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Electronic and optical properties of SnX₂ (X=S, Se) - InSe van der Waal's heterostructures from first-principle calculations

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Abstract:

Abstract: In this work from first-principles simulations we investigate bilayer van der Waal's heterostructures (vdWh) of emerging 2-dimensional (2D) optical materials SnS₂ and SnSe₂ with monolayer InSe. With density functional theory (DFT) calculations, we study the structural, electronic, optical and carrier transport properties of the SnX₂ (X=S,Se)-InSe vdWh. Calculations show SnX₂-InSe in its most stable stacking form (named AB-1) to be a material with a small (0.6-0.7eV) indirect band-gap. The bilayer vdWh shows broad spectrum optical response, with number of peaks in the infra-red to visible region. In terms of carrier transport properties, asymmetry in conductance was observed with respect to the transport direction and electron and hole transmission. The findings are promising from the viewpoint of nanoelectronics and photonics.

Keywords: 2D materials, heterostructures, DFT, RPA

I. Introduction

Layered tin dichalcogenides such as SnS₂ and SnSe₂ have recently been in focus for their novel properties [1]-[6] such as indirect to direct band-gap transition [1,5], strain tunable magnetism [3], high carrier mobility [2], low thermal conductivity [2], fast photoresponse [1] etc. These properties indicate wide-ranging potential applications of 2-dimensional (2D) SnX₂ (X=S,Se) in sensors, nanoscale FETs, thermoelectrics, catalysis, solar cells and photonic devices. [4,5,6] The industrial viability of these materials are enhanced by the choice of large number of chemical and physical synthesis techniques for layered SnX₂ [1]-[6] and the relative abundance and environmental friendliness of the constituent elements [1].

Also, another emerging material, layered InSe has shown good band-gap tunability and carrier transport properties [7]-[12] and good photo-detection and novel optical response wherein the band edge response is absent in monolayers [7,8]. As a result layered or 2D InSe is also being pursued for nanoelectronics and photonics in a significant manner. [11,12]

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Monolayer InSe has an experimentally reported lattice parameter of about 4.09Å [11], while single layer 2H-SnS₂ and 2H-SnSe₂ have lattice parameters around 3.63Å and 3.81Å respectively. [13] This indicates a much smaller lattice mismatch for SnX₂-InSe than that of InSe with TMDs such as MoS₂ (a=3.15Å), MoSe₂ (a=3.32Å), WS₂ (a=3.19Å) and WSe₂ (a=3.33Å). [14]-[16]

With the recent growing interest in vdWh structures, bilayer heterostructures of InSe-MX₂ (M=Mo, W, X= S, Se) have been reported both experimentally and theoretically. [15,16,17] A number of other 2D materials as SnS (a=4.28Å, b=4.08Å), GeS (a=4.28Å, b=3.97Å) and phosphorene (a=3.30Å, b=4.62Å) have also been theoretically explored as vdWh materials in combination with InSe. [18, 19]

However, to the best of the author's knowledge the present work is the first report to study in detail the vdWh of SnX₂-InSe. In terms of fabrication process a better lattice matching can offer possibilities of growing one material on top of another in addition to transfer based techniques. Further, standalone SnX₂ have shown novel properties as high carrier mobility [2], low thermal conductivity [2], fast photoresponse [1] etc which may work in synergy with a material such as InSe.

Thus, possessing excellent lattice matching, 2D hexagonal SnX₂ and InSe have very good potential compatibility in sequentially grown superlattices or van der Waals heterostructures (vdWh). Such a combination, could offer interesting optical and electronic properties, owing to the close values of band-gaps resulting in a high possibility of intra and inter-band transitions among the two different materials.

In this work we look to investigate SnX₂-InSe vdWh from first principle density functional theory (DFT) simulations. We identify the most stable stacking of the vdWh lattice and thereafter calculate the electronic properties and various optical properties as joint density of state (JDOS), complex dielectric functions and energy loss spectra (theoretical electron energy loss spectra or EELS), of the same. Also we investigate the carrier transport properties in such vdWh by means of non-equilibrium Green's function (NEGF) simulations.

II. Methodology

We employ generalized gradient approximation (GGA) calculations with Perdew-Burke-Ernzerhoff (PBE) exchange and correlation functional [20] in the Quantum ESPRESSO package [21]. The vdWh unit cells consisting of SnX₂-InSe had 15Å vacuum gap, and they were sampled with a 9x9x1 Monkhorst-Pack [22] k-point grid, with a cutoff energy of 150Ry. The Davidson diagonalization algorithm [23] was used in the calculations, with convergence threshold of 10⁻⁷ Ry. The fhi88pp norm-conserving basis sets of Troullier-Martins type [24,25] were used in the calculations. The van der Waals corrections were included by the Grimme's DFT-D2 method [26] and the structures were

relaxed with Broyden-Fletcher-Goldfarb-Shanno (BFGS) algorithm [27] for variable cell relaxation to a pressure convergence threshold of 0.5kBar and with Hellmann-Feynman forces reduced to less than 10^{-4} Ry/Bohr.

