



An Exo–Kuiper Belt with an Extended Halo around HD 191089 in Scattered Light

Bin Ren (彬任)^{1,2}, Élodie Choquet^{3,4,5,41}, Marshall D. Perrin⁶, Gaspard Duchêne^{7,8}, John H. Debes⁶, Laurent Pueyo⁶, Malena Rice⁹, Christine Chen^{1,6}, Glenn Schneider¹⁰, Thomas M. Esposito⁷, Charles A. Poteet⁶, Jason J. Wang^{4,42}, S. Mark Ammons¹¹, Megan Ansdell⁷, Pauline Arriaga¹², Vanessa P. Bailey⁵, Travis Barman¹³, Juan Sebastián Bruzzone¹⁴, Joanna Bulger¹⁵, Jeffrey Chilcote¹⁶, Tara Cotten¹⁷, Robert J. De Rosa⁷, Rene Doyon¹⁸, Michael P. Fitzgerald¹², Katherine B. Follette¹⁹, Stephen J. Goodsell²⁰, Benjamin L. Gerard^{21,22}, James R. Graham⁷, Alexandra Z. Greenbaum²³, J. Brendan Hagan⁶, Pascale Hibon²⁴, Dean C. Hines⁶, Li-Wei Hung²⁵, Patrick Ingraham²⁶, Paul Kalas^{7,27}, Quinn Konopacky²⁸, James E. Larkin¹², Bruce Macintosh²⁹, Jérôme Maire²⁸, Franck Marchis²⁷, Christian Marois^{21,22}, Johan Mazoyer^{5,43}, François Ménard⁸, Stanimir Metchev^{14,30}, Maxwell A. Millar-Blanchaer^{5,41}, Tushar Mittal³¹, Margaret Moerchen³², Eric L. Nielsen²⁹, Mamadou N’Diaye³³, Rebecca Oppenheimer³⁴, David Palmer¹¹, Jennifer Patience³⁵, Christophe Pinte^{8,36}, Lisa Poyneer¹¹, Abhijith Rajan⁶, Julien Rameau¹⁸, Fredrik T. Rantakyro²⁴, Jean-Baptiste Ruffio²⁹, Dominic Ryan⁷, Dmitry Savransky³⁷, Adam C. Schneider³⁵, Anand Sivaramakrishnan⁶, Inseok Song¹⁷, Rémi Soummer⁶, Christopher Stark⁶, Sandrine Thomas²⁶, Arthur Vigan³, J. Kent Wallace⁵, Kimberly Ward-Duong^{19,35}, Sloane Wiktorowicz³⁸, Schuyler Wolff³⁹, Marie Ygouf⁴⁰, and Colin Norman^{1,6}

¹ Department of Physics and Astronomy, The Johns Hopkins University, 3701 San Martin Drive, Baltimore, MD 21218, USA; ren@jhu.edu

² Department of Applied Mathematics and Statistics, The Johns Hopkins University, 3400 North Charles Street, Baltimore, MD 21218, USA

³ Aix Marseille Univ, CNRS, CNES, LAM, Marseille, France

⁴ Department of Astronomy, California Institute of Technology, 1200 East California Boulevard, Pasadena, CA 91125, USA

⁵ NASA Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, CA 91109, USA

⁶ Space Telescope Science Institute (STScI), 3700 San Martin Drive, Baltimore, MD 21218, USA

⁷ Astronomy Department, University of California, Berkeley, CA 94720, USA

⁸ Université Grenoble-Alpes, CNRS Institut de Planétologie et d’Astrophysique (IPAG), F-38000 Grenoble, France

⁹ Department of Astronomy, Yale University, New Haven, CT 06511, USA

¹⁰ Steward Observatory, The University of Arizona, 933 North Cherry Avenue, Tucson, AZ 85721, USA

¹¹ Lawrence Livermore National Laboratory, 7000 East Avenue, Livermore, CA 94550, USA

¹² Department of Physics & Astronomy, 430 Portola Plaza, University of California, Los Angeles, CA 90095, USA

¹³ Lunar and Planetary Laboratory, The University of Arizona, Tucson, AZ 85721, USA

¹⁴ Department of Physics and Astronomy, The University of Western Ontario, London, ON N6A 3K7, Canada

¹⁵ Subaru Telescope, NAOJ, 650 North A’ohoku Place, Hilo, HI 96720, USA

¹⁶ Department of Physics, University of Notre Dame, 225 Nieuwland Science Hall, Notre Dame, IN 46556, USA

¹⁷ Department of Physics and Astronomy, University of Georgia, Athens, GA 30602, USA

¹⁸ Institut de Recherche sur les Exoplanètes, Département de Physique, Université de Montréal, Montréal, QC, H3C 3J7, Canada

¹⁹ Physics and Astronomy Department, Amherst College, 21 Merrill Science Drive, Amherst, MA 01002, USA

²⁰ Gemini Observatory, 670 North A’ohoku Place, Hilo, HI 96720, USA

²¹ University of Victoria, Department of Physics and Astronomy, 3800 Finnerty Road, Victoria, BC V8P 5C2, Canada

²² National Research Council of Canada Herzberg, 5071 West Saanich Road, Victoria, BC V9E 2E7, Canada

²³ Department of Astronomy, University of Michigan, Ann Arbor, MI 48109, USA

²⁴ Gemini Observatory, Casilla 603, La Serena, Chile

²⁵ Natural Sounds and Night Skies Division, National Park Service, Fort Collins, CO 80525, USA

²⁶ Large Synoptic Survey Telescope, 950 North Cherry Avenue, Tucson, AZ 85719, USA

²⁷ SETI Institute, Carl Sagan Center, 189 Bernardo Avenue, Mountain View, CA 94043, USA

²⁸ Center for Astrophysics and Space Science, University of California San Diego, La Jolla, CA 92093, USA

²⁹ Kavli Institute for Particle Astrophysics and Cosmology, Department of Physics, Stanford University, Stanford, CA 94305, USA

³⁰ Department of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794-3800, USA

³¹ Earth and Planetary Science Department, University of California, Berkeley, CA 94720, USA

³² American Geophysical Union, 2000 Florida Avenue NW, Washington, DC 20009, USA

³³ Université Côte d’Azur, Observatoire de la Côte d’Azur, CNRS, Laboratoire Lagrange, Bd de l’Observatoire, CS 34229, F-06304 Nice cedex 4, France

³⁴ Department of Astrophysics, American Museum of Natural History, New York, NY 10024, USA

³⁵ School of Earth and Space Exploration, Arizona State University, P.O. Box 871404, Tempe, AZ 85287, USA

³⁶ Monash Centre for Astrophysics (MoCA) and School of Physics and Astronomy, Monash University, Clayton, VIC 3800, Australia

³⁷ Sibley School of Mechanical and Aerospace Engineering, Cornell University, Ithaca, NY 14853, USA

³⁸ Department of Astronomy, UC Santa Cruz, 1156 High Street, Santa Cruz, CA 95064, USA

³⁹ Leiden Observatory, Leiden University, P.O. Box 9513, 2300 RA Leiden, The Netherlands

⁴⁰ IPAC, California Institute of Technology, M/C 100-22, 770 South Wilson Avenue, Pasadena, CA 91125, USA

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Abstract

We have obtained *Hubble Space Telescope* STIS and NICMOS and *Gemini*/GPI scattered-light images of the HD 191089 debris disk. We identify two spatial components: a ring resembling the Kuiper Belt in radial extent (FWHM ~ 25 au, centered at ~ 46 au) and a halo extending to ~ 640 au. We find that the halo is significantly bluer

⁴¹ NASA Hubble Fellow.

⁴² Pegasi b Fellow.

⁴³ NASA Sagan Fellow.

than the ring, consistent with the scenario that the ring serves as the “birth ring” for the smaller dust in the halo. We measure the scattering phase functions in the 30° – 150° scattering-angle range and find that the halo dust is more forward- and backward-scattering than the ring dust. We measure a surface density power-law index of -0.68 ± 0.04 for the halo, which indicates the slowdown of the radial outward motion of the dust. Using radiative transfer modeling, we attempt to simultaneously reproduce the (visible) total and (near-infrared) polarized intensity images of the birth ring. Our modeling leads to mutually inconsistent results, indicating that more complex models, such as the inclusion of more realistic aggregate particles, are needed.

Key words: protoplanetary disks – radiative transfer – stars: imaging – stars: individual (HD 191089) – techniques: image processing

1. Introduction

Debris disks, the extrasolar analogs of the asteroid belt and Kuiper Belt, have been detected around $\sim 20\%$ of the nearest stars (A-type stars: Thureau et al. 2014; FGK stars: Eiroa et al. 2013; Montesinos et al. 2016; Sibthorpe et al. 2018). They are expected to be the result of the grinding down of larger dust (Wyatt 2008); however, the diversity in observables such as morphology and surface brightness suggests that they are shaped by a variety of mechanisms (e.g., Artymowicz & Clampin 1997; Stark et al. 2014; Lee & Chiang 2016). Imaging studies of debris disks in scattered light use not only space-based instruments (e.g., the Space Telescope Imaging Spectrograph (STIS): Schneider et al. 2009, 2014, 2016, 2018; Konishi et al. 2016; NICMOS: Soummer et al. 2014; Choquet et al. 2016, 2017, 2018) that offer the best telescope stability but also extreme adaptive optics–equipped ground-based instruments (e.g., GPI: Hung et al. 2015; Kalas et al. 2015; Millar-Blanchaer et al. 2015, 2016; Perrin et al. 2015; Draper et al. 2016; Esposito et al. 2018; SPHERE: Boccaletti et al. 2015; Lagrange et al. 2016; Wahhaj et al. 2016; Engler et al. 2017; Feldt et al. 2017; Matthews et al. 2017; Milli et al. 2017, 2019; Sissa et al. 2018; Olofsson et al. 2018) that provide the best angular resolution and probe closer-in regions of the disks.

Multiwavelength studies can provide complementary insights into understanding circumstellar disks, since different wavelengths probe distinct regions and parameter space for a disk (Ertel et al. 2012; Sicilia-Aguilar et al. 2016). In this paper, we focus on using scattered-light observations to understand one of these systems. In previous studies, the combination of space- and ground-based instruments has been implemented to study both protoplanetary (e.g., PDS 66: Wolff et al. 2016) and debris (e.g., 49 Ceti: Choquet et al. 2017; HD 35841: Esposito et al. 2018) disks, and those observations are interpreted using radiative transfer codes (e.g., Augereau & Beust 2006; Milli et al. 2015; Wolff et al. 2017; Esposito et al. 2018). We perform such an analysis for the debris disk surrounding HD 191089 to study its specific properties via measurement and radiative transfer modeling in this paper.

We list the properties of the system in Table 1: HD 191089 is an F5V star with $T_{\text{eff}} = 6450$ K located at 50.14 ± 0.11 pc (*Gaia* DR2: *Gaia* Collaboration et al. 2018). Moór et al. (2006) identified it as a member of the β Pictoris moving group with space velocities compatible with the kinematics of the group, and Shkolnik et al. (2017) estimated the age of this group to be 22 ± 6 Myr based on the consensus of the group members.

Before a resolved scattered-light image was reported, HD 191089 was first identified by Mannings & Barlow (1998) as a debris disk candidate based on *IRAS* infrared excess. Chen et al. (2014) suggested a two-temperature model to explain the spectral energy distribution (SED) of the system, while Kennedy & Wyatt (2014) argued for one temperature.

The latest SED analysis including *CSO*, *Herschel*, and James Clerk Maxwell Telescope photometry up to $850 \mu\text{m}$ seems to confirm the latter hypothesis with a best fit obtained using a single-component dust: assuming the dust behaves as a blackbody, SED analysis suggests a dust mass of $\sim 0.037 M_{\oplus}$, a temperature of 89 K, and a radius of ~ 17 au (Holland et al. 2017). However, as is commonly seen for many disks, the radius derived assuming blackbody dust is several times smaller than the radius observed in resolved images (e.g., SEDs: Mittal et al. 2015; images: Hughes et al. 2018, and references therein). This indicates that the dust grains are not simple blackbodies, and the smallest dust grains are not efficient emitters at long wavelengths.

The HD 191089 disk was first resolved using *Gemini*/T-ReCS at $18.3 \mu\text{m}$ by Churcher et al. (2011), with the region interior to 28 au reported to have little emission. The disk was then detected in scattered light in a reanalysis of the archival 2006 *Hubble Space Telescope* (*HST*)/NICMOS observations by Soummer et al. (2014), with the apparent disk extent and orientation consistent with Churcher et al. (2011).

To further characterize the debris disk, we observed the target with *HST*/STIS and *Gemini*/GPI. By carrying out a multiwavelength study, we aim to understand (1) the spatial distribution of the dust; (2) the scattered-light color of the dust; (3) the scattering phase functions (SPFs) of the dust for the different spatial components of the system (if available) and how they suit the trends of the current observed debris disks; (4) the dust properties, including size distribution, structure, and compositional information; and (5) whether a universal description of the dust is able to explain the observations across different wavelengths and observational techniques.

The structure of this paper is as follows. In Section 2, we describe our HD 191089 observations and the data reduction procedure. In Section 3, we describe measurables derived from the observations. In Section 4, we describe our radiative transfer modeling efforts in studying the disk. In Sections 5 and 6, we discuss our findings and provide concluding remarks.

2. Observations and Data Reduction

2.1. Data Observation and Reduction

2.1.1. HST/NICMOS (2006)

On 2006 May 27, HD 191089 was observed using *HST*/NICMOS (Proposal ID: 10527; PI: D. Hines) with the NIC2-CORON aperture and F110W filter ($\lambda_c = 1.12 \mu\text{m}$, inner working angle (IWA): $0''.3$, pixel scale: $75.65 \text{ mas pixel}^{-1}$; Viana et al. 2009) with two telescope orientations each observing the target for 2303.67 s (see Table 2 for the observation log). These *HST*/NICMOS data, totaling 16 frames, were previously presented in Soummer et al. (2014). We perform an updated reduction including application of two different point-spread function (PSF)

Table 1
System Properties

Properties	HD 191089	Reference
Distance (pc)	50.14 ± 0.11	1
R.A. (J2000)	20 09 05.215	1
Decl. (J2000)	-26 13 26.520	1
Spectral type	F5V	2, 3
M_* (M_\odot)	1.4 ± 0.1	4
T_{eff} (K)	6450	1
V (mag)	7.18	5
J (mag)	6.321	6
H (mag)	6.091	6
Association	β Pic moving group	7
Age (Myr)	22 ± 6	8
L_{dust}/L_*	$(14.2 \pm 0.5) \times 10^{-4}$	9
Proper motion (R.A.)	$40.17 \pm 0.07 \text{ mas yr}^{-1}$	1
Proper motion (decl.)	$-67.38 \pm 0.05 \text{ mas yr}^{-1}$	1
Radial velocity	$-5.4 \pm 0.4 \text{ km s}^{-1}$	1

References. 1: *Gaia* Collaboration et al. (2018), 2: Houk (1982), 3: Hales et al. (2017), 4: Chandler et al. (2016), 5: Høg et al. (2000), 6: Cutri et al. (2003), 7: Moór et al. (2006), 8: Shkolnik et al. (2017), 9: Holland et al. (2017).

subtraction algorithms to remove the starlight and speckle noise and reveal the debris disk around HD 191089.

We obtain the scattered-light image of the system using the multireference differential imaging (MRDI) technique. Specifically, we retrieve 849 F110W exposures of 70 diskless reference stars in the ALICE archive of the NICMOS observations (PI: R. Soummer; Choquet et al. 2014; Hagan et al. 2018).⁴⁴ For each target exposure, we first decompose its 10% closest ALICE images in correlation (i.e., L^2 -norm sense and a total of 85 images) using both the Karhunen–Loève image projection (KLIP; Soummer et al. 2012) and nonnegative matrix factorization (NMF;⁴⁵ Ren et al. 2018b) data reduction methods, then model the target with these components. The disk then resides in the residual image when the empirical PSF model is subtracted from the target exposure. The final NICMOS disk image is then the elementwise mean of the derotated individual residual exposures. We list the reduction parameters in Table 3.⁴⁶

To calibrate the NICMOS disk image and obtain a measurement of its surface brightness, we multiply the reduced data by the calibrated F110W PHOTFNU parameter⁴⁷ $F_\nu = 1.21 \times 10^{-6} \text{ Jy s count}^{-1}$, then divide the data by the NICMOS pixel area on sky to obtain the surface brightness data in units of Jy arcsec^{-2} . See Figure 1 for the results.

2.1.2. HST/STIS (2014)

On 2014 July 19 and August 13 (two visits each), HD 191089 was observed using *HST*/STIS (Program ID: 13381; PI: M. Perrin) using the 50CORON aperture ($\lambda_c = 0.58 \mu\text{m}$, pixel scale: $50.72 \text{ mas pixel}^{-1}$; Riley et al. 2018), totaling 76 frames. Each visit was performed with a different telescope orientation, with position angles of $-84^\circ 23$,

$-61^\circ 23$, $-2^\circ 23$, and $25^\circ 59$ for the y -axis in the images (N to E). These telescope orientations are selected to obtain 360° azimuthal coverage of the disk down to the occulting mask (similar to Schneider et al. 2014). In each visit, we first obtained 16 short 32 s exposures on the WEDGEA0.6 position to probe the inner region down to a half-width of $0''.3$. Then we obtained three longer 483.3 s exposures on the WEDGEA1.0 position (half-width: $0''.5$) to deeply probe the exterior region of the disk.

To perform PSF subtraction, we also observed the reference star HD 196081 (selected for color, brightness, and on-sky proximity matches to HD 191089⁴⁸) using the same aperture positions, with one visit interleaved between the two science (HD 191089) visits at each epoch. With the numerical mask created by Debes et al. (2017) to mask out the STIS occulters, we perform multiple PSF subtractions using different approaches. We first apply the classical reference differential imaging (cRDI) technique to subtract the starlight in each exposure by minimizing the residual variation in the region of the coronagraphically unapodized diffraction spikes (excluding where the disk resides). We also obtain the STIS reference exposures from the STIS PSF archive created in Ren et al. (2017) for MRDI reduction: for each target exposure, we perform NMF reduction using the 10% most-correlated references in the STIS archive (i.e., 85 images for WEDGEA1.0 and 45 images for WEDGEA0.6). The final STIS disk image is then the elementwise mean of the individual derotated PSF-subtracted exposures.

To calibrate the STIS image in physical surface brightness units, we convert the PHOTFLAM photometric parameter in the raw FITS file for the HD 191089 observations ($F_\lambda = 4.15 \times 10^{-19} \text{ erg cm}^{-2} \text{ \AA}^{-1} \text{ count}^{-1}$) to $F_\nu = 4.56 \times 10^{-7} \text{ Jy s count}^{-1}$ using the conversion equation in Appendix B.2.1 of Viana et al. (2009),

$$F_\nu = \frac{\lambda_c^2 F_\lambda}{3 \times 10^{-13}},$$

where $\lambda_c = 0.58 \mu\text{m}$ is the pivot wavelength of STIS. We then multiply our combined STIS image in $\text{count s}^{-1} \text{ pixel}^{-1}$ by F_ν and divide it by the STIS pixel area on sky to obtain the surface brightness data in units of Jy arcsec^{-2} .

2.1.3. Gemini/GPI (2015)

On 2015 September 1, HD 191089 was observed using *Gemini*/GPI in H -band ($\lambda_c = 1.65 \mu\text{m}$, pixel scale: $14.166 \pm 0.007 \text{ mas pixel}^{-1}$; De Rosa et al. 2015) polarimetric mode (H -Pol; Perrin et al. 2015) during the Gemini Planet Imager Exoplanet Survey (PI: B. Macintosh; Macintosh et al. 2014). We took 28 exposures, each with 88.74 s integration time, with a total field rotation of $102^\circ 2$. The airmass ranged from 1.002 to 1.01, the differential motion image monitoring seeing measurement was $1''.16 \pm 0''.17$, and the multi-aperture scintillation sensor seeing was $1''.1 \pm 0''.3$.

