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### Estimating the Dependence of Differential Pathlength Factor on Blood Volume and Oxygen Saturation using Monte Carlo method

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Abstract—Differential Pathlength Factor (DPF) is a vital parameter for the Beer-Lambert law based calculations in estimating tissue perfusion using non-invasive optical techniques. A significant error in the measured concentration of oxyhemoglobin and deoxyhemoglobin has been reported due to the usage of wrong DPF values. The dependence of DPF on blood oxygen saturation and blood volume has never been studied earlier. In this work, a Monte Carlo model of perfused skin tissue was developed and executed at 660 nm and 940 nm optical wavelengths at a reflectance geometry. DPFs were simulated through 1-10 mm source detector separations at different blood volumes and oxygen saturations. Results showed higher DPFs at lower wavelengths and considerable variation with blood volume and oxygen saturation.

#### I. INTRODUCTION

The clinical assessment of tissue perfusion relies on the technique of illuminating the tissue by near infrared optical wavelengths (~ 650 nm - 950 nm), and analysing the acquired optical signal by the use of the modified Beer-Lambert law [1]. The modified Beer-Lambert law describes the migration of photons through a highly scattering and absorbing medium such as biological tissue [2]. This law relates the absorbance (A) of the optical radiation (with wavelength  $\lambda$ ) to the optical properties of the tissue (attenuation coefficient,  $\mu$  and optical pathlegnth, l) by a multiplicative term called the Differential Pathlength Factor (DPF):

$$A(\lambda) = \mu(\lambda) \cdot l(\lambda) \cdot DPF(\lambda) \tag{1}$$

Differential pathlength factor plays a pivotal role in assessing tissue perfusion by estimating the concentration change in blood oxyhaemoglobin and deoxyhaemoglobin from the diffused light signal from tissue. A number of research works have been carried out previously to evaluate the dependence of DPF on tissue location, sensor geometry, optical wavelength and age [3], [4], [5], [6]. Recent studies have also identified a variation in DPF between larger and smaller source-detector separations, typically used in noninvasive applications such as Near-Infrared Spectroscopy (NIRS) and Photoplethysmography (PPG), respectively [7]. The importance of an accurate DPF assessment for a specific application has been demonstrated in previous works that have shown significant cross-talk errors in the measured concentration of oxyhaemoglobin and deoxyhaemoglobin for an inaccuracy in the DPF value [9], [10], [11].

The Differential pathlength factor is quantified as the ratio between the physical and geometrical optical pathlength through a tissue medium [8]. The dependence of the optical pathlength through a perfused tissue volume on the physiological parameters such as blood volume and blood oxygen saturation has already been demonstrated in our earlier studies [12]. DPF is directly related to the optical path, therefore, should vary with the physiological properties as well. However, the relationship between the DPF and changing physiological parameters have never been studied before. The present work is aims to investigate the relationship between the DPF and two physiological parameters (blood volume and blood oxygen saturation) at two near infrared wavelengths (i.e., 660 nm and 940 nm) through a volume of perfused skin tissue.

Monte Carlo (MC) is a stochastic procedure that simulates the propagation of light through a complex medium such as biological tissue [15]. MC has been accepted as a reliable and flexible tool for investigating various problems related to tissue optics which are difficult to solve using other approaches (e.g., diffusion approximation or electromagnetic theory based formalisms) [14]. In the present work, a Monte Carlo method based perfused skin (dermis) tissue is explored at an optimal geometry similar to a dual wavelength reflectance PPG sensor for analysing the differential optical pathlengths. Such a study is crucial for developing the fundamental knowledge on PPG DPF which could lead to more accurate assessment of tissue perfusion and oxygenation.

#### II. METHODOLOGY

#### A. Tissue characterisation

The tissue layer was presented by a slab of infinite dimensions. The slab geometry was chosen because the spatial dimension of the photon distribution was much smaller than the width of tissue. The tissue-slab was presented in a three-dimensional Cartesian co-ordinate system (x,y,z). The optical source S was placed on the tissue surface (z = 0)having its centre on the origin (0,0,0), as shown in Figure 1. The tissue was characterised by its optical properties, e.g.,  $\mu_a$ ,  $\mu_s$ , and g. The volumetric contribution of the optical properties were considered, i.e., the 'perfused' tissue layer was assumed to be a homogeneous mixture of skin-dermis and blood (comprising the main absorbers: oxyhaemoglobin and deoxyhaemoglobin). The effective optical properties incorporated the volumetric contributions from the tissuecomponents. The total absorption coefficient  $\mu_a$  of a layer of dermis perfused with a volume fraction of blood V and a total oxygen saturation  $S_t O_2$  (i.e., the total oxygen saturation

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TABLE I Optical properties of simulated components of dermis.

