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Key indicators

Single-crystal X-ray study
 $T = 150\text{ K}$
Mean $\sigma(\text{O}-\text{Ba}) = 0.008\text{ \AA}$
 R factor = 0.022
 wR factor = 0.051
Data-to-parameter ratio = 31.3

For details of how these key indicators were automatically derived from the article, see
<http://journals.iucr.org/e>.

Barium oxide iodide

Barium oxide iodide, Ba_4OI_6 , has been prepared by a solid-state reaction and shown to be isostructural with both $A_4\text{OCl}_6$, where A is Ba or Sr, and Sr_4OI_6 .

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Comment

Alkaline earth oxide chlorides and oxide bromides, of general formula $A_4\text{OX}_6$ (A = alkaline earth; $X = \text{Cl}^-, \text{Br}^-$) are known for their luminescence properties, when the alkaline earth site is doped with small amounts of Eu^{2+} or Pb^{2+} (Schipper *et al.*, 1992). We have succeeded in extending this family to the barium oxide iodide compound Ba_4OI_6 . Ba_4OI_6 was prepared by a solid-state reaction and is isostructural with Sr_4OCl_6 (Hagemann *et al.*, 1996), Ba_4OCl_6 (Bergerhoff & Goost, 1970) and Sr_4OI_6 (Barker *et al.*, 2001). The O atom is four-coordinated by Ba cations (see Fig. 1), the iodine is four- and five-coordinated by Ba cations (Figs. 2 and 3) and the Ba is eight-coordinated by one oxygen and seven iodine anions at one site, and seven-coordinated by one oxygen and six iodine anions at the other (Figs. 4 and 5). The overall structure is shown in Fig. 1 of Barker *et al.* (2001).

Experimental

BaO and BaI_2 powders were mixed in stoichiometric proportions and placed in a nickel crucible. The mixture was then heated at 1273 K for 24 h in a silica tube, under flowing nitrogen. The product was cooled to room temperature at a rate of 1 K h^{-1} .

Crystal data

Ba_4OI_6
 $M_r = 1326.72$
Hexagonal, $P6_3mc$
 $a = 10.838(4)\text{ \AA}$
 $c = 8.410(3)\text{ \AA}$
 $V = 855.5(9)\text{ \AA}^3$
 $Z = 2$
 $D_x = 5.150\text{ Mg m}^{-3}$

Mo $K\alpha$ radiation
Cell parameters from 802 reflections
 $\theta = 4.3\text{--}27.8^\circ$
 $\mu = 19.87\text{ mm}^{-1}$
 $T = 150(2)\text{ K}$
Block, colourless
 $0.18 \times 0.12 \times 0.10\text{ mm}$

Data collection

Bruker SMART1000 CCD area-detector diffractometer
 ω scans
Absorption correction: multi-scan (SADABS; Bruker, 1996)
 $T_{\min} = 0.077$, $T_{\max} = 0.137$
4900 measured reflections
842 independent reflections

732 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.040$
 $\theta_{\text{max}} = 28.8^\circ$
 $h = -14 \rightarrow 12$
 $k = -14 \rightarrow 14$
 $l = -11 \rightarrow 11$
Intensity decay: none

Refinement

Refinement on F^2
 $R[F^2 > 2\sigma(F^2)] = 0.022$
 $wR(F^2) = 0.051$
 $S = 1.09$
782 reflections
25 parameters

$w = 1/[\sigma^2(F_o^2) + (0.0263P)^2]$
where $P = (F_o^2 + 2F_c^2)/3$
 $(\Delta/\sigma)_{\text{max}} = 0.001$
 $\Delta\rho_{\text{max}} = 0.82\text{ e \AA}^{-3}$
 $\Delta\rho_{\text{min}} = -1.20\text{ e \AA}^{-3}$
Absolute structure: Flack (1983)
Flack parameter = -0.06 (10)

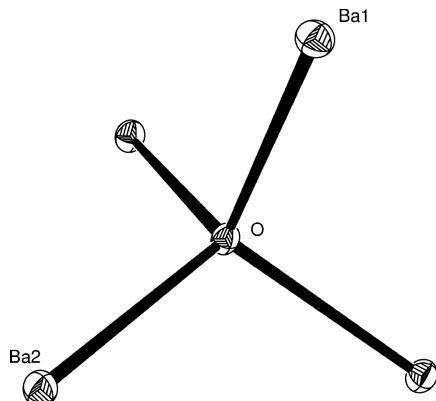


Figure 1

A view showing the tetrahedral coordination around the O atom. Displacement ellipsoids are drawn at the 50% probability level.

