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Allan T. Gulledge Dartmouth College, Allan.Gulledge@Dartmouth.edu

Jaime J. Bravo Dartmouth College

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Neuronal Excitability

Neuron Morphology Influences Axon Initial Segment Plasticity^{1,2,3}

[®]Allan T. Gulledge¹ and [®]Jaime J. Bravo²

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¹Department of Physiology and Neurobiology, Geisel School of Medicine at Dartmouth, Dartmouth-Hitchcock Medical Center, Lebanon, New Hampshire 03756, and ²Thayer School of Engineering at Dartmouth, Hanover, New Hampshire 03755

Visual Abstract



In most vertebrate neurons, action potentials are initiated in the axon initial segment (AIS), a specialized region of the axon containing a high density of voltage-gated sodium and potassium channels. It has recently been proposed that neurons use plasticity of AIS length and/or location to regulate their intrinsic excitability. Here we quantify the impact of neuron morphology on AIS plasticity using computational models of simplified and realistic somatodendritic morphologies. In small neurons (e.g., dentate granule neurons), excitability was highest when the AIS was of intermediate length and located adjacent to the soma. Conversely, neurons having larger dendritic trees (e.g., pyramidal neurons) were most excitable when the AIS was longer and/or located away from the soma. For any given somatodendritic morphology, increasing dendritic membrane capacitance and/or conductance favored a longer and more distally located AIS. Overall, changes to AIS length, with corresponding changes in total sodium conductance, were far more effective in regulating neuron excitability than were changes in AIS location, while dendritic capacitance had a larger impact on AIS performance than did dendritic conductance. The somatodendritic influence on AIS performance reflects modest somato-AIS voltage attenuation combined with neuron size-dependent changes in AIS input resistance, effective membrane time constant, and

isolation from somatodendritic capacitance. We conclude that the impact of AIS plasticity on neuron excitability will depend largely on somatodendritic morphology, and that, in some neurons, a shorter or more distally located AIS may promote, rather than limit, action potential generation.

Key words: action potential; AIS plasticity; axon; axon initial segment; dendrite; sodium channel

Significance Statement

Action potentials in vertebrate neurons are initiated in the axon initial segment (AIS), a specialized region of axon containing a high density of voltage-gated sodium channels. It has been proposed that neurons regulate their intrinsic excitability via plastic changes in AIS length and/or location. Here we use computational modeling to quantify the impact of AIS plasticity across a range of simplified and realistic neuron morphologies. We demonstrate that somatodendritic morphology will dictate both the magnitude and direction of excitability changes occurring in response to AIS plasticity. Excitability of large neurons is enhanced when the AIS is longer and/or distal from the soma, while small neurons are most excitable when the AIS is of intermediate length and/or adjacent to the soma.

Introduction

Action potentials in most vertebrate neurons are initiated in a specialized region of proximal axon known as the axon initial segment (AIS). To promote action potential initiation, the AIS is enriched with voltage-gated sodium and potassium channels that occur at densities approximately 50 times greater than those at the soma (Kole et al., 2008). Previous studies have revealed cell typedependent heterogeneity in the architecture of the AIS, including diversity in AIS length and location relative to the soma. For instance, in the nucleus laminaris of the avian auditory system, neurons processing high-frequency sounds typically have a short (\sim 10 μ m) AIS located distally (~45 μ m) from the soma, while neurons responsive to lower-frequency sounds typically have a longer (~25 μ m) and more proximal (within \sim 10 μ m of the soma) AIS (Kuba et al., 2006).

It has recently been proposed that dynamic regulation of AIS architecture provides an intrinsic homeostatic mechanism to regulate neuron excitability in response to chronic changes in synaptic drive (Grubb et al., 2011). In cultured hippocampal neurons, for instance, prolonged periods of enhanced excitatory drive reversibly translocate the AIS away from the soma (Grubb and Burrone, 2010; Evans et al., 2013; Muir and Kittler, 2014). These shifts in AIS location were correlated with decreased intrinsic excitability, as reflected in higher somatic current thresholds (rheobase currents) for action potential initiation (Grubb and Burrone, 2010; Evans et al., 2013). Similarly, in both the auditory (Kuba et al., 2014) and visual (Gutzmann et al., 2014) systems, postnatal sensory experience sculpts AIS morphology, while experimental manipulations of sensory input drive dynamic modifications of AIS architecture (Gutzmann et al., 2014; Kuba et al., 2014) that correlate with changes in neuron excitability (Kuba et al., 2010).

However, the impact of AIS morphology on intrinsic excitability is not well understood. In general, a longer AIS, containing more sodium channels, is expected to enhance excitability (Kuba et al., 2010), while translocation of the AIS to distal locations experiencing greater voltage attenuation of synaptic signals is predicted to

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Correspondence should be addressed to Allan T. Gulledge, Department of Physiology and Neurobiology, Geisel School of Medicine at Dartmouth, 1 Medical Center Drive, DHMC, Borwell 704E, Lebanon, NH 03756. E-mail: allan.gulledge@dartmouth.edu.

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reduce excitability (Grubb and Burrone, 2010). Yet the AIS does not exist in isolation; somata and dendrites generate capacitive and conductive loads that influence excitability by facilitating the escape of inward sodium current from the AIS (Eyal et al., 2014). Therefore, the most excitable AIS length or location will depend on the balance of its electrical accessibility to depolarizing drive and electrical isolation from somatodendritic conductance loads (Kuba et al., 2006; Baranauskas et al., 2013).

The diversity of dendritic and axonal morphologies complicates predictions of how changes to AIS architecture will impact neuron excitability. To better understand the interaction between somatodendritic morphology and AIS plasticity, we paired models of simplified and realistic (reconstructed) neurons with a variety of AIS architectures. Our results demonstrate that AIS performance depends heavily on somatodendritic morphology, and suggest that, in some neurons, plastic changes in AIS length and location that are typically predicted to reduce neuron excitability may instead promote action potential initiation.

Materials and Methods

Simulations were performed using NEURON 7.3 software (Carnevale and Hines, 2006). Neuronal morphologies included simple "ball-and-stick" models consisting of a cylindrical soma (20 μ m in length \times 20 μ m in diameter) attached to a variable number of tapering dendrites (300 μ m long, tapering from 2.5 to 0.5 μ m in diameter), a medium spiny neuron (Martone et al., 2002), a hippocampal dentate granule cell (Schmidt-Hieber et al., 2007), a cerebellar Purkinje cell (Roth and Häusser, 2001), a layer 5 (L5) pyramidal neuron from the somatosensory cortex (Stuart and Spruston, 1998), and a hippocampal CA3 pyramidal neuron (Hemond et al., 2009). Unless otherwise noted, cytoplasmic resistivity (R_i), specific membrane capacitance (C_M), and specific membrane resistivity (R_M) were set to 100 Ω · cm, 1 μ F/cm², and 15,000 Ω · cm², respectively, with the reversal potential for the passive conductance set to -70 mV (Table 1). Realistic morphologies were attached to myelinated (Purkinje Cell and L5 pyramidal neuron) or unmyelinated (medium spiny neuron, dentate granule cell, and CA3 pyramidal neuron) axons (see below), as appropriate. In some simulations, the electrical impact of dendritic spines in realistic neuron morphologies was simulated by doubling dendritic C_M and halving dendritic R_M (Holmes, 1989). In simulations for movies involving the L5 neuron, apical dendrites included voltage-activated sodium and potassium conductances, and a hyperpolarization- and cyclic nucleotidegated cation conductance (Hallermann et al., 2012) whose conductance density increased exponentially according to the following function: $y_0 + A \exp(d/\lambda)$, where $y_0 = -2$ $pS/\mu m^2$, $A = 4.29 pS/\mu m^2$, $\lambda = 324 \mu m$, and d = distancefrom soma in micrometers (Kole et al., 2006). These conductances were left out of the L5 neuron in most simulations to standardize dendritic membrane properties across all realistic neuron morphologies. The presence (e.g., in the ball-and-stick neurons and layer 5 pyramidal neuron for movies) or absence (e.g., in the reconstructed

