CORE

# Estimation of linear quadratic (LQ) model parameter alpha/beta $(\alpha / \beta)$ and biologically effective dose (BED) for acute normal tissue reactions in head and neck malignancies 

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Received April 02, 2016; Revised December 15, 2016; Accepted December 25, 2016; Published Online December 28, 2016

## Original Article


#### Abstract

Purpose: Linear-Quadratic (LQ) model has been widely used for describing radiobiological effectiveness of various fractionation schedules on tumour as well as normal tissues. This study estimates $\alpha / \beta$ for acute normal tissue reactions using Fe-plot method. Methods: 50 cases of locally advanced head and neck squamous cell carcinoma (stage III and IV) treated with external beam radiotherapy were included in this study. Patients were randomly distributed into Hyper-fractionation (HF) arm (1.2 Gy/fraction, twice daily, 6 hours apart) and conventional fractionation (CF) arm (2 Gy/fraction, once daily) with 25 cases in each arm. $\alpha / \beta$ and BED were calculated for acute normal tissue reactions using Fe-plot method. Results: In our study, the estimated values of $\alpha / \beta$ for RTOG (Radiation Therapy Oncology Group) grade 1, 2 and 3 skin reactions were 11.2 Gy, 10.1 Gy and 9 Gy respectively. Estimated values of $\alpha / \beta$ for RTOG grade 1,2 and 3 mucosal reactions were 9.7 Gy , 8.0 Gy and 9.1 Gy respectively. For Hyper-fractionation arm, calculated BED values for grade 1, 2 and 3 skin reactions were 54.45 Gy11.239, 66.90 $\mathrm{Gy}_{10.114}$ and 73.43 Gy 9.001 respectively and for grade 1,2 and 3 mucosal reactions were $33.5 \mathrm{~Gy} 9.797,57.8 \mathrm{~Gy} 8.011$ and 70.8 Gy 9.106 respectively. For conventional fractionation arm, calculated BED values for grade 1, 2 and 3 skin reactions were 54.09 Gy11.239, 66.88 Gy10.114 and 73.33 Gy9.001 respectively and for grade 1,2 and 3 mucosal reactions were $33.52 \mathrm{~Gy} 9.797,57.68 \mathrm{~Gy}_{8.011}$ and 70.73 Gy 9.106 respectively. Conclusion: LQ model and the concept of BED provide an excellent tool to compare different fractionation schedules in radiotherapy. The estimated values of $\alpha / \beta$ for acute reacting normal tissues are in good agreement with the available literature.


Keywords: LQ Model, $\alpha / \beta$, BED, Fe-plot method

## 1. Introduction

Management of cancer involves a complex and close integration of biological and physical science in conjunction with sound clinical principles to obtain the best possible therapeutic results. There has been a
general evolution in our basic biologic understanding of ionizing radiation and its interaction with living tissues.

Coutard ${ }^{1}$ in 1934 established that fractionation of radiation doses improve the results of radiotherapy as

[^0]compared to a single dose. Since then, radiation schedules consisting of dose per fraction of 180-200 cGy daily, 5 days per week over several weeks have become conventional in clinical practice. Some of the radiobiologists have suggested that conventional fractionation in radiotherapy may not be most optimal with respect to cellular kinetics and radio-sensitivity of proliferating tumour cells. Some biological experiments suggest that if the inter-fraction interval is reduced to $3-8$ hrs and radiation is given $2-3$ times per day, the therapeutic ratio can be improved. ${ }^{2,3,4}$ Since then, variety of dose fractionation schedules have been practiced in radiotherapy with an aim of increasing the radiation effects on malignant cells and at the same time sparing the normal cells as much as possible.

In order to compare various fractionation schedules, several mathematical models such as NSD (nominal standard dose), ${ }^{5}$ CRE (cumulative radiation effect) ${ }^{6}$ and TDF (time dose fractionation) ${ }^{7}$ have been used. These semi-empirical models were in use to assess the dose required to produce tolerable normal tissue reactions. However, such models are only capable of giving reliable results for early reactions of normal tissues but fail to do so for late reactions.

Linear-Quadratic (LQ) model ${ }^{8,9}$ has been widely used for describing radiobiological effectiveness of various fractionation schedules on tumour as well as normal tissues. LQ model has provided a satisfactory mathematical description to the mechanism of radiation induced cell kill. It is now clear that, LQ formulation may be applied to a wider variety of clinical circumstances by careful selection of parameters which are characteristic of a particular tissue response. LQ model was originally proposed by Keller and Rosi in 1972 as a consequence of the micro-dosimetry of radiation induced cellular lesions. The "linear" term results from interaction of radiation that occur along a single ionizing track, while the "quadratic" term results from the interaction of radiation occurring along two different particle tracks. The fact that LQ model could be used to obtain iso-effect relations for normal tissue damage was noted by Douglas and Fowler in 1976.

LQ model is useful in identifying the important difference in the effect of dose fraction size between rapidly proliferating tissues (acute reacting normal tissues and most tumours) and slowly proliferating tissues (late reacting normal tissues).

