

The Journal of the Acoustical Society of America

Singing Together: Pitch Accuracy and Interaction in Unaccompanied Duet Singing

--Manuscript Draft--

Manuscript Number:	JASA-03137R2
Full Title:	Singing Together: Pitch Accuracy and Interaction in Unaccompanied Duet Singing
Short Title:	Pitch Accuracy and Interaction in Singing
Article Type:	Regular Article
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Section/Category:	Musical Acoustics
Keywords:	unaccompanied singing; pitch accuracy; pitch drift; interaction in duet.
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Singing Together: Pitch Accuracy and Interaction in Unaccompanied Unison and Duet Singing

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(Dated: 16 December 2018)

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2 of unaccompanied pairs of singers. Eight pairs of singers sang two excerpts either in
3 unison or two-part harmony. The experimental condition varied which singers could
4 hear their partners. After semi-automatic pitch-tracking and manual checking, we
5 calculated the pitch error and interval error, and tested the factors of influence using
6 a one-way ANOVA and a linear mixed-effects model. The results indicate that: 1)
7 singing with the same vocal part is more accurate than singing with a different vocal
8 part; 2) singing solo has less pitch error than singing with a partner; 3) pitch errors are
9 correlated, as singers adjust their pitch to mitigate their partner's error and preserve
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PACS numbers: 43.75.Rs, 43.75.Bc, 43.75.Xz, 43.75.St

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13 I. INTRODUCTION

14 Singing is common to all human societies (Brown, 1991) and repertoire performed by
15 multiple singers is probably the most widespread type of singing (Sundberg, 1987), yet the
16 factors that affect the accuracy of group singing are still poorly understood. The main
17 motivation for this study is to improve the scientific understanding of unaccompanied duet
18 singing, and in particular the interaction between singers. We seek to explain pitch accuracy
19 and the mechanisms which may influence tuning in complex situations. The basic concepts
20 of pitch accuracy and interaction are introduced in this section and relevant research in the
21 next section.

22 *Intonation* in music is defined as a musician’s realisation of pitch accuracy (Simpson
23 *et al.*, 1989). It is one of the central parameters of singing accuracy and it is an extremely
24 significant aspect of music because of its relevance to both melody and harmony. The
25 accuracy of intonation is determined by culturally specific tuning systems such as the equal
26 tempered tuning system in Western music (Warren and Curtis, 2015). Intonation is the
27 main reported priority in choral rehearsals (Ganschow, 2014) and the focus of guides on
28 vocal practice (Crowther, 2003).

29 To produce an accurate pitch, most people rely on a recent reference (Takeuchi and Hulse,
30 1993). Therefore, the accompaniment of instruments and other singers, where present, plays
31 an important role in tuning. Although instrumental accompaniment has been shown to
32 enhance individual learning of a piece (Brandler and Peynircioglu, 2015), it can also reduce

33 pitch accuracy during singing, even when the accompaniment consists of nothing but the
34 target pitches (Dai and Dixon, 2016; Pfordresher and Brown, 2007).

35 In the case of fixed pitch instruments, such as keyboard instruments, singers adjust to
36 the tonal reference provided by the instrument. But in unaccompanied singing, the singers
37 negotiate a common reference, and this reference can change over time. Several studies
38 have investigated the intonation of unaccompanied ensembles and how their tonal reference
39 evolves over the duration of a piece, a phenomenon called *pitch drift* (see Section II). Alldahl
40 (2008) cites relative pitches, singers' memories and their muscle control as critical factors
41 influencing intonation, but little is known about the effect of interaction between singers.

42 Interaction is very important for ensemble singing, which is a cooperative activity in-
43 volving communication within the ensemble and with the audience (Potter, 2000, p. 158).
44 Attaining excellence in ensemble playing depends on finding a balance between individual
45 performance and interaction (Lim, 2014). This research investigates how singers influence
46 each other in terms of intonation and pitch variation. We focus on duet singing as the sim-
47 plest example of singing involving interaction, allowing us to design a controlled experiment
48 involving the influence of one singer upon another.

49 The remainder of the paper is structured as follows. Section II discusses existing work
50 related to singing intonation and interaction. Section III contains our research questions,
51 hypotheses, experimental design and methodology. In Section IV, we describe our data
52 analysis, including annotation and calculation of intonation metrics. Section V presents
53 our results and how they relate to the experimental hypotheses. The combined effect of
54 multiple factors is evaluated in a linear mixed effects model in Section VI. This is followed

55 by a discussion of the results (Section VII), our conclusions (Section VIII), and finally the
56 details of where the annotated data and software can be freely obtained (Section IX).

57 II. PREVIOUS WORK

58 Research quantifying the intonation of vocal sounds can be traced back over 100 years to
59 the early work of [Seashore \(1914\)](#), and continues until the present time. Pitch production
60 relies on the ability to control the tension in the vocal cords, which results in modulations of
61 the vocal fundamental frequency. Much vocal research has focussed on speech, but musical
62 pitch requires a much greater degree of accuracy, both in production and perception, than
63 speech ([Zatorre and Baum, 2012](#)). Abilities related to the control of pitch are the primary
64 indicator for distinguishing untrained but talented individuals from those with less innate
65 singing skills ([Watts *et al.*, 2003](#)).

66 In order to study intonation in audio recordings, a reliable pitch estimation algorithm
67 is required. Note that since the voiced part of vocal sounds is harmonic, pitch and funda-
68 mental frequency (f_0) are generally treated as exchangeable (although they are expressed
69 on different scales, Equation 1). Many pitch detection methods have been proposed, par-
70 ticularly for speech recognition and coding (e.g. [Gerhard, 2003](#); [Hess, 1983](#); [Rabiner *et al.*,
71 1976](#)). If only a single pitch is present in the signal, periodicity-based methods such as au-
72 tocorrelation, as in the widely used Praat system ([Boersma, 2002](#)), and difference functions,
73 as in YIN ([de Cheveigné and Kawahara, 2002](#)), are popular approaches for determining the
74 pitch of speech or musical sounds. In this work we use PYIN ([Mauch and Dixon, 2014](#)), a

75 probabilistic extension of YIN which provides robustness against errors due to suboptimal
76 threshold settings.

77 Most studies on intonation focus on accuracy, although topics such as vibrato have also
78 been investigated (Bretos and Sundberg, 2003; Ferrante, 2011). Note that we use “accuracy”
79 to refer to both the bias and spread of pitch errors (unlike Pfordresher and Brown (2007),
80 who use it specifically for the bias alone). On the one hand, pitch error is the main metric of
81 accuracy for many researchers, where each observed pitch is compared to a predetermined
82 target value. Several studies have investigated pitch drift in unaccompanied singing (e.g.
83 Devaney and Ellis, 2008; Howard, 2003; Kalin, 2005; Mauch *et al.*, 2014; Terasawa, 2004).
84 Howard (2007) tested the hypothesis that the use of *just intonation*, where the fundamental
85 frequencies of pairs of simultaneous or consecutive notes are related by ratios of small whole
86 numbers (Lindley, 2001), causes pitch drift. The hypothesis in such work is that the pitch
87 adjustments required to intone pure intervals accumulate over time resulting in a shifting
88 tonal reference (Mullen, 2000). Howard’s study confirmed that singers make use of non-
89 equal-tempered intonation to govern their tuning, and showed that it is possible to predict
90 the direction of pitch drift in controlled harmonic progressions.

91 On the other hand, interval error, the extent to which pitch differences between subse-
92 quent tones deviate from their target values, has also been investigated. Tritones (Dai *et al.*,
93 2015) and perfect fifths (Vurma and Ross, 2006) were reported to have greater interval error
94 than other intervals. Other authors observed a phenomenon called *compression*, whereby
95 sung intervals are smaller than their targets, an effect which is particularly strong amongst
96 unskilled singers (Pfordresher and Brown, 2007).

107 Individual factors such as age and sex influence pitch accuracy (Welch *et al.*, 1997).
108 Musical training and experience also have some influence on singing ability; Mauch *et al.*
109 (2014) found that self-rated singing ability and choir experience, but not general musical
110 background, correlated significantly with intonation accuracy. Singers who exhibit much
111 greater than average pitch errors are classified as *poor singers*, a phenomenon that has
112 been the focus of several studies (Berkowska and Dalla Bella, 2009; Dalla Bella *et al.*, 2007;
113 Pfordresher and Brown, 2007; Pfordresher *et al.*, 2010). For poor pitch singing, evidence
114 points to a deficiency in pitch imitation accuracy as the main cause (Pfordresher and Mantell,
115 2014), although there are several types of singing deficiency and they vary by age and training
116 (e.g. Demorest *et al.*, 2015).

