

# Ductile fracture nucleation ahead of sharp cracks

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## Abstract

Models proposed up to now to describe ductile fracture nucleation ahead of sharp cracks are reviewed and mathematical relationships, derived for calculating fracture toughness, discussed. A new model, based on the phenomenon of crack tip blunting, has been conceived. Equations relating  $J_{IC}$  or  $K_{IC}$  to inclusion spacing in a metal alloy, to its strain-hardening properties and to the maximum strain acting at ductile fracture nucleation in a blunt notch specimen have been derived. Their validity is proved with experimental results on a number of low C steels.

## Riassunto

Si sono esaminati i modelli finora proposti per descrivere il fenomeno della nucleazione di fratture duttili a partire da cricche con raggio di fondo infinitesimo e si sono discusse le relazioni matematiche derivate da tali modelli per il calcolo della tenacità a frattura. È stato introdotto un nuovo modello che tiene conto del fenomeno dell'aumento del raggio di fondo di una cricca prima che da questa si origini una rottura. Sono state inoltre derivate equazioni che permettono di calcolare i valori di  $J_{IC}$  o  $K_{IC}$  per una lega metallica, partendo dalla spaziatura media delle inclusioni non metalliche, dalle caratteristiche di incrudimento della lega e dall'allungamento massimo agente alla radice di un intaglio non acuto nel momento della nucleazione della frattura duttile. I risultati sperimentali ottenuti con parecchi acciai a basso tenore di carbonio hanno consentito di confermare la validità del modello e delle relazioni proposte.

## Introduction

For a full understanding of the process that leads to fully ductile fracture initiation and propagation in the triaxial stress field ahead of a sharp crack, you have to model completely the complex interplay between the metal matrix flow characteristics and the microstructural features that can act as substrates for void formation at various levels of stress.

The numerous attempts of this kind conducted over the past 20 years have aimed at establishing a link between readily obtainable mechanical properties, as provided by a simple tension test, and some kind of microstructural parameter on one side and the fracture toughness of a material ( $K_{IC}$  or  $J_{IC}$ ) on the other, in order to avoid the lengthy tests necessary to establish these parameters, and eventually speed up material control procedures.

A secondary more ambitious goal has been to provide the metallurgical engineer with a tool for designing tougher and more reliable alloys for structural needs. A review of plane strain ductile fracture models is presented here, followed by a new proposal, with the experimental data supporting the mathematical relationships derived from it.

## Proposed Ductile Fracture Nucleation Models

A fracture criterion adopted in many theories is that of Rice and Johnson (1); they stated that the onset of crack propagation occurs when a critical strain is

reached over a definite distance from the crack tip, which is of the same order of magnitude as the critical crack-tip opening displacement (COD).

The critical COD in plane strain,  $\delta_{IC}$ , is in turn a function of the fracture toughness,  $K_{IC}$ , via the usual correlation

$$\delta_{IC} = m K_{IC}^2 / E \sigma_y \quad (1)$$

where  $E$  is the Young's modulus,  $\sigma_y$  the yield strength and "m" a numerical constant varying between 0.425 and 0.717, according to various authors.

The above distance is a function of the microstructure of the material, i.e. of a microstructural characteristic distance (2). The concept had already been laid down in Krafft's (3) earlier model, which assumed the existence of a small "process" zone ahead of the crack tip. Zone elements were idealized as circular tensile ligaments, clinching the throat of the crack until they are drawn out to the point of tensile instability, where their rupture became inevitable. Consequently, Krafft proposed the following equation relating the plane strain fracture toughness,  $K_{IC}$ , to material parameters

$$K_{IC} = EN \sqrt{(2\pi d_T)} = E \epsilon_i \sqrt{(2\pi d_T)} \quad (2)$$

$E$  is the Young's modulus,  $N$  is the strain-hardening exponent (equal to the uniform elongation strain at the instability of a tensile specimen,  $\epsilon_i$ ), and  $d_T$  is the diameter of the idealized tensile specimens.  $d_T$  should be set equal to the average inclusion spacing in the matrix,  $s$ , as also later demonstrated by Birkle, Wei, and Pellissier (4).

The model also works with a reasonably good approximation when fracture surfaces show a series of



parallel ridges and troughs at constant spacing, as in precipitation hardening stainless steel (5) or maraging steel (6). In the latter case, a close correlation was observed between experimental values of  $K_{Ic}$  and the ones computed introducing in Eq. 1 the ridge-to-ridge distance in place of  $d_T$ .

Later models emphasized that the fracture toughness of a material should be more strongly dependent on the plane strain ductility  $\epsilon_{f,ps}$  (7) than the axisymmetric ductility, since the former reflects more closely the stress state conditions at the crack tip.

In this sense, Krafft (8) had already modified his original model proposing that

$$K_{Ic} = E [(\sigma_y + \sigma_{uts})/E + N/2] \sqrt{(2\pi d_T)} \quad (3)$$

where  $\sigma_y$  and  $\sigma_{uts}$  are the yield and tensile strengths of the material.

Hahn and Rosenfield (9) suggested that  $\epsilon_{f,ps}$  could be obtained from the true fracture strain in uniaxial tension,  $\epsilon_f$ , setting  $\epsilon_{f,ps} = \epsilon_f/3$ .