LQ model is based on the following assumptions: ${ }^{10}$
a) Ionizing radiation produce damage in cell parts which cause effective radiation damage with frequency increasing linearly with the absorbed dose (D), while other radiation induced tissue injury called sub-effective (sub-lethal) lesions can cause the same cellular effects through
mutual interaction. These later effects increase with the square of the dose ( $\mathrm{D}^{2}$ ).
b) The effective radiation damage results from the interaction of sub-effective lesions requiring production close to each other in space and in time in the same cell. In the case of low LET (linear energy transfer) radiation, each of the sub-effective lesions is produced independently i.e. by different electrons passing through the same cell.
c) The sub-effective lesions remain available for interaction during a limited time interval after their production. The decay of their capacity for interaction is assumed to be an exponential function characterized by a half-life of $0.5-2 \mathrm{hrs}$. This assumption corresponds to the concept of sub-lethal damage introduced by Elkind and Sutton on the basis of cell survival data. ${ }^{11}$
d) The influence of cell proliferation during a treatment regime must be accounted for separately for each type of tissue.
e) Equal reduction of log survival is obtained after each fraction.

LQ model is so called on account of the assumed mathematical form of underlying dose response equation. The main feature of LQ model is that the frequency of biological effect (E) i.e. log cell kill following a radiation dose ' $D$ ' is given by:

$$
E=\alpha \cdot D+\beta \cdot D^{2}
$$

where, ' $\alpha$ ' and ' $\beta$ ' are constants. ${ }^{12}$
The above equation describes two processes each of which may lead to cell death. In the first process, two critical sites within the cells are simultaneously damaged in single radiation event (single hit). Such hits in adjacent targets lead to the death of the cell. In the second process, the targets are damaged in separate radiation events after which the damaged sites may co-operate to produce cell death. When one of the target doublets is damaged by radiation, we call the cell to be sub-lethally damaged. In broad terms, $\alpha$ and $\beta$ are two measures of the relative importance of the two processes of cell kill and thus the ratio $\alpha / \beta$ is of prime significance.
' $\alpha$ ' is the linear component of cell kill, representing the intrinsic radio-sensitivity of the cells and mathematically defined as $\log$ (to the base 'e') of total number of cells killed per Gray of radiation dose in a non-repairable way. Its unit is $\mathrm{Gy}^{-1}$. ' $\beta$ ' is the quadratic component of cell kill, representing the repair capacity of the cells and hence the repairable portion the cell damage, requiring 6 hr or more for complete repair. Its unit is $\mathrm{Gy}^{-2}$.
' $E$ ' is the $\log _{e}$ sum of the non-repairable ' $\alpha$ ' term and the partly repairable ' $\beta$ ' term.

For ' $n$ ' fractions of dose ' $d$ ' per fraction (in Gray):

$$
E=n\left(\alpha \cdot d+\beta \cdot d^{2}\right)
$$

Therefore,

$$
\frac{E}{a}=n d\left(1+\frac{d}{\alpha / \beta}\right)------ \text { Eq. } 1
$$

$\alpha / \beta$ ratio precisely represents the dose at which ' $\alpha$ ' component of cell kill is equal to the ' $\beta$ ' component of cell kill (Figure 1).


Figure 1: Cell survival curve showing ' $\alpha$ ' and ' $\beta$ ' components of cell kill. ${ }^{9}$

Acute epithelial tissue reactions in radiotherapy tend to be characterised by a relatively high $\alpha / \beta$ ratio, typically in the range of 8-13 Gy with an average of about $10 \mathrm{~Gy} .{ }^{13}$ Late tissue reactions tend to be characterized by a relatively low $\alpha / \beta$ ratio typically in the range of 2-6 Gy, but spread of values may extend outside this range. ${ }^{9}$ Tumour responses tend to be characterized by a high $\alpha / \beta$ ratio, typically $6-25 \mathrm{~Gy} .{ }^{14}$

Clinical estimates of $\alpha / \beta$ are usually carried out through Fe-plots between the reciprocal of iso-effect dose and the dose per fraction. ${ }^{15}$ To plot such a graph, patients need to be irradiated to different dose fractionation schedules to obtain iso-effects for specific end point tissue effect (tumour control, early or late tissue reactions). Iso-effect doses measured for the schedules under consideration are used to plot a Fe-graph to obtain $\alpha / \beta$ for a specific end point tissue effect. Estimated values of $\alpha / \beta$ can thus be used to calculate BED (biologically effective dose) for the respective end point tissue effect and hence, evaluation of biological equivalence of various dose fractionation schedules can be done.

The basic concept of BED was defined by Barendsen ${ }^{8}$ in 1982 who first called it extrapolated tolerance dose (ETD), meaning that dose which if given in infinite number of infinitely small fractions (i.e. at very low dose rate) so that all the quadratic damage has been repaired, would cause the same log cell kill as the schedule under
consideration. ${ }^{16}$ Since it was obvious that this conceptual extrapolation to very small dose per fraction could be applied to any level of damage, not just to the maximum tolerated level or only to normal tissues, it was soon renamed as extrapolated response dose (ERD) and later to a more general term of BED. ${ }^{16}$ Because BED is defined in relation to the initial slope of cell survival curve (Figure 2) i.e. the linear component of damage, it is represented as " $\mathrm{E} / \alpha$ ".


