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Sewer Networks Optimization Using Cellular Automata

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Abstract

The Hybrid Cellular Automata (HCA) method is used in this paper for the optimal design of sewer network problems with the fixed layout. The HCA method decomposes the problem into two sub-problems with considering the pipe diameters and nodal cover depths as decision variables. Two stages are solved iteratively for determining the decision variables in a manner to minimize the total cost of the sewer network subject to the operational constraints. The HCA method is used to optimally solve three benchmark examples with different sizes and the results are presented and compared to those of the existing methods. The results indicate that the HCA method is more efficient and effective than the alternative methods.

Keywords: Sewer Network, Optimization methods, Cellular Automata, design problem.

1. Introduction

Sewer network systems as a necessary urban infrastructure play an important role in the urban areas. The main objective of optimal sewer network design problem is minimization of the capital investment on infrastructure whereas ensuring good performance under specified design criteria. This topic has received considerable attention and different numerical optimization approaches have been introduced and applied to the optimal design of sewer networks (Afshar, Shahidi, Rohani, & Sargolzaei, 2011, Afshar & Rohani, 2012). These include the Linear Programming (LP), Non-Linear Programming (NLP), Dynamic Programming (DP), and Evolutionary Algorithms.

There have been some attempts using the Linear Programming method to solve the problem of sewer network design, such as Deininger (1970), Dajani and Gemmell (1971), Froise and Burges (1978), and Walters and Templeman (1979). Gupta, Agarwal, & Khanna (1976), Lemieux, Zech, & Delarue (1976), and Price (1978) applied NLP and Swamee (2001) used the Lagrange multiplier method to yield optimal sewer network design.

Among these methods, DP is the mostly used method for the optimal design of the sewer networks due to serial features of these networks. Merrit and Bogan (1973), Mays and Wenzel (1976), Robinson and Labadie (1981), Yen, Cheng, Jun, Voohees, & Wenzel (1984), and Kulkarni and Khanna (1985) applied DP for the optimal design of wastewater and/or storm water networks. Although, DP methods are theoretically capable of finding the global optimum solution, but they suffer from the curse of dimensionality limitation and therefore are not appropriate method for the large scale real-world sewer networks.

Recently, Evolutionary approaches are being used for the problem due to their simplicity and flexibility for both continuous and discrete problems without any assumption about the optimization objectives and good results have been reported using these methods. Heaney, Wright, Sample, Field, & Fan (1999) had used Genetic Algorithm (GA) on spreadsheet templates to get near-optimal solutions for the optimal design of sewer networks. Liang, Thompson, & Young (2004) applied GA and Tabu Search (TS) algorithm for the optimal design of sewer networks. Afshar (2007) proposed the sequential feature of solution construction in the Ant Colony Optimization Algorithm (ACOA) to develop two partially constrained ACO algorithms for the solution of storm sewer network design problems. Pan and Kao (2009) had integrated Quadratic Programming (QP) with GA to solve the sewer network optimization problem. The applicability and efficiency of the GA-QP model were tested and the results indicated that the GA-QP model could obtain various near optimum design alternatives within an acceptable computational time. Wang and Zhou (2009) analyzed and compared the performances of GA, Particle Swarm Optimization (PSO) and Ant Colony Algorithms (ACA) from three aspects of convergence, speed and complexity. It was shown that ACA is superior to other methods

for better convergence and satisfactory speed. Afshar (2010) applied the Continuous Ant Colony Optimization Algorithm (CACOA) for the optimal design of sewer networks. Yeh, Chu, Chang, & Lin (2011) applied TS and Simulated Annealing (SA) for the optimization of sewer network problems.

Since the basic theories of Evolutionary Algorithms, emulating the natural optimization process of evolution, are similar to the natural evolutionary process, they need a big search space in spite of intelligent process, and so they involve high computational costs and need a large number of iteration and computational efforts to achieve the optimum solutions. Moreover, they require some free parameters that should be sensitive analyzed for obtaining the optimal solution.

Cellular Automata (CA), a novel optimization algorithm, has recently introduced and attracted much attention and has been widely applied to some engineering problems.

