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Comparison of experimental and theoretical fully differential cross sections for single ionization of the 2s and 2p states of Li by O⁸⁺ ions

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This paper presents a full three-dimensional (3D) comparison between experiment and theory for 24 MeV O^{8+} single ionization of the 2*s* ground state of lithium and the 2*p* excited state. Two theoretical approximations are examined: the three-body continuum distorted-wave (3DW) and three-body continuum distorted-wave–eikonal initial state (3DW-EIS). Normally, there is a significant difference between these two approaches and the 3DW-EIS is in much better agreement with experiment. In this case, there is very little difference between the two approaches and both are in very good agreement with experiment. For the excited 2*p* state, the 3D cross sections would exhibit a mirror symmetry about the scattering plane if all three magnetic sublevels were excited in equal proportions. For the present experiment, the 2*p*₊₁ (*m* = +1) sublevel is dominantly excited (quantization axis is the incident beam direction) and for this case there is a magnetic dichroism which is observed both experimentally and theoretically.

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I. INTRODUCTION

The importance of studies of atomic collisions in the context of the few-body problem (FBP) has frequently been pointed out [1-4]. The essence of the FBP is that the Schrödinger equation is not analytically solvable for more than two mutually interacting particles even when the underlying forces are precisely known. Therefore, theory has to resort to extensive modeling effort to obtain numerical solutions and this tends to require very large computational resources. The approximations used in these models have to be tested by detailed experimental data. The most sensitive tests of theory are offered by kinematically complete experiments, in which the momenta of all collision fragments are determined and from which fully differential cross sections (FDCSs) can be extracted. A particularly suitable collision reaction to study the FBP is ionization of the target because here the final state involves at least three unbound particles. In contrast, capture or excitation processes kinematically represent twobody scattering processes and, as a result, few-body effects tend to be less pronounced than in ionization.

Since the pioneering work of Ehrhardt *et al.* [5], FDCS measurements have been performed routinely for target ionization by electron impact [3,5-10] (for a review, see [10]). These studies have led to the development of a large variety of theoretical models ranging from perturbative approaches based on distorted-wave methods [11,12] or methods including final-state electron-electron interactions exactly [13–16] to nonperturbative time-independent methods [2,17,18] to nonperturbative time-dependent methods [19]. For atomic hydrogen and helium targets, these studies have resulted in major advancements of our understanding of the collision dynamics and these problems can be considered as essentially

"solved." However, there are still major issues for larger atoms and molecules.

Studying target ionization by ion impact, both experimentally and theoretically, is much more challenging. Kinematically complete experiments are hampered because the large projectile mass results in very small (for fast heavy-ion-impact immeasurably small) scattering angles and projectile energy losses (relative to the incident energy). Theoretically, the large projectile mass makes a pure quantum-mechanical treatment of the process very difficult because the description of the projectile requires accounting for an enormous number of angular momentum states of the scattered projectiles. As a result, distorted-wave treatments for heavy particles are currently not possible. With the advent of cold-target recoilion momentum spectroscopy (COLTRIMS) [20,21], also known as a reaction microscope (ReMi), kinematically complete experiments for ion-impact ionization became feasible [22–28] (for a review, see [28]). These measurements sparked significant theoretical activities as well. Initially, these studies were restricted to perturbative methods [29–36], but more recently nonperturbative calculations have been reported [37-39].

Given the experimental and theoretical challenges in studying ionization by ion impact, it is not surprising that our understanding of the few-body dynamics is significantly less complete than for electron impact. Part of the discrepancies between experiment and theory can be associated with the projectile coherence properties [40–43], which were not accounted for in theoretical models until recently and which have an insignificant effect on cross sections for electron impact. In addition, for highly charged ions, higher-order contributions are much stronger than for electron impact and also contribute to larger discrepancies between experiment and theory. Finally, the experimental resolution, which tends to be somewhat worse than for electron impact, complicates the comparison to theory.

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Another limitation of kinematically complete experiments for ion impact is that only a small variety of target species are accessible. COLTRIMS is only feasible for gaseous targets of relatively small mass number because the momentum resolution gets worse with increasing mass. These limitations were overcome with the recent development of MOTReMi [44]. In this device a magneto-optical trap (MOT), providing a very cold target and thereby improving the overall momentum resolution by about a factor of 3, is combined with a ReMi. With this apparatus, kinematically complete experiments for ion impact ionization of targets other than helium and molecular hydrogen, namely, for lithium, became feasible. Previously, double-differential ejected electron spectra were reported [45,46], but using the new MOTReMi apparatus FDCS were measured for the first time [47].

