

# Intercomparison of statistical models for projecting winter oilseed rape yield in Europe under climate change

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# Outline

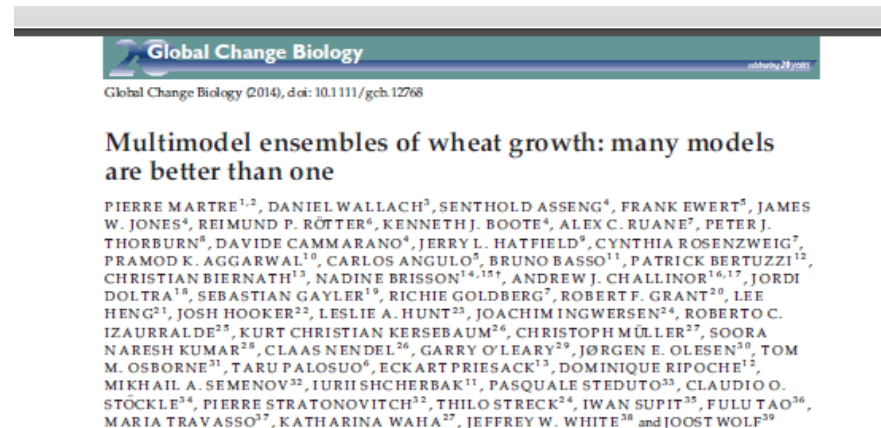
- Introduction
- Materials & Methods
- Results
  - Prediction power
  - Inference power
  - Uncertainty
- Conclusions

# INTRODUCTION

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# Some challenges in crop modelling

- Formulated and fitted to the same data
- Based on the past
- The true model is unknown
- Model uncertainties
- Ensemble models
- Pest & disease



# Process Based Models vs. Statistical models in projecting future yields

Process based models	Statistical models
Include several modules	All-in-one
Dynamic	Static
Based on several valuable studies	Empirical and difficult to interpret without prior knowledge
Require calibration	Easier to use
Complicated	Easily understandable
Uncertainty analysis is difficult	Uncertainty analysis can be done easily
Pest & disease correlation with climate variation is often absent	They can indirectly show some "hidden" correlations

# Application of statistical methods in yield predictions: Previous studies

- Ordinary Least Squares regression
  - Some studies using quadratic terms/ other regression techniques
- Limited to annual or seasonal averages (of temperature and precipitation)
- No systematic intercomparison of statistical techniques
- Less focus on uncertainty analysis

# MATERIALS & METHODS

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# Data

- Climate data
  - Daily temperature, precipitation, radiation
    - Monthly (3\*12 parameters) and fortnightly (3\*26 parameters) averages over the daily climatic data
- Winter oilseed rape (yield and sowing date)
  - Denmark, Germany, Czech, (France, Belgium)
  - More than 1000 unique (site/year) observations
  - Covering more than 20 years of data up to 2013



# Response function

$$\begin{aligned} \text{Yield} = & T_1 * \text{TEMP}_1 + \dots + T_n * \text{TEMP}_n \\ & + P_1 * \text{PREC}_1 + \dots + P_n * \text{PREC}_n \\ & + R_1 * \text{RAD}_1 + \dots + R_n * \text{RAD}_n \\ & + \text{YE} * \text{Year} \end{aligned}$$

Monthly resolution: 37 parameters

Forthnightly resolution: 79 parameters

# Regression Techniques

- Ordinary Least Squares
- Stepwise regression
- PCR
- PLSR
- Shrinkage methods
  - Ridge
  - Elastic Nets (with alpha values of 0.25, 0.50 and 0.75)
  - Lasso

(R Packages: stats, glmnet, pls)