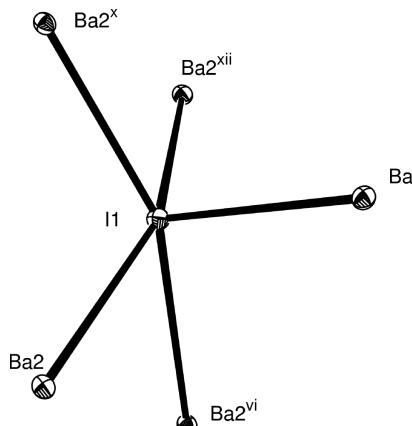


Figure 2

A view showing coordination around atom I1. Displacement ellipsoids are drawn at the 50% probability level. [Symmetry codes: (vi) $1 - y, 1 + x - y, z$; (x) $y, -x + y, \frac{1}{2} + z$; (xii) $1 - x, 1 - y, \frac{1}{2} + z$.]

Table 1
Selected geometric parameters (\AA , $^\circ$).

Ba1–O ⁱ	2.542 (12)	Ba2–I2 ^{iv}	3.5115 (16)
Ba1–I1 ⁱⁱ	3.5848 (17)	Ba2–I1 ^v	3.5560 (15)
Ba1–I2	3.6927 (18)	Ba2–I1 ⁱⁱⁱ	3.6781 (15)
Ba2–O	2.555 (4)	O–Ba1 ⁱⁱⁱ	2.542 (12)
Ba2–I2 ⁱⁱⁱ	3.467 (2)		

Symmetry codes: (i) $x, y, z - 1$; (ii) $y, 1 - x + y, z - \frac{1}{2}$; (iii) $x, y, 1 + z$; (iv) $y, -x + y, \frac{1}{2} + z$; (v) $1 - x, 1 - y, z - \frac{1}{2}$.

The origin was fixed by application of a floating origin restraint which effectively fixes the centre of gravity of the structure in the polar-axis direction. This leads to smaller correlations than fixing a single atom in structures with no dominant heavy atom (Flack & Schwarzenbach, 1988).

Data collection: SMART (Bruker, 1998); cell refinement: SAINT (Bruker, 2000); data reduction: SAINT and SHELXL97 (Sheldrick, 1997); program(s) used to solve structure: SIR97 (Altomare *et al.*, 1999); program(s) used to refine structure: SHELXL97 and WINGX (Farrugia, 1999); molecular graphics: ORTEP-3 (Farrugia, 1997);

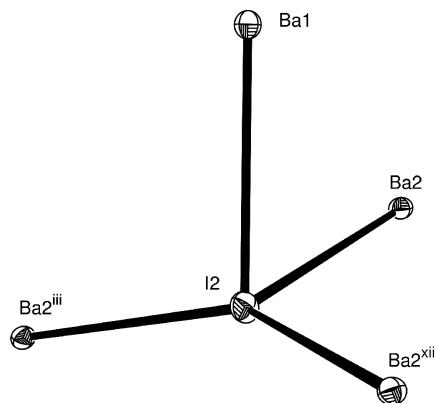


Figure 3

A view showing the coordination around atom I2. Displacement ellipsoids are drawn at the 50% probability level. [Symmetry codes: (iii) $x - y, x, z - \frac{1}{2}$; (xiii) $y, -x + y, z - \frac{1}{2}$.]

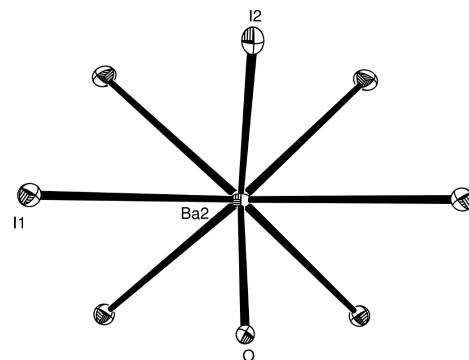


Figure 4

A view showing the coordination around atom Ba2. Displacement ellipsoids are drawn at the 50% probability level.

