

## Cut wires grating — single longitudinal wire” planar metastructure to achieve microwave magnetic-type resonance in a single wire

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### Abstract

Here we present new metastructures consisting of a cut-wire grating and a single nonmagnetic longitudinal cut-wire orthogonal to grating's wires. Experimental investigations at microwaves show that these structures can provide strong magnetically-induced resonant response of the longitudinal cut-wire depending on the geometry in the case when a metastructure is oriented along the direction of the wave propagation and the cut-wires of the grating are parallel to the electric field of the incident plane electromagnetic wave. It is supposed that this response is due to the excitation of resonant currents by magnetic field of surface polaritons in many equivalent spatial *LC-circuits* formed by cut-wire pairs of the grating and sections of the longitudinal cut-wire. Three resonant effects have been separately observed and identified by measurements in waveguides, cutoff waveguides and free space. These effects are connected with the grating, *LC-circuits* and the longitudinal cut-wire. To distinguish and tune the resonances we use split cut-wires loaded with varactor diodes.

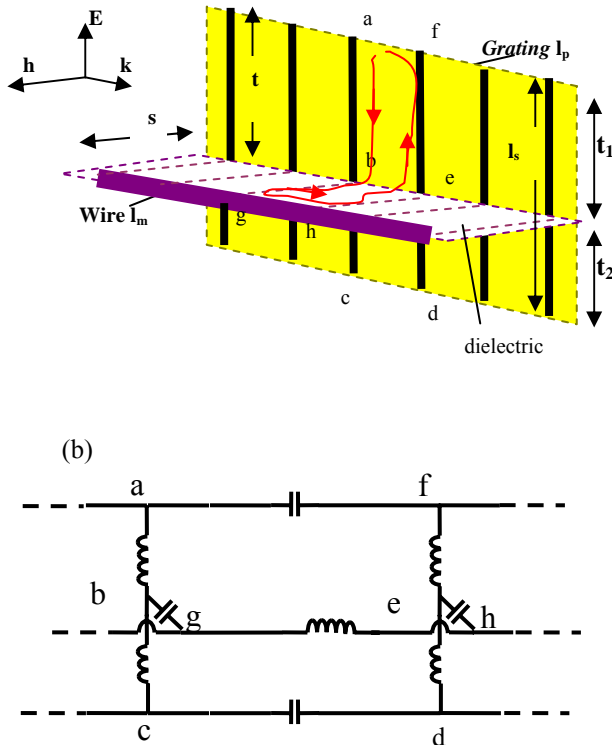
### 1. Introduction

We know, at microwaves metamaterials with conductive nonmagnetic chiral inclusions, can possess an effective magnetic permeability, which depends on the orientation of the inclusions with respect to the magnetic field  $\mathbf{h}$  of the incident electromagnetic wave. Resonance phenomena are caused by the excitation of resonance currents by the field  $\mathbf{h}$ . Presently extensive investigations are directed toward the development of magnetic metamaterials containing technologically simple linear nonmagnetic wires to apply in dispersion engineering [1]. The main attention is devoted to a cut-wire pair that possesses both the electric and magnetic responses due to the possibility of parallel currents induction by the electric field and antiparallel currents, by the magnetic field [2, 3]. Since the magnetic and electric resonance responses are generated practically at the same frequency, it is difficult to separate these signals and evaluate the magnetic contribution. Term “parallel currents” means that induced currents in parallel wires flow in the same direction in contrast to “antiparallel currents”, when induced currents flow in the opposite directions.

In paper [4] it is suggested a new way to create separately a strong microwave magnetically-induced resonance response using nonmagnetic cut-wires. Magnetic nature, magnetically-induced resonant response or magnetic-type resonance means that resonance is due to the excitation of currents by electromotive force which is caused by the alternating magnetic field with accordance of Faraday's law of electromagnetic induction. Reductive expression “excitation of currents by magnetic field”, is used rather often, e.g. [2] and references. Electric-type resonance means that resonance currents are induced by electric microwave field. In [4] it was found in waveguides that a line nonmagnetic wire of length  $l_m$  (fig. 1 a), which is oriented along waveguide axis parallel to the direction of propagation of an electromagnetic wave (and perpendicularly to its electric field  $\mathbf{E}$ ) and arranged asymmetrically near a grating of cut-wires  $l_p$  (*Grating*), can exhibit a resonance response of magnetic nature. *Grating* (wires  $l_p$  are parallel to the incident electric field  $\mathbf{E}$ ) forms surface polaritons below the resonance frequency in dependence on length  $l_p$ . Without the *Grating* there is no response of longitudinal wire  $l_m$ . Asymmetrical location corresponds to the position of longitudinal cut-wire  $l_m$ , when distance  $t_1 \neq t_2$  in contrast to symmetrical location when  $t_1 = t_2$ . A giant resonance is observed in longitudinal single cut-wire  $l_m$  of a definite (resonance) length in a certain frequency range corresponding to the existence of surface polaritons. In this paper we investigate experimentally this very interesting phenomenon in waveguides (WG), cutoff waveguides (cutoff WG) and free space depending on the geometry. We suggest and verify a concept of magnetically-induced response based on possibility of resonant currents induction by magnetic field of surface polaritons in many spatial *LC-circuits* formed by *Grating's* cut-wire  $l_p$  pairs and sections of the longitudinal cut-wire  $l_m$ . In *LC-circuits* antiparallel currents flow in adjacent wires  $l_p$  while like-directed currents flow along the longitudinal cut-wire  $l_m$ . In this paper we demonstrate and identify three separately observed resonant effects. The first resonance is due to parallel currents induction in *Grating's* wires, the second resonance effect is due to the excitation of resonance currents in *LC-circuits* and the third resonance is due to the resonance current along longitudinal cut-wire  $l_m$ . Varactor-loaded split cut-wires are applied to tune and distinguish the resonances.

## 2. Investigated metastructures. Concept of the magnetically-induced response

Investigated metastructures consist of a grating of cut parallel copper wires with length  $l_p$  (*Grating*) and a single nonmagnetic (copper) longitudinal cut-wire (length  $l_m$ ) which is placed perpendicularly to wires  $l_p$  on distance  $s$  (**fig. 1a**). One can imagine the metastructure as matter with many *LC-circuits* formed by cut-wire pairs of the *Grating* and sections of the longitudinal cut-wire. In the case when metastructure is placed along propagation direction magnetic-type resonance effects are observed. Obtained results allow to suggest a concept of the resonance responses. Metastructures “*Grating* - single longitudinal cut-wire”, “*Wire pair* - longitudinal cut-wire”, “*Grating* - parallel cut-wire” are investigated depending on geometry. Metastructures with varactor-loaded split longitudinal cut-wire and split parallel cut-wire are also investigated.



