

LETTER TO THE EDITOR

Electrons under the dominant action of shock-electric fields

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ABSTRACT

We consider a fast magnetosonic multifluid shock as a representation of the solar-wind termination shock. We assume the action of the transition happens in a three-step process: In the first step, the upstream supersonic solar-wind plasma is subject to a strong electric field that flashes up on a small distance scale $\Delta z \approx U_1/\Omega_e$ (first part of the transition layer), where Ω_e is the electron gyro-frequency and U_1 is the upstream speed. This electric field both decelerates the supersonic ion flow and accelerates the electrons up to high velocities. In this part of the transition region, the electric forces connected with the deceleration of the ion flow strongly dominate over the Lorentz forces. We, therefore, call this part the demagnetization region. In the second phase, Lorentz forces due to convected magnetic fields compete with the electric field, and the highly anisotropic and energetic electron distribution function is converted into a shell distribution with energetic shell electrons storing about 3/4 of the upstream ion kinetic energy. In the third phase, the plasma particles thermalize due to the relaxation of free energy by plasma instabilities. The first part of the transition region opens up a new thermodynamic degree of freedom never before taken into account for the electrons, since the electrons are usually considered to be enslaved to follow the behavior of the protons in all velocity moments like density, bulk velocity, and temperature. We show that electrons may be the downstream plasma fluid that dominates the downstream plasma pressure.

Key words. plasmas – Sun: heliosphere – solar wind

1. Introduction

Recent literature on astrophysical shocks concludes with increasing conviction that a shock, such as the solar-wind termination shock, is a phenomenon in which multifluid effects play an important role. This means that, for the understanding of global shock physics, effects arising from different plasma species must be taken into account while all species have to fulfill the Rankine-Hugoniot conservation laws concertedly. For instance, previous studies indicate that pickup ions substantially modify the structure of the solar-wind termination shock. In addition, pickup ions are generally considered an important fluid component since they transport a major fraction of the entropized upstream kinetic energy in the form of thermal energy into the downstream regime of the shock (see Decker et al. 2008). Zank et al. (2010) and Fahr & Siewert (2007, 2010, 2011) found relations between the upstream and downstream ion distribution functions that are different for solar-wind protons and for pickup protons, respectively. However, these refinements did not lead to a fully satisfying representation of some properties of the shocked plasma observed by Voyager 2 (Richardson et al. 2008). In fact, Chalov & Fahr (2013) demonstrate that it is necessary to allow for solar-wind electrons to behave like a third, independent plasma fluid to achieve an agreement between the model results and the plasma data presented by Richardson et al. (2008). Their parameter study shows that the best-fit results for the observed proton temperature are then achieved if the electrons are assumed to be heated to a temperature that is higher than the downstream proton temperature by a factor ≥ 10 . We refer to the works of Leroy & Mangeney (1984), Tokar et al. (1986), and Schwartz et al. (1988) on electron heating at fast-mode shocks. Also, plasma shock simulations, in which electrons are treated

kinetically, show preferential shock heating of the plasma electrons (see Lembège et al. 2003, 2004). Two-stream and viscous interactions lead to a demagnetization of the electrons; i.e., they are not Lorentz-wound by the magnetic fields and attain an increase in their temperature by a factor of 50 or more on the downstream side of the shock. In a different approach, Leroy et al. (1982) and Goodrich & Scudder (1984) predict that electrons carry out perpendicular electric drifts that are different from those of the ions due to the shock-electric field, thereby establishing an electric current that modifies the surface-parallel magnetic field.

With a similar level of consistency, Fahr et al. (2012) describe the conditions of the upstream and downstream plasma in bulk-frame systems with frozen-in magnetic fields. They treat the transition from the upstream side to the downstream side of the shock as an instantaneous kinetic reaction in the velocity distribution function via the Liouville-Vlasov theorem, predicting all of the relevant downstream plasma quantities. In this model, a semikinetic representation of the multifluid termination shock with mass- and charge-specific reactions of protons and electrons to the electric shock ramp leads to excessive electron heating as described by Fahr et al. (2012) or Fahr & Siewert (2013). Based on these studies, we assume that electrons enter the downstream side as a strongly heated, massless plasma fluid that dominates the downstream plasma pressure. A recently published multifluid termination shock reconstruction by Zieger et al. (2015), which describes the electrons as a separate, independently reacting fluid, supports this notion. This study finds that electrons are preferentially heated with respect to ions, converting overshoot velocities into thermal energy supporting the claims made by Chalov & Fahr (2013), Fahr & Siewert (2015), and Fahr et al. (2015). Furthermore, the study finds that the

