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Multi-Telescope Radio Observations for Low Frequency Gravitational Wave Astrophysics

Megan L. Jones

Dissertation Submitted to The Eberly College of Arts and Sciences at West Virginia University in partial fulfillment of the requirements for the degree of

> Doctor of Philosophy in Physics

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Abstract

Multi-Telescope Radio Observations for Low Frequency Gravitational Wave Astrophysics

Megan L. Jones

The North American Nanohertz Observatory for Gravitational Waves (NANOGrav) has the principal goal of detecting gravitational waves (GWs) in the nanohertz part of the spectrum using pulsar timing. This thesis presents results from radio campaigns at frequencies from 322 MHz to 10 GHz aimed at both multi-messenger constraints on GW sources and improving the timing sensitivity. The primary expected source of GWs at the nanohertz frequencies to which pulsar timing is sensitive are supermassive black hole (SMBH) binaries. We investigate a purported SMBH displaced from the galactic photocenter in NGC 3115. We explore the possibilities that the source is a SMBH binary or a post-merger recoiling SMBH. We place constraints on a possible SMBH companion using observations taken with the NRAO Very Large Array. If a companion SMBH can be confirmed, this system could be a future GW source detectable with pulsar timing.

In order to detect such sources, our pulsar timing array must be as sensitive as possible, requiring the mitigation of all other astrophysical delays, including those from the interstellar medium (ISM). Using NANOGrav wideband multifrequency observations obtained with the Green Bank Telescope and Arecibo Observatory, we characterize frequency-dependent dispersion. This effect is quantified by the dispersion measure (DM). We analyze trends in the DM time series, propose sources of these trends, and identify timescales over which the DM varies beyond measurement errors and therefore can no longer be modeled as constant in timing. Analyzing DM variations aids in characterizing properties of the ISM and informs our timing observation strategy.

Multi-telescope observations around the globe and at complementary frequencies can be used to more sensitively constrain DMs. We compare DMs measured with dual-frequency observations obtained using the Giant Metrewave Radio Telescope (GMRT) to those calculated in the NANOGrav 11-year data release to assess the possible precision of frequency-dependent noise measurements with the GMRT. We discuss the possibility of incorporating the GMRT into international pulsar timing efforts and anticipated challenges in future data combination.

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Chapter 1

Introduction

With the detection of gravitational waves (GWs) by the Laser Interferometer Gravitational-Wave Observatory (LIGO), we have entered a new era in GW astronomy. GW astronomy is necessary for studying phenomena only visible through gravitational dynamics and provides a multi-messenger view of processes in the Universe, like supermassive black hole (SMBH) binary mergers. GW frequencies are determined by their sources; for example, SMBH binaries in \sim year orbits emit lowfrequency GWs, while binaries nearing mergers emit much higher frequency GWs. A variety of experiments and observatories are needed to provide coverage across the GW spectrum, seen in Figure 1.1. GW detections in lower frequency regions would be complementary to those already achieved by LIGO and would offer characterization of the GW universe through the observation of a diverse population of sources. A pulsar timing array (PTA), which is made up of an accurately timed network of precise stellar rotators called pulsars, is a low-frequency GW experiment which can be used to look for a correlated signal across multiple pulsars in the network. PTAs are formed by observing pulsars using radio telescopes here on Earth, creating a Galactic scale interferometer.

In this chapter, we will give a brief description of GWs, their detection, sources, as well as pulsar timing and the effects of the interstellar medium.



Figure 1.1 Coverage of experiments across the GW spectrum and the detectable sources in each regime. Image credit: NANOGrav.

1.1 Gravitational waves

The need for an improved gravitational theory over the Newtonian description can be seen from looking at how classical mechanics deals with gravitational force

$$F = \frac{Gm_1m_2}{r^2} \tag{1.1}$$

where G is the gravitational constant, m_1 and m_2 are two masses, and r is the distance between them. Nothing travels faster than light and information is no exception; as can be seen in Eq. 1.1, Newtonian gravity does not incorporate an explicit time dependence and therefore does not account for the time it takes for information to travel. What if the Sun's mass was increasing over time? Equation 1.1 would go from $F \propto m$ to $F(t) \propto m(t)$, which suggests that the planets would feel this change in gravitational force at the same time t (i.e. instantaneously). This would require a speed faster than light and would violate the laws of physics.

The existence of GWs was posited by Einstein in his general theory of relativity (henceforth GR; Einstein, 1915). Contrary to Newton's description of gravity as a force between two objects, Einstein described the influence of gravity as curvature of 4-dimensional spacetime (three spatial dimensions, and one in time); as masses move, the curvature of spacetime changes. GWs are perturbations in spacetime that propagate outward from their source at the speed of light, carrying away energy from the source system along with them.

The effect of GWs traveling through the Universe is to warp the curvature

of spacetime by contracting or elongating space. If two masses are separated by a distance L, the fractional positional perturbation they experience due to a passing GW can be described as

$$h = \frac{\delta L}{L} , \qquad (1.2)$$

where δL is the change in L due to the warping of spacetime. This fractional change h is referred to as the GW strain. GW experiments must be able to very accurately measure L in order to detect the immensely small δL produced by GWs. The detection of δL and the precision of that measurement are determined by the noise both intrinsic and extrinsic to the detector. It is therefore paramount for GW experiments to characterize sources of noise that may be present in the data.

1.1.1 Gravitational multipoles

While any object with mass will have a gravitational field (and will therefore warp spacetime), only certain kinds of systems will emit GWs. In order to determine which systems will be GW emitters, we must be able to characterize gravitational systems, how their mass is distributed, and how they move. It is useful to make a comparison to electromagnetism in order to describe the different properties of massive systems.

The gravitational monopole (the zeroth order term in the gravitational multipole expansion) describes the total mass in a system and does not determine the emission of gravitational waves. A gravitational dipole describes how the mass is distributed. Similar to the electric dipole, the gravitational dipole can be described

$$\mathbf{d} = \sum_{i} m_i \mathbf{x}_i \ . \tag{1.3}$$

where \mathbf{x}_i is the position vector between the two ends of the dipole. When taking the first derivative of this moment, we get the momentum

$$\mathbf{p} = \dot{\mathbf{d}} = \sum_{i} m_i \dot{\mathbf{x}}_i , \qquad (1.4)$$

GWs carry energy away from the system and momentum must be conserved, therefore gravitational dipoles also do not emit gravitational waves.

The gravitational quadrupole moment describes how masses move; it can be calculated as

$$\mathbf{q} = \sum_{i,j} (m_i + m_j) \mathbf{x}_i \mathbf{x}_j \tag{1.5}$$

For instance, a perfect non-rotating sphere moving through space has a constant quadrupole moment because from the object's reference frame, it is at rest. In the case of a binary neutron star system however, regardless of which reference frame is used at least one of the stars is always going to be moving, giving the system a quadrupole moment that changes in time. Therefore the gravitational quadrupole is the first possible nonzero response and is the lowest order contributor to gravitational radiation.

The quadrupolar nature of GWs also determines the shape of the perturbation. A GW affects spacetime by contracting or lengthening space; the directions along which space is affected in either direction depend on the polarization of the GW.



Figure 1.2 A GW affects spacetime by contracting or lengthening space; the directions along which space is affected in either direction depends on the polarization of the GW. Plot A on top shows a ring of test particles unaffected by a GW. The two plots on the bottom show how the ring of test particles will behave if a GW goes through the paper. The ring of test particles initially are perturbed into stretching along the y-axis and contracting along the x-axis (shown in green), then lengthens and contracts in the other directions a half cycle later (shown in blue). Image from Wheeler (2013).

An example of GW polarizations can be seen in Figure 1.2.

1.1.2 Sources of gravitational waves

With a decade length data span and weekly to monthly observations, PTAs

are sensitive to GW frequencies in the nanohertz to microhertz part of the spectrum.

This portion of the GW spectrum includes continuous waves due to supermassive

black hole (SMBH) binaries, the stochastic GW background made from many GW

sources in the Universe, cosmic strings, and maybe even early Universe inflation (shown in Figure 1.1). Unlike electromagnetic radiation, GWs propagate through the Universe virtually unimpeded by matter, rippling the space around them as they pass.

It is widely thought that most galaxies (if not all) host a SMBH at their cores; even our own Milky Way is host to a SMBH. There are several theories on the formation of SMBHs; they are even seen in the somewhat early universe (Volonteri, 2010). Galaxies grow when smaller galaxies merge and form larger galaxies; galaxy mergers also trigger large amounts of star formation. Once black holes are formed through the death of high mass stars, they grow via accretion of matter. As a black hole grows and interacts with more matter in the galaxy, it will move towards the center of the gravitational potential well (i.e. the galactic center). SMBH binaries form following major galaxy mergers. When two galaxies merge, the central SMBHs are brought together into a binary orbit through dynamical friction; as more material is consumed or ejected from the environment around this system, the binary becomes tighter and tighter.

It is at this distance that now, due to the lack of available matter left to interact with, the merging pair can stall. This is known as the final parsec problem. At first glance, the emission of GWs may appear to be a solution to this problem; GW emission results in energy being carried out of the binary system, and with this energy loss, the potential energy of the system decreases, causing the binary orbit to decay and the orbital distance to decrease. However, GW emission does not occur until the SMBHs are much closer together ($\sim 10^{-2}$ pc). There is therefore a



Figure 1.3 Many smaller galaxies merge to form larger, more organized galaxies. This process continues, forming larger, more massive galaxies. Through merger dynamics, the central black holes in these galaxies grow as they absorb newly nearby material as well as other black holes. Image credit: ESO/L. Calada.

large amount of uncertainty regarding the SMBH merger rate due to the last parsec problem.

The expected strain from a SMBH binary in a circular orbit is

$$h \simeq 10^{-17} M_8^{5/3} f_{yr^{-1}}^{2/3} D_{Gly}^{-1} \frac{q}{(1+q)^2} ,$$
 (1.6)

where M is the mass of the binary in units of 10^8 M_{\odot} , D is the distance to the binary, f is the frequency of the gravitational waves, and q is the mass ratio of the binary. As can be seen from Eq. 1.6, given a detectable threshold value for h, then the detection of lower frequency GWs requires higher mass black holes and/or binaries that are closer to the Earth. The detection of GWs produced by SMBH mergers will inform on the percentage of galaxy mergers that eventually produce SMBH mergers, as well as provide conclusive evidence that the final parsec problem can indeed be solved.

The time to merger for a SMBH binary is

$$\tau = 10^6 M_8^{-5/3} f_{yr^{-1}}^{-8/3} \frac{(1+q)^2}{q} \text{ yr} . \qquad (1.7)$$

The stochastic background spectrum is expected to follow an $f^{-2/3}$ power law in the case of GW-only driven mergers. SMBH binaries with lower frequencies take more time to merge than those at higher frequencies, therefore low-frequency SMBH binaries have longer lifetimes. Because of this, the gravitational stochastic background is dominated by SMBH binaries with low orbital frequencies.

1.2 Pulsars

The first pulsar was discovered by graduate student Jocelyn Bell Burnell in 1967 (Hewish et al., 1968). Formed as leftover stellar cores following supernovae, pulsars are highly magnetized, rapidly rotating neutron stars. Charged particles are accelerated along the magnetic field lines of the neutron star; these particles create a beam of electromagnetic radiation as the pulsar spins. As the beam sweeps through space, scientists can detect the beam as a pulse of radiation (hence the name pulsar). The Nobel Prize was later awarded in 1974 (but not to Bell Burnell) for the discovery of pulsars.

Pulsar studies have made their way to the forefront of some of the most groundbreaking astrophysical science. The first exoplanets were discovered orbiting a pulsar, with the Wolszczan & Frail (1992) discovery of a multi-planet system around the millisecond pulsar PSR 1257+12. The first binary pulsar PSR B1913+16 discovered by Hulse & Taylor (1975) earned them a Nobel Prize in 1993. It was found that over time, this binary is losing angular momentum and the orbital separation is shrinking (reviewed in Weisberg et al., 2010). This loss is consistent with predictions from general relativity (GR), providing indirect evidence of GW emission.

1.2.1 Millisecond pulsars

Pulsars spin with periods ranging from a few tens of seconds to ~ 1 millisecond. The first millisecond pulsar (MSP) B1937+21 was detected by Backer et al. (1982) and was determined to have a period of 1.558 ms. MSPs are defined as having rotational periods less than ~ 30 ms; these short periods are a result of the pulsars having been "recycled" or spun up after accreting material from a binary companion. As a result of this recycling, MSPs have lower magnetic fields and are more precise rotators than their slower canonical counterparts due to their lower spin-down rates, making them excellent tools for precision timing. Properties of different types of pulsars can be seen in the $P - \dot{P}$ diagram in Figure 1.4. According to the ATNF Pulsar Catalogue (PSRCAT¹), ~2600 pulsars have been found to date, of which ~350 are MSPs (Manchester et al., 2005).

1.2.2 Pulsar timing

As mentioned earlier, a GW causes a change in the length of the detector (in this case, the light travel time of the pulse). This difference in light travel time causes a change in the time of arrival (TOA) of the pulse, as a different distance means a different light travel time. GWs of the amplitude expected from SMBH binaries likely cause the TOA to vary by a few tens of nanoseconds. As a result, high precision timing is necessary in order to detect this incredibly small change in light travel time.

Due to the stability of MSP rotation periods, pulse TOAs can be predicted through pulsar timing and the determination of a timing model. A basic timing model consists of a Taylor expansion of the rotation phase ϕ around some initial

¹http://www.atnf.csiro.au/people/pulsar/psrcat/



Figure 1.4 The $P-\dot{P}$ diagram. Lines indicate constant characteristic ages, magnetic fields, and spin-down luminosity. The grey region shows forbidden regions for the pulsar population. Most of the MSPs plotted above are in binary orbits; the short periods of these pulsars are a result of them having been spun up after accreting material from their binary companion. The MSP population has smaller period derivatives compared to their spin period, and therefore make more stable rotators than canonical pulsars. Plot taken from *Handbook of Pulsar Astronomy* (Lorimer & Kramer, 2012).



Figure 1.5 Effects on timing residuals for PSR B1133+16 due to errors in the timing model. Plots show (a) a good timing fit, where residuals are not structured and are randomly distributed around zero, (b) an incorrect pulse spin down in the timing model, causing pulses to arrive later and later over time, (c) an error in position which causes the Earth's motion around the Sun to be apparent in the residuals, (d) and an error in proper motion, causes an error in position that grows over time. All parameters but be fit as accurately as possible to achieve high precision in timing. Image taken from *Handbook of Pulsar Astronomy* (Lorimer & Kramer, 2012).

value of ϕ_o at a time t_o

$$\phi(t) = \phi_o + f(t - t_o) + \frac{1}{2}\dot{f}(t - t_o)^2 + \dots$$
(1.8)

where f is the pulse frequency. There are corrections for known effects that must be made before $\phi(t)$ can be predicted, making a more complex timing model. For example, effects from other planets in our Solar System, observatory clock corrections, and the difference in light travel time for different points in Earth's orbit all need to be accounted for in timing. Timing models also includes a variety of spin, astrometric, and binary (where applicable) parameters that can be fit for in order to minimize the difference between our model predicted TOAs and measured TOAs. This difference in arrival time is called the residual. These parameters characterize properties both intrinsic to the pulsar as well as extrinsic, like effects on the pulse arrival time due to the ISM. Timing is done using the TEMPO² software package, which applies a least-squares timing model fit. Errors on parameters are determined from the timing parameter covariance matrix after the least-squares fit.

Radio emission detected from pulsars is very weak; single pulses from MSPs are often too faint to detect over the noise. In addition, the pulse shape varies between pulses. As a result, pulses need to be summed in order to construct a stable average pulse profile to be used in the timing. Jitter, intrinsic variations in the pulse shape, causes the underlying pulse to vary from the summed template and introduces noise; an example of these pulse variations can be seen in Figure 1.2.2.

²http://tempo.sourceforge.net



Pulse Phase

Figure 1.6 Simulated pulse data showing variations in pulse profile that cause jitter, with the summed profile appearing at the top. The simulated data on the left shows pulses that are fairly identical over time, while the pulses on the right show shape variations between pulses (i.e. jitter). Both sets of pulses results in the same averaged pulse profile.



Figure 1.7 Pulse profile shapes for PSR J1713+0747 at different frequencies. The exponential tail visible at 150 and 350 MHz is caused by scattering. Plot from Dolch et al. (2014).

1.2.3 Pulsar timing array

In a PTA, the Earth and a pulsar each make up an end of our GW detector; the effects of a GW on each can be described by the "Earth term" and "pulsar term" respectively. While estimates of the pulsar distance may be known, they are not precise enough to enable detection of the change in distance due a GW perturbation. As a result, the pulsar term will not be correlated between pulsars. The Earth term will show a correlation between MSPs that is related to the angular separation between pulsars. This correlation function was calculated by Hellings & Downs (1983)

$$\alpha_{ij} = \frac{(1 - \cos \gamma_{ij})}{2} \ln \left(\frac{1 - \cos \gamma_{ij}}{2}\right) - \frac{1}{6} \frac{(1 - \cos \gamma_{ij})}{2} + \frac{1}{3} , \qquad (1.9)$$

where γ_{ij} is the angle between two pulsars (*i* and *j*) in the network. Due to the quadrupolar nature of GWs, pulsars in the same or opposite directions will show a correlated signal, while the residuals for pulsars at 90° angles from each other will be anti-correlated. The correlation function is illustrated by the Hellings-Downs curve, seen in Figure 1.8.

There are currently three global PTA efforts: the North American Nanohertz Observatory for Gravitational waves (NANOGrav; Arzoumanian et al., 2015), the European Pulsar Timing Array (EPTA; Desvignes et al., 2016), and the Parkes Pulsar Timing Array (PPTA; Manchester et al., 2013). These three experiments make up the International Pulsar Timing Array (IPTA; Manchester & IPTA, 2013). Other telescopes like MeerKAT and the Giant Metre-Wave Telescope (GMRT) are



Figure 1.8 The Hellings-Downs curve based on Equation 1.9. Image credit: NANOGrav.

also being used for pulsar timing, and may also be associated with future PTAs incorporated in the IPTA as well. This will be discussed more in Chapter 4.

