

2015

## Quantitative assessment of the discrimination potential of class and randomly acquired characteristics for crime scene quality shoeprints

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Quantitative assessment of the discrimination potential of class and randomly acquired characteristics for crime scene quality shoeprints

Nicole Richetelli, B.A.

Thesis submitted  
to the Eberly College of Arts and Sciences  
at West Virginia University

in partial fulfillment of the requirements for the degree of

Master of Science in  
Forensic & Investigative Science

Dr. Jacqueline Speir, Ph.D., Chair

Dr. Nicholas Petraco, Ph.D.

Dr. Gerald Lang, Ph.D.

Department of Forensic & Investigative Science

Morgantown, West Virginia  
2015

Keywords: Forensic, footwear, quantitative, crime-scene-like, automated classification, randomly acquired characteristics, similarity

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## ABSTRACT

Quantitative assessment of the discrimination potential of class and randomly acquired characteristics for crime scene quality shoeprints

Nicole Richetelli, B.A.

Footwear evidence has tremendous forensic value; it can focus a criminal investigation, link suspects to scenes, help reconstruct a series of events, or otherwise provide information vital to the successful resolution of a case. When considering the specific utility of a linkage, the strength of the connection between the source footwear and an impression left at the scene of a crime varies with the known rarity of the shoeprint itself, which is a function of the class characteristics, as well as the complexity, clarity, and quality of randomly acquired characteristics (RACs) available for analysis. To help elucidate the discrimination potential of footwear as a source of forensic evidence, the aim of this research was three-fold.

The first (and most time consuming obstacle) of this study was data acquisition. In order to efficiently process footwear exemplar inputs and extract meaningful data, including information about randomly acquired characteristics, a semi-automated image processing chain was developed. To date, 1,000 shoes have been fully processed, yielding a total of 57,426 RACs characterized in terms of position ( $\theta$ ,  $r$ ,  $r_{norm}$ ), shape (circle, line/curve, triangle, irregular) and complex perimeter (*e.g.*, Fourier descriptor). A plot of each feature versus position allowed for the creation of a heat map detailing coincidental RAC co-occurrence in position and shape. Results indicate that random chance association is as high as 1:756 for lines/curves and as low as 1:9,571 for triangular-shaped features. However, when a detailed analysis of the RAC's geometry is evaluated, each feature is distinguishable.

The second goal of this project was to ascertain the baseline performance of an automated footwear classification algorithm. A brief literature review reveals more than a dozen different approaches to automated shoeprint classification over the last decade. Unfortunately, despite the multitude of options and reports on algorithm inter-comparisons, few studies have assessed accuracy for crime-scene-like prints. To remedy this deficit, this research quantitatively assessed the baseline performance of a single metric, known as Phase Only Correlation (POC), on both high quality and crime-scene-like prints. The objective was to determine the baseline performance for high quality exemplars with high signal-to-noise ratios, and then determine the degree to which this performance declined as a function of variations in mixed media (blood and dust), transfer mechanisms (gel lifters), enhancement techniques (digital and chemical) and substrates (ceramic tiles, vinyl tiles,

and paper). The results indicate probabilities greater than 0.850 (and as high as 0.989) that known matches will exhibit stochastic dominance, and probabilities of 0.99 with high quality exemplars (Handprints or outsole edge images).

The third and final aim of this research was to mathematically evaluate the frequency and similarity of RACs in high quality exemplars versus crime-scene-like impressions as a function of RAC shape, perimeter, and area. This was accomplished using wet-residue impressions (created in the laboratory, but generated in a manner intended to replicate crime-scene-like prints). These impressions were processed in the same manner as their high quality exemplar mates, allowing for the determination of RAC loss and correlation of the entire RAC map between crime scene and high quality images. Results show that the unpredictable nature of crime scene print deposition causes RAC loss that varies from 33-100% with an average loss of 85%, and that up to 10% of the crime scene impressions fully lacked any identifiable RACs. Despite the loss of features present in the crime-scene-like impressions, there was a 0.74 probability that the actual shoe's high quality RAC map would rank higher in an ordered list than a known non-match map when queried with the crime-scene-like print. Moreover, this was true despite the fact that 64% of the crime-scene-like impressions exhibit 10 or fewer RACs.

## Acknowledgements

I would first like to acknowledge my chair, Dr. Jacqueline Speir. Thank you for all of your help and inspiration throughout the last two years. I have achieved more than I ever thought possible.

I would also like to thank the other members of my committee who took time to read my work and offer suggestions: Dr. Nicholas Petraco, Dr. Gerald Lang, and Dr. Patrick Buzzini.

Lastly, I could not have completed all of this work without the help of everyone else working in the lab! Thank you all: Mike Fagert, Adam Epler, Madonna Nobel, Renu Watalingam, Mike Hite, Carly Lasky, Anika Redden, Shreya Kamath, Josh Davis, Jonathan Thurston.

*Portions of this project were supported by Award No. 2013-DN-BX-K043, awarded by the National Institute of Justice, Office of Justice Program, U.S. Department of Justice. The opinions, findings, conclusions and recommendations expressed in this presentation are those of the authors and do not necessarily reflect those of the Department of Justice.*

*This work is dedicated to my family, who have always supported me in my academic endeavors.*

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# 1. Introduction

Footwear impression evidence can provide invaluable information to forensic scientists in order to link a suspect to a crime scene or reconstruct the series of events leading up to a crime. Despite this utility, shoeprint evidence is often “undervalued by investigators, attorneys, and the courts due to their limited knowledge of it” (1). As evidence of this, the *Census of Publicly Funded Forensic Crime Laboratories* reported that only 11,000 footwear examinations were conducted out of a total of 4 million requests in all of 2009 (2). This amounts to less than 0.3% of all forensic work carried out by 397 forensic laboratories in the United States over the course of a single year. Although it is unreasonable to anticipate that shoeprints can be detected and recovered at each and every crime scene, it is still valid to assume that some kind of footwear evidence may be present, and that the current statistics indicate underutilization of shoeprint impression evidence within the forensic community. With this in mind, the remainder of this document is divided into five chapters.

The first chapter (this chapter) reviews the current state of the footwear field, including (i.) a discussion of the relevant features in shoeprint comparisons that are typically evaluated during a forensic examination, (ii.) the types of conclusions that are reached after such an exam, (iii.) the education and training requirements associated with examiner expertise, as well as (iv.) a summary of major research contributions to the field, before closing with (v.) a brief list of topical areas that could benefit from additional research (including the three objectives of this body of work).

This introduction is followed by three chapters that are intended as stand-alone, draft, publication-quality journal submissions designed to address specific objectives from the aforementioned research list. The first describes a semi-automatic image processing chain that was implemented to streamline data acquisition for over 1,000 pairs of shoes, thereby allowing the efficient prediction of random co-occurrence in frequency of outsole features (in terms of location, shape, and similarity). This is followed by an assessment of the baseline performance of Phase Only Correlation (POC) as an automated classification technique to classify both high quality and crime-scene-like impressions. Finally, the last draft-publication reports the reproducibility of accidentals in crime-scene-like quality prints, including the assessment of similarity metrics such as Modified Phase Only Correlation, Matched Filter, Modified Cosine Similarity, Euclidean Distance and Hausdorff Distance, as well as the ability of a RAC map to mate back to its known match within a database. These three publication drafts are followed by one final (fifth) chapter that briefly reviews ways in which this research can be further prioritized and expanded.

## 1.1 Analysis and Interpretation of Footwear Impression Evidence

The methods of analysis of footwear impression evidence are often compared to that of fingerprint impression evidence. Fingerprint examination includes an evaluation of first, second, and third level detail. First level detail describes the overall pattern design, such as arch, loop, or whorl. The first level detail of fingerprints is least individualizing, but allows for impressions to be grouped. The same three basic friction ridge patterns are exhibited throughout the population and although this detail cannot lead to an identification, it helps to narrow down the comparison group (3). The second level detail includes specific ridge path and the presence of minutiae (ridge endings, bifurcations, dots, etc.). In fingerprints, comparison of this second level detail can lead to a positive identification. The locations of these details and the frequencies of the occurrence of such features in a given location help to define the “uniqueness” of a fingerprint; that is, no two people are believed to exhibit the same fingerprints (3). Lastly, the third level detail is encompassed in the pore structures and small details contained within the ridges. Throughout the comparison process, an examiner records any disagreement between the latent and the known prints (3).

Similar to fingerprints, shoeprints exhibit some characteristics that are present throughout the population and some characteristics that are believed to be random and individualizing. A shoe’s class or manufacturing characteristics include the size, shape, style, and pattern design. By definition, a manufacturing characteristic will be shared by many other shoes, as compared with the first level characteristics of fingerprints (1). Individual or acquired characteristics of a shoe include cuts, scratches, tears, gum, shoe patches, and holes; these are comparable to the bifurcations, ridge endings, and dots of a fingerprint. Footwear examiners conduct a methodical analysis of these aforementioned features in order to reach a conclusion about the origin of a given shoe impression. First and foremost, the known shoes must be used to make exemplar prints for comparison. In addition, the original lift or cast of an unknown impression must be obtained, if possible; if this evidence is not available, high quality photographs of this evidence must be used for comparison. Typically, the first of these analyses is based on class characteristics. This generally starts with a comparison of the outsole design, given that this is the most obvious feature of a shoe. The design of the questioned impression and the exemplar impression must be in agreement in order to move forward with the comparison. Next, the physical shape and size of the shoe and its design elements must be compared. This analysis includes both measuring the physical dimensions/perimeter of the outsole, if possible, as well as examining the size of the individual design features (1). The size of the design should be examined because as a sole changes size, something must change on the outsole, and this can happen in one of two ways (1):

1. The design element size will not change, but instead the number of design elements will change
2. The design element size will vary, but the number of design elements will remain constant

Should the known and the questioned impressions still correspond after the comparison of physical and design size, an analysis of randomly acquired characteristics (RACs) may ensue. The term randomly acquired refers to features that are “not planned or intentionally manufactured, and that their combined position, orientation, size, and features are unlikely to re-occur” (1). Following all of the aforementioned comparisons, the examiner can then come to a conclusion about the origin of the questioned shoeprint impression. SWGTREAD has published a standard for all forensic shoeprint examiners to reference when making conclusions about comparisons between shoeprints. These conclusions and the reasoning for each conclusion are as follows (4):

1. **Lacks sufficient detail**

- No comparison was conducted.
- A comparison was conducted but the impression did not have enough detail for a meaningful comparison.

2. **Exclusion**

- Enough detail and differences were present to conclude that the known exemplar was not the source of the impression.

3. **Limited association of class characteristics**

- Some similar class characteristics were present, but there were factors which limited the ability to make a stronger association.

4. **Association of class characteristics**

- Class characteristics of physical design and size are consistent between the known and the questioned impression. Some correspondence of wear may also be present.

5. **High degree of association**

- Correspondence of general physical design, size, and wear, as well as one or more acquired characteristics between the known and the questioned impression.



## **6. Identification**

- The known and the questioned impression correspond in class and acquired characteristics. It is the opinion of the examiner that the known footwear was the source of the questioned impression.

After conducting all relevant analyses, a footwear examiner can reach one of these conclusions, which are based on the guidelines in the SWGTREAD standards. Currently in the field, footwear evidence comparisons and the resulting conclusions are largely based on an examiner's experience, leading to some criticism. However, an analyst's experience is acquired from extensive education, training, casework and a wealth of acquired knowledge as illustrated in section 1.2.

## **1.2 Acquisition of Experience for the Forensic Footwear Examiner**

Becoming a forensic footwear examiner requires a combination of education and training. Requirements include (5):

1. Bachelor's Degree in a physical or natural science, or
2. Associate's Degree plus 2 years experience, or
3. High School Diploma plus 4 years experience.

In addition to the above, comprehensive training is required to help candidates learn standards in terminology, evidence handling, as well as legal considerations. Further, a section of supervised casework is completed and an examination may be conducted to ensure that the body of knowledge has been mastered. As outlined by SWGTREAD, the following topics are included as part of the training program for forensic footwear examiners (5):

### **1. Introduction to forensic footwear examination**

- History; value of footwear evidence.

### **2. Terminology**

### **3. Evidence handling procedures**

- Procedures and protocol; relationship of forensic footwear evidence to other forensic disciplines; collection and preservation; marking and documentation; chain of custody.

**4. Examination of impressions**

- Protocols; theory of individualization; case organization; note taking; evidence evaluation and comparison; conclusions and findings; report writing.

**5. Laboratory instrumentation and equipment**

- Procedures and protocol; photographic equipment; measuring devices; light sources; computers and peripherals; other relevant laboratory equipment.

**6. Photography**

- Theory of photography; basic camera operation; general crime scene photography; examination quality photography; two- and three- dimensional impressions; various lighting techniques; filters.

**7. Recovery by lifting**

- Electrostatic lifting; gelatin, adhesive, and other lifting methods.

**8. Recovery by casting**

- Dental stone; fixatives and release agents; snow casting.

**9. Detection of impressions**

- Visible impressions; specialized lighting; electrostatic lifting; physical and chemical methods.

**10. Enhancement**

- Photographic, chemical, physical, imaging software.

**11. Manufacturing**

**12. Preparation of test impressions**

**13. Court testimony and legal issues**

- Expert witness qualifications; legal decisions; preparations of exhibits; moot court.

### 1.3 Previous Research

While many forensic footwear examiners agree that the characteristics on a shoe are “unique” and can be used for identification, the field is often challenged due to lack of statistical evidence (6). Some footwear evidence has even faced admissibility challenges in the courtroom given the lack of quantitative support for the qualitative evidence, because the Daubert decision rejects the “general acceptance” rule (7). In an attempt to offer quantitative support to footwear examinations, a limited number of studies have assessed the discriminating potential of footwear, with implementation of mathematical methods, offering support to the assertion that footwear evidence can produce an identification of source.

Detailed below is a review of the current literature which attempts to incorporate statistics into footwear impression evidence and further support the claim that the features present on outsoles can lead to an identification. This claim is largely based on analysis of three major features associated with footwear, including:

1. Class characteristics: design, manufacturing process, etc.
2. Subclass characteristics: air bubbles, incomplete mixing, etc.
3. Randomly acquired characteristics: nicks, holes, tears, etc.

As aforementioned, class characteristics include manufacturing features, design, and size; however, shoes rarely exhibit only one class characteristic. In fact, the combination of class characteristics can greatly reduce the sample set for comparison, as illustrated in Fig. [1.1]. Though class characteristics cannot be used for an identification, the combination of these features can greatly aid in narrowing down the possible sources of a given impression by excluding shoes which do not correspond in manufacturing features (such as model, size, etc.).

Further, air bubbles, a subclass characteristic, also help to narrow down the possibilities of source of a given impression. For example, Champod et al. (2000) examined the presence of air bubbles in polyurethane shoe outsoles; the goal of the study was to “gather statistical data on the occurrence and measured features of air bubbles on shoesoles, in order to extend our knowledge of the stochastic behaviour of air bubbles” (8). The analysts examined seventy-one pairs of the same shoe and analyzed bubbles found only in the ball portion of the shoe. The results indicate that the configuration of air bubbles is highly variable, even between two shoes of the same pair.

Though class and subclass characteristics are often useful for discriminating purposes, these features cannot actually be used to reach an identification (1). Rather, an analysis of acquired characteristics is necessary in order to determine whether a given shoe was the source of a crime scene print. Wilson (2012) compared the outsoles of thirty-nine pairs of the same shoe, worn by the same person, to determine if the acquired characteristics varied enough from shoe to shoe to separate the pairs of shoes and make an identification

Combination of CLASS CHARACTERISTICS

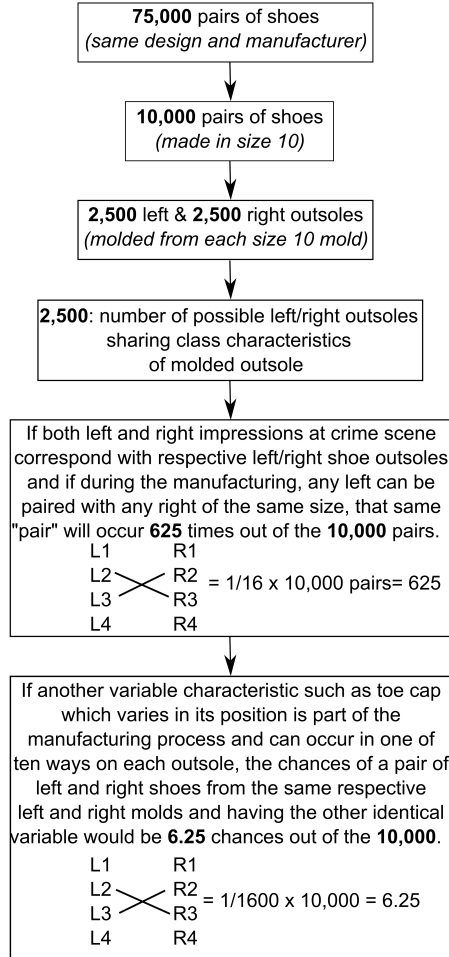


Figure 1.1: An illustration of how the presence of combined class characteristics can significantly decrease the number of suspect shoes (adapted from Bodziak (2000)).

(9). Each outsole was examined and acquired characteristics (such as cuts, gouges, and tears) were marked, counted, and recorded. Wilson (2012) found that even in shoes with a comparable number of acquired characteristics, visual examination could quickly differentiate between the location, size, and shape characteristics. In conclusion, the results indicate that “the likelihood of the characteristic(s) repeating in the same area of the same shoe with the same size and tread design is so small that it is the opinion of the experienced examiner that one would never observe the same amount of similarity between two different shoes” (9). While the results from this research indicate that the number, shape, and size of randomly acquired characteristics are not repeated, a large scale study

should be conducted in order to determine whether these results are repeatable.

While Wilson (2012) offered evidence that accidental characteristics are truly identifying, Cassidy (1995) provides some numerical estimates for the *probability* of repeated accidentals based on a dataset that consisted of boots worn by police recruits. For this study, because all of the shoes were worn for the same time span and over the same terrain, conditions favored the chance reproduction of accidental characteristics and wear (10). Two impressions from each of 97 shoes were recorded, for a total of 194 impressions. The shoes were broken into group A (59 shoes) and group B (38 shoes). From each impression, three accidentals were chosen and then compared against all other impressions to determine whether any of the accidentals were duplicated in the same position on another shoe. Results indicated that minute accidental characteristics were more prevalent on lightly worn shoes, while moderate or significant accidentals were much more likely to occur on more heavily worn shoes (10). For minute characteristics, the results indicated a 1 in 6 chance of encountering a duplicate accidental (10). However, the results for moderate characteristics indicated that these are less likely to be duplicated, likely due to increased size and/or complexity. For group A shoes, the chance of a coincidental similar accidental position was about 1 in 20, while this chance for group B shoes was even lower at approximately 1 in 38 (10). According to Cassidy (1995), the quality of accidentals greatly impacted the number required for an identification. More specifically, accidentals that are small or of poor quality require a larger number of features to reach an identification than larger or more rare characteristics (10). This study offers some numerical estimates about the probability of encountering accidentals in the same position on two different shoes. However, given the small sample size of this study, there remains a need for a large scale study concerning mathematical comparison of accidental characteristics.

While all of the above studies focus on empirical data, Stone (2006) utilized theoretical probabilities to describe the individuality of RACs. Stone (2006) identified five standardized individual characteristics. In addition, the researcher analyzed theoretical acquired characteristics based on their position, configuration, and orientation. To arrive at the computed probabilities, a hypothetical 16,000 square millimeter grid was superimposed on the theoretical shoeprint. The author then determined the hypothetical probability of encountering a given accidental on another shoe provided that the hypothetical shoe did not produce the print. For a point characteristic, the probability of a random duplication was modeled as 1 in 16,000. For a line characteristic, the length, orientation, and position were combined to obtain the probability of encountering a duplication of the given line characteristic valued at 1 in 384,000. For a curve characteristic the position, length, orientation, direction of curvature, degree of curvature, and apex location were all combined in the probability calculation to yield a 1 in 19,200,000 probability of finding a given curve characteristic in another shoe. As the characteristics became more complex, the probability of a random duplication greatly decreased. In addition, assuming that acquired characteristics occur at random and are independent from other characteristics, the probabilities of encountering several different characteristics could be multiplied together to obtain the probability of the random duplication of the entire collection. The results

reveal, “information about the sometimes incomprehensible magnitude of the ‘uniqueness’ of these types of characteristics when they occur in multiples or combinations”, though the author explains that these probabilities are theoretical and that several validation studies are required (11). While this study indicates very robust results, the empirical data obtained by Cassidy (1995) indicates a lower discrimination potential, suggesting the need for further work to determine the true value of accidental characteristics.

Petraco et al. (2010) examined footwear impressions using facial recognition techniques, namely principal component analysis (PCA) (12). PCA assumes that variance provides information about a given dataset. Ideally, PCA serves as a data reduction technique which still captures most of the variability of the original dataset (13). For this study, the authors examined five pairs of the same type of shoe, which were each worn by the same individual. The Abbott Grid Locator was utilized in order to record the position of any accidentals on the shoe outsole, ignoring size and shape. After recording accidentals and completing PCA on the dataset, the authors used Maximum likelihood Gaussian-linear classification analysis (MLG-LCA) in order to determine the similarity between patterns based on distance in principal component space (13). This metric is essentially a Mahalanobis distance using the Z (principal component derived matrix) and the pooled covariance matrix. Mahalanobis distance determines how many standard deviations away a point is from the mean of a distribution. The results indicated that the average correct identification rate of the five pairs of shoes was approximately 92%. These results indicate that shoe prints, even when the shoes are worn by the same person and exhibit the same manufacturing characteristics, are statistically separable and the acquired characteristics provide enough information to potentially be used for identification. This study provides one method of statistically analyzing footwear impression evidence and even calculates an error rate as is required by the Daubert decision.

Furthermore, Sheets et al. (2013) aimed to determine the persistence of acquired characteristics over time, similar to Petraco et al. (2010). The goal of the study was to determine the rate at which wear affects the persistence of randomly acquired characteristics. For this study, eleven pairs of the same shoe were analyzed; a set of “accidentals” was cut into the outsole of the shoe in the same location on each pair. Participants in the study wore the pair of shoes for a period of seven weeks and the outsoles were examined at four times throughout the period of wear. A square grid was used to record the size of the accidentals via percentage of grid occupied by the accidental. Therefore, only the size of the acquired characteristics was recorded and the location and shape were ignored during the analyses. PCA was utilized to determine the variation within repeated measures of the same shoes and between different shoes at each time interval. Throughout the study, intra-shoe variation was much lower than inter-shoe variation. Thus, even with additional wear, each shoe better matched itself than any other shoe to which it was compared (14).

Therefore, several studies support the theory of individuality of shoeprints and provide evidence, both empirical and theoretical, for the identification of source based upon an analysis of randomly acquired characteristics on shoe outsoles (10; 9; 12; 14).

## 1.4 Advancing the Field with Further Research Support

While research exists to support the merit of footwear evidence in narrowing down a suspect pool or even identifying the source of an impression, the current body of work focuses largely on (i.) high quality evidence samples, and generally those of (ii.) very limited sample size. Therefore, additional work is needed. Moreover, very little focus has been directed at the interpretation and discriminating power of degraded and variable *crime scene samples*. With these goals in mind, the forensic footwear community could greatly benefit from several additional research thrusts, not limited to but including:

1. Development and implementation of an automated image processing chain, allowing for several different inputs (*i.e.*, high quality exemplars, lifts, photographs, and casts of crime scene impressions), which could facilitate efficient extraction and characterization of features to be used for comparisons and assessment of similarity between two prints or specific elements on several impressions;
2. Large scale study of RACs to include an assessment of position and shapes of accidentals as well as the potential for co-occurrence;
3. A detailed evaluation of a single automated classification method. This work should include an assessment of the discrimination potential for crime scene quality impressions as well as an analysis of method limitations;
4. Analysis of the reproducibility of RACs in crime scene quality impressions as well as the potential for the features observed in evidence samples to be linked to source footwear;
5. Evaluation of the variability in examiner conclusions, including estimations of “error” rates for footwear comparisons (thus satisfying the Daubert standard);
6. Development of a national footwear database, comparable to AFIS for fingerprints;
7. Assessment of the frequency of different outsole styles and sizes;
8. Quantification of intra- and inter-analyst variability in RAC marking;
9. Investigation of the degree of uncertainty in footwear comparisons and conclusions;
10. Development of software which can automatically extract RACs for comparison from a variety of inputs, thus eliminating the need for manual identification of accidentals.

In an attempt to address some of the aforementioned research needs for footwear impression evidence, the current study executed a three-pronged research design. First, an image processing chain, with both automated and user-fed algorithms, was implemented allowing for digitization of varying impressions and extraction of feature information for

comparison between different inputs. Using this methodology, a collection of 1,000 shoes has been analyzed, including an assessment of RAC frequencies and potential for co-occurrence for 57,426 identified accidentals (thus addressing items one and two from the recommended research list). Subsequently, a random sample of 36 shoes was selected from this set to be used for creation of 108 blood and 72 dust impressions. These prints were utilized to conduct a quantitative assessment of the performance of Phase Only Correlation (POC), an automated classification method (recommended research item three) on high quality versus crime-scene-like images. This evaluation was based on a total of 1,525 high quality and 3,096 crime-scene-like print comparisons. Lastly, 200 crime-scene-like prints were examined to determine the fidelity of the impression transfer process; namely, the ability of the 6,762 randomly acquired characteristics observed in the exemplar impressions from 100 shoes to appear in the crime scene prints (recommended research item 4). In addition, an evaluation of similarity between 1,766 known match RAC mates (RACs identified in the exemplar impressions which were visible in the crime-scene-like prints) was conducted. The following three chapters are copies of draft, publication-quality journal submissions addressing said items from the recommended research list.



## **2. Technical Note**

# Technical note: Quantifying the frequency of shape and position of randomly acquired characteristics on outsoles

---

## **Abstract**

Footwear evidence has tremendous forensic value; it can focus a criminal investigation, link suspects to scenes, help reconstruct a series of events, or otherwise provide information vital to the successful resolution of a case. When considering the specific utility of a linkage, the strength of the connection between the source footwear and an impression left at the scene of a crime varies with the known rarity of the shoeprint itself, which is a function of the class characteristics, as well as the complexity, clarity, and quality of randomly acquired characteristics (RACs) available for analysis. To help elucidate the discrimination potential of footwear as a source of forensic evidence, the aim of this research is to further characterize the chance association in position, shape, and geometry of RACs on a semi-random selection of footwear. To accomplish this goal in an efficient manner, a partially automated image processing chain was required, including steps for automated feature characterization. This technical note details the methods, procedures, and the type of results available for subsequent statistical analysis after processing a collection of more than 1,000 shoes.

*Keywords:* Footwear, Shoeprints, Randomly Acquired Characteristics, Accidentals, Fourier Descriptors, Feature Vectors, Semi-Automated

---

1 **Introduction**

2        Though footwear impression evidence can provide a wealth of informa-  
3 tion about a crime, including potential suspects, the total number of possible  
4 offenders, and the most probable series of events associated with a reconstruc-  
5 tion, this evidence is often undervalued (or even overlooked) due to limited  
6 knowledge about how to collect, analyze, and interpret footwear impressions  
7 [1]. Part of the reason for this disconnect may be the difficulty associated  
8 with collecting sufficient-sized and community-shared databases for extensive  
9 research and study, which would allow the legal and forensic community to  
10 fully appreciate the value of this type of evidence. The fact is, footwear re-  
11 search is extremely time-consuming and labor intensive, regardless of whether  
12 the analyst is focused on class, randomly acquired characteristics (RACs), or  
13 both. Although class features hold incredible value, this project deliberately  
14 disregards class characteristics and instead focuses on RACs or accidental  
15 features such as nicks, tears, holes, and cuts that typically develop on out-  
16 soles as a function of wear. The reason for this narrow focus in scope is  
17 primarily four-fold. First, class features have received some research atten-  
18 tion in the past [2–11] and this trend is likely to continue in the future. As  
19 a result, this investigative effort intentionally sought out the less-traveled  
20 parallel track concerning characterization of accidental features, while si-  
21 multaneously collecting sufficient data to allow for subsequent class analysis  
22 downstream. Second, the National Academy of Sciences (NAS) 2009 report  
23 on *Strengthening Forensic Science in the United States* encouraged studies to  
24 shed light on the variability of randomly acquired characteristics, including

25 relative frequency of features, and the appropriate use of statistical standards  
26 [12]. Third, the Scientific Working Group for Shoeprint and Tire Tread Ev-  
27 idence (SWGTTREAD) requested focused research in the area of “*Random*  
28 *Placement Shape and/or Placement of Randomly Acquired Characteristics*”  
29 [13], and finally, SWGTREAD also requested focused research in the area  
30 of “*Mathematical Probabilities of Randomly Acquired Characteristics*” [14].  
31 Given these challenges, the first goal (and bottleneck) of this project was  
32 data acquisition. The remainder of this technical note describes the manner  
33 in which more than 1,000 worn shoes (obtained from a variety of sources  
34 including personal donations, corporate donations, and purchases from local  
35 thrift stores) were sequentially processed via a combination of automated  
36 and user-fed algorithms allowing for identified RACs to be extracted and  
37 characterized in terms of shape, geometry, and physical location.