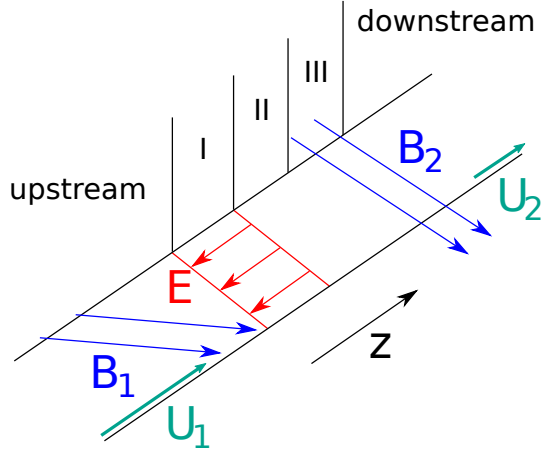


Fig. 1. Illustration of the three-phase shock. Phase I: electric forces dominate the deceleration of the plasma (demagnetization region); Phase II: magnetic Lorentz forces dominate; Phase III: quasi-equilibrium relaxation of the plasma and thermalization through plasma instabilities.

partial pressure of the heated electrons plays a dominant role in the downstream plasma flow.

In the following study, we investigate more carefully for what reason and in which way the plasma electrons behave as a preferentially heated fluid at the shock crossing.

2. The shock electric field and charge separation

Strongly space-dependent electric and magnetic fields are typical for the transition region of astrophysical shocks, and none of the conventional test-particle descriptions, such as the expansion of the particle motion into different forms of electromagnetic drifts, apply under these conditions. This is certainly the case when electric forces locally flash up and become strongly dominant over Lorentz forces so that the latter forces can be safely neglected for the first-order motion analysis. In this section, we look into the details of this special situation that arises at shocks such as the solar wind-termination shock.

We assume that the shock is characterized by a three-phase transition in space. In the first phase (the demagnetization region), electric forces dominate the deceleration of the plasma. In the second phase, Lorentz forces dominate the deceleration over the electric forces. While in the first two phases the transition is isothermal for protons, the third phase on the downstream side represents the region in which the particle thermalization due to streaming plasma instabilities takes place. We focus on the first phase of the shock transition (the demagnetization region). We illustrate the three-phase shock in Fig. 1.

We first estimate the typical field conditions at a shock of this nature. In a sufficiently small surface element of the termination shock, the curvature of the shock surface is negligible. We approximate this surface element under consideration as a planar surface and, consequently, assume a one-dimensional geometry of the system. In this approximation, the shock parameters only depend on the coordinate z parallel to the shock normal. We assume a representation of the ion bulk-flow velocity U as a function of z of the form

$$U(z) = U_1 - \frac{1}{2}\Delta U \left[1 + \tanh\left(\frac{z}{\alpha}\right) \right] \quad (1)$$

where $\Delta U = U_1 - U_2$. Indexes 1 and 2 characterize the asymptotic upstream and downstream conditions of the flow, respectively. The quantity α determines the transition length at the

shock. We choose the coordinate system in which \mathbf{B} lies in the x - z -plane. In addition, we assume that the \mathbf{B} -field is frozen into the main momentum flow (i.e., the ion flow). Therefore, the frozen-in condition under steady-state conditions, $\partial\mathbf{B}/\partial t = \nabla \times [\mathbf{U} \times \mathbf{B}] = 0$, yields

$$\mathbf{B} = B_x(z) + B_z \quad (2)$$

in our one-dimensional coordinate system, where $B_z = B_{z1} = \text{const.}$ and $B_x = B_{x1}U_1/U(z)$.

