1	Photonic Weyl points due to broken time-reversal symmetry in magnetized
2	semiconductor
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18	Weyl points are discrete locations in the three-dimensional momentum space where two bands
19	cross linearly with each other. They serve as the monopoles of Berry curvature in the
20	momentum space, and their existence requires breaking of either time-reversal or inversion
21	symmetry ¹⁻¹⁶ . Although various non-centrosymmetric Weyl systems have been reported ¹⁵ ,
22	demonstration of Weyl degeneracies due to breaking of the time reversal symmetry remains
23	scarce and is limited to electronic systems ^{17,18} . Here, we report the experimental observation of
24	photonic Weyl degeneracies in a magnetized semiconductor - InSb, which behaves as
25	magnetized plasma ¹⁹ for electromagnetic waves at the terahertz band. By varying the magnetic
26	field strength, Weyl points and the corresponding photonic Fermi-arcs have been demonstrated.

Our observation establishes magnetized semiconductors as a reconfigurable²⁰ terahertz Weyl
 system, which may prompt research on novel magnetic topological phenomena such as chiral
 Majorana type edge states and zero modes in classic systems^{21,22}.

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31 Weyl points as topologically chiral singularity points in the three-dimensional momentum space have been extensively investigated in both quantum and classical systems¹⁵. In photonics, Weyl points have 32 been observed in various systems such as gyroid photonic crystals^{7,23}, metamaterials²⁴⁻²⁶, and 33 evanescently coupled helical waveguides²⁷. However, all the previously demonstrated photonic Weyl 34 points are exclusively based on systems with broken inversion symmetry¹⁵. On the other hand, it has 35 36 been proposed that Weyl points due to breaking of the time-reversal symmetry may possess more interesting properties such as axial anomaly, giant photocurrent and novel quantum oscillation 37 phenomena²⁸⁻³⁰. They may enable multiple striking topological features such as Majorana type edge 38 states and zero mode²², which do not exist in inversion symmetry breaking systems. Although there 39 have been theoretical proposals on implementation of Weyl degeneracies by applying external 40 magnetic fields on finely designed photonic crystals^{16,31}, very few of them are easily realizable in 41 experiment due to the challenge in three-dimensional structuring of magnetic materials^{32,33}. 42 43 Interestingly, it was recently theoretically proposed that plasma, the fourth fundamental state of natural matter^{34,35}, can support Weyl degeneracies under external magnetic fields¹⁹, as well as nonreciprocal 44 wave transport³⁶⁻³⁸. Since there is no structuring involved, this represents a facile and tunable approach 45 46 for achieving photonic Weyl degeneracies arising from time-reversal symmetry breaking.

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In this work, by applying magnetic field to intrinsic semiconductor InSb, we demonstrate photonic Weyl points due to broken time reversal symmetry. Here $InSb^{39,40}$ is chosen because of its very small effective mass of electrons ($m^* = 0.015m_0$, where m_0 is the free electron mass) that can lead to a terahertz cyclotron frequency under a moderate applied magnetic field. Along the direction of magnetic field, electrons can move freely. Therefore, the dielectric function is described by the Drude model, and there exists a longitudinal bulk plasma mode along the applied magnetic field. However, in the plane perpendicular to the magnetic field, the dielectric function is significantly modified due to the cyclotron motion of electrons, which leads to the breaking of degeneracy between the left and right circular polarizing (L/RCP) modes propagating along the magnetic field^{40,36}. The linear crossing between the longitudinal plasma mode and a circular polarizing mode forms a Weyl point in the magnetized plasma system¹⁹. By considering the coupling between the electromagnetic wave and the motion of the free charges in the plasma, we can derive a full Hamiltonian *H* as (see supplementary information 1)¹⁹:

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$$\omega_{p} \begin{bmatrix} 0 & -k \times /\sqrt{\varepsilon_{\infty}}k_{p} & -i/\sqrt{\varepsilon_{\infty}} \\ k \times /\sqrt{\varepsilon_{\infty}}k_{p} & 0 & 0 \\ i\sqrt{\varepsilon_{\infty}} & 0 & (\omega_{c}\Delta - i\gamma I)/\omega_{p} \end{bmatrix} \begin{bmatrix} E \\ H \\ V \end{bmatrix} = \omega \begin{bmatrix} E \\ H \\ V \end{bmatrix}$$
(1)

where $\omega_p = \sqrt{ne^2/\varepsilon_0 \varepsilon_\infty m^*}$ and $\omega_c = eB/m^*$ are the plasma frequency and electron cyclotron 62 frequency, respectively, with *n* being the free electron density, ε_0 the permittivity of vacuum and $\varepsilon_{\infty} = 16$ 63 64 the dielectric constant at high frequencies; k_p is the vacuum wave vector at the plasma frequency, y is the damping frequency and $\Delta = [\sigma_y, 0; 0, 0]$ with σ_y being the second Pauli matrix. By carefully 65 66 controlling the temperature, the carrier density of InSb can be tuned to give a plasma frequency around 67 $\omega_p/2\pi = 0.3$ THz, which falls in the frequency range of our terahertz measurement setup. Depending on 68 the relative values of ω_c and ω_p , different numbers of Weyl points may show up in our system (see 69 supplementary information 2, Fig. S1). When $\omega_c > \omega_p$, there are two pairs of Weyl points appearing at the plasma frequency with the momentum coordinates $(k_x, k_y, k_z) = (0, 0, \pm \sqrt{\varepsilon_{\infty} \omega_c / (\omega_c \pm \omega_p)}),$ 70 71 where the magnetic field is applied along z direction. Around the outer Weyl point (located at larger 72 k_z), the first order $k \cdot p$ Hamiltonian expansion can be expressed as:

$$H_1 = \frac{N}{2}(\sigma_0 + \sigma_3)(M\delta k_z + \xi P\delta B) + N\sigma_1\delta k_y - N\sigma_2\delta k_x$$
(2)

with parameters *M*, *N*, *P* being linear dispersion coefficients defined by the coordinates at the outer Weyl point, ξ the cyclotron constant and σ_i the Pauli matrices as described in supplementary information 3.

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For a semiconductor InSb under a magnetic field strength of B = 0.19 T, the corresponding cyclotron frequency is $\omega_c/2\pi \approx 0.35$ THz, which leads to the band structure shown in Fig. 1a, where plasma frequency is taken as $\omega_p/2\pi = 0.31$ THz. Along the magnetic field, four double degenerate Weyl points 81 are located at the plasma frequency as expected. Here, we only consider the outer pair of Weyl points 82 as the inner pair with opposite topological charges are enclosed by the same equifrequency surface and 83 therefore they are not responsible for the observed topological features. Fig. 1b shows the projected 84 band structure around one of the outer Weyl points. It is shown that the dispersions of two participating 85 modes divide the momentum-energy space into four regions representing the bulk states and gaps. 86 respectively. This projected band morphology as a signature of photonic Weyl points can be observed 87 through the reflection spectra when scanning the wave vector k_z . However, in the experiment, scanning 88 k_z requires an angle resolved reflection system, which is incompatible with our magnetic terahertz 89 system. Equivalently, we can scan the magnetic field strength B instead of k_z , since they behave 90 similarly in constructing the parameter space of the Weyl point, as shown by the form of effective 91 Hamiltonian in Eq. 2. Fig. 1c shows the band structure constructed in the synthetic parameter space $[k_x]$ k_{y} , B] for a fixed incident wave vector of $k_z = 2\pi/90 \ \mu m^{-1}$. One can see that the linear crossing is 92 93 preserved in the substituted band structure (Fig. 1d, e), confirming the presence of Weyl points in the 94 synthetic parameter space (for detailed proof, see supplementary information 3).

