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Modeling the Effect of APC Truncation on Destruction Complex Function in Colorectal Cancer Cells

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Abstract

In colorectal cancer cells, APC, a tumor suppressor protein, is commonly expressed in truncated form. Truncation of APC is believed to disrupt degradation of β -catenin, which is regulated by a multiprotein complex called the destruction complex. The destruction complex comprises APC, Axin, β -catenin, serine/threonine kinases, and other proteins. The kinases CK1 α and GSK-3 β , which are recruited by Axin, mediate phosphorylation of β -catenin, which initiates its ubiquitination and proteosomal degradation. The mechanism of regulation of β -catenin degradation by the destruction complex and the role of truncation of APC in colorectal cancer are not entirely understood. Through formulation and analysis of a rule-based computational model, we investigated the regulation of β -catenin phosphorylation and degradation by APC and the effect of APC truncation on function of the destruction complex. The model integrates available mechanistic knowledge about site-specific interactions and phosphorylation of destruction complex components and is consistent with an array of published data. We find that the phosphorylated truncated form of APC can outcompete Axin for binding to β -catenin, provided that Axin is limiting, and thereby sequester β -catenin away from Axin and the Axin-recruited kinases CK1 α and GSK-3 β . Full-length APC also competes with Axin for binding to β -catenin; however, full-length APC is able, through its SAMP repeats, which bind Axin and which are missing in truncated oncogenic forms of APC, to bring β -catenin into indirect association with Axin and Axin-recruited kinases. Because our model indicates that the positive effects of truncated APC on β -catenin levels depend on phosphorylation of APC, at the first 20-amino acid repeat, and because phosphorylation of this site is mediated by CK1 ϵ , we suggest that CK1 ϵ is a potential target for therapeutic intervention in colorectal cancer. Specific inhibition of CK1 ϵ is predicted to limit binding of β -catenin to truncated APC and thereby to reverse the effect of APC truncation.

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Introduction

β -catenin (CTNNB1) is a key signaling protein in the Wnt/ β -catenin pathway [1,2], a regulator of cadherin cell adhesion molecules [3], and a regulator of the Tcf and Lef family of transcription factors [4–7]. In mesenchymal cells, β -catenin levels increase when a Wnt ligand binds a cell-surface Frizzled (Fz)-family receptor. Activation of the Wnt/ β -catenin pathway (transiently) inhibits proteasome-mediated degradation of β -catenin. Wnt binding also has other important effects on β -catenin, including regulation of phosphorylation state and redistribution of β -catenin within subcellular compartments. In colorectal cancer cells, normal control of β -catenin degradation is disrupted, resulting in elevated levels of β -catenin.

Cellular degradation of β -catenin is regulated by (in our view) oligomeric protein complexes, which have diverse compositions but common features; these complexes are often collectively referred to as the β -catenin destruction complex [8–10]. The destruction complex, which characteristically contains β -catenin

and two scaffold proteins, Axin (axis inhibition protein, AXIN1) and APC (adenomatous polyposis coli protein), mediates phosphorylation of β -catenin by recruiting GSK-3 β (glycogen synthetase kinase-3 β , GSK3B) and CK1 α (casein kinase I α , CSNK1A1) [11–15]. These kinases, upon binding Axin, catalyze phosphorylation of β -catenin on specific serine and threonine residues. Phosphorylation of Ser-45 by CK1 α and subsequent phosphorylation of Ser-33, Ser-37, and Thr-41 by GSK-3 β initiates ubiquitination and proteasome-mediated degradation of β -catenin [12–15]. The destruction complex also recruits PP2A, a multimeric protein phosphatase, which opposes the action of kinases. It has been suggested that activation of Wnt/ β -catenin signaling destabilizes the destruction complex by sequestering Axin in complexes with activated Fz receptors [16–18]. However, details about the early events in Wnt/ β -catenin signaling are still emerging [19,20]. In colorectal cancer cells, the destruction complex member APC is often truncated [21]. An important effect of APC truncation is believed to be a perturbation of the interactions amongst proteins comprising the destruction complex

Author Summary

We asked the question, how can the effects of APC truncation, a very common mutation in colorectal cancer, be understood and reversed? We addressed this question by formulating a computational model for destruction complex function that incorporates site-specific details about protein-protein interactions and protein phosphorylation and examined the differences in predicted behaviors when APC is full length, as in normal cells, and truncated, as in colorectal cancer cells. Our model offers an explanation for how and why destruction complex function is altered by APC truncation. The model indicates that phosphorylation of the first 20-amino acid repeat in APC (which is usually the only 20-amino acid repeat that remains in truncated forms of APC) together with the absence of SAMP repeats (missing entirely because of truncation) allows truncated APC to act as a diversion sink. In other words, phosphorylated APC can outcompete Axin for binding to β -catenin, provided Axin is limiting, and thereby prevent β -catenin from associating with Axin and the Axin-associated kinases CK1 α and GSK-3 β , which initiate phosphorylation-dependent degradation of β -catenin. Thus, the model identifies inhibition of APC phosphorylation, which is mediated by CK1 ϵ , as a potential means by which the oncogenic effect of APC truncation could be reversed.

that alters regulation of β -catenin degradation, perhaps by destabilizing the destruction complex in a way similar to the destabilization brought about by Wnt signaling.

The interactions responsible for assembly of the destruction complex are complex and are mediated by multiple functional sites within the member proteins of the destruction complex. The characteristic core of the destruction complex can be viewed as a ternary complex that forms through interactions of APC, Axin, and β -catenin. β -catenin contains twelve ARM (Armadillo) repeats, allowing it to bind both APC and Axin. In particular, ARM repeats 3 and 4 constitutively bind a central region of Axin [22,23] as well as a phosphorylated 20-amino acid (20-aa) repeat region of APC [24,25]. There are total of seven 20-aa repeats in this region. β -catenin ARM repeats 5–9 constitutively bind three 15-amino acid (15-aa) repeats in the N-terminal region of APC [26]. APC contains three SAMP (serine-alanine-methionine-proline) repeats, which bind the RGS (regulator of G protein signaling) domain of Axin [27]. These interactions connect the three core proteins of the destruction complex (APC, Axin, and β -catenin) and enable each protein to bind the other two core proteins, possibly within a closed/cyclic ternary complex. A cyclic complex would presumably be highly stable, because dissociation of such a complex would require the sequential break up of two protein-protein interactions.

Stability of the destruction complex may be important for its function as a platform for phosphorylation of β -catenin, and other proteins. The destruction complex mediates phosphorylation of β -catenin by allowing Axin to colocalize the kinases GSK-3 β and CK1 α with their substrate β -catenin. Axin contains binding sites for both GSK-3 β [11,28] and CK1 α [12,29]. Interestingly, the destruction complex is also thought to mediate phosphorylation of APC by colocalizing another kinase, CK1 ϵ (CSNK1E), with APC [30], although it is not known which protein in the destruction complex recruits CK1 ϵ . CK1 ϵ and GSK-3 β together mediate phosphorylation at the 20-aa repeat region of APC [30]. Recall that this region in APC, when

phosphorylated, mediates interaction with a site in β -catenin that also interacts with Axin [22–25]. Thus, phosphorylated APC and Axin compete for binding to β -catenin. The outcome of this competition is perhaps dependent on stability of the destruction complex.

Much of what we know about the functional effects of APC truncation has come from studies of a human colon adenocarcinoma cell line (SW480). SW480 cells express a truncated form of APC termed APC1338, which contains only the first 1,338 amino acids of the full-length protein [9,31]. APC1338 contains all three 15-aa repeats and the first 20-aa repeat, but is devoid of the remaining six 20-aa repeats and the SAMP repeats, which bind Axin [9,31]. Therefore, a model can be conceptualized wherein assembly of the functional destruction complex cannot be completed in the absence of interaction between APC1338 and Axin, leading to decreased phosphorylation, ubiquitination, and degradation of β -catenin [2]. However, an absence of SAMP repeats in APC does not prevent direct binding of Axin to β -catenin [22,23], and there are some uncertainties about the validity of this model [19] because reports from different laboratories have shown that expression of recombinant APC can either promote degradation of β -catenin or have no or little effect, depending on cell type and whether APC is expressed transiently or stably [31–34].

As discussed above, APC plays an important role in destruction complex function. However, APC is a multifunctional protein, subject to numerous post-translational modifications. It is believed to play a role in regulating not only phosphorylation and ubiquitination of β -catenin but also localization of β -catenin. There are several pools of β -catenin: membrane-associated (e.g., complexed with E-cadherin), cytosolic (free, α -catenin bound and Tcf bound), and nuclear. Other components of the destruction complex are also multifunctional proteins, which can be found in distinct subcellular locations and states. For example, Axin, through self-polymerization mediated by its DIX (dishevelled and axin) domain [35], localizes to cytoplasmic puncta. We will not consider these complexities, but they are mentioned at this point to caution the reader about the limitations of our study.

Here, our focus will be on APC regulation of β -catenin phosphorylation within an idealized destruction complex, taken to comprise a ternary complex of APC, Axin, and β -catenin with 1:1:1 stoichiometry. We will consider the site-specific details of the interactions amongst these proteins, because these details are relevant for understanding how the interactions of APC, Axin, and β -catenin are perturbed by an absence of SAMP repeats in truncated APC (APC1338). We also consider, with less mechanistic resolution, proteins that mediate phosphorylation and dephosphorylation of APC and β -catenin and degradation of β -catenin. The set of proteins of interest are considered in isolation. Thus, for example, we do not consider β -catenin interaction with E-cadherin, or the effects of Wnt. We also do not consider Axin puncta or the DIX domain in Axin. Axin puncta play a role in β -catenin degradation but are not required for phosphorylation of β -catenin [36].

To investigate the roles of APC and its oncogenic truncated forms in destruction complex function, we formulated a computational model for regulation of β -catenin phosphorylation and degradation using local rules to represent the protein-protein interactions of interest [37–39]. This rule-based approach, ideal for modeling the chemical kinetics of biomolecular interaction networks, allowed us to consider the mechanistic details of protein-protein interactions at the resolution level of functional sites within the proteins of interest. These mechanistic details are complex, as summarized above, and arguably beyond our ability to compre-

hend without reasoning aids, such the model considered here. Using this model, we interrogated system behavior, which emerges from the states and state changes of protein sites, with the goal of elucidating the distinctive mechanisms by which APC and APC1338 regulate the rate of β -catenin destruction in normal and SW480 colorectal cancer cells. We also used our model to investigate the functional significance of intracomplex interactions among APC, Axin, and β -catenin, which have the potential to produce a highly stable cyclic ternary complex.

Although APC is a characteristic component of the destruction complex and thought to be important for degradation of β -catenin [31–34], our analyses suggest that APC does not promote degradation of β -catenin in a normal cell when overexpressed. However, we do predict that expression of recombinant full-length APC in SW480 cells promotes β -catenin degradation, as seen in several studies [31–34]. These results are obtained because, according to our model, phosphorylated APC1338 in SW480 cells competes with Axin for β -catenin. APC1338-mediated separation of β -catenin from Axin reduces phosphorylation of β -catenin by Axin-recruited kinases, and reduced phosphorylation of β -catenin decreases its rate of degradation. In contrast, in normal cells, binding of phosphorylated full-length APC to β -catenin, in competition with Axin, is not functionally equivalent because Axin can still colocalize with β -catenin through indirect association via the SAMP repeats in APC, which are missing in APC1338. Because of these results and because CK1 ϵ is responsible for phosphorylation of APC (but not β -catenin), we identify CK1 ϵ as a potential target for therapeutic intervention in colorectal cancer. Inhibition of CK1 ϵ is predicted to limit sequestration of β -catenin away from Axin and Axin-associated kinases and thereby to lower β -catenin levels in cancer cells expressing truncated APC.