Hypothesizing a relationship between the critical COD, the critical maximum strain at the crack tip, and the width of the plastic zone, which is a function of the square of the strain-hardening coefficient of the material, they proposed the semi-empirical equation,

$$K_{Ic} = N \sqrt{\left(\frac{2}{3} E \sigma_y \epsilon_f \cdot 0.0254\right)} \quad (\text{MN} \cdot \text{m}^{-3/2}) \quad (4)$$

which is to be replaced by the following relation in the case of materials with an unusually low strain-hardening exponent ( $N < 0.02$ )

$$K_{Ic} = 5 \sqrt{\left(\frac{2}{3} E \sigma_y \epsilon_f (N^2 + 0.0005) 10^{-3}\right)} \quad (\text{MN} \cdot \text{m}^{-3/2}) \quad (5)$$

The relationship was found valid by Slatcher and Knott (10) in low alloy - high strength steels quenched and tempered at 500 - 600 °C, but not verified when the same steels are tempered at lower temperatures.

The same argument was used by Chen and Knott (11) to derive the following relationship for calculating the value of  $K$  at fracture initiation ( $K_i$ );

$$K_i = \sqrt{\left(\frac{b}{m \cdot 10A} E \sigma_c \sigma_y N^2 s D^{-1}\right)} \quad (6)$$

where  $b$  is the Burgers vector,  $A$  is a factor of proportionality having a magnitude of the order of  $Gb/2\pi$  ( $G$  is the shear modulus) and  $\sigma_c$  is the cohesion

strength at the matrix-particle interface.  $D$  is the diameter of the inclusion.

To emphasize the role of the second-phase particles on fracture toughness Hahn and Rosenfield (12) proposed different equations

$$K_{Ic} = \sqrt{(2\sigma_y E s)} \quad (7)$$

$$K_{Ic} = \left\{ 2\sigma_y \cdot E \left(\frac{\pi}{6}\right)^{1/3} \cdot D \right\}^{1/2} \cdot v^{-1/6} \quad (8)$$

Eqs. 7 and 8 reflect a model involving fracture of (or decohesion at) large second-phase particles ( $D$  is the diameter of cracked particles) and the subsequent linking of associated expanded voids by rupture of the intervening ligament, as set by the approximate failure criterion proposed by Rice and Johnson (1); i.e. a crack propagates when the extent,  $x$ , of the heavily deformed region ahead of the crack is comparable to the average width of the unbroken ligaments ( $s$ ). Eq. 8 is derived in consideration of the fact that the volume fraction of a dispersed phase ( $v$ ) is proportional to the cube of the  $D/s$  ratio.

Broek (13) had already pointed out that both second-phase volume fraction and particle spacing control the fracture toughness of a given material, implying that the critical crack tip fracture strain,  $\epsilon_t$ , is a function of the volume fraction. He derived

$$K_{Ic} = \frac{E}{1+\nu} (2\pi s)^{1/2} f(1/\nu) \quad (9)$$

where  $\nu$  is the Poisson's ratio.

Experimental independent determinations of  $K_{Ic}$  from 3-point bend test specimens, and of  $\epsilon_{f,ps}$  on Clausing's bars for 4 steels, led Barsom and Pellegrino (14) to the following semiempirical correlation between the two quantities

$$K_{Ic} = A \epsilon_{f,ps}^h \sqrt{\sigma_y} \quad (10)$$

with  $h$  being very close to 2 for low carbon alloy steels and to 3 for 18 pct Ni (grade 250) maraging steel.  $A$  is a set constant for a given steel to be determined in each case. Infact, the model implies a proportionality between the critical crack tip strain supposed equal to  $\epsilon_{f,ps}$  and  $\delta_{Ic}$ :

$$\epsilon_f = \beta \delta_{Ic}^{1/2h}$$

since  $m$  in Eq. 1 is set equal to 1,  $A$  in Eq. 10

is equal to  $\sqrt{E/\beta^{2h}}$ .

An experimental correlation between  $\epsilon_t$  and  $\delta_i$ , the COD at crack propagation, is according to Smith and Knott (15):  $\delta_i = \epsilon_t \cdot l$  where  $l$  can be considered as the gage length along the crack contour or notch tip contour over which the strain can be considered approximately constant;  $l = \rho$  or  $l = 1.2\rho$  in the case of a blunt notch with end radius equal to  $\rho$  (Griffiths and Owen, (16)).

For sharp cracks in mild steels  $l$  has to be set equal to the inclusion spacing,  $s$  (Chipperfield and Knott, (17)), so that the following equations can be derived upon conservatively setting  $\delta_{lc}$  equal to  $\delta_i$ :

$$K_{Ic} \approx \sqrt{(2\sigma_y E \cdot \epsilon_t \cdot s)} = \sqrt{(2\sigma_y \cdot E \cdot \epsilon_{f,ps} \cdot s)} \quad (11)$$

which can be approximated as,

$$K_{Ic} \approx \sqrt{\left(\frac{2}{3}\sigma_y \cdot E \cdot \epsilon_f \cdot s\right)} \quad (11')$$

Other models make a linkage between the plastic zone and the applied stress intensity factor.

