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## Random Displacement Modulus and Damping Determination Paper No. 1.30

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**SYNOPSIS:** Modulus and damping values were determined for both undisturbed and remolded silty sand specimens by cyclic triaxial methods utilizing both sinusoidal and random displacement stroke control. Remolded specimens were prepared at 3 different dry unit weights using a preparation technique that gave the same formation factor as the undisturbed specimen. Results indicated that the random displacement method tends to produce results which are similar to those obtained by the sinusoidal procedure at shearing strain levels less than  $10^{-1}$  %. At shearing strain levels greater than  $10^{-1}$  % the random displacement method gives lower modulus and higher damping ratio values when compared to the sinusoidal procedure. In addition, stress history effects as demonstrated by the location of the cycle in the record being analyzed were observed not to be important over the sample unit weights investigated.

### INTRODUCTION

During the course of a seismic event soil material undergoes a displacement which is a function of time. The displacement of the soil mass as a function of time results in changing shear modulus and material damping characteristics of the soil. Cyclic triaxial modulus tests using random displacement-time histories were conducted to evaluate this effect on silty sand material remolded to three different densities.

The conversion of an irregular series of earthquake cycles into an equivalent uniform cyclic stress history is an integral part of current seismic response analyses of soil structures. The Miner cumulative damage method (Miner 1945) and equivalent uniform cycle method (Seed and Idriss 1971, Seed et al. 1975, Lee and Chan 1972) are two methods currently in use for this conversion. The cumulative damage theory was developed for metal fatigue. According to this theory, when metals are subjected to cyclic loading, they undergo progressive weakening until they eventually fail. The primary assumptions governing this are: (1) the loading pattern is sinusoidal, and (2) no work hardening takes place in the specimen. Because the loading is assumed

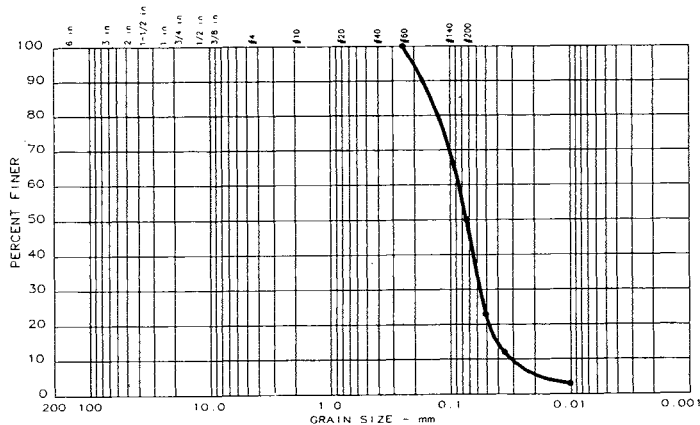
to be sinusoidal, each load cycle has the same incremental damaging effect as every other load cycle. While each cycle causes the same amount of incremental damage regardless of where in the pattern it occurs, the cumulative damage will, of course, increase with each. To determine the cumulative damage, a relationship between stress level and number of cycles to failure must be established for the material in question. In contrast, the equilibrium cycle procedure involves representing the destructive energy of irregular earthquake cycles with an equivalent series of uniform cycles. To do this, an arbitrary average stress level is chosen to which all other irregular stress levels of the earthquake are converted. This average stress level is some fraction of the maximum stress level recorded during the earthquake. All other irregular stress cycles can then be converted to an equivalent number of cycles at the average stress level. A relationship between stress level and the number of cycles to failure for the material being studied is required. Adding these equivalent cycles from each stress level gives the total number of equivalent cycles for the entire earthquake. The number of equivalent

cycles at the average stress level will have the same damaging effect on the soil as the earthquake. The equivalent uniform series thus developed is much easier to work with, both experimentally and analytically, than the actual irregular stress-time history.

The purpose of the following study was the following: (1) to verify that shear modulus and material damping results using the equivalent cycle approach (sinusoidal loading history) gave similar results as when determined using an irregular loading history, and (2) investigate the effect of stress history.

#### SAMPLE PREPARATION

Undisturbed and remolded silty sand samples were employed in this study. A grain size distribution of the material is presented in Fig. 1. A non-dimensional parameter called the formation factor (F) based on the conductivity of the pore fluid system has been developed to describe the packing characteristics of soil (Archie 1942). The formation factor



history was increased in steps until the x-y plot of load versus deformation would no longer form closed loops. After each sequence of loading pore water pressures were allowed to dissipate.



