

# 1 **Computational Simulations of Thrombolysis in Acute Stroke: Effect of Clot** 2 **Size and Location on Recanalisation**

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## 18 19 **Abstract**

20 Acute ischaemic stroke can be treated by intravenous thrombolysis whereby tissue plasminogen activator  
21 (tPA) is infused to dissolve clots that block blood supply to the brain. In this study, we aim to examine the  
22 influence of clot location and size on lysis pattern and recanalisation by using a recently developed  
23 computational modelling framework for thrombolysis under physiological flow conditions. An image-  
24 based patient-specific model is reconstructed which consists of the internal carotid bifurcation with the  
25 A1 segment of anterior cerebral arteries and M1 segment of middle cerebral arteries, and the M1

26 bifurcation containing the M2 segments. By varying the clot size and location, 7 scenarios are simulated  
27 mimicking thrombolysis of M1 and M2 occlusions. Our results show that initial breakthrough always  
28 occurs along the inner curvature of the occluded cerebral artery, due to prolonged tPA residence time in  
29 the recirculation zone. For a given occlusion site, lysis completion time appears to increase almost  
30 quadratically with the initial clot volume; whereas for a given clot volume, the simulated M2 occlusions  
31 take up to 30% longer for complete lysis compared to the corresponding M1 occlusions.

32

33 **Keywords:** Ischaemic stroke; Thrombolytic therapy; Blood clot; Tissue plasminogen activator (tPA);  
34 Computational model; Drug transport

35

## 36 **1. Introduction**

37 Ischaemic stroke is one of the leading causes of global death and the most common type of stroke [1,2]. It  
38 occurs when a cerebral artery is occluded by a blood clot, impairing blood supply to the brain. The blood  
39 clot can be removed by different medical procedures, one of which is thrombolytic therapy whereby a  
40 fibrinolytic agent, such as recombinant tissue-type plasminogen activator (tPA), is administered to  
41 patients to dissolve the clots in their cerebral arteries. However, the use of tPA is limited by bleeding  
42 complications due to the fibrin specificity of tPA [2–4]. Furthermore, the effectiveness of thrombolytic  
43 treatment is determined by many factors, such as patients’ cerebral vasculature (e.g. collateralisation  
44 determined by the architecture of the Circle of Willis) [5,6], the location, size and composition of clot and  
45 drug dosing regimens. Mechanical thrombectomy is an alternative method which aims to retrieve blood  
46 clots and is increasingly adopted following successful clinical trials [7–9]. Despite its benefits and  
47 positive outcomes, it has only been applied to patients with large vessel occlusions [10] and its safety and  
48 efficacy for small vessel occlusions remain to be answered [11–13]. It has also been reported that  
49 thrombectomy performed in combination with thrombolytic therapy may achieve enhanced treatment  
50 outcome [14–17]. Therefore, it is necessary to understand how clots would be dissolved upon tPA  
51 infusion in different clinical settings.

52

53 To do so, we investigate the effects of various factors on the outcome of thrombolysis via computational  
54 simulations using a recently developed mathematical modelling platform [18,19] Our multi-level model  
55 includes pharmacokinetics and pharmacodynamics (PKPD) for the systemic levels of tPA and fibrinolytic  
56 proteins in the plasma, blood flow and drug transport in patient-specific arterial geometry and fibrinolytic  
57 reactions within a fibrin clot [19]. The model was used to study the effects of different drug doses and clot  
58 density on the level of fibrinolytic proteins and lysis completion time, indicative of the risk of bleeding  
59 and treatment efficacy, respectively.

60

61 In addition to drug dosage and clot properties, the size and location of clot have been reported to be  
62 associated with the likelihood of successful recanalisation and favourable clinical outcomes [20–26]. A  
63 number of clinical studies reported that clot lengths in patients with occlusions in their middle cerebral  
64 arteries (MCA) were correlated with the success of recanalisation after thrombolytic therapy [20,24,25]. It  
65 was observed in almost all studies that very long clots resulted in low recanalisation rates, although a  
66 clear cut-off was not identified. A more recent study by Yoo et al. correlated non-recanalisation after  
67 intravenous thrombolysis with the volume of clot, instead of its length [26]. They found that the average  
68 clot volume in patients with non-recanalisation was significantly larger than that in patients with  
69 successful recanalisation, and clot volume  $\geq 200 \text{ mm}^3$  was predictive of non-recanalisation.

70

71 Attempts were also made to associate the location of occlusion with recanalisation rates and clinical  
72 outcomes [21–23,27]. Saqqur et al. (2007) examined stroke patients with various cerebral occlusions,  
73 ranging from internal carotid to distal MCA occlusions [23]. Distal MCA occlusions were reported to  
74 achieve high recanalisation rates, whereas terminal ICA occlusions resulted in poor recanalisation and  
75 clinical outcome possibly due to larger thrombus burden and poor collaterals. Friedrich et al. (2015)  
76 analysed over 130 patients with acute MCA occlusions to identify the relation between the distance from  
77 the internal carotid bifurcation to the clot front and clinical outcome based on the degree of impairment

78 and neurological disability caused by stroke [22]. They found that patients with distal occlusions tend to  
79 have a more favourable clinical outcome than those with proximal occlusions, and that distal clots are  
80 usually shorter than proximal clots.

81

82 Due to the combined effects of the size and location of clot in the above mentioned clinical studies, it is  
83 not possible to explain the role of each individual factor when acting alone. To this end, we have  
84 performed computational simulations using a recently developed multi-level model for thrombolytic  
85 treatment in ischaemic stroke by varying the clot size and location, one parameter at a time, while keeping  
86 the dosage regimen and initial clot resistance constant. A three-dimensional (3D) patient-specific model is  
87 reconstructed from 3D rotational angiography images, which includes the internal carotid bifurcation into  
88 the A1 segment of anterior cerebral arteries (ACA) and the M1 segment of middle cerebral arteries (M1),  
89 as well as the M1 bifurcation into the M2 segments. Simulated scenarios are divided into two groups: M1  
90 occlusion and M2 occlusion. For each occlusion site, the volume of clot is varied. Lysis completion times  
91 for the simulated scenarios are compared, along with haemodynamics variables, the extent of lysis, clot  
92 resistance and tPA concentration inside the clot.

93

## 94 **2. Methods**

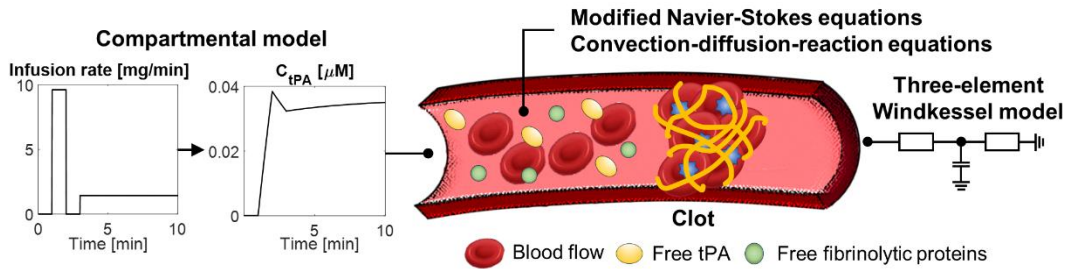
### 95 **2.1 Overview of the computational model**

96 Figure 1 presents an overview of our recently developed computational model [1], which incorporates  
97 multi-level physical and biochemical phenomena present in thrombolysis, from macroscopic blood flow  
98 and species transport to reactions of clot lysis within a clot, coupled with interactions between the  
99 macroscopic transport phenomena and the progression of clot dissolution. Blood flow and mass transport  
100 of free phase species are described by the modified Navier-Stokes equations and the convection-  
101 diffusion-reactions equations, respectively (Figure 1 (a)). Fibrinolytic reactions kinetics, illustrated in  
102 Figure 1 (b) and (c), are coupled with the macroscopic blood flow and species transport models to update  
103 the Darcian momentum and reactions source terms as clot lysis takes place. Full details of the

104 mathematical models of blood flow, species transport and fibrinolytic reaction kinetics can be found in  
 105 our previous work [19].