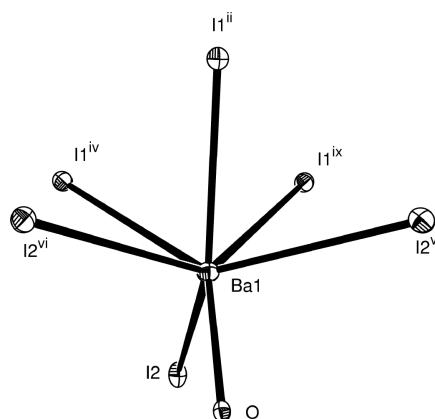


Figure 5

A view showing the coordination around atom Ba1. Displacement ellipsoids are drawn at the 50% probability level. [Symmetry codes: (ii) $y, 1 - x + y, z - \frac{1}{2}$; (iv) $1 - x, 1 - y, z - \frac{1}{2}$; (v) $-x + y, 1 - x, z$; (vi) $1 - y, 1 + x - y, z$; (ix) $x - y, x, \frac{1}{2} + z$.]

software used to prepare material for publication: SHELXL97 and PLATON (Spek, 2001).

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supporting information

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(I)

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 $V = 855.5 (9) \text{ \AA}^3$
 $Z = 2$
 $F(000) = 1100$

$D_x = 5.150 \text{ Mg m}^{-3}$
 Mo $K\alpha$ radiation, $\lambda = 0.71069 \text{ \AA}$
 Cell parameters from 802 reflections
 $\theta = 4.3\text{--}27.8^\circ$
 $\mu = 19.87 \text{ mm}^{-1}$
 $T = 150 \text{ K}$
 Block, colourless
 $0.18 \times 0.12 \times 0.10 \text{ mm}$

Data collection

Bruker SMART1000 CCD area-detector
 diffractometer
 Radiation source: fine-focus sealed tube
 Graphite monochromator
 ω scans
 Absorption correction: multi-scan
 (SADABS; Bruker, 1996)
 $T_{\min} = 0.077$, $T_{\max} = 0.137$

4900 measured reflections
 842 independent reflections
 732 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.040$
 $\theta_{\max} = 28.8^\circ$, $\theta_{\min} = 2.2^\circ$
 $h = -14 \rightarrow 12$
 $k = -14 \rightarrow 14$
 $l = -11 \rightarrow 11$

Refinement

Refinement on F^2
 Least-squares matrix: full
 $R[F^2 > 2\sigma(F^2)] = 0.022$
 $wR(F^2) = 0.051$
 $S = 1.09$
 782 reflections
 25 parameters
 1 restraint
 Primary atom site location: structure-invariant
 direct methods

Secondary atom site location: difference Fourier
 map
 $w = 1/[\sigma^2(F_o^2) + (0.0263P)^2]$
 where $P = (F_o^2 + 2F_c^2)/3$
 $(\Delta/\sigma)_{\max} = 0.001$
 $\Delta\rho_{\max} = 0.82 \text{ e \AA}^{-3}$
 $\Delta\rho_{\min} = -1.20 \text{ e \AA}^{-3}$
 Absolute structure: Flack (1983)
 Absolute structure parameter: -0.06 (10)

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R -factor wR and goodness of fit S are based on F^2 , conventional R -factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R -factors(gt) etc. and is not relevant to the choice of reflections for refinement. R -factors based on F^2 are statistically about twice as large as those based on F , and R -factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
Ba1	0.3333	0.6667	0.02342 (13)	0.0133 (2)
Ba2	0.20359 (3)	0.40719 (6)	0.62927 (8)	0.01196 (14)
I1	0.53228 (3)	0.46772 (3)	0.82627 (8)	0.01280 (15)
I2	0.13667 (3)	0.27334 (6)	0.01355 (8)	0.01651 (16)
O	0.3333	0.6667	0.7212 (15)	0.010 (2)