The optical spectra of the systems were calculated with the random phase approximation (RPA) approach, as implemented in the epsilon.x toolset [28] The joint density of states (JDOS) is defined as [28]

$$J(\omega) = \sum_{\alpha} \sum_{\beta} \frac{V}{(2\pi)^3} \int \delta(E_{k,\beta} - E_{k,\alpha} - \hbar\omega) [f(E_{k,\alpha}) - f(E_{k,\beta})] \cdot d^3k \quad (1)$$

V is the volume of the cell, α, β are states belonging to conduction and valence bands respectively, E_k are the eigenvalues of the Hamiltonian and $f(\cdot)$ is the Fermi distribution function. The Dirac delta function is approximated by a Gaussian distribution, normalized to one [28]

$$G(\omega) = \frac{1}{\Gamma\sqrt{\pi}} \exp\left\{-\frac{(E_{k,\beta} - E_{k,\alpha} - \hbar\omega)^2}{\Gamma^2}\right\} \quad (2)$$

Γ is the broadening parameter. The complex dielectric function is given by [28]

$$\begin{aligned} \varepsilon_2(\omega) = & 1 - \frac{4\pi q^2}{VN_k m^2} \sum_{\alpha,k} \frac{df(E_{k,\alpha})}{dE_{k,\alpha}} \frac{\hat{M}_{a,b}}{\omega^2 + i\eta_1\omega} + \dots \\ & \dots + \frac{8\pi q^2}{VN_k m^2} \sum_{\alpha \neq \beta} \sum_k \frac{\hat{M}_{a,b}}{(E_{k,\beta} - E_{k,\alpha}) (\omega_{k,\beta} - \omega_{k,\alpha})^2 + \omega^2 + i\eta_2\omega} f(E_{k,\alpha}) \end{aligned} \quad (3)$$

η_1 and η_2 are the inter-band and intra-band smearing respectively. The matrix element $M_{a,b}$ are defined as [28]

$$\hat{M}_{a,b} = \left\langle u_{\beta} | p_a | u_{\alpha} \right\rangle \left\langle u_{\alpha} | p_b^{\dagger} | u_{\beta} \right\rangle \quad (4)$$

With a London transformation upon ε_2 the dielectric tensor calculated on the imaginary frequency axis may be written as [28]

$$\varepsilon_2(i\omega) = 1 + \frac{2}{\pi} \int_0^{\infty} \frac{\omega' \varepsilon_2(\omega')}{\omega'^2 + \omega^2} d\omega' \quad (5)$$

The energy loss spectrum (theoretical EELS count) is obtained from the imaginary part of the inverse dielectric tensor.

The transmission is calculated with the DFT-NEGF method [29]-[35] in QuantumWise ATK 2016.4 [26], using similar DFT simulation parameters as with the Quantum ESPRESSO calculations. For the NEGF transport calculation, an FFT2D Poisson solver and Krylov self-energy calculator are

employed in ATK. [33]-[35] The detailed DFT-NEGF transport calculation methodology is well-described in literature [29]-[35] The zero-bias transmission spectra were evaluated for both the zigzag and the armchair direction. The Green's function can be expressed as [29]-[35]

$$G(\mathbf{E}) = \left[(\mathbf{E} + i\delta)\mathbf{S} - \mathbf{H} - \Sigma^R(\mathbf{E}) - \Sigma^L(\mathbf{E}) \right]^{-1} \quad (6)$$

In (X) \mathbf{H} is the Hamiltonian, and \mathbf{S} is the overlap matrix. δ is an infinitesimally small positive quantity. The self-energy matrices of the right/left contacts is $\Sigma^{R,L}$ and is related to the broadening matrix Γ as [29]-[31]

$$\Gamma = i(\Sigma - \Sigma^\dagger) \quad (7)$$

The transmission can be calculated from the Green's function as [29,30,35]

$$T(\mathcal{E}) = \text{Tr} \left[G\Gamma^R G^\dagger \Gamma^L \right] \quad (8)$$

III. Results and Discussions

The hexagonal monolayer SnX_2 has the Sn atom sitting at the centre of edge sharing octahedral and lying between two layers of chalcogen atoms. Such a structure when combined with the corrugated surface of the InSe monolayer, presents various possible configurations. Considering the three high symmetry points in the hexagonal lattice and three dissimilar atoms in the SnX_2 layer (in terms of element as well as position), and the corrugated nature of the InSe with two (chemically) distinguishable crystallographic positions, there can be in total 12 different possible structures of the SnX_2 -InSe vdWh. They are labelled as AA stacking (4 types), AB stacking (2 types) and AC stacking (6 types).