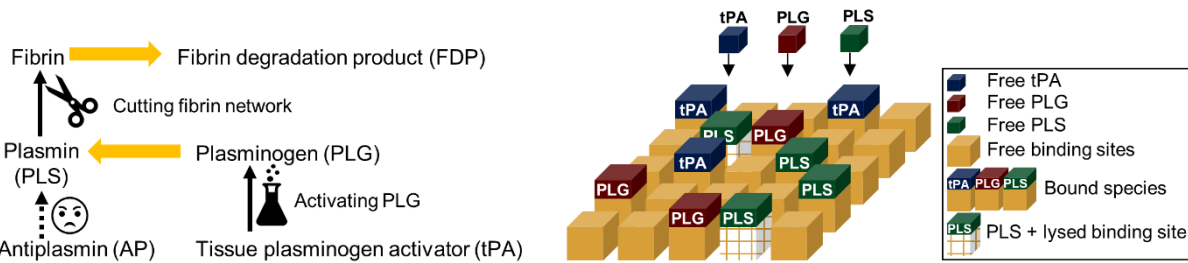
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(a)

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109

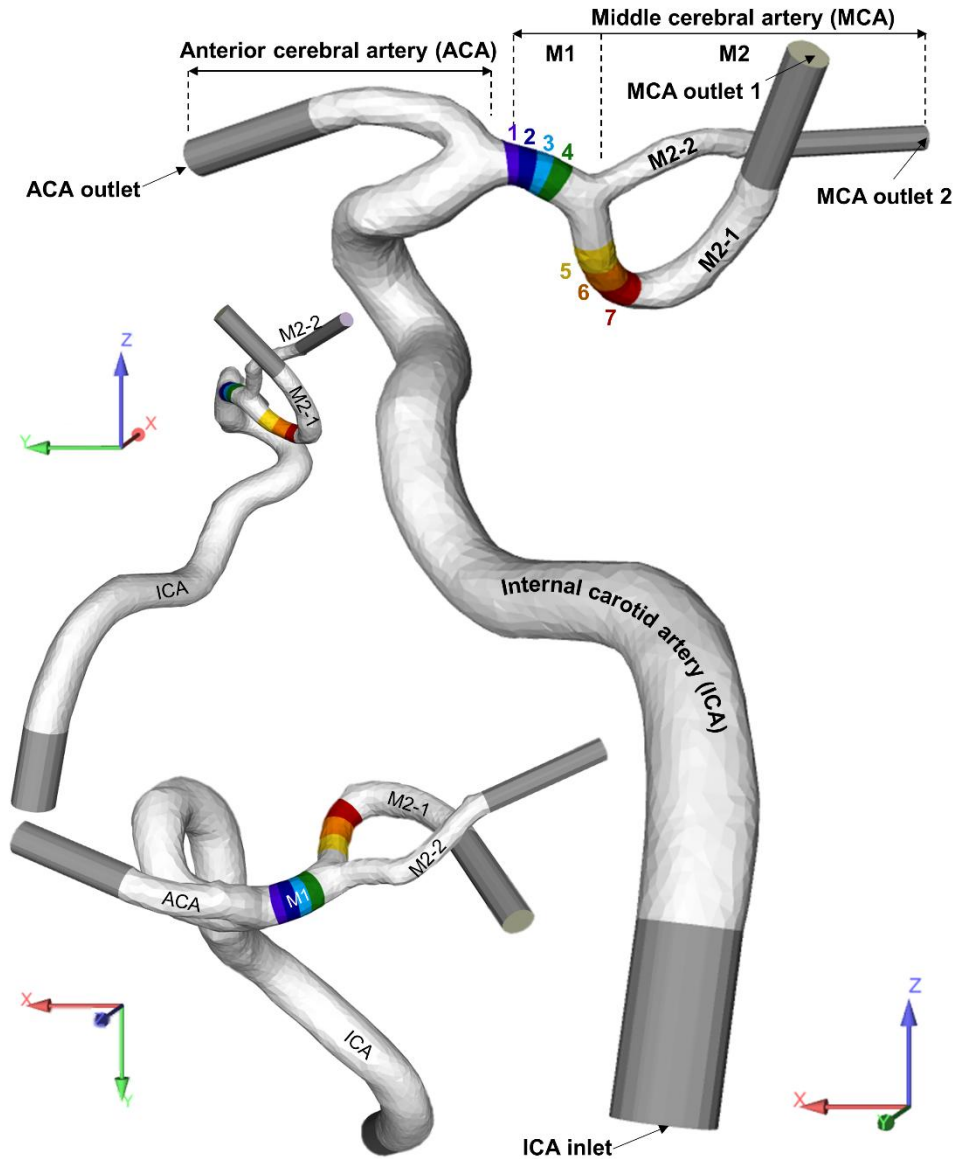
110 Figure 1. A schematic illustration of the overall computational model. (a) Models for blood flow and  
 111 species transport coupled with the compartmental model and three-element Windkessel model at the inlet  
 112 and outlet boundaries, respectively. (b) Fibrinolytic reactions involving tPA, plasminogen (PLG), plasmin  
 113 (PLS) and anti-plasmin (AP). (c) Adsorption and desorption of tPA, PLG and PLS onto and from the  
 114 binding sites in the fibrin fibre network in a clot.

115

## 116 2.2 Simulation scenarios

### 117 2.2.1 3D patient-specific arterial geometry

118 A 3D patient-specific geometry is reconstructed from 3D rotational angiography images using Mimics  
 119 19.0 (Materialise, Leuven). Formal ethics approval is not required for the use of these images which were  
 120 anonymised prior to analysis. Figure 2 displays the front, side and top views (on the right, top left and  
 121 bottom left, respectively) of the reconstructed geometry.



122

123 Figure 2. The patient-specific model used in this study. The internal carotid artery (ICA) bifurcates into  
 124 ACA and MCA (M1), with the M1 segment of MCA bifurcating further into the inferior (M2-1) and  
 125 superior (M2-2) branches. The coloured areas in the MCA represent the locations of clots. The grey parts  
 126 are artificial extensions to the inlet and outlets.

127

128 As shown in Figure 2, clot regions are artificially assigned in the M1 segment and the M2 inferior branch  
 129 (M2-1), respectively, based on clinical observations [23]. The volume of clot is varied from 4.6 to 24  
 130  $\text{mm}^3$  for M1 occlusion and from  $9.6 \text{ mm}^3$  to  $27 \text{ mm}^3$  for M2 occlusion in order to confine the obstructive

131 clot to the affected segment only. The clot volumes in our simulations are at the lower end of the range  
132 reported in a clinical study (mean volume of  $129\pm 120$  mm<sup>3</sup> for ICA, M1 and M2 occlusions) [26],  
133 because the M1 segment of our patient-specific geometry is relatively short. The coloured areas numbered  
134 from 1 to 7 in Figure 2 represent different clot sizes, with the front and rear faces of each clot being  
135 perpendicular to the local centreline. Starting with the smallest clot, corresponding to region 1 and 5 for  
136 M1 and M2 occlusions respectively, different clot sizes are simulated by adding the subsequent clot  
137 regions one by one. Therefore a total of 7 scenarios are created, with clot volume varying from 1 to (1-4)  
138 for M1 occlusions and from 5 to (5-7) for M2 occlusions. Further geometric details of the model can be  
139 found in Supporting Information A.