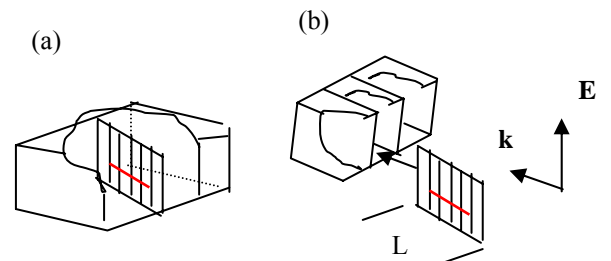
**Fig. 1a,b.** “*Grating* - single longitudinal cut-wire” metastructure (a) and its equivalent electric diagram (b).

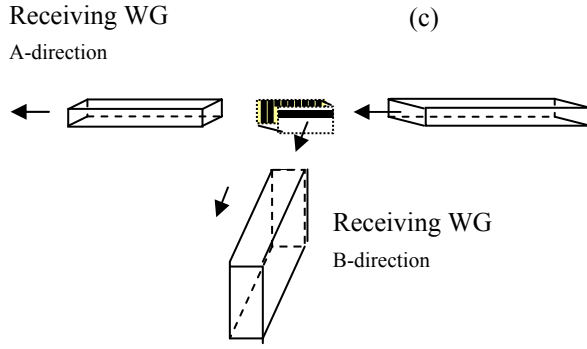
## 2.1 Measurements methods (waveguides, free space)

We have measured frequency dependence of the transmission coefficient  $T$  of electromagnetic wave of metastructures with panoramic standing-wave-ratio and attenuation meters R2-5 3 (3 -6 GHz) and R2-6 1 (8 -12 GHz). Metastructures are arranged along the  $a$  axis and oriented parallel to the side wall of a standard rectangular waveguide (**fig. 2a**). Besides we have measured frequency dependence of the transmission coefficient  $T$  of electromagnetic wave with metastructures arranged in below-cutoff rectangular section. The measurements were performed in frequency range 3-6 GHz, in this case we used WG (48 x24 mm) and a below-cutoff rectangular section (16x24 mm). We have also used a standard waveguide (23x10 mm) and a below-cutoff rectangular section (8x10mm) to measure transmission in frequency range 8-12 GHz. To prepare below-cutoff rectangular section a fragment of the main WG (of the length  $L=25$ mm) is divided into three sections by metal spacers parallel to the direction of wave propagation. Investigated metastructure is placed into a central cutoff rectangular section (**fig. 2b**).

A comparative analysis of the signal transmission spectra in the main and below-cutoff rectangular section is an important method of identification of the type of excited resonance [ 5]. For example, in the case of magnetic excitation (magnetic-type resonance in WG, **MR**) the transparency band in cutoff WG is observed above the **MR** frequency. In addition, the magnetic excitation is characterized by the presence of super-forbidden band below the **MR**. In the case of electric excitation (electric-type resonance, **ER**), the transparency band in cutoff WG is observed below the **ER** frequency.

We have also measured the frequency dependence of the transmission coefficient  $T$  of metastructures arranged in free space in the gap between transmitting and receiving waveguides for two cases. In the first case receiving and transmitting WG are placed along the same axis ( $A$  - direction). In the second case receiving WG is placed along transverse  $B$ -direction (**fig. 2c**).



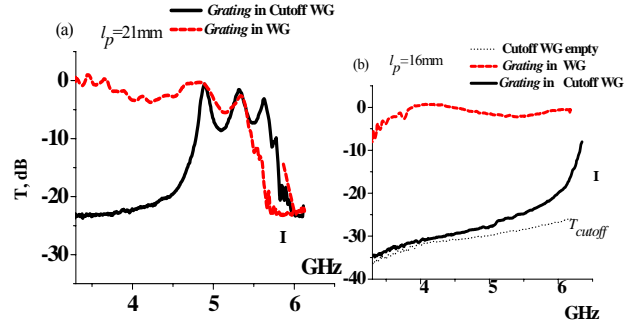
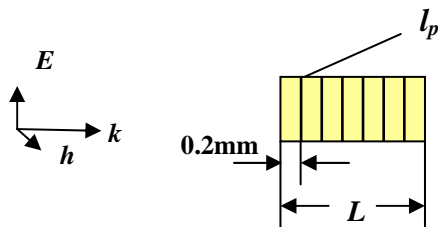


**Fig. 2.** Metastructure in (a) WG, (b) below-cutoff rectangular section and (c) free space.

## 2.2. Experimental verification

### 2.2.1. “Grating - single longitudinal cut-wire” metastructure

Below we present results of investigation of metastructure “Grating - single longitudinal cut-wire” (Fig. 1a), like [4], placed along propagation direction of electromagnetic wave and engineered to have magnetic resonance properties using only cut-wires,  $l_p$  and  $l_m$  are lengths of grating’s wire and longitudinal cut-wire,  $s$  – distance between Grating  $l_p$  and single wire  $l_m$ . Grating (wires  $l_p$  are parallel to the  $\mathbf{E}$ -field) exhibits a resonance response, which is manifested by resonance  $\mathbf{I}$  of the electric-type and characterized by a resonance dependence of the transmission coefficient with a minimum at a certain frequency dependent on the wire  $l_p$  length. This Grating is excited by the  $\mathbf{E}$ -field (induction of parallel currents) and generates surface waves (polaritons) near resonance  $\mathbf{I}$  (below the resonance frequency). Local transverse magnetic field of polaritons induces electromotive forces and resonance currents in many spatial LC-circuits (such as  $abghefa$  and  $cdehgbc$  created from cut-wire pairs of Grating and sections of longitudinal cut-wire) and resonance current along longitudinal cut-wire.



**Fig. 3.** Frequency dependences of  $T$  in the WG (dashed curves) and cutoff WG (solid curves) in the presence of (a) Grating of  $l_p=21\text{mm}$  and (b) Grating of  $l_p=16\text{mm}$ .