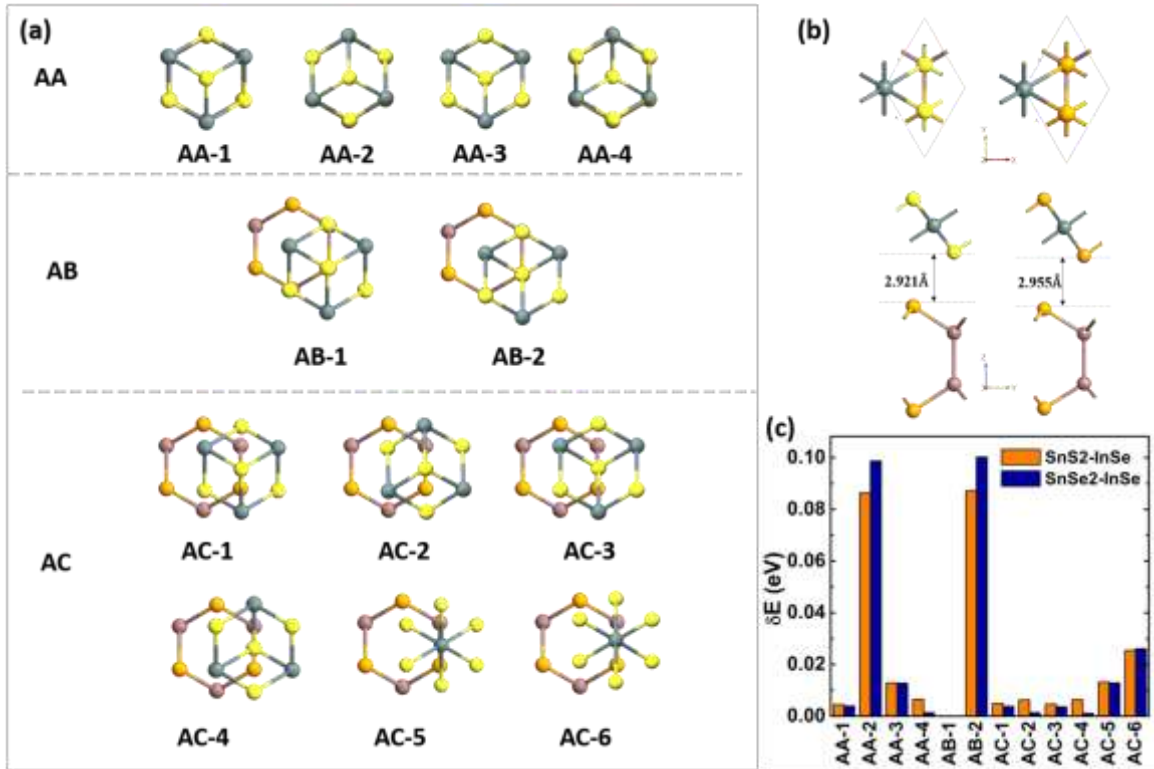


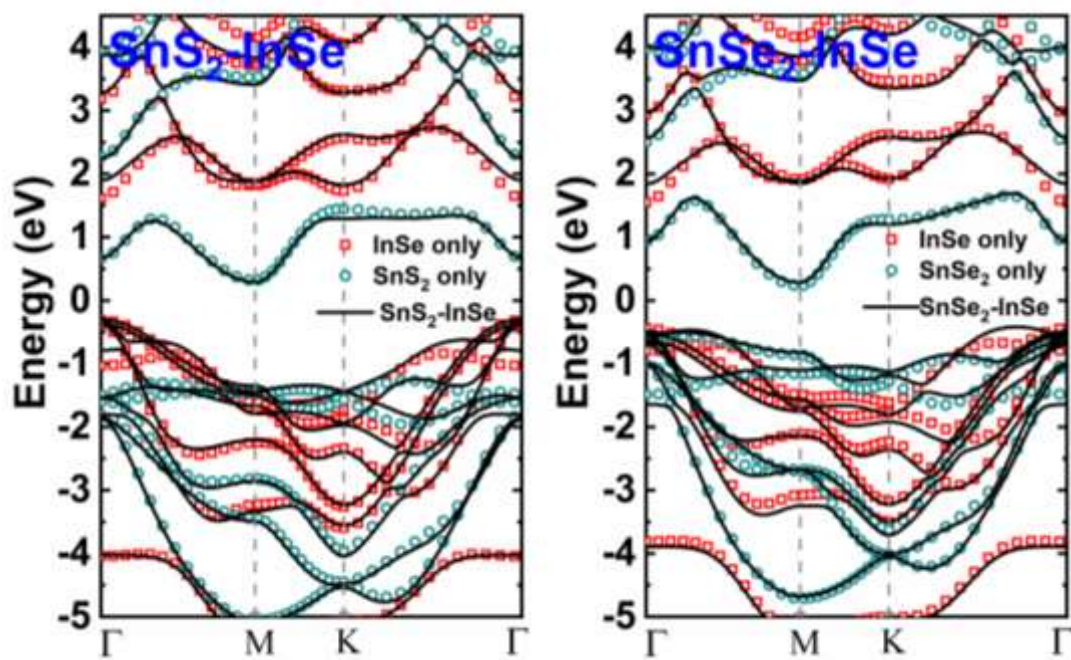
Fig. 1: (a) The top views (xy -plane) of the different possible stacking structures of the $\text{SnX}_2\text{-InSe}$ vdWh unit-cell **(b)** The top (xy -plane) and side (yz -plane) view of the most stable structure unit-cell (AB-1) and **(c)** the relative total energies with respect to the most stable structure. Structural details are presented more elaborately in the supplementary material [36]