Timing multiple pulsars forms a network of high precision Galactic clocks; this network is the PTA. The average signal-to-noise of a PTA in the intermediate GW signal limit is

$$S/N \propto N_{\rm MSP} T^{1/2} \left(\frac{c}{\sigma_{RMS}^2}\right)^{3/26}$$
, (1.10)

where N_{MSP} is the number of MSPs in the data set, T is the length of the data span, σ is the average rms and c is the average cadence of observations. Sensitivity of a PTA improves as more MSPs are added to the network; it is therefore essential to add as many well-timed MSPs as possible. A perturbation due to a passing GW at the Earth would create a correlated signal across the multi-pulsar network.

Taylor et al. (2016) calculate the probability of a GW detection as a function

of observation time. Using current estimates of merger rates, the probability of a GW detection by PTAs in the next 6 years is ~80%. PTAs will expand the range of GW astrophysics by offering constraints of the galaxy merger process, including eccentricity and stellar densities. The most recent NANOGrav limit on the GW stochastic background is $h = 1.45 \times 10^{-15}$ at a frequency of $f = 1 \text{ yr}^{-1}$ (Arzoumanian et al., 2018a).

1.3 The interstellar medium

Radio waves propagating through the interstellar medium (ISM) interact with this plasma in space, causing a variety of effects. The ISM is predominantly made up of hydrogen and helium that was created during the Big Bang. There is roughly one free electron for every 10 neutral hydrogen atoms (He et al., 2013).

1.3.1 Dispersion

Free electrons cause frequency-dependent dispersion of the pulse, which can be quantified by the dispersion measure (DM). The DM is the integrated column density of free electrons along the line of sight (LOS) to a pulsar

$$DM = \int_0^d n_e(l) dl , \qquad (1.11)$$

where n_e is the free electron density along a LOS l and d is the pulsar distance. By assuming a model for the Galactic electron density (Cordes & Lazio, 2002, i.e. NE2001;), DM can also be used to estimate the pulsar distance.



Figure 1.9 Frequency-dependent dispersion due to free electrons in the ISM. Plot taken from *Handbook of Pulsar Astronomy* (Lorimer & Kramer, 2012).

Dispersion causes a frequency-dependent time delay with pulses at lower frequency arriving later than those at higher frequencies. Because of the long distances these pulses are traveling, even a very small n_e can result in a measurable change in the pulse arrival time. In order to correct for the time delay caused by DM, timing observations must be done at multiple frequencies to quantify the DM and calculate the difference in arrival times between frequencies

$$\Delta t \simeq 4.15 \times 10^6 \text{ ms} \times \text{DM} \left(\frac{1}{\nu_1^2} - \frac{1}{\nu_2^2}\right) ,$$
 (1.12)

where the DM is in pc cm⁻³ and observing frequencies ν_1 and ν_2 are in MHz. For example, PSR J1713+0747 has a pulse period of 4.57 ms and a DM of 15.9 pc cm⁻³; if observed at $\nu_1 = 820$ MHz and $\nu_2 = 2300$ MHz (Arzoumanian et al., 2018b, as it is for NANOGrav;), the time delay due to DM would be 86 ms, roughly 19 times larger than the pulse period. The DM varies with time and needs to be fit at each observing epoch. When timing, observations at different frequencies can be timed together to estimate DM for that epoch; any TOAs within that bin are considered to have the same DM. DM is then fit over multiple windows over the data set to characterize any variations and get the clearest picture of the DM for a particular epoch.

For most pulsars, variations in DM exhibit structure over time. DMs can monotonically increase or decrease due to an increasing distance between the Earth and the pulsar, or due to stochastic variations in the ISM. Periodic variations in the form of a smooth sinusoid occur due to the Earth's motion around the Sun,



Figure 1.10 DM variations for PSR J1713+0747. Not only does the DM exhibit periodic structure, a significant dip in DM can be seen near the end of 2008 (MJD \sim 54700). DM variations are discussed more throughly in Chapter 2. Data taken from the NANOGrav 9-year data release (Arzoumanian et al., 2015).

or in sharp peaks as the LOS crosses the solar ionosphere. Studying structure can determine whether a DM trend is due to a real astrophysical effect or due to some other noise processes. Variations can occur on timescales of a few hours to years. Accounting for this DM variation timescale is important when determining DM windows for DM correction. Knowledge of such structure is helpful in understanding the ISM. Characterizing the structure seen in these variations along with possible explanations of them are laid out in Chapter 2.

1.3.2 Scattering

Pulses are scattered by irregularities in the ISM, causing variable path lengths and therefore varying time delays. This results in a scatter-broadened pulse. As seen with DM, lower frequencies are more affected by the turbulent plasma in the ISM, and so low frequencies experience more scattering than higher frequencies (scatter-



Figure 1.11 Scattering of the pulse by a turbulent plasma screen sitting between the Earth and the pulsar. Image taken from Cordes (2002).

ing scales as ν^{-4} , where ν is the observing frequency). Because DM and scattering are both frequency dependent, some scattering effects can be absorbed when fitting for DM. Low frequency observations can be used to disentangle scattering contributions from DM. The same irregularities in the ISM that cause scattering also cause scintillation. As the pulse propagation paths change with time, so does the phase of the pulse when it reaches the Earth (i.e. constructive/destructive interference of the pulse). Similar to how stars twinkle when viewed from Earth, the pulse brightness will vary with the modulation of the pulse phase. The effects of scattering in pulsar timing are discussed more in Chapter 4.

1.4 Using multiple radio telescopes for GW astrophysics

There are many radio telescopes currently being used for GW detection by PTAs as well as other PTA science. Observing with multiple telescopes improves sky coverage and cadence as multiple telescopes can observe the same source.

The EPTA utilizes the Effelsberg 100-m Radio Telescope in Germany, the Lovell Telescope at Jodrell Bank in the UK, the Nançay decimetric radio telescope in France, and the Westerbork Synthesis Radio Telescope in the Netherlands. When the Sardinia Radio Telescope in Italy comes fully online, it will also be used in EPTA science (Desvignes et al., 2016). This group of telescopes has the advantage of providing wide frequency coverage, high cadence, and a long timing baseline for many pulsars.

The PPTA uses the Parkes Observatory in Australia. Parkes is equipped with a 64-m dish and also has a long timing baseline for many pulsars. Parkes is able to observe MSPs in the Southern Hemisphere that are not visible to the other PTAs; this coverage is useful for the IPTA.

NANOGrav observes with the Arecibo Observatory in Puerto Rico and the Green Bank Observatory in West Virginia. The Arecibo Observatory hosts a 305-m dish; due to this large collecting area, Arecibo is extremely sensitive. Because of this size, the dish cannot move and therefore has limited range on the sky that it can observe. The Green Bank Observatory on the other hand can see $\sim 85\%$ of the sky; at 100-m, it is the largest steerable object on land. Both Arecibo and Green Bank are capable of observing large bandwidths, providing the highest precision TOAs.

1.4.1 Telescopes starting to do PTA science

The Giant Metrewave Radio Telescope (GMRT) and Ooty Radio Telescope (ORT) are both part of the National Centre for Radio Astrophysics (NCRA) in India. The ORT is a 530-m long and 30-m cylindrical parabolic antenna. The GMRT is made up of 30 45-m dishes and offers frequency coverage from 150 to 1500 MHz. This lower coverage will make the GMRT useful for noise and ISM studies. The Very Large Array (VLA) in New Mexico is comprised of 27 25-m dishes. Pulsar timing has been done at the VLA for the past few years; the VLA can observe PSR J0437–4715 in the south, which is a particularly bright MSP with high timing precision. The array can also observe at high frequencies (2 to 4 GHz) which is useful for ISM mitigation. The MeerKAT radio telescope is currently operating and will be made up of 64 dishes that are each comprised of a 13.5-m reflector and 3.8-m subreflector. MeerKAT will make very sensitive TOA measurements, and will be capable of forming sub-arrays to observe multiple pulsars at once.

The Canadian Hydrogen Intensity Mapping Experiment (CHIME) telescope and Five-hundred-meter Aperture Spherical radio Telescope (FAST) are both in the commissioning phase and will be used to time pulsars once completed. CHIME consists of 4 100-m by 20-m semi-cylinders in British Columbia. The telescope cannot be steered, it observes the sky overhead as the Earth turns. CHIME can observe up to 10 pulsars simultaneously (observation duration depends on declination, MSPs may be visible for \sim 10 minutes or less; Ng, 2017). CHIME will observe frequencies from 400 to 800 MHz. Daily observations with CHIME will be very useful for DM correction and characterization. FAST in China is very similar to the Arecibo Observatory, only much bigger (500-m) and can observe a larger range in declination. FAST will achieve incredibly sensitive observations of MSPs (Hobbs et al., 2014).

1.4.2 Combining timing data

There can be many difficulties in combining data from multiple telescopes as each telescope has its own aspects that may need to be taken into account. Telescope backends are also individual to the telescope and are replaced/upgraded over time, which needs to be accounted for when incorporating older data. Different observatories may use different file formats, header information, and hardware/software for data acquisition. Data processing is done differently in each PTA, and timing models can vary between PTAs. For example, DM is corrected for by a different method, different timing parameters (e.g. using a solar wind model) may be used, among other others.

1.5 Astrophysics across a wide frequency range

In this thesis multiple radio observations at various frequencies between 322 MHz and 10 GHz are used to conduct astrophysical research related to GW detection using PTAs. In Chapter 2, we discuss DM variations seen in the NANOGrav 9-year data release using wideband multi-frequency observations. Specifically, we measure and analyze trends seen in the DM time series, propose sources of these trends, and identify timescales over which the DM varies beyond measurement errors and therefore can no longer be considered constant. In Chapter 3, we analyze a previously published work that identifies the galaxy NGC 3115 as being an AGN potentially situated outside of the galactic photocenter. We investigate the possibilities that the source is a SMBH binary or a post-merger recoiling SMBH. In Chapter 4, we compare DM measurements obtained with dual-frequency GMRT observations to those calculated in the NANOGrav 11-year data release and assess the relative precision of the GMRT DM measurements. We also examine data taken with the GMRT to identify its potential for inclusion in the IPTA. In Chapter 5, conclusions are put forth based on the works presented here and discuss avenues for future works.

Chapter 2

The NANOGrav Nine-Year Data Set:

Measurement and Analysis of Variations in Dispersion Measures

2.1 Abstract

We analyze dispersion measure (DM) variations of 37 millisecond pulsars in the nine-year North American Nanohertz Observatory for Gravitational Waves (NANOGrav) data release and constrain the sources of these variations. DM variations can result from a changing distance between Earth and the pulsar, inhomogeneities in the interstellar medium, and solar effects. Variations are signicant for nearly all pulsars, with characteristic timescales comparable to or even shorter than the average spacing between observations. Five pulsars have periodic annual variations, 14 pulsars have monotonically increasing or decreasing trends, and 14 pulsars show both effects. Of the four pulsars with linear trends that have line-of-sight velocity measurements, three are consistent with a changing distance and require an overdensity of free electrons local to the pulsar. Several pulsars show correlations

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between DM excesses and lines of sight that pass close to the Sun. Mapping of the DM variations as a function of the pulsar trajectory can identify localized interstellar medium features and, in one case, an upper limit to the size of the dispersing region of 4 AU. Four pulsars show roughly Kolmogorov structure functions(SFs), and another four show SFs less steep than Kolmogorov. One pulsar has too large an uncertainty to allow comparisons. We discuss explanations for apparent departures from a Kolmogorov-like spectrum, and we show that the presence of other trends and localized features or gradients in the interstellar medium is the most likely cause.

2.2 Introduction

The principal goal of the North American Nanohertz Observatory for Gravitational Waves (NANOGrav; McLaughlin, 2013) is to detect gravitational waves in the nanohertz regime of the gravitational wave spectrum using a pulsar timing array (PTA). Sensitivity improves as more millisecond pulsars (MSPs) are added to the PTA, and therefore it is essential to have as many well-timed MSPs as possible (Siemens et al., 2013; Vigeland & Siemens, 2016). For every MSP, we must construct an accurate timing model that accounts for all known effects on the pulsar times-of-arrival (TOAs) over decade timescales (Jenet et al., 2005; Cordes & Shannon, 2010). One of the parameters that must be fit in the timing model is the dispersion measure (DM; Lorimer & Kramer, 2012). As the pulsar signal travels through the interstellar medium (ISM), it encounters ionized plasma and electron density variations along the way. The DM is the integrated column density of free electrons along the line of sight to a pulsar

$$DM = \int_0^d n_e(l) dl , \qquad (2.1)$$

where n_e is the free electron density along a line of sight l and d is the pulsar distance. When the pulsar signal propagates through the ISM, interactions with these free electrons cause dispersion that is characterized by a frequency dependent time delay

$$\Delta t \simeq 4.15 \times 10^6 \text{ ms} \times \text{DM} \left(\frac{1}{\nu_1^2} - \frac{1}{\nu_2^2}\right) ,$$
 (2.2)

where ν_1 and ν_2 are two different frequencies in MHz and DM is in pc cm⁻³. Observing at least two frequencies is necessary to solve for the DM for a measured time delay. This time delay can be significant when compared to the pulsar period, and therefore the DM must be fit when creating a timing model and corrected for at each epoch (e.g. Demorest et al., 2013; Arzoumanian et al., 2015).

Inhomogeneities in the ISM, solar wind, and differences in the relative velocity of the pulsar and the Earth can change the free electron density along the line of sight (LOS; Lam et al., 2016). The result is a DM that varies with time, changing on timescales of hours to years. In this paper we discuss the variations seen in the NANOGrav 9-year data release (Arzoumanian et al., 2015), constrain the possible sources of these variations, and use these constraints to characterize the ISM along the LOS. In §2, we discuss the data used for this analysis. In §3, we discuss the significance and trends seen in the DM time series. In §4, we perform a structure function (SF) analysis on select MSPs and put the results in the context of a Kolmogorov spectrum. In §5, we discuss the results of these analyses and in §6 we present conclusions.

2.3 The NANOGrav 9-year data set

Our analysis uses data from the NANOGrav 9-year data set (Arzoumanian et al., 2015). Pulsars were included in the data set based on the anticipated stability of their timing, their TOA precision, and their detection over a wide frequency range. Of the 37 MSPs included in the data release, 17 were reported on in Demorest et al. (2013). Observations took place roughly once a month between 2004 and 2013 with observing time spans of individual pulsars ranging from 0.6 to 9.0 years. Those MSPs with declinations between 0 and 39° were observed with the 305-m William E. Gordon Telescope at the Arecibo Observatory, and the rest were observed with the 100-m Robert C. Byrd Green Bank Telescope (GBT) of the National Radio Astronomy Observatory (NRAO); PSRs J1713+0747 and B1937+21 were observed with both telescopes. Every MSP was observed at multiple frequencies to account for frequency-dependent dispersion effects. Dual frequency observations occurred within ~ 1 hour at Arecibo and within several days at the GBT. The typical length of an observation was ~ 25 minutes. A more detailed and thorough description of these observations can be found in Arzoumanian et al. (2015).

For each pulsar, the DM was measured at nearly every observing epoch and recorded using the DMX parameter as part of the TEMPO software package¹, where DMX models DM as constant over a chosen time window (14 days in this case). The ΔDM , an offset from a globally fixed fiducial DM, is fit as a free parameter in the timing model. The possible errors in DM(t) estimation using this method are discussed in Lam et al. (2015). Errors on DM are 1σ and are determined from the timing-parameter covariance matrix after the least-squares timing model fit. Data from early single-receiver observations were omitted for PSRs J1741+1351, J1853+1303, J1910+1256, J1944+0907, and B1953+29 as it was not possible to independently measure DM and other timing properties. We plot DMs vs time (i.e., DM(t) for all of the pulsars in Figures 2.1 through 2.5. Values from the 9-year data release used in this analysis can be seen in Table 2.1. Partial DM(t) data spans have already been published for 15 pulsars (PSRs J0340+4130, J0613-0200, J1614-2230, J1713 + 0747, J1738 + 0333, J1741 + 1351, J1744 - 1134, B1855 + 09, J1909 - 3744, J1741 + 1351, J1744 - 1134, J1741 + 1351, J1744 - 1134, J1741 + 1351, J1744 - 1134, J1744 - J1J1910+1256, J1918-0642, B1937+21, J1944+0907, J2010-1323, and J2302+4442) in Levin et al. (2016).

2.4 Determining significance and trends in the variations

Variability in the DM timeseries can be seen for many pulsars; it has been a long known effect. The first detection of temporal variations was for the Crab pulsar (Rankin & Roberts, 1971). These variations were later determined to be most likely due to variations in the surrounding nebula (Isaacman & Rankin, 1977). The Vela

 $^{^1\}mathrm{TEMPO}$ software package: http://tempo.sourceforge.net

pulsar exhibits a decreasing time-dependent DM attributed to the pulsar motion through the enveloping supernova remnant (Hamilton et al., 1985).

We first determine whether the DM variations we see are significant or if they are consistent (within errors) with a constant DM value. We calculate the reduced χ^2 for each pulsar as

$$\chi_r^2 = \frac{1}{N_{\rm DOF}} \sum \frac{(\mathrm{DM}(t) - \overline{\mathrm{DM}})^2}{\sigma(t)^2} , \qquad (2.3)$$

where N_{DOF} is the number of degrees of freedom, $\overline{\text{DM}}$ is the average DM value for the data span for a pulsar (in this model), and $\sigma(t)$ is the error associated with each DM(t) value. All but two of the pulsars (PSRs J1923+2515 and J2214+3000) have $\chi_r^2 \ge 1$. Of these, we identify 15 pulsars as showing moderate variations (those with $1 \le \chi_r^2 \le 10$), and 20 pulsars with significant variations ($\chi_r^2 \ge 10$). We therefore conclude that the DMs are intrinsically variable for all of the MSPs in our sample with the possible exceptions of J1923+2515 and J2214+3000, which both show visible variation at a low level despite the statistical test. Both of these pulsars have short data sets (2.2 and 2.1 years, respectively).