There are several features offered by a lithium target which lead to qualitative differences to helium in the collision dynamics. First of all, the radial nodal structure of the groundstate wave function of the valence electron (2s) leads to richer structures in the FDCS. Second, the valence shell contains only a single electron and the inner shell is far away from the valence shell, both spatially and energetically. As a result, electron-electron correlation effects are expected to be much less important than in helium. Finally, a significant fraction of the target atoms gets excited to the 2p state in the field of the cooling laser. Due to the magnetic field of the trap, this excited state is Zeeman split and the energetically lowest lying Zeeman state ($m = \pm 1$, depending on the polarization of the magnetic field) is predominantly populated. As a result, the target is spin polarized, which leads to asymmetries in the FDCS for 2p ionization, also known as magnetic dichroism (or sometimes called orientational dichroism).

It is certainly of considerable interest to understand to what extent the few-body dynamics is affected by these features. However, the experimental data for a lithium target were only recently reported. As a result, theoretical studies have also recently started to shift focus from helium to lithium [47-52]. In this article, we present a comprehensive comparison between experiment and theory covering a broad range of kinematic parameters for ionization both from the ground state and from the 2p state. Some fully differential cross sections obtained from the same experimental run were presented in Schultz et al. [26] and Hubele et al. [47]. In [26], the postcollision interaction in 2s ionization of lithium was studied for the FDCS in the scattering plane. In [47], experiment was compared to theory for two cases in a plane perpendicular to the incident beam direction. Here, we compare experiment and theory for the full three-dimensional cross section for three cases and for each case examine results in both the scattering plane and the perpendicular plane (also sometimes called the azimuthal plane).

II. EXPERIMENT

The experiment was performed with the magneto-optical trap reaction microscope MOTReMi [44,53] implemented in the ion storage ring TSR at the Max-Planck Institute for Nuclear Physics in Heidelberg (MPI). The O^{8+} ions were created and accelerated to an energy of 1.5 MeV/amu using the MPI tandem accelerator. The ion beam was injected in the

storage ring, cooled in the TSR electron cooler, and bunched with the TSR rf cavity with bunch durations of few ns and a repetition rate of about 3 MHz. In the MOTReMi, the ion beam was intersected with a laser-cooled atomic lithium cloud. After an ionization event, electrons and lithium ions are extracted toward two detectors in opposite directions by the combination of an electric (0.6 V/cm) and a homogenous magnetic (7.7 Gauss) field. Their measured time of flight and their position on the detector are used to calculate the particles' momenta.

As compared to conventional experiments with groundstate atoms prepared in a gas jet, there are essentially two complications due to the operation of the MOT and the study of optically excited target atoms: First, the MOT requires an inhomogeneous magnetic field for the trapping of the atoms which renders the momentum-resolved detection of electrons in the reaction microscope impossible. Second, the (incoherent) optical excitation leads to a mixture of ground (2s) and excited (2p) state target atoms. Furthermore, this excitation can never result in an excited-state population exceeding 50%, so that neither a pure ground state nor a pure excited state can be achieved while the target atoms are exposed to the cooling laser light. In this experiment the excited-state population was around 20%.

Both challenges are mastered by employing a sophisticated switching cycle of the MOT magnetic field and the cooling lasers. First, the MOT magnetic field is periodically switched off for a few milliseconds. During this measurement period, the atoms are stilled located in the trap region and emitted electrons can easily be momentum analyzed. Second, the cooling lasers are also switched off, but only for a duration of a couple of hundred microseconds. In this period, all the target atoms are in the 2s ground state (the excited 2p state has a lifetime of only about 27 ns). Cross sections for excited-state ionization can be obtained by subtracting the measured spectra for the periods with the laser beams being switch on (providing the target in a 2*p*-2*s* mixture) and switched off (providing a pure 2s target). The spectrum for the laser beams switched on has to be weighted with consideration of the excited-state population of 20% (see, e.g., LaForge et al. [54]).

