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Impedance Effects of Metallic Ground Plane on the CTHA Antenna

Tao Guan

Thesis submitted to the faculty of the College of Engineering and Mineral Resources at West Virginia University in partial fulfillment of the requirements for the degree of

> Master of Science in Mechanical Engineering

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Abstract

As with the fast-paced development of the communication industry, antennas have become an indispensable part of daily life. However, everyone may have experienced the malfunction of a communication system or radio due to a nearby human body or building or automobile. Then comes the question of how adjacent objects influence the antenna. This thesis has concentrated on the study of these effects on the impedance of the CTHA (contrawound toroidal helical antenna).

The results of this study indicate the CTHA's input impedance changes as a damped sinusoid function of the distance between it and the metallic ground plane. For equivalent distances between the antenna and the metallic ground plane, the CTHA's impedance has been shown to be less affected than the impedance of a vertical dipole, a horizontal dipole, or a horizontal loop antenna. This has been shown by both simulation and experiment and is demonstrated by the plot of the magnitude of the relative impedance change. It indicates that the CTHA will have a smaller increase of the SWR than the other antennas when foreign objects are in the vicinity of the antenna.

This study has also confirmed that NEC (numerical electromagnetic code) is an effective numerical tool for modeling dipoles and loop antennas. The inability for NEC to accurately model the CTHA seems to be caused by the inability to include effects of the core material with dielectric constant other than 1 of the CTHA. Another numerical method, XFDTD (X-window finite difference time domain method), has shown better accuracy in calculating the CTHA's impedance than NEC when comparing with the experimental results.

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Table of Contents

Abstract	<i>ii</i>
Acknowledgments	iii
Table of Contents	iv
List of Figures	vii
List of Tables	ix
Nomenclature	<i>x</i>
Chapter 1 Introduction	1
1. Background	1
2. Contrawound Toroidal Helical Antenna (CTHA)	2
3. Objective	3
4. Methodology	4
5. Literature Review	4
1) Antenna Input Impedance	4
2) Related Research	7
Chapter 2 Modeling with NEC for Impedance Study	12
1. Introduction of NEC	12
2. Modeling for Metal Plate Study	13
3. Numerical Result	17
1) Vertical Dipole over 3ft x 3ft Metal Plate	17
2) Horizontal Dipole over 3ft x 3ft Metal Plate	21
3) Horizontal Loop over 3ft x 3ft Metal Plate	22
4) Horizontal CTHA over 3ft x 3ft Metal Plate	22
4. Summary	23
Chapter 3 Measurement of Antennas' Input Impedance	25
1. Introduction of Equipment	25

1	1) Anechoic Chamber	25
2	2) HP 8753D Network Analyzer	26
3	3) Setup of the 3ft x 3ft Metal Plate Study	27
4	4) Measurement Calibration	28
2.	Experimental Results	30
3.	Error Analysis of Impedance Measurement	32
Chap	ter 4 Comparison of NEC and Experimental Results	33
1.	Introduction	33
2.	Vertical Dipole	33
3.	Horizontal Dipole	35
4.	Horizontal Loop	36
5.	Horizontal CTHA	38
6.	Summary	42
Chap	ter 5 Applying XFDTD on Impedance Study	44
1.	Introduction	44
2.	Evaluation of XFDTD	44
3.	Applying XFDTD on the Metal Plate Study of the CTHA	46
4.	Summary	51
Chap	ter 6 Comparison of Antennas	52
1.	Introduction	52
2.	Magnitude of the Relative Impedance Change	52
3.	Effect of the Relative Impedance Change on SWR	53
4.	Change of the Resonance Frequency	56
5.	Exploration of the Reasons for CTHA's Relative Impedance Invariance	57
1	Effect of Wire Coupling	57
2	2) Effect of Near Field Energy Distribution	60
6.	Summary	64
Chap	ter 7 Conclusions and Recommendations	66
1.	Conclusions	66
2.	Recommendations	67
Refer	ences	68

Appendix A Numerical Model of Antennas	70
Appendix B Plain Surface Generator	85
Appendix C Properties of RANTEC FerroSorb	89
Appendix D Specifications of HP8753D Network Analyzer	90
Approval of Examining Committee	91

List of Figures

Figure	1 Geometry of the CTHA	_
Figure	2 Equivalent Circuit to a Transmitting Antenna [8]	_
Figure .	3 Input Impedance of a Horizontal Wire antenna above the Earth ($\mathcal{E}1r=10.0$, $\sigma l=1.0x10^{-3}$ S/m) [9]	
Figure	4 Vertical Electric Dipole Impedance as a Function of Height above a Homogeneous Lossy Half-Space [8,10]	1
Figure .	5 Vertical Magnetic Dipole (or small Horizontal Loop) Impedance Change as a Function of Height above a Homogeneous Lossy Half-Space [8,10]	1
Figure	6 Antennas above a 3ft x 3ft Metal Plate	1
Figure	7 Closed Patch Surfaces	1
Figure	8 Relative Impedance Change of the Vertical Dipole over the 3'x 3' Metal Plate Modeled with Different Surface Elements	2
Figure	9 Vertical Dipole Numerical Results for Different Plate Discretization	2
Figure	10 Input Impedance of Horizontal Dipole in a Function of Relative Height	2
Figure	11 3'x3' Metal Plate under the CTHA inside the CIRA Anechoic Chamber	2
Figure	12 Picture of the Testing Site	2
Figure	13 Diagram of the Setup of Impedance Measurement	2
Figure	14 Measured Free Space Impedance of a Half-Wave Dipole	
Figure	15 Relative Impedance Change of the Vertical Dipole	1
Figure	16 Resistance and Reactance of the Vertical Dipole as a Function of the Relative Height	
Figure	17 Relative Impedance Change of the Horizontal Dipole	i i
Figure	18 Resistance and Reactance of the Horizontal Dipole as a Function of the Relative Height	
Figure	19 Relative Impedance Change of the Horizontal Loop	
Figure 2	20 Resistance and Reactance of the Horizontal Loop as a Function of the Relative Height	Ĵ

Figure	21 Relative Impedance Change of the Horizontal CTHA	39
Figure	22 Resistance and Reactance of the Horizontal CTHA as a Function of the Relative Height	42
Figure	23 Relative Impedance Change of the Vertical Dipole over a 3'x3' Metal Plate	46
Figure	24 Relative Impedance Change of the CTHA over a 4"x4" Metal Plate	49
Figure	25 Magnitude of the Relative Impedance Change of the CTHA over a 4"x4" Metal Plate	51
Figure	26 Magnitude of the relative Impedance Change Resulted from the Experimental Results	53
Figure	27 Resonance Frequency Reference to the Free Space Resonance Frequency	56
Figure	28 Relative Impedance Change of the Single Helix and the CTHA Resulted from NEC	59
Figure	29 Magnitude of the relative Impedance Change of the Single Helix and the CTHA Resulted from NEC	60
Figure	30 Near-Field Intensity of Horizontal Dipole	61
Figure	31 Near-Field Intensity of CTHA	62
Figure	32 Comparison of Electric Flux Density	63
Figure	33 Comparison of Magnetic Flux Density	64
Figure	34 Plain_form	85
Figure	35 Form of Keypoint Data File Generator	86
Figure	36 Form of Grid Data File Generator	87

List of Tables

Table 1 Nomenclatures in the Thevenin Circuit Equivalent	5
Table 2 Specifications of Antennas	15
Table 3 Distances from the Antennas to the Metal Plate Used for Impedance Study (mm)	_ 16
Table 4 Free Space Frequencies and Impedance of the CTHA in NEC Analysis	_ 23
Table 5 Free Space Frequencies and Impedance	_ 31
Table 6 Percentage Difference of Numerical Result to Experimental Result	31
Table 7 Free Space Resonance Frequency and Impedance of the Vertical Dipole	45
Table 8 Percentage Difference of the Numerical Results to the Experimental Results	_ 45
Table 9 Free Space Resonance Frequencies and Impedance of the CTHA	47
Table 10 Percentage Difference of the Numerical Results to the Experimental Results	47

Nomenclature

- B Magnetic flux density
- D Electric flux density
- E Electric field intensity
- Ei ith data of the experimental results set
- H Magnetic field intensity
- Ig Current in the loop
- m Magnitude of the relative impedance change
- n Total number of data in a data set
- Ni ith data of the numerical results set
- Pr Power delivered to the antenna for radiation
- r Radius of wire-grid segment
- R Resistance of the antenna
- R0 Free space resistance of the antenna
- Ra Load resistance at terminated end of transmission line
- RA Antenna's resistance at terminals a-b
- Rc Characteristic resistance of transmission line
- Rg Resistance of the generator and transmission line impedance
- RL Loss resistance of the antenna
- Rr Radiation resistance of the antenna
- Vg Peak generator voltage
- X Reactance of the antenna
- X0 Free space reactance of the antenna
- Xa Load reactance at terminated end of transmission line
- XA Antenna's reactance at terminals a-b
- Xc Characteristic reactance of transmission line
- Xg Reactance of the generator and transmission line impedance
- ZA Antenna's impedance at terminals a-b
- Zc Complex characteristic impedance of transmission line
- Zg Internal impedance of the generator
- Δ Separation of wires in the mesh

- $\epsilon 0$ Permittivity of free space ($\approx 8.854\text{E-12 F/m}$)
- λ Wavelength
- $\lambda 0$ Free space wavelength
- $\mu 0$ Permeability of free space ($\approx 1.257\text{E-6 H/m}$)
- ρ Reflection coefficient
- σE Standard deviation of the experimental results set
- σN Standard deviation of the numerical results set

Chapter 1 Introduction

1. Background

Over the last 50 years, communication technology has experienced a breathtaking revolution; the antenna has played an indispensable role in that revolution. The antenna serves a communication system the same way that eyes and ears serve a human. More than that, the antenna has been one of the most critical components of some new technologies, such as GPS (Global Positioning System), keyless entry, etc. The need for exploring better antenna designs for all kinds of purposes is well recognized.

As defined in IEEE Transactions on Antennas and Propagation [1], an antenna is "a means for radiating or receiving radio waves." Consequently the amount of energy generated from a source that can be radiated or received through an antenna is the primary consideration of antenna design.

In general, an antenna is a special component of an electrical circuit, in which the antenna is connected to a source with a transmission line. Under ideal conditions, the energy generated by the source should be totally transferred to the antenna through a transmission line, and then radiated to space. But in a practical system, there are conduction-dielectric losses due to the lossy nature of the transmission line and the antenna, as well as reflection (mismatch) losses at the interface between the line and the antenna. The maximum radiation occurs when the system is under conjugate matching.

System matching is the match between the impedance of transmission line, the tuning circuit (matching network), and the impedance of antenna. When the impedance of the transmission line

and the tuning circuit is fixed, the system matching depends on the stability of the impedance of the antenna. The impedance of an antenna is made up of self-impedance and mutual impedance [2]. Self-impedance is the impedance that would be measured at the terminals of the antenna if it were in free space with no other antennas or reflecting objects in the vicinity. Mutual impedance accounts for the coupling between the antenna and any other source [3]. Usually, the system matching is designed by taking into account the antenna's self-impedance. In practice, all kinds of objects can exist in the vicinity of an antenna, such as human bodies, automobiles, buildings, etc. These objects could affect the antenna's mutual impedance significantly, which may result in a very poor performance of the antenna.

This research has focused on studying the impedance effect of metallic ground plane on the Contrawound Toroidal Helical Antenna (CTHA). Both experimental and numerical techniques have been used to study the CTHA.

2. Contrawound Toroidal Helical Antenna (CTHA)

"The Toroidal Helical Antenna (THA) is a new antenna design that has promising performance as it has a small profile compared to the commercial standard dipole antennas of the same resonance frequency" [6]. As an important class of THA, the Contrawound Toroidal Helical Antenna (CTHA), which has two helices with uniform pitches and opposite senses and one feeding port as shown in Figure 1, not only has the advantage of being physically small, but also has the advantages of being omnidirectional in multiple axis (isotropic radiator), circularly polarized and scaleable design [7]. With these advantages, the CTHA has promising potentials for wide applications.

This research studies the impedance variance of the CTHA in the vicinity of a metallic ground plane. Both numerical and experimental results are obtained, compared, and contrasted against the same results for a vertical dipole, a horizontal dipole, and a horizontal loop.



Figure 1 Geometry of the CTHA

3. Objective

The primary interest of this thesis is to study the effects of varying the distances between the CTHA and the metallic ground plane on the impedance of the CTHA. The impedance effect of the metallic ground plane on the CTHA is to be compared with that on the other antennas. The reasons for its relative impedance invariance are to be explored. For conducting this impedance study, both numerical and experimental approaches have been employed. The effectiveness of the numerical methods for studying the CTHA's impedance is to be evaluated.

4. Methodology

Both numerical and experimental approaches have been employed in this impedance study. The numerical methods involved include NEC (Numerical Electromagnetics Code) [11] and XFDTD (X-Window Finite Difference Time Domain) [20]. The measurement of the antenna's impedance was conducted in an anechoic chamber with the HP8753D network analyzer.

5. Literature Review

1) Antenna Input Impedance

As mentioned above, an antenna is a special kind of electrical circuit. Figure 2 shows the Thevenin circuit equivalent of an antenna. The nomenclatures involved in this circuit equivalent are listed in Table 1. The input impedance of an antenna is defined as the impedance presented by an antenna at its terminals or the ratio of the voltage to current at a pair of terminals [8] and is given as

$$Z_A = R_A + j X_A. \tag{1-1}$$

In general, the resistive part of Eq.1-1 consists of two components R_r and R_L as indicated in Eq.1-2. The generator and transmission line has internal impedance as expressed in Eq.1-3.

$$R_A = R_r + R_L. \tag{1-2}$$

$$Z_g = R_g + jX_g. \tag{1-3}$$

Term	Definition		
Ig	the current in the loop		
P _r	the power delivered to the antenna for radiation		
R _A	the antenna's resistance at terminals a-b		
R _g	the resistance of the generator and transmission line impedance		
R _L	the loss resistance of the antenna		
R _r	the radiation resistance of the antenna		
Vg	the peak generator voltage		
X _A	the antenna's reactance at terminals a-b		
\mathbf{X}_{g}	the reactance of the generator and transmission line impedance		
Z _A	the antenna's impedance at terminals a-b		
Z _g	the internal impedance of the generator		

Table 1 Nomenclatures in the Thevenin Circuit Equivalent



(b) Thevenin equivalent



According to the Thevenin equivalent circuit and circuit theory, the current in the system can be expressed as Eq.1-4 and the power delivered to the antenna for radiation can be expressed as Eq.1-5.

$$I_{g} = \frac{V_{g}}{Z_{A} + Z_{g}} = \frac{V_{g}}{(R_{r} + R_{L} + R_{g}) + j(X_{A} + X_{g})}$$
(1-4)

$$P_{r} = \frac{1}{2} \left| I_{g} \right|^{2} R_{r} = \frac{\left| V_{g} \right|^{2}}{2} \left[\frac{R_{r}}{(R_{r} + R_{L} + R_{g})^{2} + (X_{A} + X_{g})^{2}} \right]$$
(1-5)

From Eq.1-5, it can be clearly found that the maximum power delivered to the antenna occurs when conjugate matching is reached by satisfying:

$$R_r + R_L = R_g, (1-6)$$

and

$$X_A = -X_g. (1-7)$$

When there is a metallic ground plane in the vicinity of the antenna, the antenna's impedance Z_A will change. That is to say the value of R_A , which is equal to $Rr+R_L$, and X_A may no longer equal to R_g and $-X_g$, respectively. Consequently, the conjugate matching of the system will not be satisfied. This will lead to the decrease of the power delivered to the antenna. By studying how the metallic ground plane affects the impedance of the CTHA, it is expected to help to find compensations for maintaining the system matching in the case when there are objects in the vicinity of the CTHA.

2) Related Research

Several studies on the impedance effects of adjacent objects on antennas have been conducted. For example, R. C. Babu's "Impedance Calculations for Horizontal Wire Antennas above a Lossy Earth" [9] and Constantain A. Balanis' study of ground effects on an infinitesimal vertical dipole, and a small horizontal loop [8]. But this study is the first effort to study the impedance effects of the metallic ground plane on the CTHA. The conclusions of Babu's study and Balanis' study have provided valuable references for validating the approaches used in this

research for studying CTHA's impedance, and also provided guidance for studying the impedance effects of the metallic ground plane on the CTHA.