Equivalent electric diagram is shown in Fig. 1b. Directions of currents which flow in many LC-circuits  $abghefa$  are the same along wire  $l_m$  and opposed to currents of circuits  $cdehgbc$ . In the case of symmetrically located wire  $l_m$  ( $t=l_p/2$ ) these opposed currents along longitudinal cut-wire of circuits  $abghefa$  and  $abghefa$  are practically quenched. In the case of asymmetrically location ( $t=l_p/4$ ), if longitudinal cut-wire length  $l_m$  is resonant the wave of current along wire  $l_m$  and the resonance response are very strong.

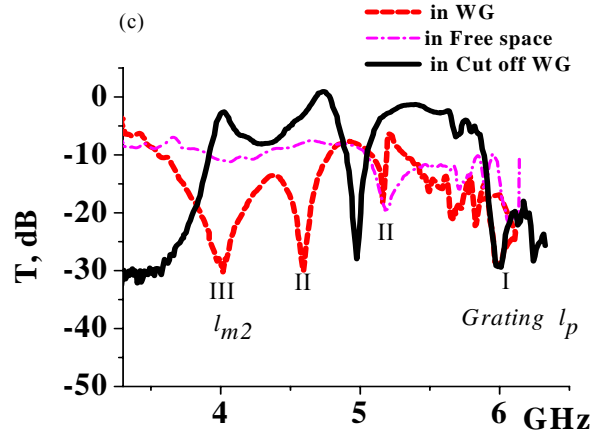
Resonance response of a longitudinal cut-wire  $l_m$  can be detected separately because its resonance frequency depends on length  $l_m$  and distance  $s$  and is different from frequencies of Grating and LC-circuits.

Results of measurements with Gratings without longitudinal wire are presented in Fig 3a,b. These Gratings are used in metastructures to achieve resonance effects in range 3 – 6 GHz. Grating with  $l_p=21\text{mm}$  allows to observe resonance effects connected with both Grating, LC-circuits and longitudinal cut-wire  $l_m$ . Grating with  $l_p=16\text{mm}$  is selected so as to shift resonance  $\mathbf{I}$  to high-frequency edge of the interval of measurements and do not overlap with resonance connected with longitudinal cut-wire  $l_m$ . Fig. 3a shows the frequency dependences of transmission  $T$  measured in the presence of Grating of wires  $l_p=21\text{mm}$ , for which resonance  $\mathbf{I}$  is observed in the WG at 6 GHz and pass-band is observed in the cutoff WG section at frequencies below the resonance. Fig. 3b shows corresponding frequency dependences of  $T$  measured in the presence of Grating of wires  $l_p=16\text{mm}$ , for which resonance  $\mathbf{I}$  and pass-band (below  $\mathbf{I}$ ) are observed above 6 GHz in the WG and cutoff WG. Position of pass-band below the resonance  $\mathbf{I}$  specifies electric excitation and electric-type resonance of the Grating.

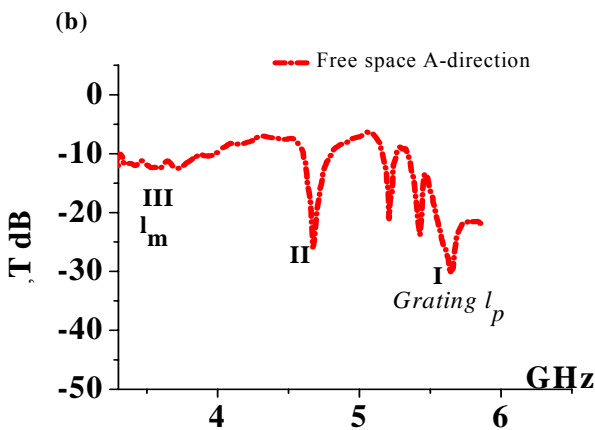
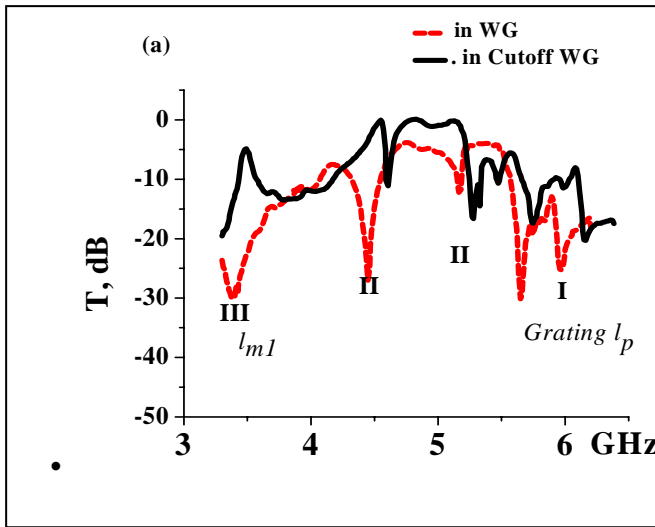
Now let us consider the results of measurements in the presence of metastructure “Grating - single longitudinal cut-wire”. In fig. 4ab we see frequency dependences of transmission  $T$  measured in WG, cutoff WG and in free space in the presence of metastructures “Grating - single longitudinal cut-wire” with the same  $l_p=21\text{mm}$ ,  $s=0.2\text{mm}$ ,  $t=l_p/4$  and  $l_m=26\text{mm}$ . In this case in addition to resonance  $\mathbf{I}$

of the *Grating* of wires  $l_p$  the metastructure exhibits magnetic-type resonances **II** (of *LC-circuits*) and **III** (of single longitudinal cut-wire  $l_m$ ), **fig. 4a**. The below-cut off section exhibits, besides pass-band due to *Grating*  $l_p$ , a new transparency band that extends from resonances **III** and **II** toward high-frequency region. Such position of pass-bands identifies magnetic excitation and magnetic-type of the resonance (**MR**). The resonance **II** is due to resonance currents in *LC-circuits* excited by transverse magnetic field of polaritons and resonance **III** is due to the total contribution of currents of *LC-circuits* along longitudinal cut-wire  $l_m$ . Circular currents in *LC-circuits* form magnetic moments; resonance current in longitudinal cut-wire  $l_m$  induces electric dipole moment.