It should be noted that there is a strong asymmetry in the population of the magnetic sublevels of the excited 2p state while the cooling lasers are switched on. This is due to the homogenous magnetic field of the reaction microscope applied to extract the collision fragments. The Zeeman splitting of the excited 2p state along with a red detuning of the laser light from the 2s-2p resonance results in the predominant population of the magnetic sublevels with lower energy (in the present case m = +1). We estimate a population of 0.86, 0.09, and 0.05 for the magnetic substates with m = +1, 0, and -1, respectively. A higher degree of polarization can be obtained by employing optical pumping [53]; however, this technique was not used in the experiment described here.

III. THEORETICAL MODELS

The two theoretical models considered here are the threebody distorted-wave (3DW) approximation and the three-body distorted-wave–eikonal initial-state (3DW-EIS) approximation. The details of these approaches can be found in [33,55,56] so only a brief overview will be given here. These two models are very similar and the only difference is the initial-state wave function for the incoming projectile.

To reduce the complexity of the few-body problem, we consider the outer-shell electron as the active electron and assume that the other electrons are frozen in their initial states during the collision process. Consequently, the scattering process can be treated as a three-body problem. The effects of the passive electrons are taken into account in the calculation of the effective potential seen by the ejected electron (the distorting potential).

Let us consider a typical three-body collision system in which the projectile P impinges on the initially bound target ion (i.e., the target atom without the active electron) plus electron (T + e) subsystem and causes the ejection of the electron e. In the 3DW approximation, the initial state of the scattering system is approximated as

$$\Phi_i^+(\mathbf{r}, \mathbf{R}) = \varphi_i(\mathbf{r}) \exp(i\mathbf{K}_i \cdot \mathbf{R}), \qquad (1)$$

where $\varphi_i(\mathbf{r})$ is the initial bound state for the active electron which is calculated using the usual self-consistent Hartree-Fock method. The projectile wave function is a plane wave with initial momentum \mathbf{K}_i and (\mathbf{r}, \mathbf{R}) are the position vectors of *e* and *P* with respect to the target nucleus. The exact final state is approximated as

$$\Psi_f^{-}(\mathbf{r}, \mathbf{R}) = \chi_e^{-}(\mathbf{r}) C_P^{-}(\mathbf{K}_f, \mathbf{R}) D_{Pe}(\mathbf{r}, \mathbf{R}), \qquad (2)$$

where $\chi_e^{-}(\mathbf{r})$ is the continuum state of the ejected electron in the field of the target ion T, $C_P^{-}(\mathbf{K}_f, \mathbf{R})$ is a Coulomb wave for P in the field of T with momentum \mathbf{K}_f , and $D_{Pe}(\mathbf{r}, \mathbf{R})$ is a function that takes into account the Coulomb interaction between the projectile and the ejected electron (postcollision interaction, PCI). The ejected-electron wave function $\chi_e^{-}(\mathbf{r})$, called a distorted wave, is a numerical solution of the Schrödinger equation

$$(T_e + U_f - E_e)\chi_e^{-}(\mathbf{r}) = 0, \qquad (3)$$

where T_e is the kinetic energy operator for the electron, the distorting potential U_f is a spherically symmetric potential for the *T*-*e* interaction which is calculated using the Hartree-Fock charge density for the final-state ion, and E_e is the energy of the ejected electron. With these approximations, the 3DW T matrix is

$$T_{\rm fi}^{\rm 3DW} = \int d\mathbf{r} \, d\mathbf{R} \Psi_f^{-*}(\mathbf{r}, \mathbf{R}) V_i(\mathbf{r}, \mathbf{R}) \Phi_i^+(\mathbf{r}, \mathbf{R}), \qquad (4)$$

where $V_i(\mathbf{r}, \mathbf{R})$ is the Coulomb *P*-*e* interaction. This six-dimensional integral is evaluated numerically.

In a second approach, the exact two-potential form of the transition amplitude first derived by Gell-Mann and Goldberger [57]

$$T_{\rm fi} = \langle \Psi_f^- | W_f^\dagger | \Psi_i^+ \rangle + \langle \Psi_f^- | V_i - W_f^\dagger | \Phi_i^+ \rangle \tag{5}$$

is used, in which Ψ_i^+ is the exact initial-state wave function, Φ_i^+ is the asymptotic initial-state wave function of Eq. (1), Ψ_f^- is an approximate final-state wave function [we use the same one as Eq. (2)] which determines the final-state perturbation W_f . If we approximate Ψ_i^+ as Φ_i^+ , the above exact amplitude reduces to the 3DW transition amplitude. However, Crothers [58] and Crothers and McCann [29] showed that a better approximation for Ψ_i^+ is to use an eikonal wave function which satisfies the correct boundary conditions. This approximation was called the CDW-EIS (continuum distortedwave–eikonal initial state). In this approach, an analytical continuum wave is used for the ejected electron, whereas we use a numerical distorted wave for the ejected electron so we call our approximation 3DW-EIS (three-body distorted-wave–eikonal initial state). The final-state perturbation potential is given by

