# The Assessment of Surface Quality in Planed and Spindle Moulded Products 

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## SUMMARY

There are a lack of objective surface quality assessment standards in the timber planing industry. The current practice, that of visual and tactile inspection, results in a wide variance in what is classed as an acceptable or a defective surface finish. These methods, by their very nature, are subjective, and restricted to post-process application. Modern woodworking machines "extrude" timber at extremely high rates, often in excess of $140 \mathrm{~m} / \mathrm{min}$. When the machining process develops a significant fault, a large quantity of defective timber is produced before the symptoms are detected by post-process inspection.

Evidently, there is a need to develop sensors capable of real-time, in-process monitoring of the surface quality. Thus, when process faults occur they are detected instantaneously, so that any necessary remedial action may be effected immediately.

Due to the high cutting speeds and vibration levels associated with wood machining, contact methods of in-process surface assessment are precluded; optical methods provided a more adequate bandwidth.

Discussions with woodworking machinery manufacturers and users reveal that the form and frequency variation of the planed surface are the critical factors that control its aesthetic qualities.

This thesis describes the development and validation of a non-contact, surface assessment system for planed and spindle moulded timber. The system uses a novel

Laser illumination and Machine Vision technique. The signal processing analyses the surface information using Fourier techniques to produce frequency "signature". These are then analysed to provide data on product quality.

The laser instrument, comprising, interface circuitry, optics and computer algorithms, to facilitate data capture from real surfaces, is a post-process device, designed using the principles of in-process assessment. A Fast Fourier Transform algorithm was used to convert the captured data to the frequency domain. In this form the data was further analysed, using tailored algorithms, to identify the nature and origins of any surface faults.

A mathematical model of the machining process was also developed and used as the nucleus around which a computer, surface simulation, algorithm was written. This model and algorithm was used as a tool to give insight into the nature of real machined surface profile faults, and to indicate their origins.

The laser instrument was validated by comparing its surface assessment results with that of an established standard engineering surface assessing system. Future work will include making the instrument more compact and adapting it for in-process use.

## CONTENTS

LIST OF FIGURES ..... vii
LIST OF TABLES ..... x
1 INTRODUCTION ..... 1
1.1 Early History of the Woodworking Industry ..... 2
1.2 Planer - Moulder Evolution ..... 5
1.3 Surface Quality. ..... 10
1.4 Modern Planers and Moulders ..... 11
1.5 Research Objectives. ..... 12
2 REVIEW OF PREVIOUS WORK ..... 14
2.1 Introduction. ..... 15
2.2 Performance Assessment. ..... 16
2.3 Contact Methods of Surface Assessment. ..... 17
2.4 Non-contact Methods of Surface Assessment. ..... 19
2.5 Surface Analysis in the Woodworking Industry. ..... 32
2.6 Application of Available Laser Techniques ..... 36
3 PROPOSAL ..... 38
3.1 Objective. ..... 39
3.2 Proposed Instrument. ..... 41
3.4 Proposed Development of Instrument ..... 42
4 MATHEMATICAL MODEL OF THE PLANING PROCESS ..... 44
4.1 Introduction ..... 45
4.2 The Planing Process. ..... 46
4.3 Curtate Trochoid Mathematical Model. ..... 48
4.4 Loci Generation. ..... 57
4.5 Loci Sampling. ..... 58
4.6 Surface Profile Simulation. ..... 65
5 DEVELOPMENT OF POST-PROCESS LASER INSTRUMENT ..... 71
5.1 Introduction / General Description ..... 73
5.2 Electronic Hardware. ..... 76
5.3 Optical Hardware ..... 88
5.4 Instrument Framework ..... 94
5.5 Data Capture Software ..... 97
5.6 Data Analysis Software ..... 102
6 TIMBER MACHINING INVESTIGATION ..... 132
6.1 Introduction ..... 134
6.2 Planer - Moulder Machine ..... 134
6.3 Machining Variables and Parameters ..... 138
6.4 Machine Preparation and Condition ..... 139
6.5 Timber Specification ..... 141
6.6 Induced and Simulated Surface Finish Defects ..... 142
6.7 Surface Finish Analysis ..... 150
7 RESULTS ..... 160
7.1 Introduction ..... 161
7.2 Theoretical Results ..... 161
7.3 Machined Timber Sample Results ..... 162
8 DISCUSSION ..... 165
8.1 Introduction ..... 166
8.2 Hardware ..... 166
8.3 Software ..... 171
8.4 Machining Investigations ..... 176
8.5 General Comments ..... 199
9 CONCLUSIONS ..... 200
9.1 Objectives Realised ..... 201
9.2 Future Work ..... 202
REFERENCES ..... 204
FIGURES ..... 212
TABLES ..... 213
APPENDICES ..... 221

## LIST OF FIGURES

Figure 1.1: Early power-operated machinery was belt driven from lineshafts
Figure 1.2: Malcolm Muir's Planer, 1827
Figure 1.3: John McDowall's Planer, 1836
Figure 1.4: First Moulder with Integral Electric Motors, 1916
Figure 1.5: Elements of a Motorised Cutterhead with Spindle and Bearings
Figure 1.6: A Modern Moulding and Planing Machine

Figure 2.1: A Method of Assessing Surface Measuring Instrumentation
Figure 2.2: Multi-feature Measurement
Figure 2.3: Deutchke's Irregular Measurement System
Figure 2.4: Pneumatic Method
Figure 2.5: Capacitive Method
Figure 2.6: Schmaltz's First Method
Figure 2.7: Basic Principles of Optical Technique
Figure 2.8: Factors of various Optical Surface Assessment Methods
Figure 2.9: Glossmeter Principle
Figure 2.10: Mitsui's Instrument
Figure 2.11: Interference Method for examining Surface form
Figure 2.12: Optical Probe
Figure 2.13: Diffractometer
Figure 2.14: Foucault Knife-edge Method
Figure 2.15: Schematic of Heterodyne Method

Figure 3.1: Up-cutting Mode
Figure 3.2: Ideally Planed Surface
Figure 3.3: Proposed Method/Technique - In process
Figure 3.4: Proposed Method/Technique - Post process

Figure 4.1: Up-cutting Mode
Figure 4.2: Trochoid Family
Figure 4.3: Ideally Planed Surface Profile
Figure 4.4: Typical Surface Profile
Figure 4.5: Schematic of Cutterhead Action
Figure 4.6: Typical knife tip Loci from SSA - stage I
Figure 4.7: Typical knife tip Loci from SSA - stage I
Figure 4.8: Typical knife tip Loci from SSA - stage II

Figure 4.9: Typical knife tip Loci from SSA - stage III
Figure 4.10: Typical knife tip Loci from SSA

Figure 5.1.1: Schematic of the Post-Process System
Figure 5.2.1: Schematic of the BBC microcomputer
Figure 5.2.2: Schematic of the 6522 VIA
Figure 5.2.3: Read Handshake Timing Diagram for Port A Only
Figure 5.2.4: Write Handshake Timing Diagram
Figure 5.2.5: Schematic of Photodiode Array
Figure 5.2.6: Sensor Geometry and Idealised aperture Response Function
Figure 5.2.7: Photodiode Relative Spectral Response as Function of Wavelength
Figure 5.2.8: Photodiode Output Charges verses Exposure Characteristic
Figure 5.2.9: Power Supply Circuit Diagram
Figure 5.2.10:Timing Diagram for Photodiode Inputs and Outputs
Figure 5.2.11: Differential Amplifier used to extract "noise-free" signal
Figure 5.2.12: Sample and Hold Boxcar Video Signal
Figure 5.2.13: Timing Diagram - Data Capture

Figure 5.3.1: Beam Expander
Figure 5.3.2: Lens Maker's Formula: symbol definition
Figure 5.3.3: Beam Expander - The optical arrangement
Figure 5.3.4: Image Focusing - The optical arrangement
Figure 5.3.5: Graph of Focal Length against Image Distance
Figure 5.3.6: Lens Mount

Figure 5.4.1: Framework
Figure 5.4.2: Timber-Sample Clamping Device
Figure 5.4.3: Helium-neon Laser and "Floating" Carriage
Figure 5.4.4: Laser beam Incidence angle Adjustment
Figure 5.4.5: Image Alignment Mechanism
Figure 5.4.6: Dark-housing to exclude Ambient light

Figure 5.5.1: Determining Optimum Photodiode Integration Period

Figure 5.6.1: Time History of Sinusoid obtained with Oscilloscope
Figure 5.6.2: Time and Frequency Description of a Sine Wave
Figure 5.6.3: Summing Frequency Description of Sinusoids
Figure 5.6.4: Composing a Non-sinusoidal Waveform by Summing Sinusoids

Figure 5.6.5: Square Wave satisfies conditions for its Fourier Series to exist
Figure 5.6.6: Magnitude and Phase Spectra for Square Wave in figure 5.6.5a
Figure 5.6.7: Fourier Series and Fourier Integral
Figure 5.6.8: Relationship between Fourier Series and Fourier Integral
Figure 5.6.9: Comparison of diagram conventions: Series and Transform Spectrum
Figure 5.6.10: A Generalised Square Pulse and its Frequency-domain Magnitude and Phase
Figure 5.6.11: The Process of Rectangular Windowing
Figure 5.6.12: Zero-order Approximation
Figure 5.6.13: Result of the first step for an $\mathrm{N}=8$ point decimation-in-time FFT
Figure 5.6.14: Result of the second step for an $\mathrm{N}=8$ point decimation-in-time FFT
Figure 5.6.15: Final flow graph for an $\mathrm{N}=8$ point decimation-in-time FFT
Figure 5.6.16: The Butterfly structure in the various stages of a decimation-in-time FFT Figure 5.6.17: Modified Butterfly structure requiring only one complex multiplication Figure 5.6.18: Rearrangement of figure 5.6.15: input in natural order, output bit-reversed Figure 5.6.19-5.6.46 Validation of FFT Algorithm

## Figure 6.1: The B-series 220 Planer - Moulder Machine

Figure 6.2: Head unit Specifications of the Modular "200B"
Figure 6.3: Final Top Head
Figure 6.4: Spindle Unit Bearing Assembly
Figure 6.5: Hydrogrip Planing Cutterblock and Cutterheads
Figure 6.6: Heavy Duty In-feedworks and In-feed Table
Figure 6.7: Out-feedworks
Figure 6.8: Chipbreaker
Figure 6.9: Side Pressure Rollers
Figure 6.10: Standard Jointer fitted to Top and Bottom Cutterheads
Figure 6.11: Dust Extractor System
Figure 6.12: Socket Screw Positions used to Induce Cutterhead Imbalance
Figure 6.13: An NX-grinder used for producing Proud-knives
Figure 6.14: Timber Sample Analysis by Laser Instrument
Figure 6.15: Timber Sample Analysis by Talyrond 200
Figure 6.16: Results from Profile Simulation - Proud-knife
Figure 6.17: Result of Pulse-train Simulation - Proud-knife

Figure 7.G0.S1 - Figure 7.G0.S6: Results: Theoretical Only
Figure 7.G1.S1 - Figure 7.G1.S8: Results: Single-knife finishes
Figure 7.G2.S1 - Figure 7.G2.S12: Results: Head Imbalance
Figure 7.G3.S1 - Figure 7.G3.S15: Results: Proud Knife finishes

Figure 7.G4.S1 - Figure 7.G4.S6: Results: Vibrational effects
Figure 7.G5.S1 - Figure 7.G5.S5: Results: Fault Combinations
TABLE 1: Calibration Table for micrometer-controlled Angle of Incidence of Timber Illumination
TABLE 2: Example of Bit Reversal for 3 bits
TABLE G1: Single knife finish
TABLE G2: Unbalanced Cutterhead
TABLE G3: Proud Knife
TABLE G4: Timber Vibration
TABLE G5: Fault Combinations

## 1 INTRODUCTION

### 1.1 Early History

### 1.1.1 Saw-mills

### 1.1.2 The Steam Engine

1.1.3 Rotating Cutterhead
1.1.4 Planing Machines
1.1.5 Lineshafts
1.1.6 Tongue and Grooving Machine

### 1.2 Planer - Moulder Evolution

### 1.2.1 Early Moulder Developments

### 1.2.2 Design Improvements

1.2.4 Electric Motors
1.2.5 Refinements and Modifications
1.2.6 Ball Bearing Electric Moulder
1.2.7 Spindle Design
1.3 Surface Quality
1.3.1 Defective Finish
1.3.2 Current Surface Analysis
1.4 Modern Planer Moulders
1.5 Research Objectives

### 1.1 Early History of the Woodworking Industry

### 1.1.1 Saw-mills

Saw-mills powered by water wheels were in general use in mainland Europe as early as the 14th Century. They were introduced in England much later; the delay was due to the fears that their use might have inflicted damage to the sawyers' trade.

These early mills used reciprocating saws; the cutting and shaping of timber products by machine is a comparatively recent practice. The spindle shaping and moulding of timber first became a practical proposition about 200 years ago when rotating cutting tools became available, coupled with an "availableon demand" source of power.

### 1.1.2 The Steam Engine

When the condensed steam engine was invented by Watt in 1769 , for the first time there was a readily available source of power which could be installed in any appropriate location. The steam engine made possible, and paved the way for, the industrial revolution in which the large scale production of timber products featured.

### 1.1.3 Rotating Cutterhead

Initially, with the exception of hand tools used on lathes, there were no implements available which could be utilised in the machine cutting of wood. The major breakthrough occurred in 1777 when Samuel Miller invented the circular saw. When, over a decade later (in 1793), Samuel Bentham
developed the rotating cutterhead, the chief concern of the industry improved surface quality coupled with increased throughput - became a possibility.

With the steam engine as a power source, the implication of the circular saw and rotating cutters set the stage for, and launched the woodworking industry into, a new era - an era which saw the development of continuous cutting woodwork machinery, enabling the mass production of items, the shapes of which could be diversely varied.

### 1.1.4 Planing Machines

The roots of most of the woodworking machinery in use today can be traced back to those invented between 1777 and 1850 (Mansfield J.H, 1952). Nine years after Samuel Bentham filed his patent in 1793, saw a further landmark in the evolution of woodworking machinery, bound to produce superior and consistent quality surface finish; in 1802 Joseph Bramah patented and started building planing machines; they were about 40 feet long and the timber was clamped to a table which moved backwards and forwards past a horizontal, primitive cutterhead.

### 1.1.5 Lineshafts

Early power-operated machinery was belt driven from lineshafts (figure 1.1). These in turn were driven from a prime mover; this was initially water power but was superseded by the steam engine.

The lineshaft's speed would vary from about 90 to $150 \mathrm{rev} / \mathrm{min}$; some were made of wood, others of cast-iron; the driving pulleys were made of laminated wood. From the lineshaft there was a belt drive to the machine or to an intermediate countershaft.

### 1.1.6 Tongue and Grooving Machine

In 1827 Malcolm Muir invented a machine from which modern planers have been developed (figure 1.2); the timber was moved by an endless chain and passed through the machine. The timber first passed a rotating cutterhead carried on a vertical spindle which machined a datum face, and then over three bottom knife blocks containing fixed knives for planing the underside of the timber.

A tongue was then cut in the datum face by saws mounted on horizontal spindles (one above the board, the other below) each cutting to a depth of the tongue. The timber then passed through two horizontal saws on vertical spindles which cut through to the saw cuts made by the vertical saws; this produced a sawn out tongue.

On the opposite side to the datum face the board was cut to width by a saw; this widthing saw was followed by a grooving saw which cut the horizontal groove. The vertical spindles on each side of the machine (used for the tonguing and grooving operation) also carried revolving cutters which machined overlapping rebates on the top of the board; this determined the thickness of the board.

Although throughput on these machines increased, the surface finish of the products was inconsistent and generally of poor quality.

### 1.2 Planer - Moulder Evolution

### 1.2.1 Early Moulder Developments

John McDowall built machines to Malcolm Muir's designs but gradually introduced his own modifications. By 1836 when he filed his patent, his modifications had converted the original machine to the form of planers currently being manufactured (figure 1.3); feed rollers replaced the endless chain; rotary cutterheads replaced the tonguing and grooving saws. This brought the woodworking industry closer to the ideal - consistent, high quality surface finish combined with continuous, high speed production.

For many years, right into the 20th century, some woodworking machinery manufacturers produced machinery of wood framed construction. There was a theory abroad that wood was better than iron for this purpose because it more readily absorbed the vibration of fast running machinery which would otherwise be conveyed to the products surface finish; also, it was thought that it would be less easy to bruise the product if the machines were built of wood rather than metal.

As general technical knowledge increased, cast-iron frames were introduced followed by phosphor bronze bearings; the bearings ran in oil or grease; fat would sometimes be packed around the bearings so that if they did get hot, the fat would melt and, hopefully, prevent the bearings from seizing up.

Worn bearings would permit play between the bearing and the journal, with consequent deterioration, in the case of planing and moulding machines, in the quality of the product's surface finish.

### 1.2.2 Design Improvements

By the end of the 19th Century the progress in technology had made it possible to manufacture machinery much more accurately; the turn of the century saw many engineering developments taking place which greatly affected the quality of timber products and the rate at which they were manufactured. These included the appearance of precision ball bearings (Burnner H.E, 1929), higher spindle speeds and better tooling.

Circular cutterheads with thin knives replaced square cutterheads with thick knives; square cutterheads were limited to only four knives; circular blocks could accommodate higher rotating speeds, larger number of knives and consequently facilitate greater feed speeds for a given surface finish. The addition of feed rollers and pressure rollers permitted multiple feeding of narrow stock of slightly differing thicknesses.

### 1.2.4 Electric Motors

Electric motors were first used in woodwork machinery shops as a means of breaking down complicated transmissions powered from a single prime mover. Situations had developed where one shaft could be driving another, perhaps on another floor or in other buildings. Thus, the larger workshops were a maze of pulleys and overhead belting. Some of the smaller woodworking
plants presented a tidy appearance by hiding the lineshafts under the floor, but the maze of belts, though hidden, were still there and the machine positioning had to be related to the lineshaft and not to the convenience of work flow through the shop.

Woodworking machines, due to their comparatively high cutting speed requirement, readily lend themselves to being driven by a compact electric motor. Initially, the convenience of electric motors was used only to drive individual lineshafts; later, machines which had an integral electric motor were being designed and manufactured (figure 1.4).

### 1.2.5 Refinements and Modifications

The power transmission from a prime mover, via lineshaft and countershaft, to machine was extremely inefficient, with approximately half the power lost. This motivated the initial efforts towards individual drives (Mansfield J.H, 1952).

Many refinements followed the integral drive; the heads were provided with a brake to bring the spindle to rest rapidly; independent start and stop button controls replaced cumbersome belt striking gear and allowed only the required heads to be selected; direction of rotation could be selected, as required, at the push of a button; it was possible to provide motors with six different speeds, at the turn of a switch - this eliminated the use of multi-step gearboxes.

This type of machine was a great success; it only required one-third of the floor space of its belt driven counterpart, with its countershaft; it eliminated the problems of belting maintenance, which was considerable on the fast machines; there was no slowing down of spindles under load because the motor speed was relatively constant and the motors were designed to cope with a $100 \%$ overload. Thus, there was no tearing of the grain, as had been the experience with belt driven spindles which would slow down under sudden load, due to belt slippage. As a result product surface quality became more consistent.

### 1.2.6 Ball Bearing Electric Moulder.

The monumental breakthrough in woodworking technology happened when the ball bearing electric moulder was introduced, with a built-in motor mounted directly on each cutterhead arbour. The absence of belts made it possible to tilt all the heads to any desired angle and thus combine several cuts in one operation; previously this had been accomplished on a number of separate machines; there was also a $40 \%$ to $60 \%$ power saving.

Some of the early electric moulders were used in motor car body plant shops on components which were concealed, so that the knife mark spacing (a measure of the quality of the surface) was not very important. It was found that with the new electric moulders, the components could be fed up to four times as fast as the belt driven machines, with a more consistent depth, spacing and parallelism of the knife marks; also, there were fewer splinters and tears, despite the faster speeds. The reason for this was that the
spindles were mounted in close-fitting, anti-friction ball bearings, in contrast to spindles which float on a film of oil (as was the case with friction bearings); ball bearings restrict the spindle's end play; also, direct driven motorised spindles were rotated by balanced magnetic forces as opposed to being subject to the pulling and pounding of high speed belts.

### 1.2.7 Spindle Design.

As soon as the importance of spindle rotation was recognised as a contributory factor in surface finish, a great deal of attention was given to the design of the motorised spindle unit. Ball bearing tolerances were considered and it was found that the original allowances, specified for the first electric moulders, should be reduced by one-tenth (Burnner H.E, 1929).

It was found that the solution to spindle design was to use a large diameter spindle with a ball bearing at either end (figure 1.5); the cutter arbour projected beyond the main bearing at one end of the spindle and the rotor for the motor projected at the other. All of this was carried in a cylindrical frame (machined on the outside) with a flange mounting at one end to carry the motor's stator frame.

Thus, the whole motorised spindle unit could be mounted in a robust sleeve on the machine. The sleeve was designed to permit lateral movement of the motorised unit together with adjustment of cutterhead position; longitudinal movement of the whole unit, with its supporting sleeve, was also catered for. Thus the complete head was concentric and rigidly secured to a main frame,
which was also of rigid construction.

### 1.3 Surface Quality.

### 1.3.1 Defective Finish.

Although other improvements followed, such as the development of long-lived, high-speed steel tooling, the introduction of power feed units, hydraulic pressure pads, pivoting chip breakers, the application of electronics, microprocessors, etc, the superior design of a moulder, assessed in terms of the surface quality produced, still depends primarily on the degree to which the cutterhead can achieve perfect rotation. This end is pursued by improving the design of spindles, the means of applying power to them, and taking steps to eliminate vibration.

For high production rates, cutterblocks which carry a large number of knives are essential. During ideal cutting conditions, for a given rotational and feed speed, the surface finish required depends on the number of knives present on the cutterhead; increasing the number of knives will reduce the surface's knife-mark pitch and consequently improve its quality.

With multi-knife cutterblocks the probability that some will stand proud of, or below, the desired common cutting circle diameter is high; the repercussion, in multi-knife planing operations, is a defective surface finish. To alleviate this, "jointing" is employed. Jointing is analogous to the dressing of a grinding wheel in order to true eccentric running and expose new grits. In a similar way, the individual knives of the cutterhead are
dressed with a carborundum stick to remove eccentric tracking and produce a new cutting edge.

The surface finish of planed and spindle moulded products may also be affected by the degree to which the cutterhead is dynamically balanced. The locus of each knife on a cutterhead will be influenced by the fact that the block is unbalanced; this is significant because the height of the cusps produced by ideal cutting action is of the order of 10 to $25 \mu \mathrm{~m}$ while the eccentricity effected by just a few grammes, at rotational speeds of 15000 rev/min, is in the region of $30 \mu \mathrm{~m}$ to $50 \mu \mathrm{~m}$; this will obviously have a marked effect on the surface finish (Jackson M.R, 1986).

### 1.3.2 Current Surface Analysis.

The woodworking industry has not yet acquired a reliable method with which to quantify and categorise the surface quality of its planed and spindle moulded products. The current practice is that of visual and tactile inspection, which results in a wide variance in what is classed as an acceptable or defective surface finish; what one manufacturer may reject as an "unacceptable standard", another may accept as "good". These methods, by their very nature, are subjective and are restricted to post-process application.

### 1.4 Modern Planers and Moulders.

Modern woodworking machinery have benefitted extensively from the technological advances, developments and discoveries of the past (Timber

Trades Journal 1986a, 1990a, 1990b; Parkin R.M, 1988). The use of computers for the control of the production process is widespread (Bolzing D, Liu F, 1987; Thomlinson J, 1987; Cowdery M.J, 1990). Contrasted with those of the past, current spindle moulders and planers (figure 1.6) are highly sophisticated and complex machines, producing elaborate, extremely accurate and superior quality components (Timber Trades Journal, 1986; Cowdery M.J, 1990).

Ever increasing production rates are being demanded of modern machines; current maximum spindle speeds are of the order of $15000 \mathrm{rev} / \mathrm{min}$, resulting in cutting speeds in the region of 100 metres per second (Timber Trades Journal, 1986b). With feed speeds in excess of 150 metres per minute, the spindle moulding process is comparable to that of an extrusion machine, the moulder employing a number of rotary heads to produce the profile, as opposed to a single die head used in the extrusion of plastics and aluminium.

### 1.5 Research Objectives.

Despite the application of the knowledge and expertise accrued during the history of the woodworking industry, there are still inherent faults and defects within the planing/moulding process which manifest themselves with undesirable frequency (Jackson M.R, 1986). With "extrusion" rates in excess of 150 metres per minute, when a process fault develops (eg. bearing failure, excessive vibration, proud knife, etc.) a considerably large quantity of sub-standard (defective surface finish) timber is produced before the symptoms are detected by post-process, visual/tactile inspection.

Evidently, to ensure consistent quality and economy, it is necessary to develop sensors capable of real-time, in-process monitoring the surface quality of the product (Goddard M, 1985). Thus, when process faults occur they are detected instantaneously, and any necessary remedial action effected immediately. Also, a practical and more precise method of specifying the surface finish of machined wood is required to ensure consistent quality of production (Jackson M.R, 1986; Goddard M, 1985).

This thesis is an account of investigations undertaken in the field of surface assessment of spindle moulded and planed products. The research sought to develop a low-cost, adequate sensor/transducer and appropriate analytical techniques for quantifying the surface finish produced by moulders/planers within the woodworking industry.

## 2 REVIEW OF PREVIOUS WORK

### 2.1 Introduction

2.2 Performance Assessment

### 2.3 Contact Methods of Surface Assessment

2.3.1 Stylus Technique
2.4 Non-contact Methods of Surface Assessment
2.4.1 Pneumatic Technique
2.4.2 Capacitance Technique
2.4.3 Ultrasonic Technique
2.4.4 Optoelectronic Techniques

### 2.4.4.1 Gloss Meters

2.4.4.2 Interferometers
2.4.4.3 Optical Probes
2.5 Surface Analysis in the Woodworking Industry
2.5.1 Visual-Tactile Methods
2.5.2 Stylus Instruments
2.5.3 Optical Techniques
2.6 Application of Available Laser Techniques

### 2.1 Introduction.

Only in the past 50 years has the importance of surface shape and texture received recognition (Harris P.G, Trigg A.D. 1987). Between 1940 and 1960 considerable research was carried out on tribology; in particular, work in contact phenomenon such as friction and wear was dominant (Hingle H. 1986). Much of the basic correlation relating such functions to the surface geometry was not discovered because of the inherent difficulty in measurement.

Another drawback was the limitation of the available instruments; only rudimentary surface parameters such as Roughness average ( $\mathrm{R}_{\mathrm{a}}$ ) and, to a limited extent, peak features could be measured. It was only with the advent of digital methods that the breakthrough occurred.

There has been slow progress in the field of instrumentation required to measure surfaces effectively. This restriction was due to a number of problems: There was not a true understanding of surfaces and their functions; the limitation in data processing power; the limitations of the instruments themselves. In recent years these three areas have been brought together by the use of random process analysis, digital methods and contacting and non-contacting methods. This chapter reviews current trends in these areas and highlights their advantages, disadvantages and present applications.

### 2.2 Performance Assessment.

One of the ways in which the performance of surface measuring instruments can be assessed is shown on figure 2.1. There are two axes; the horizontal one is the range of the instrument divided by its resolution and the vertical one is its frequency response.

As can be seen from figure 2.1, a conventional instrument has a range to resolution of about one in one thousand and a frequency response of several hundred Hertz (Whitehouse D.J, 1972). This working point is more or less fixed, at present, for a good instrument design. Future instrument designs will tend to, and attempt to, move this working point.

The implication for the axes of figure 2.1 in terms of instrumentation in engineering metrology is as follows:

The horizontal axis is, in effect, an integrated measurement axis; the further the working point moves to the right the greater the possibility of integrating many features of the geometry together in one measurement.

The vertical axis is a measure of the instrument's potential for in-process application, implicating assessment while the workpiece is being manufactured.

### 2.3 Contact Methods of Surface Assessment.

### 2.3.1 Stylus Technique.

Great advances have been made in integrated measurement using the stylus method, ie. the moving of the working point to the right of figure 2.1. For instance, by having an instrument with a large dynamic range and high resolution (such as a range to resolution ratio of one million) it is now possible to assess the track of a ball race measuring not only the radius and surface finish and centres separately but to measure its total geometry simultaneously (figure 2.2). Previously this could only be achieved with the use of three separate instruments (Phillips M.J, Whitehouse D.J. 1977; Stevens D.M.G, 1989).

Thus, by attaching a digital computer to a wide-range transducer system it is possible to achieve an integrated measurement. This does not imply that just linking a computer to the instrument achieves anything; it has to be supported by appropriate mathematics.

The use of sophisticated mathematics is also a recent trend in the field of mechanical instrumentation. It is now possible to utilise some of the mathematics which, although established for many years, have been impossible to implement due to lack of computing power. One crucial element necessary to effect the calculations is a fast computer; their availability has enabled dramatic improvements in the stylus method when observed on the merit graph of figure 2.1.

As well as good mathematics and fast computers, it is also vital that excellent
sensors and transducers are employed. To this end one of the recent achievements has been the marriage of optical methods with mechanical methods which has produced stylus sensors having large dynamic ranges (Drews W.E, 1987). Typically, it is now possible to use an interferometer as part of the transducer (Stevens D.M.G, 1989; Sherrington I, Smith E.H, 1988). Of necessity, the interferometer has to be very small; with modern polishing techniques it is possible to manufacture miniature prisms and lenses. This implies that the components are of the order of millimetres as opposed to centimetres in size. So, having measured the workpiece totally it is possible to isolate certain features of interest, amplify them using the computer, and examine them in more detail (Babus, Probert, O'Callaghan and Evans, 1988).

The other direction in which stylus instruments can improve is in that of in-process measurement. Progress in this department has not been as dramatic as in integrated measurement. The main reason for this is that stylus instruments are sluggish in their response; they have an upper bandwidth of about 450 Hz (Whitehouse D.J, Bowen D.K, Chetwynd et al, 1987) and are of delicate construction making them unsuitable for the often hostile environment of production processes (Jackson M.R, 1986).

Some advances have been made, however, in developing more portable instruments. This entails making them small, capable of being hand-held and being easily transported to the locale of use. Small instruments are particularly useful for measurement on large components which cannot be
moved. For example, a shaft in a ship engine.

Today, typical instruments for measuring surfaces or measuring roundness in situ can be small enough to be carried in the pocket (Quality Today, 1986). These instruments are, clearly, not as sophisticated as those in inspection rooms but can be very effective from the point of view of quality control.

Despite the distinct stagnation in the progress towards the in-process use of stylus instruments, attempts are still being made to measure and assess surfaces while they are actually being produced. One such method, of German origin (Deutchke S.J et al, 1973), comprises of a drum which is pushed onto the workpiece (figure 2.3). Out of the drum protrudes a single probe with a transducer on the end. As the workpiece rotates and the drum is driven, the probe is forced to make contact with the workpiece once every one revolution of the drum. The amount by which the probe penetrates the circumscribed circle about the workpiece is recorded so that over many revolutions a picture of the surface distribution is accrued. Although this method has problems because of the influence of debris and coolants it is a step in the correct direction along the road to in-process gauging using stylus instruments.

### 2.4 Non-contact Methods of Surface Assessment.

A very good criterion for a sensor-transducer system is to maximise the change of energy per unit displacement; this enables a good signal-to-noise ratio to be achieved. With this criterion, the following non-contact methods
of assessing surfaces will be considered:

Pneumatic Technique, Capacitive Technique, Ultrasonic Technique.

### 2.4.1 Pneumatic Technique.

In this method air is blown onto the object surface via a measuring head and skirt. The air which escapes between the skirt and surface can be related to the surface finish (see figure 2.4a); in practice the leakage is proportional to the surface finish and the average distance between the skirt lip and the surface.

There are two ways in which pneumatics can be employed; one is to measure the air flow directly - monitor the flow to see how it changes with the surface finish (figure 2.4b). The second is to consider the effect of the surface finish on the back pressure in the air supply (figure 2.4c).

The use of pneumatic techniques for surface evaluation has disadvantages: The range to resolution of these devices is relatively low - about 100:1-and therefore does not compare well with stylus methods. Their main advantage is that they do not contact the workpiece and are comparatively cheap. However, other problems are evident; for example the skirt geometry must approximately follow the average form of the workpiece, otherwise too much air escapes (due to mismatch of shape). Another problem is that unless the
air used is clean and dry, water can form when the air escapes from beneath the skirt of the instrument. For these reasons pneumatics are not generally considered to be viable as a method for assessing timber surface quality.

### 2.4.2 Capacitive Technique.

Another method is the use of capacitance; here an electrode is positioned above the surface to be analyzed in the presence of a dielectric between the two (figure 2.5). The capacitance between them can be used to assess the texture (Crookall J.R, Sherwood K.F, 1968). The relationship between capacitance and surface is not very straightforward - in fact, it is an inverse law in which there is an extra term, the average distance (d) of the electrode from the surface, is added to the denominator:

$$
\begin{equation*}
\text { capacitance }=\iint(d+f(x, y))^{-1} d x d y \tag{2.1}
\end{equation*}
$$

The capacitive method is very sensitive and can therefore be used quite effectively in various applications. There are problems however. The signal from the transducer is susceptible to extraneous electrical noise and therefore if very small or sensitive signals are being measured, effective shielding must be employed. Another problem is that the shape of the electrode must nominally follow the shape of the surface being assessed. Further to this, changes in moisture content or in ambient conditions of the material being assessed has a marked effect on the results obtained.

The capacitance technique does have advantages: it is non-contacting, very sensitive and it measures over an area; stylus methods, clearly, do not.

Nevertheless, for general purpose use in surface metrology it is not regarded as a preferred method.

### 2.4.3 Ultrasonic Technique.

In this method ultrasonic waves are projected onto the surface and the reflected, scattered waves are detected. From the captured signal the surface finish is assessed. One advantage of the method is that it is relatively easy and straightforward to obtain the phase as well as amplitude of the reflected signal; this is of benefit as it provides two sources of information from which to assess the surface.

In principle the method shows much promise, in practice problems arise. Ultrasonics are very difficult to propagate through air; the rate of attenuation is considerable. It is also very difficult to manufacture miniature ultrasonic sources and directionality of the received signal is hard to achieve. Research work is continuing in this field but to date no practical instrument has been realised (Smith P.F, Player M.A, Collie D.L.A, 1988).

### 2.4.4 Opto-electronic Techniques.

The "non-contact", "rapid-response" nature of light, coupled with recent advances in laser and opto-electronic technology, has brought about interesting and new possibilities for in-process assessment of product quality.

The very first optical method for assessing surface finish was that adopted by Schmaltz in 1927 (Schmaltz G, 1936); he projected a light source onto the
surface (from one angle) via a sharp edge (eg. a razor blade) and observed the interface between the illuminated and shadowed surface (from another angle), figure 2.6. This, in effect, produced a pseudo-profile which is indicative of the surface finish; the method is not quantitative.

The basic principles of most optical techniques are illustrated in figure 2.7; a ray of light (at angle of incidence $\theta$ ) impinges upon, and rebounds off, the object surface. The degree to which the surface affects the reflected light can be used as a measure of the surface finish or texture. There are four main parameters or variables in this configuration:

1) The angle of incidence of the illuminating light beam.
2) The spot size illuminated by the light on the surface.
3) The scattering angle of the light reflected from the surface.
4) The type of light source.

Figure 2.8 represents the different possibilities of assessing surfaces using optics; the abscissa, in essence, represents the spot size; the ordinate denotes three functions:

1) Cost
2) Fidelity (the degree to which the reading is compatible with a reading of the same surface made with a stylus instrument).
3) Speed of Response.

At the extreme left ("the origin") of figure 2.8 is the stylus instrument which, by virtue of the above definition, has a fidelity of one. Then comes the optical probe, which is in effect a mimic of the stylus probe; because of factors such as polarization and variation in intensity of light, the highest fidelity
obtainable is about 0.9 (Arecchi F.T, Bertani D, Ciliberto S, 1979).

Further to the right of figure 2.8 is the laser scanner, diffraction (or interference methods) and gloss meter; moving to the right increases the area of illumination. It can be seen that the methods on the left-hand side of figure 2.8 are useful in the field of technology, giving absolute readings which are traceable to standards; this truth diminishes as instruments towards the right of the figure are considered. These instruments tend to be cheaper, less accurate and, consequently, they are mostly used as comparators rather than absolute measuring systems. They have, however, a much faster dynamic response and therefore more likely to be effective for in-process measurement.

### 2.4.4.1 Gloss Meter.

On the extreme right of figure 2.8 is the simple glossmeter; the principle of which is shown in figure 2.9. A light is shone onto the surface and is scattered from it. Two photo-detectors, A and B, detect the intensity of the light falling on them; detector $A$ is positioned at the angle of specular reflection; this corresponds to the same angle from the normal as the incident light; detector B is positioned to detect diffused reflection.

By considering the way in which the surface scatters the light (ie the amount of reflected light that reaches the two detectors) the surface finish can be estimated. For example, from the very smooth surface of figure 2.9(a) most of the light is specularly reflected (as in a mirror) so the majority of the light will arrive at detector $A$ and very little at detector $B$. So the calculation of
will result in a value nearly equal to unity.

According to this rough scale, an optical finish would produce a surface having a value of 1 . This quality of surface is only detectable if the surface roughness is about one-eighth of the wavelength of the illuminating light (Whitehouse D.J, 1985). As the surface gets rougher (say $\lambda / 2$ ) more light gets scattered into $B$ than in the case of the mirror finish and the ratio of the detectors give the value 0.5 rather than 1 (figure $2.9(b)$ ). For very rough surfaces, where the surface finish is much bigger than the wavelength of the illuminating light, there is an equal probability of scattered light impinging detector $B$ as hitting $A$. The result of the calculation in equation 2.2 will be a value of zero (figure 2.9(c)). Thus, it is possible to classify surfaces according to their roughness by illuminating them with light; a good surface results in a value of one, a bad surface produces a zero.

For a specified process it is possible to obtain good correlation between the $R_{a}$ measured using a stylus instrument and the numerical value of the quotient, (A-B)/(A+B) (Whitehouse D.J, 1985); this is not necessarily linear but the curve would be constant for a particular process, albeit a different curve for every process. Thus, this merit value is not directly related to $\mathrm{R}_{\mathrm{a}}$; it can only be used as a comparator within a process and not for comparisons between processes.

A typical example of an in-process, surface assessment system being developed by Mitsui is shown in figure 2.10 (Mitsui $\mathrm{K}, 1986$ ). Mitsui uses a $\mathrm{He}-\mathrm{Ne}$ laser, of 1 mW output, as a light source. The laser beam is directed onto the object surface through a series of mirrors and an objective ( $\mathrm{NA}=0.1$, X5). For the detection of the reflected light position, a PIN photodiode array, which can measure centre position of the light spot directly as a voltage, is used. It is necessary to scan the array quickly enough to detect movement.

While Mitsui reports a measuring range of $-30 \mu \mathrm{~m}$ to $20 \mu \mathrm{~m}$ with his measuring system, like other researchers in this field (Hattori M, 1981; Inasaki I, 1982), mention is made of the effect of surface vibration on the measurement/assessment technique.

Object surface vibration would have a marked effect, introducing spurious data and causing inaccurate results.

### 2.4.4.2 Interferometers.

More sophisticated methods employ coherent light to illuminate the surface and compare the reflected light with that from a reference (eg. a glass flat or an interferometer reference mirror). The reference flat can be positioned as in a Twyman Green interferometer (or a multiple beam interferometer) by laying it on the surface. Fringe contours can be observed which give a mapping of the surface (figure 2.11). Each contour line represents a line of constant height. Careful observation of the contours can give a real insight into the general shape of the surface and by use of suitable optical processing
it can be used to make a quantitative assessment of the surface finish.

The major disadvantage with the method is that it demands a considerable amount of operator skill to unravel the fringe pattern. This has been the biggest problem using interferometers and is why they have not been used more widely. However, there have been attempts to make the use of these interferometers more accessible.

One such development makes use of the mireau interferometer principle (Wyant J.C, 1985). This interferometer technique uses a photodiode or a television camera to view the interference fringe; the fringe pattern is stored. The viewing reference optics are then moved axially using a piezoelectric transducer; this moves the reference by one-third of the light's wavelength; the camera then takes another picture of the fringes, which is stored in the computer (figure 2.12). This is repeated a third time. The basic idea being that a number of movements are made in the z-direction covering one wavelength of the light.

The stored computer images of the fringes can be used to give the actual height at any position in the plane, resulting in either a profile or an area. The area method tends to have a relatively low resolution. Both can give ambiguous results if sharp edges are present on the surface; this is due to diffraction.

The method does, however, require a reasonable flat surface and there is the problem that when the objective is moved in the vertical direction it cannot be allowed to twist, otherwise the mechanical relationship between positions is lost, which results in a considerable depreciation in fidelity between the different pictures.

Another development which fits into the same family as interference methods is that of diffraction techniques. In one embodiment (Whitehouse D.J, 1972) a collimated beam of laser light is projected onto the surface (figure 2.13). This is scattered by the surface, collected optically and directed onto a photodiode array. The diode array is addressed by a computer so interrogation can take place.

The key to the technique is that the optics in the instrument have to be arranged such that light reflected from the surface at any one angle is imaged onto the detector at one spot. This is achieved by placing the detector in the back focal plane of the objective lens. This particular configuration has considerable benefit in metrology providing certain surface-finish conditions are met; the intensity pattern on the detector can be regarded as the power spectral density of the surface geometry provided the surface finish is relatively small compared with the wavelength of light; one-eighth of the light's wavelength is considered to be small.

One advantage of the technique is that small details on the surface tend to be scattered over very wide angles which produces a large displacement
signal on the detector. Therefore, large displacements on the detector corresponds to small distances on the surface; this is unusual in the sense that small details are normally more difficult to measure than large ones.

From the power spectrum it is possible to evaluate the surface roughness $R_{a}$ value and the average or RMS slope of the surface and the RMS curvature (Rakels J.H, 1986)

There are practical problems with the technique. Because the angle of reflection rather than its position in the workpiece is being imaged the method is not sensitive to particular spots and blemishes. In fact, it measures the average surface properties and does not image directly in the same way as conventional optics, so movement of the workpiece can be tolerated; the workpiece can move in the X and Y directions and there is no effect on the detector. However, yaw of the specimen can pose a problem because the light scattered from the workpiece can miss the detector optics. Again, because an area is being assessed via scattered angles rather than an image system, any debris which emerges from the workpiece as it is being machined will have very little effect on the detector signal. This is because if one chip flies between the instrument and the component it will tend to restrict light coming from the surface at all angles by an equal amount. The result is that the total light falling on the detector drops very slightly but it drops over the whole detector and not just in one spot; all frequencies are attenuated equally. This is not important from the point of view of measuring surfaces, as it is the relative amplitudes of the spectrum which are
important not the absolute values.

The frequency response of the instrument is limited by the time taken to process the detected signal. The size of the device need not be large and bulky.

### 2.4.4.3 Optical Probes.

Optical probes are also an interesting area for consideration; in this technique an instrument has been devised in which the stylus tip is replaced by an optical spot.

The majority of instruments of this type have been achieved with a "follower" device in which, although the surface is not contacted, the sensor follows the surface at constant separation.

One method is based upon the Foucault knife-edge test (Dupuy M.O, 1967). In this method a laser is imaged onto the surface. This light is re-imaged from the surface onto a partial obstruction in the image plane (figure 2.14). Conventionally this obstruction is a knife edge but can be one from an assortment of masks.

When focused on the surface, the spot will be imaged onto the knife edge. This will produce a particular shadow pattern on the detectors which are placed behind the knife edge. If the surface has a deep valley and the spot drops into it then its image is formed in front of the knife edge. This
produces a different shadow pattern on the detectors. This difference in shadow pattern, from in focus to out of focus, operates a control system which moves the objective lens down to recreate the focus (vice versa for a peak). This is achieved using a piezoelectric device. By monitoring the movement of the objective lens and optical system it is possible to get a measure of the surface finish as a profile.

One of the most successful ways of devising an optical probe is the heterodyne methods which use common path interference in which two types of illumination come to bear on the surface simultaneously (figure 2.15). Invariably the light is split into two different wavelengths or different polarization (Sommargren G.E, 1981). The two rays of light, having different wavelengths or polarisation, focus in different places, either transversely or axially.

It is therefore possible to follow the surface geometry by examining how the surface affects the two focused spots. Using this principle (common path interference) some of the very finest surface finish measuring instruments have been made, measuring to tenths of a nanometre. They tend to be relatively slow, however, as adjustments within the instrument have to be made; also movement of the optical elements does limit the frequency response (typically less than 100 Hz ) and hence the speed at which the surface can be followed. The use of different wavelengths and different polarization can cause problems as surfaces can react differently to electromagnetic waves.

In practice there is no guarantee that the same result obtained from a mechanical stylus would be repeated by an optical stylus because of the nature of each interaction with the surface is different. Both have inherent problems; with the mechanical method the surface has to be relatively hard, with the optical method the surface has to be reflective.

### 2.5 Surface Analysis in the Woodworking Industry.

The machining of wood, as compared to that of metals, has attracted very little research since the late nineteen fifties. The little research which has been done in this area is disjointed, un-coordinated and non-sequiturial in its history.

Woodwork machinery researchers have looked at the areas of cutting forces (Kivimaa E, 1950), chip formation (Koch P, 1964), surface wave theory and vibration (Petter C, 1954; Goodchild R, 1963; Mori M, Hoshi T, 1964) and factors which affect the surface quality of rotary planed timber components (Davis E.M, Nelson H, 1954).

Currently popular methods of surface analysis have their origins within the metalworking industry. Surface roughness measurements are normally made using stylus instruments having relatively short traverse lengths. Established analysis techniques offer a means of characterising profiles; broadly speaking the various methods may be divided into categories which define the amplitude, or the wavelength, variation, although some methods are found to deal with both regimes simultaneously (Peklenik J, 1968).

### 2.5.1 Visual/Tactile Methods.

Visual/tactile methods have been used since the early days of woodworking (Brown H.P, Panshin A.J, Forsaith C.C, 1952; Koch P, 1955)). Today it is still the most popular technique used, by customers and manufacturers alike, for assessing the quality of planed timber (Jackson M.R, 1986; Goddard M, 1985; Maycock K.M, et al, 1987). Because of its subjective nature, the method has many shortcomings. There is no quantitative assessment of the degree of waviness defects and, as such, no standards can be formulated. This results in a wide variance in the classification of surface finishes throughout the industry. The problem is compounded by the fact that there are no definite standards for the waviness quality of planed timber. Considerable conflict is thus caused between manufacturers and customers when each use their own, different, subjective assessment "standards" (Deal R.C, 1951).

Research into visual/tactile methods (Stumbo D.A, 1963; Knudsen V.O, 1928; Brown I.D, 1960; Schmaltz G, 1936) has shown that roughness values of the order of $0.5 \mu \mathrm{~m}$ can be sensed by a combination of touch and sight. They also concluded that the eye is capable of sensing changes of angle of reflection of the order of 1.5 degrees on semi-transparent materials such as wood.

### 2.5.2 Stylus Instruments

Some researchers (Jackson M.R, 1986; Elmsorf A, Vaughan T.W, 1958; Stumbo D.A, 1960 and 1963), have used instruments from the metalworking industry to investigate the roughness of wood surfaces. Elmendorf and Vaughan (1958) found that the size of the stylus is critical when comparing
a Talysurf (diamond pyramid stylus, 0.002 mm wide at the tip), with a Forster Instrument (stylus tip radius 0.055 mm ). The Forster instrument provides a more consistent profile of the surface since the trace rarely goes over range, under the tested conditions. The Talysurf, however, with its smaller stylus, is more prone to go over range, making the interpretation of results an arduous task.

Han (1957) and Goodchild (1963) investigated the development of two different stylus instruments. Using a larger stylus radius (3mm) Han (1957) was able to filter out the effects of primary texture (grain structure) in obtaining traces of particle board waviness. Goodchild (1963), using a similar instrument design technique (with a 0.05 mm radius stylus), investigated the surface waves of rotary planed Beech (a very fine textured wood). A good degree of filtration was achieved using the 0.05 mm stylus.

Stumbo (1960) and Peters and Cummings (1970), looked at the performance of True Datum devices (the alternative of the surface datum using skid follower systems) which remove the effects of workpiece bow or twist. Jackson(1986) used similar stylus instruments as research tools.

The surface parameters determined by stylus instruments such as Centre Line Average ( $\mathrm{R}_{\mathrm{a}}$ ) or Root Mean Square ( $\mathrm{R}_{\mathrm{q}}$ ) parameters are very limited for describing surface profiles, and is often misleading; profiles clearly different in form can have the same numerical value of $R_{a}$ or $R_{q}$ (Greenwood J.A, 1968).

Stylus instruments are undoubtedly of interest as a research tool; their inprocess use in wood machining, with its high levels of vibration, is precluded by their small bandwidth and delicate construction. Even if stylus instruments were made more robust (Jackson M.R, 1986), their response $(400 \mathrm{~Hz}$ bandwidth) would be inadequate to track the traversing surface profiles; a stylus instrument having a bandwidth of 2.3 kHz is required to accurately track a 1 mm pitch profile (see Section 4.6.4) traversing at 140 $\mathrm{m} / \mathrm{min}$.

Extending the bandwidth of stylus instruments includes increasing the static stylus forces. This is likely to result in timber damage due to stylus "ploughing" (Han R.A, 1957).

### 2.5.3 Optical Techniques

Researchers Elmendorf and Vaughan(1958), Stumbo(1960) and Peters and Cummings(1970) have investigated the use of optical light sectioning as a technique for surface quality assessment. The method is quantitative in that measurements are taken using a microscope to assess the overall peak-to-valley height. The technique, which uses light incident at $35^{\circ}$, is very time consuming, hence it has not been generally adopted by the woodworking industry, although furniture related industries have used this technique.

A variation on the optical light sectioning technique uses oblique lighting to illuminate the object surface. This provides visual enhancement of the appearance of the forms of defect, but not a quantitative assessment of
surface waviness. Oblique illumination is sometimes used to improve the ability of the eye to ascertain variation of surface waviness (Brown I.D, 1960), but is of limited use for in-process surface assessment.

### 2.6 Application of Available Laser Techniques

In recent years, laser techniques have been, and are being, developed to measure surface profile and roughness (Broadmann R, 1986; Hitoshi F, Toshimitsu A, 1977; Pryor T.R, Hageniers O.L, North W.P.T, 1972; Pernick B.J, 1979; Dobosz M, 1984; Harris P.G, Trigg A.D, 1987). The vast majority of the techniques monitor the reflection of a laser beam focused on the surface to be assessed. The angle of incidence of the beam is of the order of 45 degrees; photo-detectors record the variation of the reflected angle as the object surface is traversed.

Most of the laser surface assessment techniques are being investigated within the context of metal machining where the workpiece is rigidly fixed to the same datum (the machine table) as the measuring device, hence, minimising relative vibration. With wood-machining, however, the workpiece is not clamped to the machine table, but is traversed across it, using pressure rollers as guides, thus a comparatively high level of vibration prevails.

For these reasons, major difficulties are envisaged in adopting any of the laser techniques described above for the in-process assessment of the surface quality of machined timber. What is required is fast-response, non-contact, vibration-resistant method of surface quality assessment, including
parameter(s) which can readily indicate and identify machining defects.

## 3 PROPOSAL

3.1 Objective
3.2 Proposed Parameter
3.3 Proposed Instrument
3.4 Proposed Development of Instrument

### 3.1 Objective.

The anisotropic nature of wood, considered with respect to its rotary planing, causes inherent difficulties in assessing the quality of surfaces produced. One of the principle factors when planing wood is that the rotating knives do not constantly move in the direction of the timber fibres (or grain). Cutting conditions become even more complex with timber which exhibit natural defects such as wavy, curly, or diagonal grain (Petter C, 1954); these increase the difficulty in producing a good surface finish (Thomlinson R, Harrington J.S, 1960).

The objective of this project was to investigate the possibility of designing and manufacturing a non-contact transducer and associated signal conditioning, that would assess the surface form of machined timber, with considerations for in-process utilisation and adaptive control. Closely associated with the development of the transducer was the investigation of appropriate parameter/s that would readily indicate the quality of a machined timber surface profile. Coupled to the investigation was the need to mathematically model the timber planing process so that machine performance could be predicted/simulated, given specific machining faults. The simulated surface profiles could then be used as templates for comparison with actual surfaces.

### 3.2 Proposed Parameter.

The timber industry uses the up-cutting mode for machining its products (figure 3.1). Due to the kinematics of the planing process, the geometry of the machined surface consists of a series of cusps; their distribution and linear
spacing (periodicity) being dependent largely on the linear feed speed of the timber, the number of knives used on the final cutter head, the rotational speed of the cutterhead, etc. Figure 3.2 shows the ideal surface profile of timber planed under ideal conditions (ie. no knives proud, zero vibration, dynamically balanced cutterhead, concentric spindle, etc).

Because the cutting circle radius used on planing machines is relatively large (typically 150 mm ), the depth, $\mathbf{h}$, of the cusps, produced on the surface (figure 3.2), is of the order of a few microns (typically $10 \mu \mathrm{~m}$ ). These are very small amplitude variations and, as such, are not readily detectable by the naked eye. Amplitude variation, then, does not account for any "defects" as perceived by the human eye. However, the eye is extremely sensitive to changes in slope (Gonzalez R.C, Wintz P, 1977) ie. boundaries or lines on the surface. Hence, the eye detects the change from positive to negative slope at the apex of each cusp.

It is the consistency with which the apexes repeat that affect the aesthetic qualities of the machined surface; ie. any variation in the surface wavelength, or long periodic "beats" superposed thereon, are detectable by the eye and, as such, render the surface quality defective (Brown I.D. 1960; Elmdorf A, Vaughan T.W, 1958).

Therefore, it would seem reasonable to analyze the surface form in terms of the frequency information inherent on any machined (planed) timber surface.

### 3.2 Proposed Instrument.

The proposed technique would use laser light to highlight the apexes at the intersection of the surface "arcs" (figure 3.3). A broad beam of laser light would be directed at grazing incidence ( $\theta<1.5$ degrees) to the surface being machined, and in the same plane as the traversing workpiece. This would have the effect of highlighting the leading slopes of each cusp in the beams path and produce a pattern of bright and dark regions on the surface of the workpiece (figure 3.3). This pattern, which contains the periodic information of interest, would be traversed past a single photodiode as the workpiece is fed through the rotating cutterhead.

The output voltage of the photodiode is proportional to the intensity of the light incident upon it. This voltage would be sampled (utilising a rotary position encoder to precisely define the sampling points), digitised (using an Analogue to Digital Convertor) and stored in memory for subsequent analysis.

The data captured would not be prone to distortion due to vibration for two reasons:

1. The aperture of the beam is wide compared to the amplitude of timber vibration so the timber will at all times be illuminated.
2. The plane of vibration would be almost perpendicular to the illuminating, incident beam; the surface finish to be assessed is bigger than the wavelength of the laser, so, the reflected light to be monitored would be diffuse (as opposed to specular (see figure 2.9 and Section 2.4.4.1). Hence, any variation in workpiece position due to vibration will be insignificant.

With appropriate sampling frequency, the data captured over a given length of timber could be analyzed, in terms of its frequency content, using Fourier Analysis Techniques.

Fourier Analysis of the data involves transforming the data from the "time" domain to the frequency domain using a fast Fourier Transform (FFT) algorithm. A "fault finding algorithm" would then have to be developed to analyse the frequency domain data to detect any machining defects which may have been induced on the timber surface.

### 3.4 Proposed Development of Instrument

The initial investigations into the technique outlined above were to be undertaken in a microprocessor/instrumentation laboratory where there was no access to woodworking machinery. The high cost of operating such machinery also meant that the collaborating machinery manufacturers (Wadkin plc, Leicester) could not produce any significant amounts of machined timber.

The philosophy adopted, therefore, was to develop the instrument/surfaceanalysis technique on stationary, pre-machined timber samples (figure 3.4). This was to be accomplished by employing a linear array of photodiodes (instead of a single diode). "Traversing" was to be achieved by scanning the diode array, instead of traversing the timber.

Optical lenses were to be used to focus the image of a given illuminated length of timber on to the photodiode array. Scanning of the array would provide data which would then be captured for subsequent analysis.

The device thus investigated would be a post-process instrument, but, established using the principles of in-process measurement. This combination of grazing incidence laser illumination and the photodiode technique is innovative and was the subject of a Patent search and provisional application. This was not pursued due to lack of funds.

## 4 MATHEMATICAL MODEL OF THE PLANING PROCESS

4.1 Introduction
4.2 The Planing Process.
4.3 Curtate Trochoid Mathematical Model
4.3.1 Ideal Cutterhead Rotation
4.3.2 Cutterhead Eccentricity
4.3.3 Cutterhead Vibration
4.3.4 Knife Locus
4.3.4.1 Displacement Component in y-direction.
4.3.4.2 Displacement Component in x-direction.
4.4 Loci Generation
4.5 Loci Sampling
4.6 Surface Simulation Algorithm Development
4.6.1 Development Stage I
4.6.2 Development Stage II
4.6.3 Development Stage III
4.6.4 Development Stage IV

### 4.1 Introduction

Before describing the development of the proposed instrument and method of surface analysis of planed timber, as outlined in chapter 3, a study of the geometry of, and the mechanics associated with, the production process will be presented in order to generate a mathematical model which can be used to represent the geometry of a spindle machined surface. This mathematical model can then form the nucleus of a profile simulation algorithm; the simulation software can then be used to test the hypothesis of, and substantiate the philosophy behind, the proposed surface assessment method. It can also be used to predict surface profiles and hence FFT (or frequency signature) templates for machine performance determination or surface profile comparisons.

In this chapter is developed a versatile, cartesian-rigorous, mathematical model for surfaces produced by the wood planing process. This is presented in terms of the actual path taken by each knife as it cuts the workpiece. The mathematical model forms the foundation of a computer algorithm which simulate the resultant surface finish produced in the vast majority of wood planing situations.

Other investigators (Kivimaa E. 1950; Goodchild R. 1963; and Jackson M.R. 1986) have produced rather limited mathematical models of spindle planed surfaces without using the true locus of the cutting knives. For the sake of simplicity they have resorted to approximating the cutting motion by employing the circular arcs of adjacent circles on a common horizontal axis.

By comparison, the novel mathematical model developed here, although containing a deeper and greater input from the world of pure mathematics, more accurately represents the actual knife locus and hence the surface finish produced by the machining process.

### 4.2 The Planing Process.

The production of machined timber has some similarities with the milling of metals; the workpiece is fed into the revolving cutterhead (consisting of a number of knives clamped in a cylindrical body) which shears chips from the surface, in the up-cutting mode (figure 4.1). The finished surface, therefore, consists of a series of elemental surfaces generated by the individual cutting edge of each knife.

With wood, however, the feed (typically $100 \mathrm{~m} / \mathrm{min}$ ) and cutter speeds (typically $15000 \mathrm{rev} / \mathrm{min}$ ) far exceed those of milling; also in metal machining the workpiece is clamped to a moving bed, whilst in wood machining the bed is fixed and the workpiece is traversed across it.

Because of the limited period of engagement of each knife, the chip removed is short and of a variable thickness; this results from the combination of translatory motion of the workpiece coupled with the rotation of the cutterhead. Thus, the direction of motion of the knife is continuously changing with respect to the direction of motion of the workpiece, so that the locus of the knife, with respects to the workpiece, is not circular but trochoidal.
"Trochoid" is the name given to a family of curves which are the locus of a point taken along a radial line, originating at the centre of a circle, generated while the circle rolls on a straight line (figure 4.2). The point chosen on this radial line at a distance from the centre of the circle may be either less, equal to, or greater than the radius of the circle and will generate, respectively, curves called, "prolate trochoid", "cycloid" and "curtate trochoid".

The cutting edge of each knife follows a curtate trochoid locus when viewed from the perspective of the workpiece which is travelling horizontally at constant linear velocity and intersecting with the cutting circle of the cutterhead.

Due to the kinematics of the planing process, the geometry of the machined surface consists of a series of cusps; their distribution and linear spacing being mainly dependent on the feed speed and the number of knives used on the final cutterhead. Figure 4.3 shows the ideal surface finish of timber planed under ideal conditions (ie. no knives proud ( $R_{1}=R_{2}=R_{3}=R_{4}$ ), no vibration, dynamically balanced spindles, etc) using a cutterhead having four knives (Jackson M.R, 1986).

As can be expected, in practice, the ideal surface is rarely achieved; vibration, spindle eccentricity, proud knives, etc, affect the locus of each knife, and hence the quality of surface profile produced. It follows that the greater the degree of vibration, dynamic imbalance, etc, the further the surface form departs from the ideal. A more typical profile of a planed surface is shown

### 4.3 Curtate Trochoid Mathematical Model.

Figure 4.5 shows a schematic diagram representing the action of a general cutterhead, having N1 knives equi-spaced about its circumference and revolving at angular velocity W1. The cutting edges of the knives are positioned a nominal distance $\mathbf{R i}$ from the centre of rotation, $\mathbf{O}$. $\mathbf{H 1}$ is the vertical distance between the machine table, $C D$, and the horizontal axis of the cutterhead spindle which passes through point 0.

The workpiece, ABCD, of initial thickness Tw, travels from right to left at constant linear velocity, V1, and interferes with the cutting circle of the knives by a nominal distance, $\mathbf{d}$, the depth of cut.

The cutting action of each knife is deemed to start at angular displacement, F1 (measured from the conventional reference plane used in trigonometry) and end after having rotated through a further angular displacement $\mathbf{T i}$.

Thus

$$
\begin{equation*}
\mathrm{Ti}=2 . \operatorname{arcCos}((\mathrm{H} 1-\mathrm{Tw}) / \mathrm{Ri}) \tag{4.1}
\end{equation*}
$$

and the angular separation of the knives, $\mathbf{L b}$, is given by:

$$
\begin{equation*}
\mathbf{L b}=2 \pi / \mathbf{N} 1 \tag{4.2}
\end{equation*}
$$

The general angular displacement, $\mathbf{L g}$ (angle of lag), between the position that the first knife contacts the workpiece and the Ith knife is given by

$$
\begin{equation*}
\mathbf{L g}=(\mathbf{I}-1) . \mathrm{Lb} \tag{4.3}
\end{equation*}
$$

### 4.3.1 Ideal Cutterhead Rotation.

Ideal rotation will occur if spindle eccentricity is zero (ie. the cutterhead is dynamically balanced and the spindle rotates concentrically) and the effects of vibration are absent. Under these conditions, provided the knives share a common cutting circle radius (ie. no knife stands proud), the instantaneous position, $\mathbf{I}(t)$, of each knife relative to the point of first contact with the workpiece (see figure 4.5), resolved in the x and y direction can be expressed as

$$
\begin{align*}
& \mathbf{I}(\mathbf{t})_{\mathbf{x}}=\mathbf{R i} \cdot \operatorname{Cos}(\mathbf{F} 1+\mathbf{W} 1 . t)-\operatorname{Ri} \cdot \operatorname{Cos}(\mathbf{F} \mathbf{1})  \tag{4.4a}\\
& \mathbf{I}(t)_{\mathbf{y}}=\mathbf{R i} \cdot \operatorname{Sin}(\mathbf{F} 1+\mathbf{W} 1 . t)-\operatorname{Ri} \cdot \operatorname{Sin}(\mathbf{F} 1) \tag{4.4b}
\end{align*}
$$

where the suffixes $\mathbf{x}$ and $\mathbf{y}$ indicate the direction of resolution.

### 4.3.2 Cutterhead Eccentricity

The cutterhead may rotate eccentrically due to a lack of spindle concentricity or dynamic imbalance; this would modify the cutterhead position in space and hence the loci of its knives. The value of the instantaneous modification in position, $\mathbf{E}(\mathbf{t})$, for a given knife, is dependent on the cutterhead's angular orientation during rotation. The circle in figure 4.5, of radius $\mathbf{R e}$ and centred at J , is used here to represent the magnitude of the eccentric motion of the cutterhead due to dynamic imbalance and spindle concentricity. Viewed from the perspective of time the loci of each displacement is clearly sinusoidal. Resolved in the x and y directions, the amount by which the cutterhead
position modified (at time $t$ ) is described by:

$$
\begin{align*}
& E(t)_{z}=\operatorname{Re} \cdot \operatorname{Cos}(\text { n.W1.t })  \tag{4.5a}\\
& E(t)_{y}=\operatorname{Re} \cdot \operatorname{Sin}(\text { n.W1.t) } \tag{4.5b}
\end{align*}
$$

where
the resolved direction is indicated by the suffices, $\mathbf{x}$ and $\mathbf{y}$, Re is the maximum amplitude of the displacement, n.W1 is the angular frequency of the eccentric action and
$\mathbf{t}$ is instantaneous time.