140

#### 141 *2.2.2 Simulation and computational details*

142 Blood flow is assumed to be Newtonian and laminar. Kinetics parameters for the fibrinolytic reactions  
143 and transport parameters are taken from our previous study, while the radius of fibrin fibre is chosen to be  
144 65 nm [19]. The standard dosing protocol for the treatment of acute ischaemic stroke is used with a high  
145 dose 1.2 mg/kg in order to accelerate clot lysis for fast computation. The model equations are  
146 implemented in open source computational fluid dynamics (CFD) code, OpenFOAM 4.0, which utilises a  
147 finite volume spatial discretisation. The compartmental model is solved in MATLAB R2017a and the  
148 results are imported in the CFD code to serve as inlet conditions for the species transport model. Further  
149 computational details and simulation conditions are included in Supporting Information (Section B).

150

### 151 **3. Simulation results**

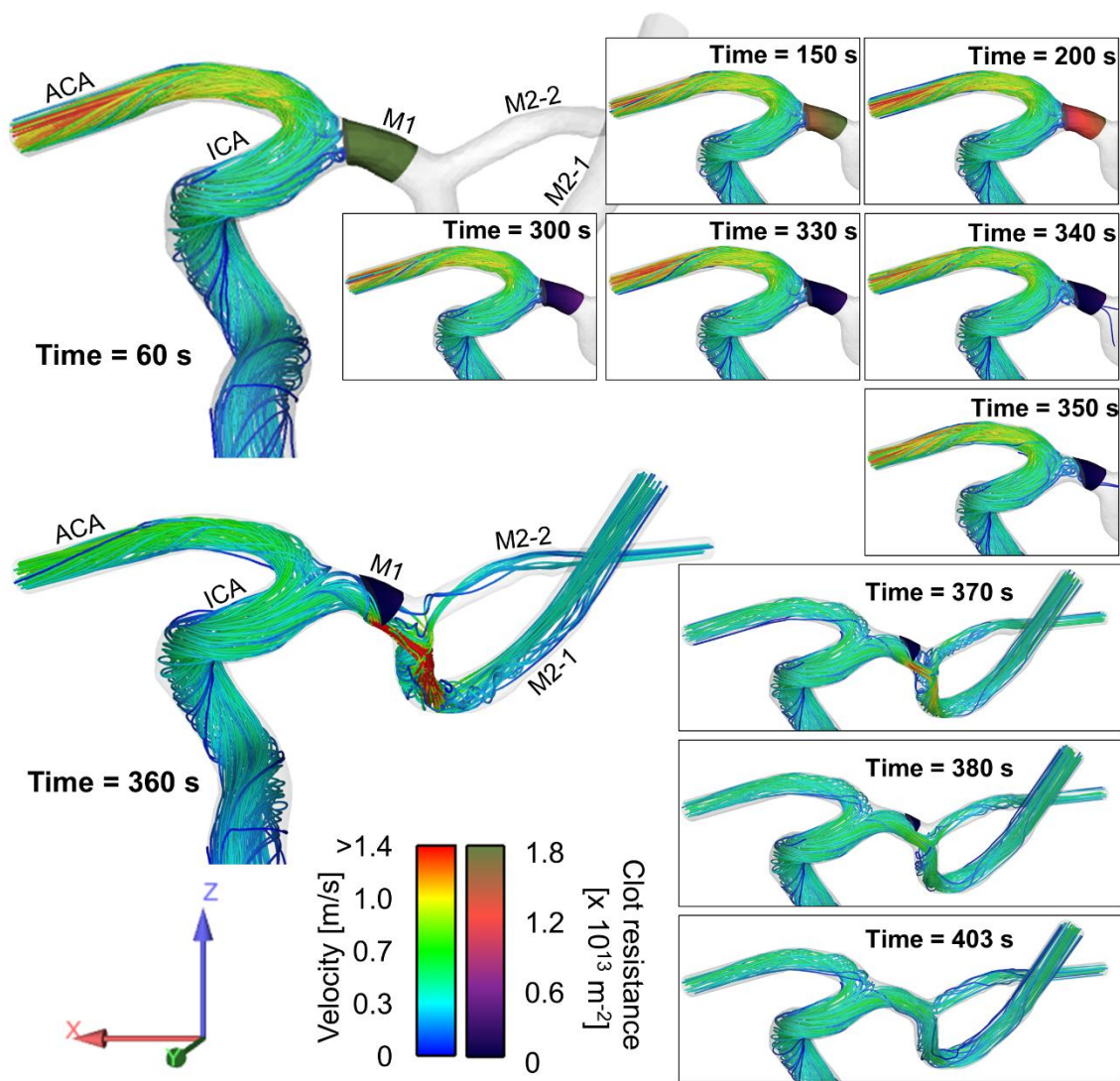
152 Here we present results for the 7 simulated scenarios with different occlusion sites and clot sizes. Each  
153 case is named based on the number of clots included in the simulation, as displayed in Figure 2. For  
154 example, the smallest and largest clots in the simulated M1 occlusions are referred to as C1 and C1-4,  
155 respectively; whereas those for M2 occlusions are C5 and C5-7, respectively.

156

157 **3.1 Flow and clot lysis patterns for the largest clots at each occlusion site**

158 First of all, flow patterns obtained from the simulations are analysed along with clot lysis patterns. Two  
 159 scenarios with the largest clot at each occlusion site are selected for visualisation of flow and lysis  
 160 patterns at representative time points.

161



162  
 163 Figure 3. Flow and clot lysis patterns for C1-4 at different time points, from 60 (when the bolus infusion  
 164 starts) to 403 seconds (when the clot completely disappears). Flow velocity and clot resistance (the  
 165 inverse of clot permeability) are also colour coded.

166



167 Figure 3 shows changes in flow velocity and clot resistance for C1-4 from the start of bolus infusion  
168 (Time = 60 s) to complete lysis (Time = 403 s). Since the occluding clot, approximately 24 mm<sup>3</sup> in  
169 volume, is located in the M1 segment of MCA and very close to the ICA bifurcation, there is initially no  
170 visible flow in the M1 and M2 segments, with high clot resistance of  $1.8 \times 10^{13} \text{ m}^{-2}$  (equivalent to  
171 permeability of  $5.6 \times 10^{-14} \text{ m}^2$ ), as can be seen at Time = 60 s in Figure 3. Relatively high flow velocities of  
172 up to 1.4 m/s can be seen at the ACA outlet as all the flow is directed to the ACA from the ICA. As a  
173 sufficient amount of tPA reaches the clot front, the clot starts to degrade from its front, leading to reduced  
174 clot resistance and increased permeability. The clot resistance gradually decreases from the time point of  
175 150 to 300 s, with the clot volume starting to shrink at Time = 330 s. Due to the wide branching angle of  
176 the MCA, a recirculation zone is formed near the lower part of the M1 arterial wall, as can be seen at  
177 Time = 330, 340 and 350 s. This leads to faster clot dissolution around these areas due to the higher tPA  
178 concentration there and its faster penetration into the clot with reduced resistance, as evidenced by the  
179 spatial distribution of tPA within a clot in our previous work [19].