Figure 2: Log Cell Survival Curve. ${ }^{16}$
Therefore, BED $=\mathrm{E} / \alpha$.
The unit of BED is Gy. Since, the definition of BED is the ratio $\mathrm{E} / \alpha$, the individual values of E and $\alpha$ are irrelevant for estimating relative total doses. The ratio $\mathrm{E} / \alpha$ is mathematically a link function, signifying biological equivalence between two schedules having equal effect (iso-effect). Values of " $\alpha$ " are particularly vulnerable to variation of tumour size, stage and accuracy of dose, but provided that the ratio $\mathrm{E} / \alpha$ does not vary between one prospective population and another, there are no effects on the ratios of doses between schedules, which is what one intends to compare. This is the important reason why BED is robust.

## 2. Methods and Materials

### 2.1. Patient selection

A total of 50 cases of locally advanced squamous cell carcinoma of head and neck region (stage III and IV) without any evidence of distant metastasis were included in this study. Patients were randomly distributed into Hyper-fractionation (HF) arm (1.2 Gy/fraction, twice daily, 6 hours apart) and conventional fractionation (CF) arm (2 Gy/fraction, once daily) with 25 cases in each arm.

Criteria for patient selection:
i. Histopathologically proven squamous cell carcinoma of head and neck.
ii. Location of primary: Tongue, tonsil, floor of mouth, palate, buccal mucosa and alveolus where tumour response and normal tissue
acute reactions can be assessed easily by clinical examination.
iii. Locally advanced disease (stage III and IV).
iv. No evidence of distant metastasis at the time of presentation.
v. Previously untreated cases.
vi. Karnofsky performance status (KPS) $\geq 70$.
vii. No evidence of second malignancy.
viii. Adequate baseline organ functions and hematological status.
ix. Age limit: 18-70 yrs.
x. No evidence of any dermatological disease or aphthous ulcers at the time of start of radiotherapy.

### 2.2. Treatment plan

All the 50 cases in this study were treated with external beam radiotherapy by parallel opposite pair technique on Cobalt-60 machine (Theratron 780 C and E).

Conventional fractionation (CF) arm received 2 Gy per fraction, treated once daily, 5 days a week over 6 weeks to a total dose of 60 Gy . Initial treatment fields included the primary tumor with adequate safe margins and primary nodal drainage regions (whole neck) and 44 Gy was delivered through these fields. Subsequently, fields were reduced to spare spinal cord. Primary site with gross nodes (if any) were further irradiated to a total dose of 60 Gy .

Hyper-fractionation (HF) arm received 1.2 Gy per fraction, 2 fractions per day separated by a gap of 6 hrs , 5 days a week over 5-6weeks (39 treatment days) to a total dose of 64.8 Gy . Initial treatment fields included the primary tumor with adequate safe margins and primary nodal drainage regions (whole neck) and 43.2 Gy was delivered through these fields. Subsequently, fields were reduced to spare spinal cord. Primary site with gross nodes (if any) were further irradiated to a total dose of 64.8 Gy.

### 2.3. Observation and evaluation

During radiotherapy, all the patients were assessed weekly once for development of acute skin and mucosal reactions. Grading of acute skin and mucosal reactions was done using RTOG criteria (Table 1). ${ }^{17}$ Doses at which patients developed graded acute skin and mucosal reactions were noted. Using these values, mean iso-effect doses were calculated for specific end point tissue reactions for both CF and HF arms. After 4 weeks of completion of radiotherapy, patients were assessed for treatment response in terms of disease control (tumor regression) using RECIST (Response Evaluation Criteria in Solid Tumors) criteria (Table 2). ${ }^{18,19}$

Table 1: RTOG criteria for grading of acute skin and mucosal reactions. ${ }^{17}$

| Grade | Acute skin reactions | Acute mucosal reactions |
| :---: | :--- | :--- |
| 0 | No reaction | No reaction |
| I | Erythema | Erythema |
| II | Dry Desquamation | Patchy mucositis |
| III | Moist Desquamation | Confluent mucositis |
| IV | Necrosis | Ulceration / Necrosis |

Table 2: Response evaluation criteria in solid tumors. ${ }^{\mathbf{1 8 , 1 9}}$

| Best response | Change in sums longest <br> diameters |
| :--- | :--- |
| Complete response | Disappearance; Confirmed at 4 |
| (CR) | weeks. |
| Partial response (PR) | 30\% Decrease; Confirmed at 4 <br> weeks. |
| Stable disease (SD) | Neither PR nor PD criteria met. |
| Progressive disease | 20\% Increase; No CR, PR or SD <br> (PD) |

### 2.4. Construction of Fe-plot

A graphical representation of the biological normal tissue response to conventional and hyper-fractionated radiotherapy was performed by taking dose per fraction on x -axis and inverse of iso-effect dose on y -axis (Figure 3 ). A plot was constructed by marking iso-effect doses for acute skin and mucosal reactions for both hyper-fractionation schedule and conventional fractionation schedule.