In the Babu's study [9], the input impedance of a thin cylindrical wire antenna kept horizontally above a lossy earth is calculated by solving the electric field integral equation for the antenna current using the method of moments (MoM). Coupled horizontal wire antennas kept at the same height from the air-earth interface are analyzed by solving the corresponding zero and first phase sequence current integral equations. The input impedance as a function of antenna height (in terms of free space wavelength) from the air-earth interface is shown in Figure 3. "For the finite conductivity of the earth, the impedance of a horizontal antenna is maximum when it is kept closest to the interface; it reaches a minimum as the separation from the interface is increased, and then increases and finally reaches the free space value at large distances from the boundary" [9].



Figure 3 Input Impedance of a Horizontal Wire antenna above the Earth ($\varepsilon 1r=10.0$, $\sigma 1=1.0 \times 10^{-3} \text{S/m}$) [9]

Babu's study has disclosed that the antenna's resistance and reactance change as a function of the distance between the antenna and the ground plane relative to the free space wavelength. In this study, the function of the resistance and reactance of the CTHA has been studied.

In the Balanis' study [8], the impedance change of an infinitesimal vertical dipole and a small loop placed a height above a homogeneous lossy half-space has been compared to the impedance in free space radiation. The relative resistance change is expressed as Eq.1-8 and the relative reactance change is expressed as Eq.1-9.

$$\Delta R / R_0 = (R - R_0) / R_0 \tag{1-8}$$

$$\Delta X / R_0 = (X - X_0) / R_0 \tag{1-9}$$

Graphical illustration of the relative impedance change of the infinitesimal vertical dipole is shown in Figure 4, and that of the small loop is shown in Figure 5. Balanis' results indicate that the antennas' relative impedance change decreases along spiral curves when the distance between the antenna and the lossy ground increases. When the distance tends to be infinity, the relative impedance change tends to be zero. This approach provides a combined consideration on both the resistance change and the reactance change. In addition, it references the impedance change to the free space impedance, which makes the impedance effects comparable among different antennas at different frequencies. In this impedance study, this analysis method has been extensively used on studying the impedance effects of the metallic ground plane on the CTHA.



Figure 4 Vertical Electric Dipole Impedance as a Function of Height above a Homogeneous Lossy Half-Space [8,10]



Figure 5 Vertical Magnetic Dipole (or small Horizontal Loop) Impedance Change as a Function of Height above a Homogeneous Lossy Half-Space [8,10]

Chapter 2 Modeling with NEC for Impedance Study

For studying the impedance effects of a metallic ground plane on the CTHA, a 3ftx3ft metal plate was modeled at a distance beneath a horizontal CTHA. In order to validate the effectiveness of NEC in impedance calculation, the 3ftx3ft metal plate has also been modeled under a vertical dipole, a horizontal dipole and a horizontal loop.

1. Introduction of NEC

The Numerical Electromagnetics Code (NEC) is "a computer program for analyzing the electromagnetic response of antennas and scatterers. The code is based on the numerical solution of integral equations by the method of moments; it combines an electric-field integral equation for modeling thin wires with a magnetic-field integral equation for closed, perfect conducting surfaces" [11].

NEC provides two options for modeling a conducting surface, namely wire-grid and surface patch. Modeling conducting surfaces with the wire-grid feature applies the equivalent of a solid conducting surface to a grid having sufficiently small mesh size. According to the description in [11], the segment length of wire should be less than 0.1λ (λ is the wavelength), and the circumference of wire segment should be less than the separation of wires. This can be used to model thin plates, open shells, and finitely conducting surfaces. Modeling conducting surfaces with the surface patch option uses the magnetic field integral equation. It is restricted to closed surfaces with a non-vanishing enclosed volume. However, results from modeling a thin reflection surface with surface patch turn out to be quite close to the experimental results, as shown in Chapter 4. For evaluating the accuracy of NEC results, wire-grid, closed patch surfaces

and thin plate composed of surface patch have been used to model the 3ft x 3ft metal plate separately.

2. Modeling for Metal Plate Study

The metal plate study is set up as shown in Figure 6. A horizontal CTHA (details as shown in Figure 1) is placed with its major radius parallel to the plate; a vertical dipole is placed with the wire perpendicular to the plate; a horizontal dipole is placed with the wire parallel to the plate and also parallel to two sides of the plate; and a horizontal loop is placed with its radius parallel to the plate. All antennas have been centered to the center of metal plate.



(a) Horizontal CTHA



Figure 6 Antennas above a 3ft x 3ft Metal Plate

The NEC cards for modeling the antennas over a 3ft x 3ft metal plate have been shown in Appendix A. The geometry specifications of the antennas are listed in Table 2.

	СТНА	Dipole	Loop
Major Radius	0.02667 m	-	0.04978 m
Minor Radius	4.7 mm	-	-
Wire Radius	0.36 mm	1.016 mm	0.5206 mm
Wire Length	0.376 m+0.378 m	0.1435 m	0.313 m
Number of Turns	10	-	1
Crossing	Тор	-	-
Feed Type	6	-	-

Table 2 Specifications of Antennas

The plain surface generator for generating geometry cards for modeling surfaces with a wiregrid and a surface patch is programmed with Visual Basic. A brief introduction of the function of the generator is in Appendix B. To move the antennas along the Z-axis and rotate the vertical loop to horizontal by 90° around the X-axis, a "GM"—coordinate transformation card, is used. The distance between the antenna and the plate is measured from the bottom of the antenna to the plate. For each antenna, 20 different distances are calculated. The distances from the bottom of the antenna to the metal plate and the corresponding distances from the feed point of the antenna to the metal plate are listed in Table 3. For most antennas, the testing frequency is around 1 GHz, this corresponds to a free space wavelength of 300 mm. Variable steps have been chosen for different distance ranges due to that the closer the antenna to the plate, the more its impedance changes.

Bottom to	Feed Point to Plate			
Plate	Hori. CTHA Vert. Dipole		Hori. Dipole	Hori. Loop
1	11	73	2	1.5
5	15	77	6	5.5
10	20	82	11	10.5
15	25	87	16	15.5
20	30	92	21	20.5
25	35	97	26	25.5
30	40	102	31	30.5
35	45	107	36	35.5
40	50	112	41	40.5
50	60	122	51	50.5
60	70	132	61	60.5
70	80	142	71	70.5
80	90	152	81	80.5
100	110	172	101	100.5
130	140	202	131	130.5
160	170	232	161	160.5
190	200	262	191	190.5
220	230	292	221	220.5
250	260	322	251	250.5
300	310	372	301	300.5

Table 3 Distances from the Antennas to the Metal Plate Used for Impedance Study (mm)

3. Numerical Result

1) Vertical Dipole over 3ft x 3ft Metal Plate

For a vertical dipole, three kinds of surfaces have been modeled, wire-grid, thin patch surface and closed patch surfaces.

I. The wire grid surface is constructed as a square mesh of segments. For accuracy, a mesh size of 30.5 mm is chosen, which is about 0.1λ . The wire radius of the wire-grid is 4.775 mm, which agrees with the rule for wire modeling [11]:

$$2\pi r = \Delta \,. \tag{2-1}$$

A total number of 1,860 wire segments are used to model the 3ft x 3ft metal plate.

- II. The thin patch surface is constructed with the square patch element. A total number of 400 (20x20) patch elements are used to model the metal plate. The individual area of each patch is 2.09E-3 m², which is less than 3.6E-3 m² ($0.04\lambda^2$) required for accuracy [11]. The normal vector of each patch element points upward.
- III. Closed patch surfaces are made up of six thin patch surfaces as illustrated in Figure 7. All patch elements involved have the same size and shape. The normal vector of each element is directed outward. A total number of 880 elements are used.



Figure 7 Closed Patch Surfaces

IV. Results

The results of the relative impedance change calculated for the different surface models have been plotted in Figure 8. It has been plotted the same way as Figure 4. The horizontal axes correspond to $\Delta R/R_{o}$, while the vertical axes correspond to $\Delta X/R_{o}$. By comparing the curves on these figures, it can easily be seen that the NEC result with the thin patch surface model agrees better with Figure 4, which is based on the numerical results obtained by Vogler and Noble [12]. Both indicate that as the distance between the antenna and the conducting surface increases, the relative impedance change decreases along a spiral curve, which is shrinking towards the origin. In Figure 4, value of Ψ depends on the value of conductivity and permittivity of the conducting surface. It means that the gradient of the spiral curve varies with different kinds of conducting surfaces in the vicinity. It provides a reason for the difference between the spirals on (b) of Figure 8 and Figure 4.



(a) Surface Model with Wire-Grid







Relative Resistance Change



Figure 8 Relative Impedance Change of the Vertical Dipole over the 3' x 3' Metal Plate Modeled with Different Surface Elements

The time spent calculating each point on the curve varies among different models. The wire-grid model takes about 1,360 sec, the 20x20 thin patch model takes about 94 sec, and the closed patch surfaces model takes about 956 sec.

Considering that there is always a compromise between the calculation time and the accuracy, various numbers of patch segments have been used for modeling the thin patch surface. Figure 9 illustrates the results from discretizing the 3ft x 3ft plate by 10x10, 20x20, and 40x40.

The calculation of each point on the curve takes $3.7 \sec$ for 10x10, $94 \sec$ for 20x20, and $11,697 \sec$ for 40x40. The result from the 20x20 agrees well with that from the 40x40, while saving quite a significant amount of time. Consequently, the 20x20 patch segment was chosen to model the metal plate for this study.



Figure 9 Vertical Dipole Numerical Results for Different Plate Discretization

2) Horizontal Dipole over 3ft x 3ft Metal Plate

The horizontal dipole is modeled to be over a 20x20 thin patch surface. Its resistance and reactance change as the height of it over the metal plate varies. Figure 10 exhibits its resistance and reactance in a function of the height relative to the free space wavelength. The numerical result of its relative impedance change is shown in Figure 17 in Chapter 4.



height/wavelength



Figure 10 and Figure 3 have extremely similar contours, except that the reactance curve in Figure 10 crosses the horizontal axis because the impedance is calculated at its resonance frequency, while Figure 3 shows the result at a frequency other than resonance frequency. Both figures indicate that as the height of the horizontal dipole over the conducting surface increases, both its resistance and reactance oscillate around the value of free space impedance, namely 72 ohms of resistance, and 0 ohms of reactance. The amplitude of oscillation decreases as the height increases.

3) Horizontal Loop over 3ft x 3ft Metal Plate

The NEC result for the relative impedance change of the horizontal loop over a 20x20 thin patch surface model is illustrated in Figure 19, and the loop's resistance and reactance as a function of the relative height to the free space wavelength is plotted in Figure 20 in Chapter 4.

4) Horizontal CTHA over 3ft x 3ft Metal Plate

Only the wires of CTHA have been modeled; the core material made of high density polyethylene, on which the wires are wound, could not be modeled with NEC, because it does not provide the function for modeling a core material with a dielectric constant other than one, which corresponds to air. However, it is possible to model different grounds with different material properties.

Using feed 6 [13], CTHA is not naturally matched. Consequently its impedance change has been studied at a high resistance resonance frequency (3rd resonance), a low resistance resonance frequency (4th resonance), and off the 3rd resonance frequency when resistance is about 50 ohms. The results of the relative impedance change are shown in Figure 21 in Chapter 4. Figure 22 illustrate its resistance and reactance as a function of relative height to the free space wavelength.

	3 rd Resonance	off 3 rd Resonance	4 th Resonance
Frequency (MHz) 917.21		937.5	1215
Resistance (ohms)	35843	51.05	0.456
Reactance (ohms)	17.4	-1345.8	0.636

 Table 4 Free Space Frequencies and Impedance of the CTHA in NEC Analysis

4. Summary

This chapter has primarily described the modeling of antennas above metal plates with NEC. The results for different models have been analyzed and compared with references. From the above discussion, the following points can be made:

- The thin patch surface is a reasonable approach for modeling the metal plate in this impedance study. Instead of representing the current flowing on the surface by the current flowing in the wires of a mesh, it represents the current as flowing on the surface in two orthogonal directions on square flat patches. The surface patch gives a more accurate representation of a surface, especially for near-field quantities, than a wire mesh because it directly models the surface and there are no problems relating to equivalence of the sort mentioned for wire meshes [14]. For calculation of the input impedance of the antennas, closed patch surfaces have not displayed much more accuracy than thin patch surfaces while taking about ten times more time to solve.
- By comparing the results given by NEC with the results of related research, it is evident that the NEC results provide a reasonable prediction of the impedance change as the distance between the antenna and the metallic ground plane changes.

- From the numerical results, it could be found that the relative impedance change of the horizontal CTHA follows the similar spiral curves as the vertical dipole, the horizontal dipole, and the horizontal loop. It decreases as the distance between the CTHA and the metal plate increases.
- For the same object in the vicinity of an antenna, its effect on the impedance of different antennas is different. Further comparison of the impedance effect on different antennas will be discussed in Chapter 6.
Chapter 3 Measurement of Antennas' Input Impedance

In Chapter 2, the NEC modeling and results for the 3ft x 3ft metal plate study have been discussed. To further evaluate the accuracy of the NEC results, the measurements of the antennas' impedance have been conducted and the NEC results will be compared with the experimental results in Chapter 4.

1. Introduction of Equipment

1) Anechoic Chamber

Above discussion has indicated that objects in the vicinity of an antenna affect the input impedance of the antenna. Generally, the impedance change is a combined result of the interaction of different objects. In order to understand this effect, it is of primary importance to study the effect of each object separately. The metal plate experiment is designed to study the effect of a metal plate on the input impedance change of antennas. To screen out the influence by the ground and other adjacent objects, an anechoic chamber is used for the experiment.

An anechoic (no echo) chamber is constructed by completely covering all room surfaces with absorbing material. "The philosophy is to provide a nonreflecting environment like in outer space, but with the distinct advantage that the room provides shielding from all of the external electromagnetic noise and interference (natural and man-made)" [15].

The Center for Industrial Research Applications (CIRA) at West Virginia University has constructed an anechoic chamber to measure antenna characteristics in free space conditions. The dimensions of the chamber are 8ft x 8ft x 18ft wooden box with 1 ft thick foam cones, resulting in a cone tip-to-tip distance of 6ft x 6ft x 16ft. The walls are covered with EHP-12 wedge absorber material supplied by RANTEC (the properties of the absorber material are shown in Appendix C). Figure 11 shows the inside view of the WVU anechoic chamber. As indicated in Pertl's report about the validation of the anechoic chamber [16], the effectiveness of the chamber for simulating a free space environment is acceptable when operating at a frequency above 900 MHz.



Figure 11 3'x3' Metal Plate under the CTHA inside the CIRA Anechoic Chamber

2) HP 8753D Network Analyzer

The HP 8753D option 011 is a high performance vector network analyzer for laboratory or production measurements of reflection and transmission parameters [17]. It provides combined digital signal processing and microprocessor controls for easy operation and measurement improvement. It is selected to measure the input impedance of antennas for the metal plate study.

The measurement results of the HP 8753D could be stored in three kinds of format: raw data, data (raw data with error-correction applied), and format (data processed to the display format).

The raw data array has the least amount of processing associated with it, while the format array is the result after corrections, electrical delay, and other processings. In this experiment, the Port Extension function is applied to calibrate out the SMA connector of antenna (details are discussed in part 4 "Measurement Calibration"). This function involves electrical compensation, so the format data is used.

Within the format data file (".F1" for channel 1 or ".F2" for channel 2), the impedance results are stored in real and imaginary data pairs (Re and Im). For interpreting the real and imaginary data pair into resistance and reactance, the following formula is applied:

$$Resistance = (1 - Re^{2} - Im^{2})/((1 - Re)^{2} + Im^{2}) \times Z_{0}$$
(3-1)

$$Reactance = (2 \times Im)/((1 - Re)^2 + Im^2) \times Z_0$$
(3-2)

where Z_0 , the characterized impedance of the system, is 50 ohms in this experiment.

3) Setup of the 3ft x 3ft Metal Plate Study

The setup of the test is as shown in Figure 11, Figure 12 and Figure 13. The central axis of the metal plate crosses the center of the antenna being tested. The level of the plate was checked before the start of the tests, and it was maintained through keeping the same length of the four pieces of strings hanging the plate throughout the tests. For testing all the antennas, impedance measurement started from the smallest distance (1 mm). The distance between the antenna and the metal plate is increased through loosing the strings controlled outside the anechoic chamber.

Each antenna was connected to a coax cable through an SMA connector. The coax cable connected the antenna inside the anechoic chamber with the network analyzer outside the chamber.