2.4.1 Systematic variations

DMs can vary in many ways, with components that appear linear, periodic, or random. Here we consider systematic DM variations such as linear trends and periodicities. Stochastic contributions are discussed in Section 2.5. Sources of linear trends and periodicities include a changing distance between the Earth and the

PSR	μ_{λ}	μ_{eta}	μ_{lpha}	μ_{δ}	DM	$d_{\rm DM}$	$d_{\rm PX}$	χ^2_r	v_T
	$(mas yr^{-1})$	$(mas yr^{-1})$	$(mas yr^{-1})$	$(mas yr^{-1})$	$(pc cm^{-3})$	(kpc)	(kpc)		$(\rm km~s^{-1})$
J0023+0923	-13.9(2)	-1(1)	-12.3(6)	-6.7(9)	14.3	0.7(2)		4.2	46(13)
J0030 + 0451	-5.52(1)	3.0(5)	-6.3(2)	0.6(5)	4.3	0.3(1)	0.30(2)	11	8.9(7)
J0340 + 4130	-2.4(8)	-4(1)	-1.3(7)	-5(1)	49.6	1.7(4)		6.8	38(12)
J0613-0200	2.12(2)	-10.34(4)	1.85(2)	-10.39(4)	38.8	1.7(4)	1.1(2)	70	55(10)
J0645+5158	2.1(1)	-7.3(2)	1.4(1)	-7.5(2)	18.2	0.7(2)	0.8(3)	2.7	29(11)
J0931-1902					41.5	1.8(5)		2.2	
J1012+5307	13.9(1)	-21.7(3)	2.5(2)	-25.6(2)	9.0	0.4(1)		1.8	49(12)
J1024-0719	-14.36(6)	-57.8(3)	-35.2(1)	-48.0(2)	6.5	0.4(1)		15	113(28)
J1455-3330	8.16(7)	0.5(3)	7.9(1)	-2.0(3)	13.6	0.5(1)		2.4	19(4)
J1600-3053	0.47(2)	-7.0(1)	-0.95(3)	-7.0(1)	52.3	1.6(4)	3.0(8)	42	100(27)
J1614-2230	9.46(2)	-31(1)	3.8(2)	-32(1)	34.5	1.3(3)	0.65(5)	20	100(8)
J1640 + 2224	4.20(1)	-10.73(2)	2.09(1)	-11.33(2)	18.5	1.2(3)		295	66(16)
J1643-1224	5.56(8)	5.3(5)	6.2(1)	4.5(5)	62.4	2.3(6)		112	84(22)
$J1713 \pm 0747$	5.260(2)	-3442(5)	4.918(2)	-3.914(5)	16.0	0.9(2)	1.18(4)	29	35(1)
11738 ± 0333	6.6(2)	6.0(4)	6.9(2)	5.8(4)	33.8	1.4(4)		5.0	59(17)
01100 0000	0.0(2)	0.0(4)	0.0(2)	0.0(4)	00.0	1.1(1)		0.0	00(11)
J1741 + 1351	-8.8(1)	-7.6(2)	-9.1(1)	-7.2(2)	24.2	0.9(2)		4.7	50(11)
J1744–1134	19.01(2)	-8.68(8)	18.76(2)	-9.20(8)	3.1	0.4(1)	0.41(2)	17	41(2)
J1747-4036	0.1(8)	-6(1)	0(1)	-6(1)	153.0	3.3(8)	—	133	_
J1832-0836					28.2	1.1(3)		16	
J1853+1303	-1.8(2)	-2.9(4)	-1.48(2)	-3.1(4)	30.6	2.0(5)		5.8	32(9)
	~ /	()	()	()		()			()
B1855 + 09	-3.27(1)	-5.10(3)	-2.651(15)	-5.45(3)	13.3	1.2(3)		1335	34(9)
J1903+0327	-3.5(3)	-6.2(9)	-2.7(3)	-6.5(9)	297.6	6(2)		27	202(71)
J1909–3744	-13.868(4)	-34.34(2)	-9.518(4)	-35.79(2)	10.4	0.5(1)	1.07(4)	1375	188(7)
J1910 + 1256	-0.7(1)	-7.2(2)	0.3(1)	-7.2(2)	38.1	2.3(6)	_ ``	2.7	79(21)
J1918-0642	-7.93(2)	-4.85(9)	-7.18(3)	-5.90(9)	26.6	1.2(3)	0.9(2)	171	40(9)
						(-)	()		- (-)
J1923 + 2515	-9.5(2)	-12.8(5)	-6.6(2)	-14.5(5)	18.9	1.6(4)		0.9	121(30)
B1937 + 21	-0.02(1)	-0.41(2)	0.07(1)	-0.40(2)	71.0	3.6(7)		1162	7(1)
J1944 + 0907	9.4(1)	-25.5(4)	14.37(11)	-23.1(4)	24.3	1.8(5)		147	232(64)
J1949 + 3106	13(15)	10(13)	10(11)	13(16)	164.1	3.6(9)		1.4	
B1953 + 29	-1.8(9)	-4.4(14)	-0.4(12)	-5(1)	104.5	5(1)		6.6	113(24)
J2010-1323	1.16(4)	-7.3(4)	2.71(9)	-6.9(4)	22.2	1.0(3)		70	35(11)
J2017+0603	2.3(6)	-0.1(7)	2.2(7)	0.5(6)	23.9	1.6(4)		2.8	
J2043+1711	-8.97(7)	-8.5(1)	-5.85(7)	-10.9(1)	20.7	1.7(4)	1.3(4)	6.3	100(23)
J2145-0750	-12.04(4)	-3.7(4)	-10.1(1)	-7.5(4)	9.0	0.6(2)	0.8(2)	24	48(12)
J2214 + 3000	17.1(5)	-10.5(9)	20.0(6)	-1.7(8)	22.6	1.5(4)		1.0	143(38)
52211 0000	11.1(0)	10.0(0)	20.0(0)	1.1(0)	22.0	1.0(1)		1.0	110(00)
J2302 + 4442	-3.3(6)	-1(2)	-2(1)	-3(2)	13.7	1.1(3)		1.5	
J2317 + 1439	0.19(2)	3.80(7)	-1.39(3)	3.55(6)	21.9	0.8(2)	1.3(4)	18732	14(4)

Table 2.1 Properties of NANOGrav MSPs in the 9-Year Data Release.

Notes. Columns are pulsar name, ecliptic proper motion (longitude and latitude), proper motion in RA and Dec, the DM, the DM-derived distance, the parallax-derived distance, the reduced chi-squared of the DM time series prior to any fitting, and the transverse velocity. The ecliptic proper motions and DMs were calculated for the 9-year data release (Arzoumanian et al., 2015). Proper motion in RA and Dec as well as parallax distances were calculated through timing observations and discussed in Matthews et al. (2016). The DM derived distances were calculated from the NE2001 model assuming 20% error (Cordes & Lazio 2002). The value for χ_r^2 was calculated using Equation 2.3. Dashes indicate that no significant measurement was possible. The transverse velocity v_T was calculated from the proper motion and the distance estimate with the smaller error (i.e. d_{DM} or d_{PX}).

$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	PSR	Trend	$d\mathrm{DM}/dt$	Amplitude	Period	χ^2_r	Pls	FAP	Length	δt
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $			$(10^{-3} \text{ pc cm}^{-3} \text{ yr}^{-1})$	$(10^{-4} \text{ pc cm}^{-3})$	(days)	701	(days)	(%)	(days)	(days)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	10000 + 0000	N		(1)				()	0.41	())
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J0023+0923	None		1.2(2)					841	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	J0030+0451	Periodic		1.2(3)	373(5)	9.2	371	6.3	3204	33
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J0340 + 4130	Linear	0.88(9)			1.7	241	6.3	613	73
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J0645 + 5158	Periodic		0.9(3)	377(29)	2.6	199	0.54	881	78
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J0931–1902	None							235	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J1012+5307	Linear	0.11(2)			0.94			3368	2286
	J1024–0719	Linear	0.39(2)			2.7			1467	148
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J1455–3330	Linear	0.15(2)			1.0	361	7.3	3368	904
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1614–2230	Periodic		3.1(5)	370(9)	11	370	0.17	1860	14
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1643 - 1224	Both	-1.02(3)	8(1)	387(4)	10	387	0.01	3293	104
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1738 + 0333	Linear	-0.8(2)			1.4			1456	213
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1741 + 1351	Linear	-0.12(4)			1.9			1224	287
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1744 - 1134	Both	-0.069(7)	0.4(2)	383(16)	8.0			3369	66
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J1747 - 4036	Linear	-7.3(4)	_	— ` `	10.0	459	6.7	608	16
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1832-0836	None							231	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1853 + 1303	Linear	0.12(9)			5.2			1468	361
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	B1855 + 09	Both	0.382(7)	0.5(3)	364(11)	15.7			3240	27
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J1903+0327	Both	-3.0(4)	31(6)	375(11)	12	371	1.0	1456	99
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J1909-3744	Both	-0.239(4)	0.7(1)	366(5)	28	366	0.25	3306	9
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J1910 + 1256	Linear	0.51(6)			0.90	404	2.9	2574	443
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	J1923 + 2515	None							803	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	11944 ± 0907	Linear	1.3(2)			44			1467	43
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	11949 ± 3106	Periodic		10(3)	391(37)	1.0			455	51
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$R1053 \pm 20$	Both	-1.3(3)	3(2)	356(72)	2.1			1967	136
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	I2010-1323	Both	0.38(2)	22(4)	372(0)	14	379	0.56	1/00	16
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12010 + 1020 12017 ± 0603	Both	0.33(2) 0.23(7)	$2.2(\pm)$ 2.3(5)	440(37)	0.04	512	0.50	600	38
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12017 ± 0003 12043 ± 1711	Both	-0.12(4)	2.5(5) 1.0(4)	300(38)	37			834	180
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$J2045 \pm 1711$ J2145_0750	Lincor	-0.12(4)	1.0(4)	030(00)	10			9910	569
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J2140-0700 J2014+2000	Daviadia	0.08(2)	4(1)		10			0010 755	17
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	12214 ± 3000 12202 ± 4442	Lincor		4(1)	319(20)	0.05			619	11
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$J_{2302} + 4442$ $J_{2317} + 1420$	Dut	-0.0(2)			1.0			2042	202
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	J2317+1439	Both	-0.550(9)	0.9(3)	311(0)	321			3243	5
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	PSR	Trend	$d\mathrm{DM}/dt$	Amplitude	Period	χ^2_{π}	Start	End	Length	δt
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			$(10^{-3} \text{ pc cm}^{-3} \text{ vr}^{-1})$	$(10^{-4} \text{ pc cm}^{-3})$	(davs)	707			(davs)	(days)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	10619 0000	D (1		1 0(1)	050(4)	0.70	59440	F 1070	0107	10
Both $0.161(7)$ $1.2(2)$ $352(5)$ 3.5 54970 56380 $ 23$ J1600-3053Linear $-0.73(4)$ $ 2.8$ 54400 55300 2184 40 None $ 55300$ 56585 $ -$ J1640+2224Linear $0.145(3)$ $ 7.0$ 53344 55850 3254 78 None $ 55850$ 56599 $ -$ J1713+0747Both $-0.066(8)$ $0.5(1)$ $400(16)$ 2.0 53393 54730 3199 38 None $ -$ Both $-0.015(5)$ $0.52(9)$ $369(7)$ 5.5 54900 56592 $ -$ J1918-0642Both $-0.49(1)$ $1.2(4)$ $385(11)$ 4.3 53292 56000 3293 24 Both $0.23(3)$ $1.2(3)$ $541(47)$ 2.9 56000 56585 $ 31$ B1937+21Both $-0.34(3)$ $3.2(4)$ $395(11)$ 28 53267 54550 3327 5 None $ -$ Both $0.050(3)$ $3.7(2)$ $469(14)$ 10 55970 $ -$	J0613-0200	Both	0.066(7)	1.8(1)	358(4)	0.72	53448	54970	3137	18
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		Both	0.161(7)	1.2(2)	352(5)	3.5	54970	56380		23
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	J1600–3053	Linear	-0.73(4)			2.8	54400	55300	2184	40
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		None	—				55300	56585		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	J1640 + 2224	Linear	0.145(3)			7.0	53344	55850	3254	78
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		None					55850	56599		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	J1713 + 0747	Both	-0.066(8)	0.5(1)	400(16)	2.0	53393	54730	3199	38
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		None					54730	54900		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		Both	-0.015(5)	0.52(9)	369(7)	5.5	54900	56592		26
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	J1918-0642	Both	-0.49(1)	1.2(4)	385(11)	4.3	53292	56000	3293	24
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		Both	0.23(3)	1.2(3)	541(47)	2.9	56000	56585		31
None54550 55970 Both $0.050(3)$ $3.7(2)$ $469(14)$ 10 55970 56594 5	B1937 + 21	Both	-0.34(3)	3.2(4)	395(11)	28	53267	54550	3327	5
Both $0.050(3)$ $3.7(2)$ $469(14)$ 10 55970 56594 — 5		None	_				54550	55970		
		Both	0.050(3)	3.7(2)	469(14)	10	55970	56594		5

Table 2.2 Fitted Trends in the DM Time Series for MSPs in the 9-Year Release

Notes. Results of fitting periodic and linear trends to the DM variations, where 1σ uncertainty in the last significant digit is expressed in parentheses. The upper section lists pulsars where a single fit was applied; columns are the detected trend, the slope, the amplitude of the periodic fit, the period of the fit, the reduced chi-squared after the fitting, the period found by the Lomb-Scargle periodogram, the false alarm probability for that period, the length of the data span for that pulsar, and the average time it takes the DM time series to vary by 1σ . The lower section contains pulsars where piecewise trends were applied. The two columns that differ from above give the final start and end dates used in the fit.

pulsar, a wedge with linear density changes in the ISM or the orbital motion of the Earth, among others; the possible geometries from which these trends arise are explained in detail in Lam et al. (2016). Both linear and periodic trends have been seen in Parkes Pulsar Timing Array (PPTA) data (You et al., 2007; Keith et al., 2013; Petroff et al., 2013; Reardon et al., 2016). Petroff et al. (2013) determine the significance of a linear trend by calculating the error of a fit to the slope; linear trends were deemed significant if the errors are less than 35% of the slope value and highly significant if the errors on the slope measurement are less than 20%. This method is not applicable for the NANOGrav 9-year data set as a large number of pulsars exhibit sinusoidal trends without linear trends.

In order to determine the scale and structure of the variations, the options being linear, periodic, both, or variations consistent with stochastic noise, we applied a non-linear least squares fit to the data using three functions,

$$\overline{\mathrm{DM}_{1}}(t) = mt + b,$$

$$\overline{\mathrm{DM}_{2}}(t) = A\cos(\omega t + \phi) + b,$$

$$\overline{\mathrm{DM}_{3}}(t) = A\cos(\omega t + \phi) + mt + b,$$
(2.4)

with the χ_r^2 calculated for the time series after each of these fits was individually subtracted off. For each fit, $N_{\text{DOF}} \approx N - N_p$, where N is the number of DM measurements and N_p is the number of free parameters being fit in that function $(N_p = 1 \text{ when } \overline{\text{DM}}(t)$ is a constant value). The three χ_r^2 values were then compared to the original value; the result producing the lowest χ_r^2 was assigned as the trend. The results of these fits can be seen in Table 2.2. There is a known complication when estimating the number of degrees of freedom for a non-linear model (Andrae et al., 2010). The χ_r^2 is only used as a metric to compare the fits of models we know to be incomplete; as stated earlier, the ISM is more complicated than a purely linear trend plus annual component. The fitting routine incorporates a non-linear least squares fit which is locally linearized around the minimum χ_r^2 . Later on, we describe χ_r^2 surfaces in the full parameter space and analyze the degree of covariance between fit parameters, finding it agrees with this fitting routine.

The periodic term in the function was fit using an initial guess of 365 days. Due to a change in sign of dDM/dt or the appearance/disappearance of a trend partway through the data span, PSRs J0613–0200, J1600–3053, J1640+2224, J1918–0642, and B1937+21 are not well characterized by a single fit. These MSPs were fit using piecewise functions, using the χ_r^2 of the fit to identify the applicable MJD range for each fit. The results of this partial fitting can be seen in Table 2.2. The fits can be seen in Figures 2.1 through 2.5. The χ_r^2 values listed in Table 2.2 are for the individual fit regions; these differ from the values shown in Figures 2.1 through 2.5 because those values incorporate both fits as well as any regions excluded from the fit.

We applied a Lomb-Scargle periodogram analysis to corroborate the best-fit periods, as an annual period was suggested during the trend fitting routine. The periodogram is also useful in possibly identifying non-annual periodicities (also seen in Table 2.2). This analysis is able to detect periodicities in unevenly sampled data (Scargle, 1982) for which a false alarm probability (FAP) may be calculated. The



Figure 2.1 The top panel shows the DM time series with the best fit function (if applicable) in blue. The bottom panel shows the DM residuals after the trend has been removed from the time series; an empty panel means no trend was found. The χ_r^2 values before and after these fits for each pulsar appear in the top and bottom panels respectively, as well as in Tables 2.1 and 2.2. PSR J0931–1902 has too short a data span for a trend to be determined.



Figure 2.2 The top panel shows the DM time series with the best fit function (if applicable) in blue. The bottom panel shows the DM residuals after the trend has been removed from the time series; an empty panel means no trend was found. PSRs J1600–3053 and J1640+2224 were not found to have significant trends in the later parts of the DM time series.



Figure 2.3 The top panel shows the DM time series with the best fit function (if applicable) in blue. The bottom panel shows the DM residuals after the trend has been removed from the time series; an empty panel means no trend was found. PSR J1832–0836 has too short a data span for a trend to be determined.



Figure 2.4 The top panel shows the DM time series with the best fit function (if applicable) in blue. The bottom panel shows the DM residuals after the trend has been removed from the time series; an empty panel means no trend was found. PSR B1937+21 could not be fit with a periodic trend throughout the data set.



Figure 2.5 The top panel shows the DM time series with the best fit function (if applicable) in blue. The bottom panel shows the DM residuals after the trend has been removed from the time series; an empty panel means no trend was found.

FAP is the likelihood that these periods would occur as a result of random white noise. We ignored periods found by the periodogram that coincided with either the length of the data set or the observing cadence. The resolution of the analysis is equal to the cadence of the observations. Any linear trend in the DM variations will mask the periodic effect, and therefore was removed from those identified to have linear effects before applying the periodogram analysis.