Figure 3: Fe plot - Isoeffect dose curve

### 2.5. Calculation of LQ parameter $\boldsymbol{\alpha} / \boldsymbol{\beta}$

The point at which the extrapolated line joining iso-effect doses for conventional and hyper-fractionated radiotherapy schedule intersects $y$-axis corresponds to $\alpha / \log _{e} S$ (I). Slope of the plot corresponds to $\beta / \log _{e} S$ (II). $\alpha / \beta$ can be calculated by dividing (II) from (I) which will give numerical value (in Gy) of $\alpha / \beta$ for acute skin/mucosal reactions.

Calculation of total dose ( Dx ) for hyper-fractionated schedule, which is biologically iso-effective to the dose given by conventional radiotherapy schedule (Dr). ${ }^{16}$

$$
\frac{D_{r}}{D_{x}}=\frac{\left(\frac{\alpha}{\beta}+d_{x}\right)}{\left(\frac{\alpha}{\beta}+d r\right)}------E q .2
$$

Where；
Dr：Known total dose（ 60 Gy ）for conventional RT schedule．
Dx：New total dose to be calculated for hyper－fractionated schedule．
dr：Dose per fraction for conventional radiotherapy schedule： 2 Gy．
dx：Dose per fraction for hyper－fractionated radiotherapy schedule：1．2 Gy．

Considering value of $\alpha / \beta$ to be $10 \mathrm{~Gy}^{3,20,21,22}$ for acute skin／mucosal reactions：

$$
\frac{60}{D_{x}}=\frac{(10+1.2)}{(10+2.0)}------ \text { Eq. } 3
$$

Therefore，

$$
\mathrm{Dx}=64.28 \mathrm{~Gy} .
$$

Approximating this value to obtain an exact multiple of 1．2 Gy，the total dose arrived at was 64.8 Gy ．

## 2．6．Calculation of biological effective dose（BED）

Using $\alpha / \beta$ values calculated from Fe－plot，BED for acute normal tissue reactions（Gy10）was calculated for both conventional and hyper－fractionated radiotherapy schedule．${ }^{9,23}$

$$
B E D=D\left(1+\frac{d}{\alpha / \beta}\right)---- \text { Eq. } 4
$$

where，＇ D ＇is total dose and＇ d ＇is dose per fraction．

## 3．Results

Table 3 shows the incidence of acute skin reactions in terms of RTOG grade as a function of treatment duration in weeks．

Table 3：Incidence of acute skin reactions．

|  | Hyper－fractionation Arm（HF） |  |  |  |  |  | Conventional fractionation Arm（CF） |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 0 \\ & \frac{0}{0} \\ & \frac{\pi}{6} \end{aligned}$ | $\begin{aligned} & \stackrel{\rightharpoonup}{\approx} \\ & \stackrel{\rightharpoonup}{\pi} \\ & 0 \end{aligned}$ | $$ | $\begin{aligned} & \text { m } \\ & \frac{0}{0} \\ & 0 \end{aligned}$ |  | $\begin{aligned} & \text { 픙 } \\ & \stackrel{0}{0} \end{aligned}$ | 范 | $\begin{aligned} & \stackrel{\rightharpoonup}{\approx} \\ & \stackrel{\pi}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { N } \\ & \text { © } \\ & \text { Tid } \end{aligned}$ |  | $\begin{aligned} & \text { + } \\ & \stackrel{0}{0} \\ & \text { تi } \end{aligned}$ | $\begin{aligned} & \text { त⿹\zh26灬 } \\ & 0 \end{aligned}$ |
| $1^{\text {st }}$ week | 25 | 0 | 0 | 0 | 0 | 25 | 25 | 0 | 0 | 0 | 0 | 25 |
| $2^{\text {nd }}$ week | 25 | 0 | 0 | 0 | 0 | 25 | 25 | 0 | 0 | 0 | 0 | 25 |
| $3{ }^{\text {rd }}$ week | 25 | 0 | 0 | 0 | 0 | 25 | 25 | 0 | 0 | 0 | 0 | 25 |
| $4^{\text {th }}$ week | 14 | 11 | 0 | 0 | 0 | 25 | 25 | 0 | 0 | 0 | 0 | 25 |
| $5^{\text {th }}$ week | 0 | 8 | 17 | 0 | 0 | 25 | 0 | 25 | 0 | 0 | 0 | 25 |
| $6^{\text {th }}$ week | 0 | 0 | 22 | 3 | 0 | 25 | 0 | 0 | 23 | 2 | 0 | 25 |
| 1 month follow up | 0 | 18 | 7 | 0 | 0 | 25 | 0 | 17 | 8 | 0 | 0 | 25 |