How can we make out the difference between resonances **II** and **III** and distinguish the resonance **III** of longitudinal cut-wire  $l_m$ ? One can easily do it by measurement of transmission  $T$  in free space (A-direction). In this case (**fig. 4b**) the resonance response of longitudinal cut-wire  $l_m$  in A-direction is practically not entered in contrast to responses of *Grating*  $l_p$  and *LC-circuits*. There is also the way to mark out the resonance response of a longitudinal cut-wire applying varactor diodes (see part 2.3).



**Fig.4a,b,c.** Frequency dependences of  $T$  in the presence of “*Grating* -single longitudinal cut-wire” metastructure with  $l_p=21\text{mm}$ ,  $s=0.2\text{mm}$  in WG (dashed) and cutoff WG (solid), in free space (dash dot): (a)  $l_{m1}=26\text{mm}$  and (b) free space (A-direction), (c)  $l_{m2}=24\text{mm}$



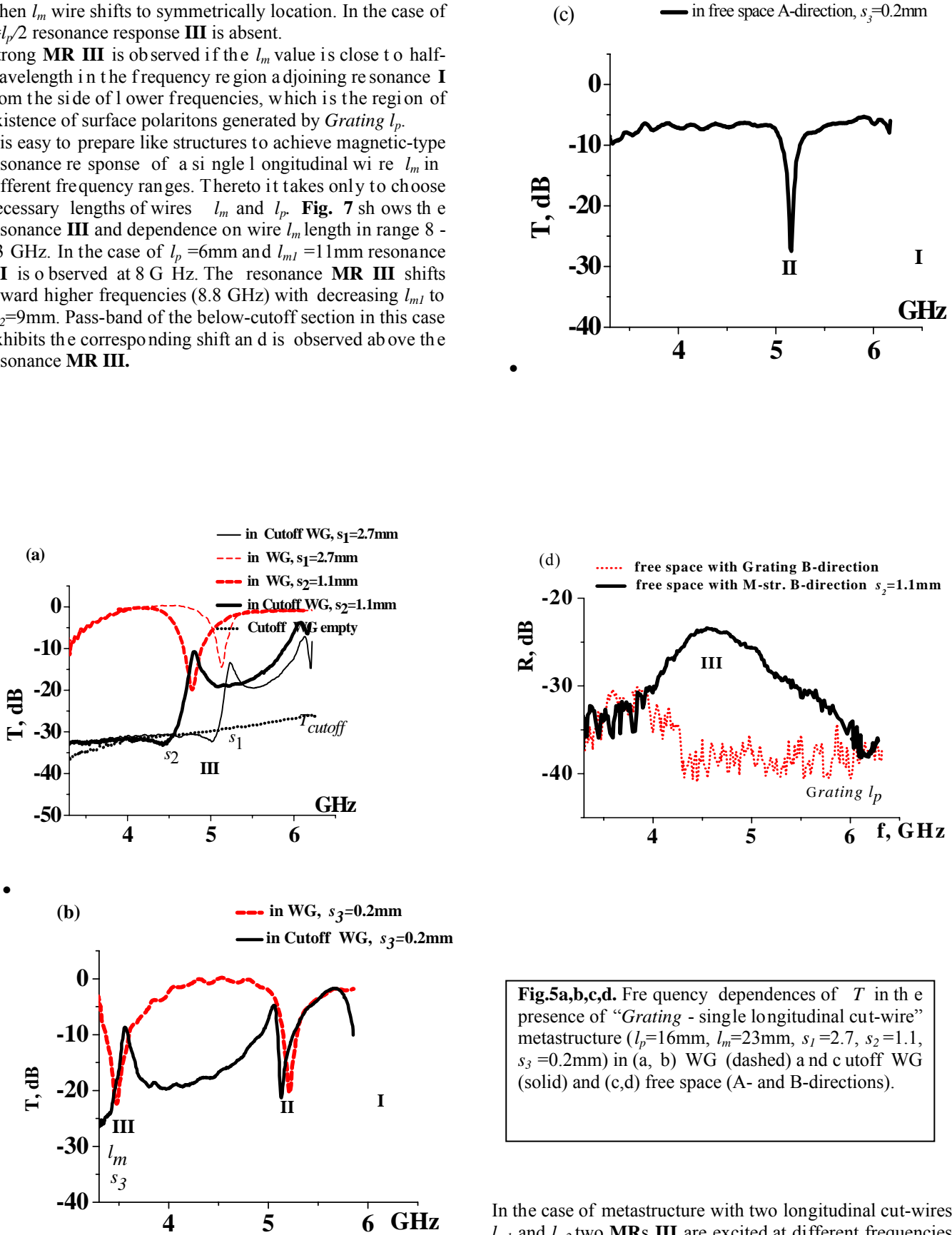
The position of resonance **MR III** depends on length  $l_m$ . The resonance **III** is observed at frequency 3.4 GHz in the case of  $l_{m1}=26\text{mm}$  (**fig. 4a**). With decreasing  $l_m$  to  $l_{m2}=24\text{mm}$  resonance **MR III** shifts to higher frequencies and observed at 4 GHz (**Fig. 4c**).

**Fig. 5** shows frequency dependences of transmission measured in WG and cutoff WG (a, b) and in free space (c, d) in the presence of metastructure “*Grating* - single longitudinal cut-wire” with the same  $l_p=16\text{mm}$ ,  $l_m=23\text{mm}$ ,  $t=l_p/4$  but different distance  $s$ . With  $l_p=16\text{mm}$  it is easy to observe how the resonance **III** shifts in dependence on  $s$  because resonance **I** and corresponding pass-band in cutoff WG would shift to the high-frequency edge of the interval of measurements and do not overlap with magnetic-type resonance **III** related to the  $l_m$  wire. Resonance **III** was excited at 5.1 GHz for a distance of  $s_1=2.7\text{mm}$  and shifted to lower frequencies (4.7 GHz) when  $s_2$  was decreased to 1.1mm (**fig. 5a**). When  $s_3=0.2\text{mm}$  resonance **III** of  $l_m$  wire was observed at frequency 3.5 GHz (**fig. 5b**). The below-cut off section exhibited the corresponding pass-bands (above frequency of the magnetic-type resonance **III** of  $l_m$  wire and super-forbidden bands (below **III**, which occur at about 5 and 4.4 GHz and follow behind the shifting resonance **III**. Resonance **II** related to the *LC-circuits* was depicted at frequency 5.2 GHz in WG and free space (**fig. 5b,c**).