$$W_f(\mathbf{r}, \mathbf{R}) = \frac{1}{\Psi_f^-(\mathbf{r}, \mathbf{R})} (H - E) \Psi_f^-(\mathbf{r}, \mathbf{R}).$$
(6)

Here *H* is the total Hamiltonian and *E* is the total energy of the system. In order to obtain an analytic expression for the perturbation, we assume that the ejected-electron wave function is a continuum wave with an effective charge of +1. The full expression for the latter case can be found in Jones and Madison [59]. The eikonal initial-state wave function is given by

DIC

$$\Psi_{i}^{+} \approx \Psi_{i}^{\text{EIS}}(\mathbf{r}, \mathbf{R})$$

$$= \Phi_{i}^{+}(\mathbf{r}, \mathbf{R}) \exp\left[i\frac{Z_{P}}{\mathbf{v}_{i}}\ln\left[\frac{\mathbf{v}_{i}R - \mathbf{v}_{i} \cdot \mathbf{R}}{\mathbf{v}_{i}|\mathbf{R} - \mathbf{r}| - \mathbf{v}_{i} \cdot (\mathbf{R} - \mathbf{r})}\right]\right],$$
(7)

where \mathbf{v}_i is the velocity of the projectile with respect to the target.

The fully differential cross section (FDCS) for scattering of the projectile into solid angle $d\Omega_P$ and ejection of the electron into solid angle $d\Omega_e$ is given by [33,55]

$$\frac{d^{3}\sigma}{d\Omega_{P}\,d\Omega_{e}\,dE_{e}} = (2\pi)^{4}N_{e}\,\mu_{Te}\,\mu_{i}^{2}\,k_{e}\,\frac{K_{f}}{K_{i}}|T_{\rm fi}|^{2},\qquad(8)$$

in which μ_i is the initial reduced mass of the whole system, μ_{Te} is the reduced mass of the subsystem (T + e) and N_e is the number of the electrons equivalent to the active electron in the target.

In the paper of Hubele *et al.* [47], experiment was compared with a CDW-EIS calculation which is a similar calculation. The differences between these two calculations are the following: (1) The CDW-EIS approach uses a semiclassical straight line approach for the projectile while our approach is fully quantum mechanical. (2) For the active electron, we use a Hartree-Fock bound state wave function and a numerical distorted wave for the continuum electron. (3) Standard CDW-EIS calculations only evaluate the first term of Eq. (5) while we evaluate both terms.

IV. RESULTS

In this section the theoretical and experimental results are presented and compared. The coordinate system we are using has the z axis in the incident beam direction and the xz plane is the scattering plane with the projectile being scattered in the direction of the +x axis. This means that the transverse momentum transfer direction is in the -x direction. Figure 1 compares three-dimensional images of 3DW-EIS results and experiment for the FDCS for ionization of the 2s and 2p states of lithium atoms by impact of bare oxygen ions with an incident energy of 24 MeV. The projectile momentum transfer is defined as $\mathbf{q} = \mathbf{K}_i - \mathbf{K}_f$ and along with \mathbf{K}_i it spans the

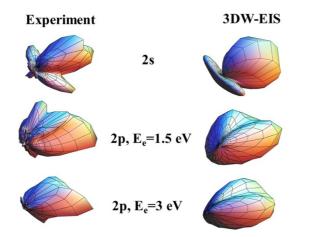


FIG. 1. Comparison of experimental and theoretical 3DW-EIS results in three dimensions for 24 MeV O⁸⁺ ionization of the 2*s* and 2*p* states of lithium. For 2*s*, $E_e = 1.5$ eV and the momentum transfer is q = 1 a.u. For 2*p* and $E_e = 1.5$ eV, the momentum transfer is q = 0.3 a.u., and for 2*p* and $E_e = 3$ eV, the momentum transfer is q = 0.4 a.u.

scattering plane. For 2s states, q and the ejected electron energy E_e are q = 1 a.u. and $E_e = 1.5$ eV. For ionization of the 2p states, two sets of these values are considered: (q = 0.3 a.u., $E_e = 1.5$ eV) and (q = 0.4 a.u., $E_e = 3$ eV).