In this paper, Hybrid CA (HCA) methods are used for the design of sewer network with the fixed layout. In the HCA methods, the problem is decomposed in two stages solved iteratively to get the results. In the first stage, nodal cover depths of the network are determined with the fixed values for pipe diameters using a CA method with the nodes considered as the CA cells and nodal cover depths as cell states. In the second stage, the obtained nodal cover depths in the first stage are used to calculate the pipe diameters with another CA method. In this stage, the pipes considered as the CA cells and their diameters as the cell states. Two different updating rules, Continuous and Discrete approaches, are used for CA updating rule of the second stage depending on the treatment of the pipe diameters. The CA updating rule is derived by requiring that the network cost is minimized in the neighborhood of each cell. The HCA methods are used to design three benchmark examples and comparison the results with the existing ones show the efficiency and effectiveness of the methods to solve the sewer design optimization problems.

2. Cellular Automata

Cellular Automata (CA), a model of self-reproducing system, was conceived by Ulam (1960) and Von Neumann (1966) and later completed and improved with the work of other researchers like Thatcher (1964), Codd (1968), and Burks (1972).

CA has a set of identical elements, called cells with finite possible value called cell state. The new states of all cells are defined simultaneously using an updating rule, which is a function of the previous state of the cell itself and its neighborhoods.

CA had been used as a simulator in various fields such as computer science, (Wolfram 1988), chemistry (Packard, 1986), and medical profession (Sentos & Coutinho, 2001). Recently, some research showed that CA can be used as a practical and efficient optimization engine, which relies on the key properties of: locality of the neighborhoods interactions, homogeneity of the evolving mechanism, parallelism of the computation, and simplicity of the model structure. CA has been extensively used as a viable and efficient optimization algorithm for the structural design (Kita & Toyoda, 2000, Missoum, Gürdal, & Setoodeh, 2005, and Setoodeh, Gürdalb, & Watson, 2006), estimating shortest path (Adamatzky 1996) or trip distribution problems (El Dessouki, Fathi, & Rouphail, 2001), and computer networks (Shuai & Zhao, 2004).

In the early applications in water resource problems, CA was used to produce good initial populations for a GA leading to improved performance of the GA (Keedwell & khu, 2005, Guo, Keedwell, Walters, & Khu, 2007a). The first use of CA as a stand-alone optimizer was demonstrated by Guo, Walters, Khu, & Keedwell (2007b) for optimal design of storm sewer networks based on the simplifying assumption of known slopes. Afshar and Shahidi (2009) were the first to propose CA with mathematically derived transition rules for the optimal water supply and hydropower operation of a single reservoir. Later, Afshar et al. (2011) proposed a single stage CA for the optimal design of sewer networks with fixed layout using the nodal excavation depth as the decision variables of the problem. Afshar and Rohani (2012) extended the single stage CA method of Afshar et al. (2011) to two stage CA and proposed Hybrid CA, in which nodal cover depths and pipes diameter were considered as decision variables.

3. Sewer Network Size Optimization

Sewer network system is one of the urban infrastructure systems with huge construction and operation cost and any attempt to reduce these costs result in considerable saving. A sewer network is an underground system built to convey waste water to one or more collection points (outfalls).

Optimal sewer network design with a fixed layout aims to find a cost-effective solution by determining the pipes diameters and slopes which minimizes the capital investment whilst ensuring a good system performance under specific design criteria. The problem of sewer network design for a fixed network layout, in the absence of pumps and drops, can be formulated as:

$$Min \ C_{network} = \sum Cp_l + \sum Cm_i = \sum L_l Kp(D_b X_b X_i) + \sum Km(hm_k)$$
(1)

Subject to:

$$V_{\min} \le V_l \le V_{\max} \qquad l=1,...,NL \qquad (2)$$

$$\beta_{\min} \leq \beta_l \leq \beta_{\max} \qquad l=1,...,NL \tag{3}$$

$$S_{min} \le S_l \le S_{max} \qquad l = 1, \dots, NL \tag{4}$$

$$X_{min} \le X_k \le X_{max} \qquad k=1,\dots,NN \tag{5}$$

$$D_l \varepsilon \mathbf{D}$$
 $l=1,...,NL$ (6)

$$D_l \le D_l' \qquad l=1,...,NL \tag{7}$$

Where, $C_{network}$ is the total cost of the network, Cp_l is the installation cost of l^{th} pipe, Cm_i is the cost of i^{th} manhole, NL is the number of pipes in the network, NN is the number of nodes in the network, L_l is the length of l^{th} pipe, Kp is the unit cost of l^{th} pipe defined as a function of its diameter (D_l) and upstream and downstream nodal cover depth (X_i, X_j) , and Km is the cost of manhole construction as a function of manhole depth (hm).