## 38 **Material and Methods**

39 Available defining characteristics associated with more than 1,000 shoes  
40 have been recorded, including make, model, size, manufacturer product code,  
41 degree of wear, and the presence of either microcellular material or Schal-  
42 lamach patterns as detailed in Tables [1] - [6]. As necessary, each shoe was  
43 gently washed (using warm water) to remove debris (*i.e.*, this research does  
44 not account for the possible presence of transient RACs, such as rocks, gum,  
45 etc.). When dry, each outsole was scanned at 600PPI with an Epson Ex-  
46 pression 11000XL Graphic Arts Scanner. Post-outsole scanning, Handiprint  
47 exemplars were created [1] and likewise scanned at 600PPI. Both are illus-  
48 trated in Fig. [1] for a size 9 men’s Converse Chuck Taylor® All Star® with

49 moderate wear and Schallamach patterns.

50 In order to facilitate the automated downstream extraction of RAC shape  
51 and position, the outsole and exemplar were background subtracted and  
52 registered using identified control points. This process required the analyst  
53 to identify common geometric shapes (usually class characteristics) that were  
54 patent on both the outsole and the exemplar. The mating of these common  
55 points allowed for the automatic computation of variations in translation,  
56 rotation, and scale between the outsole and the exemplar. Once detected,  
57 the outsole and exemplar were co-registered or adjusted to ensure that they  
58 occupied the same location in image space (centered and oriented such that  
59 the long-axis of the shoe (toe-to-heel) was North-South within the image  
60 frame). In addition to this co-registration, the background (non-tread areas)  
61 of both the outsole and exemplar were removed (Fig. [2]) to ensure the  
62 highest quality imagery moving forward (*e.g.*, removal of remnants of the  
63 analyst's hands that may have been captured during scanning when pressure  
64 was applied to the outsole to promote a nearly planar surface, and/or removal  
65 of extraneous dust and fingerprints on Handiprint exemplars).

66 Following registration and background subtraction, randomly acquired  
67 characteristics present on both the outsole and exemplar were marked. This  
68 process required the analyst to physically examine each outsole with oblique  
69 illumination and 4X magnification. Upon identifying a RAC that appeared  
70 on both the outsole and the exemplar, the analyst blacked out the RAC pixels  
71 on the Handiprint image using the pencil tool in Adobe® Photoshop® Ele-  
72 ments 10. When this registered and marked image was subtracted from its  
73 registered (but unmarked) counterpart, the result was a RAC map that high-

74 lighted the location and geometry associated with each randomly acquired  
75 feature (Figs. [3] & [4]). Using the standard image processing technique of  
76 connected components, the location of each RAC was sequentially character-  
77 ized using three parameters; the radius ( $r$ ) or distance (in pixels) between the  
78 shoe's center and the RAC's centroid, the angular ( $\theta$ ) position (in degrees) of  
79 the RAC's centroid using the shoe's center as the origin, and the normalized  
80 distance ( $r_{norm}$ ) equal to  $r$  divided by the distance (in pixels) between the  
81 shoe's center and the perimeter of the shoe at angular position  $\theta$ .

82 Following localization, each feature was automatically numbered (via its  
83 connected component value) and extracted from the total RAC map. The  
84 resulting subimages (Fig. [5]) were then evaluated to define RAC shape and  
85 geometry, based on a 5-dimensional RAC feature vector, before transforma-  
86 tion into individual RAC Fourier descriptors (FD).

### 87 *RAC Feature Vector*

88 Each randomly acquired characteristic was attributed to one of four cat-  
89 egories: lines/curves, circles, triangles, and irregular-shaped features. To  
90 determine this categorization, 5 attributes per RAC were required, including  
91 area, perimeter, linearity, circularity, and triangularity. The first 2 descrip-  
92 tions (area and perimeter) were readily available; area describes the total  
93 number of pixels comprising the RAC and perimeter evaluates the distance  
94 in pixels along a line/curve, or around a two-dimensional shape.

95 The linearity metric was also readily available and was obtained by com-  
96 puting the ratio of the first and second eigenvalues ( $\lambda_1$  and  $\lambda_2$ ) generated  
97 from eigen decomposition of the RAC coordinates [15]. Using this approach,  
98 when  $\lambda_1$  is much greater than  $\lambda_2$ , the RAC in question has a greater length

99 than width and can be classified into the line/curve category.

100 The fourth measurement was a circularity metric, computed according to  
101 Eq. [1] [16], where  $A$  is the area of the object, and  $P$  is the length of its  
102 perimeter:

$$R_c = \frac{4\pi A}{P^2} \quad (1)$$

$R_c =$  maximum of 1.0 for a perfect circle

103 The fifth and final metric was a triangularity value computed using central  
104 moments (Eq. [2]) that are invariant to translation, scale, and rotation.

$$\mu_{pq} = \sum_x \sum_y (x - x_c)^p (y - y_c)^q \quad (2)$$

105 As per Rosin (2003) [17], the variable  $I_1$  in Eq. [3] equals  $\frac{1}{108}$  for any triangle  
106 that has been affine transformed into a perfect right-angled triangle:

$$I_1 = \frac{\mu_{20}\mu_{02} - \mu_{11}^2}{\mu_{00}^4} \quad (3)$$

107 As such, the triangularity measure can be normalized to vary between 0.0 –  
108 1.0 according to Eq. [4] [17]:

$$T = \begin{cases} 108 I_1 & \text{if } I_1 \leq \frac{1}{108} \\ \frac{1}{108 I_1} & \text{otherwise} \end{cases} \quad (4)$$

109 *Categorization Parameters*

110 The 5-dimensional feature vector (Fig. [6]) describing area, perimeter,  
111 linearity, circularity, and triangularity served as a primary descriptor and  
112 comparison parameter for each randomly acquired characteristic. In addi-  
113 tion, it was used to categorize the randomly acquired characteristics into one  
114 of 4 groups; line/curve, circle, triangle, or irregular.

115 Based on a survey of known geometric shapes, absolute categorization  
116 rules were developed. More specifically (and for this dataset), circles have a  
117 circularity measure greater than or equal to 0.8, triangles have a circularity  
118 measure less than 0.8 *and* a triangularity greater than or equal to 0.9, while  
119 lines/curves have a linearity ratio greater than 5 *and* a triangularity measure  
120 less than or equal to 0.3; any shape not satisfying one of the above rules  
121 defaults into the irregular category (Fig. [7]).

122

123 *Shape Descriptor*

124 In addition to shape categorization, each RAC was treated as a closed  
125 planar figure yielding a Fourier description [18–20]. This description was  
126 generated by tracing the contour of the shape  $(x(t), y(t))$  where  $t = 0, \dots, N -$   
127  $1$  with  $N = 350$  for this dataset) and assuming a complex plane  $z(t) =$   
128  $x(t) + iy(t)$  (where  $i = \sqrt{-1}$ ). The resulting one-dimensional complex  
129 sequence of numbers was then mapped to the frequency domain via the  
130 discrete Fourier transform [19] where  $R_m$  and  $\theta_m$  are the magnitude and  
131 phase of the  $m^{\text{th}}$  coefficient, respectively [19]:



$$\begin{aligned}
Z(m) &= \sum_{t=0}^{N-1} z(t) e^{(-i2\pi mt/N)} = R_m e^{(i\theta_m)} \\
m &= -N/2, \dots, -1, 0, 1, \dots, N/2 - 1
\end{aligned} \tag{5}$$

132 As necessary, the coefficients can be normalized and forced to be invariant  
133 to translation, scale, rotation, and contour/sequence start point according to  
134 the following modifications [19]:

$$\begin{aligned}
Z(0) = 0 &\quad \Rightarrow \text{translation invariance} \\
R_m = \frac{R_m}{R_1} &\quad \Rightarrow \text{scale invariance} \\
\theta_m = \theta_m - \frac{\theta_{-1} + \theta_1}{2} &\quad \Rightarrow \text{rotation invariance} \\
\theta_m = \theta_m + m \frac{\theta_{-1} - \theta_1}{2} &\quad \Rightarrow \text{start point invariance}
\end{aligned} \tag{6}$$

135 To illustrate, consider Figs. [8] & [9]. Fig. [8] depicts a single RAC (A), along  
136 with four synthetic modifications (B-E showing changes in scale, rotation,  
137 and translation). The resulting normalized Fourier descriptors are plotted  
138 in Fig. [9]. The x- and y-axes are arbitrary dimensions since the images  
139 have been normalized, but note that all contours are normalized to the same  
140 configuration, save a single  $\pi$  radian ambiguity [21]. Unless otherwise noted,  
141 all subsequent uses of RAC Fourier descriptors make use of both translation  
142 and start point invariance modifications.

## 143 **Results**

### 144 *Database Statistics*

145 To date, more than 1,000 shoes have been pre-processed. The defining  
146 characteristics of the first 1,000 are detailed in Tables [1] - [6]. The majority

147 of shoes in this collection are athletic in nature (Table [1]), due to gener-  
148 ous corporate donations and the availability of shoes for purchase from local  
149 thrift stores. Table [2] reports the degree of wear of each shoe, which is  
150 not quite balanced between light, moderate, and heavy. For this study, shoes  
151 with “light wear” are those that exhibit discernible texture throughout. Con-  
152 versely, the label “moderate wear” describes shoes with a reasonable degree  
153 of wear, resulting in both lost texture and possible bald spots. Finally, the  
154 term “heavy wear” is reserved for shoes with a near complete loss of texture,  
155 many or large bald spots, and possible holes or areas where the outsole has  
156 completely worn through.

157 Table [3] shows that nearly 90% of the collection lacks microcellular ma-  
158 terial in outsole composition. This is fortuitous since the presence of mi-  
159 crocellular material is likely to increase intra- and inter-analyst variability  
160 in identifying randomly acquired characteristics. Conversely, approximately  
161 three-quarters of the database show Schallamach patterns (Table [4]); this  
162 is likewise fortuitous. Although current RAC data does not include the  
163 quantification of these features, the discrimination potential of Schallamach  
164 patterns can be explored in future studies.

165 Table [5] reports shoe frequency as a function of manufacturer and/or  
166 brand. Results indicate that almost 30% of the shoes processed thus far are  
167 from Nike<sup>®</sup> while another 28% are comprised of a small number of shoes, but  
168 from numerous manufacturers. Finally, Table [6] breaks down the database  
169 according to size and intended market (men or women). The results here are  
170 not random, but selective in the sense that our group did not capture data  
171 for shoes with a physical outsole size greater than the maximum length of

172 a sheet of Handiprint currently available for purchase (or approximately 13  
173 inches in total length).

174 The shoes in Table [1] generated a total of 57,426 RACs (average of 57,  
175 minimum of 1, and maximum of 410). The majority (45%) were catego-  
176 rized as lines/curves, with another 38% falling into the irregular category.  
177 Circles filled a distant third group, comprising only 11% of the database,  
178 with triangles completing the remaining 6% (Table [7]). This data has been  
179 transformed into an interactive web-based heat map that currently reports  
180 frequency data for a “normalized” shoe, based on 57,426 RACs extracted  
181 from 1,000 shoes in the database. The normalization step, although not  
182 ideal, is unfortunately a necessity since it is near impossible to collect a suffi-  
183 cient number of shoes of a given make, model, and size to allow for statistical  
184 data analysis. Instead, the semi-random selection of shoes was normalized to  
185 create a *single idealized shoe* so that all RACs could be compared as if they  
186 occupied the same image space (as per  $\theta$  and  $r_{norm}$ ). In short, a RAC near  
187 the edge of the medial part of the heel on a women’s size 6.5 could have the  
188 same  $\theta$  and  $r_{norm}$  as a RAC on the edge of the medial part of the heel of a  
189 men’s size 10.0 (*Note: we also have the capacity to report frequency values as*  
190 *absolute, physical or non-normalized values using  $\theta$  and  $r$  upon request. This*  
191 *would be equivalent to taking a stack of Handiprints, centering all shoes in*  
192 *the middle of each sheet with the toe-heel oriented North-South, and drilling*  
193 *down through all sheets at a fixed location, regardless of shoe size. To further*  
194 *elaborate, in the aforementioned example, the RAC on the medial heel portion*  
195 *of the women’s size 6.5 shoe would likely fall somewhere in the lower-instep*  
196 *area of the men’s size 10.0.)*

197 A static version of the web-based heat map is illustrated in Fig. [10]. In  
198 the associated frequency table, the numerical values in the top row remain  
199 constant regardless of the user’s interaction with the web-page, displaying  
200 data associated with total RAC count for the entire database (regardless of  
201 cell location). Conversely, the two remaining rows automatically update to  
202 display RAC count and frequency for individual cells (5mm x 5mm) when  
203 queried by the user (in this static version, data is provided for a single cell  
204 outlined in black). The heat map allows the analyst to visually and quan-  
205 titatively evaluate the spatial density of randomly acquired characteristics  
206 according to location and category, in response to the National Academy  
207 of Sciences (NAS) 2009 request for relative frequency of features, as well  
208 as SWGTREAD’s request for research on *Random Placement Shape and/or*  
209 *Placement of Randomly Acquired Characteristics* [13], and the “*Mathemat-*  
210 *ical Probabilities of Randomly Acquired Characteristics*” [14].

211 Despite this positive step (pun intended), the authors acknowledge that  
212 this database must be used with caution. The utility of the density informa-  
213 tion is its ability to shed light on the random and variable nature of RAC  
214 frequency and *possible co-occurrence*. However, the heat map data is not  
215 intended to be a quantitative collection of independent wear-related events  
216 that can be multiplied to provide a cumulative probability of occurrence for a  
217 constellation of RACs on a randomly selected outsole. Moreover, density and  
218 categorization does little to account for the clarity, quality, and complexity of  
219 a geometric feature, which is as much (if not more important) to the forensic  
220 footwear comparison than the simple assessment of presence or absence. As  
221 such, the examiner’s responsibilities cannot be deduced to a simple table of

222 frequencies, and a great deal more is required to both interpret and under-  
 223 stand how best to utilize the database this project is generating. Despite  
 224 this caveat, now that the data exists and is accessible to the community, our  
 225 new focus is how best to present it to maximize value, along with estimates  
 226 of uncertainty in frequency, analyst-variability, and quantitative metrics of  
 227 shape similarity.

Table 1: Frequency of shoe type.

Type	Number
Athletic	838
Dress Shoe	88
Boot	56
Sandal	18
<b>Total</b>	<b>1,000</b>

Table 2: Degree of wear. Shoes with light wear have discernible texture. Shoes with moderate wear may show some bald spots and lost texture. Shoes with heavy wear have a near complete loss of texture, many or large bald spots, and possible holes or areas where the outsole has worn away.

Wear	Number
Light	281
Moderate	456
Heavy	263
<b>Total</b>	<b>1,000</b>

Table 3: Presence of microcellular material on the outsole.

Microcellular Material	Number
Present	108
Absent	892
<b>Total</b>	<b>1,000</b>

Table 4: Presence of Schallamach pattern on the outsole.

Schallamach Pattern	Number
Present	743
Absent	257
<b>Total</b>	<b>1,000</b>



Figure 1: Example of outsole and Handprint exemplar scans.

Table 5: Frequency of manufacturer/brand.

Manufacturer/Brand	Number
Adidas	28
Asics	30
Brooks	10
Converse	30
Hoka	36
New Balance	20
Nike	294
Puma	14
Reebok	160
Skechers	12
Under Armour	60
Unknown	26
Other (fewer than 10 shoes)	280
<b>Total</b>	<b>1,000</b>

Table 6: Frequency of men’s and women’s shoe sizes. Note: shoes of unknown size account for the remaining 106 shoes (approximately 10%) of the database. Please note that size includes the full and half size; for example, a size 6 includes size 6 and size 6.5.

Men’s Size	Number	Women’s Size	Number
Size 5	2	Size 4	4
Size 6	4	Size 5	2
Size 7	28	Size 6	10
Size 8	54	Size 7	56
Size 9	148	Size 8	70
Size 10	200	Size 9	46
Size 11	162	Size 10	22
Size 12	62	Size 11	8
Size 13	14	Size 12	2
<b>Total</b>	<b>674</b>	<b>Total</b>	<b>220</b>

Table 7: Frequency of RAC shape categories in 1,000 shoes.

Category	Number	Percentage
Lines/Curves	25,826	45%
Irregulars	22,092	38%
Circles	6,288	11%
Triangles	3,242	6%
<b>Total</b>	<b>57,426</b>	<b>100%</b>



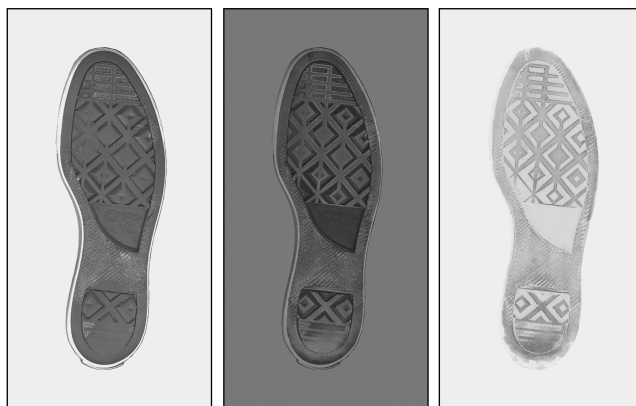


Figure 2: Registered and background subtracted outsole scan (left) and Handprint scan (right). The middle image is an overlay of the outsole and Handprint illustrating co-registration.



Figure 3: Registered and marked Handprint image (left) and resulting RAC map (right).

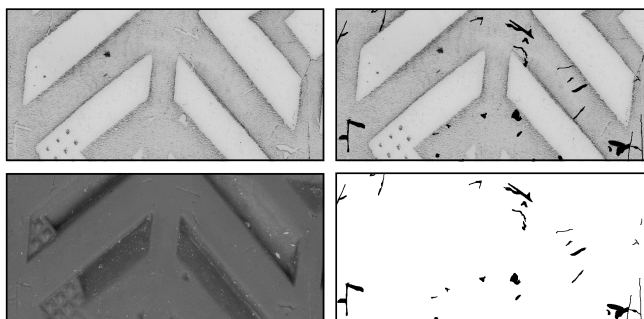


Figure 4: Example of a selected portion of the Converse Chuck Taylor<sup>®</sup> All Star<sup>®</sup>. Handprint (top left), outsole (bottom left), marked Handprint (top right), RAC map (bottom right). Note that the outsole image shown in this figure has been scanned on a flat bed scanner, but that all RACs were detected using 4X magnification and oblique illumination.

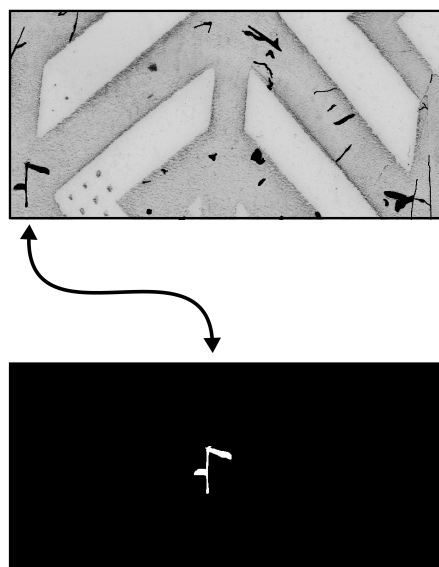


Figure 5: Subsection of RAC map and example of connected component subimages. This particular RAC was numbered #101, located at a normalized radius of 0.55 and an angle of 104°

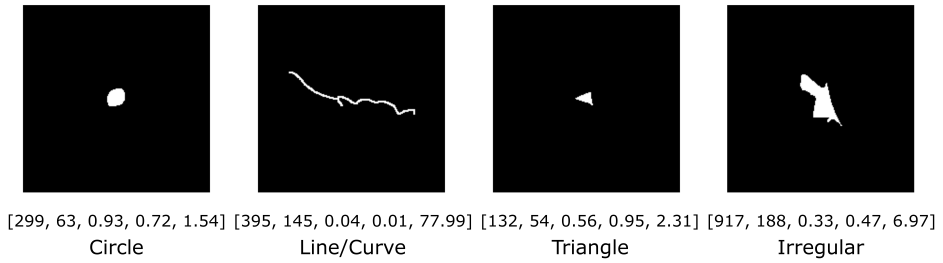


Figure 6: Four RAC images with their corresponding feature vectors [area, perimeter, circularity, triangularity, linearity].

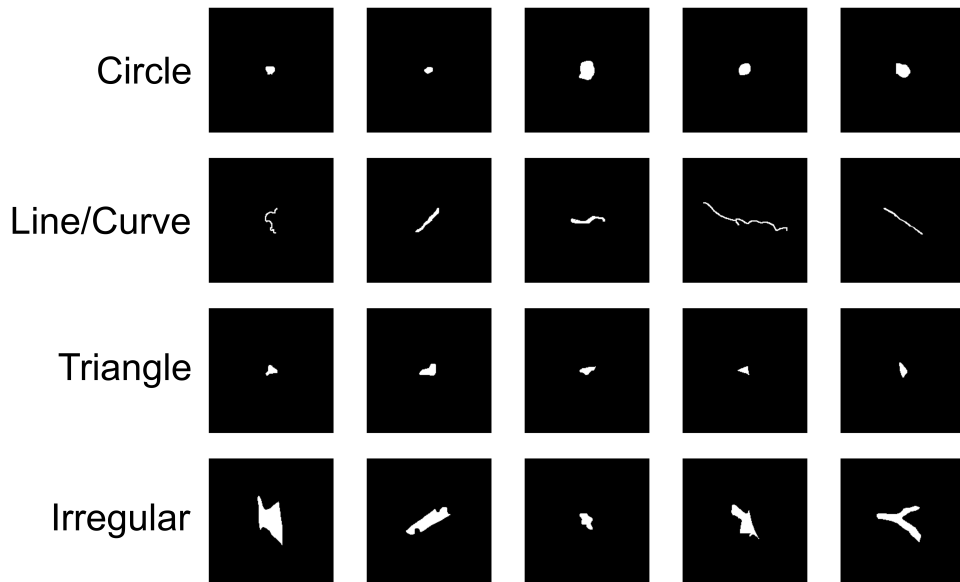


Figure 7: Examples of RACs classified as circles, lines/curves, triangles, and irregulars.

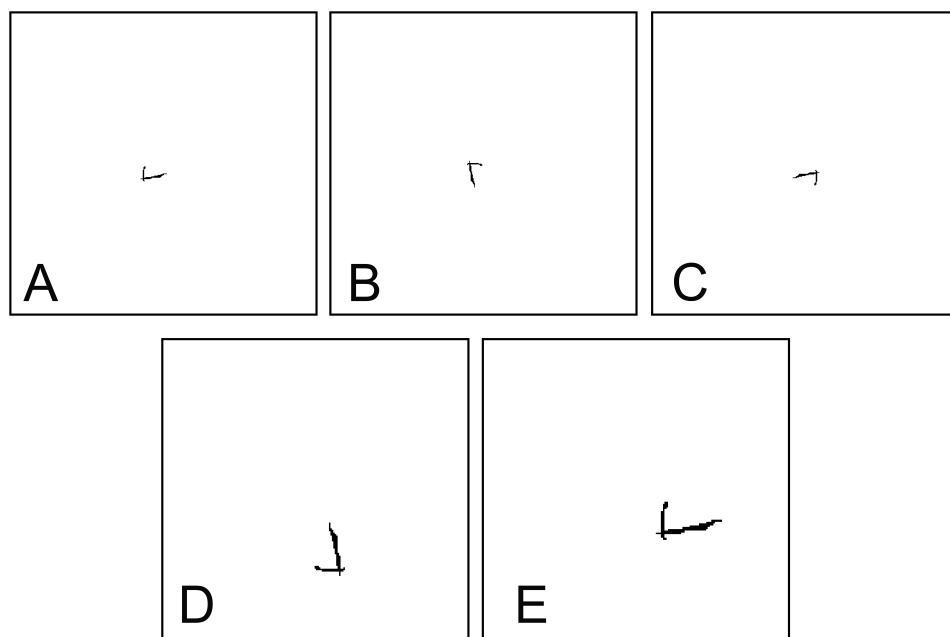


Figure 8: (A) Original RAC, (B) Rotated, (C) Rotated, (D) Rotated, Translated, and Scaled (E) Scaled and Translated.

### Normalized Shape

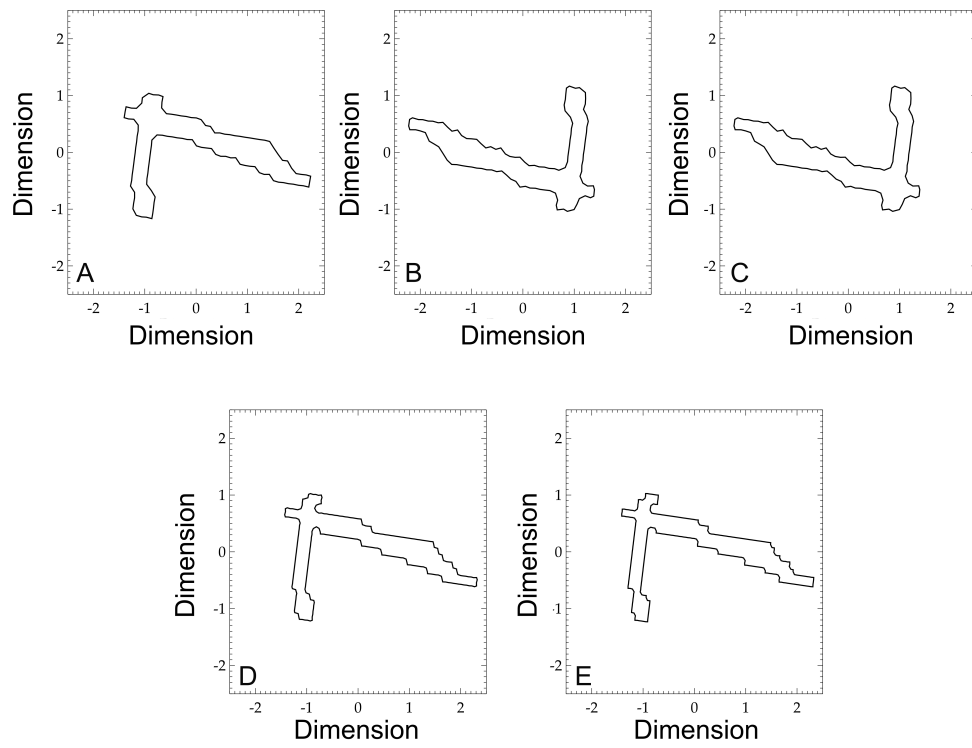


Figure 9: Plot of normalized Fourier shapes derived from the RACs shown in Fig. [8].