107 Mürbe *et al.* (2002) showed how singers' intonation accuracy is reduced by diminished
108 auditory feedback; in their experiment, auditory feedback was masked by noise. When
109 singers cannot hear themselves, they have to rely on kinesthetic feedback circuits, which
110 are less effective than auditory feedback for informing intonation. Likewise even in musical
111 situations where the accompanying sound provides the tonal reference, singers make greater
112 pitch errors when singing with accompaniment (Pfordresher and Brown, 2007), and partic-
113 ularly when the accompanying pitch content varies over the duration of a note (Dai and
114 Dixon, 2016). Thus vocal accompaniment is more difficult to sing with than instrumental
115 accompaniment, because singers are relying on unstable reference pitches from other vocal
116 parts (Liimola, 2000, p. 151). Although singing in unison with a partner may not increase
117 pitch accuracy, it may give singers more confidence than singing solo (Heath and Gonzalez,
118 1995).

119 Previous studies have investigated differences between solo and unison singing, although
120 not all studies obtained significant results. For example, [Green \(1994\)](#) claimed that children
121 singing unison, as opposed to in individually, had significantly better vocal accuracy, while
122 [Cooper \(1995\)](#) was unable to show a significant difference. There are more observations
123 also show children sing more accurately individually than in a group ((e.g. [Clayton, 1986](#);
124 [Goetze, 1985](#), [1989](#))). Besides the singing conditions, age, gender, training and number of
125 attempts were reported as significant factors for children’s singing accuracy ((e.g. [Nichols,](#)
126 [2016](#); [Nichols and Wang, 2016](#))).

127 Except for the 0.01% of the population who have absolute pitch, the ability to identify or
128 reproduce any given pitch on demand ([Bohrer, 2002](#); [Takeuchi and Hulse, 1993](#)), most people
129 rely on a reference pitch for tuning. An initial reference will be forgotten over time ([Long,](#)
130 [1977](#); [Mauch *et al.*, 2014](#)), so singers must constantly update their frame of reference as they
131 sing, based on what they have recently heard, both their own voice and any accompaniment.

132 [Brandler and Peynircioglu \(2015\)](#) observed that participants learned new pieces of music
133 more successfully when in an individual learning environment than in a collaborative one.
134 Abundant evidence shows that singers are influenced by other choral members in terms of
135 pitch accuracy (e.g. [Howard, 2003](#); [Terasawa, 2004](#)) and various approaches have been pro-
136 posed to keep singers in tune by their relative pitches, tone memories and muscle memories
137 (e.g. [Alldahl, 2008](#); [Bohrer, 2002](#)). Although various studies on singing have investigated
138 the pitch accuracy of solo singers and singing ensembles, we are not aware of any work that
139 focusses directly on the interaction between singers and its effect on intonation, the topic of
140 this study.

141 **III. METHODOLOGY**

142 In this section, we describe our hypotheses, the experimental design, musical material,
143 participants and experimental procedure. For our experiment, two *singing conditions* are
144 defined: the *unison condition*, where two singers sing the same vocal part, and the *duet*
145 *condition*, where they sing different vocal parts. There are also four *listening conditions*. In
146 the *solo* condition, the two singers cannot hear each other. The two *simplex* conditions are
147 where only one singer can hear the other singer (in either direction). The singer who cannot
148 hear her partner is called the *independent singer* while the singer who hears her partner
149 is the *dependent singer*. The *duplex* condition is where both singers can hear each other.
150 Note that according to these definitions, both singers are independent in the solo condition,
151 and both are dependent in the duplex condition. Singers can hear their own voice in all
152 conditions.

153 **A. Hypotheses**

154 Based on previous research and musical experience, we formulated five hypotheses re-
155 garding effects we expected to observe when singers interact. The experimental method was
156 designed to test these hypotheses and quantify the extent of the effects observed.

157 Hypothesis 1: *The unison singing condition has less pitch error, melodic and harmonic*
158 *interval error than the duet condition.* Participants sing the same pitch in the unison singing
159 condition while they sing harmony in the duet condition. An observation from choral singing
160 is that most singers, particularly those with less musical training, find it easier to sing their

161 vocal part when others around them are singing the same part. Singing in harmony with
162 different parts requires greater concentration, to avoid being distracted from one's own part.

163 Hypothesis 2: *Independent singers have less pitch error than dependent singers.* Audi-
164 tory feedback is essential for accurate intonation. As either noise (Mürbe *et al.*, 2002) or
165 simultaneously playing the target melody (Dai and Dixon, 2016; Pfordresher and Brown,
166 2007) reduces singers' accuracy, we expect to observe this effect in both singing conditions.
167 Although comparisons of pitch accuracy in unison versus solo singing did not always agree
168 with each other, the majority of existing evidence suggests that individual singing is more
169 accurate than unison singing (e.g. Clayton, 1986; Goetze, 1985, 1989).

170 Hypothesis 3: *The duplex condition has less harmonic interval error than the solo condi-*
171 *tion.* When singers do not hear each other, their errors are independent as it is impossible
172 for them to adjust their intervals according to their partner's intonation. When they can
173 hear their partner, they adjust their pitch in order to reduce the harmonic interval error.
174 Since most of the singers have choral experience, this hypothesis is based on the assumption
175 that such singers are somewhat able to attune to other singers and sing harmoniously as a
176 group, which is an important skill that is practised in their rehearsals (Bohrer, 2002).

177 Hypothesis 4: *There is a positive correlation between the pitch error of the dependent*
178 *singer and the independent singer in the simplex conditions.* The simplex condition allows
179 for a one-way influence of the intonation of the independent singer upon the dependent
180 singer. We predict that this influence will be seen not only in the magnitude of pitch
181 errors (it is harder to sing well when distracted by an out of tune partner), but also in the
182 direction of these errors (the dependent singer will adjust their pitch to reduce errors in

183 vertical harmonies at the expense of absolute pitch error and melodic interval error). Thus
184 a significant correlation between the pitch errors of dependent and independent singers
185 provides evidence of interaction. Although features of the score could explain correlation in
186 the unison condition (e.g. where both singers compress leaps), we predict this effect to hold
187 also for the duet condition, where the score would not have a uniform effect on both singers.

188 Hypothesis 5: *The within-note pitch variation of dependent singers is higher than that of*
189 *independent singers.* Our final hypothesis relates to the variation of pitch within each tone,
190 which provides another view of interaction between singers. In the independent condition,
191 any adjustment of pitch within a note arises from the singer’s own feedback loop and invol-
192 untary noise in the vocal production system. In the dependent condition, there is also scope
193 for intentional adjustment to improve harmonic intervals, as well as unintentional changes
194 due to the distraction of hearing another singer.

195 B. Design

196 To test these hypotheses, we designed and implemented a controlled experiment involving
197 two musical excerpts, two singing conditions (unison and duet) and three types of listening
198 conditions (solo, simplex, duplex), as listed in Table I. Each trial involves two singers,
199 denoted A and B. In the unison condition both singers sing the same vocal part (either the
200 soprano or alto part). In the duet condition, singer A sings the soprano part and singer
201 B the alto. For the listening conditions, the solo condition acts as a control, where the
202 two singers sing separately without hearing each other. In the two simplex conditions, only
203 one singer can hear their partner, with the direction of auditory feedback being reversed

Singing	Listening	A sings		A hears B	
Condition	Condition	B sings		B hears A	
Unison	Solo	Soprano	Soprano	No	No
Unison	Simplex	Soprano	Soprano	Yes	No
Unison	Simplex	Soprano	Soprano	No	Yes
Unison	Duplex	Soprano	Soprano	Yes	Yes
Unison	Solo	Alto	Alto	No	No
Unison	Simplex	Alto	Alto	Yes	No
Unison	Simplex	Alto	Alto	No	Yes
Unison	Duplex	Alto	Alto	Yes	Yes
Duet	Solo	Soprano	Alto	No	No
Duet	Simplex	Soprano	Alto	Yes	No
Duet	Simplex	Soprano	Alto	No	Yes
Duet	Duplex	Soprano	Alto	Yes	Yes

TABLE I. Experimental design for two singers A and B: singing and listening conditions.

204 between the two conditions. Finally in the duplex condition, both singers hear the voice of
205 their partner. Except for the voice of their partner in certain listening conditions, there is
206 no accompaniment during the experiment.