The angle, Ee, measured from the conventional reference plane, is the angular position at which the displacement is deemed to start to affect the cutting action of the individual knife (it ceases to do so after rotating a further angular displacement, Te) This modifies the above equations (4.5a and 4.5b) to:

$$
\begin{align*}
& E(t)_{\mathbf{x}}=\operatorname{Re} . \operatorname{Cos}(\mathrm{Ee}+\text { n.W1.t })  \tag{4.6a}\\
& \mathbf{E}\left(\mathrm{t}_{\mathbf{y}}=\operatorname{Re} . \operatorname{Sin}(\mathrm{Ee}+\mathrm{n} . \mathrm{W} 1 . \mathrm{t})\right. \tag{4.6b}
\end{align*}
$$

Being more specific, if $\operatorname{Er}(t)_{\mathbf{z}}$ and $\operatorname{Er}\left(\mathrm{t}_{\mathrm{y}}\right.$ are, respectively, the x and y components of displacement due to the spindles lack of concentricity (colloquially referred to as "spindle runout") and, similarly, $\operatorname{Ei}(t)_{\mathbf{z}}$ and $\operatorname{Ei}(t)_{y}$ are displacements caused by dynamic imbalance, then

$$
\begin{align*}
& \operatorname{Er}(t)_{\mathbf{z}}=\mathbf{r} 1 \cdot \operatorname{Cos}\left(\mathbf{E} 1+\mathbf{n}_{\mathbf{1}} \cdot \mathbf{W} 1 . t\right)  \tag{4.7a}\\
& \operatorname{Er}(t)_{\mathbf{y}}=\mathbf{r} 1 \cdot \operatorname{Sin}\left(\mathbf{E} 1+\mathbf{n}_{\mathbf{1}} \cdot \mathbf{W} 1 . t\right) \tag{4.7b}
\end{align*}
$$

and

$$
\begin{align*}
& E i(t)_{x}=r 2 \cdot \operatorname{Cos}\left(E 2+n_{2} \cdot W 1 \cdot t\right)  \tag{4.8a}\\
& E i(t)_{y}=r 2 \cdot \operatorname{Sin}\left(E 2+n_{2} \cdot W 1 . t\right) \tag{4.8b}
\end{align*}
$$

where $\mathbf{n}_{1} \cdot W 1$ and $\mathbf{n}_{2} \cdot W 1$ are respectively, the angular frequency of the eccentric action due to lack of spindle concentricity, and dynamic imbalance,
$\mathbf{r} 1$ and $\mathbf{r} 2$ are the maximum magnitude of the corresponding displacements,

E1 and E2 being the respective angular position at which each displacements are deemed to start affecting the knife's cutting action (T1 and T2 are respectively their angular duration).

### 4.3.3 Cutterhead Vibration

The instantaneous position of the cutterhead could also be affected by resonant vibration, structural vibration etc. The plane of this vibration would depend on the locale and operating conditions. The circle in figure 4.5, of radius $\mathbf{R v}$ and centred at K , is used here to represent the magnitude of the cutterhead motion due to vibration. If the magnitude of the vibration is $\mathbf{R v}$ and its frequency is v1.W1, then the instantaneous amount by which the cutterhead position is modified, $\mathrm{V}(\mathrm{t})$, is given by

$$
\begin{equation*}
\mathbf{V}(\mathrm{t})=\mathrm{Rv} . \operatorname{Sin}(\mathrm{v} 1 . \mathrm{W} 1 . \mathrm{t}) \tag{4.9a}
\end{equation*}
$$

For the purpose of this analysis, and to maintain generality, the plane of vibration is defined by the plane at angle $\mathbf{G v}$ to the horizontal. Thus the components of displacement, due to vibration, resolved in the $x$ and $y$ directions are given by:

$$
\begin{align*}
& \mathbf{V}(t)_{\mathbf{z}}=(\mathbf{R v} \cdot \operatorname{Sin}(\mathbf{v} 1 . \mathrm{W} 1 . t)) /(\operatorname{Tan}(\mathbf{G v}))  \tag{4.9b}\\
& \mathbf{V}(t)_{\mathbf{y}}=\text { Rv.Sin }(\mathbf{v} 1 . \mathrm{W} 1 . t) \tag{4.9c}
\end{align*}
$$

where the suffixes $\mathbf{x}$ and $\mathbf{y}$ indicate the direction of resolution.

### 4.3.4 Knife Locus.

The x-y co-ordinates for the locus of the cutting edge of a general knife on a cutterhead will now be defined. The knife action is viewed from the perspective of the moving workpiece and referenced with respect to the initial contact point of the first knife (point $\mathbf{Q}$, see figure 4.5). Thus, the origin of the $x-y$ plane is defined as follows:

The x-origin is the vertical plane passing through the point at which the first knife makes initial contact with the workpiece.

The $y$-origin is the horizontal plane of the machine bed

Thus, the $x$-origin moves leftwards as the cutting action progresses, while the $y$-origin remains fixed.

Alternatively, the workpiece, and hence the $x$-origin, can be considered to be stationary while the cutterhead is assumed to move rightward with linear velocity V1, rotating with angular velocity W1.

For the purposes of analysis the locus of the general knife, viewed relative to the workpiece, will be resolved into two components:

1) Component of displacement in the x-direction
2) Component of displacement in the $y$-direction

Hence the mathematical equation which describes the locus will be a function of time and in the parametric form:

$$
\begin{align*}
& \mathbf{x}=\mathbf{f}(\mathbf{t})  \tag{4.10a}\\
& \mathbf{y}=\mathbf{F}(\mathbf{t}) \tag{4.10b}
\end{align*}
$$

The co-ordinates of the general knife edge in the $x-y$ plane will be calculated using the finite difference method; that is, the difference between knife position at $t=0$ (the $x-y$ origin 0,0 ) and its position at $t=d t$ (present position $\mathrm{x}, \mathrm{y}$. So, by varying the value of dt , the complete cutting action of each knife can be mapped.

### 4.3.4.1 Component of Displacement in the $y$-direction.

The displacement of the knife in the $y$-direction, $y$, during time $d t$, can be expressed as a summation of the various elements of which it is comprised. Thus, during time period dt:

$$
\begin{equation*}
y=d I_{y}+d E r_{y}+d E i_{y}+d V_{y} \tag{4.11}
\end{equation*}
$$

where
dII $_{\mathbf{J}}=$ knife displacement due to Ideal cutterhead rotation,
$\mathbf{d E r} \mathbf{r}_{\mathbf{y}}=$ knife displacement due to spindle Runout,
$\mathbf{d E i} \mathrm{y}_{\mathrm{y}}=$ knife displacement due to Dynamic Imbalance,
and
$\mathbf{d} V_{\mathbf{y}}=$ knife displacement due to Vibration.

Now, from equation 4.4b

$$
\begin{equation*}
\mathbf{d I} \mathbf{I}_{\mathrm{y}}=\mathbf{R i} \cdot \operatorname{Sin}(\mathbf{F} 1+\mathrm{W} 1 . \mathrm{dt})-\mathbf{R i} \cdot \operatorname{Sin}(\mathbf{F} 1) \tag{4.12}
\end{equation*}
$$

from equation 4.7b

$$
\begin{equation*}
d E r_{y}=r 1 \cdot \operatorname{Sin}\left(E 1+n_{1} \cdot W 1 . d t\right) \tag{4.13}
\end{equation*}
$$

from equation 4.8b

$$
\begin{equation*}
d E i_{y}=r 2 \cdot \operatorname{Sin}\left(E 2+n_{2} \cdot W 1 . d t\right) \tag{4.14}
\end{equation*}
$$

from equation 4.9c

$$
\begin{equation*}
\mathbf{d V} V_{y}=\operatorname{Rv} . S i n(v 1 . W 1 . d t) \tag{4.15}
\end{equation*}
$$

So that:

$$
\begin{align*}
\mathrm{y}= & \operatorname{Ri} \cdot \operatorname{Sin}(\mathrm{F} 1+\mathrm{W} 1 \cdot \mathrm{dt})-\operatorname{Ri} \cdot \operatorname{Sin}(\mathrm{F} 1)+\mathrm{r} 1 \cdot \operatorname{Sin}\left(\mathrm{E} 1+\mathbf{n}_{1} \cdot \mathrm{~W} 1 \cdot \mathrm{dt}\right) \\
& +\mathbf{r} 2 \cdot \operatorname{Sin}\left(\mathrm{E} 2+\mathbf{n}_{\mathbf{2}} \cdot \mathbf{W} 1 \cdot \mathrm{dt}\right)+\text { Rv.Sin}(\mathrm{v} 1 \cdot \mathrm{~W} 1 \cdot \mathrm{dt}) \tag{4.16}
\end{align*}
$$

### 4.3.4.2 Component of Displacement in x-direction.

The displacement of the knife, relative to the workpiece, in the $x$-direction, can be divided into two major elements:

1. Knife displacement.
2. Workpiece displacement.

So that the x -displacement, x , is given by:
x=knife displacement + workpiece displacement

The knife displacement can be further sub-divided and expressed as a summation of its various elements of which it is comprised. Thus, during time
period dt:

$$
\begin{equation*}
\text { Knife displacement }=d I_{z}+d E r_{x}+d E i_{z}+d V_{x} \tag{4.18}
\end{equation*}
$$

where $\mathbf{d I}_{\mathbf{z}}=$ knife displacement due to Ideal cutterhead rotation, $\mathbf{d E} \mathbf{r}_{\mathbf{x}}=$ knife displacement due to spindle Runout, $\mathrm{dEi}_{\mathbf{z}}=$ knife displacement due to Dynamic Imbalance,
and $\quad \mathbf{d V}_{\mathbf{x}}=$ knife displacement due to Vibration

Now, from equation 4.4a

$$
\begin{equation*}
\mathbf{d I _ { r }}=\operatorname{Ri} \cdot \operatorname{Cos}(\mathbf{F} 1+W 1 . d t)-\operatorname{Ri} \cdot \operatorname{Cos}(F 1) \tag{4.19}
\end{equation*}
$$

from equation 4.7a

$$
\begin{equation*}
d E r_{x}=r 1 \cdot \operatorname{Cos}\left(E 1+n_{1} \cdot W 1 \cdot d t\right)-r 1 \cdot \operatorname{Cos}(E 1) \tag{4.20}
\end{equation*}
$$

from equation 4.8a

$$
\begin{equation*}
\mathrm{dEi}_{2}=\mathrm{r} 2 . \operatorname{Cos}\left(\mathrm{E} 2+\mathrm{n}_{2} \cdot \mathrm{~W} 1 . \mathrm{dt}\right)-\mathrm{r} 2 . \operatorname{Cos}(\mathrm{E} 2) \tag{4.21}
\end{equation*}
$$

from equation 4.9b

$$
\begin{equation*}
d V_{\mathbf{x}}=(\operatorname{Rv} \cdot \operatorname{Sin}(\mathrm{v} 1 . \mathrm{W} 1 . \mathrm{dt})) /(\operatorname{Tan}(G v)) \tag{4.22}
\end{equation*}
$$

Hence
knife displacement $=\mathbf{R i} .[\operatorname{Cos}(\mathbf{F} 1+\mathbf{W} 1 . d t)-\operatorname{Cos}(F 1)]$

$$
\begin{align*}
&+r 1 .\left[\operatorname{Cos}\left(E 1+n_{1} \cdot W 1 . d t\right)-\operatorname{Cos}(E 1)\right] \\
&+r 2 .\left[\operatorname{Cos}\left(E 2+n_{2} \cdot W 1 . d t\right)-\operatorname{Cos}(E 2)\right] \\
&+(\operatorname{Rv} \cdot S i n(v 1 . W 1 . d t)) /(\operatorname{Tan}(G v)) \tag{4.23}
\end{align*}
$$

The displacement of the workpiece can be calculated from the velocity-time relationship:

## workpiece displacement $=$ workpiece velocity $\mathbf{x}$ time taken

Since $\mathbf{L g}$ is the general lag angle between the first cutter and the active cutter - the Ith cutter (see equation 4.3) - and, W1.dt is the rotation angle during which cutting takes place, time taken to traverse angular displacement (Lg + W1.dt) is

$$
(L g+W 1 . d t) / W 1
$$

hence

$$
\begin{equation*}
\text { workpiece displacement = V1. }(\mathrm{Lg}+\mathrm{W} 1 . \mathrm{dt}) / \mathrm{W} 1 \tag{4.24}
\end{equation*}
$$

So that

$$
\begin{align*}
\mathrm{x}= & \mathrm{Ri} \cdot[\operatorname{Cos}(\mathrm{~F} 1+\mathrm{W} 1 . \mathrm{dt})-\operatorname{Cos}(\mathrm{F} 1)] \\
+ & \mathrm{r} 1 .\left[\operatorname{Cos}\left(\mathrm{E} 1+\mathbf{n}_{1} \cdot \mathrm{~W} 1 . \mathrm{dt}\right)-\operatorname{Cos}(\mathrm{E} 1)\right] \\
& +\mathrm{r} 2 \cdot\left[\operatorname{Cos}\left(\mathrm{E} 2+\mathbf{n}_{2} \cdot \mathrm{~W} 1 . \mathrm{dt}\right)-\operatorname{Cos}(\mathrm{E} 2)\right] \\
& +(\operatorname{Rv} \cdot \operatorname{Sin}(\mathrm{v} 1 . \mathrm{W} 1 . \mathrm{dt})) /(\operatorname{Tan}(\mathrm{Gv})) \\
& +\mathrm{V} 1(\mathrm{Lg}+\mathrm{W} 1 . \mathrm{dt}) / \mathrm{W} 1 \tag{4.25}
\end{align*}
$$

The x -displacement, $\mathbf{X s}$, at which the Ith knife starts to cut the workpiece is given by

$$
\begin{equation*}
\mathbf{X}_{\mathbf{s}}=\text { V1.L.Lb/W1 } \tag{4.26}
\end{equation*}
$$

The x -displacement, Xe, at which the Ith knife stops cutting the workpiece is given by

$$
\begin{align*}
\mathrm{Xe}=\mathrm{V} 1 & (\mathrm{I} \cdot \mathrm{Lb}+\mathrm{Ti}) / \mathrm{W} 1+\mathrm{Ri} \cdot\{\operatorname{Cos}(\mathrm{~F} 1+\mathrm{Ti})-\operatorname{Cos}(\mathrm{F} 1)\} \\
& +\mathrm{r} 1 \cdot\{\operatorname{Cos}(\mathbf{E} 1+\mathrm{T} 1)-\operatorname{Cos}(\mathrm{E} 1)\} \\
& +\mathrm{r} 2 \cdot\{\operatorname{Cos}(\mathbf{E} 2+\mathrm{T} 2)-\operatorname{Cos}(\mathrm{E} 2)\} \tag{4.27}
\end{align*}
$$

### 4.4 Loci Generation.

The parametric equations 4.16 and 4.25 , derived above, can be used to produce the co-ordinates of the locus of each knife, relative to the traversing workpiece, as the cutterhead rotates. The computer algorithm, entitled "LOCI-0" and listed in Appendix A0, was written to achieve this. It was designed to simulate ideal spindle rotation coupled with uniform timber feed speeds; cutterhead vibration, imbalance non-concentricity etc. was ignored at this stage. Examples of knife loci generated is shown in figures 4.6a to 4.6h.

The locus of each knife (relative to the moving timber) was plotted in turn as the cutterhead rotated through 360 degrees ( $2 \pi$ rad) starting from the location where the first knife engaged the timber. The angular velocity of the cutterhead and linear feedspeed of the timber were both constant.
"LOCI-0" is written in BBC BASIC and uses the following variable parameters:

N\% - number of knives on cutterhead (integer)
R1 - knife radius (mm)
W1 - angular velocity of cutterhead (rad/s)
V1 - linear velocity of workpiece (feedspeed) ( $\mathrm{mm} / \mathrm{s}$ )
Tw - initial workpiece thickness (mm)
H1 - distance: cutterhead centreline to machine bed (mm)
I - knife number
F1 - angular displacement of knife at initial contact (rad)
Lb - angular displacement between successive knives (rad)
Lg - angular displacement between Ith knife and 1st (rad)
dt - increment of time (s)
XORG - x-origin of the graphics $x$ - $y$ plane

YORG - y-origin of the graphics $x-y$ plane

The algorithm began by establishing the constant values of the various parameters, lines 20 to 50 . The profile of the unplanned workpiece was then drawn, and, for convenience, the $x$-origin and $y$-origin was moved to coincide with the centreline of the cutterhead.

The algorithm made use of a double nested FOR-NEXT loop as follows:
The outer FOR-NEXT loop, lines 100 to 200, introduced each knife in turn, starting with the first and progressing incrementally to the N1th. The angular displacement, Lg, between the first knife and the Ith (current) knife was calculated, line 110 , as were the co-ordinates of its initial position, lines 120 and 130. A straight line was drawn between the cutterhead's centre and the initial position of the current knife, line 140; this diagrammatically represented the knife.

The inner FOR-NEXT loop, lines 150 to 190 was used to calculate the co-ordinates of the locus of the Ith (current) knife edge, every 0.1 radians, as the cutterhead rotated, through $2 \pi$ radians. The successive knife edge positions were plotted, in the $x-y$ plane, and connected by straight lines (chord approximation).

### 4.5 Loci Sampling.

Equations 4.16 and 4.25 completely define the locus of each knife-tip as the cutterhead rotates. Thus, this mathematical model can be used to generate
simulated, machined surface profiles by considering only the sections of the knife's locus which corresponds with actual cutting taking place.

There was, however, a problem with sampling. Equations 4.16 and 4.25 describe the loci as a function of time. This description is unsatisfactory from the perspective of generating simulated surface profile data which can be sampled at uniform, linear intervals (in the x-direction); uniform sampling is essential for the subsequent Fourier analysis of the surface profile data; whilst the $x$-displacement of the workpiece with respect to time is uniform, the $x$-displacement of each knife edge is not; the $x$-velocity of each cutting edge varies in both magnitude and sense. Thus, if the coordinates of the profile are calculated (sampled) at regular time intervals, the x-displacement between calculations (sample points) would vary considerably with time; this was illustrated by modifying the computer algorithm "LOCI-0" such that the generated data was plotted as a histogram. The modified algorithm was called "LOCI-1" (see Appendix A1) and an example of the data generated is shown in figure 4.7. This clearly demonstrated the non-uniform-samplinginterval problem.

To alleviate this problem the displacement, $x$, in equation 4.25 had to become the independent variable (dt becoming the dependent variable, ie. $\mathbf{d t}$ $=\mathbf{f}(\mathbf{x})$ ); so dt could be calculated for any given $x$-displacement. Thus the linear sampling interval in the $x$-direction could be regulated; the corresponding $y$-displacements could be calculated by substituting the particular value of $\mathbf{d t}$ in equation 4.16. This was accomplish by using the trigonometric identity,

$$
\begin{equation*}
\operatorname{Cos}(A+B)=\operatorname{Cos}(A) \cdot \operatorname{Cos}(B)-\operatorname{Sin}(A) \cdot \operatorname{Sin}(B) \tag{4.28}
\end{equation*}
$$

So
$\operatorname{Cos}(F 1+W 1 . d t)=\operatorname{Cos}(F 1) \cdot \operatorname{Cos}(d t)-\operatorname{Sin}(F 1) \cdot \operatorname{Sin}(d t)$
$\operatorname{Cos}(E 1+W 1 . d t)=\operatorname{Cos}(E 1) \cdot \operatorname{Cos}(d t)-\operatorname{Sin}(E 1) \cdot \operatorname{Sin}(d t)$
$\operatorname{Cos}(Z 1+W 1 . d t)=\operatorname{Cos}(Z 1) \cdot \operatorname{Cos}(d t)-\operatorname{Sin}(Z 1) \cdot \operatorname{Sin}(d t)$

Substituting equations $4.29,4.30$ and 4.31 in equation 4.25 gives:
$\mathrm{x}=\mathrm{Ri}\{[\operatorname{Cos}(\mathrm{F} 1) \cdot \operatorname{Cos}(\mathrm{W} 1 . \mathrm{dt})-\operatorname{Sin}(\mathrm{F} 1) \cdot \operatorname{Sin}(\mathrm{W} 1 . \mathrm{dt})] \cdot \operatorname{Cos}(\mathrm{F} 1)\}$
$+r 1\left\{\left[\operatorname{Cos}(E 1) \cdot \operatorname{Cos}\left(n_{1} \cdot W 1 . d t\right) \cdot \operatorname{Sin}(E 1) \cdot \operatorname{Sin}\left(n_{1} \cdot W 1 . d t\right)\right] \cdot \operatorname{Cos}(F 1)\right\}$ $+\mathbf{r}$ \{[Cos(Z1).Cos( $\left.\left.\left.\mathrm{n}_{2} \cdot \mathbf{W} 1 . \mathrm{dt}\right) \cdot \operatorname{Sin}(\mathrm{Z} 1) \cdot \operatorname{Sin}\left(\mathrm{n}_{1} \cdot \mathrm{~W} 1 . \mathrm{dt}\right)\right] \cdot \operatorname{Cos}(\mathrm{Z} 1)\right\}$ +Rv. Sin(v1.W1.dt).Cos(Gv)+V1.Lg/W1+V1.dt

Therefore

$$
\begin{align*}
x= & R i \cdot \operatorname{Cos}(F 1) \cdot \operatorname{Cos}(W 1 \cdot d t)-\operatorname{Ri} \cdot \operatorname{Sin}(F 1) \cdot \operatorname{Sin}(W 1 \cdot d t)-\operatorname{Ri} \cdot \operatorname{Cos}(F 1) \\
& +r 1 \cdot \operatorname{Cos}(E 1) \cdot \operatorname{Cos}\left(n_{1} \cdot W 1 \cdot d t\right) \cdot r 1 \cdot \operatorname{Sin}(E 1) \cdot \operatorname{Sin}\left(n_{1} \cdot W 1 \cdot d t\right) \cdot r 1 \cdot \operatorname{Cos}(E 1) \\
& +r 2 \cdot \operatorname{Cos}(Z 1) \cdot \operatorname{Cos}\left(n_{2} \cdot W 1 \cdot d t\right) \cdot r 2 \cdot \operatorname{Sin}(Z 1) \cdot \operatorname{Sin}\left(n_{2} \cdot W 1 \cdot d t\right) \cdot r 2 \cdot \operatorname{Cos}(Z 1) \\
& +R v \cdot \operatorname{Sin}(v 1 \cdot W 1 \cdot d t) \cdot \operatorname{Cos}(G v)+V 1 \cdot L g / W 1+V 1 \cdot d t \tag{4.32}
\end{align*}
$$

Decomposing equation 4.32 further, so as to isolate $\mathbf{d t}$ from the Sine and Cosine functions, use is made of the Taylor polynomial (or series) of the respective functions:

For $\mathbf{m}$, in general,

$$
\begin{equation*}
\operatorname{Cos}(m)=1-\frac{m^{2}}{2!}+\frac{m^{4}}{4!} \cdot \ldots \ldots . \tag{4.33}
\end{equation*}
$$

and

$$
\begin{equation*}
\operatorname{Sin}(m)=m \cdot \frac{m^{3}}{3!}+\frac{m^{5}}{5!} \cdot \ldots \ldots \tag{4.34}
\end{equation*}
$$

Truncating both polynomials at the second power of $m$ gives:-

$$
\begin{equation*}
\operatorname{Cos}(m)=1-\frac{m^{2}}{2!} \tag{4.35}
\end{equation*}
$$

$\operatorname{Sin}(m)=m$

Equations 4.35 and 4.36 are accurate to two decimal places for $\mathbf{m}$ less than 0.3 radians.

Substituting, as required, equations 4.35 and 4.36 into equation 4.32, using as appropriate:-

$$
\begin{aligned}
& \mathrm{m}=\mathrm{W} 1 . \mathrm{dt} \\
& \mathrm{~m}=\mathrm{n}_{1} \cdot \mathrm{~W} 1 . \mathrm{dt} \\
& \mathrm{~m}=\mathrm{n}_{2} \cdot \mathrm{~W} 1 . \mathrm{dt} \\
& \mathrm{~m}=\mathrm{v} 1 . \mathrm{W} 1 . \mathrm{dt}
\end{aligned}
$$

gives

$$
\begin{aligned}
\mathrm{x}= & \operatorname{Ri} \cdot \operatorname{Cos}(\mathrm{F} 1)\left\{1 \cdot \mathrm{~W} 1^{2} \cdot \mathrm{dt}^{2} / 2\right\}-\operatorname{Ri} \cdot \operatorname{Sin}(\mathrm{F} 1) \cdot \mathrm{W} 1 . \mathrm{dt} \cdot \operatorname{Ri} \cdot \operatorname{Cos}(\mathrm{~F} 1) \\
& +\mathrm{r} 1 \cdot \operatorname{Cos}(\mathrm{E} 1)\left\{1 \cdot \mathrm{n}_{1}{ }^{2} \cdot \mathrm{~W} 1^{2} \cdot \mathrm{dt}^{2} / 2\right\}-\mathrm{r} 1 \cdot \operatorname{Sin}(\mathrm{E} 1) \cdot \mathrm{n}_{1} \cdot \mathrm{~W} 1 \cdot \mathrm{dt} \cdot \mathrm{r} 1 \cdot \operatorname{Cos}(\mathrm{E} 1) \\
& +\mathrm{r} 2 \cdot \operatorname{Cos}(\mathrm{Z} 1)\left\{1 \cdot \mathrm{n}_{1}{ }^{2} \cdot \mathrm{~W} 1^{2} \cdot \mathrm{dt}^{2} / 2\right\}-\mathrm{r} 2 \cdot \operatorname{Sin}(\mathrm{Z} 1) \cdot \mathrm{n}_{1} \cdot \mathrm{~W} 1 . \mathrm{dt} \cdot \mathrm{r} 1 \cdot \operatorname{Cos}(\mathrm{Z} 1) \\
& +\operatorname{Rv} \cdot \mathrm{v} 1 \cdot \mathrm{~W} 1 . \mathrm{dt} \cdot \operatorname{Cos}(\mathrm{Gv})+\mathrm{V} 1 . \mathrm{Lg} / \mathrm{W} 1+\mathrm{V} 1 . \mathrm{dt}
\end{aligned}
$$

Multiplying out and grouping matching terms to form a quadratic in dt:-$x=-R i . W 1^{2} / 2 . \operatorname{Cos}(F 1) . d t^{2} \quad$ Ri.W1.Sin(F1).dt - $n_{1}{ }^{2} \cdot \mathbf{r} 1 . W 1^{2} / 2 . \operatorname{Cos}(E 1) . d t^{2}$ - $n_{1} . r 1 . W 1 . \operatorname{Sin}(E 1) . d t$ $-n_{2}{ }^{2} \cdot \mathbf{r 2}$.W1 ${ }^{2} / 2 . \operatorname{Cos}(Z 1) . d t^{2}$ - $n_{2}$. r2.W1.Sin(Z1).dt + v1.Rv.W1.Cos(Gv).dt +V1.dt+V1.Lg/W1

Factorising:-

$$
\begin{aligned}
\mathrm{x}= & -\mathrm{W} 1^{2} / 2 \cdot\left[\mathrm{Ri} \cdot \operatorname{Cos}(\mathrm{~F} 1)+\mathrm{n}_{1}^{2} \cdot \mathrm{r} 1 \cdot \operatorname{Cos}(\mathrm{E} 1)+\mathrm{n}_{2}^{2} \cdot \mathrm{r} 2 \cdot \operatorname{Cos}(\mathrm{Z} 1)\right] \cdot \mathrm{dt}{ }^{2} \\
& +[\mathrm{Rv} \cdot \mathrm{v} 1 \cdot \mathrm{~W} 1 \cdot \operatorname{Cos}(\mathrm{Gv})+\mathrm{V} 1 \cdot \\
& \left.\mathrm{W} 1\left[\operatorname{Ri} \cdot \operatorname{Sin}(\mathrm{~F} 1)+\mathrm{n}_{1} \cdot \mathrm{r} 1 \cdot \operatorname{Sin}(\mathrm{E} 1)+\mathrm{n}_{2} \cdot \mathrm{r} 2 \cdot \operatorname{Sin}(\mathrm{Z} 1)\right]\right] \cdot \mathrm{dt}
\end{aligned}
$$

+ V1.Lg/W1

Multiplying through by 2 and rearranging:-

$$
\begin{aligned}
0=W & 1^{2}\left\{R i \cdot \operatorname{Cos}(F 1)+n_{1}{ }^{2} \cdot \mathbf{r} 1 \cdot \operatorname{Cos}(E 1)+n_{2}{ }^{2} \cdot \mathrm{r} 2 \cdot \operatorname{Cos}(\mathrm{Z} 1)\right] \cdot \mathrm{dt}^{2} \\
& +2\left\{\mathrm { W } 1 \cdot \left[\mathrm{Ri} \cdot \operatorname{Sin}(\mathrm{~F} 1)+\mathrm{n}_{1} \cdot \mathrm{r} 1 \cdot \operatorname{Sin}(\mathrm{E} 1)\right.\right. \\
& \left.\left.+\mathrm{n}_{2} \cdot \mathrm{r} 2 \cdot \operatorname{Sin}(\mathrm{Z} 1)-\mathrm{v} 1 \cdot \mathrm{Rv} \cdot \operatorname{Cos}(\mathrm{Gv})\right]-\mathrm{V} 1\right\} \cdot \mathrm{dt} \\
& +2\{\mathrm{x} \cdot \mathrm{~V} 1 . \mathrm{Lg} / \mathrm{W} 1\}
\end{aligned}
$$

Rewriting

$$
\begin{equation*}
0=\mathbf{A} \cdot d t^{2}+\mathbf{B} \cdot \mathbf{d t}+\mathbf{C} \tag{4.37}
\end{equation*}
$$

where

$$
\begin{aligned}
A= & W 1^{2} \cdot\left\{R i \cdot \operatorname{Cos}(F 1)+n_{1}{ }^{2} \cdot \mathbf{r} 1 \cdot \operatorname{Cos}(E 1)+n_{2}{ }^{2} \cdot \mathbf{r} 2 \cdot \operatorname{Cos}(\mathrm{Z} 1)\right\} \\
B= & \left\{\mathrm { W } 1 \cdot \left[\operatorname{Ri} \cdot \operatorname{Sin}(\mathrm{F} 1)+\mathrm{n}_{1} \cdot \mathbf{r} 1 \cdot \operatorname{Sin}(\mathrm{E} 1)\right.\right. \\
& \left.\left.+\mathrm{n}_{2} \cdot \mathbf{r} 2 \cdot \operatorname{Sin}(\mathrm{Z} 1) \cdot \mathrm{v} 1 \cdot R \mathrm{R} \cdot \operatorname{Cos}(\mathrm{Gv})\right]-\mathrm{V} 1\right\}
\end{aligned}
$$

and $\quad C=2\{x \cdot V 1 . L g / W 1\}$

Equation 4.37 is a quadratic in $\mathbf{d t}$ and is of the general form

$$
a x^{2}+b x+c=0,
$$

the solution of which is:-

$$
x=\frac{-b \pm \sqrt{ }\left(b^{2}-4 . \mathbf{a} . c\right)}{2 . a}
$$

Therefore the solution of equation 4.37 is:-

$$
\begin{equation*}
d t==\frac{-B \pm \sqrt{ }\left(B^{2}-4 . A \cdot C\right)}{2 \cdot A} \tag{4.38}
\end{equation*}
$$

In general, equation 4.37 will have two roots (or solutions); which may be:

1) real and different
2) real and equal
3) complex

The roots will be real if the discriminant, $\left(\mathbf{B}_{2}-4 . A . C\right)$ is positive or zero, and, complex if it is negative.

Examination of each term in the discriminant of equation 4.37 shows that: $\mathbf{B}^{2}$ is clearly always positive.
A is negative; the term Ri.Cos(F1) is negative because F1 is between 180 degrees and 270 degrees. The amplitude of the other terms of which $\mathbf{A}$ is composed is very much smaller than $\mathbf{R i}$ in reality. The $\mathbf{C}$ is positive; V1.Lg/W1, the displacement of the timber before the knife engages will always be leftward of $\mathbf{x}$ (on the $\mathrm{x}-\mathrm{y}$ plane in which the motion is being analyzed). Hence $\mathbf{x}$ is always greater than V1.Lg/W1 and the result of the subtraction always positive.

Hence the two roots of equation 4.37 are real and distinct because $A$, the coefficient of $\mathbf{d t}^{\mathbf{2}}$, is always negative, whilst $\mathbf{C}$, the constant term, is always positive resulting in a discriminant which is always positive. Both roots are significant in terms of the complete knife locus, but only one relates to the actual surface profile. The required root is obtained by considering the nature (shape) of the function, $f(d t)$, associated with, equation 4.37 ie.

$$
\begin{equation*}
f(d t)=A \cdot d t^{2}+B \cdot d t+C \tag{4.39}
\end{equation*}
$$

Factorising equation 4.39 gives

$$
\begin{equation*}
\mathbf{f}(\mathbf{d t})=\mathbf{A}\left\{\mathbf{d} \mathbf{t}^{2}+\mathbf{B} / \mathbf{A} \cdot \mathbf{d t}+\mathbf{C} / \mathbf{A}\right\} \tag{4.40}
\end{equation*}
$$

Let the two distinct roots of equation 4.37 be Rol and Ro2 so that

$$
\mathbf{f}(\mathbf{d t})=\mathbf{A}\left[\mathbf{d} t^{2}+\mathbf{B} / \mathbf{A} \cdot \mathbf{d t}+\mathbf{C} / \mathbf{A}\right]=\mathbf{A}(\mathbf{d t} \cdot \mathbf{R o} 1)(\mathbf{d t} \cdot \mathbf{R o} 2)
$$

ie.

$$
\begin{equation*}
\mathbf{f}(\mathrm{dt})=\mathbf{A}(\mathrm{dt}-\mathrm{Ro} 1)(\mathrm{dt}-\mathrm{Ro} 2) \tag{4.41}
\end{equation*}
$$

Now, let Ro1 < Ro2 :-
when dt < Rol:
(dt - Ro1) and (dt - Ro2) are both negative; therefore $f(d t)$ has the same sign as $\mathbf{A}$
when Ro1 < dt < Ro2:
(dt - Ro1) and (dt - Ro2) have opposite signs; therefore $f(d t)$ has the opposite sign to $\mathbf{A}$
when dt > Ro2:
(dt - Ro1) and (dt - Ro2) are both positive; therefore $\mathbf{f}(\mathbf{d t})$ has the same sign as $\mathbf{A}$

The coefficients A, B and C of equations 4.37 and 4.39 can be evaluated by substituting typical values for the constituent variables of which they are comprised. Typically, equation 4.39 has two roots; one root is negative whilst the other is positive. The negative root is invalid as it relates to an instant in time prior to that of the initial engagement of the knife with the timber. The valid solution is therefore the positive root.

Thus, for the Ith knife, dt can be calculated for any $\mathbf{x}$-displacement between Xs and Xe (see equations 4.26 and 4.27); this value of dt can then be
substituted into equation 4.16 to yield the corresponding $y$-coordinate.

### 4.6 Surface Profile Simulation.

The surface simulation algorithm (SSA) that was ultimately written, evolved through four main stages. At each stage various concepts were introduced and modifications made. What follows discusses the four stages of development and highlights, with subsequent solutions, the problems that were encountered.

### 4.6.1 Development Stage I

(Refer to algorithm LOCI-1 in Appendix A1)
In stage I, which has already been described, an algorithm was written which plots the locus of each knife as the cutterhead rotates through 360 degrees ( $2 \pi$ radians). This algorithm proved unsatisfactory because the sampling rate was non-uniform (see figure 4.7).

### 4.6.2 Development Stage II

(Refer to algorithm LOCI-2, Appendix A2)
Stage II incorporated the solution to the non-uniform sampling rate problem (Section 4.5) and the sampled points were restricted to the vicinity or locale in which timber removal/cutting is deemed to take place, ie. between $\mathbf{X s}$, the $x$-displacement at which the knife is deemed to start engagement with the timber, and Xe, the x -displacement at which the knife is deemed to disengage with the timber (see lines 160 to 250 and figure 4.8a).

In stage II the idea of a single proud knife was introduced; this knife can be placed in any one of the N1 positions available (lines 50 and 60) and described a cutting circle radius which is larger than that of the other knives (line 100).(see figure 4.8b).

One problem encountered in stage II was as follows:

Where, with respects to the $x$-axis, the cutting action of one knife overlapped with that of another, the sampled points of the first locus did not necessarily coincide with those of the second, within the region of overlap. This meant that, despite uniform sampling between localised start and end points (ie. Xs and Xe ), when viewed as a whole, the generated profile data again exhibit a non-uniform sampling rate (see figure 4.8c and figure 4.8d).

The remedy to the "sample-point overlap coincidence" problem was to magnify the profile by a magnification factor, $m$, such that successive sample points (sample spacing), in the $x$-direction were unit distance apart. Hence, each sample point would fall on an integer value in the $x$-direction. Under this magnification Xs and Xe, for each knife cut, could be modified slightly so as to coincide with the nearest corresponding integer value; the positional error in displacement due to this adjustment, evaluated over a sample length of 0.125 m (an adequate assessment length suggested by engineers in the woodworking industry (Goddard M, et al, 1986), see section 5.3 .3 ), is between
$0 \%$ and $0.8 \% / \mathrm{m}(=1 /(125 \times \mathrm{m}) \times 100 \%)$, where m is the magnification factor.

## ASIDE:

The magnification factor, m , calculated here, depends on the number of sample points employed between $\mathrm{X}_{\mathrm{s}}$ and Xe ; at this stage 16 sample points were used.
Thus $\quad \mathrm{m}=\frac{1}{\Delta \mathrm{x}}$
where $\Delta \mathrm{x}=\frac{\left(\mathrm{Xe}-\mathrm{X}_{\mathrm{s}}\right)}{16}$
and is the sample spacing before magnification.

Note:
The frequency content of the generated profile data is the parameter of major interest; magnification of the data has no effect on its frequency content.

### 4.6.3 Development Stage III

(Refer to algorithm LOCI-3, Appendix A3)
Stage III incorporated the solution to the "sample-point overlap coincidence" problem (lines 180 to 200 and line 290, also see figure 4.9a) and introduced the idea of eccentricity motion of the cutterhead spindle (lines 90,350 and 370 , also see figure 4.9b). The notion of a single proud knife, introduced in stage II, was expanded such that a number of proud knives and their respective positions on the cutterhead could be selected (see lines 80 and 240).

### 4.6.4 Development Stage IV

(Refer to algorithm SSA, Appendix A4)
The final stage, Stage IV, of development of the Surface Simulation Algorithm, saw the introduction of a standard sample length of 0.125 m for each simulated data set. To satisfy the Nyquist sampling theorem criterion,
which states that the sampling frequency must be at least twice that of the highest frequency component in the waveform being sampled, the maximum sample spacing had to be 0.5 mm ; a surface wave of pitch 1.0 mm is currently the highest quality finish produced in the woodworking industry (Goddard M , Garrett J, 1986). So, at least 250 equi-spaced sample points would be required in a 0.125 m sample length.

The simulated data would subsequently be analyzed in terms of its frequency content using fast Fourier analysis techniques. The use of Cooley-Tukey method (Cooley J.W, Tukey J.W, 1965) to evaluate the Fourier Transform (ie. the fast Fourier transform (FFT)) requires that the number of sampled points to be transformed must be an integer power of 2 (ie $2^{n}$ where $n$ is an integer). Hence 256 sample points satisfied both the Nyquist sampling and the FFT requirements.

The sample length ( 0.125 m ) was divided into 256 giving a sample spacing, $\Delta x$, before magnification, of $2.44 \times 10^{-4}$ metres $(=0.125 / 256$ metres). The resulting magnification factor, $\mathbf{m}$, is given by:

$$
\begin{aligned}
\mathbf{m} & =\frac{(\text { No. of sample points) }}{\text { (sample length) }} \\
& =\frac{256}{0.125} \\
& =2048 \quad \text { (see line 5090) }
\end{aligned}
$$

(At this magnification the positional error in displacement, assessed over the sample length, is

$$
\left.3.9 \times 10^{-4} \% \quad(=1 /(125 \times \mathrm{m}) \times 100 \%)\right\}
$$

The FOR - NEXT loop used in previous stages to indicate the number of knifemarks on the profile, was superseded in stage IV by a REPEAT UNTIL loop (lines 5120 and 5430). The action of this loop is to monitor the simulated profiles length and terminate when this is greater than the effective sample length of 0.125 metres. This was effected by calculating the number of revolutions the cutterhead would describe during the time it took for the workpiece to travel a distance equal to the sample length. The reasoning was as follows:

Time ( $t$ ) for workpiece, travelling at constant linear velocity ( $V$ ), to traverse sample length (smplth) is given by:-

$$
\begin{equation*}
t=\frac{(\text { smplth })}{V} \tag{4.44}
\end{equation*}
$$

Time period (T) for cutterhead, rotating at constant angular velocity (W), to complete one revolution is given by:-

$$
\begin{equation*}
T=\frac{2 \pi}{W 1} \tag{4.45}
\end{equation*}
$$

Therefore, the number of revolutions, $c$, made by the cutterhead in time $t$ is given by:-

$$
\begin{equation*}
c=\frac{\mathbf{t}}{\mathbf{T}} \tag{4.46}
\end{equation*}
$$

So

$$
\begin{equation*}
c=\frac{(\text { smplth } \times W 1)}{(V \times 2 \pi)} \tag{4.47}
\end{equation*}
$$

The current number of revolutions, nc, made by the cutterhead is calculated by dividing the current total number of knifemarks on the profile (I-1) by the total number of knives on the cutterhead (nN\%).

Hence

$$
\begin{equation*}
\mathrm{nc}=\frac{(\mathrm{I}-1)}{(\mathrm{nN} \%)} \tag{4.49}
\end{equation*}
$$

Thus, the REPEAT - UNTIL loop is terminated when nc is greater than (c+1), see line 5430

Stage IV also saw the introduction of the effects of machine/timber vibration on the simulated profile; the machine/timber was deemed to vibrate in the vertical plane with amplitude, vib, and with a frequency which was some multiple, rate, of the cutterheads angular frequency, W1 (see lines 4640 and 5300). Examples of profiles generated are shown in figures 4.10a to 4.10f.

## 5 DEVELOPMENT OF POST-PROCESS LASER INSTRUMENT

### 5.1 Introduction / General Description

### 5.2 Electronic Hardware

### 5.2.1 The Host Computer

5.2.1.1 General Description
5.2.1.2 Versatile Interface Adapter
5.2.2 Linear Photodiode Array
5.2.2.1 General Description
5.2.2.2 Photodiode Array Circuit
5.2.2.3 Sensor Geometry
5.2.2.4 Drive Requirements
5.2.2.5 Signal Extraction
5.2.2.6 Data Capture
5.2.2.7 Data Transfer
5.3 Optical Hardware

### 5.3.1 Laser Beam Production

### 5.3.2 Beam Expansion

### 5.3.3 Image Focusing and Sample Length

5.4 Instrument Framework
5.4.1 Introduction

### 5.4.2 Framework

### 5.4.3 Adjustment Mechanisms

5.4.3.1 Angle of Incidence
5.4.3.2 Object Position / Alignment
5.4.3.3 Image Focusing
5.4.3.4 Image Alignment
5.4.4 Dark-housing
5.5 Data Capture Software

### 5.5.1 Microcomputer Access to Auxiliary RAM

5.5.2 Optimum Photodiode Integration Period
5.6 Data Analysis Software
5.6.1 Fourier Transforms
5.6.1.1 Waveforms
5.6.1.2 Fourier Series
5.6.1.3 Discrete Spectra from Fourier Series
5.6.1.4 Spectral Diagrams
5.6.1.5 Non-periodic Waveforms.
5.6.1.6 Fourier Series to Fourier Integral
5.6.1.7 Frequency Domain Diagrams
5.6.1.8 Transforming Periodic Waveforms
5.6.1.9 Numerical Evaluation of Transform
5.6.2 Discrete Fourier Transforms
5.6.3 Fast Fourier Transforms
5.6.4 FFT Algorithm
5.6.5 Validating the FFT Algorithm

### 5.1 Introduction / General Description

The development of the post-process instrument was effected under three main headings:-

1) Hardware
2) Framework
3) Software
4) The hardware consisted of:-
(a) Host Computer - general purpose microcomputer (BBC Master Series) which, under program control, communicated with the electronic circuitry of the laser instrument, capturing, storing and analysing data samples.
(b) Laser Instrument Electronic Circuitry - photodiode array and peripheral array drivers, amplifier circuits, Analogue to Digital Converter (ADC), Auxiliary Memory, up-down counters, clocking circuits, sample-and hold circuits, power supplies, etc.
(c) Laser Instrument Optics - laser beam source and power supply, laser beam expander, image focusing lenses, etc.
5) The framework consists of:-
(a) A fabricated structure which supported the photodiode array, timber samples, laser light source and focusing lens in fixed, mutually orthogonal positions, and, associated adjustment and alignment mechanisms.
6) The software consists of:-
(a) Data Capture from Laser Instrument - calculation of appropriate photodiode integration period between start pulses, start pulse generation, the retrieval and storage of sampled surface data.
(b) Data Analysis - the Fast Fourier transformation (FFTs) of captured surface data to the frequency domain, the correlation/comparison of known surface defects with corresponding FFT results, the displaying of frequency signatures.

This chapter details the development of the laser, surface assessment, instrument.

Section 5.2 deals with the electronic hardware. The applicable electronic parts and functions of the host computer are described (Section 5.2.1), followed by a description of the photodiode array circuitry with which it interfaces (Section 5.2.2).

Details of the optical hardware - laser beam production, beam expansion, image focusing - are then given (Section 5.3).

Section 5.4 introduces the design of the framework and adjustment mechanisms associated with the laser instrument.

Section 5.5 deals with the software which controlled the laser instrument during the capture of data from the timber surface.

Section 5.6 describes the development of the software used in the Fourier analysis of the data.

### 5.2 Electronic Hardware.

The complete electronic hardware for the laser instrument is shown schematically in figure 5.1.1; for complete circuit diagram see Appendix C1. This section discusses the operation of the major elements of the electronic circuitry .

### 5.2.1 The Host Computer.

### 5.2.1.1 General Description.

The host computer used was a BBC Master Series general purpose microcomputer; its hardware consists of a large number of integrated circuits and various electronic components.

The general lay-out of the computer is shown in block diagram form in figure 5.2.1. At the centre of the system is the 6502 central processing unit (CPU). This chip executes all the programs, arithmetic and logical functions. It is connected to the rest of the system via three buses; the data bus, the address bus and the control bus. In figure 5.2 .1 a bus is represented by double lines terminated by arrows at each major block and is simply electrical links connected in parallel to several devices.

Normally one of these devices is talking to another device on the bus. The communication protocols which enable data transfer to take place are set up by the control, address and data buses. The address bus has 16 separate lines hence the maximum amount of directly addressable memory on a 6502 CPU chip is 65536 bytes; the address bus is unidirectional because the 6502

CPU can only supply (not receive) addresses. The data bus has 8 lines so any number between 0 and 255 can be transferred across it. Communication between the peripherals, memory and the CPU occurs over the data bus; data transfer is bidirectional

In order to control the direction of data flow on the data bus a READ or WRITE signal is provided by the control bus. Thus, hardware connected to the system can determine whether it is being sent data, or, is meant to send data back to the 6502 CPU.

The other major control bus functions are those of providing a clock, interrupts and resets. The clock signal synchronises all the chips. The RESET line allows all the hardware to be initialised to some predefined state after reset. The interrupt is a signal sent from a peripheral to the 6502 CPU requesting some form of servicing. There are two types of interrupts; maskable (IRQ) and non-maskable (NMI). The 6502 CPU can ignore a maskable interrupt under software control; a non-maskable interrupt can never be ignored.

When power is first applied to the system, a reset is generated to ensure that all devices start up in there reset states. The 6502 CPU then starts to get instructions from the MOS ROM (machine operating system read only memory) which direct the 6502 CPU's activity. A variety of functions exist, enabling reading or writing of data to memory or to an input/output device or performing arithmetic and logical operations on the data. Once entered,
the MOS (machine operating system) program gains full control of the system.

### 5.2.1.2 Versatile Interface Adapter

(Refer to figure 5.2.1 and figure 5.2.2)
There are two 6522 Versatile Interface Adapters (VIA's) inside the BBC microcomputer. One is dedicated to the MOS and controls the keyboard, sound, speech, etc., while the other drives the parallel printer port and the user port. (The user port being the interface employed to link the BBC master to the laser instrument's electronic hardware.)

Each VIA is housed in a 40 pin package (figure 5.2.2) and contains two fully programable bidirectional 8-bit input/output ports (port A and port B) each with its own handshaking capability. There are two 16 -bit programmable timer/counters, a serial/parallel or parallel/serial shift register and latched input/output registers.

On port A 8 lines (PA0 to PA7) can be individually programmed as inputs or outputs under the control of the Data Direction Register A (DDRA). The logic level on the output pins is controlled by an Output Register A (ORA) and the input data can be latched into an internal register under control of the CA1 line. These various modes of operation are controlled via internal function control registers, the peripheral control register (PCR) and the auxiliary control register (ACR), which are programmed by the 6502 CPU.

The 8 bidirectional port B lines (PB0 to PB7) are controlled by an output register (ORB) and a data direction register (DDRB) in a similar way to port A. The logic level of the PB7 output signal can also be controlled by one of the interval timers. The second timer can be programmed to count pulses on the PB6 input.

The port B control lines (CB1 and CB2) act as interrupt inputs, or, as handshake outputs (similar to port A). Each line controls an interrupt flag in the interrupt flag register (IFR) with a corresponding interrupt enable bit in the interrupt enable register (IER). The control lines can also be programmed to act as a serial port under the control of the shift register.

## Operation of Port A and Port B

There are two data direction registers, DDRA and DDRB, which specify whether the peripheral pins are to operate as input or outputs. Placing a " 0 " in a bit of a DDR will cause the corresponding bit of that port to be defined as an input; a "1" defines it as an output.

Each of the port's input/output pins is controlled by a bit in an output register (ORA or ORB) and an input register (IRA or IRB). When configured as an output, a port line will be reflect the status of the corresponding bit in the output register. If the line is defined as an input, writing data to its output register will have no effect. Reading a port will cause the content of the input register (IRA or IRB) to be transferred onto the data bus.

## Handshaking Data Transfer

The 6522 VIA allows data transfers between two asynchronous devices (in this case between the 6502 CPU and peripheral devices) through the operation of "handshake" lines. The port A lines, CA1 and CA2, handshake data on both "read" and "write" operations; port B lines, CB1 and CB2, handshake on the "write" operation only.

The "read" handshaking operates with "data ready" and "data taken" signals. The peripheral device must generate the "data ready" signal to the 6502 CPU, signifying that valid data is present on the peripheral port. This signal interrupts the 6502 CPU which then reads the data, causing the creation of a "data taken" signal. The peripheral device responds by making new data available. This process continues until the data transfer is complete (timing diagram figure 5.2.3). The "write" handshaking also operates with "data ready" and "data taken" signals. The 6522 VIA provides the "data ready" (CA2 or CB2) signal and accepts the "data taken" (CA1 or CB1) signal from a peripheral device. The "data taken" signal sets the interrupt flag and clears the "data ready" output (timing diagram figure 5.2.4). Selection of the operating modes for CA1, CA2, CB1 and CB2 is controlled by the PCR.

## Timer Operation

Timer 1 consists of two 8 bit latches and a 16 bit counter. When it is loaded the counter decrements at the system clock rate $(1 \mathrm{MHz})$ until it reaches zero. On reaching zero, if enabled, the interrupt flag will be set and an interrupt will be requested of the 6502 CPU . The timer then disables any further
interrupts, or, automatically transfers the contents of the latches to the counter and continues to decrement.

## Interrupt Operation

Interrupt flags are set either by an interrupt in the chip (eg. Timer reaching zero) or an interrupt condition on an input to the chip (eg. handshake data transfer).

The interrupt flags remain in the set condition until the interrupt has been serviced. The source of the interrupt can be ascertained by reading the interrupt flags in order - from highest priority to lowest priority. This can be done by reading the interrupt flag register into the 6502 CPU's accumulator, shifting right (or left) and using conditional branch instructions to detect an active interrupt.

### 5.2.2 Linear Photodiode Array.

### 5.2.2.1 General description.

The linear photodiode is enclosed in an integrated type package with a ground and polished glass window. The device consists of a row of 1024 silicon photodiodes ( $25 \mu \mathrm{~m}$ centre-to-centre spacing), each has an associated storage capacitor on with which to integrate photocurrent, and a multiplex switch for periodic readout via a shift register scanning circuit. A shift register clock driver is also integrated so that only a single Transistor Transistor Logic (TTL) clock is required for scanning. A row of dummy diodes is read out differentially with the photodiode to allow cancellation of the multiplex switching transients, providing a clean video signal.

The sensing elements are diffused p-n junctions (see Appendix B3) for high quantum efficiency and full silicon spectral response. Light incident on the photodiodes is converted to an electrical charge which is integrated and stored on the photodiode capacitance until readout.

### 5.2.2.2 Photodiode Array Circuit.

A circuit diagram of the linear photodiode array is shown in figure 5.2.5. Each cell consists of a photodiode and dummy photodiode, both with associated storage capacitance. These photodiodes are connected through Metal Oxide Semiconductor (MOS) multiplex switches to video and dummy recharge lines, which are common to all the cells. The switches are sequentially closed for one clock period by the shift register scanning circuit, thereby recharging each cell to -5 volts and storing about 3 pC on its capacitor.

The scanning circuit is driven by a single phase TTL clock with a periodic TTL start pulse introduced to initiate each scan. The cell-to-cell sampling rate is the clock frequency, and the total time between scans is the interval between start pulses

During the period between start pulses the charge on each photodiode is gradually removed by photocurrent; the photocurrent being a product of photodiode sensitivity and incident light intensity. The total charge removed from each cell is the product of the photocurrent and the period between start pulses. This charge has to be replaced through the video recharge gate, when the photodiode is sampled and reset, once each scan.

As well as the signal charge, switching transients are capacitively coupled to the video line by the multiplex switches. The same switching transients are introduced to the dummy line and therefore can be removed from the signal by reading the video lines differentially (common mode rejection).

### 5.2.2.3 Sensor Geometry.

In the photodiode array, the light sensing area is a long, narrow, rectangular region covered by an opaque mask. Bar shaped photodiodes extend across the region and are connected to the storage capacitors and multiplex switches buried under the mask. The entire aperture is photo-sensitive; photocurrent generated by light incident between the photodiodes is collected by the nearest photodiode. Figure 5.2 .6 shows the aperture geometry along with an idealized response function which would be obtained by scanning a point
source of visible light along the length of the aperture. Figure 5.2 .7 shows the relative spectral response as a function of wavelength and a plot of charge output versus exposure is shown in figure 5.2.8

### 5.2.2.4 Drive Requirements.

The photodiode array require two power supplies; +5 volts and -15 volts (figure 5.2.9). The ARRAY-CLOCK, RESET (ie. recharge) and START timing signals were TTL signals supplied by external circuitry:

The ARRAY-CLOCK signal was generated by a 9602 multivibrator -the ARRAY-CLOCK signal was also used to drive the SAMPLE-PULSE delay circuit which in turn drove a SHUNT-PULSE pulse generator which supplied the recharge gate of the array with the RESET (or recharge) pulse (figure 5.1.1).

The START signal was initiated by the data capture algorithm stored in the BBC microcomputer; this was synchronised with the negative a going edge of the of the ARRAY-CLOCK, using a start synchronisation circuit that also ensured that the START pulse enveloped only one positive transition of the ARRAY-CLOCK pulse.

### 5.2.2.5 Signal Extraction

The video output is a train of 1024 charge pulses flowing into the video recharge and dummy recharge line capacitances during each scan, with timing as shown in figure 5.2.10. The pulses on the dummy line contained switching transients only; those on the video line contained switching transients plus the video signal. The video and dummy lines were amplified differentially to extract a "noise-free" signal (figure 5.2.11)

Immediately after the multiplex switch is closed to sample the photodiode, the voltage change on the video line is sensed through the buffer amplifier, and sampled and held. The recharge gate is then pulsed negative to reset the video line before the next photodiode is sampled. This results in a sampled and held boxcar video signal (figure 5.2.12).

An output pulse (END-OF-SCAN) is provided by the photodiode array when the penultimate diode is sampled by the shift register scanning circuit.

### 5.2.2.6 Data Capture.

The END-OF-SCAN pulse from the photodiode array is used in conjunction with the START pulse to produce a BLANK-OUT pulse, which indicates the period during which the diodes are being scanned.

Each time a photodiode is sampled and held, the signal is digitised using a very fast ( 15 MHz sampling rate, 66 ns conversion) Analogue to Digital Converter (ADC), and stored in an Auxiliary Random Access Memory (RAM) chip. This was achieved by appropriately manipulating and applying the ARRAY-CLOCK and BLANK-OUT timing signals to the ADC and auxiliary RAM chips (figure 5.1.1 and 5.2.13).

When BLANK-OUT is LOW this indicates that the photodiodes are being sampled, so this signal was used to enable the $A D C$. When the $A D C$ is enabled the ARRAY-CLOCK synchronizes its analogue-to-digital conversions;
the rising edge of the ARRAY-CLOCK latches the data sample while the falling edge shifts the digitised data to the ADC's output register, ready for storage in the Auxiliary RAM.

Both WRITE-ENABLE and OUTPUT-ENABLE pins on the Auxiliary RAM are ACTIVE-LOW. Thus, the BLANK-OUT signal is inverted and NANDed with the ARRAY-CLOCK before connecting to the WRITE-ENABLE pin of the Auxiliary RAM. This ensures that the Auxiliary RAM is written to and read from when appropriate. A ripple through UP-DOWN counter specifies which memory address is being read from or written to; the BLANK-OUT line is connected to the UP-DOWN pin so that when the memory is being written to, the address is incremented and when read from, the address is decremented.

### 5.2.2.7 Data Transfer

The UP-DOWN counter is triggered by either the ARRAY-CLOCK or the User Interrupt Service Routine ("BBC-CLOCK"). The ARRAY-CLOCK and the BBC-CLOCK are gated so as to be mutually exclusive; at any one time either the ARRAY-CLOCK, or the BBC-CLOCK is clocking the counter.

An algorithm (interrupt service routine, see appendix A5.3) in the BBC microcomputer monitored the BLANK-OUT signal which indicated the end of data capture. When the BLANK-OUT signal went LOW, the contents of the Auxiliary RAM were copied/transferred into the microcomputer's memory for future analysis. This analysis took the form of either, predicting an optimum photodiode integration period (Section 5.2.2.6 and 5.5.2), or,
converting of the captured data from the time domain to the frequency domain (Section 5.6).

### 5.3 Optical Hardware

### 5.3.1 Laser Beam Production

Details of the low-power, Helium-Neon laser used for timber illumination are given on the manufacturer's data sheets in Appendix B1. Appendix B2 explains the process of producing monochromatic (laser) light.

Monochromatic light was used, as opposed to white light, because it precludes the problem of chromatic aberrations which would otherwise be evident when the optical lenses are employed for beam expansion, image-gathering and focusing.

### 5.3.2 Beam Expansion.

The diameter of the beam emitted by the laser is only 1 mm . This poses two potential problems; one relates to the post-process instrument, while the other concerns its in-process operation:
(1) With the post-process instrument, the $5: 1$ reduction (i.e. object to image) of the 1 mm laser beam would necessitate critically precise sample-length-image and photodiode-array alignment (the image would be only 0.2 mm wide). This implies sophisticated design of lens holders and adjustment mechanisms, and, accurate tolerancing of their component parts.
(2) With the in-process measurement, the amplitude of the vibration present could render such a small beam - directed at grazing incidence - inadequate for continuous and consistent surface illumination.

To alleviate both these potential problems a beam with a considerably larger diameter was required. This meant optically expanding the 1 mm laser beam to an appropriate size. A 1:14 beam expander was designed, using thin lens theory, manufactured and fitted to the ( 1 mm diameter beam) Helium-Neon laser (figure 5.3.1).

## ASIDE:

Thin lens theory is based on the premise that the lens is of negligible thickness and can therefore be treated as two refracting surfaces, both of which act on the ray and both of which are at the same point in space. Based on these assumptions the following expression, known as the Lensmaker's Equation, can be derived which relate the focal length of a lens to corresponding object and image distances:

$$
\begin{equation*}
\frac{1}{f}=\frac{1}{S_{0}}+\frac{1}{S_{1}} \tag{5.3.1}
\end{equation*}
$$

$$
\begin{array}{ll}
\text { where } & \mathbf{S}_{\mathbf{o}}=\text { object distance } \\
& \mathbf{S}_{\mathbf{1}}=\text { image distance } \\
& \mathbf{f}=\text { focal length of lens }
\end{array}
$$

(These are more clearly defined in figure 5.3.2)
The sign convention used is:-
All distances are measured to the optical centre, C.
Distances are positive if actually traversed by the light ray (distances to real objects and images).
Distances are negative if only apparently traversed by the light ray (distances to virtual objects and images).

Transverse magnification, $\mathbf{m}$, is defined by

$$
\begin{equation*}
\mathrm{m}=\frac{\text { height of transverse image }}{\text { height of transverse object }} \tag{5.3.2a}
\end{equation*}
$$

therefore

$$
\begin{equation*}
\mathrm{m}=\frac{\mathbf{I M}}{\mathbf{O B}} \tag{5.3.2b}
\end{equation*}
$$

The two lenses were chosen in designing the beam expander; the first was a plano-convex lens, used to diverge the laser beam; the second was a double convex to converge the diverging rays onto a path which is parallel to the optic axis.

The focal length of the respective lenses were chosen as follows:
Refer to figure 5.3.3. The diverging lens is at point O and the converging lens is at point I . With reference to the diverging lens, the incoming laser beam, LB, is parallel (ie. object at infinity) causing a virtual image to be formed at its focal point, V , ie. at focal distance $\mathbf{f}_{\mathrm{d}}$ in front of the diverging lens. In order that the converging lens emit rays which are parallel to the optic axis, the corresponding image has to be coincident with its focal point. The virtual image of the diverging lens (point V ) is thus the object for the converging lens and is at focal distance $f_{c}$ in front of the converging lens.

By similar triangles

$$
\frac{\mathbf{f}_{\mathrm{d}}}{\mathbf{O B}}=\frac{\mathbf{f}_{\mathrm{c}}}{\mathbf{I M}}
$$

Now $\mathbf{O B}=1 \mathrm{~mm}$, and, $\mathbf{I M}=14 \mathrm{~mm}$, so

$$
\frac{f_{d}}{1}=\frac{f_{c}}{14}
$$

giving

$$
\begin{equation*}
f_{c}=14 f_{d} \tag{5.3.3}
\end{equation*}
$$

Thus lenses were selected having appropriate diameters and focal lengths as specified above. A cylindrical mechanism was designed which held the two lenses in position and provided fine focusing (see figure 5.3.1).

### 5.3.3 Image Focusing and Sample Length.

Contacts within the woodworking industry (Goddard M, 1985) have indicated that a 125 mm sample length would be adequate for the purpose of surface
analysis in terms of its frequency/harmonic content. This was supported by the following reasoning:

The distance, $L$, traversed by the timber travelling at constant linear velocity, $\mathbf{V}$, during one revolution of the cutterhead that is rotating at angular velocity, $\mathbf{W}$, is given by

$$
L=\frac{V}{(2 \pi / W)}
$$

The maximum possible distance, $\mathbf{L}_{\text {max }}$, traversed during one revolution of the cutterhead then given by

$$
\begin{equation*}
\mathbf{L}_{\max }=\frac{\mathbf{V}_{\max }}{\left(2 \pi / \mathbf{W}_{\min }\right)} \tag{5.3.4}
\end{equation*}
$$

Currently, $V_{\text {max }}=150 \mathrm{~m} / \mathrm{min}$ and $W_{\text {min }}=1500 \mathrm{rpm}$, so

$$
\mathbf{L}_{\max }=\frac{(150 / 60)(2 \pi)}{(15000.2 \pi / 60)}=100 \mathrm{~mm}
$$

Thus, erring on the side of caution, 125 mm was adopted as the fundamental sample length.

This necessitated the optical reduction of a 125 mm -long object (the illuminated timber) to a 25 mm long image, which must be focused onto the 25 mm long glass window of the photodiode array. Figure 5.3 .4 shows the optical arrangement.

The appropriate lens was chosen using the restrictions in the Lensmaker's Equation (equation 5.3.1). Refer to figure 5.3.4: by similar triangles

$$
\frac{\mathrm{IM}}{\mathrm{IC}}=\frac{\mathrm{OB}}{\mathrm{OC}}
$$

therefore

$$
\begin{equation*}
\frac{I M}{O B}=\frac{I C}{O C} \tag{5.3.5}
\end{equation*}
$$

Hence from equation 5.3.2

$$
\mathrm{m}=\frac{\mathrm{IC}}{\mathrm{OC}}
$$

hence

$$
\begin{equation*}
\mathbf{m}=\frac{\mathbf{S}_{\mathbf{S}}}{\mathbf{S}_{\mathbf{o}}} \tag{5.3.6}
\end{equation*}
$$

Now

$$
\mathbf{I M}=25 \mathrm{~mm}
$$

and

$$
\mathrm{OB}=125 \mathrm{~mm}
$$

therefore substituting in equation 5.3.2b gives

$$
\begin{equation*}
m=\frac{1}{5} \tag{5.3.7}
\end{equation*}
$$

and substituting equation 5.3.7 in 5.3.6 gives

$$
\begin{equation*}
S_{0}=5 S_{i} \tag{5.3.8}
\end{equation*}
$$

which substituted in equation 5.3 .1 gives

$$
\begin{equation*}
\frac{1}{f}=\frac{1}{5 S_{1}}+\frac{1}{S_{i}} \tag{5.3.9}
\end{equation*}
$$

which gives

$$
\begin{equation*}
f=\frac{6 S_{1}}{5} \tag{5.3.10}
\end{equation*}
$$

Using equation 5.3.10, image distance $S_{1}$ was plotted against lens focal length, f , (figure 5.3 .5 ). Figure 5.3 .5 was used as a guide in the selection of lens system with appropriate focal length and image coverage ( $25 \mathrm{~mm} \times 4 \mathrm{~mm}$ ). The system selected was a projector lens of focal length 50 mm and corresponding image distance, $\mathbf{S}_{\mathbf{i}}$, of 41.7 mm with $35 \mathrm{~mm} \times 23 \mathrm{~mm}$ image coverage. The lens was mounted on a screw thread arrangement to facilitate adequate focusing of the image (figure 5.3.6).

