

# A new regression model to predict BIPV cell temperature for various climates using a high-resolution CFD microclimate model

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## Abstract

Understanding of cell temperature of Building Integrated Photovoltaics (BIPV) is essential in the calculation of their conversion efficiency, durability and installation costs. Current PV cell temperature models mainly fail to provide accurate predictions in complex arrangement of BIPVs under various climatic conditions. To address this limitation, this paper proposes a new regression model for prediction of the BIPV cell temperature in various climates and design conditions, including the effects of relative PV position to the roof edge, solar radiation intensity, wind speed, and wind direction. To represent the large number of possible climatic and design scenarios, the advanced technique of Latin Hypercube Sampling was firstly utilized to reduce the number of investigated scenarios from 13,338 to 374. Then, a high-resolution validated full-scale 3-dimensional Computational Fluid Dynamics (CFD) microclimate model was developed for modelling of BIPV's cell temperature, and then was applied to model all the reduced scenarios. A nonlinear multivariable regression model was afterward fit to this population of 374 sets of CFD simulations. Eventually, the developed regression model was evaluated with new sets of unused climatic and design data when a high agreement with a mean discrepancy of 3% between the predicted and simulated BIPV cell temperatures was observed.

**Keywords:** Building, BIPV, Latin Hypercube Sampling, Regression, CFD

## Nomenclature

$T_c$	PV cell temperature	K	$T_a$	Ambient air temperature	K
$k_r$	Ross coefficient	$m^2K/W$	$G_t$	Solar irradiance	$W/m^2$
$U$	Wind speed	$m/s$	$C_a, C_b$	SNL model coefficients	
$\Delta T$	Difference of $T_c$ and back surface temperature under $G_o$	K	$x, y, z$	Computational cell length in three dimensions	m
$L, W, H$	Dimension of objects	m	$u$	Fluid velocity	$m/s$
$p$	Fluid pressure	pa	$Q'_c$	Convective heat flux	$W/m^2$
$G_o$	Reference solar radiation	$W/m^2$	$\rho$	Air density	$kg/m^3$
$\vec{g}$	Gravitational acceleration	$m/s^2$	$\bar{\tau}_{eff}$	Effective stress tensor	
$\mu_{eff}$	Effective viscosity	$m^2/s$	$\bar{I}$	Unit tensor	
$\mu_t$	Eddy viscosity	$m^2/s$	$\mu$	Sum of molecular viscosity	$m^2/s$
$\rho_0$	Constant density under operating temperature $T_0$	$kg/m^3$	$G_k$	Mean velocity gradient contributed to k	$W/m^3$
$\beta$	Thermal expansion	$1/K$	$k$	Turbulence kinetic energy	J/kg
$\varepsilon$	Turbulence dissipation rate	$m^2/s^3$	$T_0$	Operating temperature	K

$G_b$	Buoyancy contributed to $k$	$W/m^3$	$S_k$	User-defined source of $k$	
$\sigma_k, \sigma_\varepsilon$	Prandtl number for $k$ and $\varepsilon$		$C_\mu$	Model constant	
$C_{1\varepsilon}, C_{2\varepsilon}$	Model constants		$S_\varepsilon$	User-defined source of $\varepsilon$	
$E$	Energy of unit mass component	$m^2/s^2$	$\bar{h}$	Sensitivity enthalpy	$m^2/s^2$
$\lambda_f$	Flow thermal conductivity	$W/mK$	$\lambda_t$	Turbulence conductivity	$W/mK$
$\vec{h}_j \vec{j}_j$	Enthalpy transportation of diffusion	$W/m^2$	$\lambda$	Coefficient of thermal conductivity	$W/mK$
$S_h$	User-defined source of energy		$S_r$	Solar load	$W/m^3$
$Q'$	Heat flux	$W/m^2$	$\varepsilon_{m,r}$	Emissivity of exposed roof surface	
$\sigma$	Stefan-Boltzmann constant		$T_{sky}$	Sky temperature	K
$T_r$	Roof temperature	K	$\varepsilon_{m,s}$	Sky emissivity	
$U_z$	Local flow speed at $H_z$	$m/s$	$U_{met}$	Meteorological wind velocity	$m/s$
$H_z$	Local height	m	$H_{met}$	Height of meteorological station	m
$\alpha$	Wind shear exponent		$I_z$	Local turbulence intensity	
$\delta_G$	Terrain boundary thickness	m	$k_z$	Local turbulence kinetic energy	$m^2/s^2$
$\varepsilon_z$	Local turbulence dissipation rate	$m^3/s^3$	$L_\alpha$	Vertical temperature gradient	K/m
$E_r$	Radius of the Earth	m	$PI$	PV position index	
$\theta$	Relative wind angle	$^\circ$	$N$	Population size	
$n$	Sample size		$p_s$	Sample proportion	
$z_c$	Critical value at a given confidence level		$l$	Distance between bottom edge of PV panel and roof	m
$d$	Margin of error		$R^2$	Coefficient of determination	
$Y_i$	Observed (simulated) value of each sample		$\hat{Y}_i$	Predicted value of each sample	
$\bar{Y}_i$	Mean of all observed value		$k_{coeff}$	Total number of coefficients in regression	
$RMSE$	Root mean square error		$E_1$	Relative gap	
$FAC2$	Fraction of predictions within a factor of two of observations				

25

## 26 1. Introduction

27 The share of renewable energy has increased in the world primary consumptions from  
 28 14% of global demands in 1998 to 19.3 % in 2015 (Goldemberg, 2000; Renewable Energy  
 29 Policy Network for the 21<sup>st</sup> Century [REN21], 2017). It is expected that renewable energy  
 30 share takes one quarter of the whole energy market by 2040 with an average annual increase  
 31 rate of 2.8% (Energy Information Administration [EIA], 2017) with a potential to be expanded  
 32 over a long-term period of time (up to 30-80% by 2100 according to Panwar, Kaushik, and  
 33 Kothari (2011)). Among the markets of clean energy, photovoltaic (PV) technologies have  
 34 shown a promising success during past years while it was predicted to keep permeating with  
 35 further improvements in PV's performances (REN21, 2017). Solar PVs are vastly integrated  
 36 or partially integrated to building roofs and façades, known as building integrated  
 37 photovoltaics (BIPV), converting solar energy into electricity on the site and supporting the  
 38 building energy demands (Elkarmi & Abu-Shikhah, 2012; Bramanti, 2015).

39 In ideal experimental conditions, the electrical efficiency of a typical PV system is 15-20 %  
 40 (Kalogirou, 2014). Accumulative heat impacted on a PV panel leads to the elevation of  
 41 surface/cell temperature ( $T_s/T_c$ ) and thereby causes a drop of cell efficiency, normally  
 42 occurring when operating temperature exceeds 25 °C (Solanki, 2013), with a rate of -0.2 %/°C  
 43 to -0.45 %/°C for amorphous and crystalline-silicon-based PVs (Kalogirou, 2014). In addition,  
 44 the high temperature degrades the PV materials and hence shorten their durability, which is  
 45 expected as 30-35 years for such integrated systems (Bahaj, 2003). This implies that the PV  
 46 cell temperature should be controlled either with advanced mechanical cooling approaches

47 or alternatively with natural ventilation, particularly in hot climate where there is a high risk of  
48 hot spot formations.

49 [Elkarmi and Abu-Shikhah \(2012\)](#) recommended an elaborative scrutiny of the installation  
50 site before the PV implementation to access an optimum performance. This implies that, to  
51 evaluate the reliability and feasibility of a BIPV project, tools are required to assess the near-  
52 field airflow around cell surfaces and further to estimate their operating thermal behaviour.  
53 [Skoplaki and Palyvos \(2009\)](#) undertook a literature review of methods to determine the PV  
54 operating temperate, including implicit and explicit methods. The PV temperature given by  
55 the former method depends on some variables relying on temperature, for example, the panel  
56 efficiency, while the explicit method calculates temperature directly. In general, it is crucial  
57 that these models should include the impact of surrounding environment in their calculations  
58 although there were only few developed models finding  $T_c$  from its relation with the  
59 surrounding environment. Example of such models is an explicit calculation by [\(Ross Jr,  
60 1976\)](#):

$$T_c = T_a + k_r G_t \quad (1)$$

61 where  $T_a$  is the ambient air temperature (K),  $G_t$  is solar irradiance ( $W/m^2$ ) and  $k_r$  is Ross  
62 coefficient ( $m^2K/W$ ); the adapted values of which are summarized from reference data  
63 [\(Nordmann & Clavadetscher, 2003\)](#). Another example is a model to predict PV temperature  
64 from a nominal operating cell temperature (NOCT) measured in the nominal terrestrial  
65 environment (NTE) condition, also known as the standard reference environment, which is  
66 specified as  $800 W/m^2$  irradiance normal to a free-running device mounted rack with an  
67 optimum tilt ventilation against  $1m/s$  wind at an ambient temperature of  $20\text{ }^\circ C$  [\(Markvart &  
68 Bogus, 2000\)](#):

$$T_c = T_a + (T_{c,NOCT} - 20) \frac{G_t}{800} \quad (2)$$

69 where NOCT means the referring variable to the value at the nominal terrestrial environment.  
70 Furthermore, a model was developed by Sandia National Laboratories (SNL) [\(King, Boyson,  
71 & Kratochvill, 2004; Skoplaki & Palyvos, 2009\)](#), which includes wind speed in its equation:

$$T_c = T_a + G_t \cdot (e^{C_a + C_b U}) + \frac{G_t}{G_o} \cdot \Delta T \quad (3)$$

72 where  $C_a$  and  $C_b$  are the model coefficients determined by the module type and mounting  
73 method.  $U$  represents the wind speed (m/s), and  $\Delta T$  is the temperature difference (K)  
74 between the solar cell and rear surface measured under a reference solar radiation flux of  
75  $G_o = 1000 W/m^2$ .

76 All these models included the effect of solar radiation and ambient temperature. However,  
77 the effect of wind speed was only considered by SNL model via empirical coefficients,  
78 depending on the module assembles and mountings. The NOCT model only took a default  
79 natural ventilation value against the wind of  $1m/s$  whilst the ventilation effect was simply  
80 inducted by assigning different array installations in the first model. In conclusion, none of  
81 these methods took the influence of stochastic wind directions into the account, which can

82 be source of a huge discrepancy in the prediction of PV cell temperature. For example, an  
 83 assessment undertaken by [D’Orazio, Perna & Di Giuseppe \(2014\)](#) within typical Italian  
 84 climate showed that the deviation between the calculated temperature by NOCT and  
 85 measurement was up to 12 °C while this value was 8°C between the SNL method and  
 86 measurement. In another study by [Assoa, Gaillard, Ménézo, Negri, & Sauzedde \(2018\)](#), it  
 87 was reported that NOCT model significantly overestimated the PV cell temperature while  
 88 Ross coefficient failed to evaluate the heat dissipation due to the lack in consideration of the  
 89 site wind conditions.

