

# A far-UV survey of three hot, metal-polluted white dwarf stars: WD0455–282, WD0621–376, and WD2211–495

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## ABSTRACT

Using newly obtained high-resolution data ( $R \sim 1 \times 10^5$ ) from the *Hubble Space Telescope*, and archival UV data from the *Far Ultraviolet Spectroscopic Explorer*, we have conducted a detailed UV survey of the three hot, metal-polluted white dwarfs WD0455–282, WD0621–376, and WD2211–495. Using bespoke model atmospheres, we measured  $T_{\text{eff}}$ ,  $\log g$ , and photospheric abundances for these stars. In conjunction with data from *Gaia*, we measured masses, radii, and gravitational redshift velocities for our sample of objects. We compared the measured photospheric abundances with those predicted by radiative levitation theory, and found that the observed Si abundances in all three white dwarfs, and the observed Fe abundances in WD0621–376 and WD2211–495, were larger than those predicted by an order of magnitude. These findings imply not only an external origin for the metals, but also ongoing accretion, as the metals not supported by radiative levitation would sink on extremely short time-scales. We measured the radial velocities of several absorption features along the line of sight to the three objects in our sample, allowing us to determine the velocities of the photospheric and interstellar components along the line of sight for each star. Interestingly, we made detections of circumstellar absorption along the line of sight to WD0455–282 with three velocity components. To our knowledge, this is the first such detection of multicomponent circumstellar absorption along the line of sight to a white dwarf.

**Key words:** circumstellar matter – white dwarfs – stars: individual: WD0455-282 – stars: individual: WD0621-376 – stars: individual: WD2211-495.

## 1 INTRODUCTION

White dwarf stars are ubiquitous throughout the Galaxy, and mark the final stage of evolution for main-sequence stars with masses  $< 8\text{--}10 M_{\odot}$  (Iben & Tutukov 1997). As they no longer produce heat through nuclear fusion, white dwarfs spend the rest of their lives cooling to background temperature via the emission of radiation. Through the use of calculated evolution tables, the temperature of a white dwarf can be effectively used as a means to measure how long the star has been cooling. Approximately 30–50 per cent of white dwarf stars are thought to have atmospheres polluted with metals (Barstow et al. 2014; Koester, Gänsicke & Farihi 2014) (B14 and

K14 hereafter). The mechanisms by which this pollution occurs are relatively well understood in the case of cool white dwarfs. The diffusion time-scales for metals in these cases can be of the order of days for hydrogen-rich (DA) white dwarfs with effective temperatures ( $T_{\text{eff}}$ ) ranging between  $12\,000 < T_{\text{eff}} < 20\,000$  K (Paquette et al. 2002). Therefore, for metals to be observed in the atmosphere, the reservoir of material has to be continually replenished through accretion. However, in the case of hot white dwarfs ( $T_{\text{eff}} > 20\,000$  K) the physics becomes more complex. In this case, the radiative forces in the atmosphere are efficient enough to overcome the gravitational stratification, resulting in metals such as C, N, O, and heavier being present in the photosphere through a process known as radiative levitation. In addition, as with the cool white dwarfs, accretion can also occur. Therefore, the observed photospheric abundance patterns in hot white dwarf stars will be

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a delicate balance between the flow of material sinking under gravity, the resistance to this flow from radiative levitation, and the introduction of additional material from accretion. Attempts have been made by Chayer et al. (2002b), Chayer, Fontaine & Wesemael (2002a), and Chayer et al. (2002c) (Ch94/95 hereafter) to use radiative levitation theory to predict the observed abundance patterns in white dwarf stars, however, it has often been the case that these predictions bear little resemblance to what is observed. This is a consequence of the assumptions made. In particular, Ch94/95 assumed that the reservoir of material available to be levitated was effectively infinite.

The evidence for accretion into the atmospheres of white dwarf stars is compelling. A study by K14 analysed the atmospheres of 85 white dwarf stars with  $17\,000 < T_{\text{eff}} < 27\,000$  K. From this sample, 48 out of the 85 (56 per cent) white dwarfs analysed were found to have signatures of metals in their atmospheres. Of these 48 metal-polluted white dwarfs, the photospheric compositions of 25 of these stars could be explained by radiative levitation alone. However, for the other 23 stars, K14 concluded that active accretion was taking place to account for the observed abundance patterns. B14 conducted a survey of 89 DA white dwarfs observed by the *Far Ultraviolet Spectroscopic Explorer (FUSE)* with  $16\,000 < T_{\text{eff}} < 77\,000$  K. In this sample, 33 out of 89 white dwarfs were found to have atmospheres polluted with metals. In an attempt to understand the nature of this metal pollution, the authors compared the measured photospheric abundances to those predicted by Ch94/95. Out of the 33 white dwarfs considered, 12 were found to have enhanced Si abundances relative to the predicted radiative levitation abundances, implying an external origin. Further investigating this, B14 looked at the ratios of abundances for each star, such as Si/C, Si/P, and Si/S. The authors then compared these ratios to those seen in bulk-Earth material, in CI chondrites, and in the Sun. It was shown that the white dwarf Si/C ratios were similar to those observed in CI chondrite material, further implying that metal pollution in hot white dwarf stars originates from rocky bodies.

In the case of cooler white dwarfs ( $T_{\text{eff}} < 20\,000$  K) where radiative levitation is inefficient, comparing photospheric abundance ratios such as C/O to those observed in other types of media allows the origin of the material to be inferred. Wilson et al. (2016) measured the photospheric compositions of 16 white dwarf stars with  $17\,000 < T_{\text{eff}} < 23\,000$  K and calculated the C/O ratio for each object. The authors found that four of these objects had C/O ratios coincident with that observed in bulk-Earth material, and five of these objects had C/O ratios coincident with that observed in chondrite material. Other authors have also used this technique to study the compositions of accreted material such as Kawka & Vennes (2016), Zuckerman et al. (2011), and Xu et al. (2014). As well as photospheric abundance measurements for cool white dwarfs, observational data have revealed the presence of dusty debris discs orbiting white dwarf stars. An excellent example of this is the metal-polluted white dwarf SDSS 1228+1040. Using time-resolved spectroscopic data from the William Herschel Telescope, Gänsicke et al. (2006) detected emission features from the Ca II triplet with laboratory wavelengths 8498, 8542, and 8662 Å. The authors also found that this emission did not vary over time-scales of 20 min to 1 d. The authors concluded that this emission arose from a gaseous circumstellar disc around the white dwarf. More exotic cases of debris discs have been observed, such as that of WD1145+017. Using high-cadence photometry, Vanderburg et al. (2015) made the surprising discovery that not only did WD1145+017 have a debris disc, this disc was found to be composed of several disintegrating

objects. As this debris transits the white dwarf, it causes the star's brightness to dim by up to 40 per cent. Further studies such as those by Rappaport et al. (2016), Gänsicke et al. (2016), Xu et al. (2016), and Croll et al. (2015) have focused on characterizing the type and compositions of the objects orbiting WD1145+017. Most recently, new observations by Manser (2019) of SDSS 1228+1040 have revealed the presence of an Fe-core planetesimal orbiting the white dwarf.

The extensive literature concerning the accretion of metals on to cool white dwarf stars is compelling. However, the question of the origin of metal pollution in hot white dwarfs is still an open question. In this paper, we present our photospheric and interstellar survey of three hot, DA white dwarf stars, namely WD0455–282, WD0621–376, and WD2211–495. First, we describe new *Hubble Space Telescope* observations obtained for the three white dwarfs, as well as archival *FUSE* data. We then describe the model atmosphere calculations performed, and how these were used to measure the effective temperature, surface gravity, and photospheric compositions of the stars. We then conduct a line survey of the three objects, and identify the velocity populations present along the line of sight to the white dwarfs. We then discuss the results obtained, and consider the photospheric compositions of the white dwarfs in the context of radiative levitation. We also discuss the results of the interstellar survey. Lastly, we make concluding remarks, and detail the future work planned.

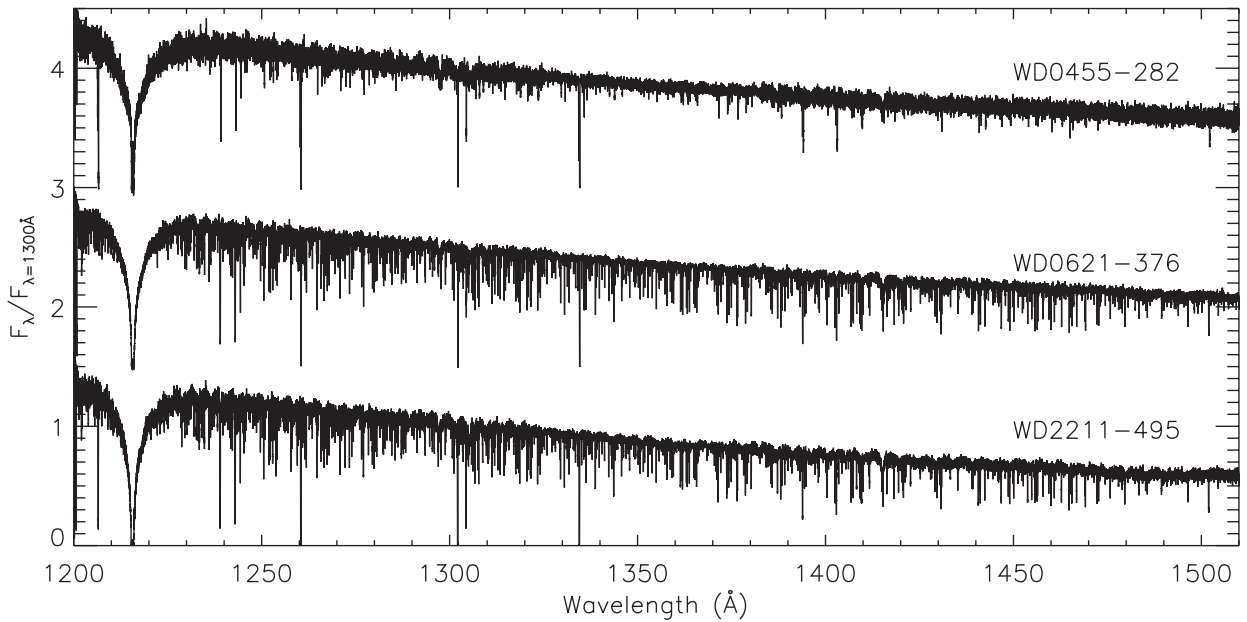
## 2 OBSERVATIONS

WD0455–282, WD0621–376, and WD2211–495 were observed using the Space Telescope Imaging Spectrometer (STIS) aboard the *Hubble Space Telescope* as part of programme GO-14791. Each star was observed using the E140H FUV/MAMA echelle grating (nominal resolution  $R = \lambda/\Delta\lambda \sim 1 \times 10^5$ , Martin & Baltimore 2012), with a  $0.2 \times 0.2$  aperture. The aperture size was chosen so as to maximize the flux throughput. Further, special, deeper than normal, exposures of the wavelength calibration lamp were taken to aid in the assignment of precise wavelength scales. The STIS echellegram reduction and co-addition procedures we adopted have been fully described in a previous paper (Hu et al. 2018). In brief, the raw spectral data sets were processed through a version of the STIS pipeline with a number of specially updated reference files, including new dispersion solutions for the specific grating settings used. The individual echelle orders of the processed echellegrams were then concatenated, imposing an active blaze correction to ensure optimum flux continuity across the overlapping zones of the adjacent orders. If multiple subexposures were taken in a given grating setting, these were co-added after aligning relative to the leading spectrum by cross-correlation. Finally, the overlapping regions between the two separate grating settings (1307 and 1416 Å) were adjusted to match the fluxes and again aligned in wavelength by cross-correlation. The alignment shifts typically were small, often only  $0.1 \text{ km s}^{-1}$  in magnitude. The final wavelength coverage for the spliced spectra was approximately 1200–1520 Å. The average signal-to-noise ratio per resolution element ( $\sim 3 \text{ km s}^{-1}$ ) in the co-added spectra ranged from about 35 (WD0455–282) to 60–70 (WD2211–495 and WD0621–376, respectively). We summarize the STIS observations for each star in Table 1, and plot the STIS spectra of each object in Fig. 1.

To complement our STIS observations, and provide a means with which to measure the effective temperature ( $T_{\text{eff}}$ ) and surface gravity ( $\log g$ ) for the three objects, we constructed high signal-to-noise spectra using archival observations from the *FUSE*. We summarize

**Table 1.** List of spectral data sets obtained from the *HST* for each object using STIS with the E140H grating.  $\lambda_c$  is the central wavelength of the exposure. The start time is given in the Universal Time Zone (UT).