The optimized cell parameters of the different structures are provided in Table I. Of the different structures the AB-1, is the most stable, for both $\text{SnS}_2\text{-InSe}$ and $\text{SnSe}_2\text{-InSe}$ vdWh structures. In this structure the top chalcogenide atom of SnX_2 lies directly over the top Se atom of InSe while the bottom chalcogenide atom of SnX_2 lies over the top In atom. While there are other structures as well which differ only by a very small amount of energy in terms of stability, we look to focus mostly on the most energetically stable configuration in the further studies. In the supplementary material [36] elaborate figures with the top view (xy plane) and the side view (yz plane) of the 12 possible structures for $\text{SnX}_2\text{-InSe}$ vdWh are presented. To make the stacking easily understandable, a 4×4 supercell is used for visualization purposes in the supplementary material.

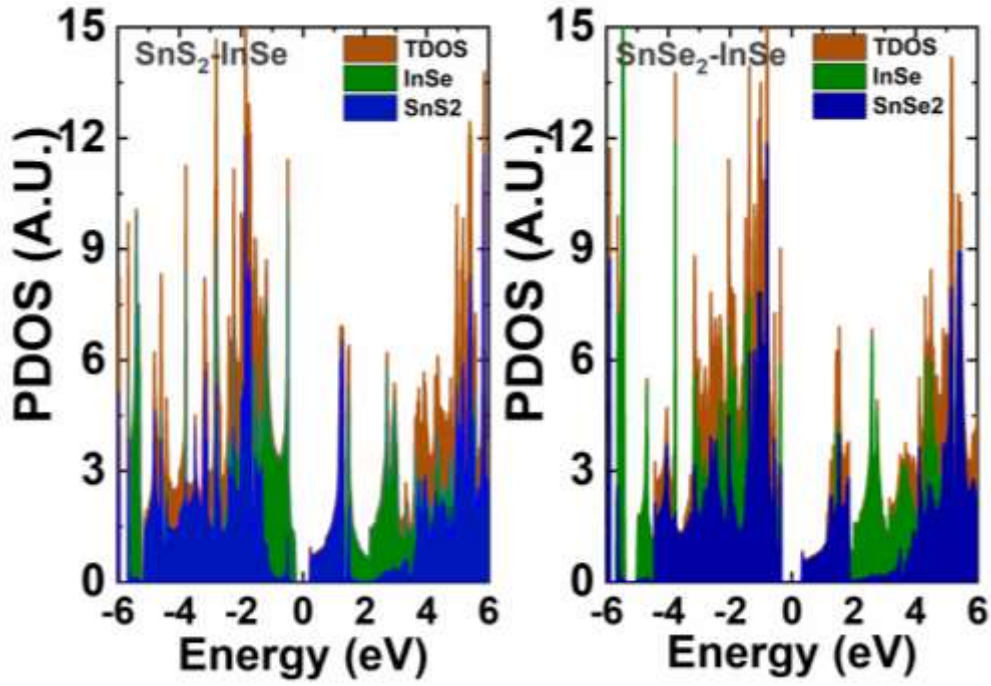
Table I: Different structures of the $\text{SnX}_2\text{-InSe}$ vdWh and associated lattice parameters and interlayer spacing.

Stacking type	Lattice parameter a (Å)		Interlayer spacing d (Å)	
	$\text{SnS}_2\text{-InSe}$	$\text{SnSe}_2\text{-InSe}$	$\text{SnS}_2\text{-InSe}$	$\text{SnSe}_2\text{-InSe}$
AA-1	3.8139	3.8894	2.9777	2.9704
AA-2	3.8098	3.8802	3.7131	3.7756
AA-3	3.8139	3.8919	2.9777	2.9772

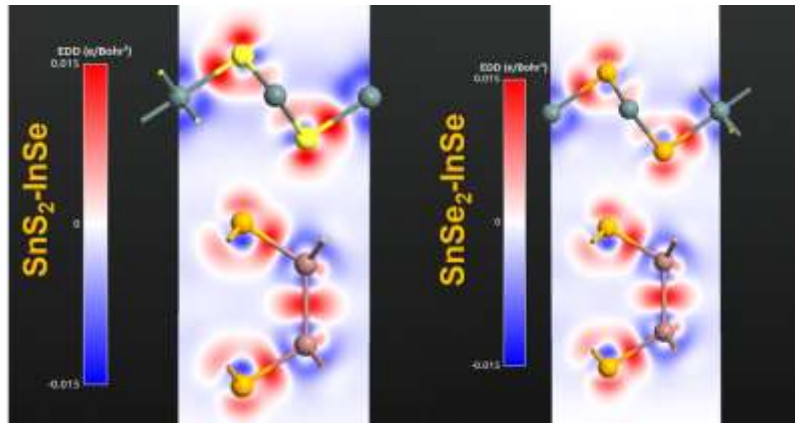
AA-4	3.8138	3.8868	2.9758	2.9375
AB-1	3.8133	3.8912	2.9213	2.9548
AB-2	3.8086	3.8801	3.7196	3.7849
AC-1	3.8114	3.8846	3.0642	3.1113
AC-2	3.8115	3.8856	3.037	3.0857
AC-3	3.8113	3.8853	3.0681	3.1131
AC-4	3.8119	3.8858	2.8639	2.9106
AC-5	3.8154	3.8843	3.0677	3.1124
AC-6	3.8056	3.8766	3.091	3.1488