Equations (2) to (7) represents the constraints of velocity, water-depth ratio, pipe slope, nodal cover depth, commercially available pipe diameter, and progressive diameter for the sewer network problem, respectively, where, V_l is the velocity of l^{th} pipe, $\beta_l = y_l/D_l$, y_l is the flow depth of l^{th} pipe, S_l is the slope of l^{th} pipe, X_k is the cover depth of k^{th} node, **D** is the set of commercially available pipe diameters, l refers to the set of pipe located downstream of pipe l, and *min, max* are the allowable minimum and maximum parameters, respectively.

4. Hybrid Cellular Automata (HCA)

Application of CA to any problem requires that four basic components of the CA method, cell, cell state, neighborhood, and updating rule, are properly defined. In this paper, pipe diameters and nodal cover depths are chosen as the decision variables.

The Hybrid Cellular Automata (HCA) formulation requires decomposing the problem into two sub-optimization problems which are solved iteratively in two stage manners. In the first stage, each node of the sewer network is regarded as a cell and nodal cover depths are considered as the cell states, which are determined with the fixed values of pipe diameters. In the second stage, the pipe diameters are calculated by solving a second nonlinear sub-optimization problem with considering the calculated nodal cover depths from the first stage as fixed values. Two different updating rules, continuous and discrete, are derived and used depending on the treatment of pipe diameters. In the continuous approach, the pipe diameters are considered as continuous variables and the corresponding updating rule is derived mathematically from the original objective function of the problem and followed by a rounding process in which the discrete approach, an ad-hoc updating rule is derived based on the discrete nature of pipe diameters. The described two stage process is iterated until convergence is achieved.

Considering the nodal cover depths, X_k ; k=1,...,NN, and pipe diameters, D_l ; l=1,...,NL, as the decision variables, these constraints can be easily applied as box constraints. Using a penalty method for satisfaction of remaining constraints, the total penalized objective function of the sewer network optimization problem can be defined as follows:

$$Min \ C = \sum Cp_l + \sum Cm_i + \sum (\alpha CSVv_l + \alpha CSVs_l + \alpha CSV\beta_l)$$
(8)

Where, α is the penalty parameters with large enough positive value, and *CSVv*, *CSVs*, *CSVβ* represent the violation from the constraints of velocity, slope, and water-depth ratio for each pipe, respectively, $CSVv_l = (1 - V_l/V_{min})^2 + (V_l/V_{max} - 1)^2$, $CSV\beta_l = (1 - \beta_l/\beta_{min})^2 + (\beta_l/\beta_{max} - 1)^2$, $CSVs_l = (1 - s_l/s_{min})^2 + (s_l/s_{max} - 1)^2$.

Subject to:

$$X_{min} \le X_k \le X_{max} \qquad \qquad k = 1, \dots, NN \tag{9}$$

$$D_{l} \epsilon \mathbf{D} \qquad \qquad l=1,\dots,NL \qquad (10)$$

The process is started with arbitrary sets of pipe diameters and nodal cover depths satisfying the constraints of (9) and (10).

4.1 First Stage

In the first stage, the nodal cover depths are calculated with the minimization of the following local objective function over the cell neighborhood (Ω_k) considering the fixed values for the pipe diameters:

$$C_k = \sum (Cp_l + \alpha CSVv_l + \alpha CSVs_l + \alpha CSV\beta_l) + Cm_k$$
(11)

Subject to the box constraints of $X_{min} \le X_k \le X_{max}$.