Schwalbe (18, 19) hypothesizes a strain distribution within the plastic zone, analogous to the one proposed by Rice (20) for shear strain upon Mode III loading; then by setting again that the plane strain fracture strain has to be reached over a distance equal to the interparticle spacing, he proposes

$$K_{Ic} = \frac{\sigma_y}{1-2\nu} \sqrt{\left(s\pi (1+N) \left[\frac{\epsilon_{f,ps}}{\sigma_y} \cdot E\right]^{1+N}\right)} \quad (12)$$

or

$$K_{Ic} = \frac{\sigma_y}{1-2\nu} \sqrt{\left(s\pi (1+N) \left[\frac{\epsilon_{f,ps}}{\sigma_y} \cdot E \cdot \frac{N}{1+N}\right]^{1+N}\right)} \quad (13)$$

Alternatively Osborne and Embury (21) considered the work done along the  $x$ -axis, in the region between  $s$  and the elastic-plastic boundary, equal to  $G_{Ic}$ . They assumed a strain distribution within the plastic zone of the type proposed by Rice and Rosengren (22) and a critical strain (this time equal to  $\frac{2}{3}\epsilon_f$ ) again reached over a distance equal to  $s$  from the crack tip. Their formulation, valid for materials with  $\sigma_y \approx 700\text{MPa}$ , reads

$$K_{Ic} = \sqrt{\left(\frac{2}{3}\sigma_{uts} \cdot E \cdot \epsilon_f \cdot s \cdot \ln \frac{2}{3} \frac{\epsilon_f}{\epsilon_y}\right)} \quad (14)$$

The crack tip blunts before fracture is nucleated in quasi-static loading. The phenomenon is taken into account in the formulation of further models. They consider numerical solutions for the strain distribution

in front of the blunted tip, adopted following Rice and Johnson's (1) calculations for a rigid ideal plastic material.

With this approach, assuming again that at fracture the critical strain has to be reached over a distance from the crack tip equal to the interparticle spacing, Schwalbe (19) set

$$\epsilon_{f,ps} = \frac{0.44 \delta_{lc}}{s} - 0.23$$

and assuming  $m$  (Eq. 1) = 0.5 obtained

$$K_{Ic} = \sqrt{[(4.55 \epsilon_{f,ps} + 0.23) E \sigma_y s]} \quad (15)$$

Similarly Pandey and Banerjee (23) set

$$\epsilon_{f,ps} = f \frac{\delta_{lc}}{x_f}$$

with  $x_f$  being the extent of the zone over which the critical strain is to be reached at fracture and  $f$  a numerical constant.

Then

$$K_{Ic} = \sqrt{\left(\frac{\epsilon_{f,ps} \cdot x_f \cdot E \cdot \sigma_y}{m \cdot f}\right)} \quad (16)$$

Ritchie, Server, and Wullaert (24) equalled  $x_f$  to a microstructurally significant characteristic distance  $l_0$  and set  $m = 0.6$  following the McMeeking (25) small scale yielding formulation. To single out the precise value of  $\epsilon_{f,ps}$  to be inserted into Eq. 16, they tested a series of circumferential notch tensile specimens with varying values of  $\rho$ , the notch-end radius, in order to determine the variation of the fracture strain as a function of the stress state (Mackenzie, Hancock, and Brown, (26)). Then, after identifying the particular stress state acting at the appropriate  $l_0$  distance from the crack-tip, employing a numerical solution by Rice and Johnson (1), the right value of  $\epsilon_{f,ps}$  valid for each steel can be determined. Experiments on SA533B and SA302B steels showed that the best values of  $l_0$  were in the region of 6-7 times the interparticle spacing for the former, and about equal to  $s$  for the latter.

## Critical Analysis of Proposed Models

Analyzing the above listed equations, it can be seen that  $K_{Ic}$  has been consistently linked to 4 tensile quantities ( $\sigma_y$ ,  $E$ ,  $N$ , and some type of fracture or instability strain) and to a microstructural parameter,  $s$ . As regarding the four mechanical characteristics,  $E$  does appear in all the relationships, whereas  $\sigma_y$  is



missing only in Eq. 2. Eq. 4 does not show either  $N$  or any type of strain (the 2 quantities can be somehow related);  $N$  is also absent in Eqs. 7, 8, 9, 10, 11, 11'. The only relationship in which neither  $s$  nor any other microstructural parameter appear is Eq. 10, although an indirect linkage between  $K_{Ic}$  and the microstructure can also be found there; in fact,  $\sigma_y$  has been related to  $s$  (27, 28), whereas  $\epsilon_f$  or  $N$  have been related to the second-phase volume fraction (see Hahn and Rosenfield (12) and Pickering (29) for reviews). The latter can explain why  $v$  appears alongside  $s$  only in Eq. 9.