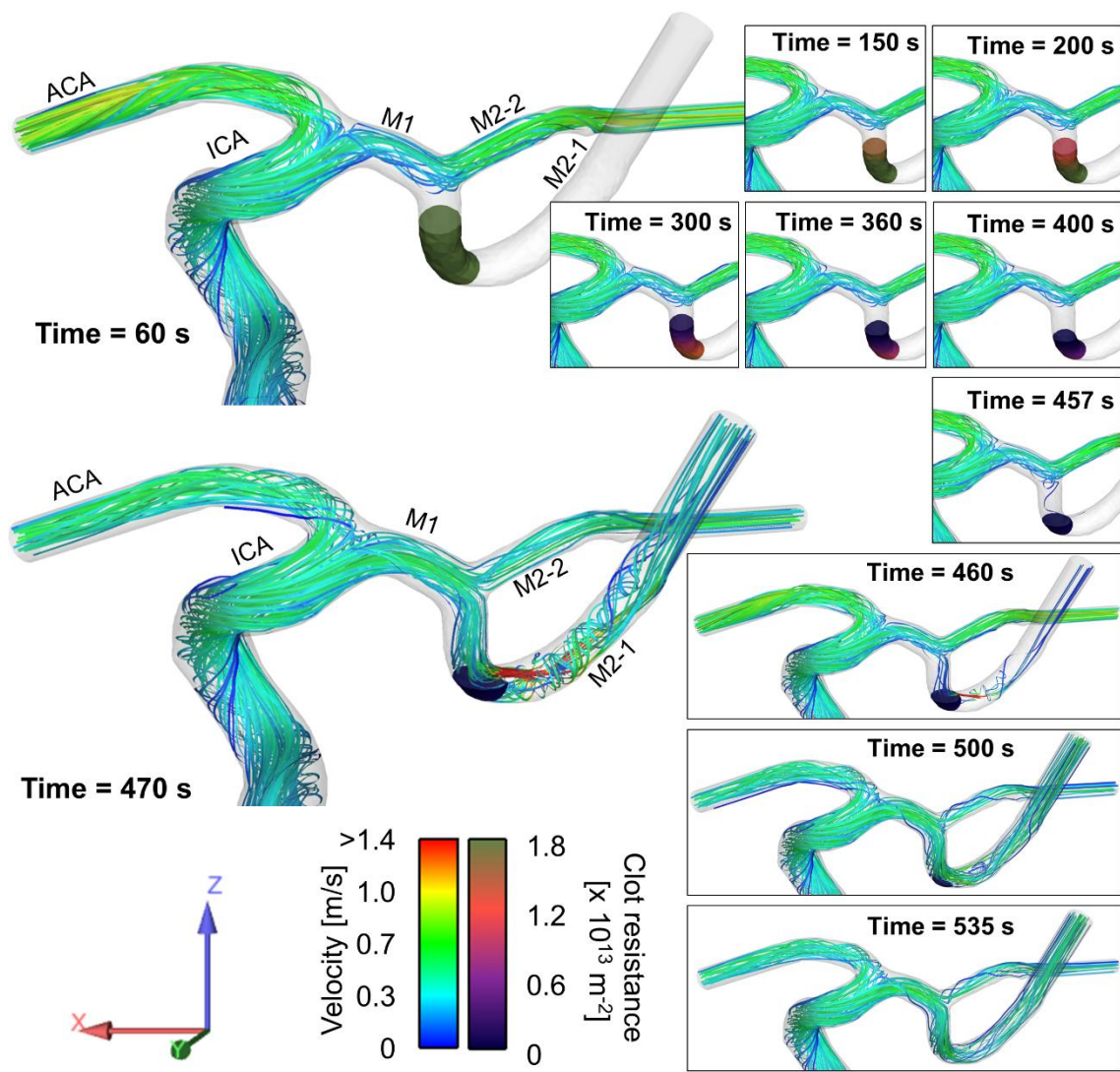
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181 When the clot is sufficiently degraded with a substantial increase in its permeability, a little amount of  
182 flow starts to seep through, with a flow rate of 0.067 mL/s at Time = 350 s in the MCA. At around 360  
183 seconds, a breakthrough path is established in the lower part of the clot, resulting in a high-velocity jet  
184 with a velocity magnitude of  $> 4 \text{ m/s}$ . After the breakthrough, convective transport of tPA becomes  
185 dominant, transiently accelerating clot lysis. A small portion of clot remains attached to the upper wall of  
186 MCA until it is completely dissolved at 403 seconds.

187

188 For the M2 occlusion scenario of C5-7 shown in Figure 4, the inlet flow splits into two streams in the  
189 ACA and M2-2 owing to the blockage in the M2-1 at Time = 60 s. It is noticed that flow velocity in the  
190 ACA is lower in this scenario than that in Figure 3. Since the clot is located slightly distal to the M1  
191 bifurcation, there is a large stagnation zone between the M1 bifurcation and the clot front in the M2-1.  
192 This results in a slower degradation of C5-7 than C1-4. The clot becomes smaller by gradual dissolution

193 from its front after Time = 300 seconds. When sufficient tPA permeates through the clot, more flow is  
 194 seen to pass through, i.e., M2-1 flow rate of 0.0025 and 0.068 mL/s at Time = 450 s and 457 s,  
 195 respectively.  
 196



197  
 198 Figure 4. Flow and clot lysis patterns for C5-7 at different time points, from 60 (when the bolus infusion  
 199 starts) to 535 seconds (when clot completely disappears). Flow velocity and clot resistance (the inverse of  
 200 clot permeability) are also colour coded.  
 201

202 Lysis patterns are rather flat before Time = 400 s due to the M2-1 segment originating almost vertically  
203 from the M1 bifurcation. Afterwards, however, the clot front becomes highly skewed with the part near  
204 the inner curvature dissolving much faster than that near the outer curvature, resulting clot breakthrough  
205 at the inner curvature, shown at Time = 460 s. The high-velocity jet is also observed in the breakthrough  
206 pathway, with a maximum velocity of 4.2 m/s. This enables faster transport of tPA to the M2-1 and  
207 consequently increases the rate of clot lysis. Due to the high flow velocity in the presence of partially  
208 dissolving clot, the flow is highly disturbed and helical, as can be seen at Time = 470 s. The clot volume  
209 rapidly decreases after the breakthrough, although the reduction in clot volume slows down slightly, as  
210 noticed at Time = 470 to 535 s. This is attributed to the high degree of curvature where the remaining clot  
211 is located.

212

### 213 **3.2 Flow rate and pressure variations over time**

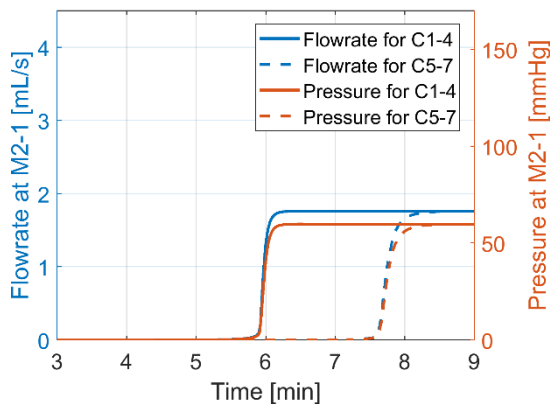
214 Figure 5 displays flow rates and pressures over time at the ICA, ACA, M2-1 and M2-2 for C1-4 and C5-7.  
215 For C1-4, flow rates at both M2 branches, M2-1 and M2-2, are initially zero and then restore to 1.76 mL/s  
216 and 0.79 mL/s, respectively, at 6.4 minutes (i.e., 5.4 minutes after the start of tPA injection at 1 min), as  
217 can be seen in Figures 5 (a) and (b). To avoid confusion, times that are referred to in this section and  
218 hereafter represent the simulation time inclusive of an initial 1 minute of flow stabilisation without tPA  
219 injection, unless otherwise stated. Pressures in the M2-1 and M2-2 follow a similar pattern, which are  
220 initially zero when there is no flow and rise to 60 mmHg after recanalization.