Description	Any Shape	Irregular	Circle	Triangle	Line/Curve
Total: In Database	57,426	22,075	6,287	3,242	25,822
Total: In Cell	86	35	12	0	39
Chance of Finding RAC in Cell	1:667	1:1,640	1:4,785	1:-,142	1:1,472

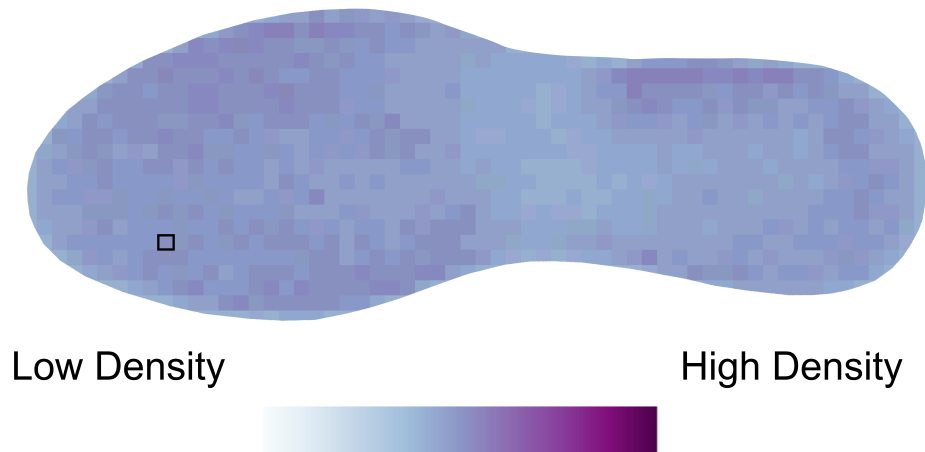


Figure 10: Static illustration of web-based heat map for a normalized shoe. Numerical values in the top row of the associated frequency table remain constant regardless of the user's interaction with the heat map, displaying data associated with total RAC count for the entire database (regardless of cell location). Conversely, the middle and bottom rows automatically update to display RAC count and frequency for individual cells (5mm x 5mm) when queried by the user. In this static example, the results are shown for a single cell outlined in black near the toe. Note that the normalized shoe was a size 10 men's Reebok® walking shoe with an area of  $21,235mm^2$ .

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### **3. POC**

# Classification of Footwear Outsole Patterns using Phase Only Correlation. Part I: Baseline Performance

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## Abstract

Successful classification of questioned footwear has tremendous evidentiary value; the result can minimize the potential suspect pool and link a suspect to a victim, a crime scene, or even multiple crime scenes to each other. To date, several different automated, semi-automated and user-driven classification models have been developed and discussed in the primary literature. Although each approach has demonstrated some level of success, most are multi-phased and susceptible to failure owing to one or more weaknesses in the image processing chain. Furthermore, there have been limited attempts to compare and quantify success when confronted with crime scene quality prints. The research presented here examines the performance of a single semi-automated shoeprint classification algorithm (based on Phase Only Correlation (POC)) for the classification of both high quality and crime-scene-like quality impressions. More specifically, the work is divided into two parts. Part I characterizes the baseline performance of POC and the loss in discrimination potential associated with this algorithm when presented with crime-scene-like prints that vary in terms of media (blood and dust), transfer mechanisms (gel lifters), enhancement techniques (digital and chemical) and variations in print substrate (ceramic tiles, vinyl tiles and paper). The results indicate probabilities greater than 0.850 (and as high as 0.989) that positive

samples (known matches) will order higher in a ranked list than negative samples (known non-match) when confronted with mixed media (blood and dust), transfer mechanisms (gel lifters), enhancement techniques (digital and LCV) and variations in print substrate (ceramic tiles, vinyl tiles, and paper). Based on this success, Part II has been initiated to further identify weaknesses. These results are forthcoming, wherein the authors intend to further characterize weaknesses in the image processing chain as a function of scale, translation, rotation, and partial print reproduction to help the footwear examiner better identify *a priori* how best to employ POC for use with crime scene marks.

*Keywords:* Footwear, Database, Classification, Phase Only Correlation, Crime Scene

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## 1 Introduction

2       With the increased popularity of crime solving dramas on television, the  
3 public is much more aware of what crime scene investigators are looking for  
4 while processing a scene. This knowledge, whether accurate or not, has al-  
5 tered the jury's expectations during a criminal trial [1]. If this knowledge  
6 has affected the jury, it is equally likely to have altered how criminals at-  
7 tempt to conceal their crimes, putting greater importance on evidence types  
8 currently outside of the limelight of the media. These alternate forms of  
9 evidence, footwear included, provide information that is critical in linking  
10 suspects to victims, crime scenes, and even multiple crime scenes to each  
11 other. In fact, when the crime scene is void of all other forms of impression

12 evidence, footwear may be the only probative information at the scene. If  
13 present, footwear class and accidental characteristics may afford the analyst  
14 the ability to focus a criminal investigation, link high volume crimes together,  
15 or otherwise provide information vital to the successful resolution of a case.  
16 Ideally, the strength of this linkage will be highly discriminating, which is  
17 often a function of several factors, including the presence of randomly ac-  
18 quired characteristics (RACs). Despite this desired result, linkage based on  
19 accidental characteristics is not always possible, and a common misconcep-  
20 tion is that impression evidence must lead to identification for it to be useful;  
21 on the contrary, class features, if present in sufficient quantity and quality,  
22 can be extremely valuable [2].

23 Presuming little debate over the expressed utility of footwear classification  
24 in forensic investigations, analysts are left with deciding how best to go about  
25 creating and searching a database of possible exemplars. Ideally, this classi-  
26 fication process should be simple, efficient, and automated, thereby freeing  
27 specialized investigators to concentrate on more demanding tasks. Regardless  
28 of the mechanism employed to elicit possible matches, footwear classification  
29 faces many challenges, including low signal to noise ratios (SNR), manufac-  
30 turing variations, limited or partial data, and variability in user-input.

31 *Footwear Classification Challenges:*

32 *Analyst versus Automated Methods*

33 Since shoeprints began being sorted and collected, there has been a use  
34 for reference sets. In 1937 the FBI started a small rubber heel file which grew  
35 into the current reference collection (comprised of thousands of photographs,  
36 catalogs, and digital impressions) [3]. A similar effort was undertaken by the

37 National Police Agency in Tokyo, Japan, also evolving into a computerized  
38 reference collection [3]. However, these are only a collection of images of  
39 shoes, not a way to compare an unknown shoe to a set of exemplars. Since  
40 these inaugural efforts, scientists have progressed from completely manual  
41 comparisons to more automated processes [4–12], but not without encoun-  
42 tering challenges along the way, including the trade-off between efficiency  
43 and accuracy.

44 In order to best evaluate crime scene quality impressions, a classification  
45 method must preserve structural outsole information while simultaneously  
46 reducing or removing noise. For this pattern recognition problem, the human  
47 observer has proven to be exceptionally skillful in every regard. Conversely,  
48 the human programmer must work diligently to overcome recognition loss  
49 when faced with what might seem like trivial differences between two images  
50 with content that varies only in size, image registration, image type (*e.g.*,  
51 photograph, cast, etc.), or signal to noise ratio.

52 For example, the human analyst has little difficulty classifying two shoes  
53 that differ only in physical size, when they match in tread design. Con-  
54 versely, size variation is a particularly difficult issue to tackle in a mathemat-  
55 ical comparison, especially because the size difference can be introduced by  
56 the manufacturer through more than one modification. For instance, shoe  
57 size can be altered by either increasing or decreasing the size of individual  
58 tread elements present on the outsole (*e.g.*, molded soles). Alternatively, the  
59 design of individual tread elements can remain constant, but the totality of  
60 the overall pattern is successively truncated (*e.g.*, die-cut soles) during the  
61 production of smaller sized soles. These size variation changes all depend

62 on the sole production method and what the company's final vision is for  
63 the shoe line. Shoe soles that are stamped out of a large piece of sole ma-  
64 terial will have the same pattern across the entire surface but as the shoe  
65 size increases, the number of repeating elements (*e.g.*, rows, columns, trian-  
66 gles) will also increase [13], thus altering the final appearance of the sole.  
67 Hence, the severity of how shoe size alters the pattern depends heavily on  
68 the above aforementioned manufacturing method. While an examiner can  
69 easily identify two outsoles of the same class, even considering differences in  
70 size or location of tread elements, successful classification with an automated  
71 system under the same conditions must include a mathematical representa-  
72 tion or normalization step for the aforementioned variations in order to avoid  
73 classification failure even under high signal to noise ratio conditions.

74 Another challenge arises when a reference shoe and an unknown are not in  
75 the same image space, specifically in the case of partial impressions. Except  
76 under extreme conditions (*e.g.*, a partial impression of less than a few tread  
77 elements) a footwear analyst can relatively easily account for missing infor-  
78 mation and visually assess region correspondence between two impressions.  
79 However, the same spatial realignment is not as easily or seamlessly achieved  
80 with a computer algorithm in an automated fashion, as evidenced by the  
81 multitude of image registration models currently accessible in the literature  
82 (see review papers by Zitova and Flusser [2003] [14] and Wyawahare et al.  
83 [2009] [15] for details).

84 Additionally, large variations in the appearance of footwear evidence can  
85 complicate outsole classification. As varied as the ways in which shoeprints  
86 can be deposited, are the methods by which they are collected and enhanced.

87 Shoeprint information at a scene can be preserved and documented using a  
88 number of methods, including photography, lifting, and casting of impres-  
89 sions. Examiners (regardless of their level of experience) are innately able to  
90 account for these variations in appearance in order to determine the type of  
91 shoe which made an impression (human observers co-mingle and synthesize  
92 the content of numerous media types on a daily basis (*e.g.*, print, video, cell  
93 phone, Internet)). However, this large variability in evidence collection and  
94 preservation method becomes an obstacle for an automated system, some-  
95 what analogous to the traditional multi-sensor fusion problem (integration  
96 of multiple sensors that vary in terms of signal to noise ratio, temporal res-  
97 olution, spatial resolution, spectral resolution, distortion, perspective, etc.).  
98 In terms of footwear classification, the fusion dilemma is the comparison of  
99 imagery that likewise differs in terms of user-input (exemplar method (*e.g.*,  
100 Handiprint, ink, Magna-brush method), collection preferences (*e.g.*, photo-  
101 graph, digital scan), resolution settings (PPI), dimensionality (2D or 3D),  
102 media (*e.g.*, blood, dust, mud), substrate (*e.g.*, tile, vinyl, carpet, wood-  
103 flooring), enhancement mechanisms (*e.g.*, physical, chemical, digital), etc.).

104 In short, examiners have exceptional pattern recognition skills, even in the  
105 presence of overwhelmingly low signal to noise ratios that are often encoun-  
106 tered when presented with low quality crime scene evidence. Conversely,  
107 automated systems require intentional and robust mathematical solutions.  
108 So why all the effort to accomplish something already elegantly solved by  
109 the evolution of the human observer? Efficiency; for all but the most com-  
110 monly encountered shoes and questioned impressions with the lowest SNR,  
111 manual classification methods are inefficient and impractical in today's rapid



112 forensic discipline. The footwear examiner has extremely specialized pattern  
113 recognition intellect which is better suited toward the skillful comparison  
114 tasks required post-classification. As such, the pursuit and accomplishment  
115 of successful automated classification frees the analyst, allowing her to de-  
116 vote time to other higher-level tasks that cannot be accomplished from the  
117 benefit of today’s ever-expanding computing efficiency.

### 118 *Models Used for Automated Classification*

119 To date, a variety of different classification algorithms have been evalu-  
120 ated for use on footwear impression evidence, including identification of local  
121 interest points in tread elements and correlation of the entire outsole design  
122 [4–12, 16, 17]. While most of these attempts are highly successful when pro-  
123 vided with high signal to noise input, the real test is how well the algorithm  
124 can tolerate degraded and variable imagery.

125 Several of the existing classification methods utilize the Fourier trans-  
126 form in one form or another. Geradts and Keijzer [1996] generated ‘Fourier-  
127 features’ to identify and compare the shape of outsole design elements [16].  
128 Later attempts focused on a fully automated classification process that used  
129 the two-dimensional discrete Fourier transform (DFT), the power spectral  
130 density, and the two-dimensional correlation coefficient as the similarity met-  
131 ric, thus considering the entire outsole design rather than focusing on specific  
132 design features [5, 7]. Gueham et al. [2008] computed a fast-Fourier trans-  
133 form (FFT) on shoeprint images and, after filtering and log-polar mapping,  
134 computed the 2D correlation of the new Fourier magnitudes [18]. Conversely,  
135 some Fourier methods compute a correlation of the Fourier phase informa-  
136 tion to automatically classify outsole patterns [6, 17]. While the magnitude

137 of an image is important, the phase information obtained from the Fourier  
138 transform holds the contextual information necessary for image reconstruc-  
139 tion, thus providing the ability to accurately analyze images of low quality,  
140 which is the most probable form of footwear evidence [19].

141 Moment invariants, a shape description method, are commonly used in  
142 the object recognition field because they can be invariant to rotation, trans-  
143 lation, and scale differences between shapes [20]. For example, AlGarni and  
144 Hamiane [2008] created a feature vector for each shoe that contained seven  
145 Hu moment invariants [8]. Similarly, in order to account for the shape irreg-  
146 ularity and complexity of shoe tread patterns, Xiao and Shi [2008] incorpo-  
147 rated an orthogonal polynomials-based (Zernike moments) shape descriptor  
148 method [7].

149 Another commonly used classification metric utilizes distance metrics to  
150 assess the similarity of feature vectors compiled using information contained  
151 within a shoeprint. Patil and Kulkarni [2009] used a Gabor transform and  
152 Euclidean distance to compare shoeprint images. For this method, images  
153 were convolved with a Gabor filter and a feature vector was constructed for  
154 each shoe. These feature vectors were compared using Euclidean distance,  
155 thus obtaining a similarity score for comparison between images [9]. Beyond  
156 simple distance metrics, statistical values such as the Mahalanobis distance  
157 can be utilized to assess the similarity of outsole textured regions as was done  
158 by Dardi et al. [2009] [10].

159 Another area of study regarding automated classification is local interest  
160 points. For these methods, interest points or features are extracted using a  
161 detector and these points are then mathematically compared using different

162 similarity metrics (*e.g.*, k-nearest neighbors, cosine similarity, etc.) [11, 12].

163       Regardless of the method employed, efficient and automated shoeprint  
164 classification has been extensively explored and success has been achieved,  
165 *though largely on high quality or synthetically degraded impressions*. Unfor-  
166 tunately, few studies have addressed the performance of these algorithms on  
167 crime scene impressions. Of course, algorithm validation is a two-step pro-  
168 cess; if an algorithm fails when presented with high quality imagery, there is  
169 no reason to move on and try to obtain a more realistic indicator of perfor-  
170 mance in the presence of complicated inputs. However, once an algorithm  
171 shows some level of success when presented with laboratory synthetic sam-  
172 ples, it becomes appropriate to identify its strengths and weaknesses and  
173 determine its utility in actual case usage.

174       To date there have been two attempts to evaluate the performance of  
175 different automated methods when presented with crime scene footwear ev-  
176 idence. In 2009, Cervelli et al. [21] sought to compare the performance of  
177 three metrics: power spectral density (PSD) [5], Modified Phase Only Cor-  
178 relation (MPOC) [6], and texture based Mahalanobis distance (MD) [10].  
179 In order to account for a range in print quality, two different sets of shoe  
180 marks were compiled. The first set was comprised of high quality exemplars  
181 with synthetic additions of noise and blur, while the second set consisted of  
182 real crime scene marks. For the synthetic shoe marks, all algorithms per-  
183 formed well, with MPOC exhibiting the best matching capacity [21]. In  
184 almost all cases, the highest MPOC score corresponded to the correct known  
185 match for each query print. However, when real crime scene impressions  
186 were tested, these results quickly diminished, indicating (as expected) that

187 synthetic crime scene marks are not an accurate indicator of an algorithm’s  
188 performance on case quality evidence. Though the correct match percentage  
189 dropped greatly for real crime scene marks, MPOC still out-performed the  
190 other models [21].

191 More recently, Luostarinen and Lehmussola [2014], evaluated the accu-  
192 racy of seven different automatic classification algorithms including PSD,  
193 Fourier transform, Hu’s moment invariants, Mahalanobis distance, Gabor  
194 transform, local interest points with RANSAC, and spectral correspondence  
195 of local interest points [22]. More specifically, these methods were tested us-  
196 ing three different image datasets of differing quality impressions, including  
197 real crime scene marks. Furthermore, partial and rotated prints were exam-  
198 ined using all algorithms [22]. Overall, the method employing local interest  
199 points and RANSAC performed the best. However, many of the algorithms  
200 proved inconsistent and inaccurate when confronted with “non-ideal” input  
201 (*e.g.*, crime scene quality impressions, rotations, etc.) [22]. Again, these  
202 results indicate that laboratory quality prints, although useful as a first-pass  
203 when comparing an algorithm’s potential performance, do little to really al-  
204 low the research analyst to truly understand the strengths and weaknesses  
205 of a given classification metric.

206 In the end, after comparison of a multitude of algorithms, the commu-  
207 nity is still left with much uncertainty as to how best to move forward. In  
208 truth, no single classification algorithm is likely to out-perform all others in  
209 every single scenario. Instead, each metric is multi-phased and susceptible  
210 to failure owing to one or more weaknesses in the image processing chain.  
211 Therefore, the goal of the current work is *not to prove that one algorithm out-*

212 *competes all others*, but to (i.) characterize the loss in discrimination poten-  
213 tial associated with a successful classification algorithm when presented with  
214 crime-scene-like prints, and (ii.) to help identify weaknesses in the image pro-  
215 cessing chain. More specifically, the goal of this work is two-phased. First,  
216 identify an algorithm that shows some level of success and characterize its  
217 baseline performance. Phase Only Correlation was selected as the algorithm  
218 of choice following a detailed literature survey and the work conducted by  
219 Cervelli et al. [2009] (based on the results from Luostarinen and Lehmussola  
220 [2014] local interest points with RANSAC could have been another likely  
221 candidate for study). Second, assess the weakest link(s) in the image pro-  
222 cessing chain associated with the selected algorithm to offer solutions that  
223 may help strengthen and reinforce weaknesses, and when not possible, offer  
224 comment so that the examiner is aware *a priori* of the expected failing.

## 225 **Material and Methods**

### 226 *Experimental Design*

227 A total of sixty-five shoes were selected as high quality controls. When  
228 possible, available defining characteristics associated with each shoe were  
229 recorded, including make, model, size, degree of wear, and the presence of  
230 Schallamach patterns. As necessary, each shoe was gently washed to remove  
231 debris (*i.e.*, this research does not account for the possible presence of tran-  
232 sient RACs such as rocks, gum, etc.). A subset of fifty outsoles were selected;  
233 these were scanned at 600PPI (3 replicates) with a Canon CanoScan8800F  
234 flatbed scanner, downsampled by 10, converted to binary, and transformed  
235 using a Canny Edge Detector [23]. The premise was to test the utility of us-

236 ing a memory-lean, low-resolution, binary edge image as the database proxy  
237 for all image types moving forward. For the remaining fifteen shoes, tradi-  
238 tional Handiprint exemplars (3 replicates) [2] were created and scanned at  
239 600PPI using an Epson Expression 11000XL Graphics Arts Scanner.

240 Using a random number generator, a total of thirty-six shoes were selected  
241 for crime scene print creation. Six analysts of differing heights, weights, and  
242 shoe sizes were selected to aid with crime scene print creation. Each analyst  
243 was randomly assigned 6 shoes (3 for dust and 3 for blood) as illustrated  
244 in Fig. [1]. Each shoe was used to create a crime scene print on different  
245 substrates, which included ceramic tiles, vinyl tiles, clear acetate sheets, and  
246 paper (dust only). Therefore, each analyst created a total of twenty-one crime  
247 scene prints (12 in dust and 9 in blood). The total number of prints created  
248 is detailed in Table [1]. All prints were co-registered using control points to  
249 minimize misclassification as a function of image registration (*Note: POC is*  
250 *a traditional image registration technique and can theoretically be modified to*  
251 *achieve both image registration and classification downstream*).

### 252 *Crime-Scene-Like Print Creation*

253 In order to best replicate crime scene conditions, analysts wore the shoes  
254 and walked over each substrate for the creation of all crime scene prints.

### 255 *Dust Impressions*

256 For creation of dust prints, analysts stepped in a tray of collected vacuum  
257 dust and walked over each substrate. Latent prints on tiles and acetates were  
258 then lifted using black gelatin lifters (13cm x 36cm BVDA Gellifters, Batch  
259 no. 2014198) and covered with the provided clear sheet; impressions on paper

260 were not lifted (Fig. [2]). Subsequently, the covered lifts and the latent  
261 impressions on paper were scanned at 600PPI using the Epson Expression  
262 Graphic Arts 11000XL and enhanced in Adobe®Photoshop®Elements 10 to  
263 increase contrast and minimize noise.

#### 264 *Blood Impressions*

265 Certified pathogen-free human blood was utilized for creation of crime-  
266 scene-like blood impressions. A paper towel was saturated with blood and  
267 analysts stepped onto the paper towel (then over two newspapers in order  
268 to minimize blood pooling), before stepping onto the substrate. These im-  
269 pressions were allowed to dry and then scanned at 600PPI using the Epson  
270 Expression Graphic Arts 11000XL. After initial scanning, the impressions  
271 were enhanced using leuco-crystal violet (LCV), prepared as detailed in [2].  
272 The enhanced impressions were again digitized after drying (Fig. [3]).

#### 273 *Post-Processing*

274 Following crime scene print creation, enhancement, and digitization, all  
275 images were registered and background subtracted [**REF: Technical Note**].  
276 In total, 66 blood and 106 dust prints were available for POC comparisons  
277 (8 dust prints and 2 blood prints were eliminated due to lack of a discernible  
278 tread pattern).

#### 279 *POC Comparison Metric*

280 The Fourier transform  $F[g(x, y)] = G(u, v)$  of a spatial domain image  
281  $g(x, y)$  gives the analyst access to frequency information associated with im-  
282 age amplitude  $A(u, v)$  and phase  $\sigma(u, v)$  as illustrated in Eqs. [1] & [2] where  
283 the subscripts refer to the two images under comparison [17].

284

$$G_1(u, v) = A(u, v)e^{j\sigma(u,v)} \quad (1)$$

$$G_2(u, v) = B(u, v)e^{j\theta(u,v)} \quad (2)$$

285 Once the Fourier transform of each input image has been calculated, the  
 286 Phase Only Correlation can be computed according to Eq. [3] [5–7] where  
 287  $F^{-1}$  is the inverse Fourier transform and  $G_2^*$  is the complex conjugate of  $G_2$   
 288 [17].

$$\begin{aligned} POC_{g_1g_2} &= F^{-1} \left[ \frac{G_1(u, v)G_2^*(u, v)}{|G_1(u, v)G_2^*(u, v)|} \right] \quad (3) \\ &= F^{-1} [e^{j[\sigma(u,v)-\theta(u,v)]}] \end{aligned}$$

## 289 Results & Discussion

290 In order to obtain a baseline for POC performance on outsole classifica-  
 291 tion, replicate high quality exemplars for each method were compared (*i.e.*,  
 292 outsole scans were compared to outsole scans and Handprints were compared  
 293 to Handprints). Of the two, the Handprint exemplar is the more traditional  
 294 impression for comparison. However, the lower-resolution edge image was in-  
 295 cluded with the hope that it would contain sufficient information to support  
 296 a high degree of classification success for two major reasons. First, reduced  
 297 computer storage needs, and second, almost every type of crime-scene print  
 298 can be converted to an edge image (of some variety), potentially reducing  
 299 variations in user-input.



300 For the known match (KM) comparisons, 3 replicates from each shoe were  
301 compared, yielding  $N=195$  scores ( $65(3) = 195$ ). For the known non-match  
302 (KNM) comparisons, a single replicate was used, yielding  $N=1,330$  scores  
303 ( $n(n-1)/2 = 50(49)/2 + 15(14)/2 = 1,330$ ). Fig. [4] illustrates the results  
304 from POC comparisons for high quality KM (solid line) versus KNM (dotted  
305 line) images. Of note is the distinct bimodal shape for the known non-match  
306 scores. The smaller, leftmost peak represents the POC scores of Handprint  
307 KNMs while the larger, broader, and rightmost peak corresponds to the POC  
308 scores for the outsole edge images. Clearly the probability density indicates  
309 that the POC metric prefers the Handprint exemplar as input imagery over  
310 the binary, downsampled edge image exemplars. Based on these results, the  
311 Handprint exemplars were selected as the database image against which all  
312 172 crime-scene-like query images (66 blood and 106 dust) were compared.

313 Fig. [5] illustrates the probability density of the log of match scores for  
314 KM and KNM comparisons of bloody crime-scene-like prints versus high  
315 quality Handprint exemplars. Overall, the KM ( $N=106$ ) scores for blood  
316 are lower than those for high quality impressions. As a result, there is  
317 more overlap between the KM and KNM densities ( $N=106(17)=1,802$  scores)  
318 wherein ambiguous classifications can occur. Fig. [6] shows that the results  
319 from dust exhibit an even larger region of overlap (KM of  $N=66$  scores and  
320  $KNM=66(17)=1,122$  scores), likely due to the decreased signal to noise ratio  
321 expected from dust impressions (and as depicted in Fig. [2]).

322 In order to compare the POC performance for the three datasets, a re-  
323 ceiver operator characteristic (ROC) curve was constructed. Fig. [7] plots  
324 the false positive versus true positive rate for each comparison scenario. In

325 order to evaluate the performance of the classifier, the area under the curve  
326 (AUC) was computed. For a perfect classifier, the AUC=1, indicating perfect  
327 stochastic dominance. Based on the POC results, high quality impressions  
328 exhibit a 0.989 probability that a randomly sampled positive and negative  
329 pair will be correctly ordered in a ranked list. For bloody crime-scene-like  
330 prints, the AUC is slightly lower, with a correct rank probability of 0.974.  
331 However, this probability drops to approximately 0.895 for dusty impressions.

## 332 **Conclusions**

333 The results from this study remain consistent with previous research find-  
334 ings in that POC performs exceptionally well when classifying *high quality*  
335 footwear imagery [21]. In addition, the current work has attempted to gen-  
336 erate a baseline level of performance for POC when presented with relatively  
337 good quality crime-scene-like prints. Results to date demonstrate reasonable  
338 levels of success (AUCs above 0.85) suggesting that the algorithm can han-  
339 dle a degree of variation in media (blood and dust), transfer mechanisms (gel  
340 lifters), enhancement techniques (digital and LCV), and substrate (ceramic  
341 tiles, vinyl tiles and paper).

342 Although these results are quite promising, the authors remain cautious,  
343 acknowledging that many vulnerabilities have yet to be tested. For example,  
344 as can be seen from Figs. [2] & [3], the “crime-scene-like” imagery gener-  
345 ated for this comparisons is still of very respectable quality and, to adopt  
346 a term from analytical chemistry, not nearly able to stress the “the limit of  
347 detection” (LOD) for this algorithm (nor near the limit in quality observed  
348 by a footwear examiner on a routine basis). Moreover, the majority of the

349 test images were more than 80% complete, so future work must assess how  
 350 well partial imagery can be classified. To this end, previous research suggests  
 351 that image overlap (or partials) as low as 30% [24] can still be registered.  
 352 This is extremely promising and suggests that a similar level of success may  
 353 be achieved here, although it is important to note that shoeprint imagery is  
 354 very different from the types of imagery traditionally registered using POC  
 355 (medical and remotely sensed aerial imagery) so it is difficult to discern if  
 356 this level of robustness will translate readily. Also of note is the need to  
 357 move to a fully automated image registration mechanism (capable of han-  
 358 dling variations in scale, rotation, and translation). Since POC is amenable  
 359 to this implementation by conversion to log-polar space, further testing will  
 360 move away from the use of ground control points for registration, testing  
 361 image comparison with a significantly reduced need for user pre-processing  
 362 [25]. These attributes (fully-automated registration, partial prints, and more  
 363 extensive image degradation) are the topic of phase-two moving forward.

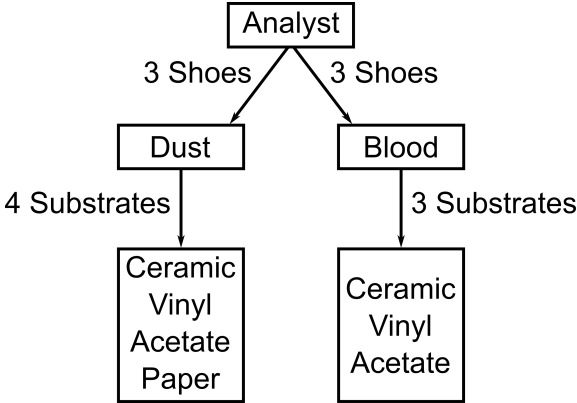


Figure 1: Work flow for crime scene print creation.