Resonance **III** of  $l_m$  is not depicted in free space in A-direction, but one can observe resonance response in B-direction by measurement of cross-polarized reflected wave from  $l_m$  wire, **fig. 5d**. In this case electric field of reflected wave is parallel to longitudinal cut-wire  $l_m$  and is orthogonal to the  $E$ -field of incident wave.

A strong resonance **III** is observed when the  $l_m$  wire is arranged asymmetrically ( $t=l_p/4$ ), its intensity decreases

when  $l_m$  wire shifts to symmetrically location. In the case of  $t=l_p/2$  resonance response **III** is absent. Strong **MR III** is observed if the  $l_m$  value is close to half-wavelength in the frequency region adjoining resonance **I** from the side of lower frequencies, which is the region of existence of surface polaritons generated by *Grating*  $l_p$ . It is easy to prepare like structures to achieve magnetic-type resonance response of a single longitudinal wire  $l_m$  in different frequency ranges. Thereto it takes only to choose necessary lengths of wires  $l_m$  and  $l_p$ . **Fig. 7** shows the resonance **III** and dependence on wire  $l_m$  length in range 8 - 13 GHz. In the case of  $l_p=6\text{mm}$  and  $l_{m1}=11\text{mm}$  resonance **III** is observed at 8 GHz. The resonance **MR III** shifts toward higher frequencies (8.8 GHz) with decreasing  $l_{m1}$  to  $l_{m2}=9\text{mm}$ . Pass-band of the below-cutoff section in this case exhibits the corresponding shift and is observed above the resonance **MR III**.



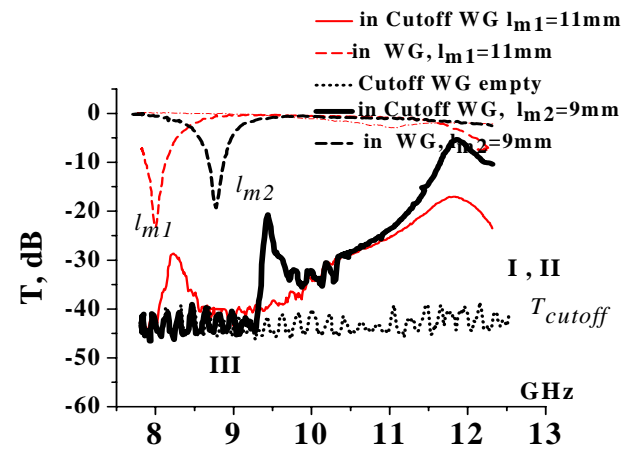
**Fig.5a,b,c,d.** Fre quency dependences of  $T$  in the presence of “*Grating* - single longitudinal cut-wire” metastructure ( $l_p=16\text{mm}$ ,  $l_m=23\text{mm}$ ,  $s_1=2.7$ ,  $s_2=1.1$ ,  $s_3=0.2\text{mm}$ ) in (a, b) WG (dashed) and cutoff WG (solid) and (c,d) free space (A- and B-directions).

In the case of metastructure with two longitudinal cut-wires  $l_{m1}$  and  $l_{m2}$  two **MRs III** are excited at different frequencies and two corresponding pass-bands (in cutoff WG section) appear above the resonances **III** (**fig. 6**). Resonance **MR III** at frequency 4.1GHz is provided by wire  $l_{m1}=25\text{mm}$  and resonance at frequency 5.3GHz is provided by wire

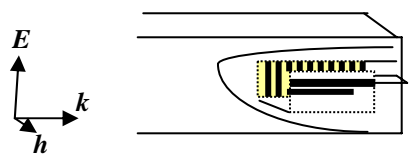


$l_{m2}=21\text{mm}$ . This experimental also confirms connection and dependence of resonance III on wire  $l_m$  length. Position of pass-bands confirms magnetic excitation and magnetic-type of the resonances III.

It is easy to prepare like structures to achieve magnetic-type resonance response of a single longitudinal cut-wire  $l_m$  in different frequency ranges (fig. 7). Thereto it takes only to choose necessary lengths of wires  $l_m$  and  $l_p$ . Fig. 7 shows the resonance III and dependence on wire  $l_m$  length in range 8 - 12 GHz. In the case of  $l_p=6\text{mm}$  and  $l_{m1}=11\text{mm}$  resonance III is observed at 8 GHz. The resonance MR III shifts toward higher frequencies (8.8 GHz) with decreasing  $l_{m1}$  to  $l_{m2}=9\text{mm}$ . Pass-band of the below-cutoff section in this case exhibits the corresponding shift and is observed above the resonance MR III.

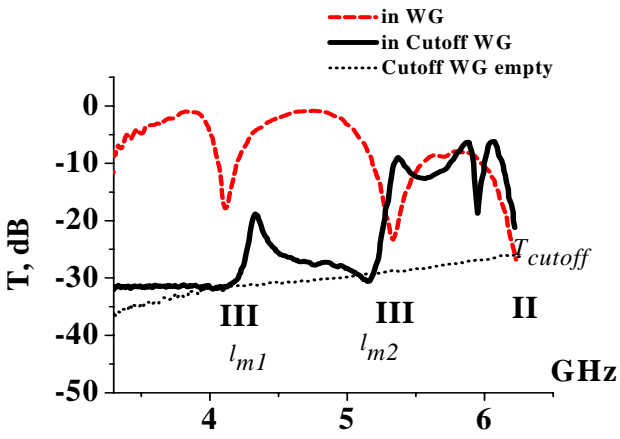


**Fig.7.** Frequency dependences of  $T$  in the WG (dashed) and cutoff WG (solid) in the presence of metastructure “Grating-longitudinal cut-wire” with  $l_p=6\text{mm}$ ,  $s=0.2\text{mm}$ :  $l_{m1}=11\text{mm}$  and  $l_{m2}=9\text{mm}$