Table 4 shows the incidence of acute mucosal reactions in terms of RTOG grade as a function of treatment duration in weeks．
Table 4：Incidence of acute mucosal reactions．

|  | Hyper－fractionation Arm（HF） |  |  |  |  |  | Conventional fractionation Arm（CF） |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 0 \\ & \stackrel{0}{0} \\ & \frac{\pi}{U} \end{aligned}$ | $\begin{aligned} & \vec{\approx} \\ & \frac{\pi}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & N \\ & \stackrel{\sim}{0} \\ & \tilde{0} \end{aligned}$ | $\begin{aligned} & m \\ & \frac{\approx}{0} \\ & \frac{\pi}{6} \end{aligned}$ | $\begin{aligned} & \text { + } \\ & \stackrel{0}{0} \\ & \text { Tid } \end{aligned}$ | $\begin{aligned} & \text { 퓽 } \\ & \stackrel{1}{6} \end{aligned}$ | $\begin{aligned} & 0 \\ & \frac{\approx}{0} \\ & \frac{i}{6} \end{aligned}$ | $\begin{aligned} & \vec{\approx} \\ & \stackrel{0}{\pi} \\ & \frac{\pi}{v} \end{aligned}$ | $\begin{aligned} & N \\ & \stackrel{\sim}{0} \\ & \text { تíd } \end{aligned}$ |  |  | $\begin{aligned} & \text { 픙 } \\ & \stackrel{0}{0} \end{aligned}$ |
| $1{ }^{\text {st }}$ week | 25 | 0 | 0 | 0 | 0 | 25 | 25 | 0 | 0 | 0 | 0 | 25 |
| $2^{\text {nd }}$ week | 25 | 0 | 0 | 0 | 0 | 25 | 25 | 0 | 0 | 0 | 0 | 25 |
| $3{ }^{\text {rd }}$ week | 0 | 25 | 0 | 0 | 0 | 25 | 6 | 19 | 0 | 0 | 0 | 25 |
| $4^{\text {th }}$ week | 0 | 13 | 12 | 0 | 0 | 25 | 0 | 22 | 3 | 0 | 0 | 25 |
| $5^{\text {th }}$ week | 0 | 0 | 15 | 10 | 0 | 25 | 0 | 3 | 22 | 0 | 0 | 25 |
| $6^{\text {th }}$ week | 0 | 0 | 0 | 25 | 0 | 25 | 0 | 0 | 0 | 25 | 0 | 25 |
| 1 Month follow up | 0 | 17 | 8 | 0 | 0 | 25 | 0 | 15 | 10 | 0 | 0 | 25 |

Table 5 shows total radiation dose delivered corresponding to the treatment duration in weeks．

Table 5: Total delivered dose (Gy) corresponding to treatment duration.

| Arm | $1^{\text {st }}$ week | $2^{\text {nd }}$ week | $3{ }^{\text {rd }}$ week | $4^{\text {th }}$ week | $5^{\text {th }}$ week | $6^{\text {th }}$ week |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HF Arm | $\begin{gathered} \hline 12 \mathrm{~Gy} \\ \text { (10 fractions) } \\ \hline \end{gathered}$ | $\begin{gathered} 24 \mathrm{~Gy} \\ \text { (20 fractions) } \\ \hline \end{gathered}$ | $\begin{gathered} 36 \mathrm{~Gy} \\ \text { (30 fractions) } \end{gathered}$ | $\begin{gathered} 48 \mathrm{~Gy} \\ \text { (40 fractions) } \end{gathered}$ | $\begin{gathered} 60 \mathrm{~Gy} \\ \text { (50 fractions) } \\ \hline \end{gathered}$ | $\begin{gathered} 64.8 \mathrm{~Gy} \\ \text { (54 fractions) } \end{gathered}$ |
| CF Arm | $\begin{gathered} 10 \mathrm{~Gy} \\ \text { (5 fractions) } \\ \hline \end{gathered}$ | $\begin{gathered} 20 \mathrm{~Gy} \\ \text { (10 fractions) } \\ \hline \end{gathered}$ | $\begin{gathered} 30 \mathrm{~Gy} \\ \text { (15 fractions) } \\ \hline \end{gathered}$ | $\begin{gathered} 40 \mathrm{~Gy} \\ \text { (20 fractions) }) \\ \hline \end{gathered}$ | $\begin{gathered} 50 \mathrm{~Gy} \\ (25 \text { fractions }) \\ \hline \end{gathered}$ | $\begin{gathered} 60 \mathrm{~Gy} \\ \text { (30 fractions) } \\ \hline \end{gathered}$ |

Table 6 shows the mean iso-effect doses of radiation as a function of RTOG grade of acute skin and mucosal reactions.
Table 6: Mean iso-effect dose (Gy) for acute skin and mucosal reactions.

| RTOG Grade | Hyper-fractionation arm (HF) |  | Conventional fractionation arm (CF) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | SKIN | MUCOSA | SKIN | MUCOSA |
| Grade 2 | 59.808 Gy | 29.904 Gy | 45.92 Gy | 27.84 Gy |
| Grade 3 | 64.8 Gy | 62.592 Gy | 55.84 Gy | 46.16 Gy |
| Grade 4 | - | - | 60 Gy | 58 Gy |

Table 6A: Statistical table.