Table 1: Model parameters

Compartment	Dimensions (length × diameter)	Segments (n)	Max g_{Na^+}/g_{K^+} (pS/ μ m ²)
Dendrites	300 μ m, tapered from 2.5 to 0.5 μ m	101	Na ⁺ , linear decrease, 100-20; K ⁺ , linear decrease, 100-20
Somata	20 $ imes$ 20 μ m	11	Na ⁺ , 100; K ⁺ , 100
Proximal axon	$0-100 \times 1.5 \ \mu m$	\sim 1/ μ m	Na ⁺ , 100; K ⁺ , 100
AIS	$5-100 \times 1.5 \mu m$	$\sim 1/\mu m$	Na ⁺ , 8000; K ⁺ , 2000
Myelin segments (20)	$100 \times 1 \ \mu m$	21	Passive; C _M /10, R _M · 10
Nodes of Ranvier (20)	$1 \times 1.5 \mu m$	3	Na ⁺ , 2,667; K ⁺ , 667
Unmyelinated axon	$2000 \times 1 \ \mu m$	401	Na ⁺ , 300; K ⁺ , 60
Axon endpoint	$10 \times 10 \ \mu m$	11	Passive; $C_M \cdot 2$, $R_M/2$
MSN, DGC, Purkinje, L5, and CA3 neurons	Reconstructed morphologies	\sim 1/ μ m	Somata: Na ⁺ , 100; K ⁺ , 100; Dendrites, passive

DGC, Dentate granule cell; E_{pas} , reversal potential for passive leak conductance; MSN, medium spiny neuron. General parameters: $R_M = 15 \text{ k}\Omega \cdot \text{cm}^2$; $C_M = 1 \mu \text{F/cm}^2$; $R_i = 100 \Omega \cdot \text{cm}$; $E_{pas} = -70 \text{ mV}$; time steps, 0.1 or 1 μ s; nominal temperature, 37°C.

neuron morphologies) of active conductances in the dendrites did not qualitatively alter the impact of AIS plasticity.

The model neurons described above were attached to one of five AIS structures (AIS Models A, B, C, D, or E; Fig. 1). AIS Model A consisted of a variable-length AIS (5-100 μ m, 1.5 μ m diameter) containing either uniform maximum conductance densities for sodium (8000 pS/ μ m², unless otherwise noted) and potassium (2000 pS/ μ m²; Hallermann et al., 2012), or adjusted conductance densities set to conserve, across all AIS lengths, the equivalent maxi-

mal total sodium and potassium conductances as exist in a 30- μ m-long AIS having the sodium and potassium conductance densities stated above. Unless otherwise noted, voltage-gated sodium and potassium conductances were NEURON implementations of currents originally published by Mainen and Sejnowski (1996; available from entry 2488 at ModelDB at http://modeldb.yale.edu/). The variablelength AIS bridged the soma with a myelinated or unmyelinated axon (see below). AIS Model B consisted of a fixed 100- μ m-long proximal axon (1.5 μ m diameter) having somatic membrane properties that connected the



Figure 1. Diagrams of somatodendritic (left) and axonal (right) compartments in a model neuron. Somata ($20 \times 20 \ \mu$ m) were attached to a variable number of dendrites (300 μ m long, tapering from 2.5 to 0.5 μ m in diameter), and to one of five AISs. The AIS in Model A was variable in length (5-100 μ m), while AIS Model B had a 30- μ m-long AIS that was translocatable (from 0 to 70 μ m from the soma) within a 100- μ m-long proximal axon segment (1.5 μ m diameter) having somatic membrane properties. AIS Model C had a similar 30 μ m AIS fixed to the axon proper on one end, and to a variable amount of proximal axon (0-70 μ m long, 1.5 μ m diameter, with somatic membrane properties) bridging itself and the soma. AIS Model D was a hybrid model combining a variable-length proximal axon with a variable-length AIS (maximum combined length was 100 μ m). Finally, AIS Model E lacked an AIS altogether and consisted of an unmyelinated axon attached directly to the soma. AIS Models A through D were attached to myelinated or unmyelinated axons (see Materials and Methods). Inset at left illustrates the simulation setup in which rheobase current injections at the soma (40 ms duration) initiate action potentials.

soma to either a myelinated or unmyelinated axon. Within this proximal axon was a 30-µm-long AIS (maximum sodium and potassium conductance densities typically set to 8000 and 2000 pS/ μ m², respectively) that could be positioned at various distances from the soma (i.e., from 0 to 70 µm from the soma). An advantage of AIS Model B was that gross morphologies, total neuron surface areas, and total membrane conductances were conserved and independent of AIS location. A morphologically more realistic model, AIS Model C, consisted of a 30 µm AIS attached to a myelinated or unmyelinated axon on one end, and to a variable amount of soma-like proximal axon (0-70 μ m, 1.5 μ m diameter) between itself and the soma. AIS Model D was a hybrid of AIS Models A and C, having a variable-length AIS (5-70 μ m) paired with a variablelength proximal axon (0-95 μ m), with the combined structure limited to a maximum of 100 μ m. Finally, AIS Model E, which lacked an AIS altogether, consisted of an unmyelinated axon attached directly to the soma.

In some simulations the ratio of AIS to somatic sodium conductances (normally 80:1) was lowered. This was accomplished primarily by proportionally lowering the maximal AIS sodium and potassium conductance densities toward somatic values (normally 100 pS/ μ m² for each; Table 1). To preserve action potential initiation in the AIS at the 5:1 AIS-to-soma conductance ratio, maximal somatic sodium and potassium densities were raised to 200 pS/ μ m² (each), and maximal AIS densities of sodium and potassium conductances were set to 1,000 and 250 pS/ μ m², respectively. In simulations in which AIS-to-soma ratios were modified while the 30 μ m AIS was moved distally from the soma, no

active conductances were inserted into the proximal axon bridging the AIS to the soma.

Myelinated axons consisted of twenty 100- μ m-long passive segments having low membrane capacitance (C_M = 0.1 μ F/cm²) and high resistivity (R_M = 150 k $\Omega \cdot$ cm²), interspersed with 20 nodes of Ranvier (1- μ m-long, diameter of 1.5 μ m) having somatic passive properties and maximum sodium and potassium conductance densities set to one-third of those in the AIS (i.e., 2667 and 667 pS/ μ m², respectively; Table 1). Unmyelinated axons were 2000 μ m long (1 μ m diameter) and contained a uniform distribution of sodium (300 pS/ μ m²) and potassium (60 pS/ μ m²) conductances. All axons terminated with a 10 \times 10 μ m passive endpoint having a C_M of 2 μ F/cm² and an R_M of 7500 $\Omega \cdot$ cm², although control simulations found that the presence or absence of axon endpoints had no effect on rheobase currents at the soma (data not shown).

To compare the effective isolation of AIS compartments from somatodendritic capacitance, we computed a "C_M isolation index." To do this, for each AIS location we measured the percentage change in rheobase current produced by adding 5% to somatodendritic capacitance (i.e., after setting C_M in those compartments to 1.05 μ F/cm²). Using the following formula, we calculated the C_M isolation index, which reflects, for any given AIS location, the percentage by which the impact of changes to somatodendritic capacitance on rheobase current (as detected to the nearest 1 fA) are reduced relative to the maximal impact on rheobase current that occurs when the AIS is adjacent to the soma (where the C_M isolation index is 0), as follows:

$C_{\rm M} \text{ isolation index} = \frac{\% \text{ change in rheobase when AIS is at 0 } \mu \text{m} - \text{ local \% change in rheobase}}{\% \text{ change in rheobase when AIS is at 0 } \mu \text{m}} \times 100$

Unless otherwise noted, simulations were performed with 1 μ s time steps, and the rheobase determined to the nearest 100 fA in response to somatic current injection from action potentials occurring in the axon, regardless of whether these AIS action potentials successfully propagated to the soma. Indeed, it is important to note that we tested a wide range of AIS lengths and locations to fully explore the impact of somatodendritic geometry and AIS architecture on neuron excitability, and that in some models in which the AIS was remote from the soma (up to 95 μ m away), action potentials failed to propagate into the soma. For any given somatodendritic morphology, when more than one AIS morphology had equal minimal thresholds (at 100 fA resolution), the shortest or most proximal AIS having that minimal threshold was recorded as having the lowest rheobase. Simulations assumed a nominal temperature of 37°C, unless otherwise noted. Averaged data are presented as the mean \pm standard deviation.