optical wavelength (nm)	bloodless dermis		oxygenated blood		deoxygenated blood	
	$\mu_a(mm^{-1})$	$\mu_s'(mm^{-1})$	$\mu_a(mm^{-1})$	$\mu_s'(mm^{-1})$	$\mu_a(mm^{-1})$	$\mu_s'(mm^{-1})$
660	0.0286	2.2336	0.15	1.3844	1.64	1.1566
940	0.0245	0.9501	0.65	1.3187	0.43	1.1124

in the arterial, venous and capillary blood) was written as the sum of the individual absorption coefficients of the components [15]:

$$\mu_a = (1 - V) \cdot \mu_{a_b} + V. \left[ S_t O_2 \ \mu_{a_{HbO_2}} + (1 - S_t O_2) \ \mu_{a_{Hb}} \right]$$
(2)

where  $\mu_{a_b}$  is the absorption coefficient of the bloodless dermis,  $\mu_{a_{HbO_2}}$  and  $\mu_{a_{Hb}}$  are the absorption coefficients of oxygenated and deoxygenated blood respectively having a haematocrit (Hct) of 45%. The total oxygen saturation  $S_tO_2$  was given by,

$$S_t O_2 = \frac{[HbO_2]}{[Hb] + [HbO_2]},$$
 (3)

where  $[HbO_2]$  and [Hb] were the concentrations of oxyhaemoglobin and deoxyhaemoglobin, respectively in the total blood volume, i.e., all blood found in the arterial, capillary and venous blood compartments. The baseline skin absorp-

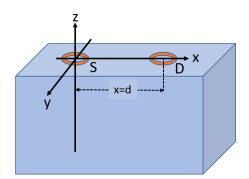


Fig. 1. The schematic representation of the tissue volume in a 3D Cartesian co-ordinate system (x,y,z) with the source S at the origin and the detector D place at a distance d on the tissue surface.

tion coefficient (i.e., the co-efficient for bloodless skin) at wavelength  $\lambda$  was expressed (in the unit of  $mm^{-1}$ ) as [16]:

$$u_{a_b} = 0.244 + 85.3 \cdot e^{-\frac{\lambda - 154}{66.2}} \tag{4}$$

The reduced scattering coefficient of bloodless dermis was estimated from the contribution of dermis collagen fibres as given by [16]:

$$\mu_{s_b}' = (2 \times 10^4) \lambda^{-1.5} + (2 \times 10^{11}) \lambda^{-4}.$$
 (5)

The values of the absorption and reduced scattering coefficient at 660 nm and 940 nm for skin dermis (calculated using above equation), and for the oxygenated and deoxygenated blood (adapted from [17]) are given in Table 1. The anisotropy factor value for the perfused skin tissue was considered to be g = 0.95 at both wavelengths, and the refractive index of the tissue layer was considered to be n = 1.

#### B. Monte Carlo method

The light propagation through the skin tissue layers was simulated using the following steps:

- A photon packet with initial weight (w = 1), position co-ordinates (x, y, z) and direction (scattering angle = θ, azimuth= φ) were supposed to be incident from the source placed on the surface of the tissue (at the origin of the Cartesian co-ordinate system).
- 2) The path of the photon packet was simulated by tracing photons steps through the medium, determined by random sampling of the probability distribution p(s) for the photons free pathlength (s) between two consecutive scattering events, which was given by

$$p(s) = \mu_s.exp(-\mu_s.s) \tag{6}$$

The step size s of a photon packet was calculated as:

$$s = -\frac{\ln(\xi)}{\mu_s} \tag{7}$$

While the photon stayed within the medium, it underwent scattering and absorption at that interaction site. Once the step-size was determined, scattering was achieved by orienting the photon direction through two randomly generated angles, zenith (θ) and azimuth (φ), given by:

$$\cos\theta = \frac{1}{2g} \left[ 1 + g^2 - \left( \frac{1 - g^2}{1 - g + 2g\xi} \right) \right]$$
(8)

$$\phi = 2\pi\xi \tag{9}$$

The scattering angle was calculated using the Henyey-Greenstein phase function, which has been experimentally proven to describe the single scattering in biological tissue very well. The azimuth was chosen randomly within the maximum value of 2π. After scattering corrections, a fraction of photon weight Δw = μa + μa. w was absorbed in the medium.
4) If the step size of the photon packet was long enough

- 4) If the step size of the photon packet was long enough so that it hit the boundary, it would undergo either reflection or transmission. The photon would terminate if its weight dropped below a threshold.
- 5) If the photon was transmitted, the detected photons were scored. The detector was basically simulated as a sliding window of a width equal to the detector diameter (0.1 mm). The distance of the point of exit of the photon on tissue surface (on z = 0) from the origin was calculated from its position co-ordinates:

$$d = \sqrt{(x^2 + y^2)} \tag{10}$$

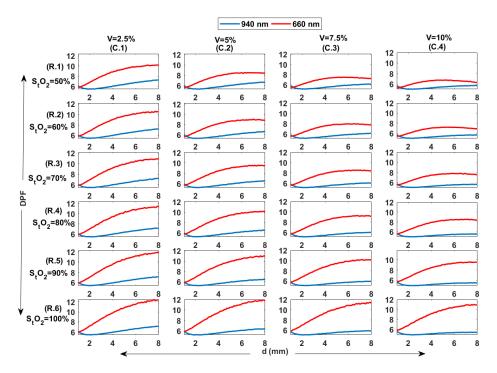


Fig. 2. Differential Pathlength Factor is estimated in monolayer perfused skin dermis. DPFs in red (660 nm) and infrared (940 nm) are evaluated at source-detector separations 1-10 mm. Results for different blood volumes ( $V_b = 2.5\%, 5\%, 7.5\%, 10\%$ ) are presented in the columns C.1-C.4, and that for different total oxygen saturations ( $S_tO_2 = 50 - 100\%$ ) are presented in the rows R.1-R.6.