Table 1: Total number of crime scene prints created for dust, blood, and blood enhanced with leuco-crystal violet (LCV).

	Ceramic	Vinyl	Acetate	Paper	Total
Dust	n=18	n=18	n=18	n=18	72
Blood	n=18	n=18	n=18	n=0	54
Blood+LCV	n=18	n=18	n=18	n=0	54

364

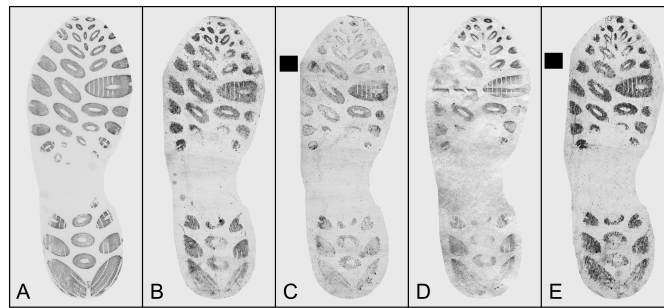


Figure 2: A) High quality exemplar; B) Digitally enhanced dust impression lifted from clear acetate; C) Digitally enhanced dust impression lifted from ceramic tile; D) Digitally enhanced dust impression from paper; E) Digitally enhanced dust impression lifted from vinyl tile. *Note: The sharp edge (denoted by a square) on the toe portion of shoe C) and E) is the demarcation of the gel lifter.*

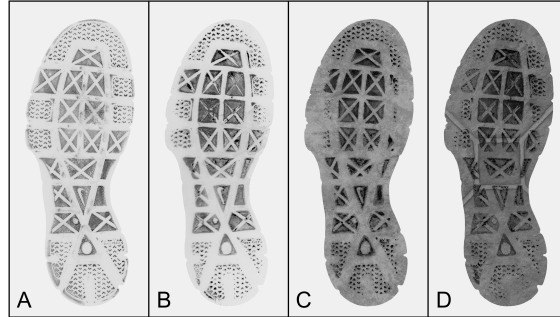


Figure 3: A) High quality exemplar; B) LCV enhanced blood impression on clear acetate; C) LCV enhanced blood impression on ceramic tile; D) LCV enhanced blood impression on vinyl tile.

Probability Density Functions for KM & KNM High Quality Prints

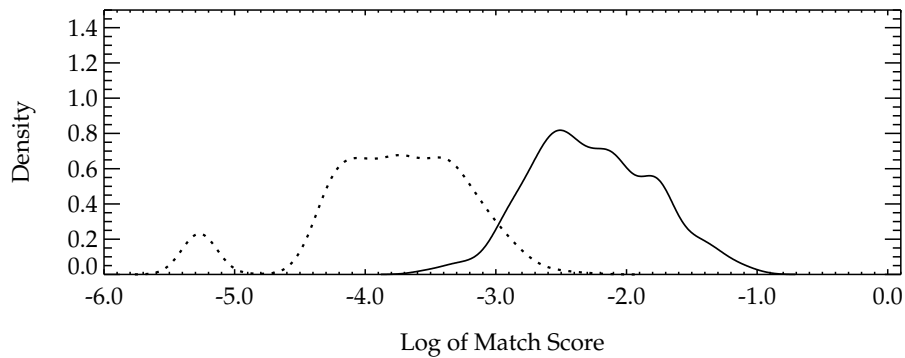


Figure 4: Probability density functions (PDFs) for KM (solid line) and KNM (dotted line) high quality prints. There were  $N=195$  KM comparisons and  $N=1,330$  KNM comparisons for the high quality exemplar dataset. PDFs were constructed using a Gaussian Kernel Density Estimator (KDE). The bin width for each density estimate was set equal to one quarter of the standard deviation of the log of the respective POC scores (or 0.118 for KMs and 0.120 for KNMs).

### Probability Density Functions for KM & KNM Blood Prints

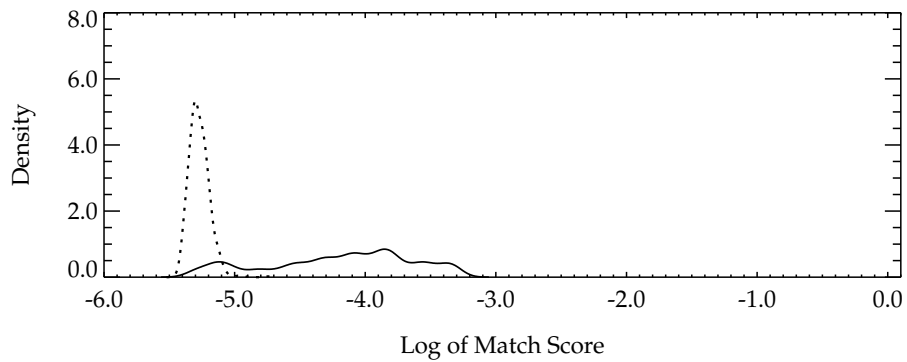


Figure 5: Probability density functions (PDFs) for KM (solid line) and KNM (dotted line) blood prints. There were  $N=106$  KM comparisons and  $N=1,802$  KNM comparisons for the blood print dataset. PDFs were constructed using a Gaussian Kernel Density Estimator (KDE). The bin width for each density estimate was set equal to one quarter of the standard deviation of the log of the respective POC scores (or 0.080 for KMs and 0.011 for KNMs).

Probability Density Functions for KM & KNM Dust Prints

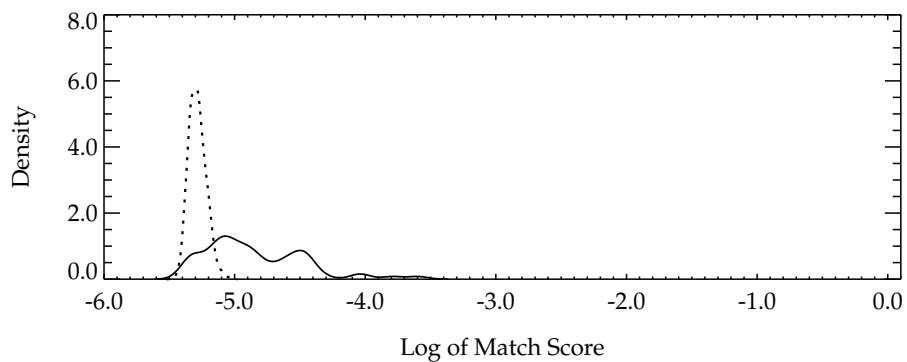


Figure 6: Probability density functions (PDFs) for KM (solid line) and KNM (dotted line) dust prints. There were  $N=66$  KM comparisons and  $N=1,122$  KNM comparisons for the dust print dataset. PDFs were constructed using a Gaussian Kernel Density Estimator (KDE). The bin width for each density estimate was set equal to one quarter of the standard deviation of the log of the respective POC scores (or 0.077 for KMs and 0.009 for KNMs).

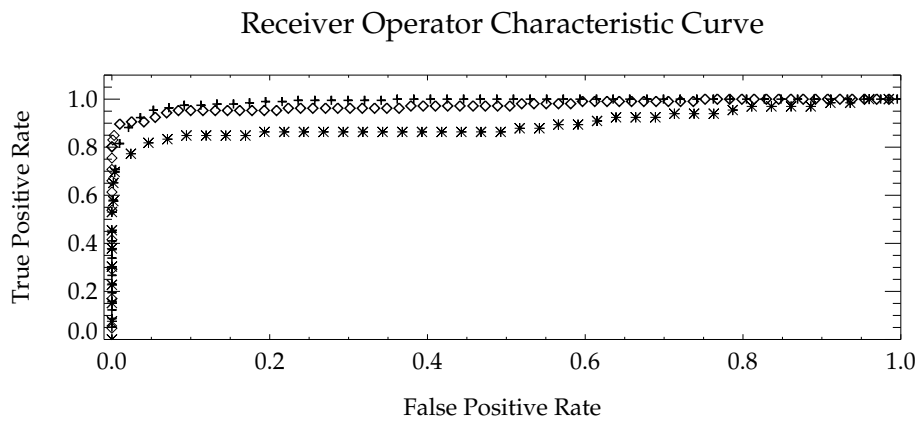


Figure 7: ROC curve for POC results. Crosses represent high quality impressions, diamonds represent the blood prints, and stars represent dust impressions. The area under the curve for high quality impressions is 0.989, for blood impressions is 0.974, and for dust impressions is 0.895.



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## 4. Wet Residue

# Evaluation of shoeprint similarity via analysis of randomly acquired characteristics: A comparison of high quality exemplars and crime scene prints

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## Abstract

Forensic footwear evidence can prove invaluable to a criminal investigation by providing information about the nature of a crime or who may have committed it. However, limited knowledge about the discrimination potential of this evidence can lead to challenges in court. Though experienced forensic footwear examiners agree that these impressions can be just as discriminating as a fingerprint, general acceptance of this assertion can benefit from quantitative research. While there are several studies detailing classification of outsole patterns, these manufacturing characteristics cannot be used for an identification. Instead, randomly acquired characteristics (RACs) must be utilized for this purpose. Although empirical studies exist describing the discriminating power and frequency of these features, there have been limited attempts to characterize the utility of accidentals in crime scene quality prints. Given the dynamic and unpredictable nature of the media, substrate and deposition process encountered during the commission of a crime, RACs on crime scene prints are expected to exhibit a large range of variability in terms of reproducibility, clarity, and quality. This study mathematically compares the presence of RACs in high quality exemplars versus crime-scene-like quality impressions as a function of RAC shape, perimeter,

and area. Furthermore, the total RAC map, a binary representation of all RACs present in an impression, has been used to illustrate the bounds by which crime-scene-like laboratory samples can be linked back to their high quality exemplars. Results indicate that the unpredictable conditions associated with crime-scene print production promotes RAC loss that varies between 33%-100% with an average of 85%, and that this loss increases proportionally as a function of RAC perimeter and area. Furthermore, when the entire outsole is taken as a constellation of features, 64% of the crime-scene-like impressions exhibit 10 or fewer RACs. Despite this, there was a 0.74 probability that the match score for a randomly selected pair of positive (known match) and negative (known non-match) samples would be correctly ranked in an ordered list. Overall, the results indicate that footwear comparisons cannot be reduced to a “simple point counting” procedure; instead, more abstract qualities less amenable to quantitation (such as RAC shape, clarity, and complexity) are extremely important and unmistakably relevant in the comparison process.

*Keywords:* Footwear, Randomly Acquired Characteristics, Accidentals, Frequency, Shape Descriptors, Feature Vectors, Crime Scene

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## 1 Introduction

2 Footwear impression evidence, which is left at almost every crime scene,  
3 can be invaluable for forensic scientists in order to link a suspect to a crime  
4 scene or reconstruct the series of events leading up to a crime. In order to  
5 maximize the utility of this evidence, it is therefore necessary to understand

6 how to properly evaluate and interpret footwear impression evidence. To this  
7 end, several studies have examined the individuality and utility of three ma-  
8 jor aspects of footwear impressions: class, subclass, and randomly acquired  
9 characteristics [1–9], the latter of which are the specific focus of this research.  
10 Of these three attributes, class characteristics (outsole design, size of outsole  
11 elements, and shoe dimensions) are the least discriminating. In combination,  
12 these features can greatly aid in narrowing down the possible sources of a  
13 given impression by excluding shoes of a given size, brand, model, etc., how-  
14 ever, they cannot be used for identification of source [10]. When present,  
15 subclass characteristics (*e.g.*, air bubbles, stippling, remnants of inconsis-  
16 tent mixing of outsole material), which are a result of the manufacturing  
17 process that may vary for different shoes or molds, can provide additional  
18 means to reduce the set of possible sources for footwear impression evidence  
19 [11]. Through the use of class and subclass characteristics, an examiner may  
20 be able to eliminate an extremely large number of possible source shoes,  
21 greatly narrowing the number of reasonable leads and possible contributors  
22 in a criminal investigation. However, to determine a more precise likeness  
23 and actual source attribution between a questioned and known footwear ex-  
24 emplar, the examiner must proceed to compare the quantity, quality, clarity  
25 and complexity of what are termed accidental or randomly acquired char-  
26 acteristics (RACs) (*e.g.*, tears, nicks, stones, holes, etc.). If these features  
27 have reproduced in the crime scene print, and are in “sufficient agreement”,  
28 the examiner is permitted to reach an actual identification of source. To  
29 reiterate and borrow a statement from the appellate court in the case of the  
30 State of Illinois vs. Charles A. Campbell [1991], “*shoe print evidence may*



31 *be as reliable and as trustworthy as any other evidence...even one individual*  
32 *characteristic, depending on the nature and uniqueness, could be enough for*  
33 *a valued comparison” [10].*

34 Since source attribution is a function of RACs, an active area of research is  
35 how best to demonstrate the degree to which information contained within  
36 shoeprints (specifically accidental features) are random and variable [6–9].  
37 Much of this work has been affirmative of previous assertions (high discrimi-  
38 nation) when conducted on high quality impressions or with theoretical data,  
39 however, there has not been a focused effort to determine how this discrimi-  
40 nation might vary as a function of RAC size or shape under dynamic print  
41 production. As such, this study focused on quantifying RAC loss and varia-  
42 tion during the production of crime-scene-like prints in order to better char-  
43 acterize the bounds by which case prints can be linked back to their high  
44 quality exemplars.

#### 45 *Sources of Variability in Footwear Impression Evidence*

46 Numerous factors can affect the appearance of footwear impressions col-  
47 lected in criminal investigations. Consequently, examination and interpreta-  
48 tion of this evidence is innately challenging and requires extensive training  
49 and accumulated expertise. More specifically, the entire process tends to  
50 be influenced by variations in print creation, collection, and enhancement,  
51 and in order for analysts to reasonably compare crime scene impressions to  
52 high quality exemplars obtained from suspect shoes, it is imperative that the  
53 sources of variability be understood and accounted.

54 *Creation of Crime Scene Impressions*

55 Despite the numerous methods of crime scene print creation, there are  
56 two major classes: two- and three-dimensional. Within each of these classes,  
57 however, exist a number of different factors which can contribute greatly to  
58 the variability present in the appearance of crime scene shoeprints.

59 Two-dimensional impressions include those which sit on top of a surface  
60 and have no discernible depth [12]. Positive impressions result from a transfer  
61 of material from the outsole to a substrate; examples include prints in blood,  
62 grease, and dust [10]. Conversely, a negative impression is left when an  
63 outsole lifts a residue from a surface. These often occur when a clean shoe  
64 comes into contact with a dirty surface and removes accumulated dirt or  
65 dust from the substrate. For negative impressions, the outsole elements are  
66 depicted in the void pattern. Clarity and quality of the impression often  
67 depends on the surface of deposition (*i.e.*, a waxed floor tile will likely capture  
68 a more detailed impression than carpet) as well as the media in which the  
69 print is made (*e.g.*, blood, grease, dust, etc.) [12].

70 Conversely, three-dimensional impressions result in deformation of the  
71 surface, resulting in an impression with depth. These prints can be found in  
72 soil, sand, and snow and the detection, preservation, and forensic utility of  
73 these impressions vary depending on a multitude of environmental conditions,  
74 including substrate composition [13, 14].

75 *Collection and Enhancement of Impressions*

76 Given the variability in the initial appearance of footwear impressions,  
77 the methods for collecting and enhancing this evidence can differ greatly de-  
78 pending on the conditions of deposition. For example, two-dimensional prints

79 are lifted to improve visibility and allow further examination, while three-  
80 dimensional impressions are often cast in order to preserve the entire depth  
81 of the impression [15]. Furthermore, the lifting method employed depends  
82 on the material deposited as well as the substrate containing the impression  
83 (*e.g.*, electrostatic lifters for dry impressions on non-porous surfaces, gelatin  
84 lifters for wet origin prints on non-porous surfaces [16–18]).

85 In addition to collection of crime scene prints for examination, enhance-  
86 ment methods may be employed to maximize visual detail. In general, im-  
87 pressions can be enhanced in four major ways: chemically, physically, digi-  
88 tally, or via electromagnetic radiation. In order to increase contrast between  
89 the impression and the background, chemical methods are carefully selected  
90 depending on the material in which the print is deposited, as well as the  
91 substrate properties. Extensive research exists detailing which methods are  
92 appropriate in a variety of scenarios [19–23]. Likewise, physical enhancement  
93 can be utilized to maximize contrast. This technique involves increasing con-  
94 trast via the use of powders [10]. For example, by applying a fingerprint  
95 or fluorescent powder to an impression on a waxed surface, the evidence  
96 will retain the powder and can be easily distinguished from the background.  
97 Further, digital enhancement techniques can be used alone or in conjunction  
98 with another technique. These methods aim to use computer programs to in-  
99 crease image quality by maximizing the signal to noise ratio, thus increasing  
100 the amount of information available to the analyst for comparison purposes  
101 [24, 25]. Lastly, enhancement via electromagnetic radiation includes the use  
102 of specialized light sources (*e.g.*, ultraviolet, infrared, etc.) to maximize con-  
103 trast of the impression against the background and therefore increase the

104 clarity and detail of evidence [26–29].

105       Given the inherent variability and complexity of footwear impression de-  
106 position, as well as the number of physical factors which can influence the  
107 appearance of prints (*e.g.*, media, substrate, enhancement methods, etc.),  
108 it is reasonable to expect variability in the appearance (clarity, quality, de-  
109 tail, etc.) of crime scene evidence. In short, a crime scene impression will  
110 rarely be an exact replicate of the source shoe or a corresponding high qual-  
111 ity exemplar print. More specifically, the RACs which are visible in a high  
112 quality image are unlikely to consistently reproduce in crime scene evidence  
113 impressions. This is especially true given that RACs show variability in re-  
114 production among high quality replicates even when prepared under ideal  
115 conditions in the laboratory! In fact, to account for this inherent variation,  
116 several replicate exemplars are typically created in the laboratory for both  
117 case and research purposes [5, 8], which further exemplifies the need to better  
118 understand RAC variation as a function of shape, perimeter, and area.

## 119 **Methodology**

120       Using a random number generator, 50 pairs of shoes were selected from  
121 a total of 400 to be used for crime scene print creation.

### 122 *Pre-Processing*

123       Available defining characteristics associated with each shoe were recorded,  
124 including make, model, size, manufacturer product code, degree of wear and  
125 the presence of Schallamach patterns. As necessary, each shoe was gently  
126 washed to remove easily dislodged debris (*i.e.*, this research does not account  
127 for the possible presence of transient RACs such as rocks, gum, etc.). When

128 dry, each outsole was scanned at 600PPI with an Epson Expression 11000XL  
129 Graphics Arts Scanner. Post-outsole scanning, Handprint exemplars were  
130 created [10], and each exemplar was likewise scanned at 600PPI.

### 131 *Exemplar Processing*

132 In order to facilitate the automated downstream extraction of RAC shape  
133 and position, the outsole and exemplar were background subtracted and reg-  
134 istered using identified control points as detailed in [REF: Technical Note].  
135 Post-registration and background subtraction, randomly acquired character-  
136 istics present on both the outsole and exemplar were marked and subse-  
137 quently localized [REF: Technical Note]. Each feature was then auto-  
138 matically numbered and extracted from the total RAC map using connected  
139 components. The resulting subimages were then evaluated to define RAC  
140 shape and geometry based on a 5-dimensional classification feature vector,  
141 and then finally transformed into individual RAC Fourier descriptors (FD)  
142 [REF: Technical Note].

### 143 *Crime-Scene-Like Print Creation*

144 Five analysts of differing heights, weights and shoe sizes were selected  
145 and randomly assigned 10 pairs of shoes to aid in print creation. In order  
146 to best replicate crime scene conditions, each analyst wore the shoes when  
147 creating impressions (*note that this methodology differed from that used in*  
148 *exemplar creation which entailed pressing an outsole onto an adhesive sheet*).  
149 Each outsole was lightly covered with shoe polish and analysts walked four  
150 steps over clear acetate sheets, thereby creating two replicate impressions per  
151 shoe for a total of 200 crime-scene-like quality prints. Each impression was

152 then developed using black magnetic powder (Lightning Powder Co. Black  
153 Magnetic 1-0160) and lifted using white gelatin lifters (13cm x 36cm BVDA  
154 Gellifters, Batch no. 2015033). Fig. [1] illustrates one “best case” and one  
155 “worst case” reproduction scenario.

#### 156 *Processing of Crime-Scene-Like Prints*

157 After lifting, all impressions were scanned at 600PPI with an Epson Ex-  
158 pression 11000XL Graphics Arts Scanner. The lifters were afixed to a scan-  
159 ning board designed to raise the gel surface off the scanner bed by approxi-  
160 mately 1mm, thus allowing for clear, focused prints without direct interaction  
161 between the lifter and the scanner’s glass surface. After scanning, lifts were  
162 covered and stored for future reference.

163 The digitized crime-scene-like print images were then background sub-  
164 tracted and registered to the corresponding high quality exemplars using  
165 identified and corresponding control points [**REF: Technical Note**]. This  
166 process ensured that all images (outsole scan, exemplar and both crime-  
167 scene-like impressions) were co-registered in the same image space.

168 Following registration and background subtraction, RACs on the crime-  
169 scene-like prints were marked and localized [**REF: Technical Note**]. Each  
170 individual RAC was again automatically numbered and saved into an indi-  
171 vidual file via connected components. Finally, feature vectors were created  
172 detailing RAC shape parameters and location information [**REF: Technical**  
173 **Note**].

174 *Identification of Known Match RAC Pairs*

175 In order to compare RACs, it was necessary to identify correspondences  
176 between accidentals on high quality exemplars and crime-scene-like prints.  
177 This was accomplished using RAC subimage location information. Features  
178 from the exemplars were automatically nominated as candidate matches if  
179 the angular ( $\theta$ ) and normalized radial value ( $r_{norm}$ ) fell within  $1 - 2^\circ$  and  
180 0.1, respectively, of the corresponding  $\theta$  and  $r_{norm}$  for the crime-scene-like  
181 RAC [**REF: Technical Note**]. These thresholds were selected in order to  
182 minimize loss of candidate RAC mates, which were subsequently manually  
183 verified (and adjusted as necessary) before moving forward. Fig. [2] illus-  
184 trates a set of these known match pairs, as well as the corresponding location  
185 information for each accidental.

186 *Similarity Metrics*

187 Five metrics were used to analyze the similarity of known match crime  
188 scene to high quality RAC pairs. These metrics were Modified Phase Only  
189 Correlation (MPOC), matched filter (MF), a modified cosine similarity (MCS),  
190 Hausdorff distance (HD), and Euclidean distance (ED).

191 *Modified Phase Only Correlation (MPOC)*

192 The Fourier transform  $F[g(x, y)] = G(u, v)$  of a spatial domain image  
193  $g(x, y)$  gives the analyst access to frequency information associated with im-  
194 age amplitude  $A(u, v)$  and phase  $\sigma(u, v)$  as illustrated in Eqs. [1] & [2] (where  
195 the subscripts reference the images under comparison and  $i = \sqrt{-1}$ ) [30].

$$G_1(u, v) = A(u, v)e^{i\sigma(u, v)} \quad (1)$$

$$G_2(u, v) = B(u, v)e^{i\theta(u, v)} \quad (2)$$

197 Once the Fourier transform of each input image has been calculated, the  
 198 Phase Only Correlation can be computed according to Eq. [3] [2, 3, 31]  
 199 where  $F^{-1}$  is the inverse Fourier transform and  $G_2^*$  is the complex conjugate  
 200 of  $G_2$  [30].

$$\begin{aligned} POC_{g_1 g_2} &= F^{-1} \left[ \frac{G_1(u, v)G_2^*(u, v)}{|G_1(u, v)G_2^*(u, v)|} \right] \\ &= F^{-1} [e^{i[\sigma(u, v) - \theta(u, v)]}] \end{aligned} \quad (3)$$

201 Eq. [3] can be modified by application of a frequency filter that selectively  
 202 limits frequencies used in the computation such that  $F[g(x, y) \cdot h(k, l)] =$   
 203  $G(u, v)$ . In this instance, each image  $g(x, y)$  was modified by the windowing  
 204 function shown in Eq. [4] with  $\alpha = 0.2$  and where  $k = l = N$  which is the  
 205 size of the RAC image in pixels (1600 x 1600):

$$\begin{aligned} h(k) &= \alpha - (1 - \alpha) \cos \left[ \frac{2\pi k}{N} \right] \\ k &= 0, 1, \dots, N - 1 \end{aligned} \quad (4)$$

#### 206 *Fourier Descriptors (FD)*

207 With the exception of MPOC which was computed using 1600 x 1600  
 208 pixel imagery, all remaining similarity metrics were based on perimeter in-  
 209 formation. More specifically, the RAC was treated as a closed planar figure



210 yielding a Fourier description (FD) [32–34]. This description was gener-  
 211 ated by tracing the contour of the shape  $(x(t), y(t))$  where  $t = 0, \dots, N - 1$   
 212 with  $N = 350$ ) and assuming a complex plane  $z(t) = x(t) + iy(t)$  (where  
 213  $i = \sqrt{-1}$ ). The resulting one-dimensional complex sequence of numbers  
 214 was then mapped to the frequency domain via the discrete Fourier transform  
 215 [33] where  $R_m$  and  $\theta_m$  are the magnitude and phase of the  $m^{\text{th}}$  coefficient,  
 216 respectively [33]:

$$\begin{aligned} Z(m) &= \sum_{t=0}^{N-1} z(t) e^{-i2\pi mt/N} = R_m e^{i\theta_m} \\ m &= -N/2, \dots, -1, 0, 1, \dots, N/2 - 1 \end{aligned} \quad (5)$$

217 The coefficients were then transformed to ensure invariance to translation,  
 218 and contour/sequence start point according to the following modifications  
 219 [33]:

$$\begin{aligned} Z(0) = 0 &\quad \Rightarrow \text{translation invariance} \\ \theta_m = \theta_m + m \frac{\theta_{-1} - \theta_1}{2} &\quad \Rightarrow \text{start point invariance} \end{aligned} \quad (6)$$

220 *Matched Filter (MF)*

221 The matched filter similarity metric between two shapes  $Z_1(m)$  and  $Z_2(m)$   
 222 was computed as illustrated in Eq. [7] [35] where  $Z(m)$  is normalized accord-  
 223 ing to  $\frac{Z(m)}{\sqrt{\sum_t |z(t)|^2}}$  such that 0.0 is the minimum (least similar) and 1.0 is the  
 224 maximum (most similar):

$$m = \operatorname{argmax} \left| \frac{1}{N} \sum_{t=0}^{N-1} Z_1(m) Z_2(m) e^{i2\pi mt/N} \right| \quad (7)$$

225 *Modified Cosine Similarity (MCS)*

226 Cosine similarity is a commonly used metric that can assess the simi-  
 227 larity between two data vectors [36]. For two *similar* inputs  $a$  and  $b$ , the  
 228 resulting angle ( $\theta$ ) between them will be small. Conversely,  $\theta$  is large for two  
 229 dissimilar inputs. Since the RAC perimeters are defined as FDs (or complex  
 230 numbers  $z = x + iy$ ), each complex vector was reduced to its magnitude  
 231  $|z| = \sqrt{x^2 + y^2}$  before employing the traditional cosine computation shown  
 232 in Eq. [8], where ( $T$ ) represents the transpose of a vector.

$$\theta = \cos^{-1} \left[ \frac{a^T b}{\sqrt{a^T a} \sqrt{b^T b}} \right] \quad (8)$$

233 *Euclidean Distance (ED)*

234 Euclidean distance was the fourth metric employed for comparison. The  
 235 distance ( $D$ ) between elements in the complex vectors is obtained as detailed  
 236 in Eq. [9], where  $x_1$  and  $y_1$  denote the real and imaginary parts of the first  
 237 vector, respectively [36]. Likewise,  $x_2$  and  $y_2$  denote the real and imaginary  
 238 parts of the second vector for comparison, respectively. The total distance  
 239 is normalized by dividing the summation by the maximum number of ele-  
 240 ments in the vectors ( $N = 350$  for this dataset), yielding an average distance.  
 241 Naturally, as elements become more dissimilar, the distance between them  
 242 increases.

$$D = \frac{1}{N} \sqrt{\sum (x_1 - x_2)^2 + \sum (y_1 - y_2)^2} \quad (9)$$

243 *Hausdorff Distance (HD)*

244 Using the Euclidean distance, Hausdorff distance was likewise computed.  
245 This is more of a variant of ED than a truly unique computation since ED  
246 was used “under-the-hood” in the HD computation (instead of a new metric  
247 such Manhattan distance, but this is something that can be remedied moving  
248 forward). In this computation, the distance ( $d(a, b)$ ) is computed between a  
249 point (*e.g.*,  $a_1$ ) on the perimeter of RAC ( $A$ ) and all points on the perimeter  
250 of RAC ( $B$ ) (Fig. [3]) using any desired distance metric (such as ED). Fol-  
251 lowing all computations, the smallest distance from  $a_1$  to  $B$  is retained. This  
252 process is then repeated for all points on  $A$  (*i.e.*,  $a_2 \dots a_n$ ), wherein  $h(A, B)$ ,  
253 or the maximum of these minimums, is retained [37]. This same process is  
254 repeated to compare all points on RAC perimeter vector  $B$  to those on RAC  
255 perimeter vector  $A$ , thus obtaining  $h(B, A)$ . The actual distance HD is then  
256 the maximum of these two values ( $h(A, B)$  and  $h(B, A)$ ) as illustrated in Eq.  
257 [10].

$$H(A, B) = \max\{h(A, B), h(B, A)\} \quad (10)$$

$$\text{where } h(A, B) = \max_{a \in A} \{\min_{b \in B} \{d(a, b)\}\}$$

258 *RAC Map Correlation*

259 In addition to individual RAC characterization and comparison, the entire  
260 RAC map for each crime-scene-like print was compared back to its high  
261 quality exemplar to determine a “*global similar metric*” or the degree to  
262 which the wet-residue images could be linked back to their source. This was  
263 accomplished using image-wide Phase Only Correlation according to Eq. [3]  
264 (without windowing), and on full RAC maps 8691 x 8691 pixels in dimension.