Results

Somatodendritic morphology influences AIS performance

We first tested the interaction of somatodendritic morphology and AIS length in regulating rheobase current thresholds in simplified ball-and-stick neurons having zero to eight dendrites and a variable-length (5-100 μ m) AIS attached to a myelinated or unmyelinated axon (Fig. 1; AIS Model A). For each morphological configuration, rheobase currents were determined to the nearest 100 fA using somatic current injections (40 ms duration). In some models, the AIS maintained constant maximal sodium (8000 pS/ μ m²) and potassium (2000 pS/ μ m²) conductance densities (Fig. 2A, left), while in other models maximum conductance densities were adjusted by AIS length, such that total conductances were length independent, and equivalent to those in a 30-µm-long AIS having sodium and potassium conductances set to 8000 and 2000 $pS/\mu m^2$, respectively (Fig. 2A, right). Given that high sodium channel densities in the AIS promote action potential initiation (Kole et al., 2008), we predicted that a longer AIS, with greater total sodium conductance, would be associated with a lower rheobase threshold. Surprisingly, this was not always the case. In smaller neurons (i.e., those with few or no dendrites), lowest rheobase current thresholds occurred when the AIS was of intermediate lengths (Fig. 2, left panels). "Optimal" AIS length (i.e., the length at which rheobase currents were minimal) was directly related to somatodendritic size: the larger the neuron, the longer the optimal AIS length. This was true in



Figure 2. Interaction of neuron size and AIS length in regulating action potential threshold. *A*, Diagrams (top) of ball-and-stick neurons having a variable-length AIS (AIS Model A) with uniform maximum sodium and potassium conductance densities (left), or with conserved (i.e., length-independent) total conductances (right). Voltage traces (below) show somatic (blue) and AIS (red) responses to somatic current injections in neurons with the indicated number of dendrites and AIS lengths of 20 (left), 40 (middle), or 60 μ m (right). *B*, Plots of normalized rheobase currents in neurons having the indicated numbers of dendrites and AIS lengths, with uniform conductance densities (left) or conserved total conductances (right). Inset, Plots of optimal (i.e., lowest rheobase current) AIS length vs the number of dendrites in model neurons having myelinated or unmyelinated axons, as indicated. Larger neurons had longer optimal AIS lengths. To facilitate comparisons across neurons, rheobase currents from the soma-only neuron having uniform AIS conductance densities were normalized to the rheobase occurring when the AIS was adjacent to the soma, as at very long AIS lengths, rheobase increased above this level in the soma-only model.

both myelinated and unmyelinated neurons (Fig. 2B, left inset).

Similarly, when total maximum sodium conductance in the AIS was preserved (i.e., was length independent), optimal AIS length was again dependent on somatodendritic size (Fig. 2, right panels). Rheobase currents were lowest in small- and medium-sized neurons when the AIS was short (5 μ m long), with correspondingly high maximal conductance densities (e.g., 48,000 and 12,000 pS/ μ m² for sodium and potassium conductances, respectively, for the 5 μ m AIS). In these neurons, rheobase currents increased as the AIS was lengthened and conductance densities diminished. However, in larger neurons (i.e., those having more than five dendrites), rheobase currents

continued to decrease as the AIS elongated with progressively lower sodium and potassium conductance densities (Fig. 2B, right inset). These results demonstrate that somatodendritic architecture independently influences AIS performance, with action potential generation in smaller neurons facilitated when the AIS is short and contains a high density of sodium channels, while excitability in larger neurons is promoted when the AIS is longer, even at the expense of high conductance densities.

We next asked how somatodendritic morphology and AIS location interact to regulate neuron excitability by pairing the same somatodendritic architectures with a $30-\mu$ m-long AIS (8000 and 2000 pS/ μ m² maximal sodium



Figure 3. Dendritic architecture influences the impact of AIS location on excitability. *A*, Diagrams (top) of the AIS of ball-and-stick models having a translocating AIS within the proximal axon (AIS Model B, left) or an AIS connected to the axon proper and positioned at variable distance from the soma (AIS Model C, right). Voltage traces show somatic (blue) and AIS (red) responses to somatic current injections in neurons in which the AIS was positioned 0 μ m from the soma (left), 35 μ m from the soma (middle), or 70 μ m from the soma (right). Data are from models with one or four dendrites (AIS Model B), or five or eight dendrites (AIS Model C), as indicated. Note that in both model configurations the addition of dendrites increased the rheobase current, but shifted the most excitable AIS locations for neurons with AIS Model B (left) or AIS Model C (right). Inset, Plots of optimal (i.e., lowest rheobase current) AIS locations vs the number of dendrites in models having myelinated or unmyelinated axons. In all cases, increasing the number of dendrites led to more distal optimal AIS locations.

and potassium conductance densities, respectively) that could be positioned anywhere from 0 to 70 μ m from the soma (Fig. 3). Regardless of whether the AIS was moved within a fixed 100 μ m stretch of proximal axon (Fig. 1; AIS Model B; see Materials and Methods) or was connected to the soma by a variable-length proximal axon (Fig. 1; AIS Model C), optimal AIS location (i.e., that having the lowest rheobase current) was again dependent on somatodendritic size (Fig. 3B). In small neurons, rheobase currents were lowest when the AIS was positioned adjacent to the soma. However, as neurons increased in size, optimal AIS position moved to progressively more distal locations. This effect was largest when the AIS was associated with myelinated axons having low membrane capacitance and conductance, but also occurred when neurons were associated with unmyelinated axons (Fig. 3B, insets).

Because excitability is critically dependent on the density and kinetics of sodium channels in the AIS, we compared the influence of somatodendritic morphologies on AIS performance in model neurons incorporating modified sodium conductances (Fig. 4). Modifications included doubling or halving the speed of activation and inactivation, lowering the voltage threshold for activation by 10 mV selectively in the AIS (as may result from selective sodium channel subunit expression in the AIS; Kole et al., 2008), implementation of an eight-state sodium channel model (Schmidt-Hieber and Bischofberger, 2010; Hallermann et al., 2012), or replacement of our standard active



Figure 4. AIS performance across a range of sodium conductance properties. **A**, Diagrams of the AIS of a one-dendrite myelinated neuron having a 50- or 65- μ m-long AIS beginning at the soma (**A**₁), and of a five-dendrite model with a 30- μ m-long AIS beginning either at the soma or 10 μ m away (**A**₂). **B**, Voltage responses at the soma (blue), AIS (red), or 10th node of Ranvier (~1 mm from the soma; yellow) in response to the indicated current steps in models having the indicated sodium conductance properties and AIS architectures. In most one-dendrite models, increasing AIS length from 50 to 65 μ m reduced neuron excitability (**B**₁), while in the five-dendrite model, moving the 30- μ m-long AIS 10 μ m away from the soma increased neuron excitability (**B**₂). **C**, Comparisons of "optimal" (i.e., lowest rheobase) AIS lengths (left) and locations (right) for myelinated (top) and unmyelinated (bottom) model neurons having the indicated number of dendrites and sodium conductance properties.

conductances with equivalent densities of the built-in Hodgkin and Huxley conductances in NEURON that simulate those in the squid giant axon (temperature in this implementation was set to 6.3°C). Modifications that slowed activation and inactivation tended to promote excitability in a longer or more distally located AIS, while increasing activation and inactivation rates favored a shorter or more proximally located AIS. Overall, the modified sodium conductances revealed gualitatively similar effects of somatodendritic morphology on AIS performance. The exception was for the NEURON Hodgkin and Huxley model, which when combined with the soma-only model neuron had "preferred" AIS lengths (i.e., lengths with lowest rheobase) beyond our normal test limit of 100 μ m (Fig. 4B,C). Across all sodium conductances tested, rheobase in neurons having two or more dendrites decreased as a 30 μ m AIS was moved distally from the soma (Fig. 4C). These data demonstrate that the impact of somatodendritic morphology on AIS performance is largely independent of the kinetics and voltage sensitivities of sodium channels.