Minimization of the local objective function of Equation (11) with respect to the nodal cover depth (X_k) leads to the nonlinear equations to be solved with the Newton-Raphson method which results in the updated nodal cover depths defined as:

$$F(X_k) = \partial C_k / \partial X_k = 0 \qquad \Delta X_k = -F_k / (\partial F / \partial X)_k \Big|^{kk} \qquad \Delta X_k = \Delta X_k^{kk+1} - \Delta X_k^{kk}$$
(12)

Where, $F_k^{kk} = F(X_k^{kk})$, kk is the nonlinear iteration index, and ΔX_k is the change in the value of the cell state. F_k and $(\partial F/\partial X)_k$ are both implicit functions of the X_k which can be calculated using the chain rule of differentiation and Manning equation. This procedure is repeated for the cell under consideration until the convergence is met and the process of updating is repeated for all cells of the network at the end of which the first stage is terminated.

4.2 Second Stage

In the second stage, the values of nodal cover depths obtained in the first stage are used to get the optimal pipe diameters. Two CA approaches are applied to solve this problem, in which the pipes and corresponding diameters are considered as the CA cell and cell state, respectively. The neighborhood of the CA is simply considered as the cell itself without any neighboring cells.

4.2.1 Discrete Approach

In discrete method, the pipe diameters are treated as discrete values leading to an ad-hoc CA updating rule derived based on engineering judgment. The diameter of each pipe is changed such that the pipe cost is minimized in a manner to satisfy the constraints of velocity and water depth ratio. The following three engineering based ad-hoc updating rule is used to update the cell state:

1) If constraints of velocity and water-depth ratio are all satisfied, pipe diameter is decreased to the lower diameter available to minimize the objective function.

2) If one or both of the maximum velocity and water-depth ratio constraints are violated, the pipe diameter is increased to the upper diameter available.

3) If one or both of the minimum velocity and water-depth ratio constraints are violated, the pipe diameter is decreased to the lower diameter available.

4.2.2 Continuous Approach

In continuous method, the updating rule is derived mathematically assuming pipe diameter as continuous variable followed by a rounding procedure to convert the continuous solutions to discrete available diameters such that the following localized objective function is minimized:

$$Minimize \ C_l = Cp_l + \alpha CSV v_l + \alpha CSV \beta_l + Cm_i + Cm_i$$
(13)

Subject to the box constraints of:

$$D_{min} \le D_l \le D_{max} \tag{14}$$

Where *i* and *j* refer to the upstream and downstream node of l^{th} pipe, D_{min} and D_{max} represent the minimum and maximum components of available commercial diameters, respectively. The updating rule is derived mathematically by requiring that the objective function of Equation (13) is stationary with respect to the cell state with applying the Newton-Raphson linearization:

$$G_l = \partial C_l / \partial D_l = 0 \qquad \Delta D_l = -G_l / (\partial G / \partial D)_l \qquad \Delta D_l = \Delta D_l^{kk+l} - \Delta D_l^{kk}$$
(15)

This procedure is repeated for the cell under consideration until the convergence is met. Once the process of updating of all cell states are completed, the continuous diameters so calculated are rounded to the upper discrete diameters available before returning to the first stage. More details of the method can be found in the work of Afshar and Rohani (2012).



Figure 1. Schematic description of the HCA method.

A schematic description of the HCA method is illustrated in Figure 1 for both discrete and continuous versions in which the cells, cell states, neighborhood and the updating rules are briefly described for more clarification.

5. Test Examples

The performance of the HCA method is investigated in this section by applying the model to three design problems with different sizes in the literature. These hypothetical test examples were previously proposed and used by Moeini and Afshar (2012 a,b) for the simultaneous layout and size optimization of sewer network using ACOA based methods.

Figure 2. Network layouts for three examples: a) small scale sewer network, b) medium scale sewer network, c) large scale sewer network.

The optimal layouts obtained by Moeini and Afshar (2012 b), shown in Figure 2, is used here to assess the efficiency and effectiveness of the CA and HCA method. The small scale sewer network consists of 9 nodes and 12 pipes, the medium scale sewer network has 25 nodes and 40 pipes and the large scale sewer network includes 81 nodes and 144 pipes. All the networks have two treatment plants with fixed elevation located at the bottom corner of the sewer network.