The optical path associated with the detected photon was recorded. DPF was calculated from the mean optical path (l) of the detected photon packets at wavelength  $\lambda$  for the source-detector separation d:

$$DPF_{\lambda_d} = \frac{l_\lambda}{d}.$$
 (11)

#### III. RESULTS AND DISCUSSION

Simulation was repeated for detecting a  $10^{10}$  number of photon packets through the range source-detector separations 1-10 mm. The smaller source detector separation (< 1cm) usually is used for monitoring the oxygen saturation of the peripheral arterial blood, especially in photoplethysmography. Through the source-detector separations within PPG region (1 < d(mm) < 10), the DPF in the perfused skin was evaluated for a range of total oxygen saturation  $(S_tO_2 = 50-100\%)$  and blood volume  $(V_b = 2.5\%, 5\%, 7.5\%, 10\%)$ . The results are demonstrated in Figure 2. A significant variation was observed between the DPFs at two wavelengths. The values of DPF was found to be changing with the blood volume as well as blood oxygen saturation.

For a clearer observation, DPFs for a fixed blood volume  $V_b = 10\%$  for different oxygen saturations, i.e.,  $S_tO_2 = 50\%, 60\%, 70\%, 80\%, 90\%$  as a function of source-detector separations are presented in Figure 3. DPF at 660 nm was shown to increase slowly with increasing d but the rate of increase gradually decreased. A considerable increase in DPF at lower wavelengths with higher oxygen saturation was noticed. The DPF at higher wavelength, on the other hand, did not change considerably with blood oxygen saturation and

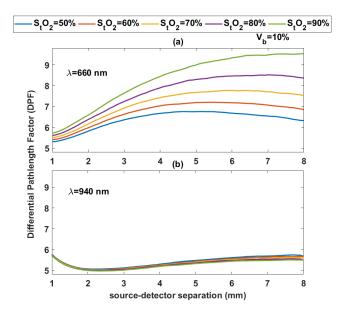


Fig. 3. Differential Pathlength Factor in perfused dermis at a fixed  $V_b = 10\%$  for different oxygen saturations  $S_t O_2 = 50\%, 60\%, 70\%, 80\%, 90\%$ . All plots are shown in the same axes limits.

slightly varied with increasing source-detector separation. Also, DPF values at a fixed  $S_tO_2 = 90\%$  for different blood volumes, i.e,  $V_b = 2.5\%$ , 5%, 7.5%, 10% are shown in Figure 4. It can be seen that for 660 nm, the DPF increased more sharply compared to 940 nm. With increasing blood volume, DPF values at two wavelengths were found to be decreasing.

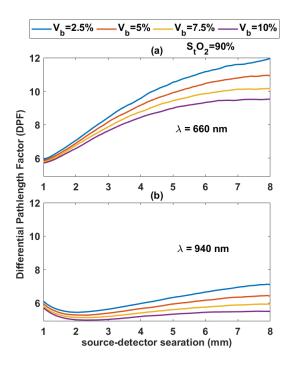


Fig. 4. Differential Pathlength Factor in monolayer perfused skin dermis at a fixed  $S_t O_2 = 90\%$  for different blood volume  $V_b = 2.5\%, 5\%, 7.5\%, 10\%$  are shown for red (660 nm) in (a) and for infrared (940 nm) in (b). All plots are shown in the same axes limits.

The results presented in Figures 2, 3 and 4 elucidate the dependence of DPF on several factors, e.g., source-detector separation, optical wavelength, physiological states such as blood volume and oxygen saturation of tissue etc. Therefore, for any further application, it is crucial to asses the DPF in the specific geometry for the specific tissue sample at a certain wavelength rather than any crude approximation. The dependence of DPF on the external factors such as the geometrical setting or the physiological states are more clearly visible in the red wavelength. Relatively lesser changes in the infrared wavelength is consistent with the previous observation by [18] where it was stated the DPF is independent of the source-detector separation at the infrared wavelength region. For PPG applications where lower wavelengths play an important role, a careful assessment is imperative.

#### IV. CONCLUSION

A robust Monte Carlo model of perfused skin was executed at near infrared optical wavelengths to analyse the relationship between differential pathlength factor and the physiological parameters such as blood volume and total (arterial, venous and capillary) blood oxygen saturation. A simplistic model was implemented for quantifying the individual effect of skin perfusion and oxygenation on the DPF. Considerable wavelength dependent deviation was found in the DPF values. With increasing blood volume, DPF was found to decrease whereas with increasing oxygen saturation, DPF was found to increase. Such variations were more noticeable for lower wavelength. All the information regarding the DPF presented in this paper are immensely important for accurate assessment of the tissue perfusion employing the Beer-Lambert law based derivations.

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