We next varied the densities of sodium and potassium conductances in the AIS (normally 8000 and 2000 pS/ μ m², respectively) to generate a range of AIS-to-soma sodium conductance ratios (Fig. 5). Across a span from our normal ratio of 80:1 to the lowest tested ratio of 5:1, somatodendritic morphologies continued to influence AIS performance, albeit to lesser extents as AIS-to-soma sodium conductance ratios became small (Fig. 5*B*,*C*). Overall, larger AIS conductance densities led to lowest rheobase currents occurring with shorter AIS lengths or more distal AIS locations.

To test the interaction of AIS length and location in setting rheobase currents, we made hybrid models having a variable-length (5–70 μ m long) AIS attached to a variable-length (0–95 μ m long) soma-like proximal axon (AIS Model D). Regardless of whether the AIS contained uniform maximal conductance densities (Fig. 6, left) or conserved total conductances (Fig. 6, right), minimal rheobase currents in small neurons occurred when the AIS was positioned adjacent to the soma. On the other hand, larger neurons exhibited enhanced excitability when the AIS was located distally from the soma, and this distance-dependent enhancement of excitability was magnified when the AIS was short in length (Fig. 6B). The interaction of AIS length and location on rheobase currents can be visualized in rotating 3-D graphs showing data for neurons having zero, four, or eight dendrites, with the AIS having conserved active conductance densities (Movie 1) or conserved total active conductance magnitudes (Movie 2).

To quantify the impact of AIS plasticity on neuron excitability, we measured the average change in rheobase current generated by small (5, 10, or 15 μ m) changes in AIS length (from a baseline length of 30 μ m, while maintaining uniform conductance densities), or position (using a 30- μ m-long AIS), across all possible AIS locations within 100 μ m of the soma. Except for the soma-only model (see Fig. 2*B*), lengthening or shortening the AIS increased or decreased, respectively, neuron excitability.

However, the magnitude of this change in excitability was dependent on somatodendritic morphology (Fig. 7A). In the soma-only model, increases or decreases in AIS length by up to 50% (i.e., adding or subtracting 15 μ m to or from the 30 μ m AIS) resulted in small (<5%) changes in excitability. In larger neurons, increasing AIS length led to ever-lower rheobase currents, with a maximal reduction of 7.5 ± 0.6% (n = 12 possible AIS locations allowing for lengthening of 15 μ m confined within 100 μ m of the soma) following 50% elongations (i.e., to 45 μ m) in the eight-dendrite model (Fig. 7A). Conversely, decreasing AIS length by 50% (i.e., to a length of 15 μ m) increased rheobase currents by up to 15.0 ± 0.4% (n = 15) in the eight-dendrite model (Fig. 7A).

Changes in AIS location were far less effective in regulating neuron excitability. Across all somatodendritic morphologies, translocations of the 30- μ m AIS by up to ±15 μ m produced only small changes in rheobase currents (Fig. 7*B*), with the magnitude and direction of those changes being dependent on neuron size (Fig. 3*B*). Mean changes in rheobase currents (absolute values) generated by translocations of 15 μ m across all possible AIS locations within 100 μ m of the soma ranged from a high of 4.1 ± 0.2% (n = 12 possible 15- μ m shifts) in the somaonly model, to a low of 0.3 ± 0.3% (n = 12) in the five-dendrite model neuron (Fig. 7*B*). These results suggest that AIS translocations of up to 15 μ m will have only limited impact on neuron excitability across a range of neuron morphologies.

AIS performance in realistic neuron morphologies

We next tested the impact of AIS length and location on rheobase currents in five reconstructed neuron morphologies (Fig. 8A). Neurons ranged from a small dentate granule neuron (total somatodendritic membrane area, $6115 \ \mu m^2$) to a large CA3 pyramidal neuron (total somatodendritic membrane area, $30,653 \ \mu m^2$). AIS segments were attached to myelinated (Purkinje and L5 neurons) or unmyelinated (dentate granule, medium spiny, and CA3 neurons) axons, as appropriate for their cell types, and rheobase currents determined to the nearest 100 fA using somatic current injections (40 ms).

When morphologically realistic model neurons were paired with a variable-length AIS having uniform maximal sodium and potassium conductances (AIS Model A), the smaller dentate granule and medium spiny neurons exhibited minimal rheobase currents when the AIS was of intermediate length (60 and 65 μ m, respectively), while larger neurons had the lowest rheobase currents when AIS length reached its maximum tested extent (100 μ m; Fig. 8*B*, top left). When dendritic spines were simulated by doubling dendritic membrane capacitance and passive conductance (see Materials and Methods; Holmes, 1989), optimal AIS lengths in the dentate granule and medium spiny neurons increased to 85 and 100 μ m, respectively (Fig. 8*B*, bottom left).

Similarly, when a 30- μ m-long AIS was positioned at variable distances (0-70 μ m) from the soma (AIS Model C), rheobase currents in smaller neurons were minimal when the AIS was adjacent to the soma, while larger



Figure 5. AlS performance across a range of AlS sodium conductance densities. *A*, Top, Diagram of a model neuron having a $30-\mu$ m-long AlS positioned 10 μ m from the soma. Bottom, Voltage responses measured at the soma (blue), in the AlS (red), or in the 10th node of Ranvier (~1 mm from the soma; yellow) in response to the indicated rheobase current steps in models having the indicated number of dendrites and AlS-to-soma sodium conductance density ratios. *B*, Comparisons of optimal (i.e., lowest rheobase) AlS lengths (left) and locations (right) for myelinated (top) and unmyelinated (bottom) model neurons having the indicated number of dendrites and AlS-to-soma sodium conductance densities.

neurons were most excitable when the AIS was moved to distal locations (Fig. 8A, traces, *B*, top right panel). Simulation of dendritic spines further favored distal AIS locations, with rheobase in the medium spiny neuron becoming lowest when the AIS was positioned 30 μ m from the soma (Fig. 8*B*, bottom right).

We quantified the impact of changes in AIS length and location on the excitability of these morphologically realistic neurons by measuring the mean changes in rheobase current generated by small (5-15 μ m) changes in AIS length or location (relative to a baseline 30- μ m-long AIS) across all possible AIS locations up to 100 μ m from the



Figure 6. Interaction of AIS length and location in setting neuron excitability. *A*, Diagrams (top) of the proximal axons of ball-and-stick neurons having variable-length AISs located at different distances from the soma (AIS Model D). The AISs had either uniform sodium and potassium conductance densities (i.e., sodium and potassium conductances increased with length; left) or conserved total sodium and potassium conductances (i.e., length-independent conductances; right). Voltage traces show somatic (blue) and AIS (red) responses to somatic current injections in model neurons having the indicated AIS lengths and locations. Note that in the 40- μ m-long AIS model with conserved total conductances, rheobase (to the nearest 100 fA) was identical in models having the AIS beginning at 0 or 25 μ m from the soma (minimal rheobase in this model occurred when the AIS was 10 μ m from the soma). *B*, Plots of optimal (i.e., lowest rheobase current) AIS position for each AIS length in models having "uniform conductance densities" (left) or "conserved total conductances" (right) in the AIS.

soma (Fig. 9). In all neuron morphologies, lengthening or shortening the AIS decreased or increased, respectively, rheobase currents (Fig. 9A). Lengthening the AIS by 50% (i.e., by 15 μm) lowered rheobase currents by a minimum of 5.2 \pm 0.3% (in the dentate granule neuron) to a maxi-

mum of 10.2 \pm 1.7% (in the CA3 pyramidal neuron; *n* = 12 possible AIS locations for each neuron), while shortening the AIS by 50% (i.e., by 15 μ m) increased rheobase currents by 14.3 \pm 1.0% (dentate granule cell) to 21.3 \pm 2.0% (Purkinje neuron; Fig. 9*A*). To further demonstrate



Movie 1. Interaction of AIS length and location in setting neuron excitability in model neurons having conserved conductance densities in the AIS. Shown is a rotating 3-D plot of normalized rheobase currents for each AIS length and location combination for the soma-only model neuron (blue), and neurons with four (green) or eight (red) dendrites in models where the AIS has conserved conductance densities (i.e., total available sodium and potassium conductances increase with AIS length).