Results

To investigate how the function of the β -catenin destruction complex changes when APC is mutated, especially as a result of a typical C-terminal truncation that removes the SAMP repeats and all but the first of the 20-aa repeats, we formulated a model (as described below) for full-length APC interactions with other components of the destruction complex. We then used this model and variants corresponding to different mutated forms of APC to predict how β -catenin levels and other readouts of system behavior depend on various parameters, such as the abundance of APC or truncated APC. Because APC contains multiple functional components or sites and we are interested in forms of APC containing different subsets of these sites, we formulated a model that tracks the chemical kinetics of the protein-protein interactions of interest with site-specific/structural resolution. This was accomplished by leveraging the rule-based modeling approach [37,40], in which local rules are used to represent biomolecular interactions and their consequences. Modeling with site-specific resolution is difficult with traditional modeling approaches, such as that of ordinary differential equations (ODEs), because of combinatorial complexity [41], which arises from multisite phosphorylation, multivalent binding, and other common aspects of biomolecular interactions involved in cellular regulation. Combinatorial complexity is a motivating factor for the use of rule-based modeling here.

Model

We developed a model for APC, Axin, and β -catenin interactions and destruction complex function using the rule-

based modeling framework of BioNetGen [37–39] (see Materials and Methods). We considered a base model, corresponding to a normal cell with full-length APC, and several variant forms of the base model. The base model is illustrated in Figs. 1 and 2. The model is annotated in Text S1 (Supporting Information). Executable BioNetGen input files are provided in the Supporting Information for the base model (Text S2) and eight variant forms of the base model (Text S3 through Text S10).

In the base model, both explicit and implicit interactions are considered. We explicitly consider the interactions of five signaling proteins (and their isoforms presumed to be functionally equivalent): APC, Axin, β -catenin, CK1 α , and GSK-3 β . We implicitly consider the interactions of CK1 ϵ , PP2A, other phosphatases, and the proteins responsible for ubiquitination and proteosomal degradation of β -catenin. In Fig. 2, proteins and their interactions are represented with site-specific/structural resolution using the conventions of Chylek et al. [42]. Briefly, proteins and their functional components are represented by nested boxes. Components excluded from consideration (e.g., the DIX domain of Axin) are not illustrated in Fig. 2. Arrows connecting boxes represent interactions. It should be noted that the visual elements of Fig. 2 correspond to the formal elements of our model [42]: boxes correspond to molecule types and arrows correspond to rules for interactions (Text S1). Each interaction included in the model is discussed below. The technical details of how these interactions are modeled/represented using rules are explained in Text S1. See also the Materials and Methods section.

Arrow 1 in Fig. 2 represents reversible binding of β -catenin ARM repeats 5–9 to the 15-aa repeats of APC [22,26]. In the model, ARM repeats 5–9 are considered to comprise a single binding site. Likewise, the three 15-aa repeats in APC are considered to comprise a single binding site.

Arrow 2 represents reversible binding of β -catenin ARM repeats 3 and 4 to phosphorylated APC 20-aa repeats [22]. In the model, ARM repeats 3 and 4 are considered to comprise a single binding site. The seven 20-aa repeats of APC are taken to function as two distinct binding sites, with binding activity of one site considered to be mutually exclusive with binding activity of the other site. The first site (labeled 1) corresponds to the first 20-aa repeat and the second site (labeled 3) corresponds to the third 20-aa repeat. We consider binding of APC to β -catenin to be mediated by the phosphorylated first repeat when the protein is APC1338 (or a comparable truncated form of APC), and predominantly (exclusively in the model as a simplification) by the phosphorylated third repeat if the protein is full-length APC. This distinction is made because APC1338 contains only the first 20-aa repeat, whereas full-length APC contains all seven 20-aa repeats. Binding of full-length APC to β -catenin is mediated primarily by the phosphorylated third 20-aa repeat [25] because the phosphorylated third repeat binds with 100- to 1000-fold higher affinity than that of any of the other phosphorylated 20-aa repeats [25]. We take the stoichiometry of a β -catenin-APC complex to be 1:1.

Arrow 3 represents reversible binding of β -catenin to Axin. ARM repeats 3 and 4 of β -catenin bind a central region of Axin [22,23]. As noted before, ARM repeats 3 and 4 also bind the phosphorylated 20-aa repeat region of APC (Arrow 2). Thus, ARM repeats 3 and 4 represent a β -catenin binding site recognized by both APC and Axin.

Arrow 4 represents reversible binding of APC to Axin. The three SAMP repeats of APC bind the RGS domain of Axin [27,43]. In the model, as a simplification, the SAMP repeats are considered to comprise a single binding site. Thus, we take the stoichiometry of an APC-Axin complex to be 1:1.

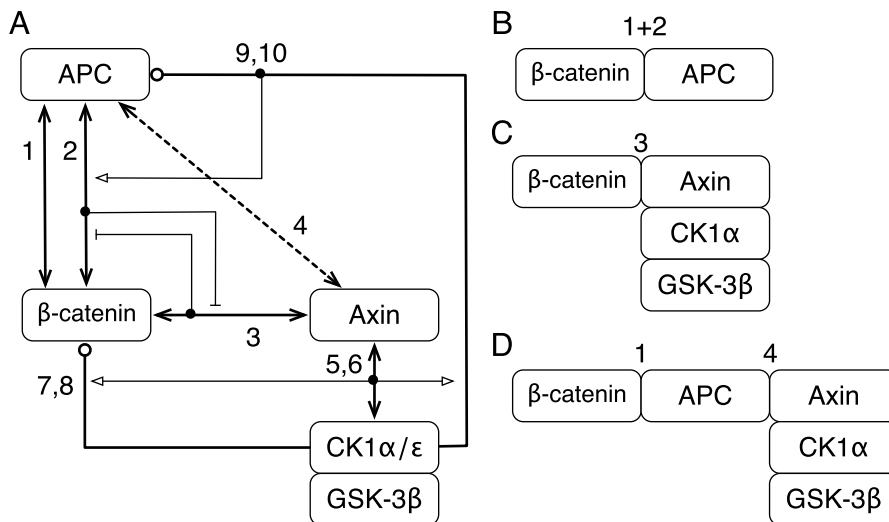


Figure 1. Overview of the signaling proteins and interactions considered in the model. Panel A is a simplified version of Fig. 2, which follows and goes beyond the diagram shown here by illustrating the functional components of proteins responsible for interactions. Selected protein complexes considered in the model are illustrated in Panels B–D. (A) Proteins are represented by boxes. In the model, five proteins, β -catenin, APC, Axin, GSK-3 β , and CK1 α , are considered explicitly, whereas CK1 ϵ , PP2A (not shown), and other proteins are considered implicitly. CK1 ϵ , which mediates phosphorylation of APC, and PP2A, which mediates dephosphorylation of APC, are assumed to be constitutively associated with Axin. In the model, their activities are engaged when Axin is in complex with APC. Interactions included in the model are represented by arrows; numbering of arrows is the same as in Fig. 2. The arrows labeled 1–6 represent reversible direct binding interactions. The arrows labeled 7–10 represent catalytic (phosphorylation) interactions (and enzyme-substrate relationships). All phosphorylation events are taken to be reversed by phosphatases. The interaction represented by Arrow 1 is constitutive. The interaction represented by Arrow 2 depends on sequential phosphorylation of APC by CK1 ϵ and GSK-3 β (Arrows 9 and 10). The interactions represented by Arrows 2 and 3 are mutually exclusive, because they involve the same binding site in β -catenin, i.e., Axin and APC compete for binding to this site. The interaction between APC and Axin represented by Arrow 4 is missing for typical truncated forms of APC (i.e., forms of APC, such as APC1338, missing SAMP repeats). Arrows 5 and 6 represent recruitment of GSK-3 β and CK1 α to Axin. Arrows 7–10 represent phosphorylation reactions mediated by Axin-associated kinases. (B) A binary complex of APC and β -catenin connected through two distinct protein-protein interfaces. The interactions represented by Arrows 1 and 2 are allowed to occur simultaneously. (C) A complex wherein β -catenin is directly bound to Axin via the interaction represented by Arrow 3. Recall that this interaction cannot occur if β -catenin is bound to APC via the interaction represented by Arrow 2. (D) A complex containing a linear (vs. cyclic) ternary complex of APC, Axin, and β -catenin. This linear complex is allowed to close and form a cyclic complex via the interaction represented by Arrow 3. Note that the complex depicted here cannot form when APC is truncated such that the interaction represented by Arrow 4 is missing. The model is further described in Fig. 2 and Text S1. doi:10.1371/journal.pcbi.1003217.g001

Arrows 5 and 6 represent reversible binding of GSK-3 β and CK1 α to Axin, respectively. GSK-3 β binds the GSK3 interaction domain (GID) of Axin [11,28,44]. CK1 α binds a central region of Axin [29], which is distinct from the binding sites in Axin recognized by other binding partners. In the model, the binding of CK1 α , β -catenin and GSK-3 β to Axin is taken to be non-competitive and non-cooperative.

Arrows 7 and 8 represent phosphorylation of β -catenin by Axin-bound CK1 α and GSK-3 β , respectively. β -catenin phosphorylation takes place in a processive manner [12,13]. CK1 α first phosphorylates Ser-45 (labeled as S45 in Fig. 1), and GSK-3 β then phosphorylates Ser-33, Ser-37, and Thr-41. In the model, as a simplification, the latter three sites are lumped together (labeled as S33/S37 in Fig. 2). We model the phosphorylation reactions as processes with first-order kinetics that occur only when kinases and substrates are colocalized within a complex. In the model, phosphorylation at S45 occurs when β -catenin is colocalized with Axin-associated CK1 α . Phosphorylation at S33/S37 occurs when β -catenin is phosphorylated at S45 and colocalized with Axin-associated GSK-3 β [12,13]. We do not consider phosphorylation of β -catenin outside the context of the destruction complex.

Arrows 9 and 10 represent phosphorylation of APC 20-aa repeats by CK1 ϵ and GSK-3 β [30,45]. Both CK1 ϵ and GSK-3 β are required for phosphorylation of APC [30]. In Fig. 2, CK1 ϵ is shown for illustration purposes only. In the model,

we implicitly consider CK1 ϵ because it is not known which protein is responsible for colocalizing CK1 ϵ with APC. Phosphorylation of APC is taken to occur through a process with first-order kinetics when APC and GSK-3 β are colocalized via Axin. Thus, we assume that CK1 ϵ is colocalized with APC in proportion to the extent to which GSK-3 β is colocalized with APC via Axin. This assumption is equivalent to assuming that CK1 ϵ associates non-competitively with Axin (or directly with GSK-3 β).

We model dephosphorylation reactions as first-order processes (without explicit consideration of phosphatases). We allow dephosphorylation to occur if a site is exposed, i.e., not occupied and shielded by a binding partner. In the model, both phosphorylation sites of β -catenin (i.e., S45 and S33/S37) are dephosphorylated according to the same rate law. In other words, the same first-order dephosphorylation rate constant is used for both sites. We allow the 20-aa repeats in APC to be dephosphorylated only if APC is in complex with Axin because Axin recruits PP2A, a phosphatase that mediates dephosphorylation of APC [46].