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96 In order to characterize the Weyl point, we apply a magnetic field along an in-plane direction (parallel 97 to the surface), as shown in Fig. 2a. It is expected that two Weyl points of opposite chiralities appear 98 along the direction of B field. They are both located outside the light cone. In order to probe the 99 reflection spectra around the Weyl points, we employ a grating to compensate the in-plane momentum 100 mismatch between the incident terahertz wave and the Weyl points. The aluminum grating, fabricated 101 directly on the surface of the InSb wafer, has a period of $p = 90 \,\mu\text{m}$, a filling ratio of 2/3 and a thickness 102 of $t = 1 \mu m$. The sample is then placed in a low temperature environment of T = 50 K to provide a plasma frequency of $\omega_p/2\pi \approx 0.31$ THz with a damping factor of $\gamma/2\pi = 3 \times 10^{10}$ Hz. A normal incidence 103 104 configuration is employed with the magnetic field applied along the grating direction, as shown in Fig. 105 2b. A high resistivity float zone Silicon 50/50 terahertz beam splitter is used for the reflection spectra 106 measurement. The grating provides a fundamental order wave vector of magnitude $G = 2\pi/p$ to excite 107 both the bulk and surface states supported by the magnetized InSb. As the magnetic field strength is 108 scanned from 0-1 Tesla, we measure the reflection spectrum. These measurements provide the 109 projected band information as shown in Fig. 2c, where the band crossing can be clearly observed at the 110 frequency of $\omega_p/2\pi = 0.31$ THz and magnetic field of B = 0.19 T. Fig. 2d shows the corresponding full 111 wave simulation results that take into account the actual dissipation in the magnetized plasma. 112 Simulation results shown in Fig. 2d show good agreement with the experimental results. On the other 113 hand, when the grating direction is rotated away from the direction of magnetic field, the crossing 114 point disappears and a bandgap is formed, as shown in supplementary information 4, Fig. S2. The 115 experimental results confirm the presence of Weyl degeneracies in a magnetized semiconductor 116 system.

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118 The most important signature of a Weyl system is the presence of Fermi-arcs. The photonics 119 Fermi-arcs in the original momentum space are explored in the supplementary information 5 where the surface states are found to be separated into two separated frequency bands: $\omega < \omega_p$ and $\omega >$ 120 $\sqrt{\omega_p^2 + \omega_c^2}$ with opposite signs of k_y , respectively, due to the magnetic field induced cyclotron 121 122 resonance. These two branches of surface states are observed in the experimentally measured *f-B* plot 123 manifested as absorption lines in the reflection spectra. The theoretically calculated surface states are 124 indicated by a black dashed line in both the experimental and simulated results in Fig. 2c-d, which fits 125 well with the corresponding surface states induced absorption.

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127 To further explore the surface state features in the magnetized Weyl system, a second experimental 128 configuration is employed as shown in Fig. 3a, in which the incidence terahertz beam and the applied magnetic field are arranged to form angles $\theta = 45^{\circ}$ and $\alpha = 45^{\circ}$ with respect to the sample normal and 129 130 sample surface, respectively. In this configuration, a beam splitter is not required and therefore the 131 signal noise ratio of the measurement is improved by approximately four times in comparison to that of 132 normal incidence. Rotating the grating around x axis by an angle of φ as shown in Fig. 3a (bottom-left inset) provides a non-zero k_y to excite the off k_z axis surface states on the k_y - k_z plane, as shown in Fig. 133 3a (right insets). Meanwhile, due to the tilted incidence, the degeneracy between $\pm 1^{st}$ grating order is 134 lifted. The $\pm 1^{\text{st}}$ order excitation wave vector is given by $[k_v, k_z]_{\pm 1} = [\pm G \sin \varphi, \pm G \cos \varphi + k_0 \sin 45^\circ]$ as 135 136 illustrated in Fig. 3a (bottom-left inset), where φ is the angle formed between the grating momentum

and z axis. For a given magnetic field, it is expected that the $\pm 1^{st}$ order with opposite signs of k_y can excite surface states at the two aforementioned frequency bands (see supplementary information 5, Fig S3).