The ground elevation of a reference point located at the middle of the upper edge of the area denoted by node 8, 23 and 77 in small, medium and large scale networks, respectively, is considered 1000 metres. The area is considered to have a constant slope of 2% from the reference point to the left and right and toward the bottom edge. The lengths of pipes in three networks are considered as 100 meters and the set of commercially available pipe diameters for all the pipes is included in the range of 100 mm to 1500 mm with an interval of 50 mm from 100 mm to 1000 mm and an interval of 100 mm from 1000 mm to 1500 mm. The Manning coefficient is considered as 0.015 and the problem is constrained to a maximum and minimum velocity of 6 m/s and 0.75 m/s, maximum and minimum cover depth of 10 m and 2.5 m, and maximum and minimum relative flow depth of 0.83 and 0.1, respectively.

The terms of pipe and manhole construction costs are defined as (Moeini and Afshar, 2012 a,b):

$$K_{p} = 10.93e^{3.43D} + 0.012X^{1.33} + 0.437X^{1.47}D$$

$$K_{h} = 41.46h_{m}$$
(16)

Where, D is the pipe diameter (m), X is the buried depth (m), and h_m is the depth of manhole (m).

These test problems are here solved using CA method of Afshar et al. (2011) and HCA methods and the results are presented and compared with other existing methods.

Test Example	Model	Cost	Time (milli second)	
	ACOA-TGA (Moeini and Afshar, 2012 a)	23467	-	
	CACOA-TGA	23467	_	
small scale network	(Moeini and Afshar, 2012 b)			
	CA	23811	1.6	
	HCA-Discrete	23460	4.7	
	HCA-Continuous	23513	3.1	
	ACOA-TGA	86204		
	(Moeini and Afshar, 2012 a)	80204	-	
	CACOA-TGA	95000		
medium scale network	(Moeini and Afshar, 2012 b)	85990	-	
	CA	88096	14.1	
	HCA-Discrete	85873	46.9	
	HCA- Continuous	86678	15.6	
	ACOA-TGA	265600		
	(Moeini and Afshar, 2012 a)	303000	-	
	CACOA-TGA	262022		
large scale network	(Moeini and Afshar, 2012 b)	363922	-	
	CA	370486	103.1	
	HCA-Discrete	361685	200.0	
	HCA- Continuous	367436	54.6	

Table 1. Optimal network cost obtained by different methods

Table 1 compares the optimal network costs and the CPU time required by the CA methods introduced here and those of ACOA-TGA (Moeini and Afshar, 2012 a) and CACOA-TGA (Moeini and Afshar, 2012 b) methods using a 2 MHz Pentium 4. It can be seen that both HCA methods produce better solutions than CA method in three sewer networks. Moreover, the HCA methods result in comparable solutions to the ACOA in small scale network, while with increasing the scale of the problem, the HCA methods produce superior solutions than ACOA. Furthermore, the HCA-discrete method results in better solution than the existing methods while requiring less than one second CPU time to achieve the solutions. It should be noted that ACOA needs much more time than CA methods, because of its mechanism and it is one the population based methods. Since the HCA method requires an initial guess for the decision variables of the problem, pipe diameters and the nodal cover depths, to start off the solution procedure, a sensitivity analysis is carried out here to assess the sensitivity of the final solution to the initial guess.

			Cost		
Test Example	Model	Minimum	Maximum	Average	Scaled Standard Deviation
	ACOA-TGA (Moeini and Afshar, 2012 a)	23467	23467	23467	0.0000
small scale network	CACOA-TGA (Moeini and Afshar, 2012 b)	23467	23467	23467	0.0000
	CA	23811	23811	23811	0.0000
	HCA-Discrete	23460	23747	23546	0.0059
	HCA-Continuous	23513	34064	25798	0.1683
	ACOA-TGA (Moeini and Afshar, 2012 a)	86204	87127	86642	0.0037
medium scale network	CACOA-TGA (Moeini and Afshar, 2012 b)	85990	86591	86187	0.0020
	CA	88096	88096	88096	0.0000
	HCA-Discrete	85873	86953	86410	0.0052
	HCA- Continuous	86678	87786	87397	0.0038
	ACOA-TGA (Moeini and Afshar, 2012 a)	365600	381484	372605	0.0127
large scale network	CACOA-TGA (Moeini and Afshar, 2012 b)	363922	367174	365606	0.0030
	СА	370486	370489	370488	0.0000
	HCA-Discrete	361685	367131	363894	0.0040
	HCA- Continuous	367436	371350	369661	0.0031