221

222 For C5-7 where only M2-1 is blocked, the ICA flow is initially divided into the M2-2 and ACA branches  
223 at 1.35 and 2.96 mL/s, respectively. Once the breakthrough path is made at 8.7 minutes, the flow in the  
224 M2-1 is fully restored to 1.76 mL/s whereas M2-2 and ACA flow rates drop to 0.80 and 1.75 mL/s,  
225 respectively. As shown in Figures 5 (b) and (c), pressures at the M2-2 and ACA outlet before the  
226 breakthrough are 100.3 and 102.2 mmHg, respectively, which fall back to 60 mmHg after breakthrough.  
227 Interestingly, initial pressures at the ICA inlet are calculated to be 160 and 110 mmHg for C1-4 and C5-7,

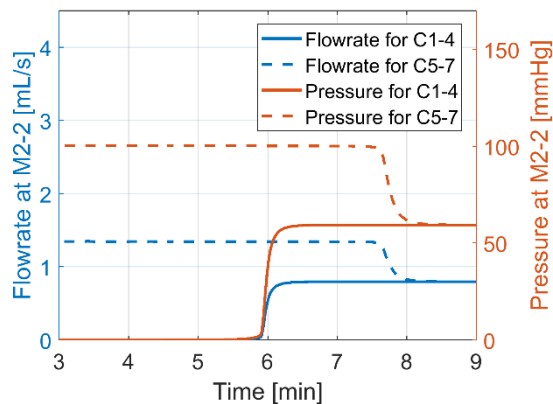
228 respectively, as depicted in Figure 5 (d), possibly due to the assumption of same inflow for the two types  
229 of occlusion.

230



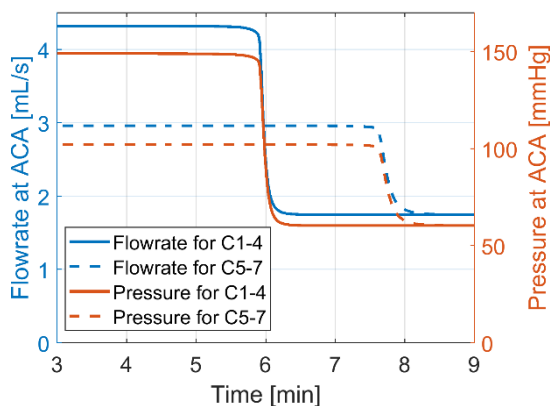
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(a)



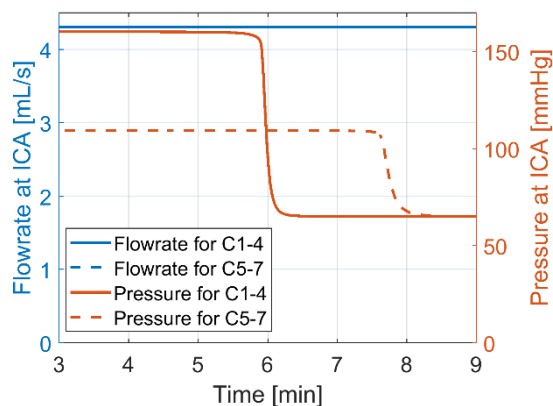
232

(b)



233

(c)



234

(d)

235 Figure 5. Flow rate and pressure variations over time for the largest clots of each occlusion. Flow rate and  
236 pressure at (a) M2-1 outlet (occluding branch for C5-7), (b) M2-2 outlet, (c) ACA outlet and (d) ICA inlet.

237 The solid and dashed lines are results of C1-4 (M1 occlusion) and C5-7 (M2 occlusion), respectively.

238 Blue coloured lines are for flow rate and orange coloured lines for pressure. The  $x$ -axis denotes the

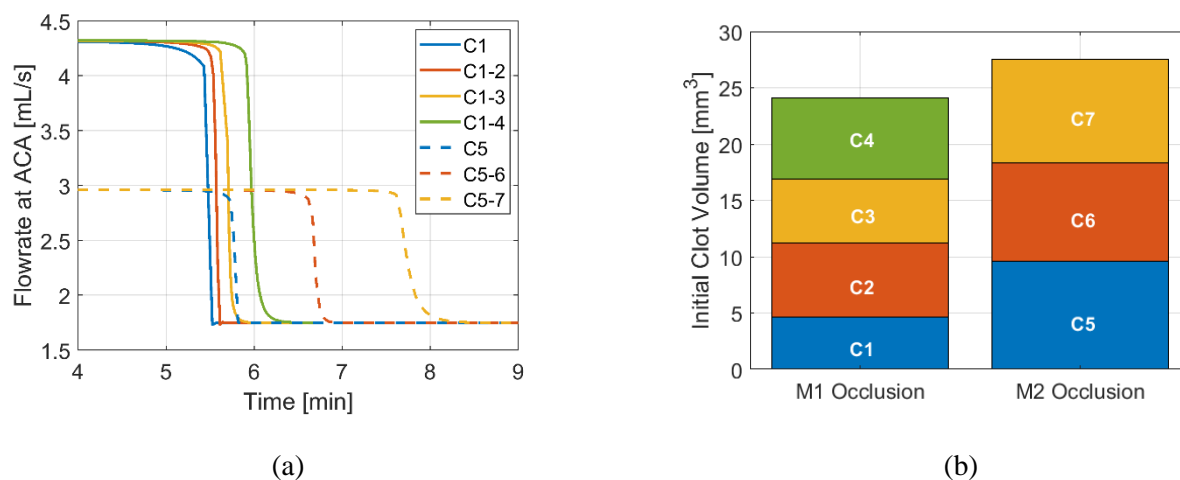
239 simulation time, inclusive of an initial 1 minute of flow stabilisation without tPA injection. This applies to

240 all subsequent figures unless otherwise stated.

241

242 In order to compare the breakthrough times of all scenarios studied here, ACA flow rates over time are  
 243 displayed in Figure 6 along with the initial clot volumes. The M1 occlusions achieve the breakthrough of  
 244 clots at around 5.6 to 6.5 min, while the M2 occlusions take between 6 to 8.7 min, as shown in Figure 6  
 245 (a). It can also be observed that the ACA flow rates slowly decrease before breakthrough due to an  
 246 increasing degree of clot degradation and clot permeability, which allows some flow to pass through the  
 247 clot, as observed in Figures 3 and 4.

248



249  
 250 (a) (b)  
 251 Figure 6. Flow rate variations in ACA outlet over time for all cases. (a) ACA flow rates and (b) initial clot  
 252 volumes.

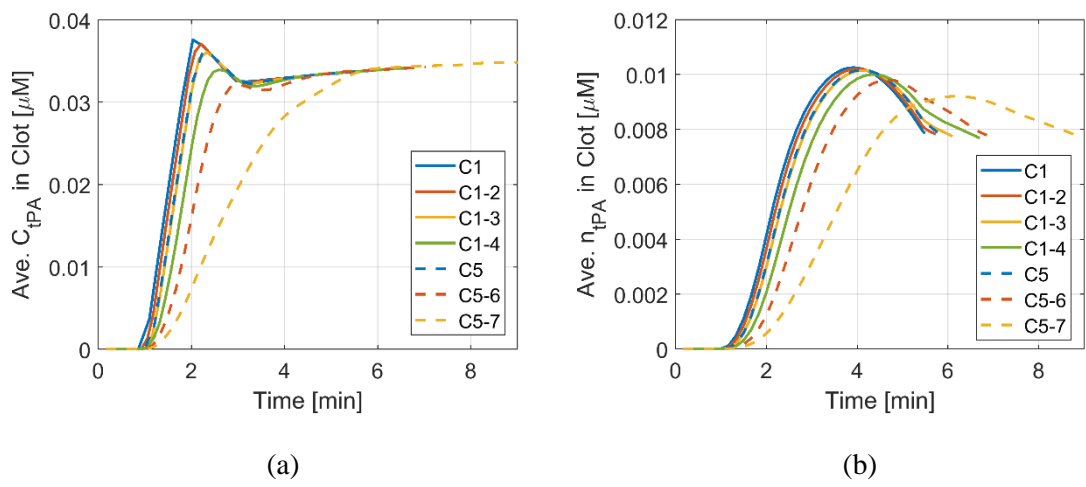
253  
 254 For clots of a similar size but at different locations, clots in M2 occlusions tend to dissolve slowly than  
 255 those in M1 occlusions. For example, C1-2 dissolves faster than C5 although the volume of C1-2 (11.3  
 256 mm<sup>3</sup>) is about 1.1 times larger than that of C5 (9.58 mm<sup>3</sup>). The discrepancy between two occlusion sites  
 257 becomes more prominent as the clot size is increased, e.g., breakthrough times of C1-4 and C5-7 differ by  
 258 2.3 min. This could be attributed to differences in the geometric features of patient-specific vasculature  
 259 and the position of clot front from each bifurcation.