All the 5 tensile and microstructural quantities appear simultaneously only in Eqs. 12 and 13. Eqs. 2, 3, 4, 7, 11, 12, 13, 14, 15 can be readily employed to calculate  $K_{Ic}$  via the 5 above listed quantities. Calculations reported by Schwalbe (19) and others, based on the data listed by him, show that the agreement between experimental and computed values of fracture toughness can be considered only fair in the best cases and decidedly bad in the others. Obviously, the quantities whose values are most affected by error are  $s$  and the value to be inserted in place of the crack tip strain. Regarding the former, the uncertainty arises from the phenomenological observation that not all second-phase particles within a material have associated voids at the same level of stress. It is generally accepted (12) that larger particles crack or decohere at lower levels of stress or strain than intermediate or fine ones. Void formation with large inclusions is enhanced by the triaxial state of stress that develops in plane strain conditions in the vicinity of the stress concentration. Then, the critical stages in fracture initiation when loading a precracked specimen are (i) the linkage of the crack-tip with some closely located voids at different positions along the crack front and (ii), most of all, the linkage of the crack front protrusions generated in the above way. These coalescence processes are the ones that control the real critical crack-tip growth and conversely COD at initiation.

Under the above assumptions, resistance to the onset of crack growth, once voids are generated, is controlled by the capacity of the matrix material between voids associated with large particles to further straining under increasing stress. Such a resistance is enhanced by the ability of the material to strain-harden and is foreshortened by the tendency to strain localization in narrow slip bands, i.e. to shearing instability. These characteristics are not independent of one another (30): materials with higher  $N$  values show a greater resistance to the development of shearing instabilities than those with lower associated  $N$  values. The matrix material between voids comprises

intermediate and fine particles which favour strain localization and therefore tend to limit fracture deformation (12). Consequently, their role can be stated as largely detrimental to fracture toughness. From what precedes, it can be inferred that the  $s$  value which controls fracture toughness is the one related to the spacing of large inclusions, especially in mild alloys where large plastic zones develop at the crack-tip. Instead, the volume fraction of all the inclusions, large, intermediate, and fine, determines the maximum strain that can be sustained in the region close to the crack-tip before the onset of critical growth. Besides the inclusion volume fraction, the stress state acting at the crack-tip at the moment of fracture nucleation also controls such a limiting strain (24).

For such a reason the suggestion by Hahn and Rosenfield or Osborne and Embury (21) that the strain to be taken into account is some fraction of the uniaxial fracture strain, can be considered as leading to an only a rough approximation. Better attempts to reproduce the stress state at a stress concentration are those made by the use of Clausing's bars (2, 19).

It has to be noted that, with the former method, it is possible to reproduce the plane strain situation acting at the stress concentration without indeed copying the same small gage length or steep stress gradients. In fact, results in predicting experimental  $K_{Ic}$  values have met with limited success.

The best procedure envisioned up to now, to identify the strain acting at the crack tip at the moment of fracture nucleation, is the one proposed by Ritchie and colleagues (24) by the use of circumferentially notched specimens as outlined previously. Unfortunately, it is a lengthy one and, furthermore, the results reported by the authors indicate that a precise prediction of  $K_{Ic}$  is not always possible, owing to the lack of a clear-cut relationship between  $l_0$  and the interparticle spacing valid for all metal alloys.

## A new model for ductile fracture nucleation

The researches performed in recent years on cracked specimens to obtain accurate variations of applied J-integral values as a function of crack extension (J R-curves) have demonstrated that the early stages of crack growth stem from the blunting of the crack under increasing loads. The passage from vanishing crack tips to finite root notches terminates when the root radius ( $\rho$ ) reaches a definite value ( $\rho_{eff}$ ). The existence of such a limiting radius in plane strain ductile fracture has been proved by Chipperfield and Knott (17) on a 0.17% C,



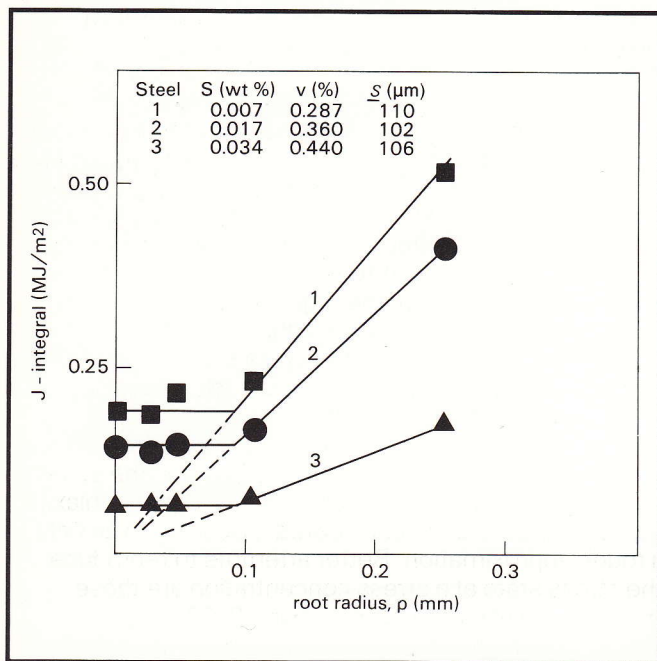


Fig. 1 - Applied J-integral values at fracture initiation vs. the notch root radius of 3-point bend specimens fabricated with C-Mn steels with various sulfur and inclusion contents ( $v$ ) and similar inclusion spacing ( $s$ ). Cracks and notches were in the T-L direction.