Movie 2. Interaction of AIS length and location in setting neuron excitability in model neurons having conserved total AIS conductances. Shown is a rotating 3-D plot of normalized rheobase currents for each AIS length and location combination for the soma-only model neuron (blue), and neurons with four (green) or eight (red) dendrites in models having conserved (i.e., length-independent) maximal sodium and potassium conductances in the AIS.

the interaction of somatodendritic morphology and AIS length in regulating neuron excitability, we compared action potential generation in response to suprathreshold current injections in two versions of the dentate granule neuron (Movie 3) and L5 pyramidal neuron (Movie 4) that differed only in their AIS lengths. As illustrated in the movies, action potential initiation in the dentate granule neuron occurred first when the AIS was shorter, while spike initiation in the L5 neuron occurred earlier when the AIS was longer.

We next quantified the impact of changes in AIS location on action potential threshold in morphologically realistic neurons. AIS translocations of up to ± 15 μ m produced only small (<5%; absolute values) changes in rheobase currents across all somatodendritic morphologies (Fig. 9B), with the magnitude of those changes being dependent on neuron size, and the direction of change depending on both neuron size and starting AIS position. Overall, mean changes in rheobase currents (absolute values) generated by 15- μ m shifts at all possible AIS locations within 100 μ m from the soma were small, ranging from a low of 0.4 \pm 0.3% (n = 12 possible 15- μ m shifts) in the medium spiny neuron to a high of 3.8 \pm 2.1% (n = 12) in the CA3 model neuron (Fig. 9B). To visualize the interaction of somatodendritic morphology and AIS location in regulating neuron excitability, we again compared action potential initiation in the dentate granule neuron (Movie 5) and the L5 pyramidal neuron (Movie 6) in response to suprathreshold somatic current current injections in models where the AIS was positioned adjacent to the soma or 15 μ m away. In the smaller dentate granule neuron, action potential initiation occurred earlier when the AIS was adjacent to the soma, while spike initiation occurred first in the L5 neuron when the AIS was moved away from the soma. Together, these data from morphologically realistic neurons reveal a profound influence of somatodendritic morphology on the outcome of plastic change in the AIS, and further demonstrate that changes in AIS length will be far more effective at regulating neuron excitability than will similar changes in AIS location.

Why do manipulations of AIS length or location in morphologically realistic neurons impact excitability in ways not predictable based purely on neuron size? For instance, the largest effects of AIS shortening were observed in the mid-sized Purkinje neuron (Fig. 9A). This likely results from several features of our realistic neuron morphologies. First, the Purkinje neuron and the layer 5 neuron were paired with myelinated axons, which enhanced the impact of neuron size on AIS performance in our ball-and-stick models. Second, the realistic morphologies were relatively large; the "small" dentate granule (6115 μ m²) and medium spiny (6622 μ m²) neurons were of sizes intermediate to the threedendrite (5498 μ m²) and four-dendrite (6912 μ m²) balland-stick model neurons, while all other realistic morphologies were larger than our eight-dendrite balland-stick neuron (12,566 μ m²). There may be a ceiling effect limiting additional impact of very large surface



Figure 7. Impact of AIS plasticity on neuron excitability. *A*, Plots of mean changes in rheobase currents (percentage \pm SD) observed after elongating or shortening a 30-µm-long AIS by 5, 10, or 15 µm across all possible AIS locations (within 100 µm of the soma) in model neurons having the indicated number of dendrites (AIS Model D; myelinated axon). Uniform sodium and potassium conductance densities were maintained across all AIS lengths (i.e., increasing AIS length proportionally increased total maximum sodium and potassium conductances). *B*, Plots of the mean absolute values of changes in rheobase (percentage \pm SD) observed after translocating a 30-µm-long AIS by 5, 10, or 15 µm across all possible AIS positions within 100 µm of the soma (e.g., 14 possible 5 µm shifts of the 30 µm AIS) in neurons having the indicated number of dendrites (AIS Model C). To facilitate comparisons, data are shown at the same scale as in *A*, with a close-up of the data inset.

areas on optimal AIS length (Fig. 2*B*). Finally, morphologically realistic neurons have unique and complicated dendritic branching patterns that distribute surface area unevenly with respect to the soma (e.g., much of the dendritic tree in the L5 pyramidal neuron is in the distal tuft, remote from the soma and AIS). Differences in dendritic proximity to the axon will likely influence AIS performance (van Ooyen et al., 2002; van Elburg and van Ooyen, 2010).

To test the impact of somatodendritic topology on AIS performance, we built a series of ball-and-stick models (AIS Model C) with zero to eight passive dendrites that conserved total somatodendritic surface area (12,566 μ m²; Fig. 10A) and compared the impact of changes in AIS length (Fig. 10B) or location (Fig. 10C) on rheobase currents. Under these conditions, where dendritic topology alone was manipulated, models in which dendrites were more numerous but shorter in length (i.e,. models in which dendritic surface area was closer to the soma) favored longer AIS lengths and more distal AIS locations, and this effect was maximal when dendrites were eliminated altogether and the soma enlarged to match the total somatodendritic surface area of the other models. The impact of dendritic topology on optimal AIS length and location was gualitatively similar in models with myelinated and unmyelinated axons (Fig. 10B,C, insets) and had an overall larger influence on optimal AIS location than on optimal AIS length (Fig. 10B,C). These data demonstrate that the impact of AIS plasticity on neuronal excitability will depend not only on overall somatodendritic size, but also on dendritic topology.

Dendritic membrane properties influence optimal AIS location

The results described above demonstrate that somatodendritic morphology will impact AIS plasticity, especially with regard to changes in AIS location. Given that neuron size primarily influences somatodendritic capacitance and conductance, we hypothesized that changes to these dendritic membrane properties should be sufficient to regulate optimal AIS architecture, even in the absence of structural changes to neuron morphology. To test this, we varied dendritic capacitance (by scaling dendritic C_M) and/or conductance (by scaling dendritic R_M) in a fourdendrite ball-and-stick model neuron and measured rheobase currents across a range of AIS architectures (Fig. 11). Overall, increases in dendritic conductance (i.e., decreases in dendritic R_M) or capacitance favored longer optimal AIS lengths (Fig. 11B,C), although changes to dendritic C_M had a larger impact on AIS performance than did changes in dendritic R_M (Fig. 11C).

We next tested the impact of manipulations of dendritic R_M and C_M on excitability in a four-dendrite neuron having a 30- μ m-long AIS connected to a myelinated axon and positioned at variable distances from the soma (AIS Model C; Fig. 12A). In baseline conditions (i.e., dendritic C_M and R_M set to 1 μ F/ μ m² and 15,000 $\Omega \cdot cm^2$, respectively), minimal rheobase currents occurred when the AIS was positioned 10 μ m from the soma. Increasing dendritic C_M , or decreasing dendritic R_M (i.e., increasing dendritic membrane conductance), shifted optimal AIS locations away from the soma (Fig. 12*B*,*C*). On the other hand, decreasing dendritic C_M , or increasing dendritic R_M , favored more proximal AIS locations. Changes to den-



Figure 8. AIS performance in morphologically realistic neurons. *A*, Morphologies of reconstructed neurons. For illustrative purposes, each morphology includes a $40-\mu$ m-long proximal axon (green), a $30-\mu$ m-long AIS (red), and a myelinated (in the Purkinje and L5 neurons) or unmyelinated (in the medium spiny, dentate granule, and CA3 pyramidal neurons) axon (yellow arrow). For each morphology, somatic and AIS voltage traces in response to the indicated somatic current injections are shown for models having a 30 μ m AIS located adjacent to the soma or 10 μ m away. Note that excitability in the smaller neurons is promoted by proximal AIS placement, but that the larger neurons favor a more distal AIS. *B*, Left panels, Plots of normalized rheobase current vs AIS length (AIS Model A; uniform sodium and potassium conductance densities) for reconstructed neurons having smooth dendrites (top) or

continued

simulated synaptic spines (bottom; see Materials and Methods). Smaller neurons exhibited minimal rheobase currents at intermediate AIS lengths, while the simulation of dendritic spines favored an elongated AIS. Right panels, Plots of normalized rheobase current vs location of a $30-\mu$ m-long AIS (AIS Model C) in reconstructed neurons having smooth (top) or simulated spiny (bottom) dendrites. Smaller neurons favored a proximal AIS, while simulating spiny dendrites shifted optimal AIS locations away from the soma.

dritic C_M had a larger impact on optimal AIS location, as doubling both dendritic C_M and R_M continued to favor more distal AIS locations (to almost the same extent as doubling dendritic C_M alone), while halving both values had minimal impact on preferred AIS location (Fig. 12*C*, bottom left traces). Reciprocal changes in dendritic R_M and C_M were most effective in moving optimal AIS locations (Fig. 12*C*, bottom right traces). Qualitatively similar effects of dendritic R_M and C_M on excitability were observed in model neurons incorporating the modified sodium conductances used in Fig. 4 (not shown), suggesting that dendritic membrane properties have a generalized impact on AIS performance.