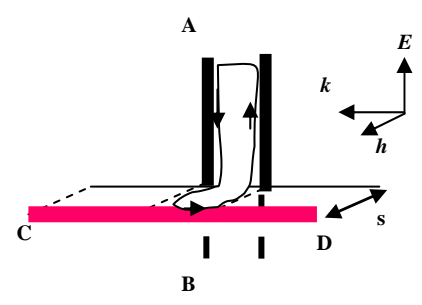


2.2.2. “Wire-pair – longitudinal cut-wire” metastructure

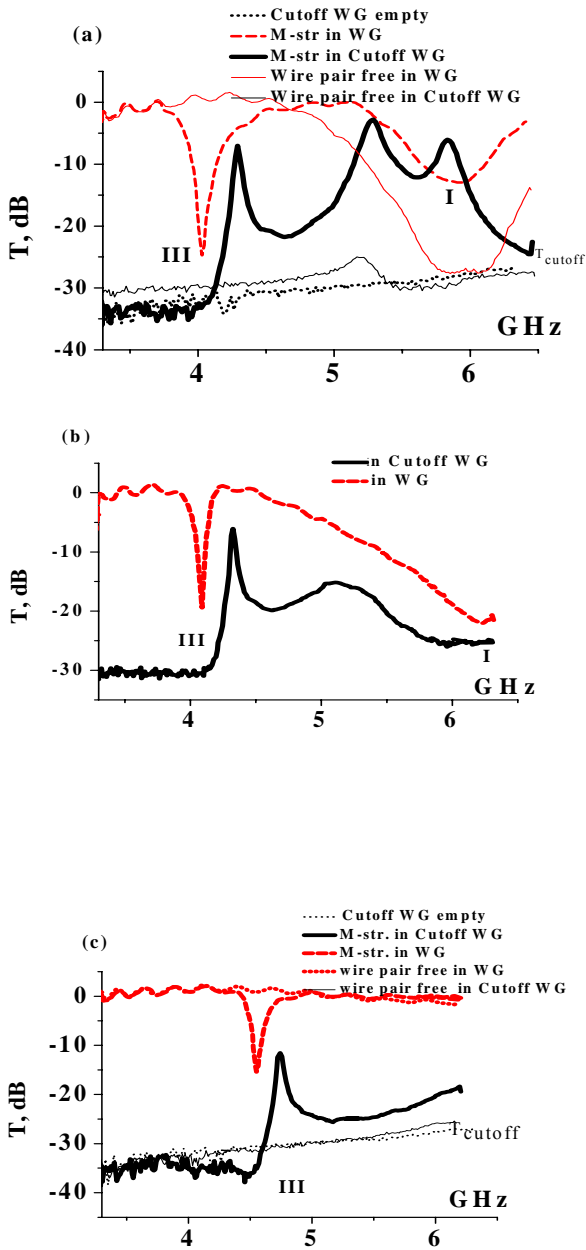
One can imagine Grating  $l_p$  as composition of many wire-pairs and confirm suggested conception by investigation of metastructure consisting one wire pair and longitudinal cut-wire. We investigate metastructure (see fig. 8), created from one pair of cut-wires AB in composition with asymmetrically located longitudinal cut-wire CD orthogonal to AB (wires AB are parallel to the electric field of incident electromagnetic wave). We show that this metastructure can also possess magnetic-type resonance of longitudinal cut-wire CD at frequencies different from electric resonance of cut-wires AB. Conditions to achieve magnetically-induced response and resonance properties are similar to the case of metastructure “Grating-longitudinal cut-wire”. In Fig. 9a we see frequency dependences of transmission  $T$  measured in WG and cutoff WG in the presence of metastructure “Cut-wire pair - longitudinal cut-wire”, distance  $d$  between wires AB is 20mm.



**Fig.6.** Frequency dependences of  $T$  in the WG (dashed) and cutoff WG (solid) in the presence of metastructure with two longitudinal wires  $l_{m1}=25\text{mm}$  and  $l_{m2}=21\text{mm}$ ,  $l_p=16\text{mm}$ ,  $s=1.1\text{mm}$ .



**Fig. 8.** Metastructure “Cut-wire pair - longitudinal cut-wire”



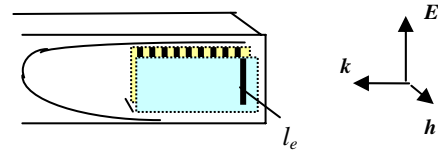
**Fig. 9a,b,c.** Frequency dependences of transmission  $T$  in the WG (dashed bold) and cutoff WG (solid bold) in the presence of metastructure “Cut-wire pair - longitudinal cut-wire”,  $d=20\text{mm}$ ,  $s=1.1\text{mm}$ : (a)  $l_{CD}=29\text{mm}$ ,  $l_{AB}=25\text{mm}$ , (b)  $l_{CD}=29\text{mm}$ ,  $l_{AB}=22\text{mm}$ , (c)  $l_{CD}=26\text{mm}$ ,  $l_{AB}=19\text{mm}$

We observe in WG electric resonance **I** related to the wire pair **AB** without longitudinal wire **CD** at 6 GHz and corresponding pass-band in cutoff WG (below resonance **I**). In addition with “Cut-wire-pair - longitudinal cut-wire” metastructure we observe magnetic-type resonance **III** related to wire **CD** and corresponding pass-band in cutoff WG (above the resonance **III**), fig. 9a. With decreasing of

the length  $l_{AB}$  resonance **I** shifts to the high-frequency edge of the interval of measurements and do not overlap with magnetic-type resonance **III** related to the **CD** wire (Fig. 9 b,c).

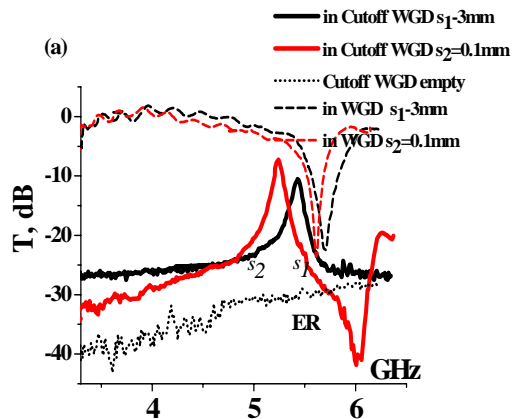
### 2.2.3. “Grating – parallel cut-wire” metastructure

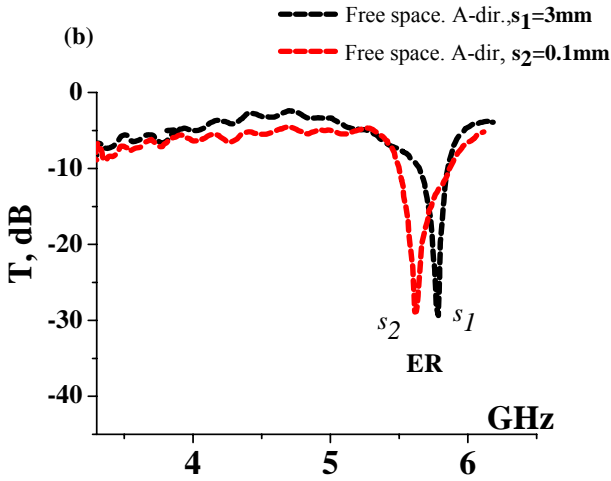
Let us consider “Grating - single parallel cut-wire” metastructure created from grating of wires  $l_p$  and a cut-wire (marked  $l_e$ ) located parallel  $l_p$  on distance  $s$  (Fig. 10.)