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141 In this tilted configuration, the Weyl points are projected onto the sample surface with a smaller in-plane wave vector $(k_z = \pm \sqrt{\varepsilon_{\infty} \omega_c / 2(\omega_c - \omega_p)})$, as shown in Fig. 3b. A different sample with a 142 greater grating periodicity of $p = 120 \ \mu m$ is therefore designed to match the momentum. The new 143 sample has a similar plasma frequency $\omega_p/2\pi \approx 0.31$ THz as the previous one. The projected bulk 144 bands on B - f plane are plotted for $\varphi = -30^{\circ}$ and -45° in Fig. 3c and f, where the bulk states excited by 145 the $\pm 1^{st}$ grating orders have a large overlap with each other and are indicated by navy and purple color, 146 respectively. The surface states excited by the $\pm 1^{st}$ grating orders are also calculated and shown in Fig. 147 3c and f, respectively. At each grating angle φ , the $\pm 1^{st}$ order excitations with opposite signs of k_v form 148 149 two separate branches, which merge into each other at zero applied magnetic field B. It is also 150 observed that at increasing φ , the angle between two surface state branches widens, due to the increase 151 in the slopes of the dispersion. It can be noticed that the surface state is interrupted around the cyclotron position, which is caused by the strong cyclotron resonance that leads to relatively high 152 reflection⁴¹. For a negative φ , the diffraction orders that excite the two surface state branches switch in 153 154 comparison to that with a positive φ (see more discussion in supplementary information 6, Fig. S4).

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The measured reflection spectra are shown in Fig. 3e and Fig. 3h for $\varphi = -30^{\circ}$ and -45° (see 156 157 supplementary information 7, Fig. S5 for more measured results), respectively, which presents the 158 superposed band projection for both bulk and surface states. The corresponding simulation results for 159 the reflection spectra shown in Fig. 3d and g are in good agreement with the experiment results. It is 160 noticed that there exists a cut-off for the surface state branch at higher frequencies, due to the limited 161 momentum provided by the grating (see supplementary information 8, Fig. S6). Higher grating orders 162 are also excited in the experiment, which contribute to the absorptions along the surface state branch at 163 the higher frequencies beyond the cut-off of the first grating order.

165 For a given grating diffraction order, the projection of photonic Weyl point can also be described in the 166 parameter space $[\varphi, B]$. Using the same configuration as in Fig. 3a, a sample with higher plasma frequency of $\omega_p/2\pi \approx 0.53$ THz and grating periodicity of $p=150\mu m$ is measured (supplementary 167 information 9, Fig. S7). The Weyl point which is projected at location $(k_v, k_z) = (0, G + k_0 \sin 45^\circ)$ in the 168 momentum space turns into $(\varphi, B) = (0, 0.472)$ for the +1 grating order (supplementary information 10, 169 170 Fig. S8). The projected dispersion of the bulk states with respect to B for $\varphi = 0$ is shown in Fig. 4a. 171 where a linear crossing indicating an effective Weyl point is observed. The linear dispersion with 172 respect to φ around the effective Weyl point is confirmed in Fig. 4b. The calculated surface states for 173 different grating orientation angle φ are shown in Fig. 4c and d, where it is clearly shown that larger 174 orientation angles lead to steeper dispersion in B. A photonic Fermi-arc in the $B-\varphi$ plane can thus be constructed at a given frequency. For the $+1^{st}$ grating order excitation, the photonic Fermi-arcs together 175 176 with the bulk bands at two different frequencies 0.46 THz and 0.6 THz are shown in Fig. 4e and f, 177 respectively. The experimental data (cyan hollow dots) is in good agreement with the theoretical result. 178 It should be noted that due to the presence of loss, the Weyl point transforms into exceptional ring¹⁹, 179 which possesses the same topological charge as a Weyl point. The size of the ring is calculated based 180 on the actual dissipation of the semiconductor and is found to be negligibly small (see supplementary 181 information 11, Fig. S9). Meanwhile, a discussion of the loss and surface wave resonance is shown in 182 supplementary information 12, Fig. S10.