To obtain the Stokes cube ($\{I, Q, U, V\}$) for the HD 191089 debris disk, we followed the recipes described in Perrin et al. (2014) and Millar-Blanchaer et al. (2015) and reduced the raw exposures using the GPI data reduction pipeline (DRP; Perrin et al. 2014, 2016) and the automated data processing architecture (Data Cruncher; Wang et al. 2018). The Q and U components in

⁴⁴ <https://archive.stsci.edu/prepds/alice/>

⁴⁵ Python-based `nmf_imaging` package; Ren (2018).

⁴⁶ The $\sim 0.9\%$ x - and y -direction scale difference in Schneider et al. (2003) is ignored.

⁴⁷ http://www.stsci.edu/hst/nicmos/performance/photometry/postnics_keywords.html

⁴⁸ <http://www.stsci.edu/hst/phase2-public/13381.pro>

Table 2
Observation Log

Instrument	Filter	λ_c^a (μm)	Pixel Scale (mas pixel $^{-1}$)	IWA b (arcsec)	T_{exp} (s)	N_{frame}	$\Delta\theta_{\text{PA}}$ (deg)	UT Date
NICMOS	F110W	1.12	75.65	0.3	4607.34	16	30.0	2006 May 27
STIS	50CCD	0.58	50.72	0.3	2048.00	64	109.8	2014 Jul 19, 2014 Aug 13
				0.5	5799.60	12		
GPI	<i>H</i> -Pol	1.65	14.166	0.123	2484.72	28	102.2	2015 Sep 1

Notes.^a For STIS, λ_c is the pivot wavelength.^b The IWA for STIS is the half-width of the wedge-shaped occulter.

the traditional Stokes cube were then transformed to the local Stokes cube ($\{Q_\phi, U_\phi\}$), with Q_ϕ representing the polarized light perpendicular or parallel to the radial direction and U_ϕ at $\pm 45^\circ$ from it (Monnier et al. 2019). On the local Stokes maps of HD 191089, we notice two similar low spatial frequency octopole structures with a rotation of $\sim 45^\circ$. However, for a U_ϕ map, we do not expect any signal from an optically thin disk with single scattering events on the dust (see Canovas et al. 2015 for a discussion of the validity and exceptions). Given that we observe similar structures in the other GPI polarimetry observations, we expect such a structure to be one of the instrumental artifacts (T. E. Esposito et al. 2019, in preparation). To reduce the systematic errors induced by it, we fit an octopole model using the U_ϕ map and remove it from the U_ϕ map, then rotate the model 45° and remove it from the Q_ϕ map.

We flux-calibrate these data following the procedure described in Hung et al. (2015, 2016). For HD 191089, we first adopt an *H*-band flux of $F_* = 3.749 \pm 0.119$ Jy (Skrutskie et al. 2006), then we adopt the satellite-to-star ratio $R = 2.035 \times 10^{-4}$ from the GPI DRP (Wang et al. 2014; Perrin et al. 2014) and average satellite spot total flux $S = (1.12 \pm 0.17) \times 10^3$ count s $^{-1}$ in the FITS file header. Combining these, we obtain a conversion factor of

$$F_\nu = \frac{RF_*}{S} = (6.87 \pm 1.06) \times 10^{-7} \text{ Jy s count}^{-1}.$$

We apply that conversion factor and normalize the local Stokes maps by the exposure time and pixel area to obtain the disk surface brightness data in units of Jy arcsec $^{-2}$. The flux-calibrated data are then geometrically corrected and smoothed by convolving with a Gaussian kernel ($\sigma = 14.166$ mas, i.e., the scale of 1 GPI pixel; Millar-Blanchaer et al. 2016) to remove the high spatial frequency noise that impacts regions smaller than the Nyquist-sampled PSF of GPI.

2.2. Noise Estimation

Based on different PSF subtraction methods for each data set, we estimate the uncertainties as follows.

NMF and cRDI (STIS, NICMOS). We estimate the noise in these reductions from the ensemble of science frames to probe the temporal variations from frame to frame (16 NICMOS frames, 64 and 12 STIS frames at the two different positions on the mask; see Table 2). We proceed as follows. After subtraction of the PSF, we compute the pixelwise standard deviation across the science frames to obtain the typical noise map per frame, which is used to account for the noise added by PSF subtraction. We then replicate this noise map for N_{frame} times and derotate each with the same angle as each science frame. We obtain the final noise map by computing the square

Table 3
Reduction Parameters

	NICMOS	STIS	GPI
Classical RDI	N ^a	Y ^a	N
Reference (classical)	N	HD 196081	N
PSF reference no.	85	45 (A0.6) 84 (A1.0)	100
KLIP truncation no.	19	N	20
NMF truncation ^b no.	10	10 (A0.6) 10 (A1.0)	20
Polarimetry	N	N	Y

Notes.^a Y: performed; N: not performed or unavailable.^b The NMF reductions become stable with more than 10 components.

root of the quadratic sum of these derotated noise maps. See Figure 2 for the S/N maps.

KLIP (NICMOS). For the NICMOS-KLIP reduction, we use the ALICE library of reference stars that are processed identically to HD 191089 to estimate the residual speckle noise. For each HD 191089 image (16 total), we first select 25% of the most-correlated images in the reference library (i.e., 212 reference images). In this way, we obtain 413 reference images that are correlated with at least one HD 191089 image (i.e., $\sim 50\%$ of the entire library). We split these 413 images into 25 groups, each containing 16 images (with the leftovers randomly discarded). In each group, the 16 images are treated as the mock target images to simulate 16 HD 191089 nondetection images. For one mock target image, we first identify the real target that was observed, then we remove the images that are taken on the same real target from the reference library to avoid self-subtraction. We then use the updated reference library to perform KLIP subtraction of the mock image following the identical procedure as for HD 191089 (i.e., 19 eigenmodes from the 84 most-correlated references). The 16 reduced mock images are then derotated using the same orientation angles as the ones in the HD 191089 observations. For each group, we take the elementwise mean of the 16 rotated reduced mock target images as the mock result for one realization of HD 191089 nondetection. We then obtain a total of 25 realizations of nondetections using the 25 full groups from the 413 mock images. We take the elementwise standard deviation from the 25 mock nondetections as the noise map for our NICMOS-KLIP reduction.

Polarimetry (GPI). For the GPI Q_ϕ map, we used the convolved U_ϕ image as a proxy for the uncertainty (Millar-Blanchaer et al. 2015). To obtain the noise map, for each angular separation to the star, we calculate the standard

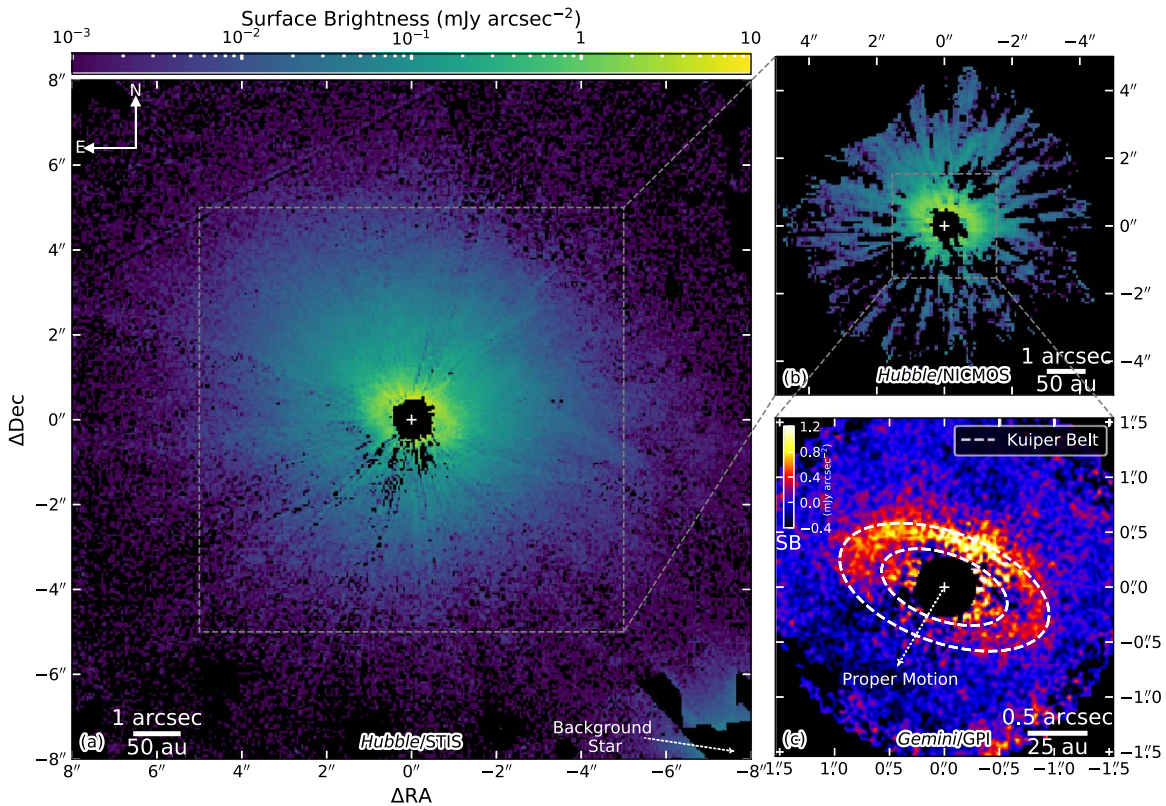


Figure 1. The 2014 *HST*/STIS (cRDI, $0.58 \mu\text{m}$), 2006 *HST*/NICMOS (NMF, $1.12 \mu\text{m}$), and 2015 *Gemini*/GPI (Q_ϕ , $1.65 \mu\text{m}$) images of the HD 191089 debris disk. The outer fanlike structure is unambiguously recovered for the first time with STIS and NICMOS. The GPI Q_ϕ image provides the highest spatial resolution. The following should also be noted. (1) The star positions are marked with white plus signs, and the corresponding S/N maps are shown in Figure 2. (2) To mask out regions of significant residual artifacts, a numerical mask with twice the radius of the GPI mask is used. (3) The units of these images are mJy arcsec^{-2} . The STIS and NICMOS data are shown in the same log scale to better display the halo, while the GPI data are shown in linear scale to best reveal the ring. (4) For scale, the solar system Kuiper Belt (30–50 au; Stern & Colwell 1997) is illustrated with dashed ellipses on the GPI image, and the proper motion of HD 191089 is marked with a white dotted arrow with length corresponding to 10 yr motion from *Gaia* DR2.

deviation of an annulus with 3 pixel width in the convolved U_ϕ image as the noise. This noise map provides a reasonable estimation of PSF subtraction residuals, photon and detector noise, and residual instrumental polarization (Millar-Blanchaer et al. 2015). See Figure 3 for the convolved Q_ϕ and U_ϕ images used for signal-to-noise ratio (S/N) calculation.

2.3. Comparison of the Reduction Methods

The HD 191089 debris disk is detected in all of our *HST* and GPI observations. Here we compare the quality of the different reductions and discuss their relative merits for measuring different quantities of interest.

STIS. The disk is detected in the STIS data with high morphological and photometric fidelity in both the cRDI and NMF reductions (Figure 4). The system shows a bright parent belt, surrounded by a faint and diffuse halo detected up to $\sim 6''$ from the star. These features are detected with a dynamic range of 3 orders of magnitude, with a peak ring surface brightness of $\sim 1 \text{ mJy arcsec}^{-2}$ and the diffuse halo detected down to a few $\mu\text{Jy arcsec}^{-2}$. Theoretically, unlike KLIP reduction, both the cRDI and NMF reduction methods are free from oversubtraction caused by overfitting disk features using the references. This was discussed in Ren et al. (2018b) and is confirmed in Ren et al. (2018a), where the NMF method is able to successfully retrieve the spiral arms for the MWC 758 system.

For HD 191089, the bright disk and excellent cRDI quality enable a quantitative comparison between cRDI and NMF. In

Figure 4, we present the reduction results from different methods for both the STIS and NICMOS data for a comparison between the methods. For the STIS data, the ring surface brightness is consistent within $\pm 10\%$ between cRDI and NMF. The NMF achieves higher S/Ns along the major and minor axes of the disk by a factor of ~ 3 , i.e., the regions containing coronagraphically unapodized diffraction spikes, which are marked by red ellipses in Figure 5.

NICMOS. The halo component discovered in STIS is confirmed in the NICMOS-NMF image. The NICMOS-KLIP image in Figure 4 is able to recover the halo that was not observed in the original discovery image (Soummer et al. 2014). The new reduction is obtained with a larger field of view and fewer KLIP components. In retrospect, it is not surprising that the original reduction by Soummer et al. (2014) did not detect the halo: the KLIP method is based on principal component analysis, which requires mean subtraction for each individual image. When modeling the target with KLIP, the reduced image also has zero mean, which offsets the faint halo as negative background; thus, the halo cannot be recovered with positive signals. In addition, to maximize the removal of the starlight, a large number of KLIP components was used in Soummer et al. (2014). In this case, KLIP also removed the halo because its extended diffuse structure resembles PSF wing.

The NMF independently confirms the existence of the halo in the NICMOS data while recovering the ring regardless of increasing component number. The NMF component basis is nonnegative—thus, not orthogonal—and it does not perform

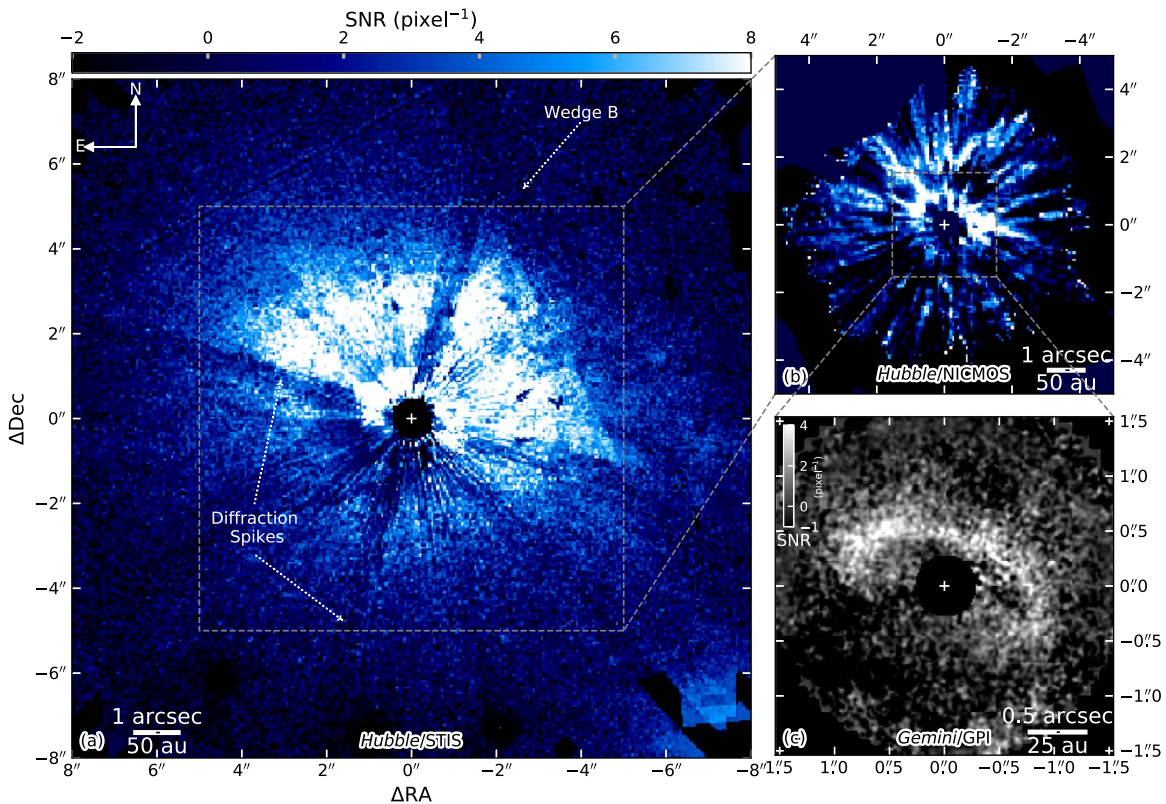


Figure 2. The S/N maps of the reduction results in Figure 1. In the STIS S/N map, the presence of Wedge B truncates the halo on the northwest side, and the coronagraphically unapodized diffraction spikes reduce the S/N. The following should also be noted. (1) The STIS and NICMOS data are shown in the same scale. (2) Unless otherwise specified, the correlated noises are not estimated in this paper. (3) The instrument pixel scales are illustrated by black dashes at the center of the scale bars.

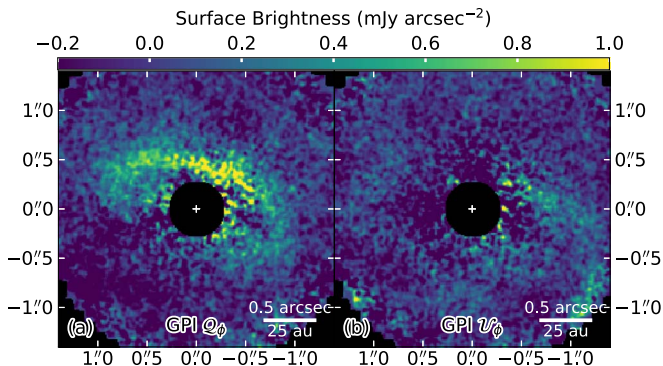


Figure 3. Smoothed and octopole-removed GPI H -band (a) Q_ϕ and (b) U_ϕ maps.

direct projection of vectors as KLIP, which falls into the overfitting regime, but instead searches for the best nonnegative combination of nonnegative NMF components. The halo does not resemble the NMF components that are used to model the PSF wings, and thus it remains in the residual after PSF subtraction.

In the NICMOS results in Figure 4, the NIMCOS-NMF image has about two times the ring surface brightness of the NICMOS-KLIP image, supporting the expected behavior of the two methods: KLIP’s overfitting because of direct vector projection cannot be avoided, even with a small number of eigenmodes, and the mean-subtraction offset reduces the overall flux of the system. In contrast, NMF is expected to preserve the surface brightness of the NICMOS disk as for the STIS data.

GPI in total intensity. We attempted to detect the disk in total intensity from this same data set with MRDI: for each polarization-direction pair of H -Pol exposures, we derive a single total intensity image. For starlight subtraction, we select the 100 most-correlated GPI H -band PSFs from the library of 15,847 exposures, then perform KLIP and NMF reductions. We present the S/N maps of the null detections in Figure 5: we do not detect the disk or any point source using either KLIP or NMF. We hypothesize that a larger or better reference library is needed to obtain the best match for HD 191089.

To estimate an upper limit on the surface brightness for the disk, we calculate the noise map for the GPI-KLIP image using the standard deviation across the individual reduced images. We estimate a 1σ uncertainty of ~ 3 mJy arcsec $^{-2}$ at the minor axis and ~ 1 mJy arcsec $^{-2}$ along the major axis. Assuming gray scattering for the dust in the ring seen with the NICMOS F110W filter and GPI H band, the NICMOS-NMF result will produce surface brightnesses of ~ 2.2 and ~ 1.0 mJy arcsec $^{-2}$, respectively. Therefore, even the disk is not removed by the reduction methods; it is below a detection threshold of 1σ (which corresponds to a total S/N of 5 for extended structure spanning ~ 25 pixels; Debes et al. 2019). In this way, its detectability is beyond the limit of the current methods with the current GPI H -band PSF library.