# Intercomparison

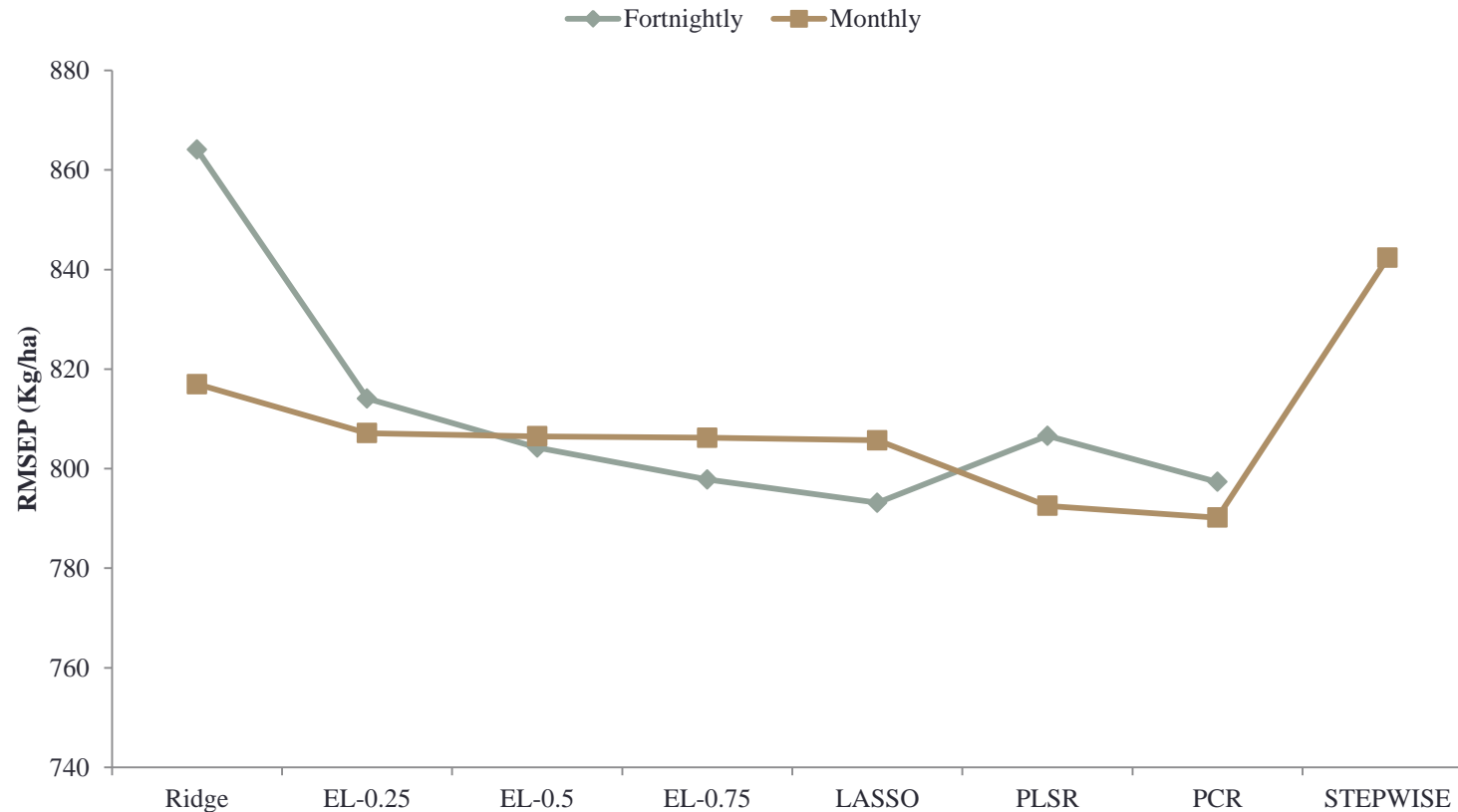
- Prediction
  - Hold-one-year-out for cross validation
- Inference
  - Features remaining in the final models