1.95% Mn steel and a high strength Ni-Cr-Mo-V steel, by Lereim and Embury (31) on a variety of HSLA steels and on AISI 4340 steel, and more recently by Roberti and colleagues (32) on different types of 0.17% C, 1.33% Mn steels (Fig. 1). All the above authors have reported that fracture toughness results from notched specimens with  $\rho$  smaller than  $\rho_{\text{eff}}$  were identical to those obtained employing precracked specimens. It can also be seen that, prior to fracture advance, both types of specimens originate analogous "stretch zones" (Fig. 2). It can be inferred that both types of specimens fail by the same mechanism, i.e. they all develop a blunt notch with  $\rho = \rho_{\text{eff}}$  and afterwards fracture when the maximum strain at the notch tip reaches a limiting value.

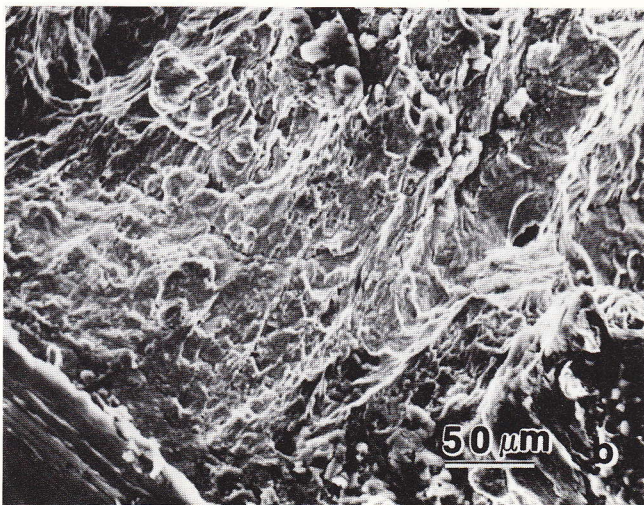
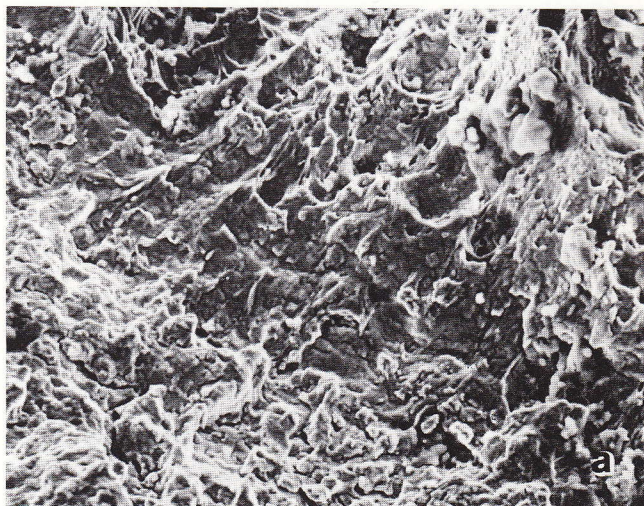
Furthermore, it has been demonstrated that blunt notch specimens of a given material with  $\rho \geq \rho_{\text{eff}}$  reach a ductile fracture initiation stage because a constant limiting strain  $\epsilon_{\text{max},f}^*$  is achieved at the notch root. In fact, Firrao and colleagues (33, 34, 35), Roberti and co-workers (32) demonstrated that applied J-integrals at the onset of fracture vary linearly with  $\rho$  (see Fig. 1), thus proving the validity of a ductile fracture initiation model from blunt notches originally proposed by Begley, Logsdon, and Landes (36). The model took into account the equation derived by Rice (37) to relate the

applied J-integral, the notch-end radius, and the strain-hardening properties of a material to the maximum strain acting at the notch root,  $\epsilon_{\text{max},f}^*$ :

$$\epsilon_{\text{max},f}^* = \epsilon_y \left[ \frac{(N+1/2)(N+3/2)\Gamma(N+1/2)}{\Gamma(1/2)\Gamma(N+1)} \frac{J}{\sigma_y \epsilon_y \rho} \right]^{\frac{1}{1+N}} \quad (17)$$

where  $\Gamma$  is the mathematical gamma function. Eq. 17 tells that, if a critical notch root strain,  $\epsilon_{\text{max},f}^*$  is the appropriate parameter for ductile crack initiation at the root of the notch, a plot of the applied J values at the onset of crack growth versus  $\rho$  should indeed be a straight line passing through the origin. Upon setting,

Fig. 2 - Stretch zones developing at the root of a fatigue crack (a) or of a 0.03 mm radius notch (b) in steel 1 specimens loaded up to a fracture..





$$F(\Gamma(N)) = \frac{(N+1/2)(N+3/2)\Gamma(N+1/2)}{\Gamma(1/2)\Gamma(N+1)}$$

Eq. 17 can then be written in the following form (38),

$$J_A = \sigma_y^{(1-N)} \frac{\epsilon_{\max,f}^{*(N+1)} E^N}{F(\Gamma(N))} Q_{\text{eff}} \quad (18)$$

where  $J_A$  is the J-integral applied at fracture initiation in a notched specimen with notch root radius  $\rho \geq Q_{\text{eff}}$ . Eq. 18 either adequately describes the resistance of blunt notch specimens to ductile rupture nucleation or can be employed to calculate an accurate value of the maximum strain active at a notch root before the onset of crack growth. For instance, values of  $\epsilon_{\max,f}^*$  equal to 0.991, 0.876, and 0.474 have been obtained for steels 1, 2, and 3 of Fig. 1 (39).