3. Disk Morphology and Measurement

3.1. Strategy to Measure Disk and Dust Properties

For the ring, the GPI Q_ϕ map provides the highest spatial sampling, with STIS and NICMOS offering total intensity

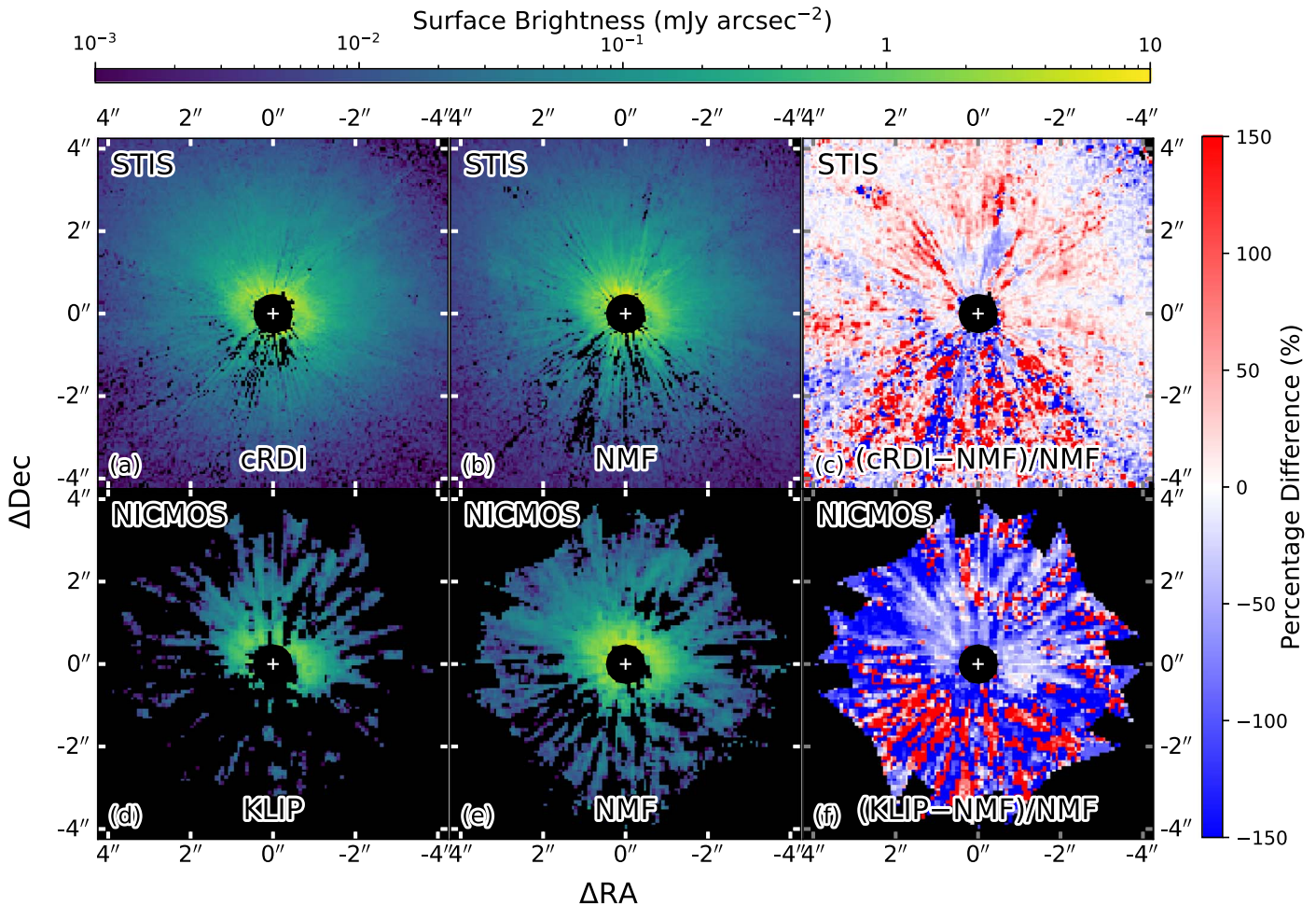


Figure 4. Comparison of the HD 191089 ring between the NMF reduction (middle) and the other reduction results (left). The right column shows the percentage difference from the NMF image when it is subtracted from the image in the left column. For the STIS data (top), the classical RDI and NMF image photometry agree to within $\sim 10\%$ pixel^{-1} for the ring; for the NICMOS data (bottom), NMF recovers nearly twice the disk flux recovered by KLIP. See Figure 5 for the S/N maps.

observations at different wavelengths. Using the GPI Q_ϕ map, we obtain the geometric structure for the ring in Section 3.3.1, including inclination, semimajor axis, position angle, ring center position, and eccentricity of the deprojected ring. With the geometric information and the parallactic distance to HD 191089, we are able to calculate the average intensity of the disk as a function of physical distance to the host star (i.e., the radial profile).

For the halo, the STIS total intensity image is able to probe the largest spatial extent with a larger field of view and high sensitivity. Assuming that the halo is coplanar with the ring, we can measure the radial profile for the halo, which will help to identify whether the halo is a geometric extension of the ring by comparing their outer power-law indices. We use the cRDI reduction for this purpose, since it covers a larger field of view than the NMF reduction obtained from the fixed-width STIS archive in Ren et al. (2017).

For both the ring and the halo, if we assume that they are coplanar, then we can measure the disk surface brightness as a function of scattering angle—the SPF. The SPF is related to properties of the dust and therefore provides insights into the composition, size distribution, and minimum dust size for the system, even though this information is degenerate. To extract the information for the dust, we adopt the spatial distribution information from GPI Q_ϕ measurements, then use radiative

transfer modeling tools to model the ring. Given that the ring is well resolved with all three instruments, the SPFs at different wavelengths are expected to help constrain the dust size and composition.

3.2. Mathematical Description

The spatial distribution of the dust in the debris disk can be parameterized using a three-dimensional function in cylindrical coordinates: the radial distribution in the midplane and the vertical distribution along the axis perpendicular to the midplane. Along the radial direction, the dust in the system follows a combination of two power laws,

$$\rho(r) \propto \left\{ \left(\frac{r}{r_c} \right)^{-2\alpha_{\text{in}}} + \left(\frac{r}{r_c} \right)^{-2\alpha_{\text{out}}} \right\}^{-\frac{1}{2}}, \quad (1)$$

where $\alpha_{\text{in}} > 0$ and $\alpha_{\text{out}} < 0$ approximate the midplane dust density power-law indices interior and exterior to $r = r_c$ (Augereau et al. 1999). Along the normal direction of the disk midplane, the dust follows a Gaussian dispersion form, i.e.,

$$Z(r, z) \propto \exp \left[- \left(\frac{z}{\zeta(r)} \right)^2 \right], \quad (2)$$

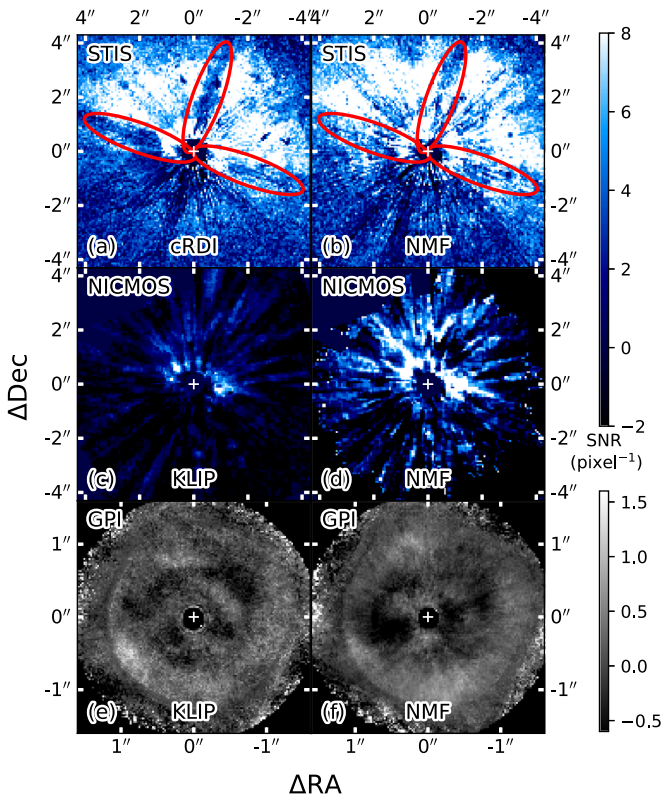


Figure 5. The S/N maps of the reduction results with different methods. For the STIS image, both cRDI and NMF reach similar S/N levels, and the regions marked by red ellipses in NMF have about three times the S/N in the cRDI result. For the NICMOS image, NMF is able to recover higher S/N than KLIP. For the GPI image, neither of the methods are able to extract the disk structure.

with

$$\zeta(r) = hr^\beta, \quad (3)$$

where

$$\beta = 1 \quad (4)$$

for a nonflared debris disk. For the HD 191089 system, $h = 0.04$ is adopted from the vertical structure study (Thébaud 2009).

The power-law index for the surface density radial profile is then (Augereau et al. 1999)

$$\Gamma = \alpha + \beta, \quad (5)$$

where α is α_{in} or α_{out} in Equation (1), with Γ being Γ_{in} or Γ_{out} as the corresponding indices.

Since illumination decreases as a function of distance from the star, our images must be corrected for illumination effects before the surface density can be measured. The relationship between the surface brightness power-law index, γ , and the surface density power-law index, Γ , is

$$\gamma = \Gamma - 2, \quad (6)$$

where γ is γ_{in} or γ_{out} , corresponding with Γ being Γ_{in} or Γ_{out} .

The radial distribution of the system in Equation (1) is supplemented with two extra parameters, r_{in} and r_{out} , which are the cutoff radii. They are introduced to describe the clearing of materials interior and exterior to the disk, i.e., when $r < r_{\text{in}}$ or $r > r_{\text{out}}$, $\rho(r) = 0$.

3.3. Disk Morphology

3.3.1. Ellipse Parameters

We measure the geometric parameters for the disk from the GPI Q_ϕ observation because it has the smallest pixels and is less biased by the reduction methods.

We assume that the peak radial polarized surface density matches the peak radial particle density and use the Debris Ring Analyzer package from Stark et al. (2014) to fit the peak intensity of the ring in 10° azimuthal wedges by minimizing the χ^2 value between the observation and an ellipse model, and we quantify the uncertainties by assessing the change of the χ^2 values for the corresponding degrees of freedom on a grid of the explored parameters (Choquet et al. 2018).

We measure an inclination⁴⁹ of $\theta_{\text{inc}} = 59^\circ_{-2^\circ}^{+4^\circ}$ from face-on, a semimajor axis of 45_{-1}^{+2} au, and a position angle of $\theta_{\text{PA}} = 70^\circ_{-3^\circ}^{+4^\circ}$ from north to east for the major axis. There is no significant offset between the location of the star and the center of the ring (3σ upper limit; 8 au). The 3σ upper limit for the eccentricity of the deprojected ellipse is 0.3.

3.3.2. Radial Distribution

We measure the surface brightness power-law indices by averaging the flux density at the same stellocentric radius in the highest-S/N regions. Although this approach implicitly assumes isotropic scattering, which is a likely incorrect assumption, we tested it by performing the fit in narrow wedges (e.g., along the minor or major axis) and obtained consistent results, indicating that the scattering anisotropy does not change our results significantly. We plot the surface brightness radial profiles for the ring and halo in Figure 6 and summarize the results in Table 4. For both the ring and the halo, we define the inner and outer cutoff radii, r_{in} and r_{out} , as the radii for which the corresponding average surface brightness is consistent with zero at the 1σ level.

We measure the following parameters for the ring from the GPI Q_ϕ observation: $\gamma_{\text{in}} = 4.9 \pm 0.2$, $r_c = 43.6 \pm 0.3$ au, and $\gamma_{\text{out}} = -6.1 \pm 0.2$.⁵⁰ We also fit a Gaussian ring to the deprojected Q_ϕ surface density map, and the ring is centered at $r_{\text{center}} = 45.6 \pm 0.2$ au with a 24.9 ± 0.4 au FWHM. We do not report the results from STIS or NICMOS, since they have low spatial sampling and are noisy near the corresponding IWAs.

We measure the geometric parameters for the halo from the STIS data because they cover the largest field of view. We measure a surface brightness power-law index of $\gamma_{\text{out}} = -2.68 \pm 0.04$. The power-law indices measured at different position angles are also consistent with the integrated measurement within 1σ . Therefore, we report the integrated radial profiles to reduce systematic uncertainty.

In the above calculation, we have assumed a flat disk (i.e., $h \ll 1$); however, the disk is not perfectly flat, and the line of sight passes through different radii at different heights. Under this scenario, for a nonflared disk, we calculate that the radial separation will be modified by multiplicative factors of

$$(1 \pm 0.5h \tan \theta_{\text{inc}})^{-1}. \quad (7)$$

⁴⁹ The uncertainties calculated in this paper are 1σ unless otherwise specified.

⁵⁰ For the input data, we have taken both x - and y -uncertainty into account with the orthogonal distance regression method (Boggs et al. 1989).

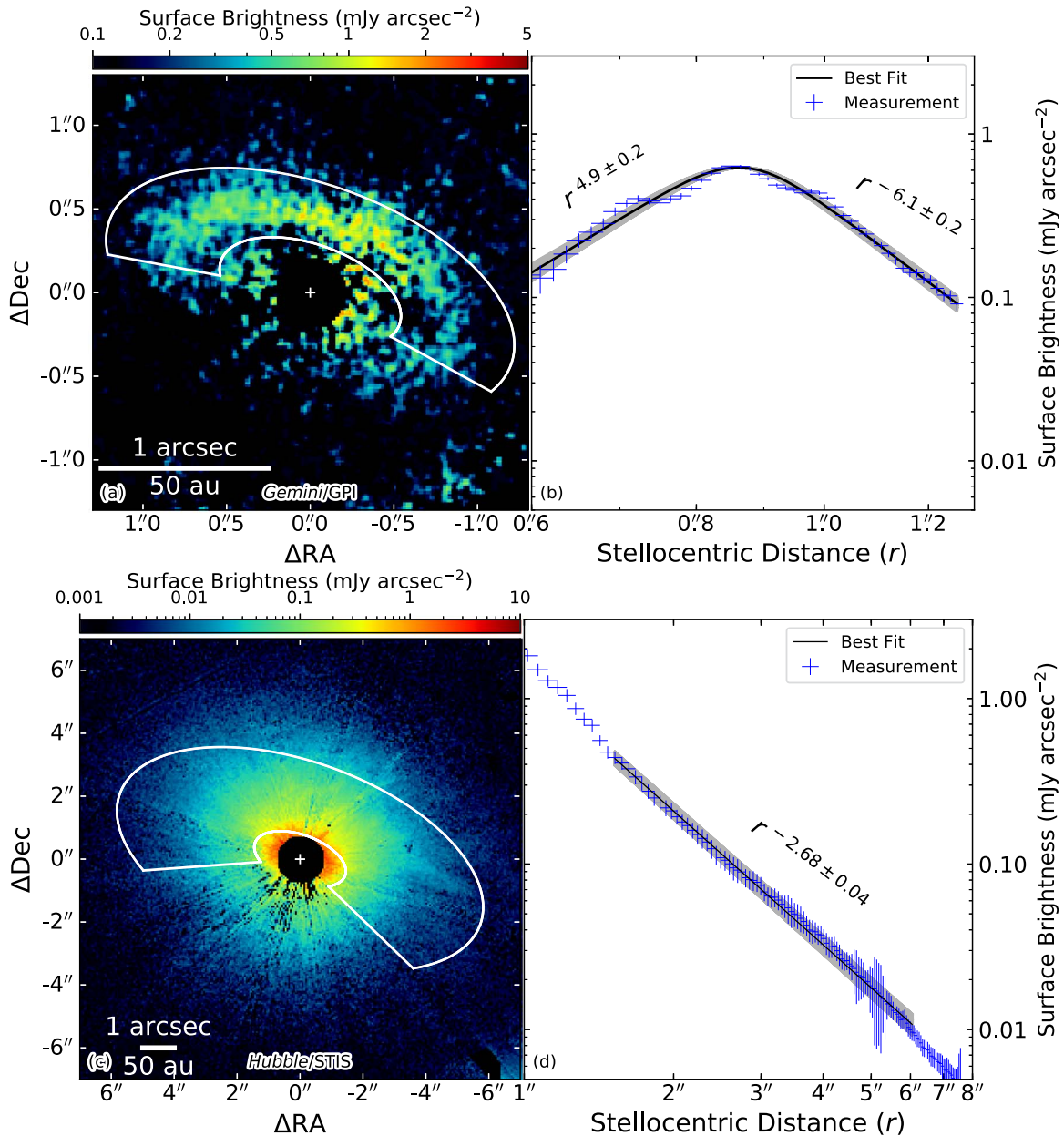


Figure 6. Left: disk images. Right: average flux density radial profiles and power-law fits for the regions enclosed by white lines (uniformly sampled in stellocentric distances). For panels (b) and (d), the shaded areas are the 1σ intervals corresponding to the fitted parameters (γ_{in} , γ_{out} , and r_c). The γ_{out} parameter for the ring and halo differs by more than 10σ , strongly indicating the different spatial distributions of the two components.

For the HD 191089 system, these line-of-sight intersections increase the uncertainties by $\sim 3\%$ for $h = 0.04$. Therefore, the approximation of a flat disk will not bias the results for a disk with small scale height. For a continuous vertical distribution of the dust that is following a Gaussian decay, this effect is then an upper limit, since most of the scatterers are close to the midplane. We thus ignore this effect, given its model-dependent minor impact on the uncertainties.

We find that the radial power-law indices, γ_{out} , for the ring and halo differ by $>10\sigma$. Despite the physical connection between the ring and the halo, although the two power-law indices are measured at different wavelengths, when the radial distribution of the dust is wavelength-independent, the indices are indicating that the halo is not a geometrical extension of the ring's outer part.

3.4. SPF

Hughes et al. (2018) summarized the SPFs for different systems including zodiacal dust and debris disks and found a tentative universal SPF trend for the dust in debris disks. To further investigate the similarities and differences of SPFs in different systems, we first derive the uncertainty for the scattering angles and the SPFs in Appendix A, then measure the empirical SPFs for the ring and halo for our HD 191089 observations.

For the ring and halo, we present in Figure 7 the SPFs averaged for both sides (i.e., the NE and SW sides) using STIS-cRDI and NICMOS-NMF results to minimize oversubtraction. We observe different trends of the SPFs between the ring and the halo: in the STIS data, the halo is more forward- and backward-scattering than the ring; in the halo, the backward

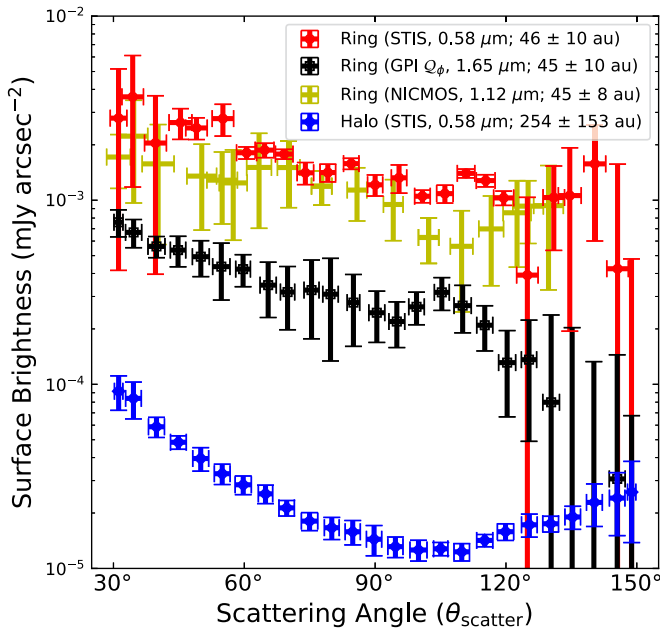


Figure 7. The SPFs for STIS-cRDI and NICMOS-NMF data and the polarized phase function for the GPI Q_ϕ data. The SPF for the halo of the STIS data is averaged from multiple SPFs at different stellocentric separations, thus minimizing the illumination and radial profile effects. See Figure 10 for a linear-scale plot. Note that the radial extent of the ring is defined by the GPI Q_ϕ image, and that of the other instruments is different due to pixel size.