# RESULTS

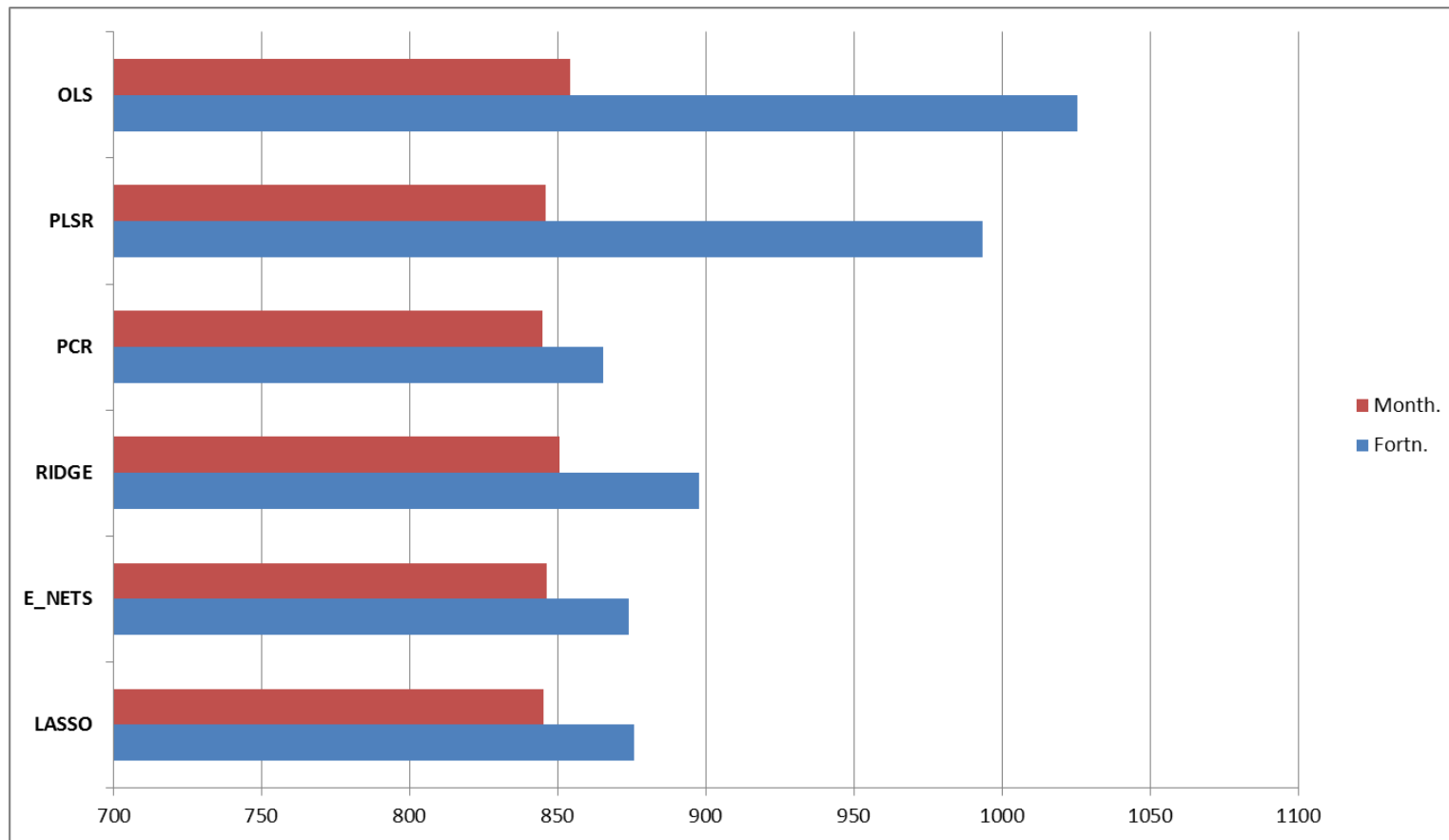
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Prediction power