265 **Results & Discussion**

266 *RAC Loss*

267 Given the inherent inconsistency present in shoeprint creation, such as  
268 pressure, torque, substrate, etc., it is expected that reproduction of RACs in  
269 crime-scene-like quality prints will be variable in comparison to high quality  
270 exemplars collected by pressing a dusted outsole against an adhesive sheet,  
271 thus ensuring full and even contact. Based on the results from this study, an  
272 average of 85% of RACs were not reproduced in crime-scene-like impressions  
273 (Table [1]). In addition, zero RACs were reproduced in 10% of the images  
274 (20 out of 200 impressions).

275 Loss was further broken down by shape, perimeter, and area to determine  
276 if RAC reproduction varied as a function of any of these factors. As detailed  
277 in Table [2], RAC loss (77% - 84%) exhibited very little variation across shape  
278 classes. However, greater variation can be observed as a function of RAC size.  
279 Generally, as a feature's size increased (in either total area or perimeter), the  
280 percent loss decreased (Tables [3] & [4]). This matched intuition in that  
281 "larger" defects are likely to persist and withstand the variation introduced  
282 during reproduction in a crime scene setting as compared to smaller features  
283 that may be more easily occluded by erratic conditions (such as differences  
284 in media, substrate, motion, etc.). Overall, Tables [1] - [4] suggest one major  
285 outcome. As with fingerprint comparisons, there is no scientific basis on  
286 which to demand a minimum number of features in order to judge source  
287 attribution in footwear comparisons. Moreover, the utility of an accidental  
288 feature should not be reduced to a simple counting exercise; its presence  
289 (and therefore its "*uniqueness*") should not be reduced to an independent

290 wear-related event that is multiplied to provide a cumulative probability of  
291 occurrence among a constellation of other RACs on a randomly selected  
292 outsole. By the same token *a RAC's absence is not a valid reason for an*  
293 *exclusion, ergo, absence of evidence is not evidence of absence.*

#### 294 *Individual RAC Similarity*

295 Five metrics were utilized to determine similarity between crime-scene-  
296 like RACs and their high quality mates (MPOC, MF, MCS, HD, and ED).  
297 This study assessed the differences in scores as a function of RAC shape,  
298 perimeter, and area. The results were illustrated in two ways: binned bar  
299 plots and probability density functions (PDFs). The bar plots display trends  
300 in the data and allowed for comparison via Chi-square tests. However, the  
301 binning process inherently fragmented the data, so full probability density  
302 functions (PDFs) were also constructed using Gaussian kernel density esti-  
303 mators (KDEs) to allow for an unabridged view of the spread in scores for a  
304 given set of conditions.

#### 305 *Similarity as a Function of RAC Shape*

306 Differences in similarity scores based on RAC shape were detected for  
307 MPOC and MCS as per the Chi-square test [38] with  $\alpha = 0.05$ . In other  
308 words, the similarity scores for different shapes were significantly different  
309 from those expected if the variables were independent.

310 For MPOC, circles exhibited higher similarity scores, while lines and  
311 curves exhibited lower similarity scores (Figs. [4] & [5]). This trend was  
312 significant for all binned scores and is believed to be a function of rotational  
313 variation. For example, a circular RAC can tolerate orientation differences

314 reasonably well (*i.e.*, no matter how you rotate a circle, the distance between  
315 features remains relatively consistent, as illustrated in Fig. [6]). Conversely,  
316 an elongated feature, when rotated, is likely to exhibit a drastic decrease  
317 in correlation between its known match. As such, a metric such as MPOC  
318 (with a theoretical maximum of 1.0) is likely to show higher dissimilarity for  
319 linear RAC features unless forced to be rotationally insensitive.

320 Dependence in similarity scores for RAC shape were also detected for  
321 MCS  $\theta$  values. As illustrated in Figs. [7] & [8], circles have the greatest den-  
322 sity in smaller angular bins, while lines and curves dominant in frequency  
323 for larger angular bins. This difference is again likely due to rotational vari-  
324 ations. As a circular object rotates, its overall appearance and orientation  
325 (and therefore similarity with another circular object) is likely to remain  
326 relatively unchanged (Fig. 6). However, if a linear RAC is skewed, the ori-  
327 entation of the feature is likewise changed, again resulting in feature vectors  
328 with detectable differences.

329 The remaining similarity metrics (MF, ED and HD) were not found to  
330 depend on RAC shape. The dependence of MPOC and MCS (as well as the  
331 lack of dependence of MF, ED and HD on RAC shape) are equally signif-  
332 icant results. For example, one might argue that circular features are less  
333 discriminating than linear features. The premise for this argument is that  
334 circular features have more degrees of freedom compared to linear features,  
335 and that this assertion is especially true if you begin to consider features in  
336 combination (*e.g.*, comparing two circles versus two lines with some fixed spa-  
337 tial relationship). However, it is also likely that not all metrics are equally  
338 sensitive to these differences, proving that *numerical* metrics of similarity,

339 although *objective* and *impartial*, are still *biased* estimators that require ex-  
340 ploration, testing and understanding before deployment.

#### 341 *Similarity as a Function of RAC Size*

342 Differences in similarity scores based on RAC size (perimeter and area)  
343 were detected for MPOC as per the Chi-square test [38] with  $\alpha = 0.05$ . In  
344 other words, the similarity scores for different sized RACs were significantly  
345 different from those expected if the variables were independent. For MPOC,  
346 small features exhibited high similarity scores, while large RACs exhibited  
347 lower similarity scores when compared to their known match mates (Figs.  
348 [9] & [10] and [11] & [12]). This likely occurred because large features can  
349 reproduce as several, smaller, and segmented versions of their original more-  
350 complex self when created under variable crime-scene-like conditions (Fig.  
351 [13]). Due to this phenomena, each individual smaller segment from the  
352 crime-scene-like RAC may compare back to a single larger feature in the  
353 high quality impression, yielding a lower numerical score. This serves to  
354 reinforce the ultimate need for an examiner’s subjective interpretation dur-  
355 ing the comparison process. Although an automated metric can provide a  
356 baseline numerical assessment of a known match that can be very beneficial  
357 moving forward, this illustration shows that a “low” *objective* similarity score  
358 still requires expert interpretation. In this instance, a visual comparison and  
359 explanation by the examiner is likely to be much more illuminating to the  
360 jury and layperson, and arguably more defensible, than a mathematical clar-  
361 ification of the reason for a low score.

362 Another interpretation of this result is that the larger the RAC, the more  
363 discriminating its potential. In other words, a single RAC, of sufficient qual-

364 ity, complexity, and similarity to a source is so unusual that its significance  
365 warrants source attribution. Can you *quantify* the degree of belief in this as-  
366 sertion with any degree of certainty? Only if you were comfortable answering  
367 this question based on the probability of encountering this score in the tail of  
368 a density estimated using a Gaussian KDE based on 200 samples. In other  
369 words, this research can be of tremendous benefit to the footwear examiner  
370 to help support courtroom testimony and conclusion protocols, but not as  
371 an automated and numerical substitute.

372 In addition to the differences detected by MPOC as a function of size, ED  
373 also exhibited differences in similarity scores as a function of perimeter (Figs.  
374 [14] & [15]), but the opposite trend was noted. Namely, as RAC size (area and  
375 perimeter) decreased MPOC scores were more likely to increase (exhibiting  
376 greater similarity). Conversely, as RAC size (perimeter) decreased ED scores  
377 were more likely to increase (exhibiting greater dissimilarity) (*note that this*  
378 *dependence was only found to be significant for ED scores between 0.01-0.02*  
379 *and greater than 0.05 for  $\alpha = 0.05$ ). A hypothesis for this observation is pos-  
380 sible interpolation effects. This research was conducted using pixel images,  
381 rather than vector graphics. Consequently, each RAC exists on a grid with  
382 the smallest subunit being a square picture element  $42\mu m$  in size. When  
383 this feature is digitally captured for analysis, the resulting imagery includes  
384 both *inherent* fluctuations in reproduction due to variations in deposition  
385 conditions, as well as *unavoidable* inter- and intra-analyst variation from the  
386 marking phase. The end result is “jitter” (or perhaps more aptly termed,  
387 *deviation from nominal*).*

388 If this RAC is to then be compared, it is important to note that many



389 similarity metrics require pre-standardization such as feature vectors of a  
390 constant size. If so, interpolation may be needed (*e.g.*,  $N=350$ ). When re-  
391 quired, minute differences from previous steps (real or analyst-based) are  
392 likely to be accentuated as a function of RAC size as shown in Fig. [16].  
393 In this illustration, although both marked RACs (small versus large) have  
394 only a single pixel difference between them, the variation in the interpolated  
395 perimeter images are markedly different. The large RAC, with a greater  
396 number of points across its perimeter is only minimally affected by interpo-  
397 lation. However, the smaller the feature, the greater the artifact observed on  
398 the perimeter, at least in theory. Since this assertion is easily tested, a small  
399 study is currently underway to test this hypothesis and better characterize  
400 the divergence in results for MPOC and ED as a function of perimeter.

#### 401 *RAC Map Correlation*

402 Table [5] reports the total frequency of RACs in the binary maps (as well  
403 as the corresponding high quality impressions). These maps were obtained  
404 during the subtraction process and are a binary representation of all acci-  
405 dentals observed on an impression. The POC was computed on all possible  
406 RAC map pairs to estimate a *global* similarity score. Results are provided  
407 as a receiver operator characteristic (ROC) curve displaying the true pos-  
408 itive and false positive rate (Fig. [17]). The area under the curve (AUC)  
409 indicates the probability of a randomly selected known match RAC map ex-  
410 hibiting a higher similarity score than a known non-match map (stochastic  
411 dominance). Based on the POC metric, there was a 0.74 probability that  
412 the match score for a randomly selected pair of positive (known match) and  
413 negative (known non-match) samples would be correctly ranked in an or-

414 dered list. Given that 64% of the query crime-scene-like maps contained 10  
415 or fewer RACs for comparison (Table [5]), these results indicate that even  
416 with a minimal amount of accidental transfer, matching RAC maps will rank  
417 higher than non-matching maps approximately 74% of the time. This result  
418 is staggering and lends very strong support to the claim that footwear ev-  
419 idence is extremely discriminating, especially given that an average of 85%  
420 of the identified randomly acquired characteristics failed to transfer to the  
421 questioned impressions. Again, although there is no scientific basis for a min-  
422 imum number of required characteristics for source attribution, these results  
423 suggest a multitude of future studies combining POC, RAC number, and  
424 RAC description (complexity, size, category (line, circle), etc.) in order to  
425 better characterize this very interesting trade space.

## 426 **Conclusions**

427 The results from this study suggest that reproducibility of RACs, in  
428 number and appearance, can vary greatly when comparing high quality and  
429 crime-scene impressions. Given that approximately 85% of these accidentals  
430 became obscured in the deposition process, it is clear that a “simple point  
431 counting” procedure cannot be used when assessing source attribution.

432 Furthermore, the correlation of RAC maps, from crime-scene-like impres-  
433 sions to high quality exemplars, offers additional support that the informa-  
434 tion contained within accidentals (*i.e.*, shape, size, and complexity) supplies  
435 greater evidence for source attribution than a simple presence, or count, of  
436 features. This is especially true considering that 64% of the crime scene  
437 prints exhibited 10 or fewer features, but that 74% of the time they ex-

438 hibit stochastic dominance. Since POC mimics some of the low-level spatial  
439 processing conducted by an experienced footwear examiner during the com-  
440 parison process, the results indicate that source attribution is possible even  
441 when presented with *very few accidentals* provided the existing RACs exhibit  
442 sufficient discrimination potential in terms of shape, size, and complexity.

443 Mathematically, the results of MPOC and MCS reported lower similarity  
444 scores for linear features as compared to circular features. This is believed to  
445 be a function of both metric's sensitivity to orientation differences. However,  
446 this sensitivity was not observed for all metrics (MF, HD, nor ED). If the  
447 concept that circular features have more degrees of freedom tends to mirror  
448 an examiner's intuition when attributing significance to RACs, then it is  
449 important to evaluate the sensitivity of numerical metrics of similarity to  
450 best understand their strengths and weaknesses. Interestingly, a strength of  
451 a similarity metric when comparing known non-matches may very well be  
452 a weaknesses for the metric when comparing known matches (pushing the  
453 threshold for exclusions too high and generating too many false negatives).  
454 In contrast, an examiner can dynamically adjust this threshold as necessary,  
455 whereas doing so in an objective sense is much more difficult.

456 Moreover, quantitative results can actually disagree. For example, the  
457 ED results presented here were opposite to those of MPOC in that small  
458 features appeared more dissimilar than large features as a function of RAC  
459 perimeter. Whether or not this is genuine, or a function of interpolation, must  
460 be further tested. However, the major point is that while an examiner can  
461 easily associate two features with differences in appearance due to deposition  
462 or marking variability, an algorithm is forced to make a decision based on

463 pixel differences, and this can become challenging depending on imaging  
464 constraints. The end result proves that numerical and objective metrics are  
465 in no way a panacea for subjective assessment, and much more research is  
466 required. Instead, the authors propose a complementary relationship between  
467 examiner expertise and quantitative metrics that in combination can best  
468 define the degree of belief in source attribution for footwear evidence. What  
469 this might look like and how it might best serve the forensic community has  
470 yet to be defined. Clearly it is a long-term goal, and instead, the focus of  
471 short-term goals will be to better understand the quantitative trade space.

Table 1: Quantifying RAC loss between high quality exemplars and replicate crime-scene-like impressions.

RACs	High Quality	Crime Scene Rep 1	Crime Scene Rep 2
Total Number	6,896	1,049	1,110
Number Lost	-	5,847	5,786
Percent Lost	-	85%	84%
Mean Number per Shoe $\pm 1$ standard deviation	$69 \pm 72$	$10 \pm 12$	$11 \pm 12$
Maximum Number	307	66	61
Minimum Number	2	0	0

Table 2: RAC loss between high quality exemplars and replicate crime-scene-like impressions as a function of RAC shape.

Shape	Total HQ RACs	Lost HQ RACs	% Loss
Circle	1,024	863	84%
Line/Curve	2,685	2,239	83%
Irregular	2,732	2,173	80%
Triangle	455	348	77%

Table 3: RAC loss between high quality exemplars and replicate crime-scene-like impressions as a function of RAC perimeter.

Perimeter	Total HQ RACs	Lost HQ RACs	% Loss
1-2mm	2,936	2,623	89%
2-4mm	2,413	1,939	80%
4-6mm	828	599	72%
6-8mm	337	217	64%
>8mm	382	245	64%

Table 4: RAC loss between high quality exemplars and replicate crime-scene-like impressions as a function of RAC area.

Area	Total HQ RACs	Lost HQ RACs	% Loss
0.0-0.25mm <sup>2</sup>	3,994	3,548	89%
0.25-0.5mm <sup>2</sup>	1,408	1,080	78%
0.5-0.75mm <sup>2</sup>	589	419	71%
0.75-1.0mm <sup>2</sup>	294	201	68%
1.0-2.0mm <sup>2</sup>	391	253	65%
>2.0mm <sup>2</sup>	220	122	55%

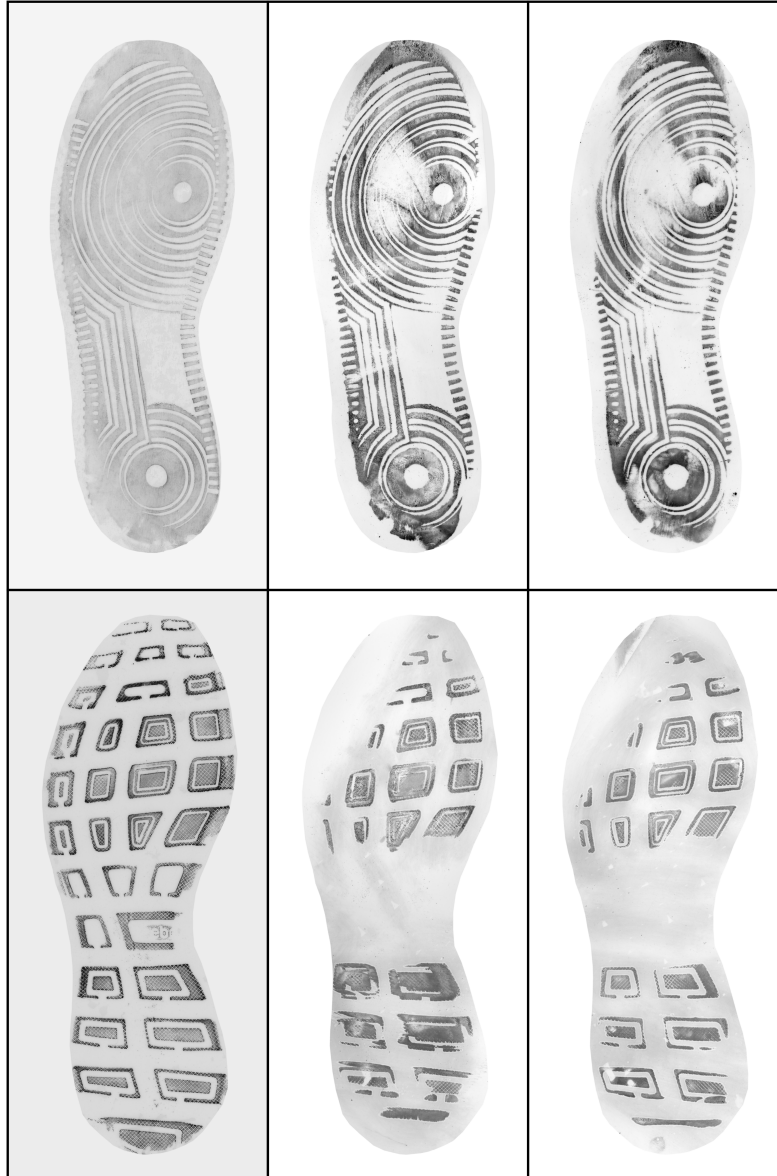


Figure 1: Top row illustrates one “best case” scenario and bottom row displays one “worst case” scenario for crime-scene-like impression production. Handprint exemplar (left) and two crime-scene-like replicates (center, right).

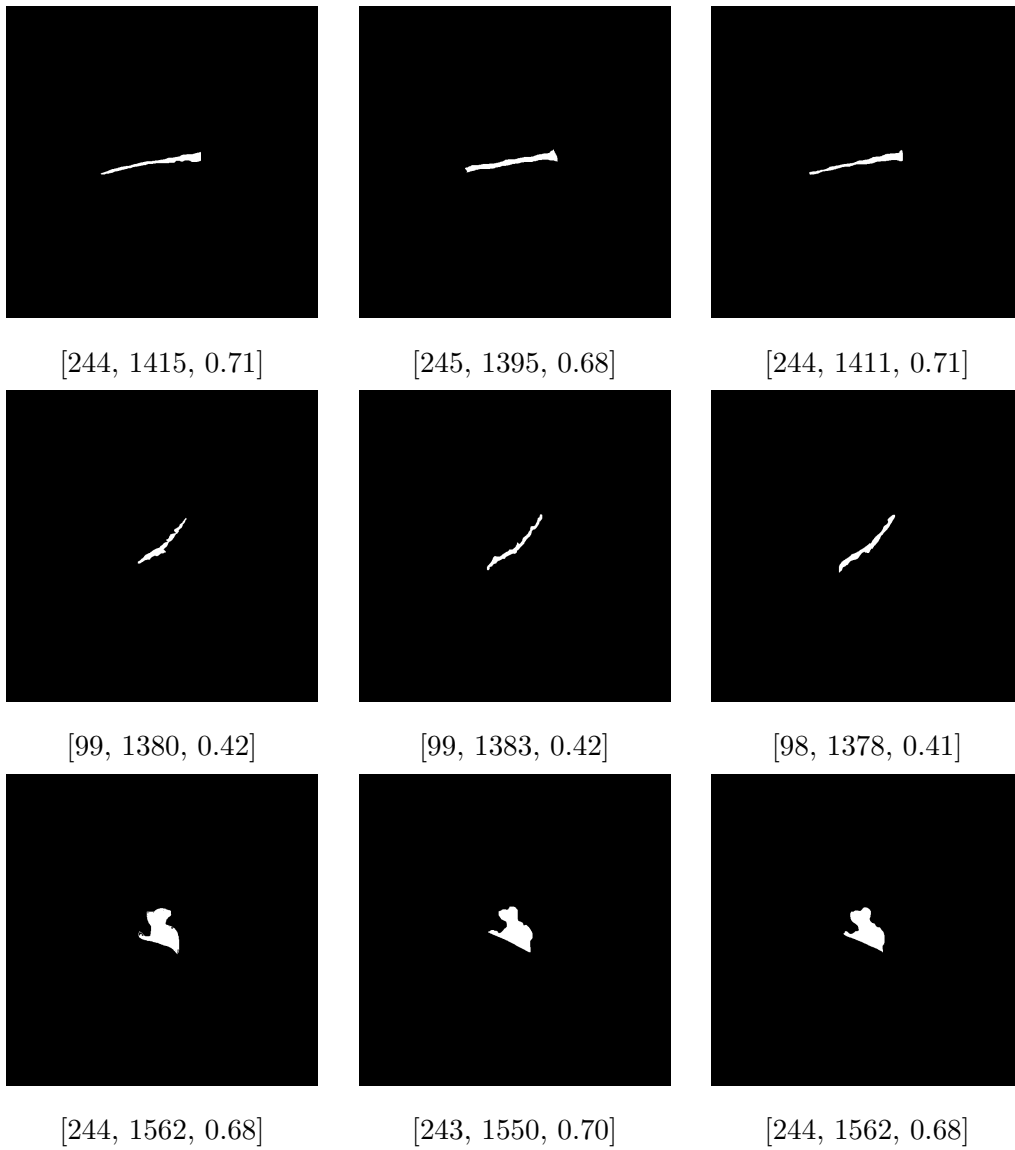


Figure 2: RAC image mates with their corresponding location information  $[\theta$  (degree),  $r$  (pixel),  $r_{norm}$ ]. High quality RAC image (right) with its detected crime scene RAC mates, one from each replicate (center, right).



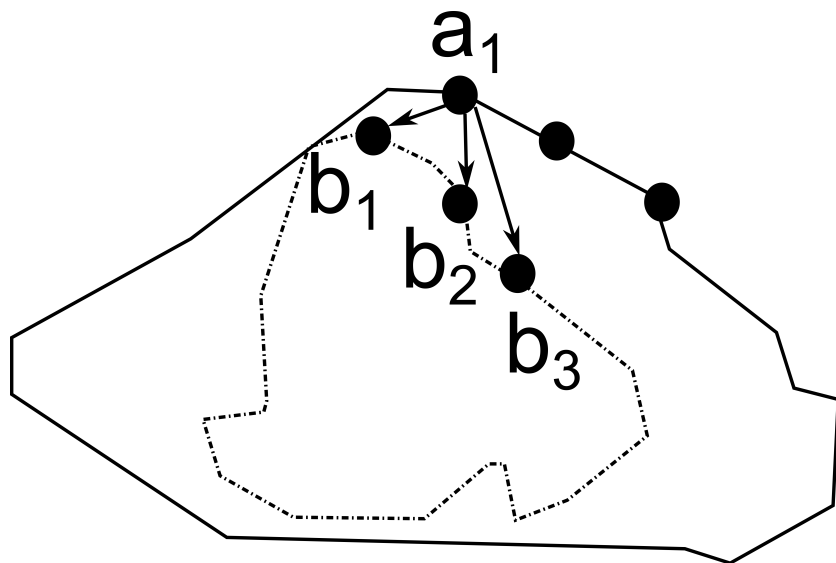


Figure 3: Two stylized RACs illustrating computation of Hausdorff distance for point  $a_1$ .

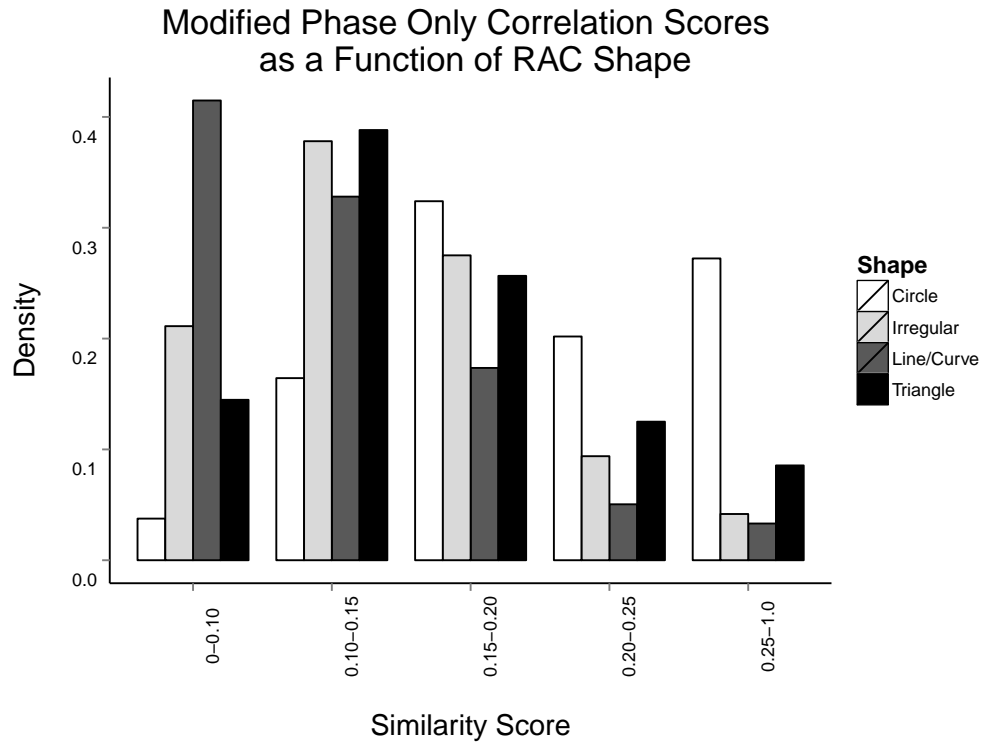


Figure 4: MPOC scores as a function of RAC shape. Circles generally have high similarity scores, while lines and curves exhibit lower similarity scores. Based on the Chi-square results, significant differences in similarity scores as a function of shape existed within all bins.