There are two features which are normally seen in the FDCS for single ionization of the target which are often described in terms of classical mechanisms. In the first, the projectile knocks the active atomic electron into its final state while the residual ion remains as a spectator. The electron emission occurs nearly in the same direction as \mathbf{q} and the cross sections normally have a peak near this direction which is called the binary peak. In the second, the collision of the active electron with the projectile is followed by a backscattering of the electron from the target core. In this mechanism, the electron ejection is nearly into the opposite direction of **q** and the peak near this direction is called the recoil peak. Normally, it is expected that these mechanisms will lead to a double-peak structure both in experimental and theoretical results for the FDCSs. From Fig. 1, we can see that the 2s results have a binary peak (large round peak to the right) and recoil peak (smaller winglike feature to the left). However, there is almost no recoil peak for the two 2p cases.

As is seen, there is reasonable good agreement between the theoretical calculations and experiment in general. The binary peak is completely dominant for all cases. The interesting experimental and theoretical 2s recoil wings are very similar, while these wings are absent in the images for the 2p electrons. Hubele *et al.* [47] as well as Walters and Whelan [50] have suggested that the wings are due to the nodal structure of the initial 2s state along with the interaction between the projectile and target nucleus, the so called nucleus-nucleus (*NN*) interaction. On the other hand, Gulyás *et al.* [51] found that the wings resulted from the *NN* interaction plus a binary collision.

The next set of figures show planar slices through the 3D plots. Figure 2 compares experimental and theoretical FDCSs for ejection of 2s and 2p electrons into the scattering plane. The angle θ_b is the ejected electron observation angle measured clockwise in the scattering plane relative to \mathbf{K}_i and the maxi-

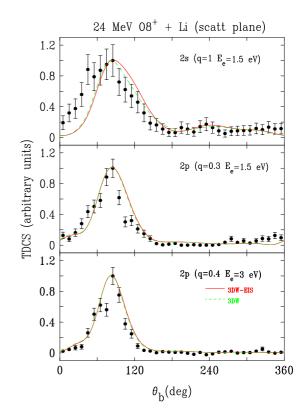


FIG. 2. Comparison of experimental and theoretical results for 24 MeV O⁸⁺ ionization of the 2*s* and 2*p* states of lithium as a function of the ejected electron angle θ_b in the scattering plane. The projectile momentum transfer *q* and ejected electron energy E_e are indicated in each panel. The solid (red) results are 3DW-EIS and the dashed (green) lines are the 3DW results. The experimental and theoretical results are both normalized to unity at $\theta_b = 180^\circ$.

mum cross sections are at 90° which is close to the momentum transfer direction. For each case, the projectile momentum transfer and ejected electron energy are the same as in Fig. 1. The experimental and theoretical results are both normalized to unity at the binary peak ($\theta_b = 90^\circ$). Both experiment and theory exhibit the same characteristic shape: a pronounced binary peak and almost no recoil peak. This observation shows the value of 3D plots. In Fig. 2, the slice selecting the scattering plane reduces this extended "recoil ring" to a narrow feature of relatively small intensity. Therefore, in the 3D plot, the recoil structure is much easier to see because it systematically spans a broad range of electron emission planes. In all cases, the 3DW and 3DW-EIS approaches predict nearly the same values for the cross sections. Typically, EIS results are significantly better than the 3DW incident plane wave results, but that is obviously not the case here, which suggests that the initial-state interaction between the projectile and target is apparently not very important at least in terms of the projectile wave function.

Overall, the agreement between experiment and theory is reasonably good. The largest difference between theory and experiment is seen for the 2s state where theory underestimates the left side of the binary peak and overestimates the right side [there is also a right-side overestimation for the 2p (q = 0.3a.u., $E_e = 1.5 \text{ eV}$) case]. The best agreement is found for the 2p state with q = 0.4 a.u. and $E_e = 3 \text{ eV}$, and there is a very good agreement for the small structure appearing in the cross

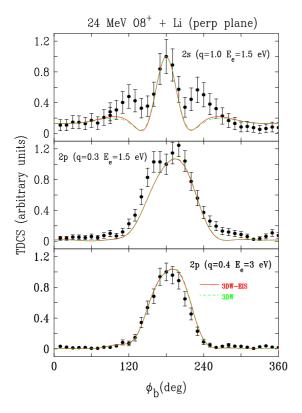


FIG. 3. Same as Fig. 2, but for the perpendicular plane. The experimental and theoretical results are normalized the same as the scattering plane.

sections for ionization in the angular region to the left of the binary peak.

