

Modelling spontaneous propagating waves in the early retina

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Modelling spontaneous propagating waves in the early retina

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Visual system



The structure of the <u>adult</u> retina

Light



Visual cortex

The structure of the retina <u>during development</u>



What are Retinal waves?



<u>Spontaneous</u> spatio-temporal waves during development Disappear short after birth when vision is functional



(Maccione et al. 2014)

MEA recording of the voltage from a P11 mouse retina in the presence of $10 \ \mu M$ bicuculline.

The timeline of retinal waves



- Chemical synapses are not formed yet
- Electrical synapses mediated

6

segregation

Nicotinic

Acetylcholine

Receptors (nAchR)

Glutamate/AMPA

Receptors

Focusing on stage II retinal waves



Why modelling retinal waves is an interesting problem?

- Retinal waves **instruct the shaping** of the visual system
- Using biophysical modelling we could

 i) find generic principles
 ii) explain experiments and propose new ones
 leading to the better understanding of the underlying
 mechanisms of waves.
- The mathematical modelling of the dynamics of a complex biological process is a very interesting physical problem with real consequences in biology
- Understanding the mechanisms that generate them may help to **control them pharmacologically**.

Variability <u>within</u> retinal waves



Time (sec)

Zheng et al. 2006

50

Maccione et al. 2014

Waves have variable shapes due to a refractory mechanism which controls their borders. It is called sAHP (slow **A**fter**H**yper **P**olarization) for stage II.

Zheng et al. 2004

21

14

Perinatal age (d)

1. D. Matzakos-Karvouniari et al., A biophysical model explains the bursting activity in the immature retina, Nat Sci Rep, 2019

The biophysics of <u>stage II</u> retinal waves

Individual SACs burst spontaneously



Immature SACs form a transient cholinergic network



Nicotinic Acetylcholine Receptors



Mutual Excitatory synapses



A model for stage II retinal waves

Matzakos-Karvouniari et al. 2019, Lansdell et al. 2014, Hennig et al. 2009, Morris-Lecar 1981 6 variables: V, N, C, R, S, A 3 time scales: Fast, Medium, Slow Nonlinear cholinergic coupling ~30 parameters

Fast
$$\begin{bmatrix}
C_m \frac{dV_i}{dt} &= -g_L(V_i - V_L) - g_C M_{\infty}(V_i)(V_i - V_C) - g_K N_i(V_i - V_K) - g_{sAHP} R_i^4(V_i - V_K) \\
-g_A(V_i - V_A) \sum_{j \in \mathcal{B}_i} \frac{A_j^2}{\gamma_A + A_j^2}$$

$$\frac{\tau_N \frac{dN_i}{dt} &= \Lambda(V_i)(N_{\infty}(V_i) - N_i) \\
\frac{\tau_C \frac{dC_i}{dt} &= -\frac{\alpha_C}{H_X}C_i + C_0 - \delta_C g_C(V_i)(V_i - V_C) \quad \frac{dA_i}{dt} &= -\mu A_i + \beta_A T_A(V_i). \\
\frac{\tau_S \frac{dS_i}{dt} &= \alpha_S(1 - S_i)C_i^4 - S_i \\
\frac{\tau_R \frac{dR_i}{dt} &= \alpha_R S_i(1 - R_i) - R_i
\end{bmatrix}$$
Fast V, N. $\tau_L = 11 \text{ ms}, \tau_N = 5 \text{ ms}. \\
Medium C, A. \tau_C = 2 \text{ s}, \tau_A = 1.86 \text{ s}. \\
Slow S, R. \tau_R = \tau_S = 44 \text{ s}.
\end{bmatrix}$

Validating our equations by reproducing experiments



I. Equations reproduce the role of voltage-gated Ca+2 channels on fast oscillations
II. We predict that a fast potassium channel is needed to produce fast oscillations

1. D. Matzakos-Karvouniari et al., A biophysical model explains the bursting activity in the immature retina, Nat Sci Rep, 2019

Fast subsystem



Fast subsystem



Bifurcation diagram of the fast subsystem (V,N) What do we learn about SACs?

I. The SACs repertoire of dynamics upon a current application



Bifurcation diagram of the fast subsystem (V,N)

What do we learn about SACs?

I. The SACs repertoire of dynamics upon a current application



Bifurcation diagram of the fast subsystem (V,N)

What do we learn about SACs?

I. The SACs repertoire of dynamics upon a current application



What do we learn about SACs?

II. The role of sAHP for the bursting mechanism



What do we learn about SACs?

II. The role of sAHP for the bursting mechanism



The biophysical interpretation



2. D. Karvouniari et al., *Spontaneous emergence of spatio-temporal structure in the early retina*, (under preparation for Phys. Review E)

How do waves propagate?



- Full interacting waves are a complex paradigm
- Waves propagate in a landscape changing constantly
 - It is hard to extract a mechanism of propagation

A network model of stage II retinal waves





The coupled dynamics of 2 SACs



Analytic form of waves propagation coupling threshold



• For the zero order approximation we assumed that V_, R and Ω do not depend on gA. Fit holds for smaller gA

Based on our model, where wave propagation is <u>only possible</u> when the **total current received by a neighbouring cell exceeds the** (saddlenode) **bifurcation threshold**, we extract the analytic form for the waves propagation coupling threshold (1D case).

$$g_{A_c} = -\frac{2\mu\sqrt{\gamma_A}}{n_i\beta\Omega} \frac{I_{SN} + g_S R^4 (V_- - V_K)}{V_- - V_A}$$

Propagation in 1D without friction



• Around the propagation threshold, waves could stop even without friction, due to noise and the fact that the Ach current is not sufficient to fulfil the propagation condition

Propagation in 2D without friction

Approximation, free propagation no friction, all cells are at rest



0.35

0.4

2

1

0 -

0

Ò.05

0.15

0.1

0.2

gA (nS)

0.25

0.3

How do waves stop? The sAHP saga



Patterns evolve within stage II



32

Synchronisation Transition



The average and the std of the population firing rate undergo a transition at a specific range of cholinergic coupling

Synchronisation Transition

Indications for criticality in experiments

Hennig et. al 2009 also found **power law -like distributions** for the waves sizes

 Criticality is a precise concept in physics and power law distributions are not enough to characterise it

Also, criticality is not a natural state and it is achieved by **bringing the system to a specific point**

Two "critical" points:

i) Experimental data need to be analysed in a more elaborate way to reveal the actual distributions of waves characteristics
ii) If indeed there is criticality and power laws, then we miss a mechanism that brings the system to the critical point

Conclusions & Perspectives

 Analysing the dynamics of our model using dynamical systems theory leading to a main hypothesis: <u>Immature SACs are near a</u> <u>bifurcation point!</u>

Consequences:

•

- individual SACs properties*
- \cdot how SACs lose their excitability upon maturation
- \cdot explain variability of wave features across species
- wave propagation conditions*
- criticality and power laws*
- spontaneous activity could be generated by a SACs network that is optimised for input processing=dynamic range
- Future direction towards completing studying waves in a dynamically changing landscape
- Characterise criticality in our model and use the same tools to characterise experimental data
- **Proposing new experiments** based on theoretical hypothesis

Thank you all :)