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In summary, we have demonstrated the first classical system possessing Weyl points due to time reversal symmetry breaking. The locations of the Weyl points can be readily tuned by varying the applied magnetic field or the temperature. Importantly, our Weyl system does not require complicated 3D fabrication as required by previously demonstrated classical Weyl systems. The observed Weyl points and topological surface states in the magnetized InSb also represent the first demonstration of topological phase in the terahertz band, which may facilitate the development of terahertz topological devices.

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193 Data availability:

- 194 The data that support the findings of this study are available from the corresponding author on
- 195 request.
- 196

197 Acknowledgement:

- 198 This work is supported by ERC Consolidator Grant (TOPOLOGICAL), the Royal Society and the
- 199 Wolfson Foundation. M. N.-C. acknowledges support from University of Birmingham (Birmingham
- 200 Fellowship).
- 201

202 **Figures:**

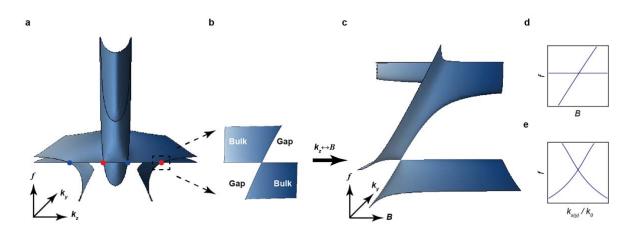
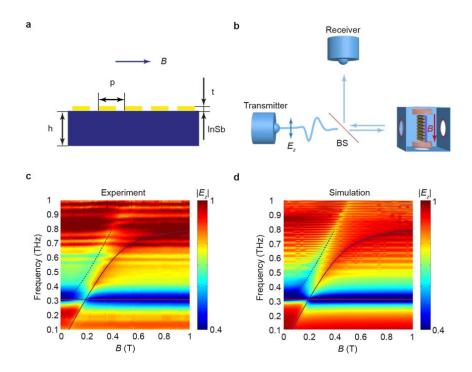




Figure 1 | Bulk states of lossless magnetized InSb. a, The band structure and Weyl points in magnetized plasma system. The parameters used in the calculation are: $\omega_p/2\pi = 0.31$ THz, B = 0.19 T and no damping is considered. b, Band projection around the outer Weyl point, whose coordinate is $(k_x, k_y, k_z) = (0, 0, 10.8)$ k_p with k_p indicating the vacuum wave vector at plasma frequency. c, Band structure with k_z been substituted by *B*. A fixed value of $k_z = 10.8$ k_p is assumed and the magnetic field scanning range is $0 \le B \le 1$ T. d, Dispersion along *B* around the outer Weyl point in c. e, Similar to d but along $k_{x(y)}$. k_0 indicates vacuum wave vector.





213 Figure 2 | Observation of terahertz Weyl point in a magnetized semiconductor system. a, 214 Schematic of the sample with metal grating on top of the InSb substrate. The specified magnetic field 215 direction is along grating, geometric parameters are: $p = 90 \ \mu m$, $h = 1250 \ \mu m$ and $t = 1 \ \mu m$. **b**, 216 Illustration of the experiment setup for terahertz reflection measurement. Two terahertz antennas are 217 placed to be right angle and form a normal incidence onto the sample. 'BS' indicates the 50/50 beam 218 splitter. The sample is placed in a commercial equipment with low temperature environment, where 219 the built in superconducting coils provide tunable magnetic field strength. Linear polarization of 220 incidence wave is indicated. c, Experimentally measured reflection spectra. The band crossing 221 coordinate can be estimated as $\omega_p/2\pi \approx 0.31$ THz and B = 0.19 T. d, Reflection spectra calculated with full wave simulation, a damping factor of $\gamma/2\pi = 3 \times 10^{10}$ Hz is considered in the simulation. Dashed 222 223 line indicates the cyclotron resonance position ($\omega_e/2\pi \approx 1.8626 \times B$ THz), red/blue curves are the bulk 224 states and black curves are surface states under lossless assumption, respectively.

