  $\alpha \in (0,1)$  $\mathcal{S}(\mathbf{R}^n)$ Schwartz space of rapidly decreasing functions the seminorm  $\sup_{x,y\in\Omega}\frac{|u(x)-u(y)|}{|x-y|^{\alpha}}$  $[u]_{C^{\alpha}(\Omega)}$ sup norm  $\|\cdot\|_{L^{\infty}(\Omega)}$  $\sum_{|\alpha| < k} \|D^{\alpha}u\|_{L^{\infty}(\Omega)} + [D^{k}u]_{C^{\alpha}(\Omega)}$  $||u||_{C^{k,\alpha}(\Omega)}$ usual Lesbegue space  $(L^p(\Omega), \|\cdot\|_{L^p(\Omega)})$  $(W^{k,p}(\Omega), \|\cdot\|_{W^{k,p}(\Omega)})$ usual Sobolev space  $W^{k,p}_{\mathrm{loc}}(\Omega)$ space of functions belonging to  $W^{k,p}(\Omega')$ for every  $\Omega' \subset \subset \Omega$  $W_0^{k,p}(\Omega)$ closure of  $C_c^{\infty}(\Omega)$  in  $W^{k,p}(\Omega)$ dual space of  $W_0^{m,p'}(\Omega)$  with  $\frac{1}{p} + \frac{1}{p'} = 1$  $W^{-m,p}(\Omega)$  $BV(\Omega)$ functions with bounded variation in  $\Omega$ 

134

Operators	
$\mathcal{A}$	linear operator
$\mathcal{A}^*$	formal adjoint operator of $\mathcal{A}$
A	realization of $\mathcal{A}$ in a Banach space $X$
D(A)	the domain of $A$
$\rho(A)$	resolvent set of the linear operator $A$
$\sigma(A)$	spectrum of the linear operator $A$
Ι	identity operator
[A,B]	the operator $AB - BA$ defined in
	$D(AB) \cap D(BA)$
Measure theory and BV functions	
$\mathcal{B}(X)$	$\sigma\text{-}$ algebra of Borel subsets of a topological
	space $X$
$[\mathcal{M}(X)]^m$	the ${\bf R}^m$ -valued finite Radon measures on $X$
$\mathcal{M}^+(X)$	the space of positive finite measures on $X$
$\mathcal{L}^n$	Lebesgue measure in $\mathbf{R}^n$
$\omega_n$	Lebesgue measure of $B(0,1)$ in $\mathbb{R}^n$
$\mathcal{H}^k$	k-dimensional Hausdorff measure
$ E $ or $\mathcal{L}^n(E)$	the Lebesgue measure of the set E
$ \mu $	total variation of the measure $\mu$
$\mu  \sqsubseteq  E$	restriction of the measure $\mu$ to the set $E$
Du	distributional derivative of $u$
$\mathcal{P}(E,\Omega)$	perimeter of $E$ in $\Omega$
$\mathcal{P}(E)$	perimeter of $E$ in $\mathbf{R}^n$
$ u_E$	generalized inner normal to $E$
$E^t$	set of points of density $t$ of $E$
$\mathcal{F}E,\partial^*E$	reduced and essential boundary of ${\cal E}$