Table 2. Maximum, Minimum and Average solution costs over 10 runs

Table 2 represents the maximum, minimum and average solution costs over 10 runs using different initial designs along with the scaled standard deviation of the solutions defined as the ratio of the standard deviation to the average solution. This table emphasizes on the insensitivity of the CA methods to the initial population.

Table 3. Results obtained from HCA method (discrete) for the small scale sewer network

Cover Depth (m)										
Pipe	D (mm)	Upstream	Downstream	V (m/s)	y/d					
1	100	2.50	4.50	1.39	0.57					
2	150	2.50	4.50	1.83	0.58					
3	200	3.40	4.50	2.04	0.67					
4	150	2.50	2.50	1.27	0.56					
5	200	2.50	4.50	2.08	0.50					
6	150	2.50	3.40	1.67	0.82					
7	150	2.50	2.50	1.27	0.56					
8	150	2.50	3.40	1.47	0.50					
9	150	2.50	2.50	1.27	0.56					
10	150	2.50	2.50	1.27	0.56					
11	100	2.50	2.50	1.05	0.73					
12	100	2.50	2.50	1.05	0.73					

Table 4 Results obtained from HCA method	(discrete) for the medium scale sewer network
rable 4. Results obtained from free method	(discrete) for the medium scale sewer network

		Cover	Depth (m)			Cover Depth (m)					
Pipe	D(mm)	Upstream	Downstream	V (m/s)	y/d	Pipe	D(mm)	Upstream	Downstream	V (m/s)	y/d
1	200	2.50	4.50	2.18	0.55	21	150	2.50	2.50	1.27	0.56
2	150	2.50	2.50	1.38	0.74	22	150	2.50	2.50	1.27	0.56
3	100	2.50	2.50	1.05	0.73	23	200	2.50	2.50	1.60	0.62
4	150	2.50	4.50	1.94	0.71	24	200	2.50	2.80	1.79	0.75
5	350	3.45	4.50	2.92	0.65	25	150	2.50	3.40	1.67	0.82
6	150	2.50	2.50	1.27	0.56	26	200	2.50	2.50	1.68	0.80
7	150	2.50	2.50	1.27	0.56	27	200	2.50	2.50	1.60	0.62
8	150	2.50	2.50	1.27	0.56	28	150	2.50	2.50	1.27	0.56
9	300	3.17	4.50	2.82	0.73	29	150	2.50	2.50	1.27	0.56
10	300	3.47	3.45	2.19	0.82	30	150	2.50	2.50	1.27	0.56
11	150	2.50	3.47	1.69	0.81	31	150	2.50	2.50	1.27	0.56
12	150	2.50	2.50	1.27	0.56	32	150	2.50	2.50	1.27	0.56
13	250	2.50	3.17	2.26	0.82	33	150	2.50	2.50	1.38	0.74
14	200	2.50	3.45	2.03	0.76	34	150	2.50	2.50	1.27	0.56
15	250	2.80	3.47	2.26	0.82	35	150	2.50	2.50	1.38	0.74
16	150	2.50	2.50	1.27	0.56	36	150	2.50	2.50	1.27	0.56
17	250	2.50	2.50	1.92	0.71	37	100	2.50	2.50	1.05	0.73
18	200	2.50	3.17	1.94	0.79	38	100	2.50	2.50	1.05	0.73
19	150	2.50	2.50	1.27	0.56	39	100	2.50	2.50	1.05	0.73
20	200	3.40	2.80	1.41	0.82	40	100	2.50	2.50	1.05	0.73

Table 5. Results obtained from HCA method (discrete) for the large scale sewer network