Table 4
Disk Morphology Parameters

Parameter	Ring	Halo	Meaning
Instrument	GPI	STIS	
θ_{inc}^a	$59^{+4}_{-2}^\circ$	59^{ob}	Disk midplane inclination from face-on
θ_{PA}^a	$70^{+4}_{-3}^\circ$	70^{ob}	Position angle for major axis (N to E)
γ_{in}^c	4.9 ± 0.2	... ^d	Surface brightness power-law indices
γ_{out}^c	-6.1 ± 0.2	-2.68 ± 0.04	
r_c^c	43.6 ± 0.3 au	... ^d	r_c in Equation (1)
r_{in}^c	26 ± 4 au	... ^d	Inner and outer clearing radii
r_{out}^c	78 ± 14 au	640 ± 130 au	
r_{center}	45.6 ± 0.2 au	... ^d	Peak position and FWHM of a Gaussian ring
FWHM	24.9 ± 0.4 au	... ^d	

Notes.

^a Fitted with Debris Ring Analyzer (Stark et al. 2014).

^b Values adopted from the GPI results.

^c Fitted for Equations (1) and (6).

^d Unconstrained from the STIS image.

scattering is less strong than the forward trend. In addition, for the phase functions of the ring, the GPI Q_ϕ polarized-light image and STIS and NICMOS total intensity images have similar trends.

We measure the polarization fraction for the ring using the GPI Q_ϕ and NICMOS-NMF images. Given the fact that we cannot recover the ring in total intensity with GPI H -band observations at $1.65 \mu\text{m}$ (Section 2.3), we instead use the

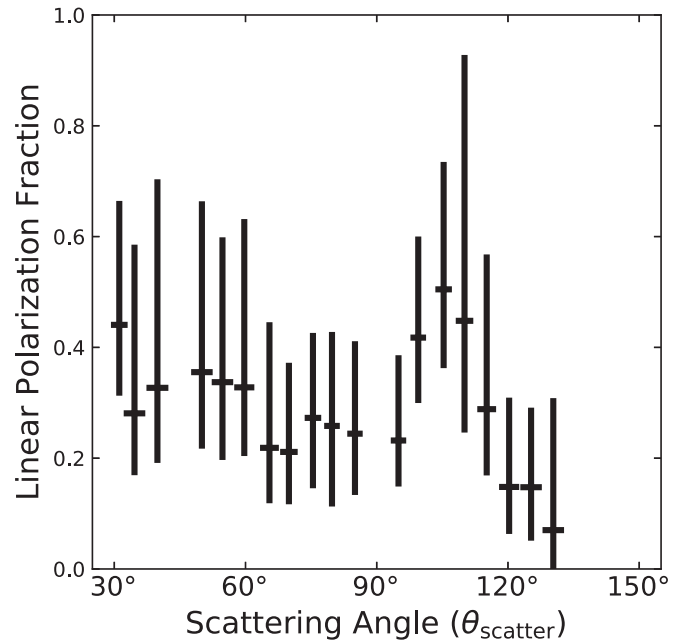


Figure 8. Polarization fraction for the ring as a function of scattering angle. The data are extracted from the ratio between the GPI Q_ϕ ($\sim 1.65 \mu\text{m}$) and NICMOS-NMF ($\sim 1.12 \mu\text{m}$) surface brightness profiles in Figure 7. We do not observe a clear trend of polarization fraction. However, it is possible that the polarization fraction peaks at $\sim 110^\circ$.

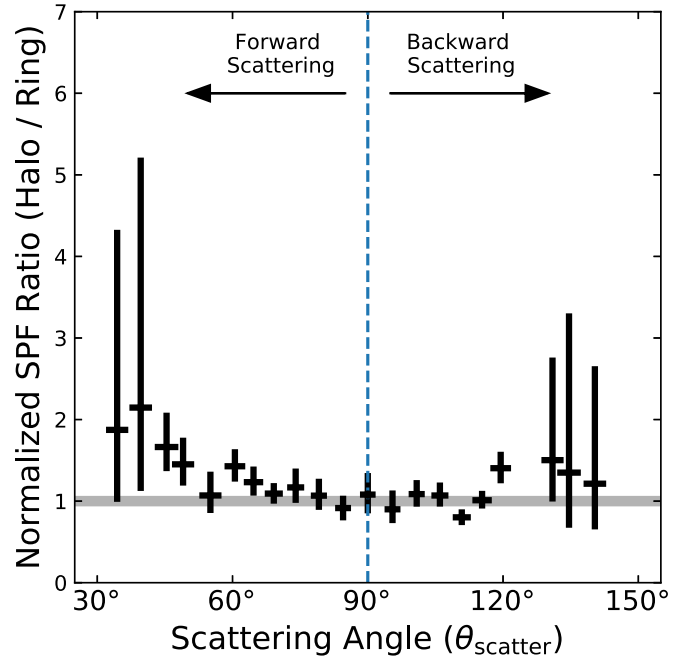


Figure 9. Normalized SPF ratios for the STIS data. The ratios are obtained by dividing the normalized SPF of the halo by that of the ring. The halo is likely both more forward- and backward-scattering in the probed scattering angles.

$1.12 \mu\text{m}$ NICMOS-NMF observation that is both close to the GPI wavelengths and has less of an oversubtraction effect. The polarization fractions derived from GPI Q_ϕ and NICMOS-NMF images are around 20%–40%, with no clear trend (Figure 8). The polarization fraction is possibly peaking at $\sim 110^\circ$; however, it cannot be as firmly established as in

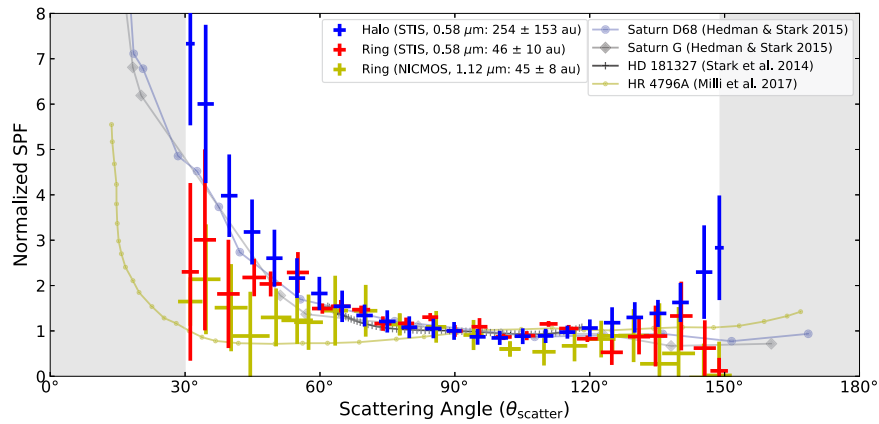


Figure 10. Normalized SPFs for the STIS and NICMOS total intensity data. The red and yellow error bars are the SPFs of the ring in the STIS-cRDI and NICMOS-NMF data, and the blue ones are for the halo in the STIS data. From the SPFs, the ring and halo are composed of two distinct populations of dust, with the halo dust more forward- and backward-scattering. For comparison, the observed SPFs for other systems are also plotted with lines. Note that due to the inclination of the HD 191089 system, the scattering angles in the shaded areas are not probed.

previous measurements (e.g., Perrin et al. 2014; Frattin et al. 2019; Milli et al. 2019). To better constrain the polarized fraction values, we need *H*-band total intensity observations to rule out the wavelength-dependent effect.

To compare SPFs in the STIS image, we first normalize the SPFs by dividing their average surface brightness at $90^\circ \pm 10^\circ$ scattering angle. We then divide the normalized halo SPF by that of the ring to illustrate the difference. In Figure 9, the halo is likely both more forward- and backward-scattering in the probed scattering angles.

To compare the HD 191089 SPFs with the ones in the literature, we present the normalized SPFs in linear scale for selected samples including both solar system objects (Saturn’s D68 and G rings; Hedman & Stark 2015) and circumstellar disk systems (HD 181327; Stark et al. 2014; HR 4796 A; Milli et al. 2017) in Figure 10. Comparing with the previous studies, the HD 191089 ring SPF lies between the Saturn rings and the other samples, while its halo SPF lies above the Saturn rings.

3.5. Disk Color

Using the *HST* disk images, we calculate the color of the dust as follows. We first bin the the $1.12 \mu\text{m}$ NICMOS-NMF image and the $0.58 \mu\text{m}$ STIS-NMF image to two images with a pixel size of ~ 150 mas to reduce correlated noise. We then divide the binned images by the corresponding `pysynphot` (STScI Development Team 2013) NICMOS or STIS counts of a $T = 6450$ K blackbody to obtain the magnitude per pixel. We calculate the difference of the two magnitude maps and present the radial profile along the ansae of the system in Figure 11.

For the ring, the dust scatters $\sim 25\%$ more light ($\Delta\text{mag} \approx 0.25$) within the NICMOS F110W passband than in the STIS 50CCD, showing a red scattering property. For the halo, $\Delta\text{mag} \approx -1$. Dust in the halo is expected to be generated in the ring through collisional cascade, then the smaller dust that is more sensitive to radiation pressure migrates outward to form the halo (e.g., Strubbe & Chiang 2006; Thébaud & Wu 2008). Assuming that scattered-light images primarily probe the cross sections of the dust whose sizes are comparable to the observing wavelength, this red-to-blue trend from the ring to the halo in Figure 11 is consistent with this scenario.

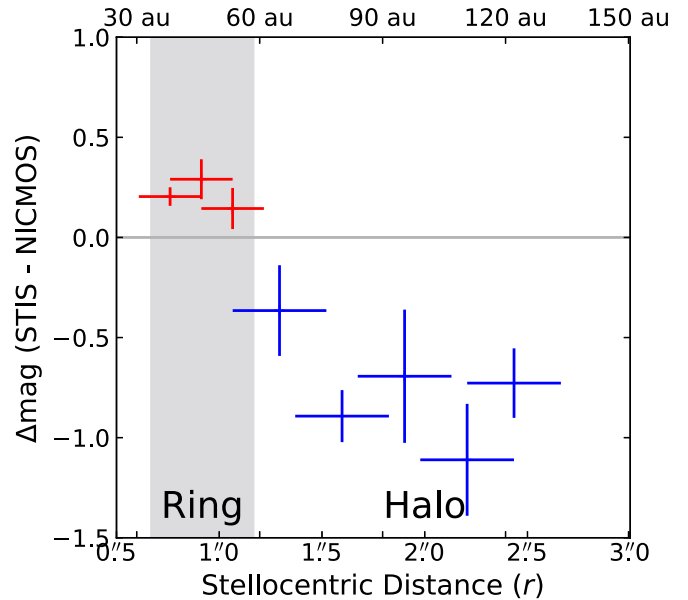


Figure 11. Average magnitude difference relative to the star along the ansae between the $0.58 \mu\text{m}$ STIS-NMF and the $1.12 \mu\text{m}$ NICMOS-NMF observations. The ring (shaded area; the FWHM of the Gaussian ring in Table 4) scatters more flux in the longer NICMOS wavelengths, indicating the red color of the dust. The halo has the opposite trend and instead scatters more flux in the shorter STIS wavelengths. The trend of the ratio is consistent with the ring containing larger dust than the halo.

4. Disk Modeling

4.1. Radiative Transfer Modeling Tool

We model the HD 191089 ring with the `MCFOST` (Pinte et al. 2006, 2009) radiative transfer modeling code and describe the dust using a distribution of hollow spheres (DHS; Min et al. 2003, 2005, 2007). As a derivative of the Mie theory, where the dust grains are assumed to be spherical (Mie 1908), DHS adopts vacuum centers for these spherical dust grains. To approximate small irregularly shaped dust, the only additional parameter in DHS from Mie—maximum vacuum fraction (f_{max})—parameterizes the central vacuum fraction in the dust that is uniformly ranging from zero to f_{max} . The DHS has been used to successfully reproduce the SPF of linearly polarized

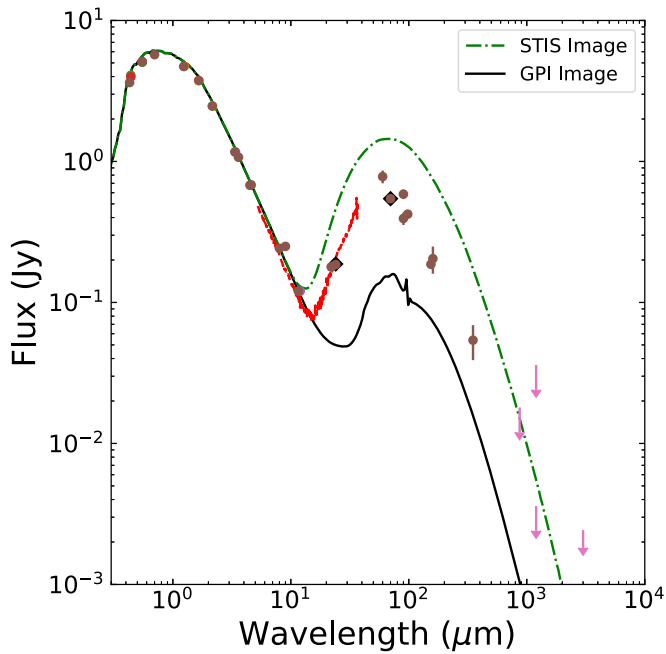


Figure 12. Observed SED and SED models for HD 191089. Green dashed-dotted line: SED generated using the best-fit STIS parameters. Black line: SED generated using the best-fit GPI Q_ϕ parameters. Other: observation data obtained from Soummer et al. (2014).

scattered light with incident unpolarized light for quartz particles in the laboratory (Min et al. 2005), characterize the spectral features of the interstellar medium (e.g., Min et al. 2007; Poteet et al. 2015), and better fit the scattering properties of the HR 4796A circumstellar disk system (Milli et al. 2015).

In our study, we adopt the geometrical parameters derived in Section 3.2 for the ring and perform radiative transfer modeling with MCFOST using the DHS theory to probe the dust properties (e.g., dust mass, minimum dust size, composition, porosity, and maximum void fraction). Due to the complex nature of the constituent dust, DHS is a computationally intensive technique, and we thus adopt parallel computation in the Python environment and use the `DebrisDiskFM` package (Ren & Perrin 2018).⁵¹ The framework is developed to efficiently explore debris disk properties through radiative transfer modeling.

`DebrisDiskFM` is based on two software codes. We use MCFOST (version 3.0.33) to generate disk model images using given input parameters. We use `emcee` (version 3.0rc1; Foreman-Mackey et al. 2013), which makes use of a Markov chain Monte Carlo (MCMC) strategy with affine invariant ensemble samplers (Goodman & Weare 2010), to obtain the posterior distributions for these parameters. With the two software codes, we use `DebrisDiskFM` to distribute posterior calculations among multiple computation nodes in a computer cluster,⁵² with each node calculating its own MCFOST models in parallel. Specifically, for each combination of input parameters, we store the model in a unique folder, with the folder named by the hashed string for the array of input parameters. We also append the folder name with a hashed

⁵¹ <https://github.com/seawander/DebrisDiskFM>

⁵² We performed the calculations at the Maryland Advanced Research Computing Center (MARCC): <https://www.marcc.jhu.edu>.

random number, preventing multiple nodes from simultaneously accessing the same folder and causing errors.

4.2. Modeling the Ring

We model the STIS-cRDI and GPI Q_ϕ rings, since they cover the largest wavelength range and have higher data quality. To study the dust properties, we assume the dust is made of different types of grains, each with a pure composition. We adopt the three compositions in Esposito et al. (2018): the amorphous silicate dust (i.e., “astronomical silicates,” denoted by “Si”; Draine & Lee 1984), amorphous carbonaceous dust (denoted by “C”; Rouleau & Martin 1991), and H₂O-dominated ice described in Li & Greenberg (1998) to model the β Pic disk (denoted by “ice”). The size of the dust, a , follows a power-law distribution with index q , i.e.,

$$dN(a) \propto a^{-q} da. \quad (8)$$

The distribution is truncated at a minimum size of a_{\min} , and we set a maximum limit of the dust size, $a_{\max} = 1000 \mu\text{m}$. For the HD 191089 system, we set $q = 3.5$ for the expected dust size distribution for debris disks undergoing collisional cascade (e.g., theory and simulation: Dohnanyi 1969; Pan & Schlichting 2012; observation: MacGregor et al. 2016; Esposito et al. 2018).

In this paper, we probe the following seven parameters of interest through disk modeling:

1. disk mass, M_{disk} , which generally controls the overall brightness of the disk at different wavelengths;
2. porosity;
3. mass fraction for “astronomical silicates,” $f(\text{Si})$;
4. mass fraction for amorphous carbonaceous dust, $f(\text{C})$;
5. mass fraction for ice, $f(\text{ice})$;
6. minimum dust size, a_{\min} ; and
7. maximum void fraction for DHS, f_{\max} .

Given the fact that the composition parameters are interconnected, i.e., $f(\text{Si}) + f(\text{C}) + f(\text{ice}) = 1$, we only explicitly sample $f(\text{Si})$ and $f(\text{C})$. We also set the lower limit for a_{\min} to be $0.5 \mu\text{m}$ based on the calculation of the blowout sizes for different dust compositions by Arnold et al. (2019). In the implementation of MCMC modeling of the system using the `DebrisDiskFM` framework, for a given set of parameters, we first generate two parameter files for MCFOST to represent the spatial sampling and field of view for the three instruments. We then perform radiative transfer modeling with MCFOST, using the DHS theory, to calculate the images for the three instruments at their central wavelengths in Table 2.

To simulate instrument responses, we convolve the disk models with `TinyTim` PSFs (Krist et al. 2011)⁵³ for STIS and a two-dimensional Gaussian profile for GPI (FWHM = 53.8 mas , corresponding to 3.8 times the pixel scale for GPI to match the GPI PSF; Esposito et al. 2018).

We compare the STIS model directly with the STIS-cRDI image. We compare the GPI model with the GPI Q_ϕ image by first converting the Stokes Q and U models to a Q_ϕ model, then comparing the PSF-convolved Q_ϕ model with the observation. With the models and observations, we maximize the following

⁵³ <http://www.stsci.edu/software/tinytim/>

Table 5
Independent Dust Properties Retrieved from Ring Image Modeling

Parameter ^a	Prior ^b	Posterior ^c	
		GPI Q_ϕ	STIS
Image			
$\log_{10} M_{\text{disk}} (M_\odot)$	(-12, -4)	$-7.462_{-0.010}^{+0.015}$	$-6.79_{-0.04}^{+0.03}$
Porosity	(0, 1)	$0.600_{-0.008}^{+0.012}$	$0.01_{-0.01}^{+0.01}$
$f(\text{Si})$	(0, 1)	$0.005_{-0.005}^{+0.016}$	$0.50_{-0.05}^{+0.04}$
$f(\text{C})$	(0, 1)	$0.004_{-0.004}^{+0.011}$	$0.50_{-0.04}^{+0.05}$
$f(\text{ice})^d$		$0.989_{-0.010}^{+0.009}$	0.003^e
$\log_{10} a_{\text{min}} (\mu\text{m})$	(-0.3, 2)	$-0.115_{-0.007}^{+0.013}$	$0.24_{-0.03}^{+0.01}$
f_{max}	(0, 1)	$0.213_{-0.014}^{+0.026}$	0.001^e
χ_ν^2 (GPI best fit)		1.05	240
χ_ν^2 (STIS best fit)		12	10
q		3.5^f	
$\log_{10} a_{\text{max}} (\mu\text{m})$		3^f	
Iteration number		9000 ^f	
Burn-in		2000 ^f	

Notes.