From what precedes it is clear that the new model proposed for ductile fractures originating from a sharp crack, based on the hypothesis of tip blunting up to a limiting radius ( $Q_{\text{eff}}$ ), allows to calculate the crack-tip strain at onset of fracture from results obtained with blunt notch specimens. Thus, the following formula can be written to compute the fracture toughness  $J_{Ic}$ ,

$$J_{Ic} = \sigma_y^{(1-N)} \frac{\epsilon_{\max,f}^{*(N+1)} E^N}{F(\Gamma(N))} Q_{\text{eff}} \quad (19)$$

By dividing Eq. 18 by Eq. 19 one obtains,

$$\frac{J_A}{J_{Ic}} = \frac{\rho}{Q_{\text{eff}}} \quad (20)$$

The experiments carried out by the authors on C-Mn steels with different microstructures (Fig. 1) allow us to prove that  $Q_{\text{eff}}$  is of the same order as  $s$ , which is to be taken as the spacing between major inclusions in accordance with previous considerations.

Therefore, it is possible to write,

$$\frac{J_A}{J_{Ic}} = \frac{\rho}{s} \quad (21)$$

Fig. 3 reports plots of  $J_A/J_{Ic}$  vs.  $\rho/s$  for the steels of Fig. 1. For values of  $\rho/s \geq 1$  the interpolating line of all the results has a 45° slope as predicted by Eq. 21 and levels off horizontally when the root radius falls below the interparticle spacing.

Similar results had also been obtained by Chipperfield and Knott (17) who measured  $\delta_{Ic}$  values and COD at fracture initiation from notches ( $\delta_A$ ) on a number of low C steels with different Mn contents. The resulting plot is presented in Fig. 4, where  $l$  has been set by the

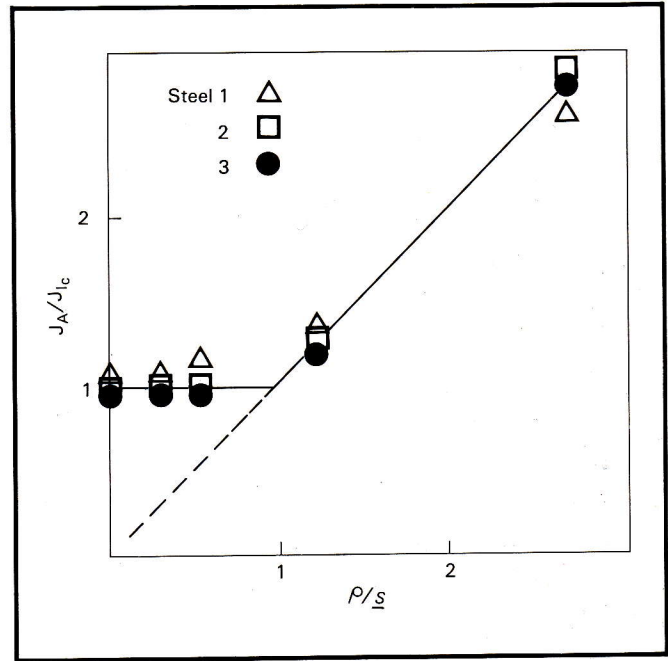
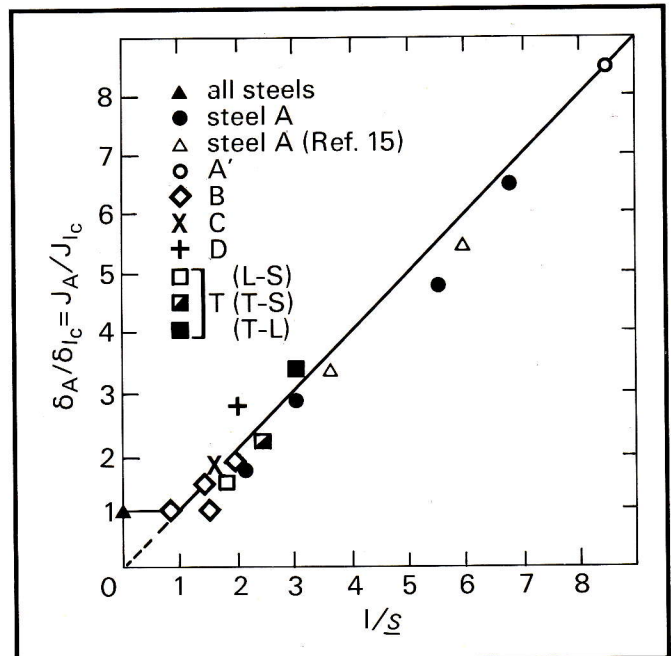


Fig. 3 - Fracture toughness results of Fig. 1 presented as adimensioned plots of the  $J_A/J_{Ic}$  ratio vs.  $\rho/s$  (see Eq. 21).

Fig. 4 - Fracture toughness results by Chipperfield and Knott (17) on a series of C-Mn steels (see Table 1). Data are presented as in Fig. 3;  $l = 1.1 \rho$ . Steel T has been tested with the stress concentration in 3 different orientations with respect to the rolling direction.