Object	Observation ID	Start time/Date	$\lambda_c$ (Å)	Exposure time (s)
WD0455–282	OD7QD0IUQ	05:43:21 15/08/2017	1307	2487.0
	OD7QD0JDQ	07:15:40 15/08/2017	1307	2964.0
	OD7QD0JHQ	08:51:06 15/08/2017	1307	2964.0
	OD7QD1010	10:29:50 15/08/2017	1416	2487.0
	OD7QD1020	12:02:00 15/08/2017	1416	2964.0
	OD7QD1030	13:37:26 15/08/2017	1416	2964.0
WD0621–376	OD7QC0H5Q	02:40:08 10/10/2017	1307	2525.0
	OD7QC0HRQ	04:04:42 10/10/2017	1307	3002.0
	OD7QC0030	05:42:08 10/10/2017	1416	2881.0
	OD7QC0030	07:15:33 10/10/2017	1416	3002.0
WD2211–495	OD7QA0MRQ	05:49:44 15/10/2017	1307	2610.0
	OD7QA0020	07:19:07 15/10/2017	1416	2966.0



**Figure 1.** STIS spectra obtained for WD0455–282, WD0621–376, and WD2211–495. The spectra have been normalized by the flux at 1300 Å, and offset from each other for clarity.

the *FUSE* exposures used in this work in Table 2, and plot the *FUSE* spectra for each object in Fig. 2. Unlike STIS, which uses echelle-blaze optics, *FUSE* used four individual mirrors to reflect light on to two detectors, resulting in eight individual spectra (see Moos et al. 2002). Collectively, these exposures spanned 905–1184 Å, and encompassed the H-Lyman series from Ly  $\beta$ , down to the Lyman limit ( $\sim 911$  Å). There were three apertures available for use. These were the LWRS (low resolution, 30 arcmin  $\times$  30 arcmin), MDRS (medium resolution, 4 arcmin  $\times$  20 arcmin), and HIRS (high resolution, 1.25 arcmin  $\times$  20 arcmin) apertures with resolutions ranging from 15 000 to 21 000. After *FUSE* launched, it became evident that there were distortions present in the optical design, caused by heating and cooling of the individual components. This resulted in the eight spectra having different wavelength shifts. In addition, these distortions meant that the object being observed often drifted out of the field of view when the MDRS and HIRS apertures were used. This resulted in the flux of the observed spectra being attenuated by arbitrary amounts. Therefore, when constructing the spectra for this work, we only included observations where the LWRS aperture was

used where possible. In the case of WD0455–282 where MDRS observations were used, we omitted exposures where the flux was attenuated, or where there was no flux at all.

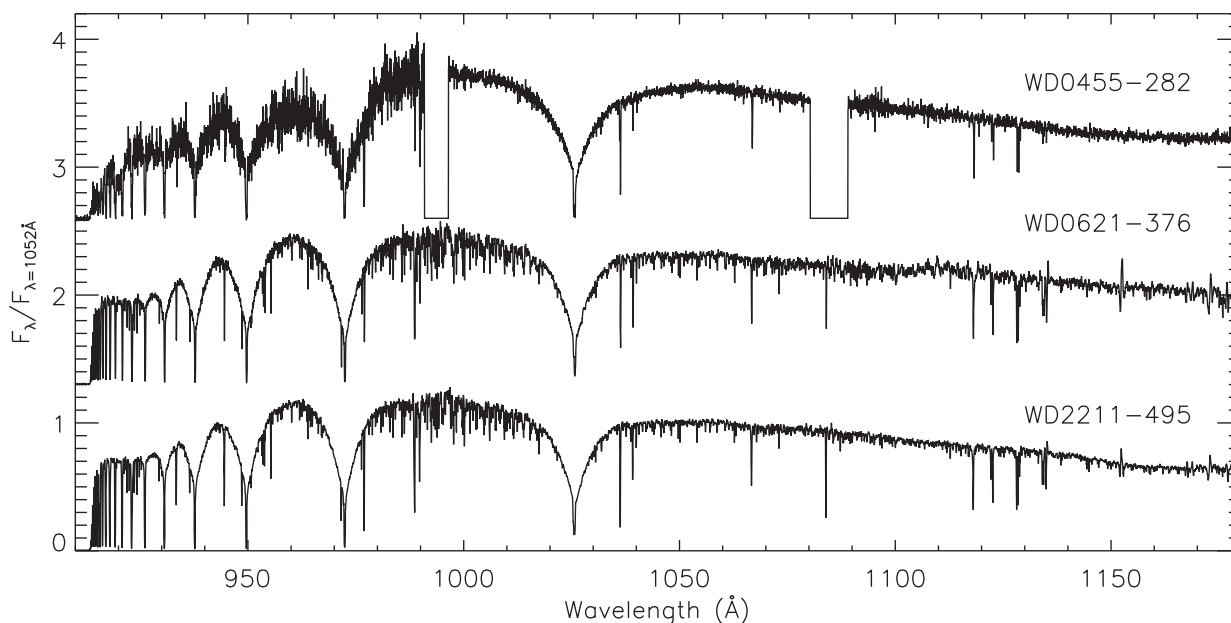
We note that, in addition to the *FUSE* and *HST* data sets, there also exists UV spectroscopy from the *International Ultraviolet Explorer* (*IUE*), with a resolution  $\sim 1 \times 10^4$ . The *IUE* data for the three objects considered in this paper were analysed by Holberg et al. (2002), who catalogued the various absorption features observed in their respective spectra. We opt not to use these *IUE* data in favour of the higher resolution *FUSE* and STIS data described hitherto.

### 3 STELLAR ATMOSPHERE MODELS

All model atmospheres described in this paper were calculated using the non-LTE model atmosphere code TLUSTY, version 201 (Hubeny 1988; Hubeny & Lanz 2002). Synthetic spectra were then generated from these model atmospheres using SYNSPEC Hubeny & Lanz (2011). These spectra spanned 900–1600 Å, and were convolved with an instrumental Gaussian profile whose FWHM (full width at

**Table 2.** List of spectral data sets obtained from *FUSE* for each object. The start time is given in the Universal Time Zone (UT).

Object	Observation ID	Exposures	Start time/Date	Aperture	Exposure time (s)
WD0455–282	P10411010	15	02:14:28 03/02/2000	MDRS	19 667.0
	P10411020	8	05:07:49 04/02/2000	MDRS	10 122.0
	P10411020	13	09:36:51 07/02/2000	MDRS	17 675.0
WD0621–376	P10415010	19	05:28:58 06/12/2000	LWRS	8371.0
WD2211–495	M10303020	5	17:18:58 21/10/1999	LWRS	2720.0
	M10303030	9	19:43:40 25/10/1999	LWRS	4160.0
	M10303040	7	21:45:44 01/11/1999	LWRS	2976.0
	M10303050	11	06:55:16 03/06/2000	LWRS	5157.0
	M10303060	8	05:15:34 29/06/2000	LWRS	4193.0
	M10303070	12	20:43:02 17/08/2000	LWRS	5260.0
	M10303080	9	06:09:32 24/10/2000	LWRS	3954.0
	M10303090	11	09:29:25 24/10/2000	LWRS	5025.0
	M10303100	9	12:49:19 24/10/2000	LWRS	5795.0
	M10303110	13	05:28:46 25/10/2000	LWRS	5877.0
	M10303120	11	10:28:36 25/10/2000	LWRS	5430.0
	M10303130	8	04:07:07 01/08/2002	LWRS	3796.0
	M10303140	7	14:23:40 10/06/2002	LWRS	3774.0
	M10303150	10	17:20:00 25/09/2002	LWRS	5460.0
	M10303160	13	23:28:41 24/05/2002	LWRS	6929.0
	M10303180	12	04:14:39 17/09/2003	LWRS	5875.0
	M10315010	7	18:26:46 07/05/2004	LWRS	3699.0
M10315040	7	17:27:33 06/07/2004	LWRS	3889.0	


**Figure 2.** *FUSE* spectra obtained for WD0455–282, WD0621–376, and WD2211–495. The spectra have been normalized by the flux at 1052 Å, and offset from each other for clarity.

half-maximum) was dependent upon the observational data being considered. For *FUSE* data, the FWHM was set to 0.0641 Å, and for the STIS data the FWHM was calculated as  $\lambda/114\,000$  as given in the STIS instrument manual. The H-Lyman absorption profiles were calculated using the Stark Broadening tables of Tremblay & Bergeron (2009). These tables are an updated version of the tables presented in Lemke (2003), including non-ideal effects such as those resulting from perturbations to the absorber due to protons and electrons.

Given the high temperature of the white dwarf stars considered, we have created new model ions for C, N, O, Si, P, and S to

account for the presence of higher ionization states. For the model atmospheres calculated, we include model ions for C I–V, N I–VI, O I–VII, Si I–VIII, P I–VIII, S I–VIII, Fe III–VII, and Ni III–VII. In addition, we also include single-level ions for C VI, N VII, O VIII, Si IX, P IX, S IX, Fe VIII, and Ni VIII.

Full line-blanketing effects for  $> 9000\,000$  transitions of Fe and Ni are accounted for via the opacity sampling method. For Fe, the atomic data including energy levels and transitions originate from Kurucz (1992), and the photoionization cross-sections (PICSS) from the Opacity Project (Seaton et al. 2014). For Ni, the atomic data also originate from Kurucz (1992), and the PICSS for Ni VII were

calculated using a hydrogenic approximation. For Ni IV–VI, we use the PICs calculated by Preval et al. (2017).

## 4 METHODOLOGY

### 4.1 General photospheric parameter measurement

It is currently untenable to calculate model atmosphere grids that can account for variations in  $T_{\text{eff}}$ ,  $\log g$ , and all of the individual abundances simultaneously. To do so would require the calculation of thousands, if not millions, of stellar atmospheric models that incorporate the various possible permutations of these variables. Therefore, for each star, we adopted an iterative procedure to determine the best-fitting values of these parameters. First, we calculated a starting NLTE model atmosphere with TLUSTY using values of  $T_{\text{eff}}$ ,  $\log g$ , and metal abundances from Barstow et al. (2003) and B14. Then, for each metal abundance we wanted to measure, we used SYNPEC to calculate a grid of model atmospheres with different abundances by stepping away from the starting model in LTE. We then measured the abundances using these grids. Once we measured the abundances, we used TLUSTY to calculate a NLTE model atmosphere grid with these abundances, varying in  $T_{\text{eff}}$  and  $\log g$ . We then measured  $T_{\text{eff}}$  and  $\log g$  using the H-Lyman lines. After measuring  $T_{\text{eff}}$  and  $\log g$ , we calculated a NLTE model atmosphere using the measured  $T_{\text{eff}}$ ,  $\log g$ , and metal abundances. We then repeated the aforementioned steps until the measured  $T_{\text{eff}}$ ,  $\log g$ , and metal abundances were converged. Our convergence criterion was defined such that the difference between the parameters measured in the previous and current iterations was less than their measurement uncertainties. In total, we performed seven iterations for WD0455–282, and six iterations for WD0621–376 and WD2211–495. Below, we describe how the metal abundances,  $T_{\text{eff}}$ , and  $\log g$  were measured in more detail.

### 4.2 $T_{\text{eff}}$ , $\log g$ , and abundance measurements

In Table 3, we list the transitions used to measure the abundances of C, N, O, Si, P, S, Fe, and Ni. Fe and Ni are difficult metals for which to measure an abundance. This is because the atomic data can be quite uncertain with respect to their centroid wavelengths, broadening parameters, and oscillator strengths. In an attempt to mitigate this, we used 8–10 Fe V and Ni V transitions, and simultaneously fit all of these lines to find the best abundance value. We note that for our abundance determinations we use only one ionization state per ion. Generally, wherever possible, we have tried to use lines arising from transitions between excited states. This is because resonant transitions have been known to be accompanied by high-ionization state interstellar medium (ISM) lines (also termed ‘circumstellar’, see Bannister et al. 2003; Dickinson, Barstow & Hubeny 2012), which can potentially compromise the abundance measurement. We discuss the lines used, and the reason why they were used here. In the case of C, only the C III transitions were visible in the spectra considered. For N, the N IV multiplet is present at 912–915 Å, however, these lines are in a region of spectrum where the signal-to-noise is suboptimal. In addition, the multiplet is contaminated by interstellar H. Therefore, we opt to use only the N V doublet. For O, there are three O IV lines and one O V line (~1371 Å) that can be used. In this case, we opted to use the O IV lines simply because there were more lines to use. For Si, the Si III ionization state has a low population relative to Si IV due to the temperatures of the objects considered (> 60 000 K). For P, the P V ionization state is the most populated relative to P IV, again

**Table 3.** List of transitions used to measure the photospheric abundances of the three white dwarfs considered. Transitions with wavelengths in the STIS range (1200–1520 Å) were used to measure the photospheric velocity.

Ion	Wavelength (Å)	$\log gf$	Extracted region (Å)
C III	1174.933	−0.468	1170–1180
C III	1175.263	−0.565	1170–1180
C III	1175.590	−0.690	1170–1180
C III	1175.711	0.009	1170–1180
C III	1175.987	−0.565	1170–1180
C III	1176.370	−0.468	1170–1180
C III	1247.383	−0.314	1245–1255
N V	1238.821	−0.505	1235–1245
N V	1242.804	−0.807	1235–1245
O IV	1338.615	−0.632	1335–1350
O IV	1342.990	−1.333	1335–1350
O IV	1343.514	−0.380	1335–1350
Si IV	1122.485	0.220	1115–1130
Si IV	1128.340	0.470	1115–1130
Si IV	1393.755	0.030	1390–1405
Si IV	1402.770	−0.280	1390–1405
P V	1117.977	−0.010	1115–1130
P V	1128.008	−0.320	1115–1130
S V	1501.760	−0.489	1495–1505
Fe V	1320.409	0.243	1315–1325
Fe V	1387.937	0.660	1385–1395
Fe V	1402.385	0.229	1390–1405
Fe V	1430.572	0.597	1425–1435
Fe V	1440.528	0.448	1440–1450
Fe V	1446.617	0.468	1440–1450
Fe V	1448.847	0.309	1440–1450
Fe V	1455.555	0.277	1450–1460
Fe V	1456.162	0.173	1450–1460
Fe V	1464.686	0.471	1460–1470
Ni V	1257.626	0.585	1255–1265
Ni V	1261.760	0.478	1255–1265
Ni V	1273.204	0.395	1265–1275
Ni V	1279.720	0.300	1275–1290
Ni V	1300.979	−0.048	1295–1305
Ni V	1307.603	0.168	1305–1315
Ni V	1318.515	0.307	1315–1325
Ni V	1336.136	0.557	1335–1345
Ni V	1342.176	0.345	1335–1345

due to the temperatures of the objects considered. For S, the S VI resonant transitions are detected at 933 and 945 Å. However, these lines are in close proximity to Ly  $\delta$  and Ly  $\epsilon$ , meaning that they are sensitive to the wings of these H lines. In addition, abundance measurements made using these S VI lines have been shown to be in great disagreement with measurements made using S IV and S V (see, for example, Preval et al. 2013). Lastly, for Fe and Ni, the strongest lines come from Fe V and Ni V. Only a few Fe/Ni VI lines are visible in the spectrum that could potentially be used. Therefore, we opted to use the Fe/Ni V lines due to the number of these lines available.