^a The morphological parameters in Table 4 are adopted.

^b The parameters are limited to three decimal digits, with uniform sampling in the prior range. For M_{disk} and a_{min} , they are log-uniformly sampled.

^c 16th, 50th, and 84th percentiles.

^d The mass fraction for ice is $f(\text{ice}) = 1 - f(\text{Si}) - f(\text{C})$; thus, only Si and C are explicitly sampled.

^e 95th percentile.

^f Kept fixed.

log-likelihood function:

$$\log \mathcal{L}(\theta|X_{\text{obs}}) = -\frac{1}{2} \sum_{i=1}^N \left(\frac{X_{\text{obs},i} - X_{\text{model},i}}{\sigma_{\text{obs},i}} \right)^2 - \sum_{i=1}^N \log \sigma_{\text{obs},i} - \frac{N}{2} \log(2\pi). \quad (9)$$

In the above equation, X is a flattened image with N pixels. Subscripts “obs” and “model” denote observation and model, respectively, and $\sigma_{\text{obs},i}$ is the uncertainty for $X_{\text{obs},i}$ at the i th pixel. We only focus on the disk region (i.e., between r_{in} and r_{out} determined by GPI Q_ϕ image) to minimize the influence from the halo. In this paper, we assume that the pixel noise follows a Gaussian distribution, and that all pixels are independent of each other (see, e.g., Wolff et al. 2017, for a proper treatment of correlated pixels).

4.2.1. GPI Q_ϕ Image

One-step GPI. While the ring is resolved with all three instruments, we first only fit the GPI Q_ϕ image to investigate the dust properties. Using the flat priors presented in Table 5, we assign 60 chains to explore the parameter space and run the MCMC modeling procedure for 9000 steps. We discard the first 2000 steps that are identified as the burn-in stage and calculate the posterior distributions using the last 7000 steps (a total of 4.2×10^5 models).

Table 5 reports the credible intervals from the posterior distributions in Figure 13 (generated by `corner`; Foreman-Mackey 2016). We notice the small uncertainties in the results; these uncertainties are underestimated, since the correlated noise is ignored in our likelihood function (e.g., Wolff et al. 2017). In

addition, we also argue that these small uncertainties are also the results from the limited dust models and that various scenarios may lead to small uncertainties (e.g., spatial distribution asymmetries, non-power-law surface density distribution); thus, the inclusion of correlated noise may still not lead to physical interpretations of the retrieved parameters.

4.2.2. STIS Image

One-step STIS. We fit the STIS image using the same priors as for the GPI image. We run MCMC modeling for 9000 steps with 60 chains and discard the first 2000 as burn-in steps, as for the GPI Q_ϕ image. For this approach, we also present the posterior results in Table 5 and Figure 13.

Two-step MCMC. Noticing the two distinct sets of MCMC posteriors for the two images, we try to establish the connection between the GPI and STIS images with a two-step MCMC fitting: we obtain the posterior distributions for the seven variables from the GPI Q_ϕ image, then use them as the priors to fit the STIS image. In this way, we use the GPI posterior distribution as the null hypothesis and test it on the STIS image.

We use the probability integral transform (PIT; Appendix B) to draw samples from the GPI posterior distributions. To find the posterior ranges from the STIS image, we only explore the GPI posteriors between their 2.5th and 97.5th percentiles as an analogy to the conventional level of significance for one parameter (i.e., p -value ≥ 0.05 for double-tailed distribution). We run MCMC modeling for 3500 steps with 60 chains and discard the first 1000 as the burn-in stage.

For the STIS modeling with the PIT approach, we generate the posterior distributions and overplot them on the one-step GPI data in Appendix B.4. From the following, we notice the statistical deviation of the STIS posteriors from the GPI posteriors: (1) the STIS posteriors using PIT are adjacent to the 2.5th- or 97.5th-percentile boundaries of the GPI posteriors, indicating the trend of drifting away from the null hypothesis; and (2) the STIS posteriors using PIT have extremely narrow credible intervals, indicating that there is no statistically preferred solution within the explored intervals.

4.2.3. Implications

We present the results from independent GPI and STIS modelings and discuss the implications as follows.

SED. We generate the SEDs corresponding to the best-fit parameters for the STIS and GPI Q_ϕ images with `MCFOST` and compare them with the observed one in Figure 12. We notice that the SED from the STIS best fit overpredicts the emission from the system, while the SED from the GPI Q_ϕ best fit underpredicts the emission. Even though different sizes of dust dominate the SED and the scattered-light images, the inability to reproduce the observed SED adds more evidence that our study using DHS models cannot provide a consistent model satisfying all observables. For instance, the true dust albedo differs from the one predicted in DHS models.

Mie versus DHS. Although we do not obtain a set of parameters that is able to explain both data sets, we can still focus on the f_{max} parameter (i.e., maximum void fraction for the DHS theory). We argue that it is the most profound parameter that is added to the DHS theory from the Mie theory; the f_{max} parameter approximates dust grains from spheres to aggregate-like structures (Min et al. 2003, 2005, 2007), and we believe it

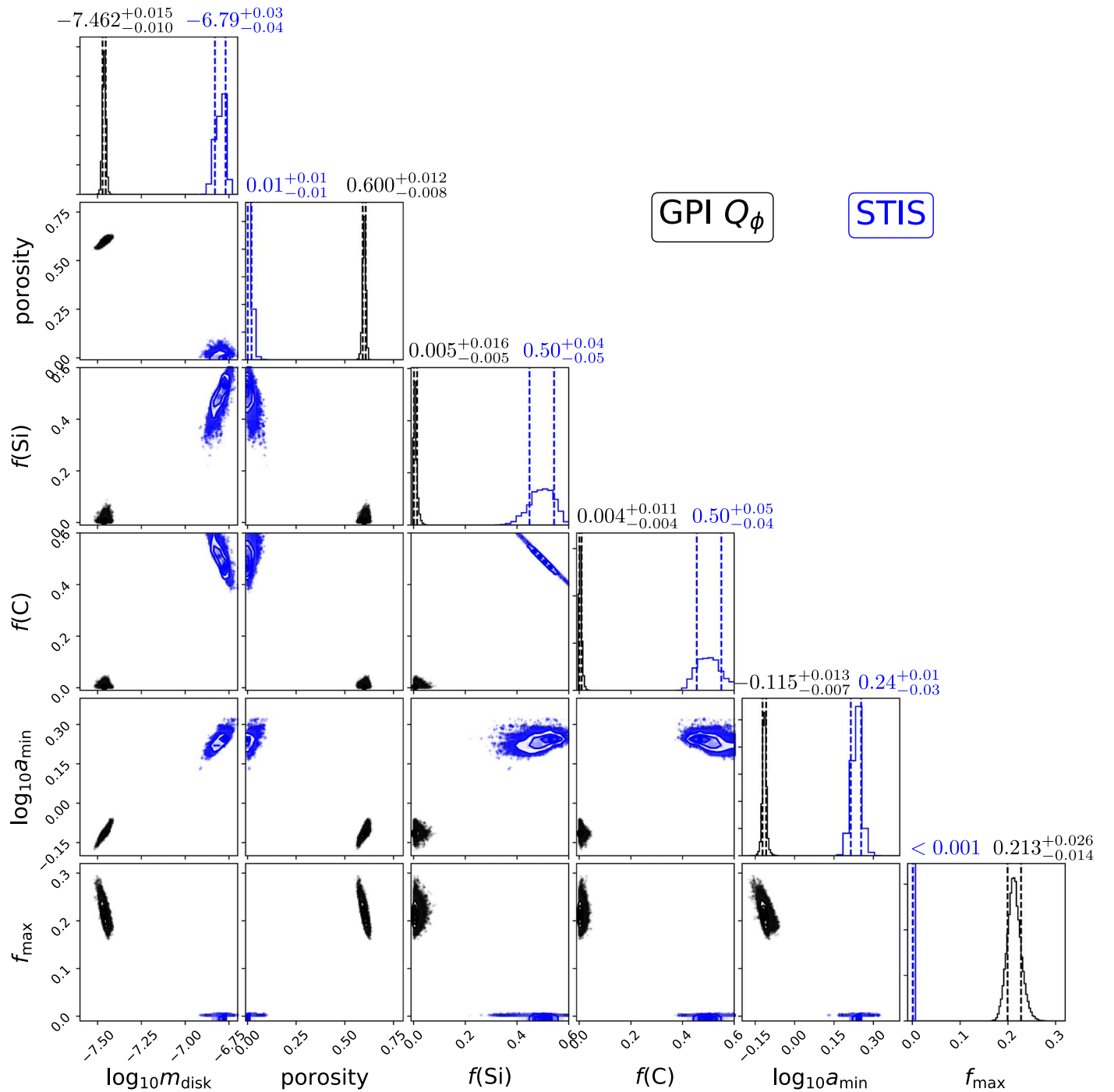


Figure 13. Posterior distribution for the variables in Table 5 used in disk modeling for the GPI Q_ϕ (black) and STIS (blue) images. The vertical dashed lines show the (16th, 84th) percentiles for the data. See Appendix B.4 for the posterior distribution focused on GPI modeling.

is one of the keys to understanding the scattered-light properties of the dust.

For the STIS image in total intensity, we obtain $f_{\max} \approx 0$. In DHS theory, this value corresponds to the Mie theory scenario. For the GPI Q_ϕ image in polarized light, we obtain $f_{\max} \approx 0.21$. In this scenario, the DHS theory is preferred to the Mie theory, and the f_{\max} parameter is smaller than what is in the interstellar dust (e.g., 0.7; Min et al. 2007), suggesting that dust properties are different under various environments. Given that the two data sets differ in two fundamental ways (different wavelengths and total intensity/polarization observation), we

cannot determine which is the root cause of this discrepancy. However, this discrepancy in the f_{\max} parameter is still informative, since it is an approximation of the dust structure—the discrepancy indicates that neither Mie nor DHS is able to well approximate the structure of the dust seen in scattered-light images.

Distinct parameters. In the radiative transfer modeling of the scattered-light images, we retrieve distinct sets of parameters in Table 5 and Figure 13. Although the best fits are not statistically consistent with each other, we categorize the difference in the dust properties in the ring into two groups.

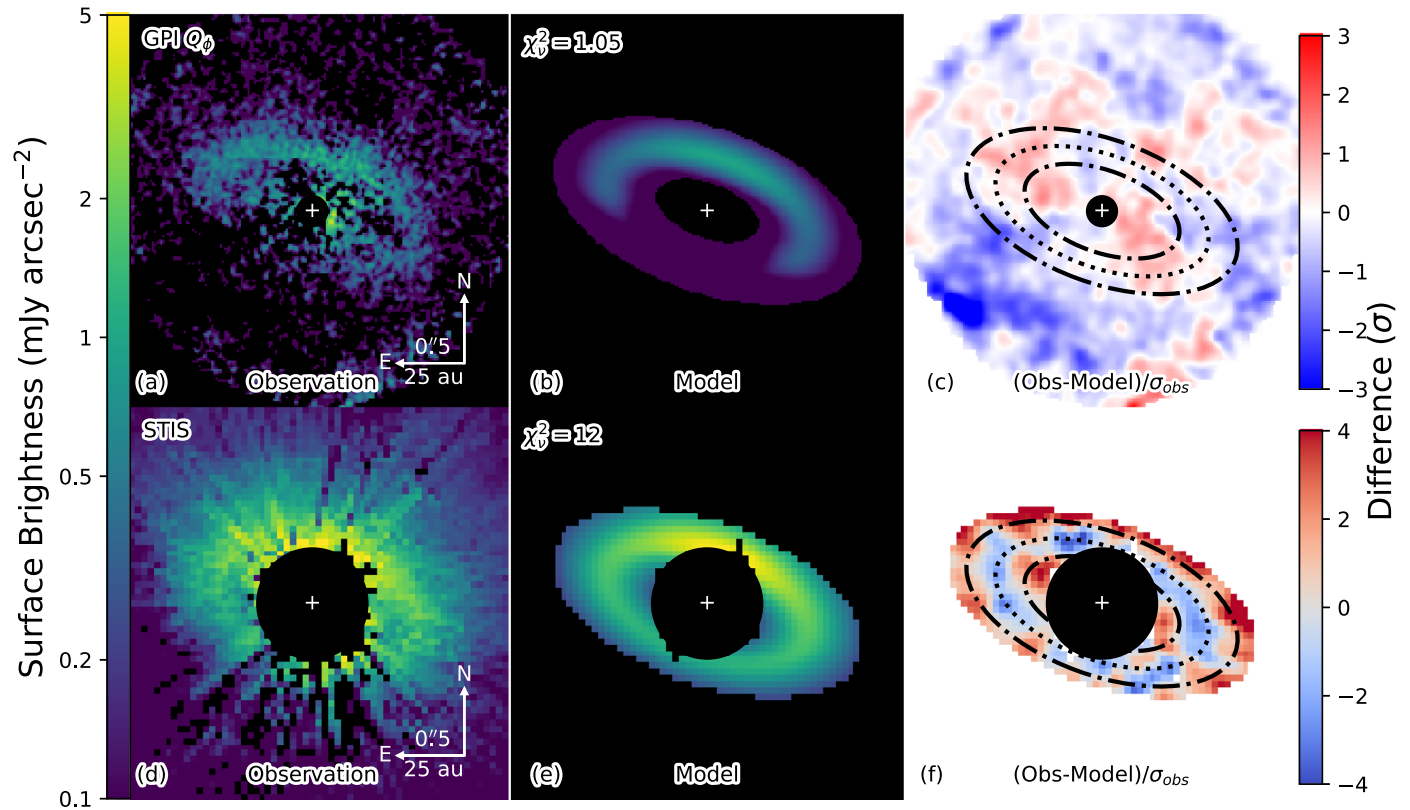


Figure 14. Best-fit results from MCMC fitting (performed individually). Shown are the observation (left), MCFOST model (middle), and residual map (right) for the GPI data (top) and the STIS data (bottom). The reduced χ^2 values are computed for the nonmasked regions, and the masked regions are denoted by black areas in the middle column. On the residual maps (both are smoothed with Gaussian kernels of $\sigma = 50$ mas to remove high-frequency noise), the dotted and dashed-dotted ellipses represent the peak location and FWHM region of the GPI Gaussian ring.

1. Physically possible: minimum dust size. The retrieved minimum dust size is $\sim 0.8 \mu\text{m}$ for GPI Q_ϕ and $\sim 1.7 \mu\text{m}$ for STIS. Both values are within a factor of ~ 2 , and the inclusion of correlated noise in the likelihood function may resolve the discrepancy. The values are reasonably consistent with blowout size calculations, although we caution that these are themselves highly dependent on disk composition, porosity, and aggregate structure—the blowout size for dust can vary by an order of magnitude for different composition and porosity (see the Arnold et al. 2019 calculation for HD 181327, a star similar to HD 191089).
2. Physically impossible: porosity and composition fraction. Specifically, these parameters take values in limited ranges (i.e., from 0% to 100%), and the discrepancy is currently at the $\sim 50\%$ level. Even though the discrepancies for these parameters can be alleviated with larger uncertainties, their physical meaning is then uninformative. A possible solution is to increase the uncertainties to $\sim 50\%$ (assuming the inclusion of correlated noise is able to achieve it); however, that would render these parameters meaningless, since the large uncertainties would not reject any values in the physically plausible values (i.e., from 0% to 100%).

We note that the above parameter values are based only on MCMC fitting results, and neither may be correct given the limitation of DHS or Mie models. Specifically, these models are optimized for spectral fitting (e.g., Min et al. 2007; Potet et al. 2015), but neither model is able to properly constrain the

composition from scattered-light images (e.g., Milli et al. 2019). See Section 5.2 for more discussion on the dust properties retrieved from radiative transfer modeling.

4.2.4. Other Attempts

In addition to the above modeling efforts, we have performed separate modeling attempts with loosened prior constraints.

For GPI. Set the lower limit in the prior for a_{\min} to be $0.01 \mu\text{m}$, and keep q unconstrained. We observed a steeper $q \approx 4.15$ with $a_{\min} \approx 0.02 \mu\text{m}$ to describe the GPI Q_ϕ image, but it still does not recover the STIS flux density. In addition, although this smaller dust is not blown out by radiation pressure, its collisional cascade suppliers (slightly larger dust) are blown out (e.g., Burns et al. 1979; Silsbee & Draine 2016; Arnold et al. 2019); thus, this scenario is not stable.

For GPI and STIS. Simultaneously model the STIS and GPI images with the conditions above (i.e., as in the previous bullet point). However, the best fits indicate a bimodal distribution, with one better recovering the STIS image and the other better recovering the GPI image. In the former model, the GPI Q_ϕ model displays negative polarization at the smallest scattering angles, failing to properly recover the observation; in the latter, the STIS model does not recover the ansae in the observed data.

Based on our modeling efforts, we conclude that the STIS and GPI data sets cannot be consistently reproduced with a single model. As a result, we present our separate models for the GPI Q_ϕ image and the STIS image in Figures 13 and 14.

See Section 5.2 for more discussion on applying the DHS theory to disk modeling.

5. Discussion

5.1. Spatial Distribution

Although our radiative transfer modeling efforts cannot explain the scattering properties of the ring, we are confident in the results of our geometrical analysis, since they are based only on the surface brightness distribution of the system.

5.1.1. Ring Measurables

Ring clearing radii (r_{in} and r_{out}). Churcher et al. (2011) observed the ring at $18.3 \mu\text{m}$, reporting a dust belt from 26 to 84 au⁵⁴, which is consistent with our fitting results of $r_{\text{in}} = 26 \pm 4 \text{ au}$ and $r_{\text{out}} = 78 \pm 14 \text{ au}$ at the 1σ level. The position angle of the major axis, as well as the inclination, is better constrained with our high spatial resolution data in scattered light with GPI.

Brightness asymmetry. For the ring, we are not able to find brightness asymmetry beyond $\sim 10\%$ or 1σ with the GPI and STIS data. Although a tentative $\sim 20\%$ asymmetry was observed at the 1.8σ level in the $18.3 \mu\text{m}$ observation by Churcher et al. (2011), if the dust follows the same spatial distribution at these wavelengths, the $18.3 \mu\text{m}$ emission asymmetry is likely a result of statistical or instrumental fluctuation.

Planet perturber. In the GPI *H*-band total intensity HD 191089 observations, we did not detect any point source (Figure 5). We report 5σ point-source contrast limits of $\sim 1 \times 10^{-5} \sim 3 \times 10^{-6}$ between $0''.3$ and $0''.8$ with the forward-modeling planet detection method to correct for selfsubtraction and oversubtraction in Ruffio et al. (2017). Using these contrast limits, if a planet is shepherding the ring, for a system with an age of 22 Myr and using the evolution tracks in Spiegel & Burrows (2012), its mass is expected be smaller than $\sim 5 M_{\text{Jup}}$.

Using the Morrison & Malhotra (2015) analysis for the outer edge of a planet's chaotic zone and assuming this outer edge is the inner edge of the ring of a debris disk, the upper limit on planet mass can be translated to the lower limit on the semimajor axis of the planet's orbit:

$$a_{\text{p}} = \frac{r_{\text{in}}}{1 + 1.7(5M_{\text{Jup}}/M_{\star})^{0.31}}. \quad (10)$$

When we substitute the measured r_{in} into the above equation, we obtain a lower limit of $a_{\text{p}} = 20 \pm 3 \text{ au}$ for the semimajor axis of the planet.