An important feature of the model is intracomplex binding of APC, Axin, and β -catenin. In Fig. 2, Arrows 1–4 each represents two distinct types of binding reactions: intermolecular binding, and intracomplex binding. The former type of binding reaction occurs when the reacting sites are freely diffusing, i.e., not tethered. The latter type of binding reaction occurs when the reacting sites are already in a complex together, i.e., tethered and

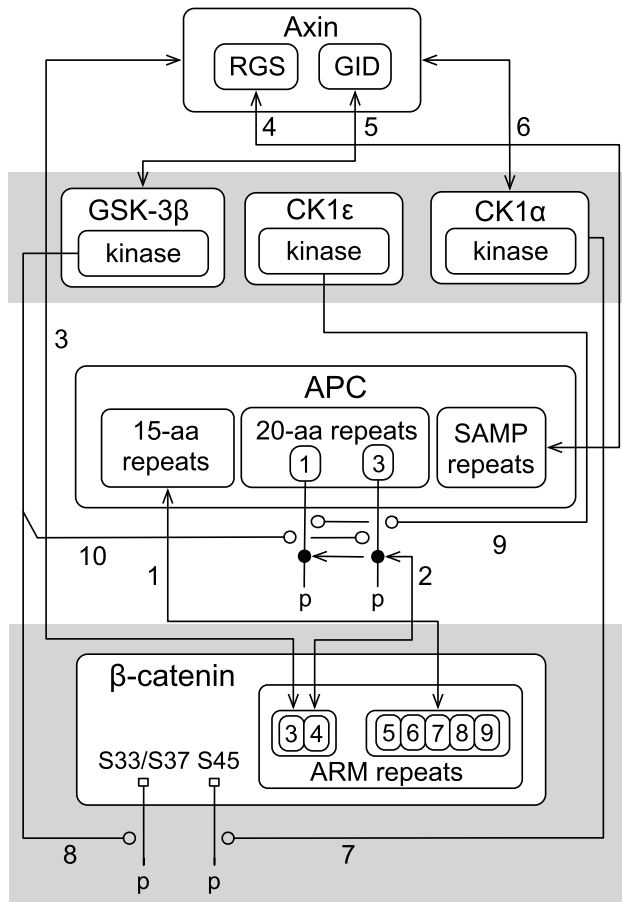


Figure 2. Site-specific details of the proteins and interactions considered in the model. Proteins, interactions, and the functional components that mediate interactions are represented according to the conventions of Chylek et al. [42]. The numbering of arrows is the same as in Fig. 1. The double-headed lines represent reversible binding interactions. The lines ending with an open circle represent enzyme-substrate relationships and point to sites of phosphorylation. In the model, β -catenin sites Ser-33, Ser-37, and Thr-41, which are GSK-3 β substrates, are lumped together as a single site labeled S33/37. β -catenin site Ser-45, which is a CK1 α substrate, is labeled S45. In the model, the seven 20-aa repeats of APC are lumped into two distinct sites labeled 1 and 3. For further information about the model, see Materials and Methods. A complete and executable specification of the model is provided in the Supporting Information as a plain-text BioNetGen input file (Text S2). Note that there is a correspondence between the arrows shown here and the rules of the model (Text S1). Model parameter values are summarized in Table 1. doi:10.1371/journal.pcbi.1003217.g002

co-confined to a small subvolume of the cytoplasm. An intracomplex reaction can be marked by a high apparent affinity because of the high local concentrations of the tethered binding partners [47]. In the model, these reactions lead to complex stabilization. We account for the high local concentration effect on an intracomplex reaction by multiplying the corresponding forward rate constant by an enhancement factor χ . For instance, if β -catenin and APC are already connected via Axin, then the effective forward rate constant for the reaction represented by Arrow 1 would be χk_f , where k_f is the intrinsic forward rate constant when the proteins are not tethered together.

It should be noted that in the model β -catenin and APC can form a binary complex held together by two-point attachment i.e., β -catenin and APC can be held together through simultaneous

interaction between β -catenin ARM repeats 3 and 4 and APC 20-aa repeats (Arrow 1) and interaction between β -catenin ARM repeats 5–9 and APC 15-aa repeats (Arrow 2). The intracomplex reactions between APC and β -catenin are allowed to occur outside the context of a completely assembled destruction complex.

In the model, except for β -catenin, the total concentrations of signaling proteins are taken to be conserved (i.e., constant). β -catenin is produced in a process with zeroth-order kinetics and degraded in either a slow or fast process with first-order kinetics. When S33/S37 is not phosphorylated, β -catenin is degraded at a slow rate, regardless of its bound state. When S33/S37 is phosphorylated, β -catenin is degraded at a fast rate, again regardless of its bound state. Thus, we allow β -catenin to be degraded, through a slow or fast process, independently of whether it is free or bound. We assume that β -catenin releases any binding partner(s) upon degradation.

The model has 27 independent parameters, including five protein concentrations and 14 binding constants (Table 1). Parameter values were specified as described in Materials and Methods. A local sensitivity analysis indicates that model behavior is not particularly sensitive to any individual parameter value (Table S1).

Effects of APC mutation on β -catenin expression

Using the estimated parameter values summarized in Table 1 (see Materials and Methods), which were selected in part to allow the model to reproduce certain system behaviors (Figs. S1 and S2), we tested whether the model is able to predict the effects of transfection of SW480 cells with different truncated forms of APC. Munemitsu et al. [31] systematically transfected SW480 cells with various forms of APC. These experiments were designed to understand the effects of deletion of different functional components of APC on β -catenin levels in SW480 cells, which almost exclusively express APC1338 instead of the full-length protein [31,48].

Munemitsu et al. [31] transfected SW480 cells with full-length APC or one of 11 different truncated forms of APC (illustrated in Fig. 3). In our model, full-length APC and the 11 truncated forms of the protein can be grouped into six distinctive classes, Classes A–F (Fig. 3). The proteins in each class are functionally equivalent based on the components and interactions of APC included in the model (Fig. 2). For example, Munemitsu et al. [31] considered three forms of APC each containing the following components: 1) a partial or complete set of the 15-aa repeats, 2) all of the 20-aa repeats, and 3) the SAMP repeats of APC. These are the functional sites that we consider to be included in full-length APC (Fig. 2). Therefore, we will use APC-A to represent all three proteins, as we take these forms of APC to be functionally equivalent. Similarly, we will use APC-B to represent two other proteins, which both contain the 15-aa repeats and only the first 20-aa repeat. We take these two forms to be equivalent to APC1338, the truncated protein in SW480 cells. Henceforth, we will use APC-A, APC-B, APC-C, APC-D, APC-E and APC-F to refer to the proteins in Classes A (e.g., full-length APC), B (e.g., APC1338), C, D, E and F (Fig. 3).

Using the model, we investigated the effects of transfection of SW480 cells with APC-A through APC-F. In the model, the endogenous concentration of APC1338 in an SW480 cell is set at 100 nM. Similarly, the endogenous concentration of full-length APC in a normal cell is set at 100 nM (Table 1). Because APC1338 does not contain the third 20-aa repeat, nor SAMP repeats, Axin interactions associated with these sites (Fig. 2) are absent in an SW480 cell. In contrast, in a normal cell, all

Table 1. Model parameter values¹.

Parameters	Comments
$BCAT_{tot} = 35 \text{ nM}$ (1.1×10^4 copies/cell)	β -catenin concentration [53,59]
$APC_{tot} = 100 \text{ nM}$ (3.2×10^4 copies/cell)	APC concentration [53,59]
$AXIN_{tot} = 10 \text{ nM}$ (3.2×10^3 copies/cell)	Axin concentration [59]
$GSK_{tot} = 100 \text{ nM}$ (3.2×10^4 copies/cell)	GSK-3 β concentration [53,59]
$CK1\alpha_{tot} = 100 \text{ nM}$ (3.2×10^4 copies/cell)	CK1 α concentration (assumed)
β -catenin ARM repeats 5–9 binding to the APC 15-aa repeat region	
$K_{D1,bap} = 273 \text{ nM}$	Equilibrium dissociation constant [43]
$k_{r1,bap} = K_{D1,bap} \times k_{f1,bap} = 0.273 \text{ s}^{-1}$	Dissociation rate constant ²
β -catenin ARM repeats 3 and 4 binding to the phosphorylated APC 20-aa repeat	
$K_{D2,bap} = 1.5 \text{ nM}$	Equilibrium dissociation constant [25]
$k_{r2,bap} = K_{D2,bap} \times k_{f2,bap} = 0.0015 \text{ s}^{-1}$	Dissociation rate constant ²
β -catenin ARM repeats 3 and 4 binding to the phosphorylated APC1338 20-aa repeat	
$K_{D3,bap} = 85 \text{ nM}$	Equilibrium dissociation constant [25]
$k_{r3,bap} = K_{D3,bap} \times k_{f3,bap} = 0.085 \text{ s}^{-1}$	Dissociation rate constant ²
β -catenin ARM repeats 3 and 4 binding to Axin	
$K_{D,ba} = 227 \text{ nM}$	Equilibrium dissociation constant [43]
$k_{r,ba} = K_{D,ba} \times k_{f,ba} = 0.227 \text{ s}^{-1}$	Dissociation rate constant ²
Axin binding to the APC SAMP repeats	
$K_{D,apa} = 100 \text{ nM}$	Equilibrium dissociation constant (assumed)
$k_{r,apa} = K_{D,apa} \times k_{f,apa} = 0.1 \text{ s}^{-1}$	Dissociation rate constant ²
GSK-3 β binding to Axin	
$K_{D,ga} = 65 \text{ nM}$	Equilibrium dissociation constant [68]
$k_{r,ga} = K_{D,ga} \times k_{f,ga} = 0.065 \text{ s}^{-1}$	Dissociation rate constant ²
CK1 α binding to Axin	
$K_{D,ca} = 100 \text{ nM}$	Equilibrium dissociation constant (assumed)
$k_{r,ca} = K_{D,ca} \times k_{f,ca} = 0.1 \text{ s}^{-1}$	Dissociation rate constant ²
β -catenin phosphorylation and dephosphorylation (at both S33/S37 and S45 sites)	
$k_{p,b} = 0.05 \text{ s}^{-1}$	β -catenin phosphorylation rate constant
$k_{-p,b} = 0.0012 \text{ s}^{-1}$	β -catenin dephosphorylation rate constant ³
APC/APC1338 phosphorylation and dephosphorylation at the 20-aa repeat region (site 1 or 3)	
$k_p = 0.05 \text{ s}^{-1}$	APC phosphorylation rate constant ⁴
$k_{-p} = 0.05 \text{ s}^{-1}$	APC dephosphorylation rate constant ⁴
β -catenin synthesis and degradation	
$k_{d,b1} = 4.28 \times 10^{-5} \text{ s}^{-1}$	Slow degradation rate constant ⁴
$k_{d,b2} = 4.28 \times 10^{-3} \text{ s}^{-1}$	Fast degradation rate constant ⁴
$k_{s,b} = 0.013 \times 10^{-3} \text{ nM s}^{-1}$ (4.0 molecules/s)	Synthesis rate constant ⁴
Enhancement factor	
$\chi = 10^4 \text{ nM}$	Enhancement factor for intracomplex binding ⁴

¹Unit conversions are based on a cell cytoplasmic volume of 10^{-12} L [59].

²For each binding reaction, the association rate constant (k_f) is assumed to be $10^{-3} \text{ nM}^{-1} \text{ s}^{-1}$.

³The half-life $t_{1/2}$ of β -catenin phosphorylation is approximately 10 min [74].

⁴The selected parameter values allow the model to reproduce a number of experimental observations, including 1) the steady-state β -catenin level, 2) the half-lives of β -catenin and S33/S37-mutated β -catenin (Fig. S1), and 3) the kinetics of dephosphorylation of β -catenin at S33/S37 and S45 upon treatment with LiCl (Fig. S2). See Materials and Methods for more details.