The STIS spectra used in this work have >50 000 data points. Reading in and fitting all of these data points are very computationally demanding. Therefore, we opted to fit individual transitions by extracting a section of spectrum encompassing the feature we want to measure. The wavelength regions extracted for each transition were the same for all three stars, and are listed in Table 3. To measure the individual metal abundances, we used the X-ray spectral analysis package XSPEC (Arnaud 1996), which uses a  $\chi^2$  minimization procedure to interpolate a model grid to the observed

data, and determine the best-fitting values for these parameters with the reduced  $\chi^2$  value ( $\chi_{\text{red}}^2$ ) being as close to unity as possible. To ensure we obtained the best-fitting abundance values, we calculated  $\chi_{\text{red}}^2$  over all abundance values in the model grid.

To measure the  $T_{\text{eff}}$  and  $\log g$  of each star, we first extracted wavelength regions from *FUSE* spectra encompassing four Lyman lines, namely Ly  $\beta$ , Ly  $\gamma$ , Ly  $\delta$ , and Ly  $\epsilon$ . Ly  $\alpha$  is present in the STIS data, however, this line cannot be used to measure  $T_{\text{eff}}$  and  $\log g$  due to contamination from interstellar H absorption. In the extracted spectra, we removed erroneous photospheric and interstellar absorption features. We then used XSPEC to interpolate our  $T_{\text{eff}}/\log g$  model grids to the Lyman lines.

The statistical uncertainties on the abundances,  $T_{\text{eff}}$ , and  $\log g$  were determined by considering the change in  $\chi^2$ . For the abundances, the uncertainties were obtained by reading off the abundance values for which  $\Delta\chi^2 = 1$  corresponding to a  $1\sigma$  confidence interval for one variable parameter. It should be noted that the abundance uncertainties do not account for the uncertainty in the  $T_{\text{eff}}$  and  $\log g$  measurement. This is because in the iteration scheme,  $T_{\text{eff}}$  and  $\log g$  are held fixed for abundance measurements. For  $T_{\text{eff}}$  and  $\log g$ , the uncertainties were calculated by reading off the  $T_{\text{eff}}$  and  $\log g$  values for which  $\Delta\chi^2 = 2.2957$  corresponding to a  $1\sigma$  confidence interval for two variable parameters. The statistical uncertainties on quantities measured in this work are dependent upon the uncertainty on the observed flux. In the case of *FUSE* data, the uncertainty on the observed flux can be greatly underestimated due to calibration issues with the instruments (Moos et al. 2002). Therefore, to determine the uncertainties on quantities measured using *FUSE* data, a few additional steps were required. First, we fit the observed data by interpolating the model grids with XSPEC. This results in a  $\chi_{\text{red}}^2$  value not equal to unity. Then, we expressed the flux uncertainties as a fractional percentage of the observed flux (e.g. 2.5 per cent). We then varied this fractional percentage so as to obtain a  $\chi_{\text{red}}^2$  of unity. We then determined the uncertainty on the relevant quantities by reading off the  $T_{\text{eff}}/\log g$  values corresponding to  $\Delta\chi^2 = 2.2957$ , and the abundance values corresponding to  $\Delta\chi^2 = 1.0$ .

### 4.3 Astrophysical and astrometric quantities

With the second data release from the astrometric observatory *Gaia*, the positions and parallaxes of hundreds of thousands of white dwarfs are now known to milli- and micro-arcsecond precision. Using parallax data information from *Gaia*, the observed STIS spectrum, and our best-fitting synthetic spectrum, we can measure the radius  $R_*$  of the white dwarf. The distance  $D$  in parsecs to the white dwarf is calculated as  $\bar{\omega}$ :

$$D = \frac{1000}{\bar{\omega}}, \quad (1)$$

where  $\bar{\omega}$  is the parallax in milliarcseconds. Then,  $R_*$  is calculated as

$$R_* = D \sqrt{\frac{F_\lambda}{4\pi H_\lambda}}, \quad (2)$$

where  $F_\lambda$  is the observed flux, and  $H_\lambda$  is the Eddington flux as obtained from the synthetic spectrum of the white dwarf in question.  $F_\lambda$  and  $H_\lambda$  are functions of wavelength. Therefore, we adopted a statistical approach to find the best value for  $F_\lambda/H_\lambda$ . First, we extracted a region of spectrum from the synthetic and observed data sets where there were relatively few absorption features. We found that the region 1480–1500 Å is suitable. We then calculated the

**Table 4.** List of transitions used to measure the ISM velocities along the line of sight to the white dwarfs.

Ion	Wavelength (Å)	$\log gf$
N I	1200.223 29	−0.4589
N I	1200.709 81	−0.7625
Si III	1206.4995	0.2057
Si II	1260.4221	0.3911
O I	1302.168 48	−0.6195
Si II	1304.3702	−0.7329
C II	1334.5323	−0.5912

mean value of  $F_\lambda/H_\lambda$ , weighted by their reciprocal squared errors. This value was then used to determine  $R_*$ . With  $R_*$  and  $\log g$ , we can then determine the mass of the white dwarf,  $M_{\text{WD}}$ , calculated as

$$M_{\text{WD}} = \frac{g R_*^2}{G}, \quad (3)$$

where  $G$  is the universal gravitational constant. Finally, with the mass and radius, we can then find the gravitational redshift  $z_{\text{gr}}$ . In velocity units, the redshift,  $V_{\text{gr}}$ , is calculated as

$$V_{\text{gr}} = cz_{\text{gr}} = \frac{GM_*}{cR_*}, \quad (4)$$

where  $c$  is the speed of light.

### 4.4 Velocity measurements

The exceptional calibration and resolution of STIS allow for the precise measurement of the photospheric (or radial) and interstellar velocities of the three white dwarfs. When measuring the abundances of the various metal absorption features, XSPEC shifts the synthetic spectrum in wavelength space to find the best fit to the data. To measure the photospheric velocity, we calculate the average velocity of all the transitions in the STIS data listed in Table 3. The uncertainty in the velocity measurement is then determined by calculating the standard deviation of the velocities.

Again, thanks to the high resolution of the STIS spectra, it is possible to separate blended ISM features into their individual components. While a detailed study of these features quantifying column densities and temperatures is beyond the scope of this work, we do, however, measure the velocities of these features. To measure the velocities of the ISM lines, we fit Gaussian profiles to the observed absorption features, parametrized by the wavelength centroid, the absorption depth, and the Doppler width. The exact parametrization is given in the Appendix. The advantage to the profile used is that it can account for line saturation. The best-fitting parameters were determined by using a  $\chi^2$  minimization procedure as implemented in the IDL package MPFIT (Markwardt 2009). The interstellar velocity was measured by calculating the average of the measured velocities of the lines listed in Table 4, weighted by their inverse square errors. The uncertainty on the weighted ISM component was determined by calculating the standard deviation of the measured velocities. When we found evidence of multiple component ISM absorption, we calculated the average velocities of lines with similar velocities. We note that there are ISM lines that exist in the *FUSE* spectra of our objects. However, we opted not to use these lines in our velocity measurements due to the lower accuracy wavelength calibration in the *FUSE* spectra.

## 5 RESULTS – PHOTOSPHERIC SURVEY

In this section, we present the results of our photospheric survey. Using the lines listed in Table 3, we measured a photospheric velocity of  $81.5 \pm 1.9$ ,  $37.4 \pm 1.8$ , and  $30.0 \pm 1.7$  km s<sup>-1</sup> for WD0455–282, WD0621–376, and WD2211–495 respectively. In Table 5, we summarize the measured stellar parameters for each star, including  $T_{\text{eff}}$ ,  $\log g$ ,  $M_*$ ,  $R_*$ , and the photospheric abundances. The abundances are expressed as number fractions of hydrogen. All uncertainties quoted are to  $1\sigma$ . In this section, we first discuss the abundance measurements made for each species detected in the three white dwarfs. We then present measurements for  $T_{\text{eff}}/\log g$  for each star. In conjunction with data from the astrometric satellite *Gaia*, we then give direct measurements of the distances, masses, radii, and gravitational redshifts for each object.

### 5.1 C abundance

In Fig. 3, we have plotted the *FUSE* spectra of the three white dwarfs spanning 1174–1178 Å, which contains the C III multiplet transition. Interestingly, we find no traces of this multiplet in the spectrum of WD0455–282. Therefore, we place a limit on the photospheric C abundance in this star of  $<1.00 \times 10^{-8}$ . The C III multiplet is only just visible in the cases of WD0621–376 and WD2211–495. As mentioned previously, the uncertainties for the *FUSE* data are unreliable. Therefore, when measuring the C abundance, we expressed the flux uncertainty as a fraction of the observed flux so as to achieve a fit with  $\chi_{\text{red}}^2$  close to unity. We measure photospheric C abundances of  $1.49^{+0.08}_{-0.08} \times 10^{-6}$  and  $5.05^{+0.55}_{-0.55} \times 10^{-7}$  for WD0621–376 and WD2211–495, respectively.

### 5.2 N abundance

In Fig. 4, we have plotted a region of the STIS spectra for the three white dwarfs containing the N V doublet. We detected the N IV multiplet in the *FUSE* spectra at 914–918 Å for all three stars, however, the signal-to-noise in this region was too low to measure an accurate abundance. The N V doublet is clearly resolved in all three stars, and we measure N abundances of  $7.71^{+0.21}_{-0.21} \times 10^{-8}$ ,  $6.45^{+0.12}_{-0.12} \times 10^{-7}$ , and  $1.49^{+0.05}_{-0.05} \times 10^{-6}$  for WD0455–282, WD0621–376, and WD2211–495, respectively.

### 5.3 O abundance

In Fig. 5, we have plotted the region of STIS spectrum containing two of the O IV transitions used to measure the O abundance for WD0455–282, WD0621–376, and WD2211–495. The O V line at 1371 Å was also detected, however, we opted to use the O IV lines as there were three lines to fit. We measured O abundances of  $1.58^{+0.12}_{-0.12} \times 10^{-7}$ ,  $2.46^{+0.03}_{-0.03} \times 10^{-6}$ , and  $2.00^{+0.03}_{-0.03} \times 10^{-6}$  for WD0455–282, WD0621–376, and WD2211–495, respectively. In Fig. 6, we have plotted a region of STIS spectrum containing the O V 1371.296 Å line for the three white dwarfs. Excellent agreement is seen between the synthetic and observed spectrum for WD0621–376. However, for WD0455–282 and WD2211–495 it can be seen that the synthetic profile for O V does not descend all the way into the observed profile. This implies that the  $T_{\text{eff}}$  may be underestimated for these stars. This may be due to our convergence criteria being too relaxed, where iterations of  $T_{\text{eff}}$ ,  $\log g$ , and abundance measurements were performed until the difference between the previous and current measurements was less than the uncertainty on the measurement.

### 5.4 Si abundance

In Fig. 7, we have plotted the region of STIS spectrum containing the resonant Si IV doublet for WD0455–282, WD0621–376, and WD2211–495. In addition to the STIS data, we also used two excited Si IV absorption features from the *FUSE* spectrum. As was the case with the C III transition, we expressed the *FUSE* flux uncertainty as a fraction of the observed flux so as to achieve a fit with  $\chi_{\text{red}}^2$  close to unity. We measured Si abundances of  $9.18^{+0.29}_{-0.29} \times 10^{-7}$ ,  $8.75^{+0.18}_{-0.19} \times 10^{-6}$ , and  $4.38^{+0.15}_{-0.15} \times 10^{-6}$  for WD0455–282, WD0621–376, and WD2211–495, respectively. We note that our Si abundance measurements for WD0621–376 and WD2211–495 are an order of magnitude larger than that of B14, who measured  $7.57^{+0.31}_{-0.31} \times 10^{-7}$  and  $2.41^{+5.21}_{-2.04} \times 10^{-7}$ , respectively. For WD0621–376, we defer discussion until later in the paper. However, in the case of WD2211–495 this large difference may be due to the higher quality observational data used in this work. For a comparison, B14 used a *FUSE* spectrum constructed with one data set (M10303160), whereas this work uses a *FUSE* spectrum with 18 data sets (see Table 2).

### 5.5 P abundance

In Fig. 8, we have plotted the region of *FUSE* spectra for the three white dwarfs that contains the P V resonant doublet. As was the case for the C III multiplet, we expressed the flux uncertainties in the *FUSE* data as a fraction of the observed flux so as to achieve a fit with  $\chi_{\text{red}}^2$  close to unity. We measured the photospheric P abundance to be  $7.58^{+0.46}_{-0.46} \times 10^{-8}$ ,  $1.70^{+0.16}_{-0.16} \times 10^{-7}$ , and  $1.73^{+0.07}_{-0.07} \times 10^{-7}$  for WD0455–282, WD0621–376, and WD2211–495, respectively.