5.1.2. Ring as an Exo-Kuiper Belt

The spatial extent of the ring ($r_{\text{center}} = 45.6 \pm 0.2 \text{ au}$, $\text{FWHM} = 24.9 \pm 0.4 \text{ au}$ for a Gaussian ring) resembles that of the solar system's Kuiper Belt (30–50 au; Stern & Colwell 1997; Bannister et al. 2018). To investigate the scenario where the ring is an extrasolar version of the Kuiper Belt, which is perturbed by a corresponding planet (i.e., Neptune), we first deproject the S/N map of the GPI observation to a face-on view, then search for possible mean-motion resonance orbits for the inner and outer radii of the disk. Based on Kepler's third law, we search for the period ratios

corresponding to different combinations of stellocentric radii in Figure 15, where the period ratios are mapped to simple fraction values that correspond to the strongest resonance orbits of a hypothetical potential well.

We set the boundary ranges to be consistent with pixelwise $\text{S/N} \approx 1$. Among different combinations of the strongest resonances, we obtain four pairs of 4:3 and 5:2 resonance orbits to resemble the extent of the solar system Neptunian resonance orbits in Chiang et al. (2003). For the other resonance pairs, their boundary ranges are too narrow to cover the GPI disk, these pairs cannot be resolved because of the limitation of instrumental spatial resolution, or these solutions are consistent with the ranges of the 4:3 and 5:2 pairs; therefore, they are not presented or analyzed in this paper.

With the four resonance radii pairs, we are able to compute the location of the potential well (i.e., 1:1 resonance) at $r_{(1:1)} = 0''.60 \pm 0''.02$, corresponding to a stellocentric distance of $r_{(1:1)} = 29.9 \pm 1.2 \text{ au}$. The mean resonance radii and the hypothesized 1:1 orbit of the potential well are shown in Figure 15. To confirm these resonances, deeper high-resolution and high-S/N observations are needed to firmly establish the edges of the ring. If the 1:1 gravitational potential is caused by a planet, it is likely of small mass and requires the future *LUVUOIR* or *HabEx* missions for observation.

5.1.3. Halo: Radial Distribution

Overall distribution. In the STIS data, the halo extends to $r_{\text{out}} = 640 \pm 130 \text{ au}$, with a surface density power-law index of $\Gamma_{\text{out}} = -0.68 \pm 0.04$. This power-law distribution index for the surface density profile is shallower than -1.5 , i.e., the classical expectation for the halo of debris disks (e.g., Strubbe & Chiang 2006; Thébault & Wu 2008). It is also shallower than the power-law index of -1 , which is expected for the steady-state radial motion of the dust (Jewitt & Meech 1987). Using the dust size-free approximation in Jewitt & Meech (1987), a gravity-dominated slowdown of the radial motion of the dust corresponds to a power-law index of -0.5 , and a constant acceleration results in an index of -1.5 .

A power-law index of $-0.68^{+0.04}_{-0.04}$ between the two values (-0.5 , -1.5) is thus caused by the joint effect from multiple force sources. In debris disks, the -1.5 power-law index has already taken into account both the slowdown from gravity and the acceleration from radiation pressure; the $-0.68^{+0.04}_{-0.04}$ power-law index is thus calling for additional slowdown sources, and the slowdown by the interstellar medium is a plausible candidate. In fact, a similar surface density profile has been observed in the outskirts of the HR 4796 A halo, which has an index of -0.7 and a large-scale structure that is strongly suggestive of interaction with the interstellar medium (Schneider et al. 2018).

Following the Jewitt & Meech (1987) analytic derivation relating surface density to the radial speed of the dust, we assume the size distribution of the dust is independent of its stellocentric distance. Under this assumption, if the dust has an outward radial speed of $v(r) \propto r^x$, where r is the radial separation, then the surface density will be $\Gamma(r) \propto r^{-x-1}$. In this way, the dust in the halo of HD 191089 has a radial speed of $v(r) \propto r^{-0.32 \pm 0.04}$.

Local distribution. The surface density power law of the HD 191089 halo deviates from the classical model at the $>10\sigma$ level, calling for detailed investigation of the local variation of the halo. As an attempt to investigate the variation of the

⁵⁴ Updated with the *Gaia* DR2 distance to HD 191089.

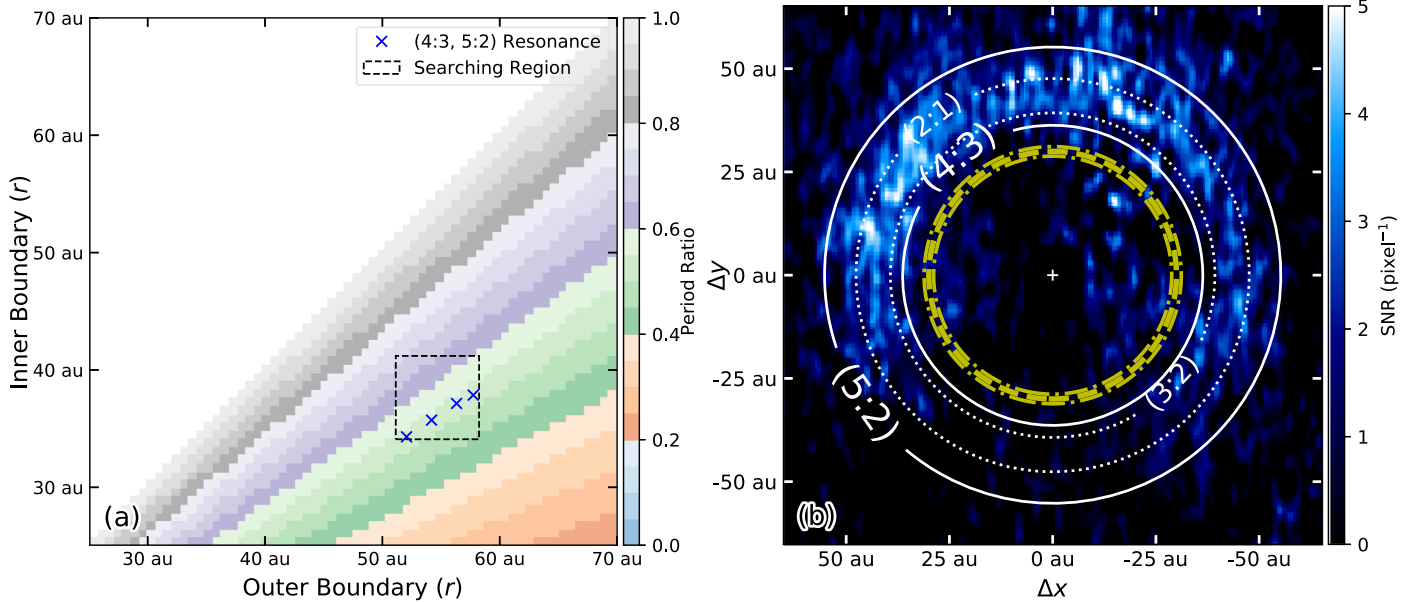


Figure 15. (a) Searching for the mean-motion resonance in HD 191089’s ring with the deprojected disk on the right; the color bar shows the orbital period ratio between the inner and outer boundary. The searching range is marked with a dashed rectangle, and the (4:3, 5:2) mean-motion resonance radii for the inner and outer boundaries are marked with blue crosses. (b) Sketch of the mean-motion resonance orbits between the deprojected HD 191089 ring and a hypothesized potential well ($r_{(1:1)} = 29.9 \pm 1.2$ au, marked with yellow dashed and dashed-dotted lines). If the extent of the primary disk matches the resonance orbits, the 4:3 orbit is at 36.2 ± 1.4 au, with the 5:2 orbit at 55 ± 2 au (white solid lines); the corresponding 3:2 and 2:1 orbits are marked with dotted lines.

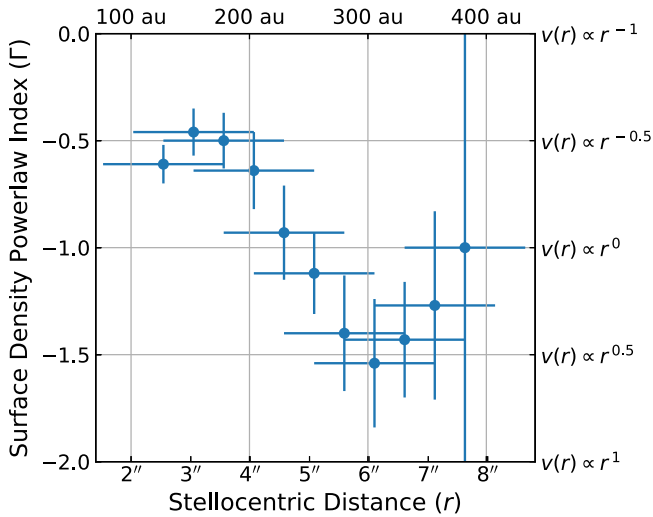


Figure 16. Power-law indices for the surface density radial profiles of the halo at different stellocentric distances and the corresponding radial speed dependence using the derivation in Jewitt & Meech (1987). The horizontal error bars are the regions where the radial profiles are calculated, i.e., $\pm 1''$.

surface density distribution at different stellocentric distances, we compute the power-law indices of the surface density radial profile for the halo at different radii in Figure 16. Assuming the dust size distribution is independent of its stellocentric distance, we also present the Jewitt & Meech (1987) analytical derivation between radial speed and surface density power-law index under difference scenarios. At different stellocentric distances, we observe the following.

1. Interior to ~ 200 au, the radial speed of dust decreases as stellocentric distance increases. This indicates the decrease of the net inward force that slows down the outward motion of the dust.

2. Between ~ 200 and ~ 300 au, the radial speed reaches a constant, then increases as stellocentric distance increases. At ~ 300 au, the surface density power-law index reaches that for the classical model for the debris disk halo (e.g., Strubbe & Chiang 2006; Thébault & Wu 2008).
3. Exterior to ~ 300 au, albeit with large uncertainty, the radial speed marginally increases, then reaches a constant as stellocentric distance increases.

Given the complex two-dimensional residual structure in the single SPF-corrected distribution of the halo (Section 5.1.4), we do not further discuss the trend of the local distribution power-law indices. In addition, our analysis is based on the assumption that dust size does not vary as a function of stellocentric separation; however, the assumption is invalid for collision-dominated debris disks (e.g., Strubbe & Chiang 2006; Thébault & Wu 2008). Therefore, a full dynamical modeling of the halo is needed to better explain the local variations of the halo.

5.1.4. Halo: Surface Density Variation

In the classical model for the debris disk halo, the dominant dust size for optical depth decreases as stellocentric distance increases (e.g., Strubbe & Chiang 2006; Thébault & Wu 2008). Using the STIS observations of the HD 181327 halo, Stark et al. (2014) found a consistency between the observed SPF change (under Mie theory) and the classical model. However, we do not find a clear SPF variation trend for the HD 191089 halo. To investigate the HD 191089 halo, we adopt the averaged halo SPF from measurement and explore the two-dimensional surface density variation for the HD 191089 halo.

To investigate the deviation of the scattering properties from the same SPF for the halo in STIS at different stellocentric radii, we first scale the whole halo by the surface brightness radial distribution as measured for Figure 6, thus eliminating

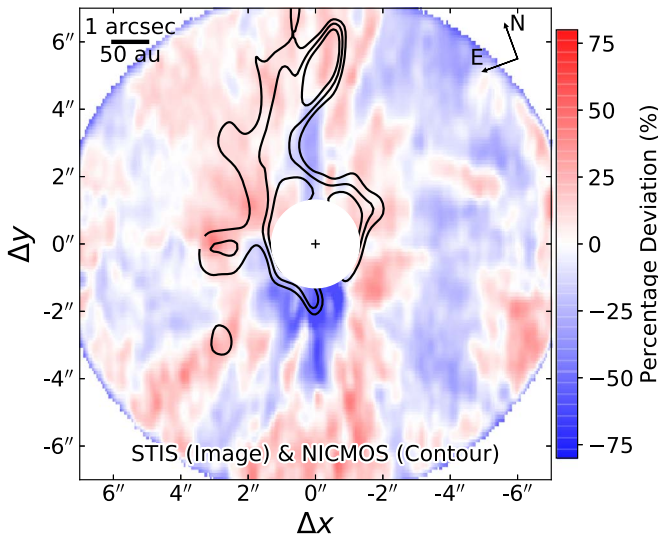


Figure 17. Demonstration of the deviation of an identical SPF for the STIS halo. For comparison and illustration, the NICMOS-NMF data are shown with black contours (arbitrary units). For the STIS halo, the NE and SW areas host overdensity regions, with the NE one likely matching that in the NICMOS-NMF data.

both the distance-dependent illumination and radial density distribution factors. We then divide the image by the empirically averaged SPF for the halo in Figure 10 based on the scattering angles for each pixel. The scaled STIS image is then deprojected to a face-on view, rotated to align the major axis with the x -axis, and subtracted by the median to show the first-order deviation from an identical SPF in all of the halo. Based on the quality of the NICMOS-NMF data, only the $\gamma_{\text{out}} = -2.68$ correction is applied.

The two-dimensional deviation from one SPF for both the STIS-cRDI and NICMOS-NMF are shown in Figure 17. We observe overdensity regions in the NE and SW sides of the STIS data at the $\sim 25\%$ level, with the STIS NE region likely matching the NICMOS NE overdensity region. The underdensity region to the NW region in the STIS image is likely influenced by the truncation of signal by STIS’s Wedge B (Figure 2).

Possible explanations for the deviation from a uniform SPF in the halo are as follows: (1) when the scattering properties of the dust are the same in the halo, the deviations are corresponding to local surface density variations; (2) when there is no density variation, the dust’s scattering properties are different; or (3) both effects are jointly affecting the SPFs in the halo.

Stellar encounter. Based on the complicated structure of the halo, we investigate the scenario of whether the halo was created by stellar encounter events (e.g., De Rosa & Kalas 2019). In the current epoch, the star at a separation of $11''.4$ to the southwest of HD 191089 in the STIS field of view (partially seen at the bottom right corner in Figure 1(a)) is a background star. It is identified by *Gaia* DR2 with Source ID 6847146784384527872 at $d = 1.06 \pm 0.06$ kpc (*Gaia* Collaboration et al. 2018); thus, it is not responsible for creating the halo.

To trace the positions of the nearby stars in the past, we retrieve 44 stars that are within 5 pc from HD 191089 using the *Gaia* DR2 archive and use the proper motions to linearly propagate the locations of the 44 stars in the past (~ 0.5 Myr ago). We notice three stars that have the nearest projected

approach from ~ 1.2 to ~ 1.5 pc, which happened between ~ 0.2 and ~ 0.35 Myr from now.⁵⁵ For star encounter events, the closest approaches are typically smaller than ~ 200 au (e.g., Pfalzner 2003; Pfalzner et al. 2018), and distinct features such as spiral arms dissipate beyond ~ 1000 yr (Pfalzner 2003). Therefore, if a star encounter event created the halo for the HD 191089 system, it should happen early in a cluster environment, where close encounters are more frequent (e.g., the solar system; Pfalzner et al. 2018). Under this mechanism, the halo would have been dissipated.

5.2. Dust Properties from Radiative Transfer Modeling

In this paper, based on previous efforts in debris disk modeling with DHS (e.g., Min et al. 2010; Milli et al. 2017), we adopted the DHS theory to model the dust in the HD 191089 ring for the GPI Q_ϕ image in polarized light and the STIS image in total intensity. We cannot yet interpret the disk images with one model across different instruments. Although we have considered a limited combination of compositions, they span the range from refractory (carbon) to pure ice and even void (through porosity). The models consider a broad range of refractive index that encompasses most standard astronomical compositions. Therefore, it is unlikely that our failure to find a good fit is solely due to not trying another composition.

In our modeling results, the STIS image favors Mie theory, and the GPI Q_ϕ image favors DHS theory with a maximum void fraction of $\sim 21\%$. The discrepancy in this parameter, which is the only additional parameter in DHS from Mie, indicates that the shape of the dust cannot be well approximated by either theory. In addition, although previous modeling attempts (e.g., Rodigas et al. 2015; Choquet et al. 2017) have encountered that simple models cannot reproduce a total intensity observation at multiple wavelengths, the analysis performed in this paper adds another dimension—polarization observation—to the complexity of disk modeling.

For some of the dust parameters (e.g., porosity, mass fraction of compositions), the discrepancies may be mathematically resolved using larger uncertainties by taking into account the correlated noise (e.g., Wolff et al. 2017). However, this resolution does not change the best-fit values, and in this way, it would make these parameters less informative, since they can only take values in a limited range (i.e., from 0% to 100%). The lack of meaning for these retrieved parameters further supports the fact that current models (i.e., Mie, DHS) cannot properly depict the debris disk images obtained at different wavelengths and with different observational techniques.

The advances in dust descriptions may solve the discrepancies in the radiative transfer modeling of debris disks, including using laboratory measurements such as the Amsterdam-Granada Light Scattering Database (Muñoz et al. 2012) or adopting advanced models for dust shapes and optical properties (e.g., discrete-dipole approximation: Purcell & Pennypacker 1973; Draine & Flatau 1994; Min et al. 2006; Rayleigh-Gans-Debye (RGD) theory: Sorensen 2001; the T -matrix method: Mishchenko et al. 1996; Gaussian random spheres: Muinonen et al. 1996; aggregation of small particles: Kempf et al. 1999; Tazaki et al. 2016; Tazaki & Tanaka 2018; Arnold et al. 2019). Given the more realistic descriptions of dust properties, the latter may help to resolve the discrepancies encountered with current dust

⁵⁵ The results do not change using the 329 stars within 10 pc.

models. For example, Tazaki et al. (2016) calculated the SPFs for aggregates using the RGD theory and found that backward scattering was underestimated in previous studies with simple models; Arnold et al. (2019) calculated blowout size for aggregates and found that the size can vary by as much as an order of magnitude for different particle models. Although these treatments may resolve the discrepancies, MCMC retrievals of dust properties for these advanced descriptions of dust are currently limited by computational power.

For the HD 191089 system, the contribution from the halo in the STIS data is also calling for a more complex structural model. In addition, if the halo is not coplanar with the ring, then the halo will bias the SPF of the ring and add another dimension of complexity to the problem.

6. Summary

In this paper, we report our detection and characterization of the HD 191089 debris disk by combining space- and ground-based instruments: *HST*/NICMOS, *HST*/STIS, and *Gemini*/GPI. Using these three instruments, we are able to study the disk in scattered light at three different wavelengths: 0.58 and 1.12 μm in total intensity and 1.65 μm (*H*-band) in polarized intensity. In the scattered-light images, we are able to identify two components in the debris disk system: a ring and a fainter fanlike halo structure. For the STIS and GPI Q_ϕ images, we implement radiative transfer modeling to retrieve the dust information. Assuming that the ring and halo are coplanar, we summarize our findings as follows.

Measurement.