207 C. Musical Materials

208 We chose the soprano and alto parts of two common choral pieces “Silent Night” (Gruber,
209 c.1816) and “O Sacred Head, Now Wounded” (melody by Hassler, c.1601, harmonised by
210 J.S. Bach, c.1729) as our experimental materials. These two pieces are examples of the
211 traditional Western church choir repertoire with the former song being particularly well-
212 known. The pitch range is from A3 to Eb5 (soprano: Bb3 to Eb5; alto: A3 to G4) with
213 various melodic and harmonic intervals up to a minor 7th. The second piece was shortened
214 to its first 12 bars as shown in Figure 1 to match the lengths of the two pieces.

216 D. Participants

217 Although factors of age and gender affect pitch accuracy (Welch *et al.*, 1997), they are
218 not a target of this research. As our musical material consisted of soprano and alto parts,
219 we recruited female singers only. Because this experiment required singers to maintain their
220 own part while the other singer sang a different part, we recruited participants who have
221 choral experience. All participants are amateur singers who have some musical training, and
222 are members of our university’s music society, a *capella* society or our research group. Pairs
223 were allocated according to voice (one soprano, one alto) and availability. Although some
224 sing together in the same choir, no pair had sung together in a duet or small group before
225 the experiment. Each participant was involved in only one pair.

226 16 female UK residents took part in this experiment, with an age range from 19 to
227 30 years old (mean: 23.1; median: 23.5; SD: 3.3). Eight of the participants identified

Silent Night

John F. Young 1863

Franz X. Gruber circa 1816-1818

$\text{♩} = 120$

Soprano

Alto

7

S.

A.

Detailed description: This block contains the musical notation for the first part of 'Silent Night'. It features two staves: Soprano (S.) and Alto (A.). The key signature is B-flat major (two flats) and the time signature is 6/8. A tempo marking of quarter note = 120 is provided. The Soprano part begins with a treble clef and a key signature of two flats. The Alto part begins with a treble clef and a key signature of two flats. Both parts start with a 7-measure rest. The Soprano part consists of a series of eighth and quarter notes, while the Alto part consists of a series of eighth and quarter notes. The piece concludes with a double bar line.

Piece 1: Silent Night

O Sacred Head, Now Wounded

James W. Alexander, 1830

Adapted by J. S. Bach 1729

$\text{♩} = 100$

Soprano

Alto

7

S.

A.

Detailed description: This block contains the musical notation for the first 12 bars of 'O Sacred Head, Now Wounded'. It features two staves: Soprano (S.) and Alto (A.). The key signature is C major (no sharps or flats) and the time signature is 4/4. A tempo marking of quarter note = 100 is provided. The Soprano part begins with a treble clef and a key signature of no sharps or flats. The Alto part begins with a treble clef and a key signature of no sharps or flats. Both parts start with a 7-measure rest. The Soprano part consists of a series of quarter and eighth notes, while the Alto part consists of a series of quarter and eighth notes. The piece concludes with a double bar line.

Piece 2: O Sacred Head, Now Wounded (first 12 bars)

FIG. 1. Musical material selected for the experiments.

228 themselves as sopranos, the other eight as altos. The sopranos (age range: 19–27; mean:
229 23.0; median: 24.0; SD: 3.0) and altos (age range: 19–30; mean: 23.3; median: 22.5; SD:
230 3.4) had similar age distributions. All the participants were able to sing the pitch range
231 from A3 to Eb5 naturally, and could sing both pieces independently. In order to identify and
232 exclude any poor singers (Pfordresher and Brown, 2007), we calculated the mean absolute
233 melodic interval error (Equation 6) of each singer and planned to exclude any with an error
234 greater than 0.5 semitones; no singer needed to be excluded.

235 For testing the effect of training, all the participants completed a self-assessment question-
236 naire based on the Goldsmiths Musical Sophistication Index (Müllensiefen *et al.*, 2014) which
237 can be grouped into 4 main factors for analysis: active engagement, perceptual abilities, mu-
238 sical training and singing ability (9, 9, 7 and 7 questions respectively). The proportion of
239 singers having more than three years of choir experience is 62.5%; all have at least one year
240 of instrumental training; and 50.0% of the participants have at least six years of formal
241 training on musical instrument or voice.

242 E. Procedure

243 The study was conducted with the approval of the Queen Mary Ethics of Research
244 Committee (approval number: QMREC1456). The participants were grouped into eight
245 pairs of singers, each consisting of one soprano (singer A) and one alto (singer B) by self-
246 identification. Each pair participated in both the unison and duet singing conditions. Each
247 singer sang the two pieces in each of the four listening conditions as a set of data, resulting
248 in eight pairs of duet datasets, eight pairs of unison soprano and eight pairs of unison alto

249 datasets collected in this experiment, each consisting of eight recordings. All 384 recordings
250 were grouped and labelled with the pair number, music piece, experimental conditions and
251 the singer’s questionnaire results for analysis.

252 Before the recording, the singers were given about half an hour to warm up and be-
253 come familiar with the pieces. Participants practised their vocal parts with piano and their
254 partners. The recording did not start until the participants could sing their vocal parts
255 individually while their partner was singing the other part. At the beginning of each trial,
256 participants heard instructions identifying the piece and condition and were given their own
257 starting pitch repeated four times on a digital piano. During each trial, singers could hear a
258 metronome and read the music score, but no further reference pitch was provided, nor did
259 the participants talk to each other until the trial was completed. The trials were recorded
260 in the same order with the same equipment (described below). To avoid any effect of vowel
261 sound, and to assist annotation of note onset times, the participants were asked to sing the
262 syllable /ta:/ rather than the lyrics. The participants could not see their partner during the
263 trials. The total time of the experiment, including rehearsal, four listening conditions and
264 questionnaire, was about one and a half hours.

265 The experiment was performed in two acoustically isolated rooms at the authors’ univer-
266 sity with facilities for multi-track recording (Morrell *et al.*, 2011). The equipment included
267 an SSL MADI-AX analogue to digital converter, two Shure SM58 microphones and sound
268 isolating headphones (Beyer Dynamic DT100). All the tracks were controlled and recorded
269 with the software Logic Pro 10. The metronome and the reference pitches were also given
270 by Logic Pro. The two microphone signals and (for reference) the two headphone signals

271 were recorded on four separate tracks with a sampling rate of 44100 Hz and stored in .wav
272 format. The total latency of the system is 4.9 ms from microphone to headphone, where 3.3
273 ms is due to the processing time of Logic Pro and 1.6 ms ($71/44100$) due to the converter.

274 IV. DATA ANALYSIS

275 This section describes the annotation procedure and the measurement of the four metrics
276 of accuracy (pitch error, melodic interval error, harmonic interval error and pitch variation;
277 defined below). These metrics are the dependent variables for hypothesis testing, while test
278 and listening conditions are the main independent variables.

279 A. Annotation

We used the software *Tony* (Mauch *et al.*, 2015) to annotate the recordings with fundamental frequencies as extracted by the PYIN algorithm (Mauch and Dixon, 2014). The *Tony* software segments the recording into notes and silences, and outputs the median fundamental frequency f_0 for each note. The conversion of fundamental frequency to musical pitch \mathbf{p} is calculated as follows:

$$\mathbf{p} = 69 + 12 \log_2 \frac{f_0}{440}. \quad (1)$$

280 This scale is chosen such that its units are semitones, with integer values of \mathbf{p} coinciding with
281 MIDI pitch numbers, and reference pitch A4 ($\mathbf{p} = 69$) tuned to 440 Hz. After automatic
282 annotation, every single note was checked manually by the first author to make sure the
283 tracking was consistent with the data and corrected if it was not. The annotation of all 384

284 files took over 31 hours, and resulted in a database of 18176 annotated notes (2 singers \times 2
285 pieces \times 4 trials \times (1 duet + 2 unison) \times 8 groups = 384 files).

286 The information in our database includes: group number, singer number, singing condi-
287 tion, listening condition, piece number, note in trial, score onset position, score duration,
288 score pitch, score interval, observed onset time, observed duration, observed pitch, pitch
289 error, melodic interval error, harmonic interval error, anonymised participant details, and
290 questionnaire scores. We also store the pitch trajectory for each note. The data will be
291 published for subsequent research (Section IX).

292 B. Metrics of Accuracy

293 Our metrics of intonation accuracy are pitch error, interval error, and pitch variation,
294 defined below. The definitions of pitch error and interval error are based on Dai and Dixon
295 (2017); Mauch *et al.* (2014), while pitch variability is inspired by Pfordresher *et al.* (2010).