90 As another limitation, the current site surveying for BIPV installation was mainly focused  
 91 on the solar data and overshadowing of surroundings, but seldom considering the wind effect  
 92 ([Bagatelos & Henson, 2012](#)). There were few studies through field measurements that  
 93 considered variation of weather conditions though entirely focused on wind speed rather than  
 94 wind direction ([Kaldellis, Kapsali, & Kavadias 2014](#); [Gökmen, 2016](#)). Despite of the well  
 95 understood fact that PVs’ natural cooling is impacted by the integration type, building  
 96 geometry, and district planning with stochastic climates, there is scarce investigation, paying  
 97 attention to the impact of these factors although difficult to predict, especially in complex  
 98 urban morphologies. In conclusion, site survey and experimental techniques in measurement  
 99 of PV cell temperature face a high operating cost and many difficulties for repetitive tests to  
 100 minimize site-dependent influences, placing them as less preferred options. On the other side,  
 101 Computational Fluid Dynamics (CFD) technique is considered as a promising approach to  
 102 deliver quantitative studies due to its high flexibility and accuracy with less operating cost.

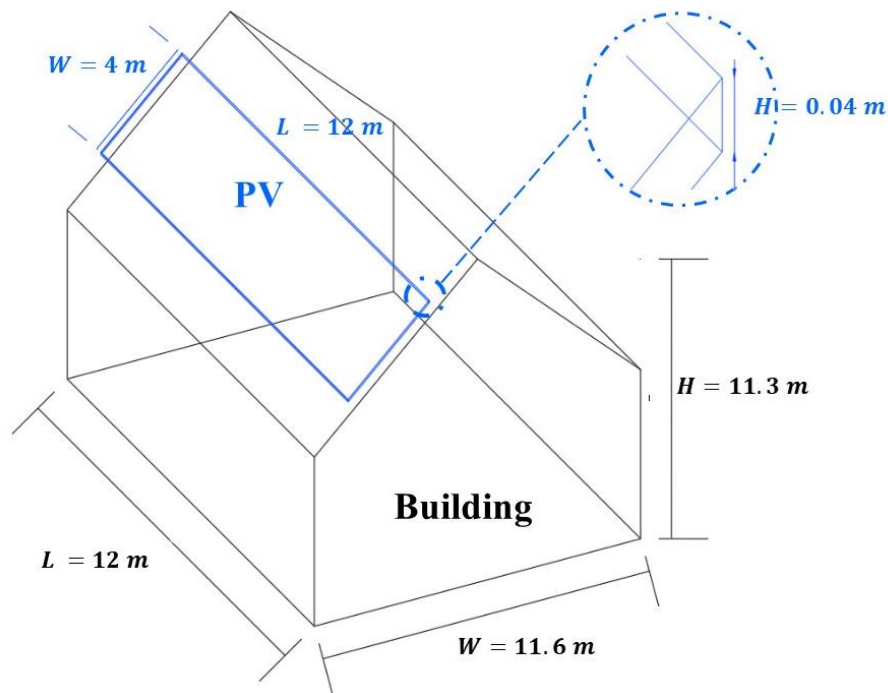
103 *Table 1 Summary of previous CFD studies for the design of BIPVs*

Authors	Type	Dimension	Turbulence model	Investigation
<a href="#">Hemmer, Saad, Popa &amp; Polidori (2017)</a>	BIPV	2D	laminar	Impact of mounting geometry impacts on convection
<a href="#">Wilson and Paul (2011)</a>	BIPV	2D	laminar	
<a href="#">Gan (2009a, 2009b)</a>	BIPV	2D	RNG k-ε turbulence	
<a href="#">Liao et al. (2005)</a>	BIPV/T	2D	k-ε model	Convection beneath/ over PV Impact of:
<a href="#">Jubayer, Karava, &amp; Savory (2010)</a>	BIPV/T	3D	Realizable k-ε / SST k-ω	-Velocity ( <a href="#">Liao, et al., 2005</a> ; <a href="#">Karava et al., 2012</a> ; <a href="#">Zogou &amp; Stapountzis 2012</a> ; <a href="#">Zhang, 2017</a> )
<a href="#">Karava, Jubayer, Savory &amp; Li (2012)</a>	BIPV/T	3D		-Solar radiation ( <a href="#">Liao, 2005</a> ; <a href="#">Zhang, et al., 2017</a> )
<a href="#">Teo, Lee &amp; Hawlader (2012)</a>	PV/T	3D	-	-Wind direction ( <a href="#">Karava, et al., 2012</a> )
<a href="#">Zogou and Stapountzis (2012)</a>	BIPV/T	3D	k-ε model	-PV tilt ( <a href="#">Karava, et al., 2012</a> )
<a href="#">Zhang, Mirzaei and Carmeliet (2017)</a>	BIPV	3D	Standard k-ε model	-Active cooling at backside ( <a href="#">Teo, et al., 2012</a> )
<a href="#">Koyunbaba, Yilmaz &amp; Ulgen (2013)</a>	BIPV	2D	Standard k-ε model	Impact of velocity on thermal behavior
<a href="#">ElSayed (2016)</a>	BIPV	2D	k-ε model	
<a href="#">Mirzaei and Zhang (2015)</a>	BIPV	3D	Standard k-ε model	
<a href="#">Jubayer (2014)</a>	PV	3D	k-ω turbulence	Impact of wind on ground mounted stand-alone PV

104 CFD has been widely applied to reproduce thermal and velocity patterns around tested  
105 panels to find optimal BIPV designs. For example, the critical cavity size was found to be  
106 0.02m by [Wilson and Paul \(2011\)](#), and 0.12-0.15 m and 0.14-0.16 m by [Gan \(2009a\)](#) for multi-  
107 and single module systems, respectively. [Table 1](#) summarizes some of the recent CFD  
108 studies related to the design of BIPVs. As it can be seen in [Table 1](#), most studies were  
109 focused on the cavity, but barely considering the airflow above the cell ([Liao, et al., 2005](#);  
110 [Gan 2009a, 2009b](#); [Wilson & Paul, 2011](#); [Koyunbaba, et al., 2013](#)); although some  
111 investigated the nearfields around, only velocity field was analysed, but no thermal  
112 performance was included ([Jubayer, et al., 2010](#); [Karava, et al., 2012](#)); furthermore, many of  
113 them also simulated the BIPV design in the limited range of variations; for example, only 0-  
114 20 degree wind directions were considered in ([Karava, et al., 2012](#)). Despite of the mentioned  
115 advantageous of CFD techniques in understanding of airflow and temperature fields around  
116 BIPVs, it is computationally impractical to investigate BIPVs with a 3D CFD model under a  
117 wide range of variation considering all influential parameters under more realistic climatic  
118 conditions, therefore, sensitivity tests of integrated PVs to different parameters are required.

119 Therefore, the aim of this study is to develop a high-resolution regression model to predict  
120 BIPVs' cell temperature, including effects of various PV design and climatic scenarios by  
121 taking advantage of a full-scale 3D CFD model, validated with a wind tunnel measurement  
122 study. The simulations of all these climatic and design scenarios are impractical as the  
123 enormous population size required to cover all of them; thus, the goal is to minimize the  
124 intensive computational load of the CFD model by only simulation of the representative  
125 samples of scenarios determined by using Latin Hypercube Sampling method. To calculate  
126 the minimum population size of the sampling method, a sensitivity analysis was initially  
127 conducted to reduce the strip amount of each variable. Finally, a new regression model was  
128 fit to the simulated scenarios and was successfully evaluated in prediction of the BIPV cell  
129 temperature under various climatic and design scenarios. It should be noted that developed  
130 CFD in this study is validated with the experimental data and has a high level of reliability and  
131 accuracy and will be used to evaluate the performance of the new regression models due to  
132 the limitation in access to the realistic experimental data.

133 **2. Methodology**



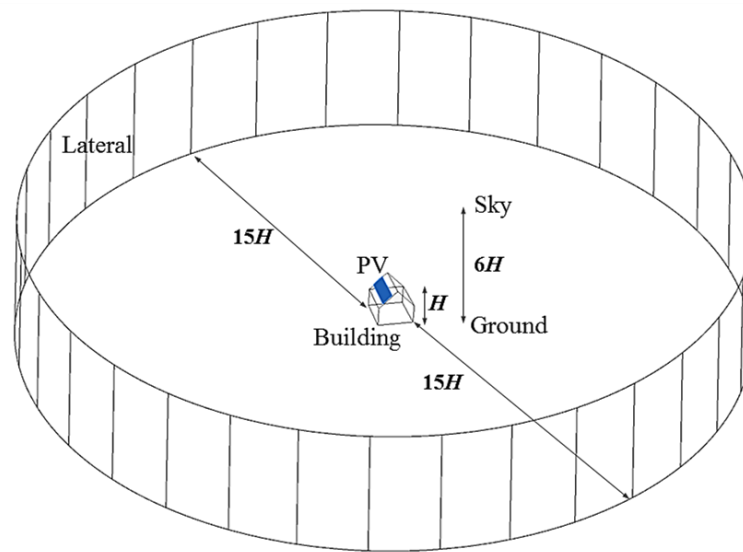
134  
135 *Figure 1 Full-scale BIPV construction*

136 **2.1. CFD modelling**

137 **2.1.1 Microclimatic and BIPV models**

138 The computational model used in this study was developed from a properly validated  
139 CFD model representing BIPV in a wind tunnel experiment (Mirzaei, Paterna & Carmeliet,  
140 2014; Mirzaei & Carmeliet, 2015; Zhang, et al., 2017). The original model was enlarged to a  
141 full-scale BIPVs as shown in Figure 1. After removing the radiation simulator, the wind tunnel  
142 surfaces were then replaced with a cylindrical microclimate, which have a minor deviation in  
143 accuracy from the wind-tunnel model with the rectangular shape (Mirzaei & Carmeliet, 2013),  
144 although with a higher flexibility in capturing the stochastic approaching wind. The lateral wall  
145 of the cylindrical domain was placed far from the building by at least  $15H$  ( $H$  is the height of  
146 the building) as shown in Figure 2 in accordance with the best practice guidelines (Tominaga,  
147 et al., 2008) to ensure the airflow from different directions reaching a fully developed condition.  
148 Also, the lateral wall was divided into multiple planes evenly to be able to assign the  
149 approaching winds from different directions. The sky boundary was settled at  $5H$  above the  
150 building. The basic mesh configuration was generated based on a previous study of (Zhang,  
151 et al., 2017) to achieve a high agreement between CFD simulation and wind tunnel  
152 experiment. The average uncertainty of computational results of developed model from the  
153 measurements was found as 8.0% in overall with 13.2% in the cavity and 7.2% for the  
154 normalized velocity in the upstream region (Zhang, et al., 2017). In terms of the temperature  
155 field, the accuracy of developed computational model exceeds 95% and 90% for temperature  
156 predictions of the BIPV surface and its surrounding airflows, respectively. As only a slight  
157 difference is implemented in the quality of both meshes, the new CFD mesh was considered

158 to perform similarly as the validated wind tunnel mesh.



159  
160 *Figure 2 Model of BIPV with cylindrical microclimatic domain*

161 A PV panel with the dimensions of 12 m × 4 m × 0.04 m ( $L \times W \times H$ ) was integrated to  
162 the pitched roof of a full-size building with dimensions of 12 m × 11.6 m × 11.3 m ( $L \times W \times$   
163  $H$ ). The PV panel covered 50 % of the roof area mounted parallel to the 45 ° inclined roof  
164 with an air cavity of 0.3 m; the fixed cavity distance satisfied the suggested minimum value  
165 to reduce the occurrence of overheating in the BIPV (Gan, 2009a). There are approximately  
166 0.16 million structured cells used to construct the BIPV and its nearby boundary layers (as  
167 seen in [Figure 3](#)) whilst the size of the whole model is about 1.85 million cells in the new  
168 mesh.