Figure 12 Picture of the Testing Site



Figure 13 Diagram of the Setup of Impedance Measurement

4) Measurement Calibration

In this metal plate experiment, the antenna input impedance is measured. However, the unknown impedance is inevitably connected to the measurement device with a length of cable. The actual impedance being measured is not the unknown impedance—it is the impedance of the

connection cable that is terminated in the unknown impedance [18]. To measure only the desired unknown impedance of the antennas, the connection cable needs to be calibrated out.

"Measurement calibration is an accuracy enhancement procedure that effectively removes the system errors that cause uncertainty in measuring a test device. It measures known standard devices and uses the results of these measurements to characterize the system" [17]. When the calibration includes the connection cable as a part of the measuring system, the cable can be calibrated out as desired. The known standard device used to calibrate the measuring system in this experiment is an HP85033D 3.5mm female calibration kit. The frequency range of 400 MHz to 1.6 GHz was selected (the frequency range of the instrument is from 30 KHz to 6 GHz), and 1601 points were set within this range.

Considering that antennas are generally used without connectors, and that the numerical models discussed above exclude the SMA connector used to connect the test antennas to the connection cable in this experiment, the Port Extension feature of the network analyzer has been applied. This feature compensates for the phase shift of the extended measurement reference plane due to the SMA connector so that the effect of the SMA connector on the antenna's impedance measurement can be canceled out.



Figure 14 Measured Free Space Impedance of a Half-Wave Dipole

Figure 14 shows the measured free space impedance of a half-wave dipole with and without the Port Extension. From the results, no crossing could be found on the reactance curve with the zero-axis without activating the Port Extension. In other words, no resonance is detected around the designed working frequency. This result does not agree with common knowledge about halfwave dipoles. Consequently using the Port Extension to cancel out the effect of the SMA connector on the measurement result of antenna impedance is necessary.

2. Experimental Results

The antennas modeled in Chapter 2, the vertical dipole, the horizontal dipole, the horizontal loop, and the horizontal CTHA, have been tested. The experimental results are shown in Chapter 4. The frequencies are selected for the impedance change study according to the free space measurement result so that the impedance study will focus on the case that antenna is at or close

to resonance. Table 5 lists the free space frequencies and impedance at the frequencies for both the numerical calculations and the experiments.

	Numerica	l Calculatio	n by NEC	Experiment			
	Freq.	R	Х	Freq.	R	X	
	(MHz)	(ohms)	(ohms)	(MHz)	(ohms)	(ohms)	
Vert. Dipole	971	71.89	-0.01	994.75	67.24	0.14	
Hori. Dipole	971	71.89	-0.01	994.75	68.71	-0.08	
Hori. Loop	1035	142.92	0.02	1026.25	131.61	0.32	
CTHA 3 rd Resonance	917.21	35843	17.4	739	575.17	10.38	
CTHA R~50ohms	937.5	51.05	-1345.8	841	49.7	-147.8	
CTHA 4 th Resonance	1215	0.46	0.64	952	1.35	-0.27	

 Table 5 Free Space Frequencies and Impedance

Table 6 Percentage Difference of Numerical Resu	ult to Ex	perimental	Result
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Relative Error	Frequency	Resistance	Reactance
Vertical Dipole	-2.4%	6.9%	*
Horizontal Dipole	-2.4%	4.6%	*
Horizontal Loop	0.85%	8.6%	*
CTHA 3 rd Resonance	24%	6100%	*
CTHA R~50ohms	11.5%	**	-810%
CTHA 4 th Resonance	27.6%	-66%	*

* For resonance evaluation, taking both experimental and numerical result of reactance as 0 ** For R~50ohms, taking both experimental and numerical result of resistance as 50ohms.

From Table 6, it can be seen that the measurement parameters of the vertical dipole, horizontal dipole, and horizontal loop are close to their numerical results. But the numerical

results of CTHA are different from the measurements because the high-density polyethylene core of CTHA could not be modeled with NEC. The result indicates that the core material of CTHA significantly affects the input impedance of the CTHA.

3. Error Analysis of Impedance Measurement

• Measuring Error of HP8753D Network Analyzer

For measurement in the range of 400 MHz to 1.6 GHz with 1,601 points, the accuracy of the resonance frequency is ± 0.4 MHz.

The precision of the measurement with the HP8753D network analyzer also depends on the specifications as shown in Appendix D.

• Error of Distance Measurement

The distance between the antenna and the metal plate is measured with measuring tape. Its accuracy is ± 0.5 mm. Considering the error with the flatness of the plate and the shape error with the antennas, the overall error with distance measuring is ± 1 mm

• Fabrication Error with Antennas

All the antennas are hand-made. Error could result from the length of wire (± 0.5 mm), soldering between the antenna and the SMA connector, and shape irregularity.

Chapter 4 Comparison of NEC and Experimental Results

1. Introduction

Chapter 2 and Chapter 3 discussed the study of the impedance effects of the 3ftx3ft metal plate on the CTHA and some other antennas by numerical approach and experimental approach, respectively. This chapter compares the NEC and experimental results.

With the development of computer technology, calculation speed and computer memory have been greatly improved, which allows extensive application of a computerized analytical method. NEC is one of the more recently developed programs for analyzing the electromagnetic response of antennas and scatterers. The computerized analytical method can be used to analyze not only ready-made designs, but also the future designs. If the results of the method are demonstrated to be close to reality, new designs can be optimized or evaluated numerically, saving time and money when generating ideal designs. With this consideration, the accuracy of the NEC results is evaluated by comparing the numerical results with the experimental results.

2. Vertical Dipole

As can be seen from Figure 15 and Figure 16, the NEC results for the vertical dipole agree well with the experimental results. The standard deviations of the numerical results to the experimental results calculated as Eq. 4-1 are 6.6 ohms and 1.8 ohms for resistance and reactance, respectively. The correlation coefficients calculated as Eq. 4-2 are 0.99 and 0.95 for resistance and reactance, respectively.

Standard Deviation =
$$\sqrt{\frac{\sum_{i=1}^{n} (N_i - E_i)^2}{n}}$$
, (4-1)

$$CorrelationCoefficient = \frac{\frac{1}{n}\sum_{i=1}^{n} (N_i - \overline{N})(E_i - \overline{E})}{\sigma_N \sigma_E}, \qquad (4-2)$$

$$\overline{N} = \sum_{i=1}^{n} N_i , \qquad (4-3)$$

$$\overline{E} = \sum_{i=1}^{n} E_i , \qquad (4-4)$$

According to the theory of data fitting [19], the closer to 1 the correlation coefficient is, the better the two sets of data fit each other. The correlation coefficients of the resistance and reactance of the vertical dipole demonstrate that the numerical results for the vertical dipole fit well with the experimental results.



Figure 15 Relative Impedance Change of the Vertical Dipole



Figure 16 Resistance and Reactance of the Vertical Dipole as a Function of the Relative Height

3. Horizontal Dipole

Figure 17 indicates that the relative impedance change of the horizontal dipole given by NEC follows the same trend as the experimental results except that when the height is less than 20mm (about 0.06λ). The standard deviations of numerical results to experimental results are 19.6 ohms and 9.3 ohms for resistance and reactance, respectively. Taking out the obviously skewed points, which correspond to the distances less than 20mm, the standard deviations are 8.7 ohms for both resistance and reactance. The correlation coefficients without the skewed points are 0.79 and 0.87 for resistance and reactance, respectively.

From the curves and the correlation coefficients, it is evident that the numerical results for the horizontal dipole do not fit the experimental results as well as they did for the vertical dipole. However, comparing the impedance of the vertical dipole with that of horizontal dipole, it is obvious that horizontal dipole's impedance is more variant as the height changes. It means the inaccuracy of the distance measurement may result in a larger error in the experimental results for the horizontal dipole.



Figure 17 Relative Impedance Change of the Horizontal Dipole



Figure 18 Resistance and Reactance of the Horizontal Dipole as a Function of the Relative Height

4. Horizontal Loop

Comparing Figure 19 with Figure 5, the similarity between the spirals can be observed. Comparing the NEC results with the experimental results shows that they agree with each other very well except when h<20 mm. The standard deviations are 16.5 ohms and 5.1 ohms for resistance and reactance, respectively. The correlation coefficients are 0.99 and 0.998 for resistance and reactance, respectively. This means that when the height is larger than 20mm, NEC results fit the experimental results very well.



Figure 19 Relative Impedance Change of the Horizontal Loop



Figure 20 Resistance and Reactance of the Horizontal Loop as a Function of the Relative Height

5. Horizontal CTHA

Figure 21 and Figure 22 exhibit significant differences between the NEC and experimental results for the horizontal CTHA at different frequencies. At the 3^{rd} resonance frequency, the standard deviations are 30,448 ohms and 7,127 ohms for resistance and reactance, respectively; when R≈50ohms, they are 24 ohms and 1,212 ohms for resistance and reactance, respectively; at the 4th resonance frequency, they are 126 ohms and 218 ohms for resistance and reactance, respectively.



(a) at the 3^{rd} Resonance Frequency



(b) off the 3^{rd} Resonance Frequency when R \approx 50 ohms





Figure 21 Relative Impedance Change of the Horizontal CTHA

At the 3rd resonance frequency and off the 3rd resonance frequency when R \approx 50ohms, the NEC results have exagerated the CTHA's resistance and the amplitude of the impedance change. To get a better view of the CTHA's resistance and reactance resulting from the experiments, its experimental results at these two frequencies have been plotted separately in addition to the comparison graphs. From the similarity of the curves, it can be found that NEC has correctly predicted the tendency of the impedance change.



(a) at the 3^{rd} Resonance Frequency







neight wavelength

(c) at the 4th Resonance Frequency

Figure 22 Resistance and Reactance of the Horizontal CTHA as a Function of the Relative Height

The experimental results of the CTHA indicate that, similar to the other antennas, the resistance and reactance of the CTHA change as a damped sinusoid function of the distance between the CTHA and the metal plate relative to the free space wavelength. The central axis of each sine wave corresponds to the value of the free space resistance and reactance, respectively.

6. Summary

From above comparisons, it can be found on the one hand, there is good agreement between the experimental results and the NEC results for the vertical dipole, the horizontal dipole and the horizontal loop; while on the other hand, an obvious disagreement between the experimental results and the NEC results for the horizontal CTHA. It implies that NEC is a reasonable numerical method for impedance calculation and metallic surface modeling, but the mismodeling of the core material of the CTHA by NEC could result in inaccuracy in calculating the CTHA's impedance. To better evaluate the impedance of a CTHA wound on materials with dielectric constant other than one, some other numerical methods need to be used.

Chapter 5 Applying XFDTD on Impedance Study

1. Introduction

As discussed in Chapter 4, NEC has displayed satisfactory accuracy for calculating the input impedance of the vertical dipole, the horizontal dipole and the horizontal loop. But its results of the impedance of the CTHA disagree with the experimental results. To improve the model of the CTHA, another numerical method, XFDTD, is used.

XFDTD apples the FDTD (the finite difference time domain method) for electromagnetic calculation under the Unix operating system. The method is a transient marching-in-time approach, in which time is divided into small discrete steps and the electric and magnetic fields on a fine grid are calculated at each time step [20]. Being different from NEC, XFDTD allows the user to specify the parameters for dielectric materials, which can be set differently for each grid. This characteristic makes XFDTD being capable of modeling the core material of the CTHA. For this reason, XFDTD is applied to further the study of the impedance change of the CTHA.

2. Evaluation of XFDTD

Before XFDTD is applied to study the CTHA, its effectiveness of impedance calculation is evaluated through the study of the vertical dipole over a 3ft x 3ft metal plate, the same study as mentioned in Chapter 2 and Chapter 3.

 Table 7 Free Space Resonance Frequency and Impedance of the Vertical Dipole

	Experiment	NEC	XFDTD
Frequency (MHz)	994.75	971	1243.9
Resistance (Ohms)	67.24	71.89	71.34
Reactance (Ohms)	0.14	-0.01	0

Table 8 Percentage Difference of the Numerical Results to the Experimental Results

(%)	NEC	XFDTD
Resonance Frequency	2.4	25
Free Space Resistance	6.9	6.1

The relative impedance change as the distance between the vertical dipole and the metal plate changes is plotted in Figure 23. From Figure 23, it can be observed that both the results of NEC and XFDTD agree with the experimental results. All of them exhibit the trend that as the distance between the vertical dipole and the metal plate increases, the relative impedance change decreases along a spiral curve, which ends at the origin of the coordinate system when the distance is larger than 100 mm. It indicates that XFDTD provides a reliable numerical method for impedance calculation.



Figure 23 Relative Impedance Change of the Vertical Dipole over a 3'x3' Metal Plate

3. Applying XFDTD on the Metal Plate Study of the CTHA

Using XFDTD, it needs to discretize the whole space involved in the metal plate study. To maintain the accuracy as well as to save some time for the calculation, the 3ft x 3ft plate is replaced by a 4in x 4in plate.

The core material of the CTHA is modeled by XFDTD with the dielectric constant of 1.75. For this model, the free space resonance frequencies of the CTHA predicted by XFDTD agree well with the experimental results.

Table 9 lists the free space resonance frequencies and impedance of the CTHA resulted from experiment, NEC and XFDTD. Table 10 lists the percentage difference of the NEC results and the XFDTD results comparing to the experimental results.

	3 rd Resonance		R≈50ohm			4 th Resonance			
	Exp.	NEC	XFDTD	Exp.	NEC	XFDTD	Exp.	NEC	XFDTD
Freq.	739	917	727	841	938	835	952	1215	949
R	575	35843	17	50	51	65	1.4	0.5	676
Х	10	17	82	-148	-1346	220	-0.3	0.6	-207

Table 9 Free Space Resonance Frequencies and Impedance of the CTHA

Table 10) Percentage	Difference o	of the l	Numerical	Results	to the	e Expe	erimental	Result	S

	3 rd Res	3 rd Resonance		ohms	4 th Resonance		
(%)	NEC	XFDTD	NEC	XFDTD	NEC	XFDTD	
Frequency	24.1	1.6	11.5	0.7	27.6	0.5	
Resistance	6100	97	**	**	66	48200	
Reactance	*	*	810	249	*	*	

* for the resonance frequencies, taking the reactance to be zero

** for R≈50ohms, taking the resistance to be 50ohms

From Table 10, it can be found that XFDTD, which has taken into account the core material of the CTHA, has provided more accurate prediction than NEC on the free space resonance frequencies and impedance for the 3^{rd} resonance and off the 3^{rd} resonance when R \approx 50ohms.

Figure 24 illustrates the relative impedance change of the CTHA over the 4" x 4" metal plate resulted from the experiment, NEC and XFDTD. On the plots, h_r represents the distance relative to the free space wavelength. In each of the three cases, namely at the 3rd resonance frequency, off the 3rd resonance frequency when R≈50ohms, and at the 4th resonance frequency, the relative

impedance change of the CTHA decreases as the distance increases at a similar trend for all the three results. But the gradients of the decrease for the three results are different. The NEC results display a relatively slower decrease comparing with the experimental results, and the XFDTD results display a relatively faster decrease. For a better view of the difference, the magnitude of the relative impedance change of the CTHA is calculated:

Magnitude =
$$\sqrt{\frac{(R - R_0)^2 + (X - X_0)^2}{R_0^2}}$$
 (5-1)

The magnitude of the relative impedance change corresponds to the distance from each point on the relative impedance change curve to the origin. Figure 25 illustrates the magnitude of the relative impedance change of the CTHA as a function of the relative distance. It can be found the XFDTD results agree well with the experimental results.



(a) at the 3^{rd} Resonance Frequency



(b) off the 3^{rd} Resonance Frequency when R \approx 50ohm



(c) at the 4^{th} Resonance Frequency





(b) off the 3^{rd} Resonance Frequency when R \approx 50ohm

height/wavelength



(c) at the 4th Resonance Frequency

Figure 25 Magnitude of the Relative Impedance Change of the CTHA over a 4"x4" Metal Plate

4. Summary

The agreement between the XFDTD and the experimental results indicates that XFDTD is a reliable numerical method for impedance study. It is a better choice comparing to NEC for modeling the CTHAs. But the calculation of each point on the relative impedance Change curve with XFDTD takes much more time (several hours per point) than with NEC (several minutes per point).

Chapter 6 Comparison of Antennas

1. Introduction

In Chapter 4, the numerical and experimental results for the relative impedance change of antennas over a 3ft x 3ft metal plate were presented and compared. From the relative impedance change plots, it can be observed that different antennas have differently shaped spirals. The magnitude of the relative impedance change, which is defined as Eq.6-1, represents the size of the spiral curves. For comparing the impedance effect of the metal plate on each antenna, the magnitudes of the relative impedance change of antennas are compared, and the relationship between the magnitude of the relative impedance change and the antenna's SWR (standing wave ratio) is analyzed.