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Ba1	0.0142 (3)	0.0142 (3)	0.0113 (5)	0.00711 (15)	0.000	0.000
Ba2	0.0109 (2)	0.0100 (3)	0.0147 (3)	0.00499 (14)	-0.00039 (13)	-0.0008 (3)
I1	0.0127 (2)	0.0127 (2)	0.0130 (3)	0.0064 (3)	-0.00047 (14)	0.00047 (14)
I2	0.0126 (2)	0.0184 (3)	0.0204 (3)	0.00919 (17)	0.00145 (15)	0.0029 (3)
O	0.008 (3)	0.008 (3)	0.013 (6)	0.0041 (16)	0.000	0.000

Geometric parameters (\AA , $^\circ$)

Ba1—O ⁱ	2.542 (12)	Ba2—I1 ^v	3.6781 (15)
Ba1—I1 ⁱⁱ	3.5848 (17)	Ba2—I1	3.6781 (15)
Ba1—I1 ⁱⁱⁱ	3.5848 (17)	Ba2—Ba1 ^{ix}	4.113 (2)
Ba1—I1 ^{iv}	3.5848 (17)	Ba2—Ba2 ^{vi}	4.218 (2)
Ba1—I2 ^v	3.6927 (18)	Ba2—Ba2 ^v	4.218 (2)
Ba1—I2 ^{vi}	3.6927 (18)	I1—Ba2 ^x	3.5560 (15)
Ba1—I2	3.6927 (18)	I1—Ba2 ^{xii}	3.5560 (15)
Ba1—Ba2 ^{vii}	4.113 (2)	I1—Ba1 ^{xii}	3.5848 (17)
Ba1—Ba2 ⁱ	4.113 (2)	I1—Ba2 ^{vi}	3.6781 (15)
Ba1—Ba2 ^{viii}	4.113 (2)	I2—Ba2 ⁱ	3.467 (2)
Ba2—O	2.555 (4)	I2—Ba2 ⁱⁱⁱ	3.5115 (16)
Ba2—I2 ^{ix}	3.467 (2)	I2—Ba2 ^{xiii}	3.5115 (16)
Ba2—I2 ^x	3.5115 (16)	O—Ba1 ^{ix}	2.542 (12)
Ba2—I2 ^{xi}	3.5115 (16)	O—Ba2 ^v	2.555 (4)
Ba2—I1 ⁱⁱⁱ	3.5560 (15)	O—Ba2 ^{vi}	2.555 (4)
Ba2—I1 ^{iv}	3.5560 (15)		
O ⁱ —Ba1—I1 ⁱⁱ	135.27 (3)	I2 ^{ix} —Ba2—I1 ^v	68.66 (2)
O ⁱ —Ba1—I1 ⁱⁱⁱ	135.27 (3)	I2 ^x —Ba2—I1 ^v	142.459 (19)
I1 ⁱⁱ —Ba1—I1 ⁱⁱⁱ	75.10 (4)	I2 ^{xi} —Ba2—I1 ^v	71.35 (2)
O ⁱ —Ba1—I1 ^{iv}	135.27 (3)	I1 ⁱⁱⁱ —Ba2—I1 ^v	74.43 (4)
I1 ⁱⁱ —Ba1—I1 ^{iv}	75.10 (4)	I1 ^{iv} —Ba2—I1 ^v	144.294 (19)
I1 ⁱⁱⁱ —Ba1—I1 ^{iv}	75.10 (4)	O—Ba2—I1	73.53 (11)