2.4.2 DM variation timescale

The DM value can vary on timescales of years, days, or even hours. Therefore it is important to know on what timescale this DM is accurate. The time δt for DM to change by $\sigma_{\rm DM}$, the rms DM in the DM time series (prior to fitting any DM trends), gives us a rough estimate for how long a single DM estimation is valid. For a linear trend

$$\frac{\sigma_{\rm DM}}{\delta t} = \frac{d\rm DM}{dt} = m \longrightarrow \delta t = \frac{\sigma_{\rm DM}}{m} , \qquad (2.5)$$

where m is the slope of the linear trend, seen also in Equation 2.4. The time associated with a periodic trend

$$\frac{\sigma_{\rm DM}}{\delta t} = \frac{d\rm DM}{dt} \approx A\omega \longrightarrow \delta t = \frac{\sigma_{\rm DM}}{A\omega} , \qquad (2.6)$$

where A and ω are the amplitude and angular frequency of the periodic trend respectively. The variation time for a DM time series showing both trends combines



Figure 2.6 MSP positions with respect to the ecliptic, shown in RA and Dec (left) as well as ecliptic coordinates (right). In the left plot, the ecliptic is depicted by the dashed line. Sources that lie within $\sim 10^{\circ}$ of the ecliptic are signified by triangles.

the dDM/dt components from both the periodic and linear components

$$\frac{\sigma_{\rm DM}}{\delta t} \approx m + A\omega \longrightarrow \delta t \approx \frac{\sigma_{\rm DM}}{m + A\omega} . \tag{2.7}$$

The δt values for the MSPs showing trends are seen in Tables 2.2. This δt can inform on what timescale our DM measurement is constant and the importance of observing at epochs with spacing smaller than this timescale.

2.4.3 Solar-angle correlation

Pulsars that lie close to the ecliptic (within approximately 10°) will have their LOS pass near the Sun during Earth's orbit. This proximity can cause a sinusoidal trend in DM variations due to the variation in n_e along the LOS from the solar wind.

We examine the pulsar positions with respect to the ecliptic to determine for which MSPs this effect could be significant. As can be seen in Figure 2.6,



Solar Elongation (degrees)

Figure 2.7 DM variations with respect to the solar position angle. The linear trend identified for PSR J2010–1323 has been subtracted in order to better identify any correlation in the DM as a function of solar angle. Note that the two highest DM points seen for PSR J0030+0451 were omitted from the 9-year data set as outliers and are not plotted in Figure 2.1 (discussed in Section 2.4.3).

PSRs J0023+0923, J0030+0451, J1614-2230, and J2010-1323 reside close (within approximately 6.3°, 1.5°, 6.8°, and 6.5° respectively on closest approach in the data set) to the ecliptic. The DM as a function of solar elongation angle can be seen in Figure 2.4.3. PSRs J0023+0923 and J2010-1323 show a slight peak in DM at the smallest pulsar-Sun angles. PSRs J0030+0451 and J1614-2230 show significant peaks at the minimal solar elongation angle. It should be noted that the two highest DM points for J0030+0451 were omitted from Arzoumanian et al. (2015) as outliers but were included for this portion of the analysis.

2.4.4 Pulsar trajectories

We have plotted the pulsar trajectories through the ISM as seen from Earth, color coded to signify the DM value at each epoch (Figures 2.8 through 2.11). For this, we assumed that all of the free electrons along the line of sight are sitting in a stationary phase screen located halfway between the Earth and the pulsar. The trajectories are the projected motions of the pulsar as seen on this phase screen. Using proper motion and distance estimates with errors from the NE2001 model (Cordes & Lazio, 2002), the transverse velocity can be calculated and used to track the pulsar's trajectory in the sky. Proper motions were taken from the data release (seen in Table 2.1). These trajectory maps can be useful in isolating features in the ISM as well as visualizing trends in the DM time series.

2.5 Structure functions

Turbulence in the ISM is typically described as having a Kolmogorov power spectrum, meaning we expect to find larger variations over longer timescales. The power spectrum used to derive the structure function has the form

$$P(q) \propto q^{-\beta}, \ q_{\text{outer}} \le q \le q_{\text{inner}}$$
 (2.8)

where q is the reciprocal of the size scale, and β is the power spectrum exponent. A Kolmogorov medium corresponds to a β value of 11/3, while the highest value expected for turbulence in the ISM (for an inner scale shorter than 10⁹m) is $\beta = 4$ (Rickett, 1990). The outer scale is described as the size at which the ISM ceases to be homogeneous, and the inner scale is the point at which dissipation occurs in the material along the line of sight.

The DM structure function (SF) is an effective analytic tool for characterizing interstellar turbulence over various time and size scales (Rickett, 1990; Cordes et al.,



Figure 2.8 MSP trajectories are plotted with color mapping the DM at each epoch. PSR J0613–0200 shows higher DM regions on one side of its trajectory over time, suggesting the presence of a DM gradient that is transverse compared to the pulsar's motion. PSR J1024–0719 shows a monotonically increasing DM, which could be due to a DM gradient oriented in the same direction as the pulsar's motion.



Figure 2.9 MSP trajectories are plotted with color mapping the DM at each epoch. PSRs J1600–3053, J1640+2224, and J1643–1224 show a monotonically increasing or decreasing DM, which could be due to a DM gradient along the direction of motion. PSR J1614-2230 has high DM regions in the same part of its trajectory every year, suggesting a localized overdensity along the line of sight to the pulsar.



Figure 2.10 MSP trajectories are plotted with color mapping the DM at each epoch. PSRs B1855+09, J1909–3744, and J1918–0642 show a monotonically increasing or decreasing DM, which could be due to a DM gradient along the direction of motion. PSR J1903+0327 has high DM regions in the same part of its trajectory every year, suggesting a localized overdensity along the line of sight to the pulsar. PSR B1937+21 shows a distinct low DM region that is also evident in the DM time series, indicative of a localized bubble in the ISM.



Figure 2.11 MSP trajectories are plotted with color mapping the DM at each epoch. PSRs J1944+0907 and J2317+1439 show a monotonically increasing or decreasing DM, which could be due to a DM gradient along the direction of motion. PSR J2010–1323 shows an increasing DM in the direction of the pulsar's motion as well as high DM regions in the same part of its trajectory every year, suggesting a localized overdensity along the line of sight to the pulsar.



Time Lag [days]

Figure 2.12 Structure functions for the DM variations, calculated for the MSPs with measured diffractive timescales. Error bars extending to the bottom of the frame signify an upper limit (in agreement with You et al. (2007)). The solid grey lines signify a quadratic power law and the dotted lines signify a Kolmogorov power law, which are anchored to the diffractive timescale, while the solid black lines are the best fits for the model. The errors associated with β are $\pm 1\sigma$ errors.



Time Lag [days]

Figure 2.13 Structure functions for the DM variations, calculated for the MSPs with measured diffractive timescales. Error bars extending to the bottom of the frame signify an upper limit (in agreement with You et al. (2007)). The solid grey lines signify a quadratic power law and the dotted lines signify a Kolmogorov power law, which are anchored to the diffractive timescale, while the solid black lines are the best fits for the model. The errors associated with β are $\pm 1\sigma$ errors.

1990; You et al., 2007; Keith et al., 2013; Fonseca et al., 2014; Lam et al., 2016). We compute SFs by binning the change in time across all epochs into equally log-spaced bins after calculating

$$D_{\rm DM}(\tau) = \left\langle [\rm DM}(t+\tau) - \rm DM}(t)]^2 \right\rangle , \qquad (2.9)$$

where τ is the time lag in days (Cordes & Rickett, 1998). The diffractive timescale $\Delta \tau_D$, the scale during which the diffraction intensity varies as a result of irregularities in the ionized plasma along the line of sight, is used to anchor the SF

$$D_{\rm DM}(\tau) = (A_{\nu}\nu)^2 (\tau/\Delta\tau_{\rm D})^{\beta-2} , \qquad (2.10)$$

where $A_{\nu} = 3.84 \times 10^{-5} \text{ MHz}^{-2} \text{ s}^{-1} \text{ pc cm}^{-3}$ and ν is the observing frequency. Epoch to epoch variations of $\Delta \tau_{\rm D}$ are expected of order 10% or more (Lam et al., 2016). The SF is poorly estimated at large time lags, and so some functions may appear Kolmogorov at shorter timescales but fall below at longer time lags; this is an indication of an underlying Kolmogorov spectrum (You et al., 2007). This is also why SF values at high time lags may have large errors on them. Quadratic SFs occur when the time lag is smaller than the timescale necessary to adequately probe the structure in a region, if any (Lam et al., 2016).

Several models were applied to the SF in order to constrain a range for β . Fitting only for Equation 2.10 is problematic because there are other contributions to the SF, such as trends and noise, among other possibilities. However, over-fitting the SF will cause the fit to fail for a number of reasons, discussed in this section. The models are of the form

$$D_{\rm DM}(\tau) = D_{\rm sto}(\tau) + D_{\rm lin}(\tau) + D_{\rm per}(\tau) + D_{\rm noise}(\tau) , \qquad (2.11)$$

where the first term is the stochastic (e.g. from the electron density wave number spectrum) component, the second term is the linear component, the third term is the periodic component, and the last term is the noise (e.g. measurement errors) component.

One method is to fit the stochastic and noise components while fixing the linear trend and periodic components to the trend values found in the time series analysis. However, we were only able to successfully fit the SF for one pulsar (PSR J1643-1224) using this model. In all other cases, the SF of the two trends is higher than the calculated SF; fitting for a stochastic component on top of that would only increase the chi-squared, and the fit fails. This failure is evidence that there is contamination between the stochastic and trend components. In many cases, a linear trend fit over the time series will absorb part of the stochastic component. Therefore, the "true" linear trend may be different than the one we fit for in the time series, which will bias the component in the SF high. Therefore, we are unable to obtain a proper fit using this model.

To bypass this contamination between the trend and stochastic aspects, we tried fitting for all parameters (stochastic, noise, linear, and periodic) without using any prior information in the hopes of allowing a fit and comparing values with those previously found. Due to the covariant nature of the parameters, we found values for the stochastic, periodic amplitude, and noise components, but the amplitude of the periodic trend was not much larger than its uncertainties while the linear trend component was found to be zero. The period was then fixed to one year in order to eliminate some of the covariance; fixing the period again gave significant values for the stochastic, noise, and periodic amplitude components, and no significance for an additional linear component. This is further evidence of the high covariance between the stochastic and linear trend components. The periodic amplitudes found here agree very well with those found previously by the trend analysis. Simultaneously fitting for both the stochastic and linear components does not appear to yield significant values for both.

The simplest model is then to only fit for stochastic and noise components while not fitting for a linear trend component. This model can be applied to all pulsars. Because the periodic component was not found to be highly covariant with the stochastic component, the periodic amplitudes were fitted as well and compared to the values from the trend analysis. In order to constrain a linear trend, we would need some prior information on the shape of the stochastic component in the time series relative to the true linear component that we do not have at this time.

Diffractive timescales, listed in Table 2.3, were calculated by creating a 2dimensional dynamic spectrum of each 1500-MHz observation in the data set and computing the 2D autocorrelation function of each spectrum, which in turn is summed over time and frequency separately. A Gaussian function is fitted to the 1D frequency-summed autocorrelation function, and the scintillation timescale is

PSR	$\nu_{\rm obs}$	$\Delta \tau_{\rm D}$	Source	β	σ_n	A
	(MHz)	(\min)		1	$(10^{-4} \text{ pc cm}^{-3})$	$(10^{-4} \text{ pc cm}^{-3})$
J0030+0451	436	167.7	1	3.6(1.3)	1.6(1)	0.9(4)
J0613-0200	1400	75	2	3.87(3)	0.4(1)	1.5(2)
J1024-0719	1400	69.7	2	3.97(1)	1.6(5)	
J1455–3330	436	17.7	3	3.80(5)	3.8(4)	
J1600-3053	1400	4.5	2	3.51(1)	1.43(3)	
	1373	4.7	4			
J1614 - 2230	1400	12.5		3.6(1)	2.0(4)	3.4(8)
	1500	8.1				
J1643 - 1224	1400	9.7	2	3.85(2)	2.2(6)	8.9(7)
J1713 + 0747	1400	47.6	2	3.56(4)	0.52(8)	0.7(2)
	430	14	4			
	436	28	4			
J1744 - 1134	1400	34.5	2	3.56(4)	1.01(9)	0.5(4)
	436	21	4			
	660	20	4			
B1855 + 09	1500	20.3		3.90(3)	0.93(7)	
	1500	24.4	2			
J1909–3744	1300	30.6		3.72(1)	0.37(2)	0.63(7)
	1400	37.6	2			
B1937 + 21	1500	4.0		3.59(1)	0.7(2)	3.2(3)
	1500	7.4				
	320	1.1	4			
	430	1.7	4			
	1400	7.4	4			
	1400	5.5	2			
J1944 + 0907	1500	2.0		3.64(1)	1.7(2)	
J2145 - 0750	1400	56.6	2	3.75(7)	2.9(2)	—
	327	6.4	4			
	436	21 - 25	4			
J2317+1439	436	13.5	3	3.94(1)	0.59(4)	0.5(2)

Table 2.3 Diffractive timescales for 18 MSPs

Notes. Diffractive timescales obtained from the PPTA and NANOGrav datasets. Values with no reference were calculated from the 9-year data set. The first value listed for each MSP is the value used in calculating the structure function. The values β , σ_n , and A are produced by fitting the SF and correspond to the stochastic power law exponent, the white noise component, and the periodic amplitude component respectively. Values in parentheses show the uncertainty in the last digit.

¹Nicastro et al. (2001), ²Keith et al. (2013), ³Johnston et al. (1998), ⁴You et al. (2007)

defined as the half-width at e^{-1} . This is following the same procedure as described in Levin et al. (2016).

Most observations in the 9-year data set are around 30 minutes long, and for many pulsars, the scintillation timescale is much longer than this integration time. Therefore, it was only possible to measure diffractive timescales in this way for a few of the pulsars in the sample.

Lag bins are equally spaced in log space. Errors on the SF were calculated by combining the propagated errors from the DM time series values and the errors due to uncertainty in the specific realizations in a stochastic process. To constrain those errors, we used simulations of different spectral slopes and different timespans of data, the standard deviation of the SF was calculated for 10^4 realizations at every time lag τ . This was saved as a 3D grid of values (timespan, β , τ) and then a function was used to interpolate over that grid to give the realization error of the SF value at each τ . We held β constant to the value for a Kolmogorov medium as varying the slope had a negligible effect on the derived errors.

2.6 Results

2.6.1 Linear trends and annual periodicities

Of the 37 MSPs in the data release, 32 show the presence of DM trends, of which five MSPs show piecewise trends over different time spans. With the least squares fitting procedure, we find periods roughly consistent with an annual periodicity \pm 54 days for 17 pulsars; seven of these periods were also detected by the

PSR	l	b	v_E	v_p
			$\rm km~s^{-1}$	$\rm km~s^{-1}$
J1012+5307	160.35°	50.86°	-6.1(3)	38(8)
J1024-0719	251.70°	40.52°	-15.8(8)	205(30)
J1738 + 0333	27.72°	17.74°	16.8(8)	-25(16)
J1903+0327	37.34°	-1.01°	16.0(8)	58(3)

Table 2.4 Positions and Corrected Velocities For Three MSPs

Notes. Columns are Galactic longitude and latitude of the pulsar, the LOS component of the solar velocity, and the corrected velocity of the pulsar with respect to its local medium. Galactic coordinates were taken from the ATNF Pulsar Catalogue (Manchester et al., 2005, http://www.atnf.csiro.au/people/pulsar/psrcat/).



Figure 2.14 Lomb-Scargle periodogram for PSR J0645+5158, shown with frequency (left) as well as period (right). The highest peak occurs at a period of \sim 200 days with a false alarm probability of 0.54%, with a secondary peak at an approximately annual period with \sim 30% FAP.

periodogram. The periodogram found significant periods that were not consistent with annual for two pulsars (PSRs J0645+5158 and J1747-4036). A period of 199 days was found for J0645+5158; this roughly semi-annual period could be indicative of several effects in the DM time series (ionosphere, refractive effects from a clump of material along the LOS, or a solar wind event, among other possibilities; Lam et al., 2016). More investigation (and probably more data) would be needed to more definitively identify the source. The power spectrum, seen in Figure 2.14, shows a significant peak at the found period of 199 days and a secondary much less significant annual period, where the uncertainty in both of these periods is equivalent to the cadence of observations. A period of 459 days was found for J1747-4036, however there are less than two years of data for this pulsar so this periodicity may not be robust. Keith et al. (2013) predicted that annual modulations would be seen based on the spectral analyses for PSRs J1024–0719 and J1909–3744, and that they are dominated by the steep linear trend. The authors suggest that a more significant detection could occur through combining data sets. Our trend analysis did not find an annual trend in PSR J1024–0719. We did, however, calculate a period of 366 ± 5 days for PSR J1909–3744. A linear trend was found in 27 pulsars, 13 of which also exhibit annual trends. Five pulsars exhibit annual trends without a linear trend.

One possible cause of linear trends in DM(t) is an increasing or decreasing distance between the Earth and the pulsar. For four of the pulsars in the nine-year data set, LOS velocities have been measured with high precision. This allows us to solve for the free electron density around the pulsar. Matthews et al. (2016) calculated the velocity along the LOS for PSRs J1012+5307 and J1903+0327 (44.0±8.0 km/s and 42.1 \pm 2.50 km/s respectively), Kaplan et al. (2016) find a LOS velocity of 221 \pm 30 km/s for J1024–0719, and Antoniadis (2013) finds a velocity of -42 \pm 16 km/s for J1738+0333. We correct these for the Sun's motion by calculating the Suns velocity with respect to the local medium along each of the three lines of sight, given a velocity of 18.0 \pm 0.9 km/s in the direction l = 47.9° \pm 3.0° and b = 23.8° \pm 2.0° (Frisch et al., 2011). The corrected pulsar velocities are given in Table 2.4. Following Lam et al. (2016), we calculate the corresponding free electron density for each linear trend in DM as

$$\frac{d\mathrm{DM}}{dt} = n_e(\mathbf{x}_p)v_p - n_e(\mathbf{x}_E)v_E \tag{2.12}$$

where $n_e(\mathbf{x}_p)$ and $n_e(\mathbf{x}_E)$ are the free electron densities at the Earth and the pulsar and v_p and v_E are the LOS velocities of the Earth and the pulsar through their local media. We calculate $n_e=2.8\pm0.8$ cm⁻³ and $n_e=1.9\pm0.3$ cm⁻³ for PSRs J1012+5307 and J1024–0719 respectively. These are higher than the typical value for our Galaxy $(n_e \approx 0.03 \text{ cm}^{-3})$ but local environments can vary drastically, so the linear trends present could be explained by the LOS velocities and could indicate increased ionization as the pulsar is moving away from us. For comparison, Lam et al. (2016) find $n_e = 7.6 \pm 2.9$ cm⁻³ around PSR J1909–3744 following the same method. For PSR J1738+0333, we find $n_e=31\pm21$ cm⁻³ which is much higher than a typical value but with high uncertainties given the uncertainties on the pulsar velocity and dDM/dt. For PSR J1903+0327, we calculate a negative dDM/dt, which is not as expected as the pulsar is moving away from us. Using a typical n_e we would expect a decreasing linear trend of order $dDM/dt \approx -7 \times 10^{-7}$ pc cm⁻³ yr⁻¹. Therefore, the DM variations must be dominated by another effect (i.e. refractive lensing, which may also explain the quasi-periodicities seen for this pulsar; Lam et al., 2016).