2. (a)



2. (b)



2. (c)

Fig. 2 : (a) PBE Bandstructures of the $\text{SnX}_2\text{-InSe}$ vdWh, showing also the contribution of the comprising layers in dashed lines. (b) Projected Density of states (PDOS) plots showing the contributions of the individual layers and the resulting total DOS in the vdWh. (c) Electron density difference (EDD) plots for the vdWh

In Fig. 2a, the bandstructures of the most stable form (AB-1 stacking) of the $\text{SnS}_2\text{-InSe}$ and the $\text{SnSe}_2\text{-InSe}$ vdWh are presented. The plots also show the contribution of individual layers to the overall bandstructure. The contributions are inclusive of the small strain that is incurred due to formation of the vdWh. This is done by calculating the bandstructure for each component at a time by removing the other layer from the optimized cell. Thus, the effect of the interlayer interaction (independent of the strain) can also be very clearly understood.

The calculated bandstructures for the most stable structure is shown in Fig. 2a. Both the vdWh show indirect band-gap. SnS₂-InSe shows a gap of 0.61eV between M point in conduction band (CB) and Γ point in valence band (VB). SnSe₂-InSe has a slightly larger gap of 0.70, with the CB minima at M point and VB maxima at a point in the K- Γ path, located about two third the distance from K to Γ point. Such gaps offer good possibilities for keeping electron and hole distributions apart.

From the bands, we see that the conduction band (CB) minima in both the vdWh are contributed by the CB from the SnX₂ layer, and are located at the M point of the hexagonal Brillouin zone. However the valence band (VB) maxima, is contributed mostly by the InSe. Among the band extrema, for SnSe₂, the VB maxima, located between K and Γ , seems to be affected more by the interlayer interactions. It is here that the SnSe₂ contribution seems to be influenced more to interlayer interactions, thus giving rise to the VB maxima of the vdWh. In general, around the Γ point the lowest conduction bands of the InSe also seem to be affected by interlayer interactions by vdWh formation.

For the carrier mobility, it can be qualitatively said that as the CB min in the vdWh is contributed by SnX₂, it possesses a slightly lesser curvature against that of intrinsic InSe. This indicates a slightly higher effective mass and as a result a slightly lesser electron mobility as compared to pure InSe. The case of the hole mobility is expected to remain more or less the same for SnS₂-InSe vdWh considering the band profile of vdWh at VB max (Γ point) which is almost identical to that for the InSe. For SnSe₂-InSe however the hole mobility is expected to degrade as the vdWh VB maxima is now much flatter in compared to that of InSe.

The PDOS plots in Fig. 2b show the vdWh conduction bands to be more influenced by the SnX₂ layer. However for the valence band (VB) maxima, the SnX₂ contribution seems to depend on chalcogen of the top layer (X=S or Se). PDOS reveals that it is InSe that has more contribution to VB edges in SnS₂-InSe as compared to SnS₂, while for SnSe₂-InSe vdWh, it is SnSe₂ which contributes more significantly to the VB states. Such different type of contributions push the VB max upwards at Γ point in case of SnS₂-InSe and somewhere between the K and Γ points for SnSe₂-InSe vdWh.

The difference in the charge distribution or transfer in the two vdWh is investigated with electron density difference (EDD) analysis, presented in Fig 2c. The more positive EDD around the chalcogen atoms of the SnX₂ in case of SnS₂-InSe, as compared to SnSe₂-InSe, indicates a stronger tendency for electron accumulation near the S atoms in SnS₂ than the Se atoms in SnSe₂ vdWh. Apart from this a tendency of developing a stronger dipole moment between the Sn-S pair as compared to the Sn-Se pair is also evident from the EDD plot. These factors revealed by the PDOS and the EDD results contribute to the bandstructure differences among the two vdWh.

The carrier effective masses (m^*) for the vdWh were calculated with a polynomial fitting formula, considering the parabolic band approximation and using the relation $\frac{1}{m^*} = \frac{1}{\hbar^2} \left(\frac{d^2 \xi}{dk_i dk_j} \right)$, ξ being the energy eigenvalue and $k_{i,j}$ the wave-vector along i, j direction at the VB maxima and the CB minima in the (100) and (010) directions. The calculated effective masses are listed in Table-II.