**Fig. 10.** Metastructure “Grating-parallel cut wire”

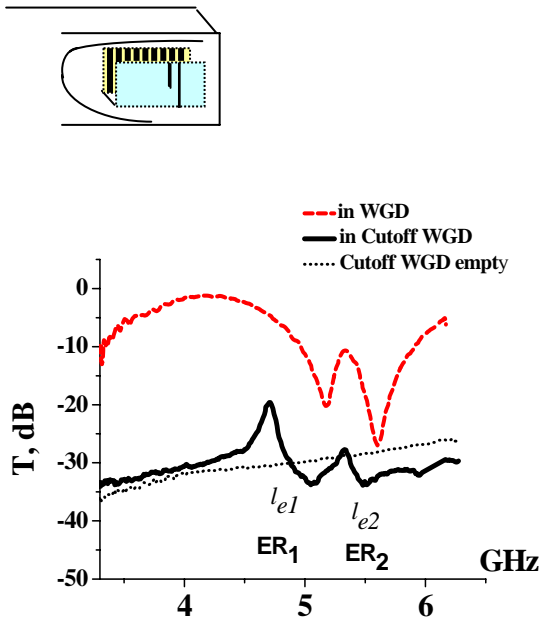
In this case electric-dipole resonance (**ER**) is excited, which depends on the wire length ( $l_e$ ) and can be observed both with and without Grating  $l_p$ . The below-cutoff section exhibits a pass-band, which situated below the **ER** frequency and is characteristic of the electric excitation. In the case of strong change of distance  $s$  resonance frequency related to  $l_e$  wire is not practically shifted (Fig. 11) in contrast to **MR** frequency related to  $l_m$  wire (Fig. 5a,b).





**Fig. 11.** Frequency dependences of transmission  $T$  in the presence of “Grating-parallel cut-wire” metastructure,  $l_p=16\text{mm}$ ,  $l_e=22\text{mm}$ ,  $s_1=3\text{mm}$ ,  $s_2=0.1\text{mm}$  in (a) the WG and cutoff WG and (b) free space A-direction

In the case of using two wires with different lengths  $l_{e1}$  and  $l_{e2}$  two ERs ( $ER_1$  and  $ER_2$ ) are excited at different frequencies and two pass-bands (in cutoff WG) appear below resonances ER that are characteristics of the electric excitation (Fig. 12).

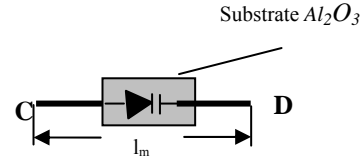


**Fig. 12.** Frequency dependences of transmission  $T$  in the WG and cutoff WG in the presence of “Grating - two parallel cut-wires” metastructure:  $l_{e1}=23\text{mm}$ ,  $l_{e2}=22\text{mm}$

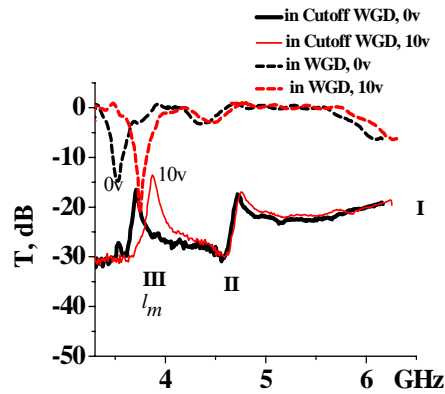
### 2.3. Split longitudinal cut-wire and parallel cut-wire loaded with varactor diodes

It is special interest to study a metastructure using varactor

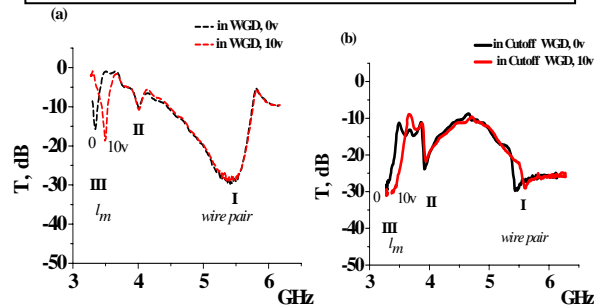
diodes. In [6] it has been demonstrated that the resonance frequency of split ring resonators (SRRs) can be tuned using varactor diodes. The resulting particle has been called a varactor-loaded split ring resonator (VLSRR). In this paper we use varactor diodes in metastructures to tune resonance response related to cut-wires and match the resonance minima of transmission  $T$  to concrete resonant elements with certainty which is important for multi-resonance system.



**Fig. 13.** Split cut-wire loaded with varactor diode



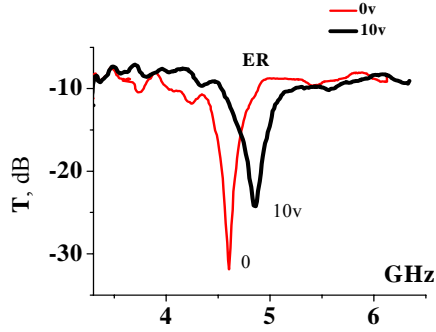
**Fig. 14.** Frequency dependences of transmission  $T$  in the WG (dashed) and cutoff WG (solid) in the presence of metastructure “Grating - varactor loaded split longitudinal cut-wire  $l_m$ ” ( $l_m=32\text{mm}$ ,  $l_p=16\text{mm}$ ,  $s=3.5\text{mm}$ ) under different bias conditions,



**Fig. 15a,b.** Frequency dependences of transmission  $T$  in the presence of metastructure “Cut-wire pair-varactor loaded split longitudinal cut-wire  $l_m$ ” ( $l_m=32\text{mm}$ ,  $l_{AB}=22\text{mm}$ ,  $s=2.5\text{mm}$ ) under different bias conditions in (a) WG and (b) cutoff WG,

By analogy with [7] we call resulting cut-wire as varactor loaded split longitudinal cut-wire  $l_m$  and varactor-loaded split parallel cut-wire  $l_e$ .