	Cover Depth (m)							Cover	Depth (m)		
Pipe	D(mm)	Upstream	Downstream	V (m/s)	y/d	Pipe	D(mm)	Upstream	Downstream	V (m/s)	y/d
1	350	4.14	4.50	2.59	0.68	73	200	2.50	2.50	1.52	0.53
2	300	3.34	4.14	2.61	0.82	74	200	2.50	3.00	1.88	0.82
3	200	2.50	3.34	1.90	0.62	75	400	3.00	3.17	2.77	0.76
4	150	2.50	2.50	1.38	0.74	76	150	2.50	2.50	1.27	0.56
5	100	2.50	2.50	1.05	0.73	77	250	3.00	2.50	1.69	0.80
6	200	2.50	2.50	1.52	0.53	78	400	4.02	4.37	2.84	0.70
7	200	2.50	2.50	1.68	0.80	79	150	2.50	2.50	1.27	0.56
8	200	2.50	4.50	2.38	0.81	80	150	2.50	2.50	1.27	0.56
9	500	3.93	4.50	3.52	0.82	81	150	2.50	2.50	1.27	0.56
10	150	2.50	4.14	1.60	0.47	82	150	2.50	2.50	1.27	0.56
11	300	3.88	3.34	1.88	0.82	83	350	2.71	3.00	2.62	0.82
12	150	2.50	2.50	1.27	0.56	84	250	2.50	3.17	2.26	0.82
13	150	2.50	2.50	1.27	0.56	85	250	3.00	2.50	1.69	0.80
14	150	2.50	2.50	1.27	0.56	86	150	2.50	3.00	1.39	0.52
15	150	2.50	2.50	1.27	0.56	87	300	2.50	4.02	2.93	0.82
16	150	2.50	2.50	1.27	0.56	88	200	2.50	2.50	1.65	0.70
17	550	3.78	4.50	3.86	0.82	89	150	2.50	2.50	1.27	0.56
18	200	2.50	3.93	2.05	0.58	90	200	2.50	3.00	1.88	0.82
19	150	2.50	2.50	1.27	0.56	91	250	3.00	2.71	1.81	0.82
20	200	2.50	3.88	2.04	0.58	92	150	2.50	2.50	1.27	0.56
21	150	2.50	2.50	1.27	0.56	93	150	2.50	3.00	1.39	0.52
22	150	2.50	3.40	1.67	0.82	94	200	2.50	3.00	1.88	0.82
23	200	3.40	3.89	1.88	0.82	95	250	2.50	4.02	2.41	0.58
24	250	3.89	3.60	1.81	0.82	96	300	2.50	2.50	2.20	0.78
25	550	3.60	3.78	3.43	0.76	97	150	2.50	2.50	1.27	0.56
26	500	3.71	3.93	3.26	0.82	98	200	2.50	2.50	1.65	0.70
27	150	2.50	2.50	1.27	0.56	99	150	2.50	3.00	1.39	0.52
28	200	2.50	3.88	1.77	0.78	100	300	2.5	2.71	2.30	0.74
29	150	2.50	2.50	1.27	0.56	101	250	2.50	2.50	1.92	0.71