Table II: The calculated band gap and carrier effective mass for the vdWh

vdWh	Band gap E_g (in eV)	electron effective mass (m_e^*)		hole effective mass (m_h^*)	
		(100)	(010)	(100)	(010)
SnS ₂ -InSe	0.61 (Indirect)	0.572 m_0	0.675 m_0	0.897 m_0	0.795 m_0
SnSe ₂ -InSe	0.70 (Indirect)	0.653 m_0	0.789 m_0	0.956 m_0	0.992 m_0

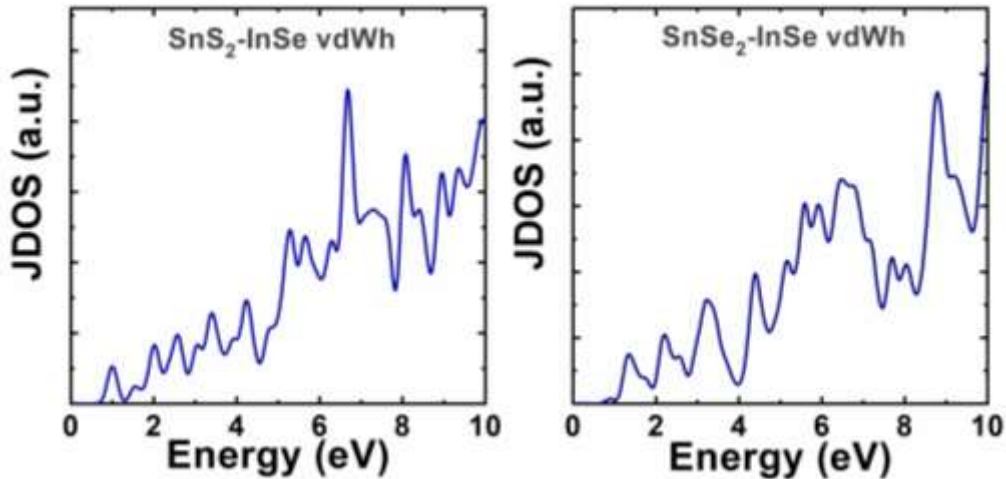


Fig 3: The calculated joint density of states (JDOS) of the SnX₂-InSe vdWh.

The calculated optical joint density of states (JDOS) of the vdWh are presented in Fig. 3. JDOS gives a qualitative idea of how many allowed optical transitions may exist between the populated valence states and the unpopulated conduction states having energy difference of $\hbar\omega$. As JDOS is an indicator of the number of available states for photons to interact with, for optical emission/absorption process, it is an important part of optical characteristics of a given material. The JDOS of the two structures differ in the sharpness of the peaks apart from their position and also the number of peaks. While the SnS₂-InSe shows a greater number of sharper peaks, the JDOS peaks for SnSe₂-InSe are more spread-out in nature, and also lesser in number. A cascade of small but well defined peaks in the range 0.5-5eV for SnS₂-InSe vdWh outnumbers those in SnSe₂-InSe. Around the 1eV energy range,

SnS₂-InSe shows more possible transitions than SnSe₂-InSe. Also around a higher energy of 6.5-7.5eV, there exists a significant difference in terms of the JDOS among the two vdWh. The SnSe₂-InSe vdWh is characterised by a significant decline in the JDOS around the 7-8eV energy range.

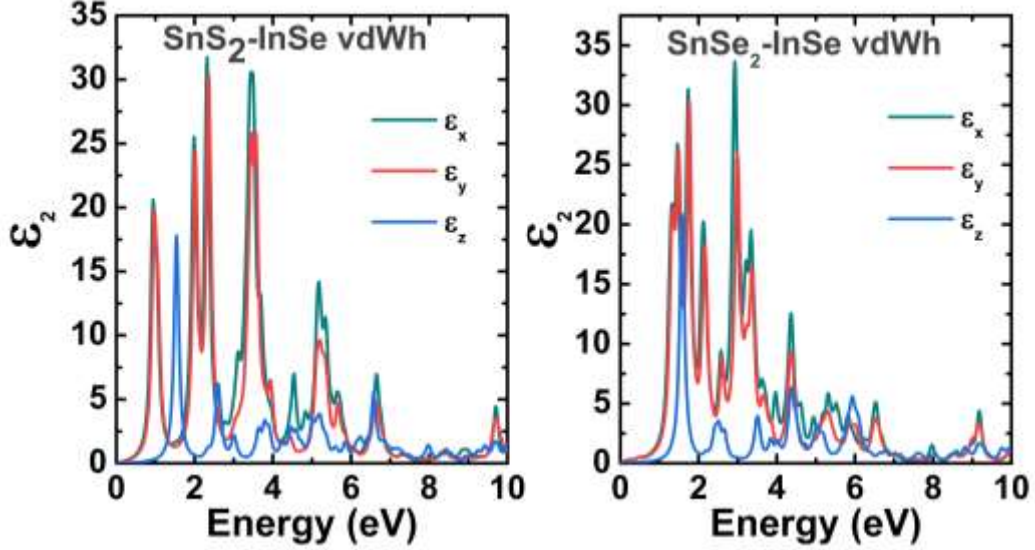


Fig 4: The calculated imaginary part of the complex dielectric function of the SnX₂-InSe vdWh.