### 169 2.1.2 Governing equations

170 ANSYS FLUENT 18.1 was employed for modelling the fluid flow and heat transfer around  
171 the PV panels in this study. Standard wall-function treatment was applied to the boundary  
172 flow around the wall surfaces where dense inflated boundary layer grids were utilized. For all  
173 the simulations, the governing equations were Reynolds Averaged Navier-Stokes (RANS)  
174 scheme with the Standard  $k-\varepsilon$  turbulence model under the steady-state conditions:

$$\frac{\partial}{\partial x_j} (u_j) = 0 \quad (4)$$

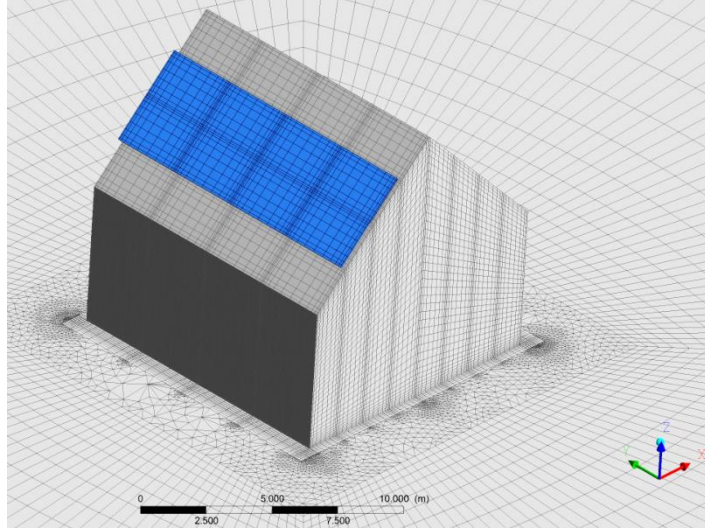


Figure 3 Computational grids of BIPV

175  
176

$$\rho u_j \frac{\partial u_i}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \bar{\tau}_{eff} + \rho \vec{g} \quad (5)$$

177 where  $u$  is the airflow velocity (m/s),  $\rho$  is the air density (kg/m<sup>3</sup>),  $p$  is the pressure (pa).  
178 Subscripts  $i, j, k$  represent the three dimensions (i.e. 1, 2 and 3).  $\bar{\tau}_{eff}$  is the effective stress  
179 tensor, which is given by:

$$\bar{\tau}_{eff} = \mu_{eff} \left[ \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \frac{\partial u_i}{\partial x_i} \bar{I} \right] \quad (6)$$

180 where  $\bar{I}$  is the unit tensor and the effective viscosity,  $\mu_{eff}$  is the sum of the molecular viscosity  
181 ( $\mu$ ) and eddy viscosity ( $\mu_t$ ):

$$\mu_{eff} = \mu + \mu_t \quad (7)$$

182 Term  $\rho \vec{g}$  in Eq. (5) is representing the gravitational force where the buoyancy effect is  
183 reflected. Boussinesq approximation was used to determine the change of air density with  
184 temperature in this term:

$$(\rho - \rho_0)g \approx -\rho_0 \beta (T - T_0) \quad (8)$$

185 where  $\rho_0$  is the constant density under the operating temperature  $T_0$ (K) and  $\beta$  is the thermal  
186 expansion coefficient (K<sup>-1</sup>). As  $\beta(T - T_0)$  is much less than one in this study, the Boussinesq  
187 model is a valid assumption. Moreover, the Standard  $k$ - $\varepsilon$  model was solved by the following  
188 equations for  $k$  and  $\varepsilon$ , respectively:

$$\frac{\partial}{\partial x_i} (\rho k u_i) = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + G_k + G_b - \rho \varepsilon + S_k \quad (9)$$



$$\frac{\partial}{\partial x_i}(\rho \varepsilon u_i) = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_\varepsilon} \right) \frac{\partial \varepsilon}{\partial x_j} \right] + C_{1\varepsilon} \frac{\varepsilon}{k} G_k - C_{2\varepsilon} \rho \frac{\varepsilon^2}{k} + S_\varepsilon \quad (10)$$

189 where  $G_k$ ,  $G_b$  and  $S_k$  are the contributed  $k$  by mean velocity gradients, buoyancy and user-  
 190 defined source, respectively.  $\sigma_k$  and  $\sigma_\varepsilon$  are the Prandtl number of turbulence  $k$  and  $\varepsilon$ ,  
 191 respectively.  $C_{1\varepsilon}$  and  $C_{2\varepsilon}$  are model constants while  $S_\varepsilon$  represents  $\varepsilon$  generated by a user-  
 192 defined source. With this model, the eddy viscosity ( $\mu_t$ ) can be calculated using the  
 193 turbulence kinetic energy and dissipation rate as follows:

$$\mu_t = C_\mu \rho \frac{k^2}{\varepsilon} \quad (11)$$

194 where the default values of model constants are found as  $C_\mu = 0.09$ ,  $\sigma_k = 1.0$ ,  $\sigma_\varepsilon = 1.3$ ,  $C_{1\varepsilon} =$   
 195  $1.44$  and  $C_{2\varepsilon} = 1.92$ . The energy of fluid region was also given by the following governing  
 196 equation:

$$\rho u_j \frac{\partial E}{\partial x_j} = \frac{\partial}{\partial x_j} \left[ (\lambda_f + \lambda_t) \frac{\partial T}{\partial x_j} \right] - p \frac{\partial u_j}{\partial x_j} - \frac{\partial}{\partial x_j} \sum_j \bar{h}_j \vec{J}_j + \frac{\partial u_j}{\partial x_j} \bar{\tau}_{eff} + S_h \quad (12)$$

197 where  $E = \bar{h} - \frac{p}{\rho} + \frac{u^2}{2}$  and  $\bar{h}$  is the sensitivity enthalpy ( $\text{m}^2/\text{s}^2$ ).  $\lambda_f$  and  $\lambda_t$  are the flow thermal  
 198 conductivity and turbulence conductivity. Term  $\sum_j \bar{h}_j \vec{J}_j$  indicates the enthalpy transportation  
 199 due to the species diffusion.  $S_h$  is the user-defined source of energy.

200 Solar radiation was projected into the PV panel in a normal direction using a solar ray  
 201 tracing model, which gave the source term in the energy equation of PV solid region as below:

$$\frac{\partial}{\partial x_j} \left( \lambda \frac{\partial T_c}{\partial x_j} \right) + S_r = 0 \quad (13)$$

202 where  $\lambda$  is the thermal conductivity ( $\text{W}/\text{mK}$ ),  $T_c$  is the PV cell temperature (K) and  $S_r$  is the  
 203 solar load ( $\text{W}/\text{m}^3$ ) added to PV cells.

204 The roof of building was insulated from the ambient environment. As the PV panel  
 205 covered only half of the roof area, the other half was exposed to the sunlight, which may  
 206 cause overheating over the roof surface. The longwave radiative heat loss to the sky was  
 207 then introduced at the exposed surfaces by editing the radiation boundary condition heat flux  
 208 ( $Q'$ ) as:

$$Q' = \varepsilon_{m,r} \sigma (T_{sky}^4 - T_r^4) \quad (14)$$

209 where  $\varepsilon_{m,r}$  is the emissivity of the exposed roof surface and  $\sigma$  is Stefan-Boltzmann constant  
 210  $= 5.670367 \times 10^{-8} \text{ W}/\text{m}^2\text{K}^4$ .  $T_{sky}$  and  $T_r$  are the sky and roof temperatures (K), respectively.  
 211  $T_{sky}$  was set at 285.13 K determined through (Gliah, Kruczek, Gh. Etemad & Thibault, 2011)  
 212 by  $T_{sky} = (\varepsilon_{m,s} T_a^4)^{1/4}$  where  $T_a$  is the air temperature set to be 298.15K in this study, and

213  $\varepsilon_{m,s} \approx 0.836$  is the sky emissivity approximated based on a range of the dew point  
 214 temperature (Chen, Clark, Maloney, Mei & Kasher, 1995).

### 215 2.1.3 CFD setup and boundary conditions

216 Solar load was directly applied to the upward PV surface and the exposed roof. An  
 217 assumption of no participation in solar model was made for the roof area covered by the PV  
 218 panel and other building surfaces. The velocity pattern at the inflow boundaries was given by  
 219 the exponent power law (Tominaga, et al., 2008):

$$U_z = U_{met} \left( \frac{H_z}{H_{met}} \right)^\alpha \quad (15)$$

220 where  $U_z$  is the local wind speed (m/s) at the height of  $H_z$  (m).  $U_{met}$  is the reference wind  
 221 velocity (m/s) measured at the meteorological station where the data are collected at the  
 222 height  $H_{met} = 10$  m.  $\alpha = 0.2$  is the wind shear exponent, which depends on the terrain  
 223 description type and it was taken as a suburban terrain in this study. The vertical profiles for  
 224  $k$  and  $\varepsilon$  were estimated from the corresponding local turbulence intensity ( $I_z$ ) given by the  
 225 following equation (Tominaga, et al., 2008):

$$I_z = 0.1 \left( \frac{H_z}{\delta_G} \right)^{(-\alpha-0.05)} \quad (16)$$

226 where  $\delta_G$  is the boundary thickness of a specific terrain taken as 450 m in this study. An  
 227 acceptable assumption of the local turbulence kinetic energy ( $k_z$ ) was utilized from  $I_z$  for the  
 228 atmospheric boundary layer flow (Tominaga, et al., 2008):

$$k_z = (I_z U_z)^2 \quad (17)$$

229 The local  $\varepsilon_z$  values were then determined through:

$$\varepsilon_z = C_\mu^{1/2} k_z \frac{U_{met}}{H_{met}} \alpha \left( \frac{H_z}{H_{met}} \right)^{(\alpha-1)} \quad (18)$$

230 The air temperature is decreasing along the vertical direction in the troposphere  
 231 (Department of Energy U.S. [DOE], 2016) and thus its profile was given by:

$$T_{a,z} = T_{a,met} - L_\alpha \left( \frac{E_r H_{met}}{E_r + H_{met}} - \frac{E_r H_z}{E_r + H_z} \right) \quad (19)$$

232 where  $T_{a,z}$  (K) is the local air temperature at elevation of  $H_z$  (m) from the ground and  $T_{a,met}$   
 233 (K) is the meteorological air temperature at its calculated height of  $H_{met}$  (m) in meteorological  
 234 station of 1.5 m.  $L_\alpha = -0.0065$  K/m is the vertical temperature gradient and  $E_r = 6356 \times 10^3$  m  
 235 is the radius of the Earth.

236 *Table 2 CFD boundary conditions*

Boundary	Type	Treatment
----------	------	-----------

Ground / building surfaces	Wall	No-slip and adiabatic Not participate in the solar model Adiabatic/Insulated
Back & lateral surfaces of PV	Wall	No-slip and adiabatic Not participate in the solar model Coupled: zero heat generation
Sky/ laterals of the climatic domain	Symmetry	-
Front surface of PV	Wall	No-slip Absorptivity = 0.9 participate in the solar model Coupled: zero heat generation
Inflow	Velocity inlet	Vertical velocity profile Normal to the boundary Vertical $k$ and $\varepsilon$ profiles Vertical temperature profiles participate in the solar model
Outflow	Pressure outlet	Gauge pressure = 0 pa Vertical $k$ and $\varepsilon$ profiles Vertical temperature profiles participate in the solar model

237 *Table 2* shows a summary of boundary conditions defined for the computational model in  
238 FLUENT 18.1 following recommendations by [Mirzaei and Haghghat \(2012\)](#). The absorptivity  
239 of the opaque dark PV surface was taken as 0.9 ([Reagan & Acklam, 1979](#)). SIMPLE algorithm  
240 was employed to solve the transport equations while all the transport equations were  
241 discretized with the second-order upwind scheme except the pressure, which was discretized  
242 with the second-order scheme. The convergence criterion was set as  $10^{-6}$  for the energy  
243 equation while the values were set as  $10^{-4}$  for the continuity, momentum and turbulence  
244 equations.