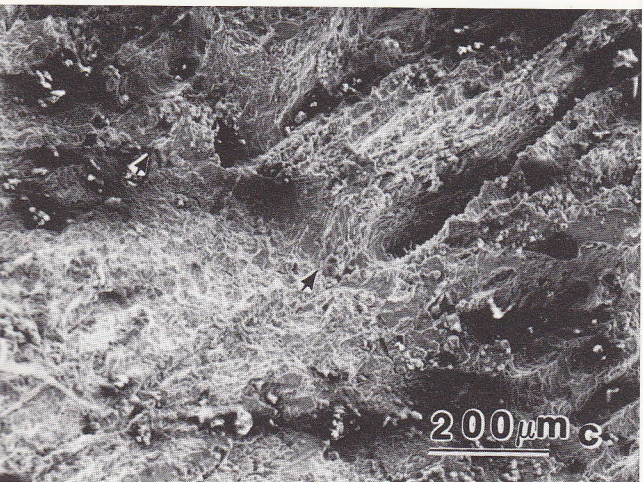
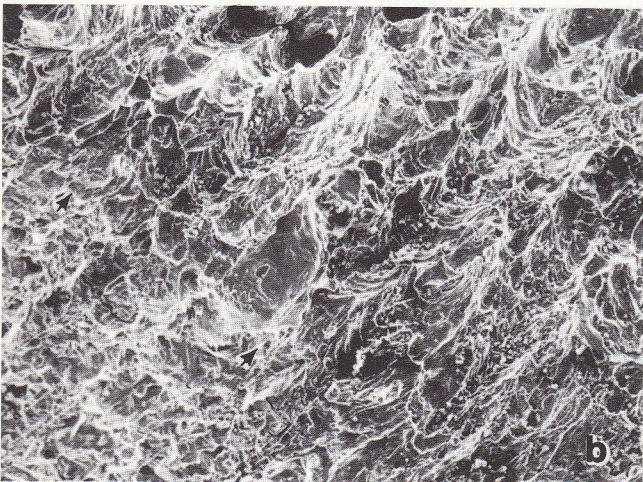
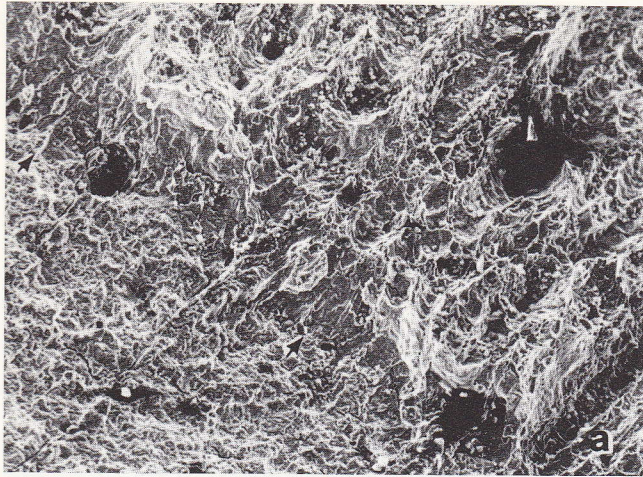


Fig. 5 - Fracture surfaces of precracked specimens of steels 1 (a), 2 (b), and 3 (c) of Fig. 1. Arrows indicate the end of the fatigue pre-cracks.

authors as  $1.1 \varrho$ . The diagram further confirms that  $\varrho_{\text{eff}}$  is of the same order as  $s$ .

Rearranging Eq. 21, it can be derived that  $J_{Ic}$  values can be computed by determining the applied J-integral values at fracture initiation in notched specimens with  $\varrho \geq \varrho_{\text{eff}}$  and calculating  $s$  by metallographic observations.

Table 1 reports experimental and calculated values of  $J_{Ic}$  for the C-Mn steels of Figs. 3 and 4. In the case of the steels tested by Chipperfield and Knott computed data have been obtained converting the  $\delta_A/\varrho$  values, determined averaging their results, into  $J_A/\varrho$  values by the usual relationship,  $J_A = 2\sigma_y \delta_A$ . Results listed in Table 1 clearly indicate the close agreement between

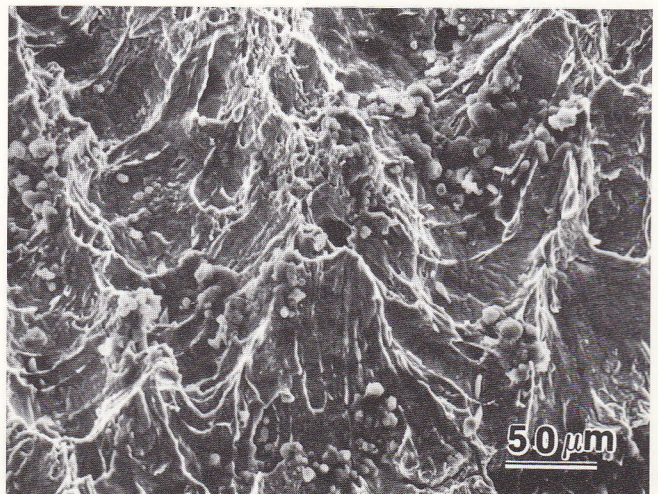
the values of fracture toughness calculated by the use of Eq. 21 and those measured on precracked samples. Only in one case (steel D) is the difference rather high, which might be ascribed to the data from which  $\delta_A/\varrho$  was calculated. It is interesting to note that, in the case of steel T, the model and the relationships based on it yield satisfactory results with specimens differently oriented in respect to the rolling direction.