30	150	2.50	2.50	1.27	0.56	102	200	2.50	3.00	1.88	0.82
31	150	2.50	3.40	1.47	0.50	103	150	2.50	2.50	1.27	0.56
32	150	2.50	3.89	1.56	0.48	104	150	2.50	2.50	1.27	0.56
33	550	4.00	3.60	2.95	0.77	105	200	2.50	2.50	1.65	0.70
34	300	2.50	3.78	2.71	0.64	106	150	2.50	2.50	1.27	0.56
35	500	4.32	3.71	2.59	0.82	107	150	2.50	2.50	1.27	0.56
36	150	2.50	4.32	1.63	0.46	108	250	2.50	2.50	1.92	0.71
37	200	2.50	2.50	1.65	0.70	109	150	2.50	2.50	1.27	0.56
38	150	2.50	2.50	1.27	0.56	110	150	2.50	2.50	1.27	0.56
39	200	2.50	2.50	1.52	0.53	111	200	2.50	2.50	1.60	0.62
40	200	2.50	3.00	1.88	0.82	112	200	2.50	2.50	1.68	0.80
41	250	3.00	4.00	2.31	0.65	113	250	2.50	2.50	1.94	0.76
42	150	2.50	2.50	1.27	0.56	114	150	2.50	2.50	1.27	0.56
43	300	2.50	3.71	2.60	0.58	115	200	2.50	2.50	1.52	0.53
44	500	5.08	4.32	2.44	0.82	116	200	2.50	2.50	1.68	0.80
45	150	2.50	2.50	1.27	0.56	117	200	2.50	2.50	1.68	0.80
46	150	2.50	2.50	1.27	0.56	118	200	2.50	2.50	1.68	0.80
47	150	2.50	2.50	1.27	0.56	119	200	2.50	2.50	1.60	0.62
48	150	2.50	2.50	1.27	0.56	120	150	2.50	2.50	1.27	0.56
49	150	2.50	3.00	1.39	0.52	121	150	2.50	2.50	1.27	0.56
50	450	3.09	4.00	3.48	0.82	122	200	2.50	2.50	1.68	0.80
51	300	2.83	2.50	2.00	0.73	123	150	2.50	2.50	1.27	0.56
52	150	2.50	2.50	1.27	0.56	124	150	2.50	2.50	1.27	0.56
53	200	2.50	5.08	2.54	0.76	125	150	2.50	2.50	1.27	0.56
54	200	2.50	2.50	1.65	0.70	126	150	2.50	2.50	1.27	0.56
55	150	2.50	2.50	1.27	0.56	127	150	2.50	2.50	1.27	0.56
56	150	2.50	3.40	1.67	0.82	128	150	2.50	2.50	1.27	0.56
57	250	3.40	2.50	1.42	0.70	129	150	2.50	2.50	1.38	0.74
58	250	2.50	3.09	2.17	0.68	130	150	2.50	2.50	1.38	0.74
59	150	2.50	2.83	1.35	0.53	131	150	2.50	2.50	1.38	0.74
60	300	2.50	2.50	2.07	0.60	132	150	2.50	2.50	1.27	0.56
61	400	4.37	5.08	3.11	0.82	133	150	2.50	2.50	1.38	0.74
62	150	2.50	2.50	1.27	0.56	134	150	2.50	2.50	1.38	0.74
63	150	2.50	2.50	1.27	0.56	135	150	2.50	2.50	1.38	0.74
64	150	2.50	2.50	1.27	0.56	136	150	2.50	2.50	1.27	0.56
65	150	2.50	3.40	1.47	0.50	137	100	2.50	2.50	1.05	0.73
66	150	2.50	2.50	1.27	0.56	138	100	2.50	2.50	1.05	0.73
67	450	3.17	3.09	2.83	0.82	139	100	2.50	2.50	1.05	0.73
68	250	2.50	2.83	2.11	0.82	140	100	2.50	2.50	1.05	0.73
69	150	2.50	2.50	1.27	0.56	141	100	2.50	2.50	1.05	0.73
70	200	2.50	4.37	2.34	0.82	142	100	2.50	2.50	1.05	0.73
71	200	2.50	2.50	1.65	0.70	143	100	2.50	2.50	1.05	0.73
72	150	2.50	2.50	1.27	0.56	144	100	2.50	2.50	1.05	0.73

Details of the optimal solution obtained by the HCA-discrete method for three sewer networks are also shown in Table 3, 4, and 5, respectively.

6. Concluding Remarks

In this paper, Hybrid Cellular Automata approach was used for the optimal solution of sewer network design problems. The problem was decomposed to two stages with considering the nodal cover depths and pipe diameters as decision variables. In the first stage, nodal cover depths were calculated assuming fixed values for the pipe diameters, while in the second stage, the pipe diameters were determined in two approaches of continuous and discrete with nodal cover depths of the first stage. Two stages were solved iteratively until the convergence was achieved. The HCA methods were used to solve three benchmark examples in the literature and the comparison of results with two versions of Ant Colony Optimization Algorithm indicated the ability and efficiency of the HCA methods to produce better results comparable to those of heuristic search methods with much higher efficiency.

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