The z -component of the ion momentum equation is written as

$$m_p U \frac{dU}{dz} = -\frac{1}{n_p} \frac{dP_p}{dz} + eE, \quad (3)$$

where m_p is the proton mass e is the elementary charge, E is the electric field that is parallel to the flow direction \hat{e}_z , P_p is the proton pressure, and n_p is the proton density (see also [Verscharen & Fahr 2008](#); [Fahr & Siewert 2013](#)). In our isothermal approximation ($T_p = \text{const.}$) for the first phase of the shock transition, we find for the pressure-gradient term in the momentum equation by applying the flux-conservation requirement $\Phi_e = \Phi_p = n_p U = \text{const.}$ that

$$-\frac{1}{n_p} \frac{dP_p}{dz} = \frac{k_B T_p}{U} \frac{dU}{dz}, \quad (4)$$

where k_B is the Boltzmann constant. This leads to the following expression for the electric field

$$E = \frac{m_p}{e} U \frac{dU}{dz} \left(1 - \frac{1}{2} \frac{c_p^2}{U^2} \right), \quad (5)$$

where $c_p = \sqrt{2k_B T_p/m_p}$ is the ion thermal speed. The correction term c_p^2/U^2 on the right-hand side is small compared to 1 for high-Mach-number shocks in the first phase of the shock transition, which justifies neglecting the pressure gradient. With Eq. (1), the electric field as a function of z is given by

$$E = -\frac{m_p}{2e\alpha} U \Delta U \text{sech}^2\left(\frac{z}{\alpha}\right). \quad (6)$$

The electric field E is self-consistently generated by the charge separation between protons and electrons according to Gauss' law:

$$\frac{dE}{dz} = 4\pi e (n_p - n_e). \quad (7)$$

3. Dominance of electric forces over Lorentz forces

We can assume that, as long as the electric force is much stronger than the Lorentz force on the electrons, the motion of a single electron with electron velocity v_{ez} corresponds to a permanent linear acceleration according to

$$m_e v_{ez} \frac{dv_{ez}}{dz} = -eE. \quad (8)$$

Integrating leads to

$$\frac{1}{2} m_e v_{ez}^2 \Big|_{-\Delta}^{+\Delta} = - \int_{-\Delta}^{+\Delta} eE dz. \quad (9)$$

We assume that the initial energy of an electron with a velocity equal to the bulk-flow velocity on the upstream side,

$\epsilon_{e0} = m_e U_1^2/2$, is negligible compared to the resulting downstream energy. We note that protons and electrons have equal upstream bulk velocities U_1 as well as equal upstream densities n_1 . With this assumption and Eq. (5) in the limit $c_p^2/U^2 \ll 1$, we find for the z -dependent kinetic energy of the electron that

$$\begin{aligned} \frac{1}{2} m_e v_{ez}^2 &= - \int_{-\infty}^z eE(z') dz' = \frac{m_p}{2\alpha} \Delta U \int_{-\infty}^z U(z') \operatorname{sech}^2\left(\frac{z'}{\alpha}\right) dz' \\ &= \frac{1}{2} m_p \Delta U \left\{ \left(U_1 - \frac{\Delta U}{2} \right) \left[1 + \tanh\left(\frac{z}{\alpha}\right) \right] + \frac{\Delta U}{4} \operatorname{sech}^2\left(\frac{z}{\alpha}\right) \right\}. \end{aligned} \quad (10)$$

For the downstream electron kinetic energy, we obtain with Eq. (10) that

$$\begin{aligned} \frac{1}{2} m_e v_{ez}^2 &= \frac{m_p}{2\alpha} \Delta U \int_{-\infty}^{+\infty} U(z) \operatorname{sech}^2\left(\frac{z}{\alpha}\right) dz \\ &= \frac{1}{2} m_p U_1^2 \left(\frac{s^2 - 1}{s^2} \right) = 0.84 \frac{1}{2} m_p U_1^2, \end{aligned} \quad (11)$$

with the observed compression ratio $s = U_1/U_2 \approx 2.5$ (see Richardson et al. 2008). Therefore, the shock electrons may consume about 84% of the upstream proton kinetic energy, which corresponds to about 0.7 keV or $v_{ez2} \approx 10^9$ cm/s, respectively.