### 5.6 S abundance

In Fig. 9, we have plotted the region of STIS spectrum containing the excited S V transition for the three white dwarfs. The resonant S VI doublet is detected in the *FUSE* spectra, however, we opted not to use these for abundance measurements. This is because they are situated close to the line centroids of the Lyman series where the wings are changing rapidly, meaning the abundance will be sensitive to the broadening of the Lyman lines. We measured an S abundance of  $2.70^{+0.25}_{-0.25} \times 10^{-7}$ ,  $1.05^{+0.15}_{-0.06} \times 10^{-6}$ , and  $8.06^{+0.46}_{-0.47} \times 10^{-7}$  for WD0455–282, WD0621–376, and WD2211–495, respectively.

### 5.7 Fe abundance

In Fig. 10, we have plotted a region of the STIS spectrum containing two of the Fe V lines used to measure the Fe abundance in the three white dwarfs. We measured Fe abundances of  $2.72^{+0.11}_{-0.11} \times 10^{-6}$ ,  $1.84^{+0.04}_{-0.04} \times 10^{-5}$ , and  $1.21^{+0.04}_{-0.04} \times 10^{-5}$  for WD0455–282, WD0621–376, and WD2211–495, respectively. In Fig. 11, we have also plotted a region of STIS spectrum containing three Fe VI absorption features with laboratory wavelengths 1295.817, 1296.734, and 1296.872 Å, respectively, for the three white dwarfs. As with the case of O V, excellent agreement is seen between the observed and synthetic spectra for WD0621–376, while the synthetic spectra for WD0455–282 and WD2211–495 do not descend completely into the observed spectrum.

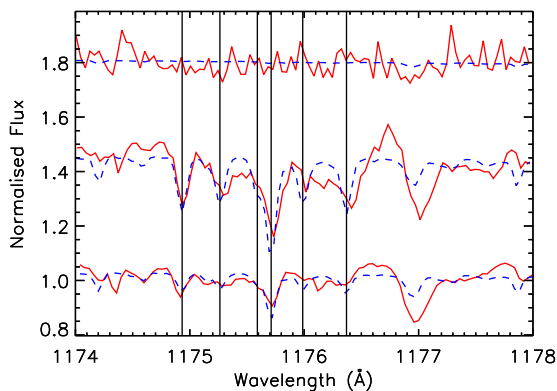
### 5.8 Ni abundance

In Fig. 12, we have plotted a region of the STIS spectrum containing one of the Ni V features used to measure the Ni abundance in the

**Table 5.** List of measured parameters for WD0455–282, WD0621–376, and WD2211–495. RA, Dec,  $G$ ,  $G_{BP}$ ,  $G_{RP}$ , and Parallax data taken from *Gaia* DR2. Note that the RA/Dec coordinates are in the ICRS reference, and the epoch is J2015.5. Bolometric magnitudes and cooling ages were determined using the Montreal Cooling tables (see Holberg & Bergeron 2006).

Parameter	WD0455–282	WD0621–376	WD2211–495
$T_{\text{eff}}$ (K)	$65\,400^{+1240}_{-1210}$	$64\,500^{+437}_{-424}$	$65\,900^{+259}_{-254}$
Log $g$ (cgs)	$7.87^{+0.09}_{-0.09}$	$7.60^{+0.03}_{-0.03}$	$7.58^{+0.02}_{-0.02}$
$v_{\text{phot}}$ (km s $^{-1}$ )	$81.5 \pm 1.9$	$37.4 \pm 1.8$	$30.0 \pm 1.7$
RA (deg)	$74.305\,75 \pm 0.253\,88$	$95.802\,94 \pm 0.047\,20$	$333.549\,73 \pm 0.042\,32$
Dec (deg)	$-28.131\,27 \pm 0.313\,15$	$-37.691\,13 \pm 0.057\,33$	$-49.324\,51 \pm 0.061\,89$
<i>Gaia</i> $G$	$13.915 \pm 0.002$	$12.041 \pm 0.002$	$11.610 \pm 0.002$
<i>Gaia</i> $G_{BP}$	$13.651 \pm 0.009$	$11.789 \pm 0.013$	$11.315 \pm 0.007$
<i>Gaia</i> $G_{RP}$	$14.236 \pm 0.003$	$12.382 \pm 0.003$	$11.951 \pm 0.002$
Johnson $V$	$13.901 \pm 0.023^a$	$12.063 \pm 0.020^a$	$11.667 \pm 0.031^a$
$M_{\text{Bol}}$	$3.220 \pm 0.190$	$2.778 \pm 0.064$	$2.641 \pm 0.042$
Cooling age (Myr)	$0.96 \pm 0.07$	$0.82 \pm 0.03$	$0.76 \pm 0.02$
Parallax (mas)	$8.237 \pm 0.354$	$13.136 \pm 0.059$	$16.992 \pm 0.082$
Distance (pc)	$121 \pm 5$	$76.1 \pm 0.3$	$58.9 \pm 0.3$
Mass ( $M_{\odot}$ )	$0.589 \pm 0.145$	$0.731 \pm 0.053$	$0.575 \pm 0.028$
Radius ( $R_{\odot}/100$ )	$1.48 \pm 0.06$	$2.24 \pm 0.01$	$2.04 \pm 0.01$
$V_{\text{grav}}$ (km s $^{-1}$ )	$25.4 \pm 6.3$	$20.7 \pm 1.5$	$18.0 \pm 0.9$
N(C)/N(H)	$1.00 \times 10^{-8}$	$1.49^{+0.08}_{-0.08} \times 10^{-6}$	$5.05^{+0.55}_{-0.55} \times 10^{-7}$
N(N)/N(H)	$7.71^{+0.21}_{-0.21} \times 10^{-8}$	$6.45^{+0.12}_{-0.12} \times 10^{-7}$	$1.49^{+0.05}_{-0.05} \times 10^{-6}$
N(O)/N(H)	$1.58^{+0.12}_{-0.12} \times 10^{-7}$	$2.46^{+0.03}_{-0.03} \times 10^{-6}$	$2.00^{+0.03}_{-0.03} \times 10^{-6}$
N(Si)/N(H)	$9.18^{+0.29}_{-0.29} \times 10^{-7}$	$8.75^{+0.18}_{-0.19} \times 10^{-6}$	$4.38^{+0.15}_{-0.15} \times 10^{-6}$
N(P)/N(H)	$7.58^{+0.46}_{-0.46} \times 10^{-8}$	$1.70^{+0.16}_{-0.16} \times 10^{-7}$	$1.73^{+0.07}_{-0.07} \times 10^{-7}$
N(S)/N(H)	$2.70^{+0.25}_{-0.25} \times 10^{-7}$	$1.05^{+0.15}_{-0.06} \times 10^{-6}$	$8.06^{+0.46}_{-0.47} \times 10^{-7}$
N(Fe)/N(H)	$2.72^{+0.11}_{-0.11} \times 10^{-6}$	$1.84^{+0.04}_{-0.04} \times 10^{-5}$	$1.21^{+0.04}_{-0.04} \times 10^{-5}$
N(Ni)/N(H)	$7.96^{+0.27}_{-0.27} \times 10^{-7}$	$4.78^{+0.08}_{-0.08} \times 10^{-6}$	$3.32^{+0.10}_{-0.10} \times 10^{-6}$

Note: <sup>a</sup>The AAVSO Photometric All Sky Survey (APASS) DR9, Henden et al. (2016).

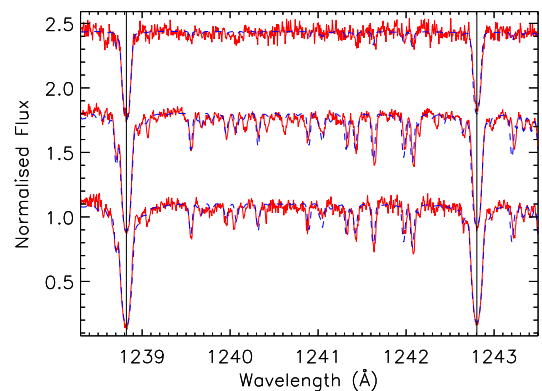


**Figure 3.** Section of *FUSE* spectra for WD0455–282 (top), WD0621–376 (middle), and WD2211–495 (bottom) containing the C III multiplet shifted to rest wavelength. The flux for each white dwarf has been normalized, and offset for clarity. The red solid line is the observed flux, while the blue dashed line is the best-fitting photospheric model. The vertical solid lines indicate the positions of the transitions used to measure the abundance.

three white dwarfs. We measured Ni abundances of  $7.96^{+0.27}_{-0.27} \times 10^{-7}$ ,  $4.78^{+0.08}_{-0.08} \times 10^{-6}$ , and  $3.32^{+0.10}_{-0.10} \times 10^{-6}$  for WD0455–282, WD0621–376, and WD2211–495, respectively.

### 5.9 $T_{\text{eff}}/\log g$ measurements

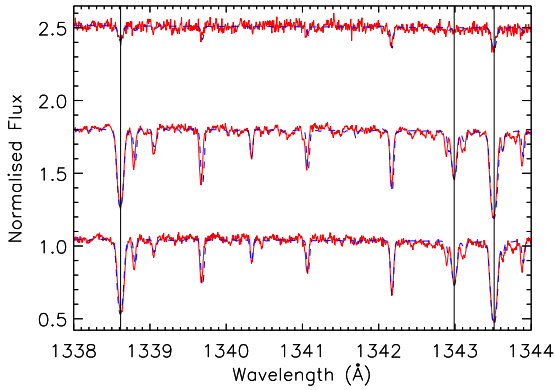
The Lyman lines (Ly  $\beta$ –Ly  $\epsilon$ ) used to measure  $T_{\text{eff}}$  and  $\log g$  are located in the *FUSE* spectrum. As mentioned previously, the flux



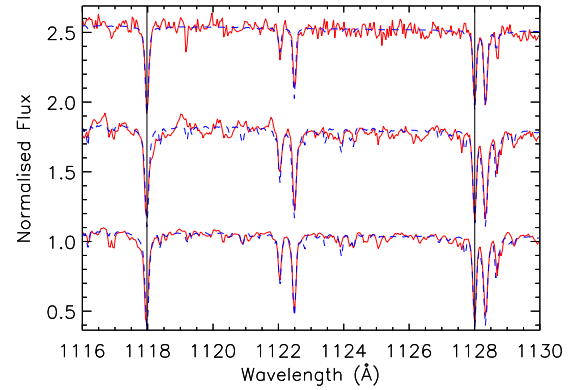
**Figure 4.** Section of the STIS spectrum from WD0455–282 (top), WD0621–376 (middle), and WD2211–495 (bottom) containing the N V doublet. The fluxes have been normalized, and offset from each other for clarity. Note that the observed flux has been shifted to rest wavelength. The red solid line is the observational data, while the blue dashed line is the best-fitting photospheric model. The vertical black lines indicate the position of the N V doublet used to measure the abundances.

uncertainties in the *FUSE* spectra are unreliable. Therefore, we express the flux uncertainties as a fraction of the observational flux so as to achieve a fit with  $\chi^2_{\text{red}}$  close to unity. For  $T_{\text{eff}}$ , we measured values of  $65\,400^{+1240}_{-1210}$ ,  $64\,500^{+437}_{-424}$ , and  $65\,900^{+259}_{-254}$  K for WD0455–282, WD0621–376, and WD2211–495, respectively. For  $\log g$ , we measured values of  $7.87^{+0.09}_{-0.09}$ ,  $7.60^{+0.03}_{-0.03}$ , and  $7.58^{+0.02}_{-0.02}$  for WD0455–282, WD0621–376, and WD2211–495,

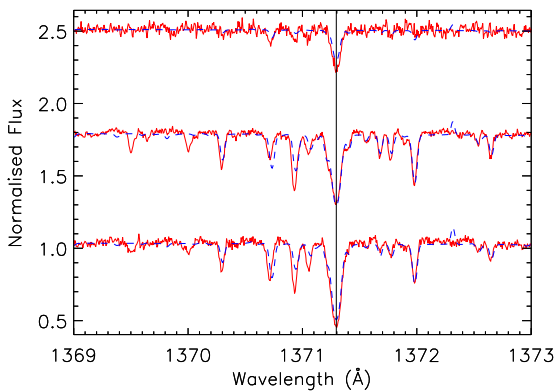




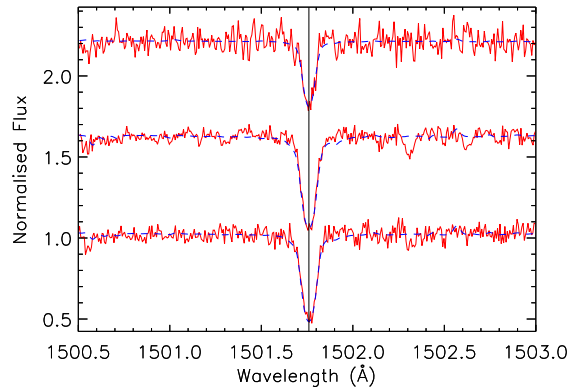
**Figure 5.** The same as for Fig. 4, but for a region of the STIS spectrum containing three O IV lines with laboratory wavelengths 1338.615, 1342.990, and 1343.514 Å, respectively.