The imaginary part of the complex dielectric function (ϵ_2), which can also act as a measure of optical absorption, is presented in Fig. 4. The two in-plane components (x and y) and the out-of plane (z) component are all shown in the plots. In perfectly isotropic bulk materials all the three components should be the same, however for heterostructures or interfaces this is seldom the case. In monolayers or vdWh assuming the light to be incident from the out-of-plane z direction, polarization is created in the in-plane x and y direction by the incident irradiation. [37] As there exist anisotropy among x and y direction of the vdWh (e.g. in terms of the structural and electronic properties as effective mass etc.), ϵ_x and ϵ_y differ from each other. A stronger absorption in the infrared (IR) to visible range is observed for both the vdWh. For both the structures, the z -component of ϵ_2 appears blue-shifted as compared to the in-plane (x and y components). The blue-shift is more prominent in case of the SnS₂-InSe vdWh. Considering the position of the in-plane characteristics, more discrete peaks at lower energies between 0.75-2.5eV can be observed for SnS₂-InSe as compared to SnSe₂-InSe vdWh. The peaks in case of the SnSe₂-Inse vdWh are more concentrated together, in the lower energy ranges. These corroborate with the JDOS spectra discussed previously. The spike in available states in SnS₂-InSe for transition around the 6.5eV mark, is also well reflected by the presence of a stronger response in this region by the SnS₂-InSe vdWh, as compared to SnSe₂-InSe vdWh.

The strongest peak for both ε_x and ε_y in SnS₂-InSe vdWh is seen around 2.33eV energy, while for ε_z it is around 1.54eV. For SnSe₂-InSe vdWh however, the strongest peak for ε_x lies around 2.95eV, while that for ε_y is situated around 1.75eV and for ε_z at 1.59eV.

Here it must also be mentioned that the results presented herein are based on a random-phase approximation (RPA) method as described by Benassi et. al. [28]. This implementation based on a multi-particle approach and offers superior accuracy over simulations with the single particle dielectric tensor. However, it does not include the excitonic effects for which GW and Bethe-Salpeter Equation (BSE) calculations could yield better results. That being said, considering the huge computational cost for GW-BSE calculations, the results presented herein can be considered a at least a good pointer towards the optical response of the vdWh systems under consideration.

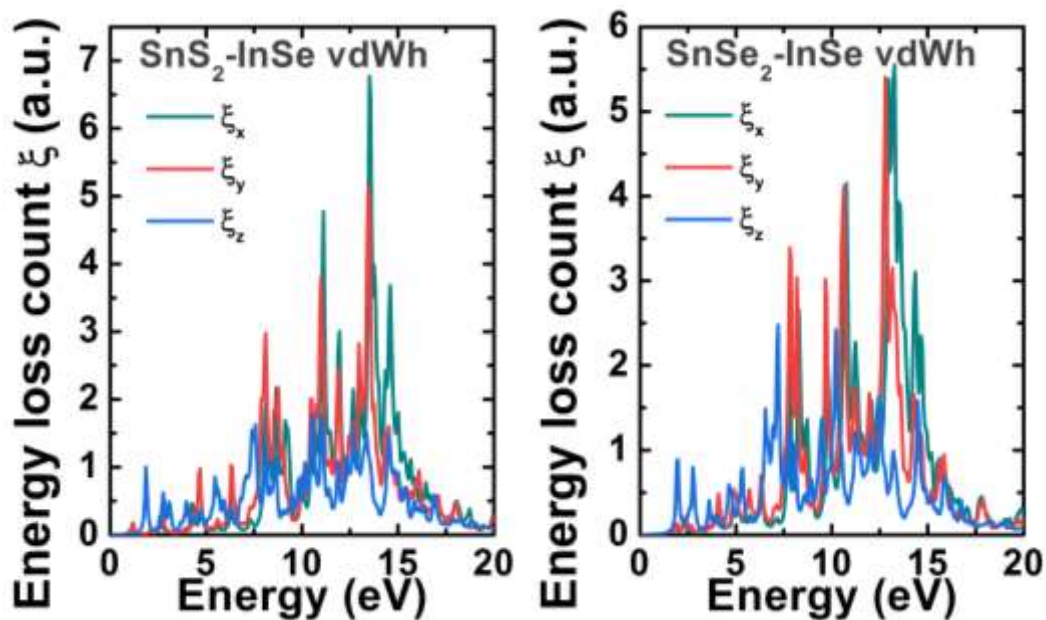


Fig 5: The energy loss spectra of the SnX₂-InSe vdWh.

The theoretical EELS count is presented in Fig. 5, shows the maxima for the SnS₂-InSe vdWh at 13.27, 12.79 and 7.21eV for the x , y and z components respectively. For the SnSe₂-InSe vdWh, the same are observed at 13.51, 13.45 and 10.57eV. The bulk plasmon frequency for these systems can thus be estimated to be $8.94 \times 10^4 \text{ cm}^{-1}$ and $1.01 \times 10^5 \text{ cm}^{-1}$ for SnS₂-InSe and SnSe₂-InSe vdWh respectively.