We choose an electron with $v_{ez1} = U_1$ and follow its trajectory through the shock. This electron fulfills $v_{ez}(z) = U_e(z)$ throughout its transit. With this condition and flux conservation, $n_e U_e = \text{const.}$, we directly determine the upstream-to-downstream density ratio for the electrons as

$$\frac{n_{e2}}{n_1} = \frac{U_1}{U_{e2}} = \sqrt{\frac{m_e}{m_p}} \sqrt{\frac{s^2}{s^2 - 1}} = 0.025, \quad (12)$$

which translates to $U_{e2} = 40U_1$.

The electric acceleration of the electron, however, only dominates compared to the acceleration due to Lorentz forces as long as

$$|eE| \geq \left| \frac{e}{c} v_{ez} B_x \right|. \quad (13)$$

This condition limits the resulting velocity to

$$|v_{ez}| \leq \left| \frac{c}{B_x} E \right| = \left| \frac{1}{2\alpha} \frac{\Delta U}{U_1} \frac{m_p c}{e B_{x1}} U^2 \operatorname{sech}^2\left(\frac{z}{\alpha}\right) \right|, \quad (14)$$

which we write in normalized units as

$$\left| \frac{v_{ez}}{U_1} \right| \leq \left| \frac{1}{2} \frac{U_1}{\Omega_{px1} \alpha} \left(\frac{U}{U_1} \right)^2 \frac{\Delta U}{U_1} \operatorname{sech}^2\left(\frac{z}{\alpha}\right) \right|, \quad (15)$$

where $\Omega_{px1} = eB_{x1}/m_p c$. We define the normalized threshold velocity v_{thr}/U_1 as the right-hand side of Eq. (15). Beyond this limit, Lorentz forces begin to compete with electric forces and need to be taken into account. We show this condition in Fig. 2. The black solid line shows the threshold velocity v_{thr} in units of the upstream bulk velocity U_1 . Considering again an electron with $v_{ez}(z) \approx U_e(z)$, we determine the profile of U_e as a function of z from Eq. (10). We show this profile as the red dashed line in Fig 2. The bulk velocity fulfills the condition in Eq. (15) in the range between $z \approx -1.5\alpha$ and $z \approx -0.1\alpha$. We also plot the sum of the electron bulk velocity and the upstream electron thermal speed as the green dashed line. This line indicates the region in

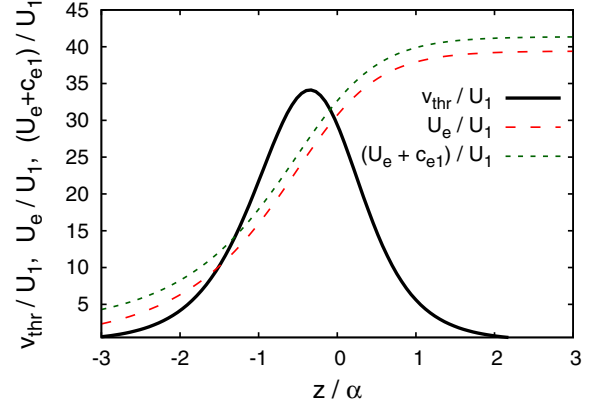


Fig. 2. Electron bulk velocity U_e from Eq. (10), threshold velocity v_{thr} from Eq. (15), and $U_e + c_{e1}$, where $c_{e1} = \sqrt{2k_B T_{e1}/m_e}$ is the upstream electron thermal speed, as functions of the spatial coordinate z . We use the following parameters: $s = 2.5$, $U_1 = 4 \times 10^7$ cm/s, $B_{x1} = 2 \times 10^{-7}$ G, $\alpha = 10^8$ cm, and $T_{e1} = 2 \times 10^4$ K.

which the majority of the solar-wind electrons fulfill Eq. (15). This condition is fulfilled between $z \approx -1.2\alpha$ and $z \approx -0.1\alpha$. As these considerations show, the demagnetization region is restricted to the region $z < 0$.

In the limit of a quasi-parallel shock, $\Omega_{px1} \rightarrow 0$ which leads to $v_{thr} \rightarrow \infty$. Therefore, the quasi-parallel shock is solely a result of the electrostatic interaction while Lorentz forces are negligible. On the other hand, a quasi-perpendicular shock still has a finite v_{thr} , which can be $> U_e$ depending on the finite shock parameters U_1 , Ω_{px1} , and α .