Reardon et al. (2016) models the DM variations for 20 PPTA-observed MSPs, nine of which are also included in the NANOGrav 9-year data release (PSRs J0613-0200, J1024-0719, J1600-3053, J1643-1224, J1744-1134, B1855+09, J1909-3744, B1937+21, and J2145-0750). The trends assignments agree between the NANOGrav and PPTA data for PSRs 1024-0719, J1600-3053, J1643-1224, J1713+0747, B1937+21, and J2145-0750. The PPTA data did not show a linear trend for PSR J0613-0200 or periodic trends for PSRs B1855+09 and J1909-3744. Discrepancies could arise due to the difference in data spans, trends that continue or vary after the end of the data set, variations in methods of DM fitting, as well as differences in the trend fitting algorithm; we fit for the period whereas it is fixed at one year by Reardon et al. (2016). There is also the possibility that the DM measured for observed epochs do not agree between the sites due to the difference in observing frequencies used and spatial location; the two data sets may essentially be sampling a different ISM due to multi-path scattering (Cordes et al., 2016).

Lentati et al. (2016) apply a Fourier-based method of DM estimation (see also Lena et al. (2014)) that allows for robust correction of DM variations during epochs without multi-frequency data in the International Pulsar Timing Array (IPTA) data release (Verbiest et al., 2016). The DM noise model used by Lentati et al. (2016) assumes the power spectrum of the variations is in the form of a frequency-dependent power law. It also includes a term that provides power at a one year period; any periodicity found would be in addition to that already included in the model. Lentati

PSR	σ	$\mathrm{DM}_{\mathrm{peak}}/\sigma$	θ
	$(10^{-3} \text{ pc cm}^{-3})$		
J0023+0923	0.53	1.2	6.3°
J0030 + 0451	0.12	44.4	1.5°
J1614 - 2230	0.22	4.3	6.8°
J2010–1323	0.18	4.2	6.5°

Table 2.5 Significance of DM peaks for MSPs within 10° of the ecliptic

Notes. Columns are the rms σ of DM measurements with a Sun-pulsar angle greater than 30°, the ratio of the highest DM value in the data set over the rms, and the minimal angle θ between the Sun and the pulsar. The rms was calculated only using DM measurements with $\theta > 30^{\circ}$ to avoid contamination from the peak DM value. The solar angle corresponds to the minimal angle seen between the pulsar and the Sun in the 9-year data.

et al. (2016) do not find significant annual components in the data set, however this is not surprising as this effect is already being taken into account.

Lentati et al. (2017) find a covariance between temporal variations in scattering and DM. By analyzing PSR J1643–1224, identified here and in the literature as showing periodic variations in DM, Lentati et al. (2017) show that not accounting for high variability in scattering over time where low-frequency (below 1 GHz) measurements are used to determine DM(t) introduces periodic structure in the DM time series. Fixing scattering timescales can also result in an underestimation of the uncertainties on DM(t). This effect is a possible cause of periodic variations in PSR J1643–1224 if the scattering is also variable on roughly annual timescales (Levin et al. (2016) were unable to measure scattering timescale variations for PSR J1643–1224).

The DM is highly anti-correlated with the solar elongation angle for PSRs J0030+0451 and J1614-2230, as can be seen in Table 2.5. There is a moderate correlation in PSRs J0023+0923 and J2010-1323. It is worth noting that in Figure

2.4.3, the DM measured for the second lowest solar elongation angle is higher than that for the minimum angle; this could be due to a random solar outflow that was not present during subsequent passes near the Sun. Comparison to an inverse square density model for the solar wind is difficult here as the model is an average and hence does not include solar events. The effects of the solar wind are clear in the pulsars with apparent anti-correlation between the peak DM and solar elongation angle. However, because the solar wind can vary stochastically, the overall model may not represent the data fully.

The DM varies by one error bar over a timescale between one month and one year (30 days $< \delta t < 365$ days) for 18 MSPs. An additional 10 MSPs had a δt approximate to or smaller than the cadence of our observations (~one month). Only four MSPs showed no DM variations beyond measurement error on timescales less than one year, with no measurement calculable for five MSPs due to the absence of a predictable trend to use as a model. This illustrates how quickly the DM can vary by a significant amount and the necessity of observing at ~week cadences and fitting for DM at every epoch.

The DM trajectory maps (Figures 2.8 through 2.11) are useful in visualizing various ISM features that the pulsar is encountering. A gradient in DM that is in the same direction as the pulsar's motion, as with PSRs J1024–0719 and J1643–1224 for example, could be indicative of an increasing or decreasing distance between Earth and the pulsar or of the pulsar moving through a density gradient. A gradient across the trajectory that is not in line with the pulsar's motion, as with PSRs J0613–0200 and J1614–2230, cannot arise solely from a change in distance. This coincides

with the presence of systematic variations; pulsars with linear trends presenting as gradients along the direction of motion and periodic variations due to an overdensity that the pulsar repeatedly probes as it passes through the same LOS annually. Using PSR J0613–0200 as an example, assuming there is a 2D gradient in DM crossing the LOS in front of the pulsar, we find that the gradient has an amplitude of $dDM/d\tilde{x} \approx 2.6 \times 10^{-4}$ pc cm⁻³ AU⁻¹ roughly perpendicular to the direction of motion on the sky.

2.6.2 Structure functions

We have computed SFs for MSPs whose diffractive timescales could be calculated or obtained from the literature, seen in Table 2.3. SFs (see Figures 2.12 and 2.13) could be calculated for 15 of 37 MSPs in the data release. Three MSPs (PSRs J1832–0836, B1953+29, and J2017+0603) whose diffractive timescales were available were omitted because there was fewer than two years of continuous DM measurements. Fit power spectral values can also be seen in Table 2.3. PSRs J0030+0451 and J2145–0750 show fairly flat SFs, which is most likely a result of a white noise dominated data set. Keith et al. (2013) show a SF for J2145–0750 exhibiting similar structure at shorter time lags, but the error bars are too large to allow a detailed comparison.

For J1600–3053, Keith et al. (2013) measure a Kolmogorov SF; You et al. (2007) mention it as being quadratic at shorter time lags becoming less steep at higher lags. Our analysis shows apparent white noise domination for time lags
below ~ 100 days, beyond which the SF is bit more shallow than Kolmogorov for the majority of time lags.

PSRs J0613–0200, J1024–0719, J1643–1224, B1855+09, and J2317+1439 show nearly quadratic power spectra. Our calculated SF for J0613–0200 agrees with You et al. (2007). The SF for J1643–1224 resembles that in Keith et al. (2013). You et al. (2007) show a power law exponent between the expected values for a quadratic and Kolmogorov medium at shorter time lags, with the SF exhibiting a power spectrum below Kolomogorov at higher lags. Our analysis shows a nearly quadratic power law with a distinct turnover present at a time lag of one year before climbing again at higher lags. This could be indicative of an underlying Kolmogorov medium.

You et al. (2007) do not calculate a SF for J1744–1134, but predict it would be Kolmogorov based on previous dDM/dt measurements. Our calculation compares well to Keith et al. (2013), starting out dominated by white noise then ends roughly Kolmogorov at higher lags. Our analysis finds a power spectrum below Kolmogorov.

PSRs J1614–2230, J2145–0750, J1909–3744, and J1944+0907 are roughly Kolmogorov. PSR J1909–3744 compares well to the calculation in Lam et al. (2016). PSRs J1600–3053, J1713+0747, J1744–1134, and B1937+21 have power-law indices lower than expected for a Kolmogorov medium. PSR J0030+0451 has too large an uncertainty on β for a definitive comparison.

The periods found by the SF fitting analysis agree within errors with those found by the DM time series trend analysis for all pulsars except one. A periodic trend was detected in the DM time series PSR B1855+09, but was not found by the SF analysis. Here we discuss specific pulsars of interest.

2.6.2.1 PSR J1713+0747

You et al. (2007) show the SF for J1713+0747 as being less steep than a quadratic power law at higher time lags, as does Keith et al. (2013). The SF calculated here looks almost white noise dominated; removing the DM event occurring around MJD 54750 (2008–2009) and re-calculating the SF still yields what looks like a white noise dominated spectrum. We do not believe this is purely white noise because of the correlated structure we see in the time series. However, if that power is evenly distributed over the range of time lags we are concerned with then the SF will appear constant with lag.

Given the time of the observation immediately before the sharp decrease in DM on MJD 54751 and the epoch at which the DM is once again within 1σ of the average value, we find an upper limit for the DM event of ~200 days; using the transverse velocity and distance from Table 2.1 and assuming the structure responsible is located at the pulsar gives an upper limit size to the dispersing region of 4.0 ± 0.1 AU. With the increased amount of data in the IPTA data set, Lentati et al. (2016) are able to sample the DM event more effectively. They identify the DM event as spanning ~100 days, with the minimum DM occurring at ~MJD 54757.

2.6.2.2 PSR B1855+09

PSR B1855+09 shows a linear SF that does not align with the Kolmogorov or quadratic trendlines when using the diffractive timescale listed in Table 2.3. This could be due to an incorrect or varying diffractive timescale; adding the diffractive timescale as another fitted parameter when fitting the SF gives a value of $\Delta \tau_D =$ 55 ± 1 minutes, which is more than double the calculated values. The resulting SF is nearly quadratic with some white noise dominating at small time lags.

2.6.2.3 PSR B1937+21

There is an extensive history of SF analysis for B1937+21. Kaspi et al. (1994) found a power law exponent of β =3.874±0.011 with a little more than 8 years of data. Cordes et al. (1990) found a similar β value that falls between a Kolmogorov and quadratic power spectrum, which agrees with our data at lower lags. Ramachandran et al. (2006) finds a lower value of β =3.66±0.04 (compared to our 3.59±0.01) from 1983 to 2004 that is consistent with a Kolmogorov medium. As with previous studies, Keith et al. (2013) also shows a steady decrease in the DM through the end of 2010, and show a similar Kolmogorov-consistent SF. However, in 2011 the DM started to continuously increase through 2013, which is not a date range that any of the previously calculated SFs covered. It is likely that this latest increase in DM is the reason for the dip at higher lags that are not present in previous data sets.

2.7 Discussion

We examined a large set of DM timeseries from the NANOGrav data set and found evidence on timescales as small as weeks of variations in the vast majority of them. We found evidence of linear trends and annual periodicities, in addition to evidence for discrete ISM structures and one significant non-annual periodicity. We calculated and interpreted SFs for a subset of MSPs and examined DM variations due to LOS motions. These structure functions often appear non-Kolmogorov, but we show that this can be due to the presence of trends in the data and does not necessarily indicate a non-Kolmogorov medium.

DM measurements can inform us about the free electron density along the LOS to a pulsar. In addition, trends due to the changing LOS over time aid in investigating structure in the ISM. Linear trends may be caused by parallel or transverse motion when the free electron density may be changing to a higher or lower than average density in a region. Lam et al. (2016) show that DM variations due to a changing distance between Earth and the pulsar is dominated by parallel motion and that the transverse motion is negligible, entering only as a second order consideration. The free electron density along a particular LOS is typically assumed to be temporally invariant. Examining the scintillation parameters and flux densities of MSPs exhibiting linear DM trends can inform if this is an accurate assumption for that particular LOS. Looking at the LOS velocities for four pulsars, we expect that three of them (PSRs J1012+5307, J1024-0719, and J1738+0333) are consistent with exhibiting linear trends due to the pulsar's increasing distance. The DM

variation amplitude is much larger than expected given the average Galactic free electron density, indicating that the pulsars may be in overdense regions or ionize the materials along their paths (Chatterjee & Cordes, 2004). The velocity and direction of motion of PSR J1903+0327 suggest that its increasing distance from the Earth cannot explain its trend. Annual variations may be due to a variety of solar effects and their amplitude is influenced by the relative velocity of the MSP when compared to the Earth's orbital motion as well as the Sun's velocity as it moves through the Galaxy. We see specific cases where the solar wind is the dominant factor in producing annual variations. For others, variations could be due to a cloud or gradient along the LOS. Scintillation parameters and fluxes could indicate whether variations were due to clumps, refraction, scattering variability, or local increases in electron density (such as solar wind) (Stinebring & Condon, 1990; Clegg et al., 1998; Stinebring et al., 2000; Lentati et al., 2017). Future work may result in some determination, particularly if scintillation parameters over time are available and incorporated.

The relationship between linear and periodic variations and the direction of a gradient along the LOS can also be seen visualized by DM trajectory maps. Five MSPs show only annual trends and 14 show only linear trends, while 13 exhibit both trends. More than half of the MSPs showed significant DM variation beyond our measurement error over the timescale of one month to one year. There are 10 MSPs with timescales less than 31 days, which is on par with the average cadence of our observations. Of those, four MSPs have timescales of 14 days or less, which is the size of the fitting window used for DMX in the 9-year data release. It is therefore

imperative that we fit for DM at every epoch due to the scale of the variations over these timescales, as well as observe as often as possible to minimize the time between DM measurements due to the rapid variation seen in some MSPs.

For three PSRs, the SFs appear to be dominated by white noise, resulting in a flat power spectrum. Three MSPs have very nearly quadratic power spectra, with two (PSRs J1024–0719 and J2317+1439) having a β value within 1% of quadratic. Lam et al. (2016) suggest discrete structures in the ISM as well as the changing distance will contaminate the SF resulting in a quadratic power spectrum. This steeper than Kolmogorov value could be indicative that the time lag is smaller than the crossing time for the structure probed during the time series. Higher values than consistent with a Kolmogorov medium could be attributed to present trends or systematic variations in addition to a Kolmogorov medium, particularly with the previously discussed difficulties in disentangling a linear trend component from a stochastic one. We cannot impose priors without assuming something about the contributions from the ISM that we are trying to constrain, and which may not actually be the case. There are also more possible sources of error in the calculation of the β values than we have included. We have accounted for the random and stochastic uncertainties but not systematic uncertainties, which can result from variability of white noise statistics over time from changing backends, the variation in the diffractive timescale, and the fact that the models used here could be incomplete in describing the ISM. Therefore, while the β values presented here are illustrative, their errors bars are likely under-estimated. In addition, care should be taken when using these values to make inferences about the ISM due to possible covariances and systematics present.

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Chapter 3

Investigating the Candidate Displaced Active Galactic Nucleus in NGC 3115

3.1 Abstract

The nearby galaxy NGC 3115 contains a known radio-emitting, low-luminosity active galactic nucleus (AGN), and was recently claimed to host a candidate AGN displaced 14.3 pc from the galaxy's optical photocenter. Our goal is to understand whether this represents a single offset AGN, an AGN in orbit around a central black hole, or something else. We present a new, sensitive (RMS = $4.5 \,\mu$ Jy beam⁻¹) 10 GHz image, which finds evidence for only one AGN. We place a stringent limit on the radio luminosity of any secondary supermassive black hole of $L_{10\,GHz} < 5.6 \times 10^{33}$ ergs/s. An analysis of the relative positioning of the radio core, X-ray nucleus, and stellar bulge in this galaxy indicate that the radio source is centrally located, and not offset from the galactic bulge. This provides an argument against a single offset AGN in NGC 3115, however does not provide conclusive evidence against the purported offset AGN as an in-spiralling secondary black hole.

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3.2 Introduction

Supermassive black hole (SMBH) binaries should form during major galaxy mergers. Through the loss of orbital energy, the SMBH pair will eventually coalesce, releasing an enormous of amount of energy in the form of gravitational waves. Gravitational waves produced by SMBH mergers would be detectable by pulsar timing arrays (e.g. Arzoumanian et al., 2018b). Asymmetric gravitational wave emission can produce a strong force—or "kick"—to the final SMBH. If this kick is smaller than the host escape velocity, it can induce oscillation of the SMBH about the galaxy's core (kick velocities can be up to several thousand km/s, causing the SMBH to be ejected from the galaxy; Blecha et al., 2013). The SMBH should eventually settle into the host galaxy's center due to drag and other dynamical interactions with the stellar and gas environment (e.g. Begelman et al., 1980; Campanelli et al., 2007). While recoiling SMBHs may return to the center after several Gyr, SMBH recoils in gas-poor galaxy mergers can remain non-centrally located for much longer periods of time (Blecha et al., 2013).

SMBH recoils induced by these kicks have astrophysical implications for the host galaxy, such as SMBH and galaxy evolution, galactic core structures, galaxy-SMBH scaling relations, and the dependence of gravitational wave signals on redshift, among others (Komossa, 2012). The identification of potential recoiling SMBHs is therefore important in exploring past galaxy mergers, information on kick properties, as well as investigating predictions made via numerical relativity.

There are not many small-orbit binary SMBH systems known, with only a

few examples below separations of 1 kpc (e.g. Rodriguez et al., 2006). There have likewise been scant discoveries of post-merger systems where the SMBH is seen in a state of offset/recoil, with only a few unconfirmed candidate systems (Komossa et al., 2008; Postman et al., 2012; Blecha et al., 2013; Lena et al., 2014; Chiaberge et al., 2017). To achieve sufficient AGN offsets such that the object is identifiable as an offset system, a large kick velocity is necessary. High kick velocities, while possible, are likely to cause stripping of much of the emissive material from the SMBH after its departure from the galactic center; therefore bright AGN with large offsets are likely to be rare.

At a distance of 10.2 Mpc, NGC 3115 is the nearest host of a billion-solarmass black hole, and represents one of the first SMBHs with an accurate mass measurement based on stellar or gas dynamics ($M_{BH} = 9.6 \times 10^8 M_{\odot}$) (Kormendy & Richstone, 1992; Gültekin et al., 2009). At the object's distance 1" = 49.5 pc, making the task of spatially resolving any offset more feasible than for more distant sources. Compact radio emission with a luminosity of 3.1×10^{35} ergs/s that is coincident with the optical center in the nucleus of NGC 3115 was first detected by Wrobel & Nyland (2012) by analyzing archival VLA data, with an Eddington luminosity of $L_{Edd} = 1.2 \times 10^{47}$ ergs/s. This detection is also coincident with an Xray candidate nucleus identified by Wong et al. (2011), who conservatively estimate the luminosity as $L_X < 4.3 \times 10^{38}$ ergs/s. These data suggest the existence of a low-luminosity active galactic nucleus (AGN) residing in the center of this galaxy.