1. The HD 191089 system has two spatial components: one exo-Kuiper Belt ring from 26 ± 4 to 78 ± 14 au and a halo extending to 640 ± 130 au. The center of the ring does not have a significant offset from that of the star. The halo has an overall radial surface density power-law index of -0.68 ± 0.04 , with local variations indicative of the interaction with the interstellar medium.
2. The ring has an inclination of $59^\circ_{-2^\circ}^{+4^\circ}$, enabling the SPF measurements for the two components from $\sim 30^\circ$ to $\sim 150^\circ$ in the STIS data. In the range of scattering angles probed by our observations, both forward and backward scattering are stronger for the dust in the halo than in the ring.
3. The polarization fraction curve calculated using 1.65 μm GPI Q_ϕ and 1.12 μm NICMOS-NMF images does not have a clear trend; however, it is possibly peaking at $\sim 110^\circ$. Our result may be influenced by wavelength, and it can be better constrained with future total intensity observations in the *H* band.
4. From the color of the dust derived from the NICMOS and STIS observations, the dust in the ring is redder than that in the halo. This is consistent with larger dust in the ring, which is also consistent with theoretical simulations that the ring serves as the “birth ring” for the smaller dust in the halo.
5. In comparison with an identical SPF trend (Hughes et al. 2018), the SPFs of the dust in the HD 191089 system are likely deviating from the trend.
6. If the ring is shaped by the strongest orbital resonances, the gravitational well is likely at 29.9 ± 1.2 au, resulting a 4:3 resonance with the inner edge and a 5:2 resonance with the outer edge.

Radiative transfer modeling.

We use DHS theory to model the HD 191089 ring images observed with STIS and GPI.

1. Most of the extracted parameters are not statistically consistent with each other (e.g., composition, porosity). Specifically, the GPI Q_ϕ ring favors DHS theory with $\sim 21\%$ maximum void fraction, while the STIS ring favors Mie theory (i.e., DHS with 0% void fraction). This maximum void fraction parameter approximates the structure of the dust, which is the only parameter that is added between the two theories. The discrepancy for this parameter thus suggests that neither DHS nor Mie is a good approximation of the dust structure. However, both values are smaller than the best fit for interstellar dust (0.7; Min et al. 2007), suggesting that dust properties are different in different environments.
2. The discrepant dust parameters retrieved in our DHS radiative transfer modeling of the ring may be mathematically resolved with larger uncertainties. However, for the parameters that take a limited range of values from 0% to 100%—e.g., porosity and mass fractions of compositions—large uncertainties will render these parameters less informative on dust properties. Advanced descriptions of dust models such as aggregates are expected to physically resolve the discrepancies; however, such MCMC analyses are currently limited by computational power.

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Software: `corner.py` (Foreman-Mackey 2016), `DebrisDiskFM` (Ren & Perrin 2018), `Debris Ring Analyzer` (Stark et al. 2014), `emcee` (version 3.0rc1; Foreman-Mackey et al. 2013), `MCFOST` (Pinte et al. 2006, 2009), `nmf_imaging` (Ren 2018), `pysynphot` (STScI Development Team 2013).

Appendix A The SPF

A.1. 3D Cartesian Coordinates of the Disk System

To quantify the coordinate values, the x and y coordinates can be directly measured in the image of the system with $(x, y) \pm (\delta x, \delta y)$, where δ denotes the uncertainty of the parameters in this paper. In this section, given the other measured quantities of the system (i.e., inclination and position angle of the semimajor axis), we obtain the z coordinates for this system.

To determine the z coordinates, we first set up the mathematical representation of the system. Let $O = (0, 0, 0)$ be the origin of the 3D Cartesian coordinate system, with O placed at the geometric center of the debris disk, and unit vector $\hat{x} = (1, 0, 0)$ pointing W, $\hat{y} = (0, 1, 0)$, N, $\hat{z} = (0, 0, 1)$, pointing toward the observer. Let $\hat{n}_{\text{disk}} = (a, b, c)$ denote the unit normal vector of the midplane of the debris disk system. Then, all of the points on the disk midplane, which also contains the origin O , satisfy

$$ax + by + cz = 0, \quad (11)$$

with $a^2 + b^2 + c^2 = 1$.⁵⁶

The inclination of the system, which is denoted by $\theta_{\text{inc}} \pm \delta\theta_{\text{inc}} \in [0^\circ, 90^\circ]$ and defined as the dihedral angle between the disk midplane and the xOy -plane, satisfies

$$\cos \theta_{\text{inc}} = \frac{\hat{n}_{\text{disk}} \cdot \hat{n}_{xOy}}{\sqrt{\|\hat{n}_{\text{disk}}\|^2 \|\hat{n}_{xOy}\|^2}},$$

where \cdot is the dot product between two vectors, and $\hat{n}_{xOy} = \hat{z}$ is the unit normal vector for the xOy -plane. The above equation becomes

$$\cos \theta_{\text{inc}} = \frac{(a, b, c) \cdot (0, 0, 1)}{\sqrt{(a^2 + b^2 + c^2)(0^2 + 0^2 + 1^2)}} = c. \quad (12)$$

The position angle of the system, which is denoted by $\theta_{\text{PA}} \pm \delta\theta_{\text{PA}} \in [0^\circ, 180^\circ]$, is defined as the angle from N to the intersecting line between the system and the xOy -plane. For the intersecting line, it satisfies $ax + by = 0$, since the points on it are represented as $(x, y, 0)$. Let the mathematical slope angle of the line be θ_{slope} , which is defined as the counterclockwise angle from \hat{x} to the line. Then, we have the relationship between the mathematical slope angle and astronomical position angle,

$$\theta_{\text{PA}} = \theta_{\text{slope}} - 90^\circ,$$

where

$$\tan \theta_{\text{slope}} = \frac{dy}{dx} = -\frac{a}{b};$$

therefore, we have

$$\tan \theta_{\text{PA}} = \tan(\theta_{\text{slope}} - 90^\circ) = -\cot \theta_{\text{slope}} = \frac{b}{a}. \quad (13)$$

For the points on the disk midplane, we can substitute Equations (12) and (13) into Equation (11); then we have the z -coordinate of the points as

$$\begin{aligned} z &= -\frac{1}{c}(ax + by) \\ &= -\sec \theta_{\text{inc}} a \left(x + \frac{b}{a} y \right) \\ &= \sec \theta_{\text{inc}} \sin \theta_{\text{inc}} \cos \theta_{\text{PA}} (x + y \tan \theta_{\text{PA}}) \\ &= \tan \theta_{\text{inc}} (x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}}). \end{aligned} \quad (14)$$

Assuming the measured parameters are independent, the squared uncertainty for z is therefore

$$\begin{aligned} \delta^2 z &= \delta^2 [\tan \theta_{\text{inc}} (x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}})] \\ &= (x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}})^2 \delta^2 (\tan \theta_{\text{inc}}) \\ &\quad + \tan^2 \theta_{\text{inc}} \delta^2 (x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}}) \\ &= (x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}})^2 \sec^4 \theta_{\text{inc}} \delta^2 (\theta_{\text{inc}}) \\ &\quad + \tan^2 \theta_{\text{inc}} \{ [x^2 \sin^2 \theta_{\text{PA}} \delta^2 (\theta_{\text{PA}}) + \cos^2 \theta_{\text{PA}} \delta^2 (x)] \\ &\quad + [y^2 \cos^2 \theta_{\text{PA}} \delta^2 (\theta_{\text{PA}}) + \sin^2 \theta_{\text{PA}} \delta^2 (y)] \} \\ &= \tan^2 \theta_{\text{inc}} \cos^2 \theta_{\text{PA}} \delta^2 (x) + \tan^2 \theta_{\text{inc}} \sin^2 \theta_{\text{PA}} \delta^2 (y) \\ &\quad + \sec^4 \theta_{\text{inc}} (x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}})^2 \delta^2 (\theta_{\text{inc}}) \\ &\quad + \tan^2 \theta_{\text{inc}} (x^2 \sin^2 \theta_{\text{PA}} + y^2 \cos^2 \theta_{\text{PA}}) \delta^2 (\theta_{\text{PA}}). \end{aligned} \quad (15)$$

Now, by combining the (x, y) coordinates and the inclination and position angle of the system, we can obtain $z \pm \delta z$ from Equation (14) and the square root of Equation (15). In this paper, for the HD 191089 disk, the 1σ uncertainties for x and y are estimated to be 0.33 pixel,⁵⁷ and the uncertainties for θ_{inc} and θ_{PA} are obtained from the GPI \mathcal{Q}_ϕ image using the Debris Ring Analyzer package by Stark et al. (2014).

A.2. Scattering Angle

From the (x, y, z) coordinates of the dust in the debris disk system, and given the position of the star at $(x_0, y_0, z_0) \pm (\delta x_0, \delta y_0, \delta z_0)$, we can then measure the scattering angle for the photons. A photon, which is emitted from the star and then interacts with the material at (x, y, z) , has an original direction of $\mathbf{r} = (x, y, z) - (x_0, y_0, z_0)$. The photon, when collected by the observer, has a final direction of \hat{z} . The scattering angle of this photon, which is defined as the angle between \mathbf{r} and \hat{z} , is

⁵⁶ Note: the a symbol in this section is not the dust size used in the main text.

⁵⁷ Scaled from a conservative 3σ uncertainty of 1 pixel.

thus

$$\begin{aligned}\theta_{\text{scatter}} &= \arccos\left(\frac{\mathbf{r} \cdot \hat{\mathbf{z}}}{\sqrt{\|\mathbf{r}\|^2 \|\hat{\mathbf{z}}\|^2}}\right) \\ &= \arccos\left[\frac{z - z_0}{\sqrt{(x - x_0)^2 + (y - y_0)^2 + (z - z_0)^2}}\right].\end{aligned}\quad (16)$$

Substituting Equation (14) into the above equation, we have the scattering angle at the (x, y) position in the detector frame (i.e., on the xOy -plane),

$$\theta_{\text{scatter}} = \arccos\left\{\frac{\tan \theta_{\text{inc}}(x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}}) - z_0}{\sqrt{(x - x_0)^2 + (y - y_0)^2 + [\tan \theta_{\text{inc}}(x \cos \theta_{\text{PA}} + y \sin \theta_{\text{PA}}) - z_0]^2}}\right\}.\quad (17)$$

Assuming the measured parameters are independent, the corresponding squared uncertainty for θ_{scatter} is then

$$\begin{aligned}\delta^2 \theta_{\text{scatter}} &= \frac{1}{1 - \left[\frac{z - z_0}{\sqrt{(x - x_0)^2 + (y - y_0)^2 + (z - z_0)^2}}\right]^2} \\ &\quad \times \delta^2 \left[\frac{z - z_0}{\sqrt{(x - x_0)^2 + (y - y_0)^2 + (z - z_0)^2}}\right],\end{aligned}$$

denoting $v' \equiv v - v_0$ for $v \in \{x, y, z\}$ and thus $\delta^2(v') = \delta^2(v) + \delta^2(v_0)$; then, the above equation becomes

$$\begin{aligned}\delta^2 \theta_{\text{scatter}} &= \frac{x'^2 + y'^2 + z'^2}{x'^2 + y'^2} \delta^2 \left(\frac{z'}{\sqrt{x'^2 + y'^2 + z'^2}} \right) \\ &= \frac{x'^2 + y'^2 + z'^2}{x'^2 + y'^2} \frac{z'^2}{x'^2 + y'^2 + z'^2} \\ &\quad \times \left[\frac{\delta^2(z')}{z'^2} + \frac{\delta^2(\sqrt{x'^2 + y'^2 + z'^2})}{x'^2 + y'^2 + z'^2} \right] \\ &= \frac{z'^2}{x'^2 + y'^2} \left\{ \frac{\delta^2(z')}{z'^2} + \frac{1}{x'^2 + y'^2 + z'^2} \right. \\ &\quad \left. \times \left[\frac{1}{4(x'^2 + y'^2 + z'^2)} \delta^2(x'^2 + y'^2 + z'^2) \right] \right\} \\ &= \frac{z'^2}{x'^2 + y'^2} \left[\frac{\delta^2(z')}{z'^2} + \frac{x'^2 \delta^2(x') + y'^2 \delta^2(y') + z'^2 \delta^2(z')}{(x'^2 + y'^2 + z'^2)^2} \right].\end{aligned}\quad (18)$$

Substituting the value and uncertainty of z from Equations (14) and (15) into Equations (16) and (18), we can obtain the value and uncertainty for the scattering angle, $\theta_{\text{scatter}} \pm \delta \theta_{\text{scatter}}$.

In this paper, the input uncertainties are obtained from the GPI \mathcal{Q}_ϕ image measured with the Debris Ring Analyzer package (Stark et al. 2014). The SPF is then the scattering-angle dependence of the flux density of the system at specific radial separations. The original measurements are then

averaged to reduce measurement errors, and the final SPF is obtained by correcting the limb-brightening effect (by dividing the observed SPF by that of an isotropic disk model; Milli et al. 2017).

Appendix B Sampling from Posterior Distributions

B.1. Glivenko–Cantelli Theorem

In probability theory, for n independent and identically distributed real-valued random variables $(X_1, X_2, \dots, X_n \in \mathbb{R})$, the empirical cumulative distribution function (ECDF) is

defined as⁵⁸

$$\hat{F}_n(x) = \frac{1}{n} \sum_{i=1}^n \mathbf{1}_{[X_i, \infty)}(x),\quad (19)$$

where $\mathbf{1}_{[X_i, \infty)}(x)$ is an indicator function that is equal to 1 only when $X_i \leq x < \infty$ (otherwise $\mathbf{1}_{[X_i, \infty)}(x) = 0$). For the ECDF, the Glivenko–Cantelli theorem (e.g., Chung 2001) describes its asymptotic relationship with the cumulative distribution function (CDF) of a random variable $X \in \mathbb{R}$, which is denoted by $F_X(x)$, that $\hat{F}_n(x)$ converges to $F_X(x)$ uniformly to $F_X(x)$ as $n \rightarrow \infty$ almost surely, i.e.,

$$\|\hat{F}_n - F_X\|_\infty \equiv \sup_{x \in \mathbb{R}} |\hat{F}_n(x) - F_X(x)| \xrightarrow{\text{a.s.}} 0.\quad (20)$$

B.2. The PIT

In statistics, for a random variable $X \in \mathbb{R}$ with CDF $F_X(x)$, the PIT states that $Y = F_X(x)$ is uniformly distributed between 0 and 1 (Rosenblatt 1952), in the sense that

$$\begin{aligned}F_Y(y) &= \Pr(Y \leq y) \\ &= \Pr[F_X(x) \leq y] \\ &= \Pr[X \leq F_X^{-1}(y)] \\ &= F_X[F_X^{-1}(y)] \\ &= y,\end{aligned}\quad (21)$$

which is the CDF of a random variable that is uniformly distributed between zero and 1, and $F_Y(y)$ is the CDF of the random variable Y . Based on this property, the PIT is used to sample distributions, especially the ones that do not have parametric expressions.

B.3. Posterior as Prior

To use the marginal posterior distribution from the previous MCMC run as the prior for the next run, we transfer the

⁵⁸ Note: the x and y symbols in Appendix B are statistical variables, not Cartesian coordinates.

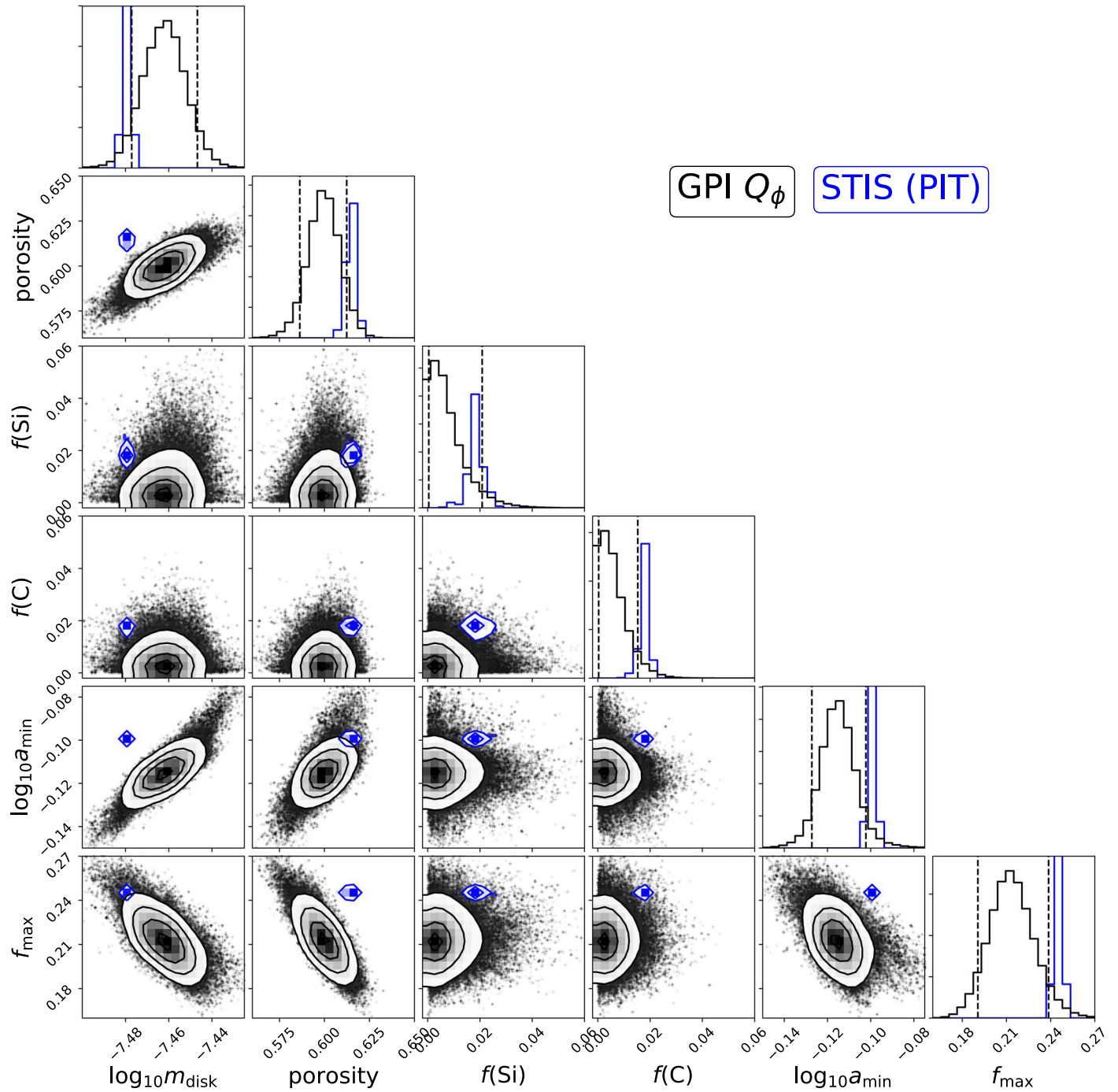


Figure 18. Posterior distributions for STIS modeling with the PIT approach (blue). The marginal distribution of the GPI posteriors (black) are used as the priors for STIS fitting. The vertical dashed lines are the GPI 2.5th and 97.5th percentiles, which are the prior ranges. The majority of the STIS PIT posteriors lie around or beyond the 2.5th and 97.5th percentiles of the priors, indicating a trend of deviating from them.

information between the two MCMC runs by combining the Glivenko–Cantelli theorem and the PIT.

First, convert discrete points to a continuous distribution. Based on the Glivenko–Cantelli theorem, for a specific random variable X with a large number of samples, we can treat its marginal ECDF from the previous MCMC run as its CDF, then use the ECDF as the prior for the next MCMC run.

Second, sample from an ECDF. We first sample a standard uniform random quantile variable $Y \in [0, 1]$, then we find the corresponding empirical quantile in the given ECDF, i.e.,

$\hat{F}_n^{-1}(Y)$. Using the PIT in Equation (21), we have

$$\hat{F}_n^{-1}(Y) \sim \hat{F}_n. \quad (22)$$

Third, combining the Glivenko–Cantelli theorem in Equation (20) with the quantile distribution in Equation (22), we have

$$\hat{F}_n^{-1}(Y) \sim F_X. \quad (23)$$

i.e., for a standard uniform random variable Y , its corresponding quantile for the ECDF of a random variable X follows the distribution of X .