## 245 2.2. Sampling and sensitivity analysis

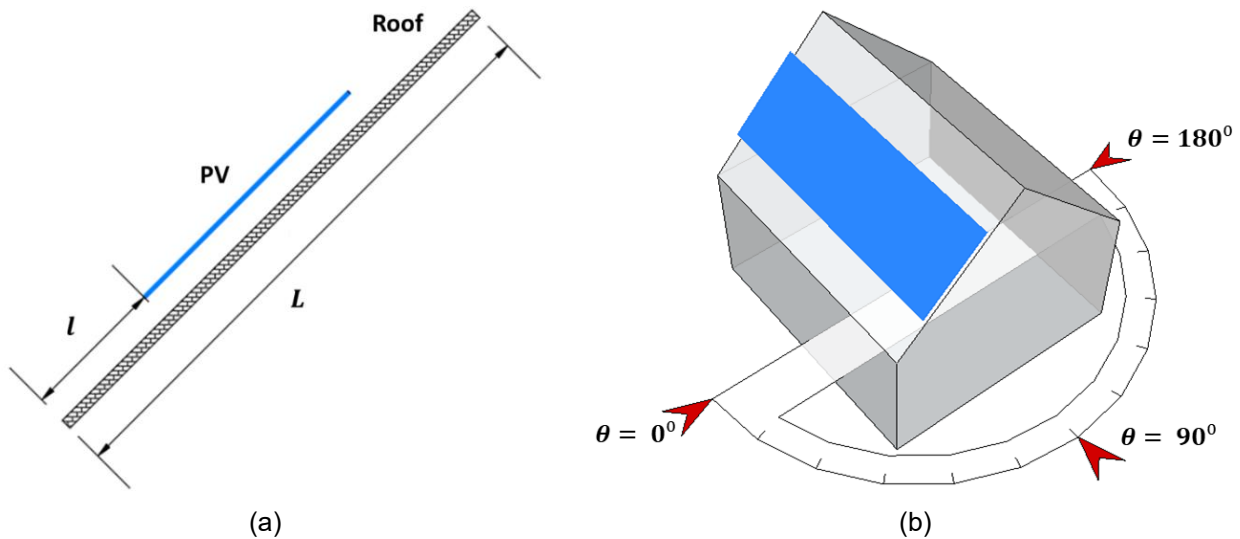
246 First, the thermal performance of PV panels was presented using the temperature  
247 difference between the cell and ambient (as the reference) temperatures. As a preliminary  
248 test, the influence of panel arrangement (stepped or flat) on its thermal performance was  
249 found to be insignificant, and thereby, only the flat PV arrangement was chosen to be  
250 simulated. Moreover, a new variable, PV position index ( $PI$ ), was introduced to represent the  
251 relative location of the PV panel as the ratio of distance between the bottom and top edges  
252 of the PV panel over the roof width as seen in [Figure 4a](#):

$$PI = l/L \quad (20)$$

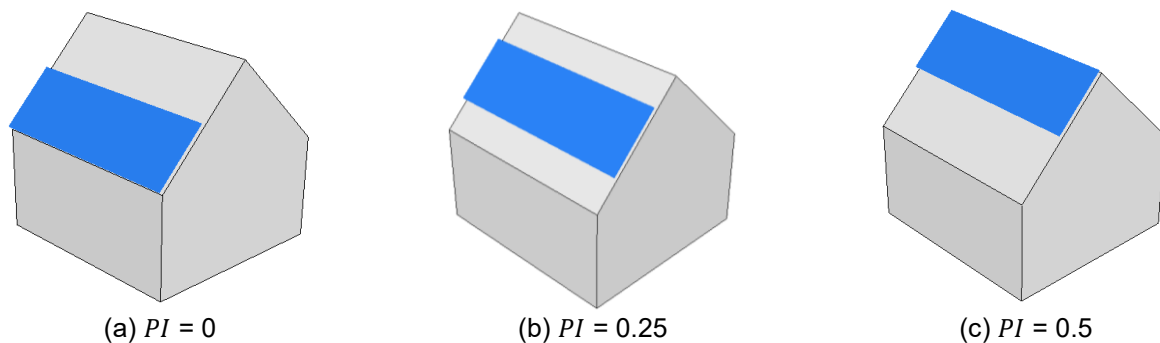
253 where  $l$  is the distance between the bottom and top edges of the PV panel.  $L$  is the width of  
254 the roof. In this study, three relative positions for the PV panel over the roof were considered,  
255 including the bottom ( $PI = 0$ ), middle ( $PI = 0.25$ ) and top ( $PI = 0.5$ ) as displayed in [Figure 5](#).

256 Then, the investigation was designed to cover ranges of different climatic variables,  
257 including solar irradiance, wind direction and wind speed. A standard range of wind speed in  
258 Northern hemisphere is between 0-20 m/s with a highest frequency band lies in the range of

259 0-5m/s (Vautard, Cattiaux, Yiou, Thépaut & Ciais, 2010). However, the lowest wind speed  
 260 was set as 0.5m/s rather than 0m/s, considering slow CFD convergence and  $k-\varepsilon$  turbulence  
 261 weakness in low Reynolds conditions. Furthermore, the solar irradiance was assumed to be  
 262 uniformly distributed from 80 W/m<sup>2</sup> to 1,200 W/m<sup>2</sup> (King, et al., 2004). The stochastic relative  
 263 wind angle was treated from  $\theta = 0^\circ$  to  $\theta = 180^\circ$ , where  $\theta = 0^\circ$  represents the direction of the  
 264 BIPV orientation as shown in Figure 4b.



265 Figure 4 Schematic description of a) PV position index ( $PI$ ) and b) relative wind angle  
 266 ( $\theta$ ) Table 3 demonstrates the detailed value ranges for each variable. As it can be seen, there  
 267 are numerous random permutation and combination of PV positions, solar radiation, wind  
 268 direction and wind speed. Thus, it is practical to perform a sampling procedure to find only a  
 269 limited number of scenarios required to be simulated with CFD that can technically represent  
 270 the entire range of climatic conditions and PV positions. Before selecting samples through  
 271 Latin Hypercube Sampling (LHS) method (Petropoulos & Srivastava 2016), a sensitivity test  
 272 was conducted to determine the minimum strips of each microclimate variable, so that a  
 273 smaller population size can be determined for the simulation. Latin Hypercube Sample  
 274 method is a form of stratified sampling that applied to multiple variables. In principle, the  
 275 method is to independently stratify each variable into  $N$  intervals with equal probability of  $1/N$   
 276 and then to pick only one random sample point in every partition for each variable (Fang, Li  
 277 & Sudjianto, 2005). It provides significant benefits in terms of sampling efficiency and  
 278 computer processing time.



279 Figure 5 Schematic plot of the relative positions of PV panel over the roof and their corresponding  $PI$

280  
281

values

Table 3 Variable ranges and distributions for the sampling procedure

PV position ( $PI$ )					
Bottom	Middle			Top	Distribution
0	0.25			0.5	Uniform
Solar irradiance ( $G_t$ ) & Relative wind angle ( $\theta$ )					
	Left bound		Right bound		Distribution
$G_t$	80 W/m <sup>2</sup>		1200 W/m <sup>2</sup>		Uniform
$\theta$	0°		180°		Uniform
Wind speed ( $U$ )					
Range	0.5 ~ 1 m/s	1 ~ 5 m/s	5 ~ 9 m/s	9 ~ 13 m/s	13 ~ 20 m/s
Frequency	0.0562	0.6387	0.2486	0.0456	0.0109

282 The benchmark case of the sensitivity analysis was defined as a PV panel mounted at  
 283 the middle of the roof area ( $PI = 0.25$ ) with a solar irradiance of 700 W/m<sup>2</sup> projected onto the  
 284 surface while the wind was approaching opposite from the PV's orientation ( $\theta = 180^\circ$ ) at a  
 285 speed of 3 m/s. Table 4 lists the tested gaps of each variable for the parametric study of their  
 286 impacts on the PV cell temperature ( $T_c$ ) and PV surface convective heat transfer ( $q_c$ ). For  
 287 example, scenarios with solar irradiance of 750, 740 and 730 W/m<sup>2</sup> were tested to determine  
 288 the sensitivity of  $T_c$  related to  $G_t$  while the critical interval was decided as one of the three  
 289 studied gaps (i.e. 50, 40 and 30 W/m<sup>2</sup>) with respect to 700 W/m<sup>2</sup> in benchmark case as  
 290 seen in Table 4.

291 Table 4 Benchmark case and parametric controls for the sensitivity analysis

	$G_t$ (W/m <sup>2</sup> )	$U$ (m/s)	$\theta$ (°)
Benchmark	700	3	180
Gap to benchmark	50	2.5	33.75
	40	2	22.5
	30	1.5	11.25

292 Hence, the sample size ( $n$ ) can be determined by (LeBlanc, 2004):

$$n = \frac{Nz_c^2 p_s(1 - p_s)}{d^2(N - 1) + z_c^2 p_s(1 - p_s)} \quad (21)$$

293 where  $N$  is the population size,  $z_c$  is the critical value at a given confidence level,  $p_s$  is the  
 294 sample proportion and  $d$  is the error margin. In this study, the confidence level and the margin  
 295 error were assumed to be 95 % and 5 %, respectively; this guaranteed 95 % of the true value  
 296 of population with an allowance of random error up to 5 %. The critical value for the  
 297 confidence level of 95 % is 1.96 while the value of  $p_s$  is usually as 0.5 to ensure that the  
 298 sample size is large enough to reflect the whole population (LeBlanc, 2004).

299 After deciding the sample size, Latin Hypercube Sampling method (Petropoulos &  
 300 Srivastava, 2016) was used to generate evenly distributed random numbers from 0 to 1 for  
 301 each investigated variable. These random numbers were then mapped into the range of each  
 302 variable to fit their corresponding real values. For example, a random number of 0.773 within  
 303 the range of 0-1 was indexed to 786 W/m<sup>2</sup> from 80-1200 W/m<sup>2</sup> solar irradiance range.

### 304 2.3. Multivariable fitting

305 After obtaining all sample results, a new regression of the cell temperature versus  
 306 microclimate conditions and PV positions was developed with a nonlinear correlation using  
 307 MATLAB none-linear-fit (NLINFIT) function. The benchmark formats for the solar irradiance  
 308 and wind speed in the new regression were referred to their formats in accordance with the  
 309 previous empirical models (i.e. NOCT and SNL). Moreover, the formats of  $PI$  and  $\theta$  were  
 310 proposed with a preliminary analysis of the simulation data. Curve fitting tool in MATLAB was  
 311 employed to obtain a rough initial guess of coefficients for NLILFIT function and then to  
 312 identify an optimum coefficient value for each term with a given explicit function format.