For the sake of comparison with equations 2 to 16, previously listed Eq. 19 can be converted to yield  $K_{Ic}$  by the usual relationship,  $K_{Ic}^2 = E J_{Ic}/(1 - \nu^2)$ , to obtain,

$$K_{Ic} = \left\{ \frac{\sigma_y^{(1-N)}}{(1-\nu^2)} \frac{\epsilon_{\text{max},f}^{*(1+N)} E^{(1+N)}}{F(\Gamma(N))} \right\}^{1/2} s^{1/2} \quad (22)$$

Eq. 22 employs all the five mechanical and microstructural quantities that enter with various arrangements in the previously examined equations. Although only one microstructural parameter,  $s$ , is directly indicated, the strong inverse dependance of  $\epsilon_{\text{max},f}^*$  on  $\nu$  is evident from data reported about steels 1, 2, and 3. Fractographs reported in Fig. 5 clearly depict the strain localization promoted in steel 3 by the large inclusion fraction. In fact, fracture surfaces between long furrows formed around major inclusions are decidedly flatter in this steel than in the other two where, instead, coalescence between first voids occurs mainly due to continuous plastic flow (see also Fig. 6). Therefore it can be stated that  $K_{Ic}$  and  $J_{Ic}$  values are controlled both by the spacing between large inclusions and by the total second-phase volume fraction, whereas  $K_A$  and  $J_A$  values for blunt notch specimens depend mainly on  $\nu$ .

Fig. 6 - Detail of surface of steel 2 in the region of ductile fracture nucleation from a sharp crack.





## Conclusions

A new model for fully ductile fracture nucleation ahead of sharp cracks has been derived on the basis of experimental results on a number of low carbon, medium manganese steels. The model hypothesizes that crack tips blunt, up to achieving a finite root radius,  $Q_{eff}$ , which is of the same order of magnitude as the spacing between major non metallic inclusions,  $s$ . Then a fracture nucleates ahead of the blunted tip when the maximum strain at the root of the notch generated in

the above way reaches a limiting value,  $\epsilon_{max,f}$ , which is inversely proportional to the inclusion volume fraction. A procedure to calculate  $\epsilon_{max,f}$  values from the applied J-integral value at fracture initiation in a blunt notch specimen with notch-end radius greater than  $s$  has been described, and applied to compare calculated  $J_{Ic}$  values with experimental ones.

The model and the relationships based on it have been seen to work with very good approximation in the case of steels with a ferritic matrix. Experiments to prove its validity in the case of different metal alloys will be performed in the near future.

**TABLE 1 - Comparison of experimental and calculated values of the fracture toughness for a number of C-Mn steels**

| Steel             | Ref.  | C %  | Mn % | S %   | $J_A/Q$ (MN/m <sup>2</sup> ) | $\delta_A/Q$ | $s$ ( $\mu$ m) | $J_{Ic}$ (calc.) (MN/m) | $J_{Ic}$ (exp.) (MN/m) |
|-------------------|-------|------|------|-------|------------------------------|--------------|----------------|-------------------------|------------------------|
| 1                 | 32    | 0.17 | 1.33 | 0.007 | 2083                         |              | 110            | 0.229                   | 0.194                  |
| 2                 | 32    | 0.17 | 1.33 | 0.017 | 1603                         |              | 102            | 0.163                   | 0.145                  |
| 3                 | 32    | 0.17 | 1.33 | 0.033 | 667                          |              | 106            | 0.070                   | 0.065                  |
| A                 | 15,17 | 0.12 | 0.90 | 0.24  |                              | 0.891        | 42             | 0.020                   | 0.020                  |
| A <sup>(o)</sup>  | 17    | 0.12 | 0.90 | 0.24  |                              | 0.687        | 32             | 0.012                   | 0.011                  |
| B <sup>(oo)</sup> | 17    | 0.17 | 1.95 | 0.26  |                              | 0.245        | 180            | 0.028                   | 0.029                  |
| C                 | 17    | 0.17 | 2.09 | 0.006 |                              | 1.96         | 95             | 0.172                   | 0.148                  |
| D                 | 17    | 0.18 | 1.29 | 0.005 |                              | 4.07         | 88             | 0.262                   | 0.154                  |
| T (T-S)           | 17    | 0.18 | 1.42 | 0.035 |                              | 1.59         | 65             | 0.067                   | 0.064                  |
| T (L-S)           |       |      |      |       |                              | 2.29         | 87             | 0.128                   | 0.119                  |
| T (T-L)           |       |      |      |       |                              | 0.60         | 131            | 0.051                   | 0.041                  |

<sup>(o)</sup> Same as steel A, but roll-bonded.

<sup>(oo)</sup> Inclusions were clustered,  $s$  is the mean spacing between clusters.

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