### 5.4 Instrument Framework

### 5.4.1 Introduction

A framework had to be designed to accommodate and support the components which comprised the Laser Instrument. The major criterion was that of:

1) Correct alignment and positioning of the photodiode array, the image focusing lens and machined timber samples.
2) Arranging the datum face, against which the machined face of the timber samples located, so that it was perpendicular to the optical axis of the image focusing lens.
3) Positioning the laser light source so that the grazing angle of incidence, for timber illumination, could be varied, and, aligning the laser beam such that the illuminated surface formed an image which aligned itself to the photodiode array.

### 5.4.2 Framework

A T-shaped framework was designed which supported the timber samples and focusing lens, such that the timber surface and optical axis of the lens were orthogonal (figure 5.4.1).

A clamping device, designed to accommodate varying thicknesses of timber, was built into the framework to securely locate the timber samples during data capture (figure 5.4.2).

### 5.4.3 Adjustment Mechanisms

### 5.4.3.1 Angle of Incidence

A "floating" carriage, located on the left of the timber clamp, was designed to support the helium-neon laser light source. The carriage was free to rotate in the horizontal plane (figure 5.4.3), thus allowing variation in the angle of incidence of the laser beam. The angle of incidence was controlled by a micrometer-spring mechanism (figure 5.4.4); Table 1 shows a look-up chart of micrometer reading versus angle of incidence.

### 5.4.3.2 Object Position / Alignment

The vertical position of the laser light source could be controlled by adjusting the length of the three legs that supported it. This in effect governed the vertical position of the "horizontal" beam and hence the vertical position of timber illumination (ie. the Object of the focusing lens). The length of the single leg, relative to that of the other pair, was used to control the yaw of the beam.

### 5.4.3.3 Image Focusing

The image focusing lens was arranged to have a course and fine focus adjustment. The course focus was effected by slot and clamp arrangement; the lens support could be positioned and clamped anywhere along the slot (figure 5.3.6). The fine focus was achieved by use of a screw thread; the male screw thread on the lens holder was used to fine-adjust the horizontal position of the lens and hence the fine-focus of the image.

### 5.4.3.4 Image Alignment

The same slot used for the course focus of the image focusing lens was used to locate and clamp the support to which the photodiode array was attached. The vertical position (alignment) of the array could be adjusted by use of a screw thread arrangement (figure 5.4.5).

### 5.4.4 Dark-housing / Canopy

A dark-housing/canopy was designed to exclude ambient light and allow access for adjustments and changing of timber samples (figure 5.4.6).

### 5.5 Data Capture Software

To obtain a data set that represent the reflected light intensities from the planed timber, two start pulses must be sent to the photodiode array. The time interval between these start pulses (the integration period) determines the magnitude of the voltage signals received from each photodiode in the array (the total output from each cell being the product of the photo current and the integration period); for example, let a timber sample being assessed reflect a light intensity pattern which covers the full length of the photodiode array; let the maximum intensity of the reflected light falling on the photodiode array impinges, say, photodiode number 7, and the output voltage from photodiode 7 , for an integration period of 5 ms , be 0.5 volts. A reduction in the integration period would result in a proportionally reduced voltage output on photodiode 7, whereas an increase in integration period would result in a proportionally increased voltage signal.

The integration period is controlled by the "Data Capture" algorithm (appendix A5.1). The design philosophy applied to this algorithm exploits automatic gain control; the criterion being, the maximising of the signal, with a view to optimising the resolution of the ADC. Thus every data set captured has the same maximum, however, the relative magnitude of the other points in the set, to this maximum, would differ from timber sample to timber sample. The process of data capture can be divided into two sections:-
a) Host computer's access to data stored in the Auxiliary RAM.
b) Computing the Optimum photodiode Integration Period.

### 5.5.1 Host Computer's Access to Auxiliary RAM

On receiving a start pulse the array is scanned, ie. all the photodiodes are sampled, the corresponding voltages digitised and stored in the Auxiliary RAM.
(Refer to schematic diagram and timing diagram, figures 5.1.1 and 5.2.13). During the scan period the BLANK-OUT line is HIGH. This line was connected to the BBC microcomputer's user port and caused an interrupt when a positive edge was detected.

The Interrupt Service Routine (Appendix A5.3) started at the label "int" and ended at the label "oldv" and its structure was as follows:-

WHILE Interrupt Request Flag Set DO<br>Save All Registers On Processor Stack<br>Check if Interrupt is from photodiode array Circuit<br>IF Array Circuit Interrupted<br>THEN<br>Copy Data from Aux. RAM to Host micros RAM<br>ELSE<br>Recover Registers From stack<br>END IF<br>Hand back control to micros Operating System<br>(Or continue Interrupt Polling)

While the array is being scanned, the counter (used as a memory location pointer) counts UP under the influence of the array's clock. At the end of the scan BLANK-OUT goes HIGH putting the counter into the DOWN mode. Decrementing the counter is effected by the User Interrupt Service Routine, which sends pulses to the counter by writing ZEROs and ONEs to the
appropriate lines on the User Port; the contents of the Auxiliary RAM are copied into the host computer's memory.

### 5.5.2 Optimum Photodiode Integration Period.

As stated above, the desired integration period for the photodiode array should be such that the maximum magnitude output signal is obtained. This was achieved by monitoring the array element on which light of highest intensity was incident and adjusting the integration period until maximum (saturation) voltage was attained.

Improvement in the estimation of the integration period was accomplished using piecewise linear approximation. Refer to figure 5.5.1a. Remembering that, as stated in the Section 5.2.2.2, the charges on the capacitors of the photodiode array are removed by photocurrent and that photodiodes only operate under negative-bias conditions, the initial (maximum) voltage on the capacitors would be zero, and saturation would occur at some negative voltage, -V . Figure 5.5 .1 b shows the general case of figure 5.5.1a.
where
$\mathbf{X}_{0}$ is the initial voltage (capacitor fully charged)
$\mathbf{X}_{1}$ is the voltage after integration period ( $\mathbf{T}_{1}-\mathbf{T}_{0}$ ).
Using similar triangles (see figure 5.5.1a), the integration period, C, for saturation can be estimated thus:-

$$
\begin{equation*}
\frac{\mathbf{A B}}{\mathbf{B F}}=\frac{\mathrm{FD}}{\mathbf{D E}} \tag{5.3.11}
\end{equation*}
$$

i.e.

$$
\begin{equation*}
\frac{\mathbf{X}_{0} \cdot \mathbf{X}}{T_{1}-T_{0}}=\frac{\mathbf{X}_{0}-V}{\mathbf{d t}} \tag{5.3.12}
\end{equation*}
$$

therefore,

$$
\begin{equation*}
d t=\frac{\left(\mathbf{X}_{i}-V\right)}{\left(\mathbf{X}_{0} \cdot \mathbf{X}_{i}\right)} \cdot\left(\mathbf{T}_{i}-T_{0}\right) \tag{5.3.13}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathbf{C}=\mathbf{T}_{c}-\mathbf{T}_{\boldsymbol{o}} \tag{5.3.14}
\end{equation*}
$$

therefore

$$
\begin{equation*}
C=T_{i} \cdot T_{0}+d t \tag{5.3.15}
\end{equation*}
$$

Therefore the prediction is that an integration period of $C\left(=\mathbf{T}_{\mathbf{i}}-\mathbf{T}_{\mathbf{0}}+\mathrm{dt}\right)$ seconds will achieve saturation voltage, $V$.

The data capture algorithm which was written (see Appendix A5.1) utilises the above equations iteratively to calculate the optimum integration period. In the algorithm:-
$\mathbf{X i}=$ max. negative sample in Aux. RAM after latest scan.
$\mathbf{X o}_{\mathbf{o}}=$ max. negative sample from penultimate scan
$\mathbf{V}=$ required maximum signal.
A FOR - NEXT loop timed out the integration period
The code labelled "start" is an assembly-code sub-routine which sends the start pulse to the array.

The structure of the computer algorithm which calculates the optimum integration period is as follows:-

## START. REPEAT. <br> Calculate new estimate of integration period. Send start pulse. <br> Time out estimated integration period. <br> Send start pulse. <br> Wait for Aux. RAM to be filled with latest data. <br> UNTIL peak signal is equal to maximum. <br> Plot data on screen. <br> END.

The algorithm uses an iterative process (REPEAT-UNTIL loop) to improve the estimation of the optimum integration period until the signal is within a given tolerance of the required maximum.

### 5.6 Data Analysis Software

When captured the data was to be analyzed; other research (Mulvaney D.J, Newland D.E, 1986) has indicated that, of the orthogonal transforms commonly used in engineering, Fourier transforms (FT's) are admirably suitable for surface analysis because of their precision and their rapid rates of convergence. What follows outlines the theory, and derivation, of Discrete Fourier transforms (DFT's) and Fast Fourier transforms (FFT"s); it shows the way in which an FFT algorithm was designed and tailored for the analysis of the data captured from the timber samples.

### 5.6.1 Fourier Transforms

### 5.6.1.1 Waveforms

To fully describe a waveform in time, values must be to assign at various points and there must be enough points of the waveform displayed in order to discern its shape or its type.

For example, if the sinusoid, shown in figure 5.6 .1 (which was captured by a cathode ray oscilloscope with a time-base setting of 1 ms ) was captured using a setting of only 0.01 ms per division, this would stretch the first tenth of the time division to cover the entire display; the waveform would thus appear to be a ramp instead of a sinusoid.

Once a waveform is completely described with respect to time, it is possible to construct a new description of it with respect to frequency. An example of this, for a sinusoid, is shown in figure 5.6.2, which depicts a
three-dimensional waveform space with amplitude as the vertical axis and time and frequency on the other two axes. The time-axis and amplitude-axis define a domain called the "time-plane", while the amplitude-axis and frequency-axis define the "frequency-plane"; the time and frequency planes (or domain) are orthogonal.

The time history of a sinusoid, such as that shown in figure 5.6.1, can be viewed as a projection on the time-plane. In concept, the sinusoid can be thought of as actually existing some distance from the time-plane; this distance is measured along the frequency axis and is equal to the reciprocal of the waveform's period. Similarly, the sinusoid also has a projection onto the frequency-plane; this projection takes the form of an impulse; the magnitude of this impulse is equal to the sinusoids amplitude. The position of the impulse coincides with the frequency of the sinusoid.

The single impulse in the magnitude diagram defines both the amplitude and frequency of the sinusoid. Although this information is sufficient to reconstruct the sinusoid in the time-domain, some additional information, phase, is needed in order to locate its position relative to the zero time reference.

This phase information is also represented in a phase diagram; this consists of an impulse located on a frequency axis, the amplitude of which is indicative of the phase associated with the sinusoid. The phase diagrams can be determined by locating the positive peak which is closest to time zero. Delay
is denoted by negative phase and advance by positive phase.

Using the type of description conventions developed above it is possible to build a variety of non-sinusoidal waveforms. For example, consider two sinusoids, one of frequency $F_{0}$ and phase - 90 degrees, the other of frequency $2 \mathrm{~F}_{\mathrm{o}}$ and phase -45 degrees; the amplitude of the first being twice that of the second. The first sinusoid is completely described (using the frequency description) in figure 5.6.3a, the second in figure 5.6.3b. The sum of the two sinusoids is shown in figure 5.6.3c.

For the complete picture figure 5.6 .3 can be redrawn in three dimensions as shown in figure 5.6 .4 where the concept of projecting onto the time plane and frequency plane is employed; here the idea of summing multiple or time-domain projections is introduced. The projections onto the time-domain is shown in dotted lines, their sum being indicated by a heavy solid line.

The technique of adding sinusoids can be continued so that various shaped projections onto the time-domain can be obtained. Each shape or waveform is characterised by a unique combination of sinusoids. If any one of the sinusoids is changed in frequency, amplitude or phase, the waveform's time-domain projection changes.

Most waveforms are measured in the time-domain; time-based measurements have historical precedence and are the most familiar data format. Time histories, however, only reveal limited information. Without a direct look at
the frequency-domain, waveshape changes are only an indication that some frequency component has been modified. There is a rule of thumb - that fast rise times indicate high frequencies - but this is a rather limited, non-specific tool for waveform analysis.

A more complete approach to getting frequency-domain information is to apply the rigorous mathematical technique known as Fourier analysis. This allows a time-domain waveform to be described in terms of both frequency-domain magnitude and phase. Fourier analysis also offers the option of results in rectangular form, which consists of real and imaginary parts of the complex frequency-domain.

However, the classical mathematical approach to Fourier analysis is frustrating for all but the simplest waveforms. If the waveform cannot be expressed as an equation, classic Fourier techniques cannot be applied. A waveform can, however, be sampled and digitized with a waveform digitizer; then discrete Fourier transforms (DFT) can be used to Fourier transform the digitized waveform.

FFT algorithms can be implemented through computer software, firmware or hardware. Their major advantage is the speed with which they analyzes large numbers of waveform samples. The following sections detail the background and theory behind the FFT algorithm; first, continuous Fourier theory for un-sampled waveforms is discussed, paving the way for the development of DFT and, subsequently, FFT.

### 5.6.1.2 Fourier Series

The general form of the Fourier series is

$$
\begin{align*}
x(t)= & a_{0}+a_{1} \cdot \operatorname{Cos}(W t)+a_{2} \cdot \operatorname{Cos}(2 W t)+\ldots \ldots \ldots+a_{n} \cdot \operatorname{Cos}(n W t) \\
& b_{0}+b_{1} \cdot \operatorname{Sin}(W t)+b_{2} \cdot \operatorname{Sin}(2 W t)+\ldots \ldots . . .+b_{n} \cdot \operatorname{Sin}(n W t) \tag{5.6.1}
\end{align*}
$$

where $\mathbf{W}=\mathbf{2 \pi f}$ and $\mathbf{f}$ is the fundamental frequency.

If a Fourier series can be written for a waveform then the components of the series completely describe the frequency content of the waveform. For this to be true certain conditions have to be met:

1) The waveform has to be periodic; ie. if the waveform is represented by $\mathbf{x}(t)$ and there is a constant time, $\tau$, that exists such that $\mathbf{x}(t)=\mathbf{x}(t+\tau)$ for all time, $\mathbf{t}$, then $\mathbf{x}(t)$ is periodic with period $\tau$. That is to say, the waveform must repeat itself in time before a Fourier series can exist for it.
2) The Dirichlet conditions must prevail; they are:
(a) If the function has discontinuities, their number must be finite in any period.
(b) The function must contain a finite number of maxima and minima during any period.
(c) The function must be absolutely integrable in any period; that is

$$
\int_{0}^{\tau}|x(t)| d t<\infty
$$

where $\mathbf{x}(\mathbf{t})$ describes the function.

There are obviously some theoretical functions for which a Fourier series does
not exist. For all practical purposes, however, the Dirichlet conditions are met when a periodic function accurately describes a physical occurrence.

### 5.6.1.3 Discrete Spectra from Fourier Series.

The Fourier Series (equation 5.6.1) can be written more concisely as

$$
\begin{equation*}
x(t)=a_{o}+\sum_{n=1}^{\infty}\left(a_{n} \cdot \operatorname{Cos}(n W t)+b_{n} \cdot \operatorname{Sin}(n W t)\right) \tag{5.6.2}
\end{equation*}
$$

The Fourier series for a specific waveform is written by using the salient features of the waveform to find specific values for the coefficients in equation 5.6.2. The frequency, $W$, is found from the period of $\mathbf{x}(t)$ and is equal to $2 \pi / \tau$ (also $W=2 \pi f$ where $f=1 / \tau$ ). The coefficient, $a_{0}$, equal to the average value of $\mathbf{x}(\mathbf{t})$ over one period, is determined by

$$
\begin{equation*}
a_{0}=\frac{1}{\tau} \int_{0}^{\tau} x(t) d t \tag{5.6.3}
\end{equation*}
$$

The remaining coefficients $\mathbf{a}_{\mathbf{n}}$ and $\mathbf{b}_{\mathbf{n}}$ are evaluated for $\mathrm{n}=1,2,3, .$. by

$$
\begin{equation*}
a_{n}=\frac{2}{\tau} \int_{0}^{\int} x(t) \operatorname{Cos}(n W t) d t \tag{5.6.4}
\end{equation*}
$$

and

$$
\begin{equation*}
b_{n}=\frac{2}{\tau} \int_{0}^{\tau} x(t) \operatorname{Sin}(n W t) d t \tag{5.6.5}
\end{equation*}
$$

For example, the Fourier coefficient for the square wave shown in figure 5.6.5 has been evaluated to give the following series:

$$
\begin{align*}
& x(t)=\frac{4 V}{\pi}[\operatorname{Cos}(W t)-1 / 3 \operatorname{Cos}(3 W t) \\
&+1 / 5 \operatorname{Cos}(5 W t)-\ldots . .] \tag{5.6.6}
\end{align*}
$$

where $\mathbf{W}=\mathbf{2 \pi f}$.

The term $4 / \pi$ is a constant resulting from the integration and $V$ is the peak value of the square waveform.

The above series is a complete description of the frequency content in figure 5.6.5; from it diagrams of both the magnitude spectrum and phase spectrum can be constructed (figure 5.6.6) using the conventions discussed earlier (Section 5.6.1.1).

### 5.6.1.4 Spectral Diagrams.

The spectra of figure 5.6 .6 are referred to as discrete spectra - each component being discretely located on a frequency axis and represented by a single line or impulse. The length of each spectral line indicates either magnitude or phase.

In the case of figure 5.6.6a the line spectrum of the magnitude is constructed from the Fourier series by first plotting the amplitude of the fundamental frequency. (The fundamental frequency is the reciprocal of the waveforms period ( $\mathbf{f}=\mathbf{W} / 2 \pi$ ) and is indicated in the Fourier series by W). The magnitude of the fundamental is given by the first trigonometric term in the series ( $\mathrm{n}=1$ )

For the square wave of figure 5.6 .5 the magnitude of the fundamental is $4 \mathrm{~V} / \pi$.

The diagram of figure 5.6 .6 is constructed by first placing the fundamental spectral line at $\mathbf{f}$ and giving it an amplitude of $\mathbf{4 V} / \pi$. Subsequent Fourier terms are plotted in the same manner.

Each Fourier term is some integer multiple of the fundamental frequency and is referred to as a harmonic. The fundamental is often referred to as the first harmonic because $f_{0}$ is multiplied by one; integer multiples greater than one are always referred to as harmonics. In the case of figure 5.6.6a the square wave is made up of odd harmonics; these are shown with spectral lines of

$$
3 f_{0}, 5 f_{0}, 7 f_{0}, \ldots, n f_{0}
$$

their magnitudes are, respectively,

$$
1 / 3,1 / 5,1 / 7, \ldots, 1 /(2 n-1)
$$

of the fundamental magnitude.

The line spectrum for phase is constructed in a similar manner. There is a corresponding spectral line in the phase diagram for each line in the magnitude diagram and they are positioned on a frequency axis in the same manner, the length of these lines, however are indicative of the phase. In figure 5.6.6b the fundamental and the fifth harmonic are positive cosines and have zero phase; their spectral line length is zero; a heavy dot is used to indicate the presence of zero-phase components. The third and seventh harmonics are negative cosines and consequently have phases of $180^{\circ}$, this is indicated by the length of their spectral lines at $\mathbf{3 f}$ and $\mathbf{7 f}$.

### 5.6.1.5 Non-periodic Waveforms.

The Fourier series is a useful tool for investigating the spectrum of periodic waveforms; unfortunately the signals in the real world are not composed exclusively of periodic waveforms.

The Fourier series and the Fourier integral, as analysis tools, are separate and distinct; the former is intended for use with periodic waveforms while the latter is reserved for non-periodic waveforms. Despite this clear distinction there is a subtle relationship which exists between the two; this relationship is helpful and useful in interpreting results.

### 5.6.1.6 Fourier Series to Fourier Integral.

Establishing the relationship between the Fourier series and the Fourier integral involves four major steps; these steps are briefly outlined below.

## Step 1

The general form of the Fourier series is:

$$
\begin{equation*}
x(t)=a_{0}+\sum_{n=1}^{\infty}\left\{a_{n} \operatorname{Cos}(n W t)+b_{n} \sin (n W t)\right\} \tag{5.6.7}
\end{equation*}
$$

This can be expressed in exponential form, which is more appropriate for developing the integral, by substituting the exponential expression for Cos(nWt) and Sin(nWt). The expressions are:

$$
\begin{equation*}
\operatorname{Cos}(n W t)=\frac{\{\exp (j n W t)+e \exp (-i n W t)\}}{2} \tag{5.6.8}
\end{equation*}
$$

# $\operatorname{Sin}(n W t)=\{\exp (i n W t)-e \exp (-i n W t)\}$ 2j 

where
$\mathbf{e}$ is the base of the natural logarithm
and
$\mathbf{j}$ is the imaginary unit in the complex number system $\{\mathbf{j}=\operatorname{SQR}(-1)\}$

## Step 2

By substituting equations 5.6 .8 and 5.6 .9 in equation 5.6.7, further manipulating and assigning new variables as appropriate, a more compact form of the Fourier series is obtained:

$$
\begin{equation*}
x(t)=\sum_{n=\infty}^{\infty} C_{n} \operatorname{e} \exp (j n W t) \tag{5.6.10}
\end{equation*}
$$

where

$$
\begin{equation*}
C_{n}=\frac{1}{\tau} \int_{-/ 2}^{\tau / 2} x(t) \exp (-j n W t) d t \tag{5.6.11}
\end{equation*}
$$

and is evaluated for $\mathbf{n}=-\infty, \ldots . .2,-1,0,1,2, \ldots .,+\infty$

For each $\mathbf{n}, \mathbf{C}_{\mathbf{n}}$ is evaluated to give the magnitude and phase of the harmonic component of $\mathbf{x}(\mathbf{t})$ having angular frequency $\mathbf{n W}$.

The Fourier series is now in exponential form (equation 5.6.10); the next step involves using the fact that each harmonic is separated by an amount $\Delta \mathrm{f}$, where

$$
\begin{equation*}
\Delta f=\frac{\Delta W}{2 \pi} \tag{5.6.12}
\end{equation*}
$$

## Step 3

Substituting equation 5.6.12 in equation 5.6.10 and manipulating further, the series can be placed into the following form (which allows inspection of the limit as $\tau$ tends to infinity):

$$
\begin{equation*}
x(t)=\lim _{L} \frac{1}{\tau} \sum_{n=} \mathbf{X}(j n W) e \exp (j n W t) \tag{5.6.13}
\end{equation*}
$$

Since $\Delta f=\Delta \mathbf{W} / 2 \pi$, equation 5.6 .13 can be written as

$$
\begin{equation*}
x(t)=\lim _{\Delta W \rightarrow 0} \frac{1}{2 \pi} \sum_{n=-\infty}^{\infty} X(j n W) \exp (j n W t) \Delta W \tag{5.6.14}
\end{equation*}
$$

Step 4
Now, as $\Delta \mathbf{W}$ tends to zero (period $\tau$ tends to infinity), the properties of the summation approaches those of an integral. This reduces the Fourier series to

$$
\begin{equation*}
x(t)=\frac{1}{2 \pi}-\Gamma(\mathrm{x}(\mathrm{~W}) \mathrm{e} \exp (\mathrm{FWt)} \mathrm{dW} \tag{5.6.15}
\end{equation*}
$$

The Fourier coefficients have now become a function of a continuous frequency variable, $\mathbf{W}$, and are given by

$$
\begin{equation*}
\mathbf{x}(j W)=\int_{-} \mathbf{x}(t) \exp (\cdot j W t) d t \tag{5.6.16}
\end{equation*}
$$

Equations 5.6.15 and 5.6.16 are together referred to as the Fourier transform pair. The former (equation 5.6.15) is generally called the inverse Fourier transform and the latter (equation 5.6.16) as the direct Fourier transform (or
simply Fourier transform).

The transform action of the Fourier integral is contrasted with that of the Fourier series in figure 5.6.7; each technique is applied to a different class of waveform and each provides different kind of frequency domain or spectral description. The Fourier series transforms time domain functions to frequency domain magnitudes and phases at specific, discrete frequencies. The Fourier integral, on the other hand, evaluates a continuous function of frequency.

Figure 5.6 .8 shows graphically how the Fourier series (with discrete spectrum) is related to the Fourier integral (with continuous spectrum) by noting what happens to the spectrum as the period (of a pulse train), $\tau$, tends to infinity.

### 5.6.1.7 Frequency Domain Diagrams

Both $\mathbf{X}(\mathbf{j W})$ and $\mathbf{x}(\mathbf{t})$ are defined over frequencies and times from minus infinity to plus infinity. The concept of negative time is intuitive; negative frequency is less so. To illustrate, figure 5.6 .9 shows a sine wave, that is periodic in the time domain from minus infinity to plus infinity, and two pairs of spectral diagrams for this sine wave.

Figure 5.6 .9 b shows the magnitude and phase information that would be obtained by writing the Fourier series for the sine wave. Note that the time domain magnitude, $V$, is reflected exactly in the magnitude spectrum. The
time domain sine wave relative to time zero shows a phase of $-90^{\circ}(-\pi / 2)$; this is shown on the phase diagram.

Figure 5.6.9c describe the sine wave in the frequency domain of the Fourier transform. Note, there are two spectral components - one at the positive frequency of the sine wave and one at its negative frequency. Each magnitude is half that of the time domain waveform (also, half the magnitude of the one in the Fourier series spectrum). The phase for the positive frequency is as for the Fourier series spectrum; $-90^{\circ}(-\pi / 2)$ at $1 / \tau$. Phase in the negative frequency domain is the inverted image of the positive domain; $+90^{\circ}(\pi / 2)$ at $-1 / \tau$.

The frequency domain diagrams of figure 5.6 .9 embody most of the conventions of magnitude and phase descriptions for the Fourier transform's frequency domain. These conventions are:

1) The magnitudes in the positive and negative frequency domain exactly duplicate each other.

For every frequency indicated in the positive domain, one of equal magnitude is indicated at the same frequency in the negative domain; their sum being equal to the amplitude of the corresponding sinusoidal component in the time domain. In the case of DC , its frequency is zero and there is no division of magnitude.
2) Phase in the positive frequency domain is duplicated in negative frequency, except the images are inverted.

This entails a sign change when passing between positive and negative frequencies.

With these conventions established, figure 5.6 .8 d can be redrawn for the Fourier integral's frequency domain; this is done in figure 5.6.10. The time domain pulse is a more generalised version with amplitude, V , and width, $2 \mathrm{~T}_{0}$, centred about time zero (figure 5.6.10a). The frequency domain diagrams are shown in figure 5.6 .10 b and figure 5.6 .10 c .

## ASIDE: Fourier Transform of a Pulse.

The integral for transformation to the frequency domain is

$$
x(j W)=\int_{\ldots}^{m} x(t) e \exp (j W t) d t
$$

For the case of a pulse, $\mathbf{x}(\mathbf{t})$ is zero everywhere except over the interval $-\mathrm{T}_{0}$ to $\mathrm{T}_{0}$ where it has a constant amplitude of $\mathbf{V}$ (figure 5.6.10). Since the Fourier transform of zero is zero, and the function (the pulse) has a constant value during the interval, the integral is reduced to

$$
X(j W)=V \int_{-T_{0}}^{T_{0}} e \exp (j W t) d t
$$

The integral evaluates to

$$
\mathbf{X}(\mathrm{jW})=2 \mathrm{VT}_{0} \frac{\sin \left(\mathrm{WT}_{\mathrm{o}}\right)}{\mathrm{WT}_{0}}+\mathrm{j} 0
$$

which is the Fourier transform in rectangular coordinates. This is a classical frequency domain waveshape description, having a major lobe with decaying side lobes (see figure 5.6.10b), and can be generalised as $(\sin \beta) / \beta$

### 5.6.1.8 Transforming Periodic Waveforms

Fourier transforms do not exist for periodic waveforms. To Fourier transform a periodic waveform, that waveform first has to be windowed ie. multiplied by a pulse (or rectangular window) of unit height.

The actual process of windowing a waveform is shown in figure 5.6.11. A cosine wave and a rectangular window is used. Each step is also shown in the frequency domain so that the effects can be illustrated. For simplicity
phase is ignored and only the frequency domain magnitude is shown.

In figure 5.6.11a an infinite extent cosine wave is shown in the time domain and two spectral components, at $\pm 1 / \tau$, in the frequency domain. Figure 5.6.11b shows a rectangular window in the time domain and its "(sin $\beta) / \beta$ " magnitude in the frequency domain. Multiplying the time domain window and the cosine wave together results in the product shown in figure 5.6.11c. This product is referred to as the rectangularly windowed cosine wave, and the magnitude of its Fourier transform is shown in figure 5.6.11d.

The transformed magnitude of the windowed cosine wave is not the product of the frequency domain functions for the cosine wave and the window (ie. multiplication in the time domain does not correspond to multiplication in the frequency domain).

It can be seen that figure 5.6.11d does exhibit some of the traits of both the cosine wave and the rectangular window:

The " $(\sin \beta) / \beta$ " magnitude of the window appears twice in figure 5.6.11d; once in positive frequency, once in negative frequency. The peaks of the double "(sin $\beta$ )/ $\beta$ " magnitude occur at the frequency $( \pm 1 / \tau)$ of the cosine wave.

The frequency domain spectrum of the cosine wave and the rectangular window have undergone a mathematical process known as convolution (Schwartz M, Shaw L, 1975). Figure 5.6.11d is the result of convolving the cosine wave's frequency domain with the window's frequency domain.

### 5.6.1.9 Numerical Evaluation of Transform.

The Fourier transform a continuous signal, $\mathbf{x}(\mathbf{t})$, is defined by:-

$$
\begin{equation*}
X(j W)=\quad \int_{-\infty}^{+\infty} x(t) e \exp (-j W t) d t \tag{5.6.17}
\end{equation*}
$$

The Fourier transform is an operation that creates from the time function, $\mathbf{x}(\mathbf{t})$, a function, $\mathbf{X}(\mathbf{j W})$, in the frequency domain. Then $\mathbf{X}(\mathbf{j W})$ displays the frequency content of the signal, $x(t)$, as a function of the continuous frequency variable, W.

To use numerical methods to evaluate Fourier transforms, a continuous signal $x(t)$ has to be approximated by discrete sets of values. The zero-order approximation is to assume $\mathbf{x}(\mathbf{t})$ to be constant at $\mathbf{x}(\mathbf{k T})$ for

$$
\mathbf{k T}<=t<(k+1) T
$$

and the integral over this time interval is then approximated by the area of the rectangle (see figure 5.6.12), which is equal to

$$
\mathbf{T} \mathbf{x}(\mathrm{kT})
$$

Hence equation 5.6.17 becomes under numerical approximation

$$
\begin{equation*}
X(j W) \approx \sum_{k=-\infty}^{+\infty} T x\left(t_{k}\right) e \exp \left(-j W t_{k}\right) \tag{5.6.18}
\end{equation*}
$$

where $\mathbf{t}_{\mathbf{k}}=\mathbf{k T}$ and the summation is over an infinite range in general.

In practice the signal duration of, say, NT and can be assumed to start at $t=0$.

Then equation 5.6 .18 becomes

$$
\begin{equation*}
\mathbf{X}(j W) \approx \sum_{k=0}^{N-1} T x\left(t_{k}\right) e \exp \left(-j W t_{k}\right) \tag{5.6.19}
\end{equation*}
$$

This represents the approximate Fourier transform of a finite duration signal. The accuracy depends on the time step; the smaller $\mathbf{T}$ is the better the approximation.

In a similar manner, the inverse Fourier transform integral, defined by

$$
\begin{equation*}
x(t)=\frac{1}{2 \pi} \int X(j W) e \exp (j W t) d W \tag{5.6.20}
\end{equation*}
$$

can be approximated by the summation

$$
\begin{equation*}
\mathbf{x}(t) \approx \frac{\Delta W}{2 \pi} \sum_{n=M}^{M-1} \mathbf{X}(j W) \operatorname{eexp}\left(j W_{n} t\right) \tag{5.6.21}
\end{equation*}
$$

where the signal is assumed to be band limited in frequency to $\mathbf{M} \Delta \mathbf{W}, \Delta \mathbf{W}$ being the step size in frequency used in the approximation of the function $\mathbf{X}(\mathbf{j W})$ and $\mathbf{W}_{\mathbf{n}}=\mathbf{n} \Delta \mathbf{W}$. Again $\mathbf{x}(\mathbf{t})$ is a continuous function of the time variable, $\mathbf{t}$, and is periodic in $\mathbf{t}$ with period

$$
\frac{2 \pi}{\Delta \mathbf{W}}
$$

The accuracy of the approximation depends on the frequency step size, $\Delta \mathbf{W}$. Suppose the two approximate functions, equations 5.6 .19 and 5.6.21, are
evaluated at N discrete points in frequency and time, respectively:

$$
\begin{equation*}
\mathbf{X}(\mathbf{j} W)=T \sum_{\mathrm{m}=0}^{N-1} \mathbf{x}\left(t_{k}\right) \mathbf{e} \exp \left(\cdot j W_{n} t_{k}\right) \tag{5.6.22}
\end{equation*}
$$

for $\mathbf{n}=\mathbf{0 , 1 , 2}, \ldots, \mathrm{N}-1$
and

$$
\begin{equation*}
x\left(t_{k}\right)=\frac{\Delta W}{2 \pi} \sum_{n=N / 2}^{N / 2} \quad X\left(j W_{n}\right) e \exp \left(+j W_{n} t_{k}\right) \tag{5.6.23a}
\end{equation*}
$$

for $\mathbf{k}=\mathbf{0 , 1 , 2}, \ldots, \mathbf{N}-\mathbf{1}$
where, for convenience, $\mathbf{M}$ was chosen to be $\mathbf{N} / 2$, so that there are the same number of data points in both time and frequency domains. It can be shown that, since the frequency function $\mathbf{X}(\mathbf{j W})$ in equation 5.6 .22 is periodic with period $\mathbf{N}$, the summation in equation 5.6 .23 a can be written as

$$
\begin{align*}
& \quad x\left(t_{k}\right)=\frac{\Delta W}{2 \pi} \sum_{n=0}^{N-1} x\left(j W_{n}\right) e \exp \left(+j W_{n} t_{k}\right)  \tag{5.6.23b}\\
& \text { for } k=0,1,2, \ldots, N-1
\end{align*}
$$

The expression in equations 5.6 .22 and 5.6 .23 represents the approximate Fourier Transform Pair at the $\mathbf{N}$ discrete points in both the frequency and time domains.

### 5.6.2 Discrete Fourier Transform.

Consider a discrete signal $\mathbf{x}(\mathbf{k T})$. If the signal has a finite number of points and its values are used in the approximate Fourier Transform derived above, then equation 5.6.22 yields the approximate frequency information about the signal at the $\mathbf{N}$ discrete frequency values.

ASIDE: Relationship between the time interval T and the frequency interval $\Delta W$.

Assume that $\mathbf{x}(\mathbf{k T})$ is obtained from a continuous signal $\mathbf{x}(\mathrm{t})$ by sampling it at a uniform rate of T seconds. Then, from the principle of sampling, the Fourier Transform of the sampled signal is periodic with period $2 \pi / \mathrm{T}$. Therefore, for the $\mathbf{N}$ frequency points to cover the entire frequency range, the following must be true:

$$
\begin{equation*}
\mathbf{N} . \Delta W=\frac{2 \pi}{T} \quad \text { thus } \quad \Delta W=\frac{2 \pi}{N T} \tag{5.6.24}
\end{equation*}
$$

Then

$$
\begin{equation*}
\frac{\Delta W}{2 \pi}=\frac{1}{N T} \quad \text { and } \quad W_{n} t_{k}=\frac{n k 2 \pi}{N} \tag{5.6.25}
\end{equation*}
$$

$\left(N B . \mathbf{W}_{\mathbf{n}}=\mathbf{n} \Delta \mathbf{W}, \mathbf{t}_{\mathbf{k}}=\mathbf{k T}\right)$
The $\mathbf{T}$ factor in equation 5.6 .22 is often absorbed as part of the signal strength when sampled. Therefore, to define the discrete Fourier Transform, let

$$
\begin{equation*}
x_{k}=T \times\left(t_{k}\right), \quad k=0,1, . ., N-1 \tag{5.6.26}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathbf{X}_{\mathrm{n}}=\mathbf{X}\left(\mathbf{j} \mathbf{W}_{\mathrm{n}}\right), \quad \mathbf{n}=\mathbf{0}, 1, \ldots, \mathbf{N}-1 \tag{5.6.27}
\end{equation*}
$$

Then equations 5.6.22 and 5.6.23, respectively, become

$$
\begin{gather*}
X_{n}=\sum_{k=0}^{N-1} x_{k} \operatorname{e~exp}(-(j 2 \pi / N) n k)  \tag{5.6.28}\\
n=0,1, \ldots, N-1
\end{gather*}
$$

and

$$
\begin{gather*}
x_{k}=\frac{1}{N} \sum_{n=0}^{N-1} X_{n} e \exp ((j 2 \pi / N) k n)  \tag{5.6.29}\\
k=0,1, \ldots, N-1
\end{gather*}
$$

and where use is made of the relations in equation 5.6.25.

The two expressions in equations 5.6 .28 and $\mathbf{5 . 6 . 2 9}$ are called the discrete Fourier transform (DFT) pair. The notation

$$
\begin{equation*}
\mathbf{X}_{\mathrm{a}}=\mathbf{D F T}\left[\mathbf{x}_{\mathbf{k}}\right] \tag{5.6.30}
\end{equation*}
$$

is used to denote the DIRECT Discrete Fourier Transform in equation 5.6.28 and

$$
\begin{equation*}
x_{k}=\operatorname{IDFT}\left[X_{n}\right] \tag{5.6.31}
\end{equation*}
$$

to denote the INVERSE Discrete Fourier Transform in equation 5.6.29. The transform in equation $\mathbf{5 . 6 . 2 8}$ can be expressed in a more concise form. To do this let

$$
\begin{equation*}
\mathbf{W}_{\mathrm{N}}=\exp (-\mathrm{j} 2 \pi / \mathbf{N}) \tag{5.6.32}
\end{equation*}
$$

Then equation 5.6 .28 becomes

$$
\begin{align*}
\mathbf{X}_{\mathrm{n}} & =\sum_{\mathbf{k}=0}^{\mathrm{N}-1} \mathbf{x}_{\mathbf{k}} \mathbf{W}_{\mathbf{N}} \mathbf{n k}^{k}  \tag{5.6.33}\\
\text { for } \mathbf{n} & =\mathbf{0 , 1 , 2}, \ldots, N-1
\end{align*}
$$

The transform in equation 5.6 .29 can also be expressed in a more concise form. To do this let

$$
\begin{equation*}
\mathbf{W}_{\mathbf{N}}=\mathbf{e} \exp (\mathbf{j} 2 \pi / \mathbf{N}) \tag{5.6.34}
\end{equation*}
$$

then equation 5.6.29 becomes

$$
\begin{equation*}
X_{k}=\frac{1}{N} \sum_{n=0}^{N-1} X_{n} W_{N}^{k n} \tag{5.6.35}
\end{equation*}
$$

for $\mathbf{k}=\mathbf{0 , 1}, \ldots, \mathrm{N}-1$
.Note that $\mathbf{W}_{\mathbf{N}}$ has the property

$$
\begin{equation*}
\mathbf{W}_{\mathbf{N}}{ }^{\mathrm{NN}+\mathrm{m}}=\mathbf{W}_{\mathbf{N}}^{\mathbf{m}} \tag{5.6.36}
\end{equation*}
$$

for any $\mathbf{m}$ and $\mathbf{n}$

### 5.6.3 Fast Fourier Transform.

A considerable saving can be made, in computational time, if algorithms known as Fast Fourier Transforms (FFT) are employed. FFTs eliminate some redundant products in the original DFT by decomposing the data sample set into smaller subsets in an orderly manner. The total number in the data sample set must be an exact power of 2 . One way of decomposing the data samples results in the "decimation in time" algorithm. The idea is to decompose the $\mathbf{N}$ point signal sequence, $\mathbf{x}_{\mathbf{k}}$, into two $\mathbf{N} / 2$ point sub-sequences, one consisting of the even numbered samples and the other consisting of the odd numbered samples, as

$$
\begin{equation*}
a_{k}=x_{2 k} \quad \text { for } k=0,1,2, \ldots, N / 2-1 \tag{5.6.37}
\end{equation*}
$$

and

$$
\begin{equation*}
b_{k}=x_{2 k+1} \quad \text { for } k=0,1,2, \ldots, N / 2-1 \tag{5.6.38}
\end{equation*}
$$

and to write the DFT in equation 5.6.28 or 5.6.33 as

$$
\begin{aligned}
X_{n} & =\sum_{k=0}^{N / 2-1} x_{2 k} W_{N}^{2 n k}+\sum_{k=0}^{N / 2} x_{2 k+1} W_{N}^{n(2 k+1)} \\
\text { for } n & =0,1, \ldots, N-1
\end{aligned}
$$

where $\mathbf{W}_{\mathbf{N}}=\mathbf{e} \exp (-\mathrm{j} 2 \pi / \mathbf{N})$ as defined in equation 5.6 .32 .
Since $\mathbf{W}_{\mathbf{N}}{ }^{2}=\mathbf{W}_{\mathrm{N} / 2}$, the above two summations can be written as

$$
\begin{align*}
& X_{n}=\sum_{k=0}^{N / 2} a_{k} W_{N / 2}{ }^{n k}+W_{N}{ }^{n} \sum_{k=0}^{N / 2} b_{k} W_{N / 2}{ }^{n k} \\
& \mathbf{X}_{\mathrm{n}}=\mathbf{A}_{\mathrm{n}} \quad+\mathbf{W}_{\mathrm{N}}{ }^{\mathrm{n}} \mathbf{B}_{\mathrm{n}} \tag{5.6.39}
\end{align*}
$$

where

$$
\begin{equation*}
A_{n}=\sum_{k=0}^{N / 21} \mathbf{a}_{\mathbf{k}} W_{N / 2}^{n k} \tag{5.6.40}
\end{equation*}
$$

is the $\mathbf{N} / \mathbf{2}$ point DFT of $\mathbf{a}_{\mathbf{k}}$ for $\mathbf{k}=\mathbf{0 , 1}, \ldots, \mathbf{N} / \mathbf{2}-1$ i.e. the even-numbered samples of the original signal sequence, and

$$
\begin{equation*}
B_{n}=\sum_{k=0}^{N / 2-1} b_{k} W_{N / 2}{ }^{n k} \tag{5.6.41}
\end{equation*}
$$

is the $\mathbf{N} / \mathbf{2}$ point DFT of $\mathbf{b}_{\mathbf{k}}$ for $\mathbf{k}=\mathbf{0 , 1}, \ldots, \mathbf{N} / \mathbf{2 - 1}$ i.e. the odd-numbered samples of the original signal sequence.

Being a N/2-point DFT, $\mathbf{A}_{\mathbf{n}}$ and $\mathbf{B}_{\mathbf{n}}$ each have only $\mathbf{N} / \mathbf{2}$ distinct elements with the property

$$
A_{n+N 2}=A_{n}
$$

and

$$
\mathbf{B}_{\mathrm{n}+\mathrm{N}_{2} 2}=\mathbf{B}_{\mathrm{n}}
$$

for $\mathrm{n}=0,1, \ldots, \mathrm{~N} / 2-1$

Since $W_{N}{ }^{n+N / 2}=-W_{N}{ }^{n}$, equation $\mathbf{5 . 6 . 3 9}$ can be written two parts as

$$
\begin{align*}
X_{n}=A_{n}+W_{N}{ }^{n} B_{n} \quad \text { for } n=0,1, \ldots, N / 2-1  \tag{5.6.42}\\
X_{n+N / 2}=A_{n}-W_{N}^{n} B_{n} \quad \text { for } n=0,1, \ldots, N / 2-1 \tag{5.6.43}
\end{align*}
$$

Thus, an N-point DFT can be found from the N/2-point DFT of its even-numbered and the $\mathrm{N} / 2$-point DFT of its odd-numbered samples. The result of this first step in deriving the FFT algorithm for $\mathrm{N}=8$ is depicted in figure 5.6.13.

The second step in the decimation-in-time derivation is to apply the same decomposition technique in the computation of the two $\mathrm{N} / 2$-point DFT's in order to obtain $\mathbf{A}_{\mathrm{n}}$ and $\mathbf{B}_{\mathrm{n}}$ for $\mathbf{n = 0 , 1 , \ldots . . . . N / 2 - 1}$. The two $\mathrm{N} / 2$-point subsequences $\mathbf{a}_{\mathbf{k}}$ and $\mathbf{b}_{\mathbf{k}}$ are each decomposed into the even-numbered samples and odd-numbered samples as

$$
\begin{align*}
& c_{k}=a_{2 k}=x_{4 k} \quad \text { for } k=0,1, \ldots, N / 4-1 .  \tag{5.6.44}\\
& d_{k}=a_{2 k+1}=x_{4 k+2} \text { for } k=0,1, \ldots, N / 4-1 .  \tag{5.6.45}\\
& e_{k}=b_{2 k}=x_{4 k+1} \text { for } k=0,1, \ldots, N / 4-1 .  \tag{5.6.46}\\
& f_{k}=b_{2 k+1}=x_{4 k+3} \text { for } k=0,1, \ldots, N / 4-1 . \tag{5.6.47}
\end{align*}
$$

Following the same derivations leading to equation 5.6 .42 and $\mathbf{5 . 6 . 4 3}$, the following formulas are obtained to express the $N / 2$-point DFT's $\mathbf{A}_{n}$ and $\mathbf{B}_{\mathrm{n}}$ in terms of the N/4-point DFT's $\mathbf{C}_{\mathbf{n}}, \mathbf{D}_{\mathbf{n}}, \mathbf{E}_{\mathbf{n}}, \mathbf{F}_{\mathbf{n}}$ :

$$
\begin{gather*}
A_{n}=C_{n}+W_{N}^{2 n} D_{n} \text { for } n=0,1, \ldots, N / 4-1  \tag{5.6.48}\\
A_{N / 4+n}=C_{n} \cdot W_{N}^{2 n} D_{n} \text { for } n=0,1, \ldots, N / 4-1  \tag{5.6.49}\\
B_{n}=E_{n}+W_{N}^{2 n} F_{n} \text { for } n=0,1, \ldots, N / 4-1  \tag{5.6.50}\\
B_{N / 4+n}=E_{n} \cdot W_{N}^{2 n} F_{n} \text { for } n=0,1, \ldots, N / 4-1 \tag{5.6.51}
\end{gather*}
$$

where the property $\mathbf{W}_{\mathrm{N} / 2}=\mathbf{W}_{\mathrm{N}}{ }^{2}$ is used.

The result of the second step in the decimation-in-time decomposition process is shown in figure 5.6.14 for $\mathbf{N}=8$

The process of computing a DFT by decomposition of the signal into two subsequences can be continued until a one point DFT is reached, which is just the sample point itself. Because $\mathbf{N}$ is some power of 2 , let $\mathbf{r}$ be that power so that $\mathbf{N}=\mathbf{2}^{\mathbf{r}}$. Thus, $\mathbf{r}$ steps are required in the above decomposition process to reach the one point DFT's.

The final result of the eight-point decimation-in-time FFT is shown in the flow graph of figure 5.6.15. The two-point DFT's require no multiplications. For example, the two-point DFT $\mathbf{C}_{0}$ and $\mathbf{C}_{1}$ can be obtained by combining the one-point DFT's of $\mathbf{x}_{0}$ and $\mathbf{x}_{4}$ which are just the signal samples themselves:

$$
\begin{equation*}
C_{0}=x_{0}+x_{4} \tag{5.6.52}
\end{equation*}
$$

and

$$
\begin{equation*}
C_{1}=x_{0}-x_{4} \tag{5.6.53}
\end{equation*}
$$

Also, since $\mathbf{W}_{\mathbf{8}}{ }^{\mathbf{2}}=-\mathrm{j}$, the four-point DFTs in equation $\mathbf{5 . 6 . 4 8}$ through to $\mathbf{5 . 6 . 5 1}$ for $\mathbf{N}=8$ do not actually require complex multiplication. Therefore, in general, in combining the one-point DFTs to form the two-point DFTs and the two-point DFTs to form the four-point DFTs, no complex multiplications are required, thus reducing the total number of multiplications for the FFT algorithm by $\mathbf{N}$.

Note that in order for the DFT [ $\left.\mathbf{X}_{\mathbf{n}}\right], \mathbf{n}=\mathbf{0 , 1}, \ldots, \mathbf{N}-1$, to appear in its natural order, the original sequence $\mathbf{x}_{\mathbf{k}}, \mathbf{k}=0,1, \ldots, N-1$, must be rearranged as shown in figure 5.6.15. The subscripts in the rearranged order have an interesting relationship with those in the natural order. The relationship is the bit reversal of the subscript. If the subscript of the natural order are represented in binary form in $r$-bits (binary digits), where $r=\log _{2} \mathbf{N}$, then by reversing the bits in each binary representation and representing the reversed $r$-bits in the decimal system, the subscript for the rearranged input sequence is obtained. The bit-reversal result is illustrated in Table 2 for the case of $\mathbf{N}=\mathbf{8}$.

With the input sequence reordered properly by using the bit-reversal procedure, the computation of the FFT can be performed in-place. To show this refer to figure 5.6 .15 for $\mathrm{N}=8$. In every stage, pairs of variables are combined to form other pairs. For example, $\mathbf{x}_{0}$ and $\mathbf{x}_{4}$ are combined to form $\mathbf{C}_{0}$ and $\mathbf{C}_{1}$, but $\mathbf{x}_{0}$ and $\mathbf{x}_{4}$ are not used to form other values, and $\mathbf{C}_{0}$ and $\mathbf{C}_{1}$ do not require other values. Similarly, only $\mathbf{C}_{0}$ and $\mathbf{D}_{0}$ are used to calculate $\mathbf{A}_{0}$ and $\mathbf{A}_{2}$, and $\mathbf{C}_{0}$ and $\mathbf{D}_{0}$ are not used to calculate any other values. Therefore, after a pair of values is used to form a pair of new values, the old values are no longer needed. Hence, the calculated new values can be stored back in the same storage locations used for the old values. This in-place computation reduces the amount of storage required in the computer.

To start the decimation-in-time FFT algorithm, pairs of adjacent values in the bit-reversed sequence are first combined to form pairs of new values, starting from the top to the bottom using the in-place procedure as shown in the
extreme left of figure 5.6.15. The operations involved in the first stage are only complex additions (subtractions), as shown in equations 5.6 .52 and

### 5.6.53.

In the second stage, pairs of newly formed valves, two positions apart, are used to calculate pairs of new values in-place.

This process of calculating pairs of new values in-place from the "old" values is continued for $\mathbf{r}\left(=\log _{2} \mathbf{N}\right)$ stages, with the separation of the variables in the pairs increased from stage to stage by a factor of 2 .

During any stage, the in-place calculation of a pair of values has the structure shown in figure 5.6 .16 known as a butterfly. As stated previously, the term $W_{N}{ }^{m} \mathbf{x}_{\mathbf{k}+\mathrm{L}}{ }^{(0)}$ is used in the calculation of both $\mathbf{x}_{\mathbf{k}}{ }^{(0+1)}$ and $\mathbf{x}_{\mathbf{k}+\mathrm{L}}{ }^{(0+1)}$ in the butterfly-structure flow graph of figure 5.6.16, where, by the concept of in-place-calculation, the signal samples are denoted by the same variables, with the added superscripts indicating the stage number. The butterfly structure can therefore be modified to the one shown in figure 5.6.17, which stresses that only one complex multiplication is required.

By reordering the nodes in figure 5.6.15, alternative forms of decimation-in-time FFT algorithm can be obtained. For example, by exchanging the rows of nodes, while carrying the branches along in each exchange, so that the input samples are in natural order, the flow graph of figure 5.6 .18 is obtained, where the resulting DFT is in bit-reversed order. In this version, in-place calculation is still possible; however, the DFT values must be reshuffled using the bit-reversal procedure. Because, in the proposed laser instrument, the photodiode array captures data in the natural order, this form of FFT algorithm was adopted for the data analysis.

The FFT algorithms derived in this section can also be used to compute the inverse DFT as defined in equation 5.6.29. To do this, the complex exponential constant, $W_{N}{ }^{m}$ has to be modified as

$$
\mathbf{W}_{\mathbf{N}}{ }^{m}=\exp (+j 2 \pi \mathrm{~m} / \mathbf{N})
$$

i.e. equation 5.6.34, and the input will consist of $\mathbf{X}_{\mathbf{n}} / \mathbf{N}, \mathbf{n}=0,1, \ldots, N-1$. The output of the algorithm is then the signal samples in the time domain.

### 5.6.4 The FFT Algorithm.

With the details outlined in Section 5.6.3 a BBC BASIC computer algorithm was developed to implemented the decimation-in-time FFT algorithm. The FFT algorithm was tailored to suit the requirements of the Laser Instrument as dictated by the Nyquist Sampling Theorem and Fast Fourier Transform Theory:

The basis of Sampling Theory (the Nyquist Theorem) is that: "a continuous-time signal can be completely recovered from its samples if, and only if, the sampling rate is greater than twice the signal bandwidth".

For the decimation-in-time FFT, however, the number of samples must be an integer power of 2 .

The surface wave pitch currently produced by woodworking machines is greater than or equal to 1 mm . For the 125 mm sample length (see Section 5.3.3), the smallest sample size which satisfies both these criteria is 256 . Thus, 256 equi-spaced data points (every fourth data point from the set of

1024 points captured using the photodiode array (see Section 5.2.2.5)) were to be used as the data set to be transformed in the BASIC FFT algorithm.

The BASIC FFT algorithm, shown in Appendix A6, starts with the input in natural order and results in bit-reversed order. As pointed out above (Section 5.6.1.9), the same algorithm can be used to compute the direct FFT and the inverse FFT, provided the complex exponential constant $\mathbf{W}_{\mathrm{N}}$ is properly assigned, as shown in equations 5.6 .32 and $\mathbf{5 . 6 . 3 4}$ for direct FFT and inverse FFT, respectively. This is accomplished in the BBC BASIC FFT computer algorithm by use of the variable SIGN (lines 760 and 960 ). SIGN equals 1 for the direct transform and -1 for the inverse transform.

The in-place calculations are implemented in lines 970 to 990 . Note that $\mathbf{W}_{\mathbf{N}}{ }^{0}=1$ requires no complex operations, so provision is made to eliminate the complex multiplication as implemented in lines 900 to 920 .

With the aid of figure 5.6 .18 it can be seen that the power $\mathbf{m}$ in $\mathbf{W}_{\mathbf{N}}{ }^{\mathbf{m}}$ in each stage has a bit-reversal relationship with the position number, as shown in lines 880 to 890 of the algorithm. The bit-reversal sub-routine, FNrbitr (lines 490 to 700), is used here (line 890) for this purpose and later in line 1100 to bit-reverse the output samples. In order to reduce the execution time of the algorithm, the bit-reversal procedure was written in Assembly language. FNrbitr, accepts an 8-bit integer, A\%, and returns a bit-reversed integer (still 8-bits).

The parameter DELTA (lines 760 and 1180) is used to multiply the samples so that the FFT algorithm can be used as an approximation to the continuous Fourier transform. According to equation 5.6.26, this factor should be T, the step size in time used in the zero-order approximation of the Fourier integral. For the inverse Fourier transform, this factor is the step-size frequency used in the zero-order approximation of the inverse integral. For the implementation of a strict DFT, DELTA is set equal to 1 for the transform and equal to $1 / \mathbf{N}$ for the inverse transform.

### 5.6.5 Validating the FFT Algorithm.

The BBC BASIC FFT algorithm, once written, had to be verified and its credibility appraised before it could be reliably employed in transforming captured data from the time domain to the frequency domain.

Verification was accomplished by synthesising data sets (using mathematical formulas) with known frequency content and observing whether the FFT algorithm produced the correct results. Figures 5.6 .19 to $\mathbf{5 . 6 . 4 6}$ show the nature of the synthesised data and the resulting frequency spectrum obtained from the algorithm.

In the first instance (figures 5.6 .19 to 5.6 .25 ), the amplitude of a sine wave was kept constant and the frequency varied. (Note that the resolution of the computer screen proved inadequate for the display of frequencies higher than about 90 Hz .)

Secondly, two sine waves of the same amplitude, but different frequencies, were summed; the frequency of one of the waves being varied (figures 5.6.26 to 5.6.29).

Further verification tests were conducted (figures 5.6 .30 to 5.6 .34 ) with the summation of two sine waves of different amplitudes and frequencies.

Finally appraisals were carried out (figures 5.6 .35 to 5.6 .46 ) with multiple summations of sine functions of differing amplitudes and phase relationships, and, pulse trains of differing amplitudes and mark-space-ratios.

## 6 TIMBER MACHINING INVESTIGATION

6.1 Introduction
6.2 The Planer - Moulder Machine

### 6.2.1 General Description

### 6.2.2 Final Top Head

6.2.2.1 Cutterhead
6.2.2.2 Cutterblock

### 6.2.3 Timber Control

6.2.3.1 Feedworks
6.2.3.2 Chipbreaker, Top and Side Pressure Rollers

### 6.2.4 Jointer

### 6.2.5 Extractor fan

6.3 Machining Variables and Parameters
6.4 Machine Preparation and Condition

### 6.4.1 Operating Conditions

### 6.4.2 Process Parameters

6.5 Timber Specification

### 6.6 Induced and Simulated Surface Finish Defects

6.6.1 Eccentric Cutterhead Rotation
6.6.1.1 Spindle Cylindricity
6.6.1.2 Cutterblock Concentricity
6.6.1.3 Spindle Concentricity/Dynamic Balance

### 6.6.2 Proud Knives

6.6.3 Workpiece Vibration
6.6.4 Single Knife finish
6.7 Surface Finish Analysis
6.7.1 Introduction
6.7.2 Laser Instrument Data Set
6.7.3 Talyrond 200 Data Set
6.7.4 Surface Simulation Data Set
6.7.5 Fast Fourier Transform of Data Sets
6.7.6 Defect Identification from FFT Spectrum
6.7.6.1 Ideal Timber Surface
6.7.6.2 Spindle Concentricity/Dynamic Balance
6.7.6.3 Proud Knives
6.7.6.4 Vibration: Timber, Spindle
6.7.6.5 Single Knife Finish
6.7.6.6 Fault Finding Algorithm

### 6.1 Introduction

Having constructed the laser instrument, it had to be tested, validated and commissioned. This was effected by machining timber samples with known and regulatable surface characteristics. The timber samples thus produced were assessed using the laser instrument and the results compared to that obtained using a conventional surface assessment instrument (Talyrond 200). In addition these results were compared with data generated using appropriate values for parameters in the surface simulation algorithm (SSA).

This chapter describes the techniques used in preparing the timber samples. A description is given of the planing machine used and the modular units of which it is comprised. The associated machining parameters are discussed and details of induced or simulated machining faults are described.

### 6.2 Planer - Moulder Machine

### 6.2.1 General Description

The planing machine used to generate all the timber samples during this investigation is known as the B -series 220 (abbreviated, 220B) and is shown in figure 6.1. The 220B is a modular, throughfeed planing and moulding machine having a choice of six or seven head configuration (figure 6.2) with the option of a four-position Universal head. The heads rotate at a maximum speed of 12,000 revs $/ \mathrm{min}$; the horizontal heads have a hydraulically pressurised outboard bearings with jointing at $6000 \mathrm{revs} / \mathrm{min}$ in order to provide multi-knife machining. The machine has a capacity of 220 mm and was designed specifically for high productivity combined with high product
quality.

The throughfeed operation incorporates driven infeed and outfeed bedrollers which simplifies feeding, especially in handling mouldings of long length and in the control of timber during straightening operations. All the feed rollers are pneumatically loaded to provide positive and consistent feeding. All heads have vertical and horizontal adjustment and are provided with chipbreaker and pressure rollers.

The 200B has a highly efficient dust extraction system built with an integral sound enclosure, which makes it intrinsically safe and noise abated.

### 6.2.2 Final Top Head

The timber surfaces to be analyzed in this investigation, were in essence machined by the final top head (figure 6.3). In detail, this top head consists of a base unit with mounting faces provided for attaching the feedworks, bedplates and the cutterhead assembly. The drive motor is mounted on the rear or the base and a standard "V" belt drive transmits power to the main spindle.

### 6.2.2.1 Cutterhead

The cutterhead's spindle is 40 mm in diameter; the spindle bearing assembly is as shown in figure 6.4. It comprises a back to back pair of angular contact bearings at the fenceside position; these are the datum bearing pair. A deep groove bearing supports the belt drive loads with another mounted in the
removable outboard bearing housing at the nearside of the cutterblock. The bearings are manufactured to EP7 standard and lubricated for life with ISOFLEX grease, KLUBER NB15. The head is driven by a 18 kW electric motor.

### 6.2.2.2 Cutterblock

The type of tooling used to produce the timber samples during this investigation is known as a Hydrogrip Planing Cutterblock. This style of cutterblock, shown in figure 6.5, comprises two hydraulic expanding bushes fixed at either end of a high strength steel body in which six high-speed steel knives are mounted. The diameter of the cutterblock was 150 mm , its length 180 mm with a design rotational speed of 6000 rpm .

The bushes are pressurised independently, to 450 bar (using a grease gun), which effectively centres the cutterblock on the spindle. This is done by hydrostatically collapsing the bore of the bush until it grips the spindle with sufficient force to enable the transmission of the power required. A fail-safe safety device is fitted such that the drive remains effective should the Hydrogrip function fail.

### 6.2.3 Timber Control

### 6.2.3.1 Feedworks

The heavy duty in-feedworks, which traverse the timber across the hard chrome machine table and pass the rotating cutterheads, is shaft driven by an infinitely-variable-speed, mechanical unit (figure 6.6). Feed speed range
from 6 to 180 metres per minute. The feedworks, which has a 22.5 kW ( 30 hp ) electric drive motor with increment and reverse feed, also have a motorpowered $(0.5 \mathrm{~kW})$ rise and fall facility. The in-feed system is pneumatically loaded and has serrated bed rollers which provide positive feeding (figure 6.6).

The out-feedworks comprise overhead, protective, polyurethane feedrollers, 140 mm in diameter, and are pneumatically loaded to 4 bar to enable frictional feeding (figure 6.7).

### 6.2.3.2 Chipbreaker, Top and Side Pressure Rollers

The chipbreaker, top pressure roller and side pressure roller assemblies enable the timber to maintain contact with the reference surfaces - the machine table and fence.

The chipbreaker (figure 6.8) has a radial action which gives precise control, close to the cutting action, without the need to allow for timber thickness or width variation. Both the chipbreaker and top pressure rollers are pneumatically loaded to a pressure of 4 bar, generating a downward force on the traversing timber.

As the timber traverses across the bedplate, the side pressures rollers, which are spring loaded, push the timber hard against the fence (figure 6.9).

### 6.2.4 Jointer

The top head is fitted with a standard jointing device (figure 6.10). Jointing is effected by the hand rotation of the cross-feed-screw thus traversing the stone across the cutterblock; the jointing stone is fed into the cutterblock, in the radial direction, by means of the down-feed-screw; this is done at the end of each cross-traverse. Thus, the cutterhead is jointed without the need to remove it from its actual cutting position.

### 6.2.5 Extractor Fan

The top head (and other heads) is also fitted with a powerful extractor fan and appropriate ducting which removes the wood chips and dust particles produced during the planing process (figure 6.11).

### 6.3 Machining Variables and Parameters

There are numerous factors, parameters and variables associated with the rotary planing of timber. Typical examples are: age of the machine; depth of cut; type of tooling material; design of the machine tool; specifications of the workpiece material; ambient temperature; etc. Each parameter or variable, to some degree, contribute to the resultant surface finish. Previous researchers (Davis E.M, Nelson H. 1954; Koch P. 1956; Goodchild R. 1963 Jackson M.R. 1986) have isolated and identified the most significant parameters, variables and phenomena which have a marked effect on the aesthetic qualities (ie. the surface finish) of a spindle-machined, timber surface; they include:

1) Timber's linear feedspeed.
2) Cutterhead's rotational speed.
3) Number of knives on the cutterblock.
4) Depth of cut.
5) Concentricity of the main cutterhead spindle.
6) Cutterhead dynamic imbalance.
7) Machine vibration
8) Vibration between the workpiece and machine table.
9) Degree to which the cutterhead is correctly jointed (cutterhead cylindricity).
10) Knifes' resilience to wear.
11) Cutting velocities
12) Rake and clearance angles of knives
13) Quality and type of timber being machined.
etc.

During this investigation steps were taken and attempts made to control, or keep constant, the parameter and variables being manipulated during the machining process. This incurred some machine preparation before timber machining commenced.