313 The results of simulations and the regression model were compared using several  
 314 metrics to assess the goodness of fitting, including the coefficient of determination ( $R^2$ ), the  
 315 adjusted coefficient of determination (*Adjusted R<sup>2</sup>*) and the root mean squared error (*RMSE*):

$$R^2 = 1 - \frac{\sum_{i=1}^n (Y_i - \hat{Y}_i)^2}{\sum_{i=1}^n (Y_i - \bar{Y})^2} \quad (22)$$

$$Adjusted R^2 = 1 - (1 - R^2) \frac{n - 1}{n - k_{coeff}} \quad (23)$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2} \quad (24)$$

316 where  $Y_i$  and  $\hat{Y}_i$  are the observed (simulated) and predicted values of each sample,  
 317 respectively.  $\bar{Y}$  is the mean of all  $Y_i$  and  $k_{coeff}$  is the total number of coefficients to be  
 318 determined in the regression. The values of  $R^2$  and *Adjusted R<sup>2</sup>* are within the range of 0-1  
 319 while a value closer to 1 means the regression covers more variability, thereby, is more  
 320 successful in fitting to the dataset. Inversely, a smaller value of *RMSE* is expected for a better  
 321 prediction.

### 322 2.4. Qualification metrics for regression validation

323 Extra 40 cases (more than 10 % of sample size without being used to develop the  
 324 multivariable regression model) randomly selected by Latin Hypercube Sampling were  
 325 simulated to assess the validity of proposed regression. Two qualification metrics were  
 326 introduced in this stage, the relative gap ( $E_1$ ) and the fraction of predictions within a factor of  
 327 two of observations (*FAC2*):

$$E_1 = \frac{1}{n} \sum_{i=1}^n \left| \frac{Y_i - \hat{Y}_i}{Y_i} \right| \quad (25)$$

$$FAC2 = \frac{1}{n} \sum_{i=1}^n n_i \text{ with } n_i = \begin{cases} 1 & \text{if } 0.5 \leq \frac{\hat{Y}_i}{Y_i} \leq 2.0 \\ 0 & \text{else} \end{cases} \quad (26)$$

328 *FAC2*, as the one of the most robust qualification metrics, with a value closer to 1 indicates  
 329 a perfect matching between predictions and the observations while a *FAC2* greater than 0.5  
 330 can be claimed as good enough criterion (Chang & Hanna, 2004).

### 331 3. Results

#### 332 3.1. Sensitivity analysis and sampling results

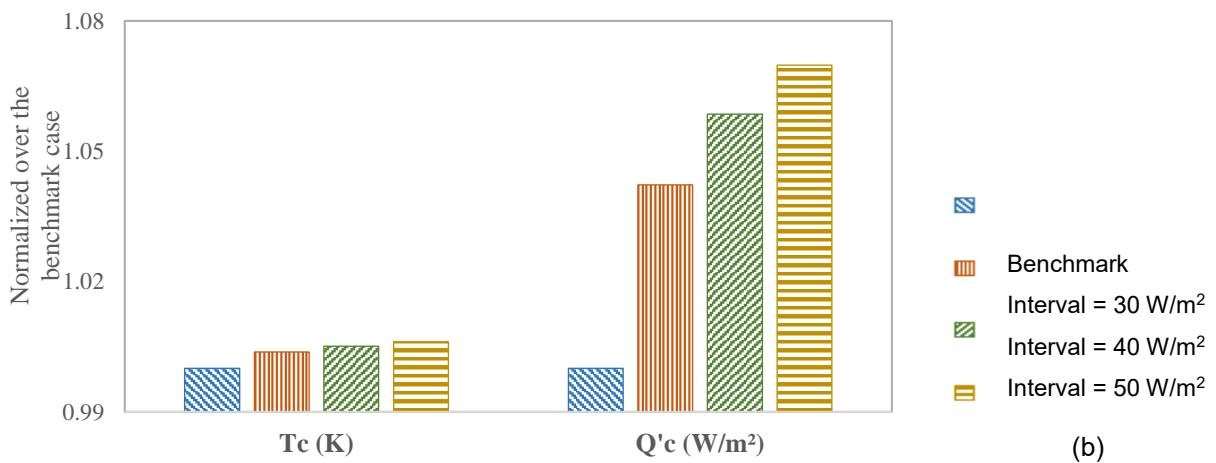
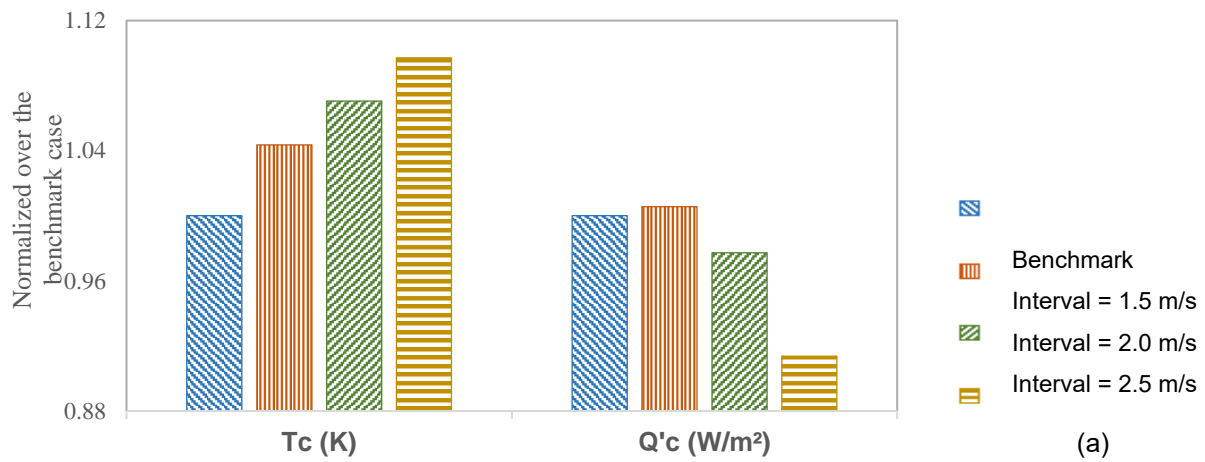
333 Normalized values over the results of the benchmark case were used to illustrate the  
 334 sensitivity analysis. Therefore, the normalized PV cell temperature ( $T_c$ ) and surface  
 335 convective heat flux ( $Q'_c$ ) for the benchmark case were defined as unity as seen in [Figure 6](#).  
 336 It is clear that the deviation of the normalized value of tested cases over unity is increasing  
 337 with the interval growth of the tested variable when compared to the benchmark case. For  
 338 example, in [Figure 6a](#), deviations of 0.04 and 0.01 of  $T_c$  and  $Q'_c$ , respectively, were found for  
 339 the case with a same PV position, similar solar irradiance and relative wind angle to the  
 340 benchmark case although with having a different wind speed with a gap of 1.5 m/s. When  
 341 increasing the interval to 2.5 m/s, the differences of  $T_c$  and  $Q'_c$  elevated to 0.1 and 0.09,  
 342 respectively. A critical interval value was defined as the deviation of a case over the  
 343 benchmark case equal or slightly less than 0.05 in accordance with the margin error of the  
 344 sampling procedure. It is noteworthy that the increase of the critical interval contributes to the  
 345 reduction of strip amount for each variable in the specific range and thus further leads to a  
 346 smaller population size for the simulations. Thereby, the critical interval of wind speed was  
 347 determined as 1.5 m/s.

348 Similarly, the critical interval for the solar irradiance was found to be 30 W/m<sup>2</sup> considering  
 349 the change of  $Q'_c$  as shown in [Figure 6b](#). As for the relative wind angle, seen in [Figure 6c](#),  
 350 both normalized  $T_c$  and  $q_c$  difference for cases with interval of 11.25° and 22.5° met the  
 351 sensitivity requirement. To reduce the population size, 22.5° was then selected as the critical  
 352 interval for the variable  $\theta$ . Therefore, the minimum required numbers of strips for the solar  
 353 irradiance, wind velocity and relative wind angle were calculated as 38, 13 and 9, respectively.  
 354 Adding three installations of the BIPV, the sampling population size was identified as 13,338  
 355 while the minimum sample size was found as 374 according to [Eq. 21](#).

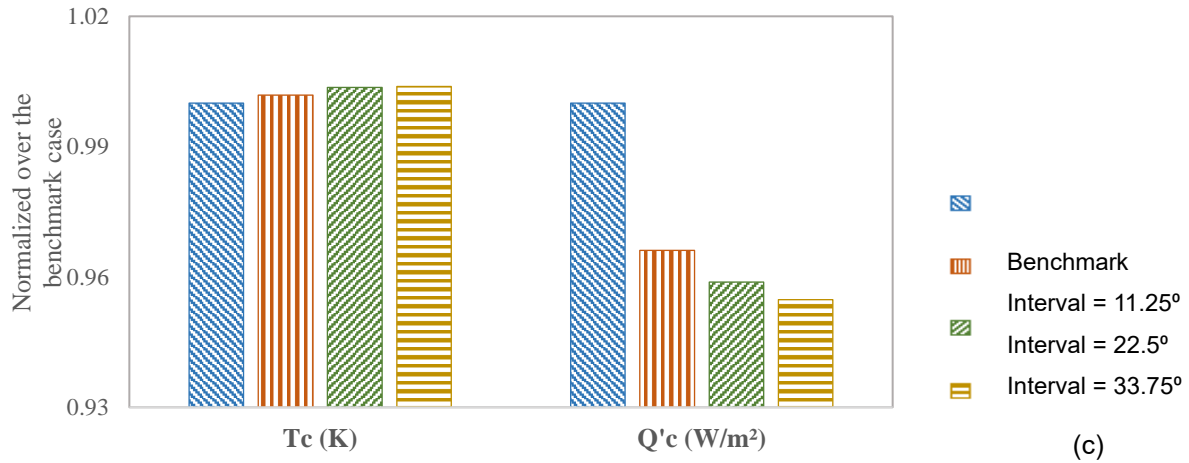
#### 356 3.2. Simulation results of sample population

357 Steady state simulations of all 374 sample cases were conducted until their  
 358 convergences were guaranteed. The value of each variable (including wind speed, solar  
 359 irradiance, relative wind angle and PV position) was unique throughout all the samples as

360 selected by Latin Hypercube Sampling method. This implies that there was no two samples  
 361 with the same exact value for each variables. Therefore, comparisons were provided for  
 362 samples to investigate the impact of different variables through a parametric study that values  
 363 of the controlled variables were similar rather than same (only with differences less than 5 %  
 364 or within the range of critical interval). For example, to explore the impact of solar irradiance,  
 365 samples # 51 and #108 were selected with very different tested variable of  $G_t$  as  $293 \text{ W/m}^2$   
 366 comparing to  $1,131 \text{ W/m}^2$ , respectively. For the rest of variables,  $PI$  is the same ( $PI = 0.25$   
 367 for both samples) as a parametric study required; however, variable  $U$  is  $3.98 \text{ m/s}$  and  
 368  $3.95 \text{ m/s}$  and  $\theta$  is  $46^\circ$  and  $53^\circ$  for both samples, respectively due to sample limitation. The  
 369 comparisons were performed through the temperature distribution plot as seen in [Figure 6-8](#).