The FDCSs for single ionization of lithium are displayed in Fig. 3 for the electrons emitted into the plane perpendicular to the incident beam direction, which we will call the perpendicular plane (it has also been called the azimuthal plane). The kinematic parameters for which the FDCSs are displayed and the normalization of the data are the same as for the previous figures. We use standard spherical coordinates with the azimuthal angle φ_b being measured relative to the x axis. As a result, the binary peak in the -x direction occurs for $\varphi_b = 180^\circ$. In the original paper of Hubele *et al.* [47], φ_b was measured relative to the positive y axis and the binary peak occurs for $\varphi_b = 90^\circ$. Again the overall agreement between experiment and theory is reasonably good with only small differences between experiment and theory for most of the scattering angles. The triple peak structure for the 2s state with a deep minimum results from the two symmetric wings seen in the 3D view of Fig. 1. The largest difference between experiment and theory is seen for ionization of the 2s state where the magnitude of the side wings is underestimated by theory. For the 2s case, the experimental data exhibit mirror symmetry with respect to 180° (scattering plane).

For the 2p case, there is only a single, much broader peak than in the 2s case and the mirror symmetry is broken. Both experiment and theory have peak maxima shifted to angles larger than 180° and the peak maxima are larger than unity in our normalization (i.e., the cross section for the momentum transfer in the scattering plane is not the maximum cross

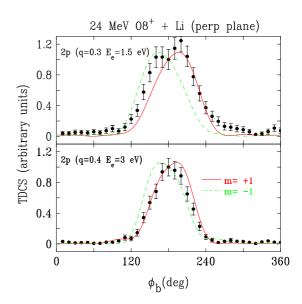


FIG. 4. Comparison of experimental and theoretical $m = \pm 1$ results for 24 MeV O⁸⁺ ionization of the 2*p* states of lithium as a function of θ_b in the scattering plane. The solid (red) lines are 3DW-EIS m = +1 results and the dashed (green) lines are the 3DW-EIS m = -1 results.

section). Again the agreement is best for the 2p case with q = 0.4 a.u. and $E_e = 3$ eV. The breaking of the mirror symmetry with respect to the scattering plane is due to the polarization of the initial target state which is called magnetic dichroism [47,60]. It is seen that both the 3DW and 3DW-EIS theories give a good description of dichroism for ionization from the initial 2p states.

There would be no dichroism if both the $2p_{+1}$ and $2p_{-1}$ substates contributed equally to the ionization cross section. For the present experiment, the relative contributions of the cross sections were 86% $2p_{+1}$, 9% $2p_0$, and 5% $2p_{-1}$ (the quantization axis is the direction of the beam axis). In Fig. 4, the individual $2p_{+1}$ and $2p_{-1}$ substate theoretical 3DW-EIS cross sections are compared with experiment for the same previous values of q and E_e . The normalized results are obtained using the 3DW-EIS approach for ionization in the perpendicular plane and shown as a function of the ejected electron angle. As has been discussed by Walters and Whelan [50], the FDCS for m = +1 is the mirror image of that for m = -1 relative to the scattering plane (i.e., $\theta_b = 180^\circ$). The m = 0 substate cross sections are symmetric about the scattering plane, but the dominant contribution of the $2p_{\pm 1}$ substate yields a cross section that is not symmetric with respect to the scattering plane, and the resulting theoretical 2p ionization cross sections show the magnetic dichroism in accordance with the experimental findings.