| Acute reactions | Grade | Hyper-fractionation Arm (HF) |  | Conventional fractionation Arm (CF) |  | t | p |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mean | S.D | Mean | S.D |  |  |
| Skin reactions | Grade 1 | 49.20 | 2.42 | 45.92 | 1.87 | 5.357 | <0.001 |
|  | Grade 2 | 59.808 | 3.21 | 55.84 | 2.76 | 4.231 | <0.001 |
|  | Grade 3 | - | - | - | - | - | - |
| Mucosal reactions | Grade 1 | 29.904 | 2.64 | 27.84 | 3.21 | 2.730 | <0.05 |
|  | Grade 2 | 50.304 | 2.99 | 46.16 | 3.91 | 4.391 | <0.001 |
|  | Grade 3 | 62.59 | 2.32 | 58.0 | 2.65 | 6.235 | <0.001 |



Figure 4: Fe-plot for grade I skin reaction.
Figure 4 shows the Fe-plot drawn for iso-effect doses of grade 1 skin reaction. X -axis shows dose per fraction of the treatment schedule and Y-axis shows inverse of total dose delivered. While HF arm patients developed grade 1 skin reaction at a mean iso-effect dose of 49.2 Gy , CF arm patients developed the same at mean iso-effect dose of 45.9 Gy. Numerical value on $y$-axis $(1 / 53.5)$ obtained by extrapolating the line joining the respective isodose points corresponds to $\alpha / \log _{e} S$ and the slope of the curve ( $1.663 \times 10^{-3}$ ) corresponds to $\beta / \log _{e} S$.

Figure 5 shows the Fe-plot drawn for iso-effect doses of grade 2 skin reaction. While HF arm patients developed grade 2 skin reaction at a mean iso-effect dose of 59.8 Gy, CF arm patients developed the same at mean iso-effect dose of 55.8 Gy . Numerical value on y -axis $(1 / 66)$ obtained by extrapolating the line joining the
respective isodose points corresponds to $\alpha / \log _{\mathrm{e}} \mathrm{S}$ and the slope of the curve ( $1.498 \times 10^{-3}$ ) corresponds to $\beta / \log _{e} S$.


Figure 5: Fe-plot for grade 2 skin reaction.


Figure 6: Fe-plot for grade 3 skin reaction.

Figure 6 shows the Fe-plot drawn for iso-effect doses of grade 3 skin reaction. While HF arm patients developed grade 3 skin reaction at a mean iso-effect dose of 64.8 Gy, CF arm patients developed the same at mean iso-effect dose of 60 Gy . Numerical value on y -axis $(1 / 72)$ obtained by extrapolating the line joining the respective isodose points corresponds to $\alpha / \log _{e} S$ and the slope of the curve ( $1.543 \times 10^{-3}$ ) corresponds to $\beta / \log _{e} S$.


Figure 7: Fe-plot for grade I mucosal reaction.
Figure 7 shows the Fe-plot drawn for iso-effect doses of grade 1 mucosal reaction. While HF arm patients developed grade 1 mucosal reaction at a mean iso-effect dose of 29.9 Gy , CF arm patients developed the same at mean iso-effect dose of 27.8 Gy . Numerical value on y -axis $(1 / 33)$ obtained by extrapolating the line joining the respective isodose points corresponds to $\alpha / \log _{e} S$ and the slope of the curve ( $3.093 \times 10^{-3}$ ) corresponds to $\beta / \log _{e} S$.


Figure 8: Fe-plot for grade 2 mucosal reaction.

Figure 8 shows the Fe-plot drawn for iso-effect doses of grade 2 mucosal reaction. While HF arm patients developed grade 2 mucosal reaction at a mean iso-effect dose of 50.3 Gy , CF arm patients developed the same at mean iso-effect dose of 46.1 Gy . Numerical value on $y$-axis $(1 / 56)$ obtained by extrapolating the line joining the respective isodose points corresponds to $\alpha / \log _{\text {e }} S$ and the slope of the curve ( $2.228 \times 10^{-3}$ ) corresponds to $\beta / \log _{e} S$.


Figure 9: Fe-plot for grade 3 mucosal reaction.
Figure 9 shows the Fe-plot drawn for iso-effect doses of grade 3 mucosal reaction. While HF arm patients developed grade 3 mucosal reaction at a mean iso-effect dose of 62.5 Gy , CF arm patients developed the same at mean iso-effect dose of 58 Gy . Numerical value on y -axis ( $1 / 69.5$ ) obtained by extrapolating the line joining the respective isodose points corresponds to $\alpha / \log _{e} S$ and the slope of the curve ( $1.58 \times 10^{-3}$ ) corresponds to $\beta / \log _{e} S$.