### 6.4 Machine Preparation and Condition

In order to maintain consistency and ensure repeatability, each time the 220B planer-moulder was used to produce a batch of timber samples, certain basic operating conditions were established and specific process parameters measured during planing. These are discussed in the following section.

### 6.4.1 Operating Conditions

During or prior to using the 220B planer-moulder to machine timber samples the following machining conditions were established:

1) All components requiring lubrication on the 220 B planer/moulder were adequately lubricated using the recommended lubricants.
2) The final top head spindle's static tracking error (eccentricity/run-out) was measured to confirm that it was less than $5 \mu \mathrm{~m}$ at its fenceside end and less than $10 \mu \mathrm{~m}$ at its nearside end, with the outboard bearing removed. This ensured tracking errors in the region of fractions of a micron when the outboard bearing was engaged.
3) The "V" belts which transmit power from the electric motor to the cutterhead were checked and belt tensions adjusted, as necessary, to comply with the manufacturers specifications.
4) The cutterblock used was dynamically balanced to within $30 \mathrm{~g} . \mathrm{mm}$ (see Section 6.6.1.3) using a two-plane balancing machine. The cutterblock was then mounted on the top head spindle such that it obtained a knife-to-knife tracking accuracy within $20 \mu \mathrm{~m}$, before jointing the cutterhead. The cutterblock was always located in the same angular position relative to the spindle by alignment to two reference marks.
5) The 220B planer-moulder drive motors were operated for one hour ("warm-up" period) with no load to establish optimum operating conditions.
6) The pressure of the feedrollers and chipbreaker were set to 4 bar.
7) All other machinery in the immediate vicinity of the 220B planer-moulder was switched off to prevent vibration being transmitted to, and affecting the action of, the final top head.
8) Vibration levels at the final top head (amplitude and frequency) were measured and recorded towards the end of the one hour "warm-up" period using a Bruel and Kjaer vibration meter (Type 2511) in conjunction with a Yokogawa Hokushin Electric Analysing recorder. (This piece of equipment was acquired late in the research period so that measurements
are not available for every timber sample).

### 6.4.2 Process Parameters

The parameters monitored during the machining of the timber samples were as follows.

1) The rotational speed of the final top head was registered during the planing of each sample.
2) When the equipment was available, vibration levels (frequency and amplitude), in the vicinity of the final top head were recorded during active planing.
3) The feedspeed of each timber sample (during the actual planing process) was noted and recorded.
4) Any induced or simulated machining faults (and associated parameters) were noted and recorded.

### 6.5 Timber Specification

The timber samples used through out this investigation were Swedish Redwood, this being commonly used in the woodworking industry in conjunction with the jointing process (Jackson M.R, 1986).

The dimensions of the workpieces were typically $50 \mathrm{~mm} \times 30 \mathrm{~mm} \times 1000 \mathrm{~mm}$ having all four sides pre-machined, which effectively straightened the underside; the underside was used as a reference surface which made contact with the machine table.

Timber was selected such that its moisture content lay between $10 \%$ and $15 \%$; this is the moisture content range recommended for ideal timber
machining (Jackson M.R, 1986).

### 6.6 Induced and Simulated Surface Finish Defects

This research concentrated on particular surface defects which were common and which could be induced by reproducing certain machining conditions or by simulating specific machine malfunctions or faults. There were three main areas:
i) Eccentric rotation of cutterhead
ii) Proud knives
iii) Workpiece support and control

### 6.6.1 Eccentric Cutterhead Rotation

Four major factors can cause a cutterhead to rotate eccentrically and hence affect the surface finish it generates. They are:
i) Spindle Cylindricity
ii) Cutterblock Concentricity
iii) Spindle Concentricity
iv) Cutterhead Dynamic Balance

### 6.6.1.1 Spindle Cylindricity

There have been immense advances in turning/grinding technology; the tight cylindricity tolerances to which spindles can now be manufactured ensures that lack of spindle cylindricity is no longer a major feature which affects the surface quality of planed timber (Goddard M,1985). Consequently, this phenomenon was not investigated during this research.

### 6.6.1.2 Cutterblock Concentricity

Similarly, lack of cutterblock concentricity as a cause of surface defects has been alleviated due to the development of hydraulically pressurised bearings; these Hydrogrip bearings are highly effective in centring the cutterblock on the spindle. Thus, cutterblock concentricity did not feature in this research. However, if the machine is operated with the hydrogrip bearings unpressurised eccentric tracking will result.

### 6.6.1.3 Spindle Concentricity and Dynamic Balance

Spindle concentricity is still an active component in the quality of the surface which a cutterhead generates. The main reason for non-concentric rotation of spindles is bearing wear; this causes the spindle to orbit, rather than rotate, about its ideal axis.

When a cutterhead is used in an unbalance state there is a tendency for the spindle to bow under the influence of the unbalanced forces; this, depending on the magnitude and position of the unbalanced forces causes eccentric tracking. This is then transmitted to, and apparent in, the surface profile produced.

The effects of lack of spindle concentricity and dynamic imbalance on the surface profile is very similar; they both result in eccentric rotation of the cutterhead. Indeed, bearing wear is often a direct result of dynamic imbalance. (Balancing a cutterhhead is the process of attempting to improve the mass distribution of the cutterhead so that it rotates in its bearings
without unbalanced centrifugal forces. This aim can be attained only to a certain degree; even after applying the balancing process the cutterhead will possess residual imbalance.)

In this research cutterhead eccentricity was investigated. The high cost, to the collaborating establishment, of producing worn bearings proved prohibitive; that of generating out-of-balance forces was more feasible; this option was selected as the means of producing eccentric rotation of the cutterhead.

Initially, the cutterhead was balanced according to balance quality grade G2.5 (International Standard 1940/1 and British Standard 5750) which specifies a permissable residual imbalance of $93 \mathrm{~g} . \mathrm{mm}$ for the cutterhead size used (see Appendix D1). The balancing machine used was a series HK, Reutlinger twoplane balancing machine (K27.00 MC120E). (The cutterblock is dynamically balanced during manufacture to within $30 \mathrm{~g} . \mathrm{mm}$. Once knives, which are weight matched to within 0.5 g , are added, the inevitable variances in location mean that residual imbalance of the cutterhead, complete with wedges, is normally within $60 \mathrm{~g} . \mathrm{mm}$. Allowance is made for a variation in imbalance due to the depressurising and re-pressuring of the hydraulic clamping sleeves (typically $10 \mathrm{~g} . \mathrm{mm}$ ).

Dynamic imbalance was induced in the cutterhead by the addition of extra masses to the periphery of the cutterblock in line with knife "number 1 ". (The cutterblock is designed so that the knives can be held in place using
socket screws; (some cutterblocks have serrations on the knife and cutterblock which allow the knife to be located in fixed radial positions.)) The degree of imbalance was varied incrementally by changing the length (and therefore the mass) of the socket screws which held knife "number 1 " in position.

Two sets of socket screws were employed:

Set 1 were 12 mm long and each one weighed 10.0 g
Set 2 were 16 mm long and each one weighed 13.0 g

Initially, with Set 1 socket screws in position, the cutterhead was dynamically balanced to within $30 \mathrm{~g} . \mathrm{mm}$ Then, the socket screws of Set 1 were replaced in stages by those in Set 2, causing varying, but incremented values of cutterhead dynamic imbalance:

In figure 6.12 points $\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}$, and E represent the arrangement of the socket screws positions at knife "number 1".

First the socket screw in position $C$ was replaced by a socket screw from Set 2, inducing the first increment of dynamic imbalance in the cutterhead. Timber samples were machined and records made of the associated machining conditions.

Dynamic imbalance was increased further by removing and replacing other socket screws in the set, but always maintaining mass symmetry about point $\mathbf{C}$; further timber samples were machined with corresponding out-of-balance conditions recorded.

The surface waveform of the timber samples were assessed using the Laser Instrument and the Talyrond 200, as described in Section 6.7. The results of these investigations are presented in Section 7.3.2 and discussed in Section 8.4.2.2.

### 6.6.2 Proud Knives.

As with dynamic imbalance, proud knife is a phenomenon which can contribute to surface defects in machined timber. The major cause of proud knifes is poor machine tool setting. The fault usually occurs on cutterheads which use friction (as opposed to serrations) to locate the knives in their radial position. If it is not adequately secured by the holding screws there is a tendency for the knife to gradually slip under the influence of the centrifugal forces associated with the cutterheads rotation. They can also be jolted radially inwards (or loosened) by shock loads from knots, or other obstructions, in the timber.

In this investigation cutterheads with proud knives were created using two methods:

## Method 1

The cutterhead was dynamically balanced to within $30 \mathrm{~g} . \mathrm{mm}$ and jointed. It was then used to machine timber samples to confirm that a "perfect" finish was being produced. Then without removing the cutterblock from the spindle, a knife was moved radially (in increments of approximately $4 \mu \mathrm{~m})$ towards the axis of rotation. The cutterhead was then used to
machine timber samples.

## Method 2

As with method 1 the cutterhead was dynamically balanced to within 30g.mm, jointed and used to machine timber samples to confirm that a "perfect" finish was being produced. Then the cutterhead was removed and specific knives ground low (in increments of approximately $4 \mu \mathrm{~m}$ ) using an NX-grinder (figure 6.13). The cutterblock was then refitted to the spindle and used to machine timber samples.

The surface waveform of the timber samples were assessed using the Laser instrument and the Talyrond 200, as described in Section 6.7. The results of these investigations are presented in Section 7.3.3 and discussed in Section

### 8.4.3.2.

### 6.6.3 Vibration: Timber, Spindle

If it is not correctly supported and controlled the workpiece will vibrate as it is traversed across the machine bed. The vibration of the workpiece (in practice due to incorrect machine configuration) will contribute to the frequency content (defects) on the machined surface. The severity of workpiece vibration will depend on the extent of inadequate support and control. In seeking to produce timber samples with defects due to workpiece vibration, some attempt was made to regulate the amount of vibration which the traversing timber experienced because of unsatisfactory support and control.

The three machine components which, in conjunction with the machine table and fence, support and control the timber in the vicinity of the final tophead/cutterhead are:

1) the chipbreaker
2) top pressure roller
3) side pressure roller

The machine table and fence are fixed reference surfaces across, and against, which the workpiece slides; the top pressure roller and the chipbreaker provide downward forces which press the workpiece hard against the machine table; the side pressure roller presses the workpiece hard against the fence.

As the vibration-prone timber samples were produced the pressure, applied to the workpiece by the chipbreaker and top pressure roller, was varied; the side pressures being always fully operative. This theoretically limited any workpiece vibration to the vertical plane only.

Incorrect support of the cutterhead's spindle, at the outboard end, will also result in the cutterhead vibrating and adversely affecting the quality of the surface finish produced. Timber samples were machined with the outboard end of the spindle experiencing reducing degrees of support.

The surface waveform of the timber samples produced using reduced timber and spindle-outboard support were assessed using the Laser Instrument and the Talyrond 200, as described in Section 6.7. The results of these
investigations are presented in Section 7.3.4 and discussed in Section 8.4.2.4.

### 6.6.4 Single Knife Finish

The term "single-knife finish" is used to describe a mode of rotary timber machining in which only one knife (ie. the most proud knife), on a multiknife, unjointed cutterhead, produces the finish surface profile. This mode is used in the industry as a dependable method of producing a high quality surface finish. The drawback, compared to a jointed multi-knife finish, is that, for a given cutterhead rotation speed (W), the timber feed speed for a required surface wave pitch ( $\mathbf{p}$ ) is much reduced: for single knife finish, the maximum timber feedspeed, $\mathbf{V}_{\text {smax }}$, is given by:

$$
\begin{equation*}
\mathbf{V}_{\mathrm{smax}}=\frac{\mathrm{p} . \mathbf{W}}{2 \pi} \tag{6.1}
\end{equation*}
$$

where $\mathbf{W}$ is in $\mathrm{rad} / \mathrm{s}$

This obviously reduces production rates, the advantage being a decrease in machine setting time and product consistency.

The surface waveform of the timber samples produced using single knife finish were assessed using the Laser instrument and the Talyrond 200, as described in Section 6.7. The results of these investigations are presented in Section 7.3.1 and discussed in Section 8.4.2.1.

### 6.7 Surface Finish Analysis

### 6.7.1 Introduction

Three surface waveform data sets were generated for each timber sample; the first set was produced using the Laser Instrument, the second using the Talyrond 200 and the third using the surface simulation algorithm (SSA). Each data set was transformed into the frequency domain using the FFT algorithm (Section 5.6.4). The FFT data was then analysed, with reference to the number of significant peaks present in the spectrum and their location in the harmonic scale range, thus ascertaining the type of faults present in the surface profile (see Section 6.7.6).

### 6.7.2 Laser Instrument Data Set

Each sample, in turn, was placed in the datum position of the Laser Instrument and illuminated with grazing incidence laser light (figure 6.14). Under software control (Section 5.5) a data set, which mirrored the frequency content of the surface waveform was captured and stored for future analysis using the FFT algorithm (Section 5.6.4)

### 6.7.3 Talyrond 200 Data Set

Each sample, in turn, was positioned on the Talyrond 200 Instrument (figure 6.15). Under software control (see appendix B4) a data set, which echoed the surface profile and hence the frequency content of the surface waveform, was captured and stored for future analysis using the FFT algorithm.

### 6.7.4 Surface Simulation Data Set

For each timber sample, a corresponding simulated data set was generated using appropriate parameter values (ie. timber feedspeed, cutterhead angular velocity, etc) in the surface simulation algorithm (SSA) (Section 4.6). The data set thus acquired was stored for future analysis using the FFT algorithm (Section 5.6.4)

### 6.7.5 Fast Fourier Transform of Data Sets

The three data sets generated for each timber sample were transformed into the frequency domain and each FFT spectrum displayed graphically. A typical result is shown in figure 7.G1.S1. For details on the full range of results see Section 7.3.

### 6.7.6 Defect Identification from FFT Spectrum

### 6.7.6.1 Ideal Timber Surface

The frequency domain description of an ideally machined timber surface should contain a single peak or local maxima (denoted, uni-modal); the pitch (ie. knife-mark or cusp distribution) of an ideal surface is uniform. The expected number of knife-marks, $\mathbf{h}_{\mathbf{j}}$, in a given sample length, $\mathbf{L}_{\mathbf{2}}$, is given by

$$
\begin{equation*}
h_{j}=\frac{W L_{8}}{2 \pi V} \tag{6.2}
\end{equation*}
$$

where
$\mathbf{W}=$ angular velocity of the cutterhead,
$\mathbf{V}=$ linear feed velocity of the timber,
$\mathbf{N}=$ number of knives (equi-spaced and jointed) on the cutterblock, and where the suffix $\mathbf{j}$ indicates a jointed cutterhead or milti-knife finish.

Thus, for an ideally planed surface, harmonic $h_{j}$ would be the only dominant (or principal) harmonic in the spectrum of the surface's profile. This was illustrated by using the SSA to generate models of ideally machined timber profiles (to varying specifications), and using the FFT algorithm to obtain their frequency or harmonic spectrum. A typical example is shown in figure 7.G0.S2c.

### 6.7.6.2 Spindle Concentricity / Dynamic Balance

Cutterheads with spindles that are not concentric, or cutterheads that are not dynamically balanced tend to produce planed surfaces which exhibit a "once per revolution" defect which is superposed onto an otherwise ideal surface profile. Such a profile will feature the expected number of knife marks, $\mathbf{h}_{\boldsymbol{j}}$, superposed onto a surface which undulates sinusoidally, due to lack of spindle concentricity.

The frequency signature of a sample length of such a surface would contain two major peaks (denoted, bi-modal); one at principal harmonic $\mathbf{h}_{\boldsymbol{y}}$ (see equation 6.2), the other at $h_{1}$ (the principal harmonic which represents the surfaces undulation) given by

$$
\begin{equation*}
h_{1}=\frac{W L_{~}^{c}}{2 \pi V} \tag{6.3}
\end{equation*}
$$

where
$\mathbf{W}=$ angular velocity of the cutterhead
$\mathbf{V}=$ linear feed velocity of the timber
$L_{1}=$ length of the sample
and where the suffix 1 indicates a once per revolution effect

This was illustrated by using the SSA to generate surface models exhibiting this "once per revolution" defect, and using the FFT algorithm to obtain the corresponding frequency spectrum (see figures 7.G0.S4).

It should be noticed that as imbalance increases, the amplitude of spindle eccentricity (runout) also increases. The trajectory of the knife whose radial direction and sense coincides with, or is closest to, that of the imbalance force will cut deeper into the timber; that of the knife whose radial direction and sense is opposite to the imbalance force will cut less deeply. As imbalance is increased, a critical point will be reached when the amplitude of the eccentricity is such that the knife opposite to the imbalance force will not contribute a knife mark to the final surface profile. At this amplitude of eccentricity, $\mathbf{d}_{\text {crit }}$, the number of knife marks in a given sample length would be ( $\mathbf{h}_{\mathbf{j}}-\mathbf{h}_{\mathbf{1}}$ ).

### 6.7.6.3 Proud Knives

As stated in Section 6.7.6.1, a perfectly functioning cutterhead would machine a surface profile whose FFT signature would contain a single peak at $\mathbf{h}_{\mathbf{j}}$. Incorporating a single proud knife, into this otherwise ideal cutterhead, would cause it to produce surface profiles whose FFT signatures contain additional, peak harmonics.

The positions of the additional peak harmonics are dependent on the depth and width of the proud-knife knifemark, and, its rate of recurrence. The peak harmonics which characterises such a profile, is very similar to the frequency
signature for a pulse train of comparable width, amplitude and frequency to the proud-knife knifemarks); the harmonic number of the peaks following and arithmetically progressing series which start at $h_{1}$ (see equation 6.3); the amplitude of the peaks diminishing with increase in harmonic number.

This was illustrated by using the SSA to generate a "proud-knife" surface profile (of sample length, $\mathbf{L}_{\mathbf{c}}(=0.125 \mathrm{~m})$ ) and using the FFT algorithm to obtain its frequency spectrum (see figure 6.16). A corresponding pulse train was also generated and transformed into the frequency domain for comparison (figure 6.17).

For a jointed, multi-knife finish, cutterheads with 4, 6, 8, and 10 knives are commonly used. With cutterheads possessing more than one proud knife, the degree of proudness of each individual knife and its possible angular position on the cutterblock are somewhat random functions but tend, in practice, to vary within certain limits:

The degree of proudness varies from zero to about $40 \mu \mathrm{~m}$ (Goddard M, Garrett J, 1986)

The possible angular location of the proud knife is dependant on the total number of knives on the cutterblock, $\mathbf{N}$, and the number of knives which are proud, $\mathbf{r}$. There will be a number of possible arrangements (permutations) of the proud knives around the cutterhead. The number of possible ways of arranging the proud knives on the cutterhead is:

$$
\begin{equation*}
\frac{\mathbf{N}_{\mathbf{P}}}{\mathbf{N}}=\frac{\mathbf{N}!}{\mathbf{N ( N - r ) !}} \tag{6.4}
\end{equation*}
$$

Thus:
Considering a 4-knife cutterblock, the number of ways of arranging:

2 proud knives is

$$
\frac{{ }^{4} P_{2}}{4}=\frac{4!}{4(4-2)!}=3
$$

3 proud knives is

$$
\frac{{ }^{4} P_{3}}{4}=\frac{4!}{4(4-3)!}=6
$$

Considering a 6-knife cutterblock, the number of ways of arranging: 2 proud knives is

$$
\frac{{ }^{6} P_{2}}{6}=\frac{6!}{6(6-2)!}=5
$$

3 proud knives is

$$
\frac{{ }^{6} P_{3}}{6}=\frac{6!}{6(6-3)!}=20
$$

4 proud knives is

$$
\frac{{ }^{6} P_{4}}{6}=\frac{6!}{6(6-4)!}=60
$$

5 proud knives is

$$
\frac{{ }^{6} P_{s}}{6}=\frac{6!}{6(6-5)!}=120
$$

Similar permutations can be calculated for the arrangement of proud knives on 8-knife and 10-knife cutterblocks.

As the number of knives on the cutterhead increases, the task of modelling the surface profiles produced by all the possible arrangements of proud knives becomes more tedious and complicated. The model experiences an even higher degree of tedium and complexity if the exact extent of the proudness of each knife is considered. Examples of "proud knife" surface models which were generated by the SSA and their corresponding frequency signatures are shown in figures 7.G0.S5a to 7.G0.S5f; here, each proud knife protrudes the nominal cutting circle diameter by exactly the same amount, $+8 \mu \mathrm{~m}$.

The frequency signature of the surface profiles show a distinct pattern or trend; as the number of proud knives is increased, the harmonic interval between $\mathbf{h}_{1}$ and $h_{j}$ becomes congested with dispersed local peaks (denoted, multi-modal), indicating a fault within the machining process.

### 6.7.6.4 Timber Vibration

There are no apparent patterns or rules which readily and clearly predict the frequency and amplitude of vibration of a workpiece which is machined while inadequately supported. Therefore the profile and frequency signature of a timber sample so machined can be somewhat unpredictable or random.

This fault requires further analytical investigation. The number of possible variables involved is considerable and if they are successfully identified many of their numerical values will be unknown. It is apparent that incorrectly supported timber will vibrate at some frequency (as its traversed across the machine table); this will be dependant on the forcing frequency, the mode of
workpiece support (ie. simply supported, cantilever, etc.), the dimensions, the elasticity/rigidity, characteristic damping factor of the timber and the masses and forces associated with the restraining components.

### 6.7.6.5 Single Knife Finish

The frequency domain description of a timber surface machined in single-knife-finish mode should contain a single peak or local maxima (similar to ideal, multi-knife mode machining) because the wave pitch should be uniform. The expected number of knife-marks, $\mathbf{h}_{\text {agl }}$, in a given sample length, $\mathbf{L}_{\mathbf{s}}$, is given by

$$
\begin{equation*}
h_{\text {agl }}=\frac{W L_{s}}{2 \pi V} \tag{6.5}
\end{equation*}
$$

where
$\mathbf{W}=$ angular velocity of the cutterhead
V = linear feed velocity of the timber
$L_{s}=$ length of the sample

The value of $h_{\text {agl }}$ is the same as principal harmonic $h_{1}$ (see equation 6.3)

### 6.7.6.6 Fault Finding Algorithm

Based on the above discussion a fault finding algorithm (FFA) was written, which, analyses the frequency signature (ie. the FFT), and attempts to detect any inherent "defects" in the surface's waveform. The FFA first scans the FFT to identify the harmonic with the maximum magnitude. The algorithm then searches through the FFT data for local maxima which are compared with an "arbitrary" threshold value, which is some fraction of the detected
maximum. Harmonics with amplitudes equal to, or greater than, this threshold are considered significant. The significant harmonics are then compared to a number of criteria (ie. the principal harmonics) which are dependent on the machining parameters used to produce the sample. Eventually, through a process of elimination, the nature or "cause" of the "fault" is identified. The structure of the FFA is as follows (see next page) and is listed in appendix A8:

## Structure of the Fault Finding Algorithm

```
Find maximum magnitude harmonic, \(h_{\text {peak }}\)
Scan FFT data
FOR harmonic \(=\) zero TO highest harmonic
    Check for local maxima
    IF \({ }_{1}\) local maxima
        THEN \({ }_{1}\)
            \(I F_{2}\) maxima \(>=\) threshold
                THEN 2
                \(\mathrm{IF}_{3}\) harmonic \(=\mathrm{h}_{1}\)
                        THEN \({ }_{3}\)
                                Check for local maxima between \(h_{1}\) and \(h_{j}\)
                                Keep record of any found
                                IF, none found
                        THEN4
                                "Fault" must be \(\mathrm{Ob}_{1}\) or Sk
                                Check for \(\mathrm{Ob}_{1}\) ie look for \(\mathrm{h}_{\mathrm{j}}\)
                                IFs \(h_{y}\) found
                            THEN 5
                                    record \(\mathrm{Ob}_{1}\) and \(h_{1}\) :to endif \(f_{5}\)
                            ELSE
                                    record Sk:to endifs
                                    MNDIF
                                    to endif 4
                            \(\mathrm{ELSE}_{4}\)
                                Could be proud knife
                                Check for proud knife
                                IFs proud knife
                        THEN 6
                        Keep record of proud knife:to endif.
                    ELSE
                                    Keep record of \(\mathrm{Ob}_{1}\) :to endif \({ }_{6}\)
                                    ENDIF 6
                                    EnDIF4
                                to endif \({ }_{3}\)
                EISE \(_{3}\)
                Must be some other fault
                        Try principal harmonics
                        IF7
                        IF harmonic \(=\mathrm{h}_{2}\) THEN fault must be \(\mathrm{Ob}_{2}\)
                                IF harmonic \(=h_{2}\) THEN single knife finish
                                    IF harmonic \(>h\), THEN high frequency vib.
                                    digital noise
                                    to endif7
                                    ELSE,
                                    Must be some other fault
                                    eg. combination of number of faults
                                    Call this a "Unknown fault":
                                    So store harmonic :to endif,
                                    ENDIE7
                                    to endif \({ }_{3}\)
                ENDIF 3
                to endif 2
            \(\mathrm{ELSE}_{2}\)
            EnDIF
        ELSE \(_{1}\) to endif \(f_{1}\)
    molr
NEXT harmonic
where \(h_{1}=\) once-per-revolution harmonic
    \(h_{2}=\) twice-per-revolution harmonic
    \(h_{j}=\) multi-knife finish harmonic
    \(h_{\text {sgl }}=\) single-knife finish harmonic
    Ob1 = once-per-revolution out-of-balance
    Ob2 = twice-per-revolution out-of-balance
```

See Appendix A8 for a listing of the FFA

## 7 RESULTS

### 7.1 Introduction <br> 7.2 Theoretical Results

### 7.2.1 Single-knife Finish

### 7.2.2 Multi-knife finish

7.2.2.1 Ideal Machining
7.2.2.2 Machining Faults
7.2.2.3 Fault Parameter Variation
7.3 Machined Timber Sample Results
7.3.1 Single Knife Finish
7.3.2 Cutterhead Imbalance
7.3.3 Proud Knives
7.3.4 Vibration: Timber, Spindle
7.3.5 Fault Combination

### 7.1 Introduction

In this chapter results from the machining investigations are presented. The theoretical results, based purely on the mathematical model (ie. the SSA (Chapter 4)), are presented in Section 7.2; those from the machined timber samples (see Section 6.6) are presented in Section 7.3.

### 7.2 Theoretical Results

The surface simulation algorithm (SSA) was used to generate a variety of theoretical profiles. These generated profiles, prefixed GO, are shown in figures 7.G0.S1 to 7.G0.S6 together with their corresponding FFT. Each figure also contains a record of the pertinent variables and parameters used in the SSA to produce the profile and the results of the analysis of the FFT spectrums using the Fault Finding Algorithm (FFA).

### 7.2.1 Single-knife Finish

Simulated, single-knife finish, profiles are presented in figures 7.G0.S1a. through to figure 7.G0.S1d

### 7.2.2 Multi-knife finish

Figures 7.G0.S2 to 7.G0.S6 illustrated simulated milti-knife finish surface profiles.

### 7.2.2.1 Ideal Machining

Simulated ideal machining finish profiles are presented in figures 7.G0.S2a through to figure 7.G0.S3a.

### 7.2.2.2 Machining Faults

Figure 7.G0.S3b to 7.G0.S3j introduced the simulated timber machining faults; they were eccentricity (out-of-balance cutterhead), proud knives and timber vibration.

### 7.2.2.3 Fault Parameter Variation

Figures 7.G0.S4, 7.G0.S5 and 7.G0.S6 illustrated the effect of varying the value of the machining fault parameters.

### 7.3 Machined Timber Sample Results

Each timber sample produced was categorised and numbered according to the type of fault induced on its surface profile. The captured data from each timber sample was presented graphically (figures 7.G1.S1 to 7.G5.S5). Each figure contains three data sets:

1) That captured by the laser instrument (LAS)
2) That captured by the Talyround 200 (TAL)
3) That generated by the surface simulation algorithm (SSA)

Directly beneath the graph of each captured data set is a histogram of its FFT spectrum or frequency signature. Underneath the three pairs of graphs are the machining parameters used to produce the timber sample and the results from assessing each FFT data set using the FFA.

The results presented here are a selection from many timber samples produced, and are divided into 5 main groups or categories:
(a) single-knife finish
(category G1)
(b) multi-knife finish
i) cutterhead imbalance
(category G2)
ii) proud knives
(category G3)
iii) timber vibration
(category G4)
(c) fault combinations

### 7.3.1 Single Knife Finish.

The first category of samples, G1, were generated using a single knife finish machining mode (see Section 6.6.4). The values of machining parameters and variables used are recorded in Table G1. The captured data corresponding to each timber sample is shown graphically in figures 7.G1.S1 to 7.G1.S8.

### 7.3.2 Cutterhead Imbalance

The second category of samples, prefixed G2, were machined using cutterheads with varying degrees of out-of-balance (see Section 6.6.1.3). The machining parameters and variables were as recorded in Table G2 while figures 7.G2.S1 to 7.G2.S12 contain the graphical representation of the captured data with their respective frequency signatures (FFT).

### 7.3.3 Proud Knives

The third category of samples, G3, investigated the proud knife fault (see Section 6.6.2). Table G3 shows a record of the machining variables and parameters used in the machining of the samples, while figures 7.G3.S1 to 7.G3.S15 show graphically the corresponding results obtained using the laser
instrument, talyrond 200 and surface simulation algorithm (SSA).

### 7.3.4 Vibration: Timber, Spindle

The forth category of timber samples, prefixed G4, were composed of those machined while the workpiece was inadequately supported or controlled (see Section 6.6.3). Table G4 shows the variables and parameters used, while figures 7.G4.S1a to 7.G4.S6c show, graphically, the associated captured data sets and their frequency spectra.

### 7.3.5 Fault Combinations.

The fifth category of timber samples, prefixed G5, were machined using process parameters and machining conditions which created surface profiles that combined the various process faults. The parameters and conditions were recorded in Table G5 an the results shown in figures 7.G5.S1 to 7.G5.S5.

## 8 DISCUSSION

### 8.1 Introduction

### 8.2 Hardware

### 8.2.1 Electronics

### 8.2.1.1 Host Computer

### 8.2.1.2 Photodiode Array

### 8.2.1.3 Data Acquisition

### 8.2.2 Optics

### 8.2.2.1 Helium-Neon Laser

### 8.2.2.2 Beam Expansion

### 8.2.3 Instrument Structure/Adjustment Mechanism

### 8.3 Software

### 8.3.1 Data Capture

### 8.3.1.1 Laser Instrument Data Capture

### 8.3.1.2 Talyrond 200 Data Capture

8.3.1.3 SSA Data "Capture"

### 8.3.2 Data Analysis

8.3.2.1 Fast Fourier Transform Algorithm
8.3.2.2 Fault Finding Algorithm

### 8.4 Machining Investigations

8.4.1 Theoretical Results
8.4.1.1 Single-knife Finish
8.4.1.2 Multi-knife finish
8.4.1.3 Superposed Machining Faults
8.4.1.4 Fault Parameter Variation
8.4.2 Timber Machining Results
8.4.2.1 Single Knife Finish
8.4.2.2 Spindle Eccentricity / Dynamic Balance
8.4.2.3 Proud Knives
8.4.2.4 Timber and Spindle Vibration
8.4.2.5 Fault Combinations
8.5 General Comments

### 8.1 Introduction

This chapter discusses the various aspects associated with, and the performance of the laser instrument for assessing the surface waviness of planed timber. Firstly the hardware is considered under three main subdivisions:

1) Electronics
2) Optics
3) Mechanics

Then the software associated with the instrument is addressed. This is dealt with under two main headings

1) Data Capture
2) Data Analysis

Finally the results of the investigation are examined. Here, theoretical results from the mathematical model (ie. SSA) are discusses followed by an examination of the results from the timber machining investigations.

### 8.2 Hardware

### 8.2.1 Electronics

### 8.2.1.1 Host Computer

The use of a BBC micro-computer as the Host proved useful as a development tool. It was a very versatile, programmable device with screen resolution germane to the application. However, there were inadequacies (such as its comparative low computing speed and its limited 8-bit capacity) which
became frustratingly apparent as the research progressed. So much so that in order to reduce computing time attempts were being made to convert the FFT algorithm to machine code version (Appendix A7). Before this was completed funding was secured to purchase a faster, higher capacity microcomputer. A 32-bit, RISC chip, BBC-Achimedes computer was acquired about two-thirds of the way through the research period which dramatically reduced computing time.

The physical size and cost of the computer and its many "redundant" components and functions, implies that it does not lend itself for incorporation into a feasible, compact instrument. What is required is a dedicated, chip level, system capable of performing the specific computing and logical tasks required. The system can be individually developed or it can be construct using a "building block" approach. The building blocks can be selected and interfaced into the system. For example, there are commercially available, DSP chips capable of preforming FFT on very large data sets in milliseconds (Gomez S, Gonzalez S, Hsu D, Kuo A. 1988) and numerous single chip microprocessors many of which have on board memory.

### 8.2.1.2 Photodiode Array

The photodiode array used in this research project performed the task required. The drive requirements were satisfied by a combination of commercially available drive cards and specifically designed interfacing. The spectral response characteristics of the array corresponded with the spectral frequency of the source of timber illumination thus effecting maximised signal
output.

The array produced a "noise free" signal despite it sometimes being used outside the linear region of its characteristic curve. This meant that the calculation of optimum photodiode integration period, estimated by the host computer, required more iterations than would otherwise be necessary. This obviously increased the data acquisition time.

The photodiode array's linear resolution ( $25 \mu \mathrm{~m}$ ) proved amply suitable for the application, allowing for a possible two-fold (100\%) increase (in resolution) should this be required.

The current application of the laser instrument is post-process; the desirable goal was to realise an in-process device. Thus the photodiode array will eventually be replaced by a single photodiode. This will, of course, imply different drive and timing requirements for data acquisition.

### 8.2.1.3 Data Acquisition - Auxiliary RAM and ADC

The interface between the photodiode array and the host computer performed the digitizing and temporary storage of the captured data as conceived. The conversion speed of the $A D C$ and the access times of the RAM proved appropriate for the application.

The rising edge of the ARRAY-CLOCK was used to clock the auxiliary RAM while the HIGH period of the ARRAY-CLOCK was used to write data to the
auxiliary RAM. The ARRAY-SAMPLE pulse is also triggered by the rising edge of the ARRAY-CLOCK. This inevitably meant that the data stored in memory location 0 was erroneous (that in locations 1 to 1023 were correct). Though this was not a serious loss, this quandary was catered for by copying into location 0 the contents of location 1023 (see line 3100 of the Interrupt Service Routine algorithm - Appendix A5.3). This served to reduce any rapid change in amplitudes between the last data sample and the first, which may give rise to high frequency noise when the FFT is applied.

### 8.2.2 Optics

### 8.2.2.1 Helium-Neon Laser

The low-power ( 5 mW ), helium-neon laser was used as a source of illumination because monochromatic light precludes aberration problems and presents a beam of uniform and constant density. The major disadvantage with the illumination source in its present form is its bulkiness. It is too large to be incorporated into a compact instrument. There are more compact semiconductor lasers which may be investigated with a view to possible replacement.

Another possible source of concern is the 15 minute warm-up period required by the current laser (see laser specification: Appendix B1). This may present unacceptable time delays in the commercial use of the instrument.

### 8.2.2.2 Beam Expansion

As detailed in Section 5.3.2, the cross section of the beam was expanded using a "home made" collimator. This component was designed and manufactured using rather limited optics expertise. It was certainly less sophisticated than commercially available collimators, but cost substantially less.

The performance of the home made collimator, however, did not seem to adversely affect the effectiveness of the instrument, although its consistency in producing a uniform density broad beam was a cause for concern. This inconsistency seemed to be caused by the use of incorrect fixing screws used to hold the collimator to the laser. The tapped screw threads in the laser became damaged and the collimator was not always securely held in the correct position (ie. collimator axis did not always align with the laser's axis).

The enlarged diameter of the illuminating laser beam was appropriate, thus alleviating the need for elaborate image and object alignment mechanisms.

### 8.2.3 Instrument Mechanism/Adjustment Mechanism

Although the adjusting mechanisms and locking mechanism performed the tasks for which they were designed some difficulty was experienced in aligning the image with the photodiode array and in insuring that only 125 mm of the timber surface was sampled. This was in part due to the primitive nature of the designs and lack of optical tools. The design tolerances were not realized in the manufacture, so that some intended sliding fits turned out to be very loose or erratic.

The fine and coarse focusing mechanisms of the imaging lens functioned according to plan and the spring loaded timber clamp was efficient in holding the timber samples against the datum face of the T-shaped framework. The hinged doors of the dark-housing allowed access to the various components of the instrument and was effective in excluding ambient light from the photodiode array.

The angle of incidence of the illuminating beam was accurately controlled by the micrometer/spring arrangement.

### 8.3 Software

### 8.3.1 Data Capture

### 8.3.1.1 Laser Instrument Data Capture

The capture of data from the timber samples using the Laser instrument (Section 5.5 and 6.7.2) was successful and consistent. The use of "automatic gain control" in acquiring the data set meant that the resolution of the ADC was always fully exploited and the best signal to noise ratio guaranteed.

Being iterative, the data capture algorithm (Appendix A5.1) required an initial start point or estimate of the integration period in order to approximate an optimum period. The closer the initial guess was to the required value the shorter would be the time required to calculate the optimum integration period.

In the algorithm the value of $\mathbf{C \%}$ was used to represent the estimated integration period and was given an empirically derived, initial value of 2000 (the final value of $C \%$ being used as representative of the optimum integration period). There were occasions when this initial value of $\mathrm{C} \%$ was so much in error that the algorithm failed (or took an unacceptably long period) to converge to the optimum integration period. When this happened the data-capture attempt was abandoned and the initial estimate of $\mathrm{C} \%$ revised manually.

This problem requires a more sophisticated solution. For example, the algorithm could be altered to monitor the value of $C \%$ so that if its value crosses a certain threshold the algorithm is re-initiated with a more appropriate initial value for $\mathrm{C} \%$.

The integration periods for the photodiode array could have been more accurately timed; instead of using a FOR-NEXT loop, one of the counters/timers in the PIA could have been employed. This will increase the repeatability and constancy of the instrument.

### 8.3.1.2 Talyrond 200 Data Capture

The capture of data from the timber samples using the talyrond 200 was successful and consistent. The method relied a ten-bit analogue to digital converter ( ADC ) with synchronising and control signals from a BBC microcomputer for the capture of data.

The Talyrond 200 is a well established, reliable instrument, with high resolution and accuracy, and was used during this research as a credible reference.

### 8.3.1.3 SSA Data "Capture"

The mathematical model on which the SSA is based is very rigorous and caters for a wide range of timber machining parameters and conditions. The conditions that it does not presently accommodate are timber slippage and sudden variation in timber feedspeed. It also needs to be modified to deal more appropriately with the various modes of timber vibration / regimes of timber support. The SSA is very accurate, versatile and has proved to be a useful tool, giving insight into machined timber profiles.

The resolution of the profile can be varied by changing the number of data points generated in a given sample length. This, of course, has the disadvantage of requiring more time to generate the profile and analysis.

### 8.3.2 Data Analysis

### 8.3.2.1 Fast Fourier Transform Algorithm

The FFT algorithm performed well the task of converting the captured data into the frequency domain. There was, however, much frustration with the time taken to complete the transform of 1024 data points. Various techniques were employed to reduce the execution time.

The first was as follows; rather than calculating the sine and cosine values
during FFT execution, a data look-up table of the sine and cosine coefficients was generated prior to run-time and referenced, at various stages, during execution. This provided a significant speed advantage over run-time computation, the only drawback being the memory requirement to store the data in the look-up table.

The second technique was to arrange so that the number of data points to be transformed was as close as possible to, but above, the Nyquist limit of 250 (ie. 256, which also satisfies the decimation-in-time FFT criteria that the number of data point to be transformed must be some power of 2). Although this greatly reduced the computing time, in a number of instances aliasing resulted, due to foldover of sidelobes (Rabiner L.R, Gold B, 1975b) whose frequencies were greater than the Nyquist limit. This was remedied by increasing the number of data points in the sample length to 512.

The third technique was to convert the algorithm from BBC BASIC to machine code (Appendix A6). As mentioned above this was abandoned due to the limited capacity of the BBC-Master computer and the purchase of a 32bit BBC Archimedes computer which implemented the algorithm in approximately 7.38 seconds (compared to the original 4.75 minutes). Also, mentioned above, there are dedicated DSP chips available (Gomez S, Gonzalez S, Hsu D, Kuo A, 1988) that can perform the FFT (in a few milliseconds), which can be used to supersede the present algorithm.

### 8.3.2.2 Fault Finding Algorithm (FFA)

The FFA analysed the FFT data by initially searching through the harmonics for local maxima and deciding if they were of significance by comparing the peaks with a specified threshold value. Then, the number of the significant harmonics were compared with the number of the principle-harmonics. Hence by a prioritised process of elimination the cause of the surface quality was identified (see Section 6.7.6.6).

The FFA is presently in a primitive/embryonic form. The algorithm is proficient at detecting machining faults such as cutterhead eccentricity (out-of-balance and runout) and proud-knives provided that the FFA threshold used is not too low. The threshold value currently used (0.4) was arrived at by an empirical, trial and error approach. With ideally machined surfaces, multi-knife or single-knife finish, the FFA proved effective.

The FFA failed to record totally accurate results when analysing frequency signatures from samples produced by cutterheads whose degree of imbalance was such that the magnitude of the eccentricity induced meant that there was a tendency for only N-1 knife-marks to be left on the machine surface for every one revolution of the cutterhead (see Section 6.7.6.2). This was because the FFA was not contrived to investigate this "secondary" phenomenon; the FFA can of course be modified to incorporate this.

### 8.4 Machining Investigations

### 8.4.1 Theoretical Results

A selected set of results, generated using the SSA, are shown in figures 7.G0.S1 to 7.G0.S6. The variables used in producing the examples were chosen so as to keep their graphical display within the screen's resolution. The results in this section were generated to demonstrate the versatility of the mathematical model and the SSA and to highlight the features of the FFA.

### 8.4.1.1 Single-knife Finish

Figure 7.G0.S1 presents surface profiles produced using single-knife finish (Section 6.6.4). The one proud knife in position 1 "satisfied" the un-jointed nature of the single-knife method. A 6-knife cutterhead with rotational speed of 5000 rpm was used and only the value of the timber speed was varied in figure 7.G0.S1.

In figure 7.G0.S1a a timber feedspeed of $7.5 \mathrm{~m} / \mathrm{min}$ resulted in a surface wave pitch of 1.5 mm (see equation 6.1). This gave a dominant peak at harmonic 83 in the FFT, as expected; there are diminishing side lobes associated with harmonic 83 (ie. harmonics 167,250 and 179) which are due to the effects of windowing (Rabiner L.R, Gold B, 1975a), see figure 5.6.11, Section 5.6.1.8. It should be noted that aliasing of the one of the side lobes has occurred in figure 7.G0.S1a. Harmonic 179 is actually harmonic 333 which has been "folded back" down the spectrum about the Nyquist frequency (256), ie.179=256-(333-256).

The analysis of the FFT by the FFA (threshold=0.4) concluded that the finish was that produced by the single-knife cutting mode, giving a dominant peak at harmonic 83.

Similarly, in figure 7.G0.S1b a timber feedspeed of $10 \mathrm{~m} / \mathrm{min}$ resulted in a surface wave pitch of 2 mm . This gave a dominant peak at harmonic 62 in the FFT. Again, there were diminishing side lobes at harmonics 125, 189, 250, 200 and 137 of which harmonic 200 and 137 were aliases of harmonics 311 and 373, respectively. The FFA analysis concluded that the finish was that produced by the single-knife cutting mode, with the dominant harmonic at 62 .

In figures 7.G0.S1c and 7.G0.S1d the timber feedspeed was increased to 12.5 $\mathrm{m} / \mathrm{min}$ and $15 \mathrm{~m} / \mathrm{min}$, respectively. Resulting in corresponding dominant harmonics at 50 and 42. In each figure there are the usual side lobes but no aliasing has occurred since the side lobes decayed to "zero" within the specified bandwidth.

The respective FFA analysis of each FFT data set concluded that the profile was consistent with that of single-knife finish. However, in figure 7.G0.S1d the stated value of $h_{1}(=41)$ varied by 1 compared to actual dominant peak value (=42) in the FFT. This was because the value of $h_{1}$ was quoted in integer form and thus had a tolerance of $\pm 1$.

### 8.4.1.2 Multi-knife finish

Figures 7.G0.S2 to 7.G0.S6 presents simulated surface profiles produced using multi-knife finish, under ideal conditions (Section 6.6), and demonstrates the effects of variation in parameters and their superposition.

Figure 7.G0.S2 deals with the variation of the basic parameters:

1) Number of Knives per cutterhead
2) Timber feedspeed
3) Cutterhead rotational speed

In figure 7.G0.S2a the number of knives on the cutterhead was 6 , the timber feedspeed was $90 \mathrm{~m} / \mathrm{min}$ and the rotational speed was 5000 rpm (these can be considered as the "nominal" values of variables for figure 7.G0.S2). The relationship between the feedspeed and rotational speed was such that each knife leaves a finish mark. There were no proud knives, hence the cutterhead is considered to be jointed $\left(h_{j}=41 \pm 1\right)$. This resulted in an ideal, simulated surface profile whose frequency spectrum had a peak at harmonic 42 and diminishing side lobes, approximately every 42 harmonics thereafter. This multi-knife, finish was detected in the FFT spectrum by the FFA, using a threshold of 0.4 .

In figure 7.G0.S2b the feedspeed was increased to $100 \mathrm{~m} / \mathrm{min}$, with number of knives and rotational speed unchanged, increasing the wave pitch $\left(h_{j}=37 \pm 1\right)$, and giving a spectrum with a peak at 38. The FFA again detected this.

In figure 7.G0.S2c the feedspeed was reduced to $80 \mathrm{~m} / \mathrm{min}$, with number of knives and rotational speed unchanged, decreasing the wave pitch ( $h_{j}=46 \pm 1$ ), and giving a spectrum with a peak at 47. Again, the FFA detected this.

Figure G0.S2d and G0.S2e shows the profile and spectrum of a simulated surface generated using the nominal values except that the rotational speed was varied; in the first instance it was increased to 6000 rpm , in the second it was reduced to 4000 rpm . The quicker rotational speed resulted in a smaller wave pitch $\left(h_{j}=50 \pm 1\right)$, with harmonic 50 being dominant; the slower speed gave a courser wave pitch $\left(h_{j}=33 \pm 1\right)$, with dominant harmonic at 33 . In each case the FFA accurately detects the multi-knife nature of the profile.

In figures 7.G0.S2f and 7.G0.S2g the number of knives are varied from the nominal value; firstly it is increased to $8\left(h_{j}=55 \pm 1\right)$, and then reduced to 4 $\left(h_{j}=27 \pm 1\right)$, giving respective peak at 56 and 28 . In each case the FFA detected the multi-knife nature and dominant harmonic of the simulated profile.

### 8.4.1.3 Superposed Machining Faults

Figure 7.G0.S3 introduced the machining faults; eccentricity (called here out-of-balance), proud knives and timber vibration. They were each introduced in turn and superposed onto the ideal finish; later these same faults were combined, permutated and superposed, again onto an ideal surface.

Figure 7.G0.S3a started with the nominal values, giving the ideal machined
surface as before.

Then, in figure 7.GO.S3b, a once per revolution eccentricity (out-of-balance) with amplitude of $8 \mu \mathrm{~m}$ was featured ( $h_{1}=6 \pm 1, h_{j}=41 \pm 1$ ). The undulating nature of the knife-marks can be clearly seen in the generated profile; the FFT peaking at harmonics 7 and 42 and the FFA (threshold=0.4) detected the two peaks.

In figure 7.G0.S3c the out-of-balance was removed and replaced with a proud knife ( $10 \mu \mathrm{~m}$ ) in position number 4. The proud knife marks can be seen on the profile as can the proud-knife, characteristic peaks at harmonics 7, 14, 21 and 28 of the FFT spectrum. The multi-knife finish of the profile transformed to a peak at harmonic 42. The FFA (threshold=0.4) detected both proud-knife and multi-knife conditions.

Figure G0.S3d introduced timber vibration to the ideal surface $\left(h_{\mathrm{j}}=41 \pm 1\right)$. The timber vibration (four cycles during the period of knife engagement with the timber) was specified and superposed onto the ideal surface. For each knife, only two (of the four) vibration cycles contributed to the final surface finish. Hence the peak at harmonic 83. The FFA analysis verified this.

Figure 7.G0.S3e combined two of the simulated faults, the proud knife (position 4) and out-of-balance ( $h_{1}=6 \pm 1$ ), and superposed them onto the ideal surface $\left(h_{j}=41 \pm 1\right)$. This resulted in a frequency signature that peaks at 42 (multi-knife finish) and the "pulse train" peak harmonics at 7, 14, 21 and 28.

The effect of the out-of-balance is masked by the proud-knife component at harmonic 7. However, comparing harmonic 7 in figure 7.G0.S3e with harmonic 7 in figure 7.G0.S3c, it is evident that harmonic 7 in figure 7.G0.S3e is of greater magnitude than that in figure 7.G0.S3c. This is because the out-of-balance component $\left(\mathbf{h}_{\mathbf{1}}\right)$ has reinforced the amplitude of harmonic 7. This, however, is not detected by the FFA in its present configuration; all it "sees" is the proud-knife effect. So some modification or "fine-tuning" of the FFA may be required.

Figure 7.G0.S3f combined the proud knife (in position 4) and out-of-balance ( $h_{1}=6 \pm 1$ ) faults, and superposed them onto the ideal surface ( $h_{y}=41 \pm 1$ ). This resulted in a frequency signature that peaked at harmonics 7 (out-of-balance), 42 (multi-knife finish) and 83 (timber vibration). The FFA accurately detected these.

Figure 7.G0.S3g combined the proud knife (in position 4) and timber vibration (4 cycles per knife cut) faults, and superposed them onto the ideal surface $\left(h_{j}=41 \pm 1\right)$. This resulted in a frequency signature with peaked at harmonic 42 (multi-knife finish) and 83 (timber vibration), and "pulse-trains", starting at harmonic 7. The FFA accurately detected these features.

All three faults were combined in figure 7.G0.S3h resulting in the expected frequency spectrum and FFA analysis. Figure 7.G0.S3i and 7.G0.S3j reflected the same conditions but the FFA employed reduced thresholds of 0.1 and 0.05 respectively. Notice the extension to the number of peak which constitutes
a proud-knife fault and to the number of harmonics attributed to timber vibration or noise. This, to some extent, illustrates that caution must be applied in selecting the threshold value when using the FFA in its present form.

### 8.4.1.4 Fault Parameter Variation

Figures 7.G0.S4, 7.G0.S5 and 7.G0.S6 illustrated the effect of varying the value of the fault parameters:

Figure 7.G0.S4a to 7.G0.S4d showed variations in the amplitude of the eccentricity (out-of-balance). The amplitudes varied from 2 microns through to 12 microns. In each case the shape of the FFT is as predicted. (In the case of figure 7.G0.S4a, where the eccentric amplitude was 2 microns, the FFA failed to detect the unbalance because the threshold of 0.4 was too high.)

In figure 7.G0.S4d there were "additional" peaks at harmonics 28 and 39. These "extra" harmonics can be accounted for as follows:

As the cutterhead spindle undulates due to eccentricity, the depth of cut of each knife will vary depending on its angular position; those cutting when the spindle is at a trough will cut deeper than those cutting when it at a crest. Hence the width (and depth) of the knife-mark will vary from a maximum through to a minimum and back to maximum, as cutting continues. The frequencies of
the sine waves in the FFT that synthesise the surface waveform will also account for this variation in the depth and width of the knife-mark. This is accounted for in the FFT by the emergence of the "extra" peaks at harmonics 28 and 39 . The "lower" harmonic, $\mathbf{h}_{\mathrm{jlo}}$ (=28), accounts for the widening and deepening of the knife-marks at the troughs; the "higher" harmonic, $\mathbf{h}_{\mathrm{jhi}}(=39)$, is associated with the shallowing and narrowing of the knifemarks at the crests. This effect can be seen in other examples such as figures 7.G0.S4b and 7.G0.S4c.

As the magnitude of the eccentricity increases its value will approach $\mathbf{d}_{\text {crit }}$ (Section 6.7.6.2). At this stage the knife that cuts at the crest of the undulation does not contribute a knife-mark to the final surface finish. So effectively, there are only N-1 knives cutting (hence one less knife-mark per revolution of the cutterhead) giving rise to an FFT signature with a peak at harmonic $\mathbf{h}_{\text {dcrit }}$. The value of $\mathbf{h}_{\text {derit }}$ is given by

$$
\begin{equation*}
\mathbf{h}_{\mathrm{dcrrt}}=\mathbf{h}_{\boldsymbol{j}} \cdot \mathbf{h}_{\mathbf{1}} \tag{8.1}
\end{equation*}
$$

As the magnitude of the eccentricity increased from zero to $\mathbf{d}_{\text {crit }}$, so the amplitude of the "shallowing" harmonic, $\mathbf{h}_{\mathrm{jh}}$, reduces while that of $\mathbf{h}_{\mathrm{jo}}$ increases (see figures 7.G0.S4e and 7.G0.S4f). Note that

$$
\begin{equation*}
h_{j h i}=h_{j}+h_{1} \tag{8.2}
\end{equation*}
$$

and

$$
\begin{equation*}
h_{10}=h_{j}-h_{1} \tag{8.3}
\end{equation*}
$$

Figure 7.G0.S5a to 7.G0.S5f show variations in the number, and position, of proud knives. The total number of knives on the cutterhead was increased to 8 and each proud knife protruded by the same amount, 8 microns.

Figures 7.G0.S5a and 7.G0.S5b shows the surface due to one proud knife, placed in position 1 and 5 , respectively. The FFT's exhibits the typical "pulse-train" effect and the FFA successfully determined the faults which caused the surface.

Figures 7.G0.S5c and 7.G0.S5d features 2 proud knives. The first had the proud knives in cutterhead positions 1 and 3 the other in positions 1 and 6. The FFT signatures generated differ from those characteristic of a single, proud-knife finish. The peaks that appear between $h_{1}$ and $h_{j}$ are not regularly spaced or necessarily positioned in order of descending magnitude. Although in figure 7.G0.S5d the FFA was "successful" in detecting "the proud knife", in figure 7.G0.S5c it failed.

Similarly, in figures 7.G0.S5e and 7.G0.S5f where 3 proud knives are featured in positions as specified, the FFTs of the surface profile take on yet different "shapes", with unsuccessful results
when the current FFA was applied.

The FFA in its present form does not contend well with detection of more than one proud knife. It presently searches only for the "pulse-train" type effect in the FFT signature. In figure 7.G0.S5c the pulse train (ie. peaks at harmonics $6,12,18,24, \ldots$ ) is missing, resulting in an incorrect diagnosis. However, the FFA did report "unknown faults" at harmonics 17,22 and 28 . The algorithm obviously needs modifying. One possibility would be to study these "unknowns" and establish the pattern or trend in the FFT which emanates from these types of faults and incorporate this into the detection process of the FFA. Another would be to create FFT "templates" of known faults and cross-correlate them with the unknown FFT signatures. Yet another would be to infer that if more than one peak is found between $h_{1}$ and $h_{j}$, this would constitute some form of proud-knife fault and allow the FFA to conclude as such, without specifying further details.

Figure 7.G0.S6a to G0.S6d shows variations in timber vibration rate. The rate was changed from 6 through to 12 in increments of 2 . (To prevent loss of discrimination, due to the host computer's screen resolution, during the variation of timber vibration rate the nominal rotational speed was reduced from 5000 rpm to 4000 rpm ).

In figure 7.G0.S6a the peak at harmonic $33\left(=\mathbf{h}_{\mathbf{\prime}}\right)$ indicated a
multi-knife finish while the peak at harmonic 100 corresponded to timber vibration, $\mathbf{h}_{\mathbf{V}}$. The effect of vibration is very similar in result to that of spindle eccentricity; the consequence of the vibration is more marked at the trough of the knife-mark than at either flank. Hence, associated with vibration harmonic, $\mathbf{h}_{\mathbf{v}}$ ( $=100$ ), is a lower, "deepening" harmonic, $\mathbf{h}_{\mathrm{vd}}(=67)$ and a higher, "shallowing" harmonic, $\mathbf{h}_{\mathrm{vs}}(=133)$, where

$$
\begin{equation*}
h_{\mathrm{Vd}}=h_{\mathrm{r}}-h_{\mathrm{H}} \tag{8.4}
\end{equation*}
$$

and

$$
\begin{equation*}
h_{v s}=h_{v}+h_{j} \tag{8.5}
\end{equation*}
$$

Similar results are shown in figures 7.G0.S6b to 7.G0.S6d. At present in the actual machining of timber the value of $\mathbf{h}_{\mathbf{V}}$ is unpredictable, due to the lack of a governing mathematical relationship and large number of unknown variables that govern it.
(It should be noticed that in figure 7.G0.S6b the FFA detected a peak at harmonic 133 because its amplitude was above the threshold of 0.4 . (due to reinforcement). This failing is partly due to the vagueness of the criterion used for detecting timber vibration (because of its current unpredictability) and the arbitrary choice of threshold).

### 8.4.2 Timber Machining Results

Figures 7.G1.S1 to 7.G1.S5 show examples of data captured from timber samples using the laser instrument and the talyrond 200, and, profiles generated using apposite variable values in the SSA. Each figure has boxes which feature:

1) the captured (or generated) data and its FFT,
2) the machining parameters used,
3) the associated principle peak harmonics
and 4) the result of analysing each FFT using the FFA.

The samples from the machining investigation were subdivided into 2 main groups:

1) Single-knife finish
2) Multi-knife finish
which broadly classified the type of "fault" or the condition of the machine at the time of machining. Multi-knife finish was further sub-divided into four groups:
3) Spindle Eccentricity/Cutterhead Imbalance
4) Proud knives
5) Vibration
6) Fault combinations

Figures 7.G1.S1 to 7.G1.S8 present data from samples produced using singleknife finish; figures 7.G2.S1 to 7.G2.S12 deal with spindle eccentricity;
figures 7.G3.S1 to 7.G3.S15 is concerned with proud-knives; figures 7.G4.S1 to 7.G4.S6 addresses samples subjected to timber vibration; finally figures 7.G5.S1 to 7.G5.S5 present data captured from timber samples featuring combinations of machining faults.

### 8.4.2.1 Single Knife Finish

## (Refer to Table G1)

In figure 7.G1.S1 a significant peak can be seen at harmonic $h_{1}(=37 \pm 1)$ on the spectrum of each data set. This was as expected for the machining parameters used, and, the FFA analysis detected a single-knife finish in each case.

There is also a significant peak at harmonic 1 in the FFT of the laser data, which is absent in the data captured using the talyrond and that generated by the SSA. This difference can be explained as follows:

The amplitude of the reflected light from sample G1.S1 showed considerable variation throughout the particular sample length considered. This was because the timber sample was resinous; the sites where the resins was high in concentration reflect light less efficiently and corresponded to regions where the reflected light intensity was relatively low; the areas of low resin concentration more effectively reflected light and corresponded to regions where the reflected light intensity was relatively high. This variation accounted for the comparatively large amplitude of
the very low harmonics (harmonics 1 and 2 ) in the spectrum. The idea that the significant peaks at very low harmonics were not due to a machining fault is substantiated by the fact that the amplitude of the very low harmonics in the FFT of data captured (from the same region of the same sample) using the Talyrond were comparatively small.

This phenomenon - resin significantly affecting the amplitude of the reflected light - was witnessed to varying degrees throughout the research; typical examples, in the investigation of single-knife finish, are figures 7.G1.S3, 7.G1.S4, 7.G1.S5 and 7.G1.S7. This is not a major drawback to the surface-form-analysis technique, however, because, in timber the resinous grains are always "very-long-wavelength" in nature, compared with the surface waves produced by the machining operation. For this reason, in developing the philosophy of the FFA, the very low harmonics of the FFT were ignored.

Timber sample number G1.S6, (see figure 7.G1.S6) had peaks at harmonic 42 when one was expected at harmonic $h_{1}(=37 \pm 1)$. This large discrepancy can be explained in terms of timber slippage:

At the time of machining the efficiency of the timber feed mechanism was less than $100 \%$. This meant that the timber was travelling slower (due to slippage) than the reading indicated by the drive unit, hence inducing a finer machined surface wave pitch than anticipated (an error of some $+\mathbf{1 6 \%}$ ).

In its present form the FFA cannot detect the fact that slippage has occurred and can only report "unknown fault". When this was discovered hand timing, with a stop watch, was employed to double check the readings indicated by the drive unit.

It is anticipated that great difficulty will be encountered in effecting an algorithm which readily detect timber slippage using the FFT data. One method of circumventing the problem is to use a rolling contact encoder which accurately monitors the timbers feed speed; instead of relying on erroneous data obtained from the drive unit's gearbox.

The other timber samples in the "single-knife" category show consistent results and good correlation between the data sets.

### 8.4.2.2 Spindle Eccentricity (Dynamic Balance)

(Refer to Table G2)
Samples G2.S1, G2.S2 and G2.S3 were produced using ideal machining conditions (see figures 7.G2.S1, 7.G2.S2 and 7.G2.S3). The samples which followed these, G2.S4a to G2.S4c were produced the same cutterhead, but, having induced it with varying degrees of imbalance (1 screw, 2 screws, 3 screws or 5 screws) (see figures 7.G2.S4a, 7.G2.S4b and 7.G2.S4c). (In the SSA each screw is deemed to induce a eccentricity of $1 \mu \mathrm{~m}$ )

In figure 7.G2.S4a the frequency signature resulting from the laser instrument and the talyrond 200 both have a peak at harmonic 40 , compared
to a peak at harmonic 38 in the SSA generated data set. The difference in can be explained in terms of timber slippage during machining. However, the harmonic value falls within the tolerance band of $h_{y} \pm 2$ specified in the FFA. Hence, analysis of the FFT signature produced the favourable verdict of "multi-knife" finish. The induced out-of-balance, though present and visible (at harmonic 10), its amplitude was below the FFA threshold value used, hence the fault was not detected.

In sample G2.S4b, during the production of which the cutterhead imbalance was increased by one increment, showed, as expected, a more pronounced peak at $\mathbf{h}_{1}(=9 \pm 1)$ than in sample G2.S4a. Harmonic $h_{j}(=38 \pm 1)$ showed comparable relative amplitude. Similarly in sample G2.S4c where before machining the value of cutterhead balance was increased by a further increment, the frequency spectrum peaked, as expected, at the principle harmonics, $h_{1}$ and $h_{y}$.

It is further noticed that as the value of cutterhead imbalance increased the amplitude of $\mathbf{h}_{\mathrm{jb}}(=28)$ and $\mathbf{h}_{\mathrm{jb}}(=47)$ - the "deepening" and "shallowing" harmonics - were significantly enhanced. Again (probably due to slippage) there was some variation in the theoretical peak harmonics and those associated with the timber sample.

Sample G2.S5 was produced using a jointed, six-knife cutterhead rotating at 6000 rpm with a timber feedspeed of $80 \mathrm{~m} / \mathrm{min}$. Analysis of the captured data (from laser instrument and talyrond) revealed two major peak in the FFT
signature; one, as expected, at harmonic $h_{j}(=56 \pm 1)$, the other (unexpected) at harmonic 17. The SSA generated data had just the one expected peak at harmonic $h_{j}$. The FFA analysis revealed that harmonic 17 corresponded to a twice-per-revolution, out-of-balance defect. However there were other "peaks" in the vicinity of harmonic 17 (such as harmonics 13 and 22) and neighbouring harmonics of considerable amplitude. Visual examination of the sample confirmed a poor surface finish. The cutterhead was again jointed and sample G2.S6 machined. This proved to be a much improved surface with only one peak (harmonic $\mathbf{h}_{\mathbf{f}}$ ) in the FFT.

Samples G2.S7a and G2.S7b were also machined using the same machining parameters as G2.S6 but with progressively induced, incremented imbalance. Figure 7.G2.S7a and 7.G2.S7b show the data obtained. Here, again, the faults are highlighted by the significant peaks in the FFT signatures, and are correctly diagnosed by the FFA. In figure G2.S7b the peaks at approximately harmonics 47 and 66 (ie. $h_{j o}$ and $h_{j h i}$ ) are very prominent.

Similar results were obtained with other timber samples that were machined with out-of-balanced cutterheads. Figures 7.G2.S8 to 7.G2.S12 catalogue the results.

Sample number G2.S9b is note worthy (see figure 7.G2.S9b); here the process of replacing the 5 fixing screws to induce cutterhead imbalance seem to have dislodged the knife, thus producing an out-of-balance, proud-knife condition. This is detected in the FFT signature by the FFA.

### 8.4.2.3 Proud Knives

(Refer to Table G3)
The timber samples with the prefix G3, were produced to investigate the proud-knife phenomenon. Samples number G3.S1 and G3.S8 were produced using ideal machining conditions (see figures 7.G3.S1 and 7.G3.S8). The other samples in the group were produced using cutterheads with various arrangements of proud knives.

Figures 7.G3.S2 to 7.G3.S4 present the results for samples machined with the cutterhead having one knife proud of the nominal cutting circle. The amount of proudness was varied in increments (of about $4 \mu \mathrm{~m}$ ) starting at about $4 \mu \mathrm{~m}$.