In addition, the reason why the CTHA is relatively invariant with its impedance is explored by comparing the impedance effect of the metal plate on the CTHA and a single helix torioid antenna, and by comparing the near field energy distribution under the horizontal dipole and under the CTHA.

2. Magnitude of the Relative Impedance Change

The magnitude of the relative impedance change is defined for comparing the impedance effect of the metal plate on different antennas by

$$Magnitude = \sqrt{\left(\frac{\Delta R}{R_0}\right)^2 + \left(\frac{\Delta X}{R_0}\right)^2} . \tag{6-1}$$

where $\Delta R = R - R_0$, $\Delta X = X - X_0$.

Eq.6-1 gives the definition of the magnitude of the relative impedance change. The smaller the magnitude, the less variant the antenna's impedance as compared to free space impedance. Figure 26 shows the magnitude of each antenna's results from the experiment as a function of the relative height to the free space wavelength. It is clear from Figure 26 that CTHA at its 3^{rd} resonance frequency and off resonance frequency has the least variance of its relative impedance change. At the 4^{th} resonance frequency, its relative impedance change is larger than that of the vertical dipole, but smaller than those of the horizontal dipole and horizontal loop.



Figure 26 Magnitude of the relative Impedance Change Resulted from the Experimental Results

3. Effect of the Relative Impedance Change on SWR

According to the definition in [21], the voltage reflection coefficient is the ratio of the reflected voltage at a given point on a transmission line to the incident voltage. The reflection coefficient is determined by the relationship between the characteristic impedance of the transmission line and the actual load at the terminated end of the line. For high-quality, low-loss

transmission lines, the characteristic impedance Z_c is almost completely resistive, meaning that $Z_c \approx R_c$ and $X_c \approx 0$. Thus the magnitude of reflection coefficient could be expressed as:

$$\left|\rho\right| = \sqrt{\frac{(R_a - R_c)^2 + X_a^2}{(R_a + R_c)^2 + X_a^2}},$$
(6-2)

For an ideally matched antenna:

$$R_a = R_c, \tag{6-3}$$

and

$$X_a = 0, (6-4)$$

such that $|\rho|=0$.

Assuming that the existence of an object in the vicinity of the antenna causes a change of resistance ΔR and reactance ΔX of the antenna, the magnitude of the reflection coefficient will be:

$$\rho' = \sqrt{\frac{(R_a + \Delta R - R_c)^2 + (X_a + \Delta X)^2}{(R_a + \Delta R + R_c)^2 + (X_a + \Delta X)^2}}.$$
(6-5)

Substituting Eq.6-3 and Eq.6-4 into Eq.6-5, the magnitude of changed reflection coefficient can be simplified to Eq.6-6. Dividing R_0 , the free space resistance of the antenna, by both the numerator and denominator of $|\rho'|$, Eq. 6-6 results in Eq.6-7.

$$\left|\boldsymbol{\rho}'\right| = \sqrt{\frac{\left(\Delta R\right)^2 + \left(\Delta X\right)^2}{\left(\Delta R + 2R_c\right)^2 + \left(\Delta X\right)^2}}\,.$$
(6-6)

$$\left| \rho' \right| = \sqrt{\frac{\left(\Delta R \right)^2 / R_0^2 + \left(\Delta X \right)^2 / R_0^2}{\left(\Delta R + 2R_c \right)^2 / R_0^2 + \left(\Delta X \right)^2 / R_0^2}} \,. \tag{6-7}$$

According to the definition of the magnitude of the relative impedance change (Eq.6-1), the relationship between the magnitude of the reflection coefficient and the magnitude of the relative impedance change (abbreviated as m) can be expressed as Eq.6-8. Because ΔR is much smaller than R_c , which is a constant for all antennas, the reflection coefficient will increase as the magnitude of the relative impedance change increases.

$$\left| \rho' \right| = \sqrt{\frac{1}{1 + 4(\Delta R R_c + R_c^2)/m^2}}.$$
(6-8)

The SWR is related to the magnitude of the complex reflection coefficient by Eq.6-9. Because |p| is larger than 0 and less than 1, Eq. 6-9 indicates that the increase of the magnitude of the reflection coefficient will raise the value of the SWR. According to the positive relation between the magnitude of the relative impedance change and the magnitude of the reflection coefficient, as well as the positive relation between the magnitude of the reflection coefficient and the SWR, it can be concluded that larger magnitude of the relative impedance change would result in larger increase of the SWR.

$$SWR = \frac{1+|\rho|}{1-|\rho|}.$$
(6-9)

From the above discussion, CTHA has relatively smaller magnitude of the relative impedance change when compared to the horizontal dipole and horizontal loop. This means in cases where there is an object in the vicinity of the antenna, CTHA will have a smaller increase of SWR than will the other antennas.

4. Change of the Resonance Frequency

The metallic ground plane in the vicinity of an antenna will change the antenna's impedance. It will also change the antenna's resonance frequency. Based on the experimental results, the resonance frequency of the antennas at each height above the 3ftx3ft metal plate reference to the free space resonance frequency is plotted as a function of the height relative to the free space wavelength in Figure 27.

From Figure 27, it can be observed that for all the antennas studied, the resonance frequency reference to the free space resonance frequency oscillates around the value of 1. As the height of the antenna above the metal plate increases, the amplitude of the oscillation decreases. It is expected that as the height tends to be infinity, f/f0 tends to be 1, which means when the metal plate is very far away, the resonance frequency will be equal to the free space resonance frequency.



Figure 27 Resonance Frequency Reference to the Free Space Resonance Frequency

Comparing the resonance frequency change of the antennas due to the metal plate in the vicinity, it can be found that the horizontal CTHA has the least change at both the 3rd resonance and the 4th resonance. This agrees with the conclusion mentioned above that the CTHA's input impedance is the least variant due to the metal plate in the vicinity. In other words, the metal plate has the least effect on the horizontal CTHA.

5. Exploration of the Reasons for CTHA's Relative Impedance Invariance

Above discussions indicate that CTHA is relatively impedance invariant to the metallic ground plane in the vicinity. Then comes the question why the CTHA has the characteristic of being relative impedance invariant. The reasons have been explored through studying its physical structure and the characteristic of its near field distribution.

1) Effect of Wire Coupling

Considering that the CTHA is a contrawound toroidal helical antenna, the coupling of the two single helices may be an explanation for CTHA's relative impedance invariance. To examine this possibility, the impedance effect of a metal plate on a single helix toroid antenna has been compared with CTHA by numerical modeling with NEC. The single helical toroid antenna has been modeled with the same dimensions as CTHA.

Figure 28 and Figure 29 graph the relative impedance change and the magnitude of the relative impedance change for the single helical toroid antenna and the CTHA. A comparison of the two shows that the coupling of the two single helices of the CTHA has not significantly changed the spiral shape of the relative impedance change curve, but the size of the spirals at different frequencies has decreased. From Figure 29, it can be more clearly observed that the

magnitude of the relative impedance change of the CTHA is much smaller than that of the single helical toroid antenna.

By modeling with NEC, the effect of the core material of the CTHA has been taken out of consideration. The difference of the impedance effect of the metal plate on the CTHA comparing with that on the single helix toroid antenna can be explained by the difference of the structure of the two antennas. Consequently, it can be concluded that the coupling of the two helices of the CTHA helps to explain the relative impedance invariance of the CTHA.



(a) at 3rd Resonance Frequency









Figure 28 Relative Impedance Change of the Single Helix and the CTHA Resulted from NEC



Figure 29 Magnitude of the relative Impedance Change of the Single Helix and the CTHA Resulted from NEC

2) Effect of Near Field Energy Distribution

Considering that significant impedance variance occurs when the distance between an antenna and a metallic ground plane is less than one wavelength, it is necessary to study the antenna's near field pattern to find more explanation for CTHA's relative impedance invariance.

The near electric and magnetic fields of the horizontal dipole and the CTHA (at 3rd resonance frequency) are evaluated numerically from NEC results. Figure 30 illustrates the electric field intensity (E) and magnetic field intensity (H) within the volume under the horizontal dipole. The width and height of the volume are about the same as the length of the dipole, and the thickness is two times the diameter of the dipole. The upper surface of the volume corresponds to the cross section of the horizontal dipole.


Figure 31 illustrates the electric field intensity and magnetic field intensity within the volume under the CTHA. The width, height, and thickness are about the same as the outer diameter of the CTHA. The upper surface of the volume corresponds to the cross section of the CTHA.



From the above field intensity contours, it can be observed that the near field energy has concentrated around the feed point and two ends of the horizontal dipole, while relatively even distributed around the CTHA. Because the field intensity has decreased sharply along the height, the vertical distribution of the near field energy can not be illustrated clearly by the 3-dimensional illustration. To get a better view of the vertical distribution of the near-filed energy, the electric flux density and magnetic flux density are calculated according to Eqs. 6-10 and 6-11 along a vertical line for each antenna. The starting point of the line is chosen with the maximum value on the upper surface of the above 3-D illustrations. For the horizontal dipole, the starting point is next to the feed point along the axis of the dipole, and for the CTHA, it is opposite the feed point as indicated in Figure 31.

$$D = \varepsilon_0 E \tag{6-10}$$

$$B = \mu_0 H \tag{6-11}$$

Figure 32 compares the electric flux density along the vertical lines under the horizontal dipole and the CTHA. It indicates that CTHA has its near electric field energy much more concentrated within 0.1λ (about 33mm) beneath the center of it, while the horizontal dipole has relatively larger near electric field energy distributed along the vertical line until the height is close to 1λ .



Figure 32 Comparison of Electric Flux Density

Figure 33 compares the magnetic flux density along the vertical lines under the two antennas. Obviously, the horizontal dipole has much larger near magnetic field energy than the CTHA.



Figure 33 Comparison of Magnetic Flux Density

From the view of the near field energy distribution of the antennas, it can be concluded that the CTHA will have smaller interaction with the metallic ground plane underneath. Consequently, the input impedance of the CTHA will not be affected as much as that of the horizontal dipole by the metallic ground plane in the vicinity.

6. Summary

From the above comparisons, it is clear that the CTHA has the advantage of being relatively impedance invariant to adjacent metal plate as compared to the other antennas. This is important because it suggests a smaller increase of SWR when foreign objects are in the vicinity of the CTHA.

The comparison of the impedance change of the CTHA with the single helical toroid antenna indicates that the coupling of the contrawound helices of the CTHA helps to explain the relative invariance of CTHA's impedance to the adjacent object. The comparison of the near field energy distribution under the horizontal dipole and the CTHA indicates that the CTHA has its near field energy more concentrated around the wires, so that the interaction between the CTHA and the adjacent object is expected to be relatively weaker. This provides another reason to explain the relative impedance invariance of the CTHA.

Chapter 7 Conclusions and Recommendations

1. Conclusions

A study of the impedance effects of a metallic ground plane on the CTHA has been conducted numerically and experimentally. Both numerical and experimental results indicate that the CTHA, similar to the other antennas such as the vertical dipole, the horizontal dipole, and the horizontal loop, has its resistance and reactance vary as a damped sinusoid function of the distance between the CTHA and the metallic ground plane reference to the free space wavelength. The relative impedance change of the CTHA decreases along a spiral curve as the distance between the CTHA and the metallic ground plane increases.

The importance of this study is that it provides guidance in understanding how a CTHA's impedance changes as a function of the distance between the antenna and an adjacent object. By accurately knowing this function, a desired height can be found at which the CTHA can maintain good matching even if there were an object in the vicinity.

As the experimental results indicate, the CTHA has the advantage of being relatively impedance invariant in comparison with the other antennas when there is an object in the vicinity. This property indicates a smaller increase of the SWR.

Some study has been made to explore the reasons for CTHA's relative impedance invariance. The coupling of the two contrawound helices of the CTHA could be one of the reasons, and that the near field energy being more concentrated around the wires of the CTHA could be another.

The agreement between the NEC results and the experimental results for the vertical dipole, the horizontal dipole and the horizontal loop indicate that NEC is an effective numerical tool for studying the antennas' impedance and modeling metallic surfaces. But being unable to model the core materials with dielectric constant other than one, NEC can not calculate the CTHA's impedance accurately.

XFDTD is a better numerical tool for modeling the CTHA comparing with NEC. But as a compromise to the accuracy of calculations, the calculating time and required memory size of XFDTD are much greater than those of NEC.

2. Recommendations

Further study, especially some theoretical analysis on the mechanism of coupling between the antenna and the adjacent objects, should be made so that a better understanding of the antenna's impedance change can be obtained. This may provide a better solution for the mismatching problem of antennas due to the objects in the vicinity.

This study has disclosed the relation between the magnitude of the relative impedance change and the SWR of the antennas. But the direct relation between the magnitude of the relative impedance change of the CTHA and the matching network has not been studied. It is believed that further study of this relationship may be beneficial to solving the mismatching problems of the CTHA. This mismatching is conjectured to be related to an interaction of the fields of the matching network and the CTHA. It is suggested that this needs further study.

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Appendix A Numerical Model of Antennas

1. The NEC Cards for Modeling the Horizontal CTHA at 1 mm above the 3ft x 3ft Metal

Plate

GW 1 3 2.587E-2 0.000E+0 5.091E-3 2.747E-2 0.000E+0 5.091E-3 3.62E-4 GW 2 1 2.587E-2 0.000E+0 5.091E-3 2.508E-2 7.883E-4 4.842E-3 3.62E-4 GW 3 1 2.508E-2 7.883E-4 4.842E-3 2.363E-2 1.487E-3 4.119E-3 3.62E-4 GW 4 1 2.363E-2 1.487E-3 4.119E-3 2.245E-2 2.122E-3 2.993E-3 3.62E-4 GW 5 1 2.245E-2 2.122E-3 2.993E-3 2.166E-2 2.736E-3 1.573E-3 3.62E-4 GW 6 1 2.166E-2 2.736E-3 1.573E-3 2.131E-2 3.376E-3 6.235E-19 3.62E-4 GW 7 1 2.131E-2 3.376E-3 6.235E-19 2.144E-2 4.090E-3 -1.573E-3 3.62E-4 GW 8 1 2.144E-2 4.090E-3 -1.573E-3 2.201E-2 4.919E-3 -2.993E-3 3.62E-4 GW 9 1 2.201E-2 4.919E-3 -2.993E-3 2.293E-2 5.888E-3 -4.119E-3 3.62E-4 GW 10 1 2.293E-2 5.888E-3 -4.119E-3 2.410E-2 7.002E-3 -4.842E-3 3.62E-4 GW 11 1 2.410E-2 7.002E-3 -4.842E-3 2.536E-2 8.241E-3 -5.091E-3 3.62E-4 GW 12 1 2.536E-2 8.241E-3 -5.091E-3 2.657E-2 9.567E-3 -4.842E-3 3.62E-4 GW 13 1 2.657E-2 9.567E-3 -4.842E-3 2.758E-2 1.092E-2 -4.119E-3 3.62E-4 GW 14 1 2.758E-2 1.092E-2 -4.119E-3 2.826E-2 1.223E-2 -2.993E-3 3.62E-4 GW 15 1 2.826E-2 1.223E-2 -2.993E-3 2.851E-2 1.342E-2 -1.573E-3 3.62E-4 GW 16 1 2.851E-2 1.342E-2 -1.573E-3 2.830E-2 1.442E-2 -1.247E-18 3.62E-4 GW 17 1 2.830E-2 1.442E-2 -1.247E-18 2.761E-2 1.518E-2 1.973E-3 3.62E-4 GW 18 1 2.761E-2 1.518E-2 1.973E-3 2.650E-2 1.567E-2 3.753E-3 3.62E-4 GW 19 1 2.650E-2 1.567E-2 3.753E-3 2.505E-2 1.589E-2 5.165E-3 3.62E-4 GW 20 1 2.505E-2 1.589E-2 5.165E-3 2.336E-2 1.588E-2 6.072E-3 3.62E-4 GW 21 1 2.336E-2 1.588E-2 6.072E-3 2.158E-2 1.568E-2 6.384E-3 3.62E-4 GW 22 1 2.158E-2 1.568E-2 6.384E-3 1.983E-2 1.538E-2 6.072E-3 3.62E-4 GW 23 1 1.983E-2 1.538E-2 6.072E-3 1.824E-2 1.509E-2 5.165E-3 3.62E-4 GW 24 1 1.824E-2 1.509E-2 5.165E-3 1.692E-2 1.491E-2 3.753E-3 3.62E-4 GW 25 1 1.692E-2 1.491E-2 3.753E-3 1.591E-2 1.494E-2 1.973E-3 3.62E-4 GW 26 1 1.591E-2 1.494E-2 1.973E-3 1.526E-2 1.526E-2 1.870E-18 3.62E-4