### 3.1. Calculation of $L Q$ model parameter $\alpha / \beta$ (Table 7)

' Y ' intercept of Fe -plot corresponds to $\alpha / \log _{\mathrm{e}} \mathrm{S}$.
Slope of the curve corresponds to $\beta / \log _{e} S$.
Hence, $\alpha / \beta=\left(\alpha / \log _{e} S\right) \div\left(\beta / \log _{e} S\right)$

### 3.2. Calculation of biological effective dose (BED) (Table 8)

$$
B E D=D\left(1+\frac{d}{\alpha / \beta}\right)---- \text { Eq. } 4
$$

Table 7: Calculated values of $\alpha / \beta$ for acute skin and mucosal reactions using Fe-plot method.

| Acute radiation reactions |  | 'Y'Intercept <br> $\left(\alpha / \log _{e} S\right)$ | Slope $\left(\beta / \log _{e} S\right)$ | $\alpha / \beta=\left(\alpha / \log _{e} S\right) \div\left(\beta / \log _{e} S\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| Skin | Grade 1 | $1 / 53.5$ | $1.663 \times 10^{-3}$ | 11.239 |
|  | Grade 2 | $1 / 66$ | $1.498 \times 10^{-3}$ | 10.114 |
|  | Grade 3 | $1 / 72$ | $1.543 \times 10^{-3}$ | 9.001 |
|  | Grade 1 | $1 / 33$ | $3.093 \times 10^{-3}$ | 9.797 |
|  | Grade 2 | $1 / 56$ | $2.228 \times 10^{-3}$ | 8.011 |
|  | Grade 3 | $1 / 69.5$ | $1.58 \times 10^{-3}$ | 9.106 |

Table 8: BED calculation: Using $\alpha / \beta$ values calculated from Fe-plot, BED for acute normal tissue reactions (Gy $\alpha / \beta$ ) was calculated.

| RTOG grade of acute reactions | BED (Gy $\alpha / \beta$ ) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | HF Arm ( $\mathrm{D}=$ iso-effect dose \& d = 1.2 Gy) |  | CF Arm (D = iso-effect dose \& d = 2 Gy ) |  |
|  | SKIN | MUCOSA | SKIN | MUCOSA |
| Grade 1 | $54.45 \mathrm{Gy11.239}^{\text {a }}$ | 33.566 Gy9.797 | 54.09 Gy11.239 | 33.52 Gy9.797 |
| Grade 2 | 66.90 Gy10.114 | 57.839 Gy8.001 | 66.88 Gy10.114 | 57.68 Gy8.001 |
| Grade 3 | 73.439 Gy9.001 | 70.84 Gy9.106 | 73.33 Gy9.001 | 70.73 Gy9.106 |

Where ' D ' is iso-effect dose and ' d ' is dose per fraction.
Table 9: Treatment response evaluation for disease control using RECIST criteria.

| Disease response | $\begin{aligned} & \ddot{0} \\ & \underset{\sim}{0} \end{aligned}$ | HF Arm |  |  |  | CF Arm |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\begin{aligned} & \text { I O } \\ & \vdots \\ & \sum_{i=1}^{0} \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { 클 } \\ & \sum_{0}^{0} \\ & \sum_{5}^{0} 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $\begin{aligned} & \ddagger \\ & \# \\ & \vdots \\ & 0 \\ & \sum_{n}^{0} \\ & 0 \\ & 0 \end{aligned}$ |  |  |
| Complete response (CR) | III | 8 | 11 | 11 | 10 | 7 | 9 | 10 | 10 |
|  | IV | 1 | 5 | 5 | 4 | 1 | 2 | 2 | 2 |
| Partial response (PR) | III | 3 | 1 | 1 | 2 | 7 | 5 | 4 | 4 |
|  | IV | 8 | 7 | 6 | 6 | 7 | 8 | 7 | 6 |
| Stable disease (SD) | III | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|  | IV | 3 | 0 | 1 | 1 | 2 | 0 | 1 | 2 |
| Progressive disease (PD) | III | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|  | IV | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Total |  | 25 | 25 | 25 | 24* | 25 | 25 | 25 | 25 |

Table 9A: Statistical table.

| Disease response | $\begin{aligned} & \text { 䃾 } \\ & \text { E } \end{aligned}$ | End of treatment |  | Month follow up |  | 3rd Month follow up |  | $6{ }^{\text {th }}$ Month follow up |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\chi^{2}$ | p | $\chi^{2}$ | p | $\chi^{2}$ | p | $\chi^{2}$ | p |
| Complete response(CR) | III | 0.0952 | >0.05 | 0.3333 | $>0.05$ | 0.0821 | >0.05 | 0 | - |
|  | IV | 0 | - | 1.495 | >0.05 | 1.495 | >0.05 | 0.7576 | >0.05 |
| Partial response (PR) | III | 2.00 | >0.05 | 3.0303 | >0.05 | 2.00 | >0.05 | 0.7576 | >0.05 |
|  | IV | 0.0952 | $>0.05$ | 0.0952 | >0.05 | 0.104 | >0.05 | 0 | - |
| Stable disease (SD) | III | 1.0204 | >0.05 | 0 | - | 0 | - | 0 | - |
|  | IV | 0.2222 | >0.05 | 0 | - | 0 | - | 0.3546 | >0.05 |
| Progressive disease <br> (PD) | III | 0 | - | 0 | - | 0 | - | 0 | - |
|  | IV | 0 | - | 0 | - | 0 | - | 0 | - |