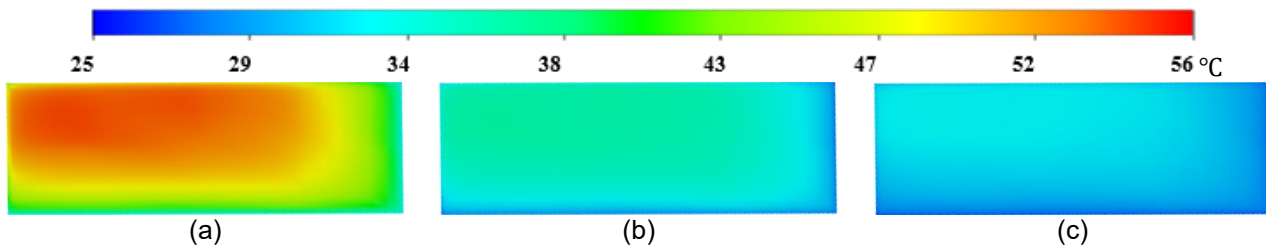




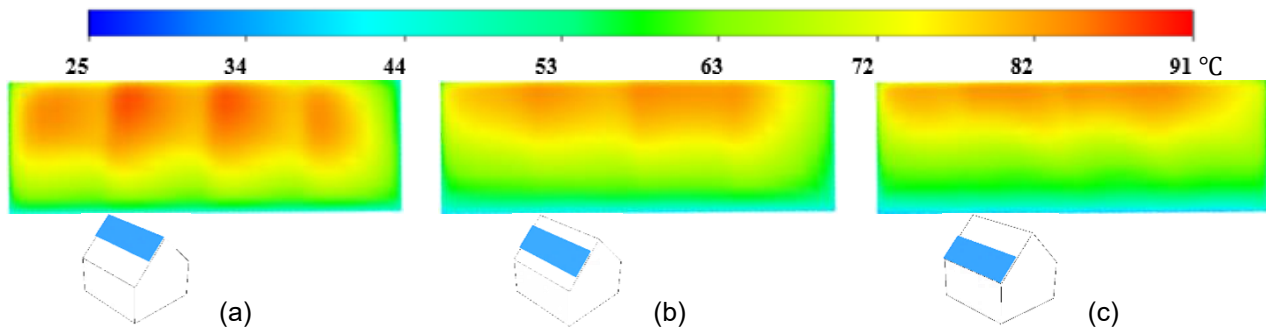


370 Figure 6 Normalized PV cell temperature ( $T_c$ ) and surface convective heat flux ( $Q'_c$ ) over the benchmark  
 371 case results for the sensitivity analysis of a) wind speed of  $U$ ; b) solar irradiance of  $G_t$  and c) relative  
 372 wind angle of  $\theta$

373 The solar irradiance ( $G_t$ ) was found as the most important factor as it was similarly  
 374 reflected in both existing empirical regressions (i.e. SNL and NOCT models). Based on the  
 375 SNL model, the PV temperature decreases with increase of wind speed ( $U$ ), however, the  
 376 decreasing gradient becomes close to zero when  $U$  approaches to high values. The  
 377 simulated results depicted consistent tendencies with SNL model's predictions. Figure 7  
 378 shows a comparison of the combined effect of the solar irradiance and wind speed. In these  
 379 three selected samples, the highest PV temperature occurred under the scenario with a high  
 380 solar irradiance and a low wind speed. The importance of parameters  $G_t$  and  $U$  can be clearly  
 381 observed by comparing Figure 7a versus Figure 7b and Figure 7a versus Figure 7c.



382 Figure 7 Temperature contour of the BIPV under scenarios of a) a high  $G_t$  with a low  $U$ ; b) a high  $G_t$  with  
 383 a high  $U$  and c) a low  $G_t$  with a low  $U$

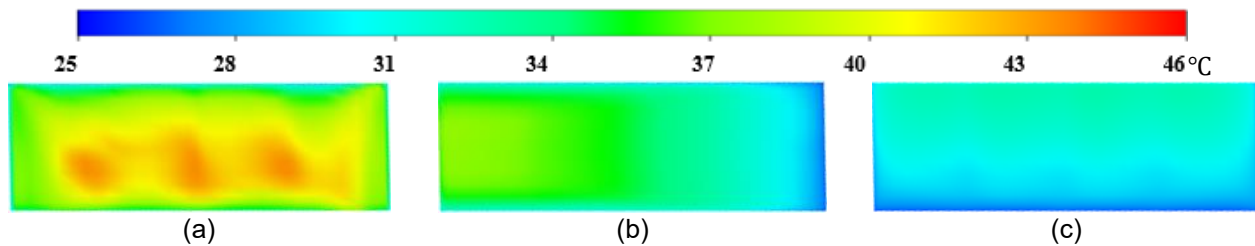


384 Figure 8 Temperature contour of the BIPV placed at positions of a)  $PI = 0.5$ ; b)  $PI = 0.25$  and c)  $PI = 0$

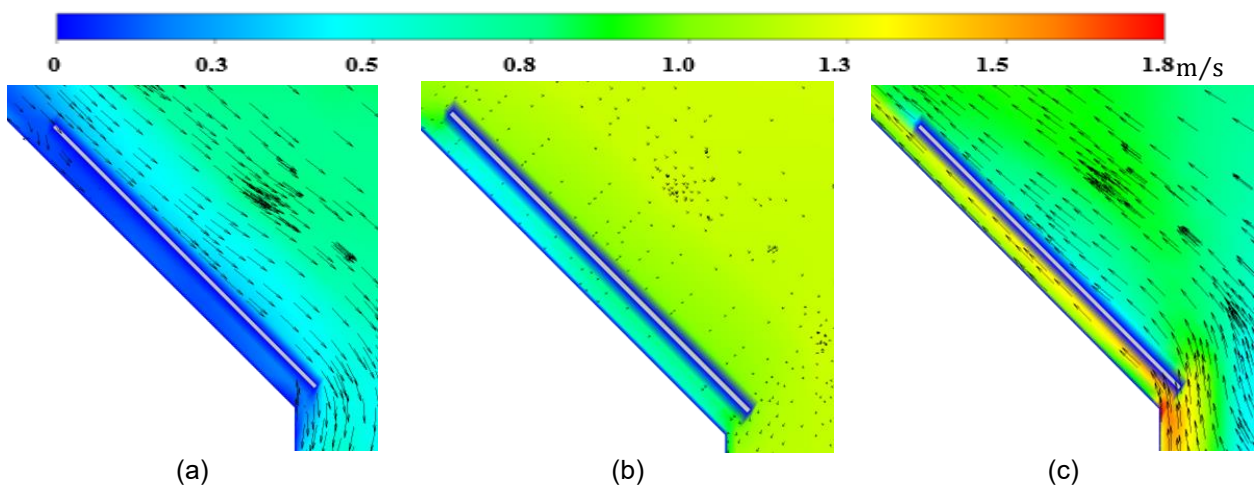
385 Figure 8 compares the impact of different PV positions ( $PI$ ) when the PV panels were  
 386 exposed to a high solar radiation with a low speed wind approaching almost parallel to the  
 387 direction of PV's orientation. As it can be seen, hot spot occurs at all three cases, however,

388 when the PV is placed closer to the top edge of the roof ( $PI = 0.5$ ), the hot spot region  
 389 becomes larger. It is noteworthy to specify that the solar irradiance in the scenario of *Figure*  
 390 *8a* ( $980 \text{ W/m}^2$ ) was even lower than that of for *Figure 8b* ( $1,122 \text{ W/m}^2$ ) and *Figure 8c*  
 391 ( $1,151 \text{ W/m}^2$ ). This can be explained by the fact that the air becoming hotter when passing  
 392 through the exposed hot roof surface and reaching to the top edge position.

393 *Figure 9* and *Figure 10* compare the impact of the relative wind angle ( $\theta$ ). The  
 394 investigated PV panels in both figures were placed at  $PI = 0$  where a clear difference in  
 395 temperature contours can be observed between *Figure 9/10a*, *Figure 9/10b* and *Figure 9/10c*.  
 396 Temperature gradient is more likely to be distributed in the streamwise direction in *Figure 9*.  
 397 As depicted in *Figure 10a*, air is moving downward when wind approaches from backside  
 398 ( $\theta = 174^\circ$ ) and, therefore, a high temperature is captured at a relatively low position as seen  
 399 in *Figure 9a*. In contrast, a higher temperature can be seen at the upper part of the PV surface  
 400 in *Figure 9c* when air is moving upward as seen in *Figure 10c*. A higher risk of overheating is  
 401 also found when wind approaches from the backside of the PV panel, which means the  
 402 panels are at the leeward where surrounded by a relatively calm air. This is supported by the  
 403 airflow pattern shown in the *Figure 10a*. With a similar climatic wind speed, a lower local  
 404 velocity is observed for larger relative wind angles (e.g.,  $\theta = 174^\circ$  compared to  $\theta = 99^\circ$  or  
 405  $\theta = 4^\circ$ ). Moreover, a complex hybrid impact of the relative wind angle and PV index can be  
 406 seen in *Figure 9*, which is further discussed in *Section 3.3*.



407 *Figure 9* Temperature contour of the BIPV under scenarios of a)  $\theta = 174^\circ$ ; b)  $\theta = 99^\circ$  and c)  $\theta = 4^\circ$   
 408



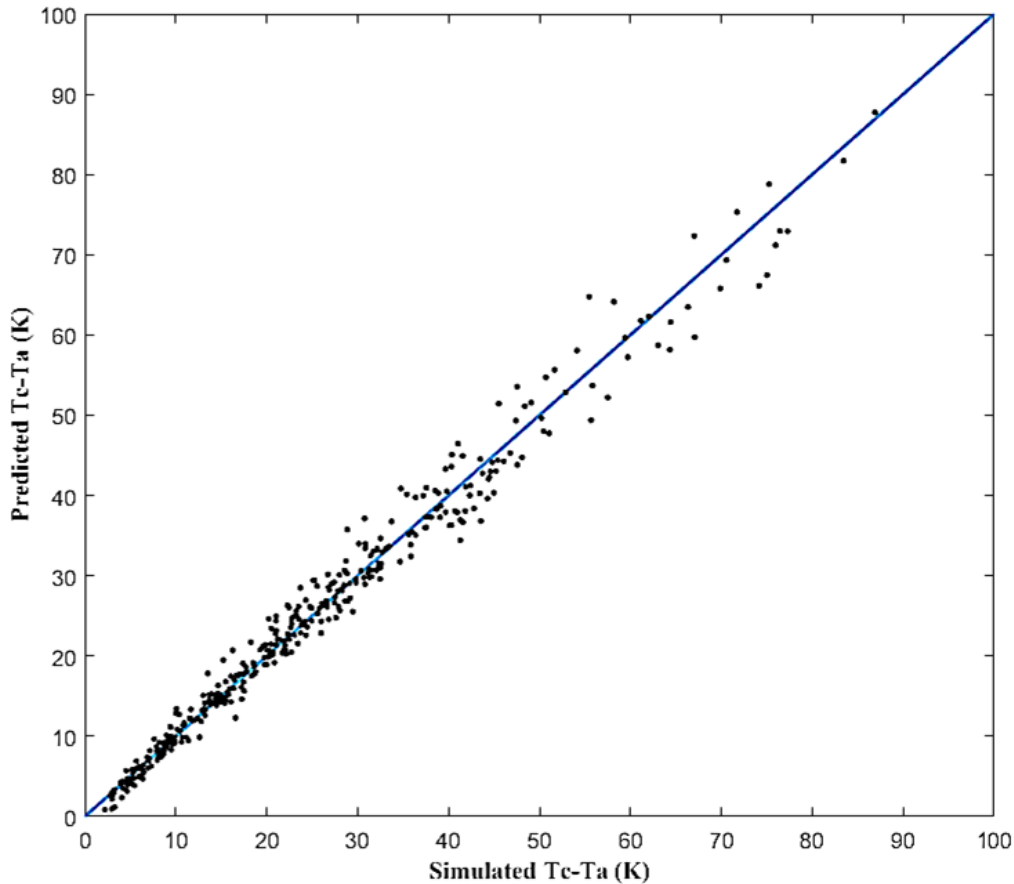
409 *Figure 10* Velocity contour and vector plot of the airflow around BIPV under scenarios of a)  $\theta = 174^\circ$ ; b)  
 410  $\theta = 99^\circ$  and c)  $\theta = 4^\circ$