B.4. GPI Posteriors as STIS Priors

In this section, we establish the connection between the GPI \mathcal{Q}_ϕ image and the STIS total intensity image through radiative transfer modeling. We first obtain the posterior distribution of the disk parameters by radiative transfer modeling the GPI \mathcal{Q}_ϕ image with MCMC (Section 4.2.1). We then calculate the marginal distributions from the MCMC posterior values⁵⁹ and use the PIT to treat them as the priors when modeling the STIS image.

The posteriors with the PIT approach for the STIS image are presented in Figure 18. In this section, our purpose is to demonstrate the statistical deviation of the posteriors from the GPI best-fit values. We thus constrain the PIT sampling ranges to be between the 2.5th and 97.5th percentiles, which is analogous to the conventional definition of two-tailed statistical significance: p -value > 0.05 .

In this paper, we have ignored the correlated spatial noise in the images in our MCMC modeling; however, correlated noise is expected to increase the uncertainty of the extracted parameters (e.g., Czekala et al. 2015; Wolff et al. 2017). To better quantify the statistical deviation of the two sets of disk parameters that are extracted from the two disk images (Table 5), rigorous treatment of the correlated noise is necessary (e.g., Wolff et al. 2017).

ORCID iDs

Bin Ren (彬 任) <https://orcid.org/0000-0003-1698-9696>
 Élodie Choquet <https://orcid.org/0000-0002-9173-0740>
 Marshall D. Perrin <https://orcid.org/0000-0002-3191-8151>
 Gaspard Duchêne <https://orcid.org/0000-0002-5092-6464>
 John H. Debes <https://orcid.org/0000-0002-1783-8817>
 Malena Rice <https://orcid.org/0000-0002-7670-670X>
 Christine Chen <https://orcid.org/0000-0002-8382-0447>
 Glenn Schneider <https://orcid.org/0000-0002-4511-5966>
 Thomas M. Esposito <https://orcid.org/0000-0002-0792-3719>
 Charles A. Poteet <https://orcid.org/0000-0003-4845-7483>
 Jason J. Wang <https://orcid.org/0000-0003-0774-6502>
 S. Mark Ammons <https://orcid.org/0000-0001-5172-7902>
 Megan Ansdell <https://orcid.org/0000-0003-4142-9842>
 Pauline Arriaga <https://orcid.org/0000-0001-6364-2834>
 Vanessa P. Bailey <https://orcid.org/0000-0002-5407-2806>
 Travis Barman <https://orcid.org/0000-0002-7129-3002>
 Juan Sebastián Bruzzone <https://orcid.org/0000-0002-2731-0397>
 Joanna Bulger <https://orcid.org/0000-0003-4641-2003>
 Jeffrey Chilcote <https://orcid.org/0000-0001-6305-7272>
 Tara Cotten <https://orcid.org/0000-0003-0156-3019>
 Robert J. De Rosa <https://orcid.org/0000-0002-4918-0247>
 Michael P. Fitzgerald <https://orcid.org/0000-0002-0176-8973>
 Katherine B. Follette <https://orcid.org/0000-0002-7821-0695>
 Stephen J. Goodsell <https://orcid.org/0000-0002-4144-5116>
 Benjamin L. Gerard <https://orcid.org/0000-0003-3978-9195>

Alexandra Z. Greenbaum <https://orcid.org/0000-0002-7162-8036>
 Pascale Hibon <https://orcid.org/0000-0003-3726-5494>
 Dean C. Hines <https://orcid.org/0000-0003-4653-6161>
 Li-Wei Hung <https://orcid.org/0000-0003-1498-6088>
 Patrick Ingraham <https://orcid.org/0000-0003-3715-8138>
 Quinn Konopacky <https://orcid.org/0000-0002-9936-6285>
 James E. Larkin <https://orcid.org/0000-0001-7687-3965>
 Bruce Macintosh <https://orcid.org/0000-0003-1212-7538>
 Franck Marchis <https://orcid.org/0000-0001-7016-7277>
 Christian Marois <https://orcid.org/0000-0002-4164-4182>
 Johan Mazoyer <https://orcid.org/0000-0002-9133-3091>
 Stanimir Metchev <https://orcid.org/0000-0003-3050-8203>
 Maxwell A. Millar-Blanchaer <https://orcid.org/0000-0001-6205-9233>
 Tushar Mittal <https://orcid.org/0000-0002-8026-0018>
 Eric L. Nielsen <https://orcid.org/0000-0001-6975-9056>
 Mamadou N'Diaye <https://orcid.org/0000-0002-1721-3294>
 Rebecca Oppenheimer <https://orcid.org/0000-0001-7130-7681>
 David Palmer <https://orcid.org/0000-0001-7128-0802>
 Christophe Pinte <https://orcid.org/0000-0001-5907-5179>
 Abhijith Rajan <https://orcid.org/0000-0002-9246-5467>
 Julien Rameau <https://orcid.org/0000-0003-0029-0258>
 Fredrik T. Rantakyö <https://orcid.org/0000-0002-9667-2244>
 Jean-Baptiste Ruffio <https://orcid.org/0000-0003-2233-4821>
 Dmitry Savransky <https://orcid.org/0000-0002-8711-7206>
 Adam C. Schneider <https://orcid.org/0000-0002-6294-5937>
 Anand Sivaramakrishnan <https://orcid.org/0000-0003-1251-4124>
 Inseok Song <https://orcid.org/0000-0002-5815-7372>
 Rémi Soummer <https://orcid.org/0000-0003-2753-2819>
 Sandrine Thomas <https://orcid.org/0000-0002-9121-3436>
 Kimberly Ward-Duong <https://orcid.org/0000-0002-4479-8291>
 Sloane Wiktorowicz <https://orcid.org/0000-0003-4483-5037>
 Schuyler Wolff <https://orcid.org/0000-0002-9977-8255>
 Colin Norman <https://orcid.org/0000-0002-5222-5717>

References

- Arnold, J. A., Weinberger, A. J., Videen, G., & Zubko, E. S. 2019, *AJ*, 157, 157
 Artymowicz, P., & Clampin, M. 1997, *ApJ*, 490, 863
 Augereau, J.-C., & Beust, H. 2006, *A&A*, 455, 987
 Augereau, J. C., Lagrange, A. M., Mouillet, D., et al. 1999, *A&A*, 348, 557
 Bannister, M. T., Gladman, B. J., Kavelaars, J. J., et al. 2018, *ApJS*, 236, 18
 Boccaletti, A., Thalmann, C., Lagrange, A.-M., et al. 2015, *Natur*, 526, 230
 Boggs, P. T., Donaldson, J. R., Byrd, R. H., & Schnabel, R. B. 1989, *TOMS*, 15, 348
 Burns, J. A., Lamy, P. L., & Soter, S. 1979, *Icar*, 40, 1
 Canovas, H., Ménard, F., de Boer, J., et al. 2015, *A&A*, 582, L7
 Chandler, C. O., McDonald, I., & Kane, S. R. 2016, *AJ*, 151, 59
 Chen, C. H., Mittal, T., Kuchner, M., et al. 2014, *ApJS*, 211, 25
 Chiang, E. I., Jordan, A. B., Millis, R. L., et al. 2003, *AJ*, 126, 430
 Choquet, É., Bryden, G., Perrin, M. D., et al. 2018, *ApJ*, 854, 53
 Choquet, É., Milli, J., Wahhaj, Z., et al. 2017, *ApJL*, 834, L12
 Choquet, É., Perrin, M. D., Chen, C. H., et al. 2016, *ApJL*, 817, L2
 Choquet, É., Pueyo, L., Hagan, J. B., et al. 2014, *Proc. SPIE*, 9143, 914357
 Chung, K. 2001, *A Course in Probability Theory* (Amsterdam: Elsevier)
 Churcher, L., Wyatt, M., & Smith, R. 2011, *MNRAS*, 410, 2
 Cutri, R. M., Skrutskie, M. F., van Dyk, S., et al. 2003, *yCat*, 2246
 Czekala, I., Andrews, S. M., Mandel, K. S., et al. 2015, *ApJ*, 812, 128
 Debes, J. H., Poteet, C. A., Jang-Condell, H., et al. 2017, *ApJ*, 835, 205

⁵⁹ Note: the correlations of the parameters are ignored.

- Debes, J. H., Ren, B., & Schneider, G. 2019, *JATIS*, 5, 035003
- De Rosa, R. J., & Kalas, P. 2019, *AJ*, 157, 125
- De Rosa, R. J., Nielsen, E. L., Blunt, S. C., et al. 2015, *ApJL*, 814, L3
- Dohnanyi, J. S. 1969, *JGR*, 74, 2531
- Draine, B. T., & Flatau, P. J. 1994, *JOSAA*, 11, 1491
- Draine, B. T., & Lee, H. M. 1984, *ApJ*, 285, 89
- Draper, Z. H., Duchêne, G., Millar-Blanchaer, M. A., et al. 2016, *ApJ*, 826, 147
- Eiroa, C., Marshall, J. P., Mora, A., et al. 2013, *A&A*, 555, A11
- Engler, N., Schmid, H. M., Thalmann, C., et al. 2017, *A&A*, 607, A90
- Ertel, S., Wolf, S., & Rodmann, J. 2012, *A&A*, 544, A61
- Esposito, T. M., Duchêne, G., Kalas, P., et al. 2018, *AJ*, 156, 47
- Feldt, M., Olofsson, J., Boccaletti, A., et al. 2017, *A&A*, 601, A7
- Foreman-Mackey, D. 2016, *JOSS*, 1, 24
- Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, *PASP*, 125, 306
- Frattin, E., Muñoz, O., Moreno, F., et al. 2019, *MNRAS*, 484, 2198
- Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2018, *A&A*, 616, A1
- Goodman, J., & Weare, J. 2010, *CAMCS*, 5, 65
- Hagan, J. B., Choquet, É., Soummer, R., & Vigan, A. 2018, *AJ*, 155, 179
- Hales, A. S., Barlow, M. J., Crawford, I. A., & Casassus, S. 2017, *MNRAS*, 466, 3582
- Hedman, M. M., & Stark, C. C. 2015, *ApJ*, 811, 67
- Høg, E., Fabricius, C., Makarov, V. V., et al. 2000, *A&A*, 355, L27
- Holland, W. S., Matthews, B. C., Kennedy, G. M., et al. 2017, *MNRAS*, 470, 3606
- Houk, N. 1982, Michigan Catalogue of Two-dimensional Spectral Types for the HD stars. Vol. 3. Declinations -40° to -26° (Ann Arbor, MI: Department of Astronomy, University of Michigan)
- Hughes, A. M., Duchêne, G., & Matthews, B. C. 2018, *ARA&A*, 56, 541
- Hung, L.-W., Bruzzone, S., Millar-Blanchaer, M. A., et al. 2016, *Proc. SPIE*, 9908, 99083A
- Hung, L.-W., Duchêne, G., Arriaga, P., et al. 2015, *ApJL*, 815, L14
- Jewitt, D. C., & Meech, K. J. 1987, *ApJ*, 317, 992
- Kalas, P. G., Rajan, A., Wang, J. J., et al. 2015, *ApJ*, 814, 32
- Kempf, S., Pfalzner, S., & Henning, T. K. 1999, *Icar*, 141, 388
- Kennedy, G. M., & Wyatt, M. C. 2014, *MNRAS*, 444, 3164
- Konishi, M., Grady, C. A., Schneider, G., et al. 2016, *ApJL*, 818, L23
- Krist, J. E., Hook, R. N., & Stoehr, F. 2011, *Proc. SPIE*, 8127, 81270J
- Lagrange, A.-M., Langlois, M., Gratton, R., et al. 2016, *A&A*, 586, L8
- Lee, E. J., & Chiang, E. 2016, *ApJ*, 827, 125
- Li, A., & Greenberg, J. M. 1998, *A&A*, 331, 291
- MacGregor, M. A., Wilner, D. J., Chandler, C., et al. 2016, *ApJ*, 823, 79
- Macintosh, B., Graham, J. R., Ingraham, P., et al. 2014, *PNAS*, 111, 12661
- Mannings, V., & Barlow, M. J. 1998, *ApJ*, 497, 330
- Matthews, E., Hinkley, S., Vigan, A., et al. 2017, *ApJL*, 843, L12
- Meshkat, T., Mawet, D., Bryan, M. L., et al. 2017, *AJ*, 154, 245
- Mie, G. 1908, *AnP*, 330, 377
- Millar-Blanchaer, M. A., Graham, J. R., Pueyo, L., et al. 2015, *ApJ*, 811, 18
- Millar-Blanchaer, M. A., Wang, J. J., Kalas, P., et al. 2016, *AJ*, 152, 128
- Milli, J., Engler, N., Schmid, H. M., et al. 2019, *A&A*, 626, A54
- Milli, J., Mawet, D., Pinte, C., et al. 2015, *A&A*, 577, A57
- Milli, J., Vigan, A., Mouillet, D., et al. 2017, *A&A*, 599, A108
- Min, M., Dominik, C., Hovenier, J. W., et al. 2006, *A&A*, 445, 1005
- Min, M., Hovenier, J. W., & de Koter, A. 2003, *A&A*, 404, 35
- Min, M., Hovenier, J. W., & de Koter, A. 2005, *A&A*, 432, 909
- Min, M., Kama, M., Dominik, C., & Waters, L. B. F. M. 2010, *A&A*, 509, L6
- Min, M., Waters, L. B. F. M., de Koter, A., et al. 2007, *A&A*, 462, 667
- Mishchenko, M. I., Travis, L. D., & Mackowski, D. W. 1996, *JQSRT*, 55, 535
- Mittal, T., Chen, C. H., Jang-Condell, H., et al. 2015, *ApJ*, 798, 87
- Monnier, J. D., Harries, T. J., Bae, J., et al. 2019, *ApJ*, 872, 122
- Montesinos, B., Eiroa, C., Krivov, A. V., et al. 2016, *A&A*, 593, A51
- Moór, A., Ábrahám, P., Derekas, A., et al. 2006, *ApJ*, 644, 525
- Morrison, S., & Malhotra, R. 2015, *ApJ*, 799, 41
- Muinonen, K., Nousiainen, T., Fast, P., et al. 1996, *JQSRT*, 55, 577
- Muñoz, O., Moreno, F., Guirado, D., et al. 2012, *JQSRT*, 113, 565
- Olofsson, J., van Holstein, R. G., Boccaletti, A., et al. 2018, *A&A*, 617, A109
- Pan, M., & Schlichting, H. E. 2012, *ApJ*, 747, 113
- Perrin, M. D., Duchene, G., Millar-Blanchaer, M., et al. 2015, *ApJ*, 799, 182
- Perrin, M. D., Ingraham, P., Follette, K. B., et al. 2016, *Proc. SPIE*, 9908, 990837
- Perrin, M. D., Maire, J., Ingraham, P., et al. 2014, *Proc. SPIE*, 9147, 91473J
- Pfalzner, S. 2003, *ApJ*, 592, 986
- Pfalzner, S., Bhandare, A., Vincke, K., & Lacerda, P. 2018, *ApJ*, 863, 45
- Pinte, C., Harries, T. J., Min, M., et al. 2009, *A&A*, 498, 967
- Pinte, C., Ménard, F., Duchêne, G., & Bastien, P. 2006, *A&A*, 459, 797
- Poteet, C. A., Whittet, D. C. B., & Draine, B. T. 2015, *ApJ*, 801, 110
- Purcell, E. M., & Pennypacker, C. R. 1973, *ApJ*, 186, 705
- Ren, B. 2018, nmf_imaging Version 1.0, Zenodo, doi:10.5281/zenodo.2424378
- Ren, B., Dong, R., Esposito, T. M., et al. 2018a, *ApJL*, 857, L9
- Ren, B., & Perrin, M. 2018, DebrisDiskFM Version 1.0, Zenodo, doi:10.5281/zenodo.2398963
- Ren, B., Pueyo, L., Perrin, M. D., et al. 2017, *Proc. SPIE*, 10400, 1040021
- Ren, B., Pueyo, L., Zhu, G. B., et al. 2018b, *ApJ*, 852, 104
- Riley, A., Biretta, J., Hernandez, S., et al. 2018, STIS Instrument Handbook (Baltimore, MD: STScI)
- Rodigas, T. J., Stark, C. C., Weinberger, A., et al. 2015, *ApJ*, 798, 96
- Rosenblatt, M. 1952, *Ann. Math. Statist.*, 23, 470
- Rouleau, F., & Martin, P. G. 1991, *ApJ*, 377, 526
- Ruffio, J.-B., Macintosh, B., Wang, J. J., et al. 2017, *ApJ*, 842, 14
- Schneider, G., Debes, J. H., Grady, C. A., et al. 2018, *AJ*, 155, 77
- Schneider, G., Grady, C. A., Hines, D. C., et al. 2014, *AJ*, 148, 59
- Schneider, G., Grady, C. A., Stark, C. C., et al. 2016, *AJ*, 152, 64
- Schneider, G., Weinberger, A. J., Becklin, E. E., et al. 2009, *AJ*, 137, 53
- Schneider, G., Wood, K., Silverstone, M. D., et al. 2003, *AJ*, 125, 1467
- Shkolnik, E. L., Allers, K. N., Kraus, A. L., et al. 2017, *AJ*, 154, 69
- Sibthorpe, B., Kennedy, G. M., Wyatt, M. C., et al. 2018, *MNRAS*, 475, 3046
- Sicilia-Aguilar, A., Banzatti, A., Carmona, A., et al. 2016, *PASA*, 33, e059
- Silber, K., & Draine, B. T. 2016, *ApJ*, 818, 133
- Sissa, E., Olofsson, J., Vigan, A., et al. 2018, *A&A*, 613, L6
- Skrutskie, M. F., Cutri, R. M., Stiening, R., et al. 2006, *AJ*, 131, 1163
- Sorensen, C. M. 2001, *AerST*, 35, 648
- Soummer, R., Perrin, M. D., Pueyo, L., et al. 2014, *ApJL*, 786, L23
- Soummer, R., Pueyo, L., & Larkin, J. 2012, *ApJL*, 755, L28
- Spiegel, D. S., & Burrows, A. 2012, *ApJ*, 745, 174
- Stark, C. C., Schneider, G., Weinberger, A. J., et al. 2014, *ApJ*, 789, 58
- Stern, S. A., & Colwell, J. E. 1997, *ApJ*, 490, 879
- Strubbe, L. E., & Chiang, E. I. 2006, *ApJ*, 648, 652
- STScI Development Team, 2013, pysynphot: Synthetic Photometry Software Package, Astrophysics Source Code Library, ascl:1303.023
- Tazaki, R., & Tanaka, H. 2018, *ApJ*, 860, 79
- Tazaki, R., Tanaka, H., Okuzumi, S., et al. 2016, *ApJ*, 823, 70
- Thébaud, P. 2009, *A&A*, 505, 1269
- Thébaud, P., & Wu, Y. 2008, *A&A*, 481, 713
- Thureau, N. D., Greaves, J. S., Matthews, B. C., et al. 2014, *MNRAS*, 445, 2558
- Viana, A., Wiklind, T., Koekemoer, A., et al. 2009, NICMOS Instrument Handbook (Baltimore, MD: STScI)
- Wahhaj, Z., Milli, J., Kennedy, G., et al. 2016, *A&A*, 596, L4
- Wang, J. J., Perrin, M. D., Savransky, D., et al. 2018, *JATIS*, 4, 018002
- Wang, J. J., Rajan, A., Graham, J. R., et al. 2014, Proc. SPIE, 9147, 914755
- Wolff, S. G., Perrin, M., Millar-Blanchaer, M. A., et al. 2016, *ApJL*, 818, L15
- Wolff, S. G., Perrin, M. D., Stapelfeldt, K., et al. 2017, *ApJ*, 851, 56
- Wyatt, M. C. 2008, *ARA&A*, 46, 339