296 1. Pitch Error

297 *Pitch error* e_i^p for note i is the difference between the observed pitch and score pitch:

$$e_i^p = \bar{p}_i - p_i^s, \quad (2)$$

298 where \bar{p}_i is the median of the observed pitch trajectory of note i (calculated over the duration
299 of an individual note), and p_i^s is the score pitch of note i as defined by the MIDI standard,
300 where pitches are indexed by the note number from the beginning of the piece.

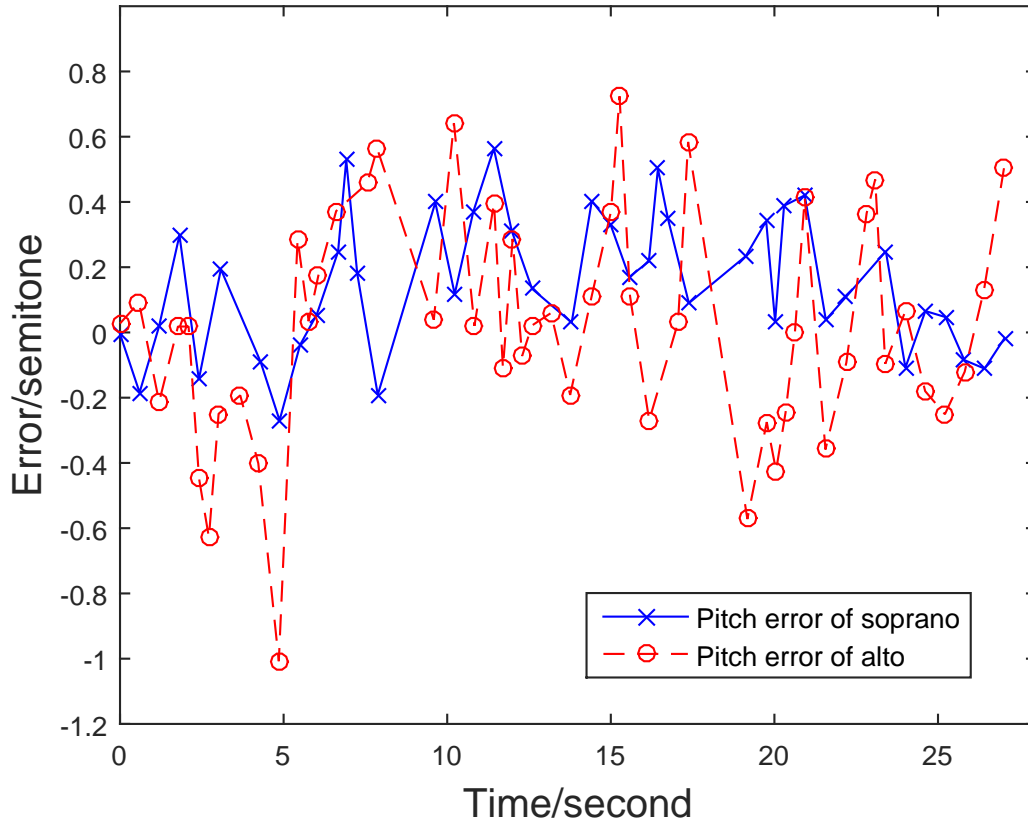


FIG. 2. Example of pitch error for piece 2, duet singing condition, duplex listening condition, for one pair of singers.

301 For example, when someone sings a score pitch of C5 at 510.34 Hz, this corresponds to
 302 $p = 71.57$ semitones (Equation 1), whereas the nominal pitch of C5 is 72. So the pitch error
 303 is $e^p = 71.57 - 72 = -0.43$ semitones. Pitch error measures the cumulative intonation error
 304 relative to the given starting tone. Figure 2 shows an example of pitch error for two singers
 305 in the duplex duet condition.

306 **2. Interval Error**

307 A musical interval is the difference between two pitches (Prout, 2011), which is pro-
 308 portional to the logarithm of the ratio of the corresponding fundamental frequencies. We
 309 distinguish two types of interval: a *melodic interval* is the pitch difference between two suc-
 310 cessive notes from a single singer, and a *harmonic interval* is the pitch difference between
 311 two simultaneous notes from different singers.

312 We define the melodic interval error e_i^m between the i th sung interval and the correspond-
 313 ing score interval as:

$$e_i^m = (\bar{p}_{i+1} - \bar{p}_i) - (p_{i+1}^s - p_i^s), \quad (3)$$

314 For example, if F4 is sung at $\bar{p}_i = 65.74$ and the subsequent note C5 at $\bar{p}_{i+1} = 71.57$, there
 315 should be a difference of $72 - 65 = 7$ semitones, but the observed difference is 5.83 semitones.
 316 So the melodic interval error for this case is -1.17 semitones.

317 The harmonic interval error is defined similarly: we subtract the score interval from the
 318 observed harmonic interval, as in equation 3. The notation is more complex in this case as:
 319 (1) a subscript is added to identify the singers; and (2) simultaneous notes might not always
 320 share the same sequence index, due to rests or multiple notes in one part while there is a
 321 single note in the other. The harmonic interval error e_k^h between singers A and B is:

$$e_k^h = (\bar{p}_{A,i} - \bar{p}_{B,j}) - (p_{A,i}^s - p_{B,j}^s), \quad (4)$$

322 where $p_{x,y}$ is the y th pitch of singer x , with \bar{p} and p^s used as above, and notes (A, i) and
 323 (B, j) are assumed to be simultaneous (or at least overlapping in time).

324 Pitch error measures the absolute tuning, while melodic interval error captures local
 325 tuning within a vocal part. Harmonic interval error captures the local tuning between vocal
 326 parts, thereby facilitating analysis of the interaction between two singers.

327 **3. Pitch Accuracy over Multiple Notes**

328 To evaluate the pitch accuracy over a group of notes, we use the mean absolute value of
 329 each type of error as a summary measurement. For a group of M notes with pitch errors
 330 $\{e_1^p, \dots, e_M^p\}$, the *mean absolute pitch error* (MAPE) is defined as:

$$\text{MAPE} = \frac{1}{M} \sum_{i=1}^M |e_i^p|. \quad (5)$$

331 The *mean absolute melodic interval error* (MAMIE) over M intervals is given by:

$$\text{MAMIE} = \frac{1}{M} \sum_{i=1}^M |e_i^m|, \quad (6)$$

332 and the *mean absolute harmonic interval error* (MAHIE) is defined similarly as:

$$\text{MAHIE} = \frac{1}{M} \sum_{i=1}^M |e_i^h|. \quad (7)$$

333 **4. Pitch Variation**

334 The pitch variation of a note is defined as the mean square pitch difference of the note
 335 trajectory from its median value. It indicates the extent of pitch variation over the duration
 336 of the note. The larger the pitch variation, the less stable the pitch. For a single note with
 337 N sampling points, where $p(i)$ represents the pitch at sampling point i and \bar{p} is the median

338 of $p(i)$ over the N points, the pitch variation V is calculated as follows:

$$V = \frac{1}{N} \sum_{i=1}^N |p(i) - \bar{p}|^2, \quad (8)$$

339 where the default sampling period for *Tony* is 5.8 ms. The *mean pitch variation* (MPV) is
340 the mean value of pitch variation over multiple notes.

341 V. RESULTS

342 We calculated MAPE (Equation 5), MAMIE (Equation 6), MAHIE (Equation 7) and
343 pitch variation (Equation 8) for each condition. In addition to the experimental conditions,
344 we tested other possible factors for their effect on singing intonation. Over all conditions,
345 the singers had an MAPE of 36 cents (SD=39), MAMIE of 24 cents (SD=28) and MAHIE
346 of 41 cents (SD=47). We grouped the MAPE according to different factors, and fitted the
347 grouped data separately into a one-way analysis of variance (ANOVA) model for testing the
348 influence of each individual factor. The ANOVAs showed that the following factors influence
349 the MAPE and MAMIE : singing condition, listening condition, score pitch, score melodic
350 interval, score harmonic interval, note duration, piece, vocal part, singer, age and musi-
351 cal background (Table II). As harmonic intervals involve notes from both singers, MAHIE
352 cannot test factors such as score pitch and vocal part. The ANOVA showed that singing
353 condition, listening condition, note number in trial, music piece and score harmonic interval
354 have a significant effect on MAHIE.

355 In this section, we focus on single factors of influence to test our hypotheses concerning
356 intonation accuracy and pitch variation across the various experimental conditions.