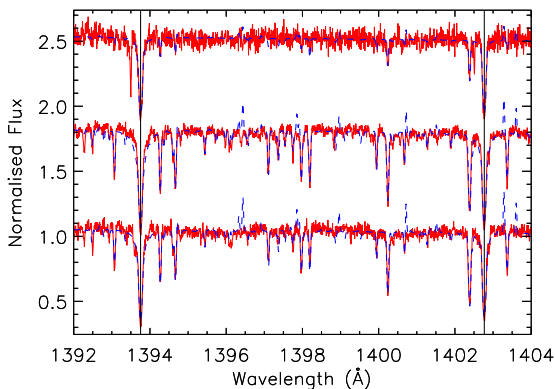
**Figure 8.** The same as for Fig. 3, but for a region of the *FUSE* spectrum containing two P V lines with laboratory wavelengths 1117.977 and 1128.008 Å, respectively.



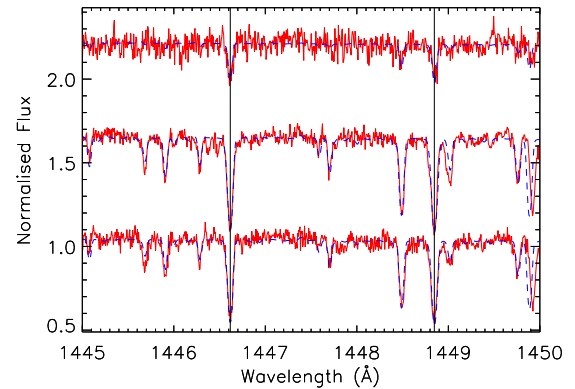
**Figure 6.** The same as for Fig. 4, but for a region of the STIS spectrum containing an O V line with a laboratory wavelength 1371.296 Å.



**Figure 9.** The same as for Fig. 4, but for a region of the STIS spectrum containing the S V line with a laboratory wavelength 1501.760 Å.



**Figure 7.** The same as for Fig. 4, but for a region of the STIS spectrum containing two Si IV lines with laboratory wavelengths 1393.755 and 1402.770 Å. For WD0455–282, the additional absorption feature next to the photospheric profile is a circumstellar line, whose discussion is deferred to Section 10.

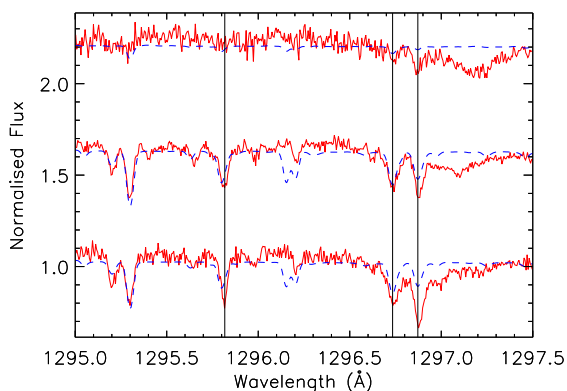


**Figure 10.** The same as for Fig. 4, but for a region of STIS spectrum containing two Fe V lines with laboratory wavelengths 1446.617 and 1448.847 Å, respectively.

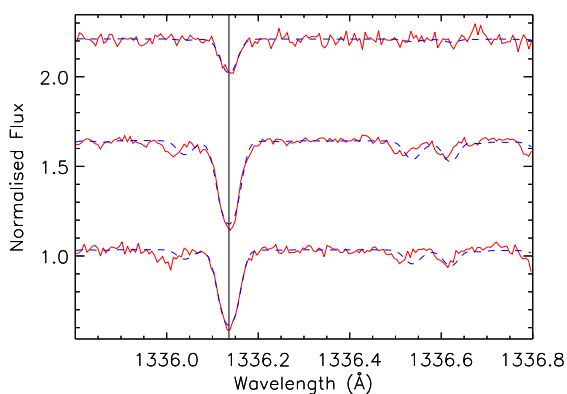
respectively. Interestingly, we noted that the  $\log g$  measurement for WD0621–376 is much higher than reported in previous works. Indeed, B14 measured  $\log g = 7.22$  for this star.

### 5.10 Mass–radius measurements

Prior to the launch of the astrometric satellite *Gaia*, measurement of astrophysical parameters such as the mass and radius of a white dwarf required the use of theoretical cooling tables such as those calculated by Holberg & Bergeron (2006), Kowalski & Saumon (2006), Tremblay, Bergeron & Gianninas 2011, and Bergeron et al.



**Figure 11.** The same as for Fig. 4, but for a region of STIS spectrum containing three Fe VI lines with laboratory wavelengths 1295.817, 1296.734, and 1296.872 Å, respectively.



**Figure 12.** The same as for Fig. 4, but for a region of STIS spectrum containing a Ni V line with a laboratory wavelength 1336.136 Å.

(2011)<sup>1</sup> (Montreal cooling tables hereafter). Thanks to the highly accurate parallax measurements made by *Gaia*, the angular diameter of any field white dwarf can be measured to a high degree of precision. Combined with the distance, we can then extract the radius, and in conjunction with  $\log g$ , we can then obtain the mass, followed by the gravitational redshift velocity. These mass and radius measurements offer a valuable means with which to test the fundamental mass–radius relationship for white dwarf stars.

For WD0455–282, the *Gaia* DR2 parallax was measured to be  $8.237 \pm 0.354$  mas, corresponding to a distance of  $121 \pm 5$  pc. Using equations (2) and (3), we extracted a mass and radius of  $0.589 \pm 0.145 M_{\odot}$  and  $1.48 \pm 0.06 R_{\odot}/100$ , respectively. The large uncertainty on the mass is dominated by the uncertainty on our  $\log g$  measurement. With the mass and radius, we then calculated a gravitational redshift velocity of  $25.4 \pm 6.3$  km s<sup>−1</sup>.

For WD0621–376, the *Gaia* DR2 parallax is  $13.136 \pm 0.059$  mas, corresponding to a distance of  $76.1 \pm 0.3$  pc. With these values, we measured a mass and radius of  $0.731 \pm 0.053 M_{\odot}$  and  $2.24 \pm 0.01 R_{\odot}/100$ , respectively. Using the mass and radius, we measured the gravitational redshift velocity to be  $20.7 \pm 1.5$  km s<sup>−1</sup>. We are sceptical of our mass measurement due to the large difference between our measured  $\log g$  (7.60), and that of Barstow et al. (2014) (7.22). If we use  $\log g = 7.22$  in

equation (3), then the measured mass decreases to  $0.305 M_{\odot}$ . We defer further exploration of this issue to the discussion.

For WD2211–495, the measured *Gaia* DR2 parallax is  $16.992 \pm 0.082$  mas, corresponding to a distance of  $58.9 \pm 0.3$  pc, making the star the closest in our sample. With this information, we measured the mass and radius to be  $0.575 \pm 0.028 M_{\odot}$  and  $2.04 \pm 0.01 R_{\odot}/100$ , respectively. Using the mass and radius, we then calculated the gravitational redshift velocity to be  $18.0 \pm 0.9$  km s<sup>−1</sup>.

## 6 RESULTS – INTERSTELLAR SURVEY

In this section, we present the results of our interstellar survey. To aid classification of the detected features, we used the Dynamical Local ISM calculator, the theory and motivation for which are described by Redfield & Linsky (2008). The calculator is freely available online,<sup>2</sup> and gives an indication of what interstellar clouds may be traversed along the line of sight given a galactic latitude and longitude. The calculator also predicts the velocity components of the cloud in question. In Table 6, we summarize the detected velocity components, and the clouds intersected by the line of sight.

### 6.1 WD0455–282

The line of sight to WD0455–282 appears to have a very interesting structure. In our line survey, we detected four distinct ISM velocity components, with average velocities of  $v_1 = -40.3 \pm 1.6$ ,  $v_2 = -32.1 \pm 3.0$ ,  $v_3 = 16.7 \pm 1.9$ , and  $v_4 = 25.1 \pm 1.1$  km s<sup>−1</sup>, respectively. In Fig. 13, we have plotted a region of STIS spectrum for WD0455–282 containing the Si II 1260 Å transition, where all four velocity components can be seen. We measured the four velocities to be  $-40.7 \pm 0.2$ ,  $-35.7 \pm 2.2$ ,  $17.9 \pm 1.2$ , and  $25.7 \pm 1.3$  km s<sup>−1</sup>, respectively. The LISM calculator states that the line of sight towards WD0455–282 traverses the Blue cloud, which has a radial velocity of  $12.6 \pm 1.0$  km s<sup>−1</sup>. While this velocity is close to our measurement for  $v_3$ , the two values are not in agreement.

Interestingly, our survey of WD0455–282 has revealed the presence of multicomponent circumstellar absorption in the Si III 1206, Si IV 1393, and 1402 Å resonant lines. In Figs 14–16, we have plotted three spectral regions containing the Si III and Si IV resonant lines, along with our best fit to these data using Gaussian profiles. The Si III 1206 Å line has three circumstellar components with velocities of  $-32.8 \pm 0.4$ ,  $12.8 \pm 1.3$ , and  $23.4 \pm 0.3$  km s<sup>−1</sup>, respectively. Si IV 1393 Å has two circumstellar components with velocities of  $17.3 \pm 4.9$  and  $25.9 \pm 0.2$  km s<sup>−1</sup>, respectively. Lastly, the Si IV 1402 Å line has two circumstellar components with velocities of  $16.1 \pm 1.4$  and  $25.3 \pm 0.4$  km s<sup>−1</sup>, respectively. For the Si III line, the circumstellar velocities are strikingly similar to those measured for the ISM velocities  $v_2$ ,  $v_3$ , and  $v_4$ . For Si IV, the circumstellar velocities are similar to those measured for  $v_3$  and  $v_4$ . To our knowledge, this is the first time that multicomponent circumstellar absorption has been observed along the line of sight to a white dwarf star.

### 6.2 WD0621–376

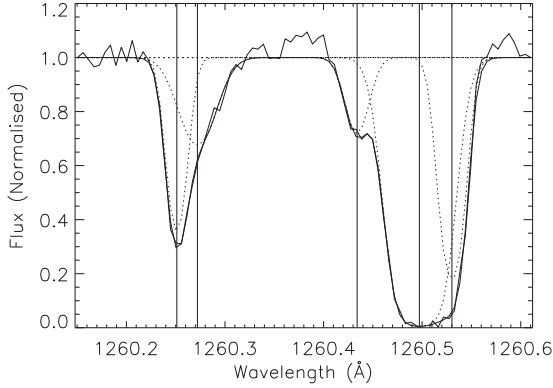
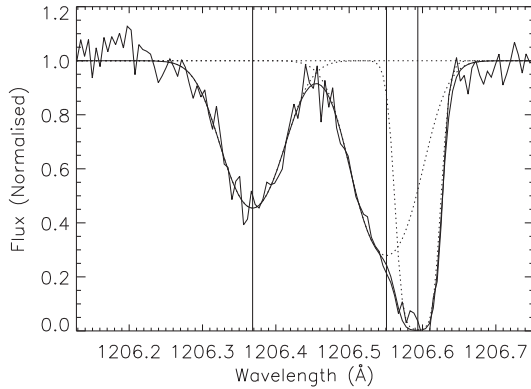
We made detections of two distinct ISM velocity components along the line of sight to WD0621–376 with average velocities of  $v_1 =$

<sup>1</sup><http://www.astro.umontreal.ca/bergeron/CoolingModels>

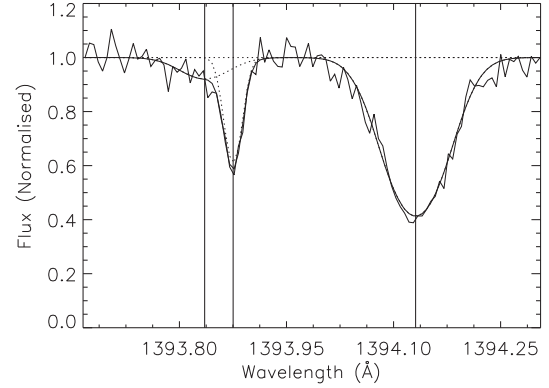
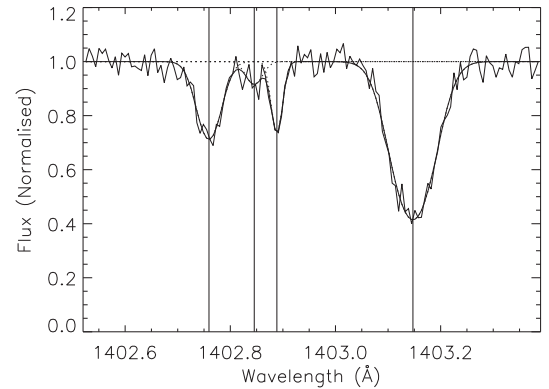
<sup>2</sup><http://lism.wesleyan.edu/LISMdynamics.html>

**Table 6.** List of measured ISM velocities for WD0455–282, WD0621–376, and WD2211–495, and the (known) clouds intersected by the line of sight.