Using the Gemini-South telescope, Menezes et al. (2014) reported the detection of a broad-line H α emission with a luminosity of $L_{H\alpha} = 4.2 \pm 0.4 \times 10^{37}$ ergs s^{-1} that was displaced from the photometric center of NGC 3115's stellar bulge by 290 ± 50 mas (14.3 ± 2.5 pc). Upon inspecting several possibilities including a rotating relativistic disk around the central black hole and imprecise starlight subtraction, they concluded that the emission is most likely associated with an offset AGN. If this detection genuinely represents an offset AGN, there are two potential interpretations. First, it is possible the black hole fueling the offset AGN is actually in a pc-scale binary with a second black hole situated at the photocenter. Alternately, the AGN displacement could be the result of a black hole that has been kicked from the galaxy photocenter via recoil.

In this paper we present a radio search for evidence of a binary or offset AGN in NGC 3115. Section 4.3 reports new 10 GHz data collected with National Science Foundation's Karl G. Jansky Very Large Array (VLA), Section 3.4 discusses the new radio measurements in the context of our detection of only one radio core, and reports a closer examination of the relative positions and astrometric errors of several different measurements of the AGN and galaxy center. We discuss the implication of these results in Section 3.5.

3.3 Very Large Array Data

We observed NGC 3115 with the VLA at X-band in the A-configuration on 12 June 2015, with 84 minutes on-target. The observational set-up had 64 frequency channels in each of 32 unique spectral windows, across the range 7.976 GHz to 12.024 GHz with a center frequency of \sim 10 GHz. The target pointing position was 10:05:13.927, -07:43:06.96. We performed primary flux density and bandpass calibration using standard VLA calibrator 3C286, and used J1007-0207 as a phase calibrator.

We calibrated the data using the VLA calibration pipeline, and interactively deconvolved the images using the CLEAN algorithm in the CASA software package. The RMS of our final image is 4.5 μ Jy beam⁻¹. The synthesized beam had major and minor axes of 340 mas and 150 mas respectively, with a position angle of 38.34°. Multi-frequency synthesis was performed to account for the large fractional bandwidth with nterms=1. We used briggs weighting with a robust value of 0.0 and a minpb of 0.2. The cellsize was set to 36 mas.

We also made a wide-field image to look for other objects in the field unrelated to this work following the same procedure discussed above; this wide-field image was not used in our analyses but was used to make Figure 3.2, hence the different beam sizes listed for Figures 3.1 and 3.2.

3.4 Analysis of Available Data

3.4.1 10 GHz Measurement Results

Our new radio image improved on the RMS sensitivity of our previous image by a factor of ~ 5 . Figure 3.1 shows a compact source located in the center of NGC 3115 down to our detection limit of three times the RMS. The IMFIT procedure in CASA was used to fit a two-dimensional elliptical-Gaussian to this sole source, yielding the integrated flux density, position, and one-dimensional position error appearing in



Figure 3.1 Contours of the 10-GHz emission from NGC 3115 at -3, 3, 6, 12, and 24 times the RMS level in the image detected with the VLA. The beam is displayed in the bottom left corner, with major and minor axes of 340 mas and 150 mas respectively and a position angle of 38.34° . The noise level is $4.5 \,\mu$ Jy beam⁻¹. The relative positioning of the kinematic center (labelled "B") and the purported offset AGN (labelled "A") of Menezes et al. (2014) are represented by the purple and red crosses, respectively. Note that these are not absolute positions; they are displayed here to demonstrate that we should have been sensitive to two AGN if both were radio-emitting at the relative separation reported by Menezes et al. (2014). The error bars on these two points represent the reported positional error for the bulge, and the AGN offset error for the AGN.

Table 1. The tabulated position errors are reported as the radius of the error circle at the 95% confidence level. The flux density error is the quadratic sum of the 3% scale error (Perley & Butler, 2013) and the fit residual. The position error is the quadratic sum of terms due to the phase-calibrator position error (less than 2 mas), the phase-referencing strategies (estimated to be 100 mas), and the signal-to-noise ratio of the component (4 mas). The source was found to be point-like, with upper limits of 200 mas (9.9 pc) on its major axis and 60 mas (3.0 pc) on its minor axis, for a position angle of 39.3 ± 2.2 degrees.

We detected two additional 10-GHz sources, each offset by more than 1.5' from the nuclear 10-GHz source and thus unlikely to be associated with it. As an independent cross-check of the VLA position error for the nuclear 10-GHz source (Table 1), we searched the literature for counterparts to the two offset sources. Only one had any counterparts. Figure 3 shows that offset 10-GHz source plus the positions of its X-ray and *ugi* counterparts (Lin et al., 2015; Cantiello et al., 2015, 2018), and serves to validate the VLA astrometry.

Using previous radio data as listed in Table 3.1 along with the data presented here, for the NGC 3115 nuclear source we measure a spectral index of $\alpha = -0.34 \pm$ 0.09. This is consistent with the index measured by Wrobel & Nyland (2012) of $\alpha = -0.23 \pm 0.20$ (Fig. 3.3). The relatively flat spectral index of the emission indicates that this emission is likely related to a radio core component, i.e. marks the location of a SMBH rather than marking a distant jet outflow. The flat spectrum and persistence of the source show that it is likely in a low-hard or quiescent state, consistent with the SMBH accreting slowly from the hot gas traced by the X-rays.



Figure 3.2 VLA image of Stokes I emission near 10 GHz centered on a background source with an X-ray counterpart (Lin et al., 2015) and an *ugi* counterpart (Cantiello et al., 2015, 2018). The symbols encode the counterpart positions and their errors at the 95% confidence level. For the 10-GHz image, the local rms noise is 11.4 μ Jy beam⁻¹ (1 σ) and the beam dimensions at FWHM are 382 mas times 173 mas with a position angle of 40° (hatched ellipse). The allowed contours are at 1 σ times -6, -4, -2, 2, 4, 6, 8, 10, 12, 14, 16, 18, and 20. Negative contours are dashed and positive ones are solid.

	Positio	n, J2000	Positional	Peak Flux Density	Int. Flux Density	Ref.
Measurement	\mathbf{RA}	\mathbf{Dec}	Uncertainty (mas)	$(\mu \mathbf{J} \mathbf{y} \mathbf{b} \mathbf{e} \mathbf{a} \mathbf{m}^{-1})$	$(\mu \mathbf{J} \mathbf{y})$	
2MASS	10:05:13.93	-07:43:07.1	170			
$10~{ m GHz}$	10:05:13.9285	$-07{:}43{:}06{.}995$	202	185 ± 4	204 ± 9	2
$8.5~{ m GHz}$	10:05:13.927	$-07{:}43{:}06{.}96$	202		290 ± 30	က
$1.4~{ m GHz}$	10:05:14.03	$-07{:}43{:}07{.}6$	1050	400 ± 200		4
X-ray	10:05:13.93	$-07{:}43{:}07{.}0$	590			ŋ
M14 AGN	10:05:13.817	-07:43:07.87				9
M14 Bulge	10:05:13.800	$-07{:}43{:}08{.}00$				9

Other Frequencies
at
Sources a
of
Comparison
Position
ц С
Astrometric
Ļ
Table 3.

ne error on our position measurement. The Chandra X-ray and Menezes et al. (2014) reference ties were obtained from comparing Chandra and Gemini data to data from SDSS (Margutti et al., 2012). As the AGN found in Menezes et al. (2014) is measured to a position relative to the stellar kinematic center, we adopt the uncertainty on that measurement as the uncertainty in the position. **References.** (1) NED/2MASS; (2) this work; (3) Wrobel & Nyland (2012); (4) White et al. (1997); (5) Evans et al. (2010); (6) Menezes

et al. (2014).

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Figure 3.3 Flux density with frequency. Magenta circles represent data at 1.5 and 8.5 GHz from White et al. (1997) and Wrobel & Nyland (2012), respectively, while the cyan squares signify data from this work, measuring the flux density after splitting the data into two sub-bands centered on 9 and 11 GHz.

The integrated flux measured in our new broadband VLA data from 8-12 GHz is consistent with that from archival VLA observations at 8.5 GHz (Table 3.1); thus, in the absence of strong variability, there is no evidence for significant deviation from a single power-law in this radio component (i.e. we are not clearly observing a self-absorption turn-over, nor do we seem to be seeing two distinct regions with vastly different properties within our beam).

It is clear that we have not detected any radio source related to NGC 3115 except for the one previously reported by Wrobel & Nyland (2012). We initially set out to test the report of Menezes et al. that there was an active nucleus offset from the kinematic and photometric center of NGC 3115. As hypothesized in their paper, this could mean they either detected a single offset black hole, or an inspiralling black hole offset from another at the galaxy center, or that there is simply a single black hole at the galaxy center and the offset emission detected by Menezes et al. is caused by, for instance, an outflow. However, several questions remain in the investigation of our initial hypotheses: First, *should* we have detected a secondary black hole, given the detection of the first one? Second, can we determine whether this object corresponds to the galaxy photocenter or to the purported offset AGN of Menezes et al. (2014)? Third, might the central radio source actually encompass two SMBHs? The first question we address here, and the latter two require a discussion of the relative astrometry of measurements in other wavebands; this is discussed in Section 3.4.3.

3.4.2 Would we have detected a distinct SMBH companion?

The radio nucleus in this system has a low luminosity of $L_{10\text{GHz}} = 8 \times 10^{34}$ ergs/s. In considering the hypothesis that this target could contain a binary SMBH, we want to assess the probability that we should have detected a secondary SMBH in our observation given our limiting flux of three times the RMS of the off-source image, $S_{\text{lim}} = 13.2 \ \mu\text{Jy}$ beam⁻¹. At the distance of NGC 3115 this corresponds to a limiting luminosity of $L_{\text{lim}} = 5.6 \times 10^{33}$ ergs/s. Due to the excellent VLA sensitivity and the small distance of this source, our limit on the luminosity of any secondary AGN is exceptionally low; in fact it lies several order of magnitudes below the span

of published radio-quiet quasar distributions. If there is a companion, we would classify any secondary SMBH in this system as "radio-silent" (Padovani et al., 2015; Padovani, 2016).

Past work has assessed the probability of finding a secondary AGN by integrating over radio luminosity functions down the limiting luminosity in an observation (e. g. Burke-Spolaor, 2011). If this target had a radio-loud or even radio-quiet secondary SMBH by the standard definitions, we should have detected it. It is possible that a secondary SMBH is not in an active state at all, in which case no waveband would have detected its emission. Lützgendorf et al. (2016) discuss gas patchiness as a result of stellar winds; the presence of a second SMBH accreting rapidly from a gas patch is also possible, which would show up as a broad-line AGN and only rarely exhibit radio emission.

3.4.3 Multi-wavelength astrometry

Understanding the relative positions of the radio and X-ray emission, the purported offset AGN of Menezes et al. (2014), and the galaxy kinematic center and/or photocenter is key to our interpretation of this object. The study of Menezes et al. (2014) benefited from precise position comparisons due to analysis of relative positioning within a single observation, while our study is by nature limited by astrometric and measurement errors. We will both examine astrometric errors, and re-examine the results of Menezes et al.

While NGC 3115 is a well-studied object, there are relatively few works re-



Figure 3.4 The relative positions of the data listed in Table 3.1, with our 10 GHz radio image shown in greyscale. The circle sizes represent the quadrature sum of the astrometric and measurement errors for each data point. The data are as follows: 2μ m 2MASS centroid (green); X-ray core (blue); our radio position (yellow). The kinematic center measured by Menezes et al. (2014) is shown in purple (Menezes, private comm.). Their reported offset AGN is shown in red, and is positioned in reference to the purple circle's position.

porting on the actual position of the galaxy's kinematic center. Here we assess the optical photocenter, the X-ray component, and the radio component to understand what confidence we can have in their relative positioning. Unfortunately, there were insufficient numbers of objects detected both in our image and the X-ray/2MASS data to do a direct astrometric comparison. Instead, the reference tie and measurement errors reported by source publications for each observation are identified in Table 3.1.

The 8.5 GHz observations were also performed with the VLA with the same frame tie accuracy (Wrobel & Nyland, 2012), while the 1.4 GHz measurement comes from the FIRST survey, which reports a mean astrometric precision of 50 mas (White et al., 1997). The 2μ m photocenter position for NGC 3115 was taken from 2MASS. The 2MASS survey is tied to the Tycho 2 catalog, which is accurate to $\sim 70 \text{ mas}$ (Cutri et al., 2003). The position and error listed is that for the NGC 3115 photocenter from the 2MASS point source catalog (Skrutskie et al., 2006). The Chandra X-ray nuclear component was obtained from the *Chandra* Source Catalog (Evans et al., 2010). The localization of any potential AGN-related nucleus is limited by the fact that there is no nuclear point source, only a plateau of X-ray emission in the core of this galaxy (Wong et al., 2011). The X-ray reference tie is as quoted by (Evans et al., 2010) for the 1σ external astrometric error. While the absolute astrometry of Gemini (used by Menezes et al. 2014) is about as accurate as that of *Chandra*, the astrometrically corrected position information was not reported by Menezes et al. (2014). The AGN and bulge reported by Menezes et al. (2014) are relative positions in the frame of their observation, thus we do not show these errors

in Fig. 3.4.

Menezes et al. (2014) fit the 2D kinematic profiles of the data in order to obtain a position measurement for the offset broad H α emission line that indicates the presence of an AGN. They compare this position to the kinematic center of the galaxy (as determined by the velocity dispersions in that region) as well as the stellar bulge center (they equate the image of their collapsed data cube as representing the center of the stellar bulge) and determine that the AGN is coincident with neither the kinematic nor stellar bulge centers of NGC 3115.

In their analysis, Menezes et al. identified an offset of $\sim 290\pm50$ mas ($\sim 14.3\pm2.5$ pc), with the uncertainties determined using a Monte Carlo simulation. They determine that the kinematic center is coincident with the stellar bulge center, however do not report an absolute position of either the kinematic center, bulge center, or offset AGN. Based on observation headers that are not likely astrometrically corrected, the Gemini pointing center (directed at the stellar bulge center) was at a position of J2000 RA, Dec 10:05:13.80, -07:43:08.00 (R. Menezes, private comm.). The position of the off-centered AGN is reported as ~ 260 mas east and 130 mas north from the stellar bulge center, giving an uncorrected AGN position of J2000 RA, Dec 10:05:13.82, -07:43:07.87.

The relative positions and net position errors are displayed atop 2MASS contours in Figure 3.4. The AGN detected by (Menezes et al., 2014) is offset 1.84" from our detected radio source, and their position measurement of the stellar kinematic center is 2.89" from the 2MASS photocenter; thus there are clear residual absolute astrometry offsets in the observations of Menezes et al. (2014).

3.5 Discussion and Conclusions

3.5.1 Where is the radio AGN in NGC 3115?

As shown in Figure 3.4, the position of our radio AGN agrees with the stellar bulge center as indicated by 2MASS, to significantly less than the separation between the offset between the bulge and AGN measured by Menezes et al. As such, it appears that the black hole related to this radio AGN is likely resident in, and not offset from, the galaxy center. As seen in Figure 3.4, the position listed in the Menezes et al. FITS data file header do not appear to have any absolute astrometric correction applied. Regardless, if the bulge center were shifted to the 2MASS position, it is clear that the radio AGN is not colocated with the purported offset AGN.

3.5.2 Does NGC 3115 contain a binary, offset, or singular central AGN?

Based on the relatively flat spectrum of the radio AGN and its colocation with the stellar bulge, it is clear that NGC 3115 does not contain a singular offset (recoiling or wandering) AGN. It is possible that the position-offset H α line does represent a separate SMBH, in which case the offset system may still be undergoing inspiral after a previous merger. Assuming this SMBH has a mass $\geq 10^8 M_{\odot}$, the dynamical friction timescale of such an object at this separation is on the order of 100 kyr, thus relatively short but not so infeasible to have detected it at this state of inspiral (Lacey & Cole, 1993). The 2D kinematic measurements of Menezes et al. demonstrated some support for this argument, indicating that the isocontours of velocity dispersion demonstrated an elongated, elliptical shape, rather than showing a singular peak at the photometric center. However, the elongation was not along the axis of the AGN offset, suggesting some ongoing mobility of this secondary SMBH in the system under this hypothesis. There are no other large-scale indications that NGC 3115 underwent a merger in the last few Gyr. Finally, it is possible that NGC 3115 simply contains a single, centrally located low-luminosity AGN that is giving rise to the radio source and some component of the central X-ray emission. If the offset source is indeed its own AGN, it appears to have no associated radio emission.

3.6 Acknowledgments

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Chapter 4

Evaluating Low Frequency Observations at the GMRT in Combination with NANOGrav Data

4.1 Abstract

The North American Nanohertz Observatory for Gravitational Waves (NANOGrav) project has the primary goal of detecting and characterizing gravitational waves through high precision pulsar timing. The characterization of interstellar effects is important in order to achieve the precision necessary for gravitational wave detection. Ionization in the interstellar medium causes frequency-dependent time delays due to effects like dispersion and scattering. The lower frequency coverage as well as simultaneous dual-frequency observations available at the Giant Metrewave Radio Telescope (GMRT) have the potential to provide better dispersion measurement than the data taken by NANOGrav. We present GMRT timing data for 10 millisecond pulsars observed at 322 and 607 MHz, and compare the dispersion measure estimates obtained with those obtained through NANOGrav observations with the Arecibo Observatory. We analyze the predicted effect of incorporating this low

In prep

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frequency data on DM uncertainties. We discuss discrepancies between DMs and investigate possible astrophysical sources of variations in DM measurements. We discuss the possible advantages of incorporating GMRT data into timing efforts for understanding and mitigating interstellar effects as well as improving timing precision.

4.2 Introduction

There are currently three global pulsar timing array (PTA) efforts: the North American Nanohertz Observatory for Gravitational waves (Arzoumanian et al., 2018b), the European Pulsar Timing Array (EPTA; Desvignes et al., 2016), and the Parkes Pulsar Timing Array (PPTA; Reardon et al., 2016). These three experiments make up the International Pulsar Timing Array (IPTA; Verbiest et al., 2016), whose primary goal is the detection of nanohertz frequency gravitational waves (GWs) using pulsar timing. The NANOGrav 11-year data set, the most recent data release from the collaboration, includes 45 millisecond pulsars (MSPs; Arzoumanian et al., 2018b). The data set includes up to 11 years of data for each MSP taken at the Arecibo Observatory and the Green Bank Observatory at frequencies between 327 MHz and 2.3 GHz.