260

261 **3.3 Concentrations of free and bound tPA within the clot**

262 Figure 7 shows free and bound tPA concentrations within the remaining clot. The free tPA concentration  
 263 increases rapidly after the bolus injection at 1 min, as seen in Figure 7 (a). For all the scenarios except for  
 264 C5-7, free tPA concentration peaks at between 2 and 3 minutes. This is due to the rapid increase in the  
 265 level of tPA in the plasma after the initial bolus injection, as can be seen in Figure 1 (a) and in our  
 266 previous work [19]. It is also noticed that the concentration peaks for C1-3 and C5 almost overlap even  
 267 though C1-3 is about 1.8 times larger than C5. This is because C5 is located more distally, meaning that  
 268 tPA transport in the M2 occlusion is initially driven by diffusion. Once the bolus injection is completed at  
 269 2 min, free tPA concentration within the clot falls slightly due to a delayed start of continuous infusion.  
 270 Thereafter, the continuous infusion keeps the level of tPA high in the clot (above  $0.03 \mu\text{M}$ ) as well as in  
 271 the plasma. In addition, it can be observed that the concentration peak at the end of bolus injection  
 272 becomes less distinct and eventually disappears as the clot becomes larger, as in C5-7.

273



274  
275

276 Figure 7. Volume-averaged concentrations of (a) free tPA and (b) bound tPA within each clot.

277

278 The concentration of bound tPA in the clot, on the other hand, seems to be less affected by the bolus  
 279 injection of tPA and time delay between two infusion modes, as displayed in Figure 7 (b). The bound tPA  
 280 smoothly increases from 1 min and continues to rise even during the delay interval, and then eventually  
 281 falls off. Peaks of bound tPA concentration lag slightly behind those of free tPA. Moreover, the

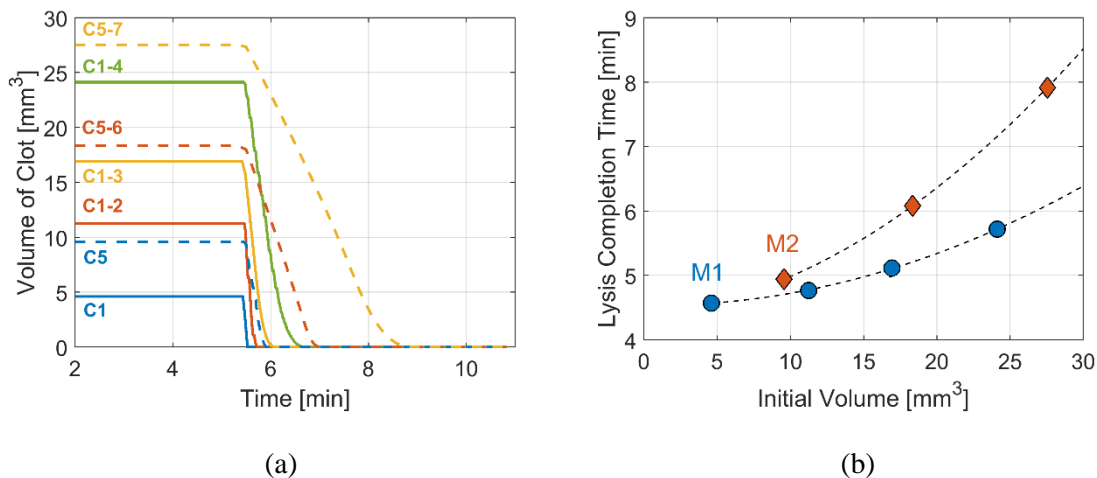
282 maximum concentration of bound tPA in each clot is much lower than that of free tPA, at a maximum of  
283 between 0.009 and 0.01  $\mu\text{M}$ . In all scenarios, the bound tPA concentration falls to around 0.008  $\mu\text{M}$   
284 before complete lysis is achieved.

285

### 286 3.4 Clot volume and lysis completion time

287 Finally, the progression of clot lysis is examined by monitoring changes in clot volume over time, as  
288 shown in Figure 8 (a). Despite the different locations of the clots between the M1 and M2 occlusions,  
289 they all start to decrease in size at around 5.4 minutes. The trend of reduction in clot volume is almost  
290 linear, while the rate of reduction slows down as approaching the completion of lysis.

291



292

293

294 Figure 8. Clot volume and lysis completion time. (a) Change in the volume of clot over time and (b) the  
295 lysis completion times from the start of bolus injection as a function of initial clot volume for each  
296 occlusion site. The black dashed lines are obtained by quadratic interpolation of simulation results for  
297 each occlusion.

298

299 For each occlusion site, complete lysis is achieved earlier for smaller initial clot volumes, as expected, at  
300 5.6 to 6.1 mins for C1 to C1-4 and 5.9 to 8.9 min for C5 to C5-7. However, when comparing different  
301 locations for similarly sized clots, M2 occlusions take longer for complete lysis than M1 occlusions, e.g.,

302 C1-2 vs C5 and C1-3 vs C5-6. This is more evident when examining the lysis completion time (i.e., the  
303 time when clot volume becomes zero–1 min, as the bolus is injected at 1 min) as a function of initial clot  
304 volume for each occlusion site, displayed in Figure 8 (b) where the simulation results (symbols) and fitted  
305 curves (black dashed lines) are shown. Lysis completion times for both occlusions exhibit approximately  
306 a quadratic increase with respect to the initial volume of clots, although the M1 occlusions are less  
307 sensitive to the size of clot than the M2 occlusions. Based on the simulation results, it can be said that M2  
308 clots take a longer time to completely dissolve than M1 clots for the same size. It is also expected that  
309 differences in lysis completion time between the two occlusions would increase as the clot becomes larger.  
310

#### 311 **4. Discussions and conclusions**

312 First of all, flow and lysis patterns in scenarios with the largest clot in the M1 and M2 segments are  
313 visualised at several time points and further analysed with respect to flow velocity and clot resistance. In  
314 both clots, an asymmetric lysis front is formed; faster lysis takes place in the inner curvature of the  
315 arterial walls than in the outer curvature. As a result, a breakthrough pathway is always established from  
316 the clot region adjacent to the inner curvature, as seen in Figures 3 and 4. Since the clot fronts are  
317 perpendicular to their local centreline, initial volume reduction is also observed at the inner curvature due  
318 to the presence of recirculation and consequently prolonged residence time of tPA in that region. This can  
319 be corroborated by the spatial distributions of fibrinolytic proteins and the extent of lysis within the clot,  
320 presented in our previous study [19]. Even when the clot front is not normal to the centreline, the trend of  
321 the breakthrough path being developed near the inner curvature is expected to be preserved with a slight  
322 variation in the initial lysis pattern.