Action potential initiation in the AIS

Action potential initiation has been observed to occur first in the distal AIS (Palmer and Stuart, 2006; Palmer et al., 2010), likely due to its relative isolation from somatodendritic capacitive loads (Baranauskas et al., 2013). To determine the extent to which somatodendritic architecture influences the timing and location of action potential initiation, we compared the location and latency of rheobase-induced action potentials in simulations run at 100 ns time steps (Fig. 13). Myelinated and unmyelinated model neurons included variable numbers of dendrites and AIS locations (AIS Model C). For comparison, we also tested an unmyelinated model neuron lacking an AIS altogether (AIS Model E). Latency to action potential initiation was influenced primarily by neuron size, with larger neurons firing rheobase action potentials earlier than smaller neurons, and by AIS location, where shorter-latency action potentials were promoted at distal AIS positions (Fig. 13*B*). When an AIS was present, action potential initiation always occurred at the distal end of the AIS, with the precise location of initiation being dependent on AIS distance from the soma, but not on somatodendritic size (Fig. 13*C*). Conversely, action potential generation in a neuron lacking an AIS occurred at very distal locations (>200 μ m from the soma; Fig. 13*B*).

In the simulations above, in which rheobase was determined to the nearest 100 fA, we observed jitter in action potential location and timing due to rounding errors (i.e., the degree to which rheobase determined to the nearest 100 fA exceeded action potential threshold for any given morphology), especially in models lacking an AIS. To explore action potential initiation at more precise values for rheobase, we determined rheobase at ever more accurate levels, from the nearest 1 pA to to the nearest 1 zeptoampere (zA; 10^{-21} A; Fig. 14). Increasing the precision of rheobase currents increased spike latency in all models and, in models lacking an AIS, moved action potential initiation to ever more distal axonal locations, up to many hundreds of micrometers from the soma (Fig. 14*B*), sites that in many neurons would be well beyond



Figure 9. Impact of AIS plasticity on the excitability of morphologically realistic neurons. **A**, Plots of the mean changes in rheobase currents (percentage \pm SD) observed after elongating or shortening the AIS by 5, 10, or 15 μ m (relative to a 30- μ m-long baseline AIS), across all possible AIS locations within 100 μ m of the soma, in reconstructed neuron morphologies having simulated dendritic spines (see Materials and Methods) and uniform sodium and potassium conductance densities in the AIS (AIS Model D). **B**, Plots of the mean absolute values of changes in rheobase (percentage \pm SD) observed after translocating the AIS by 5, 10, or 15 μ m across all possible AIS positions within 100 μ m of the soma. Note the different *y*-axis scales in **A** and **B**.





Movie 3. Impact of AIS length on action potential initiation in a dentate granule neuron. Shown are two superimposed plots of membrane voltage (in millivolts) vs compartment distance (in micrometers) from the soma, spanning the axon (positive distances from the soma) to the longest dendrite (negative distances from the soma), for two versions of the dentate granule neuron having either a $60-\mu$ m-long (red) or an $80-\mu$ m-long (green) AIS beginning adjacent to the soma. Current (100 pA) was injected into the soma of each model beginning at time = 2 ms. Note that the timescale slows down to show initiation in high temporal resolution, which occurs first in the DGC with the shorter AIS.

Movie 5. Impact of AIS location on action potential initiation in a dentate granule neuron. Shown are two superimposed plots of membrane voltage (in millivolts) vs compartment distance (in micrometers) from the soma, spanning the axon (positive distances from the soma) to the longest dendrite (negative distances from the soma) for two versions of the dentate granule neuron associated with a 30- μ m-long AIS positioned either adjacent to these soma (red) or 15 μ m from the soma (green). Current (120 pA) was injected into the soma of each model at time = 2 ms. Note that the timescale slows down to show initiation in high temporal resolution, which occurs first when the AIS is adjacent to the soma.



Movie 4. Impact of AIS length on action potential initiation in a layer 5 pyramidal neuron. Shown are two superimposed plots of membrane voltage (in millivolts) vs compartment distance (in micrometers) from the soma, spanning the axon (positive distances from the soma) to the longest dendrite (negative distances from the soma) for two versions of the L5 pyramidal neuron that have either a $60-\mu$ m-long (red) or an $80-\mu$ m-long (green) AIS beginning adjacent to the soma. Current (757 pA) was injected into the soma of each model beginning at time = 2 ms. Note that the timescale slows down to show initiation in high temporal resolution, which occurs first in the L5 neuron with the longer AIS.



Movie 6. Impact of AIS location on action potential initiation in a layer 5 pyramidal neuron. Shown are two superimposed plots of membrane voltage (in millivolts) vs compartment distance (in micrometers) from the soma, spanning the axon (positive distances from the soma) to the longest dendrite (negative distances from the soma) for two versions of the L5 pyramidal neuron associated with a 30- μ m-long AIS positioned either adjacent to these soma (red) or 15 μ m from the soma (green). Current (757 pA) was injected into the soma of each model at time = 2 ms. Note that the timescale slows down to show initiation in high temporal resolution, which occurs first when the AIS is distal from the soma.



Figure 10. Impact of dendritic topology on AIS performance. *A*, Diagrams of ball-and-stick model neurons (AIS Model C) having zero, one, or eight nontapering (2.5 μ m diameter) passive dendrites that conserve a total somatodendritic surface area of 12,566 μ m² in each model. In the soma-only model, the densities of active somatic conductances were reduced in the enlarged soma to conserve the same total conductances present in the baseline soma. *B*, Plots of normalized rheobase currents for different AIS lengths (AIS Model A; conserved sodium and potassium conductance densities) in model neurons having variable somatodendritic topology, but conserved total surface areas. Top inset, Plots of optimal AIS length vs the number of dendrites in models having preserved total somatodendritic surface area. Bottom inset, An expanded view of the indicated data points. *C*, Plots of normalized rheobase currents for the same model neurons having a 30- μ m-long AIS placed at the indicated distances from the soma (AIS Model C). Inset, Plots of optimal AIS distance from the soma vs the number of dendrites in models having preserved total surface area.

proximally located synaptic boutons. These data suggest that one advantage of having an AIS may be greater precision in action potential initiation timing and location. Nevertheless, increasing rheobase precision did not qualitatively change the impact of somatodendritic morphology on AIS plasticity in myelinated or unmyelinated neurons (Fig. 14*C*), suggesting that the impact of AIS plasticity is independent of the timing of action potential initiation relative to current onset.

Somatodendritic morphology shapes electrical properties of the AIS

Why are larger neurons more excitable when the AIS is moved to distal locations? To address this larger question, we tested AIS electrical characteristics in model neurons in which a 30- μ m-long AIS was connected to a myelinated axon and positioned at variable distances from the soma (AIS Model C). Since distance-dependent attenuation of somatic depolarization is proposed to limit excitation when the AIS is located distally from the soma (Adachi et al., 2014), we compared voltage attenuation of somatic signals at the middle of the AIS across all models. In response to a -1 pA current injection at the soma (100 ms), distance-dependent voltage attenuation to the AIS was small, with mean attenuation in the middle of an AIS positioned at the maximally tested distance of 70 μ m from the soma being only 4.32 \pm 0.03% (n = 9 somatodendritic morphologies), and independent of neuron size (Fig. 15*A*). This result is in good agreement with experimental data from Kole et al. (2007), who found only modest soma-to-AIS voltage attenuation (<10%) within the first 150 μ m of the axon.