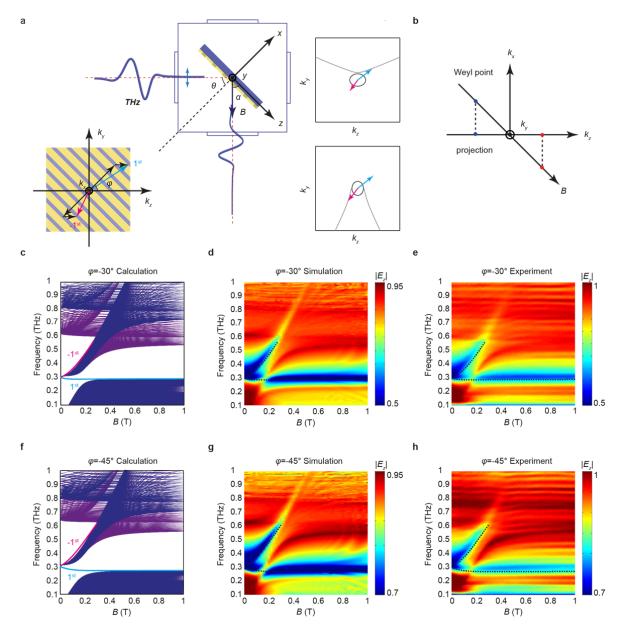


Figure 3 | Surface states under tilted incidence excitation. a, Schematic experiment configuration 226 with respect of θ =45° and α =45°. The rotation angle of grating is φ about x-axis. ±1st grating order 227 228 momentum is coupled with incidence wave and excites surface states for corresponding grating angle φ . The material parameters for the sample are $\omega_p/2\pi \approx 0.31$ THz and $\gamma/2\pi = 3 \times 10^{10}$ Hz. **b**, Projected 229 Weyl points on the sample surface plane. $\mathbf{c}, \pm 1^{st}$ grating order excited bulk bands within the range of k_x 230 \in [-100 k_0 , 100 k_0] (+1st bands are indicated with navy color and -1st with purple) and surface states for 231 $\varphi = 30^{\circ}$ on the *B* - *f* plane. Here we set $\gamma = 0$. **d**, Simulated reflection spectra for $\varphi = 30^{\circ}$, $h=10000 \,\mu\text{m}$, 232 as well as the calculated surface states (black dashed) under $\pm 1^{st}$ grating order excitation and the 233

- 234 cyclotron line (red dashed). e, Experimentally measured reflection spectra for $\varphi = 30^{\circ}$, $h=1250 \,\mu\text{m}$. f-h,
- 235 Similar to **c-e** but for $\varphi = 45^{\circ}$.

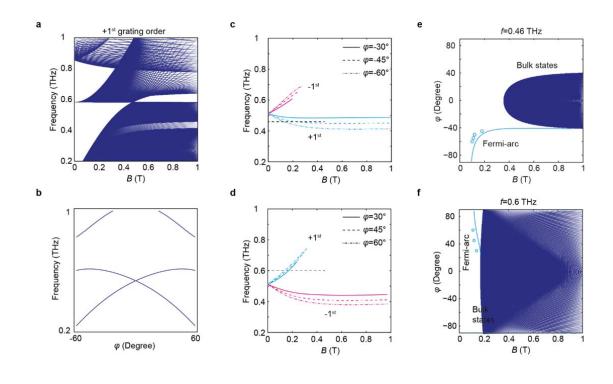




Figure 4 | Photonic Weyl points and Fermi-arcs in synthetic space. a, Projected band along k_x axis on the f - B plane, within the range of $k_x \in [-100k_0, 100k_0]$ for $\varphi=0^\circ$, the Weyl point can be found around B=0.472 T. b, The linear dispersion along φ . c, $\pm 1^{st}$ order grating selected surface state on B - fplane for $\varphi=-30^\circ$, -45° , -60° . d, Similar to c but for $\varphi=30^\circ$, 45° , 60° . e, Constructed photonic Fermi-arcs on (B, φ) space for frequency of f=0.46 THz, within the range of $k_x \in [-100k_0, 100k_0]$. f, Similar to e but for f=0.6 THz. Cyan hollow dots indicate experimentally measured results.

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