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interactions considered in the model are active, except for the low-affinity interaction between APC and β -catenin involving the phosphorylated first 20-aa repeat of APC and ARM repeats 3 and 4 of β -catenin. This low-affinity interaction is omitted when considering a normal cell as a simplification (see Materials and

Methods). In the model, when a representative of one of the six classes of APC is introduced into an SW480 cell, any novel interactions associated with the functional components of the transfected protein become active. For example, when APC-A is introduced, interactions associated with the third 20-aa repeat and

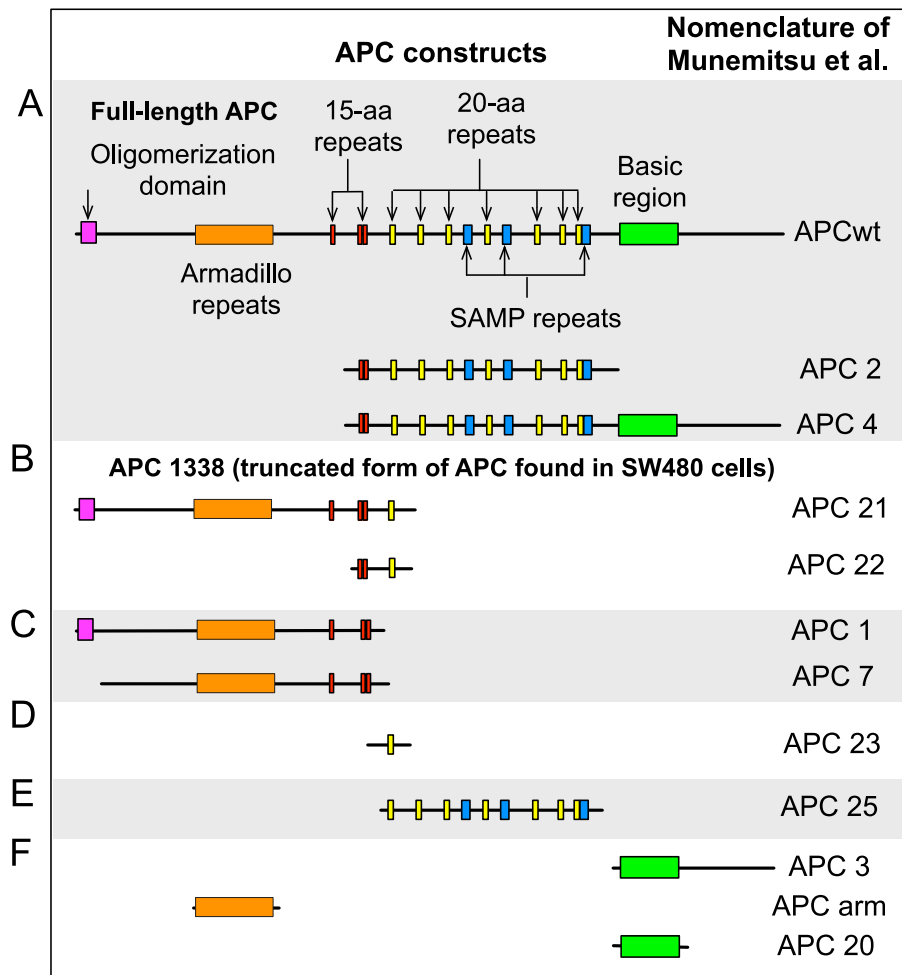


Figure 3. Summary of APC constructs considered in simulated transfections and in the experimental study of Munemitsu et al. [31]. The 12 constructs used by Munemitsu et al. [31] are divided into six classes based on their structures. Proteins within the same class are functionally equivalent according to our model. A representative of Class A (APC-A) contains all three protein binding sites considered in the model for full-length APC. This class is regarded as equivalent to full-length APC. A representative of Class B (APC-B) contains 15-aa repeats and the first 20-aa repeat. This class is regarded as equivalent to APC1338, the truncated form of APC found in SW480 cells. A representative of Class C (APC-C) corresponds to a fragment that contains only the 15-aa repeats. A representative of Class D (APC-D) corresponds to a fragment that contains only the first 20-aa repeat. A representative of Class E (APC-E) corresponds to a fragment that contains the 20-aa and SAMP repeats. A representative of Class F (APC-F) corresponds to a nonfunctional fragment that contains none of the three APC sites included in the model.
 doi:10.1371/journal.pcbi.1003217.g003

the SAMP repeats (Fig. 2) become active. These interactions are normally missing in an SW480 cell. We assume that simulated transfections each introduce 100 nM of new protein into a cell. Thus, simulated transfection of SW480 with a particular form of APC implies that the cell contains 100 nM of a protein belonging to that form in addition to the 100 nM of the endogenous form of APC (APC1338). (We systematically investigate how behavior depends on the amount of transfected protein below.)

In Fig. 4, we compare the model-predicted changes in β -catenin levels in SW480 cells after simulated transfection of different forms of APC against the findings of Munemitsu et al. [31] (Fig. 4). The model is able to recapitulate the qualitative increase or decrease in β -catenin level observed after transfection of each class of protein. Consistent with the findings of Munemitsu et al. [31], the model predicts that only transfection of APC-A and APC-E leads to a decrease in β -catenin level, whereas the other four classes of APC have the opposite or no effect on β -catenin level (Fig. 4) [31]. It should be noted that the

results in Fig. 4 were obtained without adjustment or fitting of parameter values.

Role of full-length APC in β -catenin degradation

The results of Munemitsu et al. [31] suggest that exogenous full-length APC downregulates β -catenin by promoting β -catenin degradation in SW480 cells. Similar results for SW480 cells have been obtained in other studies [33,34]. However, transfection of different cell types have yielded different results [33]. Using our model, we investigated whether overexpression of APC can generally be expected to increase the rate of β -catenin degradation in all cell types, or if the effect may be specific to SW480 cells only (Fig. 5).

Fig. 5A shows the model-predicted β -catenin level in a normal cell as a function of APC level. A normal cell in the model is taken to have endogenous full-length APC at a cytosolic concentration of 100 nM (Table 1). Fig. 5A illustrates the predicted effects of added APC. Fig. 5A shows that increased abundance of APC does not promote β -catenin degradation, rather it has a concentra-

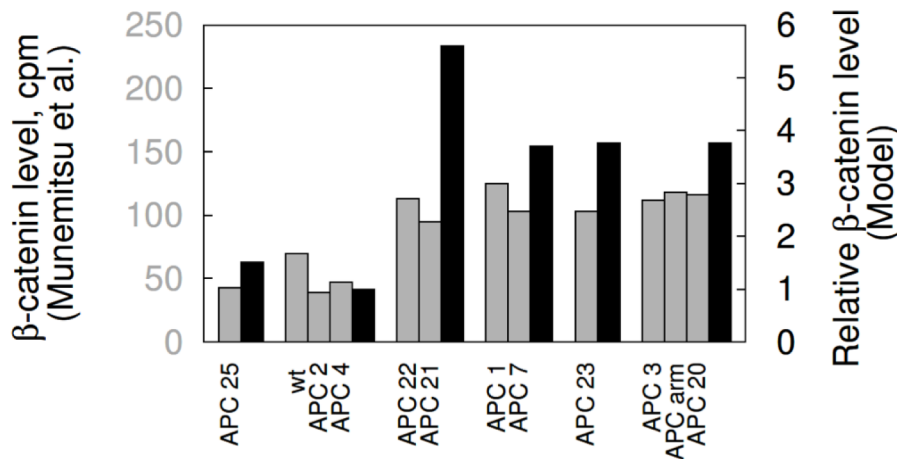


Figure 4. Comparison of simulated and observed effects of transfection of SW480 cells with APC constructs. Relative β -catenin levels in SW480 cells in response to transfection with the APC constructs of Fig. 3 are shown. The gray bars, which correspond to the left y -axis, represent experimental data from Munemitsu et al. [31]. The black bars, which correspond to the right y -axis, represent model predictions. The predicted concentrations (black bars) are each divided by the concentration of β -catenin in a normal cell (35 nM, Table 1). For all APC constructs, the same transfection efficiency is assumed. We take a transfected cell to contain 100 nM of added protein. The predicted results therefore represent the effects of 100 nM of a construct in addition to 100 nM of endogenous APC1338. The simulation results shown here were obtained using BioNetGen input files provided in the Supporting Information: Text S3 was used for the APC-B and APC-F cases, Text S4 was used for the APC-A case, Text S5 was used for the APC-C case, Text S6 was used for the APC-D case, and Text S7 was used for the APC-E case. doi:10.1371/journal.pcbi.1003217.g004

tion-dependent positive effect on β -catenin level in normal cells, in contrast to the effect in SW480 cells (Fig. 4). The effects of exogenous full-length APC at different concentrations in SW480 cells are considered in Fig. 5B, which shows the model-predicted β -catenin level in SW480 cells as a function of full-length APC level. An SW480 cell is taken to have endogenous APC1338 at a cytosolic concentration of 100 nM (Table 1). The predicted effect of added full-length APC is a significant decrease in β -catenin level in SW480 cells over a wide range of exogenous full-length APC expression levels (Fig. 5B). This finding is consistent with the effects of transient expression of full-length APC in SW480 cells [31] and to some extent also with stable expression of full-length APC in SW480 cells [34].

Concentration-dependent effects of truncated forms of APC in SW480 cells

In Fig. 4, we assumed a fixed amount (100 nM) of exogenous expression for all six classes of APC. However, the results in Fig. 4 could depend on APC concentration, as seen for APC-A (Fig. 5). Therefore, we investigated the predicted concentration-dependent effects of APC-B, -C, -D and -E on β -catenin levels in SW480 cells (Fig. 6). For APC-A, such effects have already been discussed (Fig. 5B). We do not consider APC-F because in our model it represents a non-functional form of APC with no binding sites.

The simulation results in Fig. 6 illustrate the concentration-dependent effects of APC-B, -C, -D and -E. As seen in Fig. 6A, added APC-B (e.g., APC1338) increases β -catenin level over the entire concentration range considered. The level of β -catenin doubles as the amount of exogenous APC1338 approaches a 10-fold higher amount of endogenous APC1338 (Fig. 6A). Unlike APC-B, the other three proteins do not increase β -catenin level over the entire concentration range. APC-C reduces β -catenin level at relatively high concentrations (Fig. 6B), APC-D does not alter β -catenin level at any concentration (Fig. 6C), and APC-E reduces β -catenin level over a range of intermediate concentrations in a manner similar to full-length APC (cf. Fig. 6D and Fig. 5B).

The only difference between APC-B and APC-C is that the former form of APC contains the first 20-aa repeat, whereas the latter form does not. This distinction leads to APC-B and APC-C having opposite effects on β -catenin level in SW480 cells (cf. Figs. 6A and 6B). APC-D contains the first 20-aa repeat but no other functional components of APC that are able to interact with β -catenin or Axin. Therefore, APC-D cannot interact with β -catenin because of the consequent absence of phosphorylation of the 20-aa repeat. The 20-aa repeat in APC-D is never phosphorylated because the unphosphorylated protein is unable to interact with Axin. Thus, APC-D has no effect on β -catenin level (Fig. 6C). APC-E entails all structural features of APC-B, but in addition it contains SAMP repeats, which mediate Axin binding (Fig. 2). Because of this distinctive feature, the model predicts that APC-E behaves differently from APC1338 and produces reduced β -catenin levels at intermediate concentrations of APC-E similar to the predicted effects of full-length APC (Fig. 5B). These results indicate that the absence of SAMP repeats in APC1338 may have an important role in APC1338-mediated increases of β -catenin levels in cancer cells.

Phosphorylation-dependent competition between APC1338 and Axin for binding to β -catenin

The analysis of Fig. 6 indicated that APC-B (e.g., APC1338) and APC-C have opposite effects on β -catenin level because APC-B contains a 20-aa repeat that APC-C does not. In Fig. 7, we analyze the effects of phosphorylation of the 20-aa repeat in APC-B on β -catenin levels in SW480 cells. Recall that phosphorylation of the 20-aa repeat in APC is mediated by CK1 ϵ and GSK-3 β [30,45] and that phosphorylation of this site is necessary for direct interaction of APC with β -catenin [22,25].