GW 27 1 1.526E-2 1.526E-2 1.870E-18 1.494E-2 1.591E-2 -1.573E-3 3.62E-4 GW 28 1 1.494E-2 1.591E-2 -1.573E-3 1.491E-2 1.692E-2 -2.993E-3 3.62E-4 GW 29 1 1.491E-2 1.692E-2 -2.993E-3 1.509E-2 1.824E-2 -4.119E-3 3.62E-4 GW 30 1 1.509E-2 1.824E-2 -4.119E-3 1.538E-2 1.983E-2 -4.842E-3 3.62E-4 GW 31 1 1.538E-2 1.983E-2 -4.842E-3 1.568E-2 2.158E-2 -5.091E-3 3.62E-4 GW 32 1 1.568E-2 2.158E-2 -5.091E-3 1.588E-2 2.336E-2 -4.842E-3 3.62E-4 GW 33 1 1.588E-2 2.336E-2 -4.842E-3 1.589E-2 2.505E-2 -4.119E-3 3.62E-4 GW 34 1 1.589E-2 2.505E-2 -4.119E-3 1.567E-2 2.650E-2 -2.993E-3 3.62E-4 GW 35 1 1.567E-2 2.650E-2 -2.993E-3 1.518E-2 2.761E-2 -1.573E-3 3.62E-4 GW 36 1 1.518E-2 2.761E-2 -1.573E-3 1.442E-2 2.830E-2 -2.494E-18 3.62E-4 GW 37 1 1.442E-2 2.830E-2 -2.494E-18 1.342E-2 2.851E-2 1.973E-3 3.62E-4 GW 38 1 1.342E-2 2.851E-2 1.973E-3 1.223E-2 2.826E-2 3.753E-3 3.62E-4 GW 39 1 1.223E-2 2.826E-2 3.753E-3 1.092E-2 2.758E-2 5.165E-3 3.62E-4 GW 40 1 1.092E-2 2.758E-2 5.165E-3 9.567E-3 2.657E-2 6.072E-3 3.62E-4 GW 41 1 9.567E-3 2.657E-2 6.072E-3 8.241E-3 2.536E-2 6.384E-3 3.62E-4 GW 42 1 8.241E-3 2.536E-2 6.384E-3 7.002E-3 2.410E-2 6.072E-3 3.62E-4 GW 43 1 7.002E-3 2.410E-2 6.072E-3 5.888E-3 2.293E-2 5.165E-3 3.62E-4 GW 44 1 5.888E-3 2.293E-2 5.165E-3 4.919E-3 2.201E-2 3.753E-3 3.62E-4 GW 45 1 4.919E-3 2.201E-2 3.753E-3 4.090E-3 2.144E-2 1.973E-3 3.62E-4 GW 46 1 4.090E-3 2.144E-2 1.973E-3 3.376E-3 2.131E-2 3.117E-18 3.62E-4 GW 47 1 3.376E-3 2.131E-2 3.117E-18 2.736E-3 2.166E-2 -1.573E-3 3.62E-4 GW 48 1 2.736E-3 2.166E-2 -1.573E-3 2.122E-3 2.245E-2 -2.993E-3 3.62E-4 GW 49 1 2.122E-3 2.245E-2 -2.993E-3 1.487E-3 2.363E-2 -4.119E-3 3.62E-4 GW 50 1 1.487E-3 2.363E-2 -4.119E-3 7.883E-4 2.508E-2 -4.842E-3 3.62E-4 GW 51 1 7.883E-4 2.508E-2 -4.842E-3 1.633E-18 2.667E-2 -5.091E-3 3.62E-4 GW 52 1 1.633E-18 2.667E-2 -5.091E-3 -8.871E-4 2.823E-2 -4.842E-3 3.62E-4 GW 53 1-8.871E-4 2.823E-2 -4.842E-3 -1.863E-3 2.960E-2 -4.119E-3 3.62E-4 GW 54 1-1.863E-3 2.960E-2 -4.119E-3 -2.898E-3 3.065E-2 -2.993E-3 3.62E-4 GW 55 1 -2.898E-3 3.065E-2 -2.993E-3 -3.950E-3 3.126E-2 -1.573E-3 3.62E-4 GW 56 1 -3.950E-3 3.126E-2 -1.573E-3 -4.969E-3 3.137E-2 -1.279E-17 3.62E-4 GW 57 1 -4.969E-3 3.137E-2 -1.279E-17 -5.905E-3 3.095E-2 1.973E-3 3.62E-4 GW 58 1 -5.905E-3 3.095E-2 1.973E-3 -6.716E-3 3.005E-2 3.753E-3 3.62E-4

GW 59 1 -6.716E-3 3.005E-2 3.753E-3 -7.377E-3 2.873E-2 5.165E-3 3.62E-4 GW 60 1 -7.377E-3 2.873E-2 5.165E-3 -7.880E-3 2.712E-2 6.072E-3 3.62E-4 GW 61 1 -7.880E-3 2.712E-2 6.072E-3 -8.241E-3 2.536E-2 6.384E-3 3.62E-4 GW 62 1 -8.241E-3 2.536E-2 6.384E-3 -8.501E-3 2.361E-2 6.072E-3 3.62E-4 GW 63 1-8.501E-3 2.361E-2 6.072E-3 -8.716E-3 2.201E-2 5.165E-3 3.62E-4 GW 64 1 -8.716E-3 2.201E-2 5.165E-3 -8.956E-3 2.070E-2 3.753E-3 3.62E-4 GW 65 1 -8.956E-3 2.070E-2 3.753E-3 -9.294E-3 1.975E-2 1.973E-3 3.62E-4 GW 66 1 -9.294E-3 1.975E-2 1.973E-3 -9.796E-3 1.923E-2 -4.680E-18 3.62E-4 GW 67 1 -9.796E-3 1.923E-2 -4.680E-18 -1.052E-2 1.913E-2 -1.573E-3 3.62E-4 GW 68 1 -1.052E-2 1.913E-2 -1.573E-3 -1.148E-2 1.941E-2 -2.993E-3 3.62E-4 GW 69 1 -1.148E-2 1.941E-2 -2.993E-3 -1.269E-2 1.999E-2 -4.119E-3 3.62E-4 GW 70 1 -1.269E-2 1.999E-2 -4.119E-3 -1.411E-2 2.076E-2 -4.842E-3 3.62E-4 GW 71 1-1.411E-2 2.076E-2 -4.842E-3 -1.568E-2 2.158E-2 -5.091E-3 3.62E-4 GW 72 1-1.568E-2 2.158E-2 -5.091E-3 -1.731E-2 2.232E-2 -4.842E-3 3.62E-4 GW 73 1-1.731E-2 2.232E-2 -4.842E-3 -1.891E-2 2.286E-2 -4.119E-3 3.62E-4 GW 74 1-1.891E-2 2.286E-2 -4.119E-3 -2.036E-2 2.310E-2 -2.993E-3 3.62E-4 GW 75 1 -2.036E-2 2.310E-2 -2.993E-3 -2.157E-2 2.297E-2 -1.573E-3 3.62E-4 GW 76 1 -2.157E-2 2.297E-2 -1.573E-3 -2.246E-2 2.246E-2 -1.403E-17 3.62E-4 GW 77 1 -2.246E-2 2.246E-2 -1.403E-17 -2.297E-2 2.157E-2 1.973E-3 3.62E-4 GW 78 1 -2.297E-2 2.157E-2 1.973E-3 -2.310E-2 2.036E-2 3.753E-3 3.62E-4 GW 79 1 -2.310E-2 2.036E-2 3.753E-3 -2.286E-2 1.891E-2 5.165E-3 3.62E-4 GW 80 1 -2.286E-2 1.891E-2 5.165E-3 -2.232E-2 1.731E-2 6.072E-3 3.62E-4 GW 81 1 -2.232E-2 1.731E-2 6.072E-3 -2.158E-2 1.568E-2 6.384E-3 3.62E-4 GW 82 1-2.158E-2 1.568E-2 6.384E-3 -2.076E-2 1.411E-2 6.072E-3 3.62E-4 GW 83 1 -2.076E-2 1.411E-2 6.072E-3 -1.999E-2 1.269E-2 5.165E-3 3.62E-4 GW 84 1-1.999E-2 1.269E-2 5.165E-3 -1.941E-2 1.148E-2 3.753E-3 3.62E-4 GW 85 1 -1.941E-2 1.148E-2 3.753E-3 -1.913E-2 1.052E-2 1.973E-3 3.62E-4 GW 86 1-1.913E-2 1.052E-2 1.973E-3 -1.923E-2 9.796E-3 -3.433E-18 3.62E-4 GW 87 1-1.923E-2 9.796E-3 -3.433E-18 -1.975E-2 9.294E-3 -1.573E-3 3.62E-4 GW 88 1 -1.975E-2 9.294E-3 -1.573E-3 -2.070E-2 8.956E-3 -2.993E-3 3.62E-4 GW 89 1 -2.070E-2 8.956E-3 -2.993E-3 -2.201E-2 8.716E-3 -4.119E-3 3.62E-4 GW 90 1 -2.201E-2 8.716E-3 -4.119E-3 -2.361E-2 8.501E-3 -4.842E-3 3.62E-4

GW 91 1 -2.361E-2 8.501E-3 -4.842E-3 -2.536E-2 8.241E-3 -5.091E-3 3.62E-4 GW 92 1 -2.536E-2 8.241E-3 -5.091E-3 -2.712E-2 7.880E-3 -4.842E-3 3.62E-4 GW 93 1-2.712E-2 7.880E-3 -4.842E-3 -2.873E-2 7.377E-3 -4.119E-3 3.62E-4 GW 94 1 -2.873E-2 7.377E-3 -4.119E-3 -3.005E-2 6.716E-3 -2.993E-3 3.62E-4 GW 95 1 -3.005E-2 6.716E-3 -2.993E-3 -3.095E-2 5.905E-3 -1.573E-3 3.62E-4 GW 96 1 -3.095E-2 5.905E-3 -1.573E-3 -3.137E-2 4.969E-3 -1.528E-17 3.62E-4 GW 97 1-3.137E-2 4.969E-3 -1.528E-17 -3.126E-2 3.950E-3 1.973E-3 3.62E-4 GW 98 1 -3.126E-2 3.950E-3 1.973E-3 -3.065E-2 2.898E-3 3.753E-3 3.62E-4 GW 99 1 -3.065E-2 2.898E-3 3.753E-3 -2.960E-2 1.863E-3 5.165E-3 3.62E-4 GW 100 1 -2.960E-2 1.863E-3 5.165E-3 -2.823E-2 8.871E-4 6.072E-3 3.62E-4 GW 101 1 -2.823E-2 8.871E-4 6.072E-3 -2.667E-2 3.266E-18 6.384E-3 3.62E-4 GW 102 1 -2.667E-2 3.266E-18 6.384E-3 -2.508E-2 -7.883E-4 6.072E-3 3.62E-4 GW 103 1 -2.508E-2 -7.883E-4 6.072E-3 -2.363E-2 -1.487E-3 5.165E-3 3.62E-4 GW 104 1 -2.363E-2 -1.487E-3 5.165E-3 -2.245E-2 -2.122E-3 3.753E-3 3.62E-4 GW 105 1 -2.245E-2 -2.122E-3 3.753E-3 -2.166E-2 -2.736E-3 1.973E-3 3.62E-4 GW 106 1 -2.166E-2 -2.736E-3 1.973E-3 -2.131E-2 -3.376E-3 -2.186E-18 3.62E-4 GW 107 1 -2.131E-2 -3.376E-3 -2.186E-18 -2.144E-2 -4.090E-3 -1.573E-3 3.62E-4 GW 108 1 -2.144E-2 -4.090E-3 -1.573E-3 -2.201E-2 -4.919E-3 -2.993E-3 3.62E-4 GW 109 1 -2.201E-2 -4.919E-3 -2.993E-3 -2.293E-2 -5.888E-3 -4.119E-3 3.62E-4 GW 110 1 -2.293E-2 -5.888E-3 -4.119E-3 -2.410E-2 -7.002E-3 -4.842E-3 3.62E-4 GW 111 1 -2.410E-2 -7.002E-3 -4.842E-3 -2.536E-2 -8.241E-3 -5.091E-3 3.62E-4 GW 112 1 -2.536E-2 -8.241E-3 -5.091E-3 -2.657E-2 -9.567E-3 -4.842E-3 3.62E-4 GW 113 1 -2.657E-2 -9.567E-3 -4.842E-3 -2.758E-2 -1.092E-2 -4.119E-3 3.62E-4 GW 114 1 -2.758E-2 -1.092E-2 -4.119E-3 -2.826E-2 -1.223E-2 -2.993E-3 3.62E-4 GW 115 1 -2.826E-2 -1.223E-2 -2.993E-3 -2.851E-2 -1.342E-2 -1.573E-3 3.62E-4 GW 116 1 -2.851E-2 -1.342E-2 -1.573E-3 -2.830E-2 -1.442E-2 -1.653E-17 3.62E-4 GW 117 1 -2.830E-2 -1.442E-2 -1.653E-17 -2.761E-2 -1.518E-2 1.973E-3 3.62E-4 GW 118 1 -2.761E-2 -1.518E-2 1.973E-3 -2.650E-2 -1.567E-2 3.753E-3 3.62E-4 GW 119 1 -2.650E-2 -1.567E-2 3.753E-3 -2.505E-2 -1.589E-2 5.165E-3 3.62E-4 GW 120 1 -2.505E-2 -1.589E-2 5.165E-3 -2.336E-2 -1.588E-2 6.072E-3 3.62E-4 GW 121 1 -2.336E-2 -1.588E-2 6.072E-3 -2.158E-2 -1.568E-2 6.384E-3 3.62E-4 GW 122 1 -2.158E-2 -1.568E-2 6.384E-3 -1.983E-2 -1.538E-2 6.072E-3 3.62E-4