Factor	MAPE	MAMIE	MAHIE
Singing condition	F(1, 18174) = 70.8 ***	F(1, 18174) = 17.0 ***	F(1, 9086) = 316.7 ***
Listening condition	F(3, 18172) = 52.2 ***	F(3, 18172) = 41.0 ***	F(3, 9084) = 16.1 ***
Note number in trial	F(54, 18121) = 6.4 ***	F(54, 18121) = 15.2 ***	F(54, 9033) = 1.8 ***
Score pitch	F(15, 17552) = 22.3 ***	F(15, 17552) = 12.7 ***	
Score melodic interval	F(13, 18162) = 8.0 ***	F(13, 18162) = 90.6 ***	
Score harmonic interval	F(11, 18164) = 11.8 ***	F(11, 18164) = 13.5 ***	F(11, 9076) = 34.5 ***
Score duration	F(7, 18168) = 13.8 ***	F(7, 18168) = 94.5 ***	
Piece	F(1, 18174) = 102.7 ***	F(1, 18174) = 132.0 ***	F(1, 9086) = 121.5 ***
Vocal part	F(1, 18174) = 46.8 ***	F(1, 18174) = 58.8 ***	
Age	F(9, 18166) = 166.0 ***	F(9, 18166) = 59.4 ***	
Musical background	F(13, 18162) = 177.8 ***	F(13, 18162) = 77.6 ***	

TABLE II. Results of one-way ANOVAs testing each error type grouped by different factors (**p<.001; *p<.01; *p<.05; NS: not significant).

357 A. Unison vs Duet Singing Condition

358 To test our first hypothesis, that the unison condition has lower pitch error and interval
359 errors than the duet condition, a one-way ANOVA was conducted. For testing MAPE and
360 MAMIE, we use only the data from dependent singers (those who can hear their partners),

	Condition		Significance of Difference
	Unison	Duet	
MAPE	0.3518 ± 0.0057	0.4679 ± 0.0076	F(1, 9086) = 149.38, p < .001
MAMIE	0.2587 ± 0.0039	0.2637 ± 0.0052	F(1, 9086) = 0.64, p = 0.42
MAHIE	0.3447 ± 0.0060	0.5243 ± 0.0081	F(1, 2270) = 262.23, p < .001

TABLE III. Results of one-way ANOVA testing the effect of singing condition on accuracy metrics, expressed as mean value ± the 95% confidence interval.

361 which is one of the singers in the simplex listening condition and both singers in the duplex
362 condition. Harmonic intervals involve both singers, so we only use the data from the duplex
363 condition for MAHIE. Results show a significant effect of singing condition on MAPE and
364 MAHIE, but not for MAMIE (see Table III). Post hoc comparisons using the Tukey HSD
365 test confirmed that MAPE and MAHIE were significantly lower for the unison condition
366 than for the duet condition.

367 The results confirmed our hypothesis for MAPE and MAHIE, but not for MAMIE. The
368 reason for the higher MAPE in the duet condition (by 12 cents) may be due to the distraction
369 of someone singing a different note, making it more difficult to sing one’s own note than
370 when the partner is singing the same note. For harmonic intervals, the duet condition has
371 twelve different score intervals, while the unison condition has only one score interval, the
372 unison interval. The various score intervals are more difficult to sing in tune, resulting in a
373 higher MAHIE (by 38 cents) for the duet condition.

374 For MAMIE, there is no significant difference between the unison and duet conditions, so
375 we did not find any influence of singing condition on the tuning of melodic intervals. Since
376 melodic intervals are tuned from one's own previous note, the other singer has no direct
377 effect on the target interval, unlike in harmonic intervals, where the tuning is between the
378 singers. The same argument, however, should also apply to pitch error, where a significant
379 difference was observed. The relationship between the three error measures is complex, as
380 any change in a single pitch will alter all measures. Here we see a tendency that when
381 people sing different parts, their relative tuning to each other and absolute tuning to the
382 initial reference suffer, although their local melodic intervals appear no worse. Given an
383 imperfect partner, we suggest that ideal singing would involve a tradeoff between all three
384 error types.

385 B. Effect of Listening Condition

386 Hypotheses 2 and 3 predict that the solo listening condition has less pitch error but
387 greater harmonic interval error than the duplex condition. ANOVA tests were conducted
388 to test whether the four listening conditions have an influence on each measure of accuracy.
389 Since the differences between listening conditions depend on whether singers can hear the
390 voice of their partners, we separate the data from the simplex conditions into two cases:
391 dependent singers and independent singers.

392 The ANOVA results showed that the effects of listening condition on MAPE, MAHIE
393 and MAMIE were all significant: for MAPE, $F(3, 18172) = 52.16$, $p < .001$; for MAMIE,
394 $F(3, 16956) = 38.77$, $p < .001$; and for MAHIE, $F(2, 9085) = 12.76$, $p < .001$. The ANOVA

Significance of Difference				
	Solo	NS	***	***
		Simp. Indep.	***	***
			Simp. Dep.	***
				Duplex
MAPE	0.32 ± 0.0058	0.33 ± 0.0058	0.38 ± 0.0058	0.41 ± 0.0058

TABLE IV. Results of Tukey HSD test showing the effect of listening condition (solo, simplex independent, simplex dependent, duplex) on MAPE (** $p < .001$; ** $p < .01$; * $p < .05$; NS: not significant).

The bottom line shows the mean value \pm 95% confidence interval for each group.

395 test tells whether there is an overall difference between groups, but it does not tell which
396 specific groups differed. Post hoc comparisons using the Tukey HSD test were applied to
397 find out which specific groups differed (Tables IV, V and VI).

398 The results support hypothesis 2, as the MAPE of the solo condition has 9 cents less
399 pitch error than the duplex condition (Table IV). In general, participants have more pitch
400 error when they can hear their partner singing than when they sing independently. This
401 applies not only to the solo and duplex conditions, but also to the simplex conditions; in
402 all cases, independent singers (solo and simplex independent) have significantly less MAPE
403 than dependent singers (simplex dependent and duplex).

404 We also observed that the MAPE of dependent singers in the simplex condition is better
405 than that in the duplex condition. This difference can be explained by considering that the

Significance of Difference			
Solo	***	*	
	Simplex	NS	
		Duplex	
MAHIE	0.45 ± 0.0041	0.39 ± 0.0041	0.41 ± 0.0041

TABLE V. Results of Tukey HSD test showing the effect of listening condition (solo, simplex, duplex) on MAHIE (*** $p < .001$; ** $p < .01$; * $p < .05$; NS: not significant). The bottom line shows the mean value \pm 95% confidence interval for each group.

Significance of Difference			
Solo	**	***	***
	Simp. Indep.	***	***
		Simp. Dep.	NS
		Duplex	
MAMIE	0.23 ± 0.0098	0.21 ± 0.0098	0.26 ± 0.0098

TABLE VI. Results of Tukey HSD test showing the effect of listening condition (solo, simplex independent, simplex dependent, duplex) on MAMIE (*** $p < .001$; ** $p < .01$; * $p < .05$; NS: not significant). The bottom line shows the mean value \pm 95% confidence interval for each group.

406 partner of the dependent singer is an independent singer, while the partner of the duplex
407 singer is a dependent singer. We saw above that independent singers have lower MAPE
408 than dependent singers, and accordingly their partners, who hear them, also sing with less
409 pitch error.

410 The results for hypothesis 3 are shown in Table V. In agreement with the hypothesis, the
411 duplex condition has less harmonic interval error than the solo condition, even though the
412 pitch error and melodic interval error are greater. For MAHIE, there is also a significant
413 difference between solo and simplex conditions ($p < 0.001$) but not between the simplex and
414 duplex conditions ($p > 0.05$).

415 As shown in Table VI, dependent singers in the simplex and duplex conditions have
416 more MAMIE than independent singers ($p < 0.001$ in all four cases). These results have a
417 similar pattern to those obtained for MAPE. An unexpected significant difference was found
418 between the two independent conditions (where the singer cannot hear her partner). The
419 effect size is small (2 cents), and can be explained as an order effect, as the solo condition
420 preceded the simplex conditions.

421 C. Correlation of Dependent and Independent Singers' Errors

422 We then test hypothesis 4, whether there is a linear relationship between the pitch error
423 (PE) of dependent and independent singers in the simplex condition. A linear regression
424 was performed to model the pitch error of the dependent singer e_D^p as a function of the
425 pitch error of the independent singer e_I^p (Figure 3), using the data from the duet condition
426 only. A significant regression equation was found, $e_D^p = 0.02 + 0.91e_I^p$ ($p < .001$), with

427 $R^2 = 0.28$. The unison singing condition also exhibited a significant linear relationship, but
 428 with a smaller slope than in the duet condition.