411 **3.3. New regression equation from simulations**

412 As mentioned in [Section 2.2](#), the PV cell temperature was reported to be linearly related  
 413 to the air temperature in all previous models. Hence, the new regression model was  
 414 developed to predict temperature difference between  $T_c$  and  $T_a$ . Considering the tendency of  
 415 temperature difference influenced by each variable, solar irradiance ( $G_t$ ) was found as the  
 416 most critical factor consistent with the expectations whilst the weighting of the PV position  
 417 index ( $PI$ ) was observed to be the lowest. The format of the new regression model was thus  
 418 proposed as:

$$T_c - T_a = a_1 G_t^{a_2} \cdot e^{(a_3 U^{a_4} + a_5 U + a_6 \theta + a_7 PI)} + a_8 \theta \cdot PI + a_9 \quad (27)$$

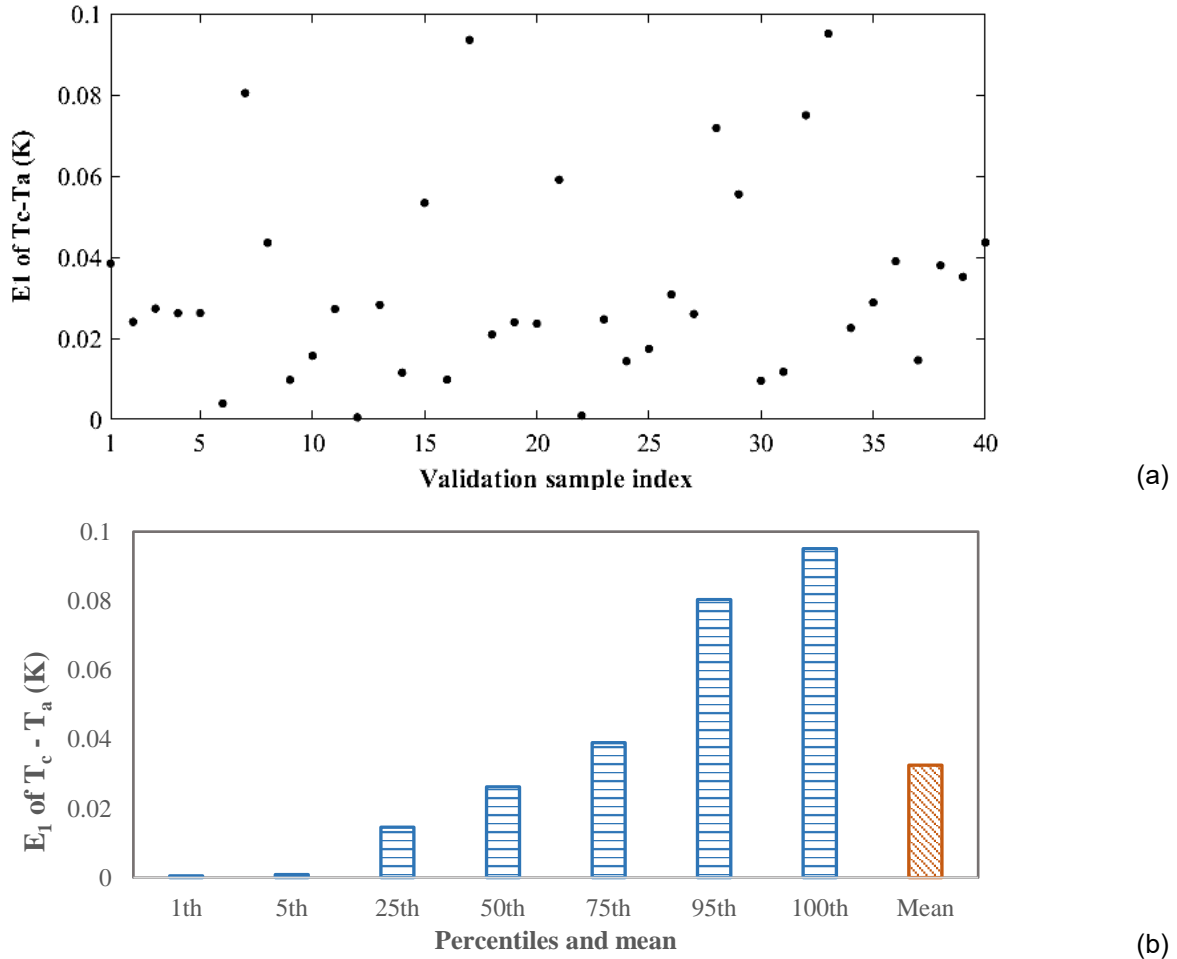
419 where  $a_n$  are the constant coefficients and after optimization by NLINFIT function in MATLAB  
 420 were found as  $a_1 = 0.2743$ ,  $a_2 = 0.8989$ ,  $a_3 = -0.9832$ ,  $a_4 = 0.5777$ ,  $a_5 = 0.181$ ,  $a_6 =$   
 421  $0.0018$ ,  $a_7 = -0.0118$ ,  $a_8 = -0.0424$ ,  $a_9 = -0.9566$ .



422  
 423 *Figure 11 Prediction of  $T_c - T_a$  by the proposed regression model (black dots) and simulation results*  
 424 *(blue line)*

425 The validity of the proposed regression model has been evaluated as displayed in [Figure](#)  
 426 [11](#). The predicted results distribute evenly around the blue straight line (with a gradient of  
 427 unity), indicating the simulated values. The goodness of fitting evaluated from [Eq. 22-24](#) was  
 428 reported as  $R^2 = 0.9813$ ,  $Adjusted R^2 = 0.9809$  and  $RMSE = 2.3674$ . Therefore, a high fitting  
 429 quality was concluded from a high Adjust  $R^2$  of 0.9809. As RMSE has the same unit as the

430 dependent variable, the value of 2.3674 K can be regarded as a small value in accordance  
 431 with the range of  $T_c - T_a$  defined between 0 K and 100 K.



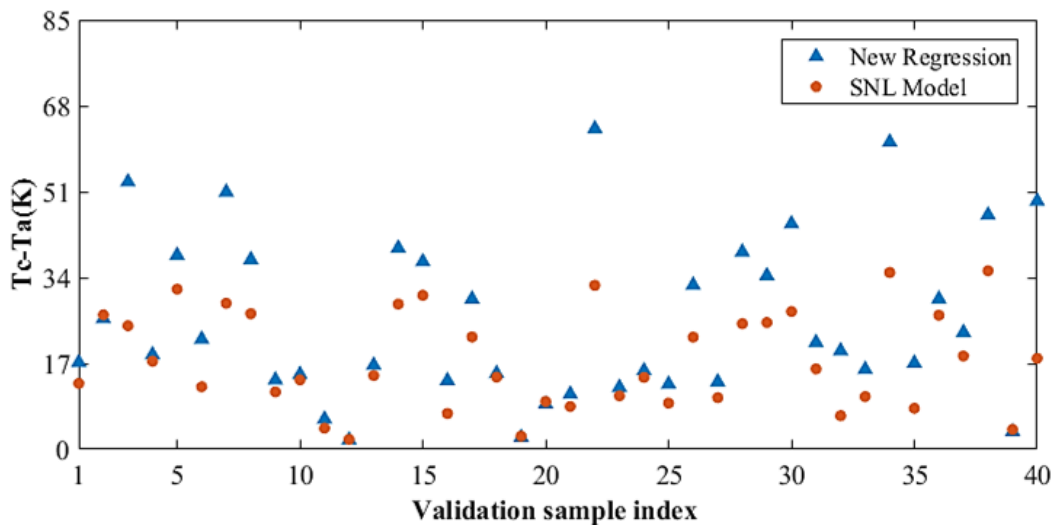
432 Figure 12  $E_1$  of  $T_c - T_a$  between predictions by proposed regression model and simulations for a) each  
 433 sample case and b) different percentile and the mean value

### 434 3.4. Validation of new regression

435 Figure 12 plots the relative gap of  $T_c - T_a$  between the prediction by proposed new  
 436 regression model and the CFD simulation of 40 extra sample scenarios for the validation  
 437 purpose, which were not initially included in the fitting procedure. Approximately 80% of 40  
 438 cases were found to have a small gap (less than 0.05) between predictions and simulations  
 439 while the 75<sup>th</sup> percentile of  $E_1$  (see Eq. 25) was around 0.039. The mean value of  $E_1$  was  
 440 found as 0.0325, slightly higher than the median value of 0.0262. Larger  $E_1$  occurred under  
 441 the condition where a low speed wind was approaching from backside of the BIPV with a  
 442 large  $\theta$  while the panel was placed closer to the top edge. For example, under a scenario of  
 443  $PI = 0.5$ ,  $G_t = 201 \text{ W/m}^2$ ,  $\theta = 174^\circ$  and  $U = 0.55 \text{ m/s}$ , the predicted temperature difference  
 444 between the PV cell and ambient was 23.10K comparing to the simulated value of 19.49 K;  
 445  $E_1$  was thereby calculated as 0.0749, which was relatively high among 40 sample cases. The  
 446 possibility of occurrence of extreme conductions (e.g.  $E_1$  exceeds 0.9) was within 5%.  
 447 Moreover, the  $FAC2$  value (see Eq. 26) of 40 validation cases was equal to 1. Therefore, it  
 448 can be concluded that the proposed regression model is highly valid to predict the simulated

449 cell temperature of PV panels.

450 *Figure 13* presents the predicted  $T_c - T_a$  by the new regression and SNL model. For  
451 individual cases that the SNL model delivers a higher temperature difference with, the  
452 prediction given by the new regression model would also be relatively higher. In general, an  
453 obvious underestimation of  $T_c$  by the SNL model can be observed when comparing to the  
454 prediction by the new regression model. The  $R^2$  of results by two models is approximately  
455 0.4760, indicating rather big deviations. A potential reason of this phenomena is due to the  
456 fact that the assumption of open-rack installed PV panels with sufficient cooling in the SNL  
457 model is not always realistic. Also, as the new proposed regression model was obtained from  
458 computational simulations, the relative discrepancies from the experimental measurements  
459 should be taken into account.