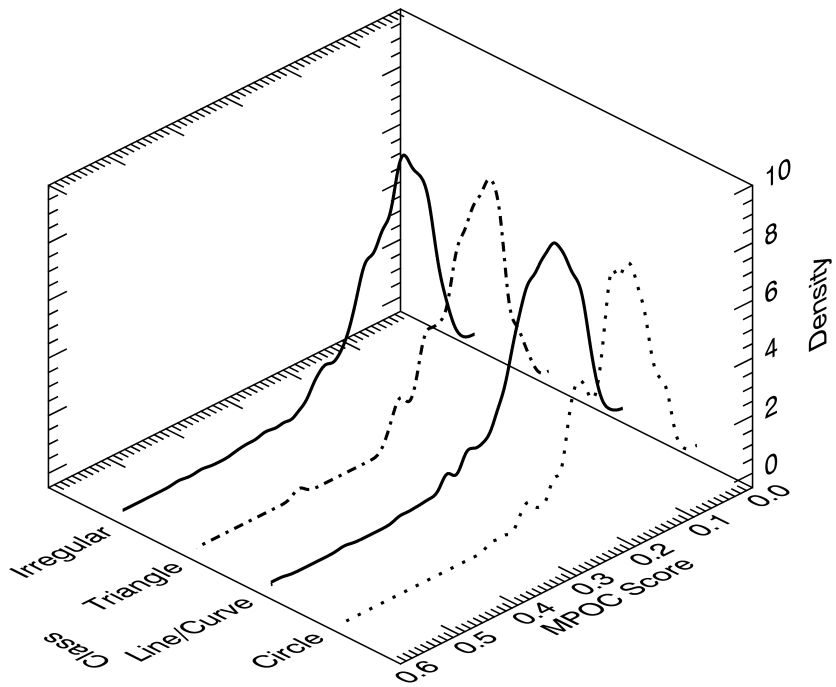


Figure 5: Probability density functions for MPOC scores as a function of RAC shape, obtained using a Gaussian kernel density estimator. Bin width information can be found in the Appendix.

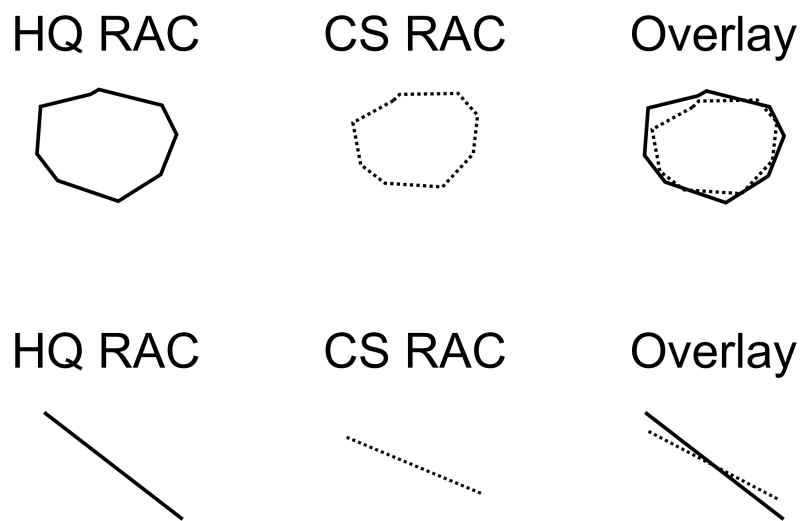


Figure 6: Example of stylized high quality (HQ) and crime scene (CS) RACs. Note that lines exhibit greater discordance (overlap very little) than circular shapes when orientation differences exists (scale and rotational differences are shown for maximum emphasis).

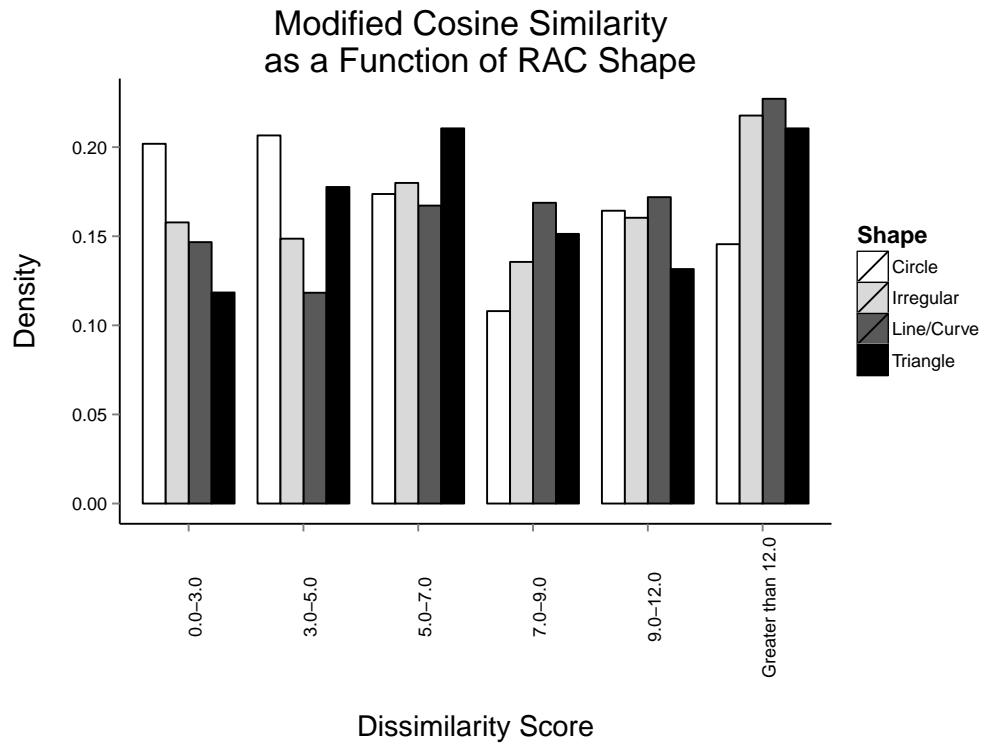


Figure 7: Modified Cosine Similarity scores as a function of RAC shape. The largest differences in RAC similarity scores, as a function of shape, exist in the bins which describe more similar features (*i.e.*, cosine angles of less than  $5^\circ$ ). Based on the Chi-square results significant differences in MCS scores as a function of shape existed for scores ranging from  $3-5^\circ$ .

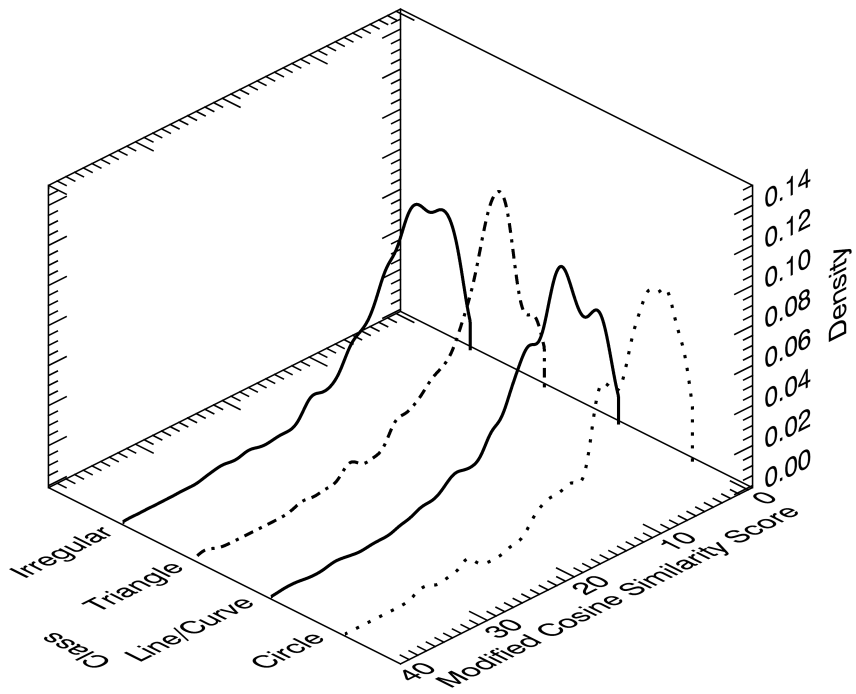


Figure 8: Probability density functions for MCS scores as a function of RAC shape, obtained using a Gaussian kernel density estimator. Bin width information can be found in the Appendix.

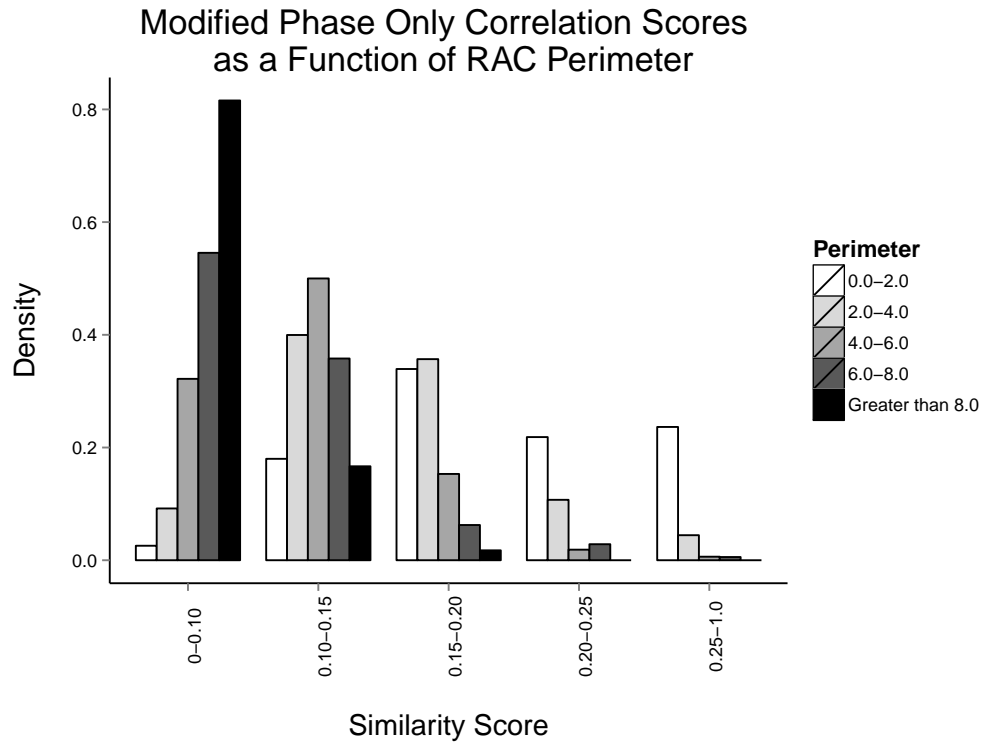


Figure 9: MPOC scores as a function of RAC perimeter. Based on MPOC, very large RACs are very dissimilar. Based on the Chi-square results, significant differences in similarity scores as a function of perimeter existed within all bins.

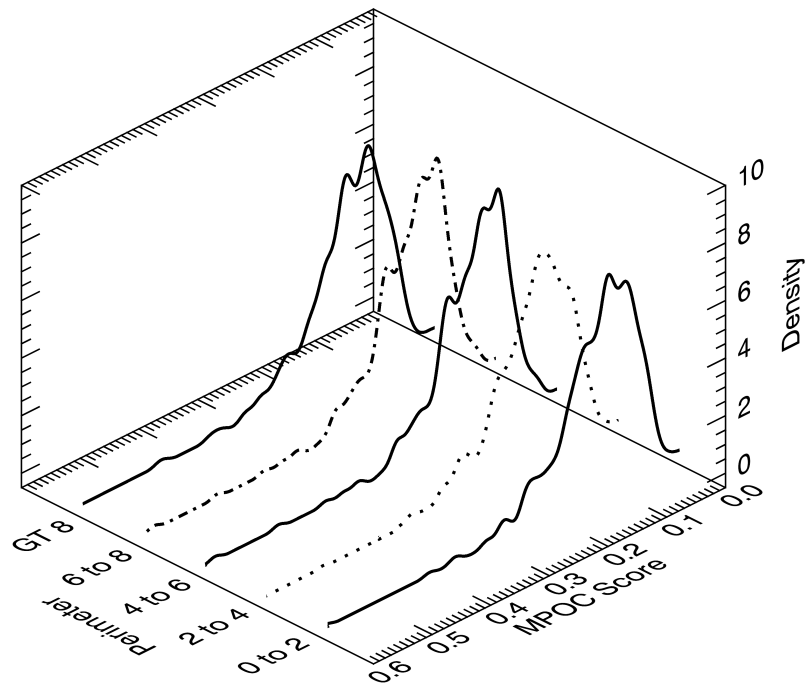


Figure 10: Probability density functions for MPOC scores as a function of RAC perimeter, obtained using a Gaussian kernel density estimator. Bin width information can be found in the Appendix.



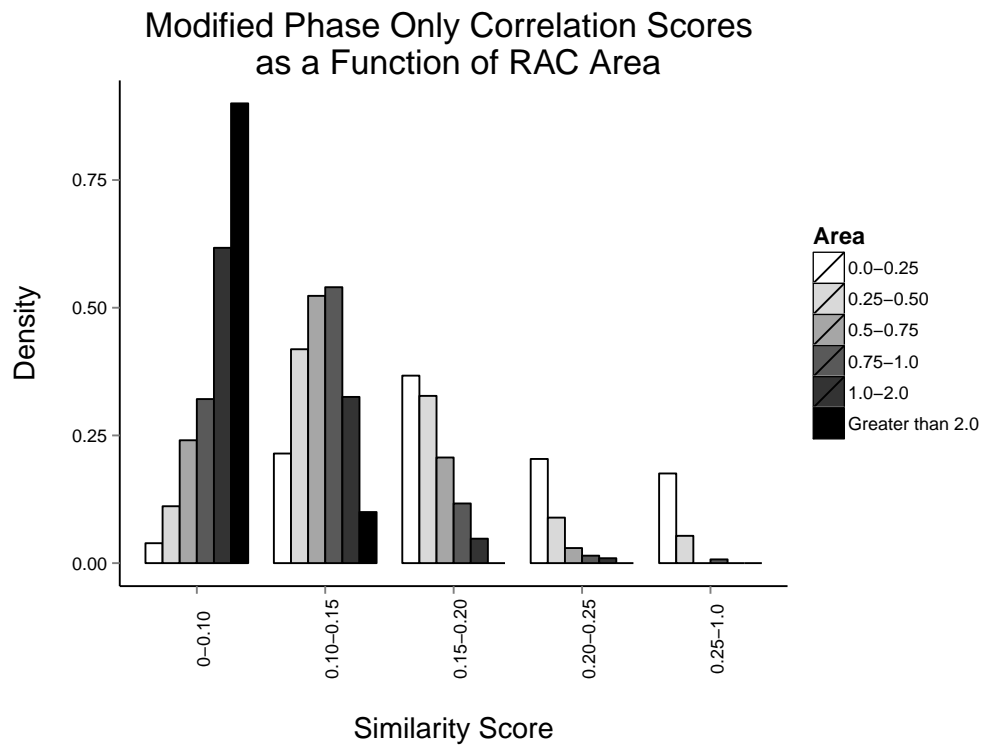


Figure 11: MPOC scores as a function of RAC area. Based on MPOC, very large RACs are very dissimilar. Based on the Chi-square results, significant differences in similarity scores as a function of area existed within all bins.

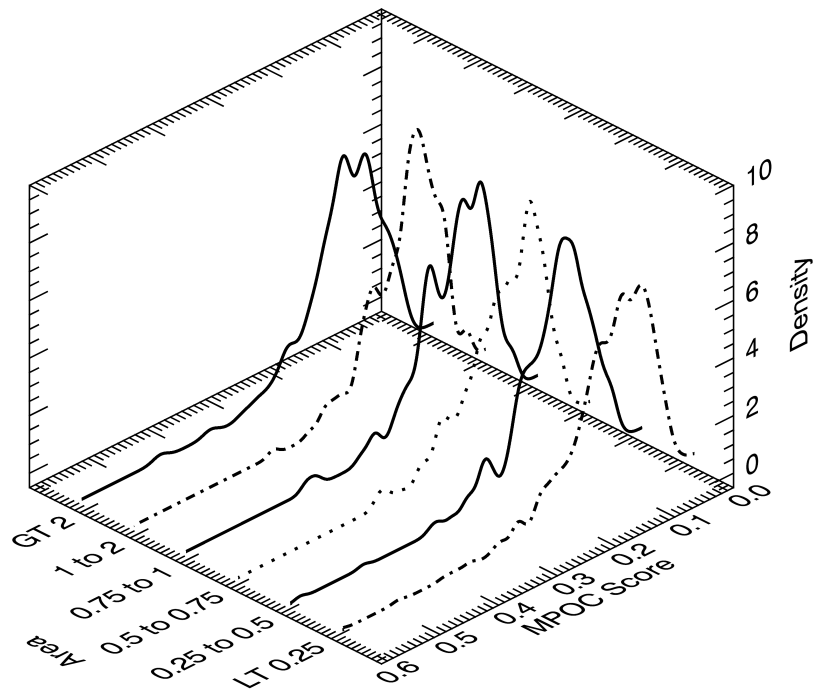


Figure 12: Probability density functions for MPOC as a function of RAC area, obtained using a Gaussian kernel density estimator. Bin width information can be found in the Appendix.

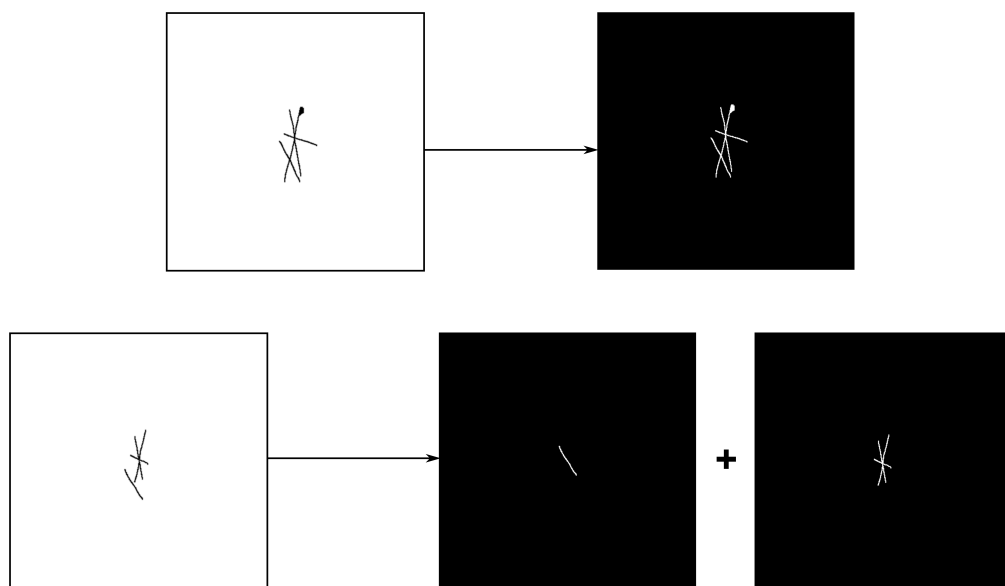


Figure 13: Original marked RAC on high quality exemplar (top left) with corresponding RAC image obtained through connected components (top right). Corresponding RAC on crime-scene-like print (bottom left) and RAC images obtained through connected components (bottom center and right). The crime-scene-like RACs exhibit more voids and are incomplete in comparison with their high quality counterparts.

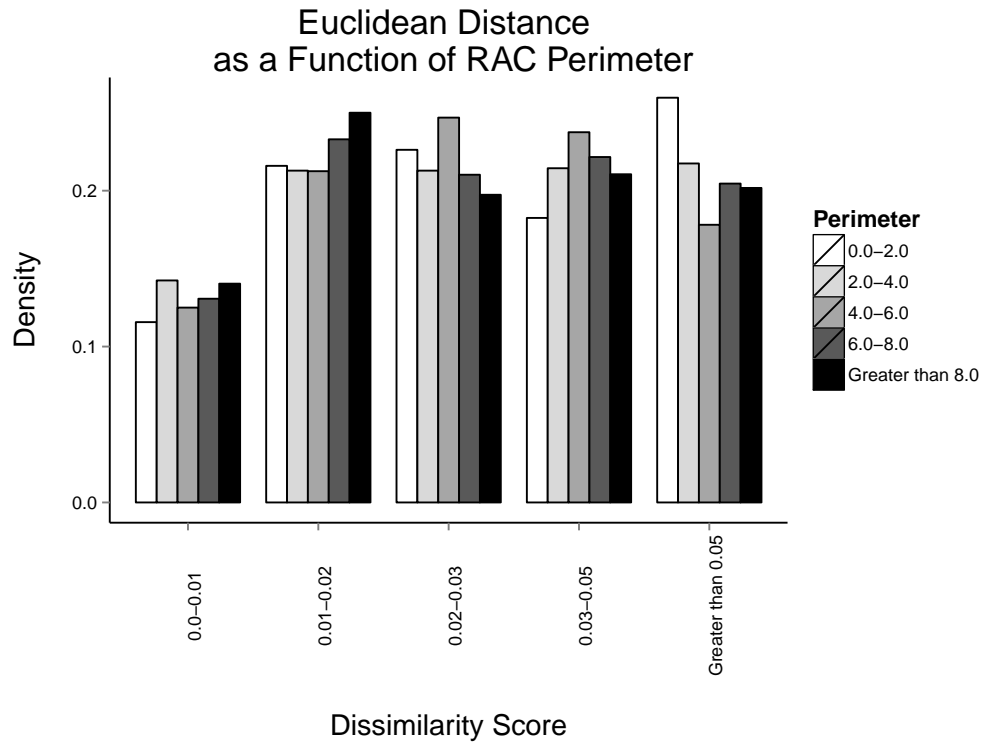


Figure 14: Euclidean distance as a function of RAC perimeter. Small RACs are more similar to their known match mates than large RACs. Based on the Chi-square results significant differences in ED scores as a function of perimeter existed for scores ranging from 0.01-0.02 and those greater than 0.05.

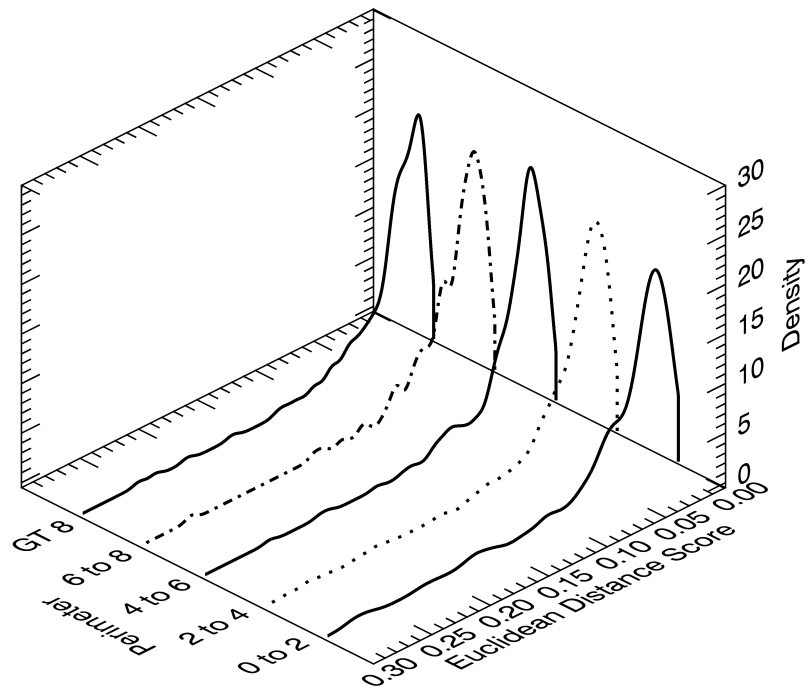


Figure 15: Probability density functions for ED as a function of RAC perimeter, obtained using a Gaussian kernel density estimator. Bin width information can be found in the Appendix.

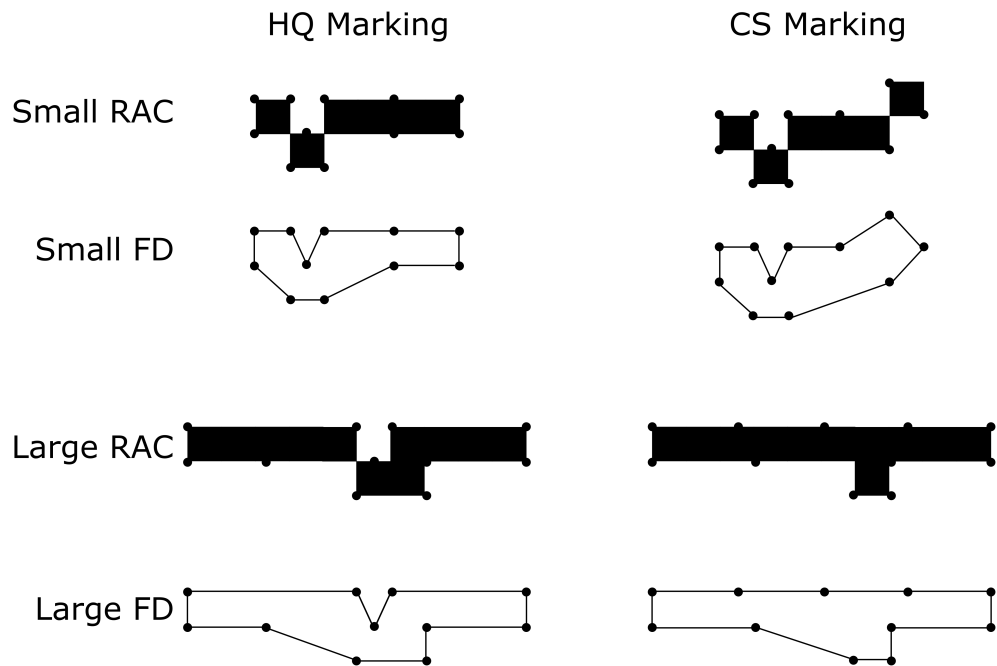


Figure 16: Example of stylized small and large high quality (HQ) and corresponding crime scene (CS) RACs. There is a 1 pixel difference between the HQ and CS marking for both the small and large features. In addition, there are 11 interpolation points which are used to extract the perimeter image of each RAC, similar to a Fourier descriptor (FD) perimeter representation. Note that the shape of the small RAC is more severely skewed by interpolation than the shape of the large feature.

Table 5: RAC map density.

Number of RACs in Map	CS Frequency	HQ Frequency
0	20 (10%)	0 (0%)
1-5	74 (37%)	7 (7%)
6-10	33 (17%)	12 (12%)
11-15	32 (16%)	5 (5%)
16-20	14 (7%)	11 (11%)
21-25	4 (2%)	2 (2%)
Greater than 25	23 (11%)	63 (63%)
<b>Total</b>	<b>200 (100%)</b>	<b>100 (100%)</b>

### ROC Curve of RAC Map POC Results

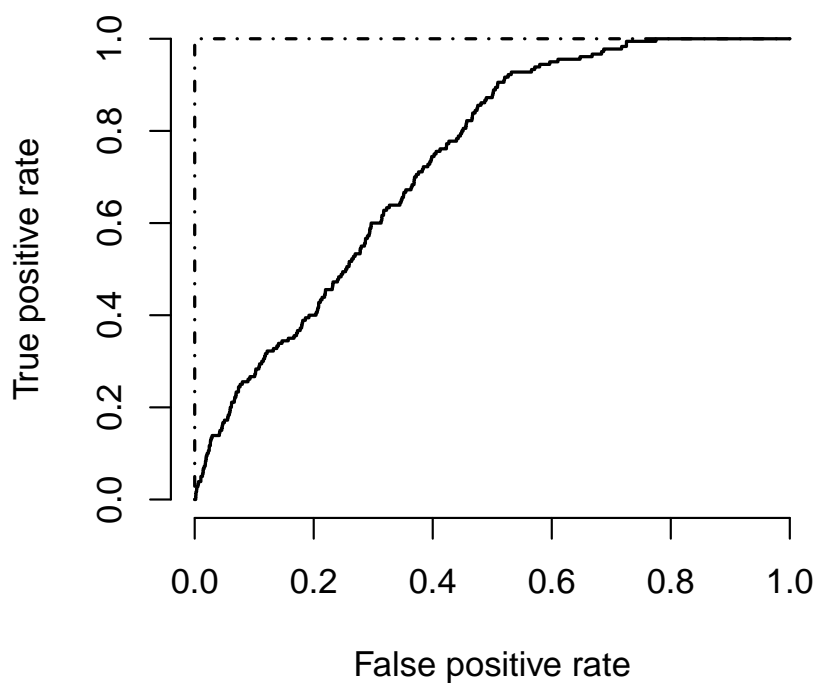


Figure 17: Receiver operator characteristic curve of RAC map POC results. High quality comparisons are represented by the dash-dotted line and exhibit an area under the curve (AUC) of 1.0. The solid line illustrates the results of crime-scene-like impressions with an AUC of 0.74.