The results were as predicted, showing the characteristic "pulse-train" effect associated with a single proud-knife, the magnitude of the harmonics due to the proud knife increasing as the proudness was incremented. The FFA successfully detected the proud knife fault from the FFT signatures.

Before machining sample number G3.S6, two adjacent knives on the cutterhead were caused to be proud. The subsequent results are shown in figure 7.G3.S6 which revealed a slightly different FFT signature to that produced by the single proud-knife. Similarly, with sample number G3.S7 where knife numbers 1 and 3 were caused to be proud before machining, the FFT signatures show a "proud-knife" fault (figure 7.G3.S7).

Sample G3.S8, machined under ideal conditions, was used as a reference for comparing the other "proud-knife" samples in its family (samples G3.S8 to G3.S11). The second member of the family was sample G3.S9 in which one knife was proud of the nominal cutting radius by about $4 \mu \mathrm{~m}$. The degree of proudness was increased to about $8 \mu \mathrm{~m}$ and $12 \mu \mathrm{~m}$ for samples G3.S10 and G3.S11, respectively. The corresponding figures show the results for each sample. The FFT signatures (and FFA results) show the expected outcomes for samples G3.S9 and G3.S10.

However, the results for G3.S11 showed some inconsistency; the FFT of the laser data did not show the characteristic "pulse-train" effect - there were significant harmonics between $h_{1}$ and $h_{j}$ which did not correspond to any of the principal or expected harmonics - whereas the talyrond 200 results revealed the anticipated FFT signature. This difference could not be readily explained. It is suspected that the two data sets did not originate form the same timber sample - a mistake may have been made in the labelling of one of the data sets.

Sample number G3.S12 (see figure G3.S12) was machined using a 8 -knife cutterhead under ideal conditions. The same machining parameters were used to produce samples G3.S13 and G3.S14 (figures 7.G3.S13 and 7.G3.S14) except that one knife was ground so its cutting edge was below the cutting radius of the jointed knives. The proudness values were approximately $-4 \mu \mathrm{~m}$ and $-8 \mu \mathrm{~m}$ respectively. In each sample the proud-knife, pulse-train effect was apparent, and was detected by the FFA.

Figure 7.G3.S15 shows the result for sample number G3.S15, which was machined using a cutterhead with two knives (in positions, diametrically opposed), having proudness values of approximately $-8 \mu \mathrm{~m}$. The FFT signatures for this sample show a distinct difference to the others machined using proud knives. Because the arrangement of the knives is symmetrical, the frequency of knifemarks due to the proud-knifes is doubled. Hence the first peak or significant harmonic in the FFT signature is $16 \pm 1$ and not $8 \pm 1$. The FFA did not cope with this, and concluded that the fault was a twice-perrevolution fault (O.balance2) with significant "unknown" faults at harmonics 33 and 50.

### 8.4.2.4 Timber and Spindle Vibration

(Refer to Table G4)
Samples in group G4 deal with vibration. Figures 7.G4.S1 to 7.G4.S6 shows the results from investigations into the effect of timber support (or timber control) and spindle support on the surface waviness/quality produced. The mathematical modelling of the various modes of timber vibration is so deficient that the SSA cannot be reliably used as a predictive tool. Hence, ideal machining parameters were used to generate the SSA data which corresponded to each timber sample.

The first two timber samples (G4.S1a and G4.S1b) were produced under "single-knife" cutting conditions. The first (see figure 7.G4.S1a) had an ideally machined surface (machine fully set), while the second (see figure 7.G4.S1b) was machined without the use of the chipbreaker. There is a
difference between the FFTs obtained from the two samples; the ideal has only one significant peak (harmonic $37 \pm 1\left(=h_{1}\right)$ ) in its FFT signature; that machined without the chipbreaker has two significant peaks, one at $\mathbf{h}_{\mathbf{1}}$ the other at harmonic 27. The FFA failed to detect the peak at the 27th harmonic because of the strategy adopted by the algorithm - that of essentially searching for the principal peaks, $\mathbf{h}_{\mathbf{1}}$ and $\mathbf{h}_{\mathbf{j}}$, and when found looking for other significant peaks in between them. Hence, harmonics lower than $h_{1}$ were ignored. The FFA needs to be amended to contend with this situation.

Sample G4.S2a and G4.S2b were produced under multi-knife-finish machining conditions; G4.S2a was ideally machined while G4.S2b was planed without the use of the top pressure roller or the chipbreaker. The difference between the FFT signatures for the two samples was marked (see figures 7.G4.S2a and 7.G4.S2b). The quality of the surface of G4.S2b was very poor; visual inspection of the sample revealed that the waviness pitch for the first one-third of its length has some resemblance to what was expected, while the other two-thirds had a much larger pitch and considerably greater amplitude (see figure 7.G4.S2b; talyrond trace - TAL). The FFA incorrectly flagged up a "proud-knife" fault for this sample.

For machining samples G4.S3a, G4.S3b, G4.S3c and G4.S4, the number of knives on the cutterhead was increased to 6 , the timber feedspeed to $80 \mathrm{~m} / \mathrm{min}$ and rotational speed of the cutterhead to 6000 rpm . These samples investigated spindle vibration by gradually reducing the degree of spindle
support at its outboard end.

Gradual deterioration of the surface quality was seen as the spindle's outboard end was freed (see figures 7.G4.S3a through to 7.G4.S3c). When the outboard bearing was completely removed for the machining of sample number G4.S4 the results on the surface finish was catastrophic (see figure 7.G4.S4). The FFA returned a "proud-knife" verdict in each case above. This verdict while being incorrect, due to the primitive nature of the FFA, indicated, however, that there was a problem with the machining process.

Samples number G4.S5a through to G4.S6c illustrated the effect of reducing the downward force applied by the chipbreaker, to the timber being machined. The first two samples (G4.S5a and G4.S5b) were machined using a timber feedspeed of $65 \mathrm{~m} / \mathrm{min}$ while the for other three (G4.S6a, G4.S6b and G4.S6c) it was increased to $75 \mathrm{~m} / \mathrm{min}$.

The results (see figure 7.G4.S5a and 7.G4.S5b) show that a machining fault was present when sample G4.S5b was produced; the FFA "failed" to accurately identify the fault but gave indications (Unknown Faults) that all was not well with the machining process.

Similarly (see figure 7.G4.S6a, 7.G4.S6b and 7.G4.S6c) with the other three samples, as the chipbreaker force was reduced, the quality of the surface finish diminished. Again the FFA indicated, without accurately specifying, that there were problems with the machining process.

### 8.4.2.5 Fault Combinations

## (Refer to Table G5)

The timber samples in Group G5 were machined with the purpose of producing surface profiles on which there were a combination of process faults. The first sample, G5.S1 (see figure 7.G5.S1) was produced under ideal conditions and used as the reference profile for in the group.

Sample number G5.S2, machined with the cutterhead in a state of out-ofbalance; the results (see figure 7.G5.S2) were as expected, with major peaks at harmonic $10\left(=h_{1} \pm 1\right)$ and $60\left(=h_{j} \pm 1\right)$.

Sample G5.S3 was produced under the same conditions as G5.S2 but with one additional fault - a proud knife. The result (see figure 7.G5.S3) were again as expected, with the "pulse-train" effect evident in the harmonic signature.

With sample G5.S4 another fault was added to those of G5.S3 - the downward pressure of the chipbreaker was reduced. This caused further deterioration in the quality of the surface finish; (see figure 7.G5.S4) the principle harmonic $h_{j}(=60)$ although "visible" on the frequency signature, was not of significantly magnitude to be detected by the FFA (threshold=0.4).

In sample G5.S5 yet another fault was added to the conditions under which G5.S4 was machined - the outboard bearing was untied before machining commenced. Surprisingly, this seemed to caused a slight improvement in the machined surface quality, as assessed by visual inspection. However, the

FFA "saw" a similar result to that for sample number G5.S4.

### 8.5 General Comments

Noise, leakage and aliasing are related to the implementation of the FFT because of the way the analogue waveform is acquired and sampled. Apart from these general types of errors, there are others related to the specific hardware and techniques used to acquire the data. For example, optical errors may have become part of the data - the lens optics system may have added geometric distortion to the acquired waveform. This distortion may have become part of the data that the FFT worked on and may have significant effect on the frequency spectrum.

9 CONCLUSIONS
9.1 Objectives Realised
9.2 Future Work

### 9.1 Objectives Realised

The objectives of the research were realised in that the design and manufacture of a non-contact transducer, with signal conditioning, for the assessment of the surface form of machined timber was investigated. The investigation of an appropriate parameter which can be used to indicate the quality of machined surface profiles was also undertaken. The timber planing-moulding process was studied with the aim of producing a mathematical model that represented a range of prevalent machining conditions and machined surface profiles.

The work carried out had a significant measure of success; a non-contact laser instrument was developed, which analysed the frequency content of planed timber surfaces; the frequency content being the parameter which indicates the aesthetic qualities of the surface, as established by isolated and identifiable machine faults. The technique was validated by comparing results with that obtained using a Talyrond 200 system, a widely accepted measurement standard in engineering.

The research also yielded a rigorous mathematical model that formed the foundation of a computer surface simulation algorithm (SSA) that simulated planed and spindle moulded surface profiles. The model and algorithm proved to be very accurate and versatile tool, giving insight into the nature of surface profile faults, and their origins.

### 9.2 Future Work

The laser instrument requires further improvements, refinements and modifications. This will include making the device more compact; the use of a single-chip microprocessor with on board RAM/ROM instead of a minicomputer; the replacing of the existing laser with a compact semi-conductor laser; the redesign of the beam expander to reduce its size and accuracy.

The software which analyses the captured data needs some refinement; the FFT algorithm can be replaced with an application specific FFT processor chip; the FFA needs to be further developed to cater for process faults such as timber slippage, poor timber support, and, combinations of separate faults. The mathematical model and the SSA can be used to assist in the improvement of the FFA.

The mathematical model and SSA, though sound, also needs to be refined; the timber slippage fault needs to be incorporated; poor support of workpiece and the associated parameters should also be researched with a view to modifying the mathematical model. The model can be further used to pioneer research into the type of frequency signature that results from certain machining conditions. These signatures can be retained for use as templates for cross correlation with data capture from actual planed surfaces. The results of the cross correlation can then be employed to determine the fault origin.

There are other types of faults that need to be investigated (such as the beating effect that occurs when two adjacent cutterheads are rotating at
almost the same frequency or the vibratory effects of drive belt on the cutterhead) and incorporated into the mathematical model, SSA and FFA. The surface assessment technique can form the basis for developing quantifiable parameters which can indicate the degree to which the surface varies from the ideal.

The laser instrument was appropriate for post-process use, but designed using the principles of in process assessment. Further to these modifications, therefore, the instrument need to be adapted for in process use; the photodiode array can be replaced by a single photodiode, with suitable signal conditioning, and, a rotary encoder added to the instrument as a means of defining data sampling points. There would obviously be a need for field trials to establish the validity of the in process instrument.

When the in process instrument is realised, it can be incorporated into a quality control strategy, facilitating adaptive control which can optimise the machining process based on prevailing machining conditions.

## REFERENCES

Arecchi F.T, Bertani D, Ciliberto S. ..... 1979
A Fast Versatile Optical Profilometer Optics Communications
December, 1979, Vol 31, part 3, pp.263-266
Babus'Haq R F, Probert S D, O'Callaghan P W, Evans G N ..... 1988
Peaks and Troughs of Surface Measurement
Professional Engineering
June, 1988, pp.52-53.
Bolzing D, Liu F. ..... 1987CIM - Integrated Engineering ConceptsIndustrial and Production Engineering1987, Vol 11, part 3, pp.28-44
Broadmann R. ..... 1986
Roughness Form and Waviness Measurement by means of Light ScatteringPrecision EngineeringOctober, 1986, Vol 8, No 4, pp.221-226
Brown H.P, Panshin A.J, Forsaith C.C. ..... 1952
Textbook of Wood Technology
Volume II
McGraw-Hill Book Co inc New York
Brown I.D. ..... 1960
Visual and Tactual Judgments of Surface Roughness Ergonomics, Vol 3, Part 1, pp.51-61.
Burnner H.E. ..... 1929
Ball Bearings as Applied to Woodworking Machinery American Society of Mechanical Engineers' Transactions 1929
Cooley J.W, Tukey J.W. ..... 1965
An Algorithm for the Machine Computation of Complex Fourier Series.Math. Comp., 19, pp.297-301
April 1965
Cowdery M.J. ..... 1990The "Intelligent" Sawmill
Mechatronics: Designing Intelligent Machines
Proceedings of the Institution of Mechanical Engineers
pp.5-15
International Conference
Robinson College
University of Cambridge
12th - 13th September, 1990
Crookall J.R. and Sherwood K.F, ..... 1968
Surface Finish Assessment by an Electrical Capacitance TechniqueProceedings of the Institute of Mechanical Engineers1968, Vol 182, p. 344
Cummings J.D. and Peters C.C ..... 1970
Measuring Wood Surface Smoothness
Forest Product Journal
December, 1970, Vol 20, part 12, pp.40-43
Davis E.M, Nelson H. ..... 1954
Machining Tests of Wood with the Moulder Journal of Forest Products Research Society October, 1954, Vol 4, part 5, pp.227-245
Deal R.C. ..... 1951
Standardization of Surface Quality of Wood Products
Woodworking Digest
February, 1951, Vol 4, part 5, pp.227-245
Dobosz M. ..... 1984
Accuracy of Profile Measurements by means of a Focused Laser Beam WearNovember, 1984, Vol 98, pp.117-126
Drews W.E ..... 1987
Surface Measurement; An Advanced Technology Quality Progress
April 1987, Vol 20, Part 4, pp.43-46.
Dupuy M.O. ..... 1967
High Precision Optical Profilometer for the Study of Micro-Geometrical Surface Defects
Proc. Inst. Mech. Engrs. ..... 1967, Vol 182, Part 3k, pp.255-259
Elmendorf A and Vaughan T.W ..... 1958A Survey of Methods of Measuring Smoothness of WoodForest Products Journal, Vol 81958
Goddard M. ..... 1985
Business Development Seminar/Technical DiscussionWoodworking Division, Wadkin Plc, Green Lane Rd, LeicesterAugust, 1985
Goddard M, Garrett J. ..... 1986
Business Development Seminar/Technical DiscussionWoodworking Division, Wadkin Plc, Green Lane Rd, LeicesterJanuary, 1986
Gomez S, Gonzalez S, Hsu D, Kuo A. ..... 1988
An Application Specific FFT Processor
Electronic Engineering Supplement June 1988, pp.99-106
Gonzalez R.C, Wintz P. ..... 1977
Digital Image Processing
Addison-Wesley Publishing Company, Inc. ..... 1977
Goodchild R. ..... 1963
Investigating Finish in Rotary Planing
Engineering
January 25th 1963, pp.172-173
Greenwood J.A. ..... 1968Surface MeasurementInstitute of Mechanical Engineers Symposium: Experimental Methods inTribology, Paper 1
13th-14th March, 1968
Harris P.G, Trigg A.D ..... 1987Surface Analysis Techniques and their Application to Material and DeviceCharacterization
G.E.C. Journal of Research
1987, Vol 5. part 2, pp.88-98
Han R.A. ..... 1957A Method of Quantitative Topographic Analysis of Wood SurfacesForest Products JournalDecember, 1957, Vol 7, part 12, pp.448-452
Hattori M. ..... 1981
Development of In-Process Sensor for Surface and Roundness Profiles Bulletin of Mechanical Engineering Laboratory 35(6)1981
Hingle H . ..... 1986Tool Wear Monitoring by the ComponentModern Production and Metrology SeminarTechnische Universitat, Vienna paper 147.31986
Inasaki I. ..... 1982
Development of In-Process Sensor for Surface Roughness MeasurementProc. 23 Int. MTDR1982
Jackson M.R. ..... 1986
Some effects of Machine Characteristics of the Surface Quality of Planed andSpindle Moulded Wooden Products
PhD Thesis, 1986
Kivimaa E. ..... 1950
Cutting Forces in Woodworking PhD Thesis
Finland Institute of Technology ..... 1950
Knudsen V.O. ..... 1928
"Hearing" with a Sense of Touch Journal of General Psychology, Vol 1 1928, pp. 320-352.
Koch P. ..... 1955
An Analysis of the Lumber Planing Process: Part I Forest Products Journal August, 1955, pp.255-263.
Koch P. ..... 1956
An Analysis of the Lumber Planing Process: Part II Forest Products Journal October, 1956, pp.393-401.
Koch P. ..... 1964
Woodmachining Processes
Roland Press Company
New York ..... 1964
Mansfield J.H. ..... 1952
Woodworking Machinery, History and Development 1852-1952 Journal of American Society of Mechanical Engineers 1952, Vol 74
Maycock K.M, Parkin R.M, Buttery T. ..... 1987
Measurement and Control Techniques for Timber Production ProcessesProc. of 3rd Conference on Sensors and their ApplicationsCambridge, September, 1987
Mitsui K. ..... 1986
In-Process Sensor for Surface Roughness and their ApplicationsPrecision Engineering, Vol 8, No. 4October 1986
Mori M and Hoshi T ..... 1964Studies of Surfacing of Wood with Planers (II)Bulletin of the Government Forest Experimental Station No. 163Tokyo, JapanFebruary 1964.
Mulvaney D.J, Newland D.E.1986A Comparison of orthogonal transforms in their Application to SurfaceTexture AnalysisProceedings of Institute of Mechanical Engineers1986, Vol 200, No. C6.
Parkin R.M. ..... 1988The Application of CIM to Planing and Moulding Machines in theWoodworking IndustryCOMODEM 88: The First UK Seminar on Condition Monitoring andDiagnostic Engineering Management
City of Birmingham Polytechnic, Birmingham
19th- 21st September, 1988
Peklenik J. ..... 1968
New Developments in Surface Characterisation and Measurements by means of Random Process Analysis
Mechanical Engineering Conference: Properties and Metrology of Surfaces, paper 24, Oxford April, 1968
Pernick B.J. ..... 1979
Surface Roughness Measurements with an Optical Fourier Spectrum Analyzer
Applied Optics 15 March, 1979, Vol 18, No. 6
Petter C. ..... 1954
Development Work on Wood Planers Journal of Forest Product Research Society 1954, Vol 561, pp. 134-136
Phillips M.J, Whitehouse D.J. ..... 1977
Some Theoretical Aspects of the Measurement of Curved SurfacesJournal of Physics E: Scientific Instruments1977, Vol 10, p. 164
Pryor T.R, Hagemoers O.L, North W.P.T. ..... 1972Diffractographic Dimensional Measurement.
Part 1: Displacement Measurement
Part 2: Profile Measurement
Applied Optics
February, 1972, Vol 11, No. 2, pp.308-318
Quality Today - Measurement and Inspection Technology ..... 1986Roughness in the Palm of Your Hands
March, 1986, p. 37
Rabiner L.R, Gold B. ..... 1975aTheory and Application of Digital Signal ProcessingPrentice-Hall inc. pp.89-901975
Rabiner L.R, Gold B. ..... 1975bTheory and Application of Digital Signal ProcessingPrentice-Hall inc. pp.26-281975
Rakels J.H. ..... 1986
Diffraction - an old optical phenomenon used as an advanced metrology toolModern Production and Metrology SeminarTechnische Universitat
Vienna paper 79.3
Schmaltz G. ..... 1936
Techinsche Oberflachenkunde
Springer, Berlin ..... 1936
Schwartz M, Shaw L ..... 1975
Signal Processing: Discrete spectral analysis, detection and EstimationMcGraw-Hill Book Company
1975 pp. 162-168
Sherrington I, Smith E.H. ..... 1988
Modern Measurement Techniques in Surface Metrology Wear
1988, Vol 125, part 3, pp.271-288
Smith P.F, Player M.A, Collie D.L.A. ..... 1988
The Determination of Surface Topology by the Signal Processing of Ultrasonic Pulses
J. Phys. E: Sci. Instrum. 1988, Vol 21, pp.397-402
Sommargren G.E. ..... 1981Optical Heterodyne ProfilometryAppl. Opt. Vol 20 p. 610
Stevens D.M.G. ..... 1989
An Investigation into the use of a Wide Range Interferometric Transducer forRoundness Measurement
M Phil Thesis
Leicester Polytechnic
August 1989.
Stumbo D.A. ..... 1960
Surface Texture Measurement for Quality of Production Control
Forest Product Journal
February, 1960, pp.122-124
Stumbo D.A. ..... 1963
Surface Texture Measurement Methods
Forest Product Journal
July, 1963, pp.299-303
Thomlinson J. ..... 1987
CIM - Bringing the Islands Together Chartered Mechanical Engineer
March, 1987, pp.49-51
Thomlinson R, Harrington J.S. ..... 1960
Rotary Cutting
Forest Products Journal
October, 1960, pp.419-421
Timber Trades Journal ..... 1986a
Weinig Launch a New CNC System
October, 1986, pp.43-44
Timber Trades Journal ..... 1986b
High-speed Spindles come of age in the new XR130 Moulder from Wadkin 22 November, 1986, pp.25-26
Timber Trades Journal ..... 1987
SCM The Dynamic Giant
9th May, 1987, pp.30-32
Timber Trades Journal ..... 1990a
Thumbs Up for Woodmex
November, 1990, pp.16-20
Timber Trades Journal ..... 1990bThe Clock WatcherOctober, 1990, pp.21-22
Toshimitsu A. and Hitoshi F ..... 1977
Roughness Measurements of metal Surfaces using Laser SpeckleJ. Opt. Soc. Am.,September, 1977, Vol 67, No. 9
Whitehouse D.J ..... 1972
Modern Methods of Assessing the Quality and Functions of SurfacesProc. Soc. Manufacturing Engineers
Chicago1972
Whitehouse D.J. ..... 1985
Instrumentation for Measuring Finish Defects and Gloss SPIE, Vol 525, p. 106
Whitehouse D.J, Bowen D.K, Chetwynd et al ..... 1987 Nano-Calibration for Stylus Based Surface Measurement Physics Engineering, Vol 21, Part 1, pp.46-51.
Wyant J.C. ..... 1985
Optical Profilometers for Surface Roughness SPIE Vol 525, p. 174

FIGURES


Figure 1.1: Early power-operated machinery was belt driven from
lineshafts


Figure 1.2: Malcolm Muir's Planer, 1827

Figure 1.3: John McDowall's Planer, 1836


Figure 1.4: First Moulder with Integral Electric Motors, 1916


Figure 1.5: Elements of a Motorised Cutterhead with Spindle and Bearings


Figure 1.6: A Modern Moulding and Planing Machine






PRIICIPLE OF CAPACITIVE METHOD

Figure 2.5




FACTORS OF VARIOUS OPTICAL SURFACE ASSESSMENT METHOOS

Figure 2.8


Figure 2.10: Mitsui's Instrument


Interference Method for examining surface form Figure 2.11







IDEALLY PIANED SURFACE

Figure 3.2





Figure 4.2


IDEALLY PLANED SURFACE

$$
R 1=R 2=R 3=R 4
$$





Figure 4.6a: Typical Knife-tip Loci fron Algorithn LOCI-8 (SSA - Stage 1)

## maCHIHE PARRMETERS

Ho. of knives 2
Feed speed 11088 main
cutter Speed 10 Ppm


Figure 4,6b: Typical Knife-tip Loci from Algorithm LOCI-8 (SSA - Stage 1)


## machine parameters

Ho. of knives 4
Feed speed $11008 \mathrm{~m} /$ min
cutter Speed 18 rpm


Figure 4.6d: Typical Knife-tip Loci fron Algorithm LOCI-8 (SSA - Stage 1)

## MACHIME PARAMETERS

Ho. of knives 1
Feed speed $18808 \mathrm{~m} / \mathrm{min}$
Cutter Speed 10 rpm


Figure 4,6e: Typical Knife-tip Loci fron Algorithm LOCI-8 (SSA - Stage 1)

## maChIME PARRMETERS

Ho. of knives 2
Feed speed 18808 whin
cutter Speed 10 rpm


Figure 4.6f: Typical Knife-tip Loci fron Algorithm LOCI-8 (SSR - Stage 1)

## maCHIME PARAMITERS

Mo. of knives 3
Feed speed 18888 wnin
Cutter Speed 10 PPM


Figure 4.6g: Typical Knife-tip Loci fron Rlgoritha LOCI-8 (SSA - Stage 1)

## maCHIME PARAMEIERS

Ho, of knives
Feed speed $18088 \mathrm{~m} /$ ain
cutter Speed if rpa


Figure 4,6h: Typical Knife-tip Loci fron Algorithn LOCI-8 (SSA - Stage 1)

## maCHINE PARAMETERS

Mo. of knives 1
Feed speed 18080 m/min
cutter Speed 10 ppm


Figure 4.7a: Typical Knife-tip Loci fron Algorithm LOCI-1 (SSA - Stage 1)

## machine parameters

Ho. of knives 2
Feed speed $18888 \mathrm{~m} /$ nin
cutter Speed 18 rpm


Figure 4.7b: Typical Knife-tip Loci fron Algorithm LOCI-1 (SSA - Stage 1)

## MACHIME PARAMETERS

## Ho. of knives 3 <br> Feed speed $18880 \mathrm{~m} / \mathrm{min}$ Cutter Speed 18 rpm



Figure 4.7c: Typical Knife-tip Loci from Algorithn LOCI-1 (SSR - Stage 1)

## MACHIHE PARAMETERS

Ho. of knives 4
Feed speed 18808 m/min
cutter Speed 18 rpm


Figure 4.7d: Typical Knife-tip Loci fron Algoritha LOCI-1 (SSA - Stage 1)

## mCHIHE PARRMETERS

Ho. of knives?
Feed speed 128 anain
cutter Speed 3500 PPA


Figure 4.8a: Typical Knife-mark Loci from Algorithm LOCI-2 (SSA - Stage II)

## MACHINE PRRRMETERS

Ho. of knives?
Feed speed $128 \mathrm{~m} / \mathrm{min}$
Cutter Speed 3588 PPM Pr.Xnife pos


Figure 4.8b: Typical Knife-mark Loci from Algorithm LOCI-2 (SSA - Stage II)

## : MaCHIHE PARAMETERS

Ho of knives 4
Feed speed $188 \mathrm{~m} / \mathrm{min}$
Cutter Speed 3588 PPM


Figure 4.8c: Typical Knife-mark Loci fron Algorithm LOCI-2 (SSA - Stage II)
$\square$


## machine parameters

## Mo. of knives 4

Feed speed 100 min
cutter Speed 3500 rpm


Figure 4.9a: Typical Knife-mark Loci from Algorithm LOCI-3 (SSR - Stage III)


Figure 4.9b: Typical Knife-mark Loci fron Algorithm LOCI-3 (SSA - Stage III)

## wuwumwumu



Figure 4.18a: Typical Surface Profile from Surface Simulation Algorithm


| SIMULATIOH PARRMETERS |
| :---: |
| Ho of knives 4 |
|  |
| Vib, rate g rm |
| Proud Knives |
| Eccirde/rev ${ }^{\text {Spindle Runout }} \frac{1}{28}$ nicrons |

Figure 4.10b: Typical Surface Profile from Surface Simlation Algorithm

## surumunuman

| SIMLALIIOH PARAMETERS |
| :---: |
| No. of knives 4 |
| cepter speed 3580 r rpm |
| Uib, rate 8 dos |
|  |
| Spindle Runout 8 nicrons |

Figure 4.18c: Typical Surface Profile from Surface Simulation Algorithm
Mquprypryprypry

SIMLATIOM PARAMETERS


Figure 4.10d: Typical Surface Profile from Surface Simlation Algorithm


| SIMNLATIOH Parameters |
| :---: |
| No. of knives 6 |
|  |
| Uib, rate 9 d |
| Proud knives 2 ll> 15 |
| Spindle Runout 28 microns |

Figure 4.18e: Typical Surface Profile fron Surface Simulation Algorithn


| SIFIULATIOK PRRAMETERS |
| :---: |
| Ho. of knives 6 |
|  |
| Vib. rate 3008 |
| Proud Knives 2 7>1 15 |
| Ecc, rate/rev ${ }^{\text {Spindle Runout }} \frac{1}{15}$ microns |

Figure 4.18f: Typical Surface Profile fron Surface Simlation Algorithm



Figure 5.2.1: Schematic of the BBC microcomputer


Figure 5.2.2: Schematic of the 6522 VIA



Figure 5.2.3: Read Handshake Timing Diagram for Port A Only


Figure 5.2.4: Write Handshake Timing Diagram



Figure 5.2.6: Sensor Geometry and Idealised apperture Response Function $\mathrm{a}=15 \mu \mathrm{~m}: b=25 \mu \mathrm{~m}: \mathrm{c}=26 \mu \mathrm{~m}$


Figure 5.2.7: Photodiode Relative Spectral Response as Function of Wavelength


Figure 5.2.8: Photodiode Output Charges verses Exposure Characteristic


Figure 5.2.10: Timing Diagram for Array clock and Start input in realation to Video and End-of-Scan Outputs




Figure 5.2.12: Sample and Hold Boxcar Video Signal




LENS MAKER'S FORMULA: S.mmbol Definition

Figure 5.3.2



$$
\begin{aligned}
O B & =\text { sample length } \\
& =125 \mathrm{~mm} \\
I M & =\text { image length } \\
& =25 \mathrm{~mm} \\
f & =\text { lens foce length } \\
& =50 \mathrm{~mm}
\end{aligned}
$$

IMAGE FOCUSING - The Optical A-rangement
Figure 5.3.4


Figure 5.3.6: Lens Mount


Figure 5.4.1: Framework


Figure 5.4.2: Timber-Sample Clamping Device


Figure 5.4.3: Helium-neon Laser and "Floating" Carrage


Figure 5.4.4: Laser beam incidence angle adjustment using Micrometer - Spring mechanism


Figure 5.4.5: Image Alignment Mechinism


Figure 5.4.6: Dark-housing to exclude Ambient light



Figure 5.6.1: Time History of Sinusoid obtained with Oscilloscope


Figure 5.6.2: Time and Frequency Description of a Sine Wave


c. Nonsinusoidal waveform composed of a and b

Figure 5.6.3: Summing Frequency Description of Sinusoids


Figure 5.6.4: Composing a Non-sinusoidal Waveform by Summing Sinusoids

a. Periodicity- $-x(t)=x(t+\tau)$.

b. Finite number of discontinuities.

d. Integrable-- $\int_{0}^{t}|x(t)| d t<\infty$.

Figure 5.6.5: Square Wave satisfies conditions for its Foueier Series to exist


Figure 5.6.6: Magnitude and Phase Spectra for Square Wave in figure 5.6.5a


Figure 5.6.7: Fourier Series and Fourier Intergral - different paths between time and frequency


Figure 5.6.8: Relationship between Fourier Series and Fourier Intergral
As $\tau \rightarrow \infty$ the spectral lines become closer, when $\tau=\infty$ the spacing between lines is


Figure 5.6.9: Comparison of daigram conventions in the Series Spectrum and Transform Frequency domain

a. Square pulse.

b. Frequency-domain magnitude.
c. Frequency-domain phase.

Figure 5.6.10: A Generalised Square Pulse and its Frequency-domain Magnitude and Phase


Figure 5.6.11: The Process of Rectangular Windowing


ZERO-ORDER APPROXIMATION

Figure 5.6.12


Figure 5.6.13: Result of the first step for an $\mathrm{N}=8$ point decimation-in-time FFT


Figure 5.6.14: Result of the second step for an $\mathrm{N}=8$ point decimation-in-time FFT


Figure 5.6.15: Final flow graph for an $\mathrm{N}=8$ point decimation-in-time FFT


Figure 5.6.16: The Butterfly structure in the various stages of a decimation-in-time FFT


Figure 5.6.17: Modified Butterfly structure requiring only one complex multplication


Figure 5.6.18: Rearangement of figure 5.6 .15 with input in natural order and output in bit-reversed order


FUNCTIOK:

$$
f(H t)=4, \operatorname{SIN}(2 \pi, 1, t)
$$



Figure 5.6.19: Typical Results from FFT Algorithm Vaildation


FUNCIIOH:
$f(H t)=4 . \operatorname{SIN}(2 \pi, 18 . t)$


Figure 5.6.28: Typical Results from FFT Algorithm Vaildation


FUKCIIOH:
$f(n t)=4 . \operatorname{SIH}(2 \pi .2 \theta . t)$


Figure 5.6.21: Typical Results fron FFT Algoritha Vaildation


Figure 5.6.22: Typical Results from FFT Algoritha Vaildation



Figure 5.6.26: Typical Results fron FFT Algorithm Vaildation

Figure 5.6.27: Typical Results from FFT Algorithm Vaildation


Figure 5.6.28: Typical Results from FFT Algoritha Vaildation


Figure 5.6.29: Typical Results fron FFT Algoritha Vaildation


Figure 5.6.38: Typical Results from FFT Algoritha Vaildation


FUACTIOH:
$f(H)=4 . \operatorname{SIM}(2 \pi .18 . t)+2 . \operatorname{SIH}(2 \pi .61 . t)$


Figure 5.6.31: Typical Results fron FFT Rlgorithn Vaildation


Figure 5.6.32: Typical Results fron FFT Algorithn Vaildation


Figure 5.6.34: Typical Results fron FFT Algorithm Vaildation

FUnCTION:


Figure 5.6.35: Typical Results from FFT Algorithm Vaildation


FUNCTION:


Figure 5.6.36: Typical Results from FFT Algorithm Vaildation


FUMCTION:


Figure 5.6.37: Typical Results fron FFT Algorithn Vaildation


FUKCTIOK:
$f(\mu t)=1 . \operatorname{SIN}(2 \pi .11 .2 . t)+1 . \operatorname{SIN}(2 \pi .22 .2 . t)+1 . \operatorname{SIN}(2 \pi .33 .3 . t)$ $+1 . \operatorname{SIN}(2 \pi .44 .2 . t)+1 . \operatorname{SIH}(2 \pi .55 .2 . t)+1 . \operatorname{SIN}(2 \pi .66 .2 . t)$


> FFT OF FUNCTIOK

Figure 5.6.38: Typical Results from FFT Algorithm Vaildation


FUnCTION:

```
f(Mt)=1.SIN(2\pi.18.t) + 8.5.SIN(2\pi.20.t) + 0.2.SIH(2\pi.38.t)
    +8.87.SIM(2\pi.48.t) + 2E-3.SIM(2\pi.50.t)
    IN
    8 10283040
FFT OF FUNCTIOM
```

Figure 5.6.39: Typical Results from FFT Algorithm Uaildation


FUNCTION:
$f(H t)=1 . S I H(2 \pi .18 .5 . t)+8.5 . \operatorname{SIN}(2 \pi .28 .5 . t)+8.2 . \operatorname{SIK}(2 \pi .38 .5 . t)$ $+8.87 . S I M(2 \pi .48 .5 . t)+2 E-3 . S I N(2 \pi .50 .5 . t)$

-1021314151 255 number fFT OF FUKCTION

Figure 5.6.48: Typical Results from FFT Algorithm Vaildation


Figure 5.6.41: Typical Results from FFT Rlgorithn Vaildation


Figure 5.6.42: Typical Results fron FFT Algoritha Vaildation



Figure 5.6.43: Typical Results from FFT Algorithm Vaildation


Figure 5.6.44: Typical Results fron FFT Algorithn Vaildation


Figure 5.6.45: Typical Results fron FFT Algorithn Vaildation


Figure 5.6.46: Typical Results fron FFT Algorithm Vaildation


Figure 6.1: The B-series 220 Planer - Moulder Machine


SIAN[JAH II IVAD\|INT SPECIFICATIONS

| Unit 8 | Unit 33 | Unit 77 | Unit 44 | Unit 66 | Unit 55 | Unit 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Top or bottom horizontal or intermediates and vertical nearside. <br> Head motor <br> 15 hp max. <br> Cutting circles <br> 125 mm min. <br> 200 mm max | Head motor 25hp max. <br> Cutting circles 125 mm min. 230 mm max. with or without jointing | Head motor 25hp max. <br> Cutting circles 125 mm min. <br> Top head 230 mm max. with jointing 250 mm max. without jointing Bottom head 230 mm max. with or without jointing | Head motor 25hp max. <br> Cutting circles 125 mm min. 230 mm max. with jointing 250mm max. without jointing | Head motor 15hp max. <br> Cutting circles <br> 125 mm min. <br> 200 mm max. <br> with or without <br> jointing | Head motor 15hp max. <br> Cutting circles <br> 125 mm min . <br> 200 mm max. <br> with or without <br> jointing | Head motor 15hp max <br> Cutting circles <br> 125 mm min. <br> 185 mm max. <br> with or without <br> jointing |

Figure 6.2: Head unit Specifications of the Modular "200B"


Figure 6.3: Final Top Head


Figure 6.4: Spindle Unit Bearing Assembly


Hydrogrip Planing Cutterblock


Hydrogrip Planing Cutterheads in situ

Figure 6.5: Hydrogrip Planing Cutterblock and Cutterheads


Heavy Duty In-feedworks


In-feed Table

Figure 6.6: Heavy Duty In-feedworks and In-feed Table


Figure 6.7: Out-feedworks


Figure 6.8: Chipbreaker


Figure 6.9: Side Pressure Rollers


Figure 6.10: Standard Jointer fitted to Top and Bottom Cutterheads


Figure 6.11: Dust Extractor System


Figure 6.13: An NX-grinder used for producing Proud-knives


Figure 6.12


Figure 6.14: Timber Sample Analysis by Laser Instrument


Figure 6.15: Timber Sample Analysis by Talyrond 200

\section*{ <br>  <br> | SIMULATIOK PARAMETERS |
| :---: |
| No. of knives 6 |
| Feed speed $88 \mathrm{~m} / \mathrm{min}$ cutter speed 4588 rpm |
| Uib. rate 88 |
| Proud Knives $\frac{1}{1}$ >>> 1 |
| Ecc, rate/rev ${ }^{\text {Spindle Runout }}$ O microns |

Figure 6.16: RESULTS OF PROFILE SIMULATION - PROUD-XHIFE


Figure 6.17: RESULTS OF PULSE-TRAIN SIMULATION - PROUD-KHIFE
cnilumum


Figure 7.68.S1a: RESULTS FOR PROFiLE SINLATION MUMBER 60.S1a



Proud Knives 1 /7) 1
Ecc.rate/reu
Spindle Runout of nicrons

## PRIHCTPAL

PEAK
harmonics
$h 1=62$
$h_{2}=124$
$h j=375$

Figure 7.68.S1b: RESULTS FOR PROFILE SIMULATIOH NUMBER 60.S1b


Figure 7.68.SIc: RESULTS FOR PROFILE SIMULATION RUMBER G8.SIc


Figure 7.60.SId: RESULTS FOR PROFILE SIMULATION Number 68.SId


Figure 7.60.S2a: RESULTS FOR PROFILE SIMULATION NUMBER 68.S2a


| 0 | 38 | 75 | 113 | 15 |
| :---: | :---: | :---: | :---: | :---: |
| SIMULATION PARAMETERS |  |  |  |  |
|  |  |  |  |  |

SSA. 68.52b

| RHALYSIS OF FFT USIHG FFA |
| :---: | :---: |
| THRESHOLD $=0.4$ |
| (Multi-knife) <br> Harmonic 38 |

    PRIMCIPA
    PEAK
HOMOHI
harmonics
$h 1=6$
$h 2=12$
$h \mathrm{~h}=37$

Figure 7.68.S2b: RESULTS FOR PROFILE SIMULATIOH RUMBER 68.s2b


Figure 7.68.S2c: RESULIS FOR PROFILE SINULATIOH NUFBER G8.S2c


roud knives
Ecciraterrev
Spindle Runout 8 nicrons
PRIMCIPAL
PEAK
harmonICS
$h 1=8$
$h 2=16$
$h j=58$

Figure 7.60.s2d: RESULTS FOR PROFILE SIMULATION RUMBER G8.s2d

MMOMMWMMWMMMMMMM


Figure 7.68.S2e: RESULTS FOR PROFILE SIFULATION NUMBER G0.S2e



Figure 7.60.s2f: RESULTS FOR PROFILE SIMULATIOH NUMBER 60.s2f


Figure 7.G8.S2g: RESULTS FOR PROFILE SIMULATION RUMBER G8.S2g


Figure 7.60.S3a: RESULTS FOR PROFILE SIMULATION NUMBER G9.53a


Figure 7.68.S3b: RESULTS FOR PROFILE SIMULATION NUMBER G0.53b





| ANALYSIS OF FFT USING FFA THRESHOLD $=0.4$ |
| :---: |
| (Proud Knif |
| Harmonic |
| Harmonic 14 |
| Marmonic 21 |
| (Malti-knife) |
| Harmonic 42 |

Figure 7.68.S3c: RESULTS FOR PROFILE SIWULATION NUMBER 68.53c


Figure 7.68.S3d: RESULTS FOR PROFILE SIMULATION NUMBER G8.53d



Figure 7.68.S3e: RESULTS FOR PROFILE SIMULATION RUMBER 60.S3e


Figure 7.68.53f: RESULTS FOR PROFILE SIFULATIOK NUMBER $60.53 f$

|  |  |
| :---: | :---: |
| L1+1. | $\ldots$ |
| 07214283 | $22^{551.68 .539}$ |
| SIMLALTION PRRAMETERS | AMALYSIS OF FFT USIHG FFA |
| Ho. of knives 6 | THRESHOLD $=0.4$ |
|  |  |
|  | (uarss or Hoise) |
|  |  |
| Figure 7.60 .53 g : RESULTS for profile simulation humber 68.53 g |  |



Figure 7.68.S3h: RESULTS FOR PROFILE SIMULATIOK NUMBER G0.S3h


Figure $7.68 .53 i$ : RESULTS FOR PROFILE SIMULATIOH NUMBER 68.53i


PRIHCIPAL

HARMONICS
$h 1=6$
$h 2=12$
$h j=41$

| AMALYSIS OF FFT USIMG FFR THRESHOLD $=8.85$ |
| :---: |
| (Proud Knife) |
| Harmonic? |
| Harmonic 14 |
| Harmonic 21 |
| Harmonic 28 |
| (Multi-knife) |
| Harmonic 42 |
| (Uibs or Hoise) |
| Harmonic 56 |
| Hapmonic 62 |
| Harmonic 83 |
| harmonic 111 |
| Harmonic 125 |

Figure 7.68.S3j: RESULTS FOR PROFILE SIMULATION NUMBER G8.53j



| SIFMLATIOH PARRMETERS |
| :---: |
|  |


| AMALYSIS OF FFT USING FFA |
| :---: |
| THRESHOLD $=0.4$ |
| Multi-knife) <br> Harmonic 33 |

PRIMCIPAL
PEAK
HARMOHICS
$h 1=5$
$h 2=18$
$h j=33$

Figure 7.68.S4a: RESULTS FOR PROFILE SIMULATION NUMBER G8.S4a



| SIMULATION PRRAMETERS |
| :---: |
|  |


| AKALYSIS OF FFT USING FFA |
| :---: |
| THRESHOLD $=8.1$ |
| (O.balance 1 ) <br> Harmonic 6 <br> (Multi-knife) <br> Harmonic 33 |

Figure 7.60.S4b: RESULTS FOR PROFILE SIWLLATION NUMBER G8.S4b



| ANALYSIS OF FFT USING FFA |
| :---: |
| THRESHOLD $=0.4$ |
| (O.balance 1$)$ |
| Harmanic 6 |
| (multiknife) |
| Harmonic 33 |

PRINCIPAL
PARK
HARHICS
$h 1=5$
$h 2=18$
$h j=33$

Figure 7.68.S4c: RESULTS FOR PROFILE SINULATION NUMBER 68.S4c


| AMALYSIS OF FFT USIMG FFA |
| :---: |
| THRESHOLD $=0.4$ |
| (Obalance 1 ( <br> Harmonic <br> (multickife) <br> Harmonic 33 |


| PRINCIPRL |
| :---: |
| PEAK |
| HRRFDHICS |
| $h 1=5$ |
| $h 2=18$ |
| $h j=33$ |

Figure 7.68.S4d: RESULTS FOR PROFILE SIMULATION RUMBER 68.S4d


Figure 7.68.S4e: RESULTS FOR PROFILE SIMLLATIOH NUMBER G8.S4e




Figure 7.68.55a: RESULTS FOR PROFILE SIMLATION RUMEER 68.55a





PRIMCIPAL
PEAK
harmonics
$h 1=5$
$h 2=18$
$h 1=44$
$\mathrm{hj}=44$

Figure 7.60.S5d: RESULTS FOR PROFILE SIMULATION NUMBER 60.55d


Figure 7.60.S5e: RESULTS FOR PROFILE SINULATION NUMBER G8.S5e


| 86172844 |
| :---: |
| SIMNLATION PARAMETERS |
|  |


| PRIMCIPAL |
| :---: |
| MREMK |
| HRHICS |
| $h 1=5$ |
| $h 2=18$ |
| $h j=44$ |

255


Figure 7.G8.S5f: RESULTS FOR PROFILE SIWULATION NUMBER G8. $55 \%$


Figure 7.60.S6a: RESULTS FOR PROFILE SIMULATIOH NUFBER 60.S6a



SSA.68.56b


| RMALYSIS OF FFT USING FFA |
| :---: |
| THRESHOLD=8.4 |
| (Melti-knife) |
| Harmonic 33 |
| (Uibs or Hoise) |
| Harmonic 133 |
| Harnonic 167 |

PRINCIPAL
PEAK
HARMOHICS

Figure 7.68.S6b: RESULTS FOR PROFILE SIMULATION RUABER 68.S6b

Whanchand

PRINCIPAL
PERK
HEROICS
$h 1=5$
$h 2=18$
$h j=33$

Figure 7.60.S6c: RESULTS fOR PROFILE SIMULATION RUABER G8.S6c


Figure 7.68.56d: RESULTS FOR PROFILE SIMULATION NUMBER G8.56d


| MaCHINIMG PRRAMETERS | PRIMCIPAL |
| :---: | :---: |
| Ho. of knives 4 <br> Feed speed  <br> Cutter Speed $15 \mathrm{~m} / \mathrm{min}$ <br> Uib. rate 888 rpm | HARHONICS |
|  | = |
|  | h2 $2=74$ |
| Proud Knives $\frac{1}{8}$ m>1 1 | hj $=149$ |
| Eccirate/rev Spinde Runout 8 microns |  |


| AMALYSIS OF FFT's USING FRULT FIMDIKG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER OATA THRESHOLD O | FFA ON TALY DATA THRESHOLD $=0.4$ | FFA ON SSA DATA THRESHOLD $=0.4$ |
| (Single knife) Harmonic 38 | (Single knife) Harmonic 37 | (Single knife) Harmonic 38 |

Figure 7.G1.S1: RESULTS FOR TIMBER SAMPLE NUMBER G1.S1


| MaCHINIIN PPRRAMIETERS | $\begin{aligned} & \text { PRIMCIPAL } \\ & \text { HARERK } \\ & \text { PRICS } \end{aligned}$ |
| :---: | :---: |
| No. of knives 4 |  |
| Feed speed $15 \mathrm{~m} / \mathrm{min}^{\text {chin }}$ | h1 $=37$ |
| Vib. rate 8 | h2 $=74$ |
| Proud Knives $\frac{1}{\text { d }}$ >> 1 | $\mathrm{hj}=149$ |
| Ecc.rate/rev ${ }^{\text {Spindle Runout }}$ a microns |  |


| AMALYSIS OF FFT's USIHG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD $=0.4$ | FFR OH TALY OATA THRESHOLD $=0.4$ | FFA ON SSA DATA THRESHOLD $=0.4$ |
| (Single knife) Harmonic 37 | $\begin{aligned} & \text { (Single knife) } \\ & \text { Harmonic } 38 \end{aligned}$ | (Single knife) Harmonic 38 |

Figure 7.61.s2: RESULTS FOR IIMBER SAMPLE NUMBER G1.S2


| MACHINIMG PARAMETERS | AL |
| :---: | :---: |
| No. of knives 4 <br> Feed speed <br> Cutter Speed <br> $1588 / \mathrm{min}$ <br> rpm | harmonics |
|  | $=$ |
|  | h2 $2=74$ |
|  | hj $=149$ |
| Ecciraterrev |  |


| AMALYSIS OF FFT's USING FRULT FIKDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA ON LASER DATA THRESHOLD=8.4 | FFA OH TRAY DATA THRESHOLD $=0$. | $\begin{aligned} & \text { FFA OH SSA DATA } \\ & \text { THRESOLD }=0.4 \end{aligned}$ |
| $\begin{aligned} & \text { (Single knife) } \\ & \text { Harmonic } 36 \end{aligned}$ | $\begin{aligned} & \text { (Single knife) } \\ & \text { Harmonic } \end{aligned}$ | (Single knif Harmonic 38 |

Figure 7.61.S3: RESULTS FOR TIMBER SAMPLE NUMBER 61.53


| MACHINING PARAMETERS | AL |
| :---: | :---: |
|  | harmonics |
|  | h1 $=37$ |
| Vib rate $\begin{aligned} & \text { Proud Knives } \\ & 1\end{aligned}$ | h2 $=74$ $h j=149$ |
| Ece, rate/rev Spindle Runout 8 nicrons |  |


| AMALYSIS OF FFT's USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFR ON LASER DATA THRESHOLD=8. 4 | FFA OH TAL THRESHOLD 08.4 | $\begin{aligned} & \text { FFA OH SSA } \quad \text { ORTA } \\ & \text { THRESHOLD }=0.4 \end{aligned}$ |
| (Single knife) Harmonic 39 | (Single Knife) Harmonic 48 | (Single knife) Harmonic 38 |

Figure 7.61.S4: RESULTS FOR TIMBER SAMPLE NUMBER G1.S4


| MACHINIMG PARAMETERS | $\begin{aligned} & \text { PRINCIPAL } \\ & \text { PARMNKICS } \end{aligned}$ |
| :---: | :---: |
| Ho. of knives 4 |  |
| cufter Speed 4588 rpm | $h 1=37$ |
| Uib. rate o 1 Pl | $\mathrm{h}^{2}=74$ |
| Proud Knives Ecc, rate/rev col | $\mathrm{hj}=149$ |
| Spindle Runout ${ }^{\text {Of }}$ microns |  |


| AMALYSIS OF FFT's USING FAULT FIHDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFR OH TALY DATR | $\begin{aligned} & \text { FFA OH SSA } \quad \text { DATA } \\ & \text { THRESHOLD }=0.4 \end{aligned}$ |
| $\begin{aligned} & \text { (Single knife) } \\ & \text { Harmonic } 39 \end{aligned}$ | $\begin{aligned} & \text { (Single Knife) } \\ & \text { Harmonic } \end{aligned}$ | (Single knife) Harmonic 38 |

Figure 7.61.S5: RESULTS FOR TIMBER SAMPLE RUMBER 61.S5


| MACHINIMG PRRAMETERS | $\begin{aligned} & \text { PRINCIPAL } \\ & \text { PARAKMICS } \\ & \hline \text { HARMAICS } \\ & \hline \end{aligned}$ |
| :---: | :---: |
| Ho. of knives 4 |  |
|  |  |
|  | h2 $=74$ $h j=149$ |
| Ecc, rate/rev Spindle Runout ${ }^{8}$ \% microns |  |


| AMALYSIS OF FFT's USING FAULT FINDIHG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8.4 | $\begin{aligned} & \text { FFG OM TALY DATA } \\ & \text { THRESHOLD=8.4 } \end{aligned}$ | FFA ON SSA DATA THRESHOLD $=8.4$ |
| (Unknown Faults) Harmonic 42 | (Unknown Faults) Harmonic 43 | (Single knife) Harmonic 38 |

Figure 7.61.S6: RESULTS FOR TIMBER SAMPLE RUMBER G1.56


| MaCHINIMG PARAMETERS | PRINCIPAL |
| :---: | :---: |
| No. of knives 4Feed speedCutter speed6880Ciminrpm | harmonics |
|  |  |
|  | h1 $h_{2}=$ |
| Proud Knives $\frac{1}{\text { a }}$ I7) 1 | $\mathrm{hj}=176$ |
|  |  |


| ANALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA OH ThLY DATA THRESHOLD=0. 4 | FFA OH SSA DATA THRESHOLD=8.4 |
| (Single knife) Harmonic 44 | (Single knife) Harmonic 44 | (Single knife) Hapmonic 44 |

Figure 7.61.57: RESULTS FOR IIMBER SAMPLE NUMBER 61.57


| MachinIng parameters | $\begin{aligned} & \text { PRINCIPAL } \\ & \text { PEEAK } \\ & \text { HRRMONCS } \\ & \hline \end{aligned}$ |
| :---: | :---: |
| No. of knives 4 |  |
| Futter Speed 68888 rpm |  |
| Vib rate 8 | $h_{2}=88$ |
| Proud Knives $\frac{1}{8}$ mpl 1 | $\mathrm{hj}=176$ |
| Eccirate/rev ${ }^{\text {a }} 8$ |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFR) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD=0.4 | FFG OH TALY DATA THRESHOLD $=0.4$ | FFA ON SSA DATA THRESHOLD $=0.4$ |
| (Single knife) Harmonic 43 | (Single knife) Harmonic 43 | (Single knife) Harmonic 44 |

Figure 7.61.S8: RESULTS FOR TIFBER SAMPLE NUMBER G1.58


| MaCHINING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
|  | HRRMOHICS |
|  |  |
|  | $h^{2}=$ |
|  | $\mathrm{hj}=37$ |
|  |  |


| AMRLYSIS OF FFT's USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8.5 | FFA OK TALY DATA THRESHOLD $=8,5$ | FFA OH SSA DATA |
| (Multi-knife) Harmonic 48 | (Unknown Faults) Harmonic 41 | (Multi-knife) Harmonic 38 |

Figure 7.G2.S1: RESULTS FOR TIMBER SAMPLE RUMBER 62.S1


| MACHINING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
|  | harmonics |
|  |  |
|  | $h^{2}=18$ |
|  | hj $=37$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0. 4 | FFA ON TALY OATA <br> THRESHOLD | FFA OH SSA DATA $\text { T̈HRESHOLÖ=0. } 4$ |
| (Multi-knife) <br> Harmonic | (multi-knife) <br> Harmonic | (multi-knife) $\text { Harmonic } 38$ |

Figure 7.62.52: RESULTS FOR IIMBER SAMPLE NUMBER 62.52


| MaCHIHING PaRameters |  |
| :---: | :---: |
| No, of knives |  |
|  |  |
| Vib, rate | $h_{2}=18$ |
| Proud Knives 8 | $\mathrm{hj}=37$ |
| Eccirate/rev |  |


| AMALYSIS OF FFT's USING FAULT FIMDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA OH TALY OATA THRESHOLD $=0.4$ | $\text { FFG OH SSA }{ }_{\text {THRESHOLD }=0.4} \text { ORTR }$ |
| (multi-knife) <br> Harmonic | (Multi-knife) <br> Harmonic 48 | (Multi-knife) Harmonic 38 |

Figure 7.62.S3: RESULTS FOR TIMBER SAMPLE NUMBER G2.53


| MACHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | HARHONICS |
|  | h1 $=9$ |
|  | $h^{2}=18$ |
|  | hj $=37$ |
|  |  |


| AMALYSIS OF FFT's USIMG FAULT FINOING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATR THRESHOLD $=0.4$ | $\begin{aligned} & \text { FFA OH TALY ORTA } \\ & \text { THRESHOLD=9.4 } \end{aligned}$ | FFA OH SSA OATA |
| (Multi-knife) <br> Harmonic 40 | (Multi-knife) <br> Harmonic | (multi-knife) Harmonic 38 |

Figure 7.62.S4a: RESULTS FOR IIMBER SAMPLE NUMBER 62.S4a


| AKALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0. 4 | fFA OH TALY DATA THRESHOLD $=0.4$ | FFA OH SSA DATA THRESHOLD=0.4 |
| cobala | (0, | (0,ba |
| Harmonic 18 | Harmonic? | Harmonic 9 |
| (Multi-knife) | (Multi-knife) | (Multi-knife) |
| Harmonic 48 | Harmonic 48 | Harmonic 38 |

Figure 7.92.s4b: RESULTS FOR IIMBER SAMPLE NUMBER 62.S4b


| MACHINING PARAMETERS | AL |
| :---: | :---: |
|  | HARMONICS |
|  | ht $=$ |
|  | $h 1$ $h_{2}=18$ |
|  | hj $=37$ |
|  |  |


| AMALYSIS OF FFT'S USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD=8.4 | FFA OH TALY DATA THRESHOLD=0.4 | FFA OM SSA DATA THRESHOLD $=0.4$ |
| (0.balance 1) <br> Harmonic 18 <br> (multi-knife) <br> Harmonic 48 <br> (Unknown Faults) | $\begin{gathered} \text { (0.balance } 1 \text { ) } \\ \text { Harmonic } 18 \\ \text { (Unknown Faults) } \\ \text { Hamonic } 31 \\ \text { Harmonic } 41 \end{gathered}$ | $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } \\ & \text { (Multi-knife) } \\ & \text { Harmonic } 38 \end{aligned}$ |

Figure 7.62.S4c: RESULTS FOR TIMBER SAMPLE NUMBER G2.S4c


| MACHIHING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
| No. of knives 6 <br> Feed speed <br> $88 \mathrm{~m} / \mathrm{min}$ <br> Cutter speed <br> 6888 rPA <br> Vib, rate <br> proud Knives <br> Ecc.rate/reu <br> Spindle Runout 8 nicrons | HARTMOHICS |
|  |  |
|  | $\frac{1}{2}=$ |
|  | $h \mathrm{j}=56$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA OH LASER OATA THRESHOLD=0. 4 | FFA OH TALY DATA THRESHOLD=8.4 | FFA OH SSA OATA |
| (0.balance 2) | $\begin{aligned} & \text { (O.balance 2) } \\ & \text { Harmonic 17 } \\ & \text { (fultitiknife) } \\ & \text { Harmonic } 56 \\ & \text { (Unknown Faults) } \\ & \text { harmonic } 39 \end{aligned}$ | (Multi-knife) Harmonic 56 |
| Harmonic 17 |  |  |
| (Multi-knife) |  |  |
| (Unknoun Faults) |  |  |
| Harmonic ${ }^{\text {a }}$ (3 Harmonic 22 |  |  |

Figure 7.62.55: RESULTS FOR TIMBER SAMPLE NUMBER G2.55


| Machining parameters | $\begin{aligned} & \text { PRINCIPAL } \\ & \text { PRREAK } \\ & \text { HRNICS } \end{aligned}$ |
| :---: | :---: |
| Ho. of knives 6 |  |
| feed speed 888 mmin | = |
| Vib. rate | $h 2=18$ |
| Proud Knives 8 | hj $=56$ |
| Eccirate/rev Spindle Runout 8 microns |  |


| AKALYSIS OF FFT's USING FAULT FIMDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFG OH LASER DATA THRESHOLD=8.4 | FFA ON TALY OATA THRESHOLD $=0.4$ | FFA OH SSA DATA THRESHOLD=0.4 |
| $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmonic } 55 \end{aligned}$ | $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmonic } 55 \end{aligned}$ | (Multi-knife) <br> Harmonic 56 |

Figure 7.G2.S6: RESULTS FOR TIMBER SAMPLE HUMBER 62.56


| MACHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | HARMONICS |
|  |  |
|  | $h^{2}=18$ |
|  | $h \mathrm{j}=56$ |
|  |  |



Figure 7.G2.57a: RESULTS FOR TIMBER SAMPLE NUMBER G2.57a


| MaCHIHING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
|  | HARTOHICS |
|  |  |
|  | $h 1$ $h 2=18$ |
|  | $\mathrm{hj}=56$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FIMDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0. 4 | FFA OM TALY DATA THRESHOLD=8.4 | FFA OH SSA DRTA THRESHOLD=8.4 |
| (0.balance 1 ) | co.balance | (0,balanc |
| Harmonic 9 | Harmonic 9 | Harmonic 9 |
| (multi-knife) | (multi-knife) | (multi-knife) |
| Harmonic 55 | (Harmonic 55 | Harmonic 56 |
| (Unknown Faults) | (Unknown faults) Harmonic 46 Harmonic 65 |  |

Figure 7.62.57b: RESULTS FOR TIMBER SAMPLE NUMBER 62.S7b


| MACHINIMG PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | HRRMOHICS |
|  | $1=$ |
|  | $h^{2}=18$ |
|  | $h \mathrm{j}=56$ |
|  |  |


| AMALYSIS OF FFT's USING FRULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA OM TALY DATA THRESHOLD=9. 4 | FFA OH SSA DATA THRESHOLD=0.4 |
| $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic }{ }^{\text {(multi-knife) }} \\ & \text { (marmonic } 55 \end{aligned}$ | (0.balance 1) Harmonic. 18 (multi-knife) Harmonic 54 (Unknown Faults) Harmonic 47 Harmonic 67 | $\begin{aligned} & \text { (O,balance } 1 \text { ( }) \\ & \text { Harmonic } \\ & \text { (hulti-knife) } \\ & \text { Harmonic } 56 \end{aligned}$ |

Figure 7.62.58a: RESULTS FOR IIMBER SAMPLE NUMBER 62.58a


| MACHIMIHG PARAMETERS | PRIMCIPRAL |
| :---: | :---: |
|  | HARHOHICS |
|  | h1 $=$ |
|  | $h^{2}=18$ |
|  | $\mathrm{hj}=56$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD $=8.4$ | FFA OH TALY DATA | FFG OH SSA ORTA |
| $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } 18 \\ & \text { (Multi-knife) } \\ & \text { Harmonic } 59 \end{aligned}$ | (0.balance 1) Harmonic 18 (multi-knife) Harmonic 54 (Unknown Faults) Harmonic 49 Harmonic 68 | $\begin{aligned} & \text { (0.balance 1) } \\ & \text { Harmonic } \\ & \text { (Multi-knife) } \\ & \text { Harmonic } 56 \end{aligned}$ |

Figure 7.62.S8b: RESULTS FOR IIMBER SAMPLE NUMBER G2.58b


| MACHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | harmonics |
|  |  |
|  | $h 2=18$ |
|  | $h j=56$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDIMG RLGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA ON TALY DATA THRESHOLD $=0.4$ | FFA ON SSA DATA THRESHOLD=8.4 |
| $\begin{aligned} & \text { (O.balance } 1 \text { ) } \\ & \text { Hidamonic } \\ & \text { (multi-knife) } \\ & \text { Harmonic } 55 \end{aligned}$ | $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } \\ & \text { (Multi-knife) } \\ & \text { Harmonic } 54 \end{aligned}$ | $\begin{aligned} & \text { (0,balance } 1 \text { ) } \\ & \text { Harmonic } \\ & \text { (multi-knife) } \\ & \text { Harmonic } 56 \end{aligned}$ |

Figure 7.G2.S9a: RESULTS FOR TIMBER SAMPLE RUMBER G2.S9a

| MACHINIMG PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | HARMONICS |
|  |  |
|  | $\mathrm{h}^{2}=$ |
|  | $h \mathrm{j}=56$ |
|  |  |


| AKALYSIS OF FFT's USING FAULT FINDIHG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0. 4 | FFR OH TAL THRESHOLD DATA | FFA OH SSA OATA |
| $\begin{aligned} & \text { (Proud Knife) } \\ & \text { Harmonic } \\ & \text { Harmonic } 18 \end{aligned}$ | (Proud Knife) <br> Harmonic 9 <br> Harmonic 18 Harmonic $2 ?$ | $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } \\ & \text { (multi-knife) } \\ & \text { Harmonic } 56 \end{aligned}$ |

Figure 7.G2.S9b: RESULTS FOR TIMBER SAMPLE NUMBER G2.59b


| MaCHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
| Ho. of knives 6Feed speed $75 \mathrm{~m} / \mathrm{min}$Cutter Speed 6888 rpmUib. rateProud Knives 8Ecc. 8Spindererev 8Runout 8 microns | HARMOHICS |
|  | $h 1=10$ |
|  | h2 2020 |
|  | $h \mathrm{j}=68$ |
|  |  |


| ANALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA OH TALY DATA THRESHOLD=0.4 | FFA OH SSA OATA |
| $\begin{gathered} \text { (O.balance } 1 \text { ) } \\ \text { Harmonic } 18 \\ \text { (Mnlifiknife) } \\ \text { Harmonic } 61 \\ \text { (Unknown Falts) } \\ \text { Harmonic } 29 \end{gathered}$ | ```(Multi-knife) Harmonic 62 (Unknown Faults) Harmonic 72``` | (Multi-knife) Harmonic 68 |

Figure 7.62.S18a: RESULTS FOR IIMBER SAMPLE NUMBER 62.S10a


| MACHINING PARPMETERS | PRIMCIPAL |
| :---: | :---: |
| No. of knives 6 <br> Feed speed <br> Cutter Speed <br> Vib, rate <br> Proud Knives <br> Ecc, rate/rev <br> Spindle Runout 3 microns | Harmorics |
|  | $h 1=18$ |
|  | h2 $=28$ |
|  | $\mathrm{hj}=68$ |
|  |  |


| AMALYSIS OF FFT's USIMG FAULT FIMDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8.4 | FFG OK TALY DATA THESHOLD $=0,4$ | FFA OH SSSA OATA |
| $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } 18 \\ & \text { (malti-knife) } \\ & \text { Harmonic } 61 \end{aligned}$ | (0,balance 1) Marmonic 18 <br> (multi-knife) Harmonic 62 <br> (Unknown Faylts) Harmonic 52 Harmonic 72 | $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } 10 \\ & \text { (multi-knife) } \\ & \text { Harmonic } 68 \text {. } \end{aligned}$ |