## 4. Discussion

This study showed the estimated values of $\alpha / \beta$ for grade 1,2 and 3 skin reactions to be $11.2 \mathrm{~Gy}, 10.1 \mathrm{~Gy}$ and 9 Gy respectively. Fowler et al. ${ }^{24}$ in 1974 estimated value of $\alpha / \beta$ for skin desquamation to be 9.4 Gy (6.1 Gy - 14.3 Gy). Douglas et al. ${ }^{25}$ in 1976 estimated value of $\alpha / \beta$ for skin desquamation to be 11.7 Gy ( $9.1 \mathrm{~Gy}-15.4 \mathrm{~Gy}$ ). Joiner et al. ${ }^{26}$ in 1986 estimated value of $\alpha / \beta$ for skin desquamation to be 10.5 Gy ( $8.5 \mathrm{~Gy}-12.5 \mathrm{~Gy}$ ). Bentzen et al. ${ }^{27}$ in 1988 estimated $\alpha / \beta$ for skin erythema to be $12.3 \mathrm{~Gy}(2 \mathrm{~Gy}-23 \mathrm{~Gy})$. Turesson et al. ${ }^{28}$ in 1989 estimated $\alpha / \beta$ for skin desquamation to be 11.2 Gy ( 8.5 Gy - 17.6 Gy). They estimated value of $\alpha / \beta$ for skin erythema to be 8.8 Gy ( $6.9 \mathrm{~Gy}-11.6 \mathrm{~Gy}$ ). In this study, the estimated values of $\alpha / \beta$ for grade 1,2 and 3 mucosal
reactions were 9.7 Gy, 8.0 Gy and 9.1 Gy respectively. Rezvani et al. ${ }^{29}$ in 1991 estimated $\alpha / \beta$ for acute mucosal reactions to be 15 Gy ( $0-45.2 \mathrm{~Gy}$ ).

Estimated values of $\alpha / \beta$ were used to calculate biologically effective dose (BED) for acute skin and mucosal reactions for both HF and CF arms. For HF arm, estimated values of BED for grade 1, 2 and 3 skin reactions were $54.45 \mathrm{~Gy}_{11.239} 66.90 \mathrm{~Gy}_{10.114}$ and 73.43Gy9.001 respectively and for grade 1,2 and 3 mucosal reactions were $33.5 \mathrm{Gy9.797}, 57.8 \mathrm{~Gy} 8.011$ and 70.8 Gy9. 106 respectively. For CF arm, estimated values of BED for grade 1, 2 and 3 skin reactions were 54.09 Gy11.239, 66.88 Gy10.114 and 73.33 Gy9.001 respectively and for grade 1 , 2 and 3 mucosal reactions were 33.52 Gy9.797, 57.68 Gy8.011 and 70.73 Gy9.106 respectively. An EORTC study ${ }^{30}$
which studied hyper-fractionated schedule of 1.15 Gy per fraction, twice a day to a total dose of 80.5 Gy in 42 days, measured the value of BED for acute skin and mucosal reactions to be $79.45 \mathrm{~Gy} 10^{10}$. An RTOG study ${ }^{31}$ which studied hyper-fractionated schedule of 1.2 Gy per fraction, twice a day to a total dose of 81.6 Gy in 42 days, measured the value of BED for acute skin and mucosal reactions to be $81.09 \mathrm{~Gy}_{10}$. Results of EORTC and RTOG studies show higher BED values from that of our study because the planned total dose in these studies were greater than that was planned in our study.

The importance of the estimated values of BED for specific end point tissue reaction lies in its utility in comparing different fractionated radiotherapy schedules. BED values obtained in our study show that the hyper-fractionated radiotherapy schedule using 1.2 Gy per fraction, 2 fractions per day for a total dose of 64.8 Gy is biologically equivalent to the conventional fractionated radiotherapy schedule of 2 Gy per fraction, 1 fraction a day to a total dose of 60 Gy in terms of acute skin and mucosal reactions. However, reactions appeared early in hyper-fractionated schedule.

Evaluation of treatment response in terms of disease control using RECIST criteria showed that $36 \%$ of HF arm and $32 \%$ of CF arm patients had complete response, $44 \%$ of HF arm and $56 \%$ of CF arm patients had partial response, $16 \%$ of HF arm and $8 \%$ of CF arm patients had stable disease and $4 \%$ of HF arm and $4 \%$ of CF arm patients had progressive disease. Statistical evaluation showed that hyper-fractionated and conventional fractionated radiotherapy used in our study are biologically equivalent in terms of disease control as well.

## 5. Conclusion

LQ model and the concept of BED provide an excellent tool to compare different fractionation schedules in radiotherapy and form the basis of selection of a particular fractionation schedule in order to achieve a better therapeutic ratio. Ample amount of work has been done in the field of radio-biology to estimate the values of LQ model parameter $\alpha / \beta$ for specific tissue reactions, however further efforts in this direction will certainly be solicited towards the ultimate goal of higher tumour control probability and low normal tissue complication probability.

## Conflict of interest

The authors declare that they have no conflicts of interest. The authors alone are responsible for the content and writing of the paper.

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