Timing models are constructed by accounting for all known effects on the pulsar times of arrival (TOAs) in order to minimize the differences between the measured and model predicted TOAs (i.e. timing residuals). The detection of GWs with pulsar timing requires TOA accuracy less than ~microsecond. In most

cases, time delays produced by interstellar effects surpass the MSP pulse periods and therefore must be accounted for in precision timing (e.g. Demorest et al., 2013; Arzoumanian et al., 2015).

One of these such effects is dispersion. As the radio pulse travels through the interstellar medium (ISM), it encounters ionized plasma along the way. The DM is the integrated column density of free electrons along the line of sight (LOS) to a pulsar

$$DM = \int_0^d n_e(l) dl , \qquad (4.1)$$

where n_e is the free electron density along the LOS and d is the distance. DM therefore can be used to infer the distance to the pulsar by assuming a free electron density model for the Galaxy (e.g. NE2001, Cordes & Lazio, 2002). The time delay due to dispersion scales as $t \propto DM/\nu^2$ where ν is the observing frequency; DM can be solved for by observing at multiple frequencies and comparing the respective time delays. Due to the changing LOS, DM is not constant in time (i.e. DM is actually DM(t)); these DM variations affect the timing and must be monitored and corrected for in the data. DM variations can arise for many reasons, including a changing distance between the Earth and the pulsar, varying solar wind, and ionospheric effects. DM variations can also exhibit structure in the form of periodicities and trends.

Trends due to the time-variant LOS are useful in investigating structure in the ISM. Linear trends may be caused by parallel or transverse motion when the free electron density may be varying to higher or lower values than the average density in a region. Lam et al. (2016) show that DM variations due to a changing distance between the Earth and the pulsar is dominated by parallel motion and that the transverse motion is negligible, becoming relevant only as a second order consideration. The free electron density along a particular LOS is generally assumed to be time invariant; the examination of scintillation parameters and flux densities of MSPs that exhibit linear DM trends can inform if this assumption is accurate given a particular LOS.

Annual variations may be caused by various solar effects; their amplitude is determined by the relative velocity of the MSP in comparison to the orbital motion of the Earth as well as the solar velocity through the Galaxy. In addition to solar effects, annual variations may also be caused by a gradient along the LOS. As with linear DMs, scintillation parameters and fluxes could inform whether variations were caused by clumps, refraction, scattering variability, or local increases in electron density (e.g. solar wind) (Stinebring & Condon, 1990; Clegg et al., 1998; Stinebring et al., 2000; Lentati et al., 2017). A more thorough analysis of DM trends seen in the NANOGrav 9-year data set (Arzoumanian et al., 2015) can be seen in Jones et al. (2017).

Turbulence in the ISM which causes trends is typically described as having a Kolmogorov power spectrum, meaning we expect to find larger variations over longer timescales. The power spectrum used to describe a Kolmogorov ISM is

$$P(q) \propto q^{-\beta}, \ q_{\text{outer}} \le q \le q_{\text{inner}}$$
 (4.2)

where q is the reciprocal of the size scale, and β is the power spectrum exponent. A Kolmogorov medium corresponds to $\beta = 11/3$, while the highest value expected for turbulence in the ISM (for an inner scale shorter than 10^9 m) is $\beta = 4$ (Rickett, 1990). The outer scale is described as the size at which the ISM is no longer homogeneous whereas the inner scale is the point where dissipation occurs in the material along the line of sight.

It is difficult to distinguish between DM trends or describe the ISM as showing a specific component. As stated above, a linear trend in DM could be due to an increasing distance between the Earth and the pulsar; however, a purely stochastic medium would also present as a monotonic increase in DM(t). There is substantial evidence of contamination between the stochastic and trend components. In many cases, a linear trend fit over the DM timeseries will absorb part of the stochastic component. Knowledge of some prior about the contributions from the ISM would need to be known in order to disentangle a linear trend component from a stochastic one. The presence of DM trends or systematic variations in addition to a Kolmogorov medium will also appear as a steeper power law. Jones et al. (2017) discuss in depth the covariances between DM trends, periodicities, noise, and a stochastic medium.

A second effect is scattering. As the pulse travels through the ISM, it will be scattered due to inhomogeneities in the ISM which cause multi-path propagation of the pulse. These multiple ray paths introduce a delay in the TOA. Like DM, scattering delays are also time variable due to dynamic processes in the Galaxy. Scattering scales as ν^{-4} and is therefore much more influential at lower observing frequencies. Pulse scattering becomes particularly pertinent for MSPs at high DMs (Bhat et al., 2004). Scattering cannot be corrected as easily as DM, but can be partially corrected using high resolution dynamic spectra due to the similar phenomenological cause behind scattering and the scintillation bandwidth size (Levin et al., 2016). One method of obtaining high resolution dynamic spectra is through cyclic spectroscopy, which recovers the un-scattered pulse by deconvolving the broadened pulse with the exponential tail caused by scattering (Demorest, 2011). Palliyaguru et al. (2015) show that the timing improvement via cyclic spectroscopy is not significant for most MSPs currently observed by NANOGrav, however high resolution dynamic spectra will allow for the accurate recovery of scattering parameters.

Because of the covariances between fitting for DM and scattering, some scattering effects will be absorbed by fitting for only DM. Low-frequency observations can be used in order to disentangle the scattering contributions from the DM as it is easier to discriminate between the ν^{-2} and ν^{-4} effects at frequencies where they are more visible. As a result of the change in scattering angle for different observing frequencies, different portions of the ISM are sampled. Cordes et al. (2016) show that DM itself is frequency dependent (i.e. chromatic DM) because of this multipath scattering; using different frequencies to calculate DM results in different DM estimates. This leads to a net difference in dispersive time delays when observing at different frequencies, which in turn increases the uncertainties in DM estimation over wide bandwidths.

Simultaneous dual-frequency observations can improve the PTAs' ability to estimate DM. As discussed above, determining DM from dual frequency observations results in a non-negligible error. Errors can be further decreased by increasing the



Figure 4.1 DM affecting the pulse arrival time for different frequencies. TOAs at lower frequencies are more affected by dispersion and arrive later than TOAs at higher frequencies. Uncertainties in timing from DM from misestimation correspond to the gray region around the black DM curve. The crossover point on the curve corresponds to some fiducial frequency.

ratio of observing frequencies. Observing at widely spaced frequencies can aid in obtaining a high precision DM measurement by filling/anchoring part of the DM curve. This more precisely measured DM can then be used to calculate the corrected infinite frequency TOA t_{∞} . A sample DM curve can be seen in Figure 4.1, along with how uncertainties in DM estimation affect the infinite-frequency pulse arrival time.

The increase in precision for DM measured with widely spaced frequencies can be estimated for the data discussed here. Assuming there are no other chromatic timing perturbations, the uncertainty on the estimated DM is

$$\delta DM \equiv DM_{true} - DM_{est} = -\frac{\epsilon_1 - \epsilon_2}{K(\nu_1^{-2} - \nu_2^{-2})},$$
(4.3)

where K is the DM constant, ϵ is the measurement error on the TOA, ν_1 is the lowest observing frequency and ν_2 is the highest observing frequency (Cordes et al., 2016). Because of the low frequency coverage of the GMRT, the bottom of Equation 4.3 will be dominated by the GMRT term. For example, if our highest frequency is $\nu_2 = 2300$ MHz and we were to go from $\nu_1 = 820$ MHz to $\nu_1 = 322$ MHz, the difference between the TOA measurement errors can be ~ 4 times higher and still achieve the same difference between the DMs. If going from 1400 MHz to 322 MHz, then the ratio gets even higher — measurement error difference can be 18.9 times higher at lower frequency and still result in the same DM uncertainty. If the errors on the lower frequency data are lower than this level, the δ DM should decrease. Therefore, lower frequency data are still valuable for estimating DM even if the TOA errors are slightly higher.

Along with wider frequency coverage, having an increased number of TOAs is also beneficial for PTAs; a higher cadence of timing observations can improve the possibility of GW detection. The average S/N in the intermediate GW signal limit

$$S/N \propto N_{\rm MSP} T^{1/2} \left(\frac{c}{\sigma_{\rm RMS}^2}\right)^{3/26}$$
, (4.4)

where N_{MSP} is the number of MSPs in the data set, T is the length of the data span, σ_{RMS} is the timing RMS and c is the cadence of observations. Having more frequent observations will improve the S/N of PTA data. The TOA RMS goes down by a factor of $\sqrt{N_{obs}}$ over time for pulsars where the red noise limit has not been reached; more observations could lower the white noise for pulsars. When the white noise becomes low, the red noise becomes the limiting factor.

Frequency independent red noise, like pulsar spin noise or external influences like an asteroid belt (Shannon et al., 2013), can be modeled but cannot be corrected for in the timing. A gravitational wave signal with a period of several years appears as a low-frequency (nHz) red noise process that is independent of radio frequency. Radio frequency dependent red noise, such as from interstellar propagation effects, will appear as a systematic frequency dependent offset in TOAs if not properly corrected for. When frequency dependent red noise processes are not properly mitigated, they present partially as frequency independent processes and can be covariant with a GW signal, making GW detection more difficult. If the goal is to detect GWs using pulsar timing, then PTAs need to optimize their ability to

PSR	(Observ	ring fr	equenc	ies
			MH	Z	
J0030 + 0451		430		1400	
J1640 + 2224		430		1400	
J1713 + 0747			820	1400	2300
J1738+0333				1400	2300
B1855 + 09		430		1400	
J1909–3744			820	1400	
B1937 + 21			820	1400	2300
J2017 + 0603		430		1400	2300
J2145-0750			820	1400	
J2214 + 3000				1400	2300
J2317+1439	327	430		1400	

Table 4.1 NANOGrav Observing Frequencies

Notes. Observing frequencies for MSPs that are discussed in this paper, observed with the Arecibo and Green Bank observatories from the NANOGrav 11-year data set (Arzoumanian et al., 2018b).

characterize and model other red noise processes like DM in the data.

The Giant Metre-wave Radio Telescope (GMRT) is located 80 km north of Pune, India. The array consists of 30 45-meter stationary antennas. Using six feeds, the array can observe frequencies ranging from 150 to 1500 MHz. The GMRT has a dual feed receiver capable of executing simultaneous dual-frequency observations that can be complementary to NANOGrav observations by offering coverage at lower frequencies.

We present timing data for 10 MSPs obtained using the GMRT. There are several questions we want to answer with these data. Are the DMs measured at high and low frequencies consistent, and what constraint can we place on DMs that differ? Can this coverage at low frequency improve DM measurements, with better precision than those attained with the Arecibo Observatory? We discuss the data and acquisition system at the GMRT in Section 4.3. We examine data taken with the GMRT along with NANOGrav observations to compare DM measurements in Section 4.4. We discuss its potential for producing higher precision DMs in Section 4.5.

4.3 Data

Data were taken simultaneously centered at 322 MHz and 607 MHz with a 32 MHz bandwidth at each frequency using the phased array mode. Observations occurred at 11 epochs between February 2nd 2013 and May 12th 2014. A test pulsar B1929+10 was observed at each epoch for ~5 minutes. The GMRT Software Backend simultaneously creates both coherently and incoherently dedispersed data (Roy et al., 2010). The analysis was performed on the coherently dedispersed pulsar data. Data were split into 32 sub-bands across each band. No flux or polarization calibrations were done during these observations. The data headers also have to be inserted after the observation using a separate script as they are not encoded during the observation. Clock correction files do not exist for the GMRT, and were thus not used in the timing. Observation information is recorded in Table 4.2.

Data were folded using parfiles obtained from PSRCAT¹. Multiple gaussian fits were used for each pulsar at each frequency for the epoch producing the highest signal-to-noise (S/N) observation in order to produce a pulse template for calculating TOAs. PSRCHIVE was used for TOA generation (van Straten et al., 2012). Fitting

¹http://www.atnf.csiro.au/people/pulsar/psrcat/

MJD	J1640 + 2224	J1713 + 0747	J1738 + 0333	J2214 + 3000	J0030 + 0451	J2017 + 0603	J2317 + 1439	J2145-0750	J1909 - 3744	B1937+21
56598	30	45	30	45	45	:	:	:	:	:
56618	30	45	25	45	45	:		:	:	:
56634	30	45	30	45	30	:	:	:	:	:
56647	:	:	15	30	60	40	30	30	:	
56659	:	:	:	60	60	30	20	30	:	:
56684	30	30	:	60	60	30		30	:	:
56690	30	30	:	60	:	:	:	:	:	:
56718	30	30	:	40	15	:		:	12	:
56732	30	30	:	60	:	:		30	30	:
56769	30	30	:	40	:	60	:	30	30	10
56789	30	30		60	45	60		30	30	10

lengths	
observation	
GMRT	
4.2	
Table	
was done using the TEMPO software package², which applies a least-squares fit to the data. Errors on DM are 1σ and are determined from the timing-parameter covariance matrix after the least-squares timing model fit. Timing was performed using parameter files produced from the NANOGrav 11-year data set (Arzoumanian et al., 2018b). The NANOGrav parameter values are more sensitive than those we would obtain from fitting just the GMRT data, therefore all parameters except DM were held constant in order to obtain a DM estimate while analyzing the GMRT data.

Observation frequencies for the NANOGrav data can be seen in Table 4.1 for comparison. GMRT data could provide low frequency coverage in complement with the NANOGrav data, and fill in the gaps where data below 820 MHz does not exist in the 11-year data set.

4.4 Comparison of DM measurements

GMRT DM measurements obtained from timing can be seen in Table 4.3 alongside DMs measured from the NANOGrav 11-year data. DMs were obtained at 322 MHz, 607 MHz, and then a joint fit for both frequencies for comparison. DMs from the NANOGrav data and the dual-frequency GMRT data sets are also plotted in Figure 4.2. Even with the larger errors on the GMRT DM estimates, the values are not consistent for many epochs.

There are several reasons why DM measurements would differ between the data

sets. Non-simultaneous measurements between the different observatories could 2^{2} TEMPO software package: http://tempo.sourceforge.net

PSR		322 MF	Iz		607	MHz		322/607 N	AHz		NANOGra	av 11y	
		${ m DM}$ ${ m pc}~{ m cm}^{-3}$	$RMS \mu s$	ϵ_{TOA}	DM pc cm ⁻³	RMS μs	ϵ_{TOA}	${ m DM}$ ${ m pc}~{ m cm}^{-3}$	$RMS \mu s$	MJD	DM pc cm ⁻³	ϵ_{TOA}	Tel.
J0030+0451	56598 56618 56634 56634 56647 56684	$\begin{array}{c} 4.325(4) \\ 4.354(9) \\ 4.329(5) \\ 4.336(5) \\ 4.336(5) \\ 4.332(2) \end{array}$	153 1653 270 127 24	78 139 81 75 32	$\begin{array}{c} 4.55(4) \\ 4.92(3) \\ 4.87(3) \\ 4.01(3) \\ 4.01(3) \\ 4.336(9) \end{array}$	$ \begin{array}{r} 1212 \\ 1396 \\ 1324 \\ 1244 \\ 14 \\ 14 \end{array} $	79 73 65 79 19	$\begin{array}{c} 4.3026(5)\\ 4.2984(9)\\ 4.3261(5)\\ 4.3295(5)\\ 4.2482(2)\end{array}$	$\begin{array}{c} 812\\ 1520\\ 1020\\ 719\\ 105\end{array}$	56599 56620	$\begin{array}{c} 4.3295(3) \\ 4.32972(4) \\ \\ \end{array}$	4.5 2.7	AO AO
J1640 + 2224	56598 56618 56634 56634 56690 56690	$\begin{array}{c} 18.4288(9)\\ 18.435(2)\\ 18.4276(3)\\ 18.4276(3)\\ 18.422(1)\\ 18.524(2)\\ 18.483(2)\end{array}$	42 673 5.53 164 830 771	15 30 5.7 21 24 24	$\begin{array}{c} 17.83(1)\\ 17.93(2)\\ 18.41(1)\\ 19.02(2)\\ 17.78(2)\\ 18.63(2)\end{array}$	$\begin{array}{c} 455 \\ 629 \\ 262 \\ 783 \\ 692 \\ 1066 \end{array}$	32 38 38 42 44 44	$18.4315(2) \\ 18.4453(3) \\ 18.4288(1) \\ 18.4616(2) \\ 18.4745(2) \\ 18.4224(3) \\$	231 667 79 397 802 786	56598 56619 	$18.4619(1) \\ 18.461897(9) \\ 18.461981(7) \\$	$\begin{array}{c c} 2.0 \\ 1.7 \\ 1.3 \\ \end{array}$	AO AO AO
J1713+0747	56732 56598 56618 56634 56634 56690 56718 56718	$18.4278(3) \\16.010(3) \\15.854(6) \\15.881(5) \\15.992(5) \\15.994(5) \\15.994(5) \\15.986(1) \\15.986(1) \\$	3.38 3.77 1311 859 304 978 150 14	$\begin{array}{c} 4.7 \\ 65 \\ 77 \\ 74 \\ 87 \\ 69 \\ 20 \end{array}$	$18.41(1) \\15.99(1) \\16.231(5) \\15.09(3) \\16.51(3) \\16.14(3) \\15.92(2) \\15.977(7)$	$\begin{array}{c} 21 \\ 165 \\ 254 \\ 1200 \\ 712 \\ 1202 \\ 295 \\ 6.2 \end{array}$	27 38 68 68 83 76 34 34	$18.42866(9) \\15.9640(3) \\15.9712(5) \\15.9428(5) \\15.9594(5) \\15.8957(6) \\15.9678(4) \\15.9678(4) \\15.9701(1) \\$	81 307 273 1077 843 1106 267 14	56738 56598 56614 56640 56640 56682 56691 56720 56733	$18.461930(9) \\ 15.917174(9) \\ 15.917174(7) \\ 15.917129(7) \\ 15.917110(8) \\ 15.917117(9) \\ 15.917117(9) \\ 15.91711(2) \\ 15.917039(9) \\ 15.91$	$\begin{array}{c} 1.3\\ 0.73\\ 1.9\\ 0.47\\ 0.13\\ 0.49\\ 0.52\\ 0.61\end{array}$	AO/GBT GBT AO/GBT AO GBT GBT GBT GBT GBT
J2145-0750	56647 56659 56684 56684 56732 56789	$\begin{array}{c} 9.0049(8)\\ 9.0036(8)\\ 9.0043(8)\\ 9.0043(8)\\ 9.0011(9)\\ 9.007(2)\end{array}$	10 11 28 28	10 7.9 5.7 14 23	$\begin{array}{c} 9.03(1) \\ 8.7(9) \\ 8.99(2) \\ 8.97(1) \\ 8.2(5) \end{array}$	29 1807 43 22 1040	31 98 11 11 38 38	$\begin{array}{c} 8.9832(4)\\ 8.96(1)\\ 8.867(2)\\ 9.147(2)\\ 9.09(1)\end{array}$	$\begin{array}{c} 45\\ 1466\\ 238\\ 253\\ 1332\\ 1332\end{array}$	56641 56675 56733 56733	$\begin{array}{c} 9.00175(5) \\$	$\begin{array}{c} 4.3 \\ - \\ 4.3 \\ 4.3 \\ 4.3 \end{array}$	GBT — GBT GBT GBT

Table 4.3 DM estimates using low frequency GMRT data

Notes. Results from daily timing of GMRT data. Columns list the pulsar name, observing epoch of GMRT data (same value for 322 607 and MHz), DM and RMS from timing just the 322 MHz as well as the and average TOA error for that epoch, DM and RMS from timing just the 607 MHz along with average TOA error, DM and RMS from timing both frequencies, the nearest MJD in the NANOGrav 11-year data and the corresponding DM for that day, the average TOA error for that epoch, and the telescope (Arecibo or Green Bank) that observed on that epoch.