460  
461

*Figure 13 Predicted  $T_c - T_a$  by the new proposed regression and SNL models*

#### 462 4. Conclusion

463 In summary, a new regression model for prediction of the BIPV cell temperature was  
464 proposed from a series of full-scaled BIPV CFD simulations. The ambient temperature, solar  
465 irradiance, wind speed, relative wind angle and PV position (PV position index) over the roof  
466 were taken into account as the influential parameters on the PV cell temperature. Using the  
467 sensitivity analysis and Latin Hypercube Sampling approach, the minimum size of the  
468 population and sampling size were identified as 13,338 and 374, respectively. Thus,  
469 simulations of sample cases were conducted to qualify and quantify the relationship between  
470 climatic variables, PV position and PV cell temperature. The simulation results demonstrated  
471 the following primary relationships among each variable and  $T_c - T_a$ :

- 472 ➤ It was found that the solar irradiance and wind speed were of the most important factors  
473 in determining the BIPV cell temperature while the PV position was the least.
- 474 ➤ Higher temperature differences were presented under high solar irradiances.
- 475 ➤ The PV panel can be cooled down against strong wind conditions. However, there existed  
476 a critical value in which, if the wind speed exceeded, the growth of cooling effect would

477 become weak.

478 ➤ The impacts of relative wind angle and wind direction were found to be complex while the  
479 possibility of a hybrid influence of two variables was observed.

480 ➤ Based on the simulation results and observed phenomena, the regression model was  
481 proposed with satisfying substantial indicators of goodness-of-fit. 80 % of validation cases  
482 were found successfully predicting  $T_c - T_a$  with a relative error of less than 5 %.

483 The main aim of this study was to provide a systematic way to predict the BIPV performance  
484 rather than using the existing empirical correlations. Thus, the future work will be focused on  
485 development of experimental measurement set ups to measure the certainty of the regression  
486 model proposed in this study.

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## 490 **References**

- 491 Assoa, Y. B., Gaillard, L., Ménézo, C., Negri, N., & Sauzedde, F. (2018). 'Dynamic prediction of a  
492 building integrated photovoltaic system thermal behaviour', *Applied Energy*, 214: 73-82.
- 493 Bagatelos, N., & Henson, J. W. C. (2012). "BIPV Facades Reconsidered: Mid-rise and High Rise  
494 Applications." In *the Third Building Enclosure Science & Technology Conference (BEST)*. Atlanta,  
495 Georgia, USA.
- 496 Bahaj, A. S. (2003). 'Photovoltaic roofing: issues of design and integration into buildings', *Renewable  
497 Energy*, 28: 2195-204.
- 498 Bramanti, O. (2015). *Solar Power Conversion - Engineering, Technology, Financing* (Youcanprint).
- 499 Chang, J. C., & Hanna, S. R. (2004). 'Air quality model performance evaluation', *Meteorology and  
500 Atmospheric Physics*, 87: 167-96.
- 501 Chen, B., Clark, D., Maloney, J., Mei, W. & Kasher, J. (1995). "Measurement of night sky emissivity in  
502 determining radiant cooling from cool storage roofs and roof ponds." In *Proceedings of the  
503 National Passive Solar Conference*, 310-13. AMERICAN SOLAR ENERGY SOCIETY INC.
- 504 D'Orazio, M., Perna, C. D. & Giuseppe, E. D. (2014). 'Experimental operating cell temperature  
505 assessment of BIPV with different installation configurations on roofs under Mediterranean  
506 climate', *Renewable Energy*, 68: 378-96.
- 507 Department of Energy U.S. (2016). "EnergyPlus Engineering Reference." In.
- 508 Elkarmi, F., & Abu-Shikhah, N. (2012). *Power System Planning Technologies and Applications:  
509 Concepts, Solutions and Management* (IGI Global: Hershey, PA, USA).
- 510 ElSayed, M. S. (2016). 'Optimizing thermal performance of building-integrated photovoltaics for  
511 upgrading informal urbanization', *Energy and Buildings*, 116: 232-48.
- 512 Energy Information Administration. (2017). "International Energy Outlook 2017." In.
- 513 Fang, K.T., Li, R. & Sudjianto, A. (2005). *Design and Modeling for Computer Experiments* (CRC Press).
- 514 Gan, G. (2009a). 'Effect of Air Gap on the Performance of Building-integrated Photovoltaics', *Energy*,  
515 34: 913-21.
- 516 Gan, G. (2009b). 'Numerical Determination of Adequate Air Gaps for Building-integrated  
517 Photovoltaics', *Solar Energy*, 83: 1253-73.

518 Gliha, O., Kruczek, B., Gh. Etemad, S. & Thibault, J. (2011). 'The effective sky temperature: an  
519 enigmatic concept', *Heat and Mass Transfer*, 47: 1171-80.

520 Gökmen, N., Hu, W., Hou, P., Chen, Z., Sera, D. & Spataru, S. (2016). 'Investigation of wind speed  
521 cooling effect on PV panels in windy locations', *Renewable Energy*, 90: 283-90.

522 Goldemberg. (2000). "World Energy Assessment: Energy and the Challenge of Sustainability." In.

523 Hemmer, C., Saad, A. A., Popa, C. V. & Polidori, G. (2017). 'Early development of unsteady convective  
524 laminar flow in an inclined channel using CFD: Application to PV panels', *Solar Energy*, 146:  
525 221-29.

526 Jubayer, C. M. (2014). 'Wind and Thermal Effects on Ground Mounted Photovoltaic (PV) Panels', The  
527 University of Western Ontario.

528 Jubayer, C. M., Karava, P., & Savory, E. (2010). "CFD Simulations for Evaluation of Forced Convective  
529 Heat Transfer Coefficients on Photovoltaic/Thermal Systems Integrated on the Windward  
530 Roof Surface of a Low-rise Building." In *The Fifth International Symposium on Computational  
531 Wind Engineering (CWE2010)*. Chapel Hill, North Carolina, USA.

532 Kaldellis, J. K., Kapsali, M. & Kavadias, K. A. (2014). 'Temperature and wind speed impact on the  
533 efficiency of PV installations. Experience obtained from outdoor measurements in Greece',  
534 *Renewable Energy*, 66: 612-24.

535 Kalogirou, S. A. (2014). *Solar Energy Engineering* (Elsevier Inc.: Oxford).

536 Karava, P., Jubayer, C. M., Savory, E., & Li, S. (2012). 'Effect of Incident Flow Conditions on Convective  
537 Heat Transfer from the Inclined Windward Roof of a Low-rise Building with Application to  
538 Photovoltaic-thermal Systems', *Journal of Wind Engineering and Industrial Aerodynamics*,  
539 104–106: 428-38.

540 King, D. L., Boyson, W. E., & Kratochvill, J. A. (2004). "Photovoltaic Array Performance Model." In.  
541 Albuquerque: Sandia National Laboratories.

542 Koyunbaba, B. K., Yilmaz, Z., & Ulgen, K. (2013). 'An Approach for Energy Modeling of a Building  
543 Integrated Photovoltaic (BIPV) Trombe Wall System', *Energy and Buildings*, 67: 680-88.

544 LeBlanc, D.C. (2004). *Statistics: Concepts and Applications for Science* (Jones and Bartlett).

545 Liao, L., Athienitis, A. K., Candanedo, L., Park, KW., Poissant, Y., & Collins, M. R. (2005). "Numerical  
546 Study of Conjugate Heat Transfer in a BIPV-Thermal System." In *ASME 2005 International  
547 Solar Energy Conference*. Orlando, Florida, USA.

548 Markvart, T., & Bogus, K. (2000). *Solar Electricity* (Wiley).

549 Mirzaei, P. A., & Carmeliet, J. (2013). 'Dynamical computational fluid dynamics modeling of the  
550 stochastic wind for application of urban studies', *Building and Environment*, 70: 161-70.

551 Mirzaei, P. A., & Carmeliet, J. (2015). 'Influence of the underneath cavity on buoyant-forced cooling  
552 of the integrated photovoltaic panels in building roof: a thermography study', *Progress in  
553 Photovoltaics: Research and Applications*, 23: 19-29.

554 Mirzaei, P. A., and Haghghat, F. (2012). 'A procedure to quantify the impact of mitigation techniques  
555 on the urban ventilation', *Building and Environment*, 47: 410-20.

556 Mirzaei, P. A., Paterna, E., & Carmeliet, J. (2014). 'Investigation of the role of cavity airflow on the  
557 performance of building-integrated photovoltaic panels', *Solar Energy*, 107: 510-22.

558 Mirzaei, P. A., & Zhang, R. (2015). 'Validation of a Climatic CFD Model to Predict the Surface  
559 Temperature of Building Integrated Photovoltaics', *Energy Procedia*, 78: 1865-70.

560 Nordmann, T., & Clavadetscher, L. (2003). "Understanding Temperature Effects on PV System  
561 Performance." In *Proceedings of the Third World Conference on Photovoltaic Energy  
562 Conversion*. Osaka, Japan.

563 Panwar, N. L., Kaushik, S. C., & Kothari, S. (2011). 'Role of renewable energy sources in environmental  
564 protection: A review', *Renewable and Sustainable Energy Reviews*, 15: 1513-24.

565 Petropoulos, G., & Srivastava, P.K. (2016). *Sensitivity Analysis in Earth Observation Modelling* (Elsevier  
566 Science).

567 Reagan, J. A., & Acklam, D. M. (1979). 'Solar reflectivity of common building materials and its  
568 influence on the roof heat gain of typical southwestern U.S.A. residences', *Energy and*  
569 *Buildings*, 2: 237-48.

570 Renewable Energy Policy Network for the 21st Century. (2017). "Renewables 2017 Global Status  
571 Report." In.

572 Ross Jr, RG. (1976). "Interface design considerations for terrestrial solar cell modules." In *12th*  
573 *Photovoltaic Specialists Conference*, 801-06.

574 Skoplaki, E., & Palyvos, J. A. (2009). 'Operating temperature of photovoltaic modules: A survey of  
575 pertinent correlations', *Renewable Energy*, 34: 23-29.

576 Solanki, C. S. (2013). *Solar Photovoltaic Technology and Systems* (Prentice-Hall of India Pvt. Ltd.: Delhi).

577 Teo, H. G., Lee, P. S., & Hawlader, M. N. A. (2012). 'An active cooling system for photovoltaic modules',  
578 *Applied Energy*, 90: 309-15.

579 Tominaga, Y., Mochida, A., Yoshie, R., Kataoka, H., Nozu, T., Yoshikawa, M., & Shirasawa, T. (2008).  
580 'AIJ guidelines for practical applications of CFD to pedestrian wind environment around  
581 buildings', *Journal of Wind Engineering and Industrial Aerodynamics*, 96: 1749-61.

582 Vautard, R., Cattiaux, J., Yiou, P., Thépaut, JN., & Ciais, P. (2010). 'Northern Hemisphere atmospheric  
583 stilling partly attributed to an increase in surface roughness', *Nature Geoscience*, 3: 756.

584 Wilson, M. J., & Paul, M. C. (2011). 'Effect of Mounting Geometry on Convection Occurring Under a  
585 Photovoltaic Panel and the Corresponding Efficiency Using CFD', *Solar Energy*, 85: 2540-50.

586 Zhang, R., Mirzaei, P. A., & Carmeliet, J. (2017). 'Prediction of the surface temperature of building-  
587 integrated photovoltaics: Development of a high accuracy correlation using computational  
588 fluid dynamics', *Solar Energy*, 147: 151-63.

589 Zogou, O., & Stapountzis, H. (2012). 'Flow and heat transfer inside a PV/T collector for building  
590 application', *Applied Energy*, 91: 103-15.