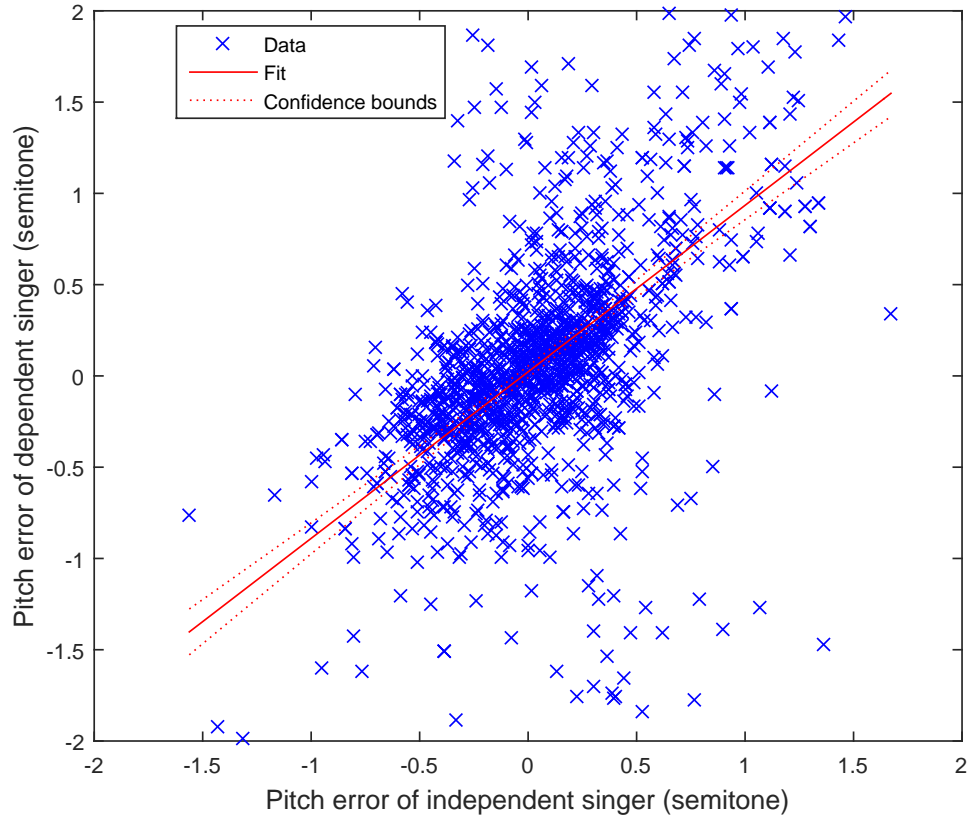


FIG. 3. Scatter plot showing the correlation between independent and dependent singers' pitch error in the duet singing condition and simplex listening condition.

429 The melodic interval error (MIE) of dependent singers is also positively correlated to the
 430 MIE of independent singers ($r = 0.41$, $p < 0.001$) in the duet condition. The weak linear
 431 relationship is described by the following formula: $e_D^m = 0.005 + 0.59e_I^m$, with $R^2 = 0.17$.
 432 There was also a significant but weak linear relationship between pitch variation of dependent
 433 singers and independent singers ($r = 0.12$, $p < 0.001$).

434 **D. Pitch Variation within Notes**

435 Hypothesis 5 concerns the pitch variation of dependent and independent singers. Pitch
436 variation (Equation 8) does not show any significant effect of listening condition ($F(3, 17564) =$
437 $1.47, p = 0.22$). Likewise, an ANOVA applied to the two groups dependent singer and inde-
438 pendent singer does not show a significant difference ($F(1, 17566) = 1.74, p = 0.19$). Thus
439 the results fail to confirm our final hypothesis. We had expected to find evidence of singers
440 adjusting to their partner’s pitch during a note. Some pairs of participants show a significant
441 difference, where the pitch variation of dependent singers is higher than that of independent
442 singers, as predicted, but this effect was not consistent across the whole dataset.

443 Moreover, the pitch variation in the unison condition (mean: 0.09; SD: 0.14) is lower
444 than in the duet condition (mean: 0.11; SD: 0.16), with a statistically significant difference
445 ($F(1, 17566) = 53.95, p < .001$). The pitch trajectories of the unison condition tend to be
446 flatter in shape than those of the duet condition. There are a few factors that significantly
447 influence pitch variation: the piece ($F(1, 17566) = 52.61, p < .001$), individual differences
448 ($F(15, 17552) = 53.62, p < .001$), and score pitch ($F(15, 17552) = 20.6, p < .001$), where
449 the high pitches (D5, Eb5) in particular exhibit greater variation. Thus pitch variation
450 appears to reflect uncertainty of the singer in trying to reach the intended pitch, rather than
451 deliberate adjustments to improve intonation.

452 E. Factors Based on the Score

453 The target pitch and its melodic and harmonic context are also expected to influ-
454 ence singing accuracy. We tested these factors with a series of ANOVAs. Score pitch
455 ($F(15, 17552) = 22.23, p < .001$), score melodic interval ($F(13, 18162) = 7.99, p < .001$) and
456 score harmonic interval ($F(11, 18164) = 11.8, p < .001$) all have a significant effect on MAPE.
457 Likewise for MAMIE, score pitch ($F(15, 16346) = 10.88, p < .001$), score melodic interval
458 ($F(13, 16946) = 89.02, p < .001$) and score harmonic interval ($F(11, 16948) = 13.3, p < .001$)
459 all have a significant effect.

460 Although the score pitch has a significant effect on MAPE, the correlation between them
461 does not show a linear trend. It is rather the musical context which dictates which notes elicit
462 larger errors, as shown by the interval-based results below. The most accurate pitch is C4
463 (0.260 ± 0.009) while the least accurate pitches are A3 (0.514 ± 0.023) and D \sharp 4 (0.452 ± 0.011).

464 Figure 4 shows the MAMIE for each score interval. The errors group into three clusters
465 corresponding to (absolute) interval size. The unison interval has the smallest error, less
466 than 15 cents, while intervals of one to three semitones have mean errors between 25 and
467 30 cents, and larger intervals have mean errors between 30 and 45 cents. All differences
468 between clusters are significant, except for the ascending minor 7th (+10 semitone) interval,
469 discussed below, and the ascending major third (+4), which lies on the border between
470 the two clusters. We thus see a general pattern of larger errors for larger intervals, with a
471 small and non-significant tendency for descending intervals to have larger errors than their
472 ascending counterparts. The ascending minor 7th interval is exceptional, being the largest

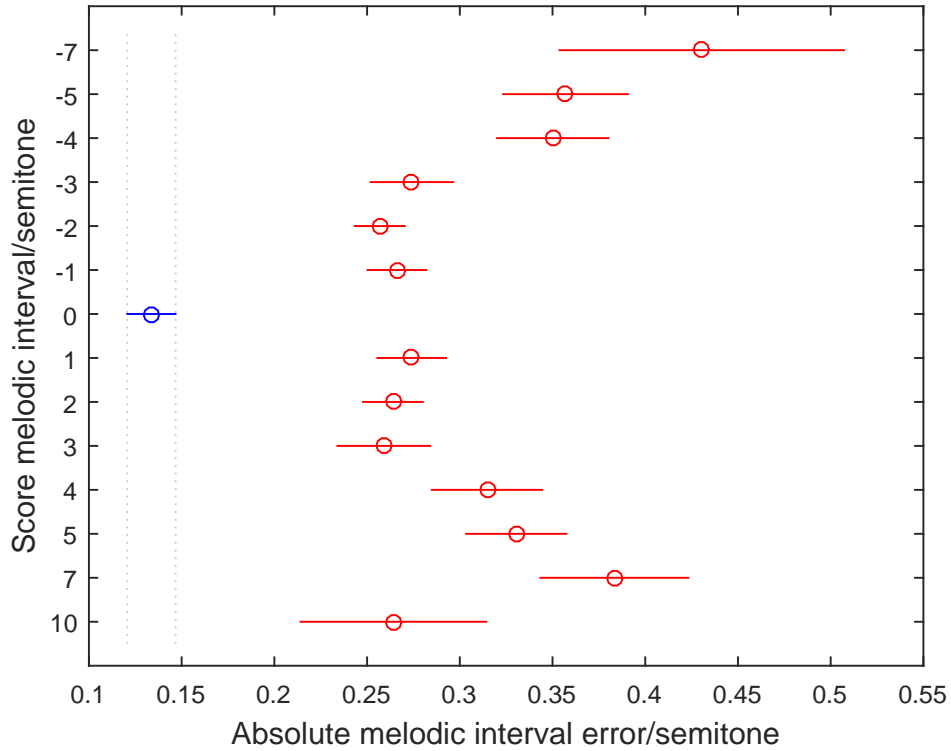


FIG. 4. The mean estimates and the standard errors of absolute melodic interval error for each score melodic interval (significant differences from the unison interval are shown in red).