# Root Mean Squared Error of Prediction - Denmark



# Root Mean Squared Error of Prediction – All countries



# RESULTS

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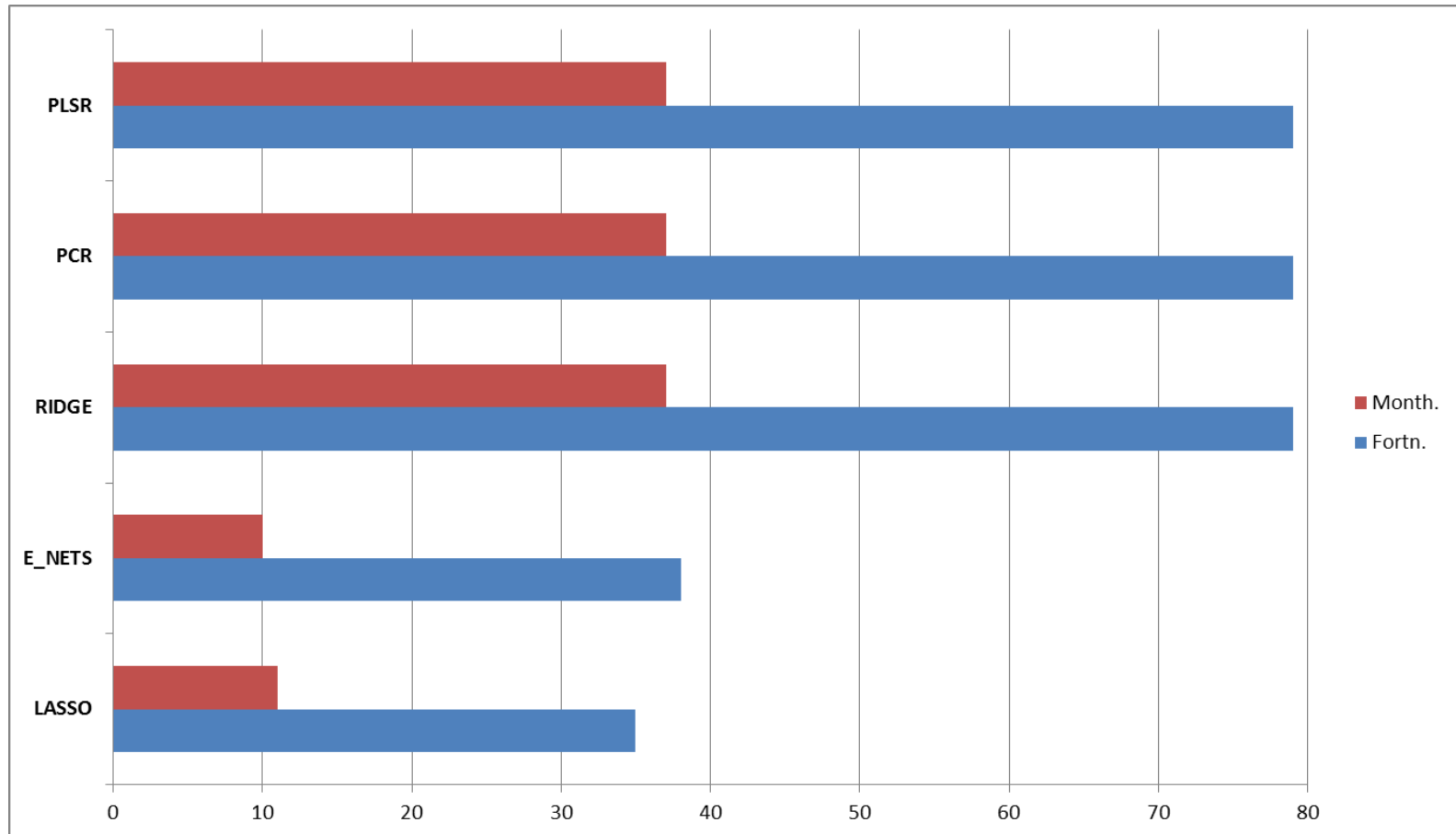
Inference power