GW 123 1 -1.983E-2 -1.538E-2 6.072E-3 -1.824E-2 -1.509E-2 5.165E-3 3.62E-4 GW 124 1 -1.824E-2 -1.509E-2 5.165E-3 -1.692E-2 -1.491E-2 3.753E-3 3.62E-4 GW 125 1 -1.692E-2 -1.491E-2 3.753E-3 -1.591E-2 -1.494E-2 1.973E-3 3.62E-4 GW 126 1 -1.591E-2 -1.494E-2 1.973E-3 -1.526E-2 -1.526E-2 -9.387E-19 3.62E-4 GW 127 1 -1.526E-2 -1.526E-2 -9.387E-19 -1.494E-2 -1.591E-2 -1.573E-3 3.62E-4 GW 128 1 -1.494E-2 -1.591E-2 -1.573E-3 -1.491E-2 -1.692E-2 -2.993E-3 3.62E-4 GW 129 1 -1.491E-2 -1.692E-2 -2.993E-3 -1.509E-2 -1.824E-2 -4.119E-3 3.62E-4 GW 130 1 -1.509E-2 -1.824E-2 -4.119E-3 -1.538E-2 -1.983E-2 -4.842E-3 3.62E-4 GW 131 1 -1.538E-2 -1.983E-2 -4.842E-3 -1.568E-2 -2.158E-2 -5.091E-3 3.62E-4 GW 132 1 -1.568E-2 -2.158E-2 -5.091E-3 -1.588E-2 -2.336E-2 -4.842E-3 3.62E-4 GW 133 1 -1.588E-2 -2.336E-2 -4.842E-3 -1.589E-2 -2.505E-2 -4.119E-3 3.62E-4 GW 134 1 -1.589E-2 -2.505E-2 -4.119E-3 -1.567E-2 -2.650E-2 -2.993E-3 3.62E-4 GW 135 1 -1.567E-2 -2.650E-2 -2.993E-3 -1.518E-2 -2.761E-2 -1.573E-3 3.62E-4 GW 136 1 -1.518E-2 -2.761E-2 -1.573E-3 -1.442E-2 -2.830E-2 -1.777E-17 3.62E-4 GW 137 1 -1.442E-2 -2.830E-2 -1.777E-17 -1.342E-2 -2.851E-2 1.973E-3 3.62E-4 GW 138 1 -1.342E-2 -2.851E-2 1.973E-3 -1.223E-2 -2.826E-2 3.753E-3 3.62E-4 GW 139 1 -1.223E-2 -2.826E-2 3.753E-3 -1.092E-2 -2.758E-2 5.165E-3 3.62E-4 GW 140 1 -1.092E-2 -2.758E-2 5.165E-3 -9.567E-3 -2.657E-2 6.072E-3 3.62E-4 GW 141 1 -9.567E-3 -2.657E-2 6.072E-3 -8.241E-3 -2.536E-2 6.384E-3 3.62E-4 GW 142 1 -8.241E-3 -2.536E-2 6.384E-3 -7.002E-3 -2.410E-2 6.072E-3 3.62E-4 GW 143 1 -7.002E-3 -2.410E-2 6.072E-3 -5.888E-3 -2.293E-2 5.165E-3 3.62E-4 GW 144 1 -5.888E-3 -2.293E-2 5.165E-3 -4.919E-3 -2.201E-2 3.753E-3 3.62E-4 GW 145 1 -4.919E-3 -2.201E-2 3.753E-3 -4.090E-3 -2.144E-2 1.973E-3 3.62E-4 GW 146 1 -4.090E-3 -2.144E-2 1.973E-3 -3.376E-3 -2.131E-2 3.083E-19 3.62E-4 GW 147 1 -3.376E-3 -2.131E-2 3.083E-19 -2.736E-3 -2.166E-2 -1.573E-3 3.62E-4 GW 148 1 -2.736E-3 -2.166E-2 -1.573E-3 -2.122E-3 -2.245E-2 -2.993E-3 3.62E-4 GW 149 1 -2.122E-3 -2.245E-2 -2.993E-3 -1.487E-3 -2.363E-2 -4.119E-3 3.62E-4 GW 150 1 -1.487E-3 -2.363E-2 -4.119E-3 -7.883E-4 -2.508E-2 -4.842E-3 3.62E-4 GW 151 1 -7.883E-4 -2.508E-2 -4.842E-3 -4.899E-18 -2.667E-2 -5.091E-3 3.62E-4 GW 152 1 -4.899E-18 -2.667E-2 -5.091E-3 8.871E-4 -2.823E-2 -4.842E-3 3.62E-4 GW 153 1 8.871E-4 -2.823E-2 -4.842E-3 1.863E-3 -2.960E-2 -4.119E-3 3.62E-4 GW 154 1 1.863E-3 -2.960E-2 -4.119E-3 2.898E-3 -3.065E-2 -2.993E-3 3.62E-4

GW 155 1 2.898E-3 -3.065E-2 -2.993E-3 3.950E-3 -3.126E-2 -1.573E-3 3.62E-4 GW 156 1 3.950E-3 -3.126E-2 -1.573E-3 4.969E-3 -3.137E-2 -1.902E-17 3.62E-4 GW 157 1 4.969E-3 -3.137E-2 -1.902E-17 5.905E-3 -3.095E-2 1.973E-3 3.62E-4 GW 158 1 5.905E-3 -3.095E-2 1.973E-3 6.716E-3 -3.005E-2 3.753E-3 3.62E-4 GW 159 1 6.716E-3 -3.005E-2 3.753E-3 7.377E-3 -2.873E-2 5.165E-3 3.62E-4 GW 160 1 7.377E-3 -2.873E-2 5.165E-3 7.880E-3 -2.712E-2 6.072E-3 3.62E-4 GW 161 1 7.880E-3 -2.712E-2 6.072E-3 8.241E-3 -2.536E-2 6.384E-3 3.62E-4 GW 162 1 8.241E-3 -2.536E-2 6.384E-3 8.501E-3 -2.361E-2 6.072E-3 3.62E-4 GW 163 1 8.501E-3 -2.361E-2 6.072E-3 8.716E-3 -2.201E-2 5.165E-3 3.62E-4 GW 164 1 8.716E-3 -2.201E-2 5.165E-3 8.956E-3 -2.070E-2 3.753E-3 3.62E-4 GW 165 1 8.956E-3 -2.070E-2 3.753E-3 9.294E-3 -1.975E-2 1.973E-3 3.62E-4 GW 166 1 9.294E-3 -1.975E-2 1.973E-3 9.796E-3 -1.923E-2 1.555E-18 3.62E-4 GW 167 1 9.796E-3 -1.923E-2 1.555E-18 1.052E-2 -1.913E-2 -1.573E-3 3.62E-4 GW 168 1 1.052E-2 -1.913E-2 -1.573E-3 1.148E-2 -1.941E-2 -2.993E-3 3.62E-4 GW 169 1 1.148E-2 -1.941E-2 -2.993E-3 1.269E-2 -1.999E-2 -4.119E-3 3.62E-4 GW 170 1 1.269E-2 -1.999E-2 -4.119E-3 1.411E-2 -2.076E-2 -4.842E-3 3.62E-4 GW 171 1 1.411E-2 -2.076E-2 -4.842E-3 1.568E-2 -2.158E-2 -5.091E-3 3.62E-4 GW 172 1 1.568E-2 -2.158E-2 -5.091E-3 1.731E-2 -2.232E-2 -4.842E-3 3.62E-4 GW 173 1 1.731E-2 -2.232E-2 -4.842E-3 1.891E-2 -2.286E-2 -4.119E-3 3.62E-4 GW 174 1 1.891E-2 -2.286E-2 -4.119E-3 2.036E-2 -2.310E-2 -2.993E-3 3.62E-4 GW 175 1 2.036E-2 -2.310E-2 -2.993E-3 2.157E-2 -2.297E-2 -1.573E-3 3.62E-4 GW 176 1 2.157E-2 -2.297E-2 -1.573E-3 2.246E-2 -2.246E-2 -2.027E-17 3.62E-4 GW 177 1 2.246E-2 -2.246E-2 -2.027E-17 2.297E-2 -2.157E-2 1.973E-3 3.62E-4 GW 178 1 2.297E-2 -2.157E-2 1.973E-3 2.310E-2 -2.036E-2 3.753E-3 3.62E-4 GW 179 1 2.310E-2 -2.036E-2 3.753E-3 2.286E-2 -1.891E-2 5.165E-3 3.62E-4 GW 180 1 2.286E-2 -1.891E-2 5.165E-3 2.232E-2 -1.731E-2 6.072E-3 3.62E-4 GW 181 1 2.232E-2 -1.731E-2 6.072E-3 2.158E-2 -1.568E-2 6.384E-3 3.62E-4 GW 182 1 2.158E-2 -1.568E-2 6.384E-3 2.076E-2 -1.411E-2 6.072E-3 3.62E-4 GW 183 1 2.076E-2 -1.411E-2 6.072E-3 1.999E-2 -1.269E-2 5.165E-3 3.62E-4 GW 184 1 1.999E-2 -1.269E-2 5.165E-3 1.941E-2 -1.148E-2 3.753E-3 3.62E-4 GW 185 1 1.941E-2 -1.148E-2 3.753E-3 1.913E-2 -1.052E-2 1.973E-3 3.62E-4 GW 186 1 1.913E-2 -1.052E-2 1.973E-3 1.923E-2 -9.796E-3 2.802E-18 3.62E-4

GW 187 1 1.923E-2 -9.796E-3 2.802E-18 1.975E-2 -9.294E-3 -1.573E-3 3.62E-4 GW 188 1 1.975E-2 -9.294E-3 -1.573E-3 2.070E-2 -8.956E-3 -2.993E-3 3.62E-4 GW 189 1 2.070E-2 -8.956E-3 -2.993E-3 2.201E-2 -8.716E-3 -4.119E-3 3.62E-4 GW 190 1 2.201E-2 -8.716E-3 -4.119E-3 2.361E-2 -8.501E-3 -4.842E-3 3.62E-4 GW 191 1 2.361E-2 -8.501E-3 -4.842E-3 2.536E-2 -8.241E-3 -5.091E-3 3.62E-4 GW 192 1 2.536E-2 -8.241E-3 -5.091E-3 2.712E-2 -7.880E-3 -4.842E-3 3.62E-4 GW 193 1 2.712E-2 -7.880E-3 -4.842E-3 2.873E-2 -7.377E-3 -4.119E-3 3.62E-4 GW 194 1 2.873E-2 -7.377E-3 -4.119E-3 3.005E-2 -6.716E-3 -2.993E-3 3.62E-4 GW 195 1 3.005E-2 -6.716E-3 -2.993E-3 3.095E-2 -5.905E-3 -1.573E-3 3.62E-4 GW 196 1 3.095E-2 -5.905E-3 -1.573E-3 3.137E-2 -4.969E-3 -2.151E-17 3.62E-4 GW 197 1 3.137E-2 -4.969E-3 -2.151E-17 3.126E-2 -3.950E-3 1.573E-3 3.62E-4 GW 198 1 3.126E-2 -3.950E-3 1.573E-3 3.065E-2 -2.898E-3 2.993E-3 3.62E-4 GW 199 1 3.065E-2 -2.898E-3 2.993E-3 2.960E-2 -1.863E-3 4.119E-3 3.62E-4 GW 200 1 2.960E-2 -1.863E-3 4.119E-3 2.823E-2 -8.871E-4 4.842E-3 3.62E-4 GW 201 1 2.823E-2 -8.871E-4 4.842E-3 2.747E-2 0.000E+0 5.091E-3 3.62E-4 GW 202 1 2.747E-2 0.000E+0 5.091E-3 2.823E-2 8.871E-4 4.842E-3 3.62E-4 GW 203 1 2.823E-2 8.871E-4 4.842E-3 2.960E-2 1.863E-3 4.119E-3 3.62E-4 GW 204 1 2.960E-2 1.863E-3 4.119E-3 3.065E-2 2.898E-3 2.993E-3 3.62E-4 GW 205 1 3.065E-2 2.898E-3 2.993E-3 3.126E-2 3.950E-3 1.573E-3 3.62E-4 GW 206 1 3.126E-2 3.950E-3 1.573E-3 3.137E-2 4.969E-3 -5.266E-36 3.62E-4 GW 207 1 3.137E-2 4.969E-3 -5.266E-36 3.095E-2 5.905E-3 -1.973E-3 3.62E-4 GW 208 1 3.095E-2 5.905E-3 -1.973E-3 3.005E-2 6.716E-3 -3.753E-3 3.62E-4 GW 209 1 3.005E-2 6.716E-3 -3.753E-3 2.873E-2 7.377E-3 -5.165E-3 3.62E-4 GW 210 1 2.873E-2 7.377E-3 -5.165E-3 2.712E-2 7.880E-3 -6.072E-3 3.62E-4 GW 211 1 2.712E-2 7.880E-3 -6.072E-3 2.536E-2 8.241E-3 -6.384E-3 3.62E-4 GW 212 1 2.536E-2 8.241E-3 -6.384E-3 2.361E-2 8.501E-3 -6.072E-3 3.62E-4 GW 213 1 2.361E-2 8.501E-3 -6.072E-3 2.201E-2 8.716E-3 -5.165E-3 3.62E-4 GW 214 1 2.201E-2 8.716E-3 -5.165E-3 2.070E-2 8.956E-3 -3.753E-3 3.62E-4 GW 215 1 2.070E-2 8.956E-3 -3.753E-3 1.975E-2 9.294E-3 -1.973E-3 3.62E-4 GW 216 1 1.975E-2 9.294E-3 -1.973E-3 1.923E-2 9.796E-3 -6.235E-19 3.62E-4 GW 217 1 1.923E-2 9.796E-3 -6.235E-19 1.913E-2 1.052E-2 1.573E-3 3.62E-4 GW 218 1 1.913E-2 1.052E-2 1.573E-3 1.941E-2 1.148E-2 2.993E-3 3.62E-4

GW 219 1 1.941E-2 1.148E-2 2.993E-3 1.999E-2 1.269E-2 4.119E-3 3.62E-4 GW 220 1 1.999E-2 1.269E-2 4.119E-3 2.076E-2 1.411E-2 4.842E-3 3.62E-4 GW 221 1 2.076E-2 1.411E-2 4.842E-3 2.158E-2 1.568E-2 5.091E-3 3.62E-4 GW 222 1 2.158E-2 1.568E-2 5.091E-3 2.232E-2 1.731E-2 4.842E-3 3.62E-4 GW 223 1 2.232E-2 1.731E-2 4.842E-3 2.286E-2 1.891E-2 4.119E-3 3.62E-4 GW 224 1 2.286E-2 1.891E-2 4.119E-3 2.310E-2 2.036E-2 2.993E-3 3.62E-4 GW 225 1 2.310E-2 2.036E-2 2.993E-3 2.297E-2 2.157E-2 1.573E-3 3.62E-4 GW 226 1 2.297E-2 2.157E-2 1.573E-3 2.246E-2 2.246E-2 1.247E-18 3.62E-4 GW 227 1 2.246E-2 2.246E-2 1.247E-18 2.157E-2 2.297E-2 -1.973E-3 3.62E-4 GW 228 1 2.157E-2 2.297E-2 -1.973E-3 2.036E-2 2.310E-2 -3.753E-3 3.62E-4 GW 229 1 2.036E-2 2.310E-2 -3.753E-3 1.891E-2 2.286E-2 -5.165E-3 3.62E-4 GW 230 1 1.891E-2 2.286E-2 -5.165E-3 1.731E-2 2.232E-2 -6.072E-3 3.62E-4 GW 231 1 1.731E-2 2.232E-2 -6.072E-3 1.568E-2 2.158E-2 -6.384E-3 3.62E-4 GW 232 1 1.568E-2 2.158E-2 -6.384E-3 1.411E-2 2.076E-2 -6.072E-3 3.62E-4 GW 233 1 1.411E-2 2.076E-2 -6.072E-3 1.269E-2 1.999E-2 -5.165E-3 3.62E-4 GW 234 1 1.269E-2 1.999E-2 -5.165E-3 1.148E-2 1.941E-2 -3.753E-3 3.62E-4 GW 235 1 1.148E-2 1.941E-2 -3.753E-3 1.052E-2 1.913E-2 -1.973E-3 3.62E-4 GW 236 1 1.052E-2 1.913E-2 -1.973E-3 9.796E-3 1.923E-2 -1.870E-18 3.62E-4 GW 237 1 9.796E-3 1.923E-2 -1.870E-18 9.294E-3 1.975E-2 1.573E-3 3.62E-4 GW 238 1 9.294E-3 1.975E-2 1.573E-3 8.956E-3 2.070E-2 2.993E-3 3.62E-4 GW 239 1 8.956E-3 2.070E-2 2.993E-3 8.716E-3 2.201E-2 4.119E-3 3.62E-4 GW 240 1 8.716E-3 2.201E-2 4.119E-3 8.501E-3 2.361E-2 4.842E-3 3.62E-4 GW 241 1 8.501E-3 2.361E-2 4.842E-3 8.241E-3 2.536E-2 5.091E-3 3.62E-4 GW 242 1 8.241E-3 2.536E-2 5.091E-3 7.880E-3 2.712E-2 4.842E-3 3.62E-4 GW 243 1 7.880E-3 2.712E-2 4.842E-3 7.377E-3 2.873E-2 4.119E-3 3.62E-4 GW 244 1 7.377E-3 2.873E-2 4.119E-3 6.716E-3 3.005E-2 2.993E-3 3.62E-4 GW 245 1 6.716E-3 3.005E-2 2.993E-3 5.905E-3 3.095E-2 1.573E-3 3.62E-4 GW 246 1 5.905E-3 3.095E-2 1.573E-3 4.969E-3 3.137E-2 2.494E-18 3.62E-4 GW 247 1 4.969E-3 3.137E-2 2.494E-18 3.950E-3 3.126E-2 -1.973E-3 3.62E-4 GW 248 1 3.950E-3 3.126E-2 -1.973E-3 2.898E-3 3.065E-2 -3.753E-3 3.62E-4 GW 249 1 2.898E-3 3.065E-2 -3.753E-3 1.863E-3 2.960E-2 -5.165E-3 3.62E-4 GW 250 1 1.863E-3 2.960E-2 -5.165E-3 8.871E-4 2.823E-2 -6.072E-3 3.62E-4