Photo 1. Conductivity Apparatus

## TEST RESULTS

The results of the individual cyclic triaxial random displacement tests are presented in Figs. 3 thru 5. The test results are presented to define the shear modulus ( $G$ ), and material damping ratio ( $D$ ) versus shearing strain amplitude ( $\gamma$ ) curve for each sample. Properties of each soil specimen and applicable test conditions are summarized in Table 1. At lower shearing strain levels ( $<10^{-1}\%$ ) shear modulus and material damping computed for the three different cycle conditions produce similar results for all unit weights, while at higher strains ( $>10^{-1}\%$ ) for the densest material ( $16.8 \text{ kN/m}^3$ ) there is a tendency for the "before peak" cycle to produce higher shear modulus and lower damping.

Cyclic triaxial modulus and material damping test results obtained utilizing sinusoidal and random displacement-time histories on both undisturbed and remolded silty sand material are compared in Fig. 6. The random displacement modulus and material damping curves presented in Fig. 6 are the average curves drawn through data points representing the three hysteresis loops: (1) before peak, (2) peak, and (3) after peak. The sinusoidal displacement-time cyclic triaxial test was conducted on a natural intact sample. In contrast, the random displacement-time cyclic triaxial test utilized a remolded soil sample ( Fig. 4 ).

At lower shearing strain levels ( $<10^{-1}\%$ ) the shear modulus determined by either sinusoidal or random displacement time histories for this specimen produced similar results, while at higher strains ( $>10^{-1}\%$ ) the shear modulus determined by the random procedure was lower. In contrast, the sinusoidal and random displacement-time histories produced similar material damping results at low shearing strain levels ( $<10^{-1}\%$ ) but at higher strain ( $>10^{-1}\%$ ) material damping determined by the random procedure was higher.

## SUMMARY AND CONCLUSIONS

Silty sand material was remolded using a technique which gave a formation factor similar to a natural undisturbed specimen. Remolded specimens produced in this manner were tested using a cyclic triaxial apparatus to evaluate modulus and damping results under a random displacement time history. An undisturbed specimen was also tested using a sinusoidal displacement

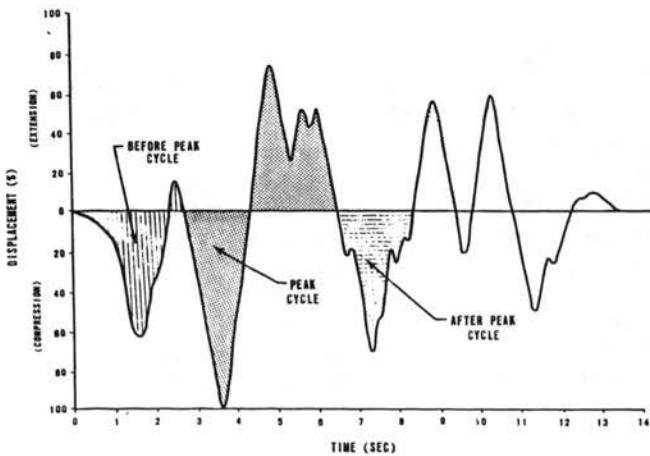


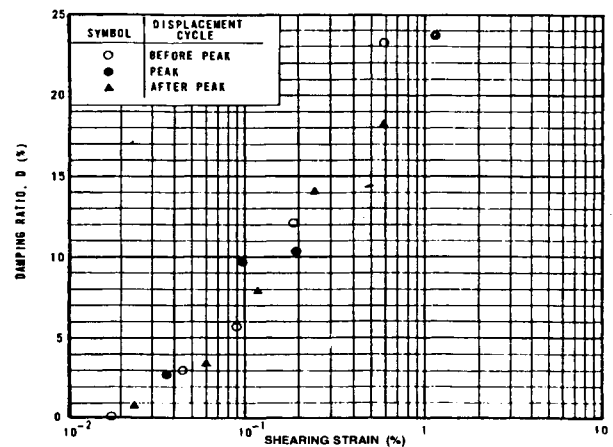
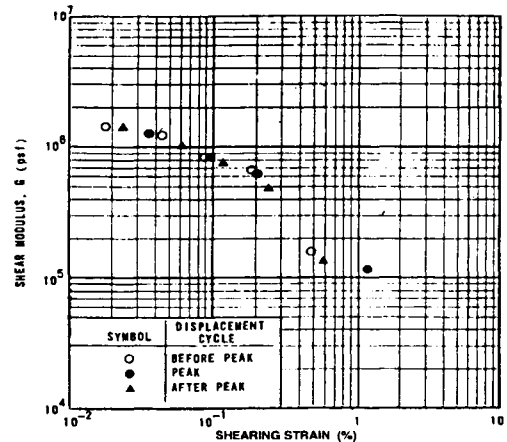
Fig. 2. Displacement Time History