There have been three previously published theoretical calculations for two of the perpendicular plane cases. There were CDW-EIS results shown in the original Hubele *et al.* [47] paper; later Gulyás *et al.* [51] used the CDW-EIS method to make a detailed study of the 2*s* wings using three different models for the effective nuclear-nuclear (*NN*) interaction, and Walters and Whelan [50] reported a coupled pseudostate (CP) calculation. Figure 5 shows a comparison of the present

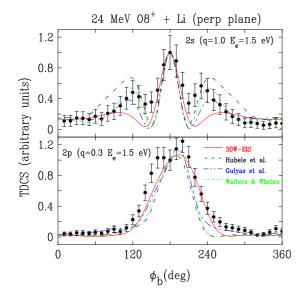


FIG. 5. Comparison of 3DW-EIS results with previous theoretical calculations. The solid (red) lines are 3DW-EIS results, dashed-dot (black) curves are the results of Hubele *et al.* [47], the long-dash, two short-dash (blue) curve are the results of Gulyás *et al.* [51], and dashed (green) curve are the results of Walters and Whelan [50].

results with the previous calculations. The Gulyás *et al.* [51] results are the ones that used the polarization approximation of Eq. (6) in that paper which gave the best agreement with experiment for the doubly differential cross sections. It is seen that the results are all pretty similar. For 2s ionization, the best overall agreement with experiment is probably the CP results of Walters and Whelan [50] although the Gulyás *et al.* [51] results are also very good. For ionization of the 2p state, the 3DW-EIS results are probably in the best overall agreement with experiment. The other theoretical approaches predict the magnitude of the 2s side peaks much better than the 3DW-EIS while the 3DW-EIS does a little better job of predicting the width of the central 2s peak and the 2p peak.

There has been a fairly extensive discussion about what causes the 2s wings. As mentioned above, Hubele et al. [47] and Walters and Whelan [50] have attributed the wings to the NN interaction and the double nodal structure of the 2s wave function. On the other hand, Gulyás et al. [51] have attributed the wings to a combination of the NN interaction and a binary interaction. In the CDW-EIS approach, the NN interaction is included through an overall phase factor containing the NN interaction. The 3DW-EIS also has the NN interaction in the eikonal phase of Eq. (7) where the screened nucleus is approximated as a particle of charge +1. Since we are treating the projectile as a wave function, the eikonal phase is part of the integral and cannot be taken out as an overall phase factor. In the present results, it is clear that the NN interaction in the eikonal phase is not responsible for the side wings since we get them using a plane wave which has no NN contributions. We can put in an approximate NN interaction by adding a nuclear potential (V_{nuc}) to the initial-state interaction V_i (the perturbation) in Eq. (4),

where V_{Pe} is the *P*-*e* interaction potential. We would note that V_{nuc} only depends on the projectile coordinate, and a single-particle potential which only depends on the projectile coordinates would not contribute to a Born-type calculation due to the orthogonality of the bound and continuum wave functions for the ejected electron. The 3DW-EIS approach does not have this orthogonality due to the ejected electron coordinates in the final-state Coulomb interaction between the ejected electron and projectile. The simplest approximation for V_{nuc} would be to treat the nucleus plus two electrons as a single proton as is done in the eikonal phase. We will call this approximation Vion. A better approximation would be to use a screened potential which has an effective charge of 3 at the origin and an asymptotic charge of unity. We have used the effective potential of Green, Sellin, and Zachor [61-63] known as the GSZ potential. The explicit form of this potential is given by

$$V_{\rm GSZ}(R) = \frac{Z_P(Z_T - n)[1 - \Omega(R)]}{R},$$
 (10)

where n + 1 is the number of electrons in the atom or ion and

$$\Omega(R) = \frac{1}{1 - \frac{\eta}{\beta} [1 - \exp(\beta R)]},\tag{11}$$

with η and β as two adjustable parameters and Z_P and Z_T the number of protons in the projectile and target core. For lithium, $\eta = 1.75$ and $\beta = 2.165$. Figure 6 compares 3DW-EIS results with no NN interaction in the perturbation to calculations using V_{ion} and V_{nuc} . It is seen that adding the NN interaction to the perturbation significantly increases the magnitude of the side wing peak. The V_{ion} results are very similar to those of Hubele *et al.* [47]. It is also seen that the width of the central peak becomes more narrow, which is also similar to the other theoretical calculations and in worse agreement with experiment. It is interesting that the presumably better screened nuclear treatment is in the worst agreement with experiment. The large sensitivity to the screening is also surprising since it would appear that it should be a small effect. For example, the

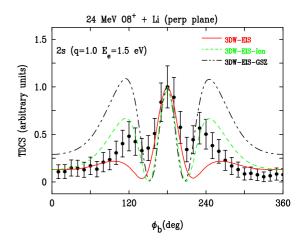


FIG. 6. Comparison of 3DW-EIS results using different approximations for the NN interaction. The solid curve (red) has no NN in the perturbation, dashed (green) uses the bare ion potential, and the long-dash, two short-dash (black) uses the GSZ screening approximation.