323  
324 It is also worth pointing out that clot lysis slows down as the clot front becomes aligned almost parallel to  
325 the flow direction. This indicates that intravenous infusion of tPA may be ineffective at this stage, which  
326 can also occur in scenarios where non-occlusive clots are present, which partially block the arteries and  
327 allow blood flow to pass through at higher velocities. Furthermore, there is a high chance of clot



328 deformation and even embolisation due to high shear rates in the partially blocked vessels, which may  
329 lead to secondary blockages in small blood vessels [28–30]. Therefore, alternative technologies might be  
330 needed in order to improve the effectiveness of thrombolytic therapy.

331

332 In addition, flow rate and pressure in each arterial branch are obtained from the simulations and compared  
333 between the largest clots in the M1 and M2 occlusions. After flow is restored in an occluded branch, both  
334 cases achieve the same flow split: 1.75 and 2.56 mL/s for ACA and MCA, respectively. These values are  
335 slightly larger than those reported in the literature [31,32] but thought to be reasonable, given that there  
336 are large individual variations of average ICA flow rate, from 3.4 mL/s to 5.4 mL/s [33]. Pressure  
337 differences between the ICA and M2-1 are calculated to be approximately 160 and 100 mmHg for M1  
338 and M2 occlusions, respectively. These seem to be within the range expected for occlusive clots, based on  
339 results of the existing computational study where the circle of Willis and its variations were simulated in  
340 the presence of up to 96% carotid stenosis [34]; approximately 100 mmHg could be expected for 100%  
341 stenosis by extrapolating their data. It is also worth mentioning that calculated ICA pressures for M1 and  
342 M2 occlusions before recanalisation differ by 60 mmHg, as shown in Figure 5 (d). This is due to the  
343 assumption of same ICA flow rate in both scenarios, which might not be realistic. It has been shown that  
344 flow distribution could be altered if there are anatomical variations or vessel occlusions in the circle of  
345 Willis when the same amount of blood flow is pumped from the heart [35]. It would therefore be  
346 necessary to apply patient-specific flow data at the inlet of ICA in order to gain more realistic pressure  
347 and flow rate at each outlet, which was not possible in this work due to the lack of patient data.

348

349 Breakthrough times are also identified for all scenarios based on temporal changes in ACA flow rate.  
350 Simulation results show that M2 occlusions tend to dissolve more slowly than M1 occlusions for the same  
351 clot size. This is mainly due to two reasons; first, the clots in the M2 segment are located more distally  
352 from the M1 bifurcation, so that majority of the tPA passing through the M1 segment is diverted to the  
353 patent M2-2 branch. As a result, it takes more time for a sufficient amount of tPA to reach the clot front

354 during the initial stage of the treatment. Second, the higher degree of arterial curvature in the M2 branch  
355 than in the M1 makes the clot lysis front parallel to the flow direction in the later stage of clot lysis,  
356 leading to rapid loss of tPA to the downstream circulation, as discussed above.

357

358 Concentrations of free and bound tPA in a clot, on the other hand, are more related to the tPA dosage  
359 regimen and resulting level of tPA in the plasma. As discussed in the previous study [19], free tPA level  
360 in the plasma rapidly increases by the initial bolus injection and then plummet due to the time delay  
361 before the continuous infusion. This dynamic change of the plasma tPA is partly mirrored in the  
362 concentration of free phase tPA delivered to the clot, while the largest clot in the M2 does not show any  
363 sign of influence by the initially elevated tPA concentration in the plasma. This suggests that occlusions  
364 with a long clot might not benefit from the bolus injection that aims to rapidly raise the tPA concentration,  
365 as concluded for fine clots in the previous study [19]. In addition, the concentration peaks of free tPA in  
366 the M2 appears slightly later than in the M1 when the clot sizes are similar, due to the distal location of  
367 the M2 clots. This implies that the distance between the bifurcation and clot front is an important factor in  
368 determining the initial transport rate of tPA to the clot.

369

370 It can also be observed that the concentration of bound tPA is approximately 3.5 times lower than that of  
371 free tPA. This could be for two reasons: competition among the fibrinolytic proteins for binding with the  
372 fibrin fibre and limited adsorption rate of tPA itself. Our computer model might therefore be  
373 advantageous in testing different tPA drugs with higher fibrin specificity or new nanomedicines that  
374 better target the clot in order to investigate their potential as an alternative method.

375

376 Finally, simulation results are analysed in terms of changes in clot volume over time and lysis completion  
377 times against the initial volume of clots in each location. All clots achieve recanalisation within 8 minutes  
378 from the start of the treatment. As addressed in the previous study, our model describes the clot as a fibrin  
379 fibre network of higher permeability than a real clot with cellular components lodged within the fibre

380 network. Moreover, a higher tPA dose, 1.2 mg/kg, is used in our simulations compared to tPA doses used  
381 in clinical studies (0.9 mg/kg or 0.6 mg/kg) [36–38]. These assumptions lead to accelerated tPA transport  
382 through the clot, hence faster recanalisation than clinical observations; mean recanalisation durations of  
383  $23\pm 16$  min [38] and  $47\pm 32$  min [37] in two separate studies of tPA-treated stroke patients where  
384 recanalisation was monitored via transcranial Doppler (TCD). Also, Christou et al. [36] correlated  
385 recanalisation timings measured through TCD with clinical outcomes in stroke patients, and they found  
386 that 50% of all studied patients achieved complete or partial recanalisation within 31-60 min after tPA  
387 bolus and 25% of them within 0-30 min. Additionally, the clot sizes adopted in our simulations are  
388 relatively small. Riedel et al. reported that clot lengths exceeding 8 mm are likely to fail in recanalisation  
389 for acute MCA stroke [25], while Yoo et al. estimated a cut-off value for non-recanalisation to be 200  
390  $\text{mm}^3$  based on a study of 214 patients with acute ischaemic stroke [26]. The largest clot in our simulation  
391 is approximately 5.7 mm in length and  $27 \text{ mm}^3$  in volume, much smaller than the reported threshold  
392 values. Furthermore, it is worth noting that there appears to be a contradiction between our simulation  
393 results and clinical observations: our model predicts that M2 occlusions need a longer time to achieve  
394 recanalisation than M1 occlusions, whereas clinical studies reported that patients with distal occlusion  
395 were more likely to have successful recanalisation and a good outcome than those with proximal  
396 occlusion [22,23,27]. However, an important difference is that in clinical studies distal clots are usually  
397 smaller than proximal clots [21,22], whereas the same clot size is assumed in our simulations when  
398 comparing M1 and M2 occlusions.

399

400 In conclusion, our simulation results for various clot sizes at two locations support clinical observations  
401 that clot size has a strong influence on recanalisation success and lysis time. Our results further reveal that:  
402 (i) arterial curvature is an important factor in determining lysis and breakthrough patterns, (ii) clot  
403 location affects the rate of tPA accumulation at the clot front and the initial lysis rate, and (iii) arterial  
404 curvature also influences the late-stage lysis rate, especially after breakthrough. This study demonstrates  
405 that our simulation platform for thrombolysis in ischaemic stroke can offer an in-depth understanding of

406 drug transport and clot lysis under various clinical scenarios where numerous parameters are involved,  
407 such as the clot location and size studied here as well as clot permeability and drug dose as addressed in  
408 our previous study. Furthermore, the model can potentially be used to help with benefit/risk calculations  
409 based on clot size and location obtained from patient scans. This would help determine which patient is  
410 more likely to achieve successful recanalisation with intravenous thrombolysis within a limited time  
411 window. In the future, we hope to further improve the model by incorporating the presence of cellular  
412 components in the clot, and to extend the model to simulate new tPA delivery systems for targeted  
413 thrombolytic therapy. The model can be further improved by applying more realistic haemodynamic  
414 conditions, e.g. physiological pulsatile flow at the inlet instead of a steady flow rate in order to capture  
415 detailed lysis patterns influenced by flow pulsatility and mixing effects near the lysis front. In addition,  
416 the potential effect of turbulence on drug transport and lysis rate is worth investigating, as the high-  
417 velocity jet observed during the clot breakthrough could induce transition to turbulence which may affect  
418 local flow and lysis patterns.