The sinusoidal and random displacements were placed on the specimen using an electro-hydraulic MTS system in conjunction with MTS Model 411 Arbitrary Function Generator.

time history. Based on the above study the following conclusions can be reached.

1. Remolded samples tested using a random displacement technique produce similar shear modulus and material damping results as an undisturbed sample tested using sinusoidal displacement for shearing strains less than  $10^{-1}$  %. At higher strains ( $>10^{-1}$ %) the shear modulus was lower and material damping was higher when using the random procedure.

2. For remolded samples at lower shearing strain levels ( $<10^{-1}$ %) the shear modulus



Note: 1 psf = 994 kPa

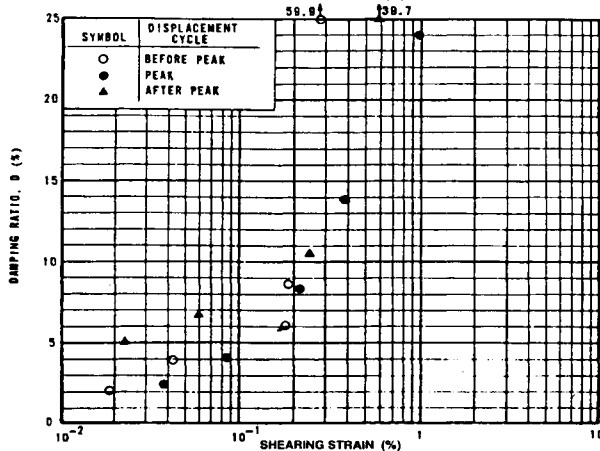
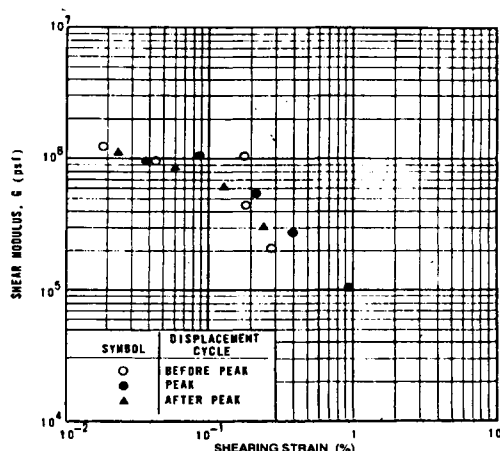
Fig. 4. Random Displacement Cyclic Properties Test, ML, Dry Unit Weight =  $16.6 \text{ kN/m}^3$   
 $w = 21.1\%$ , Effective Stress = 145 kPa

and material damping computed for hysteresis loops before peak, peak and after peak produce similar results for unit weights ranging from  $15.7 \text{ kN/m}^3$  to  $16.8 \text{ kN/m}^3$ . For higher strains ( $>10^{-1}$ %) there is a tendency for the densest material studied ( $16.8 \text{ kN/m}^3$ ) to produce a higher shear modulus and lower material damping for the before peak cycle.