# Estimated Coefficients - Denmark

Start Date	01-08	15-08	29-08	12-09	26-09	10-10	24-10	07-11	21-11	05-12	19-12	02-01	16-01	30-01	13-02	27-02	12-03	26-03	09-04	23-04	07-05	21-05	04-06	18-06	02-07	16-07		
End Date	14-08	28-08	11-09	25-09	09-10	23-10	06-11	20-11	04-12	18-12	01-01	15-01	29-01	12-02	26-02	11-03	25-03	08-04	22-04	06-05	20-05	03-06	17-06	01-07	15-07	29-07		
<b>Temperature</b>																												
RIDGE																				32	24	25		4	-18	-2	2	-2
ELNET - Alpha =0.25																				44	29	20						
ELNET - Alpha =0.50																				31	39	13						
ELNET - Alpha =0.75																				22	48	10						
LASSO																				17	53	8						
PLSR	10	10	10	4	-1	-7	-16	12	0	-4	16	8	-13	-9	-3	-13	1	-2	13	11	12		0	-8	0	-7	-4	
PCR	9	10	7	5	1	-11	-15	11	-7	-9	9	9	-20	-6	-6	-18	1	-1	12	4	7		2	0	1	-5	-2	
OLS	9	-18	232	-212	-111	135	13	-68	-36	85	-3	-51	94	24	51	-49	203	-171	12	-150	<u>425</u>		67	-73	208	-87	-263	
STEPWISE			144	-203	-126	101							70				108	-100			354			136			-285	
<b>Radiation</b>																												
RIDGE	4	-17	-7	8	32	24	-27	-70	60	2	-29	-93	13	11	9	14	10	9	16	6	-3		5	-2	-6	-2	-2	
ELNET - Alpha =0.25	3				37			-57											17									
ELNET - Alpha =0.50	6				34			-13											12									
ELNET - Alpha =0.75	9				32														10									
LASSO	11				31														8									
PLSR	16	-5	0	10	10	6	1	-3	0	1	-2	-1	2	-2	0	6	8	2	18	8	4		3	-7	-8	-12	-5	
PCR	16	-3	2	13	8	8	3	-2	0	2	-2	0	4	-1	-4	11	10	-4	16	11	0		7	-3	-6	-12	-1	
OLS	60	98	83	-67	84	-32	-195	-373	73	-216	399	-507	-48	<u>381</u>	-12	-16	-14	-44	<u>132</u>	-15	<u>-129</u>	<u>-108</u>		13	-19	25	113	
STEPWISE			62		162			-397		-496				432					95		-99	-91					82	
<b>Precipitation</b>																												
RIDGE	13	-2	-21	<u>-19</u>	-7	3	-9	<u>-29</u>	8	-9	-19	-1	-6	6	<u>-32</u>	-15	-6	-1	-1	-20	-11		-5	12	1	1	21	
ELNET - Alpha =0.25			-7	<u>-30</u>				<u>-47</u>													-2							
ELNET - Alpha =0.50				<u>-34</u>				<u>-35</u>																				
ELNET - Alpha =0.75				<u>-36</u>				<u>-28</u>																				
LASSO				<u>-37</u>				<u>-23</u>																				
PLSR	2	-2	-7	<u>-12</u>	-3	1	-12	<u>-9</u>	0	-2	-2	2	-3	0	-11	-6	-1	1	-3	-4	-4		-4	2	1	0	5	
PCR	-3	2	-3	<u>-6</u>	-5	2	-7	<u>-5</u>	-2	-2	0	4	-4	0	-9	-6	-2	3	-4	-5	-1		5	3	2	3	4	
OLS	51	-56	-46	<u>-28</u>	2	10	-47	<u>-81</u>	25	59	43	-86	83	57	<u>-190</u>	-75	156	124	8	<u>-277</u>	-32		-2	32	-79	52	<u>138</u>	
STEPWISE			-41	<u>-74</u>				<u>-142</u>						-104	143	<u>-122</u>		173	119		-200				-78		126	



# Number of Significant Features in the final model - Czech



# RESULTS

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## Uncertainties

# Variance Decomposition – Yield projection under climate change

$$\begin{aligned} V(Y) = & V_M[E_{\varepsilon, \theta}(Y|M)] \\ & + E_M[V_{\theta}(E_{\varepsilon}(Y|M, \theta))] \\ & + E_M[E_{\theta}(V_{\varepsilon}(Y|M, \theta))] \end{aligned}$$

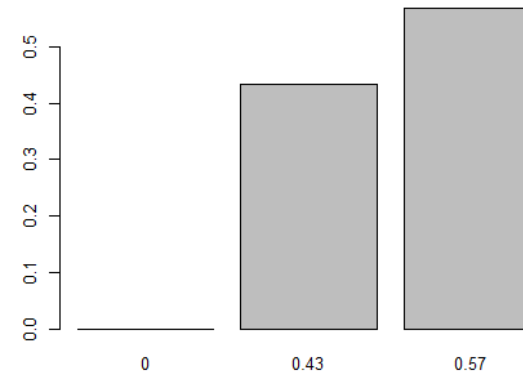
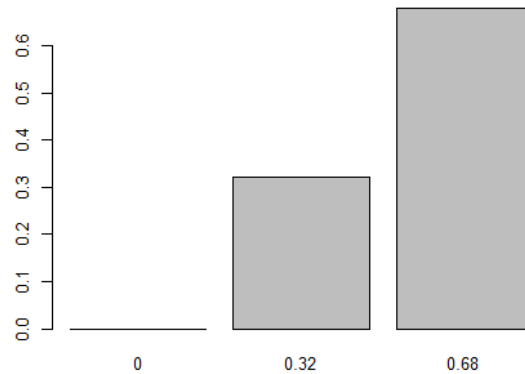
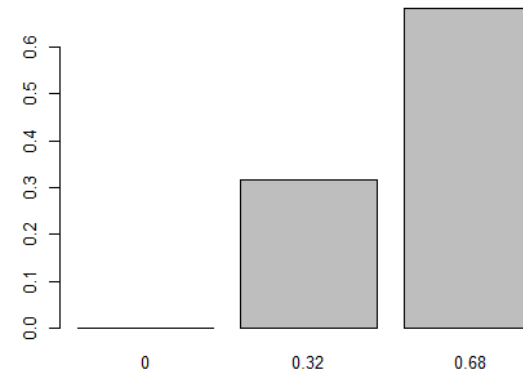
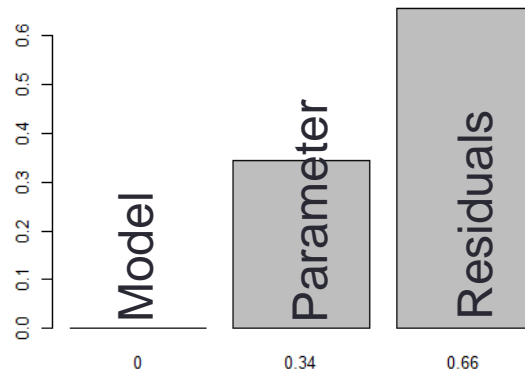
Where