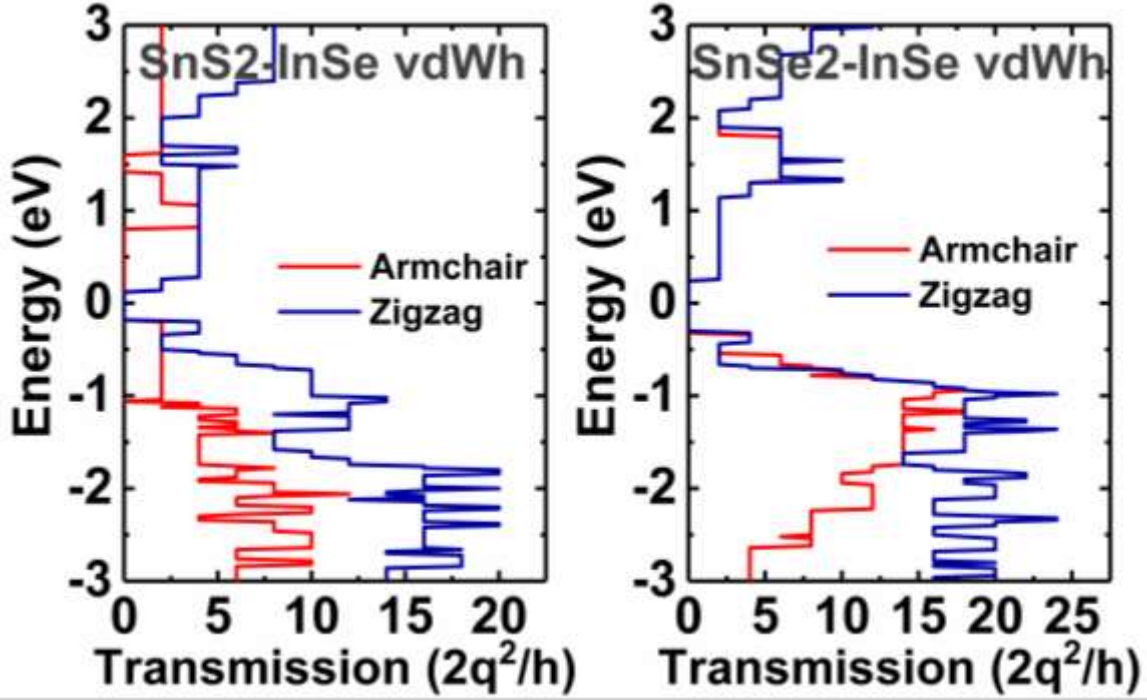


Fig 6: The carrier transmission spectra of the $\text{SnX}_2\text{-InSe}$ vdWh.

The transmission spectra of both of the vdWh show an enhanced carrier transport properties for the valence bands rather than the conduction bands. Also observable is the asymmetry in conductance in the armchair and the zigzag direction of the $\text{SnX}_2\text{-InSe}$ structures. The suppression of transport in the armchair direction than that in the zigzag direction is more significant for the $\text{SnS}_2\text{-InSe}$ vdWh, than the $\text{SnSe}_2\text{-InSe}$ vdWh. However the magnitude of transmission for holes in both transport directions is more in case of the $\text{SnSe}_2\text{-InSe}$ structure. For electron transport there exist very little asymmetry on the transport direction for $\text{SnSe}_2\text{-InSe}$ vdWh, as compared to $\text{SnS}_2\text{-InSe}$, additionally the magnitude for the zigzag direction, is also quite close for both the vdWh. While the asymmetry may be attributed to the disparity in carrier effective masses in the different transport directions, the enhanced hole conduction is a result of the larger number of valence states available near the Fermi-level (as visible in the DOS). The asymmetry in terms of transport direction and electron/ hole transmission, is something that can be utilized for novel applications in photonic and electronic devices based on $\text{SnX}_2\text{-InSe}$ vdWh.

IV. Conclusion

In this work by density functional theory simulations the structural, electronic and optical properties of bilayer van der Waals heterostructures made of 2D SnX_2 ($X=\text{S},\text{Se}$) and InSe were investigated. Among the 12 different possible stacking combinations AB-1 stacking, was found to be the most

stable for both the vdWh. The stable vdWh structures were thereafter studied for their bandstructure, DOS, JDOS and other optical parameters such as the imaginary dielectric function and theoretical EELS spectra. It was observed that SnS₂-InSe and SnSe₂-InSe vdWh form indirect-gap materials with small PBE band-gap values of 0.61 and 0.70eV respectively. The vdWh also showed moderate electron and hole effective masses ranging between 0.57-0.78m₀ and 0.79-0.99m₀ respectively depending upon the material and the transport directions. A good optical response could be observed in the IR-visible range for both the SnX₂-InSe vdWh, with the peaks in the dielectric function being more closely packed and also slightly blue shifted for the SnSe₂-InSe as compared to SnS₂-InSe. A drop in JDOS and optical response could be observed around 6-6.5eV and 6.75eV for the SnSe₂-InSe, as compared to its SnS₂ counterpart. The bulk plasmon frequency was estimated to be around 8.94x10⁴ and 1.0x10⁵ cm⁻¹ for SnS₂ and SnSe₂ based vdWh respectively. Carrier transport computed with the DFT-NEGF method, showed asymmetric conductance in terms of transport direction (armchair / zigzag) and the nature of carriers (electrons/ holes). The optical and transport properties calculated show good prospect of application of SnX₂-InSe vdWh studied in this work, in photonics and nanoelectronics. The excellent lattice matching and environmental stability of the constituent 2D materials, make a good case for not only bilayer but for multi-layer SnX₂-InSe devices.

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