Figure 7.62.S18b: RESULTS FOR TIMBER SAMPLE NUMBER G2.S18b


| MaCHINIMG PARAMETERS | $\begin{aligned} & \text { PRINCIPAL } \\ & \text { PEFAX } \\ & \text { HARMONICS } \\ & \hline \end{aligned}$ |
| :---: | :---: |
| Ho. of knives 6 |  |
| Feed speed 75 mmin |  |
| Uib, rate | $h 2=28$ |
| Proud Knives 8 | $h j=68$ |
| Eccirate/rev Spindle Runout $\frac{1}{2}$ nicrons |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA OH TALY DATA THRESHOLD $=0.4$ | $\begin{aligned} & \text { FFA OH SSA } \\ & \text { THRESHOLD }=0.4 \end{aligned}$ |
|  | $\begin{aligned} & \text { (0,balance } 1 \text { ) } \\ & \text { Harmonic } 18 \\ & \text { (Milti-knife) } \\ & \text { Harmonic } 62 \end{aligned}$ | $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } 18 \\ & \text { (hulti-knife) } \\ & \text { Harmonic } 68 \end{aligned}$ |

Figure 7.62.S11a: RESULTS FOR TIMBER SAMPLE NUMBER G2.S11a


| MRCHINIMG PARAMETERS | AL |
| :---: | :---: |
|  | HARMONICS |
|  | h1 $=$ |
|  | $h_{2}=28$ |
|  | $h \mathrm{j}=68$ |
|  |  |



Figure 7.62.S11b: RESULTS FOR IIMBER SAMPLE NUMBER 62.SIIb


| MaCHINIMG PARAMETERS | $\begin{aligned} & \text { PRINCIPRL } \\ & \text { PEAK } \\ & \text { HARMONICS } \\ & \hline \end{aligned}$ |
| :---: | :---: |
| No. of knives 6 |  |
| cutter Speed 6888 rpm | = |
| Vib, rate | $\mathrm{h}^{2}=28$ |
| Proud Knives | $h \mathrm{hj}=68$ |
| Ecci rate/rev Spinde Runout $\frac{1}{3}$ nicrons |  |


| AMRLYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD=8.4 | FFA OH TALY DRTA THRESHOLD=0.4 | FFA OH SSA DATA |
| (0.balance 1) Harmonic ${ }^{10}$ (Multi-knife) Harmonic 61 | $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } 18 \\ & \text { (multi-knife) } \\ & \text { Harmonic } 62 \end{aligned}$ | $\begin{aligned} & \text { (0.balance } 1 \text { ) } \\ & \text { Harmonic } 18 \\ & \text { (Multi-knife) } \\ & \text { Harmonic } 688 \end{aligned}$ |

Figure 7.62.S12a: RESULTS FOR IIMBER SAMPLE NUMBER G2.SI2a



Figure 7.G2.S12b: RESULTS FOR TIMBER SAMPLE NUMBER G2.S12b


| MRCHINING Parameters | $\begin{aligned} & \text { PRIMCIPRL } \\ & \text { PREAK } \\ & \text { HRRONICS } \end{aligned}$ |
| :---: | :---: |
| No of knives 6 |  |
| Cutter speed 68880 mpm | $h 1=18$ |
| proud rate ${ }^{\text {d }}$ |  |
| Proud Knives 8 | $h \mathrm{~h}=68$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FIMDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFF OH LASER DATA THRESHOLD=8.4 | FFA ON TAR Y OATA THRESHOLD $=8.4$ | FFA OH SSA DATA |
| Harmonic 61 |  | Harmonic 68 |

Figure 7.G3.S1: RESULTS FOR TIMBER SAMPLE RUMBER G3.S1


| MaCHIMING PARAMETERS | $\begin{aligned} & \text { PRINCIPAL } \\ & \text { PARMOKICS } \end{aligned}$ |
| :---: | :---: |
| Ho. of knives |  |
| Feed speed $68 \mathrm{~m} / \mathrm{min}$ | $h 1=18$ |
| Vib, rate | h2 $=28$ |
| Proud Knives $\frac{1}{\text { d }}$ ) 71 | $h j=68$ |
| Ecc.rate rev Spindle Runout 8 microns |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA OH TALY DATA THRESHOLD=0.4 | FFA oy ssa data THRESHOLD=0. 4 |
| (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> (Multi-knife) <br> Harmonic 61 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 21 <br> harmonic 38 <br> Harmonic 41 <br> (multi-knife) <br> Harmonic 61 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> Harmonic 38 <br> (Multi-knife) <br> Harmonic 68 |

Figure 7.63.52: RESULTS FOR IIMBER SAMPLE NUMBER G3.52


| MACHINING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
| Ho of knives 6 <br> Feed sped  <br> Cutter Speed  <br> Cumin  <br> vib. rate 688 rpm | harmohics |
|  | h1 $=$ |
|  | h2 $=28$ |
| Proud Knives $\frac{1}{\text { a }}$ m 171 | $h j=68$ |
| Spindle Runout ${ }^{\text {E }}$ microns |  |


| AMALYSIS OF FFT'S USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0.4 | FFA OH TALY DATA THRESHOLD $=0.4$ | FFA OH SSA DATA THRESHOLD=0.4 |
| $\begin{aligned} & \text { (Proud Knife) } \\ & \text { Harmonic } 18 \\ & \text { Harmonic } 28 \end{aligned}$ | (Proud Knife) <br> Harmonic 10 <br> Harmonic 21 <br> Harmonic 31 <br> (Multi-knife) <br> Harmonic 62 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> Harmonic 38 <br> (Multi-knife) <br> Harmonic 68 |

Figure 7.63.53: RESULTS FOR IIMBER SAMPLE NUMBER 63.53


| MaCHINING PARAMETERS | $\begin{aligned} & \hline \text { PRINCIPRL } \\ & \text { PEAK } \\ & \text { HARHONICS } \\ & \hline \end{aligned}$ |
| :---: | :---: |
| Ho, of knives |  |
| cutter speed 6888 rpm | hl $=18$ |
| Uibirate ${ }^{\text {a }}$ | h2 $=28$ |
| Proud Knives $\frac{1}{8}$ )>1 | $h j=68$ |
| Spindle Runout ${ }^{\text {en microns }}$ |  |


| AMALYSIS OF FFT's USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8. 4 | FFA OH TALY DATA THRESHOLD $=0.4$ | FFA ON SSA DATR THRESHOLD $=8.4$ |
| (Proud Knife) <br> Harmonic 18 harmonic 28 (Multi-knife) Harmonic 61 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> (Multi-knife) <br> Harmonic 62 | (Proud Knife) <br> Harmonic 10 <br> Harmonic 28 <br> Harmonic 38 |

Figure 7.g3.S4: RESULTS FOR IIMBER SAMPLE NUMBER G3.S4

| MACHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
| $\begin{aligned} & \text { No. of knives } 6 \\ & \text { Feed speed } \\ & \text { Cutter Speed } \\ & \text { Cutmin } \\ & \text { Vib, rate } \end{aligned}$ | Harmonics |
|  | h1 $=18$ |
| Proud Knives 1 l $\ggg 1$ | $h j=68$ |
| Ecc, rate/rev ${ }^{\text {Spinde Runout }}$ Ónicrons |  |


| AMALYSIS OF FFT's USING FRULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OM LASER DATA THRESHOLD=0.4 | FFA OH TALY DRTA THRESHOLD=8.4 | FFA ON SSA DATA THRESHOLD=0.4 |
| (Proud Knife) <br> Harmonic 18 Harmonic 21 (multi-knife) Harmonic 62 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> (Multi-knife) <br> Harmonic 62 <br> (Unknown Faults) <br> Harmonic 42 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> Harmonic 38 <br> (multi-knife) <br> Harmonic 68 |

Figure 7.63.55: RESULTS FOR IIMBER SAMPLE NUMBER G3.S5


| MaCHIHING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
| $\begin{aligned} & \text { No. of knives } 6 \\ & \text { Feed speed } 75 \mathrm{mmin} \\ & \text { Cutter Speed } 6888 \mathrm{rpm} \end{aligned}$ | HARMOHICS |
|  | $h 1=18$ |
|  | h2 $=28$ $h j=68$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD=8.4 | FFG OH TALY DATA THRESHOLD=0.4 | FFA OH SSA DATA THRESHOLD $=8.4$ |
| (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> (multi-knife) <br> Harmonic 61 <br> (Unknown Faults) <br> Harmonic 41 | (Proud Knife) Harmonic 18 Harmonic 28 (multi-knife) Harmonic 62 (Unknown Faults) Harmonic 42 Harmonic 52 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> (multi-knife) <br> Harmonic 68 |

Figure 7.63.56: RESULTS FOR TIMBER SAMPLE NUMBER G3.56


| MaCHINING PARAMETERS | PRINCIPRL |
| :---: | :---: |
|  | harmohics |
|  |  |
|  | $h 2=28$ $h j=68$ |
|  |  |


| AMALYSIS OF FFT's USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OM LASER DATA THRESHOLD=8.5 | FFR OH TALY DATA THRESHOLD $=8.5$ | FFA OM SSA DATA THRESHOLD $=0.5$ |
| (Proud Knife) <br> Harmonic 10 <br> Harmonic 21 <br> harmonic 3 ( <br> Harmonic 68 | (Proud Knife) Harmonic 18 Harmonic 28 Harmonic 31 Harmonic 41 (multiknike) Harmonic 62 (Unknown Faults) Harmonic 16 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> Harmonic 38 <br> (multi-knife) <br> Harmonic 68 |

Figure 7.G3.S7: RESULTS FOR IIMBER SAMPLE RUMBER G3.57


| MACHIHING PARAMETERS | L |
| :---: | :---: |
| Hoo of knives Feed speed <br> Cutter speed <br> vib. rate <br> Proud Xnives <br> Ecc, rate/rev <br> Spindle Runout 8 microns | harmonics |
|  | ht = |
|  | $\mathrm{h}^{2}=22$ |
|  | $h \mathrm{~h}=69$ |
|  |  |


| ANALYSIS OF FFT's USING FAULT FINDING RLGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA ON LRSER DATR THRESHOLD=8.4 | fFA OH TALY DATA THRESHOLD $=0.4$ | FFA OK SSA DATA THRESHOLD $=8.4$ |
| (Multi-knife) Harmonic | (Multi-knife) <br> Harmonic 69 | $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmonic } 69 \end{aligned}$ |

Figure 7.63.58: RESULTS FOR TIMBER SAMPLE NUMBER 63.58


| MACHIMING PARAMETERS | RL |
| :---: | :---: |
|  | HARMONICS |
|  |  |
|  | h2 $=22$ $h j=69$ |
| Eccirate/rev 8 8 ${ }^{\text {a }}$ |  |


| ANALYSIS OF FFT's USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA OM LASER DATA THRESHOLD=0.4 | FFA OH TALY DATA THRESHOLD $=0.4$ | FFA ON SSA ORTA |
| (Proud Knife) <br> Har monic 12 <br> Harmonic 23 harmonic 35 <br> (Multi-knife) <br> Harmonic 69 | (Proud Knife) <br> Harmonic 12 <br> Harmonic 24 <br> Harmonic 36 <br> (Multi-knife) <br> Harmonic 7 | (Proud Knife) <br> Harmonic 12 <br> Harmonic 23 <br> (multi-knife) <br> Harmonic 69 |

Figure 7.63.59: RESULTS FOR IIMBER SAMPLE RUMBER 63.59


| MaCHINING PARAMETERS | AL |
| :---: | :---: |
| Ho. of knives 6 <br> Feedd sped  <br> Cutter speed 6598 min <br> Uib. rate 88 | harmonics |
|  | h1 $=11$ |
|  | h2 $=22$ $h \mathrm{j}=69$ |
| Proud xnives ${ }^{\text {Ecc,rate/rev }}$ |  |
| Spindle Runout 8 nicrons |  |


| AMMLYSIS OF FFT's USING FAULT FINDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD=0.4 | FFA OK TALY DRTA THRESHOLD 0 . | FFA OH SSA ORTA |
| $\begin{aligned} & \text { (Proud Knife) } \\ & \text { Harmonic } 12 \\ & \text { harmonic } 24 \end{aligned}$ | (Proud Knife) <br> Harmonic 12 <br> Harmonic 24 <br> Harmonic 36 Harmonic 48 <br> (multi-knife) <br> Harmonic 70 | (Proud Knife) <br> Harmonic 12 <br> Harmonic 23 <br> Harmonic 35 <br> (multi-knife) <br> Harmonic 69 |

Figure 7.63.S18: RESULTS FOR TIMBER SAMPLE NUMBER 63.S10


| MACHINING PARAMETERS | $\begin{aligned} & \text { PRINCIPAL } \\ & \text { PAREAK } \\ & \text { PAROHICS } \end{aligned}$ |
| :---: | :---: |
|  |  |
|  | h1 $=$ |
|  | h2 $=22$ |
| Proud Knives $\frac{1}{\text { d }}$ P1 1 | $h j=69$ |
| Eccindle Runout 8 microns |  |


| ANALYSIS OF FFT's USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFG OH LASER DATA THRESHOLD=8.5 | FFG OH TALY OATA | $\begin{aligned} & \text { FFA ON SSA OATR } \\ & \text { THRESHOLD }=8.5 \end{aligned}$ |
| (Proud Knife) <br> Harmonic 11 Harmonic 24 (Unknown Faults) Harmonic 38 Harmonic 58 | (Proud Knife) Harmonic 12 Harmonic 24 Harmonic 36 (miti-knife) Harmonic 67 (0igital noise) Harmonic 184 (Unknown Faults) Harmonic 72 | (Proud Knife) <br> Harmonic 12 <br> Harmonic 23 <br> Harmonic 35 <br> (multi-knife) <br> Harmonic 69 |

Figure 7.63.S1L: RESULTS FOR TIMBER SAMPLE NUMBER G3.S11


| MACHINING PARAMETERS | AL |
| :---: | :---: |
| Ho. of knives 8 <br> Feed speed <br> $98 \mathrm{~m} / \mathrm{min}$ <br> cutter speed <br> Vib, rate <br> Proud Knives <br> Ecc.rate/rev <br> Spindle Runout 8 microns | harmonics |
|  | = |
|  | = 16 |
|  | $h \mathrm{j}=66$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA ON LASER DATA THRESHOLD=8.4 | FFA ON TALY DATA THRESHOLD $=0.4$ | FFG OH SSA DATA |
| (Multi-knife) Harmonic 67 <br> (Unknown Faults) Harmonic 28 Harmonic 33 Harmonic 42 | (Proud Knife) <br> Harmonic 9 <br> Harmonic 19 <br> (multi-knife) <br> Harmonic 68 <br> (Unknown Faults) <br> Harmonic 33 | (Multi-knife) Harmonic 67 |

Figure 7.63.S12: RESULTS FOR IIMBER SAMPLE NUMBER 63.SI2

| MRCHINING PARAMETERS | L |
| :---: | :---: |
|  | HARMONICS |
|  | $h 1=8$ |
|  |  |
|  | hj |
|  |  |


| AMRLYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LRSER DRTA THRESHOLD=0.5 | FFA ON TALY DATA THRESHOLD $=8.5$ | FFA OHRESHOLD $=0.5$ DATA |
| (Proud Knife) <br> Harmonic 8 <br> Harmonic 16 <br> Harmonic 25 <br> Harmonic 33 | (Proud Knife) <br> Harmonic 8 <br> Harmonic 17 Harmonic 25 <br> Harmonic 34 <br> Harmonic 42 <br> Harmonic 59 <br> Harmonic 59 | (Proud Knife) <br> Harmonic 8 <br> Harmonic 17 Harmonic 25 <br> Harmonic 33 <br> Harmonic 42 <br> Harmonic 58 <br> (Multi-knife) Harmonic 67 |

Figure 7.63.S13: RESULTS FOR IIMBER SAMPLE NUMBER G3.S13


| MACHINING PARAMETERS | $\begin{aligned} & \text { PRIMCIPAL } \\ & \text { HARGK } \\ & \text { HAROMCS } \end{aligned}$ |
| :---: | :---: |
| No. of knives 8 |  |
| $\begin{aligned} & \text { reed speed } \\ & \text { cutter speed } 6888 \text { ran } \\ & \text { Uib. pate } \end{aligned}$ | $\begin{array}{ll}h 1 & =8 \\ h 2 & =16\end{array}$ |
| Proud Knives ? >>1 1235678 | hj $=66$ |
| Eccirate/rev ${ }^{\text {a }}$ Sindle Runout 8 nicrons |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8.5 | FFA OH THLY DATA THRESHOLD $=9.5$ | FFA OH SSA DRTA |
| (Proud Knife) | (Proud Knife) | (Proud Kni |
| Harmonic 8 | Harmonic 8 | Harmonic |
| Harmonic 1? | Harmonic 16 | Harmonic 17 |
| Harmonic 25 | Harmonic 25 | Harmonic 25 |
|  |  |  |
| (multi-knife) | Harmonic 42 | (Multi-knife) |
| Harmonic 67 | Harmonic 51 (Multi-knife) | Harmonic 67 |
|  | (Harmonic 66 |  |

Figure 7.63.S14: RESULTS FOR IIMBER SAMPLE NUMBER G3.S14

| MACHINING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
|  | harmonics |
|  | ht $=$ |
|  | h2 $=16$ |
|  | $h \mathrm{j}=66$ |
| Spindle Runout ${ }^{\text {a microns }}$ |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DRTA THRESHOLD $=0.4$ | FFA ON TALY DATA THRESHOLD=0.4 | FFA ON SSA DATA THRESHOLD $=0.4$ |
| (0.balance 2) | (0,balance | 0.1 |
|  |  |  |
| (multi-knife) | (multi-knife) | (multi-knife) |
| Harmonic 67 | Harmonic 68 | Harmonic 67 |
| $\begin{aligned} & \text { (Unnkown Faults) } \\ & \text { Harmonic } 33 \end{aligned}$ | (Unknown Faults) Harmonic 34 Harmonic 51 | (Unknown Faults) Harmonic 33 |

Figure 7.63.S15: RESULTS FOR IIMBER SAMPLE RUMBER G3.S15


| MaCHINING PARAMETERS | L |
| :---: | :---: |
|  | HARMONICS |
|  | = |
|  | $h 2=74$ |
| Proud Knives $\frac{1}{9}$ m>1 | hj $=149$ |
| Ecc.rate/rev ${ }^{\text {Spindle Runout }} 8$ |  |


| ANALYSIS OF FFT's USING FAULT FINDIHG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { FFA OH LLSER OATA } \\ & \text { THESHOLD=0.4 } \end{aligned}$ | FFA OH TALY DRTA THRESHOLD $=8.4$ | IHRESHOLD=0.4 |
| (Single knife) Harmonic 38 | (Single knife) Harmonic 37 | (Single knife) Harmonic 38 |

Figure 7.G4.S1a: RESULTS FOR IIMBER SAMPLE NUMBER G4.S1a


| MACHIMIHG PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | Harmonics |
|  | 11 $=37$ $=37$ |
|  | hj $\mathrm{hj}=149$ |
|  |  |


| ANALYSIS OF FFT's USING FAULT FINDING RLGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0. 4 | fFA ON TALY dATA THRESHOLD=8.4 | FFA OH SSA DATA <br> THRESHOLD=0.4 |
| (Single knife) Harmonic 36 |  | (Single knife) Harmonic 38 |

Figure 7.64.S1b: RESULTS FOR IIMBER SAMPLE NUMBER G4.SIb

## 

| MACHIMING PARAMETERS | PAL |
| :---: | :---: |
|  | harmonics |
|  | $1=$ |
|  | $2=$ |
|  | hj $=37$ |
|  |  |


| AMALYSIS OF FFT'S USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OX LASER DATA THRESHOLD=8.4 | FFA ON TALY OATA THRESHOLD=0.4 | FFA OH SSA DATA THRESHOLD $=0.4$ |
| (Multi-knife) <br> Harmonic 37 | (Multi-knife) Harmonic 38 | (Multi-knife) <br> Harmonic 38 |

Figure 7.64.S2a: RESULTS FOR IIMBER SAMPLE NUMBER 64.52a


| MACHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | Hartonics |
|  |  |
|  | $\mathrm{h}^{2}=$ |
|  | $\mathrm{hj}=37$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD=8.4 | FFA ON TALY DATA THRESHOLD=8.4 | FFA OH SSSA DATA |
| (Proud Knife) <br> Harmonic 9 <br> Harmonic 18 | (Proud Knife) <br> Harmonic 9 <br> Harmonic 19 | Harmonic 38 |

Figure 7.64.S2b: RESULTS FOR TIMBER SAMPLE NUMBER G4.S2b


| MACHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | harmonics |
|  | h1 $=$ |
|  | $h^{2}=18$ |
|  | $h \mathrm{~h}=56$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA ON LASER DATA THRESHOLD=0.4 | FFG OK TARLY DATA THRESHOLD=8.4 | $\begin{aligned} & \text { FFA ON SSA DRTA } \\ & \text { THRESHOLD=8,4 } \end{aligned}$ |
| (Multi-knife) <br> Harmonic 55 | (Multi-knife) <br> Harmonic 55 | (Multi-knife) <br> Harmonic 56 |

Figure 7.64.S3a: RESULTS FOR TIMBER SRMPLE NUMBER 64.S3a


| MACHIMING PARAMETERS | AL |
| :---: | :---: |
| No. of knives Feed speed <br> cutter Speed <br> Vib. rate <br> proud Xnives <br> Ecc.rate/rev | HARHONICS |
|  |  |
|  | 1 $=18$ |
|  | hj $=56$ |
|  |  |


| AKALYSIS OF FFT'S USIHG FAULT FIHDIMG ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8.4 | FFA ON TALY DATA THRESHOLD=8.4 | $\text { FFA OH SSA } \quad \text { THTE }$ |
| (Proud Knife) <br> Harmonic 9 <br> Harmonic 18 <br> (multi-knife) <br> Harmonic 55 | (Proud Knife) Harmonic 9 Harmonic 18 (multi-knife) Harmonic 54 <br> (Unknown Faults) harmonic 4 Harmonic 64 | $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmonic } 56 \end{aligned}$ |

Figure 7.64.S3b: RESULTS FOR IIMBER SAMPLE NUMBER G4.53b


| MACHINING PARAMETERS | PRINCIPAL |
| :---: | :---: |
|  | harmonics |
|  |  |
|  | $h^{2}=$ |
|  | $\mathrm{hj}=56$ |
|  |  |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA ON LASER DATA THRESHOLD=0. 4 | FFA OH TALY DATA THRESHOLD=8.4 | FFA ON SSA OATA THRESHOLD=8.4 |
| (Proud Knife) <br> Harmonic 9 <br> Harmonic 18 | (Proud Knife) <br> Harmonic 9 Harmonic 18 Harmonic 27 | $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmonic } 56 \end{aligned}$ |

Figure 7.64.S3c: RESULTS FOR TIMBER SAMPLE NUMBER G4.S3c


| MACHIHING PARAMETERS | L |
| :---: | :---: |
| Ho, of knives 6 <br> Feed speed $88 \mathrm{~m} / \mathrm{min}$ <br> Cutter Speed 6888 rpm <br> Vib, rate 8 <br> Proud Knives 8 <br> Ecc rate/rev 8 <br> Spindle Runout 8 microns | harmokics |
|  |  |
|  | = |
|  | $h \mathrm{j}=56$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINOING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA OH LASER DATA THRESHOLD $=0.4$ | FFA OH TALY DATA THRESHOLD=9.4 | $\begin{aligned} & \text { FFA OH SSA DRTA } \\ & \text { THRESHOLD }=0.4 \end{aligned}$ |
| (Proud Knife) <br> Harmonic 9 Harmonic 18 | $\begin{aligned} & \text { (Proud Knife) } \\ & \text { Harmonic } \\ & \text { Harmonic } 18 \\ & \hline \end{aligned}$ | (Harti-knife) |

Figure 7.64.S4: RESULTS FOR TIMBER SAMPLE RUMBER G4.S4


| MACHINIHG PARAMETERS | $\begin{aligned} & \hline \text { PRINCIPAL } \\ & \text { PEAK } \\ & \text { HARMONICS } \\ & \hline \end{aligned}$ |
| :---: | :---: |
| No. of knives 6 |  |
| cutter Speed 6888 rpm | h1 $=$ |
| vib. rate | $h 2=22$ |
| Proud Knives 8 | $h j=69$ |
| Ecc, rate Spindle Runout g nicrons |  |


| ANALYSIS OF FFT's USING FRULT FINDING RLGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=0. 4 | FFA OH TALY DATA THRESHOLD $=0.4$ | FFR ON SSA DRTA |
| (Multi-knife) Harmonic 69 | (Multi-knife) <br> Harmonic 69 | (Multi-knife) Harmonic |

Figure 7.64.55a: RESULTS FOR TIMBER SAMPLE NUMBER G4.55a


| MACHINING PARAMETERS | PRIMCIPAL |
| :---: | :---: |
| Ho. of knives 6 <br> Feed speed <br> Cutter speed <br> vib, rate <br> proud Knives <br> Ecc.rate/reu <br> Spindle Runout 8 microns | harmonics |
|  | h1 $=$ |
|  | $\mathrm{h}^{2}=$ |
|  | $\mathrm{hj}=69$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8. 4 | FFA ON TALY OATA THRESHOLD $=8,4$ | FFA OH SSA DATA THRESHOLD=8.4 |
| $\qquad$ | (Multi-knife) Harmonic 71 (Unknoun Faults) Harmonic 17 Harmonic 24 Harmonic 35 Harmonic Harmonic 65 | $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmonic } 69 \end{aligned}$ |

Figure 7.64.S5b: RESULTS FOR IIMBER SAMPLE NUMBER 64.S5b


| MaCHIMIMG PARAMETERS | AL |
| :---: | :---: |
| Ho. of knives 6 <br> Feed speed <br> Cutter speed <br> vib, rate <br> Proud Knives <br> Ecc, rate/rev <br> Spindle Runout 8 microns | HARMONICS |
|  |  |
|  | h2 $=28$ |
|  | $h^{j}=68$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA OM LASER DATA THRESHOLD=8.4 | FFA OH TALY DATA THRESHOLD=8.4 | FFA ON SSA DATA THRESHOLD $=0.4$ |
| (multi-knife) <br> Harmonic 61 | (Multi-knife) <br> Harmonic 62 | (Multi-knife) Harmonic 68 |

Figure 7.64.S6a: RESULTS FOR TIMBER SAMPLE NUMBER 64.56a


| MaCHINIMG PARAMETERS | PRINCIPAL |
| :---: | :---: |
| Ho. of knives 6Feed speed $75 \mathrm{~m} / \mathrm{min}$Cutter Speed 6888 rpmVib. rateProud Knives 8Ecc.rate/rev 8Spindle Runout 8 microns | harmorics |
|  | $h 1=$ |
|  | h2 $=28$ |
|  | $h j=68$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD=8.4 | FFG OH TALY DATA THRESHOLD $=0.4$ | $\text { FFA OHRESHOLD=8.4 } 4$ |
| (Proud Knife) Harmonic 18 Harmonic 28 (Unknown Faults) Harmonic 16 Harmonic 41 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> (Multi-knife) <br> Harmonic 61 <br> (Unknoun Faults) <br> Harmonic 22 <br> Harmonic 42 <br> Harmonic 52 <br> Harmonic 73 | (Multi-knife) Harmonic 68 |

Figure 7.64.56b: RESULTS FOR TIMBER SAMPLE NUMBER 64.S6b


| MRCHINING PARRMETERS | PRINCIPAL |
| :---: | :---: |
| No. of knives 6 <br> Feed speed <br> $75 \mathrm{~m} / \mathrm{min}$ <br> cutter speed <br> Vib. rate <br> Proud Knives <br> Ecc, rate/reu <br> Spindle Runout 8 microns | harmonics |
|  | hl $=$ |
|  | $\mathrm{h}^{2}=$ |
|  | hj $=68$ |
|  |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFR OH LASER DATA THRESHOLD=0.4 | $\begin{gathered} \text { FFA OH TALY OATA } \\ \text { THRESHOLD=0. } 4 \end{gathered}$ | FFA ON SSA DATA THRESHOLD $=0.4$ |
| (Proud Knife) Harmonic 18 Harmonic 21 Harmonic 38 (Unknown Faults) Harmonic 17 |  | $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmonic } 68 \text { in } \end{aligned}$ |

Figure 7.64.S6c: RESULTS FOR TIMBER SAMPLE NUMBER 64.S6c


| MACHINING PRRAMETERS | $\begin{aligned} & \text { PRIMCIPAL } \\ & \text { PARAK } \\ & \text { HRBOHICS } \end{aligned}$ |
| :---: | :---: |
| Ho. of knives |  |
| Feed speed 75 mmin | $h 1=18$ |
| vib. rate | $h 2=28$ |
| Proud Knives 8 | $h \mathrm{j}=68$ |
| Ecc.rate/rev Spindle Runout 8 micro |  |


| AMALYSIS OF FFT's USIMG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OM LASER DATA THRESHOLD $=8.4$ | FFA OH TALY DATA | FFA OH SSA DATA THRESHOLD=0.4 |
| (Multi-knife) $\text { Harmonic } 61$ | (Multi-knife) <br> Harmonic 62 | $\begin{aligned} & \text { (Multi-knife) } \\ & \text { Harmanic } 68 \text { ) } \end{aligned}$ |

Figure 7.G5.S1: RESULTS FOR TIMBER SAMPLE RUMBER 65.51


| MACHIHING PARAMETERS | $\begin{aligned} & \text { PRIMCIPAL } \\ & \text { PBREAK } \\ & \text { HARHONICS } \end{aligned}$ |
| :---: | :---: |
| No. of knives |  |
| Feed speed $75 \mathrm{~m} / \mathrm{min}$ | h1 $=$ |
| Vib. rate | $\mathrm{h}^{2}=28$ |
| Proud Knives | $\mathrm{hj}=68$ |
| Eccinder reve $\frac{1}{2}$ microns |  |

AMALYSIS OF FFT'S USING FAULT FINDING ALGORITHM (FFA)

| FFG ON LASER DATA THRESHOLD=0.4 | FFA OH TALY <br> THRESHOLD $=8.4$ | FFA ON SSA DATA THRESHOLD=0.4 |
| :---: | :---: | :---: |
| (0.balance 1) | (0,balance 1) | (0,balance 1) |
| (Harmonic ${ }^{\text {(muli-knife) }}$ | Harmonic 18 <br> (multi-knife) | (Marmonic ${ }^{\text {(18) }}$ |
| ( ${ }^{\text {mar monic } 61}$ | Harmonic 62 | (marmonic 68 |

Figure 7.65.S2: RESULTS FOR IIMBER SAMPLE NUMBER G5.S2


| MACHINIMG PARAMETERS | $\begin{aligned} & \text { PRINCIPRL } \\ & \text { PERAK } \\ & \text { HRMONICS } \\ & \hline \end{aligned}$ |
| :---: | :---: |
| Ho. of knives 6 |  |
| Cutter speed 6888 rpm | h1 $=18$ |
| Proud Knives $\frac{1}{1}$ m>1 | hj $=68$ |
| Ecc.raterrev |  |


| AMALYSIS OF FFT's USIHG FAULT FINDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DATA THRESHOLD $=8.4$ | fFA OH TALY DATA THRESHOLD=0.4 | FFA OH SSA DATR THRESHOLD=8.4 |
| (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> Harmonic 31 <br> Harmonic 41 <br> (hulti-knife) <br> Harmonic 61 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 21 <br> harmonic 32 <br> harmonic 41 <br> (multi-knife) <br> Harmonic 63 | (Proud Knife) Harmonic 18 harmonic 28 |

Figure 7.65.53: RESULTS FOR TIMBER SAMPLE NUMBER 65.53


| MachinIHg Parameters | $\begin{aligned} & \hline \text { PRINCIPAL } \\ & \text { PEAK } \\ & \text { HARHONICS } \end{aligned}$ |
| :---: | :---: |
| Ho. of knives |  |
| Cutter Speed 6888 rpm | $h 1=18$ |
|  | hj $=68$ |
| Ecc.rate/rev Spindle Runout 2 |  |


| AMALYSIS OF FFT's USING FAULT FIHDING ALGORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| fFA OH LASER DATA THRESHOLD=8. 4 | FFA OH TALY OATA HRESHOLD=0.4 | FFA OH SSA DATA THRESHOLD=0.4 |
| (Proud Knife) Harmonic 11 harmonic 22 | (Proud Knife) Harmonic 11 harmonic 22 Harmonic 33 (Unknoun Faults) Harmonic 24 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 28 <br> (multi-knife) <br> Harmonic 68 |

Figure 7.65.S4: RESULTS FOR TIMBER SAMPLE NUMBER 65.54


| MACHINIMG PARAMETERS | PRINCIPAL |
| :---: | :---: |
| No. of knives 6 <br> Feed sped  <br> Cutter speed  <br> Cis.min  <br> Vib. rate 688 rpm | HARMONICS |
|  | h1 $=18$ |
|  | h2 $=28$ $h j=68$ |
| Eccirate/rev Spindje Runout $\frac{1}{2}$ microns |  |


| AMALYSIS OF FFT's USING FAULT FINDING ALCORITHM (FFA) |  |  |
| :---: | :---: | :---: |
| FFA OH LASER DRTA THRESHOLD=8.4 | FFA OH TALY DATA THRESHOLD=0.4 | FFA ON SSA DATA THRESHOLD=8.4 |
| (Proud Knife) Harmonic 18 harmonic 28 | (Proud Knife) <br> Harmonic 18 <br> Harmonic 21 <br> Harmonic 31 <br> (multi-knife) <br> Harmonic 62 | (Proud Knife) Harmonic 18 Harmonic 28 (multi-knife) Harmonic 68 |

Figure 7.65.S5: RESULTS FOR IIMBER SAMPLE NUMBER 65.55

## TABLES

## Table 1

## Calibration Table for micrometer-controlled

## Angle of Incidence of Timber Illumination

| Barrel | Transverse Distance | Angle of Incidence | Angle of Incidence |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | $0^{8}-0^{\circ}-0^{\prime \prime}$ |
| 1 | 6.0 | 0.1261 | $0^{\circ}-7 \cdot 34^{\prime \prime}$ |
| 2 | 12.5 | 0.2627 | $0^{\circ}-15^{\circ}-46^{\prime \prime}$ |
| 3 | 19.5 | 0.4098 | $0^{\circ}-24^{\prime}-35^{\prime \prime}$ |
| 4 | 25.5 | 0.5360 | $0^{\circ}-23^{\prime}-09^{\prime \prime}$ |
| 5 | 32.5 | 0.6831 | 0\%-40'-59" |
| 6 | 39.0 | 0.8197 | $0^{0}-49^{\circ}-11^{\prime \prime}$ |
| 7 | 45.5 | 0.9562 | $0^{0}-57^{\prime}-22^{\prime \prime}$ |
| 8 | 52.0 | 1.0928 | 1'5'-34" |
| 9 | 58.5 | 1.2294 | 1.13'-46" |
| 10 | 65.0 | 1.3659 | $1^{1-21-57 "}$ |
| 11 | 71.0 | 1.5025 | 1-30'-09" |
| 12 | 78.0 | 1.6390 | 1-38 ${ }^{\text {²0 }}$ - ${ }^{\prime \prime}$ |
| 13 | 84.0 | 1.7650 | $1^{-45}{ }^{\prime} \cdot 54^{\prime \prime}$ |
| 14 | 90.5 | 1.9015 | 1.54'-05" |
| 15 | 97.0 | 2.0379 | $2^{2}-02^{\prime}-16^{\prime \prime}$ |
| 16 | 103.5 | 2.1743 | $2^{\prime} \cdot 10^{\prime}-28^{\prime \prime}$ |
| 17 | 110.0 | 2.3108 | $2^{\text {P-1 }} 18^{\text {²-39 }}$ |
| 18 | 116.0 | 2.4366 | $2^{2}-26^{\prime} \cdot 12^{\prime \prime}$ |
| 19 | 122.0 | 2.5625 | $2^{2}-33^{\prime}-45^{\prime \prime}$ |
| 20 | 129.0 | 2.7093 | $2^{\prime \prime} 42^{\prime}-34^{\prime \prime}$ |

## Table 2

## Example of Bit Reversal for 3 bits

| Natural Order |  | Bit - reversed Order |  |
| :---: | :---: | :---: | :---: |
| Decimal | Binary | Binary | Decimal |
| 0 | 000 | 000 | 0 |
| 1 | 001 | 100 | 4 |
| 2 | 010 | 010 | 2 |
| 3 | 011 | 110 | 6 |
| 4 | 100 | 001 | 1 |
| 5 | 101 | 101 | 5 |
| 6 | 110 | 011 | 3 |
| 7 | 111 | 111 | 7 |

TABLE G1: SINGLE KNIFE FINISH

| Sample <br> Number | Number <br> of Knives | Head speed <br> (rpm) | Feed speed <br> (m/min) | Machine <br> Condition |
| :---: | :---: | :---: | :---: | :---: |
| G1.S1 | 4 | 4500 | 15 | Fully set <br> Skf |
| G1.S2 | 4 | 4500 | 15 | Fully set <br> Skf |
| G1.S3 | 4 | 4500 | 30 | Fully set <br> Skf |
| G1.S4 | 4 | 9000 | 30 | Fully set <br> Skf |
| G1.S5 | 4 | 9000 | 30 | Fully set <br> Skf |
| G1.S6 | 4 | 9000 | 30 | Fully set <br> Skf |
| G1.S7 | 4 | 6000 | 17 | Fully set <br> Skf |
| G1.S8 | 4 | 6000 | 17 | Fully set <br> Skf |

TABLE G2: UNBALANCED CUTTERHEAD

| Sample <br> Number | Number <br> of Knives | Head speed <br> (rpm) | Feed speed <br> $(\mathrm{m} / \mathrm{min})$ | Machine Condition |
| :---: | :---: | :---: | :---: | :---: |
| G2.S1 | 4 | 4500 | 60 | Fully set |
| G2.S2 | 4 | 4500 | 60 | Fully set |
| G2.S3 | 4 | 4500 | 60 | Fully set |
| G2.S4a | 4 | 4500 | 60 | O-bal:1 screw |
| G2.S4b | 4 | 4500 | 60 | O-bal:3 screws |
| G2.S4c | 4 | 4500 | 60 | O-bal:5 screws |
| G3.S5 | 6 | 6000 | 80 | Fully set |
| G2.S6 | 6 | 6000 | 80 | Fully set |
| G2.S7a | 6 | 6000 | 80 | O-bal:3 screws |
| G2.S7b | 6 | 6000 | 80 | O-bal:5 screws |
| G2.S8a | 6 | 6000 | 80 | O-bal:3 screws |
| G2.S8b | 6 | 6000 | 80 | O-bal:5 screws |
| G2.S9a | 6 | 6000 | 80 | O-bal:3 screws Wet timber |
| G2.S10a | 6 | 6000 | 75 | Fully set |
| G2.S10b | 6 | 6000 | 75 | O-bal:3 screws |
| G2.S11a | 6 | 6000 | 75 | O-bal:2 screws |
| G2.S11b | 6 | 6000 | 75 | O-bal:3 screws |
| G2.S12a | 6 | 6000 | 75 | O-bal:3 screws |
| G2.S12b | 6 | 6000 | 75 | O-bal:3 screws |

TABLE G3: PROUD KNIFE

| Sample <br> Number | Number of Knives | Head speed (rpm) | Feed speed (m/min) | Machine Condition |
| :---: | :---: | :---: | :---: | :---: |
| G3.S1 | 6 | 6000 | 75 | Fully set |
| G3.S2 | 6 | 6000 | 75 | 1 proud:+4um |
| G3.S3 | 6 | 6000 | 75 | 1 proud: +8 mm |
| G3.S4 | 6 | 6000 | 75 | 1 proud: $+12 \mu \mathrm{~m}$ |
| G3.S5 | 6 | 6000 | 75 | 1 proud: $+8 \mu \mathrm{~m}$ |
| G3.S6 | 6 | 6000 | 75 | 1,2 proud: $+8 \mu \mathrm{~m}$ |
| G3.S7 | 6 | 6000 | 75 | 1,3 proud: $+8 \mu \mathrm{~m}$ |
| G3.S8 | 6 | 6000 | 65 | fully set |
| G3.S9 | 6 | 6000 | 65 | 1 proud: $+4 \mu \mathrm{~m}$ |
| G3.S10 | 6 | 6000 | 65 | 1 proud: $+8 \mu \mathrm{~m}$ |
| G3.S11 | 6 | 6000 | 65 | 1 proud: $+12 \mu \mathrm{~m}$ |
| G3.S12 | 8 | 6000 | 90 | fully set |
| G3.S13 | 8 | 6000 | 90 | 1 proud: $-4 \mu \mathrm{~m}$ |
| G3.S14 | 8 | 6000 | 90 | 1 proud: -8 $\mu \mathrm{m}$ |
| G3.S15 | 8 | 6000 | 90 | 4,8 proud: -8 $\mu \mathrm{m}$ |

TABLE G4: TIMBER VIBRATION

| Sample <br> Number | Number <br> of Knives | Head speed <br> (rpm) | Feed speed <br> $(\mathrm{m} / \mathrm{min})$ | Machine Condition |
| :---: | :---: | :---: | :---: | :---: |
| G4.S1a | 4 | 4500 | 15 | Fully set <br> Single knife finish |
| G4.S1b | 4 | 4500 | 15 | No chipbreaker Skf |
| G4.S2a | 4 | 4500 | 60 | Fully set |
| G4.S2b | 4 | 4500 | 60 | No top pressure <br> No chipbreaker |
| G4.S3a | 6 | 6000 | 80 | Fully set |
| G4.S3b | 6 | 6000 | 80 | Outboard bearing tied <br> but un-pressurised |
| G4.S3c | 6 | 6000 | 80 | Outboard bearing untied <br> and un-pressurised |
| G4.S4 | 6 | 6000 | 80 | No outboard bearing |
| G4.Sea | 6 | 6000 | 65 | Fully set |
| G4.S5b | 6 | 6000 | 65 | chipbreaker:1Bar |
| G4.S6a | 6 | 6000 | 75 | Fully set |
| G4.S6b | 6 | 6000 | 75 | chipbreaker:2Bar |
| G4.S6c | 6 | 6000 | 75 | chipbreaker:1Bar |

TABLE G5: FAULT COMBINATION
$\left.\begin{array}{|c|c|c|c|c|}\hline \begin{array}{c}\text { Sample } \\ \text { Number }\end{array} & \begin{array}{c}\text { Number } \\ \text { of Knives }\end{array} & \begin{array}{c}\text { Head speed } \\ \text { (rpm) }\end{array} & \begin{array}{c}\text { Feed speed } \\ (\mathrm{m} / \mathrm{min})\end{array} & \text { Machine Condition } \\ \hline \text { G5.S1 } & 6 & 6000 & 65 & \text { fully set joint } \\ \hline \text { G5.S2 } & 6 & 6000 & 65 & \text { O-bal:2 screws } \\ \hline \text { G5.S3 } & 6 & 6000 & 65 & \begin{array}{c}\text { O-bal:2 screws } \\ 1 \text { proud: }+8 \mu \mathrm{~m}\end{array} \\ \hline \text { G5.S4 } & 6 & 6000 & 65 & \begin{array}{c}\text { O-bal:2 screws } \\ 1 \text { proud: }+8 \mu \mathrm{~m} \\ \text { Chipbreaker: } 1 \text { Bar }\end{array} \\ \hline \text { G5.S5 } & 6 & 6000 & 65 & \begin{array}{c}\text { O-bal:2 screws } \\ 1 \text { proud: }+8 \mu \mathrm{~m}\end{array} \\ \text { Chipbreaker: } 1 \text { Bar } \\ \text { Outboard Bearing: untied }\end{array}\right]$

## APPENDICES

## APPENDIX A: COMPUTER SOFTWARE

APPENDIX A0: LOCI-0
APPENDIX A1: LOCI-1
APPENDIX A2: LOCI-2
APPENDIX A3: LOCI-3
APPENDIX A4: Surface Simulation Algorithm (SSA)
APPENDIX A5: Data Capture Software
APPENDIX A6: FFT Algorithm: BBC BASIC Version
APPENDIX A7: FFT Algorithm: Machine Code Version
APPENDIX A8: Fault Finding Algorithm (FFA)

## APPENDIX B: LASER; PHOTODIODE; TALYROND 200

APPENDIX B1: Helium-Neon Laser data sheet
APPENDIX B2: Laser light Production
APPENDIX B3: Photodiodes
APPENDIX B4: Talyrond 200

## APPENDIX C: CIRCUIT DIAGRAMS

APPENDIX C1: Electronic Hardware

## APPENDIX D:

APPENDIX D1: Cutterhead Balancing

## APPENDIX E: PUBLISHED PAPERS

## Appendix A0: LOCI-0

10 REM LOCI-0
20 XORG=0: YORG=0
30 INPUT "NO OF KNIVES" N1
40 V1=300: W1=2
$50 \mathrm{H} 1=450: \mathrm{R} 1=200: \mathrm{Tw}=275: \mathrm{F} 1=\mathrm{PI}+\mathrm{ASN}((\mathrm{H} 1-\mathrm{Tw}) / \mathrm{R} 1)$
60 MOVE XORG,YORG:DRAW XORG,YORG+Tw:
MOVE XORG,YORG+Tw:DRAW XORG+1280,YORG+Tw
$70 \mathrm{Lb}=2 * \mathrm{PI} / \mathrm{N} 1$
80 YORG=YORG+H1
90 XORG=XORG+R1
100 FOR I=1 TO N1
$110 \mathrm{Lg}=(\mathrm{I}-1)^{*} \mathrm{Lb}$
120 X=R1*(COS(F1-Lg)-COS(PI/2))
$130 \quad \mathrm{Y}=\mathrm{R} 1 *$ SIN(F1-Lg)-SIN(0)
140 MOVE XORG,YORG: DRAW XORG+X,YORG+Y
150 FOR dt=0.1 TO PI STEP 0.1
$\begin{array}{ll}160 & Y=R 1 * S I N(F 1-L g+W 1 * d t)-R 1 * S I N(0) \\ 170 & X=R 1 *(C O S(F 1-L g+W 1 * d t)-C O S(P I / 2)\end{array}$
$170 \quad \mathrm{X}=\mathrm{R1} 1^{*}(\mathrm{COS}(\mathrm{F} 1-\mathrm{Lg}+\mathrm{W} 1 * \mathrm{dt})-\mathrm{COS}(\mathrm{PL} / 2))+\mathrm{V} 1 * \mathrm{dt}$
180 DRAWXORG+X,YORG+Y
190 NEXT dt
200 NEXT I

## Appendix A1: LOCI-1

10 REM LOCI-1
20 XORG=0:YORG=0
30 INPUT "NO OF KNIVES" N1\%
40 V1=400: W1=2
$50 \mathrm{H} 1=400: \mathrm{R} 1=200: \mathrm{Tw}=250: \mathrm{F} 1=\mathrm{PI}+\mathrm{ASN}((\mathrm{H} 1-\mathrm{Tw}) / \mathrm{R} 1)$
60 MOVEXORG,YORG:DRAWXORG,YORG+Tw:
MOVEXORG,YORG+Tw:DRAWXOR G+1280,YORG+Tw
70 Lb=2*PI/N1\%
80 YORG=YORG + H1
90 XORG=XORG+R1
100 FOR I=1 TO N1\%
$110 \mathrm{Lg}=(\mathrm{I}-1)^{*} \mathrm{Lb}$
120 X=R1*(COS(F1-Lg)-COS(PI/2))
130 Y=R1*SIN(F1-Lg)-SIN(0)
140 MOVE XORG,YORG: DRAW XORG+X,YORG+Y
150 FOR dt=0 TO PI STEP . 03
$160 \quad \mathrm{Y}=\mathrm{R} 1 * \operatorname{SIN}(\mathrm{~F} 1-\mathrm{Lg}+\mathrm{W} 1 * \mathrm{dtt})-\mathrm{R} 1 * \operatorname{SIN}(0)$
$170 \quad \mathrm{X}=\mathrm{R} 1^{*}\left(\mathrm{COS}\left(\mathrm{F} 1-\mathrm{Lg}+\mathrm{W} 1^{*} \mathrm{dt}\right)-\mathrm{COS}(\mathrm{PI} / 2)\right)+\mathrm{V} 1 * \mathrm{dt}$
180 MOVE XORG+X,YORG+R1: DRAW XORG+X,YORG+Y
190 NEXT
200 NEXT

## Appendix A2: LOCI-2

```
10REM LOCI-2
20 xx=150:yy=600: VDU28,0,25,79,0
30 XORG=200: YORG=200
40 INPUT "NO. OF KNIVES " N1
50 INPUT "POSITION OF PROUD KNIFE " kp:IF kp>N1 THEN 50
60 IF kp<1 THEN 50 ELSE kp=kp-1
70 V1=10: W1=150: R=0.2:R1=R:Rp=R+0.05:H=0.2:Tw=0.19
80 Lb=2*PI/N1
90 FOR I=0 TO 2*N1
100 IF I= kp + (I DIV N1)*N1 THEN R1=Rp ELSE R1=R
110 th=2*ACS((H-Tw)/R1):F1=PI+ASN((H-Tw)/R1)
120 Lg=(I-1)*Lb
130 Xs=V1*Lg/W1: Xe=R1*(COS(F1+th)-COSF1)+V1*(Lg+th)/W1
140 IF I=0 THEN step=ABS(Xe-Xs)/16
150 dt=0
160 FOR x=Xs TO Xe STEP step
170 a=-(W1*R1*SINF1-V1)/(W1*R1*COSF1)
180 b=SQR((2*(W1*R1*SINF1-V1))^2
                -4*W1*R1*COSF1*2*(x-V1*Lg/W1))/(2*W1*R1*COSF1)
            A=a+b:B=a-b
200 IF B>0 THEN dt=B
210 IF A>0 THEN dt=A
220 Y=R1*(SIN(F1+W1*dt)-SIN(F1))
230 X=R1*(COS(F1+W1*dt)-COSF1)+V1*(Lg+W1*dt)/W1
240 MOVE XORG+X*xx,YORG:DRAW XORG+X*xx,YORG+Y*yy
2 5 0 ~ N E X T ~
260 NEXT
```


## Appendix A3: LOCI-3

```
    10 REM LOCI-3
    20 MODE 0
    30 m=1: DIM Y(1000),kp(20): VDU28,0,12,79,0
    40 xx=600*2: yy=18000*2
    50 XORG=0: YORG=350
    6 0 ~ I N P U T ~ " N u m b e r ~ o f ~ K n i v e s ~ " ~ N \% ~
    70 REPEAT:
            INPUT "Number of Proud Knives "Nokp%:
    UNTIL Nokp%>0 AND Nokp%<N%+1: Nokp%=Nokp-1
    80 FOR J=1 TO Nokp%:
            INPUT "Position of Proud Knives " kp:
            kp(J)= kp-1:
        NEXT
    90 INPUT "MULT. REVS n1 " n1
100 Lb=2*PL/N%
110 V1=20: W1=190
120 r1=0.2:d=0.0002:R=r1:r2=r1+0.003:H1=0.4T=0.202
130 IF n1=0 THEN r=0 ELSE r=0.0005:R1=R1+r
140 th=2*ACS((H1-T)/R1):F1=PI+ASN((H1-T)/R1)
150 Es=F1+(n1-1)*PI
160 Xs=0
170 Xe=R1*(COS(F1+th)-COSF1)+r*(COS(Es+n1*th)-COSEs)+V1*(Lb+th)/W1
180 step=(Xe-Xs)/16: m=1/step:
190 V1=V1*m:r1=r1*m:d=d*m:R1=R1*m:
200 r2=r2*m:r=r*m:H1=H1*m:T=T*m
210 MOVE XORG,YORG+T/m:DRAW XORG+200,YORG+T/m
220 step=1
230 FOR I=0 TO 4*N%:
                                    IF Nokp%=0 THEN 250
            FOR J=1 TO Nokp%:
                                    R=r1:
                                    IF I=kp(J)+(I DIV N%)*N% THEN R=r2:J=Nokp%:
                NEXT
            th=2*ACS((H1-T)/R1):F1=PI+ASN((H1-T)/R1)
            Lg=I*Lb :E=Es-Lg*n1
            Xs=INT(V1*Lg/W1):
        Xe=INT(R1*(COS(F1+th)-COSF1)
                                    +r*(COS(E+n1*th)-COSE)+V1*(Lg+th)/W1)
    xs=(V1*Lg/W1):
        xe=(R1*(COS(F1+th)-COSF1)
                            +r*(COS(E+n1*th)-COSE)+V1*(Lg+th)/W1)
    FOR x=Xs TO Xe STEP step
    a=-(W1*(R1*SINF1+r*n1*SINE)-V1)/W1^2*(R1*COSF1+r*n1^2*COSE))
    b=SQR((W1*(R1*SINF1+n1*r*SINE)-V1)^2
                                    -2*W1^2*(R1*COSF1+r*n1^2*COSE)*(x-V1*Lg/W1))/
                                    (W1^2*(R1*COSF1+r*n1^2*COSE))
    A=a+b:B=a-b:dt=0
    IF B>0 THEN dt=B
    IF A>0 THEN dt=A
    Y=R1*(SIN(F1+W1*dt)-SIN(F1))+r*SIN(E+n1*W1*dt)
    IF Y < Y(x) THEN Y(x)=Y
    X=R1*(COS(F1+W1*dt)-COSF1)+
                r*(COS(E+n1*W1*dt)-COSE)+V1*(Lg+W1*dt)/W1
        MOVE XORG+x*xx/m,YORG:
        DRAW XORG+x*xz/m,YORG+Y*yy/m
390
        NEXT
400 NEXT
410 CLS :CLG
```

420 FOR X=0 TO 1000
430 MOVE XORG $+\mathrm{X}^{*} \mathrm{x} \times / \mathrm{m}, \mathrm{YORG}$ :
DRAW XORG+X*xz/m,YORG+Y(X)*yy/m
440 NEXT

## Appendix A4: SSA (Surface Simulation Algorithm)

```
4570DEF PROC SSA (Surface Simulation Algorithm)
4 5 7 1 ~ N O S = 0
4580 m=1: ASUM=0:SCALE=0 :VDU28,40,26,79,8
4590 xx=32000/16*3*4/6*2
4600 yy=400000
4610 XORG=0 TTX=0:BLK$=" "
4620 YORG=1000:TY=10
4630 VDU31,TX,0:PRINT"No of knives":
PRINT"Feed speed":
PRINT"Cutter Speed":
PRINT"Vib rate":
PRINT"Proud Knives":
PRINT"Mult. of Revs":
    PRINT"Spindle Runout"
4640 VDU31,15,0:PRINT;nN%:
    VDU31,15,1:PRINT;V*60:
    VDU31,15,2:PRINT;rpm:
    VDU31,15,3:PRINT;rate:
    VDU31,15,4:PRINT;Nokp%:
    VDU31,15,5:PRINT;n:
    VDU31,15,6:PRINT;r/10^-6
4650 TXX=18:TYY=4:IF Nokp%=0 THEN 4670
4660 FOR J=1 TO Nokp%:VDU31,TXX,TYY:PRINT;kp(J)+1:TXX=TXX+2:NEXT
4 6 7 0 \text { smplth=0.125}
4680 CHANGE=0
4 6 9 0 ~ R E P E A T ~
4700 IF FIRST=1 OR SCALE=4 THEN 4710 ELSE 4910
4710 VDU31,TX,TY:PRINT"f0 - change data
4720 PRINT"f9 - to run
4 7 3 0 ~ C H A N G E = ~ G E T ~
4740 IF CHANGE=130 THEN 4750 ELSE }490
4750 REPEAT:VDU31,TX,TY:PRINT"Select function button "
4760 REPEAT:CHANGE=GET:UNTIL CHANGE>130 AND CHANGE<140
4770 ON CHANGE-130 GOTO 4780,4790,4800,4810,4820,4860,4860,4880,4890
4780 VDU31,TX,TY:INPUT "NO. OF KNIVES " nN%:
    IF nN%=0 THEN 4780 ELSE VDU31,15,0:PRINTBLK$:
                                    VDU31,15,0:PRINT;nN%:GOTO 4890
                                    VDU31,TX,TY:PRINTBLK$:
                                    VDU31,TX,TY: INPUT "WOOD FEEDSPEED m/min"V:
            IF V=0 THEN 4790 ELSE
                    VDU31,15,1:PRINTBLK$:V=V/60
                            VDU31,15,1:PRINT; V*60: GOTO }489
    VDU31,TX,TY:PRINTBLK$:
    VDU31,TX,TY:INPUT "CUTTER SPEED rpm " rpm:
        IF rpm=0 THEN 4800 ELSE W=2*PI*rpm/60:
                                    VDU31,15,2:PRINTBLK$:
                                    VDU31,15,2:PRINT ;rpm :
                                    GOTO }489
        VDU31,TX,TY:PRINTBLK$:
            VDU31,TX,TY:INPUT "VIBRATION rate " rate:
            VDU31,15,3 :PRINTBLK$:
            VDU31,15,3:PRINT ;rate:GOTO 4890
4820 VDU31,TX,TY:PRINTBLK$:
            VDU31,TX,TY: INPUT "NUMBER OF PROUD KNIVES "Nokp%:
            VDU31,15,4 :PRINTBLK$:
            VDU31,15,4 :PRINT;Nokp%:
            FOR J=0 TO 20:kp(J)=0:NEXT:REM zero store proud knife
TXX=18:TYY=4:REM start position to display position of proud knife FOR J=1TO Nokp\%: REPEAT:
VDU31,TX,TY:PRINTBLK\$:
VDU31,TX,TY:
INPUT"POSITION OF PROUD KNIFE" kp:
UNTIL kp>0 AND kp<nN\% +1 :
VDU31TXX,TYY:PRINT;kp:kp(J)=kp-1:TXX=TXX+2: NEXT:GOTO 4890
VDU31,TX,TY:PRINTBLK\$: VDU31,TX,TY:INPUT"MULT. of REVS for spindle runout \(n\) " n : VDU31,15,5:PRINTBLK\$: VDU31,15,5:PRINT;n :GOTO 4890
IF n<>0 THEN 4880 ELSE r=0:GOTO 4890
VDU31,TX,TY:PRINT;BLK\$:
VDU31,TX,TY:INPUT"Spindle runout (microns)"r: VDU31,15,6 :PRINTBLK\$: VDU31,15,6 :PRINT;r:r=r*10^-6:GOTO 4890
4890 UNTIL CHANGE=139
4900 GOTO 5030
4910 FIRST=1
4920 VDU31,TX,TY:INPUT "NO. OF KNIVES " nN\%:
IF nN\%=0 THEN 4920 ELSE VDU31,15,0 :PRINT BLK\$ :
VDU31,15,0 :PRINT ;nN\%
4930 VDU31,TX,TY:PRINTBLK\$:
VDU31,TX,TY:INPUT "WOOD FEEDSPEED m/min " V:
IF V=0 THEN 4930 ELSE
VDU31,15,1:PRINT BLK\$:
VDU31,15,1:V=V/60:PRINT;V*60
4940 VDU31,TX,TY:PRINTBLK\$:
VDU31,TX,TY:INPUT "CUTTER SPEED rpm " rpm:
IF \(\mathrm{rpm}=0\) THEN 4940 ELSE \(\mathrm{W}=2^{*} \mathrm{PI}^{*} \mathrm{rpm} / 60\) :
VDU31,15,2:PRINT BLK\$:
VDU31,15,2:PRINT ;rpm
4950 VDU31,TX,TY:PRINTBLK\$:
VDU31,TX,TY:INPUT "VIBRATION rate " rate:
VDU31,15,3 :PRINTBLK\$:VDU31,15,3:PRINT ;rate
4960 VDU31,TX,TY:PRINTBLK\$:
VDU31,TX,TY:INPUT"NUMBER OF PROUD KNIVES "Nokp\%:
VDU31,15,4 :PRINTBLK\$:
VDU31,15,4 :PRINT;Nokp\%:
IF Nokp\% =0 THEN 4980
4970 TXX=18:TYY=4:
FOR J=1TO Nokp\%:
REPEAT:VDU31,TX,TY:PRINTBLK\$:
VDU31,TX,TY:
INPUT"POSITION OF PROUD KNIFE "kp:
UNTIL kp>0 AND kp<nN\% +1 :
VDU31,TXX,TYY:PRINT;kp:kp(J)=kp-1:TXX=TXX+2:
NEXT:
4980 VDU31,TX,TY:PRINTBLK\$:
VDU31,TX,TY:INPUT "MULT. of REVS for spindle runout n " n:
VDU31,15,5 :PRINTBLK\$:
VDU31,15,5:PRINT;n
4990 IF n<>0 THEN 5010 ELSE r=0:GOTO 5030
5010 VDU31,TX,TY:PRINT;BLK\$:
VDU31,TX,TY:
INPUT "INPUT Spindle runout in microns " r :
VDU31,15,6 :PRINTBLK\$:
VDU31,15,6:PRINT; r
```

$5020 \quad r=r^{*} 10^{\wedge}-6$ : REM out of true radus of spindle
5030 UNTIL CHANGE=139
$5040 \mathrm{Lb}=2 * \mathrm{PI} / \mathrm{nN} \%$ : $\mathrm{c}=$ smplth ${ }^{*} \mathrm{~W} /\left(2^{*} \mathrm{PI}{ }^{*} \mathrm{~V}\right)$
$5050 \mathrm{r} 1=0.1: \mathrm{d}=0.0002: \mathrm{R}=\mathrm{r} 1: \mathrm{r} 2=\mathrm{r} 1+.05^{*} \mathrm{~d}: \mathrm{H}=\mathrm{r} 1+0.2^{*} \mathrm{~d} . \mathrm{vib}=0.000003$
5060 th=2*ACS ((R-d)/R):F=PI+ASN((R-d)/R)
$5070 \mathrm{Es}=\mathrm{F}+(\mathrm{n}-1) * \mathrm{PI}:$ REMstart angle for out of balance term
5080 Xs=0:Xe=R*(COS $(\mathrm{F}+\mathrm{th})-\operatorname{COSF})+\mathrm{r}^{*}(\mathrm{COS}($ Es + th $)-\operatorname{COSEs})+\mathrm{V}^{*}(\mathrm{Lb}+$ th $) / \mathrm{W}$
5090 step=smplth $/ 256: \mathrm{m}=1$ step: : REM increment of 1 for each step
$5100 \mathrm{~V}=\mathrm{V}^{*} \mathrm{~m}: \mathrm{r} 1=\mathrm{r} 1^{*} \mathrm{~m}: \mathrm{d}=\mathrm{d}^{*} \mathrm{~m}: \mathrm{R}=\mathrm{R}^{*} \mathrm{~m}: \mathrm{r} 2=\mathrm{r} 2^{*} \mathrm{~m}: \mathrm{r}=\mathrm{r}^{*} \mathrm{~m}$ :
$\mathrm{H}=\mathrm{H}^{*} \mathrm{~m}$ :SMPLTH=smplth ${ }^{*}$ m:vib=vib*${ }^{*} \mathrm{~m}$
5110 step $=1: I=-1: Y \mathrm{Yi}=-10000: Y \mathrm{Y}=100000:$ REM Y values for determine peaks later
5120 REPEAT
5130 I=I+1 :IF Nokp\%=0 THEN 5180
5140 FOR J= 1 TO Nokp\%
5150 R=r1
$5160 \quad \mathrm{IF} \mathrm{I}=\mathrm{kp}(\mathrm{J})+(\mathrm{I}$ DIV nN\%)*nN\% THEN R=r2:J=Nokp\%:REM detect Proud knife
5170 NEXT
5180 th=2*ACS((R-d)/R):F=PI+ASN((R-d)/R)
5190 L=I*Lb :E=Es-L*n
$5200 \mathrm{Xs}=\mathrm{INT}\left(\mathrm{V}^{*} \mathrm{~L} / \mathrm{W}\right): \mathrm{Xe}=\mathrm{INT}\left(\mathrm{R}^{*}(\operatorname{COS}(\mathrm{~F}+\mathrm{th})-\operatorname{COSF})+\mathrm{r}^{*}(\mathrm{COS}(\mathrm{E}+\mathrm{th})-\mathrm{COSE})+\mathrm{V}^{*}(\mathrm{~L}+\mathrm{th}) / \mathrm{W}\right)$
$5210 \quad \mathrm{Ys}=\mathrm{H}+\mathrm{R}^{*}$ SINF $+\mathrm{r}^{*}$ SINE
5220 MOVE XORG,YORG:DRAW XORG+Xs/m,YORG+Ys/m
$\left.5240 \mathrm{dt}=0: \mathrm{xMAX}=\mathrm{V} * \mathrm{~F} / \mathrm{W}+\left(1 / \mathrm{W}^{\wedge} \mathbf{2}^{*} \mathrm{COSF}\right)^{*}(\mathrm{~W} * \mathrm{SINF}-\mathrm{V} / \mathrm{R})^{\wedge} 2-2^{*}(\mathrm{COSF}-1)\right)^{*} \mathrm{R} / 2$
5250 FOR $x=X s$ TO Xe STEP step
$5260 \quad \mathrm{a}=-\left(\mathrm{W}^{*}\left(\mathrm{R}^{*} \mathrm{SINF}+\mathrm{r}^{*} \mathrm{n}^{*} \mathrm{SINE}\right)-\mathrm{V}\right) /\left(\mathrm{W}^{\wedge} 2^{*}\left(\mathrm{R}^{*} \mathrm{COSF}+\mathrm{r}^{*} \mathrm{n}^{\wedge} \mathbf{2}^{*} \mathrm{COSE}\right)\right)$
$\left.5270 \quad \mathrm{~b}=\operatorname{SQR}\left(\mathrm{W}^{*}\left(\mathrm{R}^{*} \operatorname{SINF}+\mathrm{n}^{*} \mathrm{r}^{*} \operatorname{SINE}\right)-\mathrm{V}\right)^{\wedge} 2-2^{*} \mathrm{~W}^{\wedge} 2^{*}\left(\mathrm{R}^{*} \operatorname{COSF}+\mathrm{r}^{*} \mathrm{COSE}\right)^{*}(\mathrm{x}-\mathrm{V} * \mathrm{~L} / \mathrm{W})\right)$ /(W^2*( $\left.\mathrm{R}^{*} \mathrm{COSF}+\mathrm{r}^{*} \mathrm{n}^{\wedge} \mathbf{2}^{*} \mathrm{COSE}\right)$ )
$5280 \quad \mathrm{~A}=\mathrm{a}+\mathrm{b}: \mathrm{B}=\mathrm{a}-\mathrm{b}$
5290 IF $\mathrm{B}>0$ AND A>B THEN dt=BELSE IFA>0 THEN dt=A ELSE dt=B
$5300 \quad \mathrm{Y}=\mathrm{H}+\mathrm{R}^{*} \operatorname{SIN}\left(\mathrm{~F}+\mathrm{W}^{*} \mathrm{dt}\right)+\mathrm{r}^{*} \operatorname{SIN}\left(\mathrm{E}+\mathrm{n}^{*} \mathrm{~W}^{*} \mathrm{dt}\right)+$ vib*SIN(F+rate*$\left.{ }^{*}{ }^{*} \mathrm{dt}\right)$
$5310 \quad \mathrm{Y}=\mathrm{Y}-1 * \mathrm{~d}:$ REM invert value
$5320 \quad \mathrm{X}=\mathrm{R}^{*}\left(\operatorname{COS}\left(\mathrm{~F}+\mathrm{W}^{*} \mathrm{dt}\right)-\operatorname{COSF}\right)+\mathrm{r}^{*}\left(\operatorname{COS}\left(\mathrm{E}+\mathrm{n}^{*} \mathrm{~W}^{*} \mathrm{dt}\right)-\operatorname{COSE}\right)+\mathrm{V}^{*}\left(\mathrm{~L}+\mathrm{W}^{*} \mathrm{dt}\right) / \mathrm{W}$
5330 IF x<extra OR x>255+extra GOTO5390
$5340 \quad$ IF $\mathrm{Y}<\mathrm{Y}(\mathrm{x})$ THEN $\mathrm{Y}(\mathrm{x})=\mathrm{Y}:$ REM store lowest current value of over lap cusps
5350 IF $\mathrm{Y}(\mathrm{x})>$ Yhi THEN Yhi $=\mathrm{Y}(\mathrm{x}):$ Xhi $=\mathrm{x}$-extra
5360 IF $\mathrm{Y}(\mathrm{x})+1^{*} \mathrm{~d}<\mathrm{Ylo} \mathrm{THEN} \mathrm{Y} \mathrm{l}_{0}=\mathrm{Y}(\mathrm{x})+1^{*} \mathrm{~d}: X 10=\mathrm{x}$-extra
$5370 \quad \mathrm{a}=\mathrm{x}-\mathrm{extra}: \mathrm{XR}(\mathrm{a})=\mathrm{Y}(\mathrm{x}): \mathrm{XI}(\mathrm{a})=0$ :
5380 MOVE XORG $+\left(x^{*} x\right.$ x/m)-(extra*x $\left./ \mathrm{m}\right)$,YORG:

5390 REM PRINTx;" ",X;" ",Y;" ",I
5400 NEXT
5420 nc=(I-1)/nN\%
5430 UNTIL nc>c+1
5440 IF A\$="" THEN A\$="SIMULATION"
5450 VDU31,TX,TY+6:PRINT"h1= ";m*W*smplth/(2*PI*V)
5460 VDU31,TX,TY+7:PRINT"hp= "; $\mathrm{m}^{*} \mathrm{~W}^{*}$ smplth ${ }^{*} \mathrm{nN} \% /\left(2 * \mathrm{PI}{ }^{*} \mathrm{~V}\right)$
$5470 \mathrm{~h} 1=\mathrm{m}^{*} \mathrm{~W}^{*}$ smplth/( $\left.2^{*} \mathrm{PI}{ }^{*} \mathrm{~V}\right): \mathrm{h} 2=\mathrm{m}^{*} \mathrm{~W}^{*} \mathrm{smplth} /\left(\mathrm{PI}^{*} \mathrm{~V}\right): \mathrm{hp}=\mathrm{m}^{*} \mathrm{~W}^{*}$ smplth* $\mathrm{nN} \%\left(2^{*} \mathrm{PI}^{*} \mathrm{~V}\right)$
$5480 \mathrm{hs}=\mathrm{h} 1$
$5490 \mathrm{hv}=2 * \mathrm{hp}$
$5500 \mathrm{~V}=\mathrm{V} / \mathrm{m}$ :r=r/m:SCALE=4
5510ENDPROC

## Appendix A5 Data Capture Software

## A5.0 Computer Initilisation

70DEF PROCinitial
80 YY=400000:m=1:xx=512000
90 extra=20:TX=0:TY=8:BLK\$=" ":ADD=\&23000
100 VDU 28,40,20,79,17
110 FLAG=0:WHICH=0:*EX225,129
120 DIMC (790), S (790), Y(256+extra),kp(20), XRR(1024), $\mathrm{Hx}(255), \mathrm{Hy}(255), f f t(128)$
130 DIM coder \&FF
140 DIM screendump 2000
$150 \mathrm{Z} \%=\mathrm{code} \%+820$
160 black=\&00:mode=0:print-1:colAcc1=1:colAcc2=2:
colAcc3=3:mask=4: row=5: across=6:partByte=7:pinIdent=8:downCol=9 pointer=10:SP=13
165 1vhi=\&207:iv10=\&206:pcr=\&FE6C:1fr=\&FE6D:1er=\&FE6E:ddrb=\&FE62: orb=\&FE60
170 SCL=6:XORG=50:LTH=4:1nv=0
$180 \mathrm{Nq}=1024 / \mathrm{LTH}: \mathrm{J} \%=\mathrm{LN}(\mathrm{N} \%$ ) /LN2
190
200 DIM XR(Nq+extra), XI (Nq+extra)
210REM Set Function Keys
220 *FX 225,130
230REM State Addresses
240 A\% $=0: B \%=0: V D U 21$
250 PROCassemble
260 PROCdumper
270 VDU 6
280 BLANK\$="
290 PRINT"LOADING SINE AND COSINE TABLES":PROClookup:CLS
$300 \mathrm{nN} \%=0: V=0: r \mathrm{pm}=0:$ rate $=0:$ Nokp $\%=0: \mathrm{n}=0: r=0$
310ENDPROC

## A5.1 Laser Instrument

```
470DEFPROClaser
4 8 0 ~ R E M ~ S a t u r a t i o n ~ V o l t a g e
490 V=&20
500 CLG
510 C%=0:2%=0:Cn=0:dt%=0
520 REM Repeat 1
530 C% = C% +2000
540 XO=&3F:Xi=&3F
550 REPEAT
560 CLS:PRINT"LASER MEASUREMENT IN PROGRESS"
570 Cn=Cn+1:dt%=0
580 IF Cn=1 THEN }62
590 IF XO=Xi THEN Xi=Xi+1
600
610
620
630
C%=C%+dt%
CALI start
640 TIME=0
650 FOR D= O TO C% :NEXT
6 6 0
670
680REM
6 9 0
700REM
710 XO=X1:Xi=?storelo
720 UNTIL ABS (V-XI)<=1
730 Cn=0:VDU5:MOVE 0,1000
740 PRINT"C%=";C%,
"INTEGRATION TIME=";T/100" ;"SEC.",":
"Z%="; 2%,"dt%=";dt%,
"Xi=";Xi,"XO=";XO;" V=";V:VDU4
750 PROCPLOT (500,1)
7 6 0 ~ E N D P R O C
```


## A5.2 Talyrond 200

1120DEF PROCtallyrond
1130 CLG:CLS:*FX 15,0
1140 PRINT"Press any key after starting traverse"
1150 delay=25000:x=GET
1160 ?latchlo=delay MOD 256
1170 ?latchhi=delay DIV 256
1180 CALL start2
1190 ? counthi=delay DIV 256:TIME=0
1200 CLS:PRINT"TALYROND MEASUREMENT IN PROGRESS":PRINT
1210 IF FLAG=1 THEN 1230
1220 PRINT" AND LOADING SINE \& COSINE TABLE":
PROClookup:FLAG=1:VDU31,0,2:PRINT BLANK\$
1230 REPEAT:UNTIL ?Xstore=0
1240 XORG $=50$ : YORG $=500$
1250 CLS:MOVE XORG,YORG
1260 FOR I=O TO 1023
1270 DRAW XORG+I,YORG+?(\&1300+I)*SCL
1280 NEXT
1290ENDPROC

## A5.3 Interrupt Service Routine

| 2540DEF PROCassemblel |  |  |  |
| :---: | :---: | :---: | :---: |
| 2550 DIM 2\% 400 |  |  |  |
| 2560 FOR Op | $t \%=0$ | O 2 STEP 2 |  |
| 2570 P\% $=$ \%\% |  |  |  |
| 2580 [ |  |  |  |
| 2590 OPT opt\% |  |  |  |
| 2600.init | SEI |  | ; DIS INT |
| 2610 | LDA | ivhi | ; check |
| 2620.if | CMP | \# \& E6 | ; chech if already initiated |
| 2630 | BNE | els | ; yes. THEN branch to els |
| 2640 | STA | oldv+1 | ; save old vec |
| 2650 | LDA | ivlo | ; save old vec |
| 2660 | STA | oldv | ; save old vec |
| 2670 | LDA | *int MOD256 | ;new vec lobyte |
| 2680 | STA | ivlo | instate new NEWvec 10 |
| 2690 | LDA | *int DIV256 | ; new vec hibyte |
| 2700 | STA | ivhi | ;instate new vec hi |
| 2710.els | CLI |  | ; clear int disable |
| 2720 | RTS |  | ; return |
| 2730 |  |  |  |
| 2740.int | IDA | \&FC | ; save reg's |
| 2750 | PHA |  | ; A |
| 2760 | PHX |  | ; X |
| 2770 | PHY |  | ; $\mathbf{Y}$ |
| 2780 | IDA | ifr | ; did CB1 interrupt? |
| 2790 | AND | * \& 10 | ; check CB1 |
| 2800.1fCB1 | BEQ | exit | ; if CB1 load array data ELSE exit |
| 2810.then | LDA | *\&FF | ;then |
| 2820 | STA | orb | ; clear int by writing to PORT B |
| 2830.page | LDA | * 800 | ; first page lobyte |
| 2840 | STA | \& 70 | iinstall lobyte |
| 2850 | LDA | * 813 | ; first page hibyte |
| 2860 | STA | *\&71 | ;install hibyte |
| 2870 | LDA | \# \& 3F | ; min data= $\& 0$, max data= $\& 3 F$ |
| 2880 | STA | storelo | ;store for min data |
| 2890 | STZ | storehi |  |
| 2900 | LDX | \# 804 | ; page count |
| 2910 | LDY | * 800 | ;page line pointer |
| 2920.rpt1 | LDA | * \& 00 | ; REPEAT |
| 2930 | STA | orb | ; clk array RAM |
| 2940 | LDA | * 840 | ; clk array RAM |
| 2950 | STA | orb | ; clk array RCM |
| 2960 | LDA | orb | ; load data |
| 2970 | AND | * \& 3F | ; \& 3F because 6 bits only |
| 2980 | STA | (\&70), Y | ; store data |
| 2990 | CMP | storelo | ; compare data with current min |
| $3000.1 f 1$ | BPL | elsel | ;if larger ignore |
| 3010 | STA | storelo | ;if smaller save in storelo |
| 3020.else1 | CMP | storehi | ; compare data with current max |
| 3030.if2 | BMI | else2 | ;if smaller ignore |
| 3040 | STA | storehi | iff larger save in storehi |
| $3050 . e l s e 2$ | INY |  | ; point to nextline on current page |
| 3060.unt1 | BNE | rptl | ; UNTIL Y=0 |
| 3070 | INC | \& 71 | ; point to next page |
| 3080 | DEX |  | ; dec page count |
| 3090 | BNE | rpt1 | ;UNTIL $\mathrm{X}=0$ |
| 3100 | LDA | \&1300 | ;fill-in "missing" data |
| 3110 | STA | \&16FF | ; at \&16FF |
| 3120 | INC | flag | ;signal end of data transfer |
| 3130 | JMP | exit2 |  |
| 3140.01 dv | NOP |  | ; reserve space for old vec add |
| 3150 | NOP |  | ;reserve space for old vec add |
| 3180.exit | LDA | ifr | ; get system VIA interrupt status |
| 3190 | AND | * \& 40 |  |
| 3200 | CMP | * \& 40 | ;if timer 1 interrupt then |
| 3210 | BNE | exit2 |  |
| 3220 | LDA | countlo | ; clear interrupt |
| 3230 | LDY | Ystore |  |
| 3240 | LDA | *\&20 |  |


| 3250 | STA | orb | iline 6 hi |
| :---: | :---: | :---: | :---: |
| 3260 | LDA | orb |  |
| 3270 | AND | * 81 F | ; read data |
| 3280 | STA | temploc | ; store data |
| 3290 | LDA | * 810 | ; get ready for BIT test |
| 3300 | STZ | orb | iline 6 lo |
| 3310 | BIT | orb |  |
| $3320.1 f 3$ | BNE | else3 |  |
| 3330.then3 | SEC |  |  |
| 3340 | JMP | endif3 |  |
| $3350 . e l s e 3$ | CLC |  |  |
| 3360. endif3 | ROL | temploc |  |
| 3370 | IDA | temploc |  |
| 3380 | STA | (addlo), Y |  |
| 3390 | INC | Ystore |  |
| 3400 | BNE | exit2 |  |
| 3410 | INC | addh1 |  |
| 3420 | DEC | Xstore |  |
| 3430 | BNE | exit2 |  |
| 3440 | SEI |  |  |
| 3450 | LDA | ier |  |
| 3460 | AND | *\&40 |  |
| 3470 | STA | ier |  |
| 3480 | CLI |  |  |
| 3490 exit2 | PLY |  |  |
| 3500 | PLX |  |  |
| 3510 | PLA |  |  |
| 3520 | STA | \&FC |  |
| 3530 | JMP | (oldv) | ; continue interrupt chain |
| 3540.start | SEI |  |  |
| 3550 | LDA | * 890 | ; enable int. |
| 3560 | STA | 1er | ; enable int |
| 3570 | LDA | pcr | ; load pcr |
| 3580 | ORA | * \&FO | ; conserve port A CA1/CA2 |
| 3590 | STA | pcr | ; configure port B CBI +edge CB2 hi |
| 3600 | LDA | orb | ; dummy load to clear interrupt if any occured |
| 3610 | LDA | \#\&FF | ;all outputs hi |
| 3620 | STA | orb | ;all outputs hi |
| 3630 | LDA | \#\&C0 | ; configure PORT B direction as |
| 3640 | STA | ddrb | ; 6 inputs, 2 outputs |
| 3650 | CLI |  |  |
| 3660 | STZ | flag | ;flag to signal data transfer end |
| 3670 | LDA | pcr | ; SEND start pulse |
| 3680 | AND | \# \& DF | ;by conserving PORT A directives |
| 3690 | STA | pcr | ; and strobing CB2 |
| 3700 | ORA | \# \& 20 |  |
| 3710 | STA | pcr | ; DONE |
| 3720 | RTS |  | ; Return |
| 3730 |  |  |  |
| $3740 . s t a r t 2$ | LDA | * \& 20 |  |
| 3750 | STA | ddrb | ;configure output port |
| 3770 | STZ | addlo | ;start address |
| 3780 | LDA | \# 813 |  |
| 3790 | STA | addhi |  |
| 3800 | STZ | Ystore |  |
| 3810 | LDA | * \& 4 |  |
| 3820 | STA | Xstore |  |
| 3830 | LDA | \#\&40 | ; set aux. cont reg |
| 3840 | ORA | acr |  |
| 3850 | AND | \#\&7E |  |
| 3860 | STA | acr |  |
| 3870 | LDA | \# 820 \} |  |
| 3880 | STA | ddrb |  |
| 3890 | SEI |  |  |
| 3900 | LDA | \# \& C0 |  |
| 3910 | ORA | ier | ; set int. enable reg |
| 3920 | STA | ier |  |
| 3930 | CLI |  |  |
| 3940 | RTS |  |  |

3170 J
3970 NEXTopt
3980ENDPROC

## Appendix A6 FFT Algorithm :BBC BASIC

```
REM>FFTTHE
490 DEF FNrbitr=USR sss
520 DEFPROCassemble
530 FOR pass=0 TO 3 STEP 3
540 p%=2%
550 [OPT pass
560 .sss
660 MOV RO,R1
670 IDMFD (SP)!,{R1,R9,pc}
690 NEXT pass
7 0 0 ~ E N D P R O C
830 FOR IS%= 1 TO IR%
850 FOR I%=1 TO L%
860 REM K%=K%+1 N/A SEE LINE }100
1080 FOR Kg
NEXT K%
1160 IF DELTA<>1 THEN 1170 ELSE ENDPROC
1170 FOR K%=0 TO N%-1
482
511
570
580
590
600
610
620
630
640
650 ;
680 J
751
760
770
780
790
800
810
840
870
880
890
900
910
920
930
940
950
960
970
980

\section*{AppendixA7 FFT Algorithm:AssemblyLanguage}
\(5 \mathrm{CN}=0\)
10 IF PAGE<>\&2800 THEN PAGE=\&2800:CHAIN"TEST3"
20 REM A.FFT256WOOD ASSEMBLY LANGUAGE
30 MODE128
40 LTH=4 :complo=PAGE-1:comphi=PAGE-2:countlo=PAGE-3:counthi=PAGE-4
\(41 \mathrm{nnn}=\) PAGE-5: \(\mathrm{cn}=\) PAGE-6: \(\mathrm{aa}=\mathrm{PAGE}-7: \mathrm{nn} 1=\) PAGE-8:is=PAGE-9:
count4=PAGE-10:REM*
45 ?countlo=0:?counthi=0 :? \(\mathrm{cn}=0\)
46 INPUT "IScount" nn: ?is=nn-1:INPUT "Icount" nn: ?nnn=nn-1:
INPUT "A\%" nn:?aa=nn MOD 256:?nn1=nn DIV 256
50 SCL=6:
60 XORG=50:YORG=800
\(70 \mathrm{ADD}=\& 1300\)
80 reall \(0=\& 1700\)
90 realhi=\&1801
100 imaglo=\&1902
110 imaghi=\&1A03
120 sinlo=\&1B04
130 sinhi=\&1E06
140 coslo=\&2108
150 coshi=\&240A
\(160 \mathrm{XR} 1 \mathrm{l} 0=\& 1800\)
170 XR1hi=\&1901
180 XI \(110=\& 1 \mathrm{~A} 02\)
190 XI1hi=\&1B03
192 sinl =\&74:?sinl=sinlo MOD 256:?(sinl+1)=sinlo DIV 256
\(194 \sinh =\& 76: ? \sinh =\operatorname{sinhi}\) MOD 256:?(sinh+1)=sinhi DIV 256
\(196 \mathrm{cosl}=\& 78\) :?cosl=coslo MOD 256:?(cosl+1)=coslo DIV 256
198 cosh =\&7A:?cosh=coshi MOD 256:?(cosh+1)=coshi DIV 256
200 storelo \(=\& 72\)
210 storehi \(=\& 73\)
\(220 \mathrm{mpdlo}=\& 270 \mathrm{C}\)
\(230 \mathrm{mpdhi}=\& 270 \mathrm{D}\)
\(240 \mathrm{mprlo}=\& 270 \mathrm{E}\)
\(250 \mathrm{mprhi}=\& 270 \mathrm{~F}\)
260 prod \(1=\& 2710\)
270 prod \(2=\& 2711\)
280 prod3 = \& 2712
290 prod \(4=\& 2713\)
300 divlo \(=\& 7 \mathrm{C}\)
310 divhi \(=\& 7 \mathrm{D}\)
320 pdivlo \(=\& 80\)
330 divqlo \(=\& 7 \mathrm{E}\)
340 divqhi \(=\& 7 \mathrm{~F}\)
350 pdivhi \(=\& 81\)
360 l=\&82
370 Icount=\&83
\(380 \mathrm{k}=\& 84\)
\(390 \mathrm{kpl}=\& 85\)
\(400 \mathrm{aA}=\& 86\)
410 IScount=\&87
420 flag \(=\& 88\)
430 addlo \(=\& 89\)
440 addhi=\&8A
450 adrlo=\&8B
460 adrhi=\&8C
470 IR1=\&8D

480 loo= 88 E
490 ivhi \(=\) \& 207
500 ivlo \(=\$ 206\)
510 pcr \(=\&\) FE6C
520 ifr \(=\&\) FE6D
530 ier \(=\& F E 6 E\)
540 ddrb \(=\) \&FE62
550 orb \(=\&\) FE 60
555 IF CN>0 THEN 590
560 PROClookup:CN=1
570 FOR 1\%=0 TO 255 : A=A+(63-?(ADD+LTH*I\%)):NEXT
580 AVE=A/256:MOVE XORG,YORG
590 FOR I\%=0 TO 255
640 ?(reallo \(+1 \%)=4 * \operatorname{SIN}(8 * \mathrm{PI} * \mathrm{I} \% / 256)+4: ?(\) realhi \(+1 \%)=0\)
650 ?(imaglo+1\%)=0:?(imaghi \(+1 \%\) ) \(=0\)
740 DRAW XORG+LTH*I\%,YORG+?(reallo+I\%)*5
760 NEXT
765 IF CN=2 THEN 4600
770 DIM Z\% 1000
780 FOR pass\%=0 TO 2 STEP 2
790 P\%=Z\%
800 [
810 OPT pass\%
\(820 \backslash\)
830 .fft LDA \#128

840
850
860
880
890
910
920
930.

940
950
960
970
980
990
1000
1002
1010
1020
1030 BNE loop1 \K\%/(2^IR1)
1110 .endifO STA loo
1120
1130
1140
1150
1160
1170 STA XR1lo
1180 LDA realhi, \(X\)
1190 STA XR1hi \(\quad\) XRR1=XR(KPL\%)
\(1200 \backslash\)
1210 LDA imaglo,X
1220 STA XIllo
1230 LDA imaghi,X
1240 STA XI1hi \(\quad\) XXI1=XI(KPL\%)
1250 JMP enif1
1260 .else1 LDX kpl
\begin{tabular}{|c|c|c|}
\hline 1270 & LDA & imaglo, X \\
\hline 1280 & STA & mprlo \\
\hline 1290 & LDA & imaghi, \(X\) \\
\hline 1300 & STA & mprhi \\
\hline 1310 & LDY & aA \\
\hline 1320 & LDA & (sinl), Y \\
\hline 1330 & STA & mpdlo \\
\hline 1340 & LDA & (sinh), Y \\
\hline 1350 & STA & mpdhi \\
\hline 1360 & JSR & mult16 \S(A\%)*XI(KPL\%) \\
\hline \multicolumn{3}{|l|}{\(1370 \backslash\)} \\
\hline 1375 & JSR & shift4 \\
\hline 1380 & LDA & prod2 \\
\hline 1390 & STA & complo \\
\hline 1400 & LDA & prod3 \\
\hline 1410 & STA & comphi \\
\hline 1420 & JSR & twocmp \2's comp for subtraction \\
\hline \multicolumn{3}{|l|}{\(1430 \backslash\)} \\
\hline 1440 & LDA & complo \\
\hline 1450 & STA & adrlo \\
\hline 1460 & LDA & comphi \\
\hline 1470 & STA & adrhi \store for "addition" \\
\hline \multicolumn{3}{|l|}{\(1480 \backslash\)} \\
\hline 1490 & LDA & reallo,X \\
\hline 1500 & STA & mprlo \\
\hline 1510 & LDA & realhi, X \\
\hline 1520 & STA & mprhi \\
\hline 1530 & LDA & (cosl),Y \\
\hline 1540 & STA & mpdlo \\
\hline 1550 & LDA & (cosh), Y \\
\hline 1560 & STA & mpdhi \\
\hline 1570 & JSR & mult16 \C(A\%)*XR(KPL\%) \\
\hline \multicolumn{3}{|l|}{\(1580 \backslash\)} \\
\hline 1585 & JSR & shift 4 \\
\hline 1590 & LDA & prod2 \\
\hline 1600 & STA & addlo \\
\hline 1610 & LDA & prod3 \\
\hline 1620 & STA & addhi \store for "addition" \\
\hline 1630 & JSR & add16 \do "addition" \\
\hline \multicolumn{3}{|l|}{\(1640 \backslash\)} \\
\hline 1650 & LDA & addlo \\
\hline 1660 & STA & XR1lo \\
\hline 1670 & LDA & addhi \\
\hline 1680 & STA & XR1hi \(\quad\) XR1=C(A\%)*XR(KPL)-S(A\%)*XI(KPL) \\
\hline \multicolumn{3}{|l|}{\(1690 \backslash\)} \\
\hline 1700 & LDA & imaglo, X \\
\hline 1710 & STA & mprlo \\
\hline 1720 & LDA & imaghi, X \\
\hline 1730 & STA & mprhi \\
\hline 1740 & LDA & (cosl),Y \\
\hline 1750 & STA & mpdlo \\
\hline 1760 & LDA & (cosh), Y \\
\hline 1770 & STA & mpdhi \\
\hline 1780 & JSR & mult16 \C(A\%)*XI(KPL) \\
\hline \multicolumn{3}{|l|}{\(1790 \backslash\)} \\
\hline 1795 & JSR & shift4 \\
\hline 1800 & LDA & prod2 \\
\hline 1810 & STA & addlo \\
\hline 1820 & LDA & prod3 \\
\hline 1830 & STA & addhi \store for addition \\
\hline
\end{tabular}

1850
1860
.rrr

LDA reallo,X
STA mprlo
LDA realhi, \(X\)
STA mprhi
LDA (sinl),Y
STA mpdlo
LDA (sinh),Y
STA mpdhi
JSR mult16 \S(A\%)*XR(KPL)
JSR shift4
LDA prod2
STA adrlo
LDA prod3
STA adrhi \store for addition
JSR add16 \do addition
LDA addlo
STA XIIlo
LDA addhi
STA XI1hi \(\quad \backslash \mathrm{XI} 1=\mathrm{C}(\mathrm{A} \%)^{*} \mathrm{XI}(\mathrm{KPL})+\mathrm{S}(\mathrm{A} \%) * \mathrm{XR}(\mathrm{KPL})\)
LDA cn
CMP nn1
BNE rrr
LDA aA
CMP aa
BNE rrr
LDA Icount
CMP nnn
BNE rrr
LDA IScount
CMP is
BNE TrT
RTS

INC aA
BNE enif1
INC sinl+1
INC \(\sinh +1\)
INC cosl+1
INC cosh+1
INC en
LDA en
CMP nn1
BNE eee
LDA aA
CMP aa
BNE eee
LDA Icount
CMP nnn
BNE eee
LDA IScount
CMP is
BNE eee
RTS
LDY k
LDA XR1lo
STA complo
LDA XR1hi
\begin{tabular}{|c|c|c|}
\hline 2110 & STA & comphi \\
\hline 2120 & JSR & twocmp \two's comp XR1 for subtraction \\
\hline \multicolumn{3}{|l|}{\(2130 \backslash\)} \\
\hline 2140 & LDA & complo \\
\hline 2150 & STA & adrlo \\
\hline 2160 & LDA & comphi \\
\hline 2170 & STA & adrhi \store XR1 for subtraction \\
\hline \multicolumn{3}{|l|}{\(2180 \backslash\)} \\
\hline 2190 & LDA & reallo, Y \\
\hline 2200 & STA & addlo \\
\hline 2210 & LDA & realhi,Y \\
\hline 2220 & STA & addhi \store XR(K\%) for subtraction \\
\hline \multicolumn{3}{|l|}{\(2230 \backslash\)} \\
\hline 2240 & JSR & add16 \do subtraction \\
\hline 2250 & LDA & addlo \\
\hline 2260 & STA & reallo, X \\
\hline 2270 & LDA & addhi \\
\hline 2280 & STA & realhi, X \storeresultXR(KPL) \(=\mathrm{XR}(\mathrm{K} \mathrm{\%})-\mathrm{XR} 1\) \\
\hline \multicolumn{3}{|l|}{\(2290 \\) \} \\
\hline 2300 & LDA & XIIlo \\
\hline 2310 & STA & complo \\
\hline 2320 & LDA & XIIhi \\
\hline 2330 & STA & comphi \\
\hline 2340 & JSR & twocmp \2's comp XI1 for subtraction \\
\hline 2350 & LDA & complo \\
\hline 2360 & STA & adrlo \\
\hline 2370 & LDA & comphi \\
\hline 2380 & STA & adrhi - \(\\) store XI1 for subtraction \\
\hline \multicolumn{3}{|l|}{2390 \} \\
\hline 2400 & LDA & imaglo, Y \\
\hline 2410 & STA & addlo \\
\hline 2420 & LDA & imaghi,Y \\
\hline 2430 & STA & addhi \store \(\mathrm{XI}(\mathrm{K} \mathrm{\%})\) for subtraction \\
\hline 2440 & JSR & add16 \ do subtraction \\
\hline \multicolumn{3}{|l|}{\(2450 \backslash\)} \\
\hline 2460 & LDA & addlo \\
\hline 2470 & STA & imaglo, X \\
\hline 2480 & LDA & addhi \\
\hline 2490 & STA & imaghi, X \store result \(\mathrm{XI}(\mathrm{KPL})=\mathrm{XI}(\mathrm{K} \mathrm{\%}) \cdot \mathrm{XI} 1\) \\
\hline \multicolumn{3}{|l|}{\(2500 \backslash\) ( \({ }^{\text {a }}\)} \\
\hline 2510 & LDA & reallo, Y \\
\hline 2520 & STA & addlo \\
\hline 2530 & LDA & realhi, Y \\
\hline 2540 & STA & addhi \store XR(K\%) for addition \\
\hline \multicolumn{3}{|l|}{\(2550 \backslash\)} \\
\hline 2560 & LDA & XR1lo \\
\hline 2570 & STA & adrlo \\
\hline 2580 & LDA & XR1hi \\
\hline 2590 & STA & adrhi \store XR1 for addition \\
\hline 2600 & JSR & add16 \do addition \\
\hline \multicolumn{3}{|l|}{\(2610 \backslash\)} \\
\hline 2620 & LDA & addlo \\
\hline 2630 & STA & reallo, Y \\
\hline 2640 & LDA & addhi \\
\hline 2650 & STA & realhi, Y \store result \(\mathrm{XR}(\mathrm{K} \%)=\mathrm{XR}(\mathrm{K} \mathrm{\%} \%)+\mathrm{XR1}\) \\
\hline \multicolumn{3}{|l|}{\(2660 \backslash\)} \\
\hline 2670 & LDA & imaglo, Y \\
\hline 2680 & STA & addlo \\
\hline 2690 & LDA & imaghi,Y \\
\hline 2700 & STA & addhi \store \(\mathrm{XI}(\mathrm{K} \mathrm{\%})\) for addition \\
\hline
\end{tabular}
\(2710 \backslash\)
2720
2730
2740
2750
2760
2770
2780
2790
2800
2801
2802
2803
2804
2805
2806
2807
2808
2809
2810
\(2811 \backslash\)
2820 .bbb INC k \(\quad\) K \(\%=K \%+1\)
2821
\(2830 \backslash\)
2840
2850
2860
2870
\(2880 \backslash\)
2890 LDA k
2900
2910
2920
2930 \}
2950
\(2960 \backslash\)
2970
2980
2990
\(3000 \backslash\)
3010
3020
3030
3040
3050
3060 .here
3065 .herel
3070 .rept4
3080
3100
3110
3130
3140
3150
3160
3170
3180
\(3190 \backslash\)
3200
3210
LDA XI1lo
STA adrlo
LDA XIlhi
STA adrhi \store XIl for addition
JSR add16 \do addition
LDA addlo
STA imaglo, \(Y\)
LDA addhi
JMP bbb \LDA cn
CMP nn1
BNE bbb
LDA aA
CMP aa
BNE bbb
LDA countlo
CMP nnn
BNE bbb
RTS

INC Icount
LDA Icount
CMP 1
BNE here1 \FOR I\%=1TO L\% NEXT

CLC
ADC 1
STA \(\mathbf{k} \quad \backslash \mathrm{K} \%=\mathrm{K} \%+\mathrm{L} \%\)
BCC here \UNTIL K\%>=N\%
STZ \(k \quad\) KK\%=0
DEC IR1 \IR1\%=IR1\%-1
LSR \(1 \quad \backslash L \%=L \% / 2\)
INC IScount
LDA IScount
CMP \#8
JMP rept4
JMP rept1
JMP rept3
LDY \(k\)
STY 100
JSR rbitr \PROCRBITR
LDX 100
CPX k
BMI else2 \IF K1\%>K\% then2 else2
LDA reallo, \(Y\)
STA XR1lo
LDA realhi, \(Y\)
STA XR1hi \(\quad\) XR1=XR(K\%)
LDA imaglo,Y
STA XIIlo

STA imaghi, Y \store result \(\mathrm{XI}(\mathrm{K} \%)=\mathrm{XI}(\mathrm{K} \%)+\mathrm{XII}\)

BNE here \(\backslash F O R\) IS\%=1 TO IR\% NEXT
3510 EOR \#\&FF
3520 STA comphi
3530 LDA complo
3640 LDX \#8

LDA imaghi, \(Y\)

LDA reallo, \(\mathbf{X}\)
STA reallo, \(\mathbf{Y}\)
LDA realhi, X

LDA imaglo, \(\mathbf{X}\)
STA imaglo, \(Y\)
LDA imaghi, \(X\)
LDA XR110
STA reallo,X
LDA XR1hi

LDA XIIlo
STA imaglo, X
LDA XIlhi

LDA \(k\)
CLC
ADC \#1
RTS

STA comphi
LDA complo
EOR \#\&FF
CLC
ADC \#1
STA complo
BCC end
INC comphi
RTS
PHX
PHY
LDX \#8
ROR 100
ROL A
DEX
BNE loop2
STA loo
PLY
PLX
RTS
PHX
PHY
JMP mult
LDA mprhi
AND mpdhi
BPL mult
LDA mprlo
STA complo

STA XI1hi \(\quad\) XII1=XI(K\%)

STA realhi, \(\mathrm{Y} \backslash \mathrm{XR}(\mathrm{K} \%)=\mathrm{XR}(\mathrm{K} 1 \%)\)

STA imaghi, \(\mathrm{Y} \backslash \mathrm{XI}(\mathrm{K} \%)=\mathrm{XI}(\mathrm{K} 1 \%)\)

STA realhi, \(\mathbf{X} \quad \mathbf{X R}(\mathrm{K} 1 \%)=\mathrm{XR} 1\)

STA imaghi, X \(\backslash \mathrm{XI}(\mathrm{K} 1 \%)=\mathrm{XI} 1\)

BCC rept4 \NEXT K\%
\begin{tabular}{|c|c|c|c|}
\hline 3800 & LDA & mprhi & \\
\hline 3810 & STA & comphi & \\
\hline 3820 & JSR & twocmp & \\
\hline 3830 & LDA & complo & \\
\hline 3840 & STA & mprlo & \\
\hline 3850 & LDA & comphi & \\
\hline 3860 & STA & mprhi & \\
\hline 3870 & & & \\
\hline 3880 & LDA & mpdlo & \\
\hline 3890 & STA & complo & \\
\hline 3900 & LDA & mpdhi & \\
\hline 3910 & STA & comphi & \\
\hline 3920 & JSR & twocmp & \\
\hline 3930 & LDA & complo & \\
\hline 3940 & STA & mpdlo & \\
\hline 3950 & LDA & comphi & \\
\hline 3960 & STA & mpdhi & \\
\hline 3970 & & & \\
\hline 3980 .mult & LDA & \#\&0 & \\
\hline 3990 & STA & prod3 & \;hi byte of product \(=0\) \\
\hline 4000 & STA & prod4 & \;hi byte of product \(=0\) \\
\hline 4010 & LDX & \# 16 & \;set bit counter \\
\hline 4020 .next1 & LSR & mprhi & \} \text { ;shift hi-byte of multplier } \\
\hline 4030 & ROR & mprlo & \;catch carry/next multplier bit intocarry \\
\hline 4040 & BCC & rotate & \;branch if multplier bit was zero \\
\hline 4050 & LDA & prod3 & \;get third byte of product \\
\hline 4060 & CLC & & \;prepare to add \\
\hline 4070 & ADC & mpdlo & \;add to low byte of multplicand \\
\hline 4080 & STA & prod3 & \;store new third byte of product \\
\hline 4090 & LDA & prod4 & \;get forth byte of product \\
\hline 4100 & ADC & mpdhi & \;add to hi byte of multplicand \\
\hline 4110 .rotate & ROR & A & \\
\hline 4120 & STA & prod4 & \;store new forth byte of product \\
\hline 4130 & ROR & prod3 & \;rotate third byte of product \\
\hline 4140 & ROR & prod2 & \;rotate second byte of product \\
\hline 4150 & ROR & prod1 & \;rotate first byte of product \\
\hline 4160 & DEX & & \;dec;ent counter \\
\hline 4170 & BNE & next1 & \;loop back if more bits \\
\hline 4180 & PLY & & \\
\hline 4190 & PLX & & \\
\hline 4200 & RTS & & \\
\hline \(4210 \backslash\) & & & \\
\hline 4220 .div16 & PHX & & \\
\hline 4230 & PHY & & \\
\hline 4240 & LDA & \#\&0 & \\
\hline 4250 & STA & pdivlo & \;set lo partial dividend \\
\hline 4260 & STA & pdivhi & \;set hi partial dividend \\
\hline 4270 & LDX & \#16 & \\
\hline 4280 .next2 & ASL & divqlo & \;shift dividend/quotent left \\
\hline 4290 & ROL & divqhi & \;shift dividend/quotent left \\
\hline 4300 & ROL & pdivlo & \;shift bits into partial dividend \\
\hline 4310 & ROL & pdivhi & \;shift bits into partial dividend \\
\hline 4320 & LDA & pdivlo & \;load lo byte of partial dividend \\
\hline 4330 & SEC & & \;prepare to subtract lo bytes \\
\hline 4340 & SBC & divlo & \;subtrect lo divisor \\
\hline 4350 & TAY & & \;save result in Y \\
\hline 4360 & LDA & pdivhi & \;load hi partial dividend \\
\hline 4370 & SBC & divhi & \;subtract hi divisor \\
\hline 4380 & BCC & done & \;skip subtraction if dividend less than divisor \\
\hline 4390 & INC & divqlo & \;incriment quotent \\
\hline
\end{tabular}
pdivhi
pdivlo
,save new hi pratial dividend
STY
DEX
BNE PLY
PLX
RTS
4460
\(4470 \backslash\)
4480 .add16
4490
4500
4510
4520
4530
4540
4550
4560
45701
4571 .shif
4572
4573 .rept
4574
4575
4576
4577
4578
LDA
CLC
ADC
STA
LDA
ADC
STA
RTS
LDA
STA count4
ASL prod1
ROL prod2
ROL prod3
DEC count4
BNE rept

4770 ? (coslo+1)=(C\% AND \&FFFF) MOD 256: ?(coshi+I)=(C\% AND \&FFFF) DIV 256

4800 ? (sinlo+I)=(S\% AND \&FFFF) MOD 256:?(sinhi+I)=(S\% AND \&FFFF) DIV 256
4805 REM PRINT TAB(0);"C="; ~(?(coslo+I)+(?(coshi+I))*256),TAB(20); TAB(40);"S=";~(?(sinlo+I)+(?(sinhi+I))*256);TAB(60)
4810 NEXT:CLS
4820 CLOSE\# Y
4830 CLOSE\# X
4840ENDPROC
4999DEFPROClooksin
5000 A=0 :CN=0
5010 sinh=\&1E06
5020 sinl=\&1B04
5030 REPEAT
5040 PRINTA,CN, \(\sim\) ? \((\sin l+A)+?(\sinh +A) * 256\)
5050 A \(=\mathrm{A}+1: \mathrm{CN}=\mathrm{CN}+1\)
5060 IF A=256 THEN \(\operatorname{sinl}=\sin l+\& 100: \sinh =\sinh +\& 100: A=0\)
5070 UNTIL CN=770
5080 ENDPROC
6000DEFPROCmathstest
6010 INPUT"FIRST" FFFF
6020 INPUT"SECOND" SSSS
6030 ?mprhi= (FFFF AND \&FFFF) DIV 256:PRINT" \({ }^{2}\) mprhi=";~?mprhi
6040 ?mprlo= (FFFF AND \&FFFF) MOD 256:PRINT"mprlo=";~?mprlo
6050 ?mpdhi= (SSSS AND \&FFFF) DIV 256:PRINT"mpdhi \(=\) ";~?mpdhi
6060 ?mpdlo = (SSSS AND \&FFFF) MOD 256:PRINT"mpdlo=";~?mpdlo
6070 CALL mult16
6080 PRINTFFFF;"*";SSSS;"=";~?prod1+?prod2*256,~SSSS*FFFF
6090 PRINT"prod1=";~?prod1,"prod2=";~?prod2
6999ENDPROC

\section*{Appendix A8}

Fault Finding Algorithm FFA
```