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Note: 1 psf = 994 kPa

Fig. 3. Random Displacement Cyclic Properties Test, ML, Dry Unit Weight =  $15.7 \text{ kN/m}^3$   
 $w = 17.3\%$ , Effective Stress = 145 kPa

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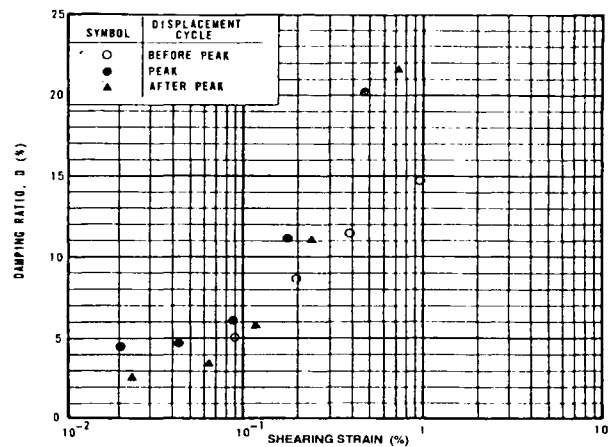
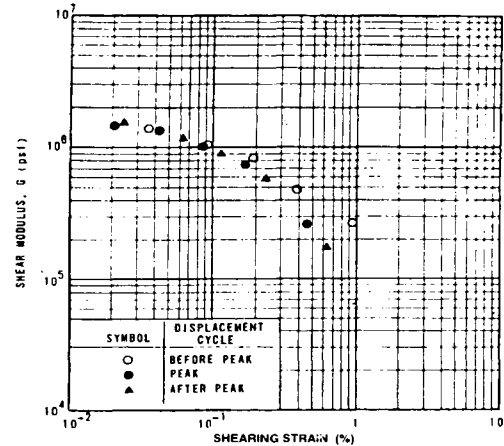
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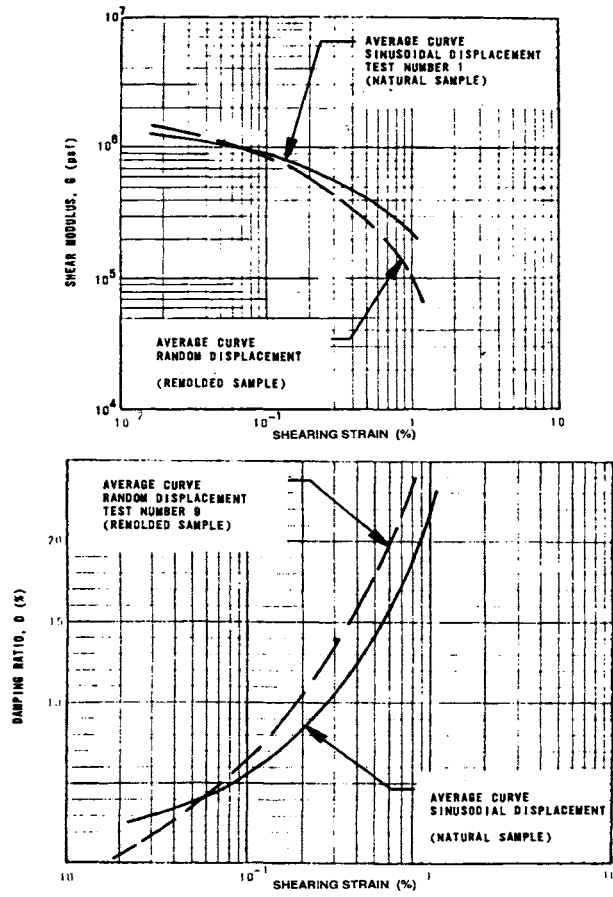


Note: 1 psf = 994 kPa

Fig. 5. Random Displacement Cyclic Properties<sub>3</sub>, Test, ML, Dry Unit Weight = 16.8 kN/m<sup>3</sup>, w = 15.5 %, Effective Stress = 145 kPa

TABLE I. Summary of Test Samples

Test Sample/ Loading	Dry Unit Weight (kN/m <sup>3</sup> )	Compaction Water Content	Void Ratio (e)	Effective Stress (kPa)	Type of Sample
1/Random	16.8	15.5	0.55	145.0	Remold
2/Random	16.6	21.1	0.58	145.0	Remold
3/Random	15.7	17.3	0.66	145.0	Remold
4/Cyclic	16.5	17.3	0.58	145.0	Undist.



Note: 1 psf = 994 kPa

Fig. 6. Comparison of Random and Sinusoidal Displacement Modulus and Damping Curves, ML, Dry Unit Weight  $\approx 16.5 \text{ kN/m}^3$ ,  $w = 17.3 \%$ , Effective Stress = 145 kPa