Although modest, distance-dependent voltage attenuation would, on its own, favor lower rheobase currents at proximal AIS locations. However, distal locations also isolate the AIS from somatodendritic capacitive loads (Kuba, 2012). We quantified distance-dependent isolation from somatodendritic capacitance by calculating a C_M isolation index for each AIS location (see Materials and Methods; Fig. 15*B*). The C_M isolation index increased with distance in all morphologies, but exhibited a steeper relationship with distance in larger neurons, from a 17% reduction in the influence of somatodendritic capacitance in the soma-only model when the AIS was positioned 70 μ m from the soma, to a 44% reduction in a similar model having eight dendrites. This distance-dependent isolation from somatodendritic capacitance will tend to facilitate



Figure 11. Impact of dendritic membrane properties on optimal AIS length. *A*, Diagram of a neuron with four dendrites having variable dendritic membrane properties and a variable-length AIS attached to a myelinated axon (AIS Model A). *B*, Voltage responses in the AIS following somatic current injections under baseline conditions (far left) and after manipulations of dendritic R_M and/or C_M , as indicated. Responses from three model neurons having AIS lengths of 75 (blue), 85 (green), and 95 (red) μ m are superimposed. *C*, Plots of normalized rheobase current vs AIS length for the four dendrite model having modified dendritic R_M (top left; inset shows close-up of indicated area), dendritic C_M (top right), parallel changes in both dendritic R_M and C_M (bottom left), or reciprocal changes in dendritic R_M and C_M (bottom right). Dendritic properties (bottom right), the C_M/R_M ratios represent reciprocal changes to C_M and R_M around the baseline (C_M/R_M ratio = 1) values (e.g., a ratio of 0.25 indicates that dendritic C_M was multiplied by 0.5 and dendritic R_M was multiplied by 2.0). Increasing dendritic C_M favored a longer AIS, regardless of whether there were also co-occurring changes in dendritic conductance (i.e., changes in dendritic R_M). Shaded bars indicate the AIS lengths for which traces are shown in *B*.



Figure 12. Dendritic membrane properties influence optimal AIS location relative to the soma. *A*, Diagram of a neuron with four dendrites having variable dendritic membrane properties and a 30 μ m AIS positioned at variable distances from the soma (AIS Model C; myelinated axon). *B*, Voltage responses in the AIS during somatic current injections under baseline conditions (far left) and after manipulations of dendritic R_M and/or C_M, as indicated. Responses from three models are superimposed: those having the AIS beginning 0 (blue), 20 (green), or 50 μ m (red) from the soma. *C*, Plots of normalized rheobase current vs AIS location for the four-dendrite models having modified dendritic R_M (top left), dendritic C_M (top right), parallel changes in both dendritic R_M and C_M (bottom left), or reciprocal changes in dendritic properties (bottom right). Dendritic C_M and/or R_M were multiplied by the indicated modification factors. C_M/R_M ratios in reciprocal manipulations of R_M and C_M are centered around baseline (C_M/R_M ratio = 1) values. Increasing dendritic C_M and/or dendritic conductance (lower dendritic R_M) enhanced excitability at more distal AIS locations. Shaded bars indicate the AIS locations for which traces are shown in *B*.



Figure 13. Dendritic architecture influences action potential initiation. *A*, Left, Diagram of a model neuron having zero to eight dendrites, a 30 μ m AIS located 20 μ m from the soma, and a myelinated axon. Pipettes indicate the location of recording electrodes at the soma (where rheobase current is injected), toward the end of the AIS (where action potential initiation occurred) and at the first node of Ranvier. Right, Traces of the action potential generated by rheobase somatic current injection, as recorded at the indicated locations in the model cell. These simulations were run with 100 ns time steps to pinpoint action potential initiation to the nearest 1 μ m. *B*, Plot of spike latency vs location of spike initiation for myelinated and unmyelinated neurons with different numbers of dendrites (as indicated by color) and variable AIS locations (AIS Model C), and for neurons having uniform unmyelinated axons lacking an AIS (AIS Model E). The AIS constrained the location of action potential initiation, but increased the influence of dendrite number on spike latency. *C*, Plot of the location of action potential initiation within the AIS for myelinated and unmyelinated neurons vs the distance of the AIS from the soma. When the AIS was placed at distal locations, action potential initiation occurred in slightly more proximal AIS compartments, an effect that was more pronounced in neurons with unmyelinated axons.

action potential generation at more distal AIS locations, especially in larger neurons.

Action potential initiation is directly influenced by the magnitude and speed of local membrane depolarization in the AIS (Baranauskas et al., 2013; Eyal et al., 2014), and therefore the local input resistance (R_N) and effective membrane time constant (τ_{M}) of the AIS will influence rheobase currents. We therefore measured R_N (Fig. 15C) and $\tau_{\rm M}$ (Fig. 15D) at the middle of the AIS in response to local current injections (-1 pA) delivered at resting membrane potentials. In small neurons (those with fewer than two dendrites), local R_N in the AIS decreased with distance from the soma (by 10.7% in the soma-only model), while in larger neurons local R_N increased with distance, exhibiting up to a 27.4% increase over 70 μ m in the eight-dendrite model neuron. On the other hand, the effective local $\tau_{\rm M}$, calculated empirically by measuring the latency at which the local voltage response reached 63.2% of its steady-state value (Fig. 15D), increased negligibly with AIS distance in the soma-only model (by 0.5%

over 70 μ m), but decreased with distance in larger neurons, by as much as 33.2% over 70 μ m in the eightdendrite model neuron (Fig. 15D). The impact of these physiological properties on AIS performance is summarized in Fig. 15E. When remeasured after moving the reversal potential of leak conductances closer to the action potential threshold (from -70 to -55 mV), maximum soma-to-AIS voltage attenuation remained at <5% for all models, and the impact of somatodendritic architecture on local R_N , effective τ_M , and isolation from somatodendritic capacitance was qualitatively similar to that measured at -70 mV (data not shown). Thus, while modest soma-to-AIS voltage attenuation will tend to decrease excitability in all neurons, local properties promoting action potential generation (higher R_N , faster effective τ_M , and more effective isolation from somatodendritic capacitance) are more pronounced at distal AIS locations in larger neurons and, therefore, allow rheobase currents to decrease, rather than increase, as the AIS is lengthened or translocated away from the soma.



Figure 14. Impact of rheobase precision on action potential initiation and AIS plasticity. **A**, Plots of action potential waveforms recorded in the AIS (red; 30 μ m long and 30 μ m from the soma) or in the soma (blue) of neurons with four dendrites and either an AIS associated with a myelinated axon (left), an unmyelinated (middle) axon (AIS Model C), or an unmyelinated axon lacking an AIS (AIS Model E; right). Shown are traces in which rheobase current was calculated to the nearest pA or to the nearest zA, as indicated (simulations used 100 ns time-steps). **B**, Plots of spike latency vs the location of spike initiation in myelinated and unmyelinated neurons having an AIS (Model C), or in a neuron lacking an AIS (Model E), for rheobase current injections at the indicated precision levels (i.e., rounded up to the nearest suprathreshold stated unit). Note that approaching ever more precise rheobase currents increased the latency to spike initiation and, in the absence of an AIS, moved the location of initiation to very distal regions of the axon. **C**, Plots of AIS lengths (left) or locations (right) having the lowest rheobase currents, as determined to the nearest 100 fA (open symbols) or 1 zA (closed symbols) in myelinated and unmyelinated neurons.