13390 DEF PROC FFA fault finding algorithm
13400 IF NOS=0 THEN INPUT"THRESHOLD "thresh
13410 VDU31,0,0:PRINT "
13420 VDU31,0,0:IF NOS=0 THEN PRINT"FFA ON LASER DATA"
13430 IF NOS=1 THEN PRINT"FFA ON TALY DATA"
13440 IF NOS=2 THEN PRINT"FFA ON SSA DATA"
13450 VDU31,0,1:PRINT" THRESHOLD=";thresh
13460 peak=0 :h1=INT(h1):hj=INT(hj)
13470 FOR I=INT(h1-3) TO N%/2-1
13480 IF fft(I) > peak THEN peak=ff(I):hp=I
13490 NEXT
13500 VDU31,0,3
13510 problem=0
13520 X=0.f1=1:f2=2.f3=4:f4=8:f5=16:f6=32:f7=64:f8=128:
13530 lock1=0:lock2=0:lock3=0:lock4=0
13540 single=0:exist=0:hjfound=0:LL=0:MM=0:NN=0:PP=0
13550 Jp1=0:Jp2=0:Jp3=0:pk1=0:pk2=0:pk3=0:peakj=0:
13560 FOR I=0 TO N%-1:Hx(I)=0:Hy(I)=0:Hz(I)=0:Hp(I)=0:NEXT
13570 FOR I=INT(h1-5) TO N%/2-3
13580 REM IF1 local max
13590 IF(fft(I+1)-ft(I))>0AND(fft(I+2)-ff(I+1))<0
ANDft(I+3)<ff(I+1)ANDft(I+4)<ff(I+1)
ANDff(I-1)<ff(I+1) AND fft(I-2)<ff(I+1)
AND ff(I-3)<ff(I+1)
THEN 13600 ELSE }1461

```

REM THEN1 compare with threshold REM IF2
IF ff(I +1 )> peak*thresh THEN 13630 ELSE 14590: REM THEN2
REM IF3 peak is h1 then check for proud knife OR Ob1
IF ABS(I+1-h1)<=2
THEN 13650 ELSE 14340:REM THEN3 REM search for other peaks between h1 and hj peak1 \(=0\) :peak2 \(=0\) :peak3 \(=0: L L=0\) \(\mathrm{Hy}(\mathrm{LL})=\mathrm{I}+1\) FOR J=INT(I+1) TO INT(hj-4): IF (fft \(\mathrm{J}+1\) )-ff(J) \()>0\) AND (fft \((\mathrm{J}+2)\)-ff( \(\mathrm{J}+1)\) ) \(<0\) AND fft \((\mathrm{J}+3)<\mathrm{fft}(\mathrm{J}+1)\) AND ff(J+4)<ff(J+1) THEN 13700 ELSE 13760
IF ff(J+1)> peak*threshstorepeak IF pk1>peak1

THEN peak1=pk1:Jp1=J+1:
IF fft(J+1)< peak1 AND fft(J+1)> peak \(1^{*}\) thresh THEN pk2=ff(J+1):
IF pk2>peak2 THEN peak2=pk2:Jp2=J+1:
IF ff( \(\mathrm{J}+1\) )< peak2 AND fft \((\mathrm{J}+1)>\) peak \(2^{*}\) thresh THEN pk3=fft(J+1):
IF pk3>peak3 THEN peak3=pk3:Jp3=J+1:
NEXT:
REM keep record of any peaks between h1 and hj
REM IF4 If no peaks found - Obl or Sk
REM THEN4 check for Ob1 ie. hj
IF LL=0
THEN 13810 ELSE 14040
peakK=0
FOR K= INT(hj/2) TO INT(1.5*hj):REM PRINT K
IF ff(K) \(>\) peakK THEN peakK=ff( K : \(\mathrm{Kp}=\mathrm{K}\)
NEXT :peakj=0:REM PRINT"peakK="peakK,Kp
IF ABS(Kp-hj)>3
THEN 13860 ELSE 13950
FOR K=INT(hj/2) TO INT(1.5*hj):REM PRINT K IF \((\mathrm{fft}(\mathrm{K}+1)-\mathrm{ft}(\mathrm{K}))>0\) AND \((\mathrm{ft}(\mathrm{K}+2)-\mathrm{ff}(\mathrm{K}+1))<0\) AND fft \((\mathrm{K}+3)<\mathrm{fft}(\mathrm{K}+1)\) THEN 13880 ELSE 13940
IF fft(K+1)>thresh*thresh*peakK THEN 13890 ELSE 13940 IF ABS(K+1-hj)<3

THEN 13900 ELSE 13940
\(\mathbf{K j}=\mathrm{K}+1\) :peakj=ff( Kj ): hjfound=1:Kjj=Kj:
\(\mathrm{K}=\mathrm{INT}\left(1.5^{*} \mathrm{hj}\right):\)
:GOTO 13940
REM else
endif
REM elseendif
REM else endif
NEXT: GOTO 13970
REM else
Kj=Kp:peakj=ff(Kj):GOTO 13970
REM IF5
IF peakj> thresh*thresh*peak
THEN 13980 ELSE 14000:REM THEN5
X=X+f1:lock1=1:PRINT" (O.balance 1)":PRINT" Harmonic ";I+1 PRINT" (Multi-knife)":PRINT" Harmonic ";Kj:
\(\mathrm{X}=\mathrm{X}+55:\) lock2 \(=1: \mathrm{Kjj}=\mathrm{Kj}:\) hjfound=1: GOTO 14030:REM TO ENDIF5
REM ELSE5
X=X+f8:lock3=1:PRINT" (Single knife)":
PRINT" Harmonic ";I+1:GOTO 14030:REM TO ENDIF5
REM ENDIF5
GOTO 14320:REM TO ENDIF4
REM ELSE4 could be proud knives, check for proud knives
IF lock1=0 AND lock3=0 THEN 14060 ELSE 14310:REM ELSE4
RR=LL:pcount=0
FOR M=0 TO LL-1:REM RR-1
Proud=0
IF M+1>RR THEN GOTO 14180
REPEAT
IF ABS(Hy(M)-Hy(M+1))>(Hy(0)-2.5)
AND ABS(Hy(M)-Hy(M+1))<(Hy(0)+2.5)
THEN 14120 ELSE 14130
\(\mathrm{PP}=\mathrm{PP}+1: \mathrm{Hp}(\mathrm{PP})=\mathrm{Hy}(\mathrm{M}+1):\) pcount \(=\) pcount +1 :
Hp(0)=Hy(0):Proud=1:GOTO 14160
\(\mathrm{NN}=\mathrm{NN}+1: \mathrm{Hx}(\mathrm{NN})=\mathrm{Hy}(\mathrm{M}+1): \mathrm{REM}\) Unknown fault
FOR QQ=M+1 TO RR:Hy(QQ)=Hy(QQ+1):NEXT
RR=RR-1
UNTIL Proud=1 OR RR=0
IF RR=0 AND pcount=0 THEN M=LL-1
NEXT:REM FOR QQ=0 TO LL:PRINTQQ;" ";Hy(QQ):NEXT
REM IF6
IF pcount>0
THEN 14220 ELSE 14270
REM THEN6

14660 PRINT" (Digital noise)":
14670 FOR I=1 TO MM
14680 PRINT" Harmonic "; \(\mathrm{Hz}(\mathrm{I})\)
14690
NEXT
14700 IF NN>0 THEN 14710 ELSE 14840
14710 first=1
14720 FOR I=1 TO NN
14730 exist=0
14740 IF LL>0 THEN 14750 ELSE 14780
14750 FOR J=1 TO LL
14810 IF first=1 PRINT"(Unknown Faults)":first=0
14820 PRINT" Harmonic "; \(\mathrm{Hx}(\mathrm{I})\)
14830 NEXT

14840 vpos=VPOS:IF vpos>Vpos THEN Vpos=vpos: 14850ENDPROC
14860

\section*{APPENDIX B}

\title{
COHERENT LIGHT, LASERS and PHOTODIODE
}

Contents
APPENDIX B1: The Helium-Neon Laser
APPENDIX B2: The Production of Coherent Light
APPENDIX B3: Photodiodes
APPENDIX B4: Talyrond 200

Appendix B1
Helium-Neon Laser Data Sheet

\section*{Spectra•Physics Model 105 5mW Helium-Neon Laser}


\section*{Features}
- Hard Sealed Plasma Tube
- Typical Lifetime Exceeding 22,000 Hours
- Outstanding Beam Pointing Performance
- Low Amplitude Noise
- Consistent Level of Power Output Over the Life of the Laser

Spectra-Physics' Model 105 laser head with the Model 205 power supply delivers performance unmatched in a 5 mW Helium-Neon laser system. The Model 105 is based on the Model 089 plasma tube, a hard-seal tube with a solid reputation among our most sophisticated OEM customers. This tube delivers remarkably constant output power over an extended life, a characteristic exclusive to Spectra-Physics hard-seal plasma tubes. This unique feature minimizes service calls and eliminates expensive system elements required to compensate for power degradation seen in other lasers. The Model 105 has driven dynamic beam pointing performance and static beam alignment precision beyond the demands of most OEM optical systems. In many cases, this eliminates costly realignment steps each time a laser is installed. The Model 105 is both physically and electrically compatible with standard OEM 5 mW He-Ne's. making improved performance easily available to current 5 mW users

\section*{Model 105 Laser Head}

The Model 105 Helium-Neon laser head delivers 5 mW of power output at 632.8 nm . The plasma tube is hard-sealed to permit high temperature bakeout of the tube, yielding a contaminant-free product and an extended lifetime of nominally 22,000 hours. Proprietary cathode processing leads to a constant power output leve over the life of the laser, a characteristic exclusive to SpectraPhysics hard-seal plasma tubes.
Using advanced tooling techniques, the plasma tube is packaged in a cylindrical aluminum housing to provide static beam align ment precision unequaled in \(5 \mathrm{~mW} \mathrm{He}-\mathrm{Ne}\) lasers. The tube is heat
shielded and the housing specially finished to minimize therma gradients. The result is outstanding dynamic beam pointing performance. The laser head is equipped with a beam attenuator to block laser emission while the unit is in operation.
The Model 105 comes in both polarized (Model 105-1) and nonpolarized (Model 105-2) versions. In addition, an optional \(1^{\prime \prime}-32\) accessory bezel is available to attach directly to the front face plate of the laser head. The bezel provides a convenient method of mounting special optics to be used with the laser.


Model 105 Performance Specifications

3. Beam Alignment Parameters
3.1 Static Alignment

Beam Location at Exit Aperture \(\quad<0.004^{\prime \prime}(0.1 \mathrm{~mm})\) Beam Angle \(<400\) microradians
3.2 Beam Angle Stability

Beam Angle Drift From Cold Start \(<100\) microradians Steady State Beam Angle Fluctuations <20 microradians peak

\section*{4. Environmental Limits}
4.1 Operating

Temperature
Altitude
Humidity
Vibration
Temporary power degradation due to
sinusoidal vibration in the given fre-
quency range and with the specified amplitude
\(\begin{array}{ll}5-1000 \mathrm{~Hz}, 0.5 \mathrm{G} & <5 \% \\ 5.1000 \mathrm{~Hz}, 1.0 \mathrm{G} & <10 \%\end{array}\)
\(5-1000 \mathrm{~Hz}, 1.0 \mathrm{G}<10 \%\)
\(5-1000 \mathrm{~Hz}, 1.5 \mathrm{G}\)
\(<25 \%\)
Permanent power change due to sinusoidal vibration in the frequency range \(5-200 \mathrm{~Hz}\), at a level of 1.5 G : \(<5 \%\)
4.2 Non-operating
\begin{tabular}{ll} 
Temperature & \(-40^{\circ} \mathrm{C}\) to \(80^{\circ} \mathrm{C}\) \\
Altitude & 0 to 70,000 fee \\
Humidity & 0 to \(95 \%\)
\end{tabular}

Humidity 0 to \(95 \%\)
Vibration
Shock
\begin{tabular}{ll} 
5. Electrical Parameters & \\
5.1 Operating Current & \(6.5 \pm 0.1 \mathrm{~mA}\) \\
5.2 Operating Voltage & \(2350 \pm 100\) Volts \\
5.3 Starting Voltage & \(<10 \mathrm{kV}\) \\
5.4 Drop-out Current & \(<5.5 \mathrm{~mA}\) \\
6. Mechanical Parameters & \\
6.1 Weight & \(1.94 \mathrm{lbs} / 880 \mathrm{~g}\). \\
6.2 Dimensions & See Outline Drawing
\end{tabular}

The following notes provide supporting details to the Model 105 and 205 performance specifications. The notes are numbered to correspond with the specification to which they refer.

\section*{Model 105 Laser Head}

Unless otherwise noted or implied, all performance specifications apply after the completion of a 15 minute warm-up penod.
1.3 Polarization Extinction Ratio: Less than one part in \(500(0.2 \%)\) of the total output power is contained in a plane at nght angles to the primary plane of polarization.
1.4 Beam Diameter: The beam diameter is as measured at the front face plate of the laser and at the \(1 / e^{2}\) intensity pornts of the beam.
1.5 Beam Divergence: The stated value is the full cone angle divergence. In the far field (roughly, greater than 100 cm from the laser front face plate) the \(1 / 0^{2}\) beam diameter can be estimated by the following equation:
\[
w(z)=20
\]
where 8 is the full cone angle divergence in radians and \(w(z)\) is the \(1 / e^{2}\) beam diameter at a distance \(z\) from the front face plate of the laser. At any distance from the laser, the \(1 / \mathrm{c}^{2}\) beam diameter can also be determined by the following exact equation:
\[
w(z)=w(0) \sqrt{1+\left(4 z \lambda / \pi w(0)^{2}\right)^{2}}
\]
where \(\lambda=632.8 \times 10^{4} \mathrm{~mm}\) and \(w(0)\) is the \(1 / \sigma^{2}\) beam diameter at the front face plate of the laser.


Figure 2.
1.6 Beam Quality; Random Spatual Noise: Percent of output power lying outside a disk capable of occulting more than \(999 \%\) of the theorett cally perfect Gaussian intensity distrbution; includes AR spot intensity. Beam Quality; AR Spot Intensity: Percentage of output power con tained in multuple refiections from the anti-refiection coating of the output coupler.
2.1 Warm-up Characterstics: The powers listed are percentages of the steady state power of the fully warmed-up unit. The steady state power is determined by averaging the power over a minimum period of one hour after a warm-up period of 30 minutes. After 15 minutes, the power will fall within \(85 \%\) of the steady state power, i.e., within the band defined by the long-term power dritt specification of \(\pm 5 \%\).
2.2 Long-term Power Drift: This stated value gives the maximum percentage change in power relative to the steady state power (see Note 2.1) during a period of continuous operation and under constant ambient conditions. Long-term relers to a tume period on the order of days.
2.3 Mode Sweeping Contribution: Of the total 5\% long-term power dnft. a maximum of \(2 \%\) is due to the sweeping of longitudinal modes under the gain curve.
2.4 Power Changes Over the Specried Operating Environmental Range: The spectication is determined after a 30 minute warm-up penod The ambient temperature is cycted through the operating temperature range at a rate less than \(10^{\circ} \mathrm{C}\) per hour and the laser output monitored. The output power will vary less than \(5 \%\) relative to the steady state power at \(25^{\circ} \mathrm{C}\) (see Note 2.1). All other ambiem condithons are maintained constant.
2.5 Beam Amplitude Norse: The beam amplitude noise is partially contributed by noise inherent in the power supply (see Model 205. Note
7. These specfications, therefore, are applicable only when the Mode 05 power supply is used to drive the Model 105 laser head.
Beam Amplitude Noise, Typical Spectral Density: This plot is intended to provide typical narrow band frequency information; the data is not guaranteed. The typical beam amplitude noise for a particular frequency range \(F_{n, 1}\) to \(F_{n}\) over which the spectral density has a constant value S.D.n can be estimated by the following equation.
Beam Amplitude \(=\) RMS \(_{n}=(S . D .)_{n} \sqrt{F_{n} \cdot F_{n 1}}\)
Noise (\%rms)
The total notse over several frequency ranges can then be found from:
Total Beam Amplitude \(=\sqrt{R M S_{1}{ }^{2}+\text { RMS }_{2}{ }^{2}+\ldots+\text { RMS }_{n}{ }^{2}}\) Nouse (\%rms)
To illustrate, the noise from 1 kHz to 10 kHz can best be estumated by dividing the frequency range into two parts (Note: scales are logarithmic):

RMS, \((1 \mathrm{kHz}\) to 5 kHz\()=\left(5 \times 10^{-4}\right) \times \sqrt{\left(4 \times 10^{2}\right)}=0.0003 \% \mathrm{rms}\)
\(\mathrm{RMS}_{2}(5 \mathrm{kHz}\) to 10 kHz\()=\left(1.5 \times 10^{.5}\right) \times \sqrt{\left(5 \times 10^{0}\right)}=0.001 \% \mathrm{rms}\)
Total Beam Amplitude \(=\sqrt{(0.0003)^{2}+(0.001)^{2}}=0.001 \% \mathrm{rms}\)
Noise (1 kHz to 10 kHz )
The data gren in this section is a worst case situation for any fre quency band when observed over a long tume penod relative to the trme scale of tongitudinal mode sweeping. Over this the penod, noise resulting from intermode competition will move over several treresuting from intermode cormpelted more than once. As a result. the total noise calculated from 20 Hz to 2 MHz may well exceed the broadband value, \(0.5 \%\).
3. Beam Alignment Parameters: The specifications under this section define the beam alignment accuracies of the Model 105 laser head with respect to the recommended mounting areas at the two ends of the laser housing (see Outhne Drawing, Modet 105 Laser Head). The the laser housing (see Outhne values isted are valid at constant \(25^{\circ}\) ambient temperature and are values listed are valid at constant 25 ambien tomper ture and a taken with respect to anean beal comtorlne defned by the recomary mended mounting bands. The mean best centertne is that stationary axis which traces out the smallest possibie patterns on two umaginary planes at the mounting bands as the laser is rotated through \(360^{\circ}\) on the mounting surfaces. If the mounting bands were perfectiy crecular. both patterns would shrink to points and would define a centerine in the usual sense. The specifications in this section inctude the beam displacement effects of housing eccentricity in the mounting areas. but not the effects of tolerance in the iaser housing diameter. This tolerance ( \(\pm 0.001\) ), must be considered along with the users specrfic mounting scheme when determuning the exact tolerance in beam position felative to the user's mounting surfaces.
3.1 Static Alignment: This specrication describes the steady state location in both angle and position of the laser bearm. This steady state location is determined by averaging over a penod of one hour after a warm-up period of 30 minutes.
Beam Location at Exit Aperture: This specification describes the tolerance in sleady state beam position at the front face plate of the laser. The beam will therefore fall within \(0.004^{\prime \prime}\) of the mean best centertine.
Beam Angle: The steady state angle at which the beam exits the laser can fall within a cone of half angle 400 microradians. To illustrate. observe the cross sectional view taken at \(1000^{\circ}\) from the front face plate of the laser. Al this distance. the effect of the tolerance in steady state beam position ( \(0.004^{\prime \prime}\) ) will be negigible relative to the displace-

cimurn 3
ment due to the steady state beam angle tolerance. The beam will therefore fall within a circle of radius \(0400^{\prime \prime}\left(400 \times 10^{4}\right.\) radians \(\times\) 1,000 ) of the mean best centerline or within the shaded area as illustrated in Figure 3.
3.2 Beam Angle Drift From Cold Start: During the period from cold start to steady state. the beam angle will fall within a cone of half angle 100 microradians relative to the steady state (see Note 3.1 static alignment) beam direction. At 1,000 from the laser front face plate. assume that the steady state position of the beam is at point A. Prior to reaching steady state, the beam will tall within a circle of radius \(0.100^{\prime \prime}\left(100 \times 10^{4}\right.\) radians \(\left.\times 1,000^{\prime \prime}\right)\) about point \(A\), or within the cross hatched area in Figure 3.
Steady State Beam Angle Fluctuations: After a 30 minute warm-up the beam will reman within a cone of hall angle 20 microradian relative to the steady state beam direction (see Note 3.1 static bearn alignment). At \(1,000^{\circ}\) from the laser front face plate, the beam will fall within \(0.020^{\prime \prime}\left(20 \times 10^{4}\right.\) radians \(\left.\times 1.000^{\prime \prime}\right)\) of the steady state beam
position \(A\). position A.
4.1 Operating Environmental Limits:

Temperature, Autude, Humidity: Unless otherwise stated, all spectfications will be met over the entire operating range. The humidity range given is in a non-condensing environment.
Vibration, Temporary Power Degradation: The values given are worst case values observed at resonances when the sinusordal vibration is produced along any of three mutually perpendicular axes.
Vibration. Permanent Power Change: This specrfication is stated per MIL-STD-810C Method 514.2 Category g. It a permanent power change does occur as a result of vibration, all specifications which are expressed relative to power (e.g., long-term power ditt, beam amplitude noise) will then be based on the new steady state power output.
4.2 Non-operating Environmental Limits:

Humidity: The humidity range given is in a non-condensing environment.
Vibration: The laser will meet all performance specifications after the unit is subjected to as sinusondal vibration at 1.5 G amplitude over the frequency range of \(5-200 \mathrm{~Hz}\) per MIL-STD-810C Method 514.2 Category 9.
Shock: The laser will meet all performance specifications after withstanding three 15G 11 msec. shocks along each of three mutually perpendicular axes per MIL-STD-810C.
5.1 Operating Current: The laser must be driven by a current source with current output \(6.5 \pm 0.1 \mathrm{~mA}\).
5.3 Starting Voltage: The voltage required to start the head will be less than 10kV. Hl using a power supply other than the Model 205, the start pulse must be 10 kV or greater to provide the capability of starting all possible laser heads satustying the start voltage specification. The user should also be aware that factors other than the magnitude of the start pulse (e.g., the pulse risetume and environmental conditions) will affect the exact starting charactenstics of the laser. If using a power supply other than the Model 205, these factors must be considered.
5.4 Drop-out current: Current below which the laser will cease to operate Use of a power supply other than the Model 205 may change the drop-out charactenstics of the laser.

\section*{Model 205 Power Supply}
1. Input Vottage: The Model 205-0 or 205-1 power supply must be wired to a fuse protected AC power cord for operation on the user's avaliabie AC line voltage. Reler to the Model 205 Outine Drawing for the correct whing scheme for 100, 110,200 and 220 volt oparation. All three connections (hot. neutral, and ground) must be made for proper operation of the laser. CAUTION: The green lead must be connected to ground through the AC ins. Failure to do 80 will create a safety hazard and may damage the power supply. A 100 ohm resistor may be wired in senes between the green lead and ground in order to avord any poten thal ground toops.
3. Recommended Fusing: A 0.5 Amp fuse should be wired in series with the hot lead. Fusing will protect the power supply from continuous high input current and sateguard against shorting of the AC line
4. Start Voltage: Feedback regulation of the start voltage assures a constant voltage start pulse independent of line voltage and leakage currents.
5. Output Voltage Compliance Range: The Model 205 power supply is a current source. The laser head bad will therefore determine the oprating voltage. It this operating voltage remains within the stated compliance range, the output cuprent will be regulated. The Noder 105 laser head's allowed range of running voltages assures that this condition is met.
6. Output Current: The output current regulation of . 1 mA refers to a worst case situation which would result from combined \(10 \%\) line and \(10 \%\) load voltage changes. This assurnes that the operating voltage falls within the complance range. \(H\) is possible to estmate the actual change in laser output which is directly attributable to changes in the power supply output current. The following rule of thumb apples:
\begin{tabular}{ll} 
Laser Amplitude Change (\%) Change in Power Supply \\
Attributable to Changes & \(=\) Output Current (\%)
\end{tabular} in Power Supply Output Current

Change in Power Supply
\(=\) Output Current (\%)

Therefore, \(\pm 0.1 \mathrm{~mA}\) or \(\pm 1.5 \%\) change in current will produce approximately \(\pm 0.3 \%(1.5 \% / 6)\) change in laser output.
7. Output Current Amplitude Ripple: The amplitude ripple of \(2 \%\) peak to peak ( \(7 \% \mathrm{rms}\) ) refers to both random and repettive noise in the power supply output current at frequencres greater than 10 Hz . Using the above rule of thumb (see note 6), this amplitude npple will produce a norse in laser output power of approximately \(0.1 \% \mathrm{rms}\).
9. BRH Time Delay: The Bureau of Radiological Health requires that any taser system maintan a sufficient tume delay ( \(\sim 3\) sec.) between system turn-on and emission of laser radiation, to warn the user of potential radiation exposure. The Model 205 can provide a 3.5 sec. tume delay if the user so desires. To activate the time delay, the violet wre indicated in the Model 205 Outhe Drawing should remain shorted. Cutting this wire will eliminate the tome delay.

\section*{Model 205 Power Suppiy}

The Spectra-Physics Model 205 is a feedback-regulated current supply which drives the Model 105 laser head to produce a rellable, high-performance system. Utilizing high-frequency switching regulator technology, the supply features efficient, cool operation without the need for a heat sink. Feedback current regulation and an electronic output filter yield a very stable, low-ripple output current to the laser. Complete dielectric isolation is provided between the AC line and the output circuits. Full protection is provided against both short and open circuits at the output.
The Model 205 contains an optional time delay circuit which inhibits laser ignition for approximately 3.5 seconds after the input power is applied. The tume delay, which can be activated by the user at his option (see Model 205 Outine Drawing), is one feature required by the Bureau of Radiological Health for laser devices. The Model 205 is available in two versions; the Model 205-0 which operates on 110 or 220 VAC power and the Model 205-1 which operates on 100 or 200 VAC power.

\section*{Model 205 Performance Specifications}

\section*{1. Input Voltage}

Model 205-0
Model 205-1
2. Input Current (average)
3. Recommended Fusing
4. Start Voltage (feedback regulated)
5. Output Vollage Compliance Range
6. Output Current
7. Output Current Amplitude Ripple
8. Conversion Efficiency
9. BRH Time Delay
10. Operatung Temperature (No heat anking required)
11. Weight
12. Dimensions
\(110: 220\) VAC \(=10 \%\);
\(50-400 \mathrm{~Hz}\)
100/200 VAC \(\pm 10 \%\) :
50.400 Hz

120 mA at \(100,110 \mathrm{VAC}\) 60 mA at 200.220 VAC
0.5 Amp.
\(>10 \mathrm{kVDC}\)
(1850) VDC-2450 VDC
\(6.5=0.1 \mathrm{~mA}\)
<2\% peak to peak
\(>87 \%\)
-3.5 Sec .
\(-20^{\circ} \mathrm{C}\) to \(+50^{\circ} \mathrm{C}\)
\(1.3 \mathrm{lbs} / 580 \mathrm{~g}\).
See Outline Drawing

\section*{Outline Drawings}


Model 205 Power Supply

i) Green iesd must be compacted to ground Mrough

2) A 100 Onim resistior may be wred in zeries
 iwnen otientiter ground booss
3) mansure ot AC ine must be luse protected Aoc-
4) treulate all unusedipads

\section*{Appendix B2: Laser light Production}

\section*{The Production of Coherent Light - The Laser Beam}

For their operation, lasers rely on the phenomenon of stimulated emission of radiation. This is achieved by forcing atoms into an excited energy state; an electron in an excited atom may decay to a lower energy level, and, in so doing, it will emit a photon of energy, E, given by:-
\[
\begin{align*}
& \quad \mathbf{E}=\mathbf{h v}  \tag{B2.1}\\
& \text { where:- } \\
& \mathbf{h} \text { is Plancks Constant } \\
& \mathbf{v} \text { is the photon frequency }
\end{align*}
\]

This constitutes spontaneous emission of radiation. The emitted photon may pass close to another atom in a similar excited state and it may induce an identical transition; the emitted and stimulating photons will be the same in every aspect, having the same frequency, phase, direction and polarisation.

LASER is the acronym for Light Amplification by Stimulated Emission of Radiation. Laser oscillation can only be achieved if the probability of stimulated emission is greater than that of spontaneous emission and absorbtion. This is done by a process known as inversion, in which more atoms exist in an excited energy state than in some lower state to which direct transition is possible. This imbalance must be maintained or laser oscillation will fail.

\section*{The Helium-Neon Laser}

In the Helium-Neon Laser a mixture of helium and neon gases is contained in a narrow tube. The mixture is predominantly helium - about \(90 \%\). An electrical discharge ionises the gas in the narrow tube. The plasma, thus formed, contains many helium atoms in metastable states. In these states, one of the valence electrons has been raised to the 1 s and 2 s levels where it will remain for a long time, the downward transition being forbidden by the rules of quantum mechanics.

Neon, having an atomic number of 10 , normally has 10 electrons residing in the 1 s 2 s 2 p configuration. Collisions between the metastable helium atoms and neon atoms cause one of the neon electrons in the \(2 p\) level to be raised to the 4 s and 5 s levels. The energy match between the 2 s helium levels and the 4 s and 5 s neon levels is very close and it is therefore more probable that this excitation will take place than one to the 3 s or 3 p levels. When a neon atom is excited in this way, the helium atom drops back to the ground state but, because there are many more helium atoms than neon atoms, the metastable collision probability remains very high.

For helium laser action to occur, the majority of neon atoms must remain with electrons in the 4 s and 5 s energy levels than the 3 p level. There are many downward transitions available in the excited neon electrons; the major neon laser line transitions are shown in the energy level diagram (figure B2.1).

Some of the radiation will be emitted in a direction parallel to the axis of the narrow tube; the rest is emitted through the tube walls and does not take part in the laser action. A photon travelling along the tube has a probability of passing close to a second excited neon atom and stimulating the emission of another identical photon. The probability of this happening depends on the gas density and the length of the tube; a single pass of a photon along the tube constitutes a probability of 0.1 ( \(10 \%\) ).

Mirrors are placed at both ends of the tube, reflecting the photons many times along its length, thus increasing the probability of further stimulated emission. Each stimulated photon is capable of stimulating another photon which is coherent with itself and those already present, thus, light amplification is achieved.

The two mirrors are coated to have a high reflectance of the laser wavelength of interest, but to transmit unwanted laser lines, thus amplification is restricted to the desired wavelength. Misdirected photons of the desired wavelength escape from the tube and are not amplified, which gives rise to the highly directional characteristic of laser output.

In order to utilise the desired laser radiation, some of it must be allowed to escape from the tube as a beam. This is done by coating one of the mirrors to permit about \(1 \%\) transmission of the laser wavelength. This \(1 \%\) of light which escapes constitutes the usable output of the laser.


Figure B2.1: Energy Level Diagrams for Helium and Neon

\section*{Appendix B3}

\section*{The Photodiode}

The initial stage in the action of a photoelectric semiconductor device is that the radiation quanta are absorbed, and free charge carriers are generated, in the semiconductor. These carriers immediately cause the conductivity of the semiconductor to increase; a phenomenon called photoconductivity.

Silicon photoconductors have a number of advantages over the germanium type. The resistivity of silicon can be much higher (of the order of several thousand ohm \(/ \mathrm{cm}\) ) with the consequence that photoconductors of much higher resistance can be obtained. The temperature dependence of the resistance is also many times smaller.

A photodiode is a device which makes use of the variations that occur in the current-voltage characteristics of a photoconductor p-n junction under the action of electromagnetic radiation. The effect of such radiation on this characteristic of the p-n junction depends on factors such as :-
1) the intensity and wavelength of the incident radiation.
2) the geometrical dimensions and physical parameters of the p-n junction
3) the direction of incidence of the radiation with respect to the plane of the junction.

In photodiodes, effective absorbtion of radiation occurs in a very thin surface layer (about 1 micron thick), and most of the carriers are generated in this layer. Referring to the junction shown in figure B3.1, the photon flux, Q , is perpendicular to the plane of the junction. The equations for the characteristics of the photodiode, so illuminated, have been derived by Cummerow (Ref. B3.1).

The relationship between the current, \(\mathbf{I}\), and voltage, \(\mathbf{V}\), in a photodiode is given by:-
\[
\begin{equation*}
I=I_{z}\left(e^{q V I K T}-1\right)+I_{p h} \quad=\left(I_{d}+I_{p h}\right) \tag{B3.1}
\end{equation*}
\]
where:-
\(I_{s}=\) saturation current of \(p-n\) junction
q = electronic charge (1.6x10 Coulomb)
\(\mathbf{K}=\) Boltzmanns constant ( \(1.38 \times 10 \mathrm{~J} / \mathrm{C}\) )
\(\mathbf{T}=\) absolute temperature
\(\mathrm{I}_{\mathrm{ph}}=\) photoelectric current
The first term of equation B3.1 determines the characteristic of an unilluminated photodiode; this is known as the dark current \(\mathbf{I}_{\mathrm{d}}\). The second term which, as can be seen, is independent of the voltage applied, represents the current due to carriers generated by radiation, \(\mathrm{I}_{\mathrm{ph}}\).

Typical characteristics of a photodiode, represented by equation B3.1, are plotted in figure B3.2. A photodiode is normally operated in the region to the


\section*{P-N JUNCTION PHOTODIODE}

Illumination perpendicular to the junction plane

left of the I axis on this diagram, ie. under reverse bias conditions.

\section*{References \\ B3.1 Cummerow R L,Photovoltaic Effect in P-N Junctions Physical Review 95 No 1, 1954}

\section*{Appendix B 4}

\section*{Talyrond 200 \\ Mode of Operation}

Amongst its many features, the Talyrond 200 has a 300 mm straightnes column (figure B4.1) with motorised vertical traverse. This has two travese speeds, giving rise to "horizontal" magnification of \(x 1\) and \(\times 5\).

The output signal from the stylis, which would normally be used to drive the linear recorder, was intercepted and gated through a 10 -bit Analogue to Digital Converter (ADC) (figure B4.2). The synchronizing of the analogue to digital conversions was controlled by an algorithm (see Appendix A5.2 and A5.3) in the BBC micro-computer to which the ADC was connected (see figure B4.2). The algorithm used the programmable timers in the 6522 VIA in conjunction with part of the interrupt service routine (see lines 3200 to 3300 , appendix A5.3) to send precice timing signals which identified distances along the timber sample length ( \(=125 \mathrm{~mm}\) ) in increments of 0.122 mm . The number of sample points per sample length was 1024. Hence the profile of the machined timber could be captured in the form of a digitised series of numbers. The data caputred was stored in the computer's RAM for future analysis.


Figure B4.1: Talyrond 200 data capture.


Figure B4.2: Analogue to Digital Converter used with Talyrond 200.

Appendix C
APPENDIX C1


Appendix D
APPENDIX D1


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40.00 A
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{\[
\begin{gathered}
\text { OHEAD } \\
\text { OIA }
\end{gathered}
\]} & \multicolumn{15}{|c|}{LENGTH Of Cutieernead} \\
\hline & 25 & 40 & 50 & 60 & 80 & 150 & 130 & 150 & 160 & 180 & 230 & 260 & 300 & 310 & 320 \\
\hline 101 & 4 & 6 & 7 & 8 & 11 & 14 & 18 & 21 & 23 & 25 & 33 & 37 & 42 & 44 & 45 \\
\hline \(1: 2\) & 5 & 9 & 11 & 13 & 17 & 22 & 28 & 33 & 35 & 39 & 50 & 57 & 66 & 68 & 70 \\
\hline 137 & 7 & 11 & 14 & 17 & 23 & 28 & 37 & 42 & 45 & 5! & 65 & 73 & 85 & 88 & 90 \\
\hline 150 & 9 & 14 & 17 & 21 & 27 & 34 & 45 & 52 & 55 & 62 & 79 & 89 & 103 & 107 & 110 \\
\hline 163 & 10 & 16 & 21 & 25 & 33 & 41 & 53 & 62 & 66 & 74 & 94 & 107 & 123 & 127 & 131 \\
\hline 177 & 12 & 20 & 24 & 29 & 39 & 49 & 64 & 73 & 78 & 88 & 112 & 127 & 147 & 152 & :56 \\
\hline 195 & 15 & 24 & 30 & 36 & 48 & 60 & 78 & 90 & 96 & 108 & 138 & 156 & 180 & 186 & 192 \\
\hline 215 & 18 & 29 & 37 & 44 & 59 & 73 & 95 & 110 & 117 & 132 & 169 & 191 & 220 & 227 & 235 \\
\hline 230 & 21 & 34 & 42 & 31 & 67 & 84 & 110 & 127 & 135 & 152 & 194 & 219 & 253 & 261 & 270 \\
\hline 300 & 36 & 58 & 73 & 87 & 116 & 145 & 189 & 218 & 233 & 262 & 334 & 378 & 436 & 451 & 465 \\
\hline
\end{tabular}

Appendix E: Published Papers

\title{
LAMDAMAP 93, SOUTHAMPTON
}

Laser Metrology and Machine Performance Int. Symp. pp.147-154 July 1993

\author{
A Laser Based Method for the Assessment of Machine Tool Performance \\ K.M. Maycock and R. Parkin \\ Department of Mechanical and Manufacturing Engineering, De Montfort University, Leicester, UK
}

\begin{abstract}
The problems of in process assessment of the surface quality of machined timber (high levels of vibration etc.) render most data acquisition methods inadequate. This paper describes the development and validation of a post process measurement system, capable of being transferred to the "in process" environment. The system uses a novel Laser illumination and Machine Vision technique. The signal processing analyses the surface information using Fourier techniques to produce frequency "signature". These are then analysed to provide data on product quality.
\end{abstract}

\section*{INTRODUCTION}

The wood-working industry need a reliable method to quantify and categorise the surface quality of its planed and spindle moulded products. The current practice, that of visual and tactile inspection, results in a wide variance in what may be classed as acceptable or defective surface finish. These methods are very subjective and restricted to post process application.

Modern wood-working machines "extrude" timber at extremely high rates, often in excess of \(140 \mathrm{~m} / \mathrm{min}\). When the process develops a significant fault a large quantity of defective timber is produced before the symptoms are detected by post process inspection. Evidently, to ensure consistent quality and economy, it is necessary to develop sensors capable of monitoring the quality of the product, at the instant that it is produced, so that any necessary remedial action may be effected immediately. Meanwhile, a practical and more precise method of specifying machined wood finish is required to ensure consistent quality of production.

Current surface analysis instrumentation is biased toward metalworking, has relatively short traverse lengths and use parameters which have little relevance to wood-working. Within the context of wood machining, with its high levels of vibration, the in process monitoring of surface quality using delicate stylus instruments is impossible. A fast-response, non-contact method of surface quality assessment, including parameters that can readily indicate and identify
machining defects, is required.

\section*{MACHINING PROCESS}

The timber industry uses the up-cutting mode for machining its products. Due to the kinematics of the planing process, the geometry of the machined surface consists of a series of cusps; their distribution and linear spacing being dependant largely on the linear feed speed of the timber, the number of knives on cutterhead, the rotational speed of the cutterhead, etc. In practice, the ideal surface is not achieved; vibration, spindle dynamic imbalance, proud knives, etc., all affect the locus of the knives and therefore the surface form.

\section*{ASSESSMENT PARAMETERS}

The cutting circle radius used on planing machines is relatively large (typically 150 mm ) and the depth of the cusps produced on the surface, is few microns (typically \(10 \mu \mathrm{~m}\) ). These very small amplitude variations are not detectable by the naked eye and do not account for any perceived "defects". The eye, however, is extremely sensitive to changes of slope (Gonzalez \({ }^{1}\) ). The eye detects the change from positive to negative slope at the apex of each cusp. It is the consistency with which the apexes repeat that affect the aesthetic qualities of the machined surface; any variation in the surface wavelength, or long periodic "beats" superposed there on are noticed and render the surface quality defective (Brown \({ }^{2}\) and Elmdorf \({ }^{6}\) ). Therefore it seems reasonable to develop an instrument that could analyse the frequency information inherent on machined timber surfaces.

\section*{PROPOSED INSTRUMENT}

The principles of the proposed laser instrument are as follows. A broad beam of laser light would be directed at grazing incidence to the surface being machined, and in the same plane as the traversing workpiece (figure 1). This would have the effect of producing a pattern of bright and dark regions on the surface to be assessed. This pattern, which contains the frequency information of interest, would move past a single photodiode as the workpiece is traversed. The output voltage of a photodiode would be sampled (using a rotary position encoder to define precisely the sampling points), digitised (using an Analogue to Digital Convertor) and stored for subsequent analysis.

With appropriate sampling frequency, the data captured over a given length of timber could be analysed in terms of its frequency content. This would involve transforming the data from the "time" domain to the "frequency" domain using a fast Fourier Transform (FFT) algorithm, then using a "fault finding algorithm" (FFA) to analyse the
frequency signature to detect any machining defects that may have been induced on the timber surface.

\section*{DEVELOPMENT OF LASER INSTRUMENT}

For financial and practical reasons the philosophy adopted was to develop the instrument using stationary, pre-machined timber samples. This was accomplished by employing a linear array of photodiodes (instead of a single diode), "traversing" being achieved by scanning the diode array, as opposed to moving the timber. Optical lenses were used to focus the image of a given illuminated length of timber on to the photodiode array. Scanning of the array provided data, which was captured and stored for subsequent analysis. The device, thus investigated, was a post process instrument but established using the principles of in process measurement.

\section*{Mathematical Model}

The geometry of, and the mechanics associated with, the production process was also investigated to generate a mathematical model that could be used to represent the profile of a machined timber surface. The rigorous mathematical model developed formed the nucleus of a computer surface simulation algorithm (SSA); the SSA was used to test the hypothesis of, and substantiate the philosophy behind, the proposed surface assessment method. It was also used to predict surface profiles and therefore FFT templates (or frequency signatures) for machine performance determination or surface profile comparisons.

\section*{DEFECT IDENTIFICATION FROM FFT SIGNATURES}

The frequency signature of an ideal machined timber surface will contain a single peak (or local maxima) because the pitch (or knife mark distribution) of an ideal surface is uniform. The expected number of knife-marks, \(h_{y}\), in a given sample length, \(L_{b}\), is given by
\[
\begin{equation*}
h_{j}=\frac{W L_{A}}{2 \pi V} N \tag{1}
\end{equation*}
\]
where \(\mathbf{W}\) is angular velocity of the cutterhead, V is linear feed velocity of the timber, \(\mathbf{N}\) is number of knives on the cutterhead and the suffix \(\mathbf{j}\) indicate a jointed, multi-knife finish.

Cutterheads that are not dynamically balanced produce planed surfaces that exhibit a "once-per-revolution" defect due to lack of spindle concentricity. Such a profile will feature the expected number of knife marks, \(\mathbf{h}_{\mathrm{j}}\), superposed onto a surface that undulates sinusoidally because of the imbalance. The frequency signature of a sample length of such a surface will contain two major peaks; one at principal
harmonic \(h_{j}\) (see Equation 1), the other at \(h_{1}\) (the principal harmonic which represents the surfaces undulation) given by
\[
\begin{equation*}
\mathrm{h}_{1}=\frac{\mathrm{WL}}{2 \pi \mathrm{~V}} \tag{2}
\end{equation*}
\]
where the symbols are as defined in Equation 1 and where the suffix 1 indicate a once-per-revolution defect.

A single proud knife on otherwise ideal cutterhead, would cause it to machine a surface whose frequency signature contain additional peak harmonics to that of an ideal finish. The peaks that characterise such a profile was illustrated by using the SSA to generate a "proud-knife" surface and transforming it to a frequency signature (see figure 2). The harmonic number of the peaks can be seen to follow an arithmetically progressing series that start at \(h_{1}\) (Equation 2), the amplitude of the successive peaks diminishing with increase in harmonic number.

\section*{INDUCED DEFECTS AND SURFACE ANALYSIS}

Four categories of "faults" were investigated: Ideal machining (no defects); cutterhead imbalance; proud knives; poor workpiece support and control. Timber samples were produced using machining conditions that reflected these faults; the machining parameters and machine conditions being recorded for each sample in Table 1 and corresponding data plotted in figures 3 to 6 .

TABLE 1
\begin{tabular}{|c|c|c|c|c|}
\hline Sample No. & No. Knives & Head speed & Feed speed & Machine Condition \\
\hline G2.S1 & 4 & 4500 rpm & \(60 \mathrm{~m} / \mathrm{min}\) & ideal \\
\hline G2.S4 & 4 & 4500 rpm & \(60 \mathrm{~m} / \mathrm{min}\) & out-of-balance \\
\hline G3.S9 & 6 & 6000 rpm & \(65 \mathrm{~m} / \mathrm{min}\) & I proud knife \\
\hline G4.S4 & 6 & 6000 rpm & \(80 \mathrm{~m} / \mathrm{min}\) & poor timber support \\
\hline
\end{tabular}

Three surface waveform data sets were generated from each timber sample; the first came from the Laser Instrument (LAS), the second from the Talyrond 200 (TAL) and the third from the surface simulation algorithm (SSA). Each data set was transformed into the frequency domain. The frequency signature was then analysed, using the FFA which examined it with respect to the number of significant peaks present (significance being determined by comparison with a preset threshold value), and the position that the peaks occupied in the harmonic spectrum. This showed the type of defects present in the surface and the machining faults from which they may have originated.

\section*{DISCUSSION}

For sample number G2.S1 (see figure 3), the frequency signature resulting from the laser instrument and the talyrond 200 both have a peak at harmonic \(40 \pm 1\), compared to the expected peak at harmonic \(38 \pm 1\left(=\mathbf{h}_{\mathrm{j}}\right)\) in the SSA generated data set. The difference in can be explained in terms of timber slippage during machining. However, harmonic 40 falls within the tolerance band of \(\mathbf{h}_{\mathbf{g}} \pm 2\) specified in the FFA with harmonic 41 just outside it. Hence, FFA analysis of the laser instrument's FFT signature produced the "multi-knife-finish" verdict, while that of the talyrond resulted in "unknown fault". The peak at harmonic 1 is due to variations in the timber's reflectivity because of its resinous condition. This is not a major drawback to the analysis technique, because, in timber the resinous grains are always "very-longwavelength" in nature, compared to the surface waves produced by the machining operation. Consequently, in developing the philosophy behind the FFA, the very low peak harmonics in the FFT signature were ignored.

Similar results are shown for sample G2.S4 (figure 4), where, as expected there are two significant peaks in the FFT signature, one due to cutterhead imbalance, the other to multi-knife finish. With the proud knife sample, G3.S9 (figure 5), the characteristic arithmeticallyprogressing, diminishing-harmonic phenomenon is present and was detected by the FFA for each data set. The poorly supported timber sample, G4.S4 (figure 6), could not be accurately simulated because of the large number of unknowns (forcing frequency, mode of vibration, timber stiffness, etc.). So, although some fault was obviously present, the ill equipped FFA, highlighted, but incorrectly identified, the fault.

\section*{CONCLUSIONS}

The system is successful in quantifying timber surface quality and, to some extent, identifying the causes of defects. This is a considerable step forward as it provides a basis for establishing standards and removing the subjective human link. Future work will attempt to realise an in process device with a view to adaptive process control.

\section*{References}
1. Gonzalez, R.C and Wintz P., Digital Image Processing AddisonWesley Publishing Company, Inc. 1977
2. Brown, I.D. "Visual and Tactile Judgments of Surface Roughness." Ergonomics, Vol 3, Part 1.
3. Elmdorf, A and Vaughan, T.W. "A Survey of Methods of Measuring Smoothness of Wood." Forest Products Journal, Vol 8, 1958


Figure 1: Schematic Diagram of the Proposed Technique


Figure 2: Results for Profile Simulation of Proud Knife
\begin{tabular}{|c|c|c|c|c|}
\hline \multicolumn{5}{|l|}{} \\
\hline \multicolumn{5}{|l|}{} \\
\hline \multicolumn{5}{|l|}{ \(\qquad\) TAL.62.51} \\
\hline \multicolumn{5}{|l|}{WMMMOMMMMMOMOMOMMOMOC} \\
\hline \multicolumn{5}{|l|}{\begin{tabular}{lllllllll}
1 & 38 & 75 & 113 & 150 & 188 & 225 & 255
\end{tabular}} \\
\hline \multirow[t]{2}{*}{} & \multicolumn{4}{|l|}{MMALYSIS OF FFT's USIMG FAULT FIMOLMG ALGORITMM (FFA)} \\
\hline & \multicolumn{2}{|l|}{FFA OH LASER OATA
IHRESHOLDEA.} & \[
\begin{gathered}
\text { FFA OH TAAY OATA } \\
\text { THRESHOLD }=1.5
\end{gathered}
\] & \[
\begin{aligned}
& \text { FFA OH SSA OATR } \\
& \text { THRESOOLD }
\end{aligned}
\] \\
\hline \[
\begin{aligned}
& n=9 \\
& n_{1}=8 \\
& h j=38 \\
& h j=37
\end{aligned}
\] & & \[
\begin{aligned}
& \text { (Multi-knife) } \\
& \text { Harmonic }
\end{aligned}
\] & (Unknown faults) Marmonic 41 & \[
\begin{aligned}
& \text { (Multi-knife) } \\
& \text { Harmonic } 38
\end{aligned}
\] \\
\hline
\end{tabular}

Figure 3: Results for Timber Sample Number G2.S1

Figure 4: Results for Timber Sample Number G2.S4
\begin{tabular}{|c|c|c|c|}
\hline \multicolumn{4}{|l|}{\begin{tabular}{l}
\[
-\infty-
\] \\

\end{tabular}} \\
\hline \multicolumn{4}{|l|}{} \\
\hline \multicolumn{4}{|l|}{แumu} \\
\hline  & \multicolumn{3}{|l|}{} \\
\hline h1
\(h_{2}=9\)
\(h j=18\)
¢ &  & (Proud Cnife (e) & (Malti-knify) \\
\hline
\end{tabular}
Figure 6: Results for Timber Sample Number G4.S4


Figure 5: Results for Timber Sample Number G3.S9

\title{
Surface Measurement of Planed and Moulded Timber Products
}

\author{
F. CLTRI. \(X\) MAYCOCR and R PARXI:
}
 PO Bir Itl Lemeine LEI USH Il \(\boldsymbol{x}\),

\section*{Abstract}

The surface quality of planed and moulded wooden components is primarily affected by machine performance during manufacture. Wooduorking machinery has unique problems due to high speeds of operation. With raw material throughpur rates of \(180 \mathrm{~m}: \mathrm{min}\) and cutter head speeds of 15000 rev min . large quantities of poor-quality material can arise in short periods if machine faults are allowed to develop. At present the quality of the product is principally assessed by subjective visualitactile means.

Preceding research has explored specific types of machine fault that give rise to identifiable surface waveforms, inherently found on moulded wooden components.

With the present deficiency of in-process surface monitoring systems for moulded artifacts. the aim of this work is the development of an optical non-contact measuring transducer. The in-process system will be used to measure the surface waveforms of the timber sections produced in order to identify machine faults prior to taking corrective action.

Contact measurement methods are inadequate for this application due to the high levels of vibrations and feed speeds present in the process. This paper discusses the underlying principles of the overall measuring system. and the novel laser/photodiode combination.

With the quality of the process being reflected in the resultant surface finish. fast Fourier analysis is performed on accumulated surface data. The surface data samples are
transformed to associate harmonic frequencies for surface evaluation.

The possible applications of the system are widespread. i.e., any process where surface wavelengths of 1 mm or more are important.

\section*{Introduction}

As current trends of technology advance. machines and processes becomes more complex and sophisticated. It is usually desirable for duty eycles, where possible. to be optimized and waste materials to be curtailed. However, the quality of the end commodity will always remain one of the highest production constraints. Within woodworking machinery manufacturing, competitiveness and saleability are essential [1]. Therefore it is always paramount that the machinery produced is economic. moderate in setting times and capable of high material throughput in addition to yielding good-quality artifacts.

The emphasis of this paper is that of material quality, as produced by planers and spindle moulders. It is possible for a variety of these machines to extrude timber up to a maximum rate of \(180 \mathrm{~m} / \mathrm{min}\). Allowing such a process to develop operational faults would result in large quantities of sub-standard timber being produced in a short period of time.

Palpably, to ensure consistent high quality and efficiency, a system capable of monitoring the surface quality of machined material is essential. The monitoring system would evidently have to be an optical non-contact solution due to the inherent high speeds and excessive vibration levels of the process. A

\footnotetext{
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}
cumplete appreciation of the procests and the uurface grometry of the product is requirad before developing such a measuremeni s!stem.

\section*{The Procrsis}

When planing of moulding compunents. the feed materisl is not clamped to the machine table. The wordpiece is pressed to the table. using pressurued foed rollers, as it passes the culter heads (Fig. 1). The machine thed of the planar moulder is fixed and the work. piece traverses the rotalung culter heads.

Due to the physes of the process. the geometry of the machined product surface consists essentially of circular arcs (2). As can be expected. in pracuce. the ideal is never achicred: vibration. spindle dynamic imbalance and proud hniver all alfect the cutter locus and hence the surface protile. Obviously. the greater the level of vibration. dynamic imbalance. etc., the further the surface departs from the ideal.


Fig. 1. Disgram of a spokal planer moubler. \(T=\) iop head. \(\mathrm{B}=\) bollum head. \(\mathrm{F}=\) Fence head. \(\mathrm{N}=\) near head.

\section*{Surface Gencration}

The wood removal process of planing/ moulding machines is intermittent. as shown in Fig. ? (3). The locus talen by a culter-head knife tip. while in the process of chip sever-


Fif: Moukling process showing single culter head. The wornprece is traversed past the cutter head.


Fig. 3. Surface profice obtained when the cutter head is displaced once every two revolutions.
ance. is actually cycloidal or, more broadly speaking. trochoidal [4].

In practice it is difficult to reproduce ideal machine-operating conditions. The resultant arcs produced on the machined part give rise \(t o\) many different perturbations of shape due to the practical effects already mentioned. Figure 3 shows a common surface profile obtained with a displacement effect of the culter head once every two revolutions.

As the planing and spindle moulding process generates a variety of surface shapes on the product. which are dependent on the machine operating conditions. monitoring of the product's surface profile is important.

\section*{Surface Assessment Instrumentation}

At present there are several types of surface measurement instruments and techniques capable of post-process assessment of surface finish. These range from visual/tactile and optical techniques to precision stylus instrumentation. the latter being capable of calculating surface roughness values with permanent recording facilities. Obviously each method of surface assessment has its own merits and draubacks.

Although a bariety of techniques and instrumentation capable of post-process measurement of surface irregularities exist. they are either very subjective or very time consuming. Contact instrumentation is inadequate for the measurement of in-process surface profiles. as traversing rates are of the order of millimerres per minute itspical machining rates being hundreds of metres per minute for the moulding process).

It is therefore evident. mainly because of the production speeds. that a non-contact in-process surface monitoring system needs to be developed and evaluated.

\section*{In-process Mieasurement Proposal}

The monitoring system has been designed to measure the surface characteristics of the uooden component as it is processed. Figure \(t\) represents the basis of the in-process measurement system. A broad laser beam illuminates the machined surface at grazing incidence \((0<1.5)\). The illumination is in the same plane as the traversing norkpiece. which gives prominence to the leading slope faces of each surface cusp. A fringe pattern of bright and dark regions is readily observed. representing the surface slope along the product.

A single-element silicon photodiade is used to detect variations in diffusely retfected laser light as the timber passes from the

Srace lidand:n


Fig. 4. Basis of the surface characterization ss stem for A workpiece iraversed pust a single culter head. P.D. = photodiode: S C. = signal conditioning: C.C. conirol circuiry: D.S. - dala store: D.A. - data analy. sis: FB \(=\) feedbuch: \(A D C=\) analog digital converier.
machine. Automatic gain control and signalconditioning circuitry is used to amplify and filter the output voltage of the photodiode to give maximum dynamic range to the analog-to-digital converter. The sampled output voltage of the photodiode is synchronized using the output of a rotary position encoder as the system clock for the analog-to-digital converter. Additional electronics control the clock signal for correct read/urite operations and memory sequencing. As soon as the periodic surface information has been captured (in real time) in the computer memory, it can be analysed in terms of its frequency content using Fourier analysis techniques. The data captured are not prone to distortion due to vibration. as the plane of vibration is almost perpendicular to the illumination. As the laser beam is broad and of grazing incidence to the surface. the vibration levels do not exceed the outer limits of the beam. This phenomenon only occurs because diffuse and not specular reflection is being monitored.

At present. actual material throughput is in the region of \(2-2.5 \mathrm{~m} / \mathrm{s}\). The new system has been designed to cope with a maximum material movement of \(5 \mathrm{~m} / \mathrm{s}\), thus allowing increased capacity as machine operating conditions improve. The system is capable of monitoring wavelengths of 1 mm and longer (a 1 mm wavelength represents a very fine planed surface, suitable for furniture manufacturers' requirements).

With appropriate sampling frequency. the data captured over a given sample length can be analysed in terms of frequency content using Fourier analysis techniques.

\section*{Results}

Figure \(5(\mathrm{a}, \mathrm{b})\) shows the resultant surface profiles and associated frequency spectra of a machined surface, obtained using a Talyrond and the novel laser monitoring system respecively. Figures 6 and 7. in the same manner. show other machined surfaces.

To obtain the results in Fig. 5, the machine's cutter head was set up containing six

(a)


(b)

Fig. 5. Resultant surface profiles and associated frequency spectra (harmonic nos. 1-128) obtained using (a) a Talyrond and (b) the laser monitoring system.

(a)

(b)

Fig. 6. As Fig. 5, but with a once per revolution effect caused on a four-knife cutter head and a slower feed speed.
knives and a deliberate out-of-balance effect was generated at knife number three (added weights).

With a sample length of 125 mm and 128 frequency harmonics shown, wavelengths of 125 mm down to approximately 1 mm can be represented. The dominant frequency har-

(b)

Fig. 7. As Fig. 5, but for a single-knife surface finish.
monics present in Fig. 5(b) are numbers ten and nineteen. These peaks are caused by the out-of-balance effect and individual cutter head knife markings of the process.

Figure 6 shows similar conditions to those in Fig. 5. Again there is a deliberate effect caused on a four-knife cutter head once per revolution. In this case the feed speed of the machine is much slower.
- Figure 7 shows a single-knife surface finish. This surface was obtained using a four-knife cutter head with three of the knives used as balancing masses only. With no out-of-balance effect present, the dominant frequency in the frequency spectra is now due to the cutter knife marks on the surface.

\section*{Conclusions}

Good correlation between existing surface measuring systems (Talyrond) and the novel laser measurement system has been obtained using harmonic analysis. This comparison has been achieved using a fast Fourier algorithm to convert real-time surface data to the frequency domain.

\section*{References}

1 B. Garratt. Business Development Seminar, Nov. 1988. Wadkin PLC. Green Lane Road, Leics., U.K.

2 M. R. Jackson. Some effects of machine characterisation in planed and spindle mounted wooden prod-
ucts. Ph.D. Thesis. Department of Mechanical and Production Engineering, Leicester Polytechnic, June 1986.

3 M. E. Martellotti. An analysis of the milling process. Trans. ASME. (Nov. 1941) 255-264.
4 P . Koch. An analysis of the lumber planing process. For. Prod. J.. (Aug. 1955) 677-700.

\title{
The Use of In-Process Surface Topography Measurements as a Predictor of Machine Performance and Condition by FA Cutri, RM Parkin and K Maycock
}

As manufacturing industries become progressively automated emphasis is increasingly placed on machine or process control. To this end research work presently under way at Leicester Polytechnic has concentrated on an automatic surface monitoring system for in-process production control.
Recent woodworking machinery has achieved large increases in material feed rates and cutter head spindle speeds. Typical spindle speeds of modern machinery is in the region of \(6000 \mathrm{rev} / \mathrm{min}\). For high quality machined components, spindle speeds of \(15000 \mathrm{rev} / \mathrm{min}\) (max) are required with multi knife cutter head assemblies.
Advancements in technology contribute dominantly to the high production rates and associated component quality which can now be produced. However, the adoption of technology has brought with it some undesirable and expensive problems. As the quality of the process is reflected in the surface finish of the artifact, and production rates are very high, the development of a non-contact surface monitoring system is examined.
Consideration is given to machine vibration origins, with correlation of specific topographical anomalies to machined surfaces. Prediction software and Fourier analysis have been used to attain encouraging results from machinery exhibiting know'n operational parameters.

\section*{1. Background}

Manufacturing industries are becoming increasingly automated, using complex computers for the control of production processes and machinery \({ }^{(1)}\). However, the processes and machines still propagate functional vibrations to the components under production. The period and energy content of the inherent cyclic undulations, when analysed, build up a frequency signature which is representative of characteristic operational conditions.
The repetition and amplitude of generated vibrations are usually unique for individual machines. However a machine vibration frequency spectrum can generally be predicted when analysing the design specifications. Distinctive periodic peaks, present within resultant frequency spectra, can be detected and, usually, associated with specific system mechanisms. Important, machine related. period information can be utilised as a basis for machine condition evaluation.
Machine vibration can be segregated into low, medium and high frequency ranges. dependent on origin. Usually large periodic oscillations are produced from such mechanisms as out of balance

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rotating masses, misalignments or bent shafts. Medium range undulation components such as meshing gears within gearboxes give rise to multiple shaft revolution frequencies. Short wavelength fluctuations generally originate from areas such as rolling element bearings.

\section*{2. Vibration Origins}

A rotating system and resultant frequency spectrum can be seen in Figure 1 illustrating the origins of typical periodic undulations. Point A on the spectrum identifies a spectral peak produced from an out of balance; this type of fault appears at shaft revolution frequencies. Point B (Figure 1) correlates the spectral crest to gear teeth meshing. The frequency of tooth mesh corresponds to rotational speed multiplied by the number of teeth located on the gear. As imperfect rolling action (sliding due to wear), loading and deflection (dependent on the number of teeth in mesh) vary, then high harmonics, in addition to the tooth meshing frequency, are present (Figure 2).


Fig 1 Machine Element Frequency Ranges
If local incipient faults such as a cracked (but not fully broken) tooth occurs on a gear wheel. then the resultant time and frequency spectra are affected. The damaged tooth will deflect more in mesh altering normal operational vibration characteristics as shown in Figure 3(a). The effect of a single crached tooth in the time domain signal is that of a healthy, or maybe wom gearbox signal with a series of superimposed pulses upon it. This type of local fault generates low level sidebands in the frequency domain spectrum (Figure 3(b)). As this type of fault propagates (ie several faulty teeth in mesh) then the periodic characteristics alter (Figure f(a)). An amplitude modulated effect transpires transforming the time domain signal. The effect of this change in the frequency

\section*{Gear Mesh}


\section*{Fig 2 Typical Gearmesh Waveform}
domain being an increase in the sideband amplitudes (Figure 4(b)). Point C of Figure 1 represents a typical defect frequency generated from rolling element bearings. There are several defects possible within rolling element bearings (Figure 5(a)). Faults such as cracks or blemishes (corrosion pits) can develop on either of the bearing races or even on the rolling elements themselves. If a fault occurs on the surface of the outer race (outer race fixed) then small amplitude impulses arise every time a rolling element passes
a)

b)


Fig 3 Local Incipient Gearbox Fault

over the affected area. The amplitude of these impulses are constant (Figure 5(b)), with frequency rates as indicated in Figure 6. If an imperfection arises on the surface of the inner race (rotating race), then the resultant energy impulses vary in amplitude with the changes in rolling element load (Figure 5(c)). In both cases the energy impulses are transmitted to the bearing housing, which in tum vibrates at its natural frequency.
As vibration origins can be identified using machine frequency spectra. it is possible to monitor machine status. Transitions between initial "healthy" and eventual wom or failed machine spectra can be recorded. As the operation time of the system increases and the frequency spectrum alters, thresholds can be established on required operating conditions. The thresholds imposed can be used to initialise planned preventative maintenance work, before eventual failure occurs.
As incipient operational vibrations can, and are, transferred to the workpiece, analysis of the machined commodity surface can provide (using suitable measurement/monitoring facilities) important machine operating status information.

\section*{3. The Process}

This paper will investigate planed and spindle moulding of wooden artifacts. The woodworking industry desperately requires a reliable method by which to quantify and categorise the surface quality of its planed and spindle moulded products. The current practice is that of visual tactile inspection, which results in a wide variance in what is classed as an acceptable or defective surface finish: what one manufacturer may reject as an unacceptable standard. another may accept as "good". These methods, by their very nature. are subjective and restricted to post process applications.
Woodworking machinery has unique problems due to high speeds of operation. Modern woodworking machines "extrude"


Fig 5 Bearing Defects

\(N=\) Nunber of Balls or Rollers
I = Relative rev/s Between Imer and Outer Races
1 lapact Rates f(hz) (assuming pure rolling aotion)
For Outer Race Defect: \(f\left(H_{z}\right)=N / 21(1-(B 2 P D) \cos \beta)\)
For Imer Race Defect: \(f\left(H_{2}\right)=N 21(1+(B 2 P D) \cos \beta)\)
For Ball Defect: \(f(\) hz \()=(\) PDBC \()](1-((\) PD BD \() \cos \beta))\)
Fig 6 Rolling Element Bearing Frequencies


Workpiece Traversed Past the Cutter Head Moulding Process Showing Single Cutter Head

Fig 7
timber at extremely high rates, often in excess of \(140 \mathrm{~m} / \mathrm{min}\). To achieve these rates, high cutter head rotational speeds are used (up to \(15000 \mathrm{rev} / \mathrm{min}\) ) resulting in high levels of noise and vibration with attendant risk of machine bearing failure. Thus if the process develops a fault; eg, blunt cutters, imbalance, then a considerably large quantity of sub standard (defective surface finish) timber can be produced before the symptoms are detected. It is evident. due to these operational speeds, that non-contact sensors capable of monitoring the quality of the product require development.

The planed and spindle moulding process is comparable with the milling of metals in the up cutting mode (Figure 7). Although these operations are analogous, there are some fundamental differences. The major discrepancy is that milled components are firmly clamped to the machine bed, while the bed is traversed past the cutting head. With planing and spindle moulding, the bed and the cutter heads are fixed and the workpiece is traversed using pressurised feed rollers (Figure 8). Also material machining speeds are extremely high when compared to the milling process.

Because the cutting circle diameter used on planing machines is relatively large (typically 200 mm ), the depth. h (Figure 9) of each cusp. produced on the surface of the product, is of the order of a few microns. Due to the surface amplitudes being small. height variations, as such, are undetectable by the naked eye. Investigations \({ }^{(2)}\) have shown that it is the consistency with which the apexes repeat that affect the aesthetic qualities of the machined surface. It is then surface wavelength, or periodic beat. information that is essential for product evaluation by the manufacturer.

\section*{4. Surface Finish}

As faults develop within the system. the surface contours generated on the artifact depart from the ideal. This departure contains information regarding the corresponding anomalies. As machine faults develop. changes in the surface parameters may be


Fig 4 Head Planer-Moulder

\[
\begin{aligned}
& =-R \cdot h \\
& a^{2}=R^{2} \cdot(P / 2)^{2} \\
& ==\left(R^{2} \cdot(P / 2)^{2}\right)^{1 / 2} \\
& h=R \cdot R \\
& h=R \cdot\left(R^{2} \cdot P^{2} / 4\right)^{1 / 2}
\end{aligned}
\]
\[
P=\left(f .10^{3}\right) / \mathrm{nN}
\]

\section*{Fig9 Surface Profile Height and Pitch}
analysed to predict the mechanism of the defect. The defects may be either slow moving trends or catastrophic in nature.
If machine culting conditions were ideal. with all operational factors hnown. the profile of the resultant manufactured surface would be that shown in Figure 10. The profile would consist of knife traces (arcs), detailed \(A_{1}\) to \(A_{n}\), with corresponding arc radii \(R_{1}\) to \(R_{n}\). The origin of each arc being separated by a theoretical feed pitch per hnife (identical wavelength \({ }^{(33)}\) ). However. in practice, the ideal is rarely achieved: vibration. spindle dynamic imbalance. proud hnives. etc all affect the cutter locus and hence surface profile. The greater the level of vibration. dynamic


Fig 10 Surface Profile


Fig 11 Once EveryTwo Revolution Effect
imbalance, etc the further the surface departs from the ideal. A more typical profile of a planed surface is shown in Figure 11. With a single knife finish the displacement ( \(\delta\) ) of the cutter head occurs every two revolutions of the cutter head (2P). With a total head displacement of (2 \(\delta\) ) between the theoretical feed pitch ( \(P\) ), an imperfect surface profile results. Instead if identical wavelengths of \((P)\) (ideal surface profile), the wavelengths of arc \(A_{2}\) and \(A_{3}\) are in fact equal to:
\[
\begin{aligned}
& (P+(4 R \delta / P)) \\
& \text { and } \\
& (P-(4 R \delta / P))
\end{aligned}
\]
respectively \({ }^{(t)}\). Where ( \(R\) ) is the radius of the cutter head and ( \(\delta\) ) is the instantaneous cutter head displacement.
This type of effect could be generated if an out of balance drive motor pulley was run at half the angular velocity of the cutter head spindle ( \(2: 1\) pulley ratio). Amplification of the drive motor pulley imbalance. due to structural resonance. could create significant cutter head displacement.

As machine setup and operational conditions vary widely. it is evident that many surface contours are achievable on the product. With the realisation of this phenomenon. two stages of research were undertahen. Initially simulation software was uritten. for the prediction of surface profiles obtainable on moulding machines exhibiting hnown operating conditions. In conjunction with this research. an opto-electronic non-contact. in-process surface measurement/monitoring syvtem was developed.

\section*{5. Surface Simulation}

Extensive software has been developed which explored the geometric trochoidal relationship between the cutter locus and the worhpiece traverse. All practical operating conditions, such as out of balances. proud hnives, revolution effects. etc were incorporated

within the software.
The programs allowed Fourier analysis of the simulated data, for data conversion from the time domain to that of the frequency domain (wavelength being essential surface information). Real data, gathered from the optical measuring system and a more classical stylus system (contact, post process), could also be processed by the software to establish the frequency content of real surface data. With the whole process accurately modelled the simulation software could be used to predict machined surface profiles. The accuracy of the model was evaluated against the existing surface measurement systems and the novel opto-electronic surface measurement system mentioned previously. The results and comparisons of the simulated data are discussed and illustrated later with correlation to the advanced opto-electronic surface measurement system.

\section*{6. Optical Surface Measurement System}

\subsection*{6.1 Objective}

The foregoing discussion clearly indicates the requirement for a fast-response non-contact, method of measuring the surface quality of machined timber; an integral part of this requirement is the determination of parameters) which can readily indicate and identify defects.
The "non-contact-rapid-response" nature of light, coupled with recent advances in laser and opto-electronic technology, has brought about interesting and new possibilities for in-process assessment of product quality.

\subsection*{6.2 Realisation}

Previous work has investigated certain types of machine faults that give rise to identifiable surface waveforms on produced timber \({ }^{(s)}\). The monitoring system has been designed to measure the surface characteristics of the wooden component in-process. Figure 12 represents the basis of the in-process measurement system. A broad laser beam illuminates the machined surface at grazing incidence \((\theta<1.59)\). The illumination is in the same plane as the traversing workpiece, which gives prominence to the leading slope faces of each surface cusp. A fringe pattern of bright and dark regions is readily observed representing the surface slope along the product.
A single element silicon photo diode is used to detect variations in diffusely reflected surface laser light as the timber passes from the machine. Automatic gain control and signal conditioning circuitry is used to amplify and filter the output voltage of the photo diode to give maximum dynamic range to the analogue to digital convertor. The sampled output voltage of the photo diode is synchronised using the output of a rotary position encoder, as the


Fig 12 Surface Illumination
system clock for the analogue to digital convertor. Additional electronics control the clock signal for correct read/write operations and memory sequencing. As soon as the periodic surface information has been captured (in real time) in the computer memory, it can be analysed in terms of its frequency content, using Fourier Analysis Techniques. The data captured is not prone to distortion due to vibration, as the plane of vibration is almost perpendicular to the illumination. As the laser beam is broad and of grazing incidence to the surface the vibration levels do not exceed the outer limits of the beam. This phenomenon only occurs because diffuse and not specular reflection is being monitored.

At present, actual material throughput is in the region of two to two and a half metres per second. The new system has been designed to cope with a maximum material movement of five metres per second, thus allowing increased capacity as machine operating conditions improve. The system is capable of monitoring wavelengths of one millimetre and greater (one millimetre being a very fine planed surface suitable for furniture manufacturers requirements).

\subsection*{6.3 Results}

Figure 13(a,b,c) shows the resultant surface profiles and associated frequency spectra of a machined surface, obtained using a Talyrond, the novel laser monitoring system and simulation software respectively. Figures 14 and 15 , in the same manner, show other machined surfaces. To obtain the results in Figure 13, the responsible machines cutter head was set up containing six knives and was run at six thousand rev/min. With a material feed speed of ninety metres per minute and a deliberate out of balance effect generated at knife number three (added weights). Figure 13(b) was recorded using the laser system.
With a sample length of one hundred and twenty five millimetres and one hundred and twenty eight frequency harmonics shown; wavelengths of one hundred and twenty five millimetres down to approximately one millimetre can be represented. The dominant frequency harmonics present in Figure 13(b) are numbers ten and

a)

b)




Fig 13 Surface Data

\section*{Text cut off in original}
 with these specific operating conditions. It would take 8.33 seconds to pass one hundred and twenty five millimetres of material, through the machine, at a feed rate of ninety metres per minute. With a cutter head speed in the order of six thousand rev/min there would be approximately eight and one half revolutions within the sample length. In fact from Figure 13(b) it can be seen that there are ten revolutions present. This small discrepancy is due to inaccuracies arising from the feed and cutter head speed equipment. As there is an out of balance effect, the knife marks vary in surface wavelength, thus in the frequency spectrum the knife marks are spread over several rather than a single harmonic (eg harmonic numbers \(10,19, \mathrm{etc}\) ).
Figure 14 shows similar conditions as that in Figure 13. Here again there is a deliberate once per revolution effect caused on a four knife cutter head. In this instant the feed speed of the machine (eighteen metres per minute) is much slower, but the cutter head speed of six thousand rev/min remains the same. The effect of the slow feed speed on the surface is the translation of the out of balance dominant frequency along the frequency spectrum (Higher frequency due to slower moving feed material). A second effect being the smoothing of knife marks on the surface, which is indicated in the frequency spectrum due to a lack of other higher dominant frequency harmonics.
Figure 15 shows a single knife finish surface. This surface was obtained using a four knife cutter head with three of the knives used as balancing masses only. With no out of balance effect present, the dominant frequency in the frequency spectra is now due to the cutter knife marks on the surface. With a feed speed of eighteen metres per minute it would take 0.416 seconds to pass one hundred and twenty five millimetres of timber past the cutter head. Again with a six thousand rev/min cutter head there would
b)


c)
mownownownownowruwow


Fig 1s Surface Data
be 41.6 revolutions of the cutter head (with a single knife this would be 41.6 identical knife marks) in the sample length. As shown in each of the frequency spectra the dominant harmonic is number forty five (wavelengths of 3 mm ). This small discrepancy resulting again from feed and cutter head equipment inaccuracie

\section*{7. Conclusions}

This paper has discussed typical vibration origins of machines and the effects they have on the surface of the manufactured component. Prediction software as well as non-contact measuring/monitoring hardware has been developed to control t quality of the artifacts and the process. Good correlation betwee: existing surface measuring systems (Talyrond) and the novel lase measurement system has been obtained using harmonic analysis This comparison has been achieved using a Fast Fourier Algorithm to convert real time surface data to the frequency domain. Faults such as corrosion pits or cracks on bearing races gears will be present at higher harmonics of the frequency spects Future work regarding the frequency spectra of trend or catastrophic failures is required for correct initialisation of feedback action.

\section*{8. References}
1. LR Rakowoski. Blasting Off with CIM. Machine and Tool Blue Book. June 1987.
2. B Garratt. Business Development Seminar. Nov 1988. Wadkin Plc. Green Lane Road. Leics
3. R Goodchild. Investigating Finish of Rotary Planing. Engineering. Jan 25th 1963.
4. MR Jackson. Some effects of machine characterisation in planed and spindle moulded wooden products. PhD Thesi Dept of Mechanical and Production Engineering, Leicesti Polytechnic. June 1986.
5. MS Hundral. Mechanical Signature Analysis. Dept of Mechanical Engineering. University of Vermont. Burlingt

Measurement and Control Techniques for Timber Production Processes

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Woodworking machinery has unique problems due to the high speed of operation. The production rate of planed and spindle moulded timber products is currently running at approximately \(1 \mathrm{~m} / \mathrm{s}\). To achieve these rates high speed cutters are used (up to 15000 rev/min) resulting in high levels of noise and vibration and product. The quality of the product is normaly assessed by subjective visual means, i.e. does it look alright?

Previous work has investigated certain types of machine fault that give rise to identifiable surface waveforms of the produced timber. Nis paper proposes and rectify product defects.

An important feature of this work is the development of a "smart" sensor to identify machine faults, prior to taking corrective action.

Contact measurement methods are inappropriate due to high speeds and vibration levels present in the process. This paper describes a microprocessor machine management and control system.

The measurement system incoporates a novel laser and photodiode array combination and utilises real time Fast Fourier analysis techniques. The the surface waviness (wavelength \(\Rightarrow 1 \mathrm{~mm}\) ) is important (e.g. steel production, plating/coating industry). The sensor system is the subject of a patent
1.0 Introduction

The woodworking industry desperately needs a reliable method by which to quantify and categorise the surface quality of its planed and spindle moulded products. The current practice is that of visual and tactile inspection, which
results in a wide variance in what is classed as an acceptable or defective surface finish; what one manufacturer may reject as an unacceptable standard, another may accept as "good". These methods, by their very nature, are another mactive and are restricted to post-process application.
Modern woodworking machines "extrude" timber at extremely high rates, of en in excess of \(140 \mathrm{~m} / \mathrm{min}\). Thus, when the process develops a fault, eg blunt cutters, timber is produced before the symptoms are detected by post-process inspection.
Evidently, to ensure consistent quality and economy, it is necessary to effected immediately.
1.2 Surface Ceometry
Machined timber production has some similarities with the milling of metals; the revolving cutter shears chips from the surface in the up-cutting mode. own, wood, 15000 , \(\mathrm{m} / \mathrm{min}\) ) and cutter speeds workpiece is clamped to a moving bed, whilst in wood machining the bed is fixed and the workpiece is traversed.
Due to the physics of the process, the geometry of the machined surface consists of a series of, essentially, cicular arcs. As can be expected, in practice, the ideal is never achieved; vibration, spindle hence surface profile. Obviously, the greater the level of vibration, dynamic imbalance, etc, the further the surface form departs from the ideal.
On considering the methods of surface analysis currently available (ie.stylus, visual/tactile, opotical and laser/optoelectronic techniques) none was found which would satisfy the criterion demanded by wood machining:-
i) Stylus instruments proved too delicate and possessed too small a

> ii) Optical techniques are too time consuming.
> iii) Laser/Optoelectronic techniques proved prone to object surface vibration which is inhrent in wood machining.

\subsection*{2.0 Objective}
The foregoing discussion indicates the requirement for a fast-response, non-contact, method of measuring the surface quality of machined timber; an
integral part of this requirement is the determination of parameter(s) which can readily indicate and identify defects.
The "non-contact-rapid-response" nature of light, coupled with recent advances in laser and opto-electronic technology, has brought about interesting and new
2.2 Proposed Parameters large (typically 200 mm ), the depth of each cusp produced on the surface is of the order of a few microns (typically \(10 \mu \mathrm{~m}\) ). These are very small amplitude variations and, as such, are not detectable by the naked eye. Amplitude

 to negative slope, where the cicular arcs intercept, ie the apexes.
linear array of photodiodes rather than a single diode. Iraversing was achieved by scanning the diode array instead of traversing the timber. Optical photodiode array. Scanning of tise array provides data which is then captured for suosequent analysis.
4.0 Results
4.1 Data Capture
Figure \(2(b)\) shows a typical graphical display of surface data captured from a
timber sample (relative lightintensity being plotted against lateral position) which had been planed using a feedspeed of \(106 \mathrm{~m} / \mathrm{min}\), cutterspeed of 6000 rpm and 6 kni ves on the cutter head. Figure \(2(a)\) shows the correspondin. lalysurf trace of the same sample.


The in-process application of the technique will be pursued; this necessitates dispensing with the use of a general purpose computer, replacing it with a incorporating the use of maths coprocessors and FFI analysers.
8.0 Bibliography
Knidsen \(V\)
V1, 1928
Rafael C. Gonzalez, Paul Wintz, Digital Image Processing, Addison-Wesley Publishing Company, Inc. 1977
Schmaltz G, Vechnische Oberflachenkunde, Springer, Berlin, 1936

\title{
BHRA Lond Monitoring Journal Tech Note Vol 4, Noil, Jan 199/
}

\author{
In-Process surface Topography Measurements Predict Machine Performance and Condition. \\ F. Cutri BEng \\ R. Parkin B. Sc, PhD, Eng, MIEE, MIMechE R. Haycock B. Bc
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\section*{Introduction}

This review investigates planed and spindle moulding of wooden artifacts (Figure (1)). The woodworking industry desperately requires a reliable method by which to quantfy and categorise the surface quality of its planed and spindle moulded products. The current practice is that of visual tactile inspection, which results in a wide variaance in what is classed as an acceptable or defective surface finish; what one manufacturer may reject as an unacceptable standard, another may accept as "good". These methods, by their very nature, are subjective and restricted to post process applications.

Woodworking machinery has unique problems due to high speeds of operation. Modern woodworking machines "extrude" timber at extremely high rates, often in excess of \(100 \mathrm{~m} / \mathrm{min}\). To achieve these rates, high cutter head rotational speeds are used (up to 15000 rev/min) resulting in high levels of noise and vibration with attendant risk
of machine bearing failure. Thus if the process develops a fault; eg, blunt cutters, imbalance, then a considerably large quantity of sub standard (defective surface finish) timber can be produced before the symptoms are detected. It is evident, due to these operational speeds, that noncontact sensors capable of monitoring the quality of the product require development.

Because the cutting circle diameter used on planing machines is relatively large (typically 200 mm ), the depth, \(h\) (Figure (2)) of each cusp, produced on the surface of the product, is of the order of a few microns. Due to the surface amplitudes being small, height variations, as such, are undetectable by the naked eye. Investigations have shown that it is the consistency with which the apexes repeat that affect the aesthetic qualities of the machined surface. It is then surface wavelength, or periodic beat, information that is essential for product evaluation by the manufacturer.

\section*{Realisation}

The foregoing introduction clearly indicates the requirement for a fast-response non contact, method of measuring the surface quality of machined timber. Thus the "non-contact-rapid-response" nature of light, coupled with recent advances in laser and opto-electronic technologies, brings about interesting and new possibilities for the in-
process assessment of product quality.

Previous work has investigated certain types of machine faults that give rise to identifiable surface waveforms on produced timber. The monitoring system has been designed to measure the surface characteristics of the wooden component in-process. Figure (3) represents the basis of the in-process measurement system. A broad laser beam illuminates the machined surface at grazing incidence \(\left(\theta<1.5^{\circ}\right)\). The illumination is in the same plane as the traversing workpiece, which gives prominence to the leading slope faces of each surface cusp. A fringe pattern of bright and dark regions is readily observed representing instantaneous surface slope along the product.

A single element silicon photo diode is used to detect variations in diffusely reflected surface laser light as the timber passes from the machine. Automatic gain control and signal conditioning circuitry is used to amplify and filter the output voltage of the photo diode to give maximum dynamic range to the analogue to digital convertor. The sampled output voltage of the photo diode is synchronised using the output of a rotary position encoder, as the system clock for the analogue to digital convertor. Additional electronics control the clock signal for correct read/write operations and memory sequencing.

As soon as the periodic surface information has been captured (in real time) in the computer memory, it is analysed in terms of its frequency content, using Fourier Analysis Techniques (Fast Fourier Transforms). The data captured is not prone to distortion due to vibration, as the plane of vibration is almost perpendicular to the laser illumination. As the laser beam is broad and of grazing incidence to the surface the vibration levels do not exceed the outer limits of the beam. This phenomenon only occurs because diffuse and not specular reflection is being monitored.

At present, actual material throughput is in the region of two to two and a half metres per second. The new system has been designed to cope with a maximum material movement of five metres per second, thus allowing increased capacity as machine operating conditions improve. The system is capable of monitoring wavelengths of one millimetre and greater (one millimetre being a very fine planed surface suitable for furniture manufacturers requirements).

\section*{Results}

Figure ((4) \(a, b\), ) show the resultant surface and illumination profiles with their associated frequency spectra of a machined timber surface, obtained using a Talyrond and novel laser monitoring system respectively. Figures (5)
and (6), in the same manner, show other typical machined timber surfaces. The resulting profiles in figure ((4)a,b) were obtained on a six knife cutter head machine. The cutter head was run at six thousand rev/min with a corresponding material feed speed of ninety metres per minute. A deliberate out of balance effect was generated at knife number three on the cutter head (added weights), which resulted in the creation of particular frequency harmonics.

With sample lengths of one hundred and twenty five millimetres and one hundred and twenty eight frequency harmonics shown; wavelengths of one hundred and twenty five millimetres down to approximately one millimetre are representable. The dominant frequency harmonics present in Figure ( \((4) a, b)\) are numbers ten and nineteen \((12.5 \mathrm{~mm}\) and 6.58 mm wavelengths). These peaks are caused by the out of balance effect and individual cutter head knife markings respectively. Because the out of balance effect occurred once every revolution of the cutter head the approximate frequency harmonic expected was number eight or nine, with these specific operating conditions. It would take 0.0833 seconds to pass one hundred and twenty five millimetres of material, through the machine, at a feed rate of ninety metres per minute. With a cutter head speed in the order of six thousand rev/min there would be
approximately eight and one half revolutions within the sample length. In fact from Figure ( \((4) a, b)\) it can be seen that there are ten revolutions present. This discrepancy is due to inaccuracies arising from the feed and cutter head speed equipment. As there is an out of balance effect, the knife marks vary in surface wavelength, thus in the frequency spectrum the knife marks are spread over several rather than a single harmonic (eg harmonic numbers 10, 19, etc).

Figure (5) shows similar conditions as that in Figure (4). Here again there is a deliberate once per revolution out Of balance effect caused, however, now on a four knife cutter head. In this instant the feed speed of the machine ( eighteen metres per minute) is much slower, but the cutter head speed of six thousand rev/min remains the same. The effect of the slow feed speed on the surface is the translation of the out of balance dominant frequency along the frequency spectrum (Higher frequency due to slower moving feed material). As it would take 0.4166 seconds to pass one hundred and twenty five millimetres of timber at eighteen meters per minute. An out of balance frequency would now be generated at approximately harmonic No forty two (Figure((5)a,b)) in the frequency spectra. In addition to the out of balance phenomenon there is a secondary effect resulting in smoothed surface knife
marks, this event is indicated in the frequency spectrum due to a lack of other higher dominant frequency harmonics.

Figure ((6)a) shows a single knife finish surface. This surface was obtained using a four knife cutter head with three of the knives used as balancing masses only. With no out of balance effect present, the dominant frequency in the frequency spectra is now due solely to the cutter knife marks on the surface. With a feed speed of eighteen metres per minute it would again take 0.416 seconds to pass one hundred and twenty five millimetres of timber past the cutter head. With a six thousand rev/min cutter head there would be 41.6 revolutions of the cutter head (with a single knife this would be 41.6 identical knife marks) in the sample length. As shown in each of the frequency spectra (figure ((6)a,b)) the dominant harmonic No is number forty five (wavelength of 3 mm ). The discrepancy resulting again from feed and cutter head equipment inaccuracies.

\section*{Conclusion}

Non-contact measuring/monitoring hardware and software has been developed to control the quality of planed artifacts. Good correlation between existing surface measuring systems (Talyrond) and the novel laser measurement system has
been obtained using harmonic analysis. This comparison has been achieved using a Fast Fourier Algorithm to convert real surface data from the time to the frequency domain. Results have shown that certain machine fault signatures are inherent within manufactured product surface contours. Future work regarding the frequency spectra of trend or catastrophic failures is required for correct initialisation of machine feedback action.


\section*{Surface Profile Height and Pitch'}

\(\mathrm{a}=\mathrm{R}-\mathrm{h}\)
\(\mathrm{a}^{2}=\mathrm{R}^{2}-(\mathrm{P} / 2)^{2}\)
\(P=\left(f .10^{3}\right) / \mathrm{nN}\)
\(a=\left(R^{2}-(P / 2)^{2}\right)^{1 / 2}\)
\(h=R-a\)
\(h=R \cdot\left(R^{2} \cdot P^{2} / 4\right)^{1 / 2}\)
Figure 2


\section*{Talyrond surface Data}

4a)
(A)

(A)


Laser slope Intensity Data

4b)
(I)
 Distance
(A)
 Harmonic No 1-128
(A) Amplitude

Figure 4


\section*{Talyrond surface Data}

6a)
(A)

(A)
 Harmonic No 1-128

\section*{Laser slope Intensity Data}

6b)
(I)


Distance
(A)


Harmonic No 1-128
(A) Amplitude
(I) Intensity```