GW 251 1 8.871E-4 2.823E-2 -6.072E-3 1.633E-18 2.667E-2 -6.384E-3 3.62E-4 GW 252 1 1.633E-18 2.667E-2 -6.384E-3 -7.883E-4 2.508E-2 -6.072E-3 3.62E-4 GW 253 1 -7.883E-4 2.508E-2 -6.072E-3 -1.487E-3 2.363E-2 -5.165E-3 3.62E-4 GW 254 1 -1.487E-3 2.363E-2 -5.165E-3 -2.122E-3 2.245E-2 -3.753E-3 3.62E-4 GW 255 1 -2.122E-3 2.245E-2 -3.753E-3 -2.736E-3 2.166E-2 -1.973E-3 3.62E-4 GW 256 1 -2.736E-3 2.166E-2 -1.973E-3 -3.376E-3 2.131E-2 -1.216E-17 3.62E-4 GW 257 1 -3.376E-3 2.131E-2 -1.216E-17 -4.090E-3 2.144E-2 1.573E-3 3.62E-4 GW 258 1 -4.090E-3 2.144E-2 1.573E-3 -4.919E-3 2.201E-2 2.993E-3 3.62E-4 GW 259 1 -4.919E-3 2.201E-2 2.993E-3 -5.888E-3 2.293E-2 4.119E-3 3.62E-4 GW 260 1 -5.888E-3 2.293E-2 4.119E-3 -7.002E-3 2.410E-2 4.842E-3 3.62E-4 GW 261 1 -7.002E-3 2.410E-2 4.842E-3 -8.241E-3 2.536E-2 5.091E-3 3.62E-4 GW 262 1 -8.241E-3 2.536E-2 5.091E-3 -9.567E-3 2.657E-2 4.842E-3 3.62E-4 GW 263 1 -9.567E-3 2.657E-2 4.842E-3 -1.092E-2 2.758E-2 4.119E-3 3.62E-4 GW 264 1 -1.092E-2 2.758E-2 4.119E-3 -1.223E-2 2.826E-2 2.993E-3 3.62E-4 GW 265 1 -1.223E-2 2.826E-2 2.993E-3 -1.342E-2 2.851E-2 1.573E-3 3.62E-4 GW 266 1 -1.342E-2 2.851E-2 1.573E-3 -1.442E-2 2.830E-2 -5.303E-18 3.62E-4 GW 267 1 -1.442E-2 2.830E-2 -5.303E-18 -1.518E-2 2.761E-2 -1.973E-3 3.62E-4 GW 268 1 -1.518E-2 2.761E-2 -1.973E-3 -1.567E-2 2.650E-2 -3.753E-3 3.62E-4 GW 269 1 -1.567E-2 2.650E-2 -3.753E-3 -1.589E-2 2.505E-2 -5.165E-3 3.62E-4 GW 270 1 -1.589E-2 2.505E-2 -5.165E-3 -1.588E-2 2.336E-2 -6.072E-3 3.62E-4 GW 271 1 -1.588E-2 2.336E-2 -6.072E-3 -1.568E-2 2.158E-2 -6.384E-3 3.62E-4 GW 272 1 -1.568E-2 2.158E-2 -6.384E-3 -1.538E-2 1.983E-2 -6.072E-3 3.62E-4 GW 273 1 -1.538E-2 1.983E-2 -6.072E-3 -1.509E-2 1.824E-2 -5.165E-3 3.62E-4 GW 274 1 -1.509E-2 1.824E-2 -5.165E-3 -1.491E-2 1.692E-2 -3.753E-3 3.62E-4 GW 275 1 -1.491E-2 1.692E-2 -3.753E-3 -1.494E-2 1.591E-2 -1.973E-3 3.62E-4 GW 276 1 -1.494E-2 1.591E-2 -1.973E-3 -1.526E-2 1.526E-2 -1.341E-17 3.62E-4 GW 277 1 -1.526E-2 1.526E-2 -1.341E-17 -1.591E-2 1.494E-2 1.573E-3 3.62E-4 GW 278 1 -1.591E-2 1.494E-2 1.573E-3 -1.692E-2 1.491E-2 2.993E-3 3.62E-4 GW 279 1 -1.692E-2 1.491E-2 2.993E-3 -1.824E-2 1.509E-2 4.119E-3 3.62E-4 GW 280 1 -1.824E-2 1.509E-2 4.119E-3 -1.983E-2 1.538E-2 4.842E-3 3.62E-4 GW 281 1 -1.983E-2 1.538E-2 4.842E-3 -2.158E-2 1.568E-2 5.091E-3 3.62E-4 GW 282 1 -2.158E-2 1.568E-2 5.091E-3 -2.336E-2 1.588E-2 4.842E-3 3.62E-4

GW 283 1 -2.336E-2 1.588E-2 4.842E-3 -2.505E-2 1.589E-2 4.119E-3 3.62E-4 GW 284 1 -2.505E-2 1.589E-2 4.119E-3 -2.650E-2 1.567E-2 2.993E-3 3.62E-4 GW 285 1 -2.650E-2 1.567E-2 2.993E-3 -2.761E-2 1.518E-2 1.573E-3 3.62E-4 GW 286 1 -2.761E-2 1.518E-2 1.573E-3 -2.830E-2 1.442E-2 -4.056E-18 3.62E-4 GW 287 1 -2.830E-2 1.442E-2 -4.056E-18 -2.851E-2 1.342E-2 -1.973E-3 3.62E-4 GW 288 1 -2.851E-2 1.342E-2 -1.973E-3 -2.826E-2 1.223E-2 -3.753E-3 3.62E-4 GW 289 1 -2.826E-2 1.223E-2 -3.753E-3 -2.758E-2 1.092E-2 -5.165E-3 3.62E-4 GW 290 1 -2.758E-2 1.092E-2 -5.165E-3 -2.657E-2 9.567E-3 -6.072E-3 3.62E-4 GW 291 1 -2.657E-2 9.567E-3 -6.072E-3 -2.536E-2 8.241E-3 -6.384E-3 3.62E-4 GW 292 1 -2.536E-2 8.241E-3 -6.384E-3 -2.410E-2 7.002E-3 -6.072E-3 3.62E-4 GW 293 1 -2.410E-2 7.002E-3 -6.072E-3 -2.293E-2 5.888E-3 -5.165E-3 3.62E-4 GW 294 1 -2.293E-2 5.888E-3 -5.165E-3 -2.201E-2 4.919E-3 -3.753E-3 3.62E-4 GW 295 1 -2.201E-2 4.919E-3 -3.753E-3 -2.144E-2 4.090E-3 -1.973E-3 3.62E-4 GW 296 1 -2.144E-2 4.090E-3 -1.973E-3 -2.131E-2 3.376E-3 -1.466E-17 3.62E-4 GW 297 1 -2.131E-2 3.376E-3 -1.466E-17 -2.166E-2 2.736E-3 1.573E-3 3.62E-4 GW 298 1 -2.166E-2 2.736E-3 1.573E-3 -2.245E-2 2.122E-3 2.993E-3 3.62E-4 GW 299 1 -2.245E-2 2.122E-3 2.993E-3 -2.363E-2 1.487E-3 4.119E-3 3.62E-4 GW 300 1 -2.363E-2 1.487E-3 4.119E-3 -2.508E-2 7.883E-4 4.842E-3 3.62E-4 GW 301 1 -2.508E-2 7.883E-4 4.842E-3 -2.667E-2 3.266E-18 5.091E-3 3.62E-4 GW 302 1 -2.667E-2 3.266E-18 5.091E-3 -2.823E-2 -8.871E-4 4.842E-3 3.62E-4 GW 303 1 -2.823E-2 -8.871E-4 4.842E-3 -2.960E-2 -1.863E-3 4.119E-3 3.62E-4 GW 304 1 -2.960E-2 -1.863E-3 4.119E-3 -3.065E-2 -2.898E-3 2.993E-3 3.62E-4 GW 305 1 -3.065E-2 -2.898E-3 2.993E-3 -3.126E-2 -3.950E-3 1.573E-3 3.62E-4 GW 306 1 -3.126E-2 -3.950E-3 1.573E-3 -3.137E-2 -4.969E-3 -2.809E-18 3.62E-4 GW 307 1 -3.137E-2 -4.969E-3 -2.809E-18 -3.095E-2 -5.905E-3 -1.973E-3 3.62E-4 GW 308 1 -3.095E-2 -5.905E-3 -1.973E-3 -3.005E-2 -6.716E-3 -3.753E-3 3.62E-4 GW 309 1 -3.005E-2 -6.716E-3 -3.753E-3 -2.873E-2 -7.377E-3 -5.165E-3 3.62E-4 GW 310 1 -2.873E-2 -7.377E-3 -5.165E-3 -2.712E-2 -7.880E-3 -6.072E-3 3.62E-4 GW 311 1 -2.712E-2 -7.880E-3 -6.072E-3 -2.536E-2 -8.241E-3 -6.384E-3 3.62E-4 GW 312 1 -2.536E-2 -8.241E-3 -6.384E-3 -2.361E-2 -8.501E-3 -6.072E-3 3.62E-4 GW 313 1 -2.361E-2 -8.501E-3 -6.072E-3 -2.201E-2 -8.716E-3 -5.165E-3 3.62E-4 GW 314 1 -2.201E-2 -8.716E-3 -5.165E-3 -2.070E-2 -8.956E-3 -3.753E-3 3.62E-4

GW 315 1 -2.070E-2 -8.956E-3 -3.753E-3 -1.975E-2 -9.294E-3 -1.973E-3 3.62E-4 GW 316 1 -1.975E-2 -9.294E-3 -1.973E-3 -1.923E-2 -9.796E-3 -1.590E-17 3.62E-4 GW 317 1 -1.923E-2 -9.796E-3 -1.590E-17 -1.913E-2 -1.052E-2 1.573E-3 3.62E-4 GW 318 1 -1.913E-2 -1.052E-2 1.573E-3 -1.941E-2 -1.148E-2 2.993E-3 3.62E-4 GW 319 1 -1.941E-2 -1.148E-2 2.993E-3 -1.999E-2 -1.269E-2 4.119E-3 3.62E-4 GW 320 1 -1.999E-2 -1.269E-2 4.119E-3 -2.076E-2 -1.411E-2 4.842E-3 3.62E-4 GW 321 1 -2.076E-2 -1.411E-2 4.842E-3 -2.158E-2 -1.568E-2 5.091E-3 3.62E-4 GW 322 1 -2.158E-2 -1.568E-2 5.091E-3 -2.232E-2 -1.731E-2 4.842E-3 3.62E-4 GW 323 1 -2.232E-2 -1.731E-2 4.842E-3 -2.286E-2 -1.891E-2 4.119E-3 3.62E-4 GW 324 1 -2.286E-2 -1.891E-2 4.119E-3 -2.310E-2 -2.036E-2 2.993E-3 3.62E-4 GW 325 1 -2.310E-2 -2.036E-2 2.993E-3 -2.297E-2 -2.157E-2 1.573E-3 3.62E-4 GW 326 1 -2.297E-2 -2.157E-2 1.573E-3 -2.246E-2 -2.246E-2 -1.562E-18 3.62E-4 GW 327 1 -2.246E-2 -2.246E-2 -1.562E-18 -2.157E-2 -2.297E-2 -1.973E-3 3.62E-4 GW 328 1 -2.157E-2 -2.297E-2 -1.973E-3 -2.036E-2 -2.310E-2 -3.753E-3 3.62E-4 GW 329 1 -2.036E-2 -2.310E-2 -3.753E-3 -1.891E-2 -2.286E-2 -5.165E-3 3.62E-4 GW 330 1 -1.891E-2 -2.286E-2 -5.165E-3 -1.731E-2 -2.232E-2 -6.072E-3 3.62E-4 GW 331 1 -1.731E-2 -2.232E-2 -6.072E-3 -1.568E-2 -2.158E-2 -6.384E-3 3.62E-4 GW 332 1 -1.568E-2 -2.158E-2 -6.384E-3 -1.411E-2 -2.076E-2 -6.072E-3 3.62E-4 GW 333 1 -1.411E-2 -2.076E-2 -6.072E-3 -1.269E-2 -1.999E-2 -5.165E-3 3.62E-4 GW 334 1 -1.269E-2 -1.999E-2 -5.165E-3 -1.148E-2 -1.941E-2 -3.753E-3 3.62E-4 GW 335 1 -1.148E-2 -1.941E-2 -3.753E-3 -1.052E-2 -1.913E-2 -1.973E-3 3.62E-4 GW 336 1 -1.052E-2 -1.913E-2 -1.973E-3 -9.796E-3 -1.923E-2 -1.715E-17 3.62E-4 GW 337 1 -9.796E-3 -1.923E-2 -1.715E-17 -9.294E-3 -1.975E-2 1.573E-3 3.62E-4 GW 338 1 -9.294E-3 -1.975E-2 1.573E-3 -8.956E-3 -2.070E-2 2.993E-3 3.62E-4 GW 339 1 -8.956E-3 -2.070E-2 2.993E-3 -8.716E-3 -2.201E-2 4.119E-3 3.62E-4 GW 340 1 -8.716E-3 -2.201E-2 4.119E-3 -8.501E-3 -2.361E-2 4.842E-3 3.62E-4 GW 341 1 -8.501E-3 -2.361E-2 4.842E-3 -8.241E-3 -2.536E-2 5.091E-3 3.62E-4 GW 342 1 -8.241E-3 -2.536E-2 5.091E-3 -7.880E-3 -2.712E-2 4.842E-3 3.62E-4 GW 343 1 -7.880E-3 -2.712E-2 4.842E-3 -7.377E-3 -2.873E-2 4.119E-3 3.62E-4 GW 344 1 -7.377E-3 -2.873E-2 4.119E-3 -6.716E-3 -3.005E-2 2.993E-3 3.62E-4 GW 345 1 -6.716E-3 -3.005E-2 2.993E-3 -5.905E-3 -3.095E-2 1.573E-3 3.62E-4 GW 346 1 -5.905E-3 -3.095E-2 1.573E-3 -4.969E-3 -3.137E-2 -3.152E-19 3.62E-4

GW 347 1 -4.969E-3 -3.137E-2 -3.152E-19 -3.950E-3 -3.126E-2 -1.973E-3 3.62E-4 GW 348 1 -3.950E-3 -3.126E-2 -1.973E-3 -2.898E-3 -3.065E-2 -3.753E-3 3.62E-4 GW 349 1 -2.898E-3 -3.065E-2 -3.753E-3 -1.863E-3 -2.960E-2 -5.165E-3 3.62E-4 GW 350 1 -1.863E-3 -2.960E-2 -5.165E-3 -8.871E-4 -2.823E-2 -6.072E-3 3.62E-4 GW 351 1 -8.871E-4 -2.823E-2 -6.072E-3 -4.899E-18 -2.667E-2 -6.384E-3 3.62E-4 GW 352 1 -4.899E-18 -2.667E-2 -6.384E-3 7.883E-4 -2.508E-2 -6.072E-3 3.62E-4 GW 353 1 7.883E-4 -2.508E-2 -6.072E-3 1.487E-3 -2.363E-2 -5.165E-3 3.62E-4 GW 354 1 1.487E-3 -2.363E-2 -5.165E-3 2.122E-3 -2.245E-2 -3.753E-3 3.62E-4 GW 355 1 2.122E-3 -2.245E-2 -3.753E-3 2.736E-3 -2.166E-2 -1.973E-3 3.62E-4 GW 356 1 2.736E-3 -2.166E-2 -1.973E-3 3.376E-3 -2.131E-2 -1.840E-17 3.62E-4 GW 357 1 3.376E-3 -2.131E-2 -1.840E-17 4.090E-3 -2.144E-2 1.573E-3 3.62E-4 GW 358 1 4.090E-3 -2.144E-2 1.573E-3 4.919E-3 -2.201E-2 2.993E-3 3.62E-4 GW 359 1 4.919E-3 -2.201E-2 2.993E-3 5.888E-3 -2.293E-2 4.119E-3 3.62E-4 GW 360 1 5.888E-3 -2.293E-2 4.119E-3 7.002E-3 -2.410E-2 4.842E-3 3.62E-4 GW 361 1 7.002E-3 -2.410E-2 4.842E-3 8.241E-3 -2.536E-2 5.091E-3 3.62E-4 GW 362 1 8.241E-3 -2.536E-2 5.091E-3 9.567E-3 -2.657E-2 4.842E-3 3.62E-4 GW 363 1 9.567E-3 -2.657E-2 4.842E-3 1.092E-2 -2.758E-2 4.119E-3 3.62E-4 GW 364 1 1.092E-2 -2.758E-2 4.119E-3 1.223E-2 -2.826E-2 2.993E-3 3.62E-4 GW 365 1 1.223E-2 -2.826E-2 2.993E-3 1.342E-2 -2.851E-2 1.573E-3 3.62E-4 GW 366 1 1.342E-2 -2.851E-2 1.573E-3 1.442E-2 -2.830E-2 9.318E-19 3.62E-4 GW 367 1 1.442E-2 -2.830E-2 9.318E-19 1.518E-2 -2.761E-2 -1.973E-3 3.62E-4 GW 368 1 1.518E-2 -2.761E-2 -1.973E-3 1.567E-2 -2.650E-2 -3.753E-3 3.62E-4 GW 369 1 1.567E-2 -2.650E-2 -3.753E-3 1.589E-2 -2.505E-2 -5.165E-3 3.62E-4 GW 370 1 1.589E-2 -2.505E-2 -5.165E-3 1.588E-2 -2.336E-2 -6.072E-3 3.62E-4 GW 371 1 1.588E-2 -2.336E-2 -6.072E-3 1.568E-2 -2.158E-2 -6.384E-3 3.62E-4 GW 372 1 1.568E-2 -2.158E-2 -6.384E-3 1.538E-2 -1.983E-2 -6.072E-3 3.62E-4 GW 373 1 1.538E-2 -1.983E-2 -6.072E-3 1.509E-2 -1.824E-2 -5.165E-3 3.62E-4 GW 374 1 1.509E-2 -1.824E-2 -5.165E-3 1.491E-2 -1.692E-2 -3.753E-3 3.62E-4 GW 375 1 1.491E-2 -1.692E-2 -3.753E-3 1.494E-2 -1.591E-2 -1.973E-3 3.62E-4 GW 376 1 1.494E-2 -1.591E-2 -1.973E-3 1.526E-2 -1.526E-2 -1.964E-17 3.62E-4 GW 377 1 1.526E-2 -1.526E-2 -1.964E-17 1.591E-2 -1.494E-2 1.573E-3 3.62E-4 GW 378 1 1.591E-2 -1.494E-2 1.573E-3 1.692E-2 -1.491E-2 2.993E-3 3.62E-4