The simulation results shown in Fig. 7A indicate that phosphorylation of the 20-aa repeat is needed for APC-B/APC1338-mediated stabilization of β -catenin. In the figure, the solid line corresponds to default rate constants for phosphorylation and dephosphorylation of APC in the model (Table 1). For these

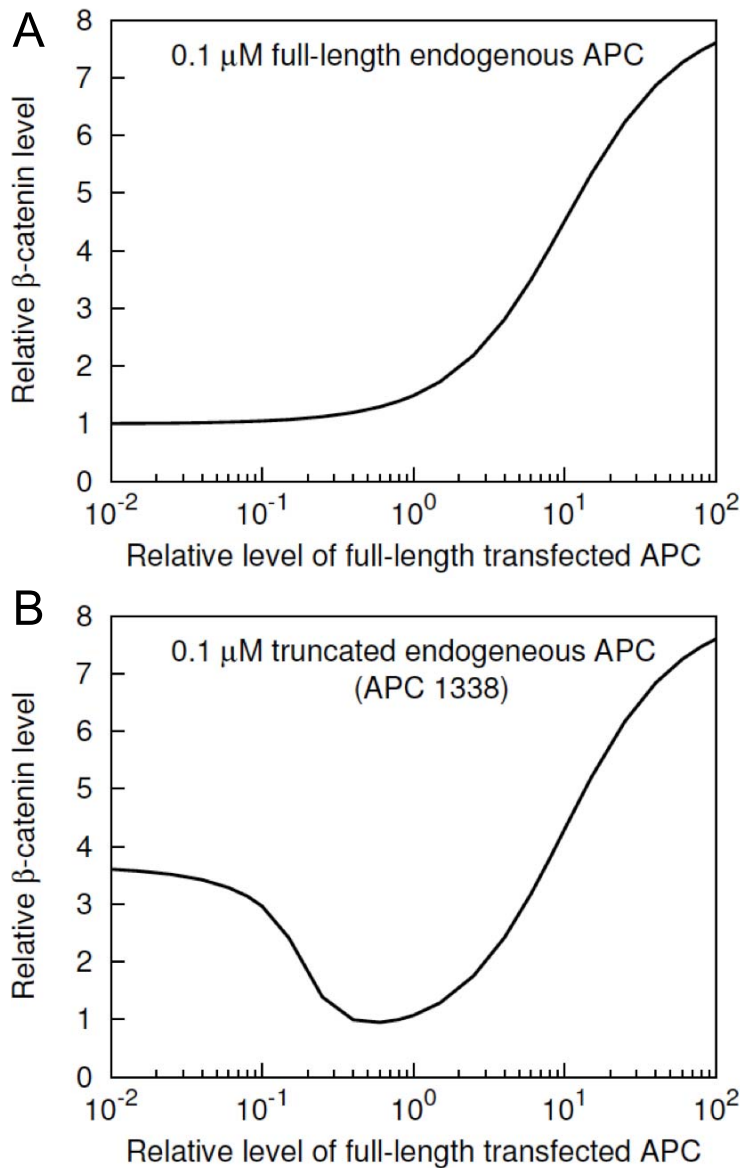


Figure 5. Concentration-dependent effects of full-length APC on β -catenin. (A) β -catenin level in a normal cell is shown as a function of APC concentration. The x -axis represents the relative amount of APC introduced exogenously with respect to the endogenously present 100 nM of full-length APC in a normal cell. The y -axis represents the level of β -catenin relative to its nominal level in a normal cell (Table 1). (B) β -catenin level in an SW480 cell is shown as a function of APC concentration. The x -axis represents the amount of APC introduced exogenously relative to the endogenously present 100 nM of APC1338 in an SW480 cell. The y -axis represents the level of β -catenin relative to its nominal level in a normal cell, as in panel A. The simulation results shown here were obtained using BioNetGen input files provided in the Supporting Information: Text S2 was used for panel A and Text S4 was used for panel B. doi:10.1371/journal.pcbi.1003217.g005

parameter values, the 20-aa repeat is nearly always phosphorylated. This case can be viewed as the extreme opposite of the case where the 20-aa repeat is deleted and therefore never present in phosphorylated form. When the 20-aa repeat is deleted, APC-B becomes equivalent to APC-C and downregulates β -catenin in a similar manner (cf. Fig. 7A and Fig. 6C).

Phosphorylated APC1338 binds to ARM repeats 3 and 4 in β -catenin, which is also a binding site for Axin (Fig. 2). Thus, phosphorylated APC1338 competes with Axin for binding to β -catenin and can inhibit phosphorylation of β -catenin by sequestering β -catenin away from Axin-associated kinases. Fig. 7B illustrates the predicted effect of APC1338 phosphorylation on association of β -catenin and Axin. The simulation results

of Fig. 7B show that phosphorylation of APC1338 inhibits interaction of β -catenin with Axin.

Mechanism of β -catenin upregulation by APC1338

The results of Fig. 7 suggest that competition between APC1338 and Axin for β -catenin binding upregulates β -catenin levels in SW480 cells. These results however do not explain how APC1338 and APC regulate β -catenin differentially. Differential regulation is somewhat paradoxical because both proteins have phosphorylation sites in the 20-aa repeat region, which mediates β -catenin binding. The distinction between APC and APC1338 can be attributed to the absence of SAMP repeats in APC1338, as explained fully below. In short, APC1338 sequesters β -catenin

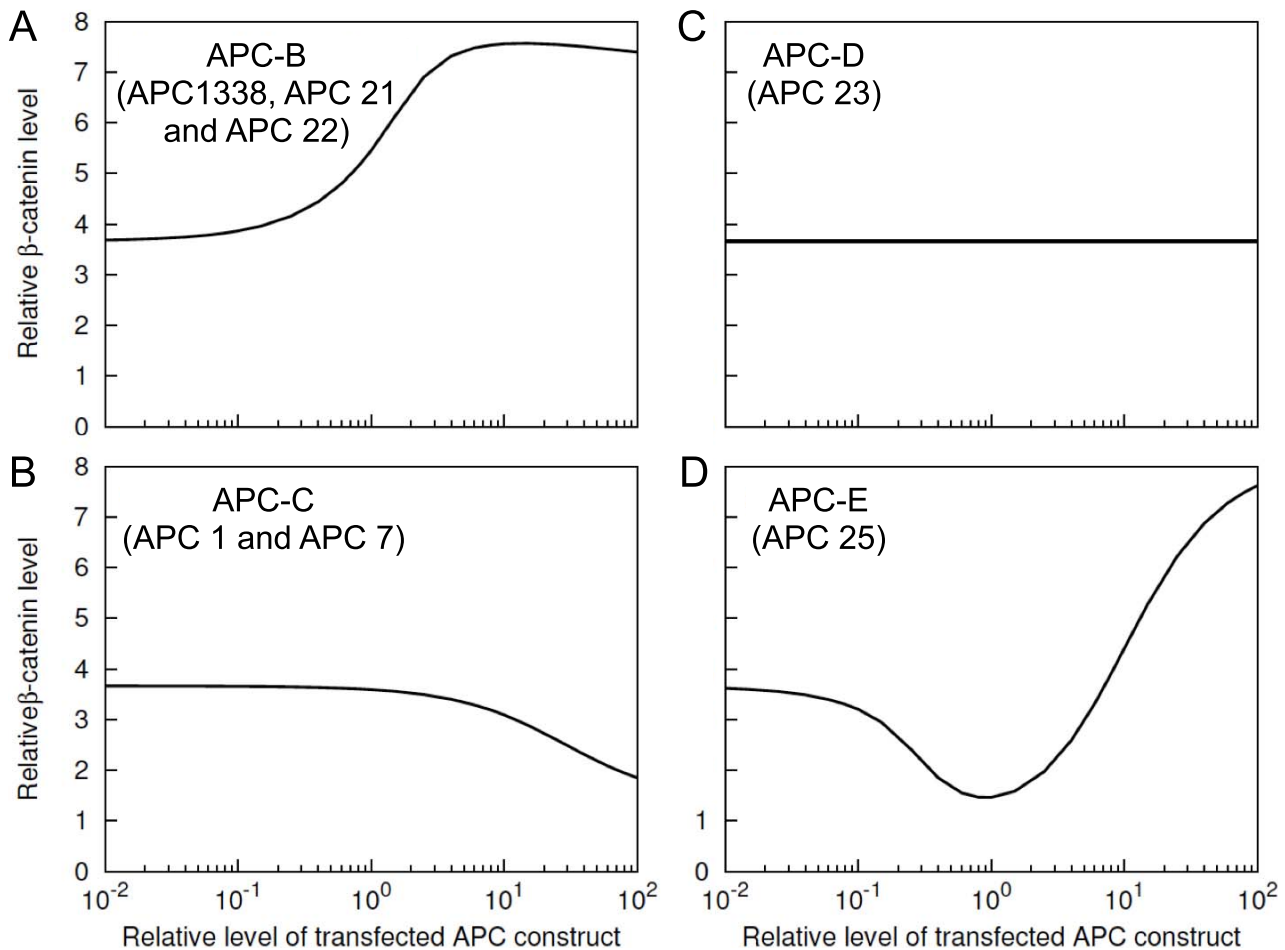


Figure 6. Concentration-dependent effects of APC constructs in SW480 cells. Predicted β -catenin level is shown as a function of expression level for APC-B, -C, -D, and -E. In each panel, the x -axis represents the amount of expression relative to the endogenous level of APC1338 (100 nM). The y -axis represents the β -catenin level relative to the nominal level in a normal cell (35 nM, Table 1). Thus, a value of 1 on the x -axis corresponds to a concentration of 100 nM of transfected protein, and a value of 1 on the y -axis corresponds to a concentration of 35 nM of β -catenin. The simulation results shown here were obtained using BioNetGen input files provided in the Supporting Information: Text S3 was used for panel A, Text S5 was used for panel B, Text S6 was used for panel C, and Text S7 was used for panel D.
doi:10.1371/journal.pcbi.1003217.g006

away from Axin, whereas APC fails to do so (Fig. 8). The sequestration effect arises because APC1338, lacking SAMP repeats, cannot mediate indirect association of β -catenin with Axin. We note that the bell-shaped curve in Fig. 8B represents a characteristic scaffold effect [49,50]. Here, the scaffold is APC and the scaffold ligands are Axin and β -catenin.

In normal cells, β -catenin can associate with Axin in two ways: 1) direct binding via ARM repeats 3 and 4 in β -catenin (Arrow 3; Fig. 2), and 2) indirect binding via APC, with APC acting as a linker between β -catenin and Axin (Arrows 2 and 4; Fig. 2). As in an SW480 cell, the direct interaction in a normal cell is also inhibited by phosphorylation of the 20-aa repeat region in APC because of competition between phosphorylated APC and Axin for binding to ARM repeats 3 and 4 in β -catenin. Nonetheless, in a normal cell, the indirect interaction still enables β -catenin to colocalize with Axin via APC [30], thus allowing phosphorylation of β -catenin to occur via Axin-associated kinases, which leads to degradation of β -catenin. In contrast, in SW480 cells, β -catenin can associate with Axin only through direct interaction. The indirect interaction does not occur because APC1338 lacks the SAMP repeats necessary for Axin binding. Thus, in SW480 cells, APC1338 phosphorylation effectively blocks

β -catenin association with Axin, leading to less degradation. A corollary of this finding is that increased expression of Axin would be expected to increase the degradation of β -catenin, which has been observed [36,51,52].

Effect of stability of the core destruction complex on β -catenin level

The stability of the destruction complex can be perturbed (decreased) by preventing APC, Axin, and β -catenin from forming a closed/cyclic ternary complex. The cyclic complex, which we assume can form in normal cells, cannot form in SW480 cells as a result of APC truncation. Formation of the cyclic ternary complex can be prevented not only by truncation of APC but also by other mutations. Any mutation affecting one of the three protein-protein interfaces of the ternary complex would prevent closure of the cyclic structure. Using our model, we simulated inhibition of formation of the cyclic structure by systematically blocking each of the three protein-protein interfaces of the closed/cyclic ternary complex, and we determined the resulting effect on β -catenin level. As seen in Fig. 9, blocking the contact between APC and β -catenin or β -catenin and Axin did not change