4. Motion under first-order Lorentz forces

We assume that, within a finite region, the electric forces are strongly dominant according to Eq. (13). The zeroth-order motion of an electron is then determined by

$$\frac{dv_e^0}{dt} = -\frac{e}{m_e} \mathbf{E}, \quad (16)$$

while the first-order Lorentz force is given by

$$\mathbf{K}_L^1 = -\frac{e}{c} [\mathbf{v}_e^0 \times \mathbf{B}]. \quad (17)$$

Under the assumption that the electric field is purely oriented along the z -direction, we obtain

$$v_e^{02}(z) - v_{e1}^{02} = -2 \int_{-\infty}^z \frac{e}{m_e} E(z') dz'. \quad (18)$$

We furthermore assume that the upstream electron velocity v_{e1}^0 is negligible. Now we allow for a first-order velocity component in the y -direction (i.e., the $\hat{e}_z \times \hat{b}$ -direction, where $\hat{b} = \mathbf{B}/|\mathbf{B}|$) due to the first-order Lorentz force K_L^1 :

$$v_{ey}^1 = \int_{-\infty}^z \frac{1}{m_e} K_L^1(z') \frac{dt}{dz'} dz', \quad (19)$$

where K_L^1 is given by

$$K_L^1(s) = -\frac{e}{c} \left| [\mathbf{v}_e^0(z) \times \mathbf{B}(z)] \right| = -\frac{e}{c} B_x(z) \sqrt{-\frac{2e}{m_e} \int_{-\infty}^z E(z') dz'}. \quad (20)$$

With Eq. (19), we find

$$v_{ey}^1 = - \int_{-\infty}^z \frac{e}{m_e c} B_x(z') \sqrt{-\frac{2e}{m_e} \int_{-\infty}^{z'} E(z'') dz''} \frac{dt}{dz'} dz'. \quad (21)$$

Using $dt/dz = 1/v_e^0(z)$, we obtain the solution

$$v_{ey}^1 = - \int_{-\infty}^z \frac{e}{m_e c} B_x(z') dz' = - \int_{-\infty}^z \Omega_{ex}(z') dz' = -z \langle \Omega_{ex} \rangle_z, \quad (22)$$

where $\Omega_{ex}(z)$ denotes the local electron gyro-frequency based on B_x , and $\langle \Omega_{ex} \rangle_z$ is the average gyro-frequency in the integration domain.

It is noteworthy that the electron motion in the y -direction does not depend on the electric-field configuration in the transition region as long as the Lorentz force can be considered to be of higher order than the electric force. Therefore, the curling of the particle trajectory around the frozen-in field only happens after a time τ_{Le} when the action of the Lorentz force changed the velocity by about its magnitude, $(e/c)v_{ez}\tau_{Le} \approx m_e v_{ez}$, yielding $\tau_{Le} \approx m_e c / e B_x = 1/\Omega_{ex}$. During this period, the electron moves in the z -direction by the amount $\Delta z = \tau_{Le} v_{ez} = v_{ez}/\Omega_{ex}$. With our results for v_{ez} from Sect. 3, we find that the permitted extent of the overall transition region can roughly be estimated as $\Delta z \approx v_{ez}/\Omega_{ex} \approx 10^8$ cm.

5. Discussion and conclusions

In this paper, we study the action of shock-electric fields on electrons and ions entering from the upstream regime of the shock into the shock transition region. We split the latter into three consecutive regions: the first is demagnetized and operates like an electric double layer where the action of the upflashing shock-electric field strongly dominates over Lorentz forces. In the second region, Lorentz forces due to the piled-up magnetic fields compete with or even dominate compared to electric forces. In the third phase, the overshooting energy is transferred into proton and electron heating by the action of kinetic plasma instabilities.

In Sect. 3, we determine the electron velocity profile. The downstream electron velocity before entering phase three of the shock is about 40 times the upstream velocity, while the downstream electron density is about 0.025 the upstream density. The shocked plasma opens up a new thermodynamic degree of freedom allowing that a substantial fraction (about 84 percent) of the upstream ion kinetic energy gets stored in the overshoot velocities of the electrons which, in the second region of the shock transition, is deposited into a shell in velocity space centered around the downstream ion bulk velocity. In that case, a major fraction of the upstream ion bulk-flow energy is available to be transferred into electron thermal energy. We determine the threshold velocity v_{thr} , which defines the separation between phases one and two of the shock transition. The electron motion is dominated by electric forces for all electrons with a velocity $< v_{thr}$. For typical termination-shock parameters, we find that the region in which this condition is fulfilled for electrons with the electron bulk velocity extends from $z = -1.5\alpha$ to $z = -0.1\alpha$.