419

420

#### 421 **Conflicts of interest**

422 None.

423

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432

433 **Ethical approval**

434 Not required.

435

436 **Data statement**

437 Data are available from the corresponding author on request.

438

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554 Supporting Information

555

## 556 **Computational Simulations of Thrombolysis in Acute Stroke: Effect of Clot** 557 **Size and Location on Recanalisation**

558

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573

### 574 **A. Further geometric details**

575 It consists of an ICA that bifurcates into the A1 segment of ACA and the M1 segment of MCA that  
576 further bifurcates into the superior and inferior branches, namely M2-2 and M2-1, respectively. Suitable  
577 extensions are added to the inlet of ICA and exits of the three cerebral branches, coloured in grey, to  
578 allow for flow development and ensure numerical stability. The selection of clot size is limited by the  
579 dimensions of the patient-specific arterial geometry used in this study; the M1 segment is relatively short  
580 at 7.24 mm compared to a reported average length of 9.4 mm with a range of 4.3 to 19.5 mm [1], and the  
581 maximum size of M2 clot is adjusted to be comparable to that of the M1 clot. Geometric details are listed  
582 in Table A.1 where the length of each branch is measured along the vessel centreline.

583

584

585

586

587 Table A.1. Geometrical parameters

Description	Value [mm or mm <sup>3</sup> ]
Diameter of ICA inlet	5.59
Diameter of ACA outlet	2.52
Diameter of M2-1 outlet	2.55
Diameter of M2-2 outlet	1.73
Mean diameter of clots in M1	3.07
Mean diameter of clots in M2-1	2.48
Length of ICA	79.2
Length of ICA extension	10.0
Length of ACA	12.1
Length of ACA extension	10.0
Length of M1	7.24
Length of M2-1	22.2
Length of M2-1 extension	9.55
Length of M2-2	16.4
Length of M2-2 extension	9.78
Volume of Clot 1	4.61
Volume of Clot 1-2	11.3
Volume of Clot 1-3	16.9
Volume of Clot 1-4	24.1
Volume of Clot 5	9.58
Volume of Clot 5-6	18.4
Volume of Clot 5-7	27.5

588

589 **B. Computational Details**590 **B.1 Model parameters and simulation conditions**

591 Blood flow is assumed to be Newtonian and laminar. Kinetics parameters for the fibrinolytic reactions  
592 and transport parameters are taken from our previous study, while the radius of fibrin fibre is chosen to be  
593 65 nm [2]. A steady flow rate of 4.31 mL/s is imposed at the ICA inlet, which is obtained by averaging  
594 the pulsatile flow rate over a cycle found in the literature [3]. No-slip conditions and rigid wall are  
595 specified at all parts of arterial walls. The three-element Windkessel model is adopted as the outflow  
596 boundary condition at all outlets, with its parameters being calculated based on flow distributions  
597 proportional to the cross-sectional areas of each outlet [4] and an outlet pressure of 60 mmHg [5,6], in the

598 absence of patient-specific flow and pressure measurements. The derived parameter values are listed in  
 599 Table B.1. For the species transport equations, time-varying concentrations of tPA, PLG, PLS and AP  
 600 calculated from the compartmental model are provided to the 3D model to serve as its inlet boundary  
 601 condition. The recommended dosage regimen for the treatment of acute ischaemic stroke is intravenous  
 602 (IV) administration of 0.9 mg of tPA/kg of patient weight with 10% of the total dose administered as an  
 603 initial bolus over 1 minute and the remaining 90% infused over an hour [7]. It was found in our previous  
 604 study that higher tPA doses would accelerate clot lysis without affecting lysis patterns [2]. Since  
 605 simulations to capture the progression of clot lysis until complete dissolution are computationally  
 606 intensive, a high dose 1.2 mg/kg with a patient weight of 80 kg is chosen for simulations in this study. It  
 607 is also assumed that there is a short delay of 1 minute between the bolus and continuous infusion. The  
 608 concentration of tPA obtained from the compartmental model for the first 10 minutes is included in  
 609 Figure 1, along with the infusion rate. Temporal concentrations of other proteins can be found in the  
 610 previous work [2].

611

612 Table B.1 Three-element Windkessel model parameters

Outlet	Description	Symbol	Value	Unit
ACA	Total resistance	$R_{T,ACA}$	$4.61 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Proximal resistance	$R_{p,ACA}$	$2.17 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Distal resistance	$R_{d,ACA}$	$2.44 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Capacitance	$C_{ACA}$	$3.88 \times 10^{-10}$	$\text{m}^3 / \text{Pa}$
MCA 1	Total resistance	$R_{T,MCA-1}$	$4.53 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Proximal resistance	$R_{p,ACA}$	$2.13 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Distal resistance	$R_{d,ACA}$	$2.40 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Capacitance	$C_{MCA-1}$	$3.95 \times 10^{-10}$	$\text{m}^3 / \text{Pa}$
MCA 2	Total resistance	$R_{T,MCA-2}$	$9.87 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Proximal resistance	$R_{p,ACA}$	$5.17 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Distal resistance	$R_{d,ACA}$	$4.70 \times 10^9$	$\text{Pa} \cdot \text{s} / \text{m}^3$
	Capacitance	$C_{MCA-2}$	$1.81 \times 10^{-10}$	$\text{m}^3 / \text{Pa}$

613

614

## 615 B.2 Computational details

616 The model equations for blood flow and species transport are implemented in open source computational  
 617 fluid dynamics (CFD) code, OpenFOAM 4.0, which utilises a finite volume spatial discretisation. The  
 618 PIMPLE algorithm is employed for pressure-velocity coupling with a tolerance of  $10^{-5}$  and  $5 \times 10^{-5}$  for

619 velocity and pressure, respectively. A blending function of Euler and Crank-Nicolson schemes is chosen  
620 for temporal integration with a blending coefficient of 0.9, recommended to ensure accuracy and  
621 robustness in OpenFOAM. A time step of 0.005 seconds and maximum iteration of 500 are used to ensure  
622 robust convergence and solution accuracy. The compartmental model is solved using an inbuilt ordinary  
623 differential equations solver in MATLAB, which is based on the Runge-Kutta method.

624

625 A computational mesh containing approximately 2 million hexahedral elements for the reconstructed  
626 geometry is created in ICEM CFD 15.0. This mesh is deemed sufficient following a mesh independence  
627 study with two additional meshes, consisting of around 0.9 million and 1.5 million elements, for the case  
628 of clot No. 1. Differences in lysis completion time are less than 4 seconds and calculated ACA pressures  
629 at 330 seconds (around lysis completion) differ by less than 0.01 %. Nevertheless, the finest mesh is used  
630 for more detailed lysis patterns. For spatial interpolation, a linear scheme is adopted for all simulations.

631

632 Results are saved every 2 to 10 seconds of simulation time depending on the phase of simulation, i.e.,  
633 more frequent data acquisition during clot dissolution. All simulations start with zero pressure and  
634 velocity in the whole computational domain at the initial time  $t = 0$ . Initial concentrations of tPA, PLG,  
635 PLS and AP are  $7 \times 10^{-5}$  [8], 2 [9], 0 [9] and 1 [10]  $\mu\text{M}$ , respectively.

636

637 Further details regarding the OpenFOAM solver settings and case files are available upon request.

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