Discussion

The AIS represents the final locus of synaptic integration and, therefore, is an ideal target for regulating action potential initiation. Indeed, the AIS is often a site of inhibitory synaptic input, and is enriched with a diverse range of voltage- and ligand-gated ion channels that can



Figure 15. Mechanisms controlling the impact AIS plasticity. *A*, Steady-state voltage attenuation, measured in the middle of a $30-\mu$ m-long AIS positioned at the indicated distances from the soma (AIS Model C) in response to a somatic current injection (-1 pA) delivered at the resting membrane potential. Data are from model neurons having zero (black symbols) to eight (red symbols) dendrites. *B*, C_M-isolation index (see Methods) vs AIS distance from the soma for neurons having zero to eight dendrites. *C*, Normalized local steady-state input resistance (R_N) vs AIS location. *D*, Local effective membrane time constant (τ_{M}) in the AIS vs distance from the soma. *E*, Summary diagrams of location-dependent changes in the biophysical properties of the AIS in neurons of different sizes. Arrows indicated the direction of change in the indicated biophysical property as the AIS moves distally away from the soma. Arrow colors indicate whether such changes will limit (blue) or enhance (red) neuron excitability.

promote or suppress action potential generation (for review, see Kole and Stuart, 2012). Several recent studies have described a novel intrinsic mechanism for homeostatic regulation of neuronal excitability: dynamic structural remodeling of the AIS in response to altered excitatory drive (Grubb and Burrone, 2010; Kuba et al., 2010; Muir and Kittler, 2014; Chand et al., 2015). These structural modifications, which include changes to AIS length and/or location, are hypothesized to stabilize the mean level of output of a neuron following chronic changes in synaptic drive (Grubb et al., 2011). Our simulations tested the impact of AIS architecture on intrinsic neuronal excitability across a wide range of somatodendritic morphologies. Our results demonstrate that somatodendritic morphology will have a profound impact on AIS performance and plasticity.

Impact of somatodendritic morphology on AIS plasticity

Using a wide range of neuron morphologies and sodium conductance properties, we found that smaller neurons tended to be most excitable when the AIS was of intermediate length and located adjacent to the soma, while excitability in larger neurons was enhanced when the AIS was longer and more distally located. Modifications of AIS length were far more effective in regulating neuron excitability, and less dependent on somatodendritic morphology, than were changes in AIS location. While AIS elongations of 15 μ m were capable of increasing neuron excitability by up to \sim 20%, AIS translocations of 15 μ m had only modest impact on excitability ($\leq 4\%$ change), with the direction of change being dependent on somatodendritic morphology and AIS starting position within the axon. Further, because distal translocations of the AIS can limit action potential propagation into somata and dendrites (Fig. 3A), such plasticity may prove maladaptive to neurons that depend upon backpropagating action potentials for normal synaptic integration or plasticity (Bi and Poo, 1998; Larkum et al., 1999). Overall, the impact of neuron size on AIS performance was similar in both myelinated and unmyelinated neurons, with unmyelinated neurons of a given size acting like somewhat smaller myelinated neurons in their response to changes in AIS length or location. This difference likely reflects the greater asymmetry of capacitive and conductance loads between somatodendritic domains and axons in myelinated neurons.

Mechanisms of somatodendritic impact on AIS plasticity

How does somatodendritic size impact AIS performance? Action potential initiation depends on the speed and magnitude of depolarization in the AIS. Under physiological conditions, depolarization of the AIS starts with passive spread of excitatory synaptic potentials arriving from the soma, and ends with rapid recruitment of local voltage gated sodium conductances in the AIS. Because voltage attenuation of somatic signals in the thin (~1.5 μ m diameter) AIS is small (~4% at 85 μ m from the soma; see also Kole et al., 2007) and not dependent on neuron size, there is only modest distance-dependent reduction of excit-

atory drive as the AIS is moved distally from the soma. On the other hand, intrinsic AIS properties that determine the magnitude and rise time of local depolarization from sodium currents are both location and neuron size dependent. Local R_N, which determines the magnitude of local depolarization, was negatively correlated with AIS distance in small neurons, but increased, and with a progressively steeper relationship, with distance from the soma as neurons increased in size. Similarly, in all but the soma-only model, the effective local $\tau_{\rm M}$ in the AIS became faster with distance from the soma, again with progressively steeper dependencies on distance as neurons increased in size. Combined with the reduced impact of somatodendritic capacitance at distal AIS locations (which contributes to the faster effective τ_{M}), these intrinsic AIS properties facilitate action potential initiation at distal AIS locations in larger neurons (Fig. 15). Thus, while small neurons gain little, if any, enhancement to excitability from distance-dependent changes in local R_N or τ_M , in larger neurons these AIS properties can more than balance the modest voltage attenuation of somatic depolarizing drive.

Consistent with the impact of neuron size on AIS performance, increasing dendritic capacitance and/or conductance alone mimicked enlarging the dendritic tree. However, changes in dendritic C_M were more effective at shifting optimal AIS length and location than were changes of similar magnitude to dendritic R_M. This likely results because changes in dendritic R_M , but not C_M , influence the electrotonic length constant (λ) of dendrites. For instance, in addition to increasing dendritic conductance (shifting optimal AIS locations distally), lowering dendritic R_M decreases dendritic λ , thereby reducing the influence of more distal dendritic capacitance on the AIS. Conversely, increasing dendritic R_M, which shifts optimal AIS locations toward the soma, also increases dendritic λ values and, therefore, enhances the impact of distal dendritic capacitance on AIS performance. Thus, changes in dendritic membrane conductance may to some extent be self-limiting, stabilizing AIS performance in the face of the rapid changes in dendritic membrane conductance typical of neurons in vivo (Destexhe et al., 2003). Since dendritic capacitance is expected to be uniform in the absence of structural changes to the dendritic tree, it is likely that plastic changes to AIS architecture are better suited for adapting to structural changes in dendritic morphology, or chronic changes in afferent synaptic drive, than for adapting to changes in membrane conductance.

The functional role of AIS plasticity

Throughout this article, we have arbitrarily referred to those AIS lengths and locations having minimal rheobase currents as being "optimal," "favored," or "preferred." However, there is no evidence that neurons strive to maximize their intrinsic excitability. On the contrary, neurons use numerous intrinsic and extrinsic mechanisms to effectively dampen excitability. More practically, there is little evidence that AIS architectures *in vivo* maximize excitability. For instance, in the developing visual cortex, the AISs of smaller L2/3 neurons tend to be longer than

those of larger L5 neurons (Gutzmann et al., 2014), while both pyramidal neurons and Purkinje neurons have AIS starting locations within a few micrometers of the soma (Khaliq and Raman, 2006; Palmer et al., 2010; Galiano et al., 2012; Harty et al., 2013; Gutzmann et al., 2014; Hamada and Kole, 2015; but see Thome et al., 2014), a structural arrangement that is expected to limit, rather than enhance, the excitability of these relatively large neurons. A more plausible hypothesis is that AIS plasticity, primarily through changes in AIS length, acts as a homeostatic mechanism to fine-tune excitability at relatively slow timescales. This type of AIS plasticity appears to be robust during development (Kaphzan et al., 2011, 2013; Gutzmann et al., 2014; Kuba et al., 2014) but is more modest in adulthood (Gutzmann et al., 2014), with only limited plasticity observed in mature animals following traumatic brain injury (Baalman et al., 2013), pharmacologically induced seizures (Harty et al., 2013), or demyelination (Hamada and Kole, 2015).

Plasticity of AIS location, which itself has only a modest impact on intrinsic excitability, may be more important for tuning frequency response characteristics of neurons. Simulations by Kuba et al. (2006) found that a short AIS, positioned distally from the soma (as found in highfrequency-responsive neurons in the avian nucleus laminaris) enhanced the fidelity of action potential generation in response to simulated high-frequency synaptic input. Since somatodendritic morphology influences AIS performance in the frequency domain (Hay et al., 2013; Eyal et al., 2014), it is possible that neurons adjust AIS location to stabilize frequency response characteristics following changes in somatodendritic morphology. Alternatively, it is possible that AIS translocation could have indirect effects on excitability by changing the spatial relationship between axoaxonic GABAergic inputs and the AIS (Muir and Kittler, 2014; Wefelmeyer et al., 2015).

Overall, our results demonstrate the substantial impact that somatodendritic morphology will have on the direction and magnitude of excitability changes following AIS plasticity. Additional studies that directly test for correlations of AIS architecture, dendritic morphology, and *in vivo* neuronal output, under baseline conditions and following manipulations of afferent input, will be needed to clarify the physiological impact of the different forms of AIS plasticity during normal neuronal development and following injury or disease.

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