472 **Appendix**

473 As previously stated, similarity score were analyzed as a function of RAC  
 474 shape, perimeter, and area. Detailed in Tables 6, 7, 8 are the bin widths used  
 475 to best approximate the true data when constructing the PDFs. Therefore,  
 476 a total of 75 individual PDFs were constructed. Subsequently, the plots for  
 477 related conditions (*i.e.*, MPOC as a function of shape) were compiled into  
 478 3-dimensional plots, thus allowing for easier visual comparison.

Table 6: Bin widths for PDFs (obtained using a Gaussian kernel density estimator) for similarity scores as a function of RAC shape. The bin width for each density estimate was set equal to one seventh of the standard deviation of the similarity scores.

	Circle	Line/Curve	Triangle	Irregular
MPOC	0.008	0.010	0.010	0.009
MF	0.003	0.002	0.004	0.003
MCS	0.804	0.827	0.942	0.864
HD	1.033	0.969	0.646	0.995
ED	0.006	0.006	0.006	0.005

Table 7: Bin widths for PDFs (obtained using a Gaussian kernel density estimator) for similarity scores as a function of RAC perimeter. The bin width for each density estimate was set equal to one seventh of the standard deviation of the similarity scores.

	0-2	2-4	4-6	6-8	Greater than 8
MPOC	0.009	0.009	0.009	0.009	0.011
MF	0.003	0.003	0.002	0.002	0.002
MCS	0.815	0.903	0.763	0.867	0.872
HD	1.109	0.949	0.843	0.981	0.886
ED	0.007	0.005	0.005	0.005	0.005

Table 8: Bin widths for PDFs (obtained using a Gaussian kernel density estimator) for similarity scores as a function of RAC area. The bin width for each density estimate was set equal to one seventh of the standard deviation of the similarity scores.

	0-0.25	0.25-0.5	0.5-0.75	0.75-1.0	1-2	Greater than 2
MPOC	0.010	0.009	0.009	0.010	0.009	0.013
MF	0.003	0.003	0.003	0.002	0.003	0.002
MCS	0.855	0.860	0.833	0.823	0.896	0.813
HD	1.043	1.059	0.799	0.914	0.884	0.754
ED	0.006	0.005	0.005	0.005	0.005	0.004

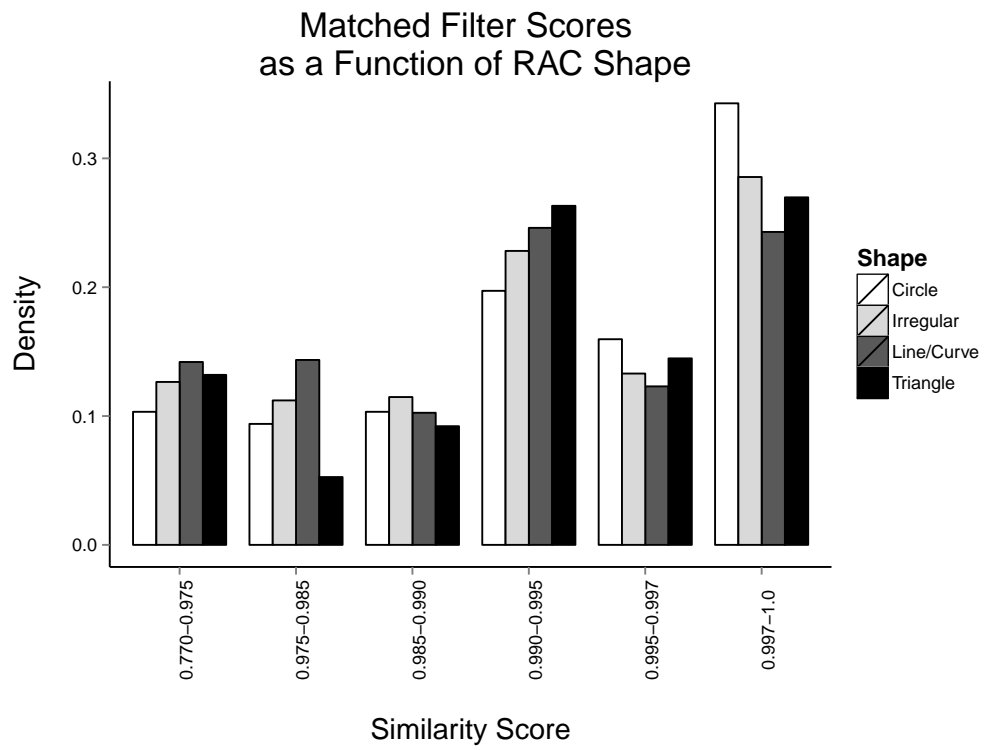


Figure 18: MF scores as a function of RAC shape.

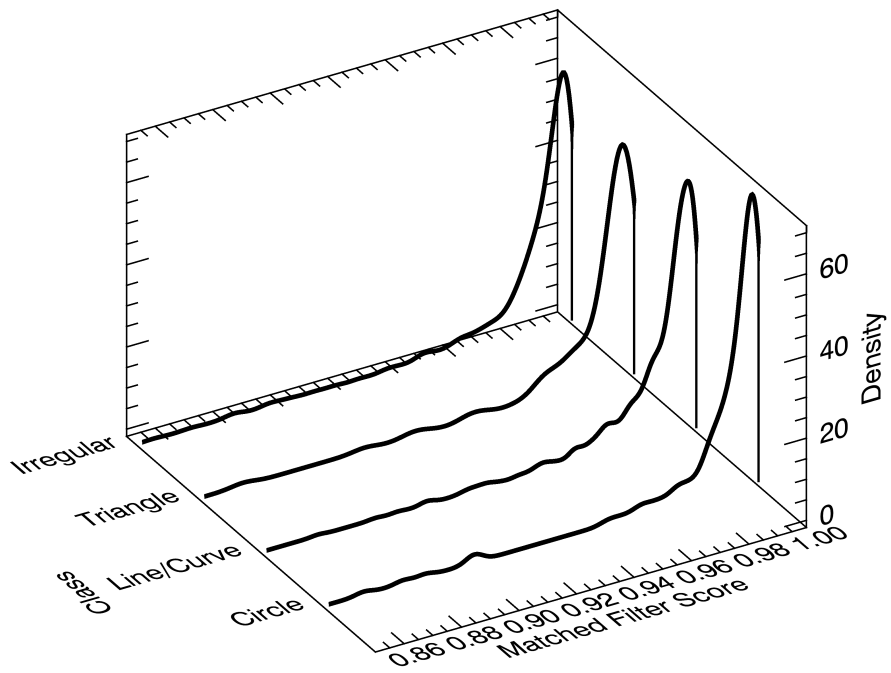


Figure 19: Probability density functions for MF scores as a function of RAC shape, obtained using a Gaussian kernel density estimator.

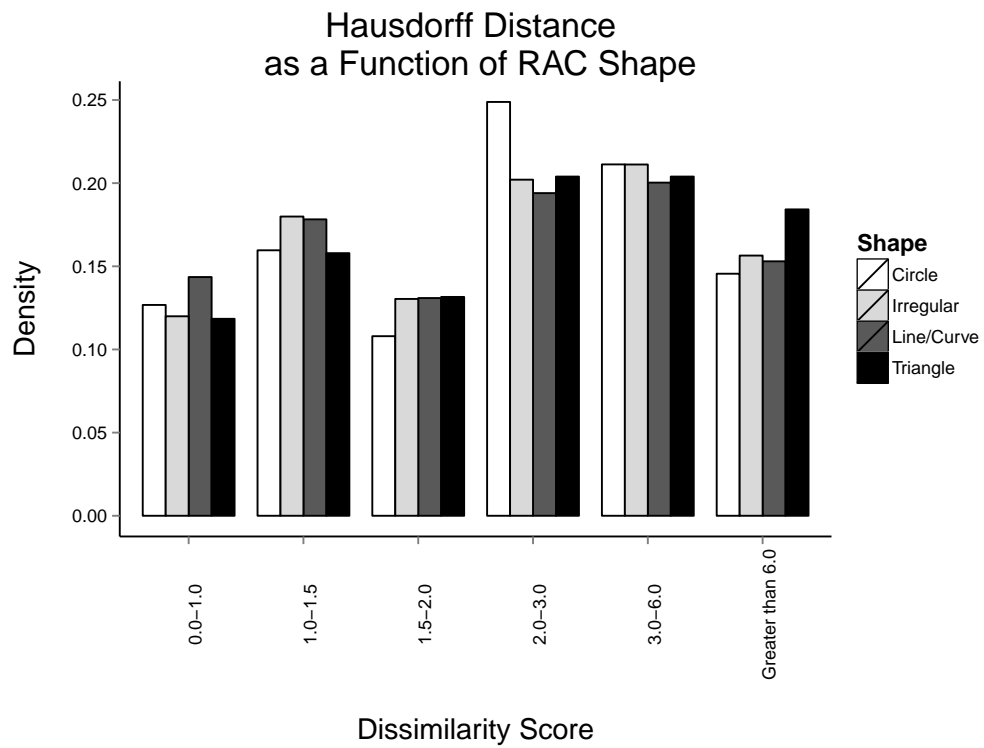


Figure 20: Hausdorff distance as a function of RAC shape.

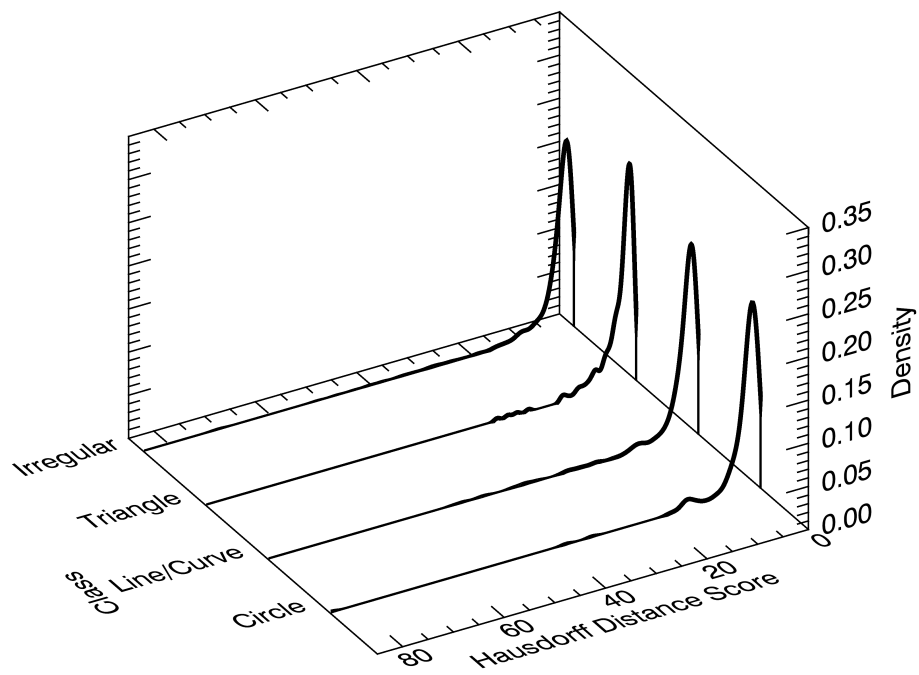


Figure 21: Probability density functions for Hausdorff distance as a function of RAC shape, obtained using a Gaussian kernel density estimator.

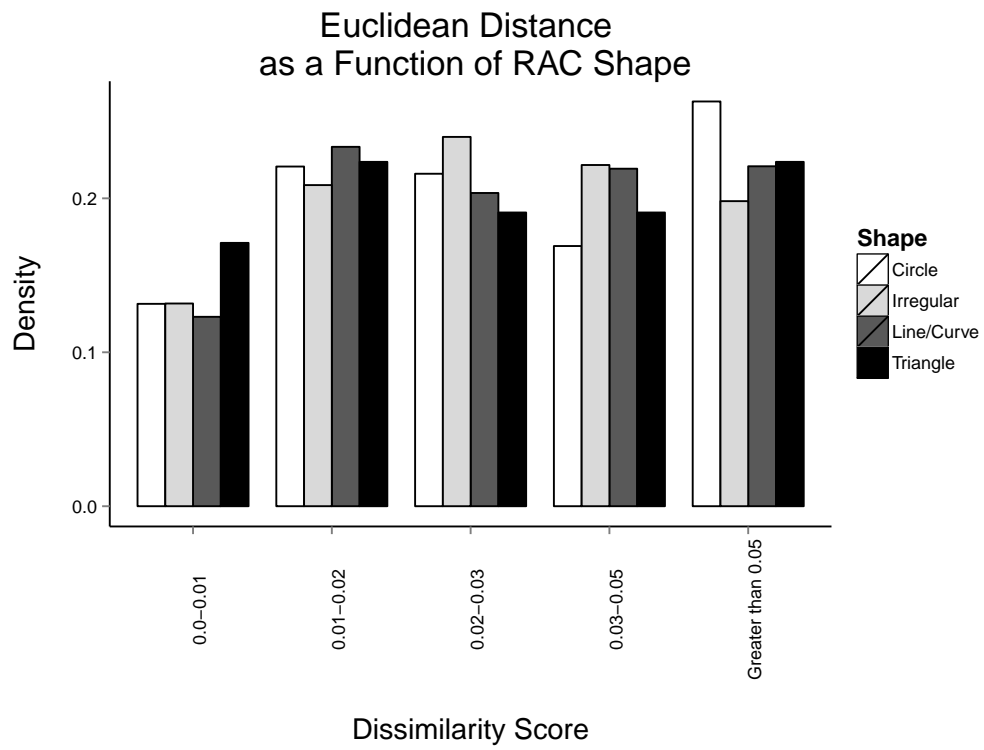


Figure 22: Euclidean distance as a function of RAC shape.

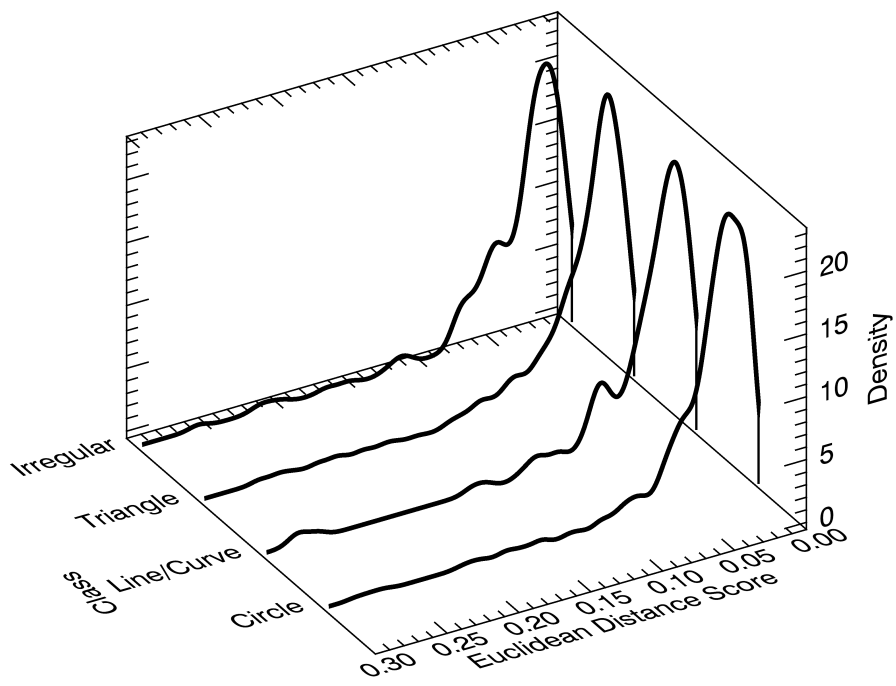


Figure 23: Probability density functions for Euclidean distance as a function of RAC shape, obtained using a Gaussian kernel density estimator.



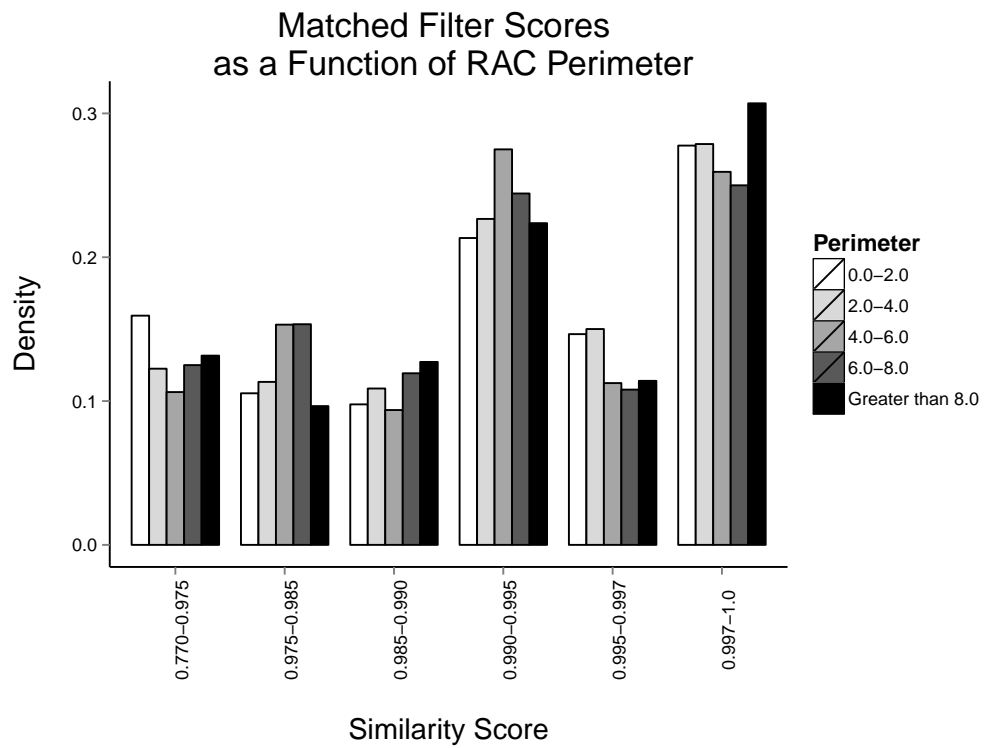


Figure 24: MF scores as a function of RAC perimeter.

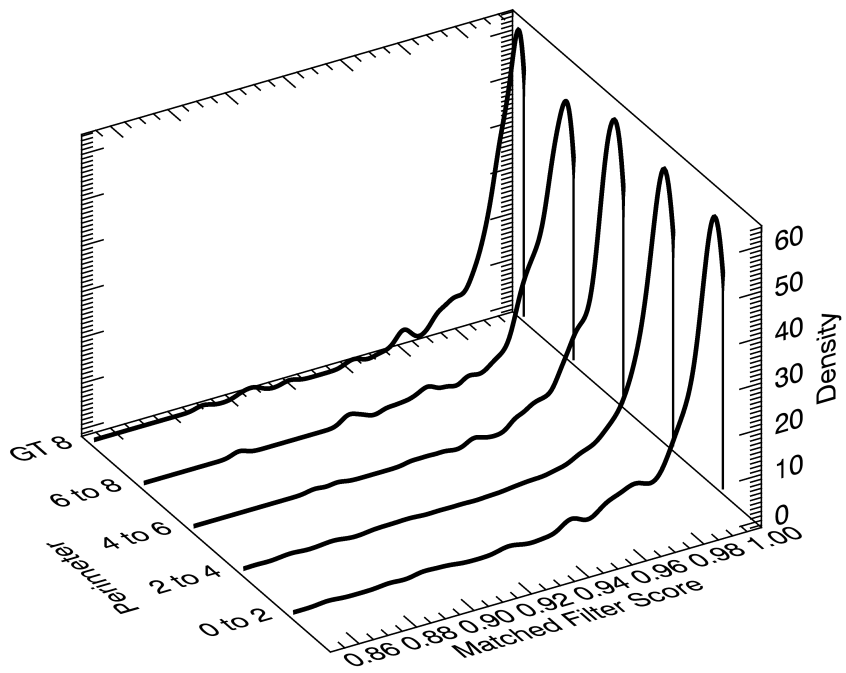


Figure 25: Probability density functions for MF scores as a function of RAC perimeter, obtained using a Gaussian kernel density estimator.

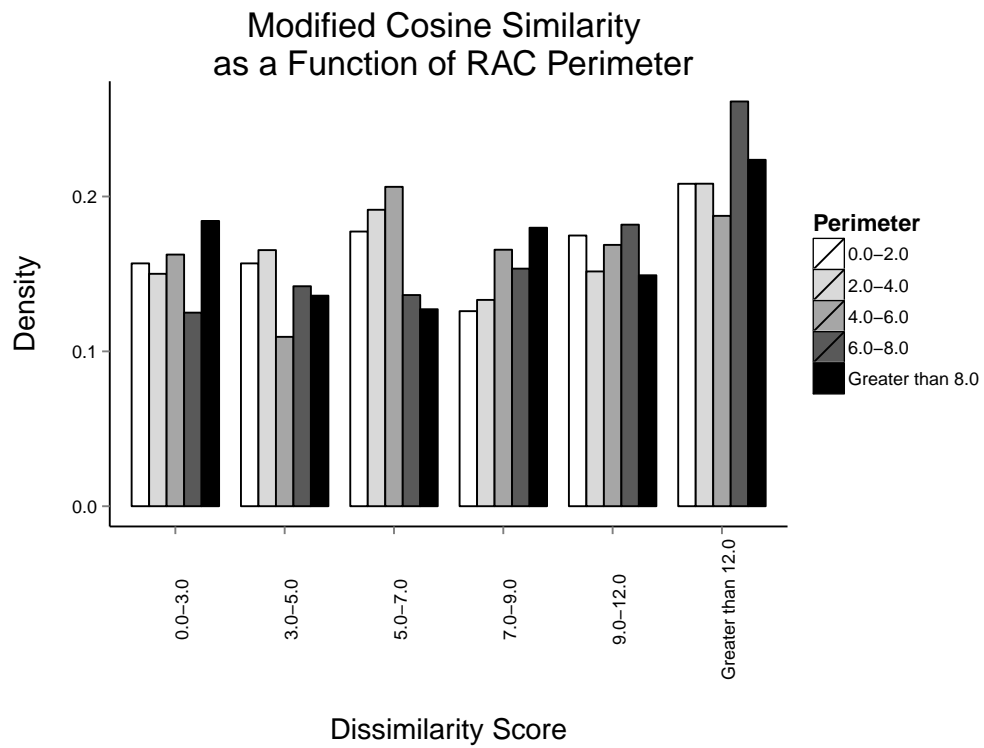


Figure 26: MCS scores as a function of RAC perimeter.

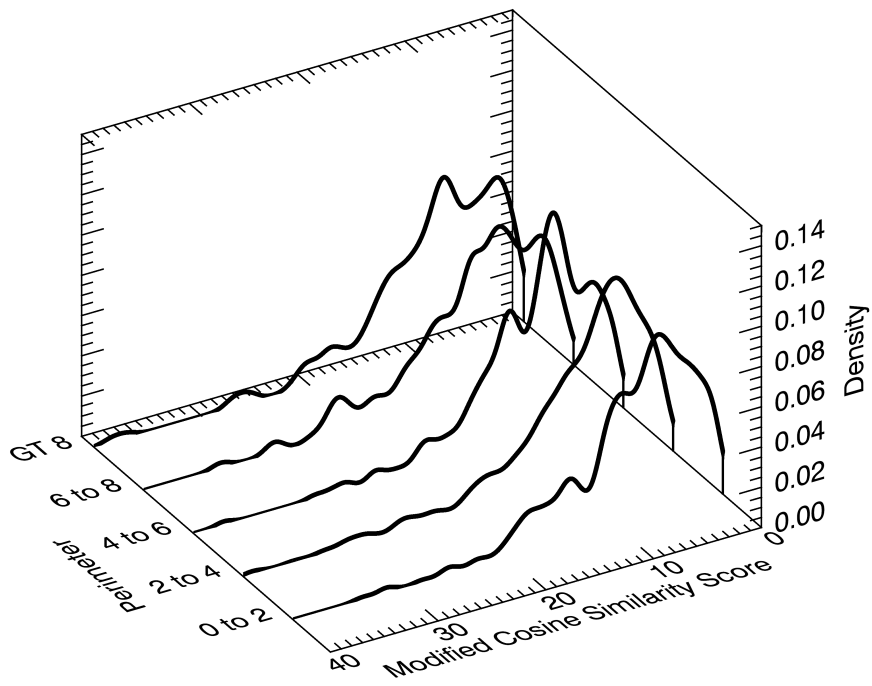


Figure 27: Probability density functions for MCS scores as a function of RAC perimeter, obtained using a Gaussian kernel density estimator.

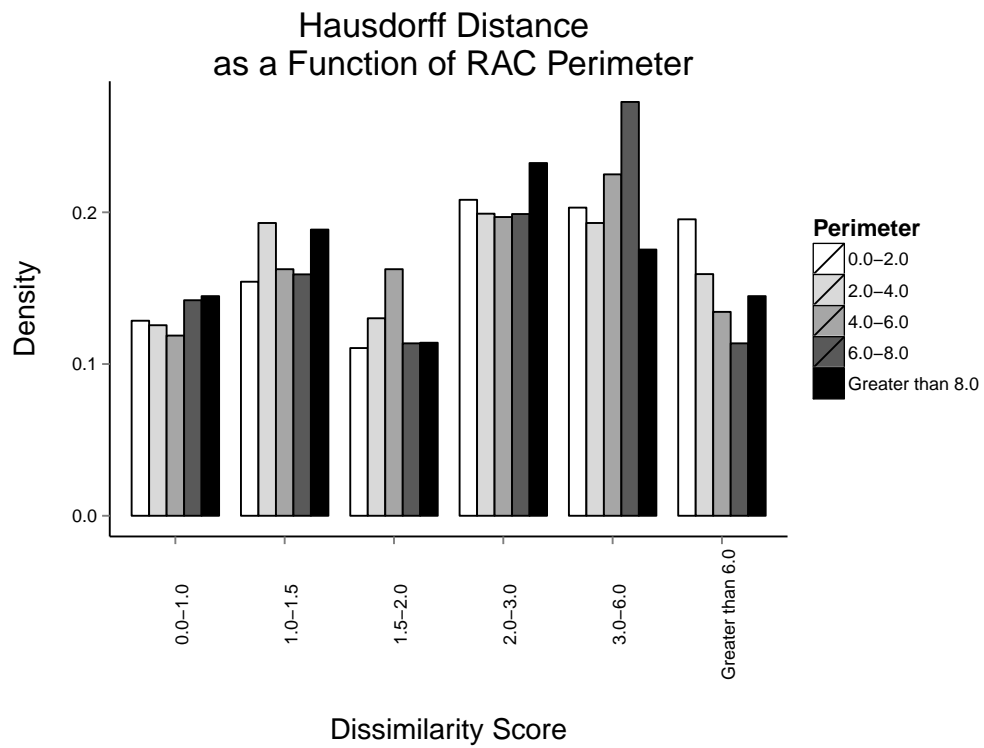


Figure 28: Hausdorff distance as a function of RAC perimeter.