Figure 4.2 DM comparison from timing. DM measurements obtained from the combined 322/607 MHz GMRT data are shown on the x-axis, while DMs from the NANOGrav 11-year data are on the y-axis. Note that the two axes are not to the same scale due to the high precision of the NANOGrav measurements. If the estimates matched, they would sit at 0, signifying a 1:1 relation.

cause discrepancies. Some of DM measurements have ~week differences between epochs. Jones et al. (2017) calculate the timescales it takes for the DM to vary beyond the measurement errors. The DM variation timescales for the pulsars timed here are all greater than one month, so this is unlikely to be the reason for the discrepancies. Lam et al. (2016) modeled ionospheric effects and place an upper limit of their DM contribution of $\sim 10^{-4}$ pc cm⁻³, two orders of magnitude smaller than all of the DM differences seen in Table 4.3. The largest time between epochs is 9 days, making the upper limit on such a change in $DM \sim 6 \times 10^{-6} \text{ pc cm}^{-3}$ (the scaling over time is sub-linear). Following Equation 12 in Cordes et al. (2016) which assumes scattering is due to a thin screen, a fiducial pulsar observed at 322 and 607 MHz would result in an RMS DM offset due to chromatic DMs of $\sim 10^{-4}$ pc cm⁻³. Correcting for only DM and not scattering will cause discrepancies as the DM fit will absorb some scattering effects. However, all four MSPs have DMs below 19 pc cm^{-3} , so they likely do not show significant amounts of scattering. Lam et al. (2015) estimate the expected DM change per day from a strictly Kolmogorov medium of $\sim 10^{-6} \text{ pc cm}^{-3}$. However, this number is a lower limit due to the covariance between the power spectrum of a Kolmogorov medium and the presence of a DM trend; the presence of a trend would results in a slightly higher DM change.

Here we discuss the DMs for each MSP in more detail, which can be seen in Table 4.3. DM trends listed below were calculated for NANOGrav 9-year data set and discussed by Jones et al. (2017).

4.4.1 PSR J0030+0451

For MJD 56598, PSR J0030+0451 has a mean TOA uncertainty of $\epsilon_{\text{TOA}} =$ 78 μs at 322 MHz. Following Equation 4.3, the expected uncertainty in DM when just using the 322 MHz data is δ DM=0.003 pc cm⁻³. For comparison, the actual DM uncertainty for this day is 0.004 pc cm⁻³, which agrees with the predicted δ DM value. By combining the 322 MHz and NANOGrav data (where ν =1400 MHz for this epoch), the expected DM uncertainty becomes δ DM= 4×10⁻⁴ pc cm⁻³ whereas the NANOGrav data alone has a DM uncertainty of 3×10⁻⁴ pc cm⁻³. For this particular MJD, adding in the 322 MHz data neither helps nor hurts DM uncertainty as the two values are comparable. Other MJDs have a lower average TOA uncertainty, but did not have a NANOGrav observation within a few weeks that could be used for a comparison.

A linear trend was not found for PSR J0030+0451.A periodic component was found with a peak amplitude of $1.2 \pm 0.3 \times 10^{-4}$ pc cm⁻³. This DM variation amplitude is an order of magnitude smaller than the variations between DMs seen for this pulsar at 322 MHz and two orders of magnitude smaller than those at 607 MHz. It is therefore not feasible that this periodicity is causing the variation seen between DMs.

4.4.2 PSR J1640+2224

Using timing data from MJD 56732, PSR J1640+2224 has a mean TOA uncertainty of $\epsilon_{\text{TOA}} = 4.7 \ \mu s$ at 322 MHz. The expected uncertainty in DM when just using the 322 MHz is $\delta DM = 2 \times 10^{-4} \text{ pc cm}^{-3}$. The actual DM uncertainty for this day is $3 \times 10^{-4} \text{ pc cm}^{-3}$, which agrees with the predicted value. By combining the 322 MHz and NANOGrav data (where $\nu = 1400 \text{ MHz}$), the expected DM uncertainty becomes $\delta DM = 2 \times 10^{-5} \text{ pc cm}^{-3}$; for comparison, the NANOGrav data alone is $9 \times 10^{-6} \text{ pc cm}^{-3}$, which means the two values are fairly similar. The majority of TOA uncertainties for other epochs at both 322 and 607 MHz are ~an order of magnitude larger the uncertainty for this epoch, so it is unlikely that adding in other days would improve the DM uncertainty.

A linear trend was calculated to be $dDM/dt = 1.45 \pm 0.03 \times 10^{-2} \text{ pc cm}^{-3}$ yr⁻¹ (4.0 ± 0.08 × 10⁻⁵ pc cm⁻³ day⁻¹). This value is too small to account for the DM changes seen over ~ 20 days between observing epochs, so a linear trend cannot account for these variations.

4.4.3 PSR J1713+0747

For MJD 56732, PSR J1713+0747 shows a mean TOA uncertainty of $\epsilon_{\text{TOA}} = 20 \ \mu s$ at 322 MHz. The expected uncertainty in DM when just timing the 322 MHz data are $\delta \text{DM}=9 \times 10^{-4} \text{ pc cm}^{-3}$. The actual DM uncertainty for this epoch is 0.001 pc cm⁻³, which agrees with the predicted value. By combining the 322 MHz and NANOGrav data (where $\nu = 1400 \text{ MHz}$), the expected DM uncertainty becomes $\delta \text{DM}=9\times 10^{-5} \text{ pc cm}^{-3}$. Timing the NANOGrav data alone gives a DM uncertainty of $9\times 10^{-6} \text{ pc cm}^{-3}$, an order of magnitude more precise than that calculated from including the low frequency data. The TOA uncertainty is 2–3 orders of magnitude

larger for other epochs at both 322 and 607 MHz, therefore incorporating more of the current low frequency data will not improve the precision of DM measurements for this MSP.

PSR J1713+0747 was found to show a linear trend of $dDM/dt = -6.6 \pm 0.8 \times 10^{-5}$ pc cm⁻³ yr⁻¹ (-1.8 ± 0.2 ×10⁻⁷ pc cm⁻³ day⁻¹) as well as a periodic component with a peak amplitude of 5 ± 1 ×10⁻⁵ pc cm⁻³. These trends are much too small to account for the variations in DMs seen here. The DMs are not varying monotonically, which is uncharacteristic for a linear trend but is expected for a periodicity; however the DM variations are still ~2 orders of magnitude too large to be accounted for by this periodic component.

4.4.4 PSR J2145–0750

For MJD 56684, PSR J2145–0750 has a mean TOA uncertainty of $\epsilon_{\text{TOA}} = 5.7 \ \mu s$ at 322 MHz. The expected uncertainty in DM when just using the 322 MHz data are $\delta \text{DM}=2.5\times10^{-4} \text{ pc cm}^{-3}$. The actual DM uncertainty for this epoch is $8\times10^{-4} \text{ pc cm}^{-3}$, which is comparable to the predicted value. By combining the 322 MHz and NANOGrav data (where $\nu=820$ MHz for this epoch), the expected DM uncertainty becomes $\delta \text{DM}=3\times10^{-5} \text{ pc cm}^{-3}$. The NANOGrav data alone has a DM uncertainty of $7\times10^{-5} \text{ pc cm}^{-3}$; this is the only MSP for which adding in the 322 MHz data in its current state will improve the uncertainty on DM (data at 607 MHz is much less precise on two epochs, and comparable for three epochs).

PSR J2145–0750 exhibits a linear trend of $d\text{DM}/dt = 8 \pm 2 \times 10^{-5} \text{ pc cm}^{-3}$

 yr^{-1} (2.2 \pm 0.5×10⁻⁷ pc cm⁻³ day⁻¹). The DMs for J2145–0750 vary on a scale \sim 2 orders of magnitude higher than this. In addition, the DM values do not vary monotonically, so a linear trend is not the cause of these varying DMs.

4.5 Conclusions

The 9-year data set shows DM variations on the scale of the sources of varying DM discussed in §4.4. The DMs measured for the GMRT show variations much greater than these, which suggests that the reasons for these variations are not astrophysical.

For all of the MSPs discussed above, previously measured DM trends could not account for the variations seen between DM measurements. A DM variation amplitude much larger than would be expected given the average Galactic free electron density could indicate that the MSP is located in an overdense environment or is ionizing the material in the ISM along its path. However, it is unlikely that all of the pulsars discussed here are sitting in localized overdense regions, and this explanation does not account for the large difference in DMs measured between the GMRT and NANOGrav data. Due to chromatic DMs, we would not expect agreement between DMs measured at different frequencies, but as discussed above these difference are outside the range possible if caused by chromatic DMs.

For one MSP, PSR J2145–0750, incorporating the low frequency data did lower the predicted DM uncertainty when combined with NANOGrav data. However, this prediction is based solely on the mean TOA uncertainties and as explained above

T_{sky}	Flux	T_{sys}/G
Κ	mJy	$\rm K/(\rm K/Jy)$
41	1.4	211
60	1.0	43
128	6.3	516
46	3.2	30
	$\begin{array}{c} {\rm T}_{sky} \\ {\rm K} \\ 41 \\ 60 \\ 128 \\ 46 \end{array}$	$\begin{array}{c c} T_{sky} & Flux \\ K & mJy \\ \hline 41 & 1.4 \\ 60 & 1.0 \\ 128 & 6.3 \\ 46 & 3.2 \\ \end{array}$

Table 4.4 Sky and system temperatures

Notes. Sky and system temperatures for GMRT pulsars. Spectral index values were assumed to be $\alpha = -1.6$ (Jankowski et al., 2018). Flux density measurements are for 1400 MHz. System temperatures were calculated via Equation 4.5.

does not explain why the DMs between frequencies are so variant. None of the MSPs that we calculated DMs for were observed at 2300 MHz by NANOGrav; conducting this analysis with MSPs for which NANOGrav has measured TOAs at this higher frequency could produce a higher precision DM estimate when combined with low frequency data.

The ratio of the system temperature T_{sys} and the gain G can be calculated by

$$\frac{T_{sys}}{G} = \sigma_{\rm RMS} \sqrt{2\Delta\nu\Delta t} \tag{4.5}$$

where σ_{RMS} is the off pulse RMS, $\Delta \nu$ is the observing bandwidth and Δt is the number of seconds per channel (t_{obs}/n_{bins}) . The expected flux at 322 and 607 MHz can be scaled from other know values at other frequencies; scaling factors for a few of these pulsars can be seen in Table 4.4 along with calculated system temperatures.

We are not currently obtaining better DM measurements with the GMRT data. As outlined in previous sections, there are some missing pieces to the data that could improve the timing and make it useful for inclusion into the IPTA. As mentioned in Section 4.3, polarization calibration was not done when the GMRT data used here were obtained. Not accounting for polarization causes TOA uncertainties due to deviations from the pulse profile template. Using fiducial values for NANOGrav data, Lam et al. (2018) calculate the TOA uncertainty induced by errors in polarization calibration to be ~ 1 μ s for narrow frequency channels (this value averages down per observation, but may change systematically between epochs); as no polarization calibration was performed, the errors for the GMRT data are likely larger. The reason for the large errors currently seen in the GMRT data are unclear. Uncertainties like these would need to be mitigated before inclusion into the IPTA.

Chapter 5

Conclusion

We have utilized multiple radio telescopes to investigate astrophysics related to the detection of GWs using PTAs. We used data from the Arecibo and Green Bank observatories to study scale and structure in DM variations, and to characterize components in the ISM. We analyzed VLA data to follow up on a (relatively) nearby SMBH binary candidate that could be a detectable GW source in the future. We compared DM measurements obtained with the GMRT to those measured by NANOGrav to assess their precision and the possibility of including the GMRT into IPTA efforts. Here we summarize the importance of these works, future works that can be done, and future directions for PTAs as a whole.

5.1 Importance of DM characterization and understanding the ISM

We examined a large set of DM timeseries from the NANOGrav 9-year data set and found evidence of timescales as small as weeks of variations in the vast majority of MSPs. We found evidence of linear trends and annual periodicities, in addition to evidence for discrete ISM structures. We calculated and interpreted structure functions (SFs) for a subset of MSPs and examined DM variations due to LOS motions. These SFs often appear non-Kolmogorov, but we showed that this can be due to the presence of trends in the data and does not necessarily indicate a non-Kolmogorov medium.

As stated in previous sections, DM characterization is crucial for PTA success in the search for GWs. Monitoring DM gives us information about the ISM along the LOS, specifically the free electron density. The changing LOS over time that causes trends in DM can inform us on structure in the ISM. Understanding structure in the ISM and being able to distinguish ISM effects from other noise will help us form a more complete model of the time delays present in PTA data. More telescopes with a wider frequency range, like the GMRT, and more frequent observations (like CHIME's ability to get daily DMs) will improve our ability to measure and correct for DM and monitor variations.

5.2 Investigating a potential SMBH binary candidate

We investigated the hypothesis that the central SMBH in NGC 3115 was in fact offset from the galactic center, which could represent a single offset active galactic nucleus (AGN) or an AGN in orbit around a central black hole. We analyzed 10 GHz VLA data and found evidence for only one AGN. We placed a limit on the radio luminosity of any secondary supermassive black hole. We analyzed the relative positioning of the radio core, X-ray nucleus, and stellar bulge in this galaxy and determined that the radio source is centrally located with no offset from the galactic bulge.

NGC 3115 is a relatively nearby galaxy; if a SMBH binary was confirmed, it would be a potential future GW source for PTAs. Once GWs are detected with

PTAs, multi-messenger observations will give additional information about astronomical events that we have never had before and can aid in identifying possible sources that in the future may be GW emitters. One difficulty in investigating these sources is the comparison of reference frames between wavelengths and data sets. Each observation and instrument has its own astrometric offset (e.g. from the International Celestial Reference Frame); accurately accounting for these differences in reference frames can be complex.

5.2.1 Data combination and PTA data standards

We discussed the importance of lower frequency coverage as well as simultaneous dual-frequency observations available at the GMRT, and its potential to provide higher precision dispersion measurements than the data taken by NANOGrav. We compared the DMs obtained through both data sets. We discussed the possible advantages of incorporating GMRT data into timing efforts, as well as anticipated challenges.

There are several telescopes starting pulsar timing now, and many more that are anticipated to be useful instruments for pulsar timing. With more telescopes comes higher cadence, more TOAs, better frequency coverage, and improved sky coverage. Some future telescopes will be larger and/or have more advanced electronics, and will surpass current observatories in sensitivity. Incorporating these additional instruments will increase GW sensitivity.

As more telescopes come online in the next few years, along with new PTAs

forming that may join the IPTA, establishing minimum data standards and uniformity in data acquisition/recording will become necessary, particularly when those working on data combination efforts are not familiar with a specific telescope. PTAs must establish a minimal documentation requirement for observers or data processors to use to avoid reinventing the wheel each time data change hands. It would also establish a norm so that all data used for the same purpose would be processed the same way to avoid discrepancies in different pipelines.

There are several implementations that could be made to improve data processing. There is a difference between the terrestrial time standard (that must be converted to the Solar System barycenter) and the observatory clocks; this offset can be corrected for in the timing using a clock correction. These time corrections are required to avoid a systematic offset for every TOA measured at that observatory.

Headers must be recorded for every observation to avoid confusion and an opportunity for mistakes during the processing. The headers must include information like the pulsar name, RA and Dec, observing frequency, and the offset from UTC that needs to be added to the timestamp. For the GMRT, timestamp information is recorded in Indian Standard Time (IST) that must be converted to UTC. Errors in the header may be overridden in PSRCHIVE if necessary. A standard requirement of creating and incorporating headers in data would alleviate concerns about incorrect header information and the necessity to manually update each data header.

Polarization calibration must be done for all observations; errors in calibration (or an absence of calibration) introduce uncertainty to the timing residuals. As mentioned above, different observatories use different hardware and software; calibration observations when observing pulsars are very important for correcting and assessing data from multiple sites.

5.3 Going forward

We are entering a new era in GW astronomy. More telescopes are coming online with wideband systems which will not only improve our ability to measure DM but also increase TOA sensitivity. As time goes on, pulsar searches will find more MSPs which may be viable for PTA inclusion. For certain types of GW sources, a few well-timed pulsars are more useful than having many pulsars (e.g. continuous waves or bursts with memory). PTAs will become more sensitive as time goes on; certain telescopes will bring specific advantages, which can be exploited to maximize our sensitivity for searches for a particular GW source. Data combination will result in more data accessible to the IPTA as well as more algorithms for data processing and analysis.

PTAs are likely to detect GWs from the stochastic background in the next \sim 5 years. NANOGrav is already probing into the region of strain amplitude phase space where we expect GWs to exist. Placing these constraints can inform on the SMBH binary environments, like gas/stellar content and orbital eccentricity. PTAs also put limits on cosmic string tension that are more precise than other experiments such as Planck. PTAs will continue to increase sensitivity and improve limits, and by doing so will explore a new frontier in the GW universe not accessible by other experiments. The detection of low-frequency GWs will be another step towards

the characterization of our Universe. We have entered the era of GW astronomy, where GW and electromagnetic emission can be used to learn more about exotic astronomical events than has ever been possible before.

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