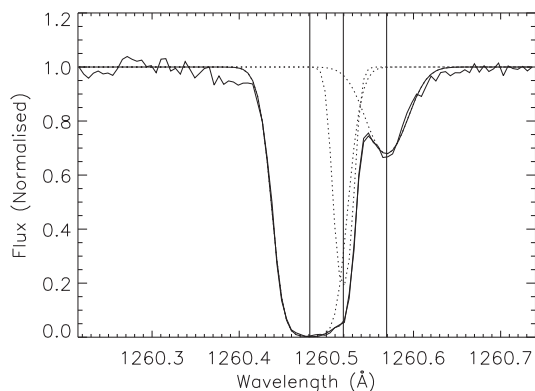
Parameter	WD0455–282	WD0621–376	WD2211–495
No. of components	4	2	2
$V_i$ (km s <sup>-1</sup> )	$-40.3 \pm 1.6$ , $-32.1 \pm 3.0$ $16.7 \pm 1.9$ , $25.1 \pm 1.1$	$12.1 \pm 2.3$ , $23.1 \pm 2.4$	$-9.91 \pm 1.39$ , $-2.18 \pm 2.43$
Clouds intersected	Blue	Blue	LIC

**Figure 13.** Best fit to the absorption features detected between 1260.2 and 1260.7 Å using six Gauss profiles for WD0455–282. From left to right, the first two features correspond to interstellar Si II with velocities of  $-40.7 \pm 0.2$  and  $-35.7 \pm 2.2$  km s<sup>-1</sup>, respectively. The third feature is a photospheric line, and the last two features are interstellar Si II with velocities of  $17.9 \pm 1.2$  and  $25.7 \pm 1.3$  km s<sup>-1</sup>, respectively.**Figure 14.** Best fit to the absorption features detected between 1206.2 and 1206.7 Å using three Gauss profiles for WD0455–282. All three features arise from Si III 1206 Å, with velocities of  $-32.8 \pm 0.4$ ,  $12.8 \pm 1.3$ , and  $23.4 \pm 0.3$  km s<sup>-1</sup>. All three components are circumstellar.

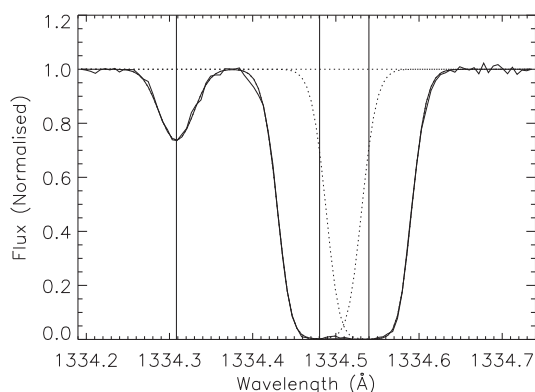
$12.1 \pm 2.3$  and  $v_2 = 23.1 \pm 2.4$  km s<sup>-1</sup>, respectively. The LISM calculator indicated that the line of sight to WD0621–376 intersects the Blue cloud, with a predicted radial velocity of  $11.1 \pm 0.9$  km s<sup>-1</sup>. Based on this value, our first ISM component appears to originate from the Blue cloud. In Fig. 17, we have plotted a region of spectrum containing the Si II 1260 Å transition, where both ISM components can be seen with velocities of  $14.0 \pm 0.3$  and  $23.2 \pm 0.3$  km s<sup>-1</sup>, respectively.

**Figure 15.** Best fit to the absorption features detected between 1393.7 and 1394.3 Å using three Gauss profiles for WD0455–282. All three features arise from Si IV 1393 Å, with velocities  $17.3 \pm 4.9$ ,  $25.9 \pm 0.2$ , and  $80.9 \pm 0.2$  km s<sup>-1</sup>. The first two components are interstellar, and the third component is photospheric.**Figure 16.** Best fit to the absorption features detected between 1402.5 and 1403.4 Å using three Gauss profiles for WD0455–282. The latter three features arise from Si IV 1402 Å, with velocities of  $16.1 \pm 1.4$ ,  $25.3 \pm 0.4$ , and  $80.6 \pm 0.2$  km s<sup>-1</sup>, respectively. The absorption feature on the far left is a photospheric Fe line. The second and third components are circumstellar Si IV, and the fourth component is photospheric Si IV.

Unlike WD0455–282, we did not detect any circumstellar features along the line of sight to WD0621–376. In addition, we made no detections of the Si III 1206.4995 Å transition. The significance of this result will be explored shortly.



**Figure 17.** Best fit to the absorption features detected between 1260.2 and 1260.7 Å using three Gauss profiles for WD0621–376. The first two features are interstellar Si II with velocities of  $14.0 \pm 0.3$  and  $23.2 \pm 0.3$  km s<sup>-1</sup>, respectively, while the third feature is a photospheric line.

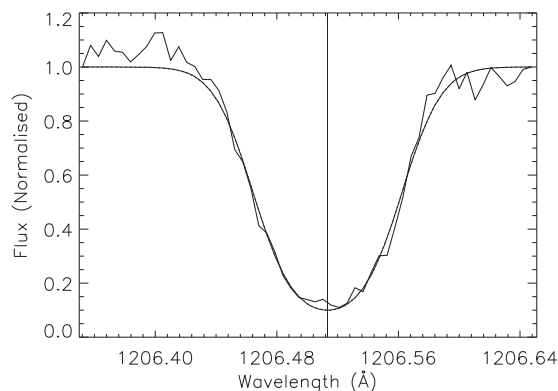


**Figure 18.** Best fit to the absorption features detected between 1334.2 and 1334.7 Å using three Gauss profiles for WD2211–495. The first feature is photospheric, while the second and third features are interstellar C II with velocities of  $-11.7 \pm 0.8$  and  $1.67 \pm 0.85$  km s<sup>-1</sup>, respectively.

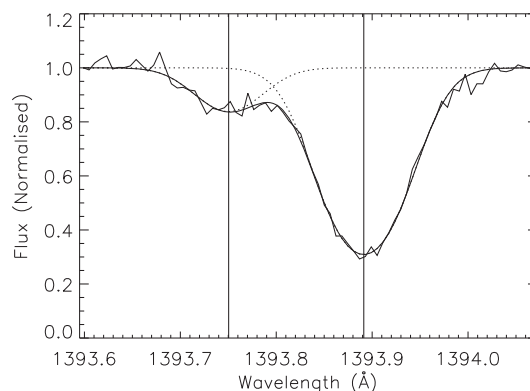
### 6.3 WD2211–495

We have identified two distinct ISM velocity components along the line of sight to WD2211–495, with average velocities of  $v_1 = -9.91 \pm 1.39$  and  $v_2 = -2.18 \pm 2.43$  km s<sup>-1</sup>, respectively. In Fig. 18, we have plotted a region of STIS spectrum for WD2211–495 containing the C II 1334 Å line, where both ISM components can be seen with velocities of  $-11.7 \pm 0.8$  and  $1.67 \pm 0.85$  km s<sup>-1</sup>, respectively. The LISM calculator indicated that the line of sight traversed two clouds, namely the Local Interstellar Cloud (LIC), and the Dor cloud, with velocities  $-8.80 \pm 1.32$  and  $9.93 \pm 0.60$  km s<sup>-1</sup>, respectively. Our first ISM velocity is in agreement with the value predicted for the LIC, suggesting that this component is associated with the LIC. However, our last component is not in agreement with the Dor cloud velocity. This may be due to a limitation in the LISM model, which is based upon four sightlines for the Dor Cloud (contrast with 79 sightlines for the LIC, and 10 for the Blue cloud). This could also be explained if the Dor cloud does not intersect the line of sight to the white dwarf.

We made a detection of a single circumstellar component in the Si III 1206 line, and the Si IV 1393 Å line. We do not detect a circumstellar line in the Si IV 1402 Å line due to the presence of strong Fe/Ni absorption features. In Figs 19 and 20, we have plotted regions of STIS spectra for WD2211–495 encompassing the Si III



**Figure 19.** Best fit to the absorption features detected between 1206 and 1207 Å using one Gauss profile for WD2211–495. This feature is circumstellar Si III, with a velocity of  $3.43 \pm 0.10$  km s<sup>-1</sup>.

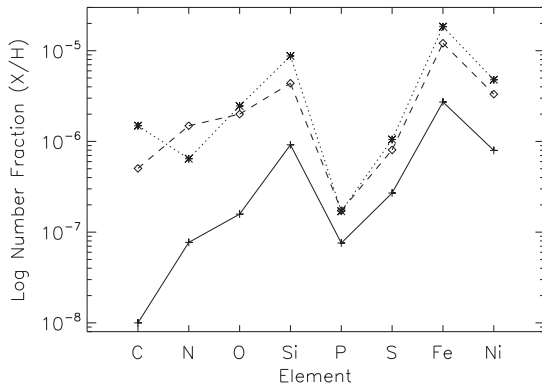


**Figure 20.** Best fit to the absorption features detected between 1393.7 and 1394.3 Å using two Gauss profiles for WD2211–495. The first feature is circumstellar Si IV with a velocity of  $-1.00 \pm 0.56$  km s<sup>-1</sup>, while the second feature is photospheric Si IV with a velocity of  $29.3 \pm 0.12$  km s<sup>-1</sup>.

and Si IV transitions, respectively. We measured the velocity of the circumstellar component to be  $3.43 \pm 0.10$  km s<sup>-1</sup> for the Si III line, and  $-1.00 \pm 0.56$  km s<sup>-1</sup> for the Si IV line. The measured circumstellar velocities are similar to the velocity measured for the ISM component  $v_2$ .

## 7 DISCUSSION: RADIATIVE LEVITATION

It is well established that metals are able to be supported against gravitational diffusion in white dwarf atmospheres thanks to radiative levitation. The efficiency of radiative levitation is a sensitive function of  $T_{\text{eff}}$  and  $\log g$ , meaning the observed abundance patterns in a white dwarf atmosphere will also be a function of  $T_{\text{eff}}$  and  $\log g$  (neglecting accretion). In Fig. 21, we have plotted the measured abundances in all three white dwarfs as number fractions of H. A general trend can be seen for all three objects, where the abundance of the metals increases steadily from C to Si, followed by a drop for the P abundance, followed by a steady increase again for S to Fe. It can also be seen that the abundance curves for WD0621–376 and WD2211–495 overlap one another. Furthermore, because WD0455–282 has a similar abundance pattern to the other two white dwarfs, it appears that the WD0455–282 curve can be brought up to meet the other two curves through the application of a multiplicative constant. This is simply explained by considering the  $T_{\text{eff}}$  and  $\log g$  values for each white dwarf. The measured



**Figure 21.** Plot of observed photospheric abundances for WD0455–282 (solid line, plus-symbols), WD0621–376 (dotted line, asterisk symbols), and WD2211–495 (dashed line, diamond symbols). Note that the C abundance for WD0455–282 is an upper limit.

$T_{\text{eff}}$  and  $\log g$  for WD0621–376 and WD2211–495 are very similar. Therefore, material in the atmospheres of these two stars will experience a similar radiative acceleration. WD0455–282 has a similar  $T_{\text{eff}}$ , but a higher  $\log g$ , meaning the equilibrium abundances will be smaller in this object compared to the other two. This point is further reinforced by considering the Fe/Ni abundance ratio. The Fe/Ni ratios observed in WD0455–282, WD0621–376, and WD2211–495 were calculated to be  $3.42^{+0.18}_{-0.18}$ ,  $3.85^{+0.10}_{-0.10}$ , and  $3.64^{+0.16}_{-0.16}$ , respectively. Within error the Fe/Ni ratio observed for WD2211–495 is in agreement with that observed for WD0621–376, while the ratio observed for WD0621–376 is in agreement with that observed for WD0455–282.

There is continuing disagreement between the photospheric abundances observed in white dwarf atmospheres and the photospheric abundances predicted by radiative levitation theory. The most well-known set of radiative equilibrium abundances for white dwarf stars was calculated by Ch94/95. This disagreement is thought to be due to a number of simplifying assumptions used in calculating the abundances. These assumptions include assuming no momentum redistribution of levitated material, and that the reservoir of material that could be levitated was effectively infinite. However, these values are useful to compare against, as they define the maximum possible abundance that can be supported in the atmosphere through radiative levitation. In Table 7, we have tabulated the predicted abundances from radiative equilibrium theory, and compare them to the measured photospheric abundances from WD0455–282, WD0621–376, and WD2211–495. In all three stars, it can be seen that for C, N, O, P, S, and Ni the measured abundances are smaller than those predicted by Ch94/95. However, in the case of Si, the observed abundance is larger by several dex than those predicted by Ch94/95. As mentioned above, the abundances from radiative equilibrium theory will be the maximum possible abundance that can be supported through radiative levitation alone. Therefore, material exceeding this quantity should sink into the core. This implies that the reservoir of Si and Fe is being continually replenished.

In addition to the calculations performed by Ch94/95, more detailed models were considered by Landenberger-Schuh (2005) that included the effects of gravitational diffusion and radiative levitation in a self-consistent manner. Schuh was able to show that the radiative support for Si plummets for DA white dwarfs with  $T_{\text{eff}} > 60\,000$  K. This is because the population of Si IV decreases as Si V becomes populated with increasing temperature. This means that there should

be little to no Si present in the white dwarfs considered in this work. This corroborates the prediction by Ch94/95, providing further support to the idea that the three objects are potentially accreting material. However, it is not clear where this material originates from. The interplay between the flow of material sinking into the core via gravitational diffusion, the retardation of this flow by radiative levitation, and the introduction of additional material through accretion makes the problem complex. Therefore, this means that the methods used in studying metal pollution in cool white dwarfs (where radiative levitation is inefficient) cannot be applied to the stars studied in this paper. Future work will focus on developing the necessary computational and theoretical framework to study these processes, and how they affect the observed photospheric abundance patterns in white dwarf star atmospheres.