In Sect. 4, we treat Lorentz-forces as a first-order correction to the plasma deceleration. We show that the first-order shock-perpendicular component of the electron velocity is determined by the average electron gyro-frequency in the shock layer. With this result, we determine the size of the demagnetization region (phase one) as $\Delta z \approx 10^8$ cm for typical solar-wind parameters.

In earlier work (see Chalov & Fahr 2013; Fahr & Siewert 2013, 2015), we emphasized the fact that the creation of energetic electrons at the plasma passage over the shock is essential to fulfill the thermodynamic entropy requirements (Fahr & Siewert 2015) and to arrive at downstream plasma properties that nicely fit the Voyager-2 measurements of Richardson et al. (2008). Zieger et al. (2015) recently published a multi-fluid study of the solar-wind termination shock, which strongly supports our claim for the occurrence of energetic downstream electrons by showing that the Voyager-2 measurements allow for a reasonably good theoretical fit with the model results only if the appearance of energetic downstream electrons is taken into account.

The remaining question as to why these predicted energetic electrons were not detected by the Voyager plasma analyzers, can most probably be answered along the argumentation developed in a recent paper by Fahr et al. (2015). These authors show that the energetic electrons create a strongly increased electric charge-up of the spacecraft detectors and thereby, owing to electric screening, impede the detectors in measuring countable fluxes of these electrons.

We intend to continue the studies presented in this Letter by kinetically analyzing the physics relevant for phases II and III of the three-phase shock.

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References

- Chalov, S. V., & Fahr, H. J. 2013, *MNRAS*, 433, L40
 Decker, R. B., Krimigis, S. M., Roelof, E. C., et al. 2008, *Nature*, 454, 67
 Fahr, H.-J., & Siewert, M. 2007, *Astrophys. Space Sci. Trans.*, 3, 21
 Fahr, H.-J., & Siewert, M. 2010, *A&A*, 512, A64
 Fahr, H.-J., & Siewert, M. 2011, *A&A*, 527, A125
 Fahr, H.-J., & Siewert, M. 2013, *A&A*, 558, A41
 Fahr, H.-J., & Siewert, M. 2015, *A&A*, 576, A100
 Fahr, H.-J., Siewert, M., & Chashei, I. 2012, *Ap&SS*, 341, 265
 Fahr, H. J., Richardson, J. D., & Verscharen, D. 2015, *A&A*, 579, A18
 Goodrich, C. C., & Scudder, J. D. 1984, *J. Geophys. Res.*, 89, 6654
 Lembège, B., Savoini, P., Balikhin, M., Walker, S., & Krasnoselskikh, V. 2003, *J. Geophys. Res.*, 108, 1256
 Lembège, B., Giacalone, J., Scholer, M., et al. 2004, *Space Sci. Rev.*, 110, 161
 Leroy, M. M., & Mangeney, A. 1984, *Ann. Geophys.*, 2, 449
 Leroy, M. M., Winske, D., Goodrich, C. C., Wu, C. S., & Papadopoulos, K. 1982, *J. Geophys. Res.*, 87, 5081
 Richardson, J. D., Kasper, J. C., Wang, C., Belcher, J. W., & Lazarus, A. J. 2008, *Nature*, 454, 63
 Schwartz, S. J., Thomsen, M. F., Bame, S. J., & Stansberry, J. 1988, *J. Geophys. Res.*, 93, 12923
 Tokar, R. L., Aldrich, C. H., Forslund, D. W., & Quest, K. B. 1986, *Phys. Rev. Lett.*, 56, 1059
 Verscharen, D., & Fahr, H.-J. 2008, *A&A*, 487, 723
 Zank, G. P., Heerikhuisen, J., Pogorelov, N. V., Burrows, R., & McComas, D. 2010, *ApJ*, 708, 1092
 Zieger, B., Opher, M., Tóth, G., Decker, R. B., & Richardson, J. D. 2015, *J. Geophys. Res.*, 120, 7130