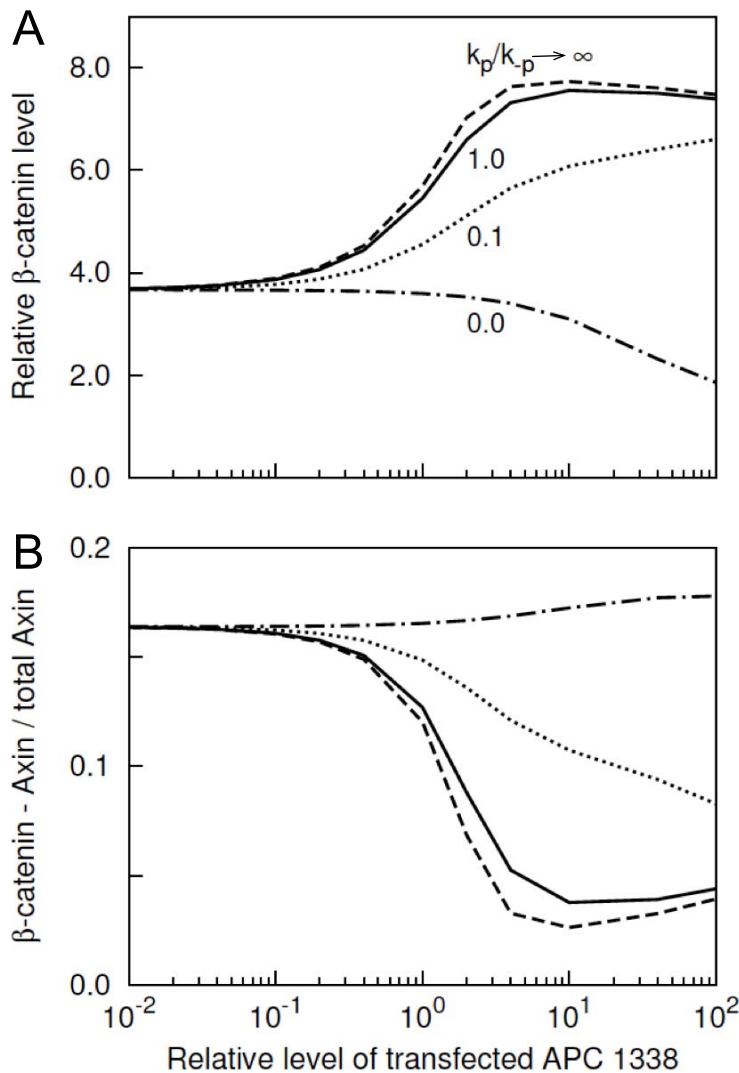


Figure 7. APC1338 phosphorylation and its competition with Axin for β -catenin. (A) β -catenin level is shown at different levels of APC1338 phosphorylation. Phosphorylation of APC1338 at the first 20-aa repeat is modulated by changing the values of the phosphorylation and dephosphorylation rate constants k_p and k_{-p} . In the figure, the ratio, $k_p/k_{-p}=1$ corresponds to the default values of k_p and k_{-p} in the model, which are taken to be the same (Table 1). The case where $k_p/k_{-p}\rightarrow\infty$ represents an extreme, where the 20-aa repeat always remains phosphorylated. The case where $k_p/k_{-p}=0$ represents the opposite extreme, where APC1338 never becomes phosphorylated. (B) Competition effects on β -catenin–Axin binding arising from APC1338 phosphorylation. The y -axis represents the fraction of Axin in complex with β -catenin. The patterns of the lines represent different phosphorylation and dephosphorylation rate constants, as labeled in panel A. The simulation results shown here were obtained using Text S3, a BioNetGen input file provided in the Supporting Information. doi:10.1371/journal.pcbi.1003217.g007

β -catenin level, indicating that the cyclic structure is unimportant for regulation of β -catenin level. Only blocking of the interface between APC and Axin (by removal of SAMP repeats) is predicted to upregulate β -catenin level. However, as established above, this behavior arises for reasons other than destabilization of the cyclic ternary complex of APC, Axin, and β -catenin. Thus, our model indicates that destabilization of this complex (through ablation of cyclization) is not an important effect of APC truncation.

Discussion

In this study, we have modeled β -catenin regulation by the destruction complex in normal and colorectal cancer cells, which express full-length and truncated APC, respectively. Our model,

illustrated in Figs. 1 and 2, incorporates site-specific mechanistic details about the destruction complex, which comprises a number of signaling proteins. In colorectal cancer cells (e.g., SW480 cells), the interactions of these proteins are altered by truncation of APC. We have used our model to study the function of APC and the effects of its truncation on β -catenin phosphorylation and phosphorylation-dependent degradation. We caution that our results pertain to only the function of APC within an idealized destruction complex and furthermore that we considered the interactions of particular (multifunctional) proteins in isolation from most of their binding partners. Thus, within the context of a cell, the functional effects of APC or truncated APC overexpression could potentially be very different from what our model predicts. Nevertheless, the model is qualitatively consistent with the observed effects of transient expression of various recombinant

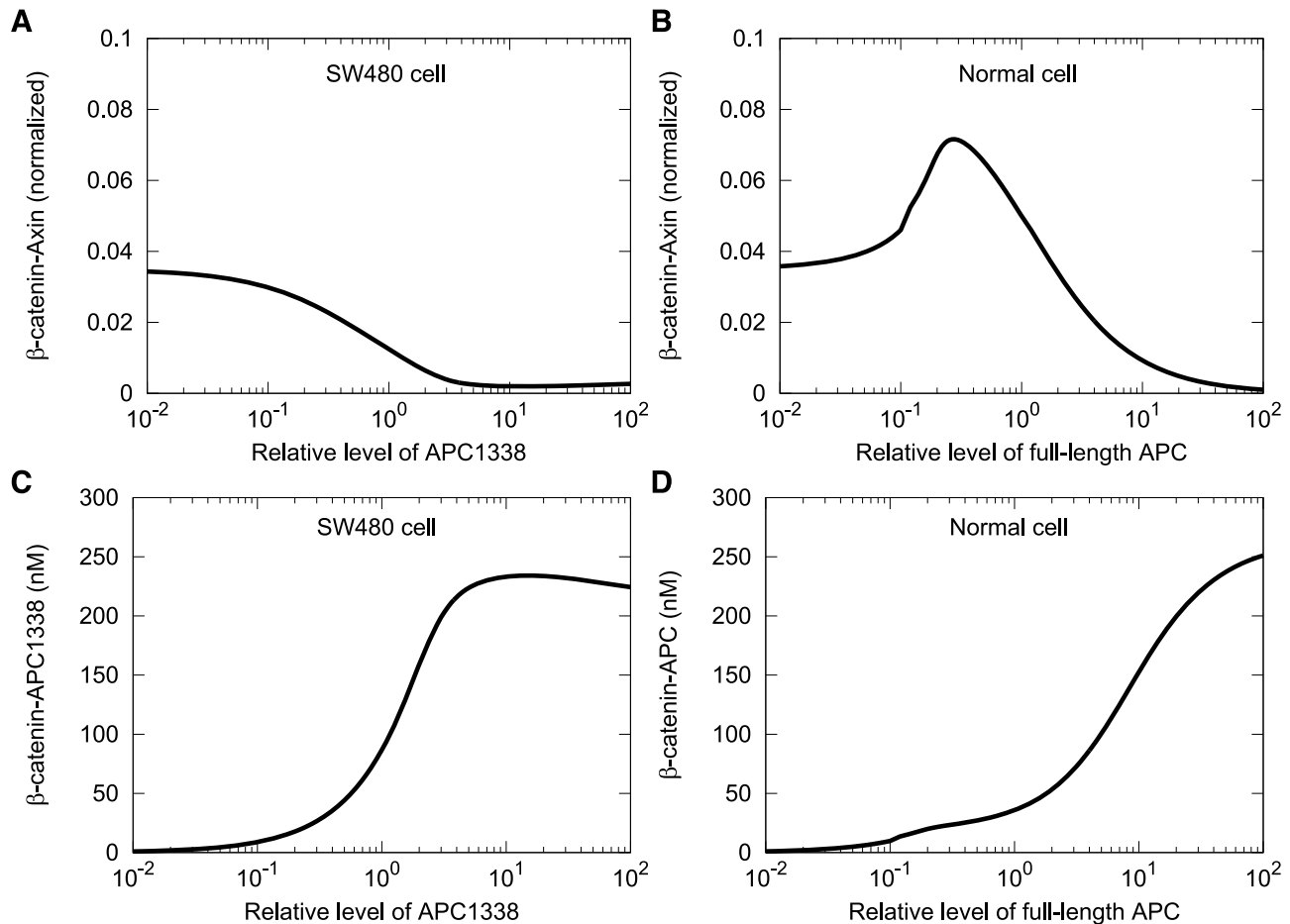


Figure 8. Sequestration of β -catenin away from Axin by APC1338. (A) Predicted amount of β -catenin associated either directly or indirectly with Axin is shown as a function of APC1338 concentration in the background of an SW480 cell. The horizontal axis indicates the amount of APC1338 divided by the nominal amount of APC1338 in an SW480 cell (100 nM). The vertical axis indicates the amount of Axin-associated β -catenin divided by the total amount of β -catenin at steady state, which is a function of APC1338 concentration. (B) Predicted amount of β -catenin associated either directly or indirectly with Axin is shown as a function of full-length APC concentration in the background of a normal cell. The horizontal axis indicates the amount of full-length APC divided by the nominal amount of full-length APC in a normal cell (100 nM). The vertical axis indicates the amount of Axin-associated β -catenin divided by the total amount of β -catenin at steady state, which is a function of full-length APC concentration. (C) Predicted amount of β -catenin associated directly with APC1338 as a function of relative APC1338 concentration. (D) Predicted amount of β -catenin associated directly with full-length APC as a function of relative full-length APC concentration. All results shown were obtained using the parameter values of Table 1, except as indicated. The following BioNetGen input files were used to obtain simulation results: Text S3 was used for panels A and C and Text S2 was used for panels B and D. doi:10.1371/journal.pcbi.1003217.g008

forms of APC in SW480 cells [31] (Fig. 4). Stronger, less ambiguous tests of model predictions in the future would ideally be performed using an *in vitro* reconstituted or cell-free system [53] to eliminate the uncertainties and complexities of the cellular milieu.

Our analyses indicate that whilst the expression of full-length APC in SW480 cells can be expected to increase degradation of β -catenin, APC overexpression in normal cells may decrease β -catenin degradation or have no effect. We show that phosphorylation of the first 20-aa repeat in truncated APC, together with the absence of the SAMP repeats, is crucial for the effect of APC1338 on β -catenin levels in SW480 cells (Figs. 7 and 8). We suggest that phosphorylated APC1338 sequesters β -catenin from Axin, thus blocking β -catenin phosphorylation by Axin-bound kinases, viz. CK1 α and GSK-3 β . In contrast, phosphorylation of full-length APC, because of its SAMP repeats, which provide an indirect means for interaction between Axin and β -catenin, does not block β -catenin association with Axin and

Axin-bound kinases, except at significantly higher levels of expression (cf. panels A and B in Fig. 8).

Several experimental studies have detected competition between phosphorylated full-length APC and Axin for β -catenin binding [24,30,54,55], although the effect of such competition on β -catenin levels has not been previously characterized.

Our results suggest that APC1338, similar to full-length APC, can efficiently mediate competition with Axin for β -catenin binding, even though it lacks the third 20-aa repeat (Fig. 3), the high-affinity β -catenin binding site in full-length APC. In the model, APC1338 associates with β -catenin with sufficient strength to displace Axin because of two-point attachment via its 15-aa and phosphorylated 20-aa repeat sites (i.e., because of the combined action of the interactions represented by Arrows 1 and 2 in Figs. 1 and 2). The single-site K_D 's for the interactions mediated by these sites are ≈ 273 and 80 nM, respectively [25,43]. The affinities are comparable to the affinity of Axin for β -catenin ARM repeats 3 and 4 ($K_D = 227$ nM [43]). However, if two-point

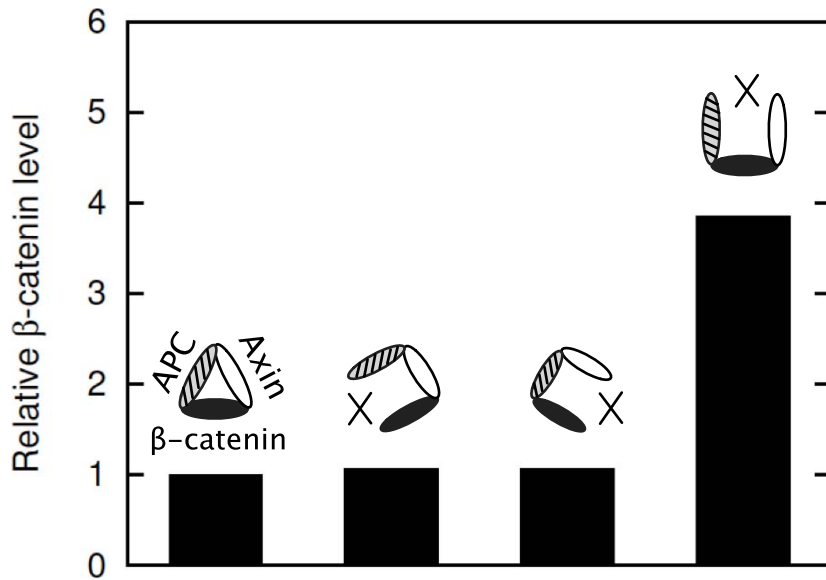


Figure 9. Effects of simulated perturbations of the putative closed/cyclic core destruction complex. Three cases are considered, as indicated in the descriptions of Text S8, S9, S10 (Supporting Information). Each of the three protein-protein interfaces, APC- β -catenin (Text S8), β -catenin-Axin (Text S9), and APC-Axin (Text S10), is ablated such that a closed/cyclic structure cannot form. The relative β -catenin level in each case is compared with the nominal β -catenin level in a normal cell.
doi:10.1371/journal.pcbi.1003217.g009

attachment is possible, as we have postulated in our model, then there is an avidity effect. This effect has been studied in other systems [56–58] and may confer on phosphorylated APC1338 a competitive advantage, allowing it to outcompete Axin for β -catenin.