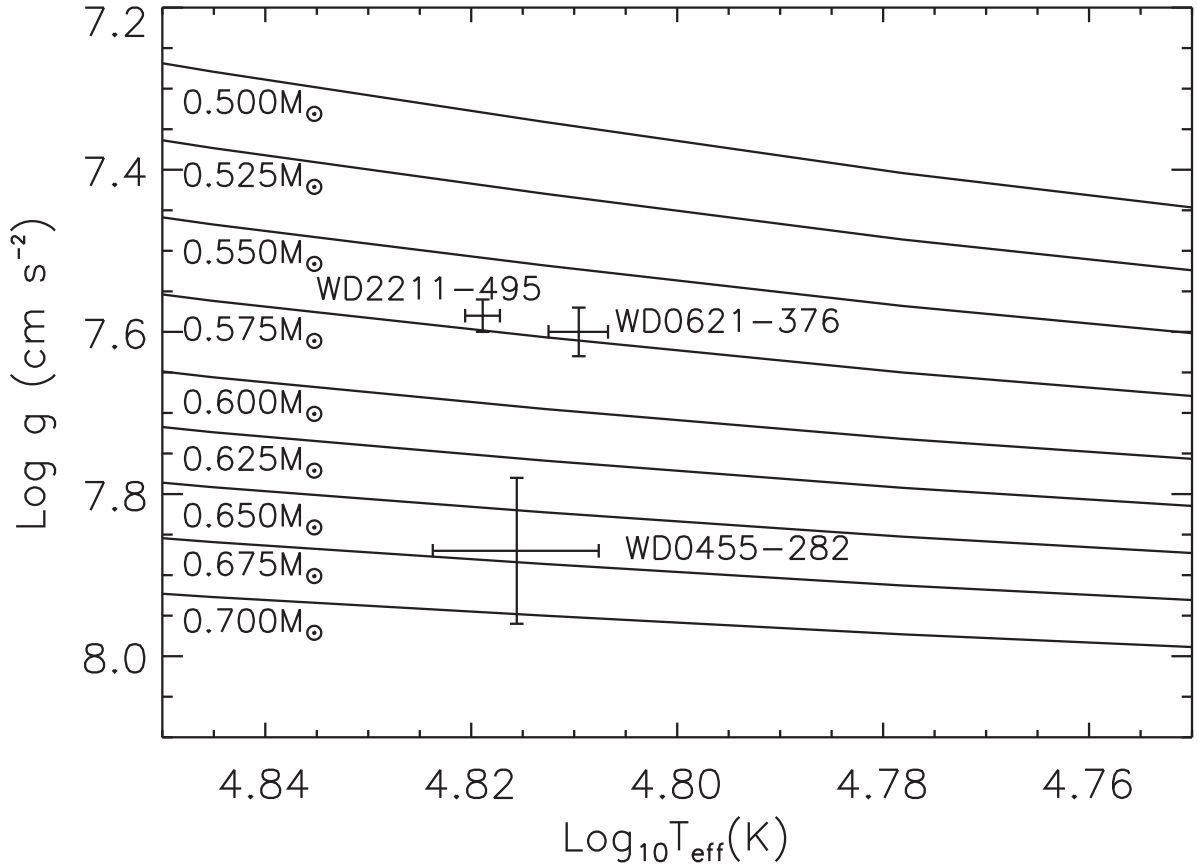
## 8 DISCUSSION: THE MASS–RADIUS RELATIONSHIP

As mentioned previously, the high-precision astrometric data from *Gaia* provide an excellent means with which to test the mass–radius relationship for white dwarf stars. In Fig. 22, we have plotted our measured  $T_{\text{eff}}/\log g$  values for the three white dwarfs, and the predicted  $T_{\text{eff}}/\log g$  values from the Montreal cooling tables for white dwarfs with masses ranging from 0.5 to 0.7  $M_{\odot}$ . The cooling tables assume a thick H envelope of  $M_{\text{H}}/M_{*} = 1 \times 10^{-4}$ , where  $M_{\text{H}}$  is the mass of the H layer and  $M_{*}$  is the mass of the star. Using the best-fitting synthetic spectrum and data from *Gaia*, we measured the masses of WD0455–282, WD0621–376, and WD2211–495 to be  $0.589 \pm 0.145$ ,  $0.731 \pm 0.053$ , and  $0.575 \pm 0.028 M_{\odot}$ , respectively. Comparatively, if we use the cooling tables to obtain the masses, we measure the masses to be  $0.676 \pm 0.033$ ,  $0.576 \pm 0.011$ , and  $0.572 \pm 0.007 M_{\odot}$  for WD0455–282, WD0621–376, and WD2211–495, respectively. For WD0455–282 and WD2211–495, the masses measured using the *Gaia* data are in agreement within error with those measured using the cooling tables. However, there is a significant discrepancy in the case of WD0621–376. There are multiple potential explanations for this mass discrepancy, which we now consider in turn.

The first possibility concerns the accuracy of the parallax used in the measurement. Stassun & Torres (2018) found evidence of a  $-82 \pm 33 \mu\text{s}$  systematic offset in the *Gaia* DR2 parallaxes. As the calculated mass is dependent upon the radius, and, therefore, the parallax measurement, this shift will make the mass more uncertain. To check this, we applied this offset to the *Gaia* DR2 parallax for WD0621–376 and recalculated the mass. This results in a mass of  $0.740 \pm 0.053 M_{\odot}$ , showing that the parallax measurement is not the cause of the discrepancy. Further reinforcing this is the fact that WD0621–376 is not variable to within 0.0029 mag (Marinoni et al. 2016), ruling out uncertainties on the parallax due to variability. A second possibility concerns interstellar reddening, which can affect the UV flux and introduce uncertainties in the measured  $T_{\text{eff}}$  and  $\log g$ . However, using the 3D dust maps of Lallement et al. (2014), we find that the extinction along the line of sight to WD0621–376 is negligible, and is unlikely to affect  $T_{\text{eff}}$  and  $\log g$ . A third possibility is the thickness of the H envelope assumed in the model calculation. Using detailed pre-white dwarf evolutionary sequences, Romero et al. (2019) showed that the thickness of this envelope decreases as the total mass of the star increases, leading to a decrease in the radius of the star of up to  $\sim 12$  per cent. However, this effect is too small to explain the discrepant mass. Lastly, a fourth possibility is that the STIS spectrum is poorly calibrated. As an additional check, the

**Table 7.** Comparison between predicted photospheric abundances from radiative levitation theory (Ch94/95), and those measured in this work (Observed column) for WD0455–282, WD0621–376, and WD2211–495, as a number fraction relative to H.

N(X)/N(H)	WD0455–282 Ch94/95	Observed	WD0621–376 Ch94/95	Observed	WD2211–495 Ch94/95	Observed
N(C)/N(H)	$1.51 \times 10^{-6}$	$1.00 \times 10^{-8}$	$2.82 \times 10^{-6}$	$1.49 \times 10^{-6}$	$3.02 \times 10^{-6}$	$5.05 \times 10^{-7}$
N(N)/N(H)	$3.72 \times 10^{-6}$	$7.71 \times 10^{-8}$	$6.76 \times 10^{-6}$	$6.45 \times 10^{-7}$	$7.76 \times 10^{-6}$	$1.49 \times 10^{-6}$
N(O)/N(H)	$4.07 \times 10^{-6}$	$1.58 \times 10^{-7}$	$7.24 \times 10^{-6}$	$2.46 \times 10^{-6}$	$8.32 \times 10^{-6}$	$2.00 \times 10^{-6}$
N(Si)/N(H)	$5.75 \times 10^{-9}$	$9.18 \times 10^{-7}$	$2.14 \times 10^{-8}$	$8.75 \times 10^{-6}$	$1.91 \times 10^{-8}$	$4.38 \times 10^{-6}$
N(P)/N(H)	$1.78 \times 10^{-6}$	$7.58 \times 10^{-8}$	$3.72 \times 10^{-6}$	$1.70 \times 10^{-7}$	$4.07 \times 10^{-6}$	$1.73 \times 10^{-7}$
N(S)/N(H)	$2.57 \times 10^{-6}$	$2.70 \times 10^{-7}$	$5.13 \times 10^{-6}$	$1.05 \times 10^{-6}$	$5.62 \times 10^{-6}$	$8.06 \times 10^{-7}$
N(Fe)/N(H)	$4.37 \times 10^{-6}$	$2.72 \times 10^{-6}$	$1.02 \times 10^{-5}$	$1.84 \times 10^{-5}$	$1.15 \times 10^{-5}$	$1.21 \times 10^{-5}$
N(Ni)/N(H)	$1.07 \times 10^{-4}$	$7.96 \times 10^{-7}$	$2.09 \times 10^{-4}$	$4.78 \times 10^{-6}$	$2.51 \times 10^{-4}$	$3.32 \times 10^{-6}$



**Figure 22.** Comparison of the measured values of  $T_{\text{eff}}/\log g$  for the three white dwarfs with the Montreal cooling curves for white dwarfs with masses ranging from 0.5 to 0.7  $M_{\odot}$ . For a comparison, the masses measured for WD0455–282, WD0621–376, and WD2211–495 were  $0.589 \pm 0.145$ ,  $0.731 \pm 0.053$ , and  $0.575 \pm 0.028 M_{\odot}$ , respectively.

$V$  magnitude can be used to determine the mass of WD0621–376. This has the advantage of using optical rather than UV fluxes. In this case, the ratio  $F_{\lambda}/H_{\lambda}$  seen in equation (2) is calculated by determining the flux  $F_{\lambda}$  in the  $V$  band:

$$F_{\lambda} = F_0 \times 10^{-0.4V}, \quad (5)$$

where  $V$  is the  $V$  magnitude,  $\lambda = 5423 \text{ \AA}$ ,  $F_0 = 3.804 \times 10^{-9}$  (see table 15 in Holberg & Bergeron 2006), and  $H_{\lambda}$  is the Eddington flux at  $\lambda = 5423 \text{ \AA}$ . The mass is then calculated using equation (3). By using  $V = 12.063 \pm 0.020$  from Table 5, we calculate the mass to be

$0.804 \pm 0.018 M_{\odot}$ . This is slightly larger than the value measured using the STIS data. This shows that the STIS calibration is not the cause of the discrepant mass value.

The origin of this mass discrepancy is currently unknown, and requires further study. This mass discrepancy could originate from the so-called Lyman/Balmer line problem described in Barstow et al. (2003), where the measured  $T_{\text{eff}}/\log g$  values for a DA white dwarf differ depending on whether the Lyman or Balmer lines are used. We plan to explore this further in future work.

**Table 8.** Comparison of metal abundances measured for WD0621–376 using a model atmosphere with  $\log g = 7.60$  and  $\log g = 7.22$ . Both models have  $T_{\text{eff}} = 64\,500$  K. We have tabulated the per cent difference between the measured abundances, defined in the text.

N(X)/N(H)	$\log g = 7.60$	$\log g = 7.22$	Per cent difference
N(C)/N(H)	$1.49^{+0.08}_{-0.08} \times 10^{-6}$	$2.24^{+0.09}_{-0.09} \times 10^{-6}$	50.1
N(N)/N(H)	$6.45^{+0.12}_{-0.12} \times 10^{-7}$	$2.99^{+0.04}_{-0.03} \times 10^{-7}$	– 53.7
N(O)/N(H)	$2.46^{+0.03}_{-0.03} \times 10^{-6}$	$1.70^{+0.03}_{-0.03} \times 10^{-6}$	– 30.7
N(Si)/N(H)	$8.75^{+0.18}_{-0.19} \times 10^{-6}$	$9.27^{+0.17}_{-0.17} \times 10^{-6}$	5.86
N(P)/N(H)	$1.70^{+0.16}_{-0.16} \times 10^{-7}$	$1.69^{+0.16}_{-0.16} \times 10^{-7}$	– 0.19
N(S)/N(H)	$1.05^{+0.15}_{-0.06} \times 10^{-6}$	$8.69^{+0.39}_{-0.40} \times 10^{-7}$	– 17.1
N(Fe)/N(H)	$1.84^{+0.04}_{-0.04} \times 10^{-5}$	$9.85^{+0.10}_{-0.10} \times 10^{-6}$	– 46.5
N(Ni)/N(H)	$4.78^{+0.08}_{-0.08} \times 10^{-6}$	$2.74^{+0.02}_{-0.02} \times 10^{-6}$	– 42.7

## 9 DISCUSSION: DISCREPANCIES IN WD0621–376

The large difference between our value of  $\log g$  and that measured by B14 for WD0621–376 is a mystery. As well as the disagreement between our  $\log g$  measurement and that of B14, there is also disagreement with the value measured by Gianninas et al. (2010). Using the Balmer H-lines, the authors measured  $\log g = 7.12$ . The disagreement between the optical and UV  $\log g$  measurements is not surprising as this has been seen in other stars as a consequence of the Lyman/Balmer line problem. A detailed discussion of the problem is beyond the scope of this paper. Despite the large disagreement between the various  $\log g$  measurements, we are confident that our measured  $T_{\text{eff}}$  for WD0621–376 is correct. This is because the ionization equilibria for O IV and O V are in excellent agreement with the observational data in Figs 5 and 6, respectively. This can also be seen in the case of Fe V and Fe VI in Figs 10 and 11, respectively.

Our measured  $\log g$  should at least be similar to that measured by B14 as we both used the same *FUSE* data set (P10415010). However, the *FUSE* spectrum used in this work was constructed independently of B14. To see if using different spectra resulted in the discrepancy, we measured  $T_{\text{eff}}$  and  $\log g$  of WD0621–376 using the same reduced *FUSE* spectrum as B14. For this measurement, we used the  $T_{\text{eff}}/\log g$  grid from the final iteration in this work for WD0621–376. Using the B14 spectrum, we measured  $T_{\text{eff}} = 64\,800^{+504}_{-521}$  K and  $\log g = 7.63^{+0.03}_{-0.03}$ . Compared with the values measured in this work of  $T_{\text{eff}} = 64\,500^{+437}_{-424}$  K and  $\log g = 7.60^{+0.03}_{-0.03}$ , the two results are in good agreement, implying that the  $\log g$  discrepancy does not originate from the data set used.