M: Model

$\theta$  : Set of parameters

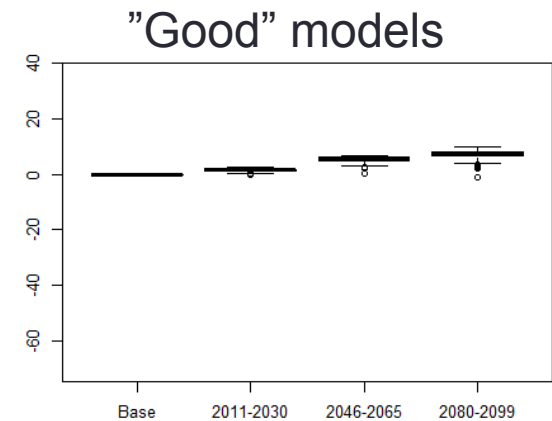
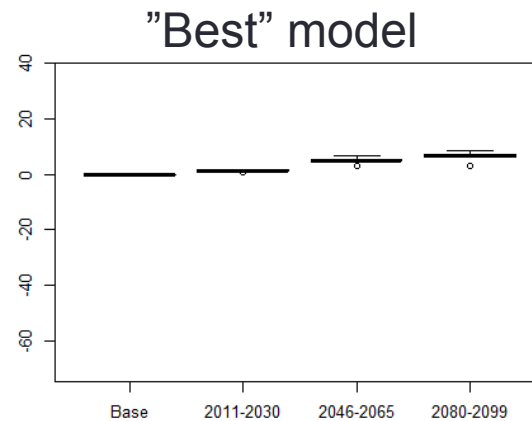
$\varepsilon$  : Residual errors

# Variance decomposition - Czech

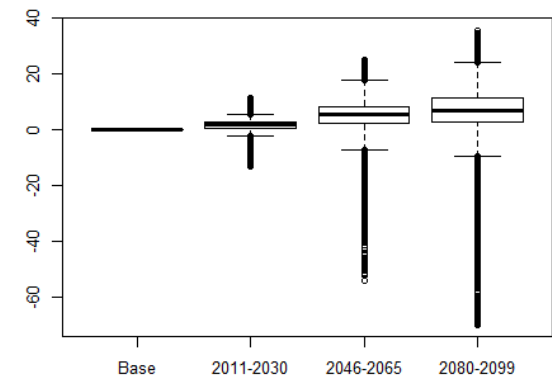
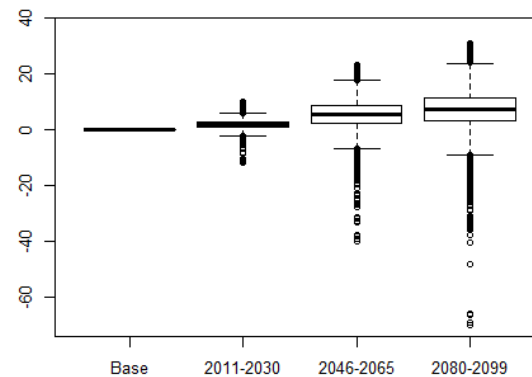


# Effect of model and parameter uncertainty percent of yield change predictions - Czech

Main Sample



bootstrapping



# Conclusions

- State-of-the-art regression techniques could be useful, both in prediction and inference.
- Regression techniques can be useful in pointing out which climatic factors are influential for yield during which growth phases
- Cross-validation of regression models across space (between countries) can provide a method for validating validity for use in climate change projections
- Regression techniques offer a direct method for addressing parameter uncertainty

# THANK YOU!

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