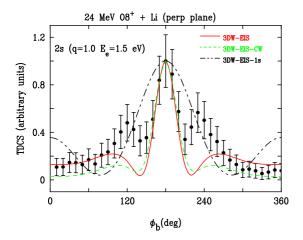


FIG. 7. Comparison of different types of 3DW-EIS calculations. The solid curve (red) is the normal, the dashed (green) uses a Coulomb wave for the ejected electron, and the long-dash, two short-dash (black) is a 1s bound state wave function instead of a 2s.

effective charge is 3.00 at the origin, 1.28 at R = 1 a.u., 1.03 at R = 2 a.u., and 1.00 at R = 3 a.u., so it deviates from unity only in a very small region of space.

We also investigated the source of the wings we get without having a NN term in the perturbation. Typically, CDW-EIS calculations use Coulomb waves for the ejected electron so we tried that. In Fig. 7, 3DW-EIS results calculated using a distorted wave for the ejected electron are compared with a completely equivalent calculation using Coulomb waves. It is seen that the side wings are greatly reduced. This calls attention to the importance of the more realistic description of the ejected electron using a screened potential. To check the effect of the double nodal wave function, we performed a completely equivalent 3DW-EIS calculation except we used a 1s wave function instead of 2s and those results are also shown in Fig. 7. It is seen that the wings are completely gone. Consequently, our results support the conclusions of Hubele et al. [47] and Walters and Whelan [50] attributing the wings to the NN interaction and the double nodal structure of the 2s wave function. However, we find that the NN interaction is important in the perturbation and not in the eikonal phase and we also find an additional enhancement to the wings from using a screened potential for the calculation of the ejected-electron wave function.

V. CONCLUSIONS

We have presented a full 3D comparison between experiment and theory for 24 MeV O^{8+} single ionization of the 2s ground state of lithium and the 2p excited state. Two theoretical approximations were examined: the three-body continuum distorted wave (3DW) and 3-body continuum distorted wave–eikonal initial state (3DW-EIS). The difference between these two calculations is that the 3DW-EIS uses an eikonal approximation for the incident projectile wave function and the 3DW uses a plane wave. In the 3D images for ionization of the 2s state, a prominent binary peak was seen and a recoil peak which had an interesting wing-type structure. In the 3D images for ionization of the 2p state, a prominent binary peak was seen and essentially no recoil peak. Normally, there is a significant difference between the 3DW and 3DW-EIS results and 3DW-EIS is in much better agreement with experiment. In this case, there is very little difference between the two approaches and both are in very good agreement with experiment. For ionization of the 2s state, the 3D images have a mirror symmetry about the scattering plane while for ionization of the 2p state, this symmetry is broken. The 2p state would have mirror symmetry if the $2p_{-1}$ and $2p_{+1}$ substates were excited in equal proportions. For the present experiment, the $2p_{\pm 1}$ sublevel is dominantly excited (quantization axis is the incident beam direction) and for this case there is a magnetic dichroism which is observed both experimentally and theoretically.

There were three previous theoretical calculations: two CDW-EIS calculations by Hubele *et al.* [47] and Gulyás *et al.* [51] and a CP calculation of Walters and Whelan [50] for the perpendicular plane only; and we compared with these results as well. We found that the Walters and Whelan and Gulyas *et al.* results gave the best agreement with experiment for the 2s state while the 3DW-EIS results were in the best overall agreement for the 2p state. The 3DW-EIS predicted the central width a little better for both the 2s and 2p states.

There has been considerable discussion about the source of the 2s wings. Hubele et al. [47] and Walters and Whelan [50] have attributed the wings to the NN interaction and the double nodal structure of the 2s wave function. Gulyás et al. [51] have attributed the wings to a combination of the NN interaction and a binary interaction. All three of those calculations use the semiclassical straight line approximation for the projectile. We use a full quantum-mechanical wave treatment for the projectile and we get wings even if the NN interaction is neglected for the incident projectile wave function. However, the wings were greatly enhanced if we added a NN interaction to the initial-state perturbation. We found that the wings go away if we neglect NN in the perturbation, use a Coulomb wave for the ejected electron, and use a 1s wave function for the ejected electron. Consequently, while our results support the wings resulting from the NN interaction and the double nodal structure of the 2s wave function, we find an additional enhancement from using a screened potential for the calculation of the ejected-electron wave function.

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