A critically important feature of our model is a greater abundance of APC than Axin (Table 1). According to our model, as discussed above, truncated APC in SW480 cells acts as a diversion sink that sequesters β -catenin away from Axin. This diversion-sink mechanism cannot be operative if Axin is more abundant than APC. Recent measurements of APC and Axin in SW480 cells indicate that the total amounts of Axin and APC are comparable [59]. At first, these results might seem to contradict the model presented here, which takes APC to be 10-fold more abundant than Axin. However, Axin is not homogeneously distributed in a cell. Much of the Axin in a cell is found in cytoplasmic puncta [35,36]. Thus, only a fraction of total Axin may be available in a form capable of joining a destruction complex having the composition and structure considered here. A more complicated model than that presented here would be required to account for subcellular compartmentalization of APC, Axin and β -catenin, which clearly play an important role in Wnt/ β -catenin signaling [2,3]. Such an effort is beyond the intended scope of our study.

The role of colocalization of signaling proteins within the destruction complex is not completely understood. In our model, we assumed that the core of the destruction complex, formed by mutual interactions of APC, Axin, and β -catenin, has a closed/cyclic structure (as depicted in the cartoon diagram at the far left of Fig. 9). Within this cyclic structure, there are three protein-protein interfaces, and each of the three interfaces involves interaction between two adjacent proteins, which are connected indirectly via the third protein. Therefore, the binding sites at each interface are confined together in a volume that is small relative to the total volume of the cytoplasm and the local concentrations of tethered

binding partners are high. Such high local concentrations can confer on a cyclic structure more stability than a linear structure of the same composition [60]. It has been assumed that the destruction complex provides a stable platform for phosphorylation of β -catenin by the Axin-recruited kinases GSK-3 β and CK1 α . However, according to our analyses, stability of the core destruction complex (i.e., the cyclic ternary complex of APC, Axin and β -catenin) is not important for efficient degradation of β -catenin. By systematically simulating ablation of each possible contact between β -catenin, APC, and Axin, we demonstrate that stability of the complex has little if any influence on β -catenin degradation (Fig. 9). (Note that the bar at the far right of Fig. 9 is explained by the diversion-sink mechanism.) We caution that, in the model, stability of the cyclic structure is also determined by factors other than the local concentration effect. Degradation of β -catenin in a core complex can terminate its cyclic structure, leaving behind a complex of APC and Axin only. In addition, phosphorylated APC can disrupt the cyclic structure by breaking the β -catenin-Axin interface through competitive binding and sequestering of β -catenin away from the complex.

Questions may arise as to what other roles APC plays besides destruction complex-mediated regulation of β -catenin because our model indicates that elevated expression of APC in a normal cell does not have a positive effect on β -catenin degradation (Fig. 5A), i.e., an increase in APC abundance is not predicted to cause a decrease in β -catenin level. A variety of other potential functions of APC have been suggested. Phosphorylated APC has been implicated in subcellular localization and nuclear shuttling of β -catenin [32,61–63], and high-affinity binding of phosphorylated APC with β -catenin has been suggested to disrupt β -catenin interaction with other binding partners, such as E-cadherin and the Tcf and Lef family transcription factors [24]. It has been shown that APC competes with E-cadherin for binding to the ARM repeat region of β -catenin [64]. Indeed, the main effect of stable expression of full-length APC in SW480 cells is not

a reduction of β -catenin level (although there is an approximate 2-fold reduction in the total amount of β -catenin), but rather a redistribution of β -catenin from the nuclear and cytosolic compartments to the plasma membrane [34]. Transient expression of APC (at higher levels) causes a more dramatic reduction in the level of β -catenin [31,34]. In future work, it would be interesting to investigate how E-cadherin may regulate β -catenin and *vice versa* [3].

Our study identifies CK1 ϵ as a potential target for therapeutic intervention in colorectal cancer. Inhibiting CK1 ϵ is expected to reverse the effect of truncation of APC in SW480 cells. According to the model, phosphorylation of APC1338 at the first 20-aa repeat plays a key role in upregulating β -catenin in cancer cells (Fig. 7). Therefore, inhibition of phosphorylation of APC at this site might be an effective way to normalize β -catenin levels in cancer cells. Phosphorylation of APC requires the combined action of two kinases, CK1 ϵ and GSK-3 β [30]. Therefore, blocking of either kinase is predicted to reduce APC phosphorylation, as shown by Ha et al. [30]. Because GSK-3 β is a common kinase for both β -catenin and APC (Fig. 1) and its inhibition would stabilize β -catenin, only CK1 ϵ is a potential target. We note that targeting of CK1 ϵ should be feasible in preclinical studies, as pharmacological kinase inhibitors specific to CK1 ϵ are available [65–67].

In this study, we used a detailed mechanistic modeling approach based on the principles of chemical kinetics to investigate regulation of β -catenin phosphorylation and degradation by full-length and truncated APC. In a previous study, Lee et al. [53] developed a related model to investigate regulation of β -catenin by Wnt stimulation. However, this model does not consider truncated APC. Another notable difference is that the model of Lee et al. [53] is an ordinary differential equation (ODE)-based model, wherein molecules and complexes of signaling proteins are treated as reactive chemical species, which must be enumerated along with all possible reactions to obtain an executable model. In contrast, because of the goals of our study, we developed our model using the rule-based modeling approach [37–40]. With this approach, local rules are used to represent protein-protein interactions, which are assumed to be modular. Assumptions of modularity can greatly reduce the complexity of a model for protein-protein interactions, and as a result, enable explicit consideration of multiple functional components within proteins (e.g., the multiple sites of phosphorylation in β -catenin). In our model, the components of the proteins considered are the basic reactive elements, i.e., we consider biochemical reactions, such as reversible binding and phosphorylation, to occur at the level of protein sites. This approach was critical for the goals of our study, which included a characterization of the effects of loss of sites in APC. Such effects, and biomolecular site dynamics in general, are difficult to capture in an ODE model [40]. The study presented here provides an example of how rule-based modeling, a fairly new approach in biology, can be used to study biomolecular site dynamics.

We focused on a part of the Wnt/ β -catenin signaling pathway that controls β -catenin degradation and expression level. Our primary goal was to understand the differential regulation of β -catenin in normal and cancer cells at steady state and in the absence of Wnt signals, unlike in other modeling studies that have focused on the dynamics of β -catenin regulation in response to a Wnt ligand [20,53]. In future work, it would be interesting to extend our model by connecting it to other components of the Wnt/ β -catenin signaling pathway and to further investigate the dynamics of regulation of β -catenin.

Materials and Methods

Parameter values

Model parameter values are listed in Table 1. Most of the parameter values are based on previously reported estimates. However, some parameter values were set to allow the model to capture a set of observed system behaviors.

In the model, the concentration of β -catenin depends in part on its rates of synthesis and degradation. As discussed below, we set parameters for these and other processes considered in the model such that the nominal, steady-state concentration of β -catenin is 35 nM [53], which corresponds to 11,000 copies/cell assuming a cytoplasmic volume of 10^{-12} L [59]. This concentration is consistent with the concentration of β -catenin measured in *Xenopus* egg extract [53]. It is also consistent with the cytosolic (but not total) concentration of β -catenin measured in HEK293T and MDCK cells, kidney epithelial cell lines, and in Caco-2 cells [59], an intestinal cell line. We take both APC and GSK-3 β concentration to be 100 nM (31,540 copies/cell). Concentrations of APC and GSK-3 β have been measured to be 100 nM and 50 nM, respectively, in *Xenopus* egg extract [53], and measured concentrations of these proteins in mammalian cells fall in the ranges of 4–34 nM and 10–120 nM, respectively [59]. We take CK1 α concentration to be the same as GSK-3 β , 100 nM. We assume Axin to be present at 10 nM (3,154 copy/cell), which is consistent with recent measurements of Axin abundance in mammalian cells; the Axin concentration measured in mammalian cells ranges from 20 to 150 nM [59]. Lee et al. [53] reported that Axin is present in *Xenopus* egg extract at a very low concentration, in the range of 10 to 20 pM [53]. We rejected this value, while accepting and using the qualitative observation of Lee et al. [53] that Axin is less abundant than APC, because a concentration of 20 pM corresponds to only six copies of Axin per cell for a human epithelial cell, which as stated above is taken to have a cytoplasmic volume of 10^{-12} L [59].

For association of any two proteins that are not already in a complex together we assume the same forward rate constant (k_f) for all interactions: 10^{-3} nM $^{-1}$ s $^{-1}$ (Table 1). Each reverse rate constant (k_r) is determined from the relation $k_r = k_f \times K_D$, where K_D is the equilibrium dissociation constant for the reaction of interest. Equilibrium dissociation constants are set at values reported earlier in the literature, as indicated below.

In the model, the region in β -catenin containing ARM repeats 5–9 interacts with the 15-aa repeat region in APC (Arrow 1) with $K_{D1,bap} = 273$ nM ($k_{r,bap} = 0.273$ s $^{-1}$) [43]. The region in β -catenin containing ARM repeats 3 and 4 interacts with the phosphorylated 20-aa region in APC (Arrow 2) with an affinity that depends on whether APC is full length or truncated (APC1338). Phosphorylated full-length APC binds the β -catenin ARM repeats 3 and 4 with $K_{D2,bap} = 1.5$ nM ($k_{r2,bap} = 1.5 \times 10^{-3}$ s $^{-1}$), whereas phosphorylated APC1338 binds with $K_{D3,bap} = 85$ nM ($k_{r3,bap} = 0.085$ s $^{-1}$) [25]. We assume that APC binds β -catenin via only a single 20-aa repeat, which is consistent with binding of β -catenin at one 20-aa repeat sterically hindering binding of additional copies of β -catenin at other 20-aa repeats. When phosphorylated, the third 20-aa repeat mediates binding with $K_{D2,bap} = 1.5$ nM, whereas the other six 20-aa repeats appear to bind with much lower affinities [25]. β -catenin binds the central region of Axin via ARM repeats 3 and 4 (Arrow 3) with $K_{D,ba} = 227$ nM ($k_{r,ba} = 0.227$ s $^{-1}$) [43]. GSK-3 β binds the Axin GID domain (Arrow 5) with $K_{D,ga} = 65$ nM ($k_r = 0.065$ s $^{-1}$) [68]. We assume that APC and CK1 α bind

Axin (Arrow 4 and 6, respectively) with the same K_D : $K_{D,apa} = 100$ nM ($k_{r,apa} = 0.1$ s $^{-1}$) and $K_{D,ca} = 100$ nM ($k_{r,ca} = 0.1$ s $^{-1}$).

In the model, β -catenin level is determined not only by β -catenin synthesis and degradation rate constants, but also by other parameters that affect the phosphorylation of β -catenin and APC. These parameters include phosphorylation and dephosphorylation rate constants and the enhancement factor χ . All of these parameters directly or indirectly determine the total level of β -catenin. We selected values for these parameters, which are given in Table 1, such that the model captures a set of experimentally-observed system behaviors.

With the parameter values listed in Table 1, the model reproduces a steady-state concentration of (cytosolic) β -catenin of 35 nM, which as discussed above is consistent with some measurements [53,59]. Furthermore, the model predicts the effective half-life of β -catenin to be ≈ 30 min, and the half-life of β -catenin mutated at S33/S37 to be ≈ 4.5 h, which is consistent with the observations of Rubinfeld et al. [14] (Fig. S1). The model also reproduces the experimentally-determined kinetics of β -catenin dephosphorylation at distinct phosphorylation sites in response to treatment with LiCl, an inhibitor of GSK-3 β [12] (Fig. S2). The consistency of the model with observed system behaviors is further discussed in the Results section.