O ⁱ —Ba1—I2 ^v	88.71 (2)	I2 ^{ix} —Ba2—I1	68.66 (2)
I1 ⁱⁱ —Ba1—I2 ^v	70.379 (15)	I2 ^x —Ba2—I1	71.35 (2)
I1 ⁱⁱⁱ —Ba1—I2 ^v	70.379 (16)	I2 ^{xi} —Ba2—I1	142.459 (19)
I1 ^{iv} —Ba1—I2 ^v	136.01 (4)	I1 ⁱⁱⁱ —Ba2—I1	144.29 (2)
O ⁱ —Ba1—I2 ^{vi}	88.71 (2)	I1 ^{iv} —Ba2—I1	74.43 (4)
I1 ⁱⁱ —Ba1—I2 ^{vi}	70.379 (16)	I1 ^v —Ba2—I1	123.13 (4)
I1 ⁱⁱⁱ —Ba1—I2 ^{vi}	136.01 (4)	O—Ba2—Ba1 ^{ix}	36.1 (3)
I1 ^{iv} —Ba1—I2 ^{vi}	70.379 (16)	I2 ^{ix} —Ba2—Ba1 ^{ix}	57.55 (4)
I2 ^v —Ba1—I2 ^{vi}	119.950 (2)	I2 ^x —Ba2—Ba1 ^{ix}	130.653 (17)
O ⁱ —Ba1—I2	88.71 (2)	I2 ^{xi} —Ba2—Ba1 ^{ix}	130.653 (17)
I1 ⁱⁱ —Ba1—I2	136.01 (4)	I1 ⁱⁱⁱ —Ba2—Ba1 ^{ix}	112.46 (4)
I1 ⁱⁱⁱ —Ba1—I2	70.379 (16)	I1 ^{iv} —Ba2—Ba1 ^{ix}	112.46 (4)
I1 ^{iv} —Ba1—I2	70.379 (16)	I1 ^v —Ba2—Ba1 ^{ix}	62.97 (2)
I2 ^v —Ba1—I2	119.950 (2)	I1—Ba2—Ba1 ^{ix}	62.97 (2)
I2 ^{vi} —Ba1—I2	119.950 (2)	O—Ba2—Ba2 ^{vi}	34.36 (12)
O ⁱ —Ba1—Ba2 ^{vii}	36.31 (2)	I2 ^{ix} —Ba2—Ba2 ^{vi}	108.287 (17)
I1 ⁱⁱ —Ba1—Ba2 ^{vii}	111.36 (4)	I2 ^x —Ba2—Ba2 ^{vi}	108.049 (12)
I1 ⁱⁱⁱ —Ba1—Ba2 ^{vii}	111.36 (4)	I2 ^{xi} —Ba2—Ba2 ^{vi}	160.488 (17)
I1 ^{iv} —Ba1—Ba2 ^{vii}	171.58 (2)	I1 ⁱⁱⁱ —Ba2—Ba2 ^{vi}	91.216 (11)
I2 ^v —Ba1—Ba2 ^{vii}	52.41 (3)	I1 ^{iv} —Ba2—Ba2 ^{vi}	53.62 (2)
I2 ^{vi} —Ba1—Ba2 ^{vii}	106.13 (2)	I1 ^v —Ba2—Ba2 ^{vi}	107.812 (11)
I2—Ba1—Ba2 ^{vii}	106.13 (2)	I1—Ba2—Ba2 ^{vi}	55.009 (12)
O ⁱ —Ba1—Ba2 ⁱ	36.31 (2)	Ba1 ^{ix} —Ba2—Ba2 ^{vi}	59.152 (19)
I1 ⁱⁱ —Ba1—Ba2 ⁱ	171.58 (2)	O—Ba2—Ba2 ^v	34.36 (12)
I1 ⁱⁱⁱ —Ba1—Ba2 ⁱ	111.36 (4)	I2 ^{ix} —Ba2—Ba2 ^v	108.287 (17)
I1 ^{iv} —Ba1—Ba2 ⁱ	111.36 (4)	I2 ^x —Ba2—Ba2 ^v	160.488 (17)
I2 ^v —Ba1—Ba2 ⁱ	106.13 (2)	I2 ^{xi} —Ba2—Ba2 ^v	108.049 (12)
I2 ^{vi} —Ba1—Ba2 ⁱ	106.13 (2)	I1 ⁱⁱⁱ —Ba2—Ba2 ^v	53.62 (2)
I2—Ba1—Ba2 ⁱ	52.41 (3)	I1 ^{iv} —Ba2—Ba2 ^v	91.216 (11)
Ba2 ^{vii} —Ba1—Ba2 ⁱ	61.70 (4)	I1 ^v —Ba2—Ba2 ^v	55.009 (12)
O ⁱ —Ba1—Ba2 ^{viii}	36.31 (2)	I1—Ba2—Ba2 ^v	107.812 (11)
I1 ⁱⁱ —Ba1—Ba2 ^{viii}	111.36 (4)	Ba1 ^{ix} —Ba2—Ba2 ^v	59.152 (19)
I1 ⁱⁱⁱ —Ba1—Ba2 ^{viii}	171.58 (2)	Ba2 ^{vi} —Ba2—Ba2 ^v	60.0
I1 ^{iv} —Ba1—Ba2 ^{viii}	111.36 (4)	Ba2 ^x —I1—Ba2 ^{xii}	72.76 (4)
I2 ^v —Ba1—Ba2 ^{viii}	106.13 (2)	Ba2 ^x —I1—Ba1 ^{xii}	104.53 (4)
I2 ^{vi} —Ba1—Ba2 ^{viii}	52.41 (3)	Ba2 ^{xii} —I1—Ba1 ^{xii}	104.53 (4)
I2—Ba1—Ba2 ^{viii}	106.13 (2)	Ba2 ^x —I1—Ba2 ^{vi}	156.07 (2)
Ba2 ^{vii} —Ba1—Ba2 ^{viii}	61.70 (4)	Ba2 ^{xii} —I1—Ba2 ^{vi}	103.52 (3)
Ba2 ⁱ —Ba1—Ba2 ^{viii}	61.70 (4)	Ba1 ^{xii} —I1—Ba2 ^{vi}	99.29 (4)
O—Ba2—I2 ^{ix}	93.6 (3)	Ba2 ^x —I1—Ba2	103.52 (3)
O—Ba2—I2 ^x	140.63 (2)	Ba2 ^{xii} —I1—Ba2	156.07 (2)
I2 ^{ix} —Ba2—I2 ^x	89.79 (3)	Ba1 ^{xii} —I1—Ba2	99.29 (4)
O—Ba2—I2 ^{xi}	140.63 (2)	Ba2 ^{vi} —I1—Ba2	69.98 (2)
I2 ^{ix} —Ba2—I2 ^{xi}	89.79 (3)	Ba2 ⁱ —I2—Ba2 ⁱⁱⁱ	109.018 (17)
I2 ^x —Ba2—I2 ^{xi}	78.50 (2)	Ba2 ⁱ —I2—Ba2 ^{xiii}	109.018 (17)
O—Ba2—I1 ⁱⁱⁱ	84.4 (2)	Ba2 ⁱⁱⁱ —I2—Ba2 ^{xiii}	140.98 (3)
I2 ^{ix} —Ba2—I1 ⁱⁱⁱ	141.96 (2)	Ba2 ⁱ —I2—Ba1	70.05 (3)
I2 ^x —Ba2—I1 ⁱⁱⁱ	115.40 (4)	Ba2 ⁱⁱⁱ —I2—Ba1	100.378 (13)