**Fig. 16.** Frequency dependences of transmission  $T$  in the presence of metastructure “*Grating* - varactor loaded split parallel cut-wire  $l_e$ ” ( $l_e=32\text{mm}$ ,  $l_p=16\text{mm}$ ,  $s=1\text{mm}$ ) under different bias conditions in free space  $A$ -direction,

Split longitudinal cut-wire is loaded with varactor diode placed on substrate  $Al_2O_3$  in the gap as we see in **Fig. 13**.

Frequency dependences of transmission  $T$  in the WG and cutoff WG in the presence of metastructures “*Grating*-varactor loaded split longitudinal cut-wire  $l_m$ ” and “*Cut-wire pair* - varactor loaded split longitudinal cut-wire  $l_m$ ” are demonstrated in **Fig. 14, 15** under different bias conditions. These metastructures show electric resonance response **I** related to *Grating*  $l_p$  (or wire pair **AB**), resonance **II** and magnetic-type resonance **III** related to split longitudinal cut-wire  $l_m$  (or split cut-wire **CD**) loaded with varactor diode SMV1234. Resonance **III** of varactor loaded split longitudinal cut-wire  $l_m$  shifts from 3.53 GHz to 3.74 GHz (**Fig. 14**) and from 3.34 GHz to 3.49 GHz (**Fig. 15**) with the tuning voltage  $V_{DC}$  from 0 to 10V. Corresponding pass-band in cutoff WG (above **III**) follows the shifting resonance **III**. Positions of resonances **I** and **II** are practically not changed. Metastructure “*Grating*- varactor loaded split parallel cut-wire  $l_e$ ” consists of *Grating*  $l_p$  and split cut-wire  $l_e$  loaded with varactor. This metastructure exhibits electric resonance response **I** related to *Grating* of wires  $l_p$  and electric resonance **ER** related to varactor loaded split parallel cut-wire  $l_e$ . **Fig. 16** shows that the resonance **ER** shifts from 4.6 GHz to 4.86 GHz with the tuning voltage  $V_{DC}$  from 0 to 10V corresponding to varactor tuning capacitance from 9.63 to 1.47 pF.

### 3. Discussion

Obtained results allow to suggest a concept of magnetically-induced resonance response (magnetically-type resonance) based on excitation of resonant currents by electromotive force which, with accordance of Faraday’s law of electromagnetic induction, is caused by the transverse magnetic field of surface polaritons in many equivalent spatial *LC-circuits* formed by cut-wire pairs of the *Grating* and sections of the longitudinal cut-wire  $l_m$ . Is there any possibility of traditional electric excitation of current in cut-wire  $l_m$ ? Theoretically, yes, because near each

cut-wire-end of the *Grating* the real electric field’s longitudinal components in mutually opposite directions (parallel and antiparallel to the wave vector  $k$ ). Therefore these components of the field can induce currents in opposite directions along the longitudinal cut-wire; so, total longitudinal current must be practically absent. Besides practical existence of the longitudinal electric field near the *Grating* has been not depicted [7] when double split ring was used as a probe for determining the orientations of surface polaritons local fields.

### 4. Conclusions

1. Microwave properties of new metastructures consisting of *Grating* with nonmagnetic cut-wires (length  $l_p$ ) and a single nonmagnetic longitudinal cut-wire (length  $l_m$ ) orthogonal to *Grating*’s wires are investigated in waveguides, cutoff waveguides and in free space. The metastructure can be considered as composition of many *LC-circuits* formed by cut-wire  $l_p$  pair of the *Grating* and sections of the longitudinal cut-wire  $l_m$ . The metastructures are designed for the observation and investigation of microwave magnetic and electric resonance effects. Type of the resonance (magnetic-type resonance excited by magnetic field or electric resonance excited by electric field) can be identified using comparative analysis of the transmission in the main and below-cutoff waveguides.

2. Three separate resonance effects **I**, **II**, **III** are observed in the case when metastructure is oriented along propagation direction and cut-wires of the *Grating* are parallel to the electric field of the incident electromagnetic wave. The resonances are connected with *Grating* (resonance **I**), as well with both *LC-circuits* (resonance **II**) and longitudinal cut-wire  $l_m$  (resonance **III**).

It has been shown that metastructure exhibit electric-type resonance **I** of the *Grating* forming surface polaritons below the resonance frequency depending on length  $l_p$ . This resonance is due to the excitation of parallel resonance currents in cut-wires  $l_p$  by electric field.

It has been shown that metastructure exhibit magnetic-type resonance **II** of *LC-circuits* depending on length  $l_p$  and distance  $s$  between the longitudinal cut-wire  $l_m$  and the *Grating*.

It has been shown that metastructure exhibit magnetic-type resonance **III** in range of surface polaritons existence, depending on length  $l_m$  and distance  $s$ . This resonance is due to the excitation of resonance current in a single longitudinal cut-wire  $l_m$ .

3. Concept of magnetic-type resonances (magnetically-induced resonances) is presented. The concept is based on the excitation of circular resonance currents in many equivalent spatial *LC-circuits* and corresponding induced magnetic moments by the transverse magnetic field of surface polaritons (resonance **II**). In this case antiparallel currents flow in the *Grating*’s adjacent cut-wires  $l_p$  while like-directed currents flow along cut-wire  $l_m$ . Currents contribution of many *LC-circuits* provides strong resonance current and electric dipole moment along cut-wire  $l_m$  and strong resonance effect (resonance **III**).

So, presented metastructure containing nonmagnetic line cut-wires can possess induced magnetic and electric dipole moments and can exhibit magnetic-type resonances excited by magnetic field.

Using the observed phenomena, it is possible to create new magnetic metamaterials (in particular, those possessing magnetic permeability) tunable in a broad frequency range.

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