473 interval, but having an error in the range of the smaller interval cluster. This interval only
 474 occurs twice, both times in the soprano part of the first piece. We believe the lower error is
 475 due to the fact that this melody (Silent Night) is particularly well-known.

476 The score harmonic interval has a significant effect on MAHIE ($F(11, 9076) = 34.48, p <$
 477 $.001$), as shown in Figure 5. Again the unison interval has the lowest error, and most
 478 score harmonic intervals have significant differences in MAHIE from the unison interval,
 479 except the major second and major sixth intervals. The least consonant intervals have the
 480 greatest error, with the minor second (mean:0.66; SD=0.98) and diminished fifth (mean:0.67;
 481 SD=0.79) having the largest MAHIE and also the largest spread of values.

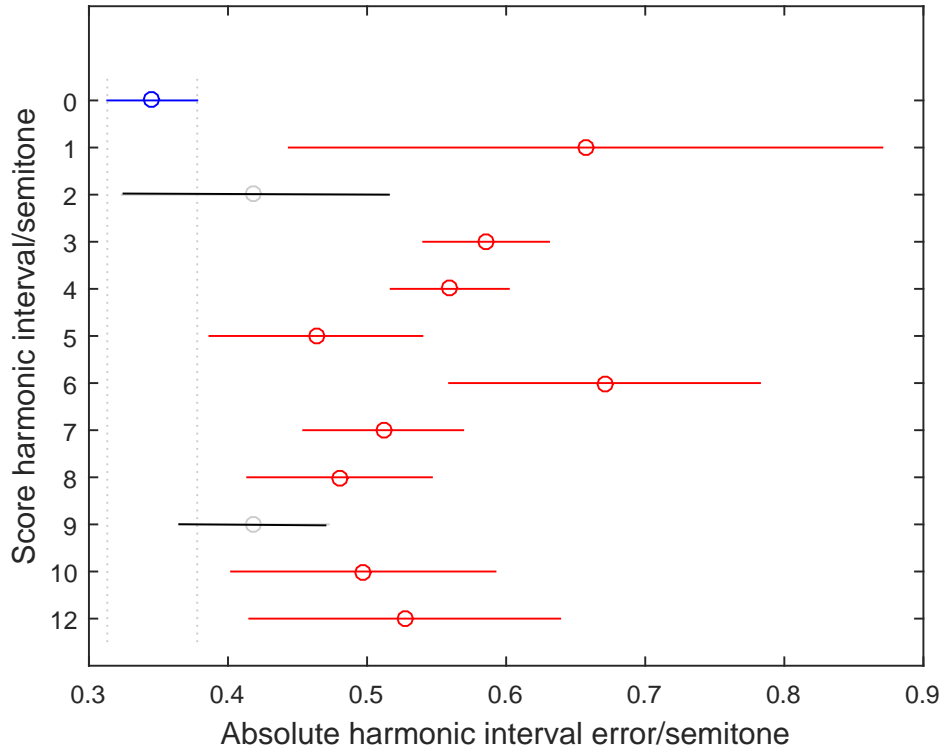


FIG. 5. The mean estimates and the standard errors of absolute harmonic interval error for each score harmonic interval (significant differences from the unison interval are shown in red).

482 F. Vocal Part

483 The effect of vocal part (soprano, alto) on intonation accuracy was also investigated.
 484 Based on a one-way ANOVA, the vocal part has a statistically significant effect on MAPE
 485 ($F(1, 18174) = 46.78, p < .001$) and MAMIE ($F(1, 18174) = 58.76, p < .001$).

486 According to Section [VA](#), the unison condition has less MAPE and MAMIE than the
 487 duet condition in general. However, we find an interaction with the factor of the vocal
 488 part. A two-way ANOVA was performed to examine the effect of singing condition and
 489 vocal part on MAPE. There is a significant interaction between the effects of vocal part and

490 singing condition ($F(1, 18172) = 61.96, p < .001$). Simple main effects analysis (Table VII)
 491 showed that sopranos have significantly less MAPE than altos in the duet singing condition
 492 ($F(1, 6462) = 82.14, p < .001$) but there are no significant differences between vocal parts
 493 in the unison condition ($F(1, 11710) = 1.08, p = 0.30$). Further, the MAPE of the soprano
 494 part does not change significantly between the unison and duet conditions, but the alto part
 495 has a significantly larger MAPE in the duet condition as opposed to the unison condition.
 496 For MAMIE in both vocal parts, the duet condition has lower MAMIE than the unison
 497 condition, and in both conditions, the alto part has greater MAMIE than soprano.

	Unison	Duet	Significance:
	singing condition		
MAPE Soprano	0.34	0.34	NS
MAPE Alto	0.34	0.44	***
Significance: vocal part	NS	***	
MAMIE Soprano	0.23	0.21	***
MAMIE Alto	0.26	0.25	**
Significance: vocal part	***	***	

TABLE VII. MAPE and MAMIE of soprano and alto in unison and duet singing conditions, and dependent listening conditions, showing the significance of differences between vocal parts and between singing conditions (*** $p < .001$; ** $p < .01$; * $p < .05$; NS: not significant).

498 G. Pitch Drift

499 Besides the previous factors, the note number in the trial also has a significant influence
500 on MAPE ($F(54, 18121) = 6.44, p < .001$ in Table II). Note number in trial is positively
501 correlated with MAPE, which means that the absolute pitch error increases with time.
502 The regression equation describing the relationship of note number in trial i and MAPE
503 is: $MAPE = 0.235 + 0.002i$, with $R^2 = 0.016, p < .001$. For each adjacent note, MAPE
504 increases by 0.2 cents, resulting in about 10 cents of increase in MAPE from the beginning
505 to the end of each trial.

506 The direction of the drift varies according to individual differences (Dai *et al.*, 2015; Mauch
507 *et al.*, 2014); there was no overall trend to drift upwards or downwards. The magnitude of
508 drift is similar to that found in a previous study (Mauch *et al.*, 2014), where drift of 13.8
509 cents over 50 notes was found.

510 VI. A COMBINED MODEL FOR PITCH ERROR

511 Section V investigated single factors that influence the pitch accuracy of solo, unison and
512 duet singers. In this section, we fit the investigated factors to a single linear mixed effects
513 model for absolute pitch error, in order to test whether such a joint model can account for
514 the variations in MAPE.

515 The multiple factors were analysed using linear mixed-effects regression (LMER), using
516 the `fitlme` function in Matlab and MAPE as the dependent variable. LMER has an ad-
517 vantage over standard data aggregation and repeated-measures ANOVA analysis, in that it

518 controls for the variance associated with random factors without data aggregation. Before
519 building the LMER model, the candidate factors were each tested with a one-dimensional
520 linear regression. Some factors such as score pitch, score melodic interval, score harmonic
521 interval, age, musical background and note duration have a significant effect according to
522 the ANOVA test, but their effect is not linear. (Added: Applying simple non-linear transfor-
523 mations to these variables does not change this fact: the effect of pitch and interval depends
524 on the musical context, e.g. the tonality and the consonance or otherwise of the notes (see
525 Figures 4 and 5); age has a limited range; musical background is sparse, dominated by indi-
526 vidual factors; and duration is dominated by other score factors (the pitches of the longest
527 and shortest notes).) For the factors which have a linear effect, we add them one by one
528 into the LMER model and compare with the previous model (i.e. without that factor), using
529 0.05 as the p-value threshold for rejecting insignificant factors.

530 The resulting model involved singing condition, vocal part, listening condition and note
531 number in trial as fixed effects. As random effects, we have two factors: the individual singer
532 and the piece. Visual inspection of residual plots did not reveal any obvious deviations from
533 normality. P-values were obtained by likelihood ratio tests of the full model with the effect
534 in question against the model without the effect in question. Table VIII shows the resulting
535 LMER model, where all the tested factors are significant. The same process was attempted
536 for MAMIE and MAHIE, but did not give a significant result.

537 In Section V A, the duplex condition has a larger MAPE than the other listening condi-
538 tions, but the LMER gives the opposite result. To investigate further, we applied the LMER
539 model to each group of participants individually, and found that the effect size and tendency

Factor	Coeff.	SE	Significance
(Intercept)	0.0014	0.0500	NS
Note number in trial	0.0007	0.0002	**
Unison condition	-0.0378	0.0076	***
Simplex dependent	0.0300	0.0103	**
Simplex independent	0.0235	0.0103	**
Duplex	-0.0459	0.0100	***
Alto part	0.0528	0.0078	***

TABLE VIII. A linear mixed-effects regression model for absolute pitch error, showing coefficient estimate (Coeff.), standard error (SE) and significance level of all predictors in the analysis (** $p < .001$; ** $p < .01$; * $p < .05$; NS: not significant).