I2 ^{xi} —Ba2—I1 ⁱⁱⁱ	69.600 (17)	Ba2 ^{xiii} —I2—Ba1	100.378 (13)
O—Ba2—I1 ^{iv}	84.4 (2)	Ba1 ^{ix} —O—Ba2 ^v	107.6 (3)
I2 ^{ix} —Ba2—I1 ^{iv}	141.96 (2)	Ba1 ^{ix} —O—Ba2	107.6 (3)
I2 ^x —Ba2—I1 ^{iv}	69.600 (17)	Ba2 ^v —O—Ba2	111.3 (2)
I2 ^{xi} —Ba2—I1 ^{iv}	115.40 (4)	Ba1 ^{ix} —O—Ba2 ^{vi}	107.6 (3)
I1 ⁱⁱⁱ —Ba2—I1 ^{iv}	75.81 (4)	Ba2 ^v —O—Ba2 ^{vi}	111.3 (2)
O—Ba2—I1 ^v	73.53 (11)	Ba2—O—Ba2 ^{vi}	111.3 (2)

Symmetry codes: (i) $x, y, z-1$; (ii) $y, -x+y+1, z-1/2$; (iii) $x-y, x, z-1/2$; (iv) $-x+1, -y+1, z-1/2$; (v) $-x+y, -x+1, z$; (vi) $-y+1, x-y+1, z$; (vii) $-x+y, -x+1, z-1$; (viii) $-y+1, x-y+1, z-1$; (ix) $x, y, z+1$; (x) $y, -x+y, z+1/2$; (xi) $x-y, x, z+1/2$; (xii) $-x+1, -y+1, z+1/2$; (xiii) $y, -x+y, z-1/2$.