GW 379 1 1.692E-2 -1.491E-2 2.993E-3 1.824E-2 -1.509E-2 4.119E-3 3.62E-4 GW 380 1 1.824E-2 -1.509E-2 4.119E-3 1.983E-2 -1.538E-2 4.842E-3 3.62E-4 GW 381 1 1.983E-2 -1.538E-2 4.842E-3 2.158E-2 -1.568E-2 5.091E-3 3.62E-4 GW 382 1 2.158E-2 -1.568E-2 5.091E-3 2.336E-2 -1.588E-2 4.842E-3 3.62E-4 GW 383 1 2.336E-2 -1.588E-2 4.842E-3 2.505E-2 -1.589E-2 4.119E-3 3.62E-4 GW 384 1 2.505E-2 -1.589E-2 4.119E-3 2.650E-2 -1.567E-2 2.993E-3 3.62E-4 GW 385 1 2.650E-2 -1.567E-2 2.993E-3 2.761E-2 -1.518E-2 1.573E-3 3.62E-4 GW 386 1 2.761E-2 -1.518E-2 1.573E-3 2.830E-2 -1.442E-2 2.179E-18 3.62E-4 GW 387 1 2.830E-2 -1.442E-2 2.179E-18 2.851E-2 -1.342E-2 -1.973E-3 3.62E-4 GW 388 1 2.851E-2 -1.342E-2 -1.973E-3 2.826E-2 -1.223E-2 -3.753E-3 3.62E-4 GW 389 1 2.826E-2 -1.223E-2 -3.753E-3 2.758E-2 -1.092E-2 -5.165E-3 3.62E-4 GW 390 1 2.758E-2 -1.092E-2 -5.165E-3 2.657E-2 -9.567E-3 -6.072E-3 3.62E-4 GW 391 1 2.657E-2 -9.567E-3 -6.072E-3 2.536E-2 -8.241E-3 -6.384E-3 3.62E-4 GW 392 1 2.536E-2 -8.241E-3 -6.384E-3 2.410E-2 -7.002E-3 -6.072E-3 3.62E-4 GW 393 1 2.410E-2 -7.002E-3 -6.072E-3 2.293E-2 -5.888E-3 -5.165E-3 3.62E-4 GW 394 1 2.293E-2 -5.888E-3 -5.165E-3 2.201E-2 -4.919E-3 -3.753E-3 3.62E-4 GW 395 1 2.201E-2 -4.919E-3 -3.753E-3 2.144E-2 -4.090E-3 -1.973E-3 3.62E-4 GW 396 1 2.144E-2 -4.090E-3 -1.973E-3 2.131E-2 -3.376E-3 -2.089E-17 3.62E-4 GW 397 1 2.131E-2 -3.376E-3 -2.089E-17 2.166E-2 -2.736E-3 1.573E-3 3.62E-4 GW 398 1 2.166E-2 -2.736E-3 1.573E-3 2.245E-2 -2.122E-3 2.993E-3 3.62E-4 GW 399 1 2.245E-2 -2.122E-3 2.993E-3 2.363E-2 -1.487E-3 4.119E-3 3.62E-4 GW 400 1 2.363E-2 -1.487E-3 4.119E-3 2.508E-2 -7.883E-4 4.842E-3 3.62E-4 GW 401 1 2.508E-2 -7.883E-4 4.842E-3 2.587E-2 0.000E+0 5.091E-3 3.62E-4 GM 0 0 0 0 0 0 0 0 0.005699 0 0 0 0 SM 20 20 4.5720E-1 -4.5720E-1 0 4.5720E-1 4.5720E-1 0 SC 0 0 -4.5720E-1 4.5720E-1 0 GE 0 0 GN -1 0 0 0 0.000 0.000 LD 5 0 0 0 5.8E7 EX 0 1 2 0 1.000 0 FR 0 1 0 0 917.21 0

RP 0 1 1 1001 0.0 0.0 5.0 5.0 0.0

2. The NEC Cards for Modeling the Vertical Dipole at 1 mm above the 3ft x 3ft Metal

Plate

GW 1 3 0 0 0.06375 0 0 0.07975 1.016E-3 GW 1 5 0 0 0 0 0 0.06375 1.016E-3 GW 1 5 0 0 0.07975 0 0 0.1435 1.016E-3 GM 0 0 0 0 0 0 0 0 0.001 0 1 0 13 SM 20 20 4.5720E-1 -4.5720E-1 0 4.5720E-1 4.5720E-1 0 SC 0 0 -4.5720E-1 4.5720E-1 0 GE 0 GN -1 0 0 0 0 0 0 0 0 0 0 LD 5 0 0 0 58000000 0 0 0 0 0 EX 0 1 2 0 1 0 0 0 0 0 FR 0 1 0 0 971 0 0 0 0 0 RP 0 1 1 1001 0 0 5 5 0 0 EN

3. The NEC Cards for Modeling the Horizontal Dipole at 1 mm above the 3ft x 3ft Metal

Plate

GW 1 3 0 1.594E-2 0 0 -1.594E-2 0 1.016E-3 GW 1 5 0 1.594E-2 0 0 7.175E-2 0 1.016E-3 GW 1 5 0 -1.594E-2 0 0 -7.175E-2 0 1.016E-3 GM 0 0 0 0 0 0 0 0 0.002016 0 1 0 13 SM 20 20 4.5720E-1 -4.5720E-1 0 4.5720E-1 4.5720E-1 0 SC 0 0 -4.5720E-1 4.5720E-1 0 GE 0 GN -1 0 0 0 0 0 0 0 0 0 0 LD 5 0 0 0 58000000 0 0 0 0 0 EX 0 1 2 0 1 0 0 0 0 0 FR 0 1 0 0 971 0 0 0 0 0 RP 0 1 1 1001 0 0 5 5 0 0 EN

4. The NEC Cards for Modeling the Horizontal Loop at 1 mm above the 3ft x 3ft Metal

Plate

GA 1 3 0.04978 -5 5 5.206E-4 GA 4 25 0.04978 5 355 5.206E-4 GM 0 0 90 0 0 0 0 1.5206E-3 0 1 0 28 SM 20 20 4.5720E-1 -4.5720E-1 0 4.5720E-1 4.5720E-1 0 SC 0 0 -4.5720E-1 4.5720E-1 0 GE 0 GN -1 0 0 0 0 0 0 0 0 0 0 LD 5 0 0 0 58000000 0 0 0 0 0 EX 0 1 2 0 1 0 0 0 0 0 FR 0 1 0 0 1035 0 0 0 0 0 RP 0 1 1 1001 0 0 5 5 0 0 EN

Appendix B Plain Surface Generator

🐂 plain_form		
Patch Surface	C Wire-Grid Surface	Tag Number of First Segment
Data Files for Generating Plain Surface		NEC File of Plain Surface
C Keypoint Data File	● Grid Data File	C:\users\tao\PlayVB\sur_generator\da
C:\users\tao\PlayVB\sur_generator\	C:\users\tao\PlayVB\sur_generator	psur2.nec sur1.nec
C:\ Susers Tao PlayVB Sur_generator Atafile	kf1.dat kf2.dat pgf1.dat pgf3.dat wgf1.dat wgf2.dat wgf2.dat	sur2.nec wsur1.nec wsur2.nec
Generating Keypoint Data File	Generating Grid Data File	Generating Surface

Figure 34 Plain_form

This form is used when the keypoint data file and the grid data file have been prepared. Two kinds of surfaces can be constructed; one is a patch surface, and the other is a wire-grid surface. For a wire-grid surface, the tag number of the first wire segment can be defined by user. With the keypoint data file and grid data file defined, the NEC file for plain surfaces could be generated.

🐃 keypoint form			
💿 New Data File 💦 🔿) Existing Data File		
Keypoint Data File Name			
C:\users\tao\PlayVB\sur_ge	enerator\datafile		
C:\ users tao PlayVB sur_generator datafile	kf1.dat kf2.dat pgf1.dat pgf2.dat pgf3.dat wgf1.dat wgf2.dat wkf2.dat		
- Keypoints			
Keypoint Number	(1-100)		
X Coordinate			
Y Coordinate			
Z Coordinate			
Add Keypoint	Change Coordinate		
Return			

Figure 35 Form of Keypoint Data File Generator

The keypoint data file generator is used to generate a keypoint data file, which includes the total number of keypoints for constructing the surfaces, the keypoint number of each point, and its Cartesian coordinates (in meters). Keypoints are the corner points of each piece of a plain surface. Four keypoints are needed for each quadrilateral surface, and three keypoints are needed for each triangular surface.

🐃 grind form	×		
New Grid Data File Existing Grid Data File			
Grid Data File Name			
C:\users\tao\PlayVB\sur_generator\datafile			
Image: Series kf1.dat Image: Series kf2.dat Image: Series pg1.dat Image: Series pg2.dat Image: Series pg3.dat Image: Series wg1.dat Image: Series wg2.dat Image: Series wg2.dat Image: Series wg2.dat Image: Series wg2.dat			
Grid Data Grid Number (1-100) Grid Shape © Rectangular © Triangular © Quadrilateral			
The Keypoint Number of Corner Points of Grid (Sequence of the Number according to Right Hand Rull)			
Number of Segments between Point 1_2			
Number of Segments between Point 2_3			
Add Grid Delete Grid Change			
Return			

Figure 36 Form of Grid Data File Generator

The grid data file generator is used to generate a grid data file, which includes the total number of surface grids, the grid number of each grid, the shape of the grid (shape information will appear only in the grid data file of a patch surface), the keypoint numbers of the four/three keypoints of the grid, and the number of segments on each side of the grid (for a patch surface,

only 1 segment is allowed for a triangular grid). For a patch surface, the normal vector of each grid is very important. It should direct outward for closed surfaces. The normal vector direction is determined by the ordering of the keypoints and the right-hand rule. For a wire-grid surface, the keypoints number should also be input in order.

Appendix C Properties of RANTEC FerroSorb

Rantec[®] FerroSorb is fire retardant and meets the standards of Navel Research Laboratory Report 8093, Texas Instruments Report #2693066, and MIT MS-8-21.

Rantec[®] FerroSorb is tested in a non-destructive process using a coaxial reflectometer or an NRL arch. This process assures quality and performance, allowing us to guarantee Rantec[®] FerroSorb's integrity.

Electrical Properties

FREQUENCY Range	ABSORÐTION/ REFLECTIVITY AVERAGE	POWER HANDLING Continuous CW
30 MHz - 40 GHz	20 dB over 30 MHz - 40 GHz	200 V/m

Applications

Rantec[®] FerroSorb's ultra broadband frequency range, high absorption and power handling capabilities are ideal for IEC 801-3, MIL-STD 461/462D, and ANSI C63.4. Rantec[®] FerroSorb can be used for new construction as well as upgrading the performance of existing rooms. Chamber performance is guaranteed when installed and tested by Rantec technicians / RF engineers.

Physical Properties

HEIGHT OVERALL	UNIT Size	NDMINAL WEIGHT	MOUNTING	RATINGS: Fire Retardant
410 MM 16.1 in.	60 cm \$quare 23.62 in.	19 kg 42 lbs.	Epoxy or Mech. Plate	NRL 8093 DN 4102-82



Appendix D Specifications of HP8753D Network Analyzer

Test Port Input Characteristics

Test Port Output Characteristics Prequency Characteristics

requency Characteristics		Frequency range:	300 kHz to 3 GHz	
Range:	300 kHz to 3 GHz		30 kHz to 6 GHz (with Option 006)	
	30 kHz to 6 GHz (with Option 006)	Average noise level:	-90 dBm (3 kHz BW, 50 kHz to 3 GHz)	
Resolution:	1 Hz		-110 dBm (10 Hz BW, 50 kHz to 3 GHz)	
Stability:	typically ±7.5 ppm 0° to 55°C		-120 dBm (10 Hz BW, 50 kHz to 3 GHz)	
	typically ±3 ppm/year		(typical)	
	With Option 1D5:		-85 dBm (3 kHz BW, 3 to 6 GHz)	
	typically ±0.05 ppm 0° to 55°C		-105 dBm (10 Hz BW, 3 to 6 GHz)	
	typically ±0.5 ppm/year		-115 dBm (10 Hz BW, 3 to 6 GHz) (typical)	
Accuracy:	±10 ppm at 25°C±5°C	Maximum input level:	0 dBm	
Power range:	-5 to +20 dBm	Damage level:	20 dBm or 35 VDC	
	-5 to +18 dBm (with Option 006)	Impedance: 50 obms:	≥10 dB RL, 30 kHz to 50 kHz	
Resolution:	0.05 dB		≥20 dB RL, 50 kHz to 300 kHz	
Level accuracy?:	$\doteq 1.0 \text{ dB}$		≥23 dB RL, 300 kHz to 1.3 GHz	
Level linearity ^{7,8,88} 2	$(-5 \text{ dBm to } + 15 \text{ dBm}) \pm 0.25 \text{ dB}$		≥20 dB RL, 1.3 GHz to 3 GHz	
	(+15 dBm to +20 dBm) ≈ 0.5 dB		≥8 dB RL, 3 GHz to 6 GHz	
Impedance:	50 Ω ; typically	Frequency response:	± 1.0 dB, 300 kHz to 3 GHz	
	\geq 16 dB RL (<1.38 SWR) to 3 GHz	(25° <u>+</u> 5°C)	± 2.0 dB, 3 GHz to 6 GHz	
	≥14 dB RL (<1.50 SWR) to 6 GH≯	Harmonics (Option 002):		
Spectral purity:		2nd harmonic:	<-1\$ dBc at 0 dBm	
2nd harmonic ² :	< -25 dBe at 20 dBm		<-35 dBc at -10 dBm (typical)	
	< 40 dBc at 10 dBm (typical)		<-45 dBc at -30 dBm (typical)	
	< -50 dBc at 0 dBm (typical)	3rd harmonic:	<-30 dBc at 0 dBm	
3rd barmonie ¹⁴ :	< -25 dBc at 20 dBm		< 50 dBc at -10 dBm (typical)	
	<-40 dBc at 10 dBm (typical)		<-50 dBe at -30 dBm (typical)	
	< -50 dBe at 0 dBm (typical)	Harmonic Measuremen	nt Accuracy: (25° <u>+</u> 5°C)	
Nonharmonic spurious:		16 MHz to 3 GHz	<u>+</u> 1 dB	
Mixer related:	<-30 dBc at 20 dBm (typical)	3 GHz to 6 GHz:	$\pm 3 dB$ (With Option 006)	
	< -55 dBc at 0 dBm (typical)	Harmonic Measurement Dynamic Range:		

-40 dBe (output = -10 dBm, input < -15 dBm)

Approval of Examining Committee

Roy S. Nutter, Ph.D.

Gregory J. Thompson, Ph.D.

James E. Smith, Ph.D., Chairman

Date