The large uncertainty in  $\log g$  for WD0621–376 will also introduce large uncertainties in the measured abundances. To gauge this effect, we remeasured the metal abundances for WD0621–376 using a model atmosphere with  $\log g = 7.22$ . The method used is the same as described in Section 4.1. We set  $T_{\text{eff}} = 63\,900$  K as measured from the Lyman lines. In Table 8, we list the measured abundances for WD0621–376 when using a model atmosphere with  $\log g = 7.60$ , and when using a model atmosphere with  $\log g = 7.22$ . We also list the per cent difference between the two abundance measurements, calculated as

$$\text{per cent difference} = 100 \frac{(X - X_0)}{X_0}, \quad (6)$$

where  $X$  is the abundance measured using the  $\log g = 7.22$  model, and  $X_0$  is the abundance measured using the  $\log g = 7.60$  model.

It can be seen that the C, N, O, Fe, and Ni abundances are highly sensitive to the different  $\log g$  values, with the abundance difference between the two models being 50.1, –53.7, –30.7, –46.5, and –42.7 per cent, respectively. The Si, P, and S abundances are much less sensitive, with the abundance differences being 5.86, –0.19, and –17.1 per cent, respectively.

The insensitivity of the Si abundance to  $\log g$  is surprising. In Section 5.4, we noted that our Si abundance measurement for WD0621–376 was an order of magnitude larger than that measured by B14. Given the large difference between the  $\log g$  values measured in this work and in B14, we would have expected at least some dependence upon  $\log g$ . Based on this fact, and the other factors hitherto discussed, it appears that the discrepancies described in this paper arise as a result of the stellar atmosphere grid used to make the measurements. Several differences exist between the model grids used in B14 and those used in this work. First, the models calculated in this work included more model atoms/ions than the B14 work, and covered a wider range of ionization states. Secondly, the Ni ions in this work used the PICs calculated by Preval et al. (2017) using AUTOSTRUCTURE (Badnell 2011), whereas the B14 models used hydrogenic PICs. Thirdly, the model grids used in the B14 study were not calculated based on an iterative scheme. In this case, the model grids calculated by B14 varied in  $T_{\text{eff}}$ ,  $\log g$ , and metal abundance scaled by a multiplicative factor. Future work will be focused on a detailed exploration of all of these differences.

## 10 DISCUSSION: INTERSTELLAR AND CIRCUMSTELLAR ABSORPTION

The work presented in this paper has been valuable in terms of our understanding of circumstellar absorption. In Section 6, we discussed our detections of circumstellar absorption features in WD0455–282, WD0621–376, and WD2211–495. As seen in previous works on circumstellar features, the absorption features detected in this work are all blue-shifted with respect to the photospheric velocity. We made several interesting observations in our study of the circumstellar absorption features, which we now discuss in turn.

### 10.1 Si III detections

Interestingly, while WD0455–282 and WD2211–495 showed signatures of circumstellar absorption, we made no detections of circumstellar absorption in the case of WD0621–376. However, the most interesting feature of this non-detection concerns the case of the Si III resonant feature with a laboratory wavelength 1206.4995 Å. In the case of WD0621–376, we do not detect this feature at all, whereas for WD0455–282 and WD2211–495, we do detect this feature. Because of the high temperatures and gravities of the stars studied, absorption from the Si III resonant transition in the photosphere will be very weak. This means that the feature should not be detected in any of the stars studied. Indeed, in a study by Preval et al. (2013), the authors also detected the Si III resonant transition in high-resolution STIS spectra of the hot white dwarf G191–B2B (see fig. 9 in the paper). The authors also detected a circumstellar component in the C IV resonant doublet at 1548 and 1550 Å, and in the Si IV resonant doublet at 1393 and 1402 Å (see figs 5, 6, 10, and 11 in Preval et al. 2013). In the aforementioned works, Si III has not previously been considered as a circumstellar line. However, in the context of the stellar atmospheric ionization fractions, this line can only be circumstellar. Therefore, this implies

that the resonant Si III line in hot white dwarfs could be a useful tracer of circumstellar absorption.

## 10.2 Relation to the ISM

Previous studies such as those conducted by Bannister et al. (2003), Dickinson et al. (2012), and Preval et al. (2013) have attempted to understand the origin of circumstellar absorption using velocity discrimination. For example, as mentioned previously in the case of G191–B2B, the C IV doublet has both a photospheric and circumstellar component. Preval et al. (2013) measured the velocity of the circumstellar components to be  $8.26 \pm 0.18 \text{ km s}^{-1}$  for the 1548 Å line, and  $8.30 \pm 0.15 \text{ km s}^{-1}$  for the 1550 Å line. The authors also measured the average velocity of two ISM components along the line of sight to G191–B2B using low-ionization state resonant transitions commonly found in the ISM. They measured the velocities of these two components to be  $19.4 \pm 0.03$  and  $8.64 \pm 0.03 \text{ km s}^{-1}$ , respectively. Redfield & Linsky (2008) showed that these two velocity components arise as a result of absorption from the LIC and the Hyades cloud, respectively. Interestingly, the velocities of the C IV circumstellar components are very similar to the velocity measured for the Hyades cloud, tentatively implying a connection between the two.

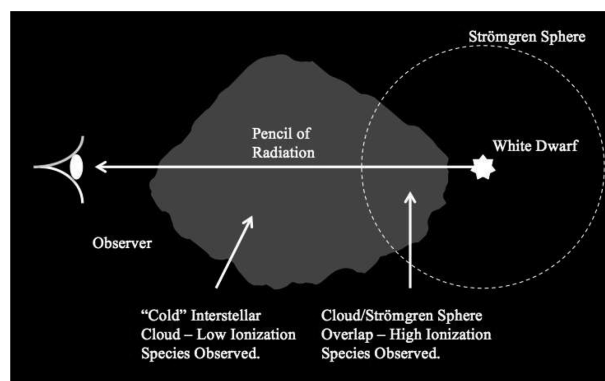
In this work, four ISM velocity components were detected along the line of sight to WD0455–282 with velocities of  $v_1 = -40.3 \pm 1.58$ ,  $v_2 = -32.1 \pm 3.04$ ,  $v_3 = 16.7 \pm 1.85$ , and  $v_4 = 25.1 \pm 1.06 \text{ km s}^{-1}$ , respectively. For the Si III 1206 Å line, we detected three circumstellar components with velocities of  $-32.8 \pm 0.35$ ,  $12.8 \pm 1.25$ , and  $23.4 \pm 0.25 \text{ km s}^{-1}$ , respectively. For the Si IV 1393 Å line, we detected two circumstellar components with velocities of  $17.3 \pm 4.89$  and  $25.9 \pm 0.23 \text{ km s}^{-1}$ , respectively. Finally, for the Si IV 1402 Å line, we detected two circumstellar components with velocities of  $16.1 \pm 1.43$  and  $25.3 \pm 0.36 \text{ km s}^{-1}$ , respectively. The similarity of the circumstellar velocities to the  $v_2$ ,  $v_3$ , and  $v_4$  components is difficult to miss, and, like G191–B2B, implies some connection.

In the case of WD2211–495, we detected two ISM components with velocities of  $v_1 = -9.91 \pm 1.39$  and  $v_2 = -2.18 \pm 2.43 \text{ km s}^{-1}$ , respectively. The velocity of the circumstellar component detected in the Si III 1206 Å line was measured to be  $3.43 \pm 0.10 \text{ km s}^{-1}$ , and the velocity for the circumstellar component detected in the Si IV 1393 Å line was measured to be  $-1.11 \pm 0.56 \text{ km s}^{-1}$ . Both of these circumstellar velocities are similar to the ISM component  $v_2$ .

## 10.3 Strömgren sphere ionization

Dickinson et al. (2012) conducted a detailed survey of 23 white dwarf stars with the aim of determining the origin of circumstellar absorption features. One potential explanation touted in this work is that of the Strömgren sphere. In this case, the UV radiation field of the white dwarf ionizes material within a certain radius of the object known as the Strömgren radius (Strömgren 1939). If a cloud in the ISM falls within this radius, it will produce lines from high-ionization state ions, while any material outside this radius will produce lines from neutral and low-ionization state elements. To aid visualization of this phenomenon, we have provided an illustration in Fig. 23.

In this work, we have identified circumstellar absorption in WD0455–282 and WD2211–495. We have also seen that the velocities of the highly ionized circumstellar components are strikingly similar to those observed in the ISM lines with low-ionization



**Figure 23.** Schematic of Strömgren sphere interacting with a cloud of gas. Radiation passing through the cloud outside the sphere produces low-ionization state absorption features, while radiation passing through the cloud inside the sphere produces high-ionization state absorption features.

states. Furthermore, prior to this work, circumstellar absorption has only been observed as a single velocity component. Now, for the first time, we have observed circumstellar absorption with multiple velocity components along the line of sight to WD0455–282. These circumstellar velocities are all very similar to the average ISM velocities along the line of sight to WD0455–282. This is, perhaps, the strongest evidence to date that circumstellar absorption arises as a result of Strömgren sphere ionization.

While Strömgren sphere ionization explains how the low- and high-ionization state lines form, it does not explain where this material comes from. This material could potentially be inherent to the ISM, or could even be inherent to the white dwarf itself, arising from the post-RGB pulsations of the object’s progenitor state.

In Dickinson et al. (2012), the authors provide a table of predicted column densities for absorption features arising from Strömgren sphere ionization. These column densities differ depending upon the transition considered. The largest predicted column density occurs for the resonant C IV doublet at 1548 and 1550 Å. Unfortunately, the STIS data used in this work stop short of the doublet. Therefore, for future work, it would be useful to obtain high-resolution spectroscopy for WD0455–282 to observe the C IV doublet. If the double component circumstellar feature is real, then this will also be observed in the C IV doublet.

## 11 CONCLUSIONS

We have presented a detailed UV survey of three hot, DA white dwarf stars. Using data obtained with *FUSE* and *HST*, we have measured  $T_{\text{eff}}$ ,  $\log g$ , and atmospheric compositions of these objects. In conjunction with measurements from the astrometric satellite *Gaia*, we have also directly measured the masses, radii, and gravitational redshift velocities of these stars. Upon comparison with the work of B14, we found that our measurement of  $\log g$  (7.60) for WD0621–376 was much larger than the authors’ value (7.22). We tested the sensitivity of our abundance measurements for WD0621–376 to the different  $\log g$  values, and found that the abundance measurements differed greatly for C, N, O, Fe, and Ni (>30 per cent). More work needs to be done to understand the reason as to why our  $\log g$  measurement for WD0621–376 is much larger than that measured by B14.

We considered the question of why the three white dwarfs studied have metals in their atmospheres. To address this question,



we compared the observed atmospheric abundances in the three white dwarfs to those predicted by radiative levitation theory as calculated by Ch94/95. We found that the observed Si abundance in all the three white dwarfs was larger than predicted by an order of magnitude. We also found that the Fe abundance in WD0621–376 and WD2211–495 was larger than predicted by an order of magnitude. Given that the Ch94/95 abundances constitute a maximum possible supported abundance, this tentatively implies an external origin for metal pollution. However, it is not clear what this origin might be. This is further complicated by the interplay between radiative levitation and gravitational diffusion. Therefore, to make any definitive progress on this topic, more sophisticated stellar atmospheric modelling including these processes is required.

In addition to our work on the photospheric features in the atmospheres of the three white dwarfs, we also conducted a survey of lines arising from absorption in the ISM. We made an interesting discovery along the line of sight to WD0455–282, where, for the first time, we detected multiple component circumstellar absorption in the Si III and Si IV resonant lines. We also detected circumstellar absorption along the line of sight to WD2211–495 in the Si IV 1393 Å line. We did not detect a circumstellar feature in the 1402 Å line. Interestingly, we made no detections of any circumstellar absorption along the line of sight to WD0621–376. We also could not detect the resonant Si III 1206 Å line along the line of sight to this white dwarf. This is in contrast to WD0455–282 and WD2211–495, where we detected very strong Si III absorption in both cases. This runs contrary to stellar atmosphere model predictions, where Si III is weakly populated in comparison to Si IV. This implies that the Si III line can be used as a reliable tracer of circumstellar absorption along the line of sight to hot white dwarf stars.

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**APPENDIX A: GAUSSIAN PARAMETRIZATION**

To parametrize the non-photospheric absorption features, we used a Gaussian profile. Because there can be a large number of absorbers along the line of sight, the profile can often become saturated. We account for this by using the full expression

$$F_\lambda = \prod_{i=1}^N F_i = F_0 \prod_{i=1}^N \exp[-P_{0,i}\phi], \quad (\text{A1})$$

where  $F_0$  is the continuum flux,  $P_{0,i}$  is the absorption strength for the  $i$ -th Gaussian profile, and  $\phi$  is the normalized Gaussian function.

The product is calculated out over  $N$  absorption profiles.  $\phi$  is then written as

$$\phi_\lambda = \frac{1}{P_{1,i}\sqrt{\pi}} \exp\left[-\frac{(\lambda - P_{2,i})^2}{P_{1,i}^2}\right], \quad (\text{A2})$$

where  $P_{1,i}$  is the Doppler width of the  $i$ -th Gaussian, and  $P_{2,i}$  is the centroid wavelength of the  $i$ -th Gaussian. Details on the fitting procedure can be found in the text.

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