540 vary across groups. For 3 of the groups, the duplex condition has a significant positive effect
541 on MAPE, while 4 groups show a significant negative effect size, and one has no significant
542 difference between conditions. (Added: To account for these group differences the model
543 was refitted with random slopes for condition across groups. However, after refitting with
544 random slopes, the listening conditions do not show any significant results in the LMER
545 model.) Other research on individual versus unison singing has similar controversial results.
546 In a pilot study, [Smith \(1973\)](#) observed some fifth and sixth grade children who sang accu-
547 rately in a group but not alone, and others who sang more accurately alone. Some report
548 a positive effect of unison singing ((e.g. [Smith, 1973](#))) while others report negative results

549 ((e.g. [Goetze, 1989](#))). Our study includes duet as well as unison singing, and we find that
550 listening condition generally has a significant effect on pitch accuracy, but the tendency and
551 effect size vary due to individual differences.

552 VII. DISCUSSION

553 It is evident that dependent singers adjusted their pitch influenced by their partners'
554 pitch. An important question to resolve is whether these adjustments were deliberate (e.g.
555 to mitigate inaccuracies in their partner's singing), or inadvertent changes caused by the
556 distraction of the partner's voice. [Table V](#) shows that the MAHIE in the simplex and
557 duplex conditions is smaller than in the solo condition ($p < .001$). At the same time, singers
558 who hear the voice of their partners (dependent singers) have higher MAPE and MAMIE
559 than independent singers. Taken together, this supports the view that singers sacrifice some
560 accuracy in singing their own part in order to harmonise (or sing in unison) better with their
561 partner.

562 In this work, we report averages across singers (and their partners), not taking into ac-
563 count individual characteristics which may vary from pair to pair, for example the tendency
564 of a singer to lead or follow, regardless of their partner's accuracy. One could characterise
565 such tendencies by the extent of influence of the partner's singing, where a leader would be
566 influenced less and a follower more by their partner's pitch. It is likely that such character-
567 istics of interaction exist and influence the results, but our experimental design (each singer
568 sings with a fixed partner) does not allow us to determine such cases unambiguously, as a
569 singer's behaviour might arise in part from a reaction to their particular partner.

570 In a standard choral situation, multiple singers are assigned to each of several parts. Our
571 study only considers the simpler case of two singers, and we must use caution in extrapolating
572 to the more general case. Conventionally, conductors group singers with the same vocal
573 part together. The overall lower pitch error for the unison condition supports this practice,
574 although the interaction with vocal part suggests that it might not be necessary for the sake
575 of a dominant part such as soprano. Another choral practice supported by these results is to
576 place weaker singers next to strong singers so that they can intentionally follow their pitch.

577 Although the participants of this study were selected as having vocal performance and
578 choral experience, they are all amateur singers. They were given limited time to learn their
579 parts (although one can assume that they already knew the melody of Silent Night), so
580 some of the error could be due to lack of familiarity with the parts. We might have obtained
581 different results if we had focused on professional singers, where the overall level of accuracy
582 is likely to have been much higher.

583 **VIII. CONCLUSIONS**

584 This paper presented an experiment investigating pitch accuracy and interaction in un-
585 accompanied duet singing. 16 female participants sang two pieces of music in two singing
586 conditions (unison and duet) and three types of listening condition (solo, simplex and du-
587 plex). The results indicated significant effects of the following factors on absolute pitch
588 error: singing condition, listening condition, vocal part, and note number in trial, as well
589 as score factors and individual factors of the singer. Likewise the melodic intervals and the
590 harmonic intervals were affected by the same factors.

591 In terms of singing conditions, the unison condition has 12 cents less mean absolute pitch
592 error and 38 cents less mean absolute harmonic interval error than the duet condition. This
593 gives some measure of the additional difficulty of singing in harmony, and particularly of
594 tuning non-unison intervals.

595 The general effect of singing with a partner is an increase in errors of individual pitches
596 and intervals, but a reduction in the error of the interval between singers. That is, singers
597 adjust their pitch to harmonise better with their partner, at the expense of continuity of
598 tonal reference. Independent singers have 7 cents less pitch error than singers who can hear
599 their partner.

600 The target harmonic interval has a significant effect on MAHIE, with dissonant intervals
601 having the largest errors and the unison interval the smallest. For melodic intervals, the
602 perfect fifth had the largest MAMIE, which is somewhat surprising considering the previous
603 result and the fact that it is a consonant interval. However it is one of the largest melodic
604 intervals in our material (exceeded only by the two minor 7th leaps in the soprano part of
605 Silent Night), and thus we suggest the size of the interval to be a contributing factor in this
606 case. We would expect consonance of intervals to play a smaller role for melodic intervals
607 than harmonic intervals, since the pitches do not sound simultaneously in the melodic case.

608 We found a positive correlation between the signed pitch errors of dependent singers and
609 independent singers in the simplex condition. In other words, if one singer sings sharp, their
610 partner is influenced to sing sharp as well. The correlation of pitch errors is again evidence
611 of interaction, that singers adjust their pitch to improve harmonic intervals at the expense
612 of melodic intervals and preservation of the tonal reference.

613 Analysis of the pitch trajectories within tones revealed greater stability of pitch in the
614 unison condition than the duet condition, but not in independent singers over dependent
615 singers. Although stability is correlated with singing accuracy, pitch variation is necessary
616 if singers are to adjust dynamically to the pitch of an imperfect partner, which is what we
617 expected to find in the data. However, our results suggest that the observed pitch variation
618 arises more from imprecision or uncertainty than deliberate adjustment. Further analysis of
619 the pitch trajectories would be an interesting avenue for future work.

620 We also tested the obtained factors in a combined model using linear mixed-effects regres-
621 sion. The model shows note number in trial, singing condition, listening condition and vocal
622 part have a significant influence on absolute pitch error. More specifically, the absolute pitch
623 error increases about 10 cents over a trial, indicating the existence of pitch drift. The unison
624 condition has 4 cents less absolute pitch error than the duet condition. For singing condition,
625 the simplex conditions involve a small increase in pitch error, in agreement with results in
626 Section VB, but the duplex condition gave a decrease of 5 cents, contrary to the previous
627 results. The effect of the duplex condition varied in direction and size between groups, with
628 some groups performing better together while other groups sing better individually.

629 There is considerable scope for further work on singing intonation and interaction, either
630 by extending the analysis of the dataset, which is released as open data (Section IX), or by
631 collecting further data for analysis. In particular, in order to move towards more typical
632 musical settings, we would need to investigate cases where there are multiple (more than
633 two) singers per part, multiple parts, and instrumental accompaniment. In a follow-up

634 study, we have recorded several quartets singing in an SATB setting, the preliminary results
635 of which have been reported (Dai and Dixon, 2017).

636 IX. DATA AVAILABILITY

637 The code and the data needed to reproduce our results (note annotations, question-
638 naire results, score information) are available from [https://code.soundsoftware.ac.uk/
639 projects/pitch-accuracy-and-interaction-in-unaccompanied-duet-singing/repository](https://code.soundsoftware.ac.uk/projects/pitch-accuracy-and-interaction-in-unaccompanied-duet-singing/repository).

640 ACKNOWLEDGMENTS

641 The study was conducted with the approval of the Queen Mary Research Ethics Com-
642 mittee (approval number: QMREC1456).

643 Many thanks to all of the participants who contributed to this project, including the
644 QMUL *A Capella* Society, QMUL Music Society. We also thank Marcus Pearce and Daniel
645 Stowell for their advice on data analysis. Jiajie Dai is supported by a China Scholarship
646 Council and Queen Mary Joint PhD Scholarship.

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List of Changes

Added: Applying simple non-linear transformations to these variables does not change this fact: the effect of pitch and interval depends on the musical context, e.g. the tonality and the consonance or otherwise of the notes (see Figures 4 and 5); age has a limited range; musical background is sparse, dominated by individual factors; and duration is

dominated by other score factors (the pitches of the longest and shortest notes). , on page 35, line 522.

Added: To account for these group differences the model was refitted with random slopes for condition across groups. However, after refitting with random slopes, the listening conditions do not show any significant results in the LMER model., on page 36, line 542.



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