We note that the model is not entirely consistent with recent measurements of APC, Axin, (cytosolic) β -catenin, and GSK-3 β concentrations in SW480 cells [59]. The model cannot simultaneously reproduce these concentrations and observed system behaviors. This could be because the measured concentrations do not reflect the subcellular concentrations relevant for destruction complex function. Alternatively, our mechanistic knowledge of destruction complex function could be incomplete. We formulated our model to probe the limits of understanding of destruction complex function. In setting parameter values, we put an emphasis on selecting values that allow the model to reproduce observed system behaviors, rather than measured system parameters (viz., protein concentrations). This approach is guided by findings from computational analyses of model sloppiness, which indicate that fitting tends to improve the accuracy of model predictions more than parameter measurement [69].

Model specification

We will refer to the model illustrated in Figs. 1 and 2 as the base model. The base model corresponds to the case of a normal cell with full-length APC. Variants of the base model correspond to SW480 cells with APC1338, SW480 cells transfected with different forms of APC, and other cases considered in this study (see below for further details). The base model and each of its variants was formulated using BNGL, a model-specification language [39]. Executable model-specification files are provided in the Supporting Information for the base model (Text S2) and its variants (Text S3, S4, S5, S6, S7, S8, S9, S10). BNGL is compatible with BioNetGen [39,70], a software tool for rule-based modeling, and a number of other tools, such as RuleBender [71], an interface for BioNetGen. In addition to parameter values and initial data, each model-specification included molecule type definitions and rules. Molecule type definitions delimit the functional components of proteins and their possible phosphorylation states. The rules characterize protein-protein interactions and other processes (viz., synthesis and degradation of β -catenin). The rules that characterize protein-protein interactions can be subdivided into 10 sets, with one set for each arrow in Fig. 1 or 2. An arrow corresponds to multiple rules if the interaction represented by the rule can take place in multiple contexts and the context influences the rate of reaction. For example, Arrow 3 in Fig. 1 or 2 represents

an interaction that can take place between either unconnected proteins or tethered proteins. Thus, there is a rule for each of these two cases.

Simulation

The base model (Figs. 1 and 2) and each variant model was simulated by submitting the corresponding model-specification file to BioNetGen [39,70] for processing. Model-specification files are provided in the Supporting Information (Text S2, S3, S4, S5, S6, S7, S8, S9, S10); the format of these files is plain text. Simulation protocols are included in each model-specification file. The captions of figures indicate which model-specification files were used in calculations. In all cases, the method used for simulation was an indirect method, meaning that the rules of the model being simulated were not used directly in the simulation procedure. Rather, the rules were expanded (i.e., used to exhaustively enumerate the distinct chemical species and individual chemical reactions implied by the rules) by invoking the `generate_network` function of BioNetGen to obtain a reaction network. The corresponding system of ODEs describing the mass-action kinetics of this network were then numerically integrated by invoking the `simulate_ode` function of BioNetGen. BioNetGen uses CVODE [72,73] for numerical integration of ODEs. For the base model, the reaction network obtained by expansion of its rules comprises 410 distinct chemical species. The size of this network does not reflect the intrinsic complexity of the base model. Rather, the intrinsic complexity of this model is reflected by the number of its rules. The base model includes 29 rules. We used scripts to systematically vary default parameter values specified in BioNetGen input files to produce many of the figures shown in the Results section. Parameter scans are enabled by a function available within RuleBender [71].

Supporting Information

Figure S1 The model reproduces the half-lives of β -catenin and β -catenin mutated at S33/S37. The model predicts the half-life of β -catenin in a normal cell to be 30 min (solid line) and the half-life of β -catenin mutated at the S33/S37 phosphorylation site to be 4.5 h (dashed line). These predicted values are consistent with the measured values reported by Rubinfeld et al. [14]. The figure illustrates model-predicted decay of cellular β -catenin or β -catenin mutated at S33/S37 in a simulated pulse-chase experiment [14]. The model was used to simulate the pulse-chase experiments of Rubinfeld et al. [14], which were carried out to determine the half-lives of the proteins. (EPS)

Figure S2 The model reproduces the effects of LiCl treatment on phosphorylation of cellular β -catenin. The figure shows predicted and measured phosphorylation of β -catenin at S45 and S33/S37 in response to LiCl treatment of cells. The solid lines represent model predictions, and the points represent experimental data of Liu et al. [12]. The solid line/filled circles correspond to S45, and the dashed line/open circles correspond to S33/S37. In the model, LiCl addition is simulated by assuming a 20-fold decrease in kinase activity of GSK-3 β (i.e., 20-fold reduced rate of phosphorylation of the APC 20-aa repeats and S33/S37 in β -catenin). The kinase activities of CK1 α and CK1 ϵ are assumed to be unaffected by LiCl treatment. Time $t=0$ represents the time of LiCl addition. The y -axis values represent phosphorylation of S45 or S33/S37 relative to the steady-state levels of phosphorylation of these sites in the absence of LiCl. (EPS)

Table S1 Local parameter sensitivity analysis. The steady-state level of β -catenin is insensitive to variations of model parameter values, as assessed by local sensitivity coefficients. (PDF)

Text S1 Model annotation wiki. This TiddlyWiki (tiddlywiki.com), which takes the form of a single HTML file, provides extensive annotation of the molecule type definitions and rules that comprise the base model, as well as discussion of various modeling assumptions. The wiki can be viewed and navigated using a Web browser. It contains links to relevant information available in public online resources, including UniProt [75], OMIM [76], and Pfam [77]. (TXT)

Text S2 BioNetGen input file for model illustrated in Figs. 1 and 2. This file, which can be processed by BioNetGen (after changing the file name extension to .bngl), provides a complete executable specification of the base model M_0 , i.e., the model for a normal cell with full-length APC. In this model, the low-affinity interaction of β -catenin with the first (phosphorylated) 20-aa repeat in APC (Arrow 2 in Figs. 1 and 2) is omitted for simplicity. This simplification does not prevent interaction of β -catenin with phosphorylated APC, because a rule is included for the (dominant) high-affinity interaction of β -catenin with the third (phosphorylated) 20-aa repeat (Arrow 2 in Figs. 1 and 2). Note that the base model and all of its variants include rules not only for the interactions illustrated in Figs. 1 and 2 but also for synthesis and degradation of β -catenin as well as rules for dephosphorylation of APC and β -catenin. We note that this file can be viewed as specifying a model for a normal cell transfected with APC-A (full-length APC, APC2 or APC 4) (Fig. 3). All forms of APC-A are taken to be functionally equivalent to full-length APC, because each form contains the same functional components that are considered in the base model for full-length APC (15-aa repeats, 20-aa repeats, and SAMP repeats). In simulated transfections of APC-A, the amount of added APC-A (taken to be equivalent to an increase in full-length APC) was varied systematically. See the Simulation subsection in the Materials and Methods section for more information. (TXT)

Text S3 BioNetGen input file for model variant 1. This file specifies the model for an SW480 cell with truncated APC (APC1338). This model (M_1) differs from M_0 in that full-length APC is replaced by APC1338, meaning that the rule for interaction of Axin with the SAMP repeats in APC is removed (Arrow 4 in Figs. 1 and 2) and the rule for high-affinity interaction of β -catenin with the third (phosphorylated) 20-aa repeat is replaced by a rule for the low-affinity interaction of β -catenin with the first (phosphorylated) 20-aa repeat (Arrow 2 in Figs. 1 and 2). Other interactions involving APC remain the same. These changes are intended to capture the effects of C-terminal truncation of APC, which commonly and in the case of APC1338 means a loss of the SAMP repeats and all but the first 20-aa repeat. We note that this file can also be viewed as specifying a model for an SW480 cell transfected with APC-B or APC-F. Recall that the APC-F class of proteins (APC 3, APC arm, and APC 20) do not contain any of the functional components of full-length APC considered in the model (Fig. 3). Thus, in the model, APC-F does not participate in any interactions (i.e., there are no rules that involve APC-F). Recall that APC-B includes APC 21 and APC 22 (Fig. 3), both of which are taken to be functionally equivalent to APC1338 because these forms of APC, like APC1338, each includes 15-aa repeats and the first 20-aa repeat.

Thus, rules for APC1338 interactions are the same as rules for APC-B interactions. In simulated transfections of APC-B, the amount of added APC-B (taken to be equivalent to an increase in endogenous APC1338) was systematically varied. Finally, we note that this file was used for simulating the effect of varying the rate at which the 20-aa repeat region in APC is phosphorylated. In these simulations, the rate constant for APC phosphorylation (denoted as k_p in Table 1 and as `kp` in model-specification files) was systematically varied. (TXT)

Text S4 BioNetGen input file for model variant 2. This file specifies a model for an SW480 cell (i.e., a cell expressing APC1338 endogenously) transfected with APC-A (M_2). The amount of added APC-A was systematically varied in simulations. Recall that APC-A includes full-length APC, APC 2 and APC 4 (Fig. 3), which are taken to be functionally equivalent because these forms of APC contain 15-aa repeats, all 20-aa repeats, and SAMP repeats. In this model, separate rules are specified for APC1338 and APC-A interactions. The rules account for all of the APC interactions considered in models M_0 and M_1 . (TXT)

Text S5 BioNetGen input file for model variant 3. This file specifies a model for an SW480 cell transfected with APC-C (M_3). The amount of added APC-C was systematically varied in simulations. Recall that APC-C includes APC 21 and APC 22 (Fig. 3), which are taken to be functionally equivalent because both of these forms of APC contain 15-aa repeats while missing all 20-aa repeats and the SAMP repeats. In this model, separate rules are specified for APC1338 and APC-C interactions. The only interaction in which APC-C can participate is the constitutive interaction between APC and β -catenin (Arrow 1 in Figs. 1 and 2). (TXT)

Text S6 BioNetGen input file for model variant 4. This file specifies a model for an SW480 cell transfected with APC-D (M_4). The amount of added APC-D was systematically varied in simulations. Recall that APC-D includes only APC 23 (Fig. 3), which contains only the first 20-aa repeat. Although APC-D contains a 20-aa repeat, APC-D cannot be phosphorylated because it lacks other components needed for association with Axin. Thus, this model is essentially the same as model M_1 . (TXT)

Text S7 BioNetGen input file for model variant 5. This file specifies a model for an SW480 cell transfected with APC-E (M_5). The amount of added APC-E (or APC 25, Fig. 3) was systematically varied in simulations. In this model, separate rules are specified for APC1338 and APC-E interactions. APC-E participates in the same interactions as APC1338 except for the constitutive interaction between APC and β -catenin (Arrow 1 in Figs. 1 and 2), which is mediated by the 15-aa repeats that are missing in APC-E. (TXT)

Text S8 BioNetGen input file for model variant 6. This model (M_6) is the same as M_0 except that the association rate constant for APC binding to β -catenin $k_{f1,bap}$ (denoted as `kf1_bap` in model-specification files) has been set to 0. Note that $k_{f1,bap}$ characterizes the interaction represented by Arrow 1 in Figs. 1 and 2. (TXT)

Text S9 BioNetGen input file for model variant 7. This model (M_7) is the same as M_0 except that the association rate constant for Axin binding to β -catenin (denoted as $k_{f,ba}$ in Table 1 and as `kf_ba` in model-specification files) has been set to 0. Recall that Arrow 3 in Figs. 1 and 2 represents the interaction between Axin and β -catenin. (TXT)

Text S10 BioNetGen input file for model variant 8. This model (M_8) is the same as M_0 except that the association rate constant for APC binding to Axin (denoted as $k_{f,apa}$ in Table 1 and as `kf_apa` in model-specification files) has been set to 0.

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Recall that Arrow 4 in Figs. 1 and 2 represents the interaction between APC and Axin. (TXT)

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Author Contributions

Conceived and designed the experiments: DB WSH. Performed the experiments: DB WSH. Analyzed the data: DB WSH. Contributed reagents/materials/analysis tools: DB WSH. Wrote the paper: DB WSH.

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