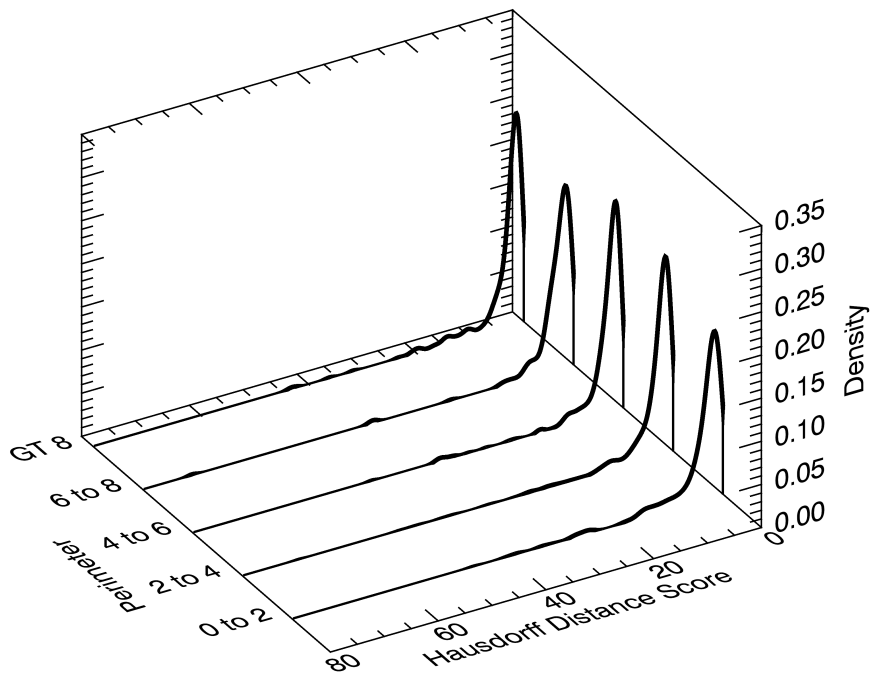


Figure 29: Probability density functions for Hausdorff distance as a function of RAC perimeter, obtained using a Gaussian kernel density estimator.

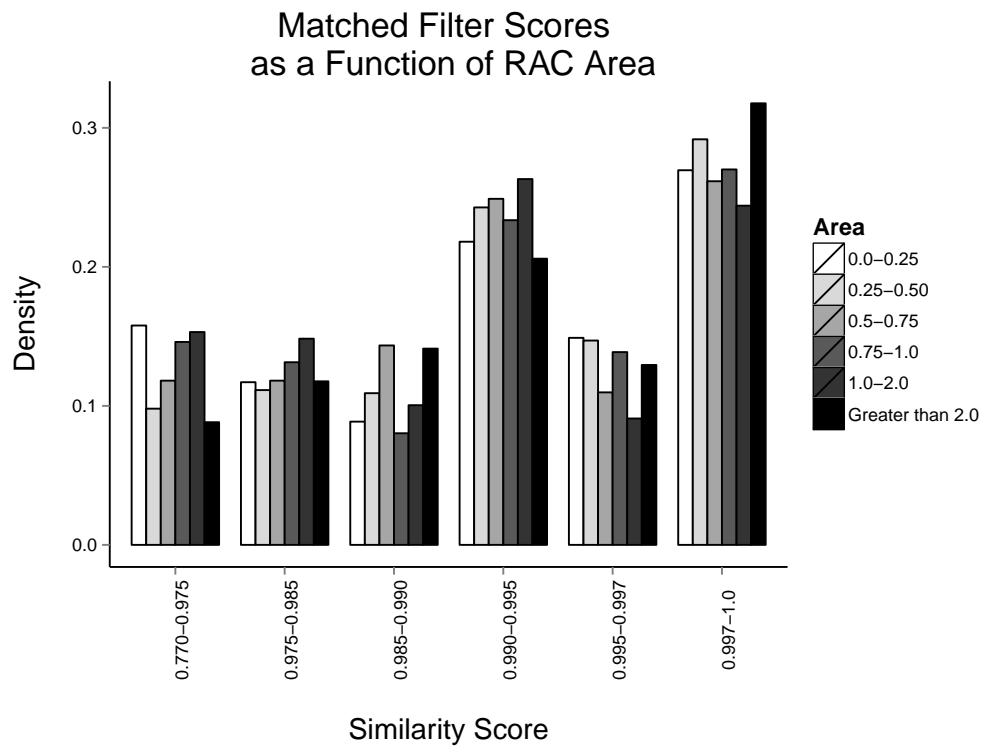


Figure 30: MF scores as a function of RAC area.

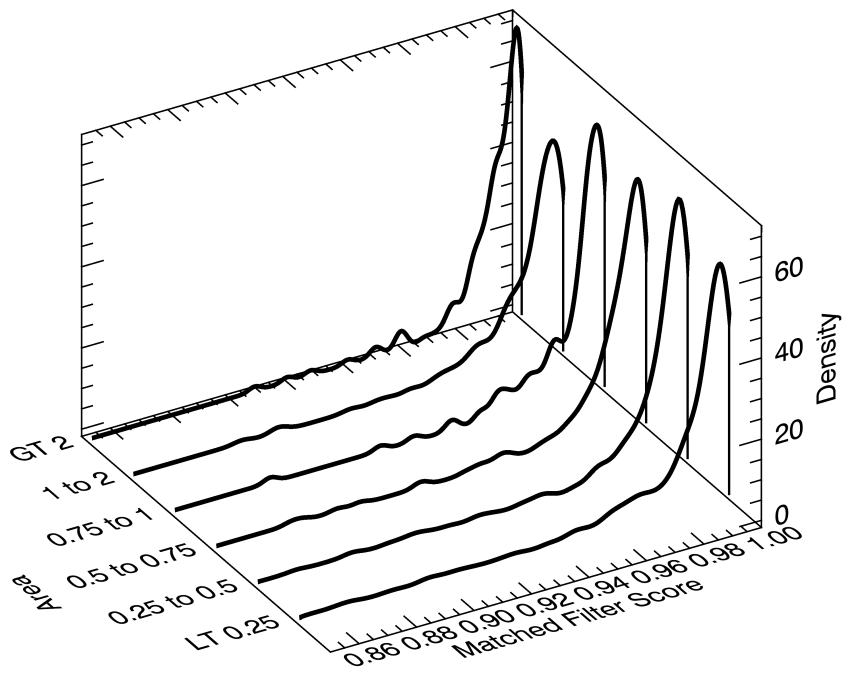


Figure 31: Probability density functions for MF scores as a function of RAC area, obtained using a Gaussian kernel density estimator.



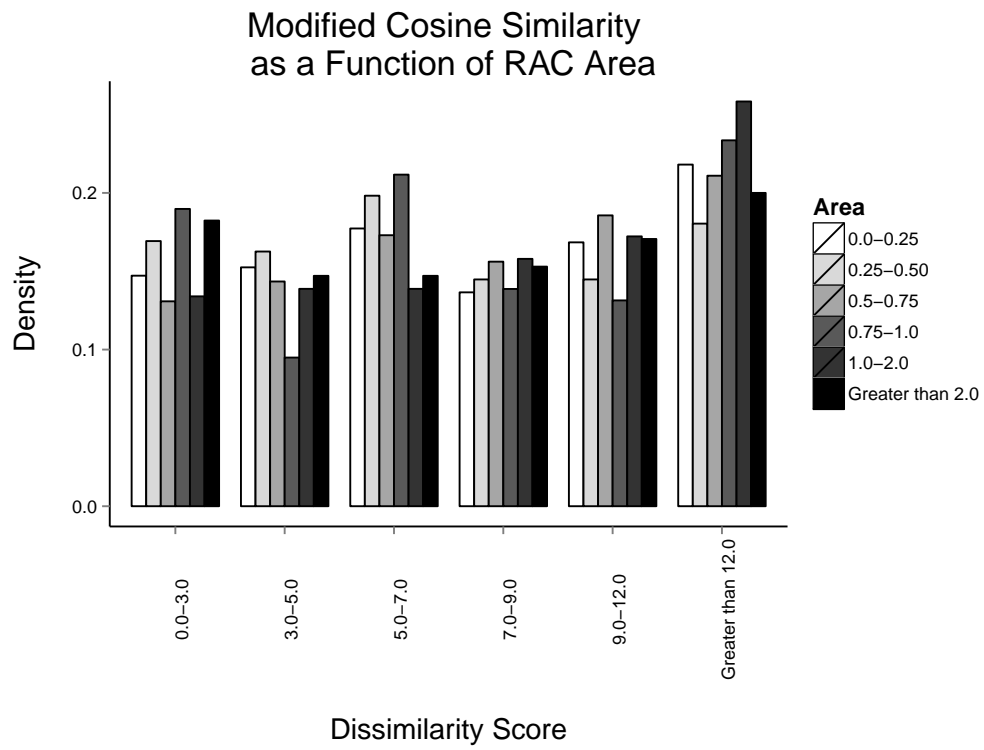


Figure 32: MCS scores as a function of RAC area.

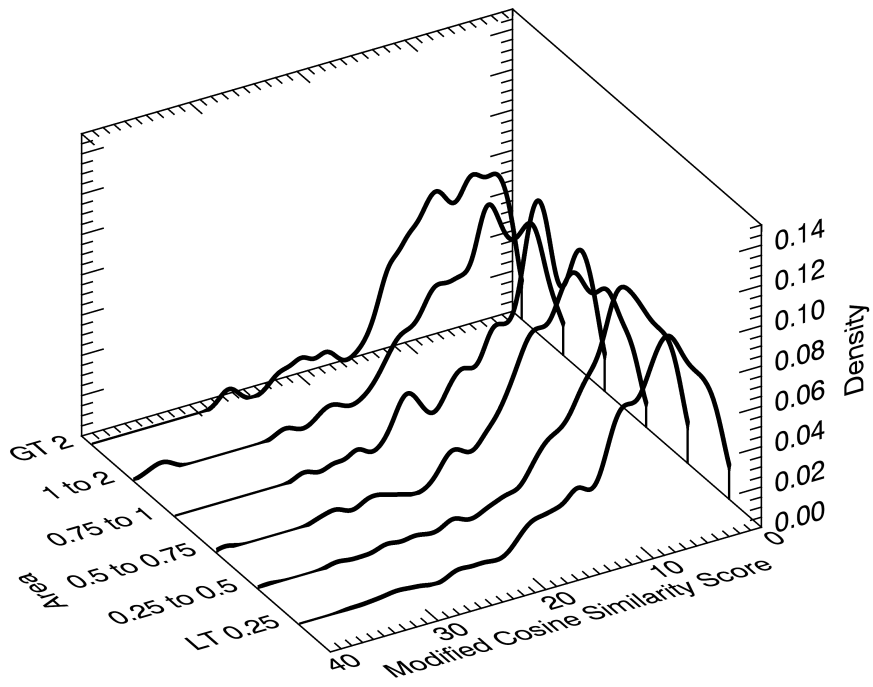


Figure 33: Probability density functions for MCS scores as a function of RAC area, obtained using a Gaussian kernel density estimator.

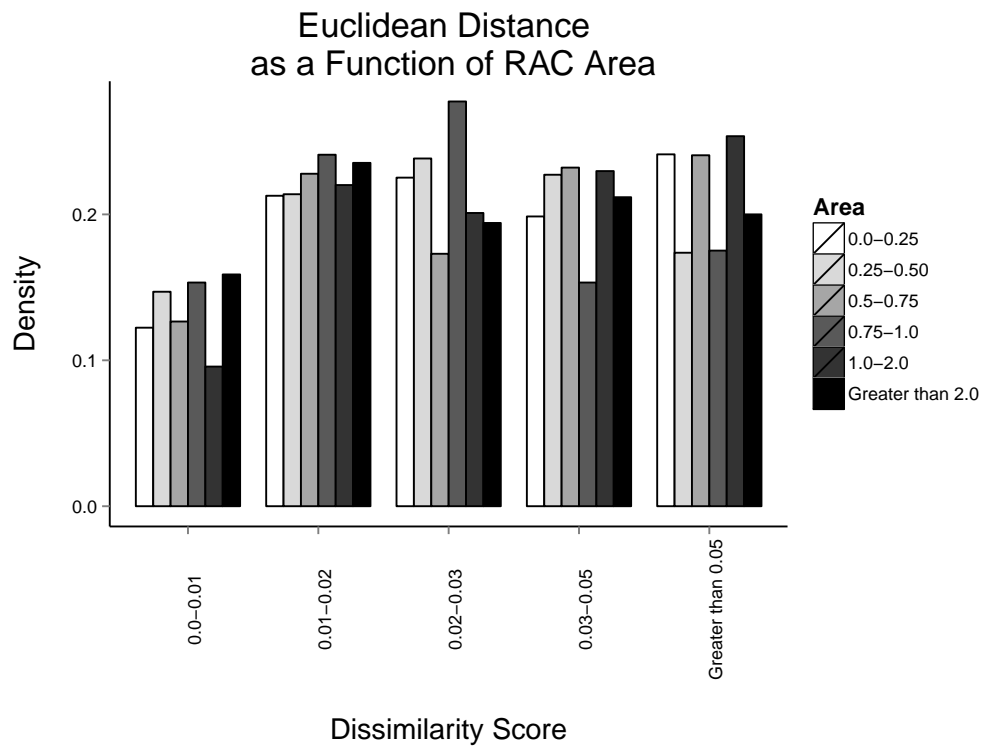


Figure 34: Euclidean distance as a function of RAC area.

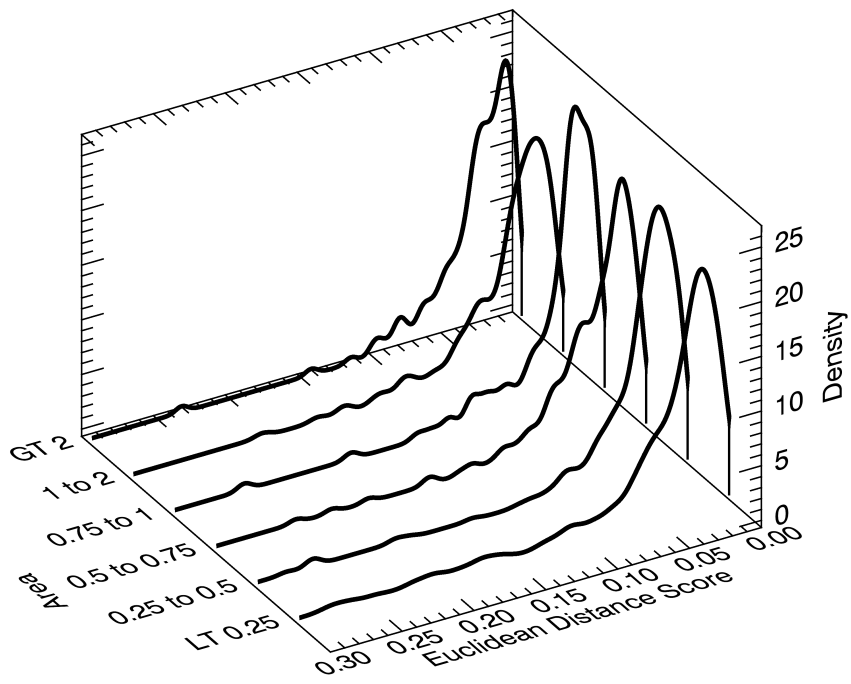


Figure 35: Probability density functions for Euclidean distance as a function of RAC area, obtained using a Gaussian kernel density estimator.

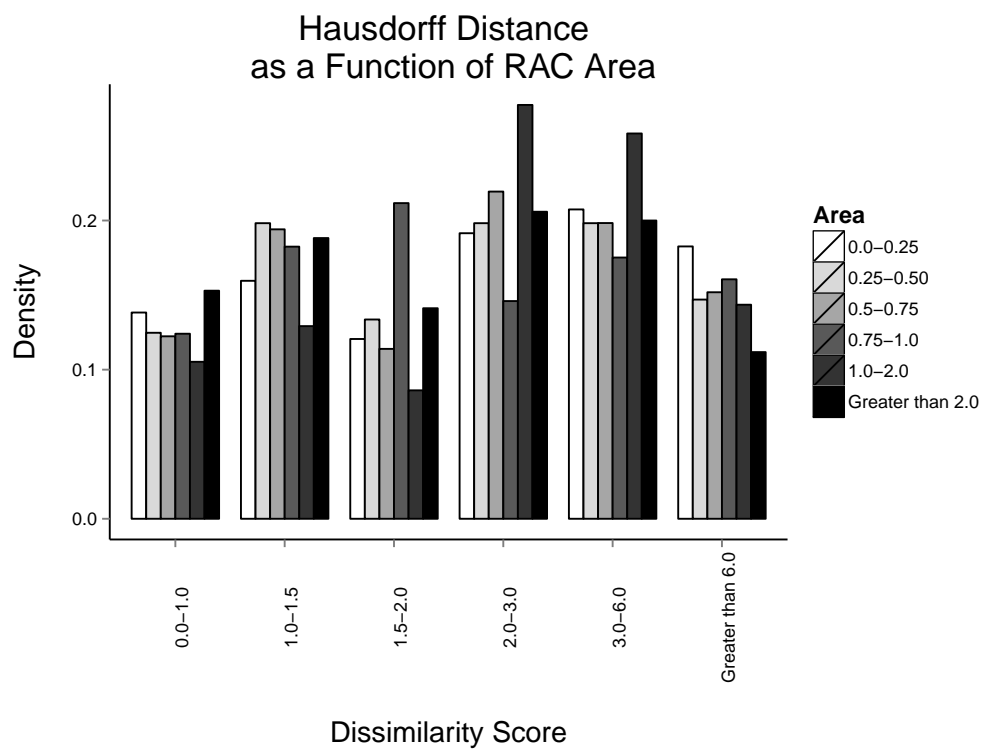


Figure 36: Hausdorff distance as a function of RAC area.

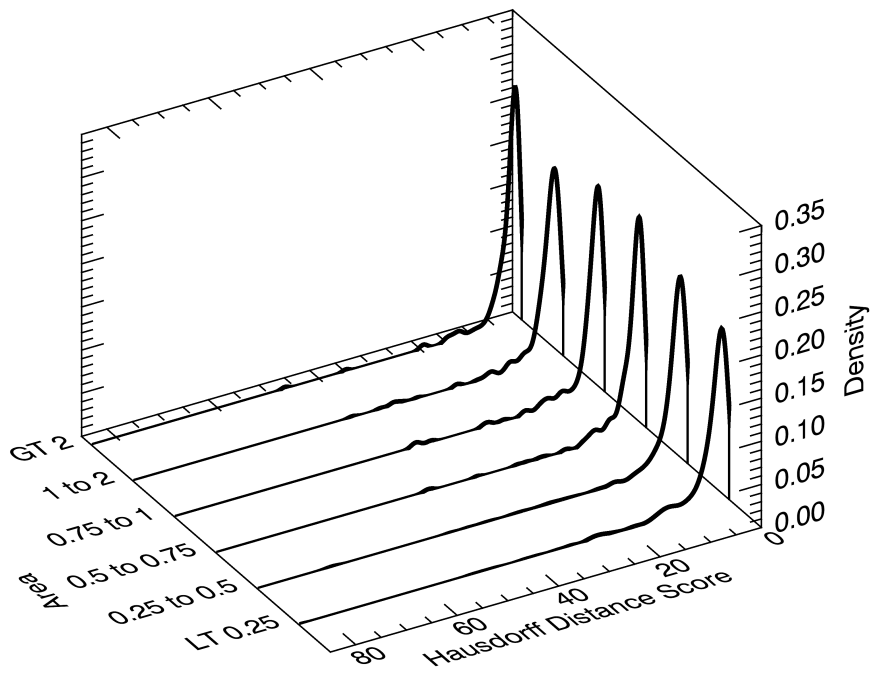


Figure 37: Probability density functions for Hausdorff distance as a function of RAC area, obtained using a Gaussian kernel density estimator.

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# 5. Future Directions

## 5.1 Chance Co-occurrence in Position & Shape

The normalized shoe used in this study was a men’s size 10 Reebok<sup>®</sup> walking shoe with an outsole surface area of 21,235mm<sup>2</sup>. Using  $\theta$  and  $r_{norm}$  each RAC (total of 57,426 RACs from 1,000 shoes) was localized into a cell measuring 5mm x 5mm in area, generating what is referred to as a heat-map or a plot of frequency versus position. Based on this plot, one bin was found to contain the greatest potential for RAC co-occurrence in position, as illustrated in Table [5.1]. When this result was further broken down as a function of shape category, the probability in co-occurrence ranged from 1:756 to 1:9,571 within a single 5mm x 5mm bin.

Table 5.1: Frequency of RACs and potential for co-occurrence as a function of position and shape for bin located approximately 5mm from the lateral edge and 70mm from the heel of the shoe.

Description	Any Shape	Irregular	Circle	Triangle	Line/Curve
Total: In Database	57,426	22,075	6,287	3,242	25,822
Total: In Cell	132	39	11	6	76
Chance of Finding RAC in Cell	1:435	1:1,472	1:5,220	1:9,571	1:756

Following localization, all pairwise comparisons in similarity were computed based on shape categorization and using Modified Phase Only Correlation (MPOC). The results are shown in Fig. [5.1], which report MPOC scores, RAC images, and Fourier images for the two most similar RACs detected within the bin. In contrast with all former published results, *some level of visual similarity* can be discerned. This is not to suggest that the accidentals are indistinguishable, since clearly each pair can be differentiated based on size, shape and/or orientation. However, it is relevant to note that there is *some level of expressed similarity* that should not be ignored. Moreover, most accidentals with possible co-occurrence in position and some expressed similarity in shape are *extremely minute in size*. This clearly indicates that more work is needed to better understand the limit of discrimination as a function of RAC size and complexity. To address this need, the database of 1,000 shoes will be doubled. If past RAC frequency is a good indicator

of future counts, then the end-goal of a complete database of 2,000 shoes is likely to contain more than 100,000 RACs, allowing for a detailed statistical analysis of RAC co-occurrence in terms of shape category (lines/curves, circles, triangles, and irregular-shaped features) and position  $(\theta, r, r_{norm})$ . In addition, the line/curve category is currently being subdivided into lines, simple curves, and compound curves to increase discriminating power. When complete, a detailed analysis of co-occurrence in position and shape will be provided, similar to that shown in Fig. [5.1], along with recommendations regarding limits in discrimination as a function of RAC size, area, geometry, and complexity.

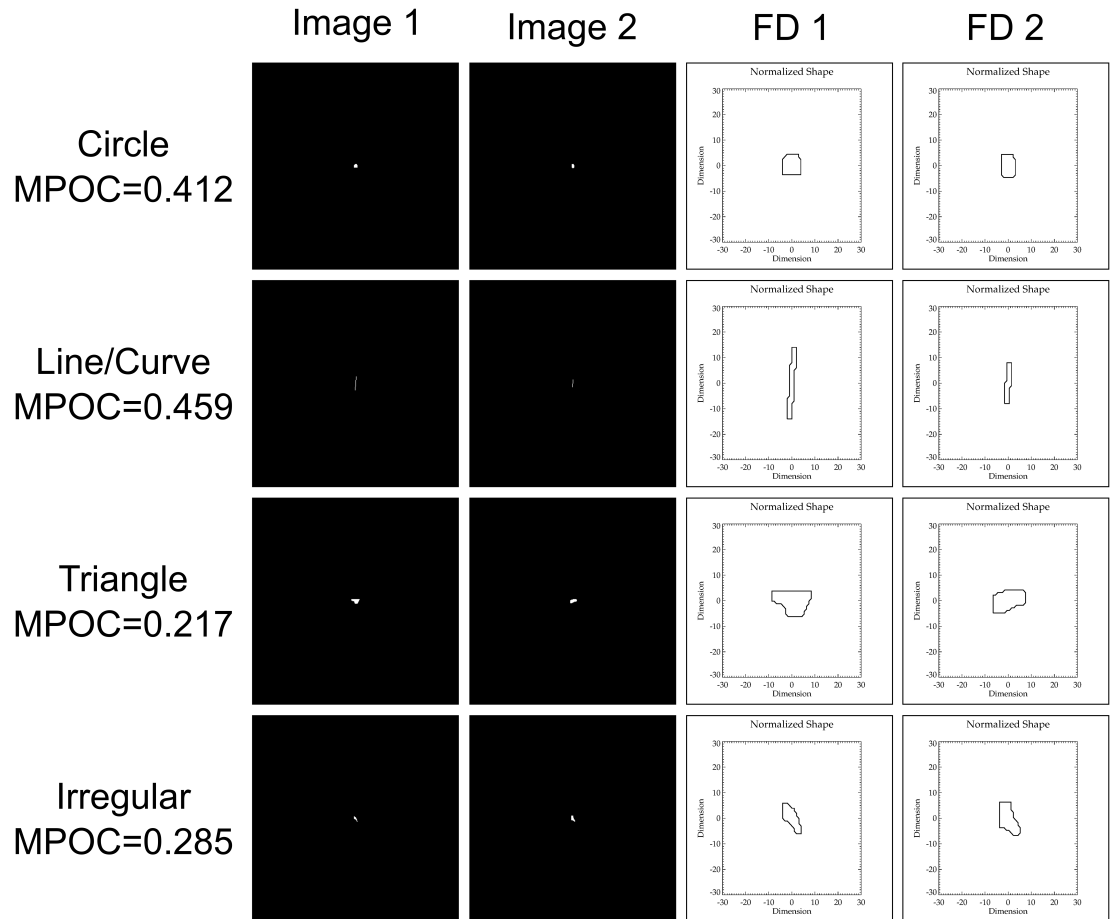


Figure 5.1: An illustration of the most similar RACs (*i.e.*, highest MPOC score) in each shape category within the bin located approximately 5mm from the lateral edge and 70mm from the heel of the shoe. The two RAC images, obtained through connected components, are displayed in the first two columns. In addition, the Fourier descriptors (FD) for both images are included for easier visualization (last two columns). Note that the most similar RACs are distinguishable based upon visual inspection and a correspondingly low MPOC score.

## 5.2 Phase Only Classification

### 5.2.1 Automated Classification

Based on the preliminary results for automated classification of outsole patterns for crime scene quality prints, Phase Only Correlation is a promising method. However, the crime-scene-like prints used for this phase of the research still contained more information than is often found at crime scenes (*i.e.*, they contain 80% or more of the outsole pattern based upon visual inspection). Thus, future imagery will be generated to increasingly stress the algorithm via fractional losses more comparable to that encountered in casework. In addition, 3-dimensional casts will be included to increase the variation in substrate/media input.

### 5.2.2 RAC Maps

Further research will be conducted regarding the reproducibility of RACs in crime scene impressions. Namely, the results for RAC map correlation will be broken down and analyzed in order to determine matching accuracy as a function of RAC number, size, shape and complexity. This data will offer some insight into the amount of information that is required for accurate identification of source (*i.e.*, are several small RACs equal to a few, large, complex features).

## 5.3 Addressing Remaining Research Needs

Although the current research attempted to address several forensic footwear research needs in order to increase efficiency and offer support to examiner conclusions (specifically regarding the interpretation of crime scene quality evidence), it was not possible to concentrate on all of the aforementioned recommended research areas. A suggested approach for addressing the remaining research topics is as follows:

- First, an assessment of the variability in examiner conclusions should be conducted. A similar study was previously conducted for fingerprint examiners (15). From the data collected, quantification of error rates for examiner conclusions was possible. Therefore, it may be possible to identify the error rates for footwear examinations, thus offering additional support to examiners in courtrooms when defending their conclusions.
- In addition, measures of uncertainty for examiner conclusions could be developed. While the current scale of conclusions allows an examiner some flexibility (*i.e.*, different levels of association between exclusion and identification), there is currently no method to report a quantitative level of uncertainty to accompany evidence comparisons. Although it is not clear how this might be achieved, research and discussion

should consider if and how uncertainty may benefit the footwear examiner moving forward.

- Further, an evaluation on intra- and inter-examiner variability in detecting and marking RACs should be pursued. Given that the automated comparison of RACs is contingent on the marking of features, it is important to understand the expected variability in identification and tracing of these accidentals. Based on an analysis of this variation, estimates of uncertainty may be developed for the results obtained through automated measures (*i.e.*, a confidence interval which accounts for inherent, and unavoidable, analyst variation in the absence of an automated extraction mechanism).
- Even better, the development of automated RAC extraction software should be explored. In theory, this algorithm could be used to search through an image for the presence of acquired features and segment the image to allow for evaluation of individual RACs or comparison of all features. This would offer tremendous increases in research efficiency, although it is clearly an extremely difficult image processing problem in its own right (*e.g.*, like finding the needle in the haystack).
- Lastly, estimates on the frequency of outsole information (make, model, size, etc.) should be gathered. This task is immensely difficult to tackle given the number of unknowns, such as number of shoes of a given type, how long shoes remain in the population before they are discarded, and the production of counterfeits for popular types of shoes. All of these factors complicate the estimation of frequency for outsole designs in the population, and therefore great attention will be required in order to account for or somehow overcome these unknown factors.



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